Hyperon puzzle and RMF models

with scaled hadron masses and coupling constants

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"Hyperon puzzle" and constraints on the nuclear EoS maximum mass of a neutron star constraint on pressure from HIC constraint from direct Urca (DU) processes "hyperon puzzle"

Cut mechanism for hardening the nucleon EoS.
Non-linear Walecka model: Play with a scalar-field potential

Scaling of meson masses and coupling constants

Solution of the hyperons puzzle in neutron stars

 $\succ \Delta$ baryons









http://www.stellarcollapse.org/

Constraint on the stiffness of nuclear EoS [Danielewicz, Lacey, Lynch, Science 298, 1592 (2002)]

directed and elliptic flow of particles in heavy-ion collisions



Neutron star cooling and direct Urca reactions

DU:
$$n \rightarrow p + e^- + \bar{\nu}_e$$

 $\epsilon_{\rm DU} = 10^{27} T_9^6 \frac{\rm erg}{\rm cm^3 \, s}$
MU: $n + n \rightarrow n + n + e^- + \bar{\nu}_e$
 $\epsilon_{\rm MU} = 10^{22} T_9^8 \frac{\rm erg}{\rm cm^3 \, s}$
tandard scenario (MU+pairing)

only "slow" cooling can be described

Neutron stars with $M > M_{\text{crit}}^{\text{DU}}$ will be too cold

DU process schould be "exotics" (if DU starts it is dificult to stop it)

 $M_{
m crit}^{
m DU} \stackrel{>}{_\sim} 1.3~M_{\odot}$ weak constraint

 $M_{
m crit}^{
m DU} \stackrel{>}{_\sim} 1.5 \,\, M_\odot \,\,$ strong constraint

 $Log(T_{surface}/K)$



[Blaschke, Grigorian, Voskresensky A&A 424 (2004) 979]



constraint on the symmetry energy

[EEK, Voskresensky NPA759 (2005) 373]

"Hyperon puzzle"

If we allow for a population of new Fermi seas (hyperon, Δ baryons, ...) EoS will be softer and the NS will be smaller



Simple solutions: -- make nuclear EoS as stiff as possible [flow constraint] -- suppress hyperon population (increase repulsion/reduce attraction)

against phenomenology of YN,NN,YY interaction in vacuum +hypernuclear physics



[Weissenborn et al., NPA 881 (2012) 62]

"Cut" mechanism for hardening the nuclear EoS.

Maslov, EEK, Voskresensky, PRD92 (2015) 052801(R)

The standard non-linear Walecka (NLW) model

$$\begin{split} \mathcal{L} &= \overline{\Psi}_N \begin{bmatrix} \left(i \,\partial_\mu - g_\omega \omega_\mu - g_\rho t \boldsymbol{\rho}_\mu \right) \gamma^\mu - m_N + g_\sigma \sigma \end{bmatrix} \Psi_N \text{ nucleons} \\ &+ \frac{1}{2} [\left(\partial_\mu \sigma \right)^2 - m_\sigma^2 \sigma^2] - U(\sigma) & \text{scalar field} \\ &- \frac{1}{4} \omega_{\mu\nu} \omega^{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu^2 - \frac{1}{4} \boldsymbol{\rho}_{\mu\nu} \boldsymbol{\rho}^{\mu\nu} + \frac{1}{2} m_\omega^2 (\boldsymbol{\rho}_\mu)^2 & \text{vector fields} \end{split}$$

$$U(\sigma) = \frac{b}{3}m_N(g_{\sigma N}\sigma)^3 + \frac{c}{4}(g_{\sigma N}\sigma)^4$$



Input parameters

$$n_0 = 0.16 \,\mathrm{fm}^{-3}, \, \mathcal{E}_0 = -16 \,\mathrm{MeV}, \, K = 250 \,\mathrm{MeV}$$

 $\mathcal{E}_{\mathrm{sym}} = 30 \,\mathrm{MeV}, \, m_N^*(n_0)/m_N = 0.8$
 $\Longrightarrow M_{\mathrm{max}} = 1.92 \, M_{\odot}$

For better description of atomic nuclei one Includes no-linear terms $\omega_{\mu}^4, \, \omega_{\mu}^2 \rho_{\nu}^2$

→ softening of EoS and M_{max} reduction

Maximum mass strongly depends on $m_N^*(n_0)$ and weakly on K.

In NLW the scalar field is monotonously increasing function of the density

$$m_{\sigma}^2 \sigma + U'(\sigma) = g_{\sigma} \left(n_{\mathrm{S},p} + n_{\mathrm{S},n} \right)$$

dimensionless scalar field $~f=g_{\sigma}\sigma/m_N$

$$\frac{f}{C_{\sigma}^2} + \frac{U'(f)}{m_N} = n_{\mathbf{S},p} + n_{\mathbf{S},p}$$

$$\frac{\mathrm{d}f}{\mathrm{d}n} = \frac{2\partial(n_{\mathrm{S},p} + n_{\mathrm{S},n})/\partial n}{m_N^3 C_\sigma^{-2} + \tilde{U}''(f)/m_N - 2\partial(n_{\mathrm{S},p} + n_{\mathrm{S},n})/\partial f}$$

 $n_{\mathrm{S},i} = \int_{0}^{p_{\mathrm{F},i}} \frac{m_N^* p^2 \mathrm{d}p / \pi^2}{(p^2 + m_N^{*2})^{1/2}}$

source is the scalar density

$$egin{aligned} m_N^* &= m_N - g_\sigma \sigma \ m_N^* &= m_N (1-f) \ C_\sigma^2 &= g_\sigma^2 m_N^2 / m_\sigma^2 \end{aligned}$$

$$egin{aligned} &rac{\partial n_{\mathrm{S},i}}{\partial n} = rac{m_N^*}{2\sqrt{p_{\mathrm{F},i}^2+m_N^{*2}}} \ &rac{\partial f}{\partial f} & -rac{\partial n_{\mathrm{S},i}}{\partial f} = \int\limits_{0}^{p_{\mathrm{F},i}} rac{m_N p^4 \mathrm{d} p/\pi^2}{(p^2+m_N^{*2})^{3/2}} \end{aligned}$$

If we modify the scalar potential $\widetilde{U}(\sigma) = U(\sigma) + \Delta U(\sigma)$ so that the m^{*}_N(n) levels off



Simulation of excluded volume effect

If m*N(n) saturates then the EoS stiffens

$$f_{
m s.core}=f_0+c_\sigma(1-f_0)$$



P.-G. Reinhard, [Z. Phys. A 329 (1988) 257] introduced a "switch function" to get rid off the scalar field fluctuations

$$\mathscr{U}''(\Phi) = m_{\infty}^2 + \Delta m^2 \cosh^{-2}\left(\frac{\Phi - \Phi_0}{\delta \Phi}\right)$$



The effect is more pronounced if the input parameter of the model $m_N^*(n_0)$ is chosen smaller

Todd-Rutel, Piekarewicz, Phys. Rev. Lett. 95 (2005) 122501



Alternative FSUGold2 model: W.-Ch. Chen, Piekarewicz, Phys. Rev. C 90 (2014) 044305 $M_{\rm max} = 2.1 \ M_{\odot}$

Attempts to solve the hyperon puzzle

quark counting SU(6) for vector couplings:

scalar couplings:

$$egin{aligned} g_{\omega N} &: g_{\omega \Lambda} : g_{\omega \Sigma} : g_{\omega \Xi} = 3:2:2:1 \ g_{
ho N} &: g_{
ho \Lambda} : g_{
ho \Sigma} : g_{
ho \Xi} = 1:0:2:1 \end{aligned}$$

$$x_{\sigma H} = \frac{x_{\omega H} n_0 C_{\omega}^2 / m_N^2 - U_H(n_0)}{m_N - m_N^*(n_0)} \qquad \qquad \begin{cases} U_{\Lambda}(n_0) = -28 \text{ MeV} \\ U_{\Sigma}(n_0) = +30 \text{ MeV} \\ U_{\Xi}(n_0) = -15 \text{ MeV} \end{cases}$$

extensions

phi meson: HH' repulsion

$$g_{\phi N}:g_{\phi \Lambda}:g_{\phi \Sigma}:g_{\phi \Xi}=0:2:2:1$$
 $g_{\phi \Lambda}=-rac{\sqrt{2}}{3}g_{\omega N}$

[J. Schaffner et al., PRC71 (1993), Ann.Phys. 235 (94), PRC53(1996)]

play with hyperon coupling constants

SU(3) coupling constants: extra parameters to tune. two effects: $|g_{\omega H}|$ increases; $g_{\phi N}$ non zero

[Weissenborn et al., PRC85 (2012);NPA881 (2012); NPA914(2013)]

<u>alternative</u>

mass of ϕ meson If we take into account a reduction of the ϕ mass in medium we can increase a HH repulsion

 $x_{mH} = rac{g_{mH}}{g_{mN}}$

EEK and D.Voskresensky NPA 759 (2005) 373

• in standard RMF model m_{σ} , m_{ω} , and m_{ρ} do not change

Can the in-medium modification (decrease) of meson masses be included in an RMF model??

• Song, Brown, Min, Rho (1997) $m_{\sigma}^*/m_{\sigma} \approx m_{\omega}^*/m_{\omega} \approx m_{\rho}^*/m_{\rho} = \Phi(n)$

Lattice QCD (SC-QCD): common drop of meson masses [Ohnishi Miura Kawamoto Mod.Phys.Lett A23, 2459]

- decreasing functions of σ : $m^*_{\omega}(\sigma)$, $m^*_{\rho}(\sigma) \leftarrow$ self-consistent σ field results in *increase* of ρ an ω masses
- $\bullet~\sigma$ field dependent masses and couplings constant

Generalized RMF Model

Nucleon and meson Lagrangian

$$\mathcal{L} = \mathcal{L}_{N} + \mathcal{L}_{M}$$

$$\mathcal{L}_{N} = a_{N} \bar{\Psi}_{N} (i \ D \cdot \gamma) \Psi_{N} - m_{N} \phi_{N} \bar{\Psi}_{N} \bar{\Psi}_{N}$$

$$D_{\mu} = \partial_{\mu} + i g_{\omega} \tilde{\chi}_{\omega} \omega_{\mu} + \frac{i}{2} g_{\rho} \tilde{\chi}_{\rho} \rho_{\mu} \tau$$

$$\mathcal{L}_{M} = a_{\sigma} \frac{\partial^{\mu} \sigma \partial_{\mu} \sigma}{2} - \phi_{\sigma}^{2} \frac{m_{\sigma}^{2} \sigma^{2}}{2} - \tilde{U}(\sigma)$$

$$- a_{\omega} \frac{\omega_{\mu\nu} \omega^{\mu\nu}}{4} + \phi_{\omega}^{2} \frac{m_{\omega}^{2} \omega_{\mu} \omega^{\mu}}{2} - a_{\rho} \frac{\rho_{\mu\nu} \rho^{\mu\nu}}{4} + \phi_{\rho}^{2} \frac{m_{\rho}^{2} \rho_{\mu} \rho^{\mu}}{2}$$

All scaling functions a_i , $\tilde{\chi}_i$, ϕ_i depend on $g_\sigma \tilde{\chi}_\sigma \sigma$

Field redefinition

$$\Psi_N \to \Psi_N / \sqrt{a_N} \ , \ \sigma \to \sigma / \sqrt{a_\sigma} \ , \ \omega_\mu \to \omega_\mu / \sqrt{a_\omega}, \rho_\mu \to \rho_\mu / \sqrt{a_
ho}$$

$$\mathcal{L}_{N} = \bar{\Psi}_{N} (i \ D \cdot \gamma) \Psi_{N} - m_{N} \Phi_{N} \bar{\Psi}_{N} \bar{\Psi}_{N},$$

$$D_{\mu} = \partial_{\mu} + ig_{\omega} \chi_{\omega} \omega_{\mu} + \frac{i}{2} g_{\rho} \chi_{\rho} \rho_{\mu} \tau$$

$$\mathcal{L}_{M} = \frac{\partial^{\mu} \sigma \partial_{\mu} \sigma}{2} - \Phi_{\sigma}^{2} \frac{m_{\sigma}^{2} \sigma^{2}}{2} - U(\sigma)$$

$$- \frac{\omega_{\mu\nu} \omega^{\mu\nu}}{4} + \Phi_{\omega}^{2} \frac{m_{\omega}^{2} \omega_{\mu} \omega^{\mu}}{2} - \frac{\rho_{\mu\nu} \rho^{\mu\nu}}{4} + \Phi_{\rho}^{2} \frac{m_{\rho}^{2} \rho_{\mu} \rho^{\mu}}{2}$$

 $m_i^*/m_i = \phi_i(\chi_\sigma\sigma)/\sqrt{a_i(\chi_\sigma\sigma)} = \Phi_i(\chi_\sigma\sigma)$ mass scaling function $\chi_i = \tilde{\chi}_i(\chi_\sigma\sigma)/\sqrt{a_i(\chi_\sigma\sigma)}$ coupling-constant scaling function

where

Energy-density functional for infinite matter

minimized with respect to ω and ρ fields

$$C_i = rac{g_{iN}m_N}{m_i}, \ i = \sigma, \omega,
ho$$

$$E_{N}[\rho_{n},\rho_{p};f] = \frac{m_{N}^{4}f^{2}}{2C_{\sigma}^{2}}\eta_{\sigma}(f) + U(f) + \frac{C_{\omega}^{2}(\rho_{n}+\rho_{p})^{2}}{2m_{N}^{2}\eta_{\omega}(f)} \\ + \frac{C_{\rho}^{2}(\rho_{n}-\rho_{p})^{2}}{8m_{N}^{2}\eta_{\rho}(f)} + \left(\int_{0}^{P_{F,n}} + \int_{0}^{P_{F,p}}\right)\frac{p^{2}dp}{\pi^{2}}\sqrt{m_{N}^{2}\Phi_{N}^{2}(f) + p^{2}}$$

scalar field: $f = g_{\sigma N} \chi_\sigma \sigma_0$ nuclear effective masses: $m_N^*/m_N = \Phi_N(f)$

scaling functions:
$$\eta_i(f) = rac{\Phi_i^2(f)}{\chi_i^2(f)}$$
 $i=\sigma,\omega,
ho$

 σ -field potential can be included in the scaling functions

$$\eta_{\sigma}(f) o \widetilde{\eta}_{\sigma}(f) = \eta_{\sigma}(f) - rac{2 C_{\sigma}^2}{m_N^4 f^2} U(f)$$

Equivalence of RMF models



control of EoS stiffness in ISM and BEM

Choice of scaling functions:

- •monotonous increase of the scalar field as a function of density f(n)
- absence of several solutions for f(n) and jumps among them

KVOR model [EEK, Voskresensky NPA759, 373 (2005)]

$$\eta_{\sigma}^{\text{KVOR}} = 1 + 2\frac{C_{\sigma}^2}{f^2} \left(\frac{b}{3}f^3 + \frac{c}{4}f^4\right) \qquad \eta_{\omega}^{\text{KVOR}} = \left[\frac{1 + zf_0}{1 + zf}\right]^{\alpha} \qquad \bar{f}_0 = f(n_0)$$
$$\eta_{\rho}^{\text{KVOR}} = \left[1 + 4\frac{C_{\omega}^2}{C_{\rho}^2} \left(1 - [\eta_{\omega}^{\text{KVOR}}(f)]^{-1}\right)\right]^{-1} \qquad \alpha = 1 \quad z = 0.65$$



Comparison by Th. Klahn et al., PRC74, 035802 (2006)



Extended to finite temperature:

Khvorostukhin, Toneev, Voskresensky, NPA791, 180 (2007); NPA813, 313 (2008)

Aim: Construct a better parameterization which satisfies new constraints on the nuclear EoS Inclusion of hyperons. "Hyperon puzzle".

Increase of hyperon-hyperon repulsion due to phi-meson exchange (phi-mass reduction)

Apply cut-scheme to η_{ω} function

$$\eta_{\omega}^{\text{KVOR}}(f) \to \eta_{\omega}^{\text{KVOR}}(f) + \frac{a_{\omega}}{2} \left[1 + \tanh(b_{\omega}(f - f_{\text{cut},\omega})) \right]$$



D C	\mathcal{E}_0	n_0	K	$m_N^*(n_0)$	\widetilde{J}_0	L	K'	$K_{\rm sym}$
EoS	[MeV]	$[fm^{-3}]$	[MeV]	$[m_N]$	[MeV]	[MeV]	[MeV]	[MeV]
MKVOR	-16	0.16	240	0.73	30	41	557	-159

scaling functions for coupling constants vs scalar field:

saturate f growth





Neutron matter EoS

empirical constraints on symmetry energy

-- (AIS) analog isobar states [Danielewicz, Lee NPA 922 (2014) 1] -- α_D electric dipole polarizability ²⁰⁸Pb [Zhang, Chen 1504.01077]

microscopic calculations

Akmal, Pandharipande, Ravenhall -- (AFDMC) Gandolfi et al.MNRAS 404 (2010) L35 Hebeler, Schwenk EPJA 50 (2014) 11



Scalar and vector potentials in KVOR and MKVOR models vs. DBHF calculations



BM: Brockmann – Machleidt PRC42 (1990)

KS: Katayama-Saito PRC88 (2013)

Scaling functions for coupling constants





Compare with scaling frunctions from DD-F,DD models [Typel,PRC71,064301(2005)]

Nuclear optical potential

$$U_{\rm opt}^{(b)}(\varepsilon) = \varepsilon - \sqrt{(\varepsilon - V_b)^2 - S_b (2 m_b + S_b)}$$

[Feldmeier, Lindner ZPA341 (1991) 83]

Data: Hama, Clark et al., Phys. Rev. C 41 (1990) 2737



$$S_{b} = m_{b} \Phi_{b} (x_{\sigma b} \frac{m_{N}}{m_{b}} f) - m_{b}$$
$$V_{b} = x_{\omega b} \frac{C_{\omega}^{2} n}{m_{N}^{2} \eta_{\omega}(f)}$$

m

Constraints on EoS from HICs

Particle flow: Danielewicz, Lacey and Lynch, Science 298 (2002) 1592

Kaon production: Fuchs, Prog. Part. Nucl. Phys. 56 (2006) 1



Scalar field in dense matter



Gravitational vs baryon mass of PSR J0737-3039(B)

PSR J0737-3039(B): double pulsar system

- 1. Podsiadlowski et al., MNRAS 361 (2005) 1243
- 2. Kitaura et al., A&A 450 (2006) 345





Inclusion of hyperons: energy-density functional

 $B \in SU(3)$ ground state multiplet scalar field $f = g_{\sigma} \chi_{\sigma} \sigma / m_N$ $E[f, \{n_{\rm B}\}] = \sum E_{\rm kin}(p_{{\rm F},B}, m_B \Phi_B(f)) + \sum E_{\rm kin}(p_{{\rm F},l}, m_l)$ $+\frac{m_N^4 f^2}{2C_-^2}\eta_{\sigma}(f)+\frac{1}{2m_{\omega}^2}\left[\frac{C_{\omega}^2 \widetilde{n}_B^2}{n_{\omega}(f)}+\frac{C_{\rho}^2 \widetilde{n}_I^2}{n_{\omega}(f)}+\frac{C_{\phi}^2 \widetilde{n}_S^2}{n_{\omega}(f)}\right],$ $C_i = \frac{g_{iN}m_N}{m_i}, i = \sigma, \omega, \rho$ $C_\phi = m_\omega C_\omega/m_\phi$ effective densities: $\widetilde{n}_B = \sum_{B} x_{\omega B} n_B$ $\widetilde{n}_I = \sum_{B} x_{\rho B} t_{3B} n_B$ $\widetilde{n}_S = \sum_{H} x_{\phi H} n_H$ with coupling constant ratios $x_{\omega(\rho)B} = \frac{g_{\omega(\rho)B}}{g_{\omega(\rho)N}} \quad x_{\phi H} = \frac{g_{\phi H}}{g_{\omega N}}$ scaling functions mass scaling: $\eta_i(f) = rac{\Phi_i^2(f)}{\sqrt{2}(f)}, \quad i = \sigma, \, \omega, \,
ho$ $\Phi_m(f) \approx \Phi_N(f) = 1 - f$ $\Phi_H(f) = 1 - x_{\sigma H} \frac{m_N}{m_H} \xi_{\sigma H} f$

The standard sigma potential can be introduced as $\eta_{\sigma}(f) = 1 + rac{2 C_{\sigma}^2}{m^4 - f^2} U(f)$

Inclusion of hyperons: coupling constants

1) standard. extension: H

Vector coupling constants from SU(6) symmetry:

data on hypernuclei

Scalar coupling constants from hyperon binding energies

$$U_H(n_0) = C_{\omega}^2 m_N^{-2} x_{\omega H} n_0 - (m_N - m_N^*(n_0)) x_{\sigma H}$$
$$x_{\omega(\rho)B} = g_{\omega(\rho)B} / g_{\omega(\rho)N}$$

$$U_{\Lambda}(n_0) = -28 \,\mathrm{MeV}$$

 $U_{\Sigma}(n_0) = +30 \,\mathrm{MeV}$
 $U_{\Xi}(n_0) = -15 \,\mathrm{MeV}$

2) +phi mesons. extension: Ho

$$\Phi_{\phi} = 1 - f, \quad \chi_{\phi H} = 1 \qquad \eta_{\phi} = \frac{\Phi_{\phi}^2}{\chi_{\phi}^2} = (1 - f)^2$$

Phi meson mediated repulsion among hyperons is enhanced

<u>3) + hyperon-sigma couplings reduced. extension</u>: $H\phi\sigma$

 $\Phi_H(f) = 1 - x_{\sigma H} \frac{m_N}{m_H} \xi_{\sigma H} f$

 $\xi_{\sigma H}(n \le n_0) = 1$ but $\xi_{\sigma H}(n \gtrsim n_\Lambda) \to 0$ hyperon-nucleon mass gap grows with density

QMC model: Guichon, Thomas

Strangeness concentration



Maximum NS mass and the strangeness concentration



Weissenborn, Chatterjee Schafner-Bielich

Mass-radius constraints



BPA: Bayesian probability analysis [Lattimer, Steiner ...]

msp PSRJ0437-4715: 3σ confidence Bogdanov ApJ 762, 96 (2013)

Inclusion of Δ (1232) baryons

vector meson couplings
quark counting SU(6) $g_{\omega\Delta} = g_{\omega N}, \quad g_{\rho\Delta} = g_{\rho N}, \quad g_{\phi\Delta} = 0$ scalar couplings: $x_{\sigma\Delta} = \frac{x_{\omega\Delta}C_{\omega}^2 n_0/m_N^2 - U_{\Delta}(n_0)}{m_N - m_N^*(n_0)}$ $x_{m\Delta} = \frac{g_{m\Delta}}{g_{mN}}$

Photoabsorption off nuclei with self-consistent vertex corrections: $U_{\Delta}(n_0) \simeq -50 \,\mathrm{MeV}$



We allow for a variation of parameters $-100 \text{ MeV} \le U_{\Delta} \le -50 \text{ MeV}$

critical densities for Δ appearance

beta-equilibrium matter





MKVOR* model

isospin symmetric matter



RMF model with scaled meson masses and coupling constants

✓ Universal scaling of hadron masses. Not universal scaling of coupling constants

✓ The model is flexible enough to satisfy many astrophysical constraints, constraints from HIC and microscopic calculations.

✓ Hyperon puzzle can be partially resolved if the reduction of phi meson mass is taken into account

 \checkmark Models are safe against the inclusion of \triangle baryons