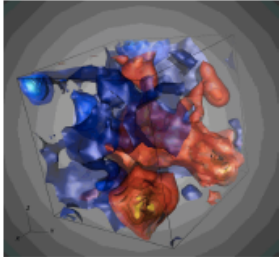


Baryon Interactions from Lattice QCD

QCD vacuum

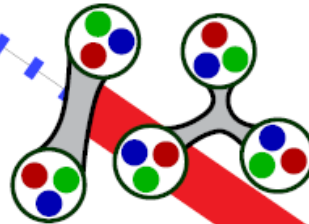


$$\mathcal{L}_{\text{QCD}} = \bar{\psi} [i\gamma^\mu D_\mu - m] \psi - \frac{1}{2} \text{Tr} G_{\mu\nu} G^{\mu\nu}$$

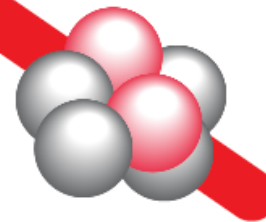
Baryons



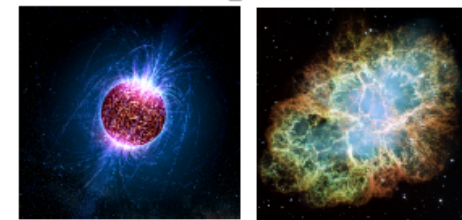
Interactions



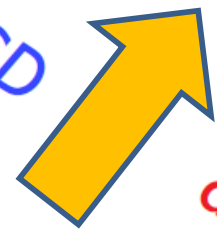
Nuclei



**Neutron Stars
Supernovae
Nucleosynthesis**



Lattice QCD



ab-initio nuclear calc.

Tetsuo Hatsuda (iTHEMS, RIKEN)

NFQCD @ YITP (June 14, 2018)

Di-Omega and all that from Lattice QCD

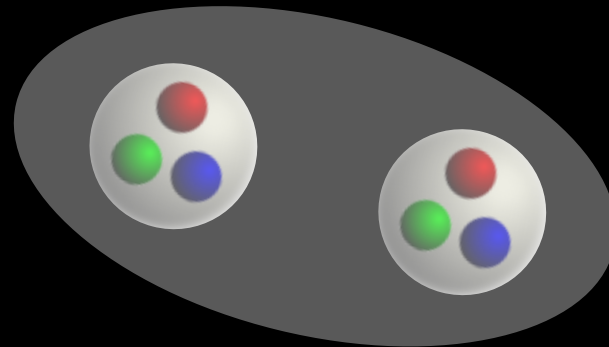
Gongyo+ [HAL QCD Coll.],
Phys. Rev. Lett. 120 (2018) 212001

Baryon



Proton, Neutron,
Hyperons, ...

Dibaryon



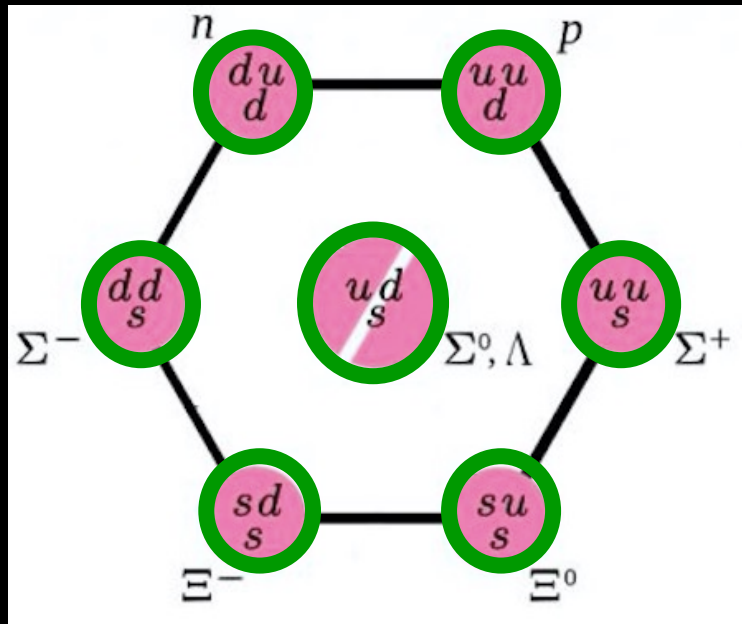
Deuteron (1931, Urey)
No more?

Contents

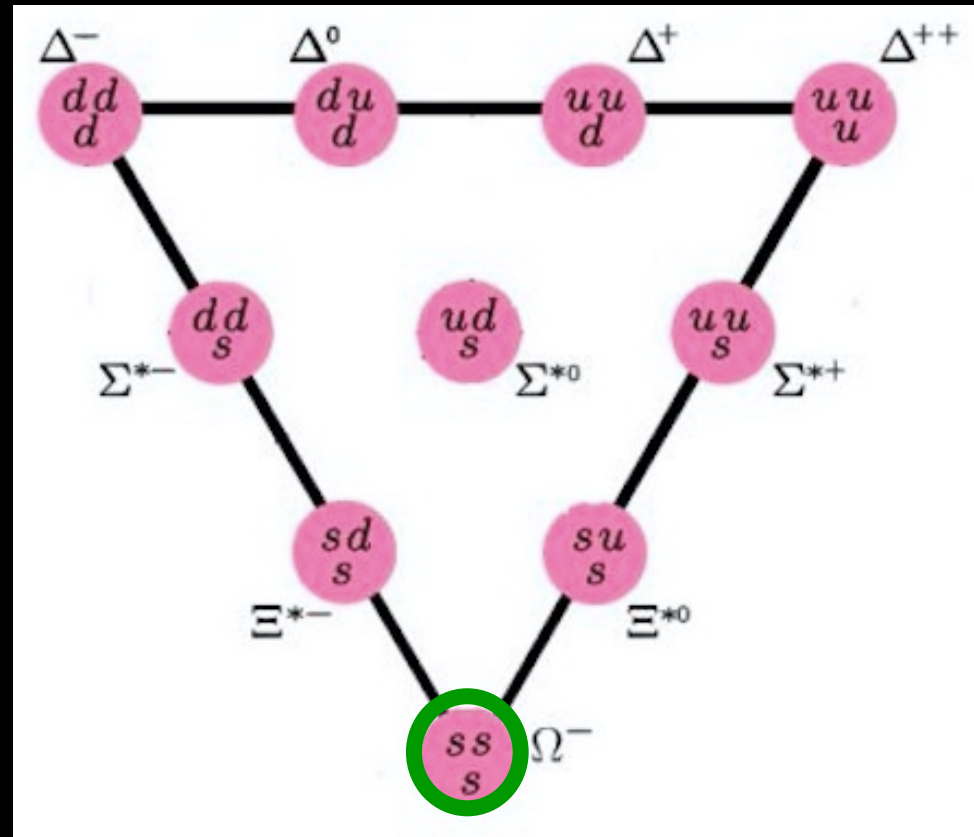
- I. Baryon on the Lattice
- II. Baryon interactions on the Lattice
- III. $\Lambda\Lambda$, $N\Xi$, $\Omega\Omega$ from lattice QCD
- IV. Observations at RHIC and LHC

Flavor SU(3) Classification : B=1

8 (Octet)



10 (Decuplet)

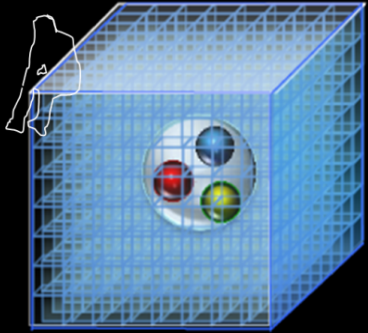


Ω^- (1672)

Only weak decay ($\rightarrow \Lambda K, \Xi \pi$)

Mean Life $\sim 0.8 \times 10^{-10}$ sec

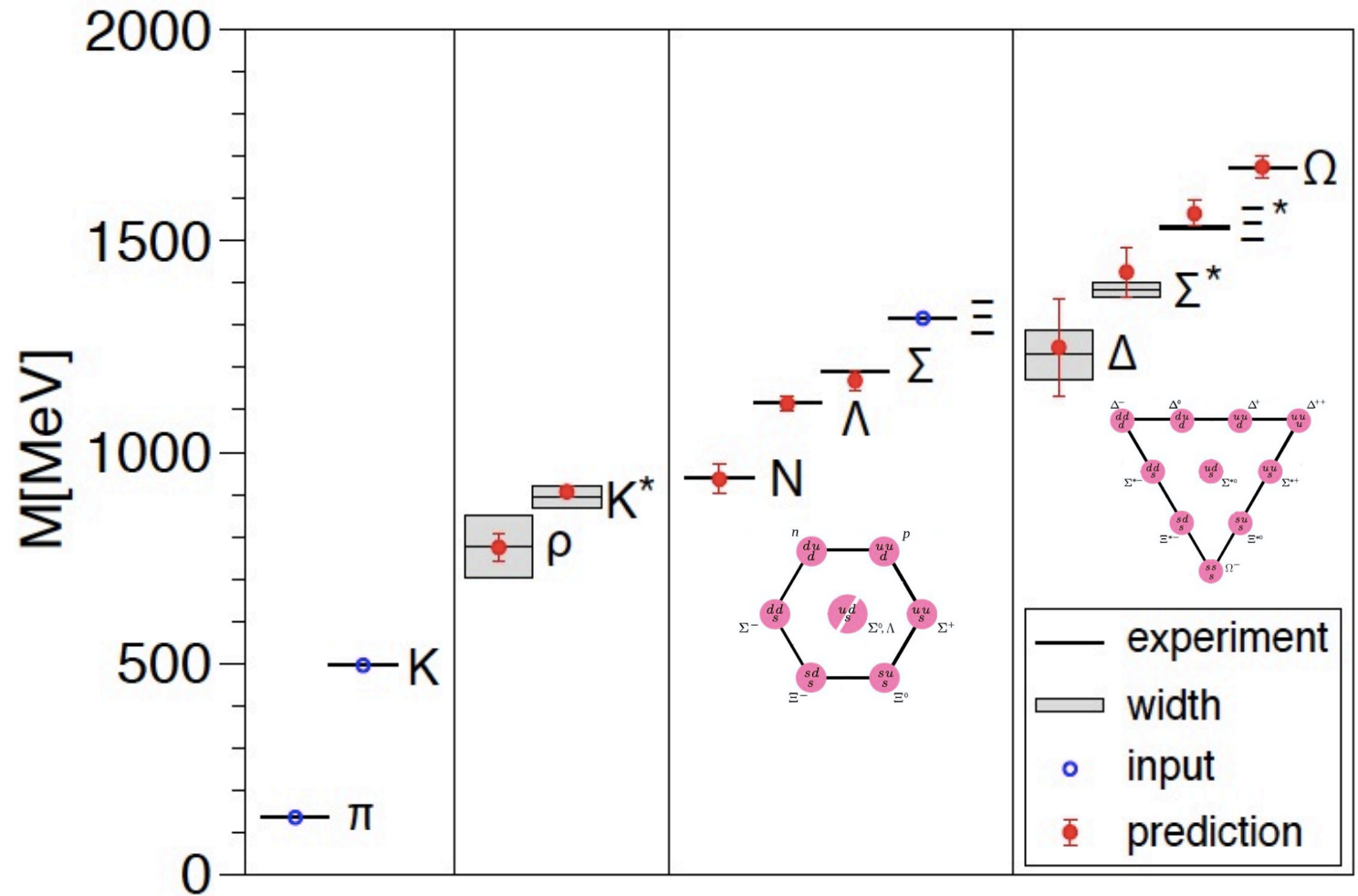
Octet and Decuplet Baryons from Lattice QCD



$a_{\min} = 0.065 \text{ fm}$

$L_{\max} = 4.1 \text{ fm}$

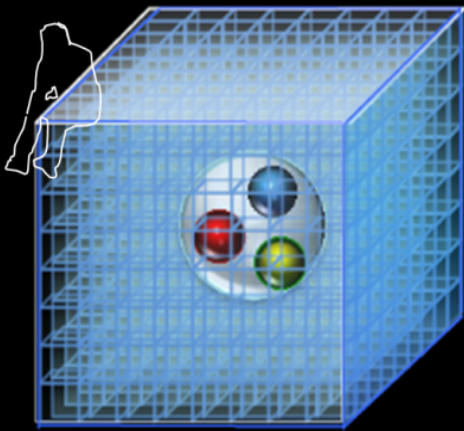
$m_{\pi, \min} = 190 \text{ MeV}$



taken from Fodor and Hoelbling, Rev. Mod. Phys. 84 (2012) 449

Lattice QCD with isospin breaking

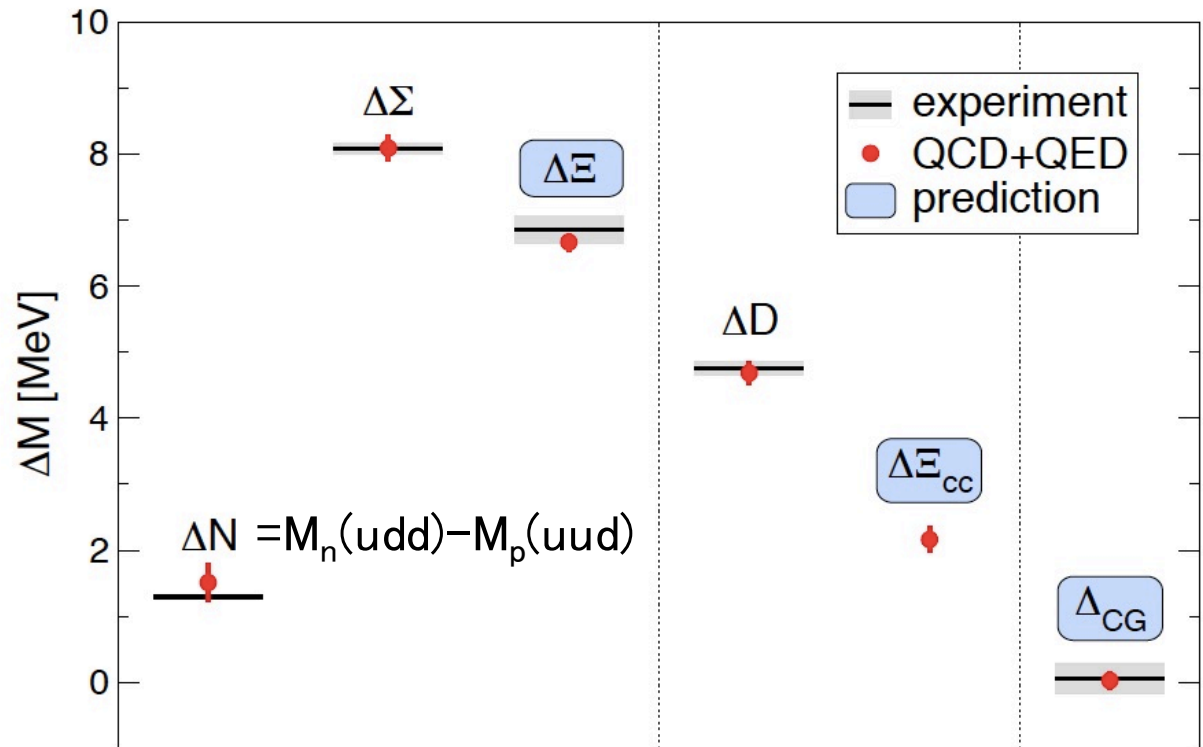
BMW Coll., Science 347 (2015) 1452



$$a_{\min} = 0.054 \text{ fm}$$

$$L_{\max} = 8 \text{ fm}$$

$$m_{\pi, \min} = 190 \text{ MeV}$$

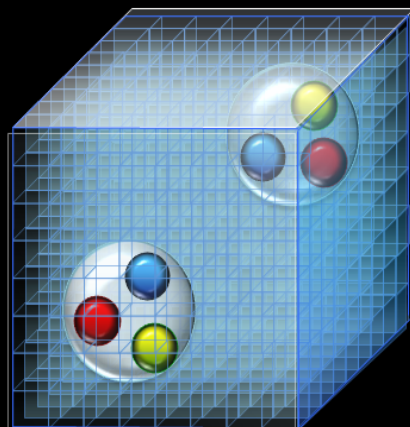
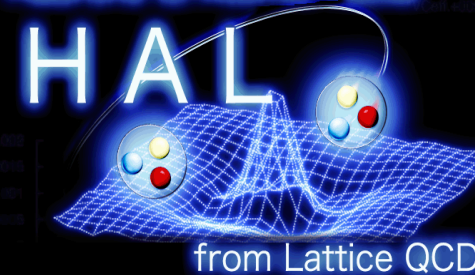


$$(M_n - M_p)_{\text{lat}} = 1.51(16)(23) \text{ MeV}$$

$$(M_n - M_p)_{\text{exp}} = 1.29 \text{ MeV}$$

BB Interactions from LQCD at almost physical point

Hadrons to Atomic nuclei



$a = 0.085 \text{ fm}$

$L = 8.1 \text{ fm}$

$m_\pi = 146 \text{ MeV}$

$M_K = 525 \text{ MeV}$



K computer RIKEN (10 PFlops)

$S=0$

$S=-1$

$S=-2$

$S=-3$

$S=-4$

$S=-5$

$S=-6$

NN

$N\Lambda, N\Sigma$

$\Lambda\Lambda, \Lambda\Sigma, \Sigma\Sigma, N\Xi$

$\Lambda\Xi, \Sigma\Xi$

$\Xi\Xi$

$\Xi\Omega$

$\Omega\Omega$



EXP

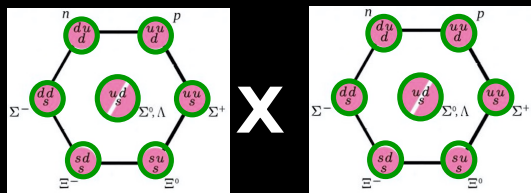
rich data

LQCD

better S/N

Flavor SU(3) Classification of BB system

c.f. Dyson & Young,
PRL 14 (1965)



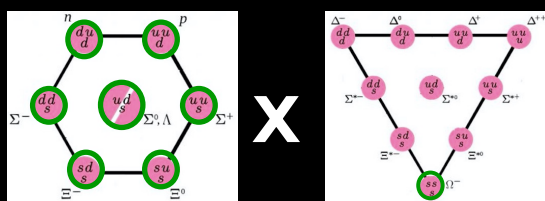
$$8 \times 8 = 27 + 8_s + 1 + 10^* + 10 + 8_a$$

$$H_{\Lambda\Lambda-NE-\Lambda\Sigma} (J=0)$$

Jaffe (1977)

$$D_{pn} (J=1)$$

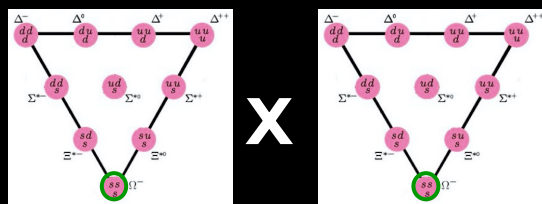
Rarita-Schwinger (1941)



$$8 \times 10 = 35 + 8 + 10 + 27$$

$$N\Omega (J=2)$$

Goldman et al (1987)



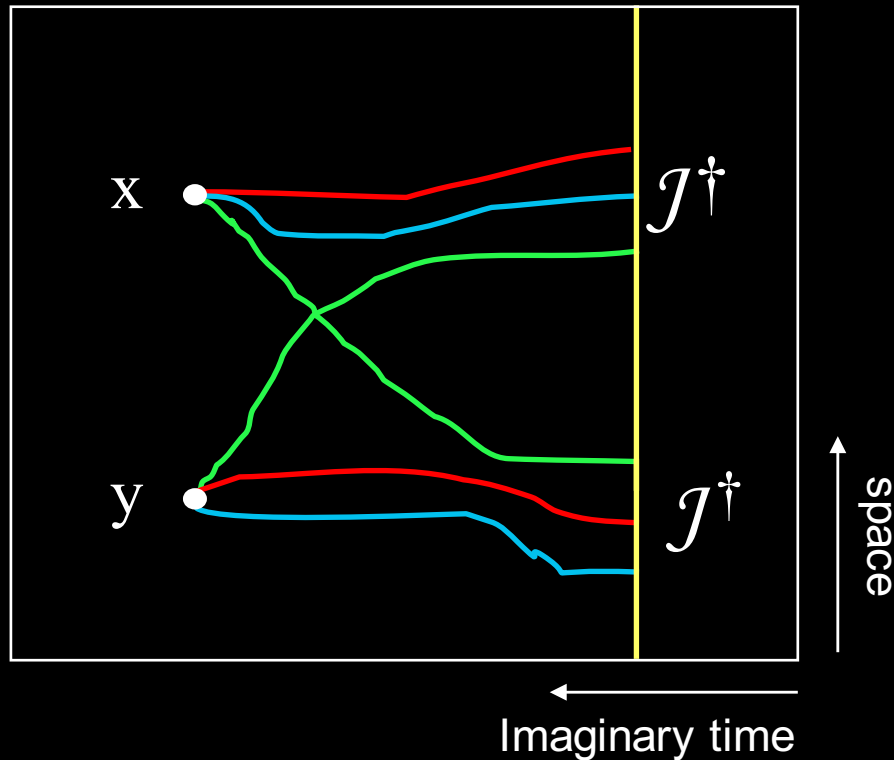
$$10 \times 10 = 28 + 27 + 35 + 10^*$$

$$\Omega\Omega (J=0)$$

Di-Omega (strangeness = -6)

Zhang et al (1997)

Scattering problem in LQCD

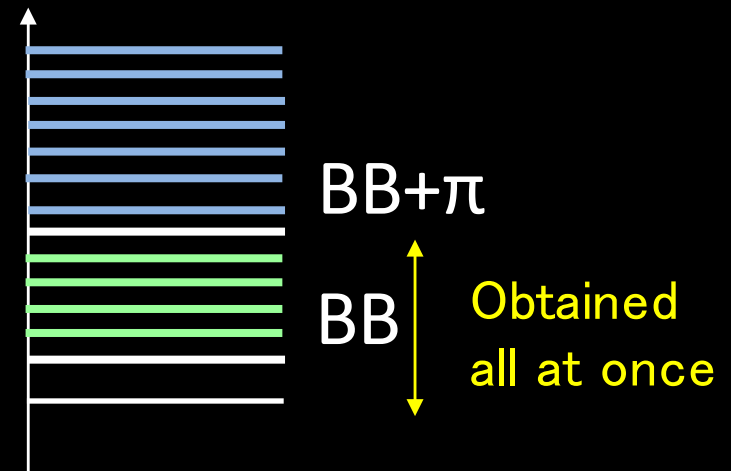


$$\begin{aligned} & \langle N_1(\mathbf{x}, t) N_2(\mathbf{y}, t) \mathcal{J}_1^\dagger(0) \mathcal{J}_2^\dagger(0) \rangle \\ &= \sum_n \langle 0 | N_1(\mathbf{x}) N_2(\mathbf{y}) | n \rangle a_n e^{-E_n t} \\ & \xrightarrow{t > t^*} \phi(\mathbf{r}, t) = \sum_{n < n^*} b_n \phi_n(\mathbf{r}) e^{-E_n t} \end{aligned}$$

HAL QCD Method

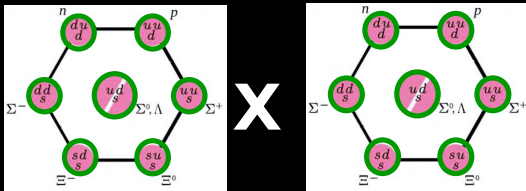
$\phi(\mathbf{r}, t) \rightarrow$ 2PI kernel (T=U+GUT)
 \rightarrow phase shift, binding energy

Ishii, Aoki & Hatsuda, PRL 99 (2007) 022001
 Ishii et al. [HAL QCD Coll.], PLB 712 (2012) 437



Flavor SU(3) Classification of BB system

c.f. Dyson & Young,
PRL 14 (1965)

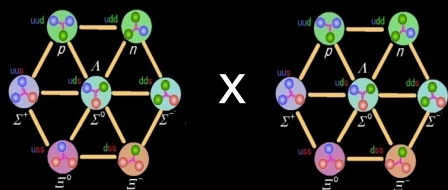


$$8 \times 8 = 27 + 8_s + 1 + 10^* + 10 + 8_a$$

8x8 BB interactions with flavor basis: $V_C(r)$

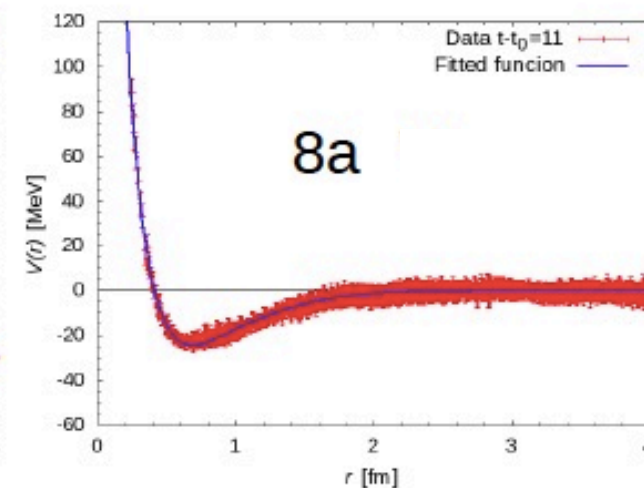
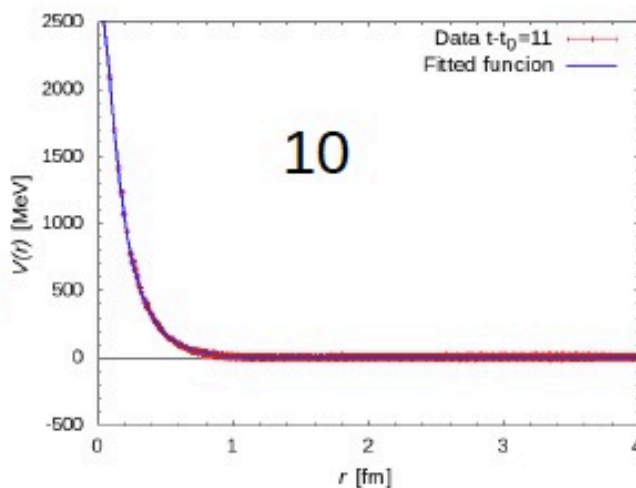
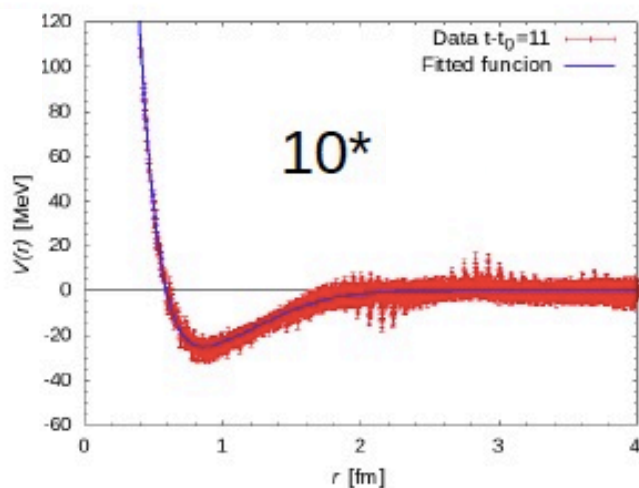
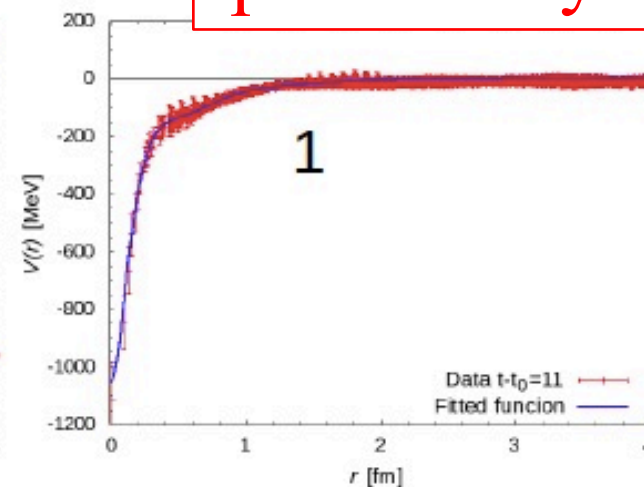
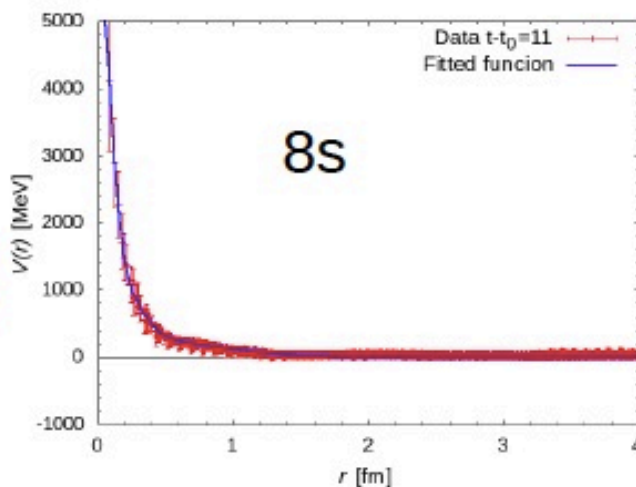
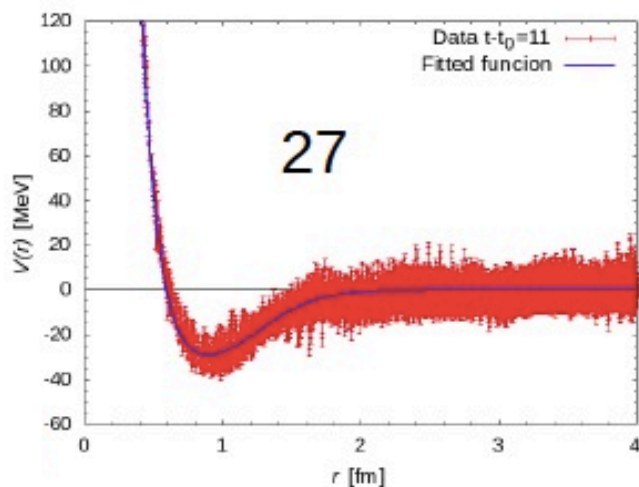
K. Sasaki+ HAL QCD Coll.

T. Inoue+ HAL QCD Coll.



$$8 \times 8 = \frac{27 + 8s + 1}{^1S_0} + \frac{10^* + 10 + 8a}{^3S_1, ^3D_1}$$

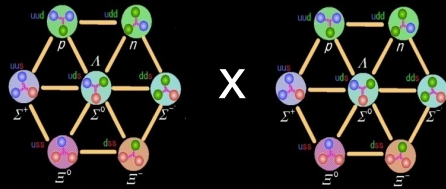
preliminary



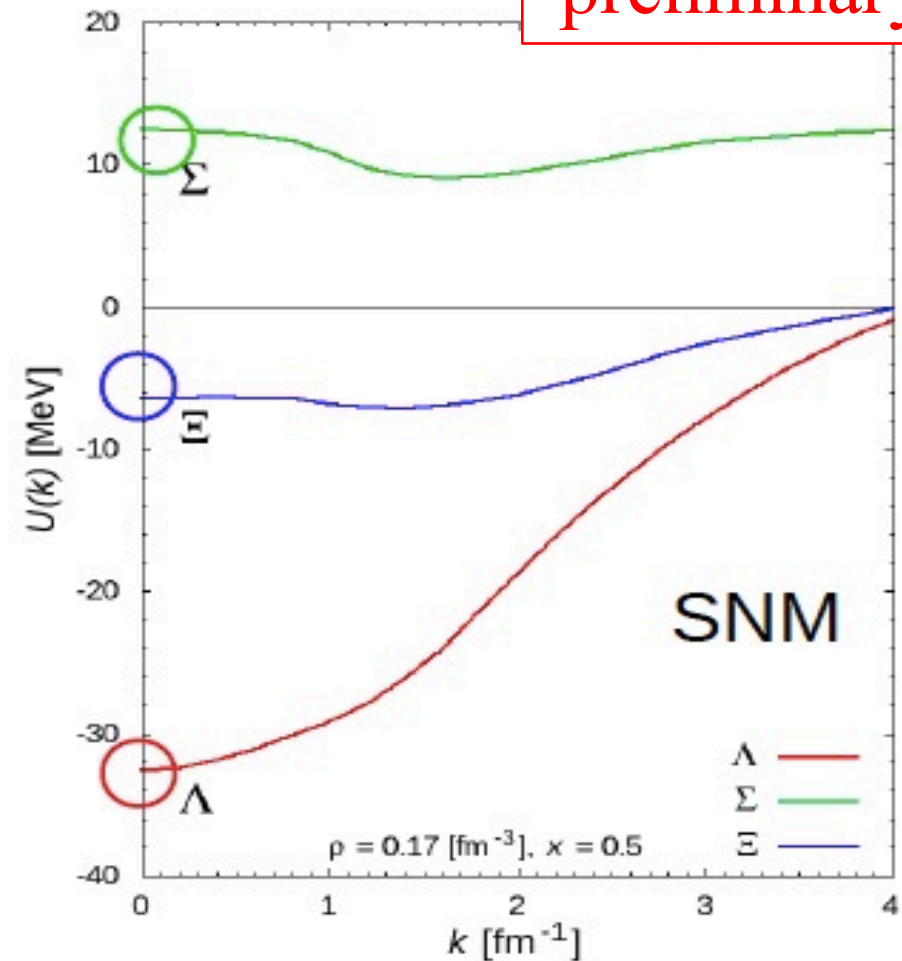
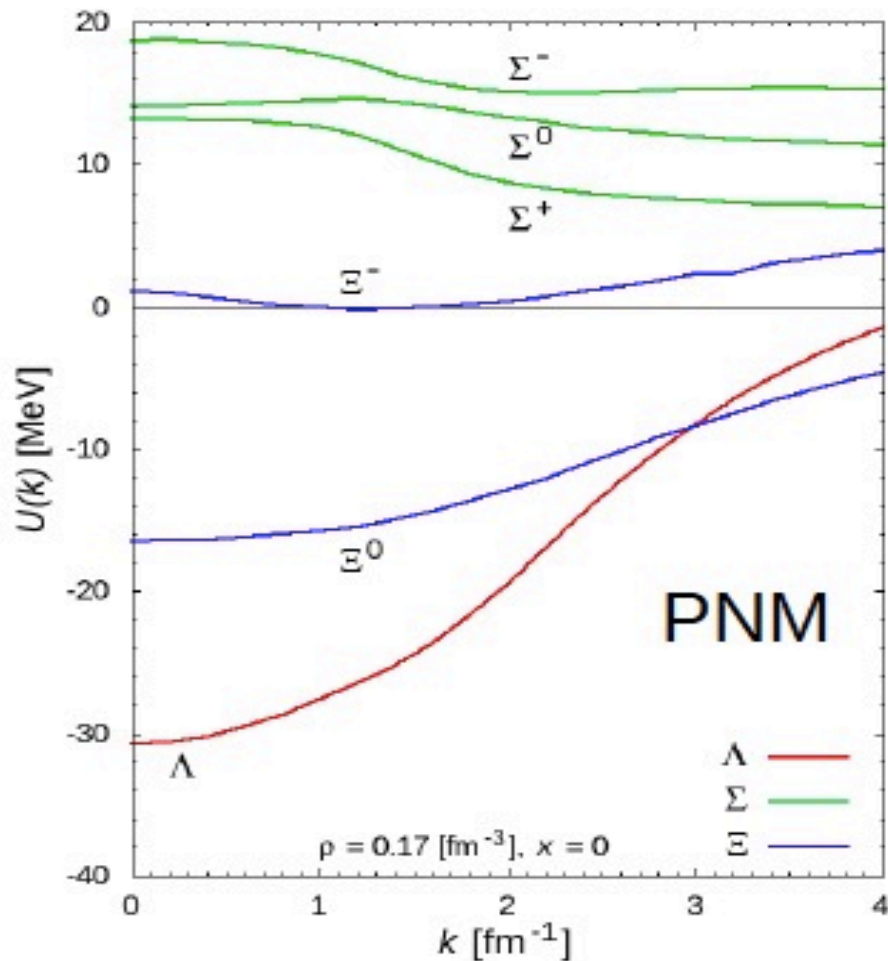
8x8 BB interactions with flavor basis: $V_C(r)$

K. Sasaki+ HAL QCD Coll.

T. Inoue+ HAL QCD Coll.



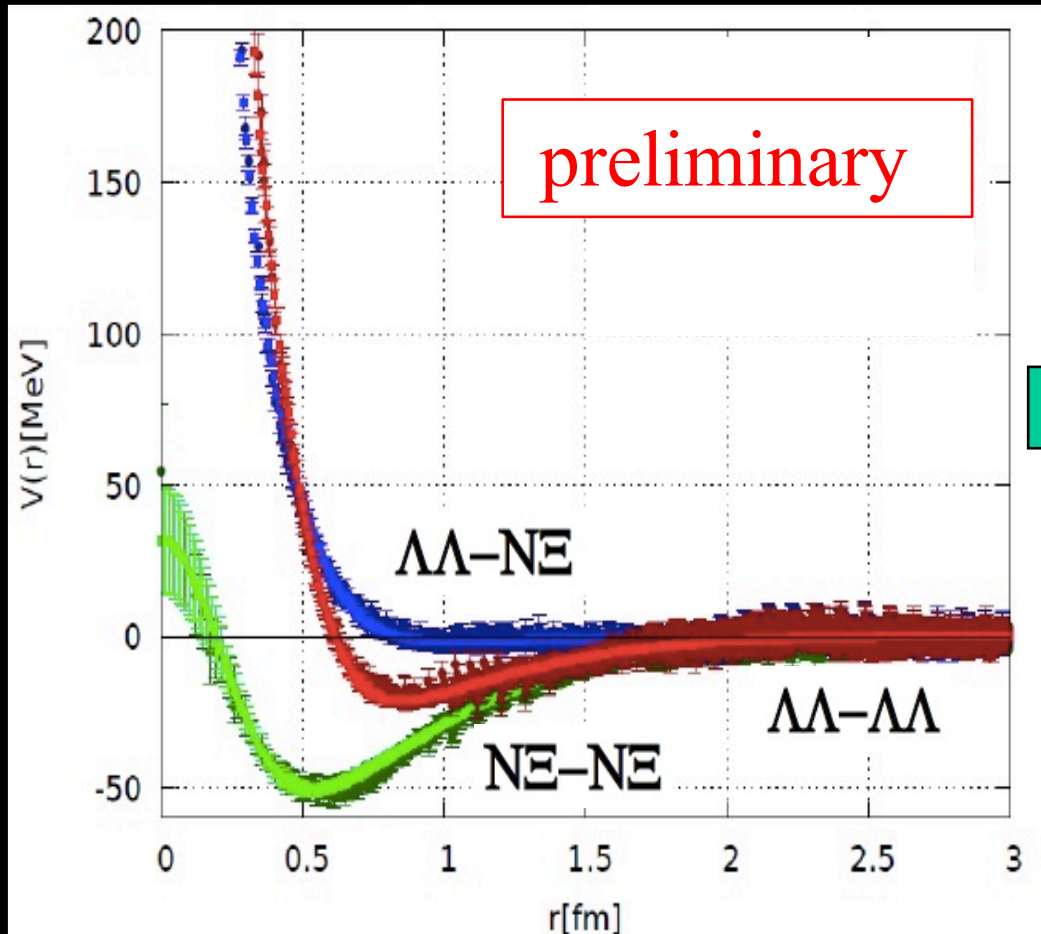
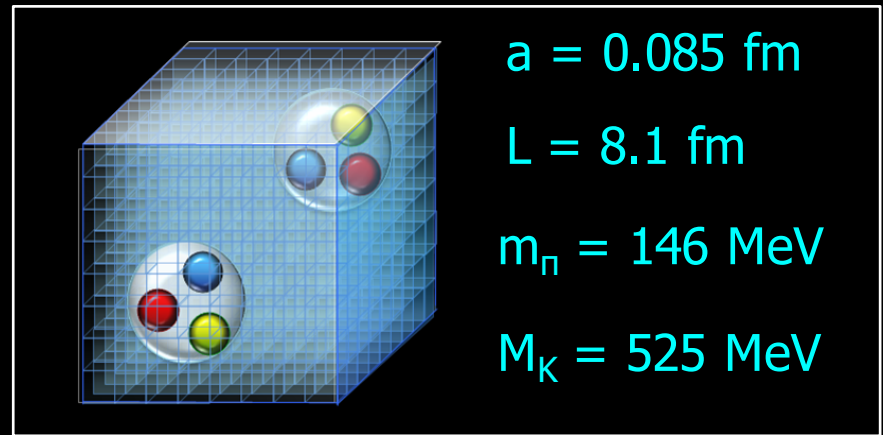
$$8 \times 8 = \frac{27 + 8s + 1}{1S_0} + \frac{10^* + 10 + 8a}{3S_1, 3D_1}$$



preliminary

S=-2 BB interactions
in particle basis: $V_C(r)$

K. Sasaki+ HAL QCD Coll.



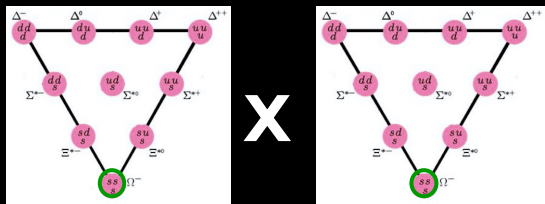
Coupled channel analysis
to search for H-like resonances

$$m_{N\Xi} = 2260 \text{ MeV}$$

$$m_{\Lambda\Lambda} = 2230 \text{ MeV}$$

Flavor SU(3) Classification : B=2

c.f. Dyson & Young,
PRL 14 (1965)



x

$$10 \times 10 = 28 + 27 + 35 + 10^*$$

Di-Omega (strangeness = -6)

$\Omega\Omega(J=0)$

Zhang et al (1997)

Di-Omega: $\Omega\Omega$ (1S_0)

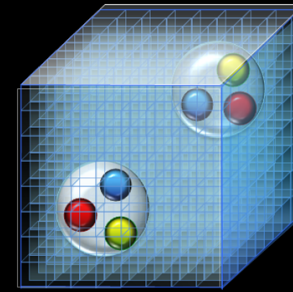
Gongyo+ [HAL QCD Coll.],
Phys. Rev. Lett. 120 (2018) 212001

$a = 0.085$ fm

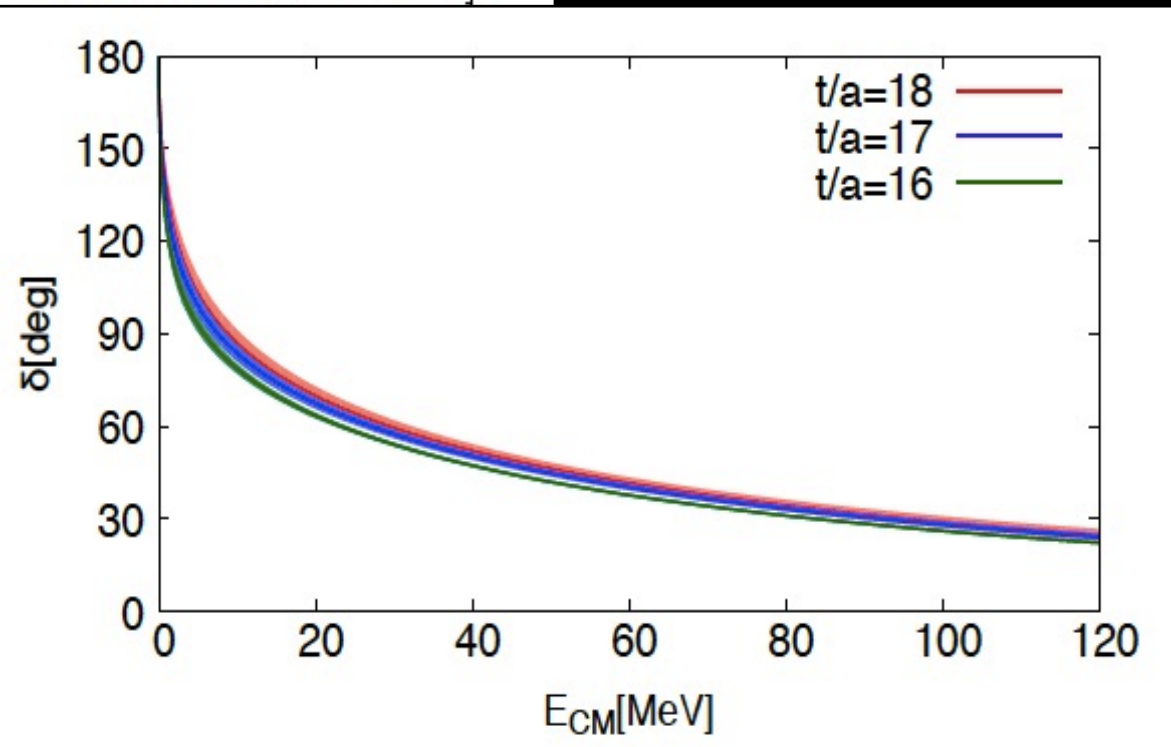
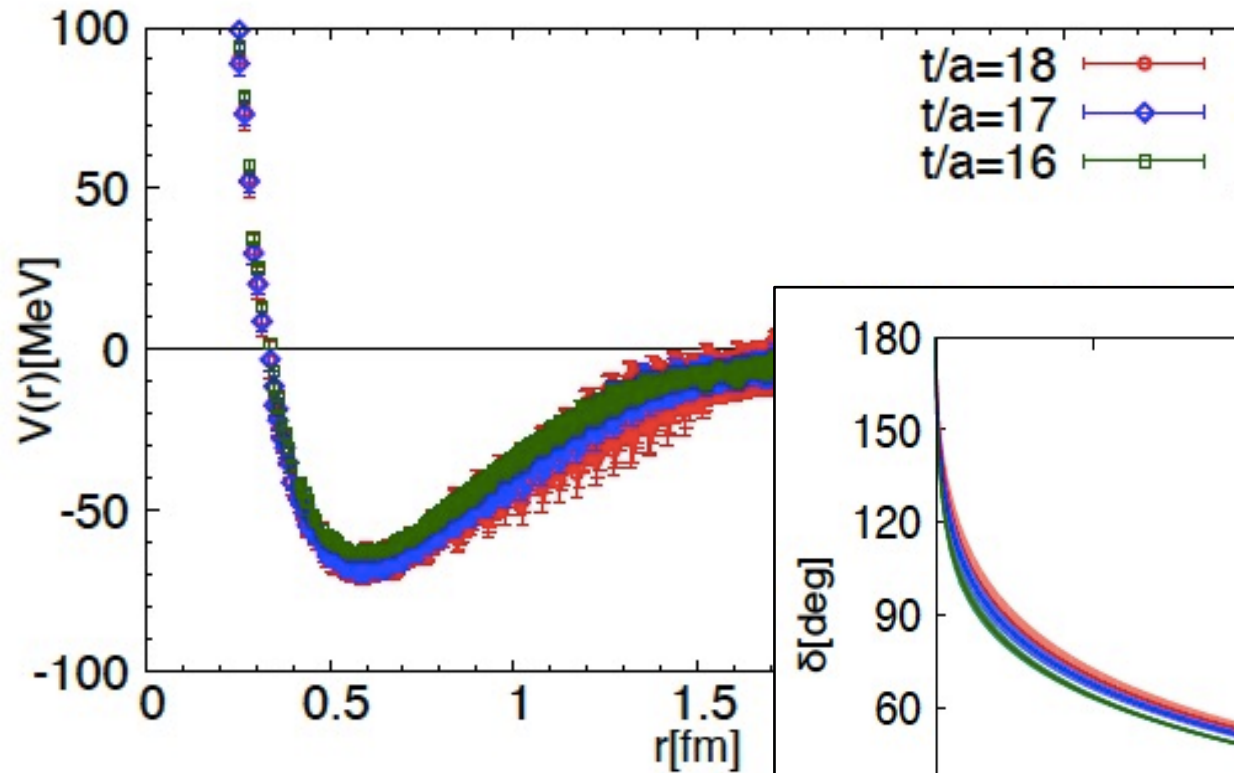
$L = 8.1$ fm

$m_n = 146$ MeV

$M_K = 525$ MeV



S. Gongyo



Di-Omega: $\Omega\Omega$ (1S_0)

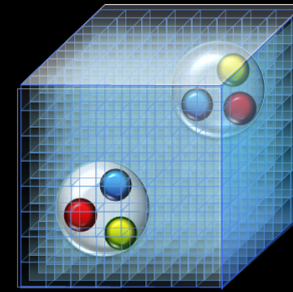
Gongyo+ [HAL QCD Coll.],
Phys. Rev. Lett. 120 (2018) 212001

$a = 0.085$ fm

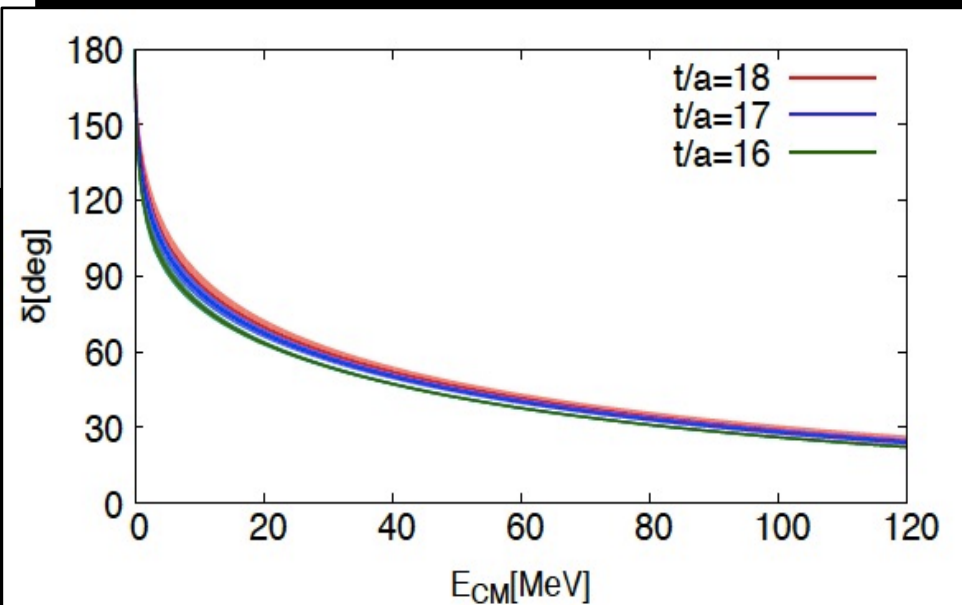
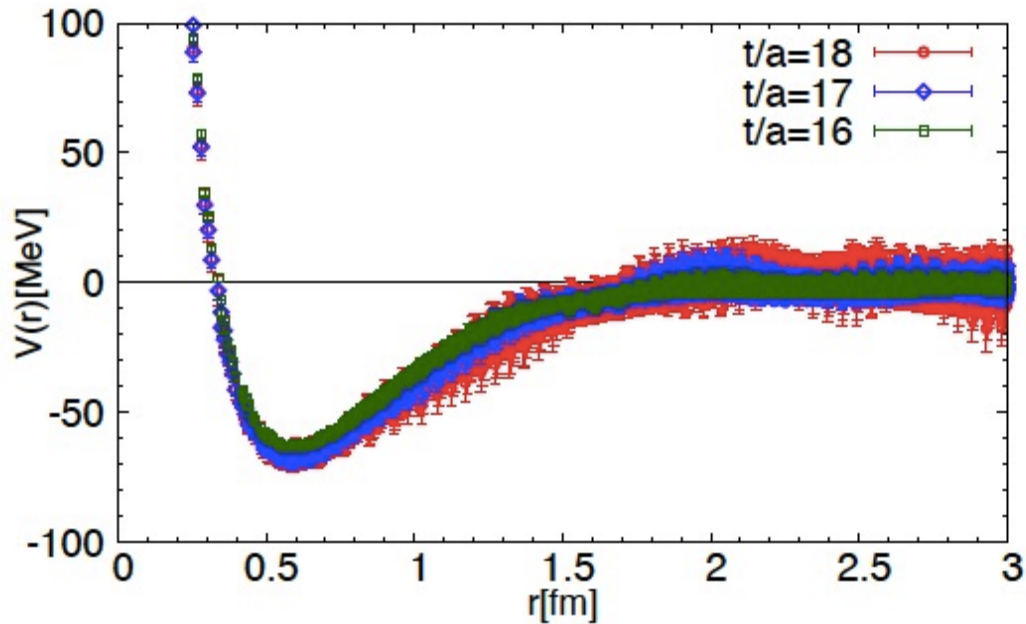
$L = 8.1$ fm

$m_n = 146$ MeV

$M_K = 525$ MeV



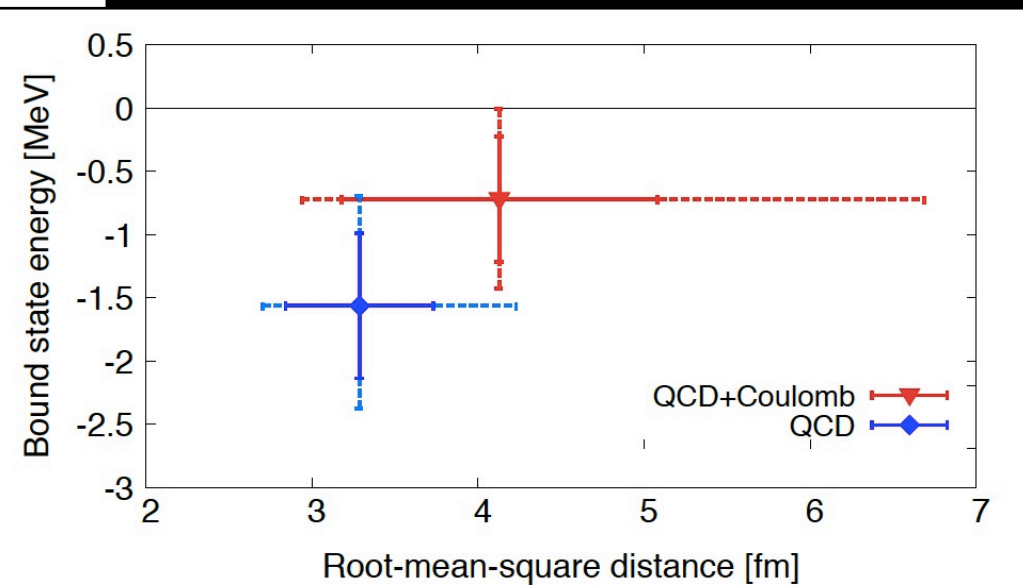
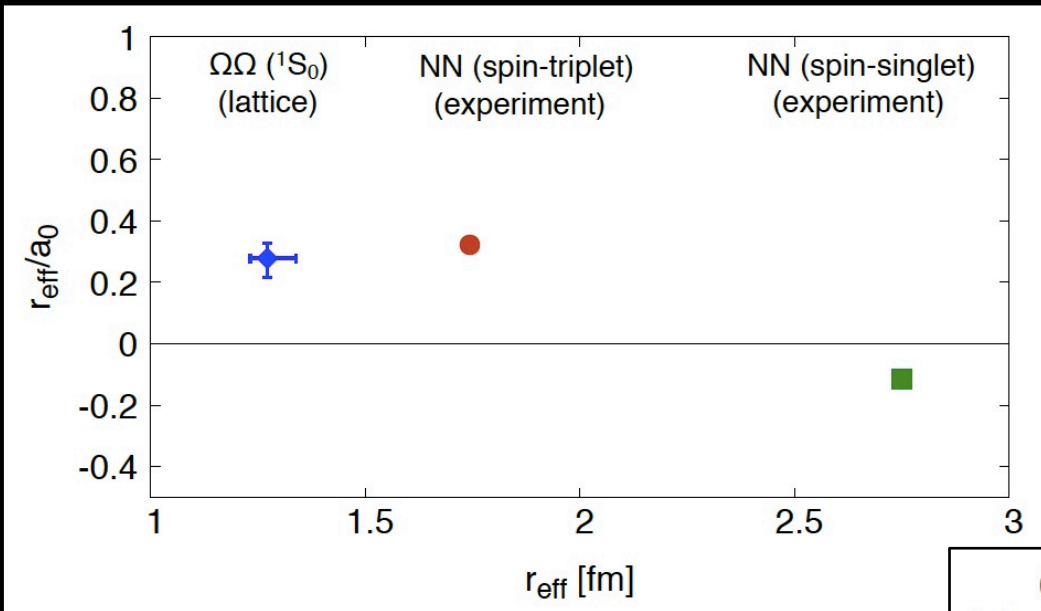
S. Gongyo



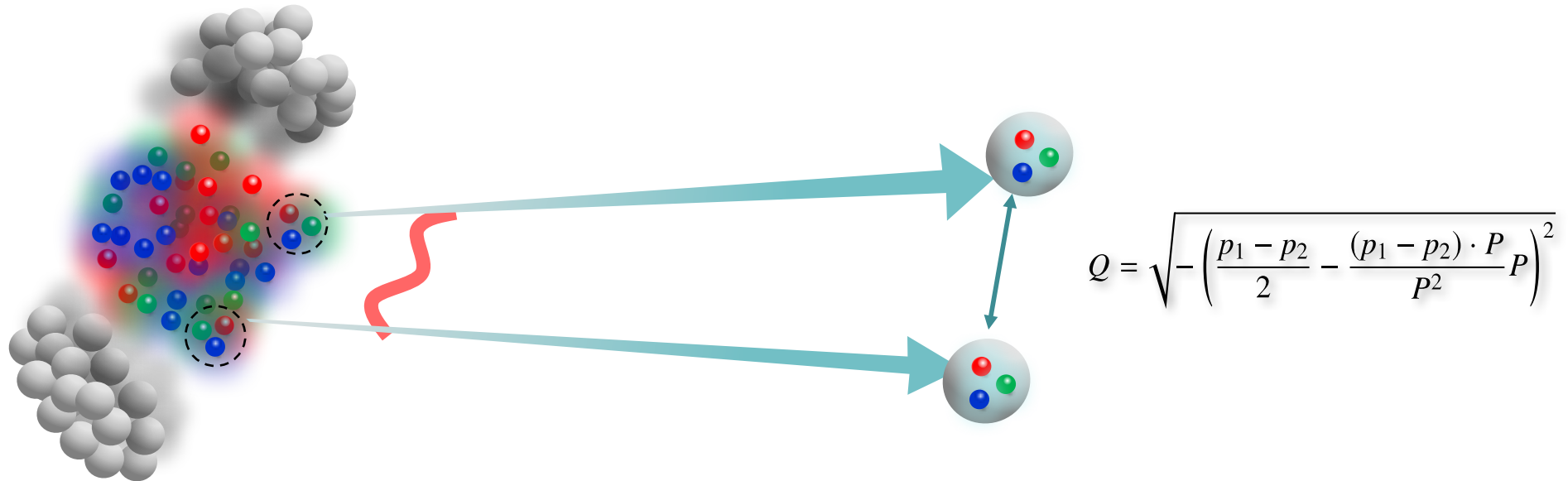
$\Omega\Omega$ near unitarity

$$k \cot \delta(k) = -\frac{1}{a_0} + \frac{1}{2} r_{\text{eff}} k^2 + \dots$$

$$a_0^{(\Omega\Omega)} = 4.6(6)_{-0.5}^{+1.2} \text{ fm},$$
$$r_{\text{eff}}^{(\Omega\Omega)} = 1.27(3)_{-0.03}^{+0.06} \text{ fm}.$$



How HIC can tell us about interaction?



Measuring **Pair Correlation** → Constraint on **Pairwise Interaction**

$$C_{AB}(Q) = \frac{N_{AB}^{\text{pair}}(Q)}{N_A N_B(Q)} = \begin{cases} 1 & \text{No Correlation} \\ \text{others} & \text{Interaction, Quantum Interference etc} \end{cases}$$

Correlation from FSI

Lednický+ 1982

$$C_{AB}(Q) - 1 = \frac{4\pi}{(2\pi R^2)^3} \int dr r^2 S^{\text{rel}}(r) [|\chi_Q(r)|^2 - |j_0(Qr)|^2]$$



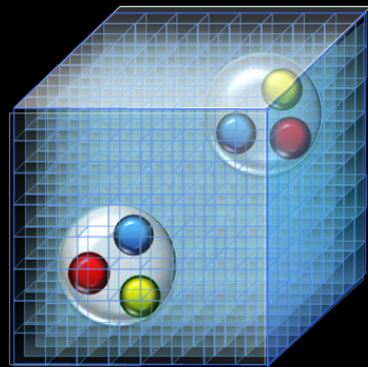
Static/Spherical Source:

$$S^{\text{rel}}(r) \sim (\pi R^2)^{3/2} \exp\left(-\frac{r^2}{4R^2}\right)$$

Asymptotic wave function:

$$\chi_Q(r) \sim \sin(Qr + \delta)/(Qr)$$

$$Q \cot \delta = -\frac{1}{a_0} + \frac{1}{2} r_{\text{eff}} Q^2$$



$a = 0.085$ fm

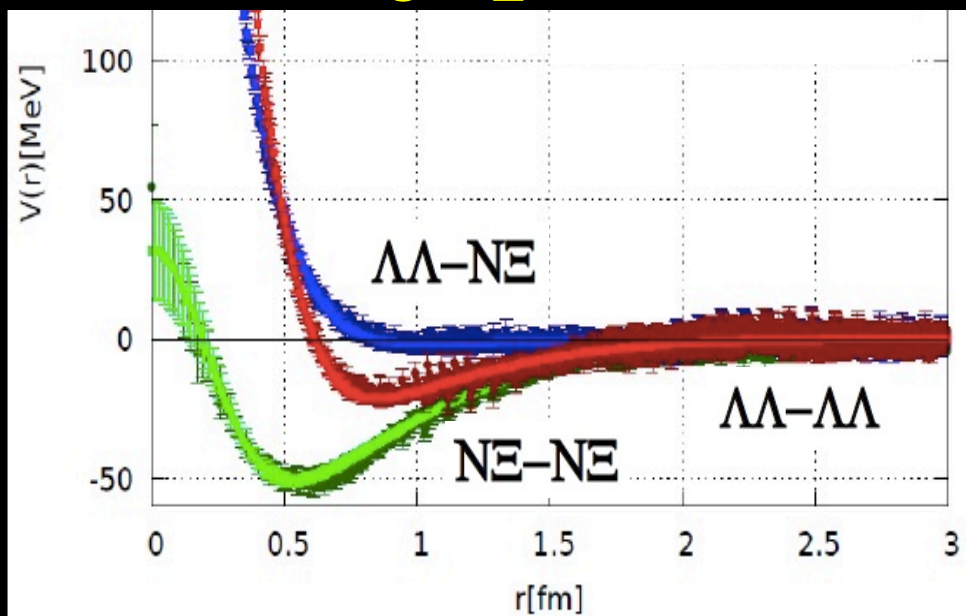
$L = 8.1$ fm

$m_\pi = 146$ MeV

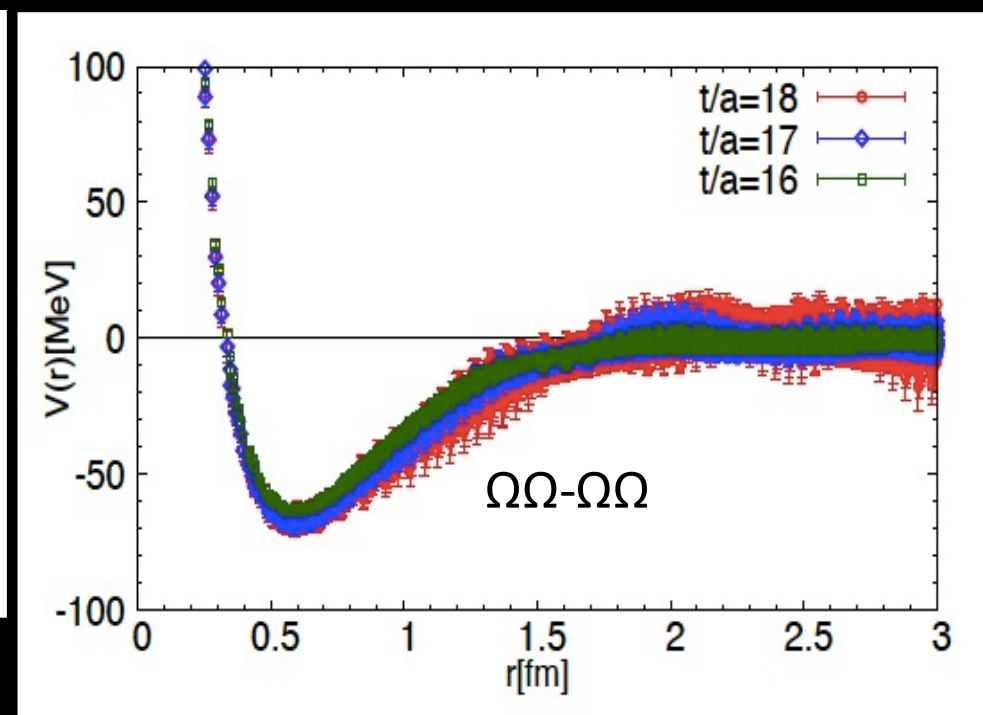
$M_K = 525$ MeV

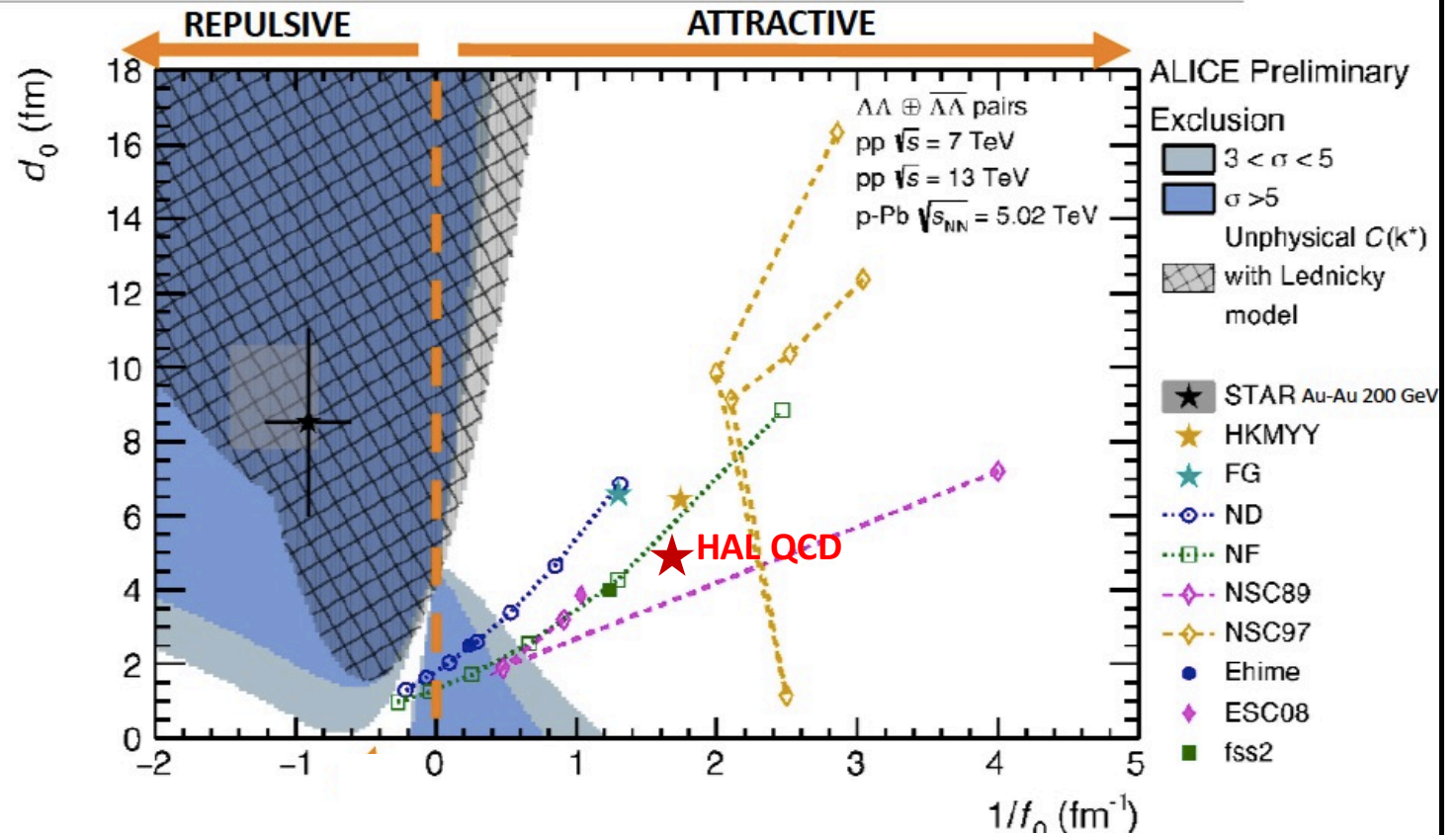
HAL QCD Potential for $J^P=0^+$

$S=-2$



$S=-6$





- First observation of strong attractive interaction in p-Ξ⁻**

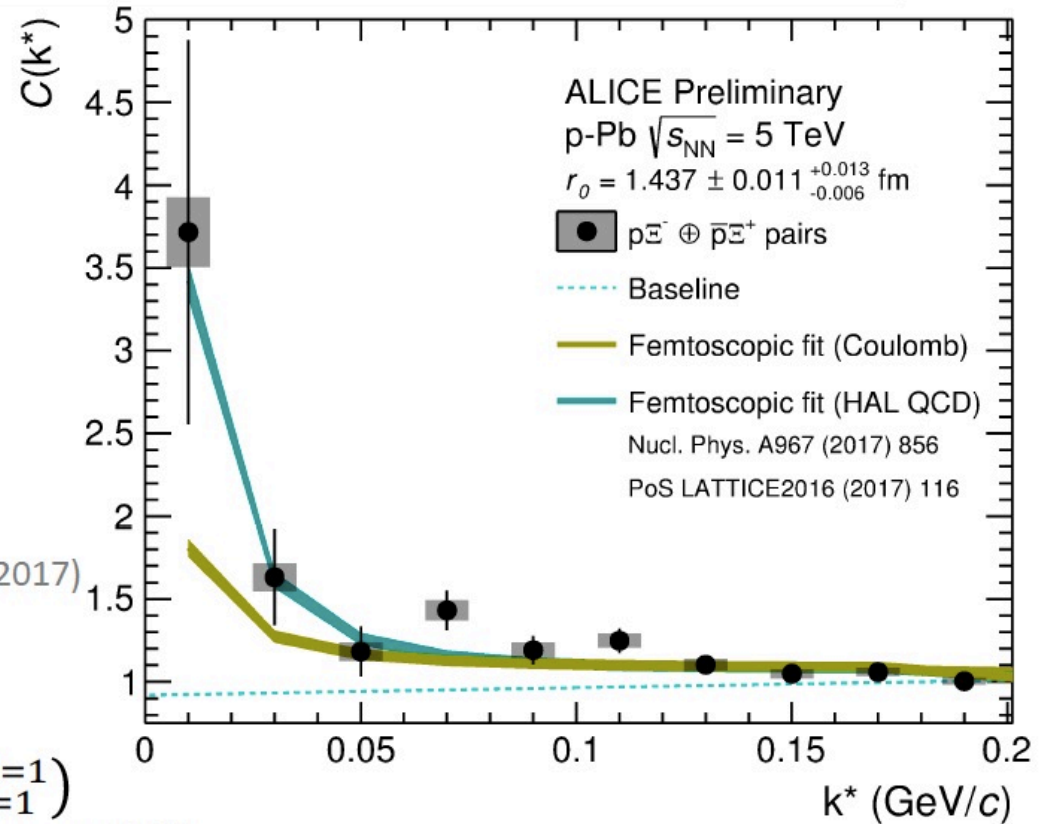
- p-Value with and without strong potential (Coulomb only): 0.055 vs. 0.004

- modeled with preliminary QCD strong potential by the HAL QCD collaboration

(Hatsuda et al., NPA967 (2017) 856, PoS Lattice2016 (2017) 116)

$$C(k^*) = \frac{1}{8} (C_{I=0}^{S=0} + C_{I=1}^{S=0}) + \frac{3}{8} (C_{I=0}^{S=1} + C_{I=1}^{S=1})$$

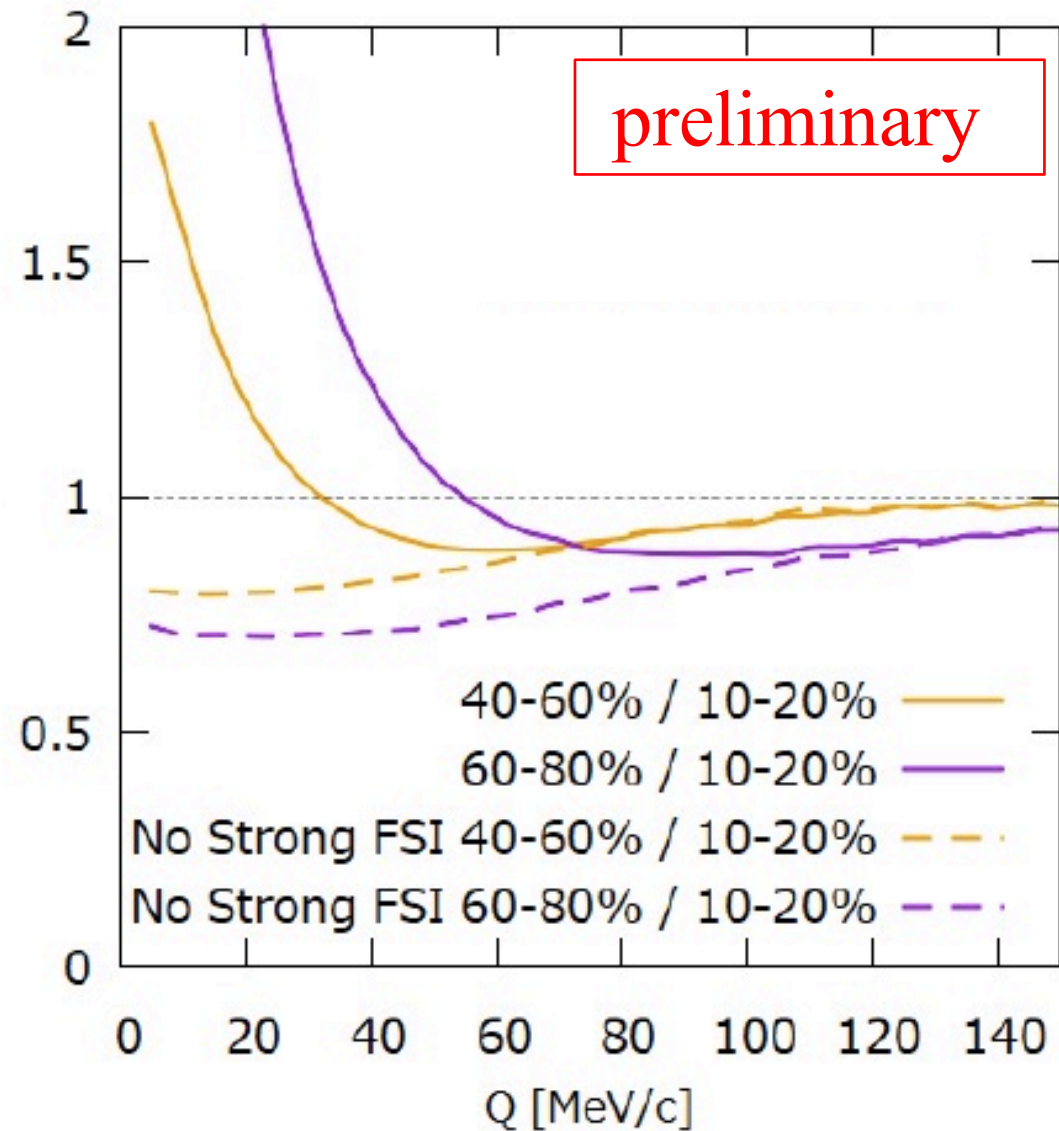
ALI-PREL-144825



$\Omega\Omega$ correlation from HIC

$$= C^{\text{Small-R}}(Q) / C^{\text{Large-R}}(Q)$$

Morita+
(in preparation)



Summary

BB interactions on the lattice ($L=8.1\text{fm}$, $m_\pi=146\text{ MeV}$, $m_K=525\text{ MeV}$)
Prediction by HAL QCD Collaboration

$S=0$	$S=-1$	$S=-2$	$S=-3$	$S=-4$	$S=-5$	$S=-6$
NN	$N\Lambda, N\Sigma$	$\Lambda\Lambda, \Lambda\Sigma, \Sigma\Sigma, N\Xi$	$\Lambda\Xi, \Sigma\Xi$	$\Xi\Xi$	$\Xi\Omega$	$\Omega\Omega$

EXP
rich data

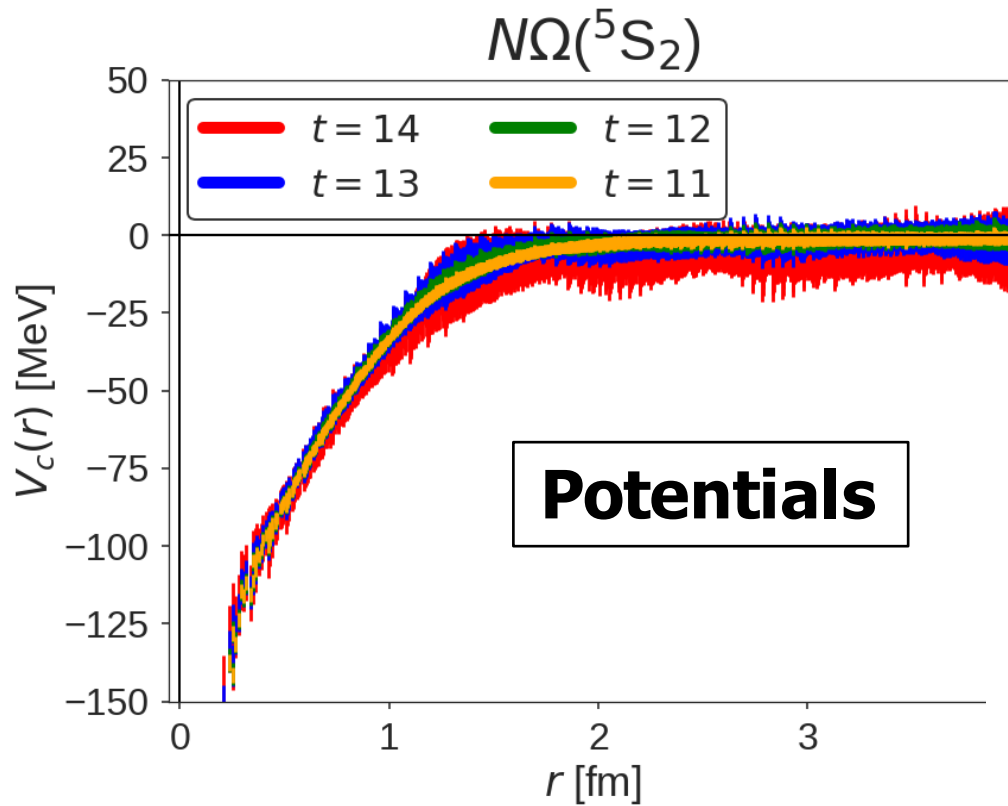
LQCD
better S/N

Hypernuclei
FSI at RHIC, LHC

FSI in
Future HIC

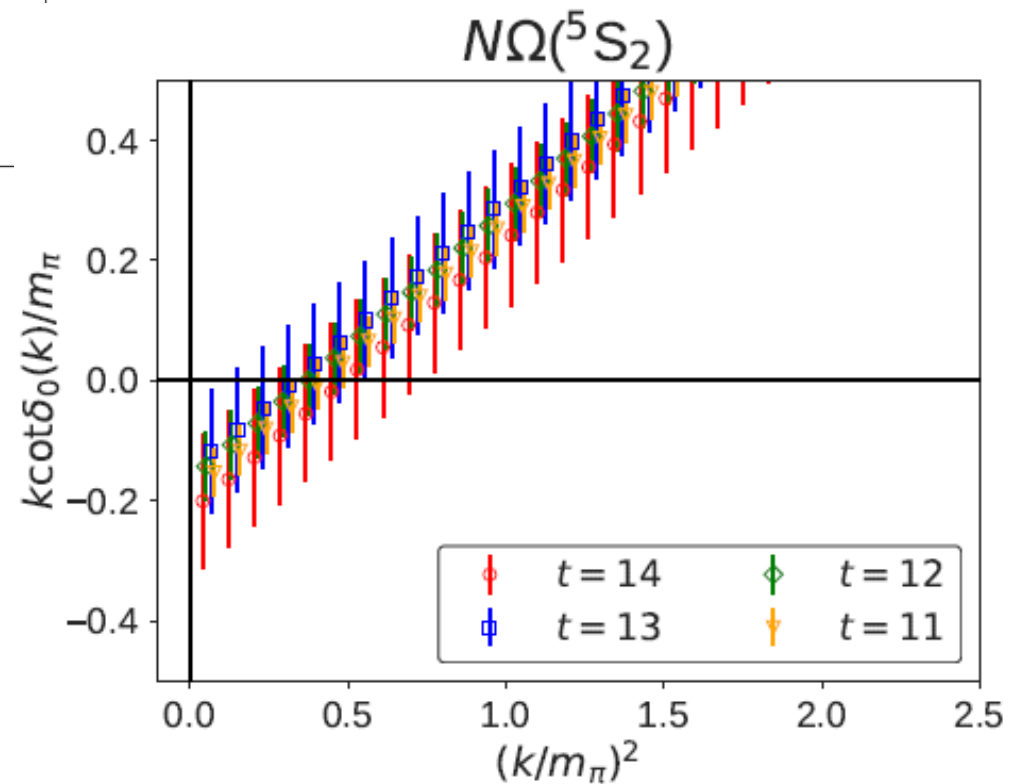
Backup slides

$N\Omega$ system (5S_2)



preliminary

Phase Shifts



Strong Attraction
possibly **"Bound"**

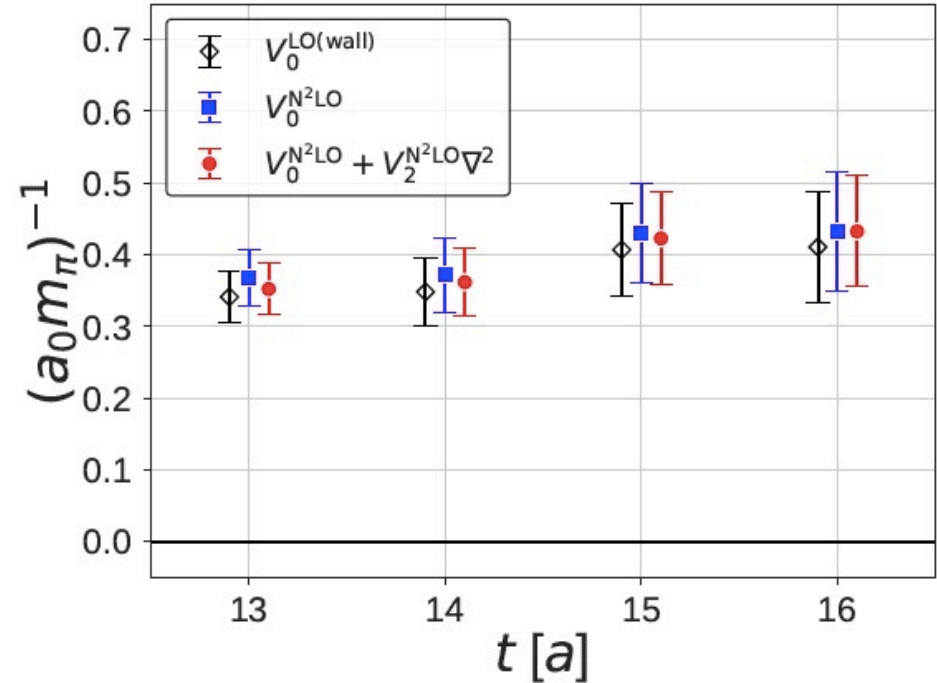
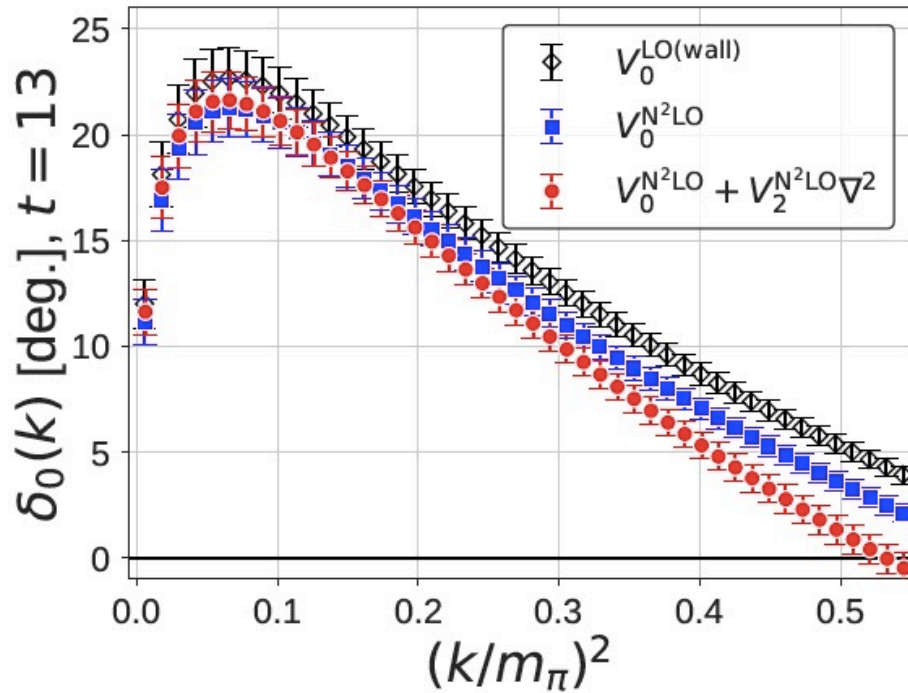
\longleftrightarrow **$N\Omega$ correlation in HIC**

Systematics of the HAL QCD Potential at Low Energies in Lattice QCD

Takumi Iritani,¹ Sinya Aoki,^{2,3} Takumi Doi,^{1,4} Shinya Gongyo,¹ Tetsuo Hatsuda,^{4,1}
Yoichi Ikeda,⁵ Takashi Inoue,⁶ Noriyoshi Ishii,⁵ Hidekatsu Nemura,⁵ and Kenji Sasaki²

(HAL QCD Collaboration)

$$U(\vec{r}, \vec{r}') = \{V_0^{N^2LO}(r) + V_2^{N^2LO}(r)\nabla^2\}\delta(\vec{r} - \vec{r}').$$



The fate of the direct method (check on NN)

T. Iritani et al. (HAL Coll.) PRD96(2017)034521

Data	$NN(^1S_0)$				$NN(^3S_1)$			
	Source independence	Sanity check			Source independence	Sanity check		
		(i)	(ii)	(iii)		(i)	(ii)	(iii)
YKU2011 [24]	†	No	No	*	†	No	No	*
YIKU2012 [25]	No	†	No	*	No	†	No	*
YIKU2015 [26]	†	†	No	*	†	†	No	No
NPL2012 [27]	†	†	No	*	†	†	*	*
NPL2013 [28, 29]	No	*	*	No	No	*	*	?
NPL2015 [30]	†	No	*	No	†	No	*	No
CalLat2017 [31]	No	?	*	No	No	?	*	No

All data for NN by the direct method fail these "minimum" tests so far

→ Studies w/ the variational method are mandatory