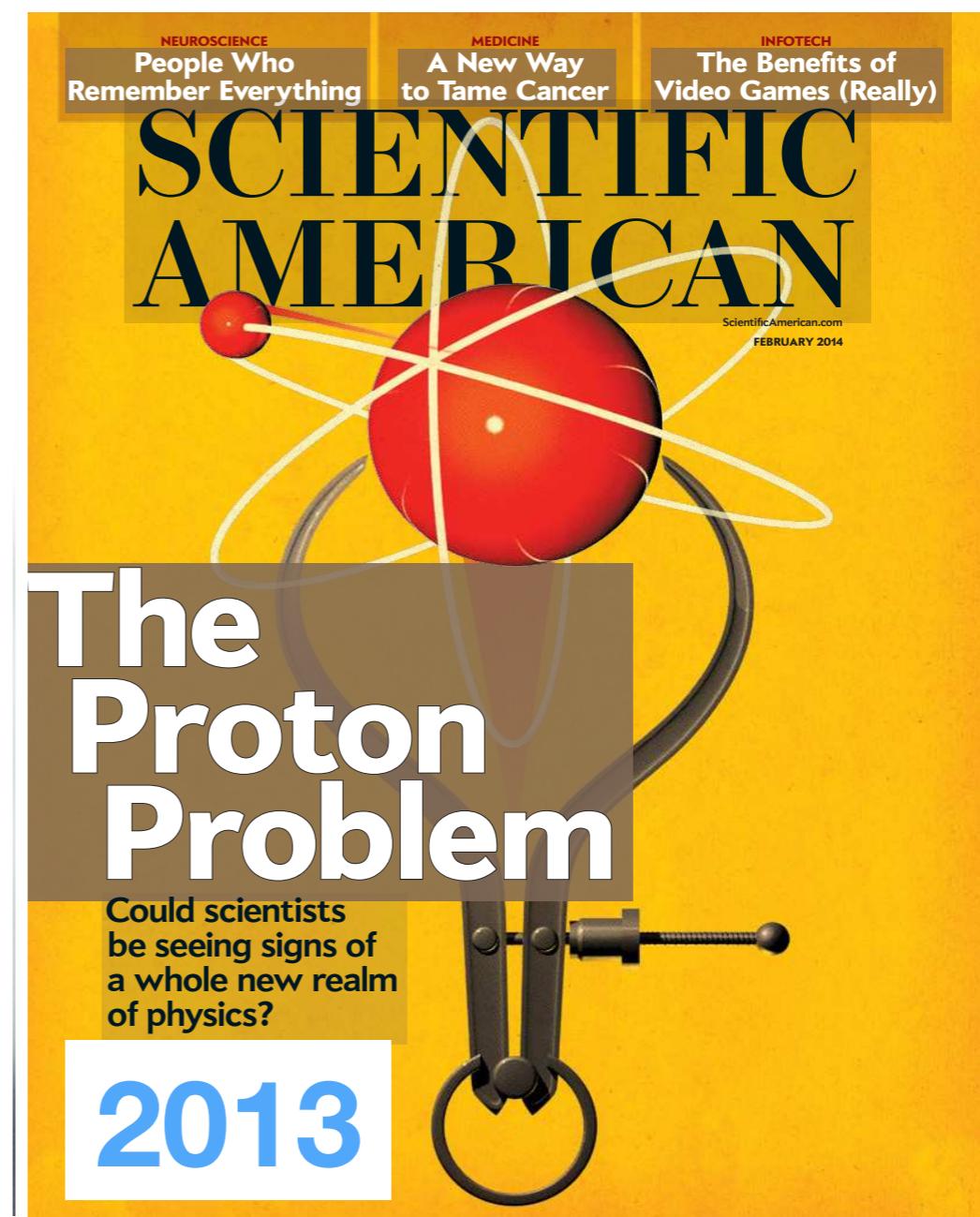


# **Electron scattering experiment off proton at ultra-low $Q^2$**

**Toshimi Suda**

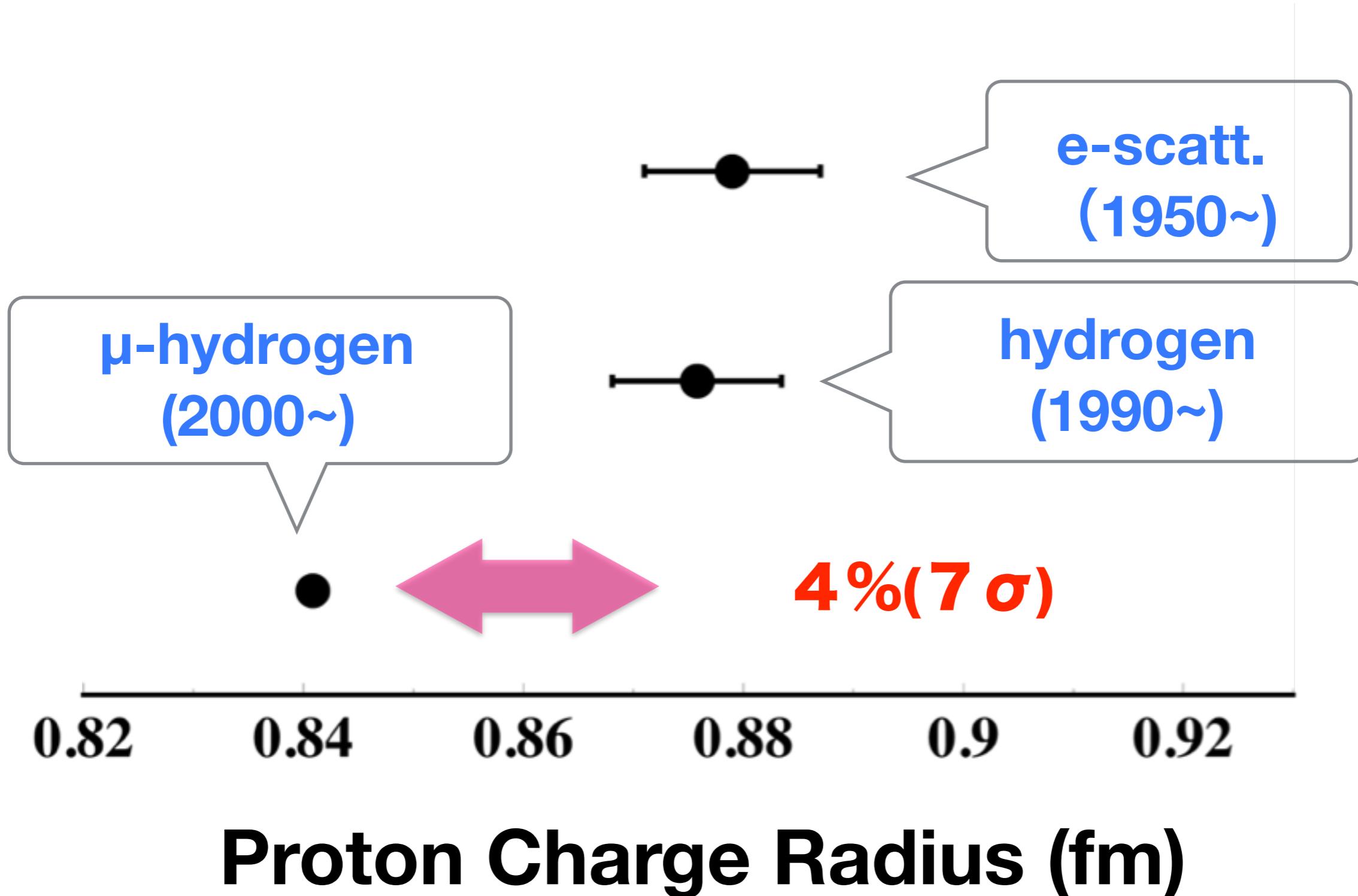
**Research Center for Electron-Photon Science,  
Tohoku University,  
Sendai**

# Proton Radius Puzzle



# Proton charge radius puzzle

MIN2016, Kyoto  
July 31-Aug.2, 2016



# Proton charge radius puzzle

MIN2016, Kyoto  
July 31-Aug.2, 2016

*many many discussions ..*

e-scatt.

*Data ? Interpretation ?* (1950~)

$\mu$ -hy

*Higher order effects ?* hydrogen  
(2000~, 1990~)

*QED calculation ?*

4% (7 $\sigma$ )

*New Physics (beyond SM ?)*



Proton Charge Radius (fm)

# Proton charge radius puzzle

MIN2016, Kyoto  
July 31-Aug.2, 2016

*many many discussions ..*

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1% (7 $\sigma$ )

**New Physics (beyond SM ?)**

0.82      0.84      0.86      0.88      0.9      0.92

*not yet settled*

*New experiments ...*

# Who are we ?

MIN2016, Kyoto  
July 31-Aug.2, 2016

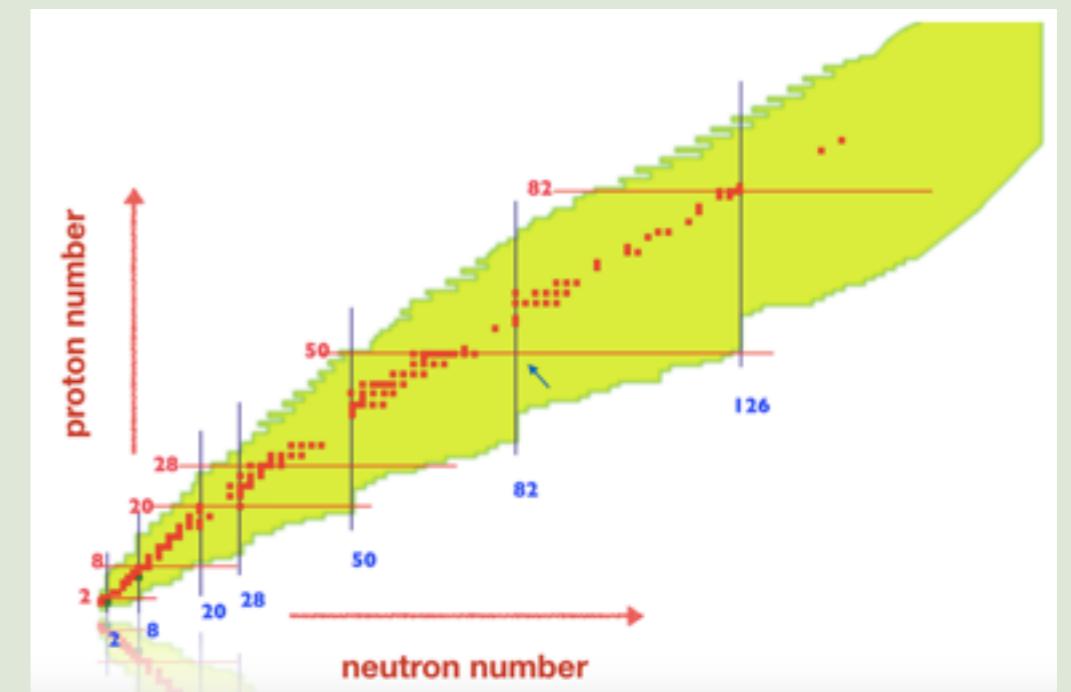
**We are “(low-energy) Electron Scatterers”.**

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“classical” elastic electron scattering  
to study the charge density distributions  
pioneered by R. Hofstadter in 1950s !

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} |F_c(q)|^2$$

$$F_c(\vec{q}) = \int \rho(\vec{r}) e^{-i\vec{q}\cdot\vec{r}} d\vec{r}$$

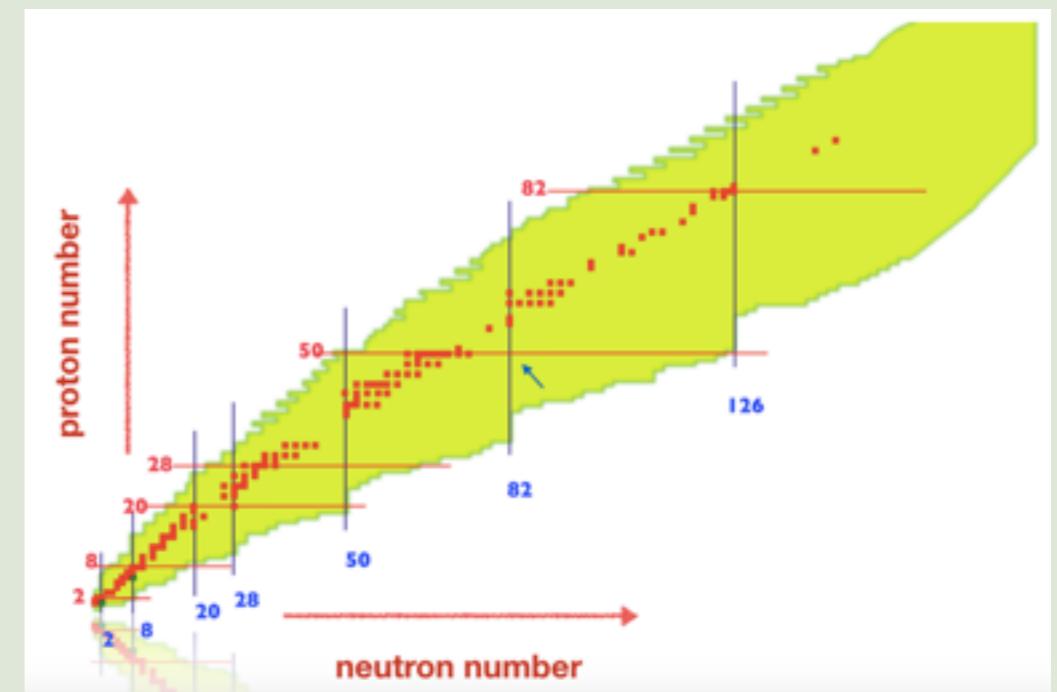


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Not for stable nuclei,,,,,

BUT never-yet-performed Short-Lived Exotic Nuclei !

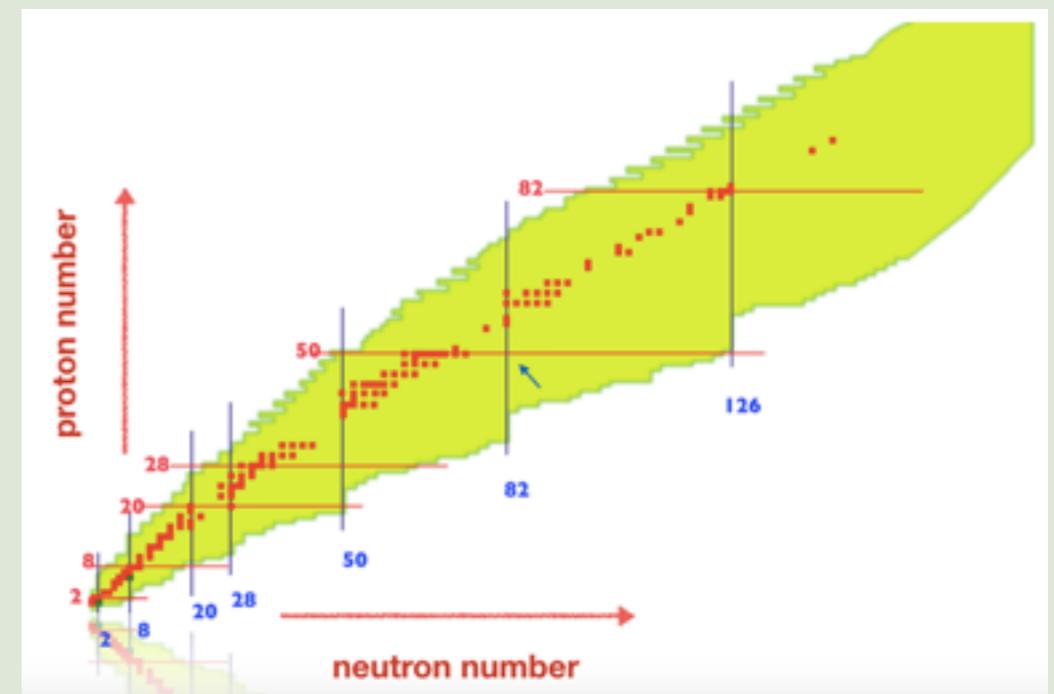
→ “Hofstadter’s experiments” for exotic nuclei

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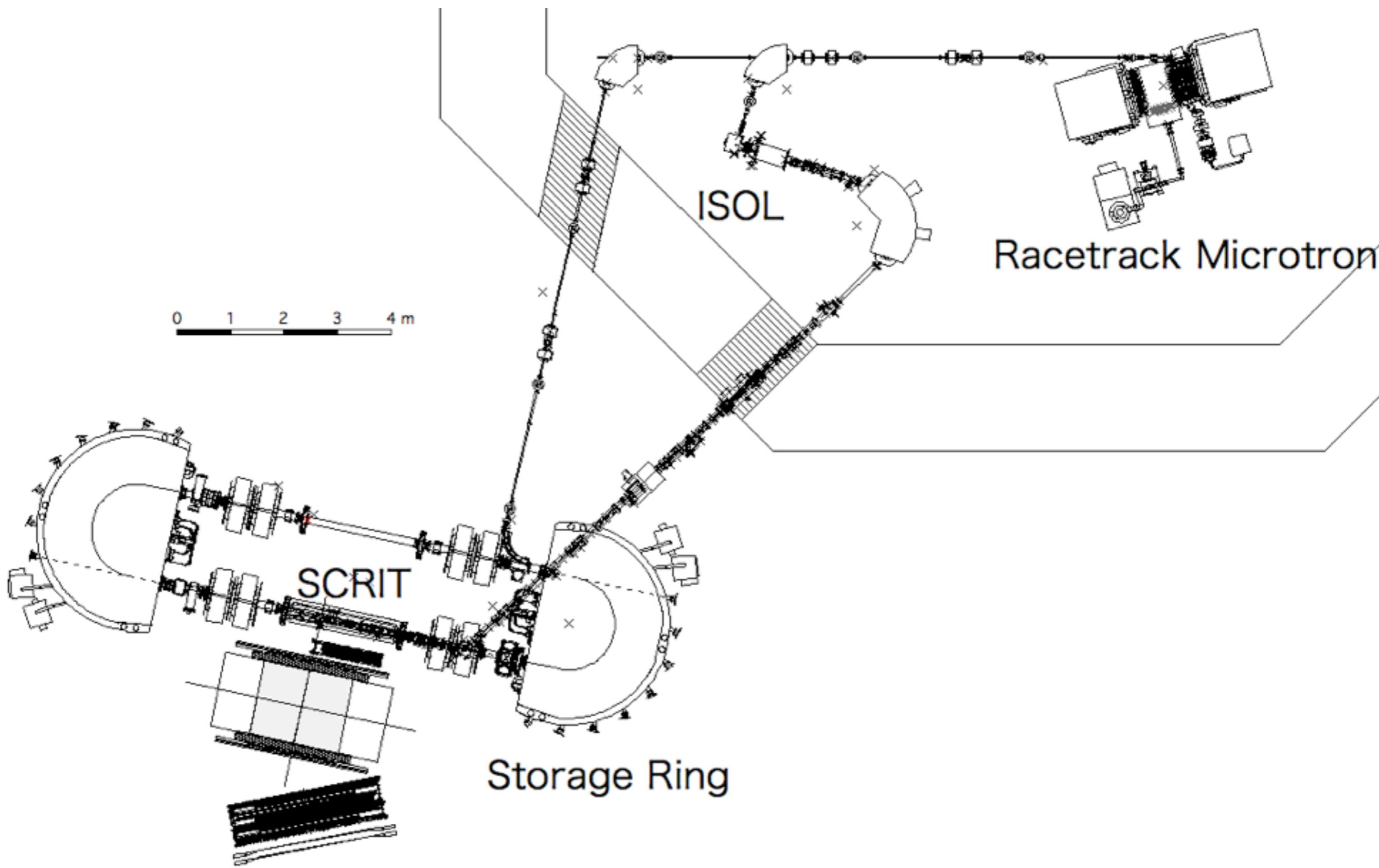
BUT never-yet-performed Short-Lived Exotic Nuclei !

→ “Hofstadter’s experiments” for exotic nuclei

we are currently operating  
the World’s first electron scattering facility  
dedicated for exotic nuclei.

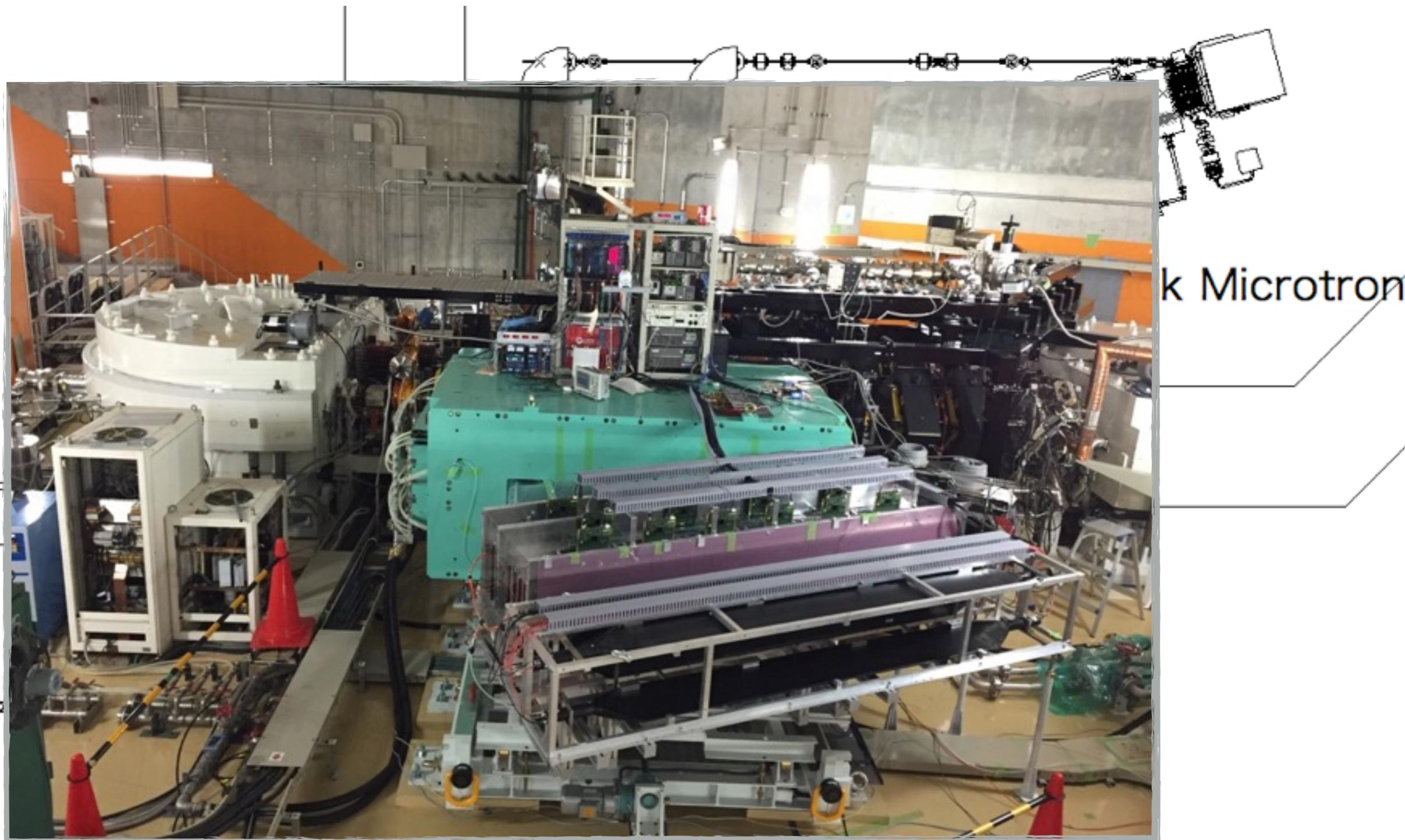
# SCRIT electron scattering facility

WS @ RIKEN  
Aug. 3, 2016

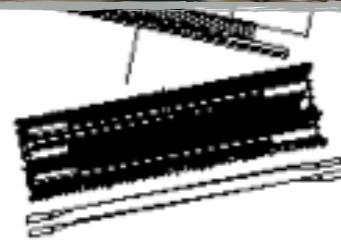


# SCRIT electron scattering facility

WS @ RIKEN  
Aug. 3, 2016

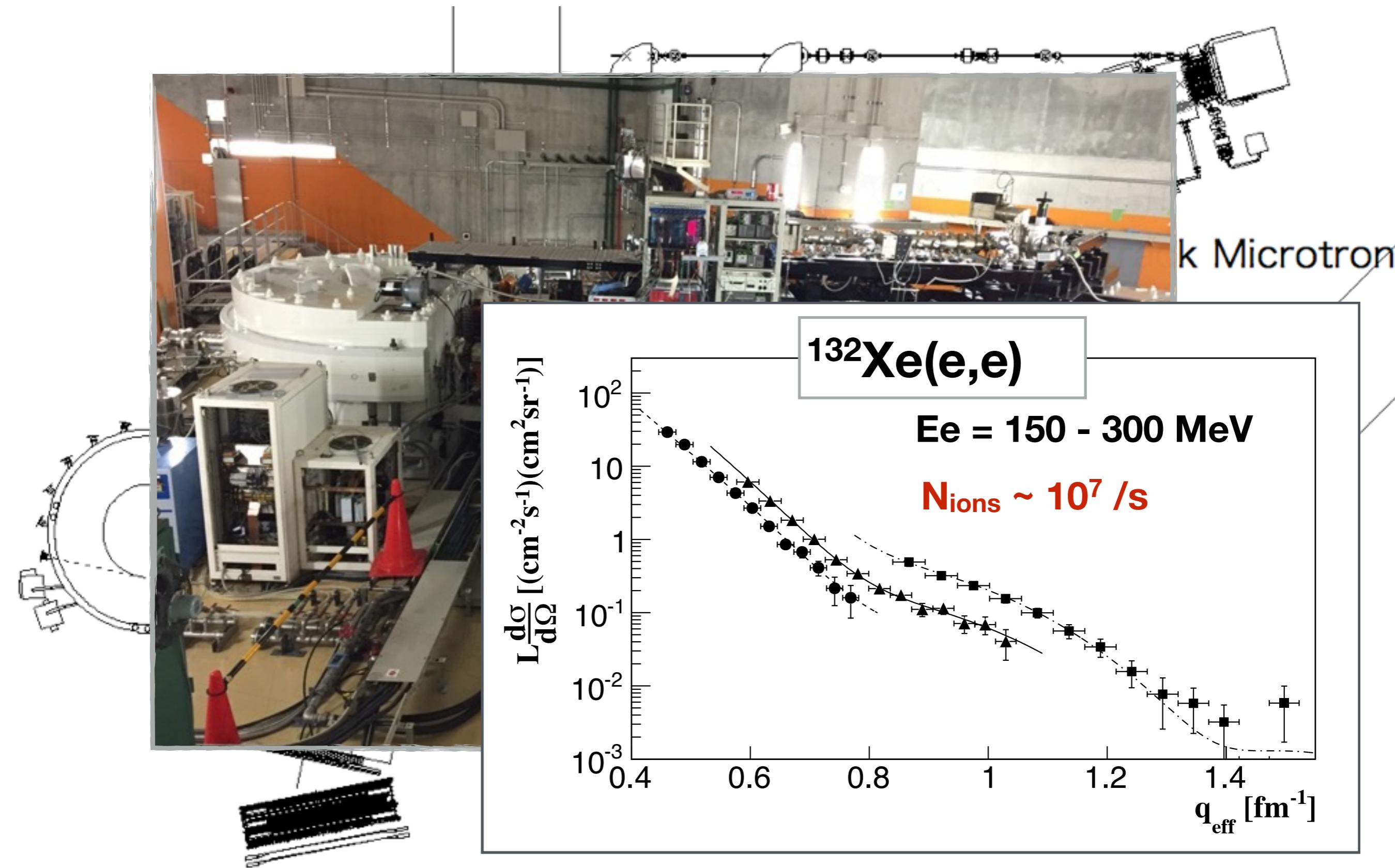


Storage Ring



# SCRIT electron scattering facility

WS @ RIKEN  
Aug. 3, 2016



# Electron scattering off proton

MIN2016, Kyoto  
July 31-Aug.2, 2016

1960

1970

1980

1990

2000

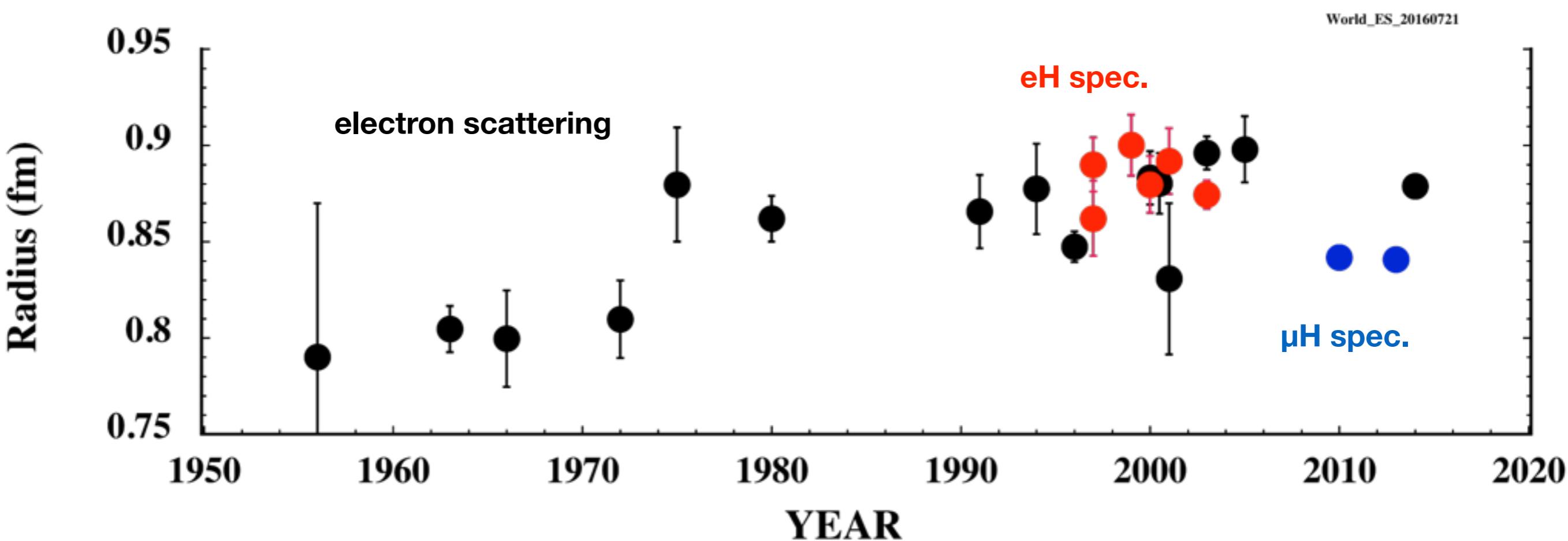
2010



e+p, e+A elastic scattering  
R. Hofstadter  
(1961)



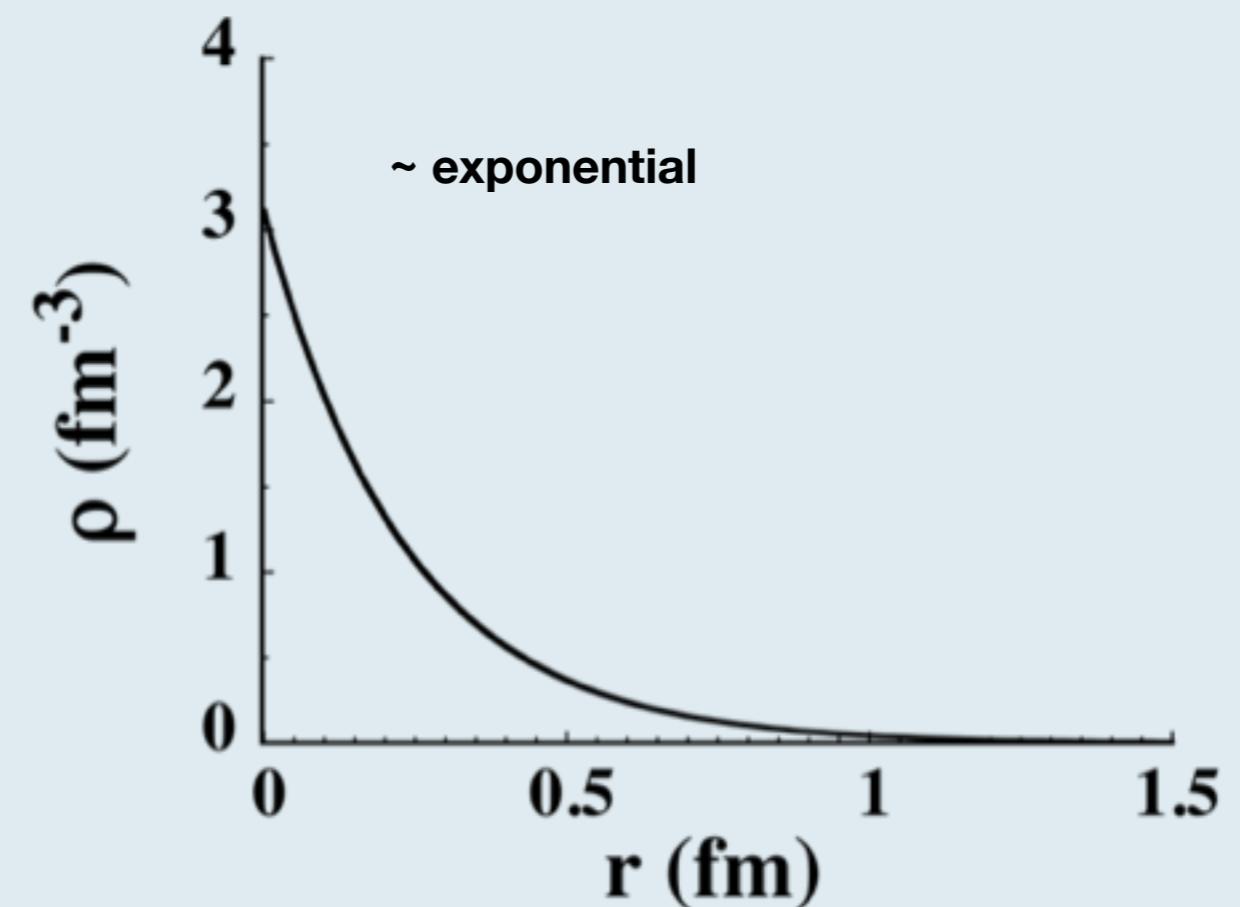
e+p deep inelastic scattering  
J. Friedman, H. Kendall and R. Taylor  
(1990)



## RMS radius

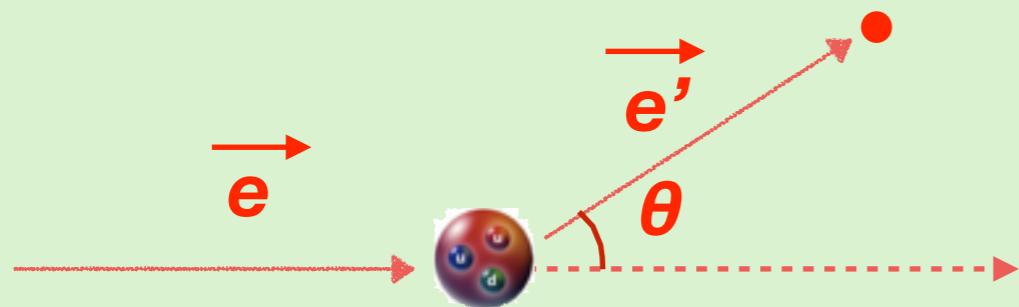
$$\begin{aligned}\langle r^2 \rangle &= \int r^2 \rho(\vec{r}) d\vec{r} \\ &= 4\pi \int r^4 \rho(r) dr\end{aligned}$$

$\rho(r)$



# Proton charge radius by e-scattering

WS @ RIKEN  
Aug. 3, 2016



**momentum transfer**

$$\vec{q} = \vec{e} - \vec{e}'$$

**energy transfer**

$$\omega = e - e'$$

**4 momentum transfer**

$$\begin{aligned} Q^2 &= q^2 - \omega^2 \\ &= 4 e e' \sin^2(\theta/2) \end{aligned}$$

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} \frac{G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2)}{1 + \tau}$$

$$\left( \frac{d\sigma}{d\Omega} \right)_{Mott} = \frac{z^2 \alpha^2}{4e^2} \frac{\cos^2(\theta/2)}{\sin^4(\theta/2)} \propto \frac{e^2}{q^4}$$

$$\epsilon = \frac{1}{1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}}$$

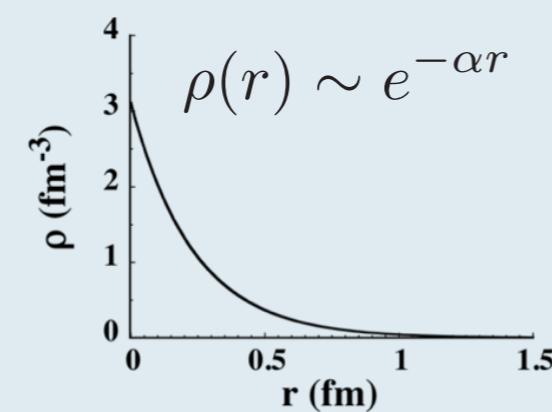
$$\tau = \frac{Q^2}{4m_p^2}$$

## 1) high $Q^2$ : charge density $\rho(r)$

Electric Form Factor GE



$$\langle r^2 \rangle = \int r^2 \rho(\vec{r}) d\vec{r}$$



radius is sensitive to  $\rho(r)$  at large distance  
( even at  $r \sim 4$  fm )

## 2) low $Q^2$

$$G_E(Q^2) \sim 1 - \frac{\langle r^2 \rangle^{1/2}}{6} Q^2 + \frac{\langle r^4 \rangle^{1/2}}{120} Q^4 - \dots$$

$$\langle r^2 \rangle \equiv -6 \frac{dG_E(Q^2)}{dQ^2} \Big|_{Q^2 \rightarrow 0}$$

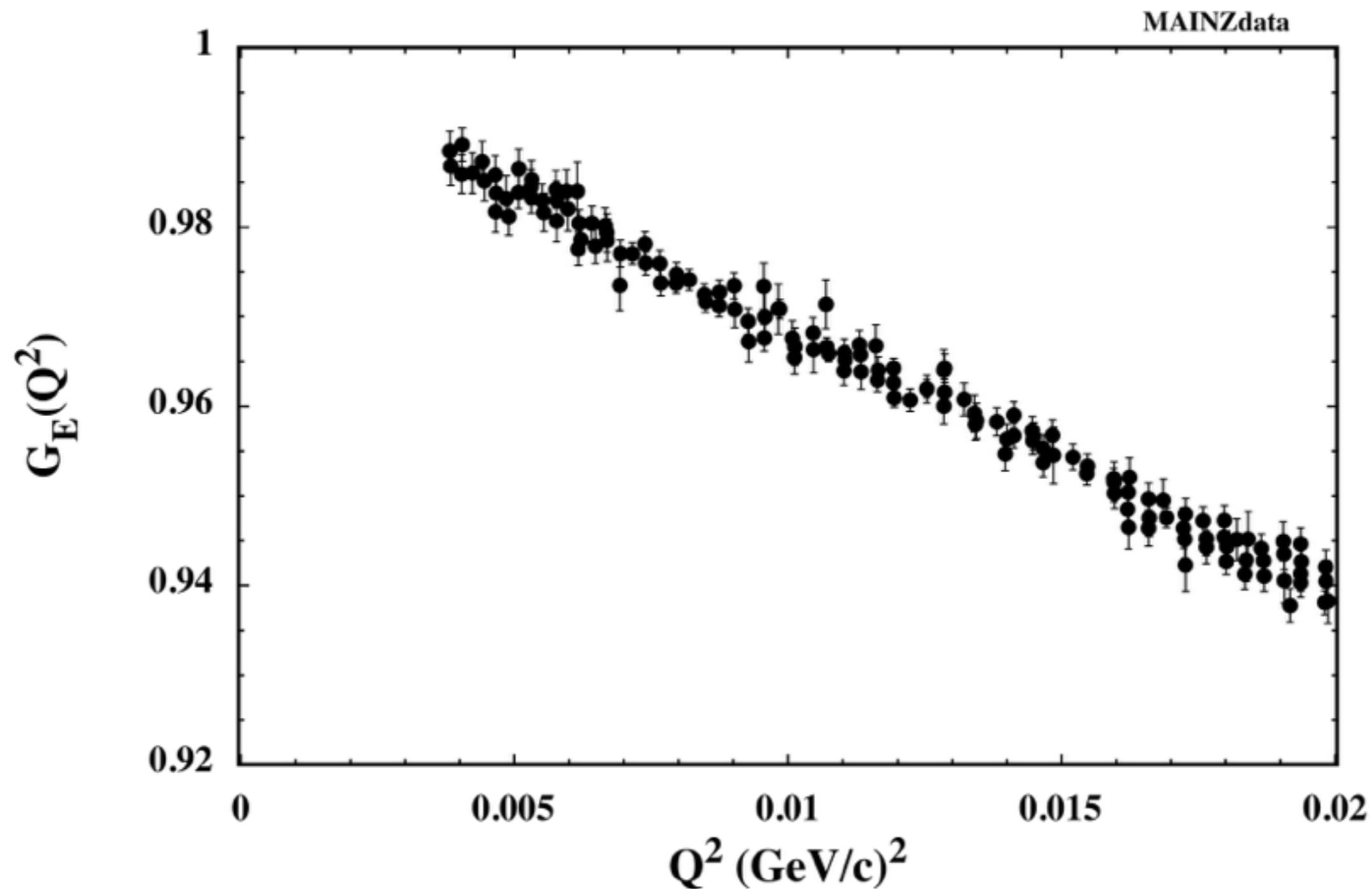
ill problem : higher order contribution



lower  $Q^2$  as possible

# Electron scattering at Low $Q^2$

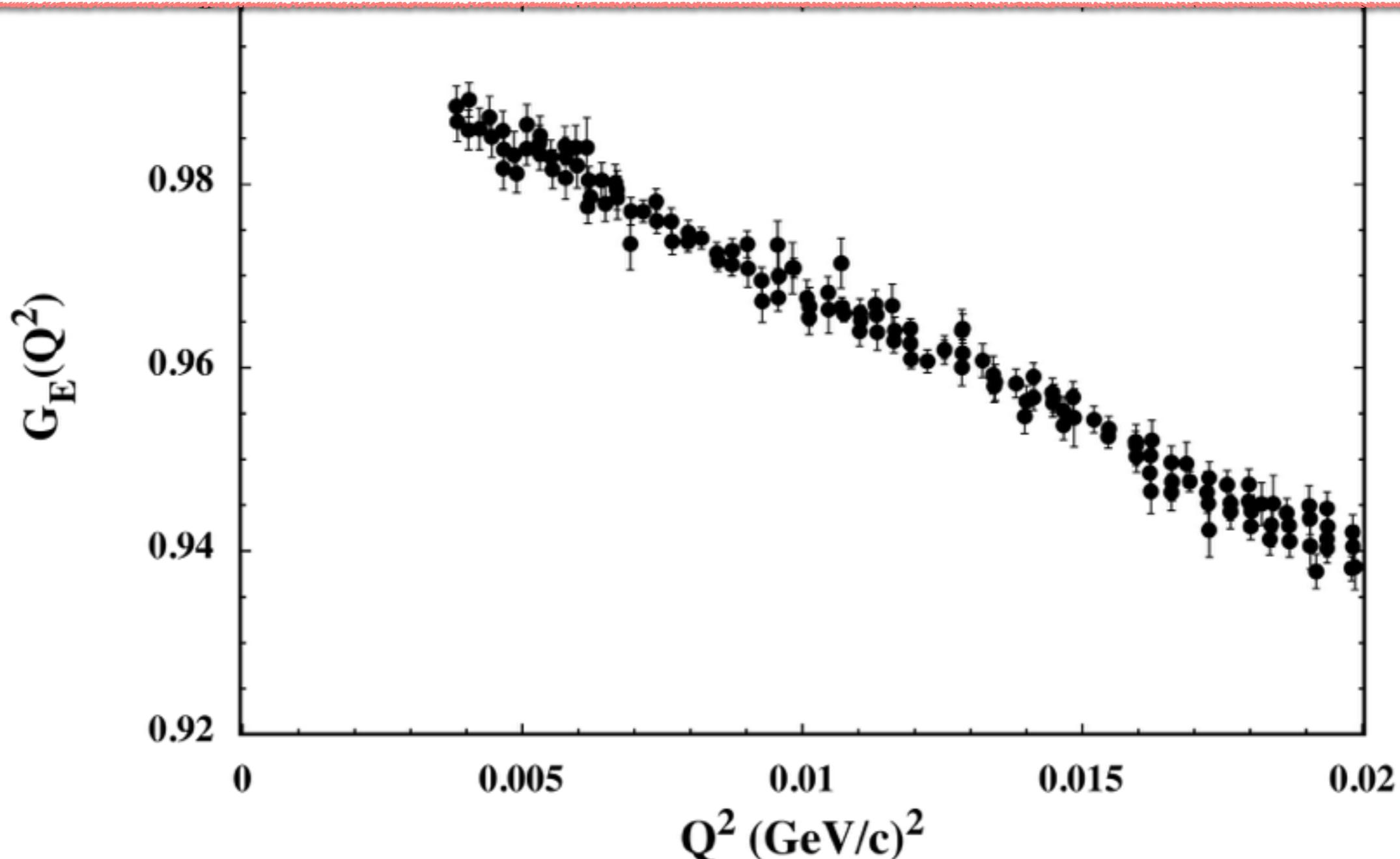
MIN2016, Kyoto  
July 31-Aug.2, 2016



# Electron scattering at Low $Q^2$

MIN2016, Kyoto  
July 31-Aug.2, 2016

$$G_E(Q^2) \sim 1 - \frac{\langle r^2 \rangle}{6} Q^2 + \frac{\langle r^4 \rangle}{120} Q^4 - \frac{\langle r^6 \rangle}{5040} Q^6 + \dots$$

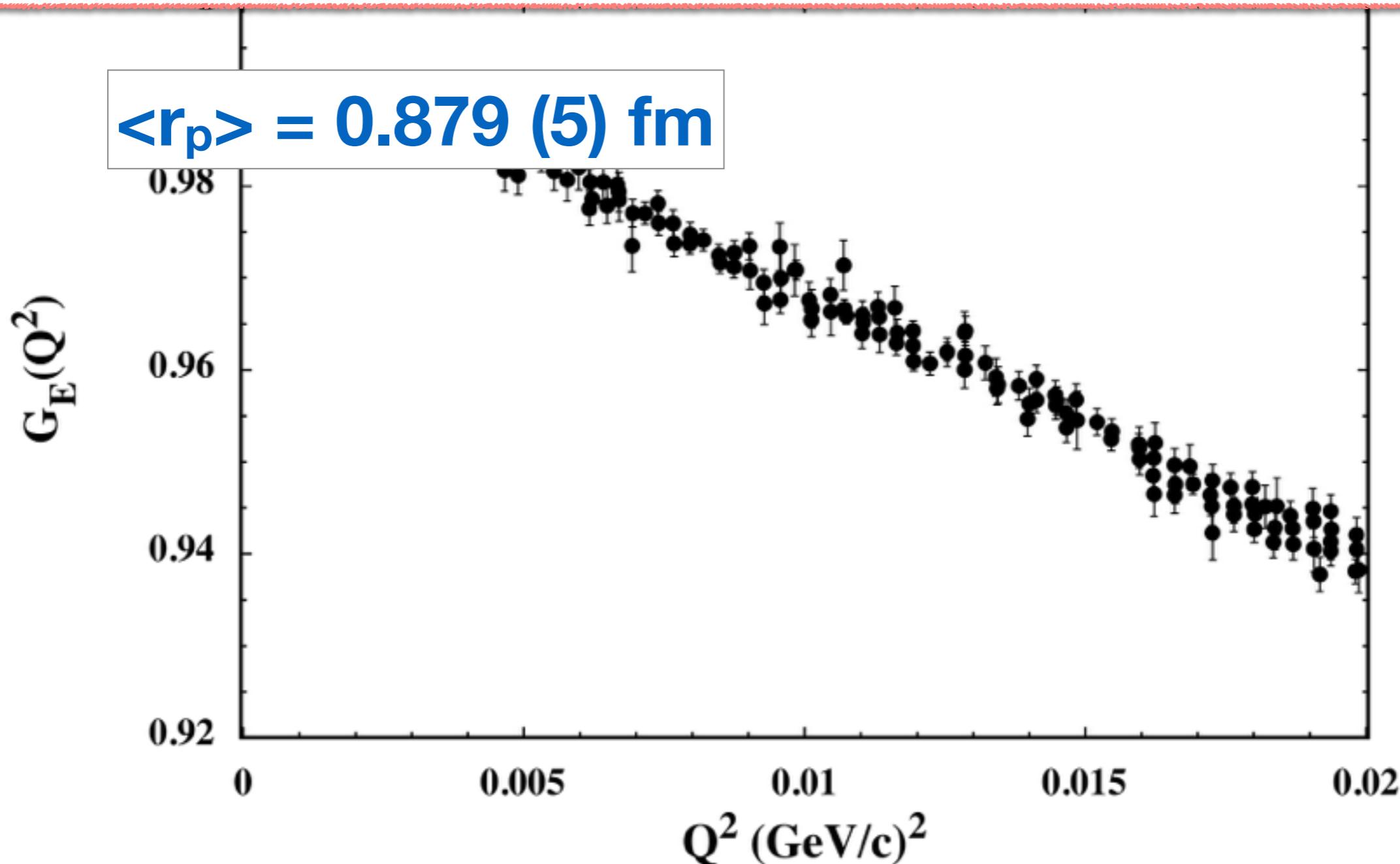


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MIN2016, Kyoto  
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$\langle r_p \rangle = 0.879 (5) \text{ fm}$

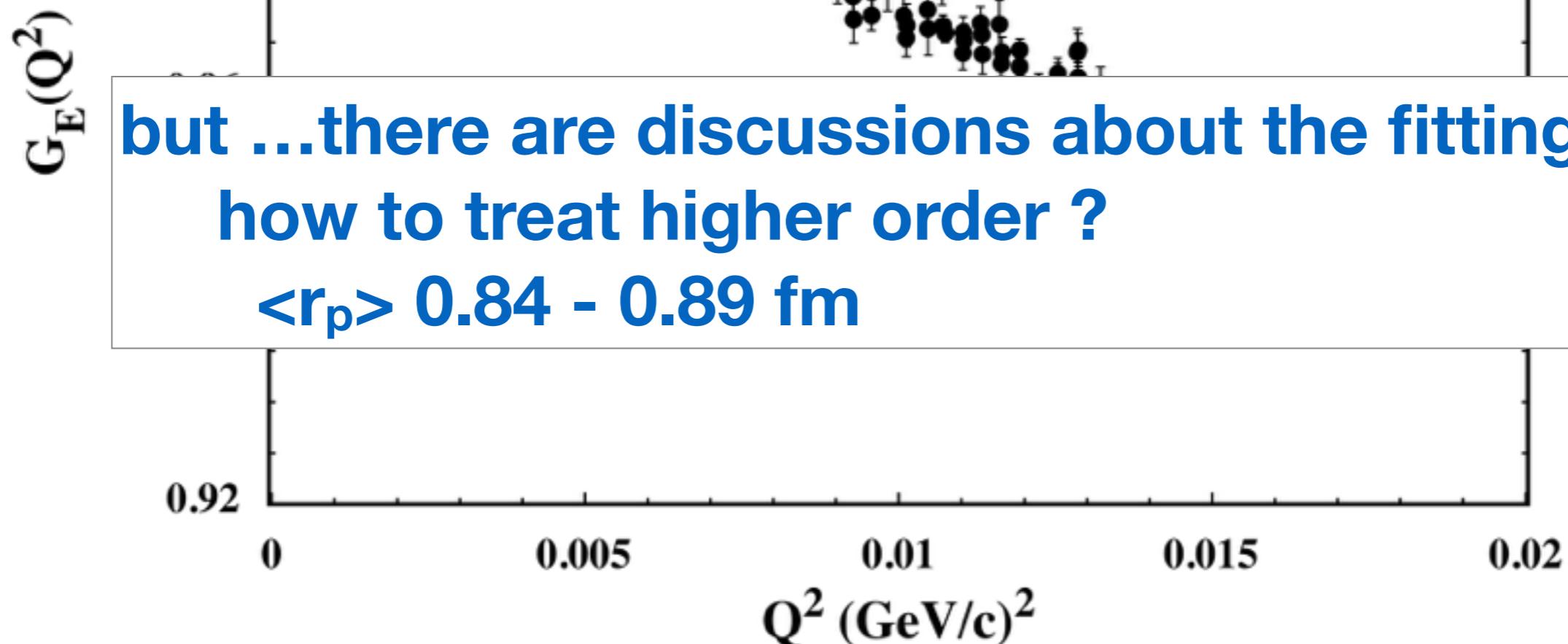


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MIN2016, Kyoto  
July 31-Aug.2, 2016

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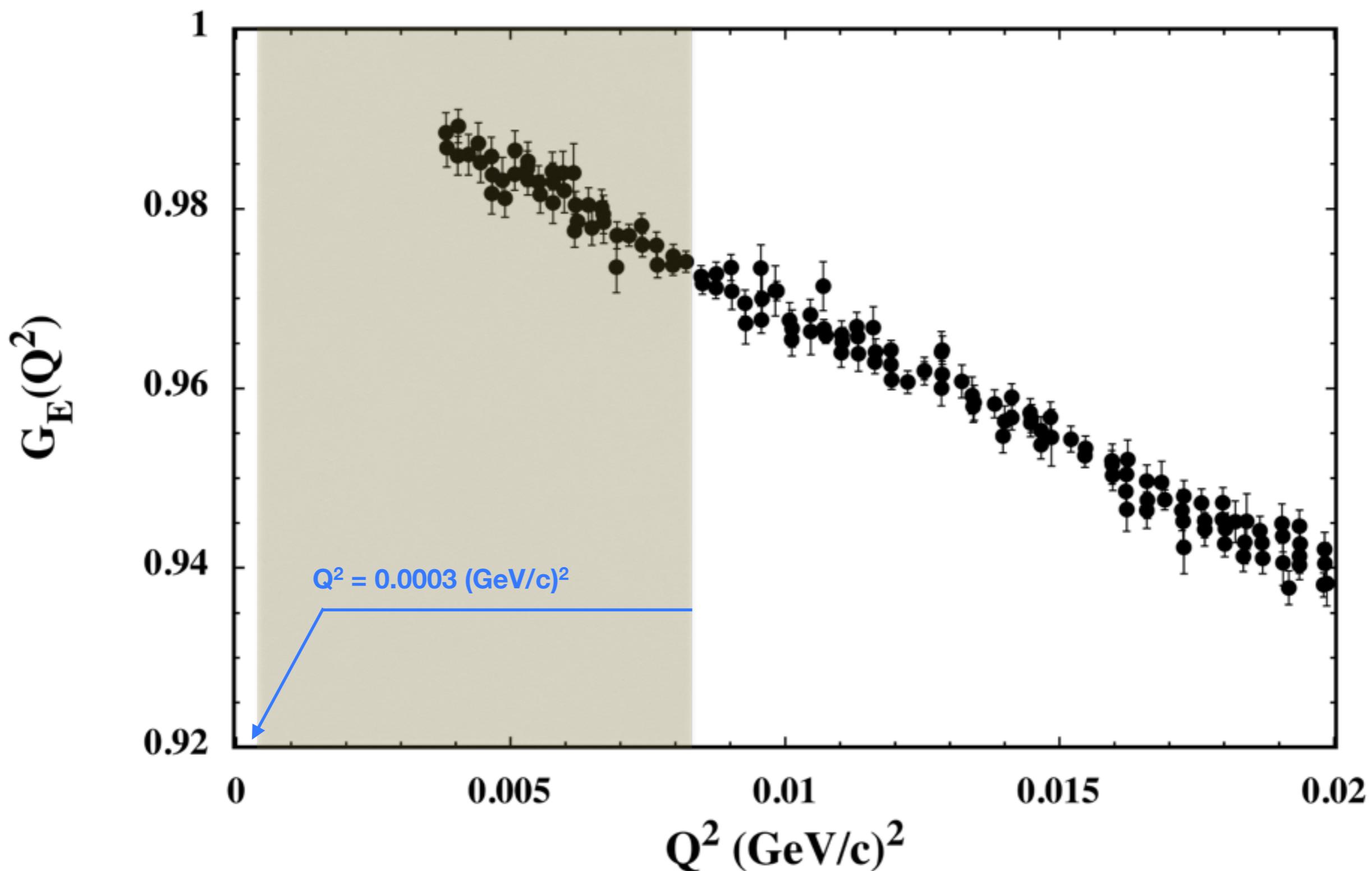
$\langle r_p \rangle = 0.879 (5) \text{ fm}$



# What are we going to do ???

MIN2016, Kyoto  
July 31-Aug.2, 2016

## Reduction of the higher order contribution



# What are we going to do ?

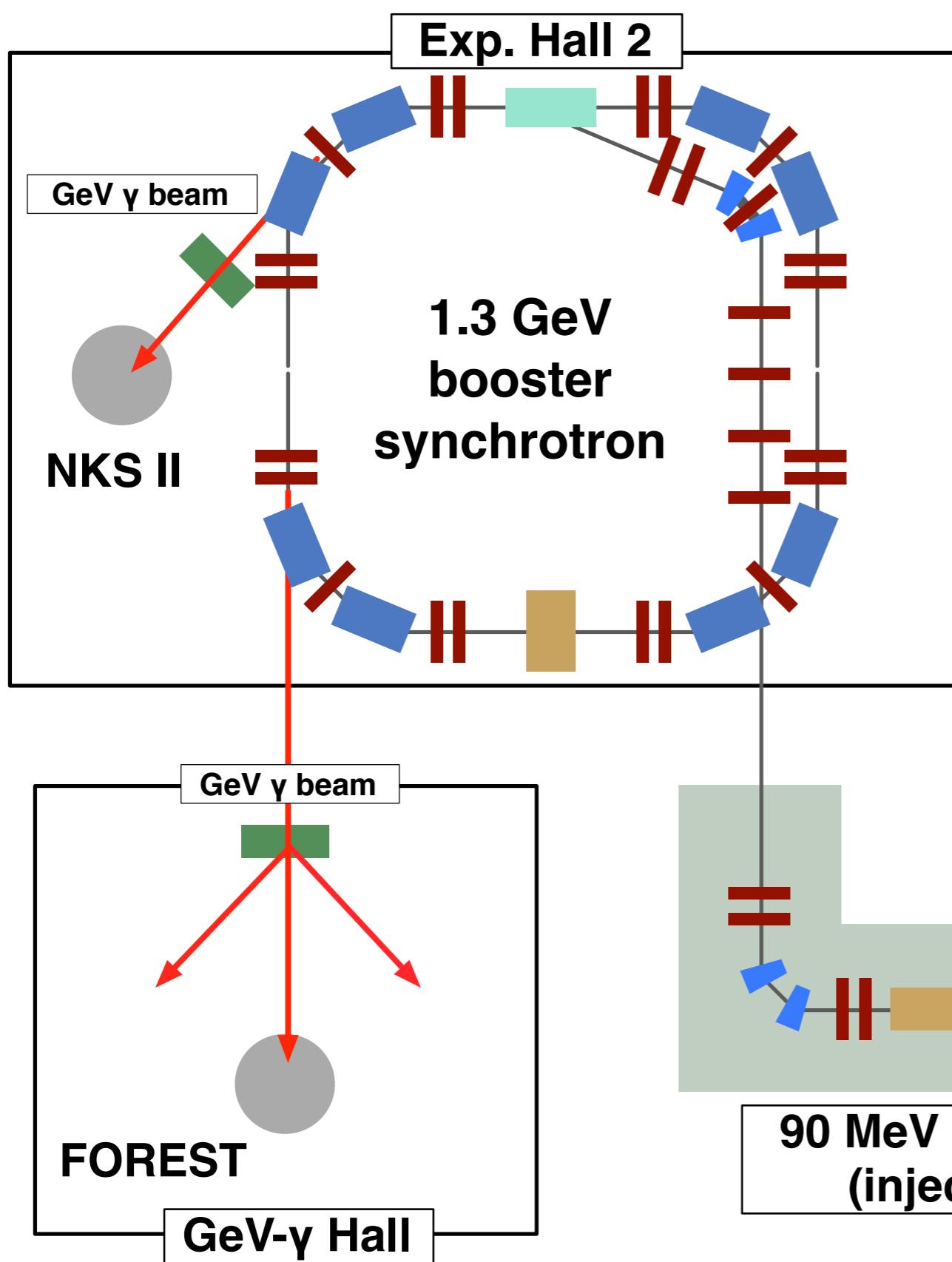
MIN2016, Kyoto  
July 31-Aug.2, 2016

	Mainz	Tohoku
$Q^2_{\min} \text{ (GeV/c)}^2$	0.004	0.0003
$E_e \text{ (MeV)}$	180 ~ 850	20 ~ 60
absolute $d\sigma/d\Omega$	x	o
$G_E/G_M$ separation	x	o

# Electron scattering at Lower $Q^2$

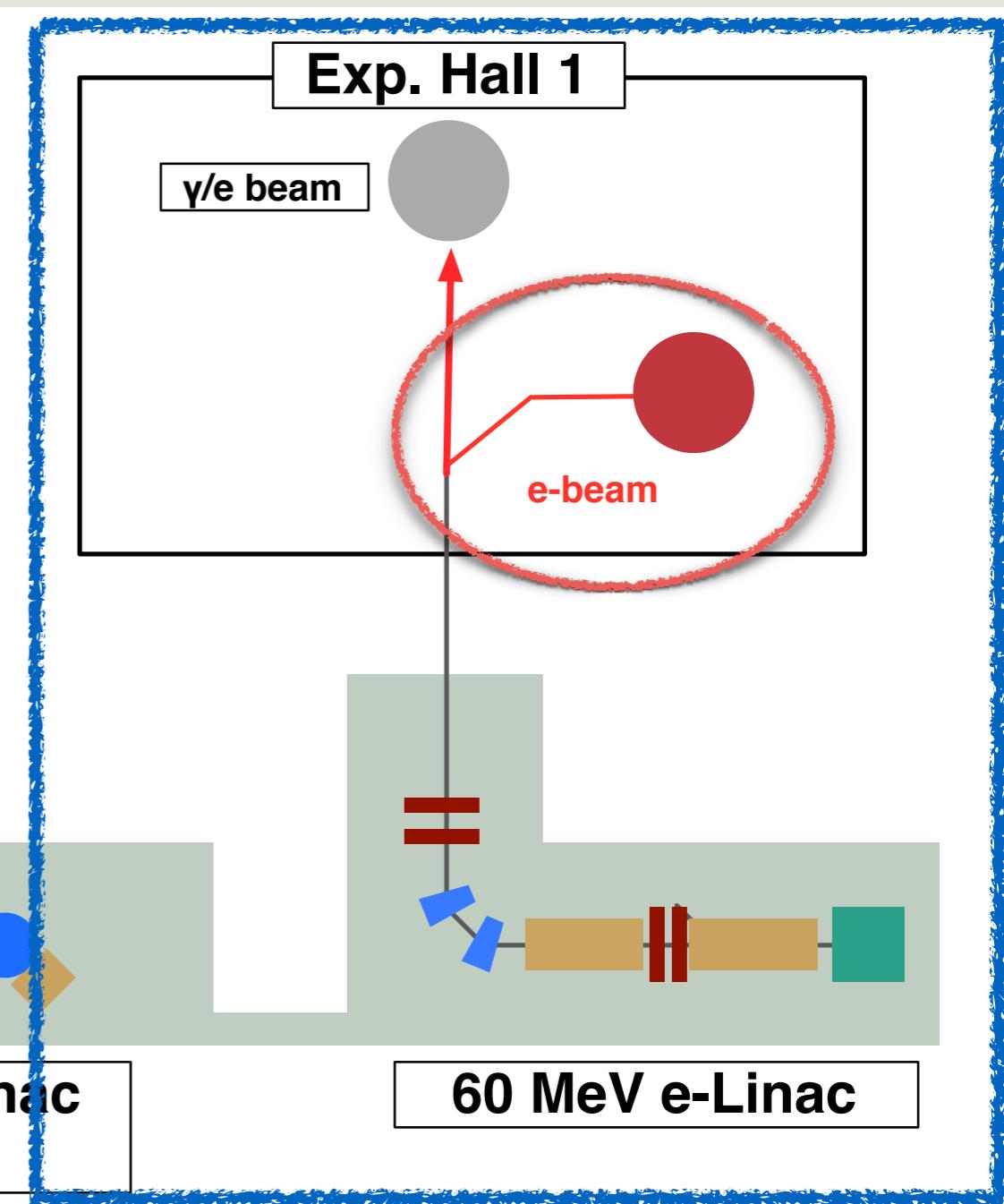
MIN2016, Kyoto  
July 31-Aug.2, 2016

Lab.		Ee	$\theta$	absolute $d\sigma/d\Omega$	$G_E, G_M$ separation
JLAB (USA)	Ultra-forward	1.1 - 2.2 GeV	1 - 4 deg.	O	X
Mainz (Germany)	lower Ee by Bremsstrah- lung	195, 330, 490 MeV		X	X
TOHOKU	low Ee	20 - 60 MeV	30 - 150 deg.	O	O



## “OLD” Low-Energy Electron Linac

$E_e : 20 \sim 60 \text{ MeV}$  variable  
 $I_e : 0 \sim 150 \mu\text{A}$



## Goal of our experiment

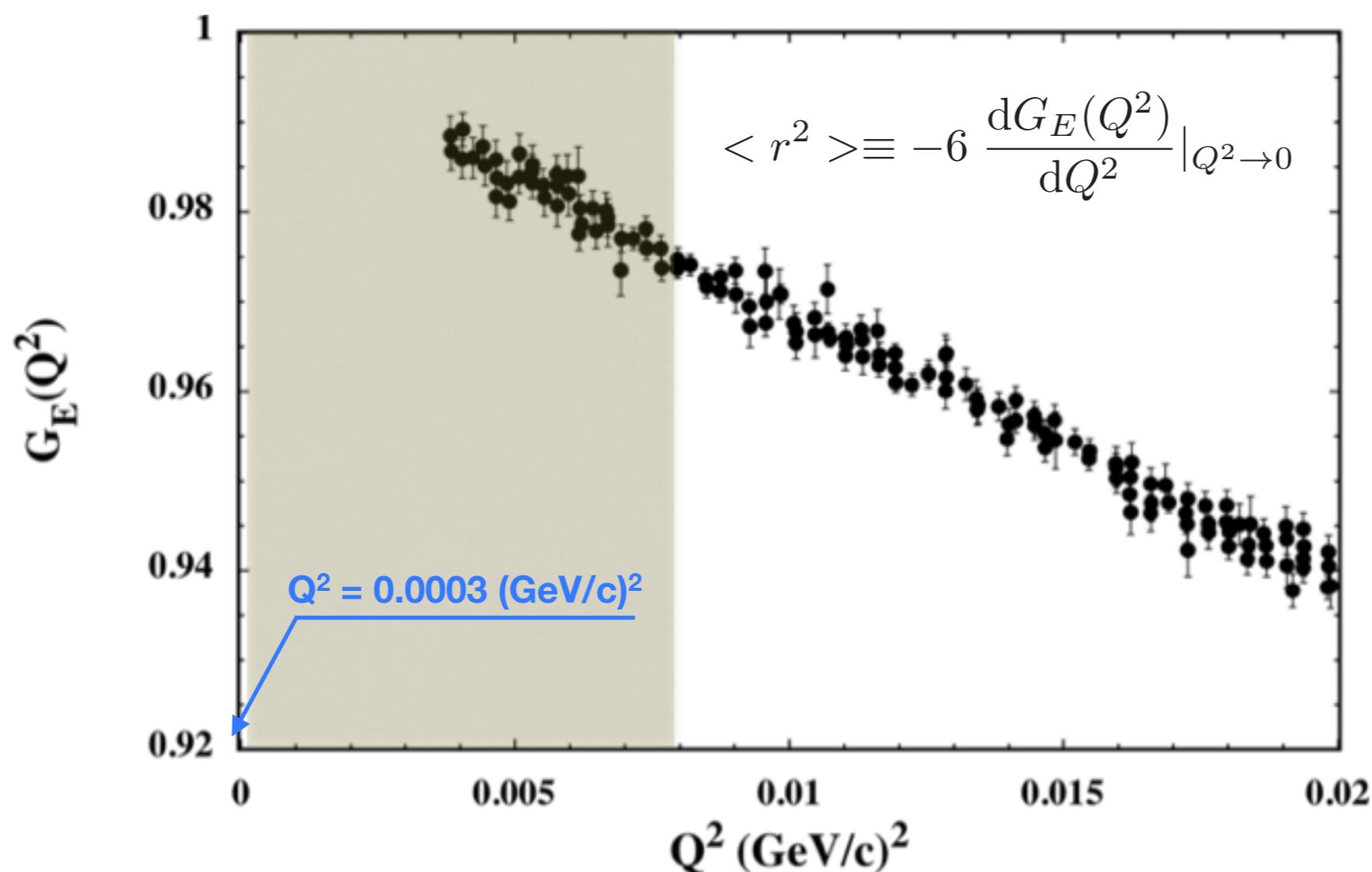
**$G_E(Q^2)$  measurements in  $0.0003 \leq Q^2 \leq 0.008 \text{ (GeV/c)}^2$**

## Our experiments

**Low energy electron beam ( $20 \leq E_e \leq 60 \text{ MeV}$ )**

**Absolute cross section measurement**

**Rosenbluth separation ( $G_E(Q^2)$ ,  $G_M(Q^2)$  separation)**

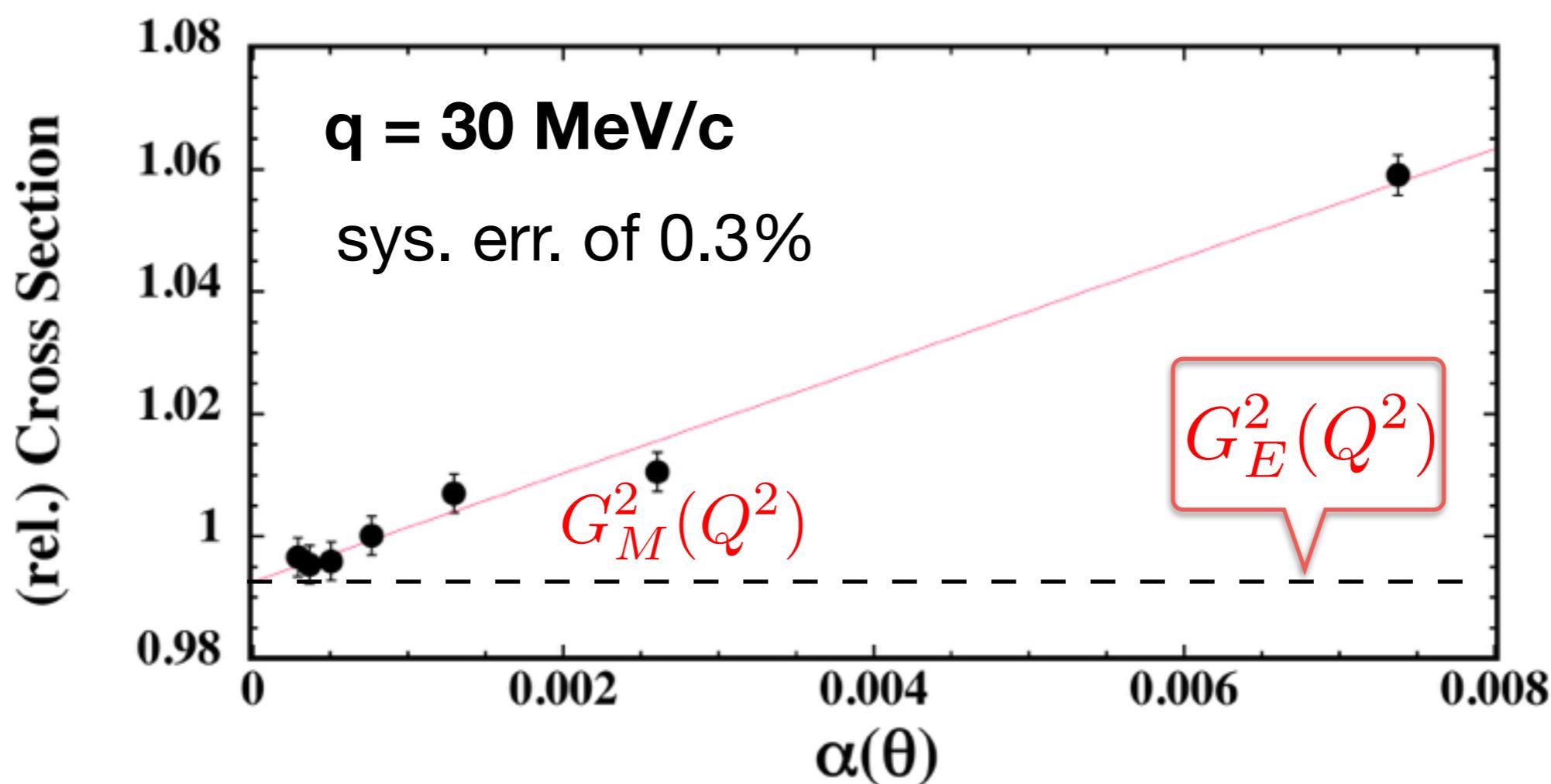


## Elastic cross section

$$\frac{d\sigma}{d\Omega} \propto G_E^2(Q^2) + \alpha(\theta) G_M^2(Q^2) \quad Q^2 = 4ee'\sin^2(\theta/2)$$

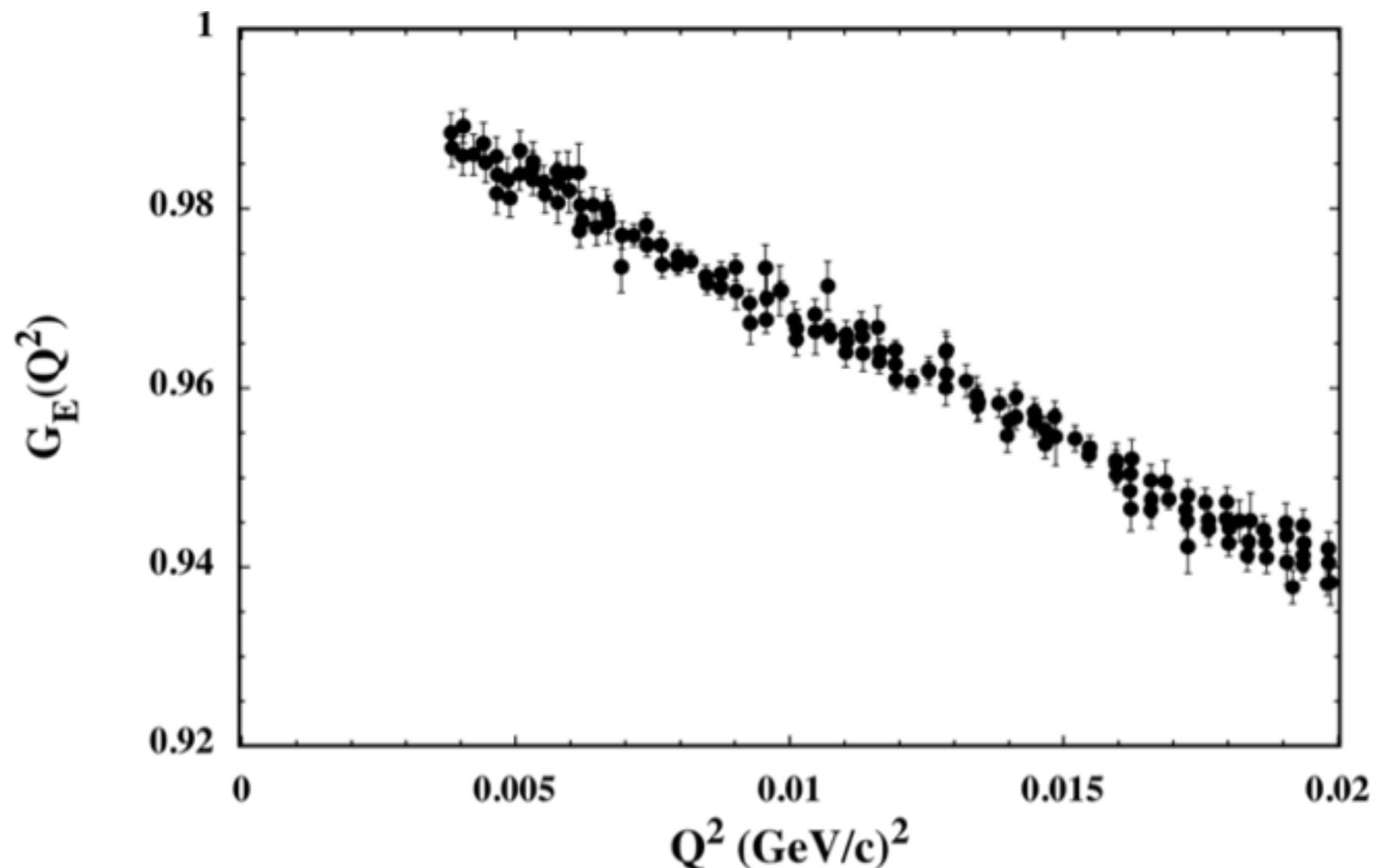
change  $\alpha(\theta)$  under fixed  $Q^2$   different electron beam energies

### Rosenbluth separation



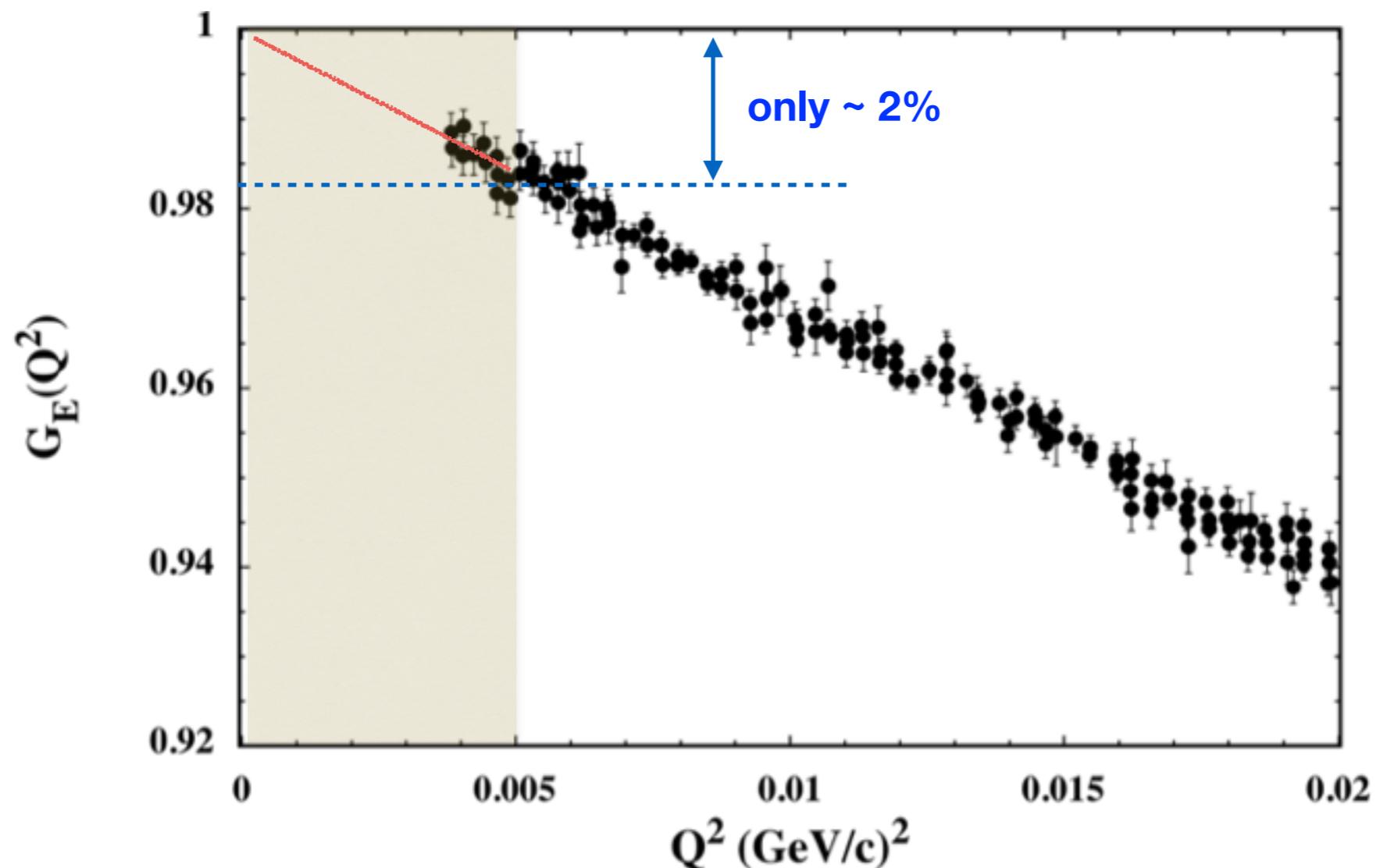
# A key of the e+p experiments at ULQ<sup>2</sup>

MIN2016, Kyoto  
July 31-Aug.2, 2016



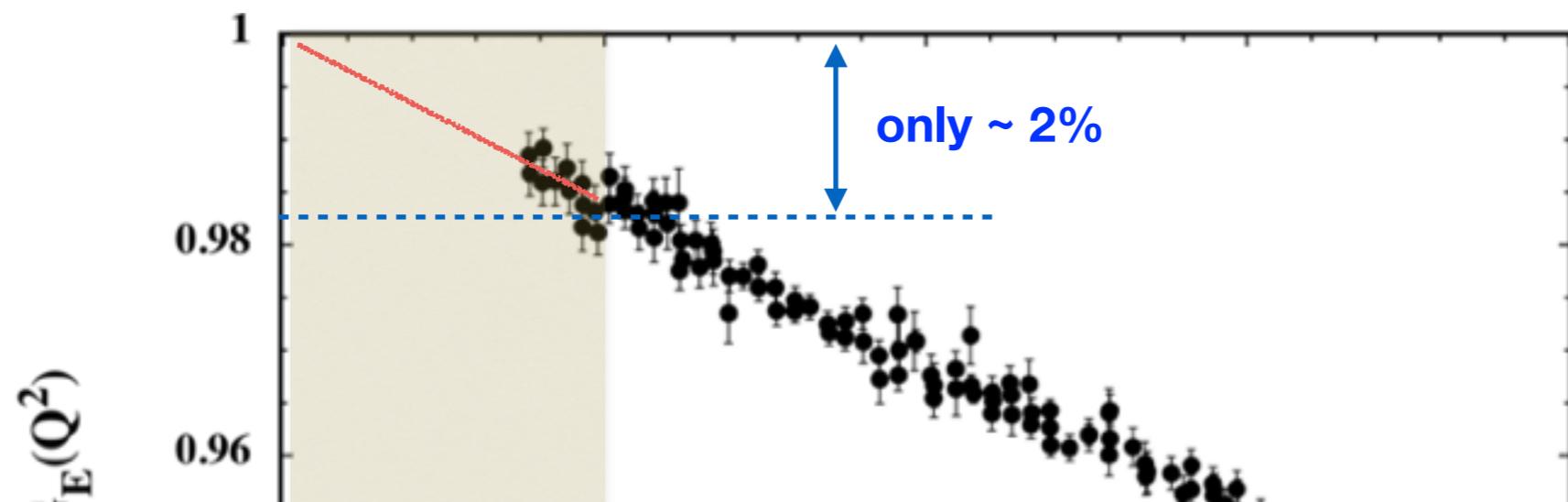
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MIN2016, Kyoto  
July 31-Aug.2, 2016

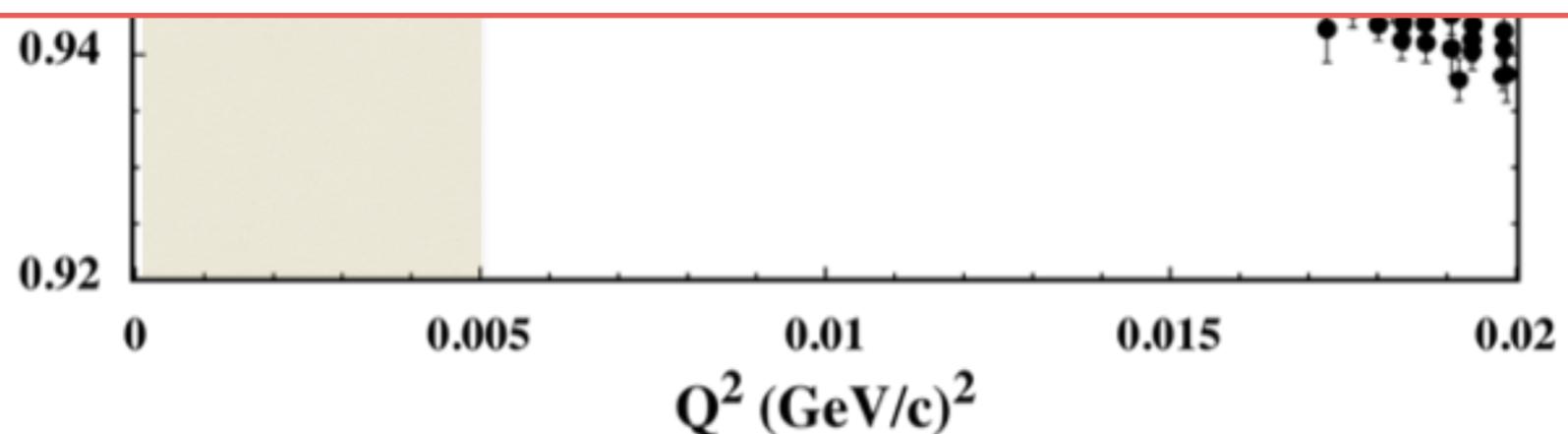


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MIN2016, Kyoto  
July 31-Aug.2, 2016

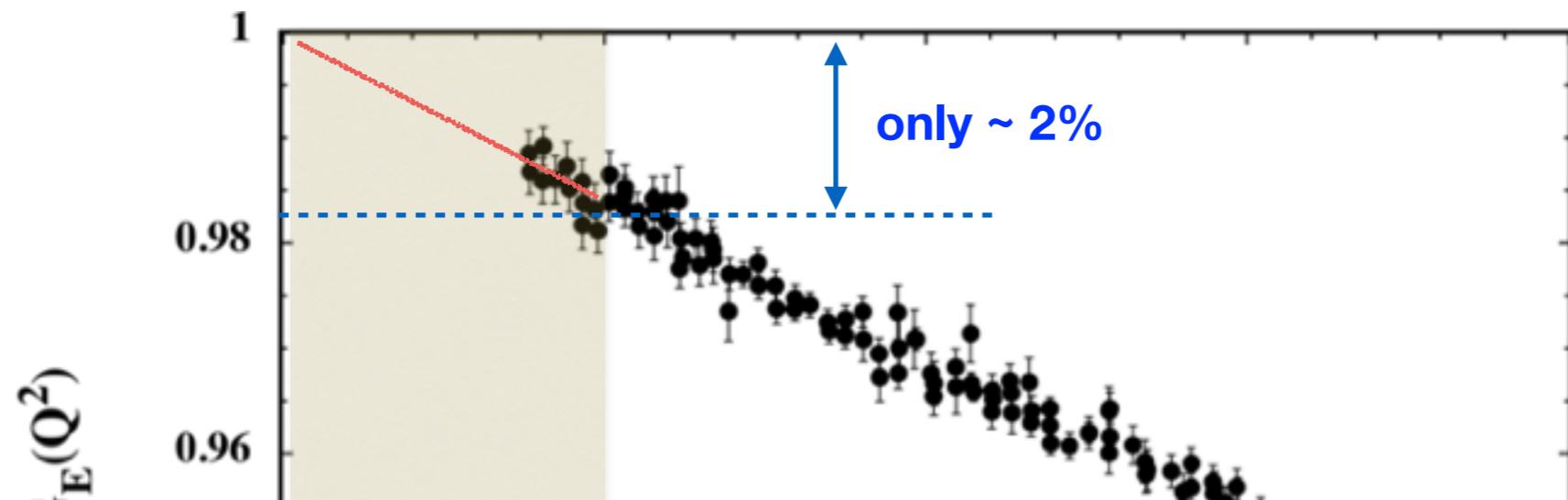


Uncertainty of  $G_E(Q^2)$  must be controlled to be an order of  $\Delta G_E/G_E \sim 10^{-3}$

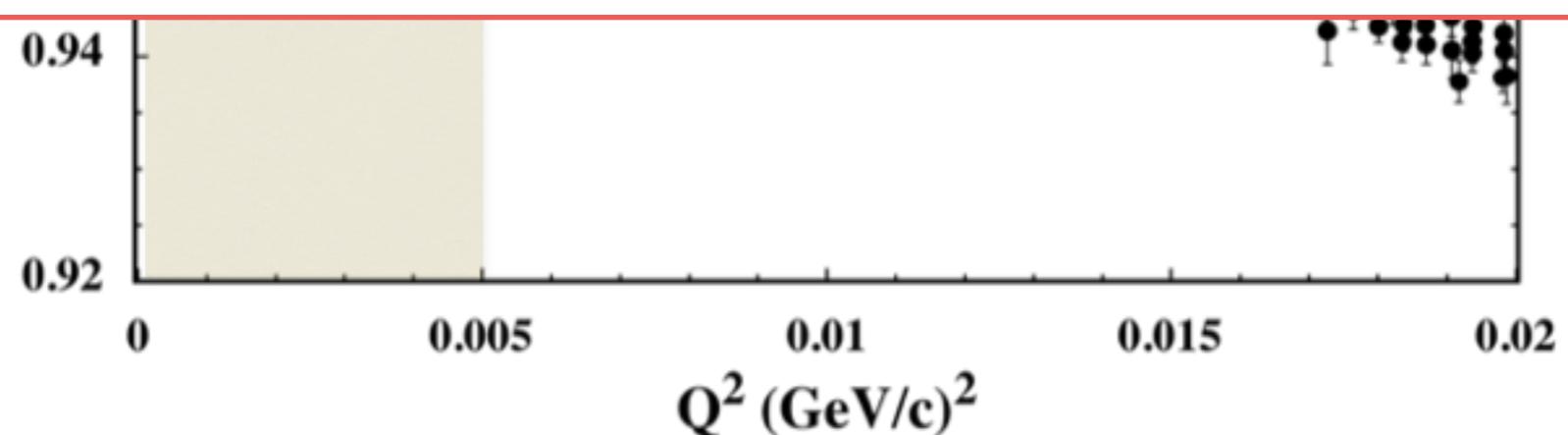


# A key of the e+p experiments at ULQ<sup>2</sup>

MIN2016, Kyoto  
July 31-Aug.2, 2016



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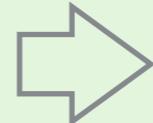
$$\frac{dN_{evt}}{d\Omega} = \frac{d\sigma}{d\Omega} \frac{N_{target}}{\text{target thickness}} \frac{N_{beam}}{\text{beam dose}} \frac{\Delta\Omega}{\text{spectrometer acceptance}}$$

Statistics : at least  $> 10^6$  for each  $(E_e, \theta)$  measurements

Target thickness

Beam dose at various intensities

Acceptance at various scattering angle



accuracy of  $\sim 10^{-3}$   
not obvious !

## Relative measurement for $^{12}\text{C}(\text{e},\text{e})^{12}\text{C}$ and $\text{p}(\text{e},\text{e})\text{p}$

$$\frac{dN^{e^{12}C}/d\Omega}{dN^{ep}/d\Omega} = \frac{d\sigma^{e^{12}C}/d\Omega}{d\sigma^{ep}/d\Omega} \cdot \frac{N_{target}^{^{12}C}}{N_{target}^H}$$

$$\frac{dN_{evt}}{d\Omega} = \frac{d\sigma}{d\Omega} N_{target} [N_{beam} \Delta\Omega]$$

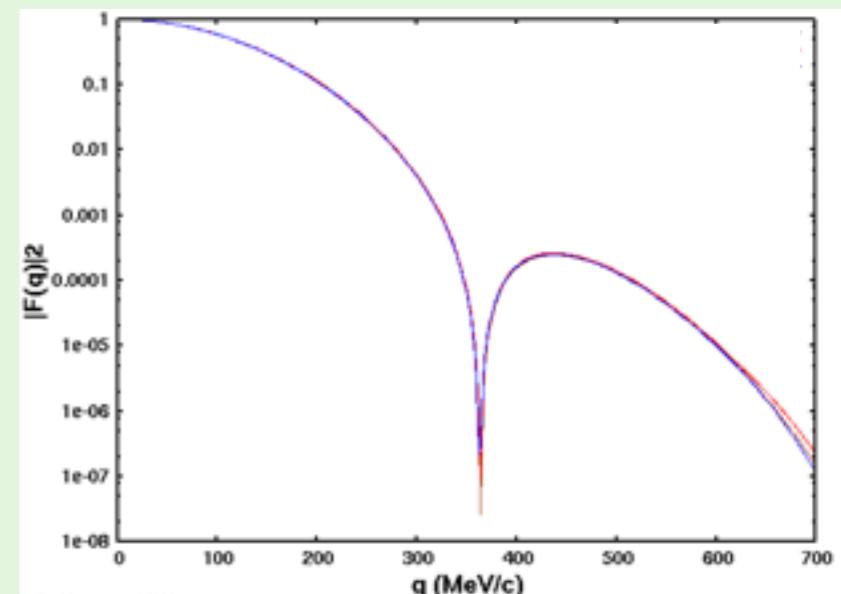
Canceled out  
in relative measurements

- 1) RMS charge radius (or  $\rho(r)$ ) of  $^{12}\text{C}$  ??
- 2)  $^{12}\text{C}(\text{e},\text{e})^{12}\text{C}$ ,  $\text{p}(\text{e},\text{e})\text{p}$  by kinematics ??
- 3) change of C/H ratio by beam irradiation ??

## 1) $^{12}\text{C}$ : “standard” nucleus for (e,e')

$\mu$ -Xray  
electron scattering

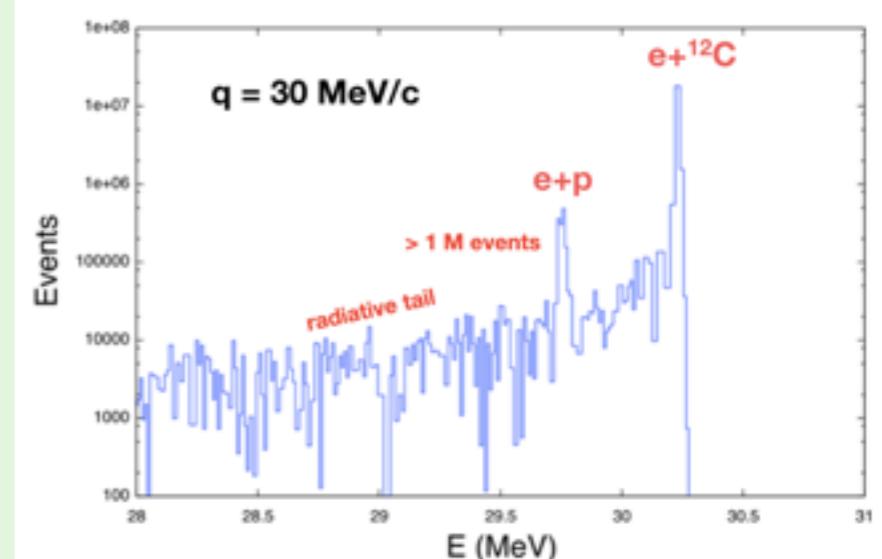
$$\frac{\Delta \langle r_{^{12}\text{C}}^2 \rangle^{1/2}}{\langle r_{^{12}\text{C}}^2 \rangle^{1/2}} \sim 3 \times 10^{-3}$$



## 2) $^{12}\text{C}(\text{e},\text{e})^{12}\text{C}$ , p(e,e)p by kinematics

$\Delta E = 0.2 - 4 \text{ MeV}$   
for  $q = 20 - 90 \text{ MeV}/c$

$$\Delta p/p \sim 10^{-3}$$



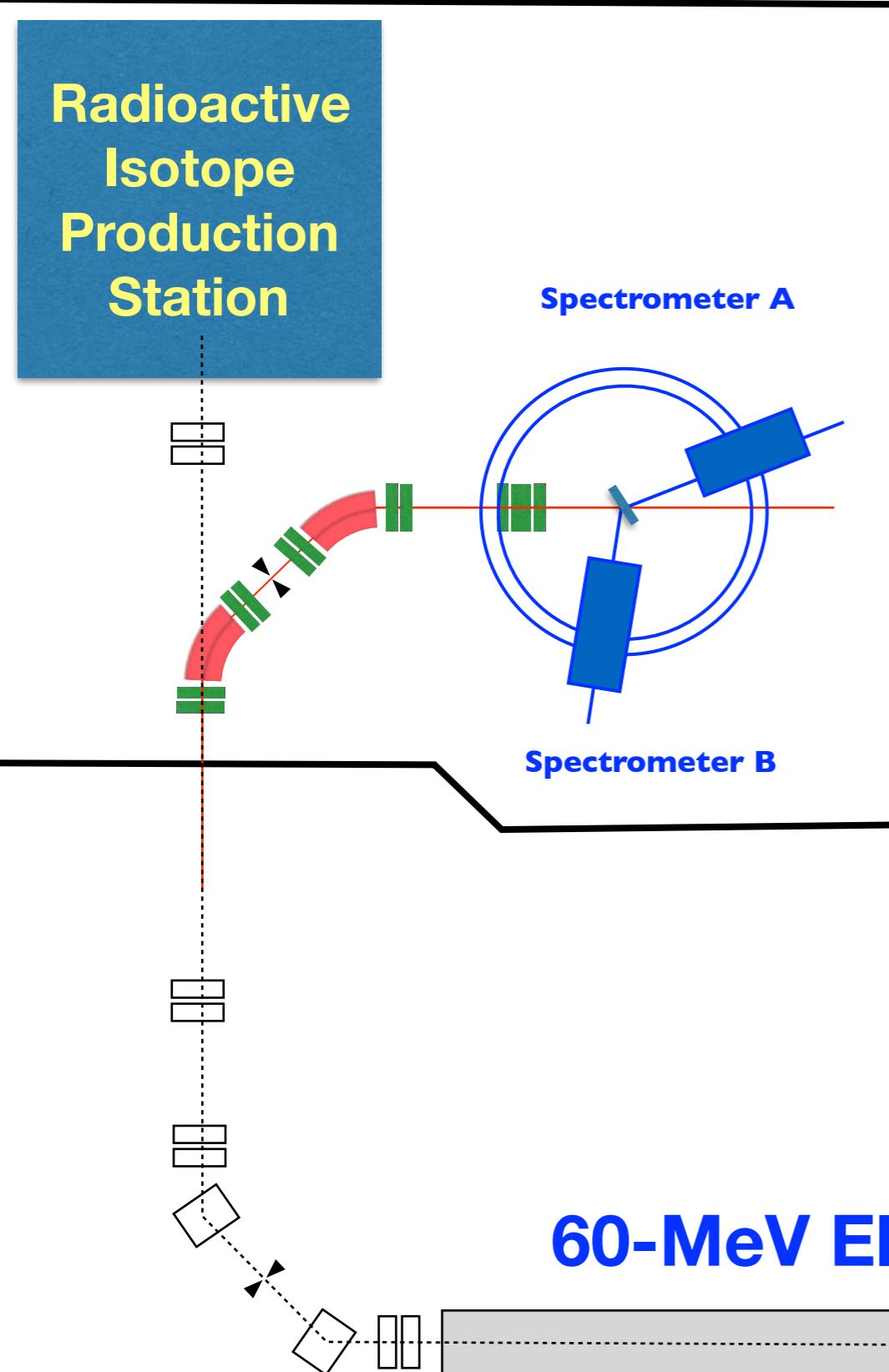
## 3) no severe damage of target is expected

large cross section :  $\frac{d\sigma}{d\Omega} \propto 1/q^4$   
 $I_e \sim 1 \text{ nA} - 1 \mu\text{A}$

# Experimental setup at ULQ<sup>2</sup> exp.

MIN2016, Kyoto  
July 31-Aug.2, 2016

22 m



$E_e = 20 \sim 60 \text{ MeV}$   
 $I_e \sim 1 \text{ nA} - 1 \mu\text{A}$

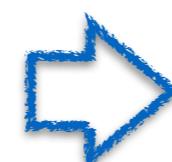
- 1) new beam line
  - 2) two magnetic spectrometers
- Rosenbluth measurements  
Luminosity monitoring

$\text{CH}_2$  target ( $\sim 0.1 \text{ mm t}$ )  
 $\Delta p/p \sim 1 \times 10^{-3}$

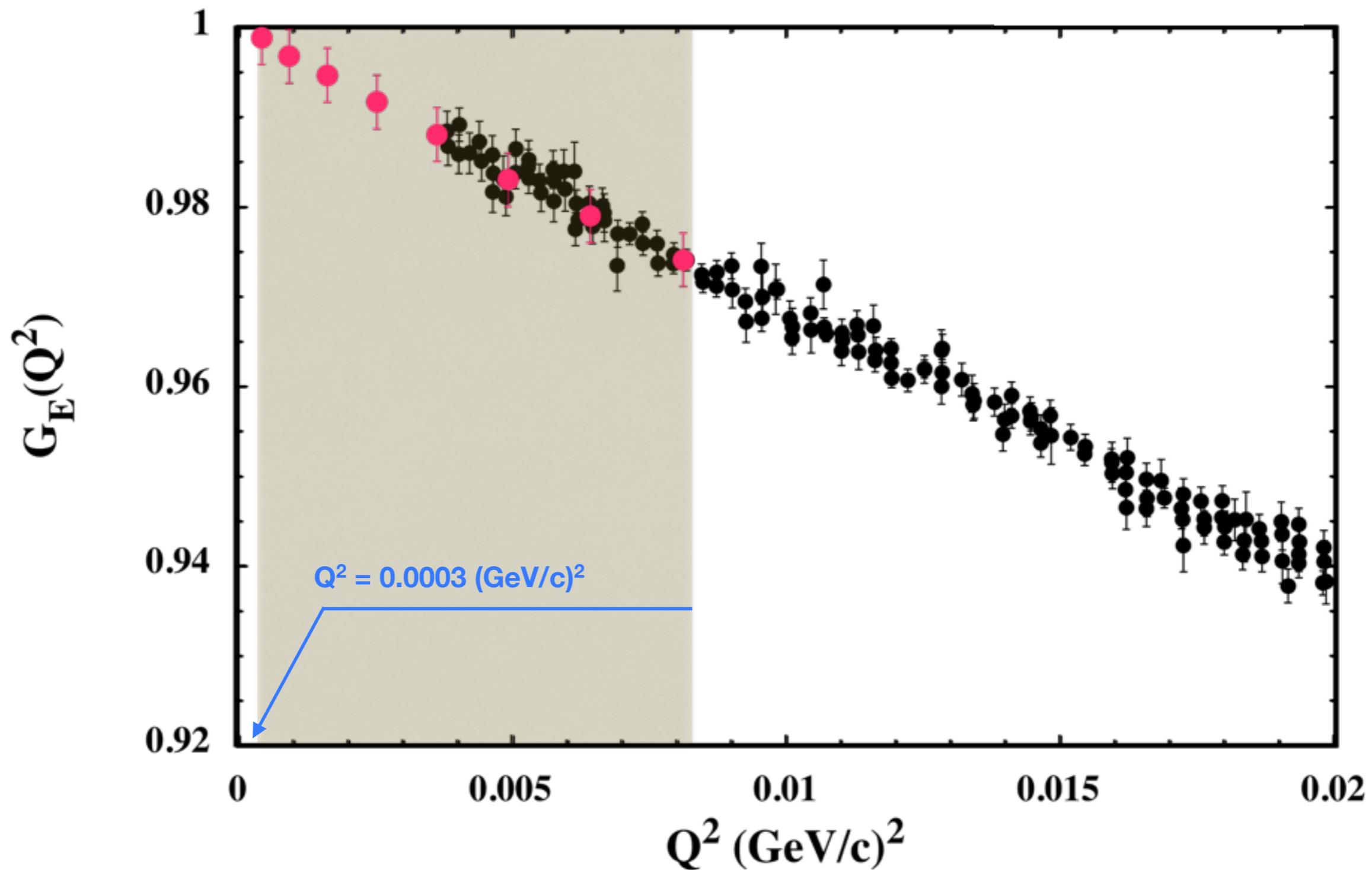
# Rosenbluth-Separated $G_E(Q^2)$ at ULQ $^2$

MIN2016, Kyoto  
July 31-Aug.2, 2016

Absolute cross section  
Rosenbluth separation



$G_E(Q^2)$



- 1) elastic e+p scattering at ultra-low  $Q^2$  region
- 2)  $G_E(Q^2)$  at  $0.0003 \leq Q^2 \leq 0.008 \text{ (GeV/c)}^2$
- 3)  $G_E$  is extracted by the Rosenbluth separation
- 4) absolute cross section measurement  
relative to  $^{12}\text{C}(e,e)^{12}\text{C}$  : sys. err.  $\sim 3 \times 10^{-3}$
- 5)  $E_e = 20 - 60 \text{ MeV}$ ,  $\theta = 30 - 150^\circ$
- 6) constructing of new beam line, and spectrometers
- 7) the experiments will start in 2019