

Temperature Dependence of Transport Coefficients of QCD in High-Energy Heavy-Ion Collisions



Kobayashi-Maskawa Institute
for the Origin of Particles and the Universe

Kobayashi-Maskawa Institute, Nagoya University
Department of Physics, Nagoya University

Chiho NONAKA

June 12, 2018@YKIS2018b Symposium



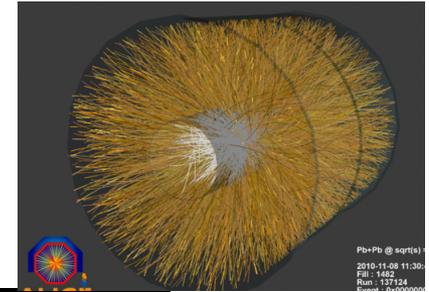
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Quark-Gluon Plasma

RHIC:2000

Strongly interacting QGP

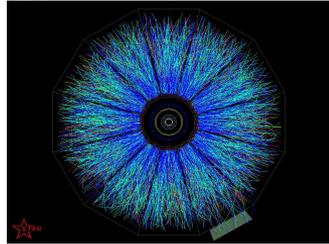
- Relativistic hydrodynamics
- Recombination model
- Jet quenching
- Color Glass Condensate



LHC:2010

Heavy Ion collisions start!

STAR



Heavy Ion Collisions:
LHC,RHIC

T

sQGP

QCD Critical Point

Quark-Gluon Plasma

QCD phase diagram

LHC: Energy frontier
RHIC: Beam Energy Scan
FAIR, NICA, J-PARC
: high density

Hadron Phase

Color Super Conductor

Neutron star

μ_B

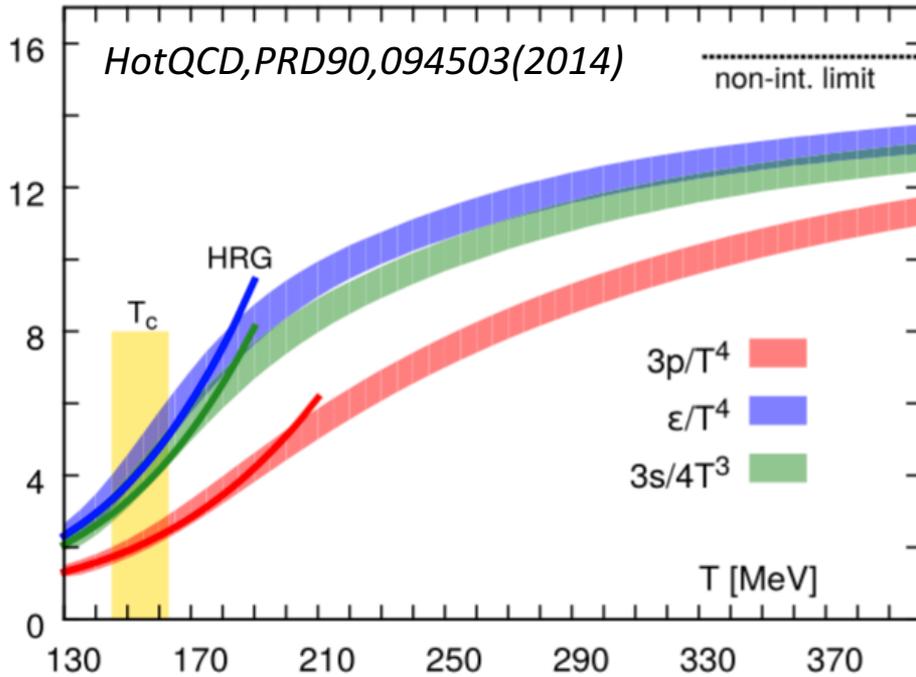


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Property of QGP

- Equation of State

- Lattice QCD



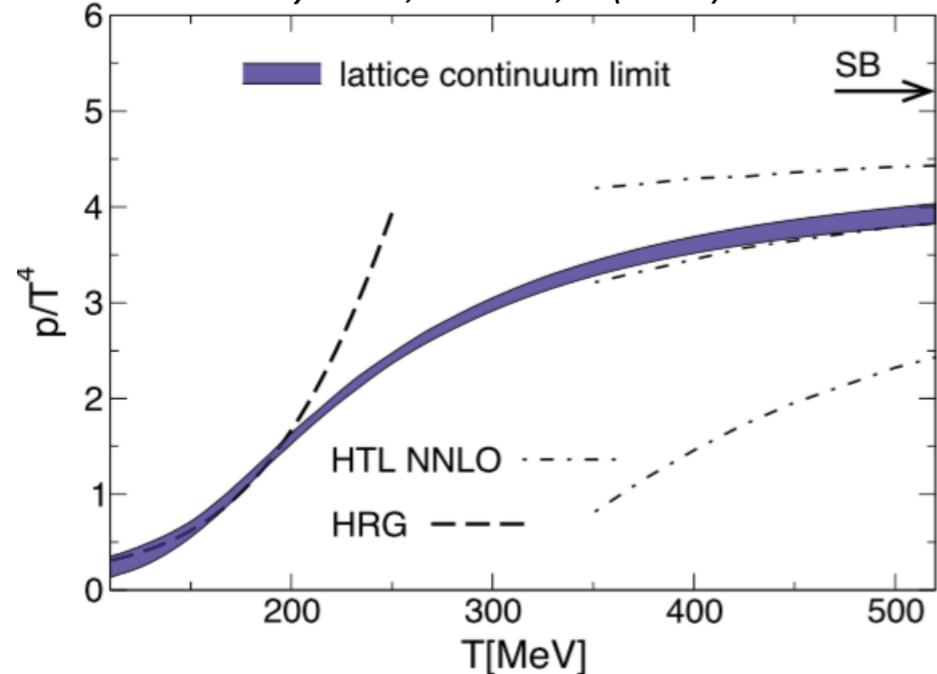
(2+1) flavor, Highly improved staggered quark action

$N_t=6,8,10,12, N_s=4N_t \rightarrow$ continuum limit

Parametrization of EoS

$T_c \sim 155$ MeV

Borsanyi et al, PLB730,99(2014)



(2+1) flavor, Symanzik improved gauge and a stout-link improved staggered fermion action

$N_t=6,8,10,12,16 \rightarrow$ continuum limit

Parametrization of EoS

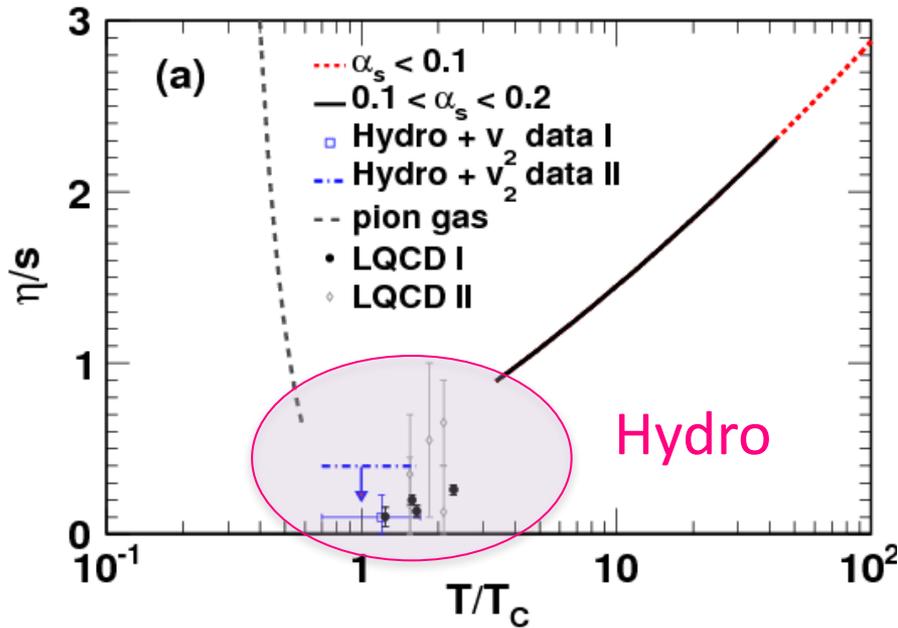
finite μ : sign problem



Property of QGP

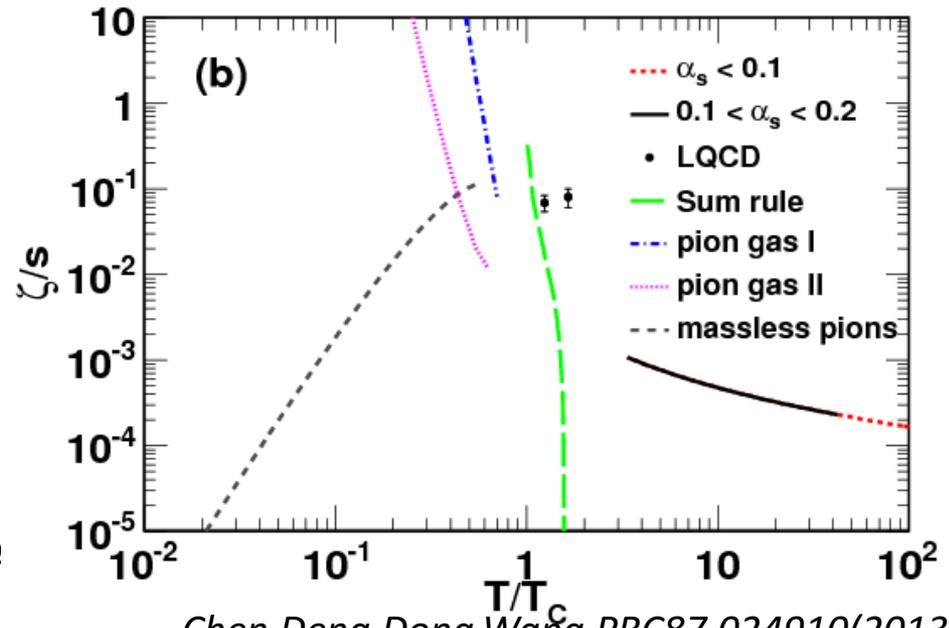
- Current Status for transport coefficients

shear viscosity



- Shear viscosity takes the minimum around T_c . Cf. $\eta/s = 1/4\pi$ AdS/CFT
- Hydrodynamic model constant η/s

bulk viscosity

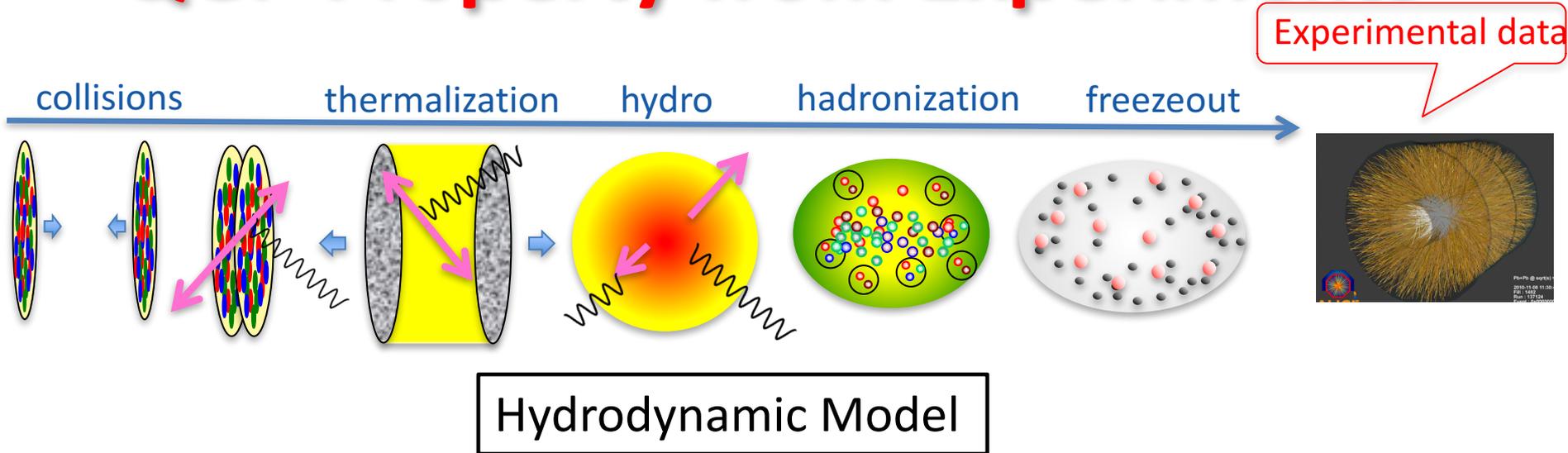


Chen, Deng, Dong, Wang, PRC87,024910(2013)

- Bulk viscosity
- Temperature dependence is unclear.
- Hydrodynamic model vanishing

Detailed feature of shear and bulk viscosities

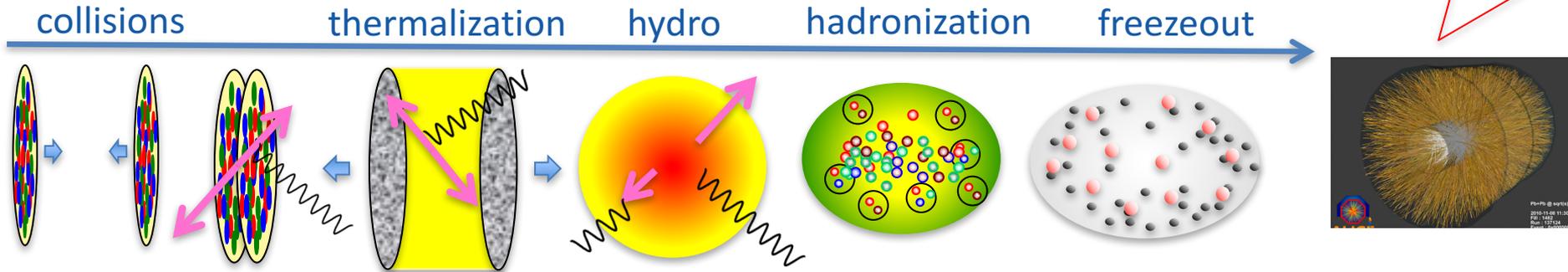
QGP Property from Experiments



- One of successful phenomenological models
- Close relation to QGP bulk property
- Strong tools for understanding shear and bulk viscosities through experimental analyses

QGP Property from Experiments

Experimental data



Initial conditions

Fluctuations:
Glauber, KLN,
IP-Glasma...

Hydrodynamics

QGP bulk property
EoS: lattice QCD
**Shear and bulk
viscosities**

Final state interactions

Hadron based event
generator

Relativistic viscous hydrodynamic equation

$$\partial_\mu T^{\mu\nu} = 0$$

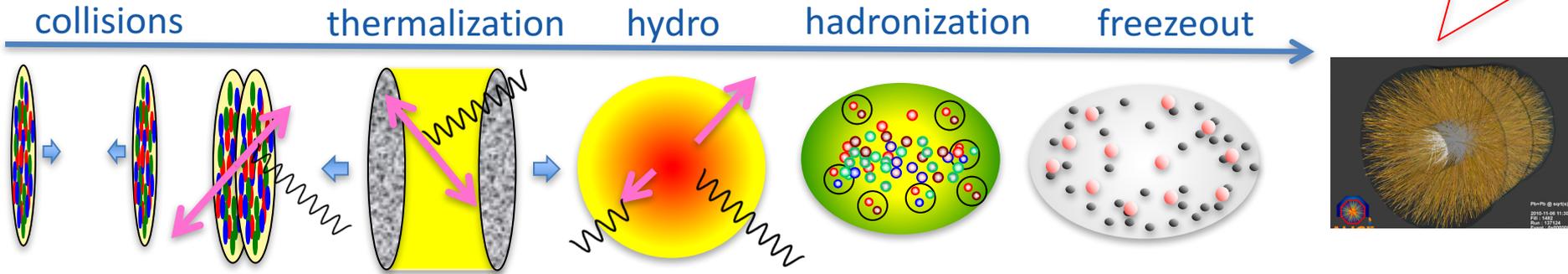
$$T^{\mu\nu} = (\epsilon + p)u^\mu u^\nu - pg^{\mu\nu} + \Delta T^{\mu\nu}$$

Denicol, Niemi, Molnar, Rischke, PRD85, 114047 (2012)

Denicol, Jeon, and Gale, Phys. Rev. C90, 024912 (2014)

QGP Property from Experiments

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Hydrodynamics

QGP bulk property
EoS: lattice QCD
**Shear and bulk
viscosities**

New
hydrodynamics
code

Final state interactions

Hadron based event
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Akamatsu et al, JCP256,34(2014)

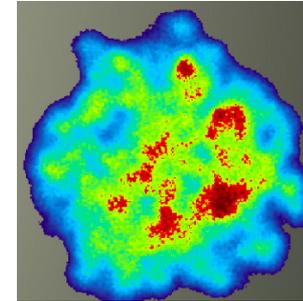
Okamoto, Akamatsu, Nonaka, EPJC76,579(2016)

Okamoto and Nonaka, EPJC77,383(2017)

Our Strategy

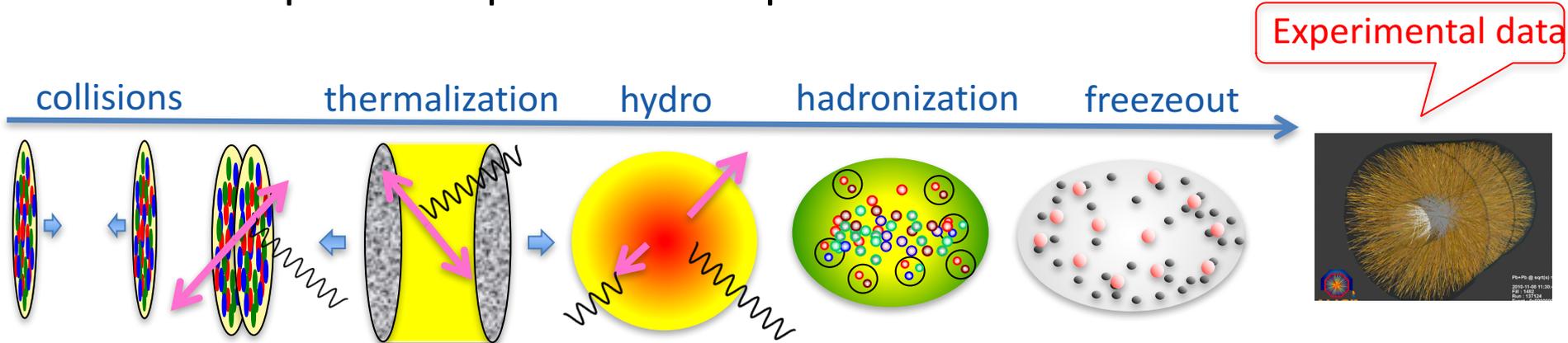
1. Development of new hydrodynamics code

- Stable with small numerical dissipation
- Shock wave
- Strong expansion in longitudinal direction
- Conservation property



2. Application to phenomenological analyses of LHC data

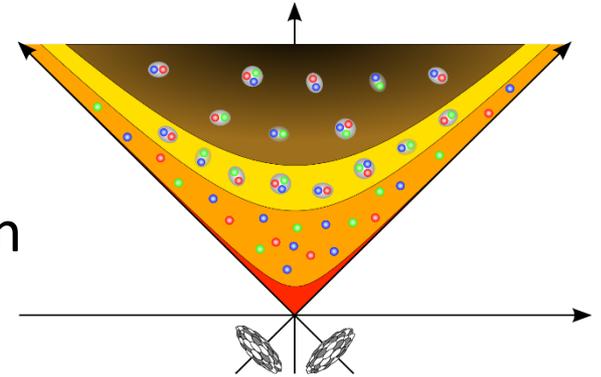
- Description of space-time expansion after collisions



Our Strategy

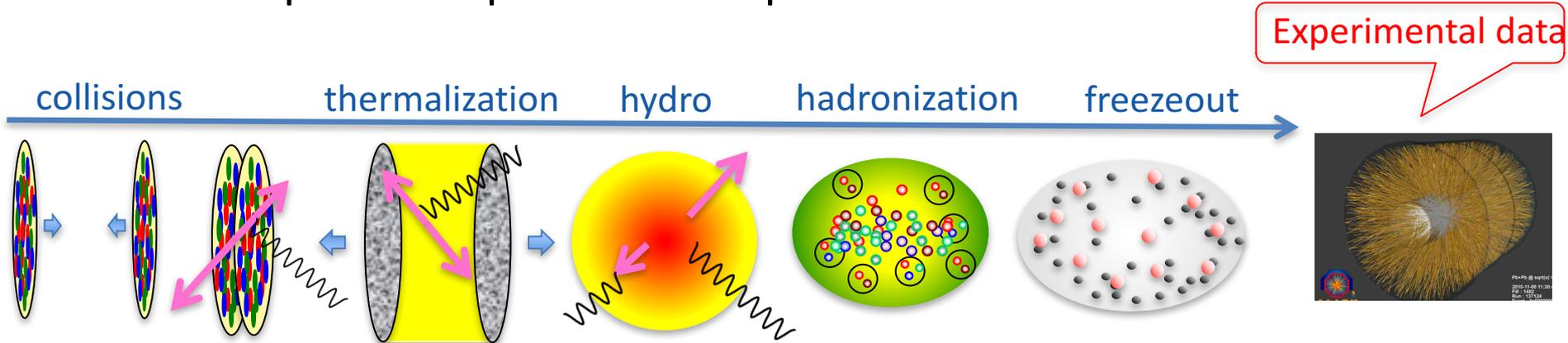
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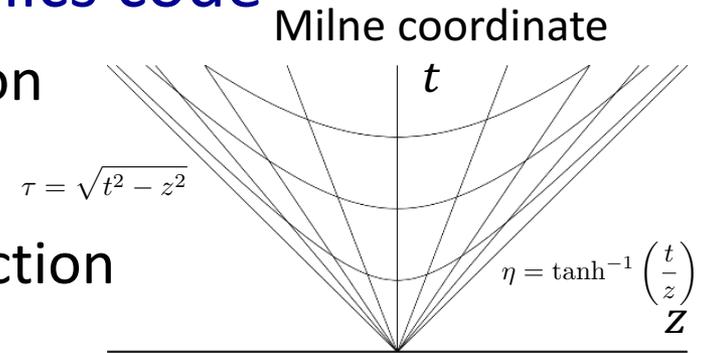
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Our Strategy

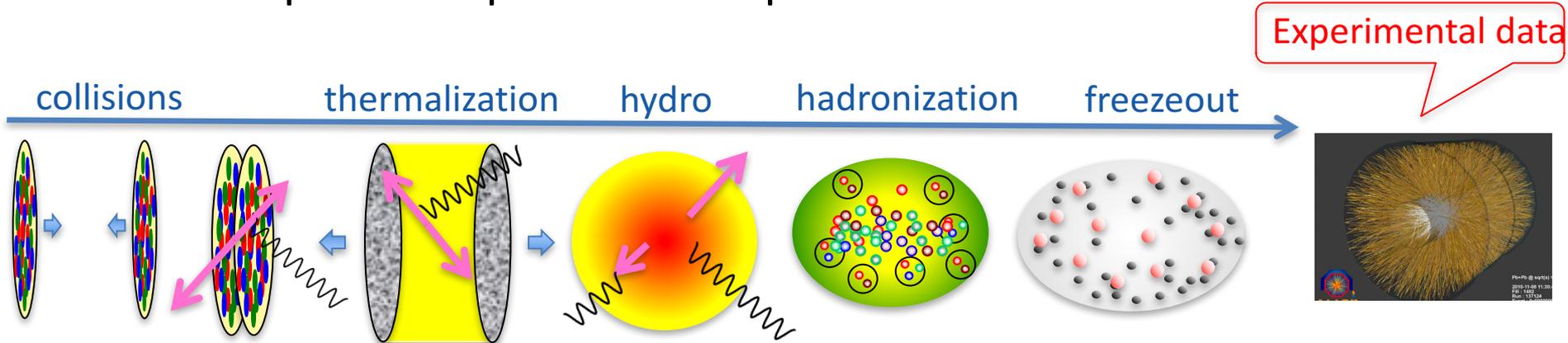
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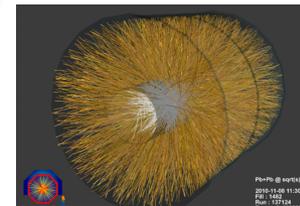
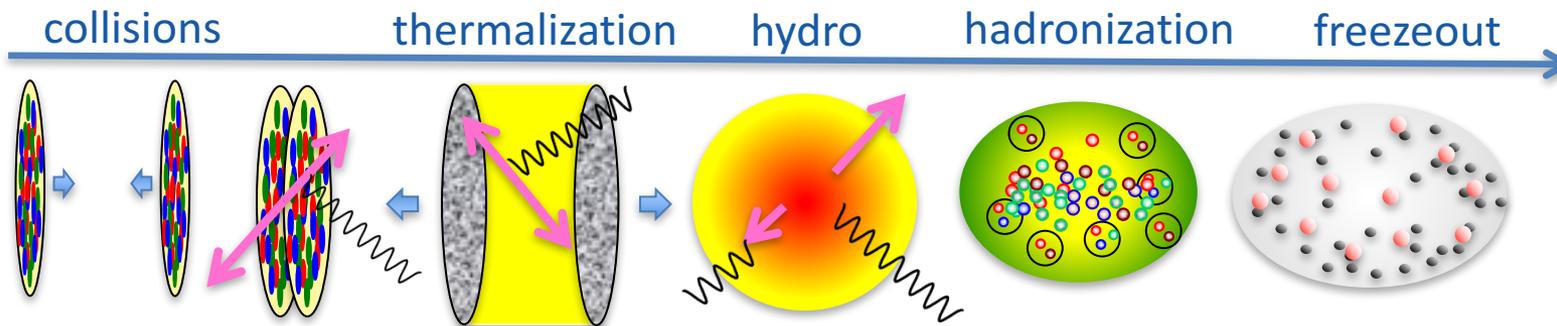
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Riemann solver
in Milne coordinates

2. Application to phenomenological analyses of LHC data

- Description of space-time expansion after collisions

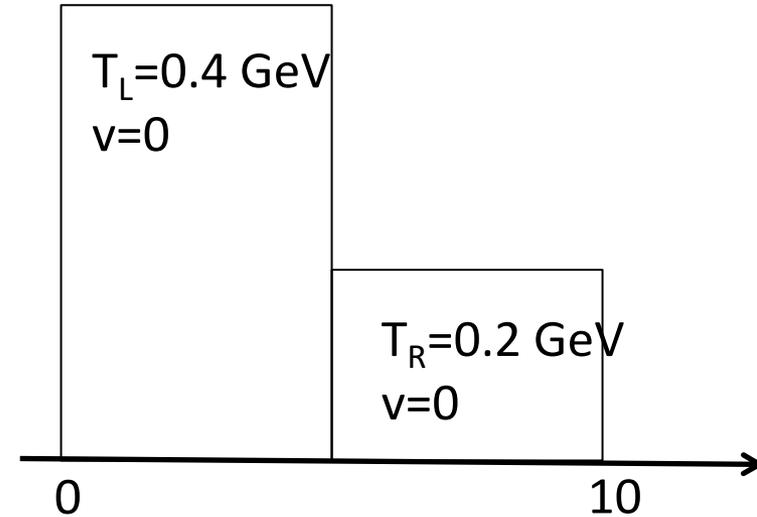
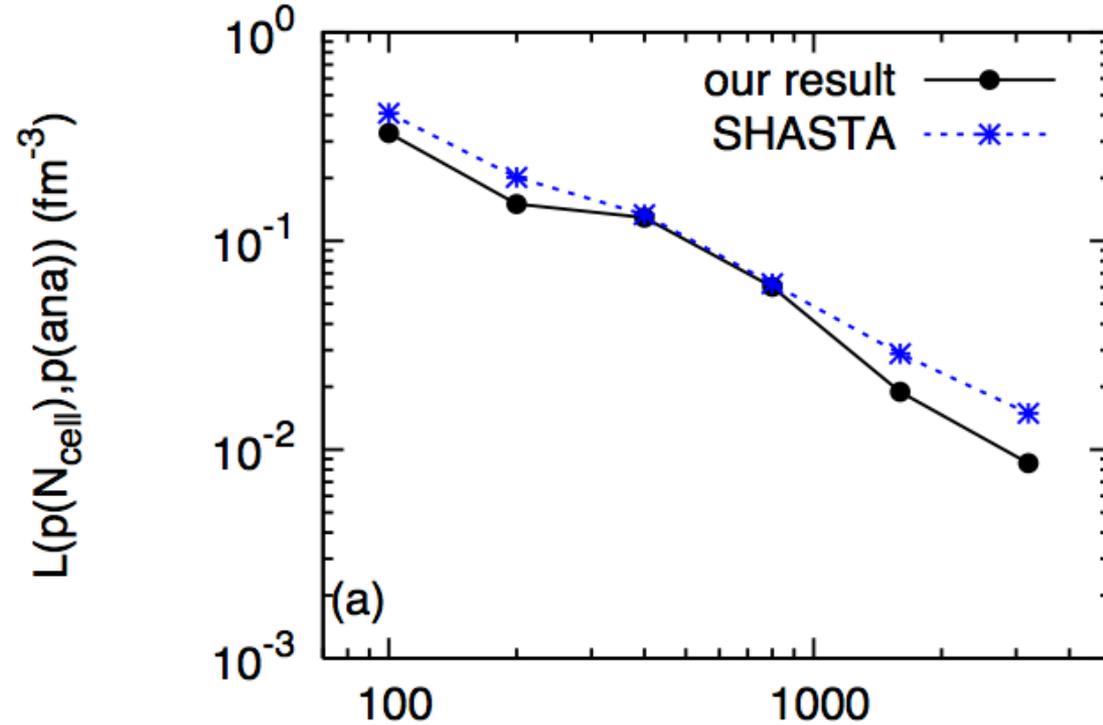
Experimental data



Small Numerical Dissipation

Akamatsu et al, JCP256,34(2014)

- Numerical dissipation: deviation from analytical solution



For analysis of heavy ion collisions

$N_{\text{cell}}=100: dx=0.1 \text{ fm}$

$$\frac{\lambda}{N_{\text{cell}}}$$

$\lambda=10 \text{ fm}$

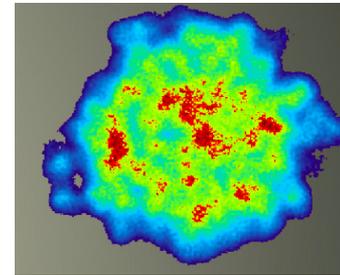
$$L(p(N_{\text{cell}}), p(\text{analytic})) = \sum_{i=1}^{N_{\text{cell}}} |p(N_{\text{cell}}) - p(\text{analytic})|$$



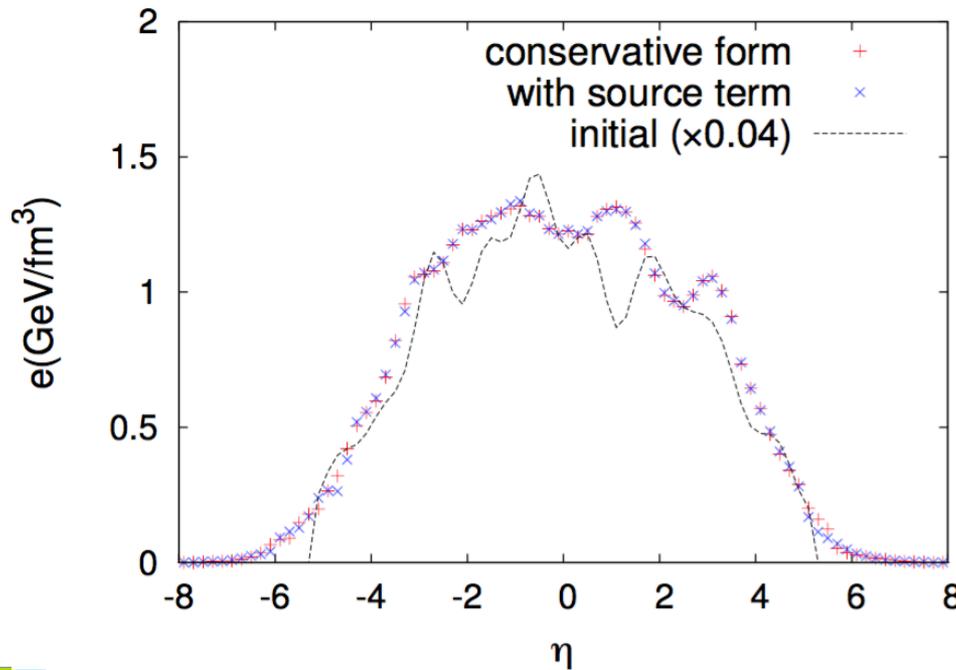
Numerical Tests in 1D

- ✓ Bjorken's scaling solutions
- ✓ Landau-Khalatnikov Solution (1D)
- ✓ Longitudinal fluctuations
- ✓ Conservation property

*K. Okamoto, Y. Akamatsu and CN,
Eur. Phys. J. C76 (2016)579*



fluctuations



Sum of violation of conservation

	ϵ_E	ϵ_M
conservative	1.38E-09	8.59E-09
with souce	1.27E-02	5.61E-02

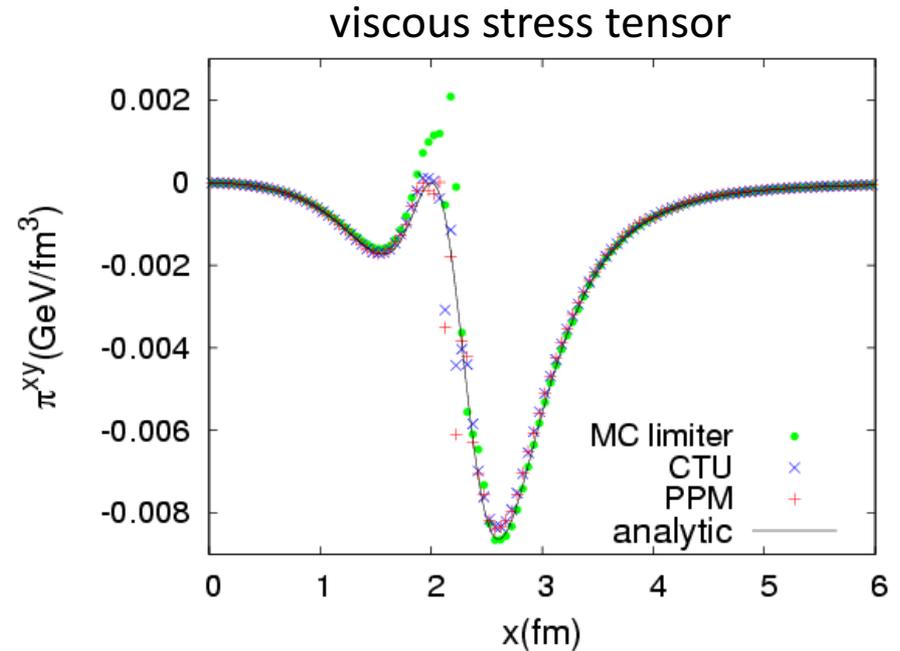
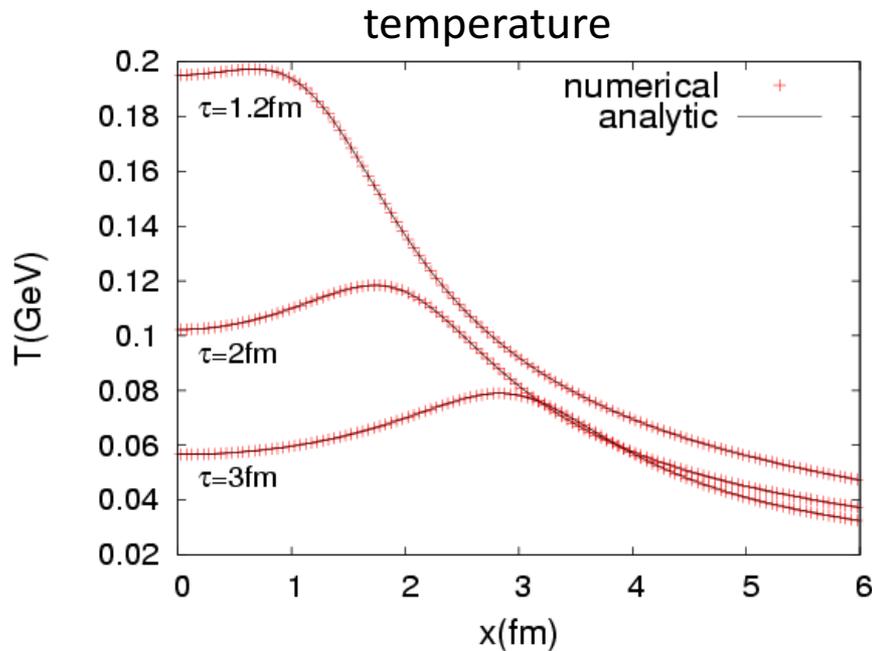
Gubser Flow with Finite η/s

Okamoto and Nonaka, EPJC77,383(2017)

- Analytical solution

- Bjorken flow + transverse expansion

Marrochio et al, PRC91,014903(2015)



Our computed results show good agreement with analytical solution.

Our Strategy

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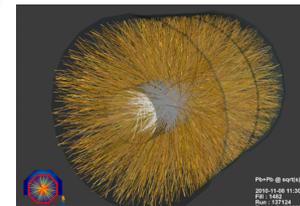
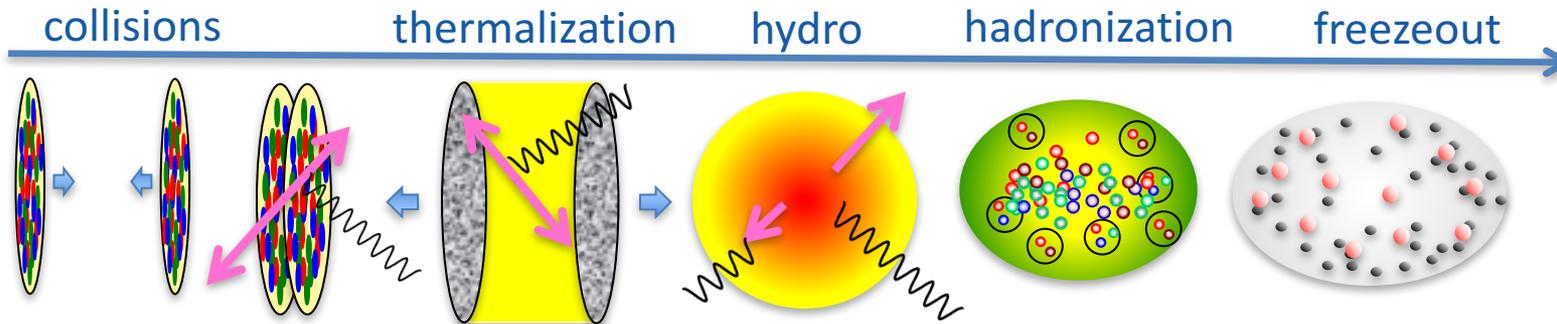
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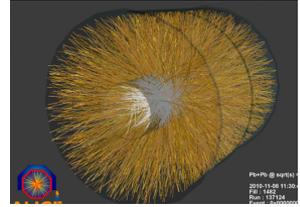
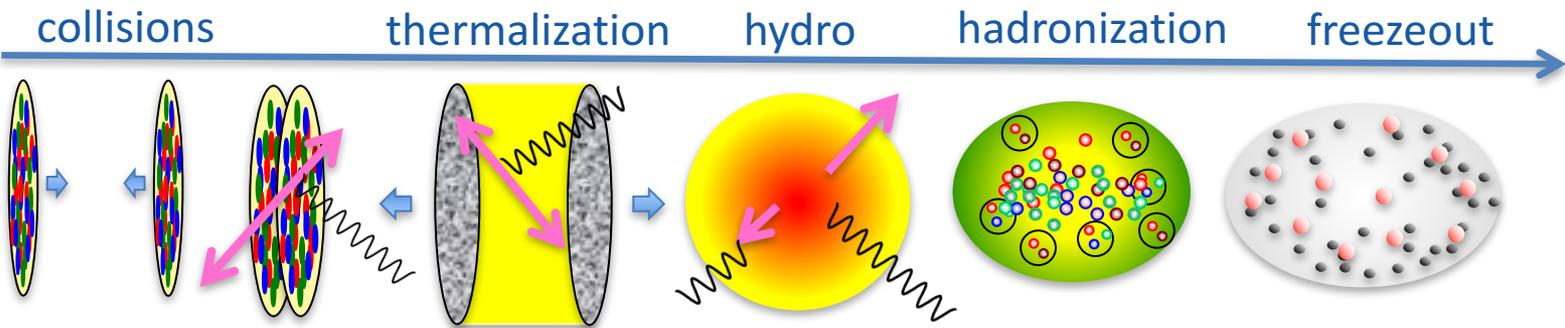
- Description of space-time expansion after collisions

Experimental data



Quantitative Analyses

Experimental data



Initial conditions

Fluctuations:
Glauber, KLN,
IP-Glasma...

TRENTO

Phenomenological model
Parametrization

Moreland et al., PRC92,011901(2015)
Ke et al., PRC96,044192(2017)

Hydrodynamics

QGP bulk property
EoS: lattice QCD
Shear and bulk viscosities

New hydrodynamics code

Final state interactions

Hadron based event generator

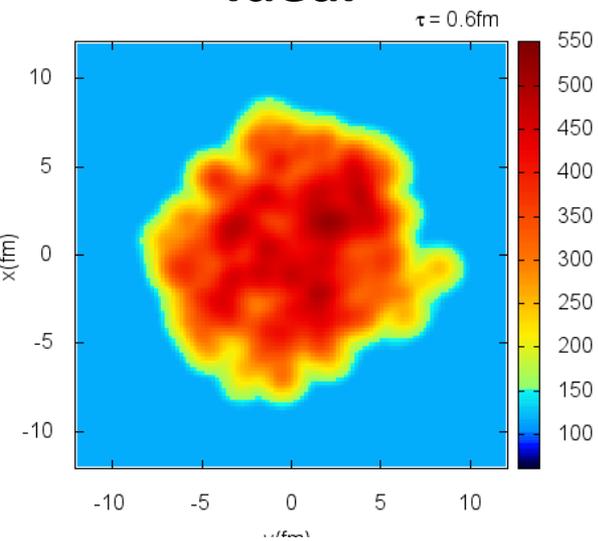
UrQMD

Bass et al., Prog.Part.Nucl.Phys.(1998)
Bleicher et al., J.Phys.G25,1859(1999)

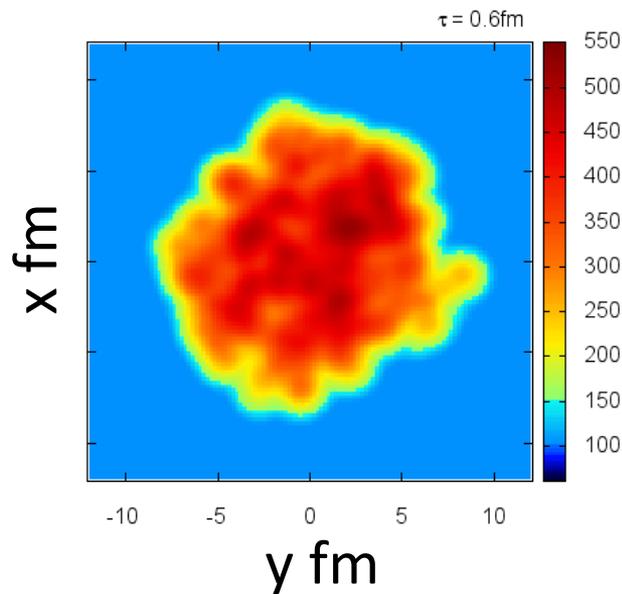


Time Evolution of Temperature

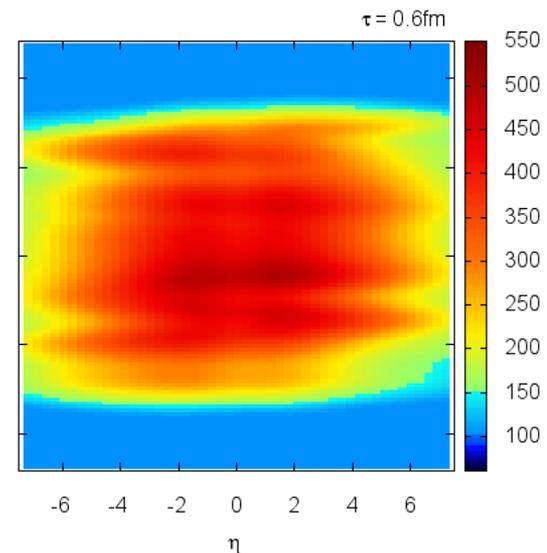
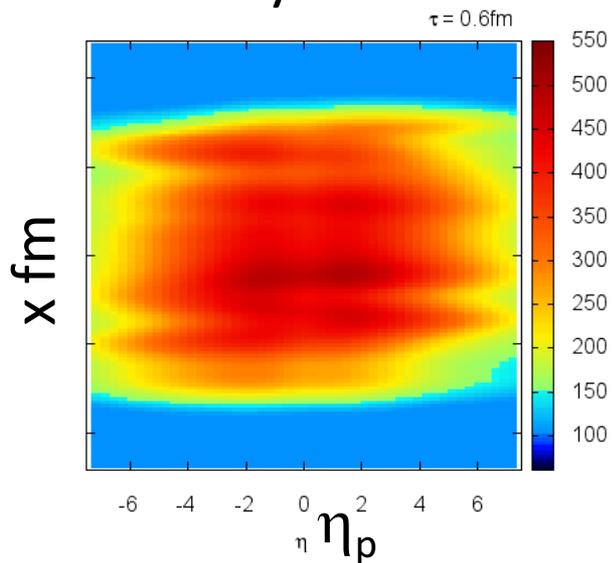
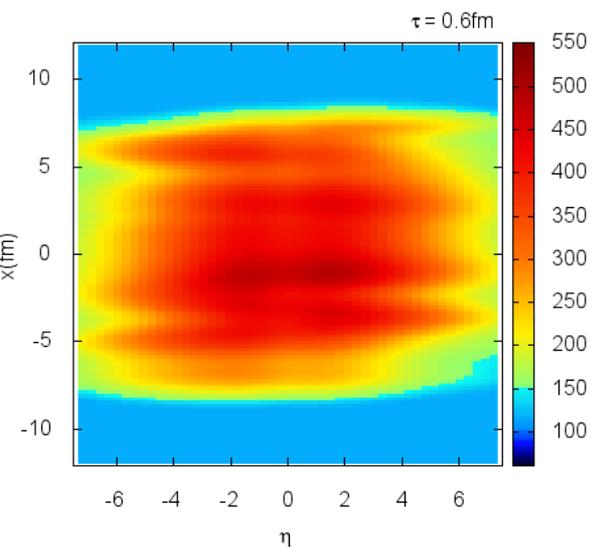
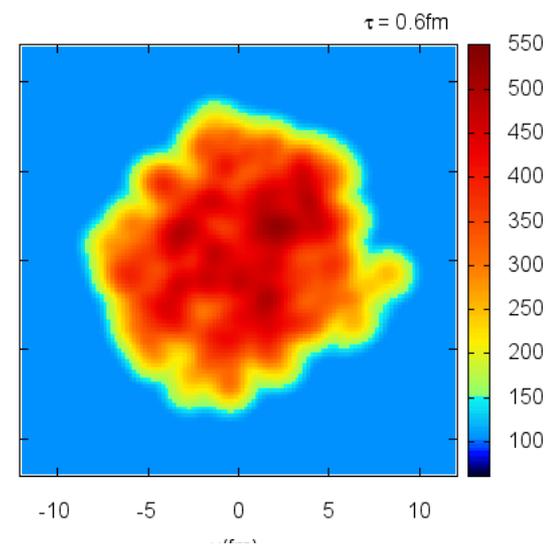
Ideal



shear



shear+bulk



Shear and Bulk Viscosities

shear viscosity

↓ $\eta/s = 0.17$

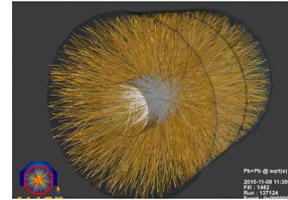
shear + bulk viscosities

↓ $\eta/s = 0.17$

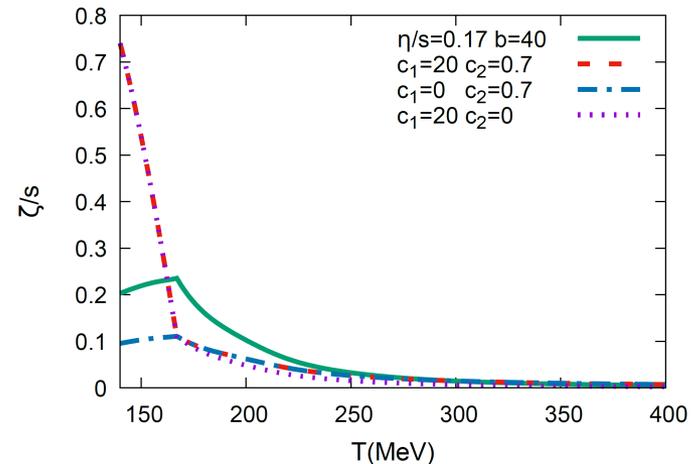
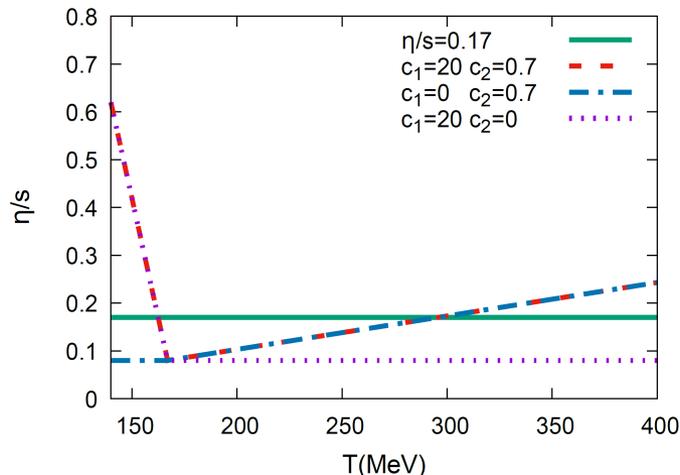
$$\zeta = b\eta \left(\frac{1}{3} - c_s^2 \right)^2 \quad b = 40 \quad \text{Molnar et al., PRC89,074010(2014)}$$

ALICE Pb+Pb $\sqrt{s_{NN}} = 2.76$ TeV, LHC

- ✓ Rapidity distributions
central collision: parameter fixing
- ✓ P_T distributions
- ✓ Mean P_T
- ✓ Collective flow v_2, v_3



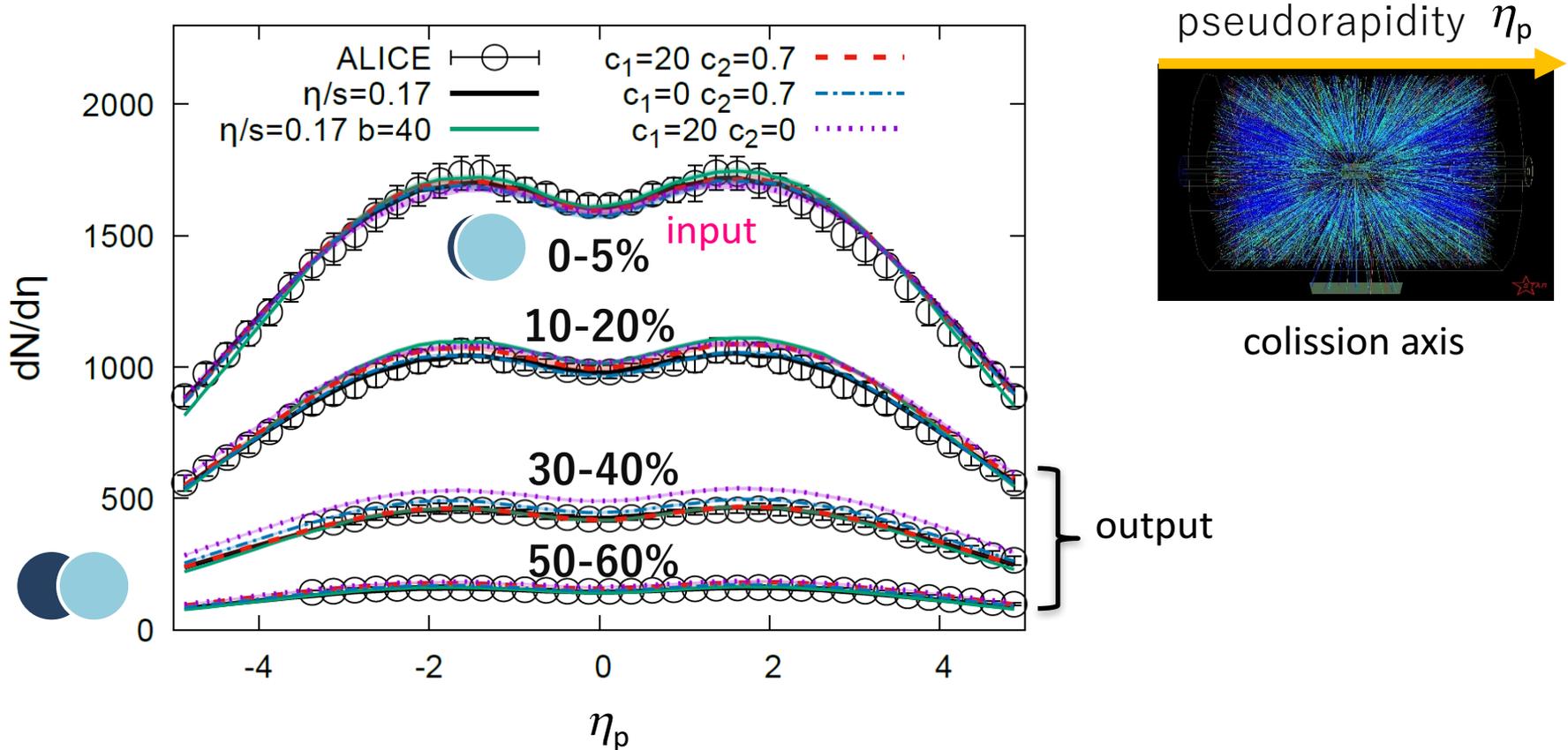
temperature dependent shear + bulk viscosities



Niemi, Eskola, Paatelainen, PRC93, 024907(2016)

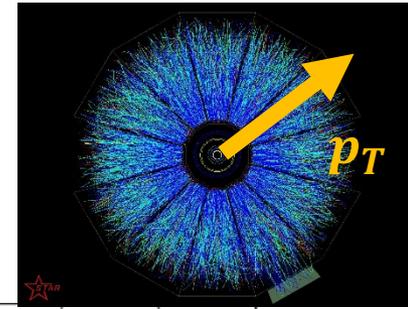
C. NONAKA Denicol, Monnai, Schenke, PRL 116, 212301 (2016)

Rapidity Distributions

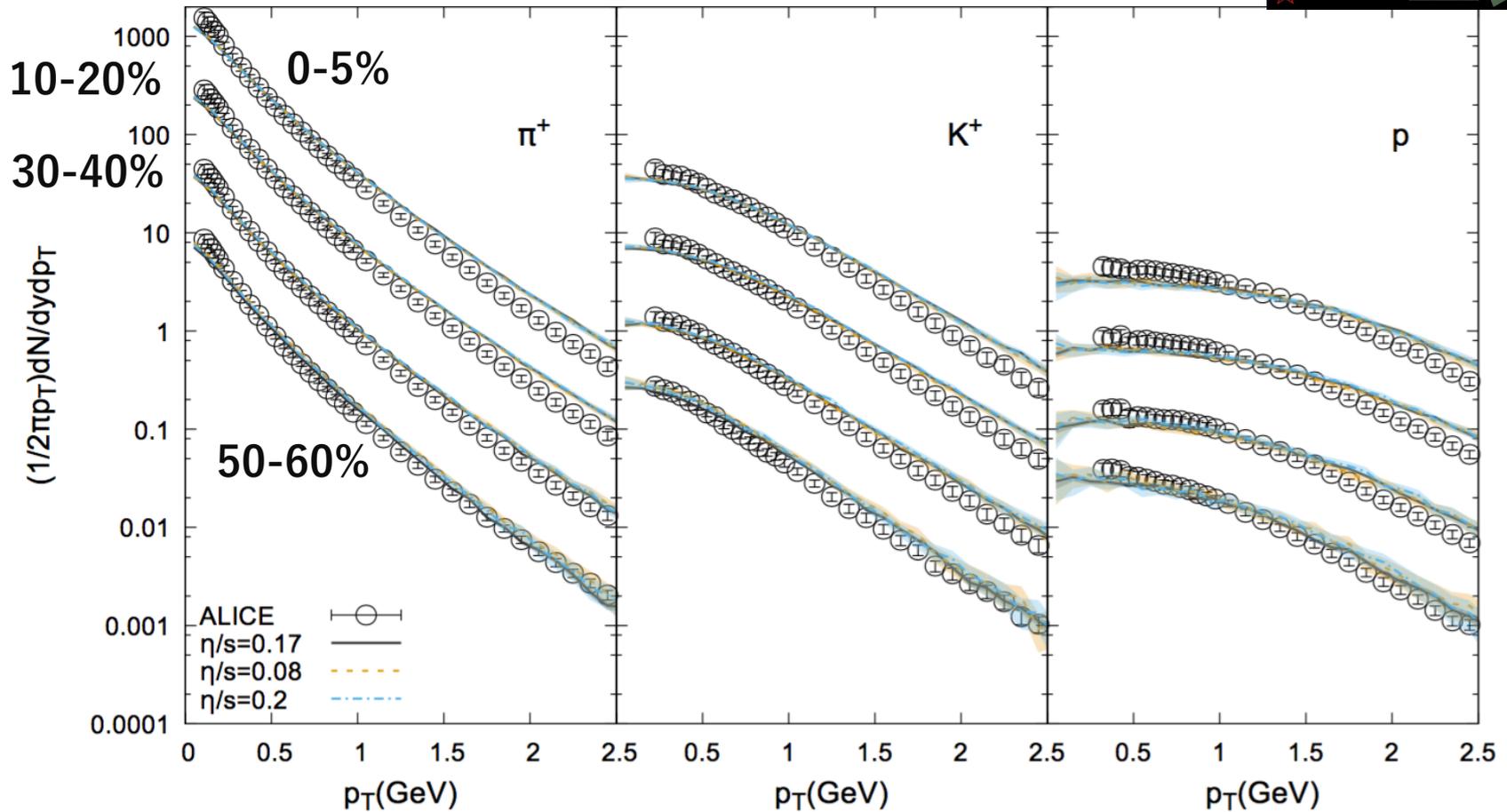


- Parameters in initial condition TRENTO are fixed from comparison with experimental data at 0-5 % centrality.

η/s dependence

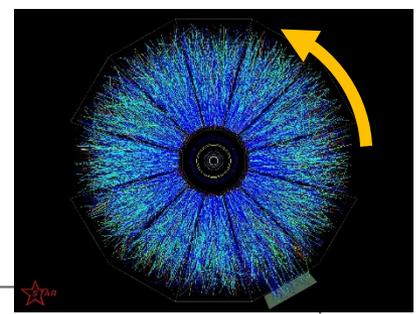


- p_T spectra

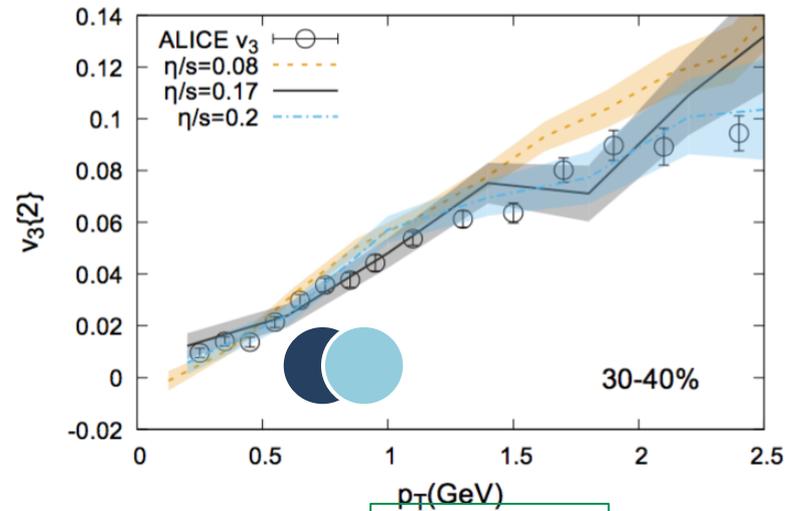
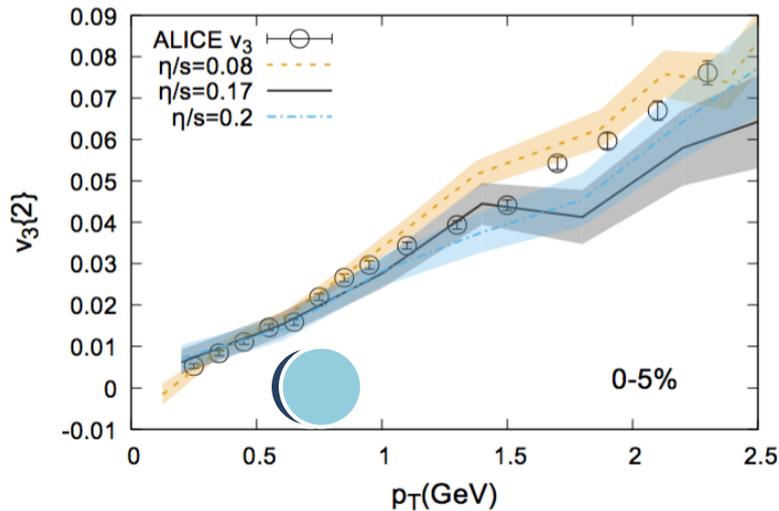
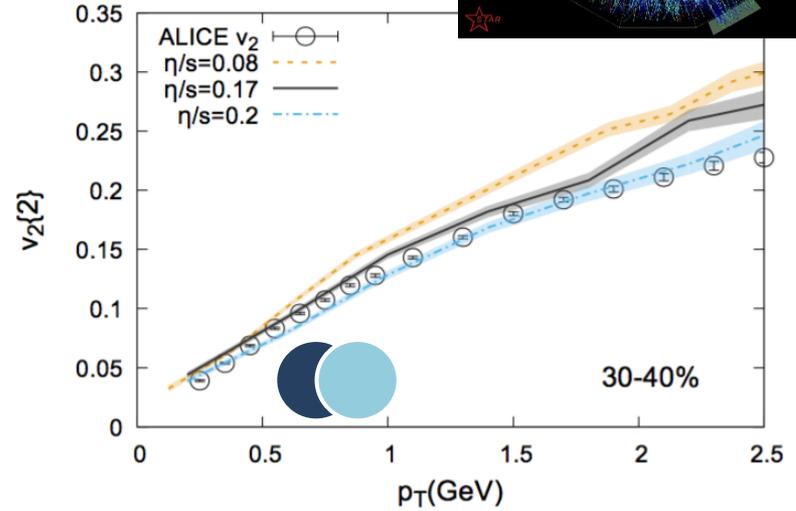
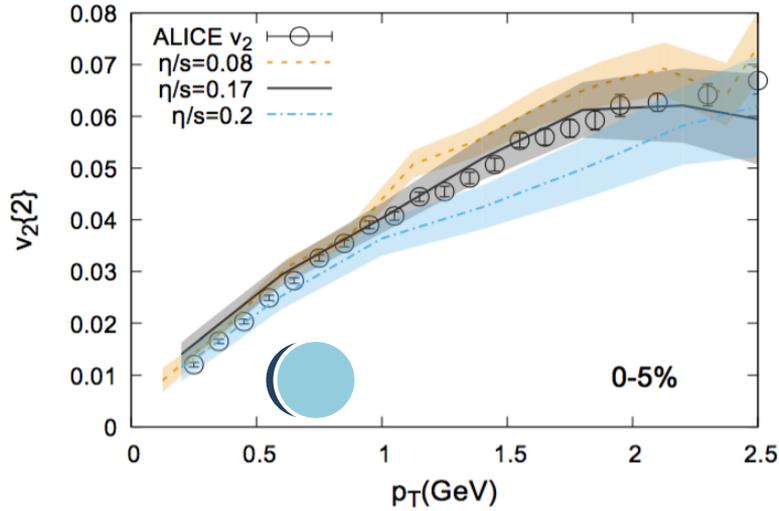


p_T spectra do not depend on η/s .

η/s dependence



- Collective Flows



C. NONAKA

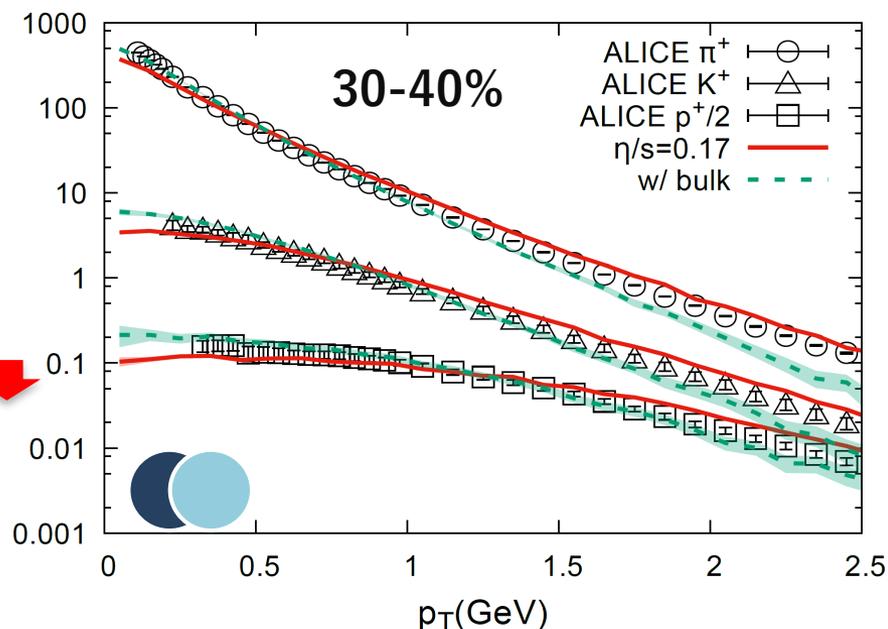
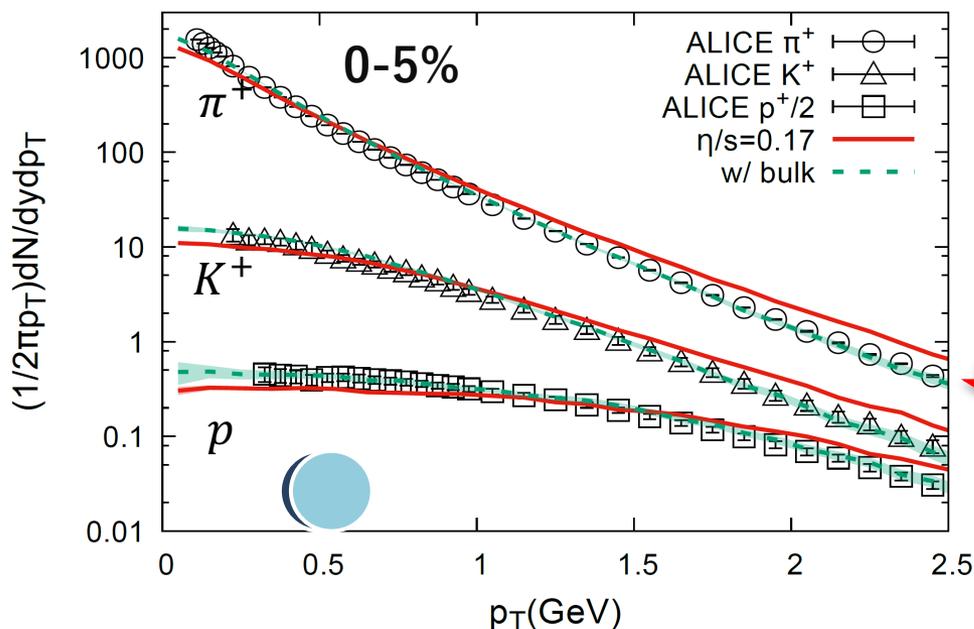
v_2 and v_3 are smaller at larger η/s .



$\eta/s=0.17$

Effect of Bulk Viscosity

- Shear + Bulk viscosities $\zeta = b\eta \left(\frac{1}{3} - c_s^2 \right)^2$



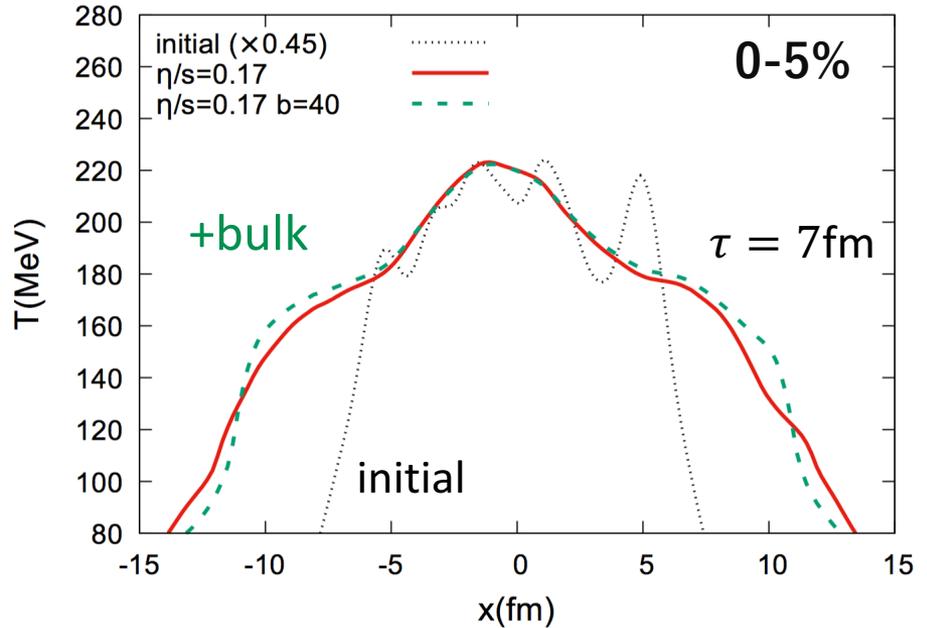
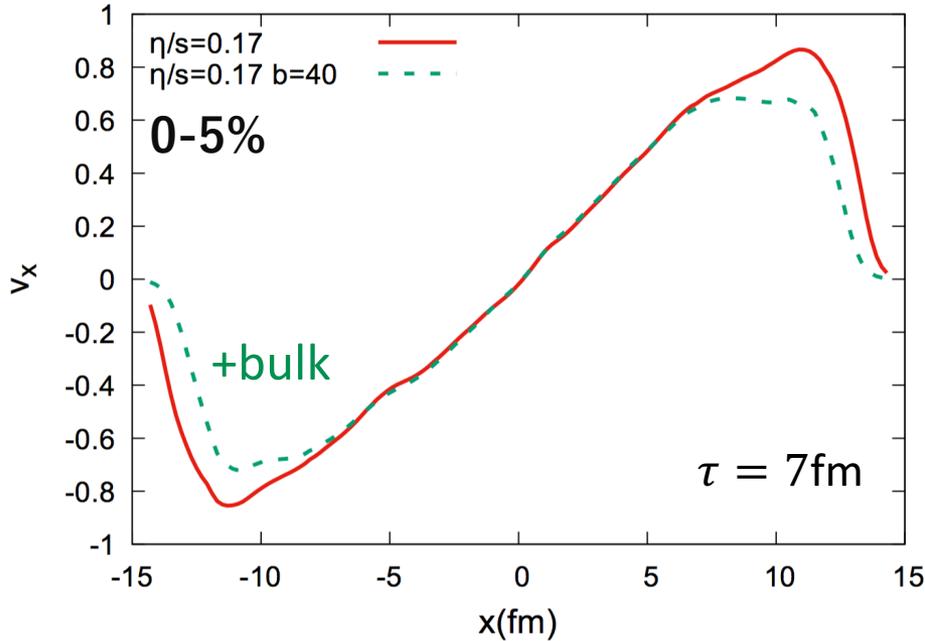
Bulk viscosity reduces the transverse expansion.

-> Slope of P_T spectra becomes steep.

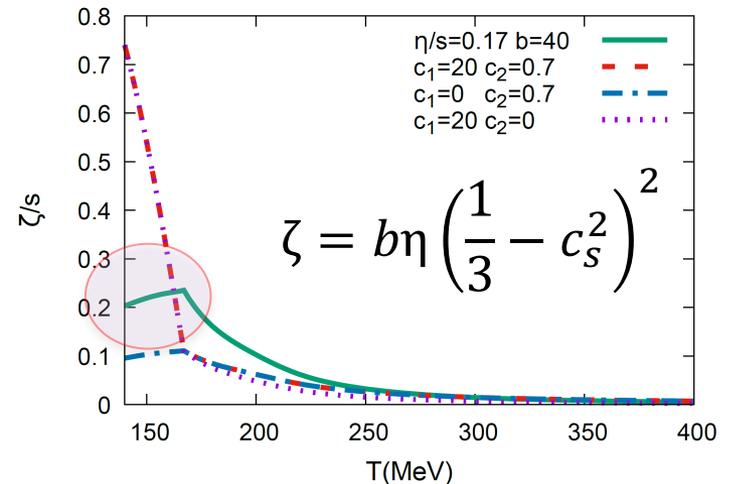
-> Close to ALICE data.

Finite bulk viscosity

Effect on Expansion

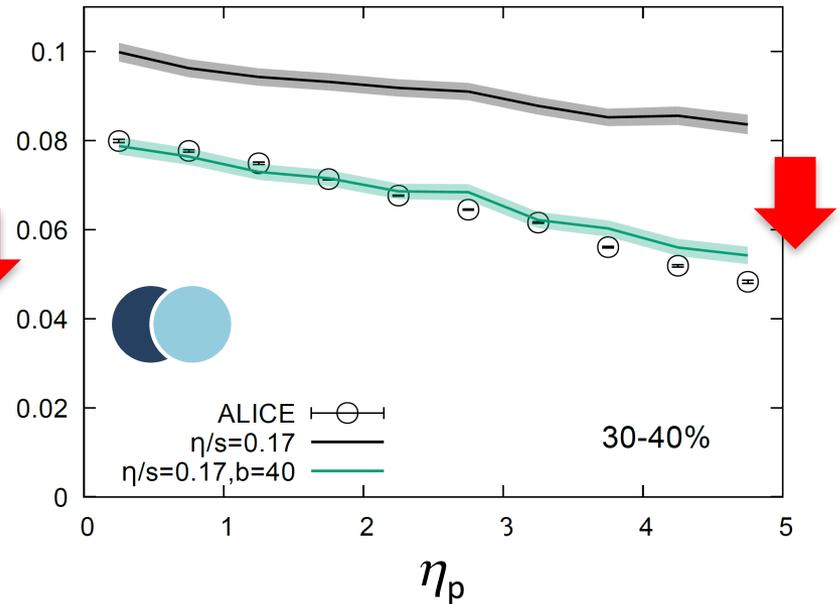
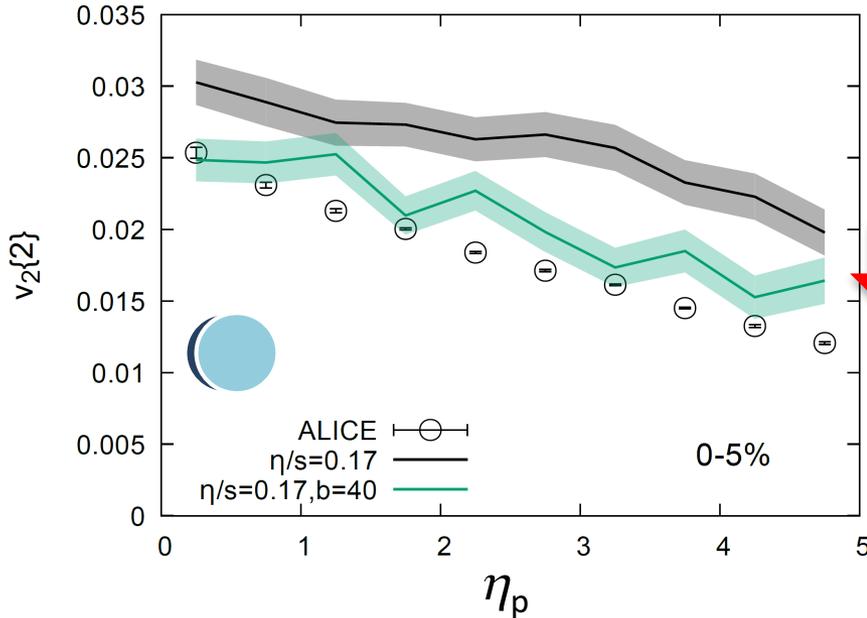


- Bulk viscosity is large below 200 MeV.
- > Its effect appears around $T_c \sim 160$ MeV.
- > Expansion rate decreases in lower temperature region.
- > Volume elements of fluid remain around T_c temperature longer.



Effect on Collective Flow

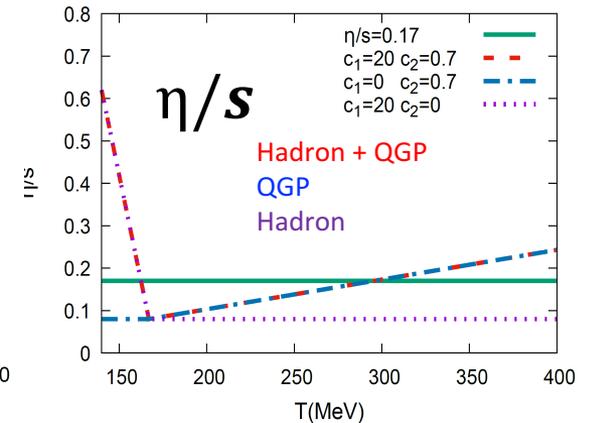
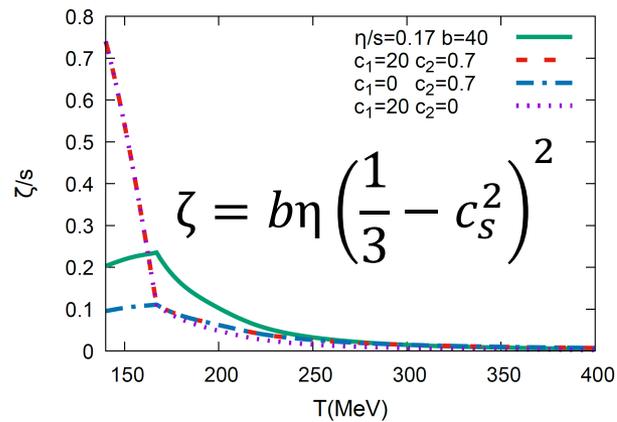
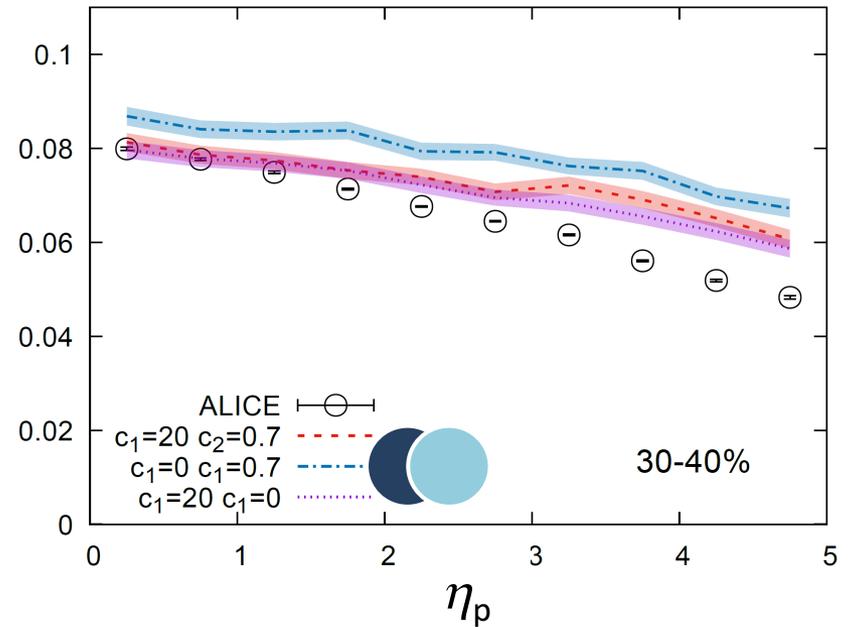
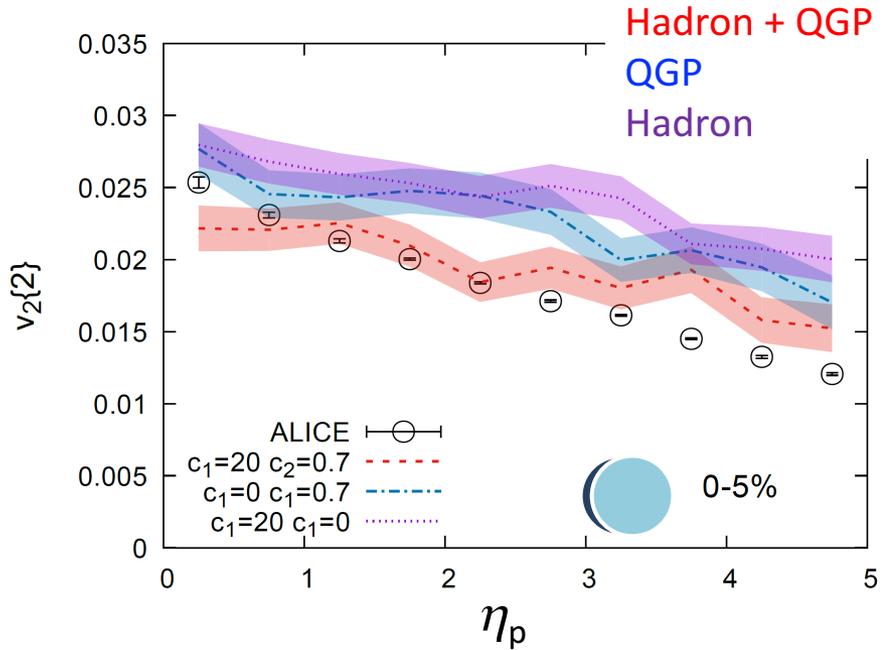
- Collective flow as a function of η_b



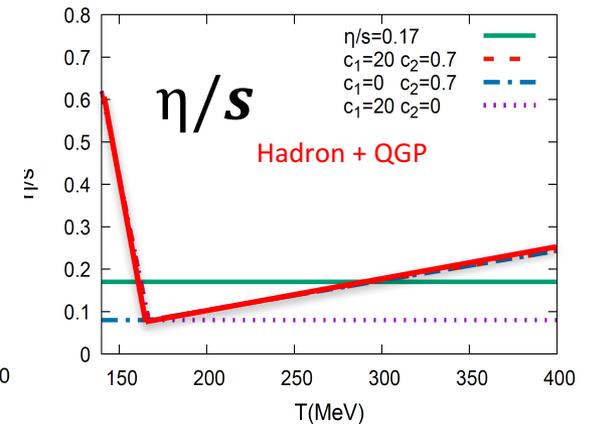
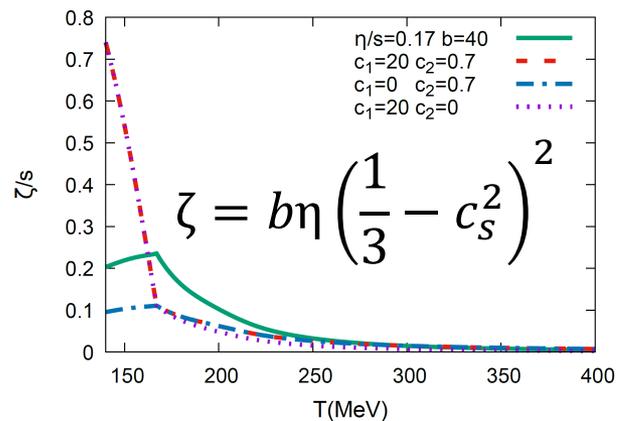
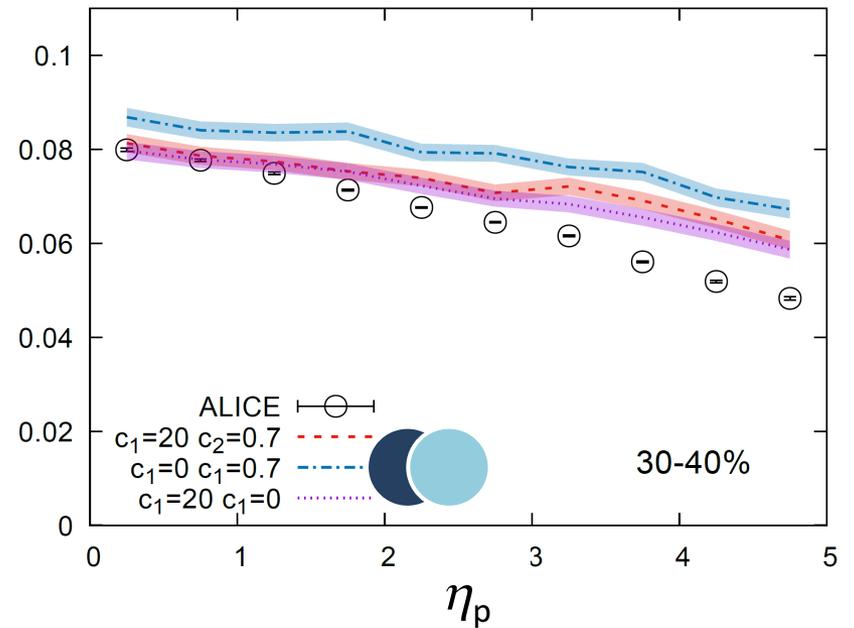
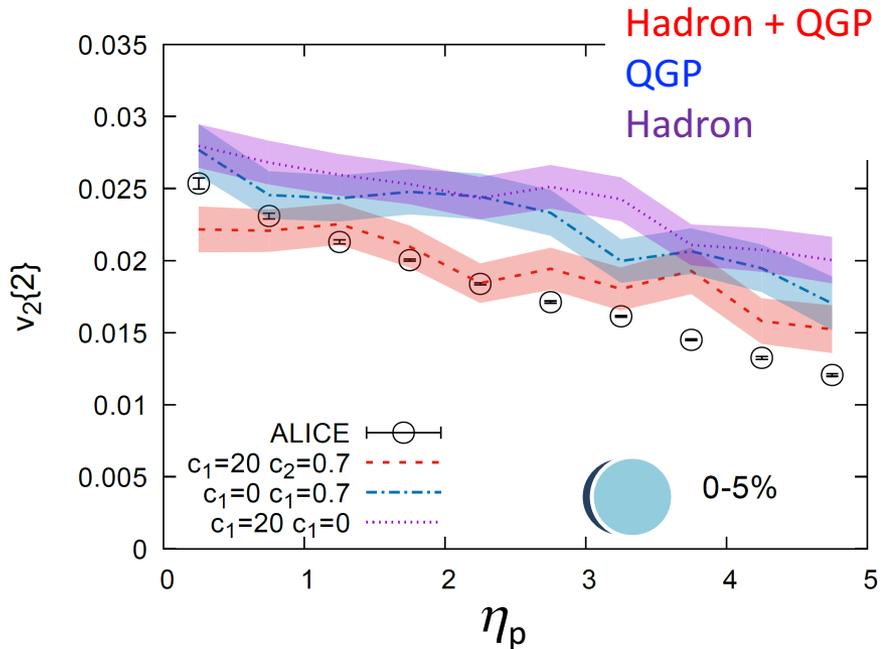
- (3+1)-d calculation
- v_n with bulk viscosity is much closer to the ALICE data: amplitude and slope
- Effect of bulk viscosity at forward rapidity is large.

Finite bulk viscosity

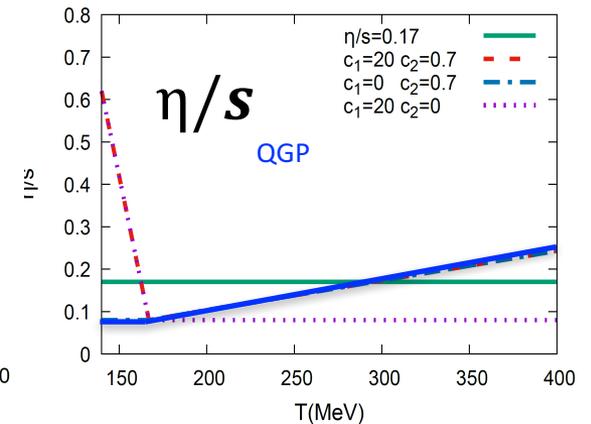
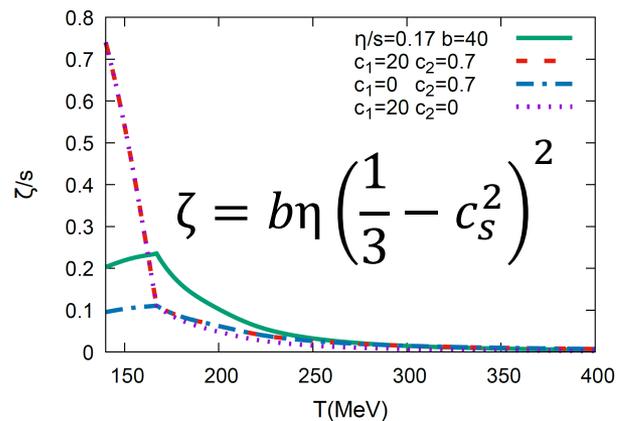
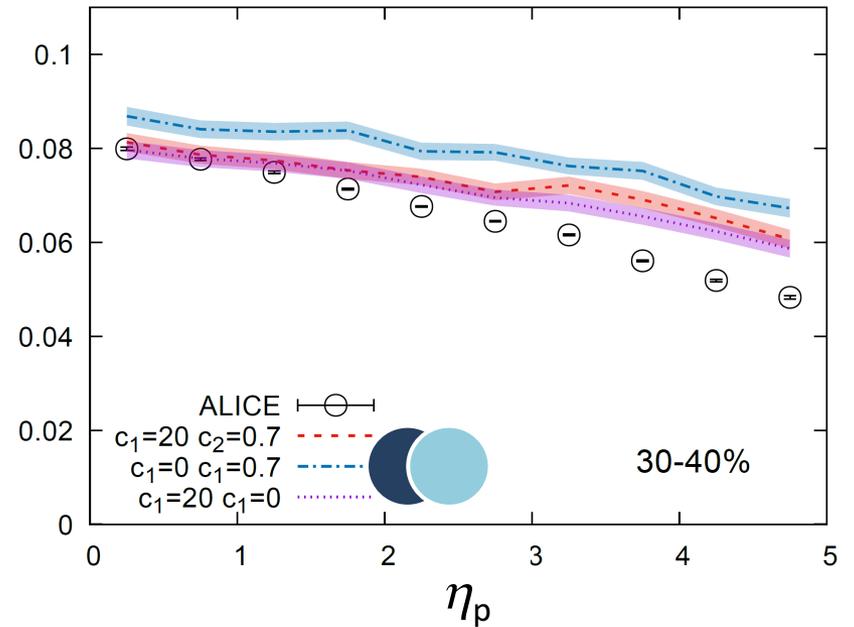
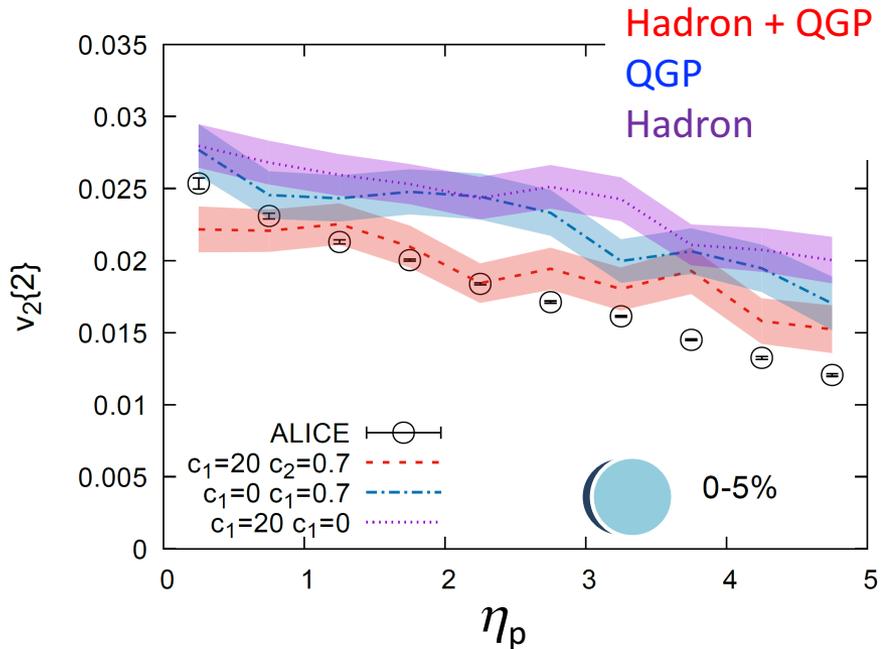
Temperature Dependent η/s



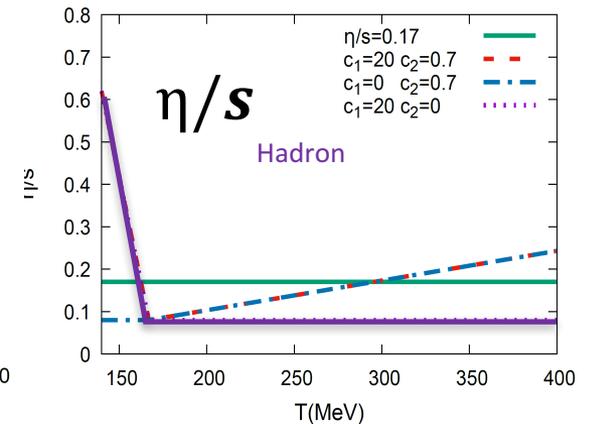
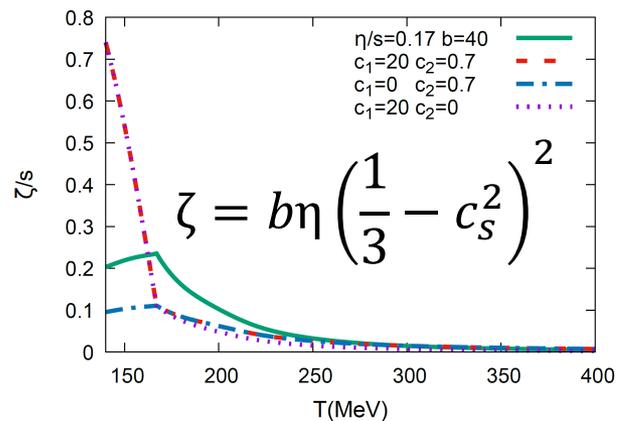
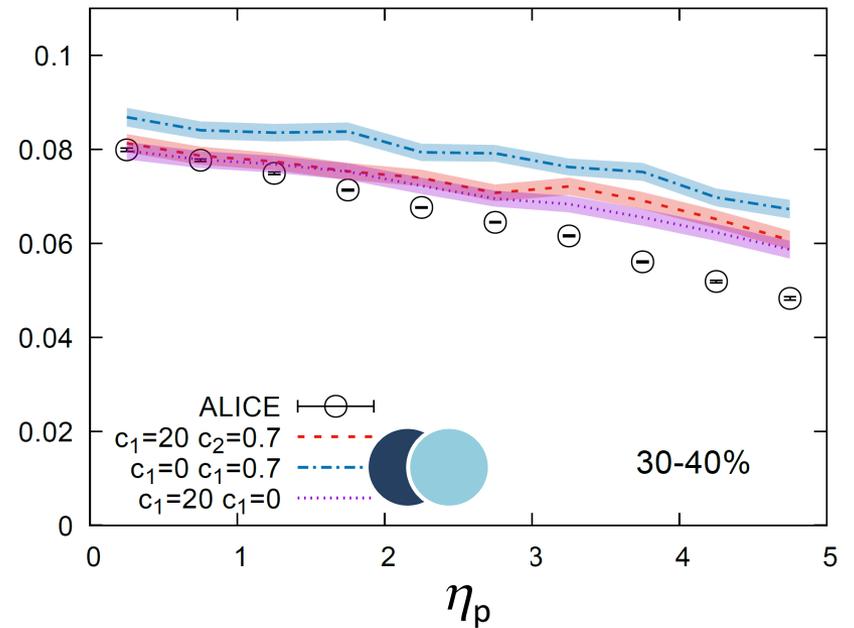
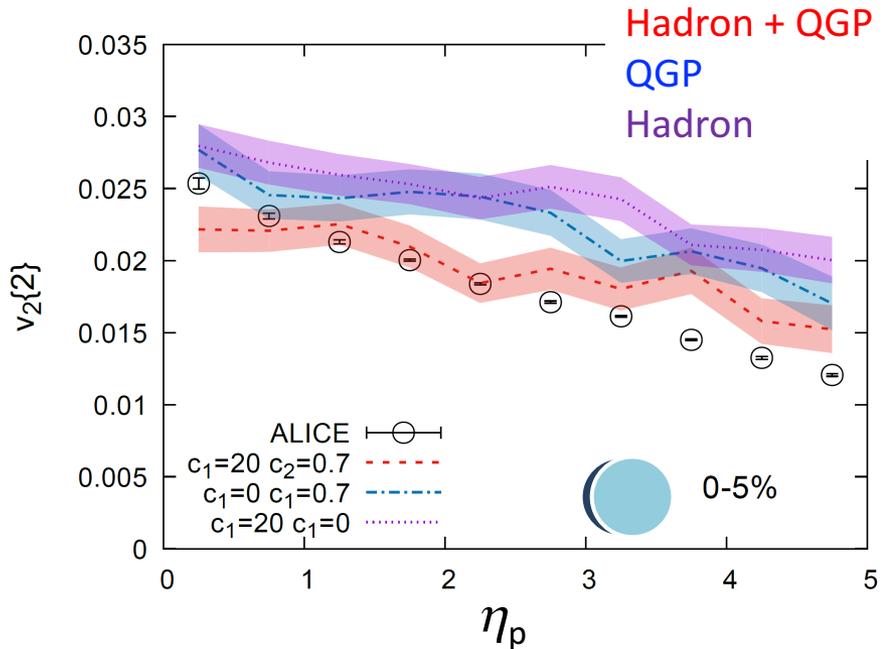
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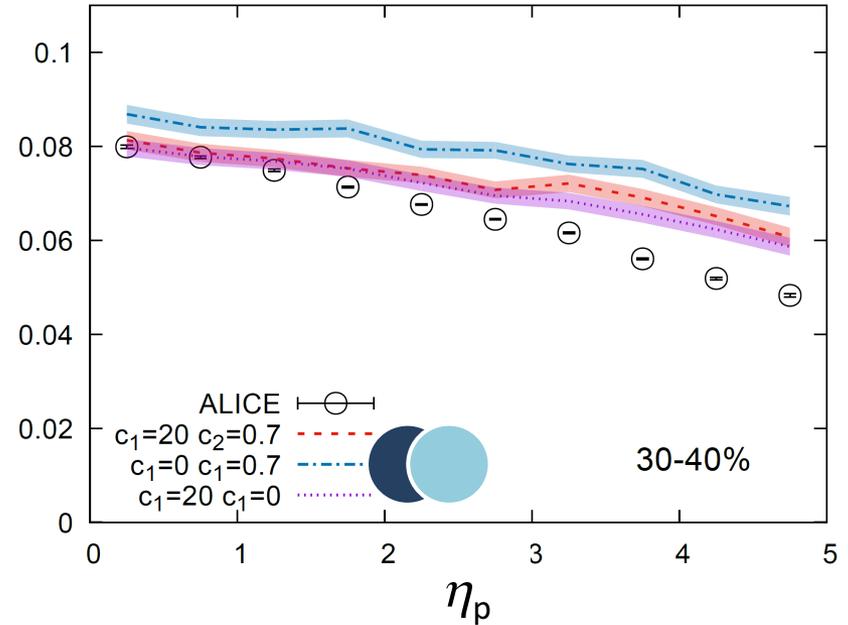
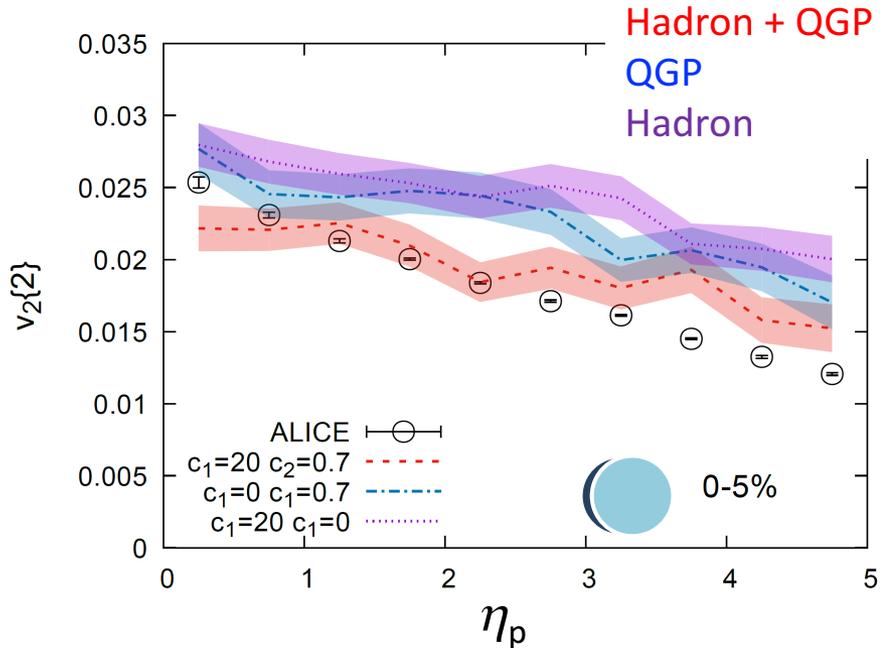
Temperature Dependent η/s



Temperature Dependent η/s



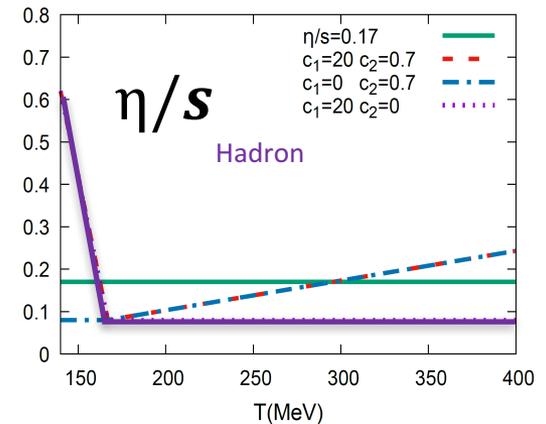
Temperature Dependent η/s



- 0-5 % centrality
 η/s of QGP and hadron phases is important.
- 30-40 % centrality
 η/s of hadron phase is dominant.

$$\zeta = b\eta \left(\frac{1}{3} - c_s^2 \right)_{\eta/s}^2$$

Central dependence of $v_2(\eta_p)$ reveals temperature dependence of η/s .



Summary

Understanding QGP bulk property

- New relativistic viscous hydrodynamics code
 - Stable with small numerical dissipation
 - Phenomenological model: TRENTO — Hydro — UrQMD
 - Quantitative analyses
- QGP bulk property
 - Shear and bulk viscosity
 - Finite bulk viscosity, central dependence of $v_2(\eta_p)$
- Future works
 - Two particle correlations (HBT)
 - Electromagnetic probes

Quantitative analyses

TRENTO — Hydro — UrQMD

Akamatsu et al, JCP256,34(2014)

Okamoto, Akamatsu, Nonaka, EPJC76,579(2016)

Okamoto and Nonaka, EPJC77,383(2017)

Okamoto and Nonaka, arXiv:1712.00923

Bayesian analyses, deep learning: Bass, Bernhard, Moreland, Pang....