#### **Core-Collapse Supernova Overview**

t = 287.37 ms

#### Christian D. Ott TAPIR, Caltech



**Collaborators:** 

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Sherman Fairchild Foundation





# **Collapse and Bounce**



### **Collapse and Core "Bounce"**

Central rest-mass density in the collapsing core:





# **An Aside on the Nuclear EOS**



### **Available Core-Collapse Supernova EOS**

Richer+16 in prep, see <u>https://stellarcollapse.org</u> for tables and references



- ~18 hot nuclear EOS available for CCSN & NS merger simulations.
- Many ruled out by experiments / astrophysical constraints (-> Jim Lattimer's talk on November 1). Need more EOS!

### **Situation after Core Bounce**



### **Situation after Core Bounce**



The shock always stalls:
 Dissociation of Fe-group nuclei @ ~8.8 MeV/baryon (~17 B/M<sub>Sun</sub>).
 Neutrino losses initially @ >100 B/s (1 [B]ethe = 10<sup>51</sup> ergs).

# "Postbounce" Evolution



# "Postbounce" Evolution



#### What is the mechanism that revives the shock?

# Supernova Mechanisms

#### **Neutrino Mechanism**

- Neutrino heating; **turbulent convection**, standing accretion shock instability (SASI).
- Works (even in 1D) for lowest mass massive stars.
- Sensitive to (multi-D) progenitor star structure.
- Inefficient ( $\eta \le 10\%$ ); difficulty explaining  $E_{explosion}$ ?





#### **Magnetorotational Mechanism**

Ott+13

- Magneto-centrifugal forcing, hoop stresses.
- For energetic explosions and CCSN-LGRB connection?
- Very rapid core rotation + magnetorotational instability + dynamo for large-scale field.
- Needs "special" progenitor evolution.
- Jets unstable, may fail to explode in proto-NS phase; black hole formation, GRB central engine?

#### **Basic Stalled-Shock Situation**



http://stellarcollapse.org/

#### **Basic Stalled-Shock Situation**



http://stellarcollapse.org/

### **Neutrino Mechanism: Heating**

Bethe & Wilson '85; also see: Janka '01, Janka+ '07



#### **Basic Stalled-Shock Situation**



GR1D simulation http://stellarcollapse.org/

# 2D and 3D Neutrino-Driven CCSNe

- Progress driven by advances in compute power!
- First 2D (axisymmetric) simulations in the 1990s: Herant+94, Burrows+95, Janka & E. Müller 96.



2D simulations now self-consistent & from first principles.
 E.g.: Bruenn+13,16 (ORNL), Dolence+14 (Princeton),
 B. Müller+12ab (MPA Garching), Nagakura+16 (YITP/Waseda),
 Suwa+16 & Takiwaki+14 (YITP/NAOJ/Fukoka)



Dessart+ '05

### Standing Accretion Shock Instability (SASI)

Blondin+'03 Foglizzo+'06 Scheck+ '08 and many others

Movie by Burrows, Livne, Dessart, Ott, Murphy'06



### **The 3D Frontier** – Petascale Computing!



- Some early work: Fryer & Warren 02, 04
- Much work since ~2010:

Fernandez 10, Nordhaus+10, Takiwaki+11,13,14, Burrows+12, Murphy+13, Dolence+13, Hanke+12,13, Kuroda+12, Ott+13, Couch 13, Couch & Ott 13, 15, Abdikamalov+15, Couch & O'Connor 14, Lentz+15, Melson+15ab, Kuroda+16, Roberts+16

Approximations currently made:
(1) Gravity (2) Neutrinos (3) Resolution



Ott+13 Caltech, full GR, parameterized neutrino heating -6.18 ms



#### **Multi-Dimensional Simulations: Effects**

(e.g., Hanke+13, Couch&Ott 15, Murphy+08, Murphy+13, Ott+13, Dolence+13)



#### **Accounting for Turbulent Ram**

(Couch & Ott 2015, Murphy+13)



#### 2D & 3D Explosions!

(e.g., Lentz+15, Melson+15ab)



### 1D, 2D, 3D

(Couch & Ott 2015)



(1) 2D & 3D explode with less neutrino heating.(2) 2D explodes more easily than 3D!

(see also: Couch & O'Connor 14, Hanke+13)

#### Some Facts about Supernova Turbulence

(e.g., Abdikamalov, Ott+ 15, Radice+15ab)

- Neutrino-driven convection is turbulent.  $\mathcal{R}e=rac{lu}{l}pprox 10^{17}$
- **Kolmogorov** turbulence: Kolmogorov 1941 isotropic, incompressible, stationary.
- Supernova turbulence: anisotropic (buoyancy), mildly compressible, quasi-stationary.
- Reynolds stresses (relevant for explosion!) dominated by dynamics at largest scales.

$$R_{ij} = \overline{\delta v_i \delta v_j}$$

 $E(k) \propto k^{-5/3}$ 

### **Kolmogorov Turbulence**



#### 2D vs. 3D

(e.g., Couch 13, Couch & O'Connor 14)



### **Turbulent Cascade: 2D vs. 3D**



#### Couch & O'Connor 14

see also: Dolence+13, Hanke+12,13, Abdikamalov+'15, Radice+15ab

### **3D: Sensitivity to Resolution**

Abdikamalov+15



#### **Resolution Comparison** (Radice+16)

 semi-global simulations of neutrino-driven turbulence.

> dθ,dφ = 1.8° dr = 3.8 km

(typical resolution of 3D rad-hydro sims)



 $d\theta$ ,  $d\phi = 0.45^{\circ}$ dr = 0.9 km

 $d\theta, d\phi = 0.3^{\circ}$ dr = 0.64 km



#### **Turbulent Kinetic Energy Spectrum**

(Radice+16)



**Core-collapse supernova turbulence obeys Kolmogorov scaling!** 

But: Global simulations at necessary resolution currently impossible! Way forward? -> Subgrid modeling of neutrino-driven turbulence?

### Summary of 2D & 3D Neutrino-Driven CCSNe

- More efficient neutrino heating, turbulent ram pressure.
- **2D simulations** explode but can't be trusted (unphysical turbulence).
- 3D simulations:
  - (1) most not yet fully self consistent (parameterized);
  - (2) numerical bottleneck in energy cascade (resolution).
- How much resolution is necessary?
- Subgrid model for 3D neutrinodriven turbulence?
  - See also Luke Robert's conference talk on Nov. 4!



Ott+13



# **Magnetorotational Explosions**



• Differential rotation -> reservoir of free energy.

•

Spin energy tapped by magnetorotational instability (MRI)?



[LeBlanc & Wilson '70, Bisnovatyi-Kogan '70 & '74, Meier+76, Ardeljan+'05, Moiseenko+'06, Burrows+'07, Bisnovatyi-Kogan+'08, Takiwaki & Kotake '11, Winteler+ 12, Mösta+14,15]

Rapid Rotation + B-field amplification to > 10<sup>15</sup> G (need magnetorotational instability [MRI])

MHD stresses lead to outflows.

2D: Energetic "bipolar" explosions.

Results in ms-period "proto-magnetar." -> connection to GRBs, Superluminous SNe?

Problem: Need high core spin; only in very few progenitor stars?

Burrows+'07


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Burrows+'07

(10<sup>11</sup> G seed field)

## **3D Dynamics of Magnetorotational Explosions**

New, full 3D GRMHD simulations. Mösta+ 2014, ApJL. Initial configuration as in Takiwaki+11, 10<sup>12</sup> G seed field.





 $t = -3.00 \, \text{ms}$ 

Pseudocolor Var: HYDROBASE-entropy - 10.00

Max: 4.135 Min: 1.187



#### Octant Symmetry (no odd modes)

t = -3.00 ms

Mösta+ 2014 ApJL

# **Observing the Heart of a Supernova**

Probes of Supernova & Nuclear Physics:

- Neutrinos
- Gravitational Waves
- EM waves (optical/UV/X/Gamma): secondary information, late-time probes.

Red Supergiant Betelgeuse



# **SN 1987A: Neutrino Detection!**



# Supernova Neutrino "Lightcurves"



# Probing Stellar Structure and the Nuclear EOS with Pre-Explosion Neutrinos

O'Connor & Ott '13, ApJ

- Neutrino signal in the pre-explosion phase determined by (1) the accretion rate of the stellar envelope,
  (2) by the core temperature of the collapsing star.
- EOS dependence: softer EOS -> more compact proto-NS -> harder spectrum, higher luminosity

$$\xi_M = \frac{M/M_{\odot}}{R(M_{\text{bary}} = M)/1000 \,\text{km}} \Big|_{t=t_{\text{bounce}}}$$



"compactness parameter" (O'Connor & Ott '11)

### **Probing Stellar Structure with Pre-Explosion Neutrinos**

O'Connor & Ott '13, ApJ



### **EOS Dependence of the Early Neutrino Signal**

O'Connor & Ott '13, ApJ



### **EOS Dependence of the Early Neutrino Signal**

O'Connor & Ott '13, ApJ



Note: Extracting EOS information will require precise knowledge of distance to source.

# **Gravitational Wave (GW) Refresher**

• Emission: Accelerated quadrupole bulk mass-energy motion.



- -> must measure relative displacements of 10<sup>-22</sup>
- Detection:

Measure changes in separations of test masses with laser interferometry. ->Advanced LIGO, Kagra Advanced Virgo, LIGO India.



### **Gravitational-Waves from Core-Collapse Supernovae**

Reviews: Kotake 11, Fryer & New 11, Ott 09

Need:  

$$h_{jk}^{TT}(t, \vec{x}) = \left[\frac{2}{c^4} \frac{G}{|\vec{x}|} \ddot{I}_{jk}(t - \frac{|\vec{x}|}{c})\right]^{TT} \longrightarrow$$

accelerated aspherical (quadrupole) mass-energy motions

#### **Candidate Emission Processes:**

- Turbulent convection
- Rotating collapse & bounce
- 3D MHD/HD instabilities
- Aspherical mass-energy outflows



### **GWs from Convection & Standing Accretion Shock Instability**

Recent work: Murphy+09, Kotake+09, 11, Yakunin+10,16, E. Müller+12, B.Müller+13



### **Time-Frequency Analysis of GWs**

Murphy, Ott, Burrows 09, see also B. Müller+13, Sotani & Takiwaki 16



### **Detectability?**



### **GWs from Rotating Collapse & Bounce**

Recent work: Dimmelmeier+08, Scheidegger+10, Ott+12, Abdikamalov+14



- Axisymmetric: ONLY h<sub>+</sub>
- Simplest GW emission process: Rotation + mass of the inner core + gravity + stiffening of nuclear EOS
- Strong signals for rapid rotation (-> millisecond proto-NS).
- Magnetorotational mechanism.

# **Probing Multi-Dimensional Supernova Dynamics**

• Rotating core collapse: Correlated neutrino and gravitational-wave signal. Ott+2012



# **EOS Dependence of the GW Signal?**

Richers+2016, in preparation, talk on November 10.

- 2D general-relativistic hydrodynamics.
- 18 EOS, taken from <a href="http://stellarcollapse.org">http://stellarcollapse.org</a>
  - ~1800 **Parameter Value** simulations.  $M_{\rm max} > 1.97 \, M_{\odot}$  $220 \,\mathrm{MeV} < K < 260 \,\mathrm{MeV}$  $28 \,\mathrm{MeV} < S(0) < 34 \,\mathrm{MeV}$ ☆  $20 \,\mathrm{MeV} < L(0) < 120 \,\mathrm{MeV}$ Λ  $\mathbf{N}$ max ☆ ☆ ☆ Constrained  $1.\,97\,M_{\odot}$ min Parameters between the lines satisfy constraints. LS220 LS375 SFHo HShen SFHx HShenH 180HSDD2 BHBL HSIUF HSFSG GSFSU1.7 **GSNL3 HSNL3** BHBLF HSTMA **HSTM1 3SFSU2.**



# **EOS Dependence of the GW Signal?**

Richers+2016, in preparation, talk on November 10.

### **Example result:**





Sherwood Richers

- Rotating core collapse
   GW signal:
   determined by mass
   and angular mom. of
   inner core.
- Dependence on nuclear EOS is weak.

# Summary

- Core-Collapse Supernovae are fundamentally 3D: Turbulence (not resolved!), magnetic field
- 2D/3D simulations: neutrino-driven explosions with limitations -> "supernova problem" not yet solved. Main issues:
  - Progenitor star structure (-> Suwa & Müller 16).
  - Neutrino transport & gravity approximations.
  - Numerical resolution.
  - Neutrino oscillations? (v-v interactions)
  - Input microphysics (EOS, v interactions).
- Probably need magnetorotational mechanism to explain hypernovae.
- Neutrino and GW signals carry information on supernova thermodynamics, dynamics, and nuclear EOS.



# **Supplemental Slides**

# **Technical Details: The Caltech CCSN Code**

[Ott+09, Ott+12, Reisswig+13, Ott+13, Roberts+16]

 Based on the open-source Einstein Toolkit (<u>http://einsteintoolkit.org</u>) and the Cactus Framework.



- Fully general-relativistic using numerical relativity.
- Cartesian AMR grids, cubed-sphere generalized grids.
- Spacetime solvers based on BSSN formalism of numerical relativity.
- Finite-volume GR hydrodynamics, magnetohydrodynamics.
- Microphysical finite-temperature nuclear equations of state.
- Neutrino treatment:

(1) Multi-group two-moment + analytic closure relation.

(2) Extremely efficient gray "leakage"+heating scheme.





- 12 first-order hyperbolic *evolution* equations.
- 4 elliptic *constraint* equations
- 4 coordinate gauge degrees of freedom:  $\alpha$ ,  $\beta^i$ .

# "Equation of State" of Turbulent Pressure

(Radice+15a)

- Reynolds tensor:  $R_{rr} \approx R_{\theta\theta} + R_{\phi\phi}$  (buoyancy)  $R_{ij} = \delta v_i \delta v_j$
- Specific turbulent energy:  $\epsilon_{turb} = \frac{1}{2} |\delta \mathbf{v}|^2$

$$|\delta \mathbf{v}^2| = (\delta v_r)^2 + (\delta v_\theta)^2 + (\delta v_\phi)^2 \approx 2 (\delta v_r)^2$$
 (buoyancy)

$$(\delta v_r)^2 \approx \frac{1}{2} |\delta \mathbf{v}|^2 = \epsilon_{\text{turb}}$$

Rankine-Hugoniot with turbulence:

$$P_d + \rho_d v_d^2 + \rho_d (\delta v_r)^2 = \rho_u v_u^2 \qquad \Gamma_{\rm th} \approx 4/3$$
  

$$(\gamma_{\rm th} - 1)\rho\epsilon_{\rm th} + \rho_d v_d^2 + \rho(\delta v_r)^2 = \rho_u v_u^2 \qquad \Gamma_{\rm turb} \approx 2$$
  

$$(\gamma_{\rm th} - 1)\rho\epsilon_{\rm th} + \rho_d v_d^2 + \rho\epsilon_{\rm turb} = \rho_u v_u^2$$
  

$$(\gamma_{\rm th} - 1)\rho\epsilon_{\rm th} + \rho_d v_d^2 + (\Gamma_{\rm turb} - 1)\rho\epsilon_{\rm turb} = \rho_u v_u^2$$

# How much resolution is needed?

• Must (at least) capture correct rate of kinetic energy flux from largest scales. Normalized kinetic energy flux.



## Can this work at all?

Mösta+15, Nature

- All simulations of the magnetorotational mechanism **assume**: MRI works + large-scale field created by dynamo.
- So far impossible to resolve fastest-growing MRI mode in global 3D simulations.
- Unstable regions (roughly):  $\frac{d\ln\Omega}{dr} < 0$
- Precollapse field 10<sup>10</sup> G,
   ~10<sup>14</sup> G at bounce.
- Fastest growing mode:
   λ ~ 1 km.



# **Simulation Setup**

Mösta+15, Nature

- Rapidly spinning, magnetized proto-NS.
- Global simulation in quadrant symmetry: 70 km x 70 km x 140 km box
- Resolutions: 500 m/200 m/100 m/50 m
- hot nuclear eq. of state, neutrinos, fixed gravity, GRMHD.
- Simulations on 130,000 CPU cores on NSF Blue Waters, simulate for 10-20 ms.

### **Key questions:**

- Does the MRI efficiently build up dynamically relevant field?
- Saturation field strength? Global field structure?





### **Global Field Structure**

Mösta+15, Nature



dx = 500 m







Caltech

C. D. Ott @ NPCSM 2016

## **Local Magnetic Field Saturation**

Mösta+15, Nature

- Initial exponential growth resolved with 100m/50m simulations.
- Saturated turbulent state within 5 ms.



### **Energy Spectra**

Mösta+15, Nature



Magnetic energy spectrum very resolution dependent.



### **Energy Spectra**

Mösta+15, Nature



- Turbulent saturated state after ~3 ms.
- Inverse cascade (dynamo) afterwards.

## **B-Field Growth at Large Scales**

Mösta+15, Nature

- k=4; corresponding roughly to width of shear layer
- Field will grow to saturation at large scales within ~60 ms.



### Implications: Magnetars, Hypernovae, GRBs

- MRI+dynamo -> prompt formation of "proto-magnetar."
  - -> magnetorotational explosions possible -> hypernovae?
     -> could drive relativistic jet at late times -> GRB? (Metzger+11)



Artist's impression of the magnetar in Westerlund 1



- Power
   "superluminous
   supernovae"?
   (Kasen & Bildsten 10)
- ~10% of Milky Way neutron stars are magnetars.



# What is happening here?

Mösta+14, ApJL

• B-field near proto-NS:  $B_{tor} >> B_z$ 



- Unstable to MHD screw-pinch kink instability.
- Similar to situation in Tokamak fusion reactors!





Credit: Moser & Bellan, Caltech



Braithwaite+ '06

C. D. Ott @ NPCSM 2016

## **Explosion?**





t = -4.95 ms

#### Mösta+ 2014 ApJL Plasma β

$$\beta = \frac{P_{\text{gas}}}{P_{\text{mag}}}$$


## **Neutrinos: Mean Energies**

