

# Dynamical mass ejection from black hole-neutron star binaries

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KK, K. Ioka, M. Shibata, PRD 88 (2013) 041502(R)

K. Kawaguchi, KK, et al., PRD 92 (2015) 024014

KK, K. Ioka, H. Okawa, M. Shibata, K. Taniguchi, PRD 92 (2015) 044028

K. Kawaguchi, KK, M. Shibata, M. Tanaka, ApJ 825 (2016) 52

KK, K. Kiuchi, Y. Sekiguchi, M. Shibata, K. Taniguchi, in preparation

# Plan of the talk

1. Introduction
2. Study in hydrodynamics
3. Study in neutrino-radiation hydrodynamics
4. Future direction and summary

# Prefetch: Summary

- Black hole-neutron star binary mergers can eject  $\sim 0.01 - 0.1 M_{\odot}$  with  $\sim 0.2 - 0.3c$  dynamically in a highly anisotropic manner for various cases.
- The electron fraction of dynamical ejecta is low because they do not experience shock heating.
- Neutrinos are not important for dynamical mass ejection and do not drive a strong disk wind.
- Other disk winds could dominate mass ejection and require more investigation.

# 1. Introduction

# Why do we investigate BH-NS?

- Gravitational-wave astronomy  
accessible to a larger distance than with NS-NS
- Short-hard gamma-ray burst  
many possibilities from the BH mass/spin diversity?
- Mass ejection and electromagnetic counterpart  
r-process nucleosynthesis  
macronova/kilonova, synchrotron radio flare, ...

# Gravitational-wave detector

[http://gwcenter.icrr.u-tokyo.ac.jp/wp-content/themes/lcgt/images/img\\_abt\\_lcgt.jpg](http://gwcenter.icrr.u-tokyo.ac.jp/wp-content/themes/lcgt/images/img_abt_lcgt.jpg)

## KAGRA (Kamioka)



## Advanced LIGO (Hanford)

<https://www.advancedligo.mit.edu/graphics/summary01.jpg>

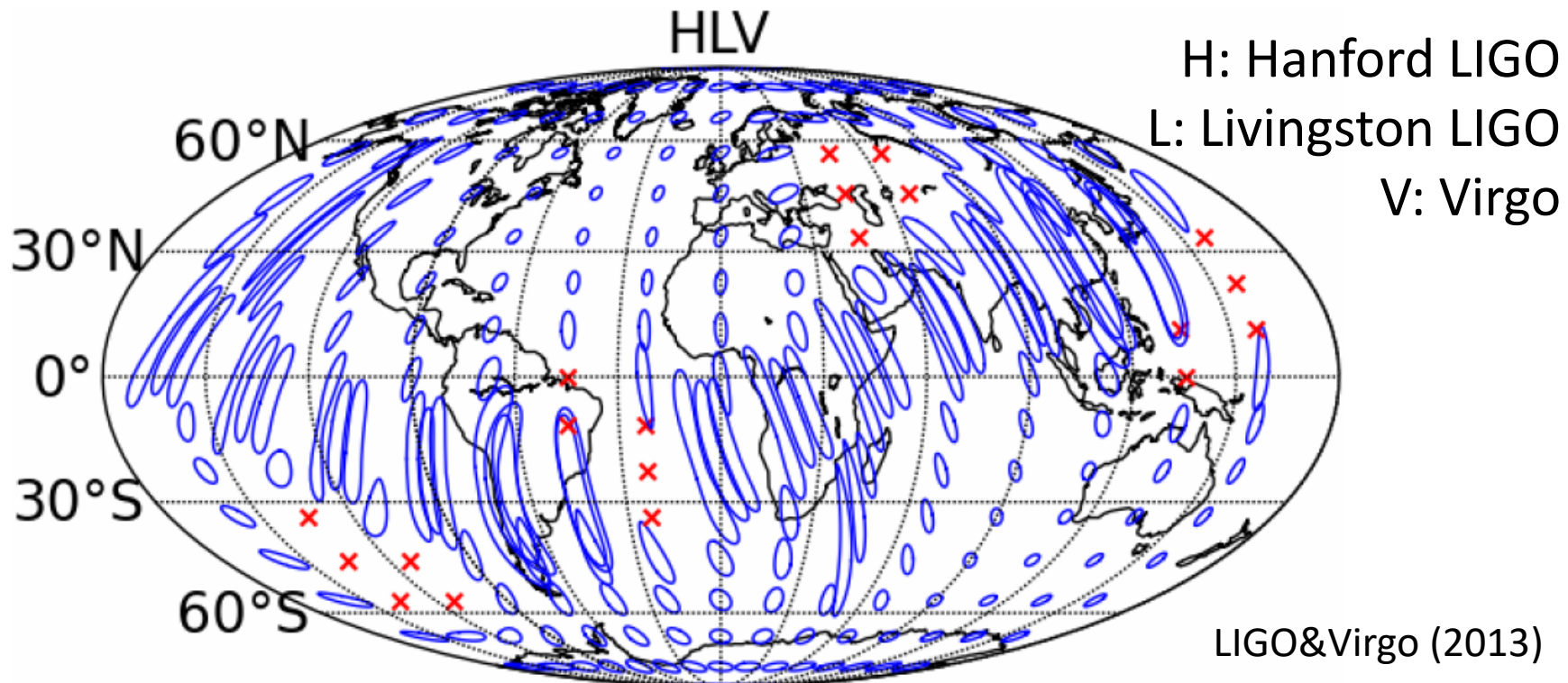
## Advanced Virgo (Pisa)

<http://virgopisa.df.unipi.it/sites/virgopisa.df.unipi.it.virgopisa/files/banner/virgo.jpg>

# Poor gravitational-wave localization

Typically  $\sim 20\text{-}30 \text{ deg}^2$  by multiple GW detectors

-> need EM counterparts for accurate localization



# Are BH-NS promising targets?

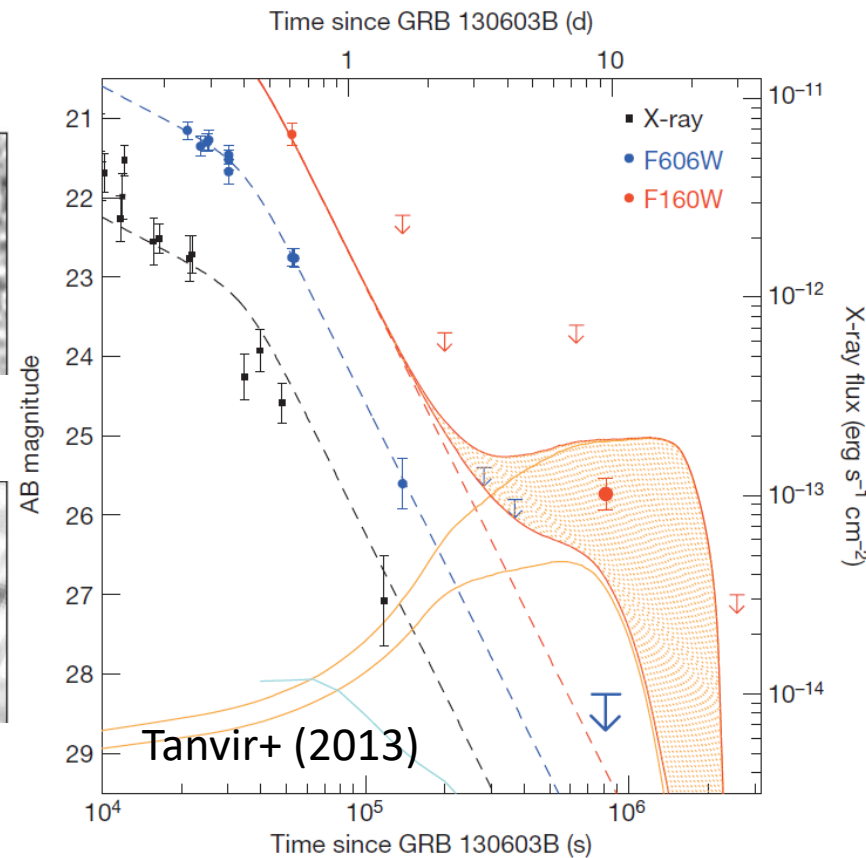
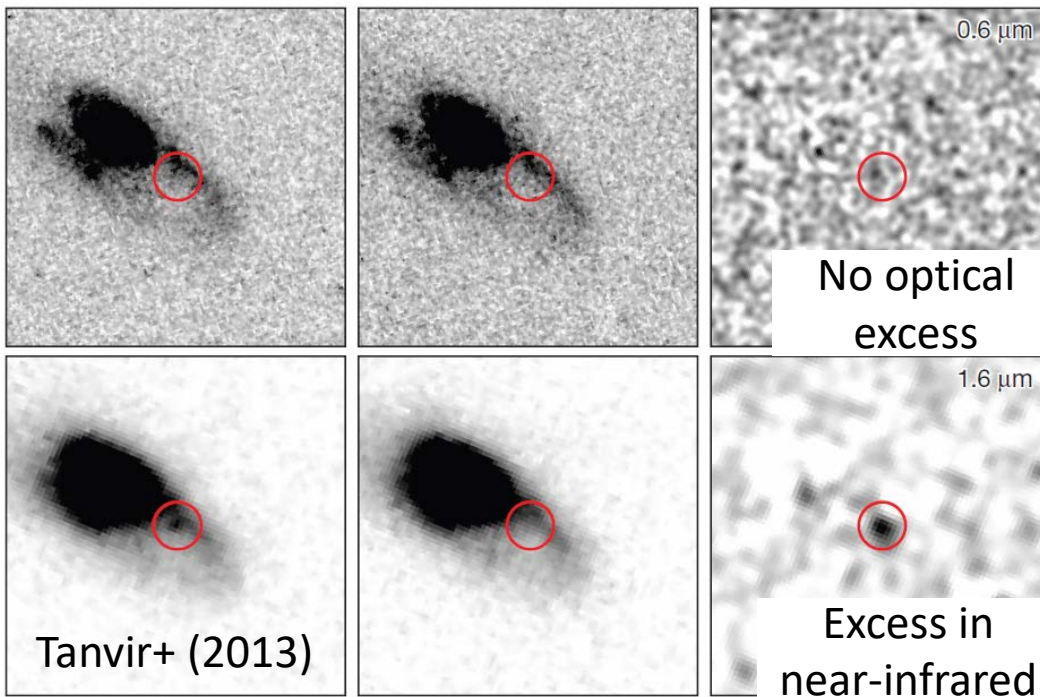
- No observed black hole-neutron star binaries
  - a Be/X-ray binary MWC 656 may be a progenitor
- If many massive black holes exist, gravitational waves are more frequent for BH-NS than NS-NS
  - LIGO O2 will tell us the answer
  - but if the black hole is massive, the neutron star is not likely to be disrupted for most parameters, and such binaries may not be interesting as a target of electromagnetic counterpart searches



# Near-infrared excess of GRB 130603B

$M_{ej} = 0.02 \sim 0.1 M_{\odot}$  may be required ... BH-NS?

9day (event?) - 30day (background) = Excess brightening



# Channel of mass ejection

## Dynamical mass ejection

gravity+pure hydrodynamics may be sufficient  
(we explicitly confirm this expectation later)  
sometimes obviously dominates disk activity

Disk activity = disk wind

- nuclear heating, viscous heating
- magnetically driven wind (cf Kiuchi+KK+ 2015)
- **neutrino driven wind (Kyutoku+ in prep.)**

# Problem to be answered

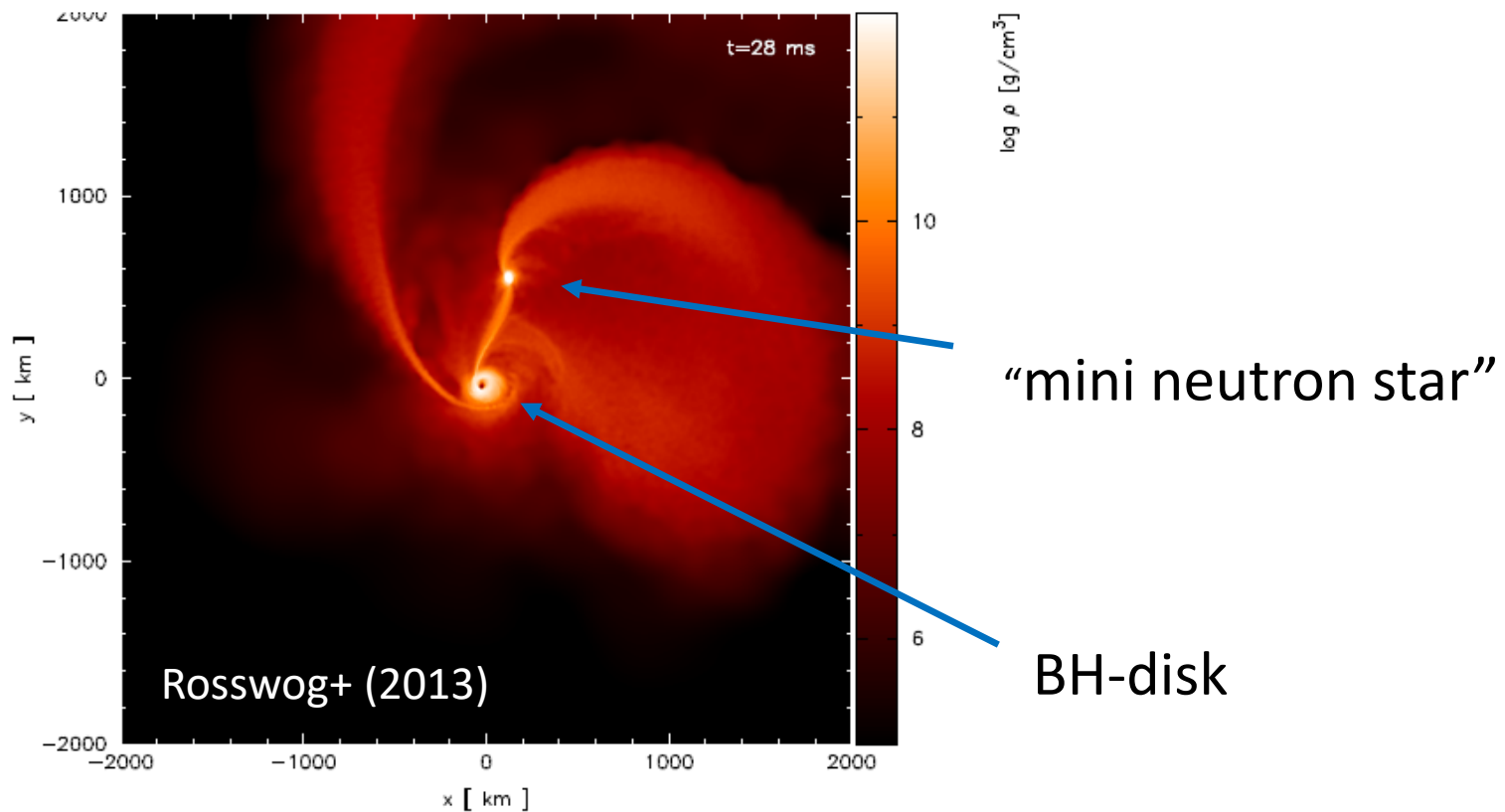
- How the mass is ejected in the merger process of black hole-neutron star binaries?
- What are characteristic quantities of ejecta? mass, velocity, morphology, electron fraction...
- How do they depend on binary parameters?
- What are features of associated electromagnetic counterparts? (not to discuss in detail today)

**Numerical-relativity simulations will give answers**

# Newtonian BH-NS simulation

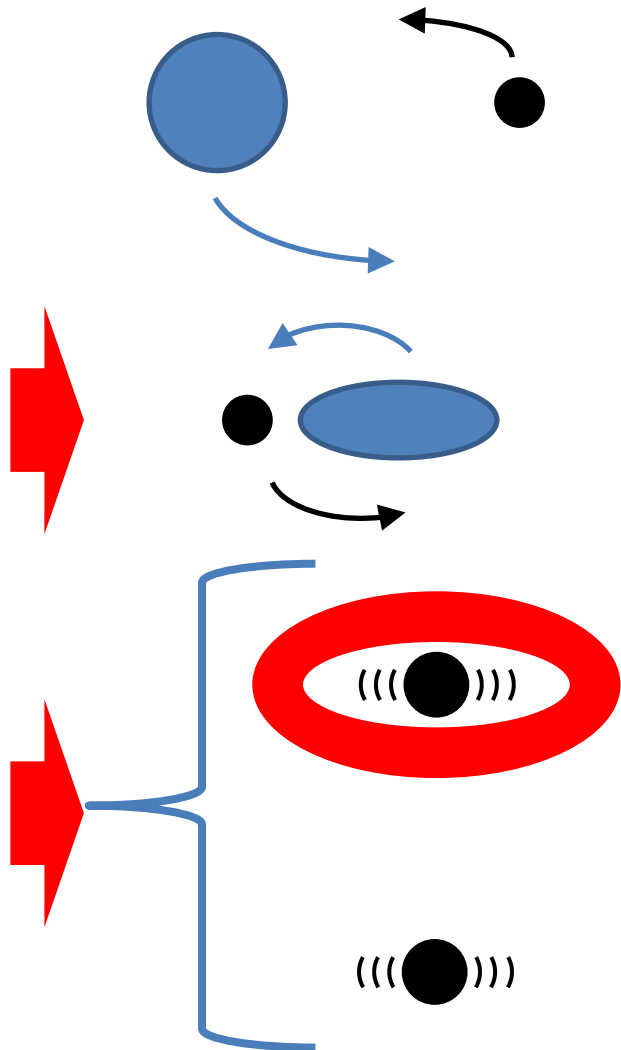
Episodic (repeated stable) mass transfer

qualitatively different from full GR results



# 2. Study in hydrodynamics

# Merger dynamics



inspiral due to GW backreaction

NS deformation due to tidal force  
further drive the inspiral motion

$r_{\text{tidal}} > r_{\text{ISCO}}$ : tidal disruption  
mass ejection, disk formation...

$r_{\text{tidal}} < r_{\text{ISCO}}$ : like BH-BH

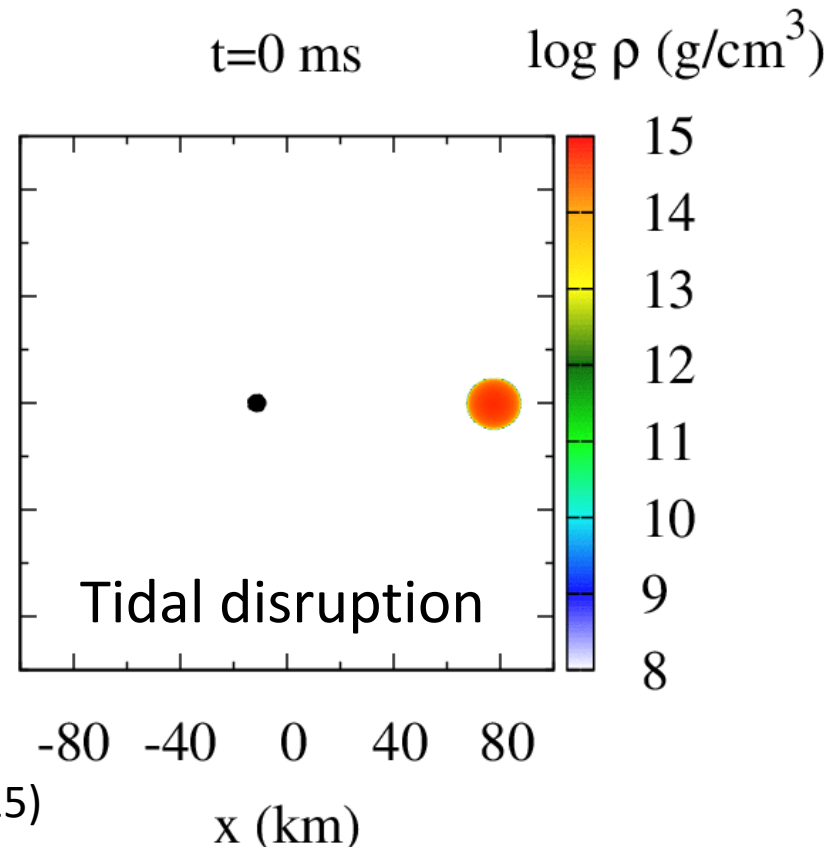
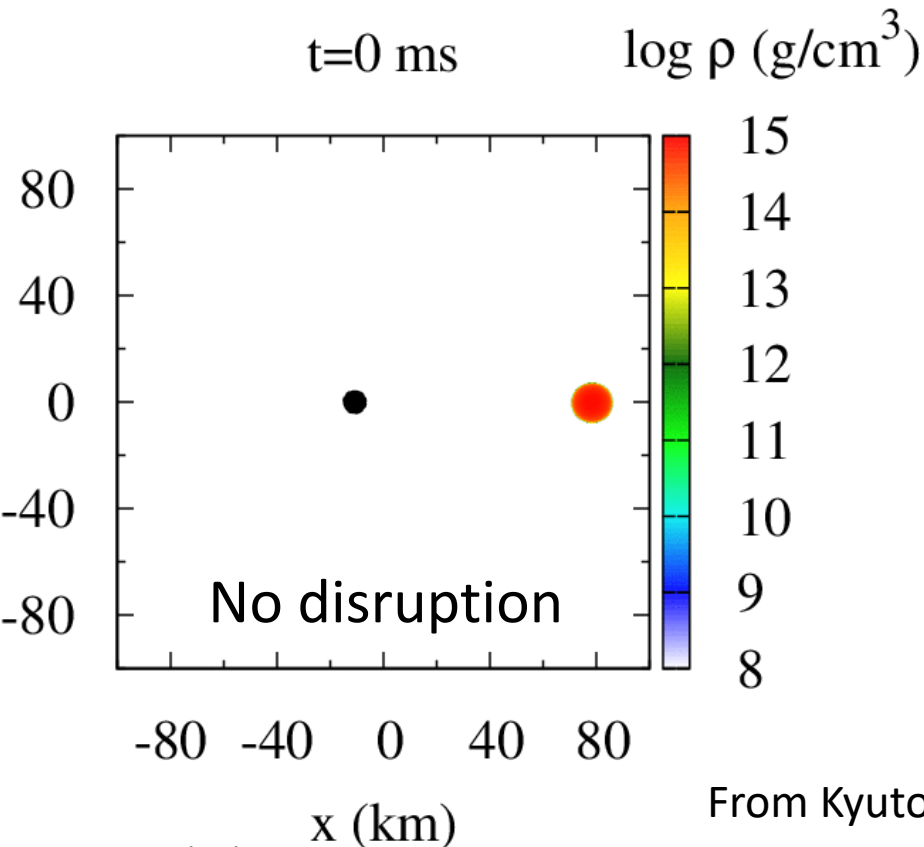
# Movies for two cases (6.75Mo BH)

NS radius 11.1km

BH spin 0.5

NS radius 13.6km

BH spin 0.75



From Kyutoku+ (2015)

# Mass shedding condition

1. BH tidal force=NS self gravity at the NS surface

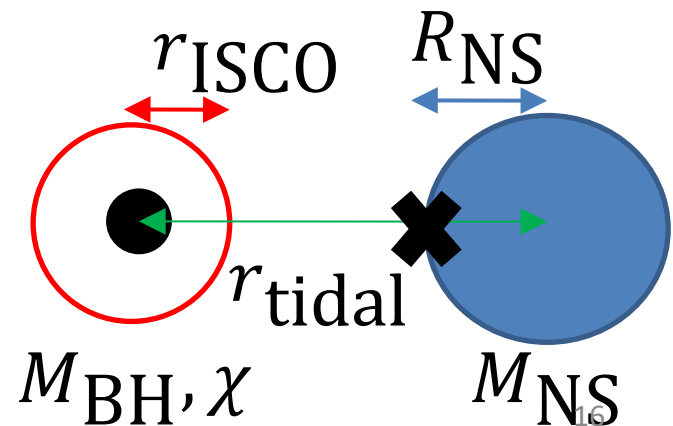
$$\frac{M_{\text{BH}} R_{\text{NS}}}{r_{\text{tidal}}^3} \sim \frac{M_{\text{NS}}}{R_{\text{NS}}^2} \Rightarrow r_{\text{tidal}} \sim M_{\text{BH}} \left( \frac{M_{\text{NS}}}{M_{\text{BH}}} \right)^{2/3} \left( \frac{R_{\text{NS}}}{M_{\text{NS}}} \right)$$

2. BH innermost stable circular orbit w/ spin  $\chi$

$$r_{\text{ISCO}} = \hat{r}(\chi) M_{\text{BH}} \quad (\hat{r} \text{ is a decreasing function of } \chi)$$

3. Disruption if this value is large

$$\frac{r_{\text{tidal}}}{r_{\text{ISCO}}} \sim \frac{1}{\hat{r}(\chi)} \left( \frac{M_{\text{NS}}}{M_{\text{BH}}} \right)^{2/3} \left( \frac{R_{\text{NS}}}{M_{\text{NS}}} \right)$$





# Important parameters

Three dimensionless parameters

1. NS compactness:  $C \equiv M_{\text{NS}}/R_{\text{NS}}$
2. Mass ratio of the BH to NS:  $Q \equiv M_{\text{BH}}/M_{\text{NS}}$
3. Dimensionless BH spin:  $\chi \equiv a_{\text{BH}}/M_{\text{BH}}$

For a fixed value of the NS mass, tidal disruption if

1. The NS radius is large, i.e.,  $C$  is small
2. The BH mass is small, i.e.,  $Q$  is small
3. The BH spin is large, i.e.,  $\chi$  is large

# Model parameters

NS mass fixed to be  $M_{\text{NS}} = 1.35M_{\odot}$

NS radius  $R_{\text{NS}} = 11.1, 12.4, 13.6, 14.4\text{km}$

piecewise polytrope (+ ideal-gas-like thermal part)

Mass ratio  $Q = 3, 5, 7$  ( $M_{\text{BH}} = 4.05, 6.75, 9.45M_{\odot}$ )

BH spin parameter  $\chi = 0, 0.5, 0.75$  (prograde)

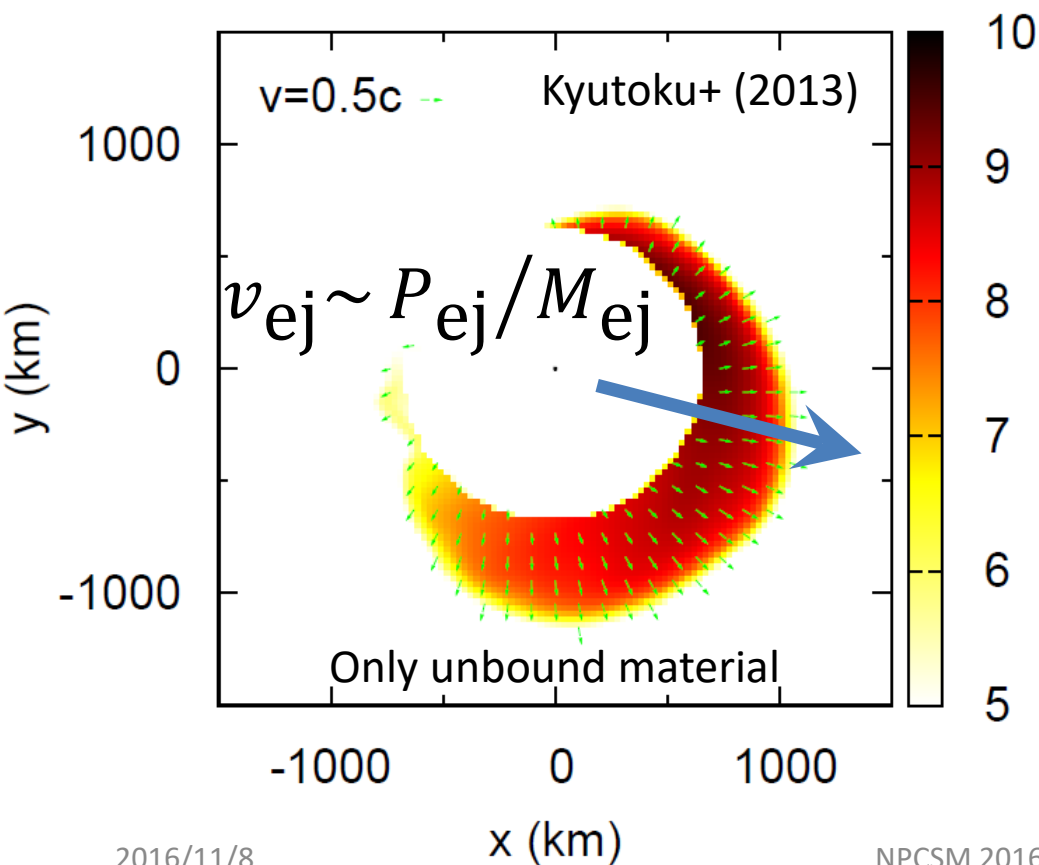
+ spin inclination  $i = 30^{\circ}, 60^{\circ}, 90^{\circ}$  available for  
 $Q = 5, \chi = 0.75$  (Kawaguchi, KK+ 2015)

# Movie

# Characteristic quantities

Ejection is efficient when the NS radius is large

opposite to NS-NS mass ejection (Hotokezaka+KK+ 2013)



ejecta mass

$$(0 \sim) 0.08 M_{\odot}$$

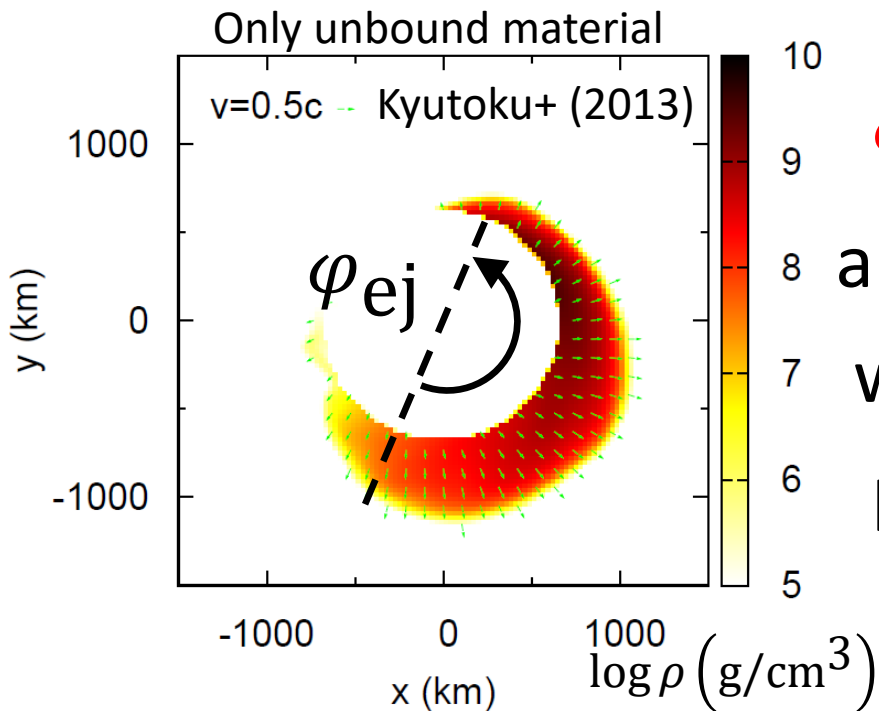
kinetic energy

$$(0 \sim) 5 \times 10^{51} \text{ erg}$$

“bulk” velocity

$$v_{ej} \sim 0.1 - 0.2c$$

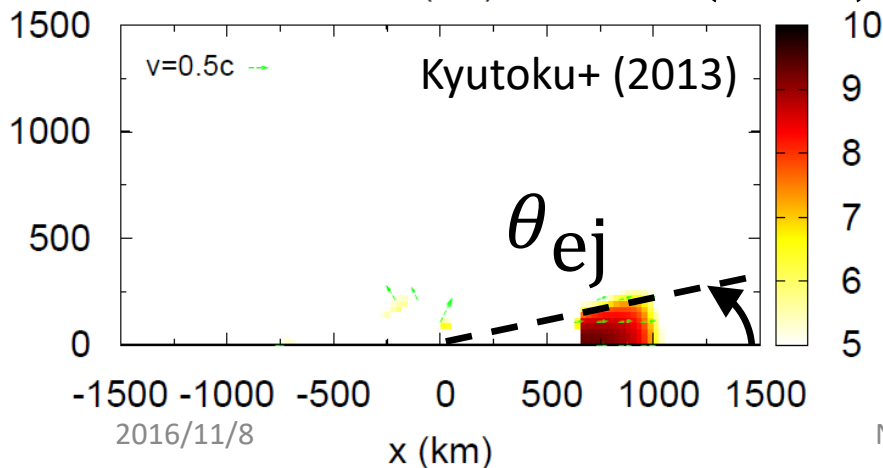
# Crescent-like ejecta anisotropy



$$\varphi_{ej} \approx 180^\circ$$

also can become  $\sim 360^\circ$

when tidal disruption is weak  
probably periastron advance

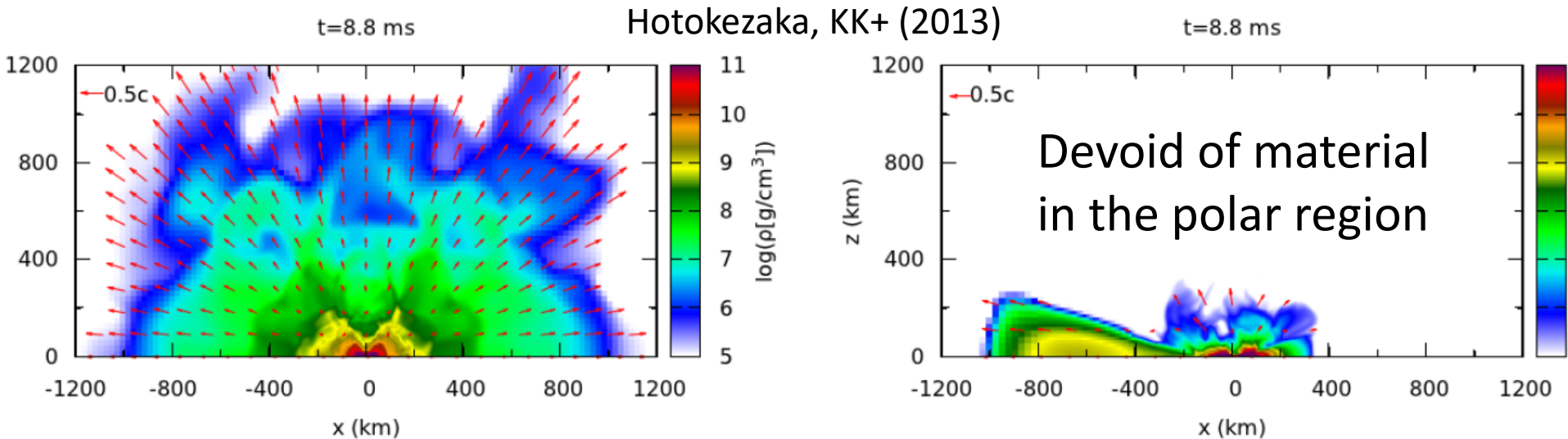


$$\theta_{ej} \approx 10^\circ - 20^\circ$$

relatively universal

# Comparison with NS-NS

## Density profile in the meridional plane



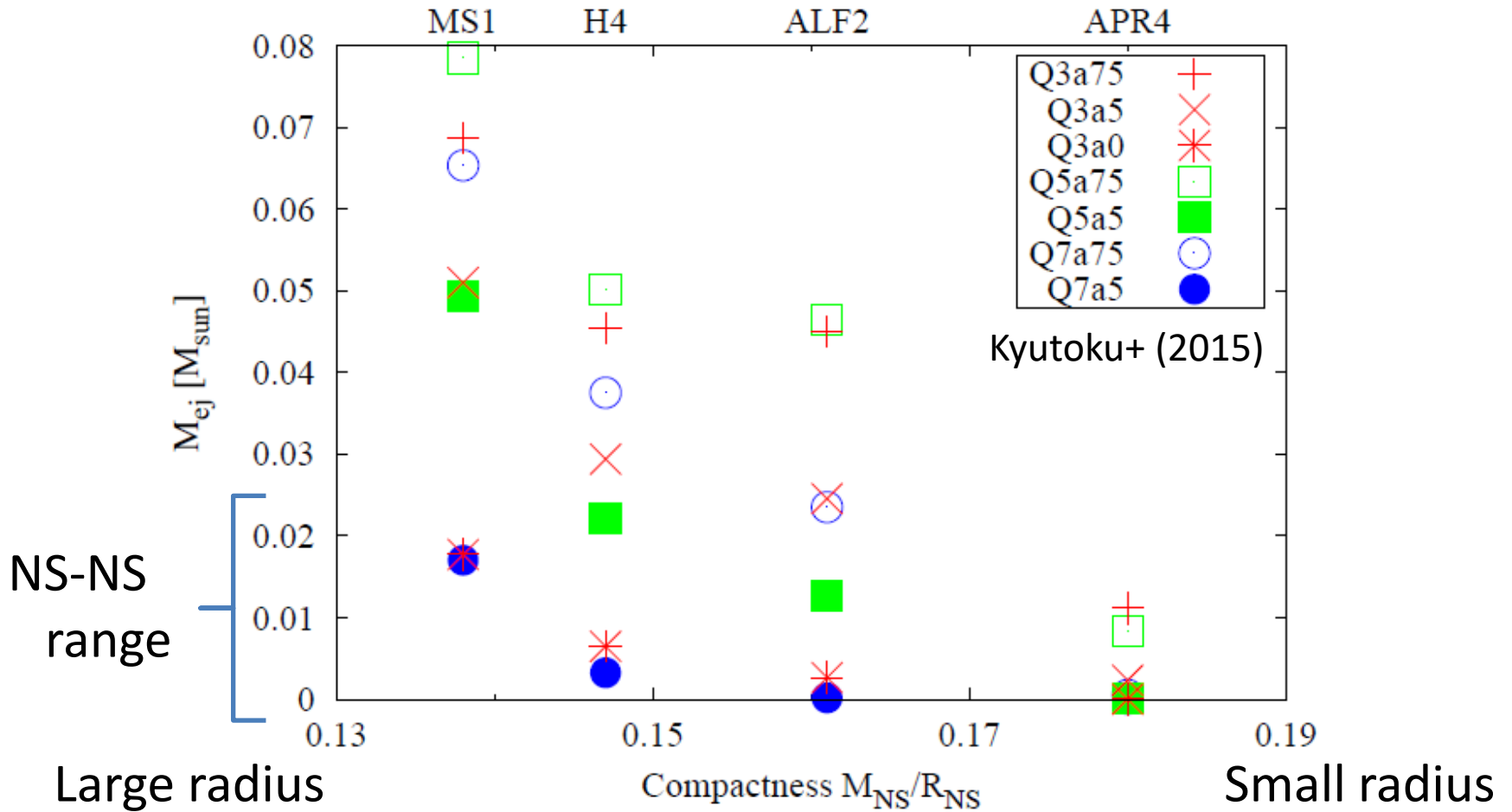
NS-NS: hypermassive NS

BH-NS: BH-disk

(but the reality depends on the disk wind)

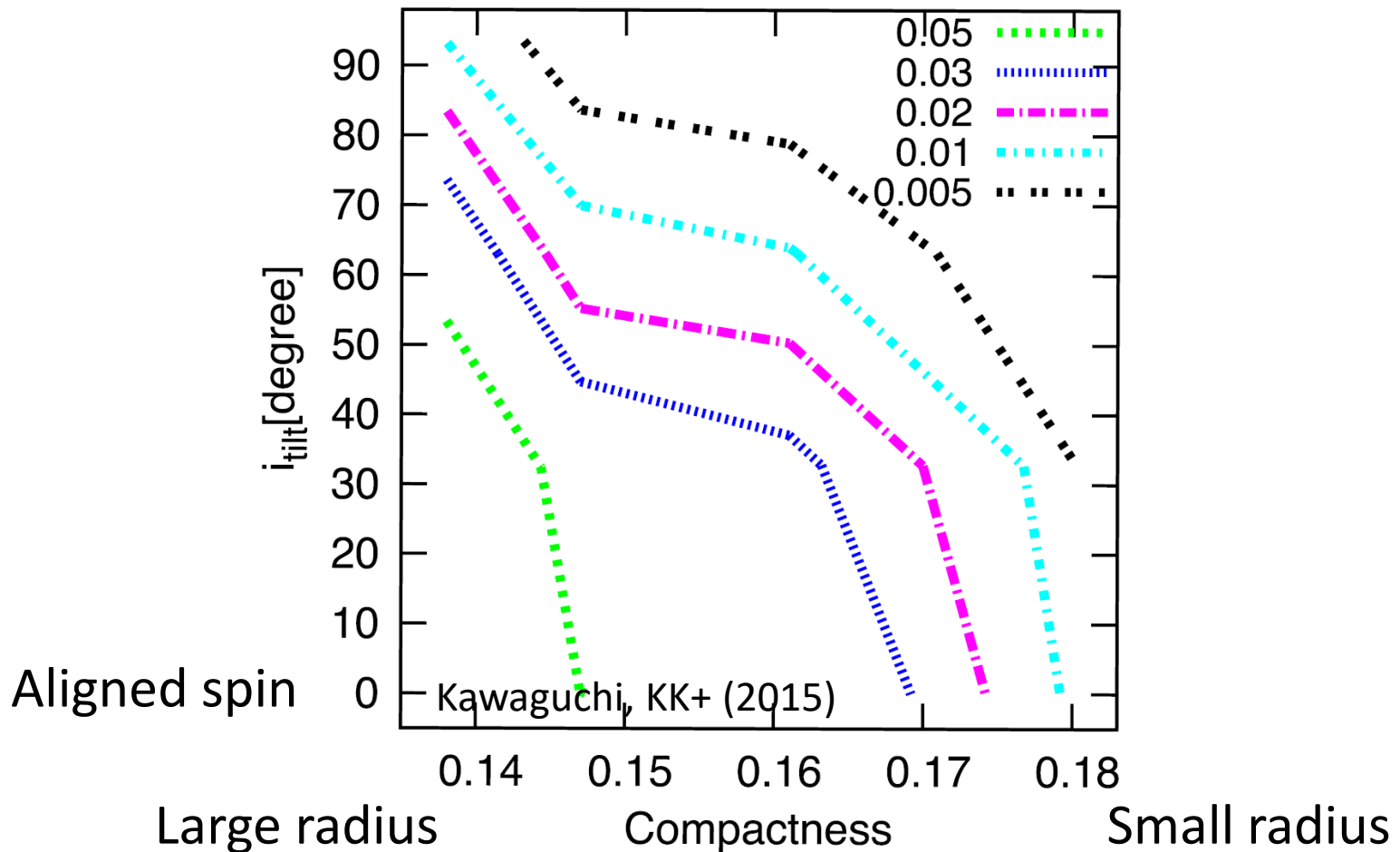
# Ejecta mass

The ejecta mass is large when the NS radius is large



# Misaligned BH spin

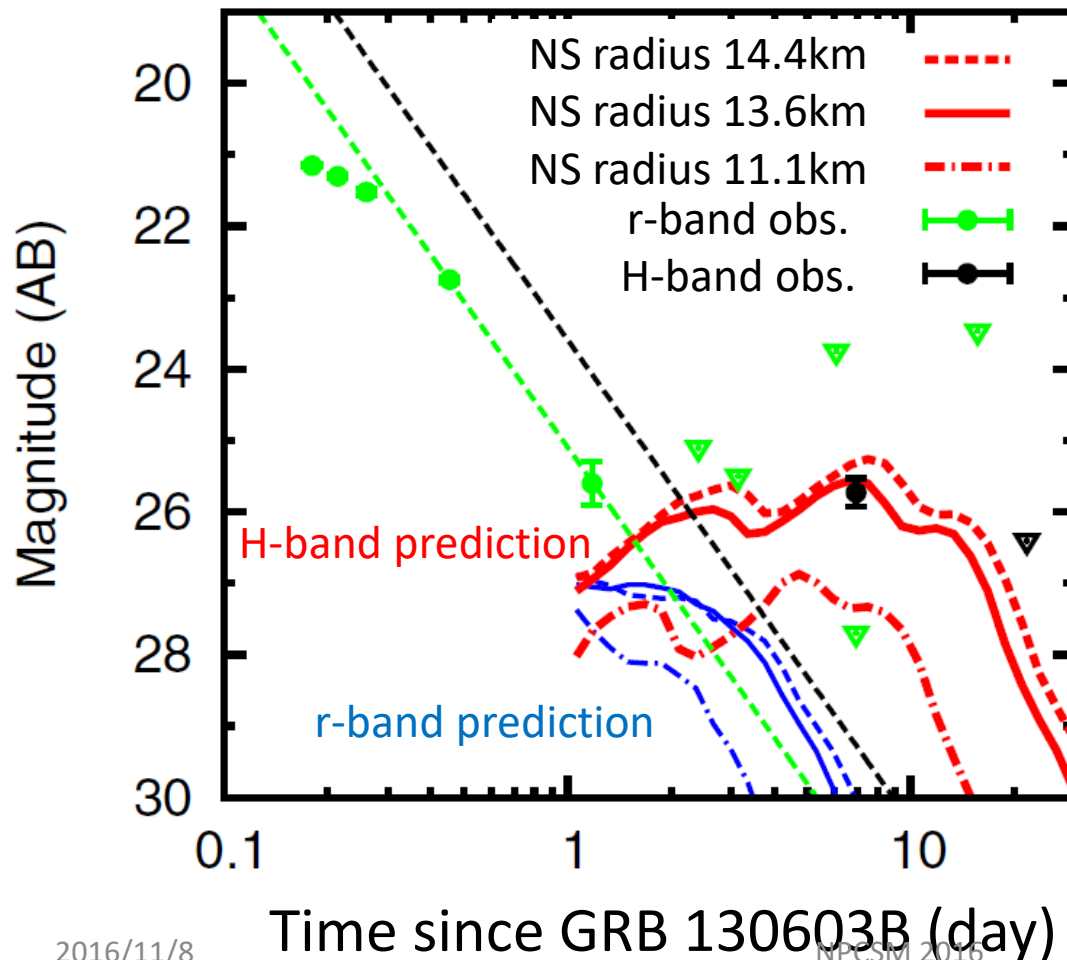
Spin inclination decreases the ejecta mass





# Radiation transfer simulation

IR excess of GRB 130603B can be explained

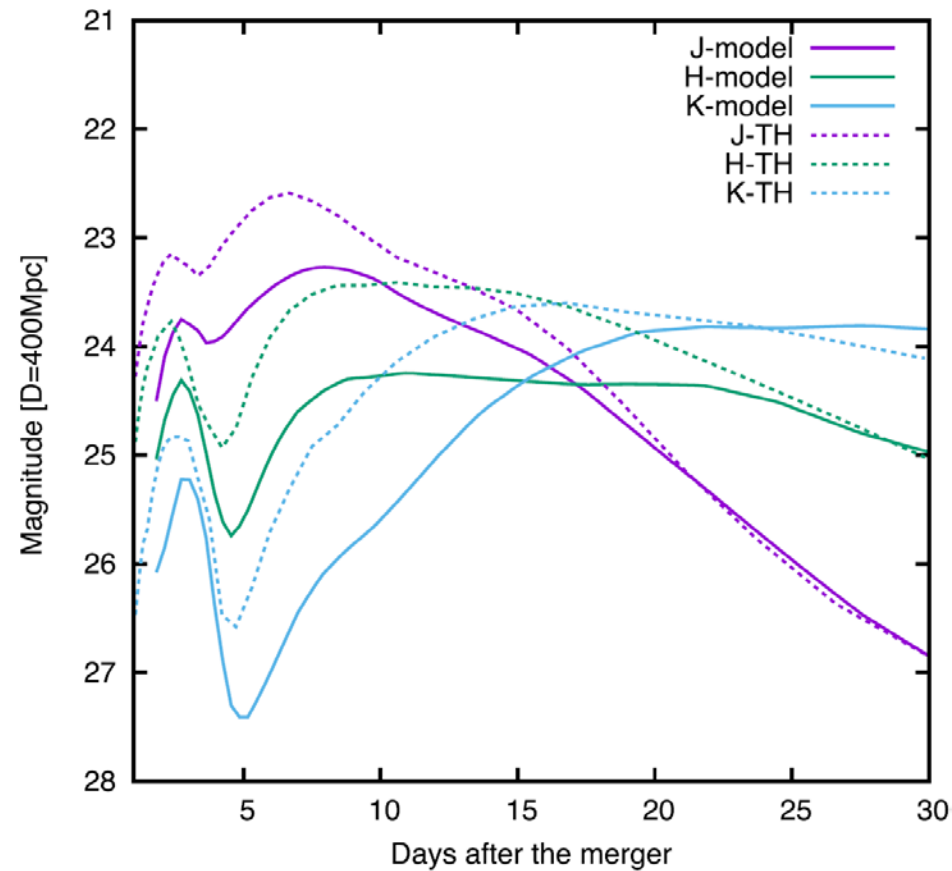
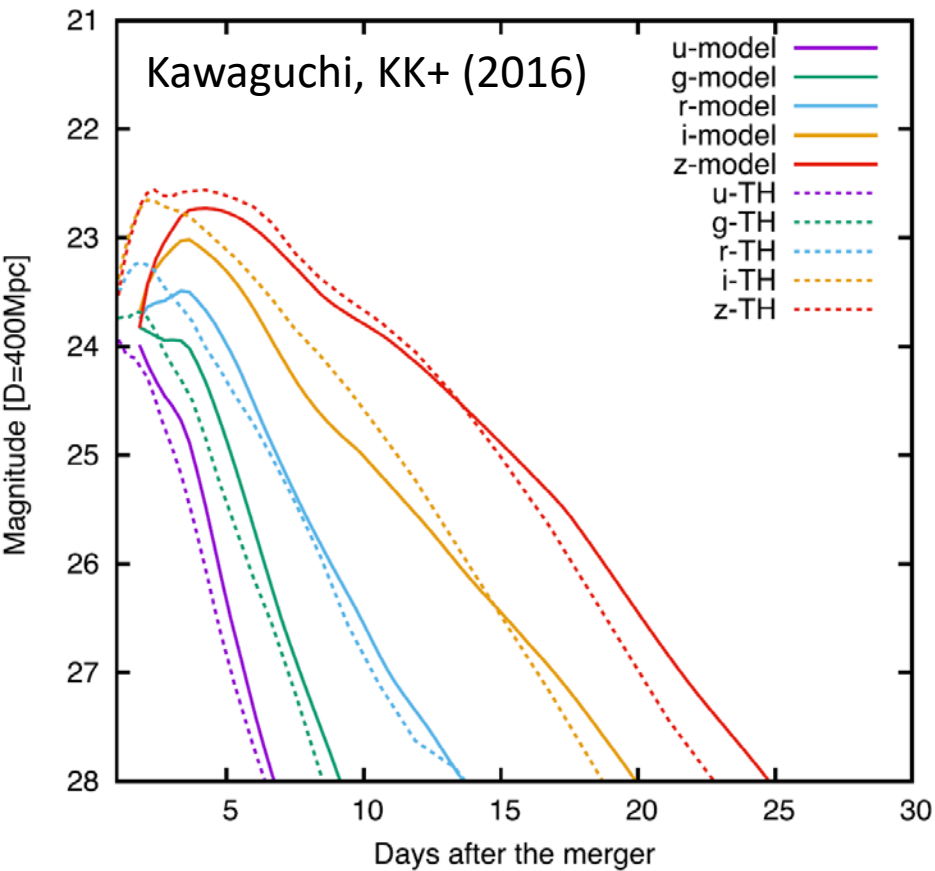


promising as  
EM counterparts  
to observed GWs  
  
could indicate  
r-process events?

# Phenomenological model

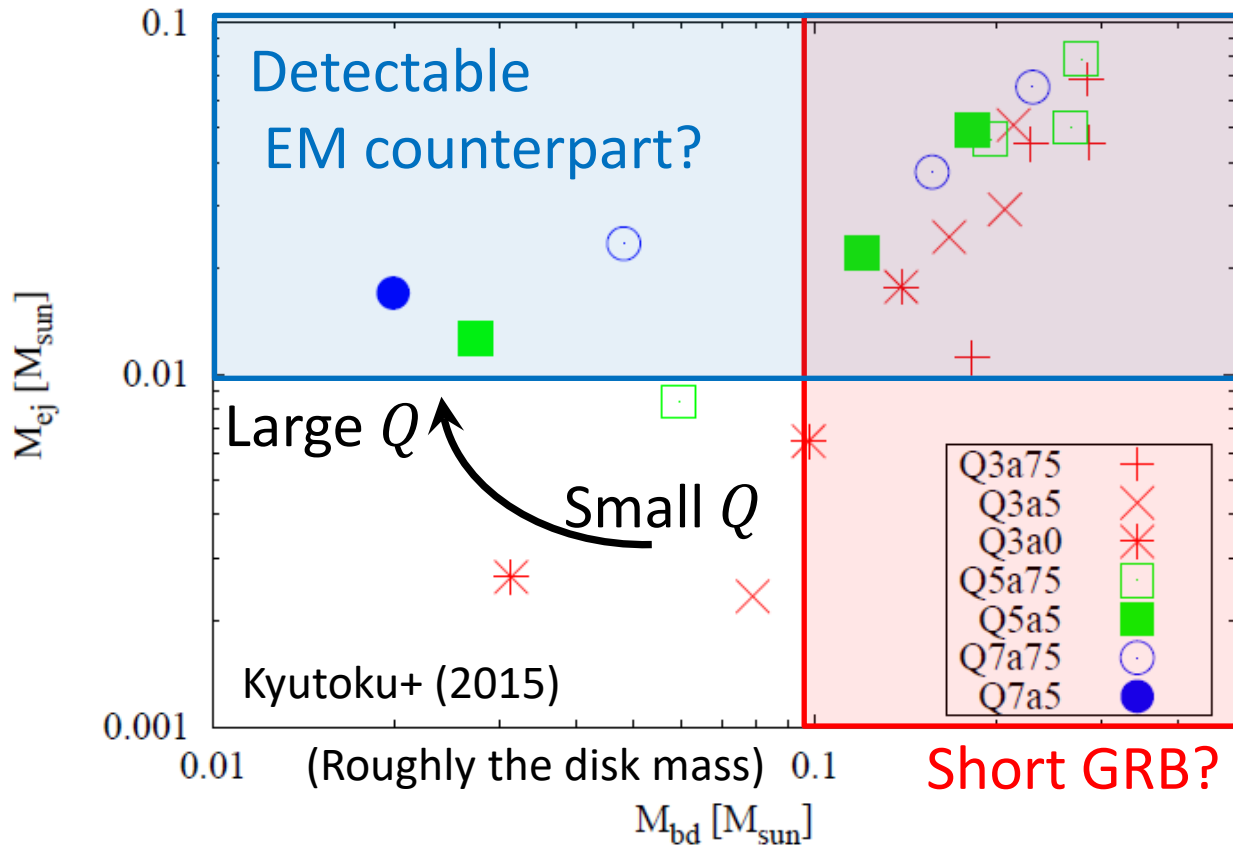
## Ejecta mass/velocity, multiband light curve

[http://www2.yukawa.kyoto-u.ac.jp/~kyohei.kawaguchi/kn\\_calc/main.html](http://www2.yukawa.kyoto-u.ac.jp/~kyohei.kawaguchi/kn_calc/main.html)



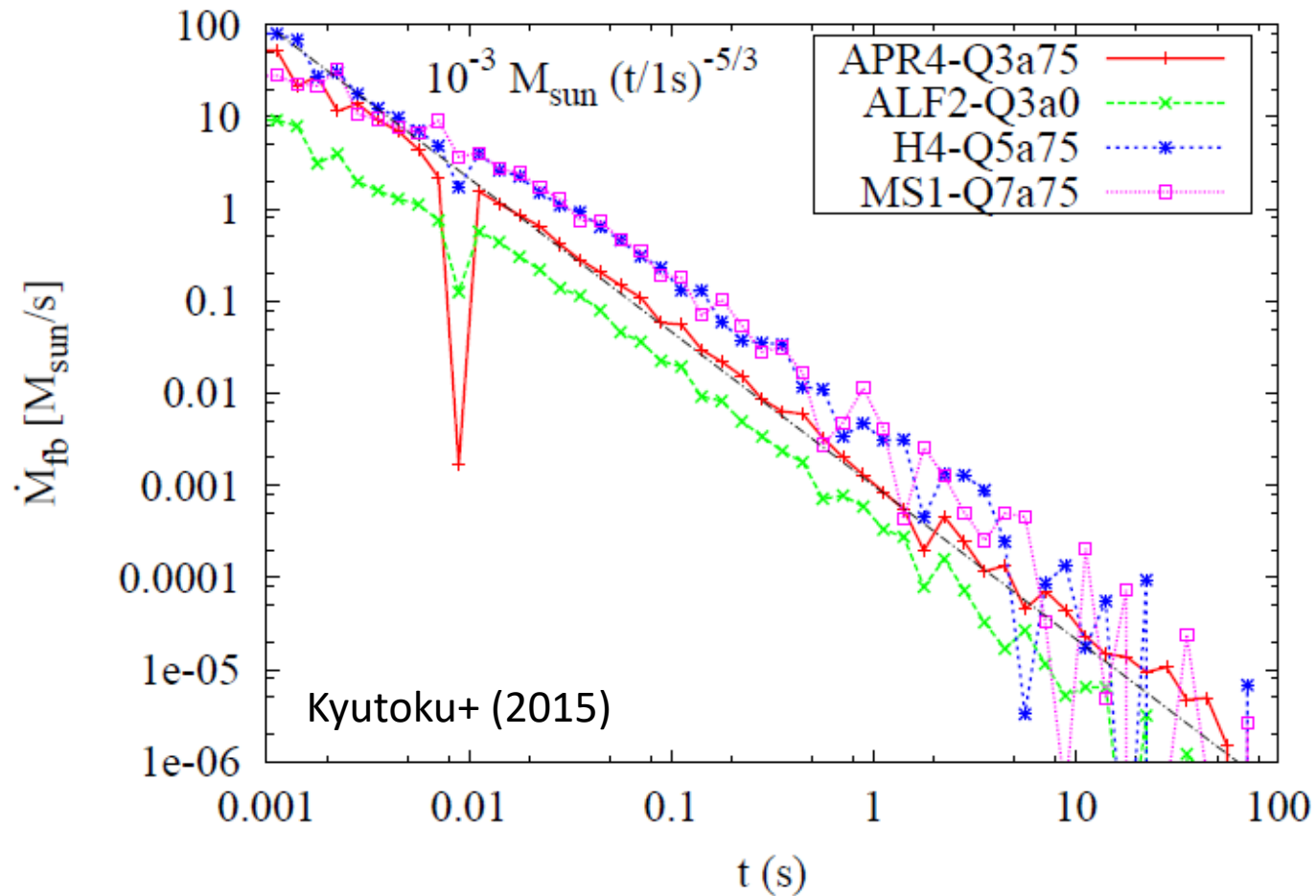
# Mass ratio dependence

The ejecta mass to disk mass ratio increases as the mass ratio increases (maybe realistic cases)



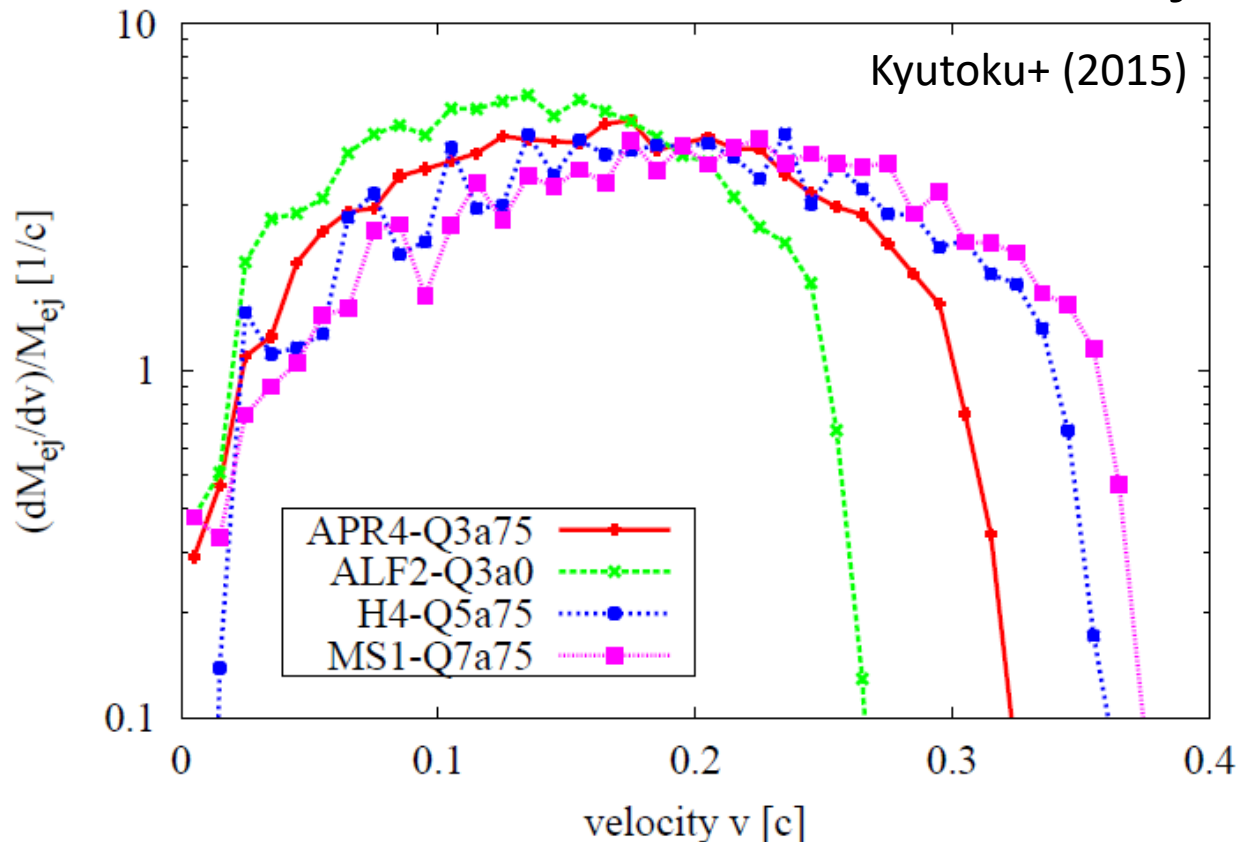
# Fallback material

“canonical” power law with the index  $-5/3$



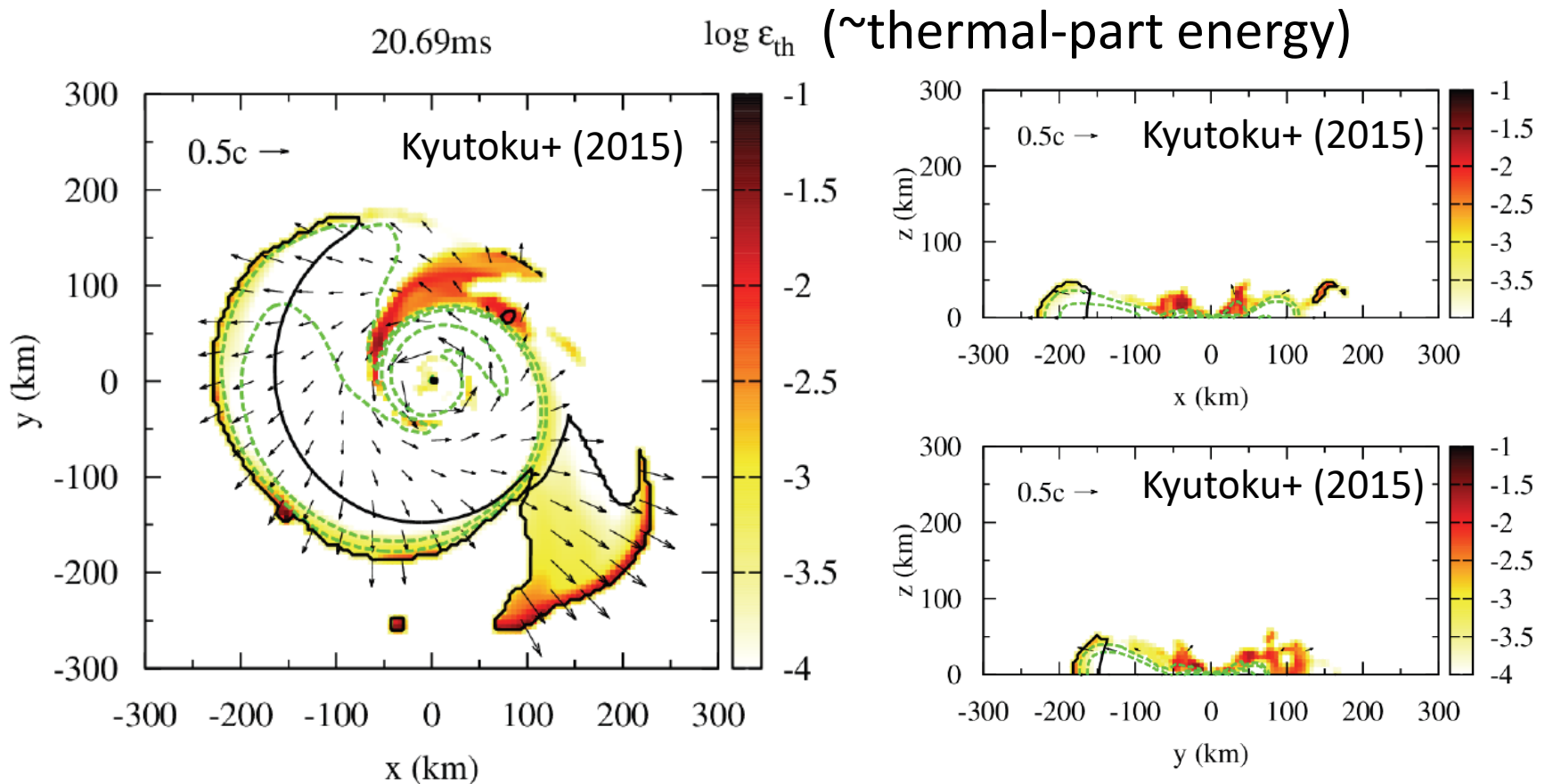
# Velocity distribution

Relatively flat w/ cutoffs rather than a power law seems to be flatter than that for NS-NS ejecta



# BH-NS Ejecta is very cold

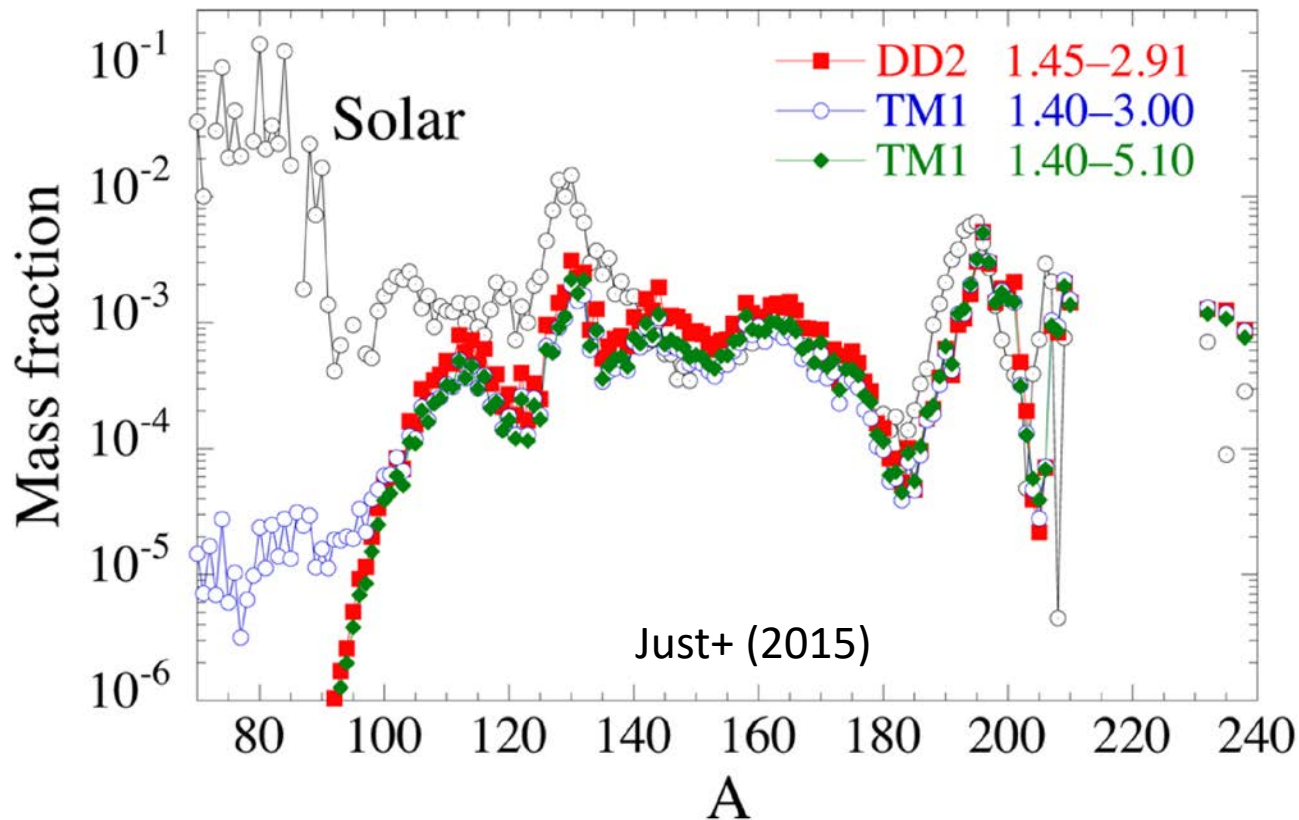
Because the ejecta experience no shock heating



# Expected nucleosynthetic yield

Significant fission cycling -> 2nd/3rd peak formation

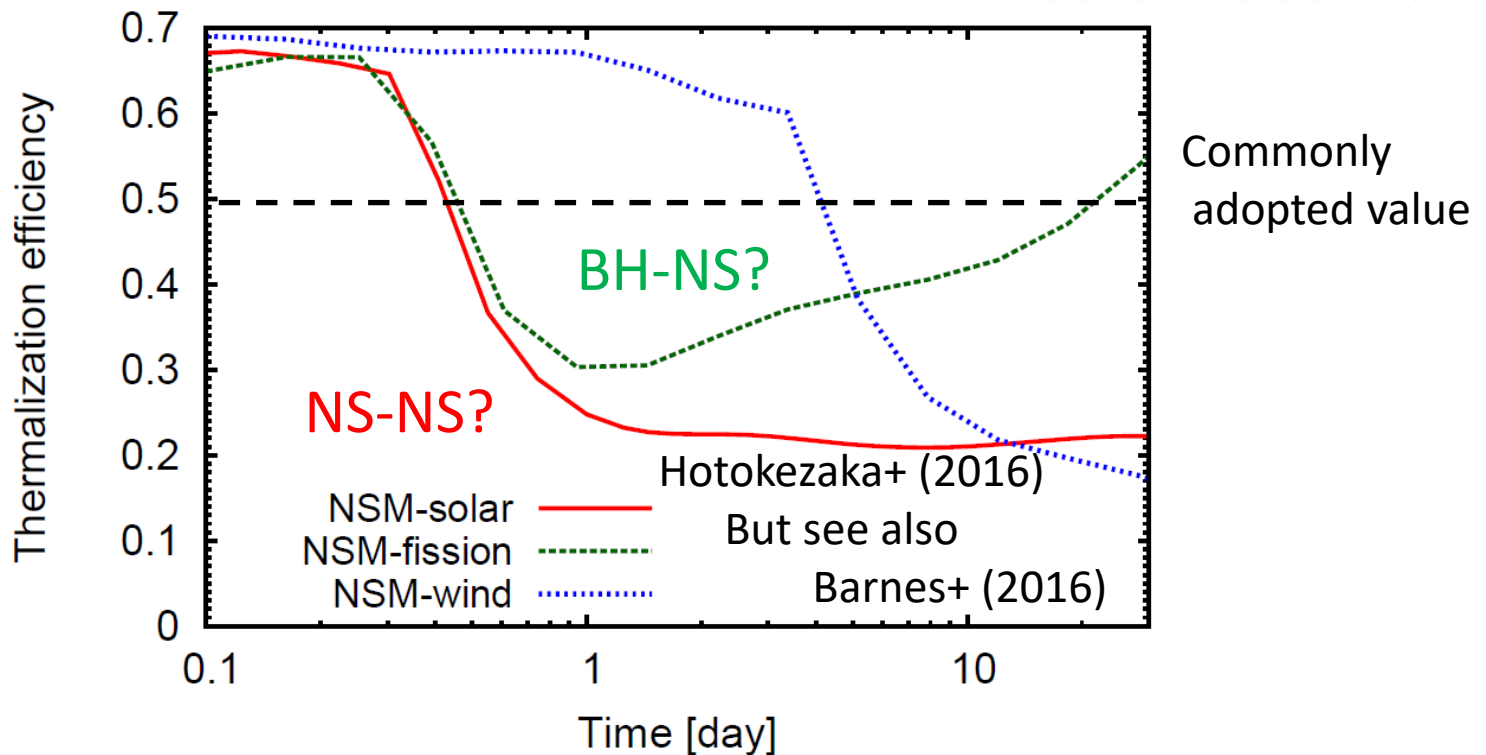
- our own nuclear network calculations are ongoing



# Bright macronova/kilonova?

Heavy r-process elements may result in efficient, fission-dominated heating on a week time scale

$M_{ej}=0.01M_{sun}$  ... if fission occurs

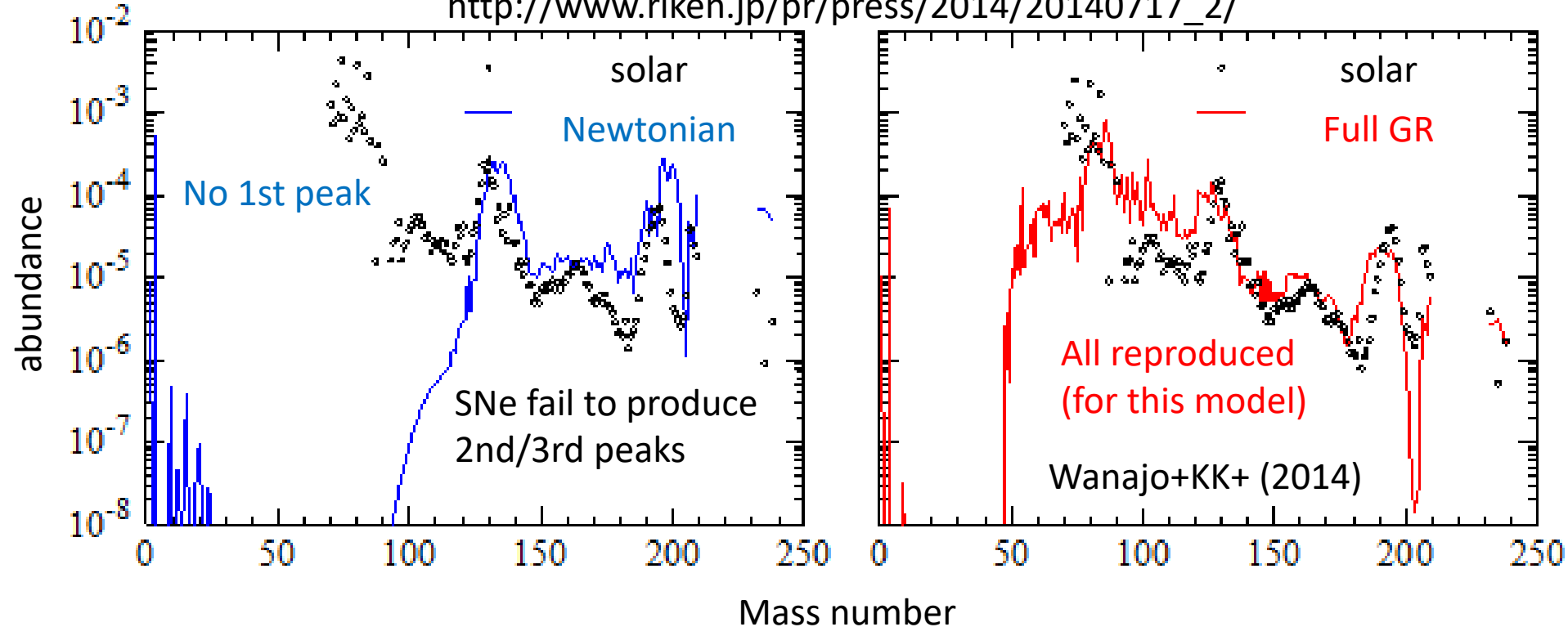




# Lesson from binary neutron stars

Numerical relativity with neutrino transport could be crucial for reproducing r-process abundances

[http://www.riken.jp/pr/press/2014/20140717\\_2/](http://www.riken.jp/pr/press/2014/20140717_2/)



# 3. Study in neutrino-radiation hydrodynamics

# Necessity of neutrino transport

How do neutrinos affect the merger dynamics and mass ejection in black hole-neutron star mergers?

What is the electron fraction of the ejecta?

$Y_e \equiv n_e/n_B$ : #electron per #baryon (p+n)

small  $Y_e$  = neutron rich,  $< \sim 0.1$  for neutron stars

How bright is the neutrino emission? Flavors?

Is the neutrino-driven wind launched from the disk?

# Numerical method

Einstein equation: BSSN formalism+puncture gauge

Radiation transfer (neutrino transport):

fully general-relativistic leakage scheme + heating

$$\text{fluid+trapped } \nu: \nabla_{\beta} T^{\alpha\beta} = -Q_{\text{cool}}^{\alpha} + Q_{\text{heat}}^{\alpha}$$

Equation of state: tabulated finite-temperature EOS

$$\text{streaming } \nu: \nabla_{\beta} T_S^{\alpha\beta} = Q_{\text{cool}}^{\alpha} - Q_{\text{heat}}^{\alpha}$$

An M1 closure is applied to the streaming neutrino

# Model parameters

We fix some parameters as  $M_{\text{NS}} = 1.35M_{\odot}$ ,  
 $M_{\text{BH}} = 5.4M_{\odot}$ ,  $\chi = 0.75$  due to limitations

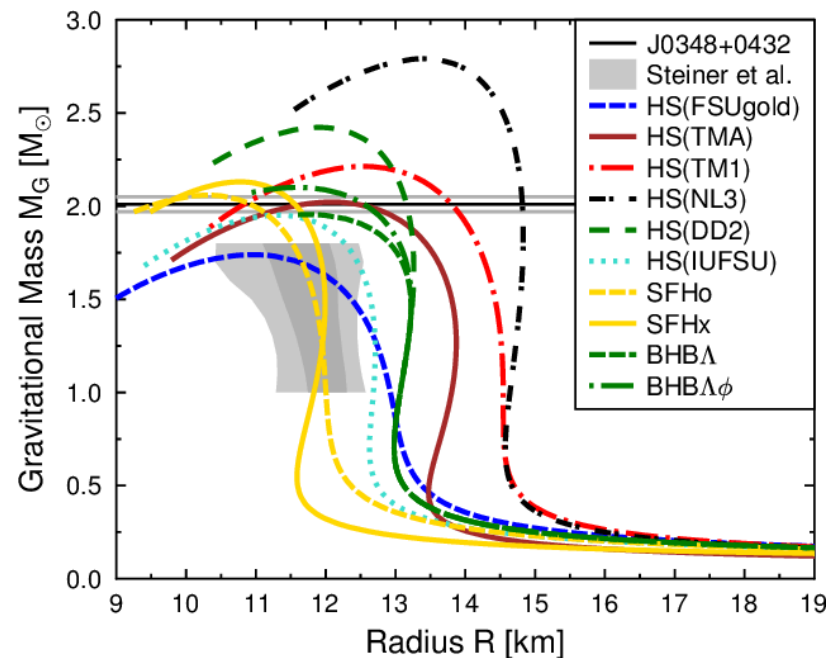
- systematic study is planned in the near future

Equations of state are  
chosen from 3 models

SFHo: 11.9km (soft)

DD2: 13.2km (middle)

TM1: 14.5km (stiff)

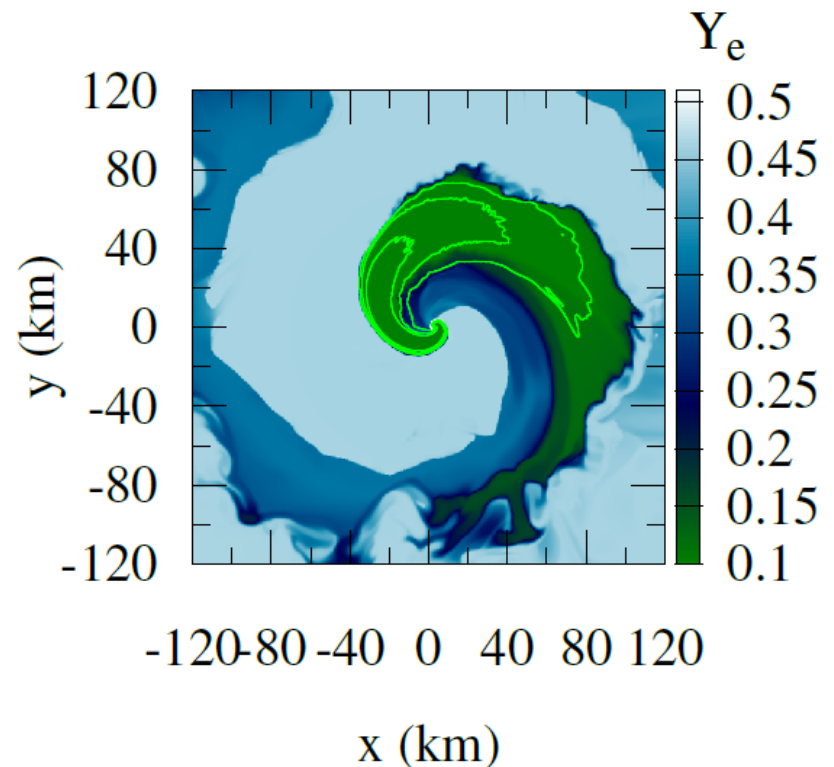
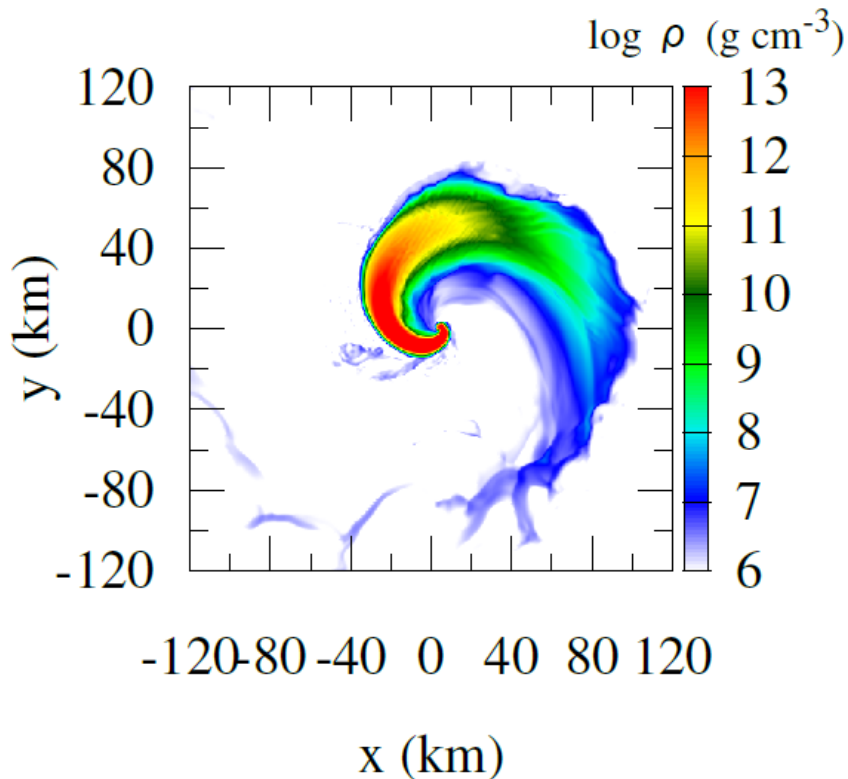


<http://www.hou.usra.edu/meetings/gammaray2016/pdf/program.pdf>

# Overview of the merger dynamics

Similar to the results of hydrodynamics study

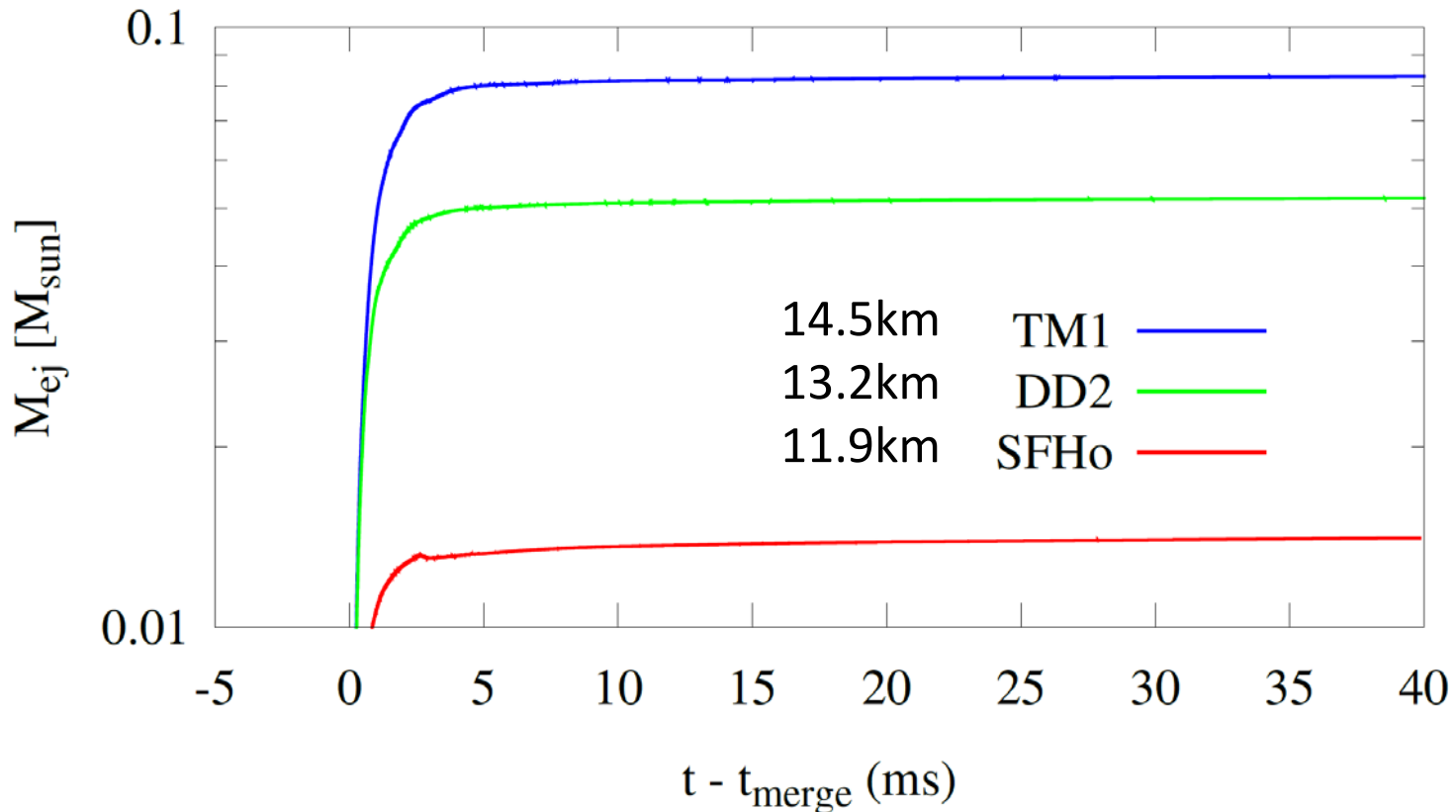
- outer parts become unbound ejecta with low  $Y_e$



# Ejecta mass

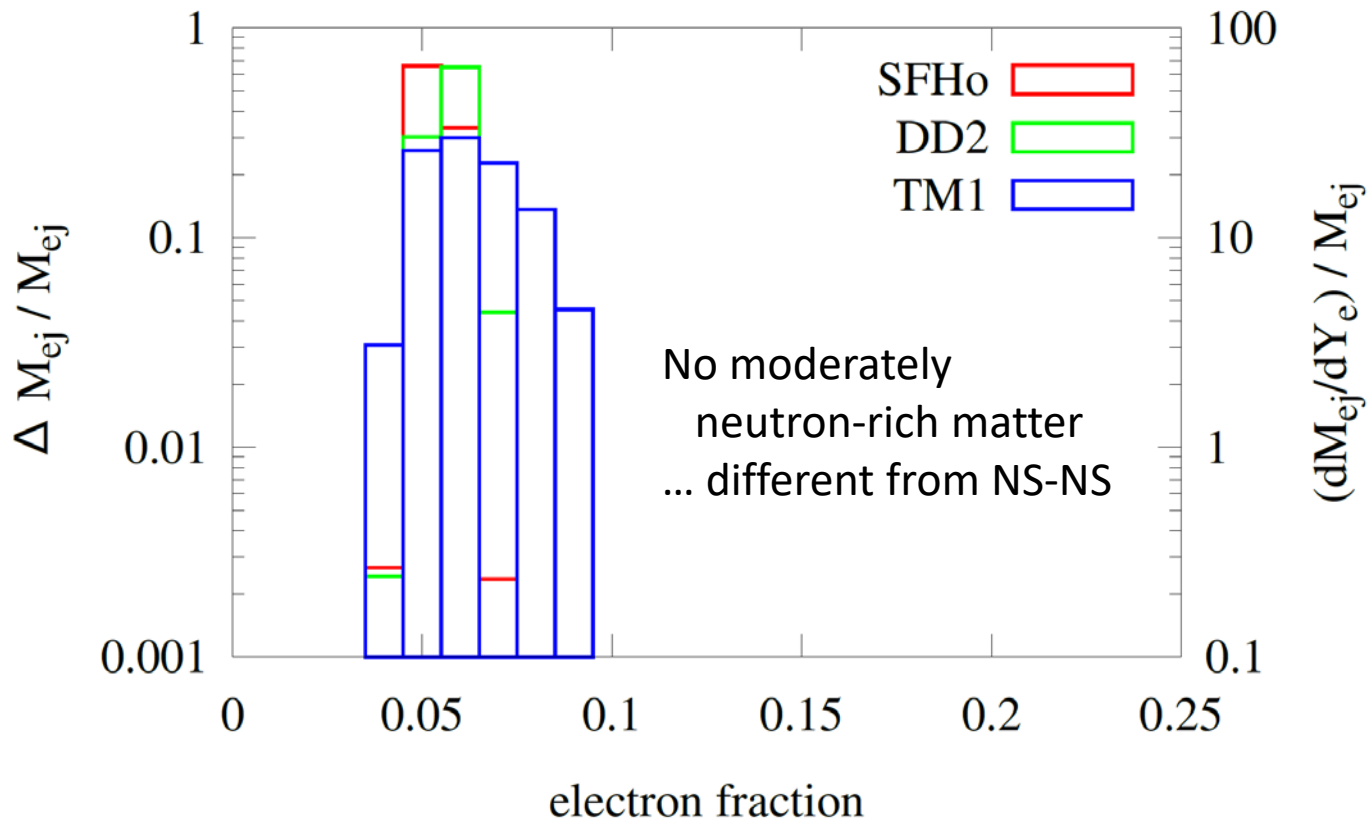
Larger ejecta mass for larger neutron-star radii

Agree w/ previous hydro. dynamical mass ejection



# Electron fraction distribution

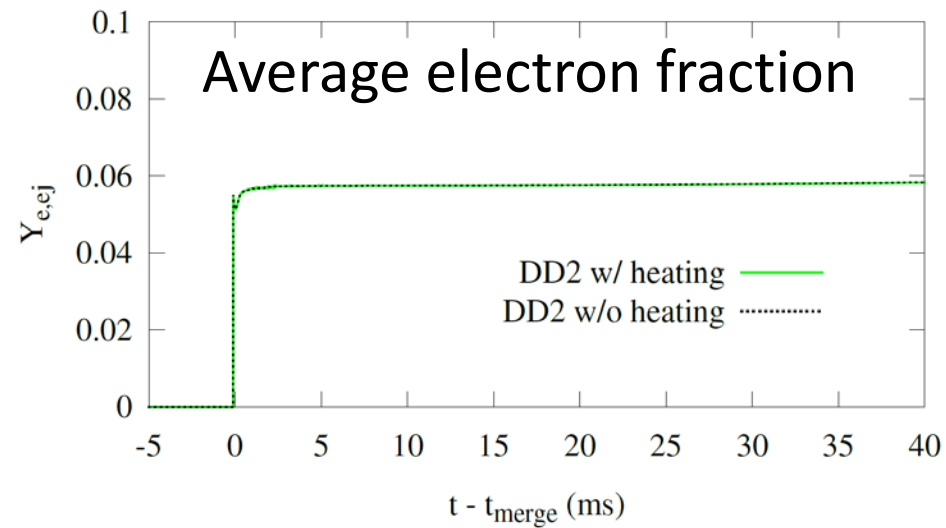
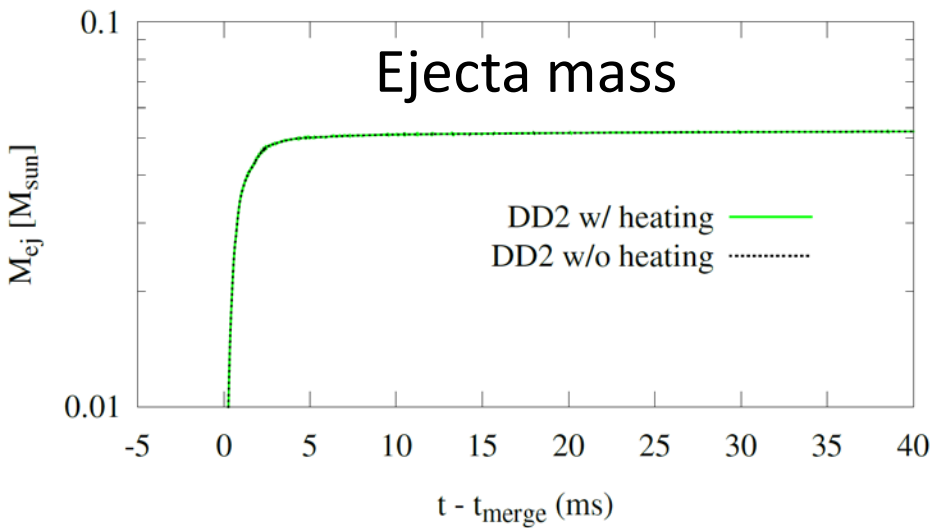
Strongly peaked below  $Y_e = 0.1$  for all the models  
i.e., original composition of neutron stars is kept





# Negligible neutrino-driven wind

The ejecta properties do not depend on  $\nu$ -heating  
- consistent with previous Newtonian simulations

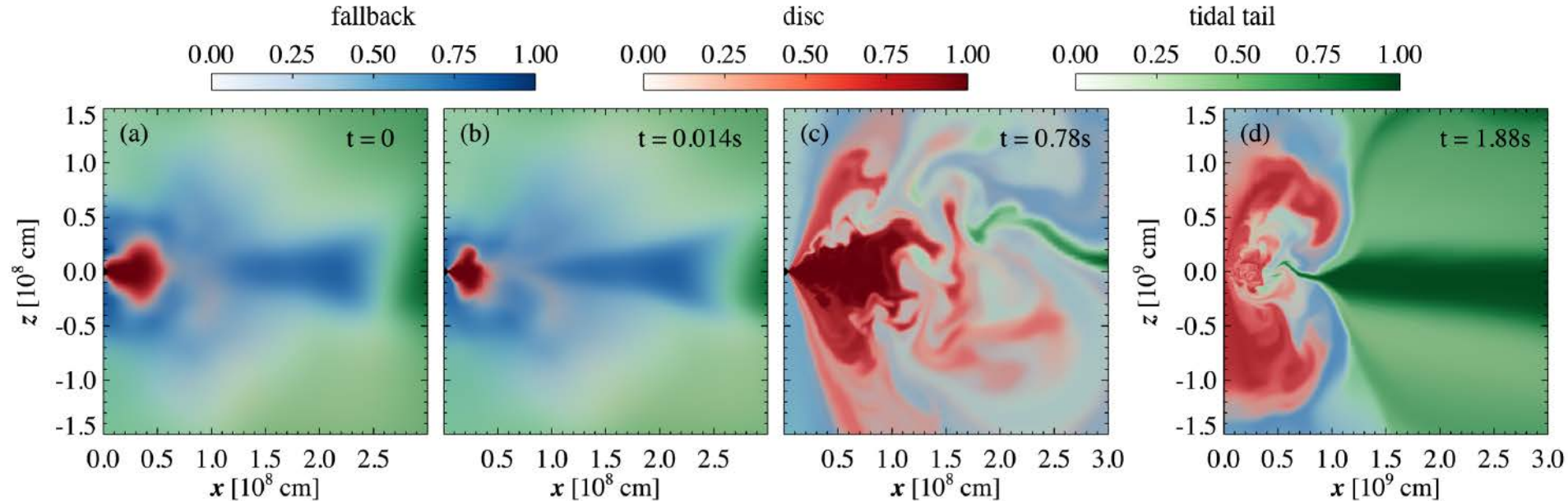


Are the disk winds negligible in the mass ejection?

# 4. Future direction and summary

# Viscously-driven wind

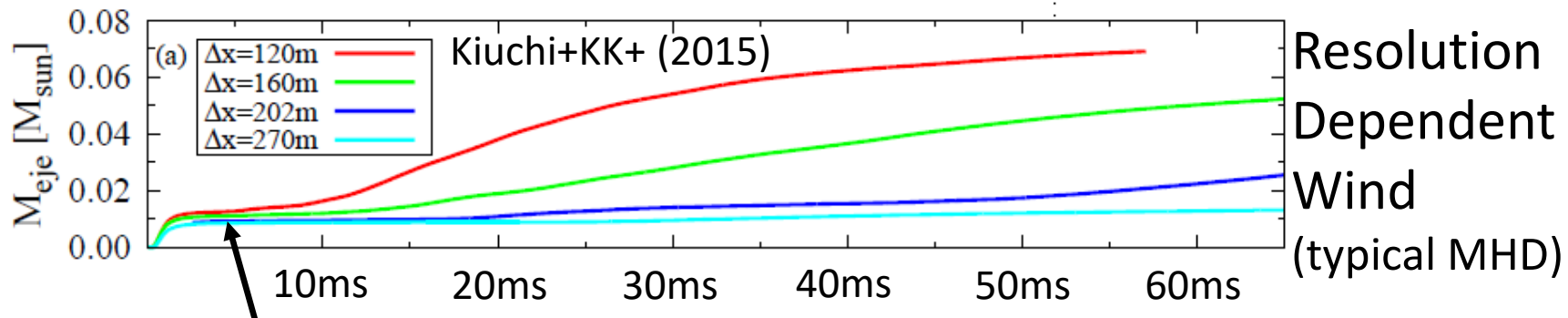
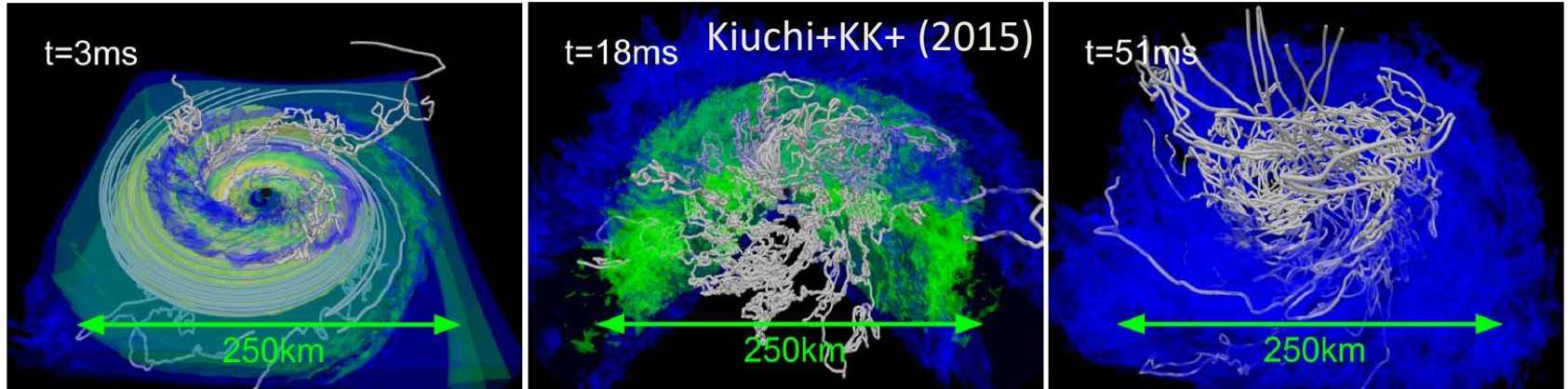
Should be more important than  $\nu$ -driven winds, where the viscosity comes from magnetic effects



Fernandez+ (2015)

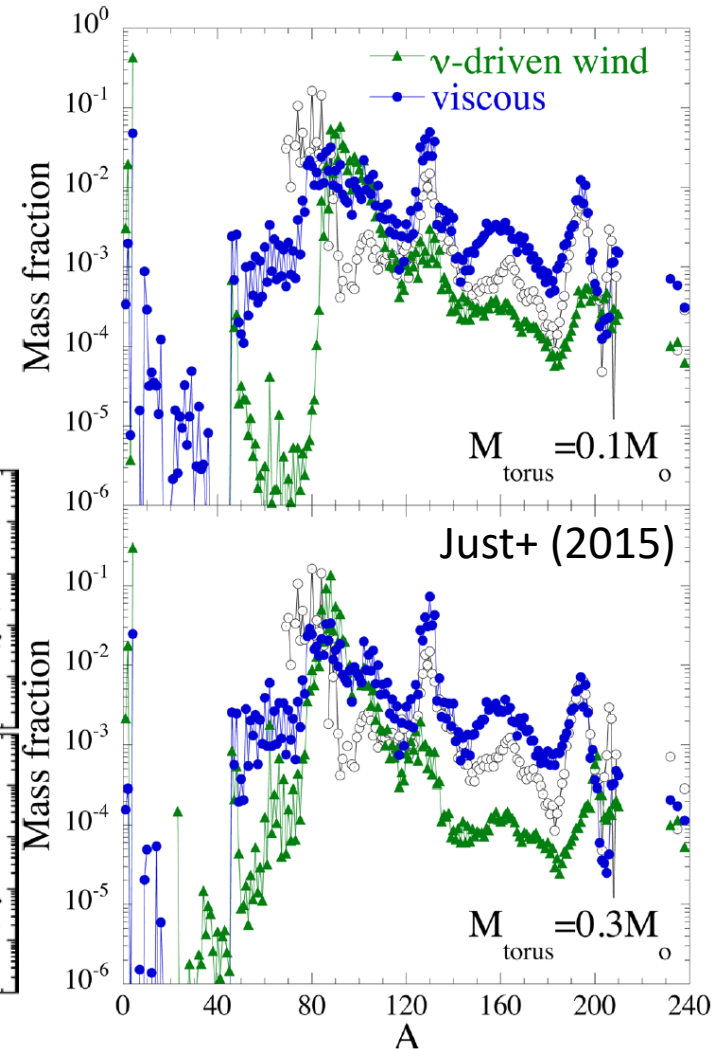
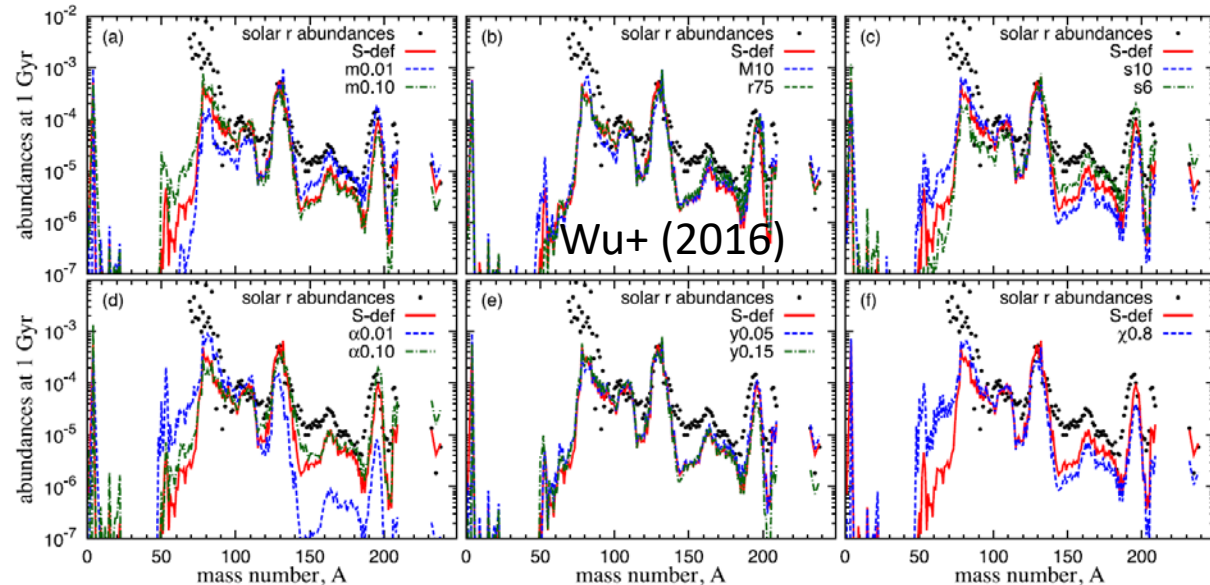
# Thermally-driven wind in MHD

High-resolution MHD simulations launch winds via turbulence-like states and efficient thermalization



# Diversity of the nucleosynthesis

When  $Y_e$  is high (say  $>0.25$ ),  
 lanthanoids may not be formed  
 Low velocity traps gamma-rays  
 -> bright macronova/kilonova?



# Summary

- Black hole-neutron star binary mergers can eject  $\sim 0.01 - 0.1 M_{\odot}$  with  $\sim 0.2 - 0.3c$  dynamically in a highly anisotropic manner for various cases.
- The electron fraction of dynamical ejecta is low because they do not experience shock heating.
- Neutrinos are not important for dynamical mass ejection and do not drive a strong disk wind.
- Other disk winds could dominate mass ejection and require more investigation.



# Appendix



# Event rate estimation (to change)

Uncertainties are orders of magnitude

Table 5. Detection rates for compact binary coalescence sources.

IFO	Source <sup>a</sup>	$\dot{N}_{\text{low}} \text{ yr}^{-1}$	$\dot{N}_{\text{re}} \text{ yr}^{-1}$	$\dot{N}_{\text{high}} \text{ yr}^{-1}$	$\dot{N}_{\text{max}} \text{ yr}^{-1}$
Initial	NS–NS	$2 \times 10^{-4}$	0.02	0.2	0.6
	NS–BH	$7 \times 10^{-5}$	0.004	0.1	
	BH–BH	$2 \times 10^{-4}$	0.007	0.5	
	IMRI into IMBH			$<0.001^{\text{b}}$	$0.01^{\text{c}}$
	IMBH–IMBH			$10^{-4\text{d}}$	$10^{-3\text{e}}$
Advanced	NS–NS	0.4	40	400	1000
	NS–BH	0.2	10	300	
	BH–BH	0.4	20	1000	
Abadie+ (2010)	IMRI into IMBH			$10^{\text{b}}$	$300^{\text{c}}$
	IMBH–IMBH			$0.1^{\text{d}}$	$1^{\text{e}}$

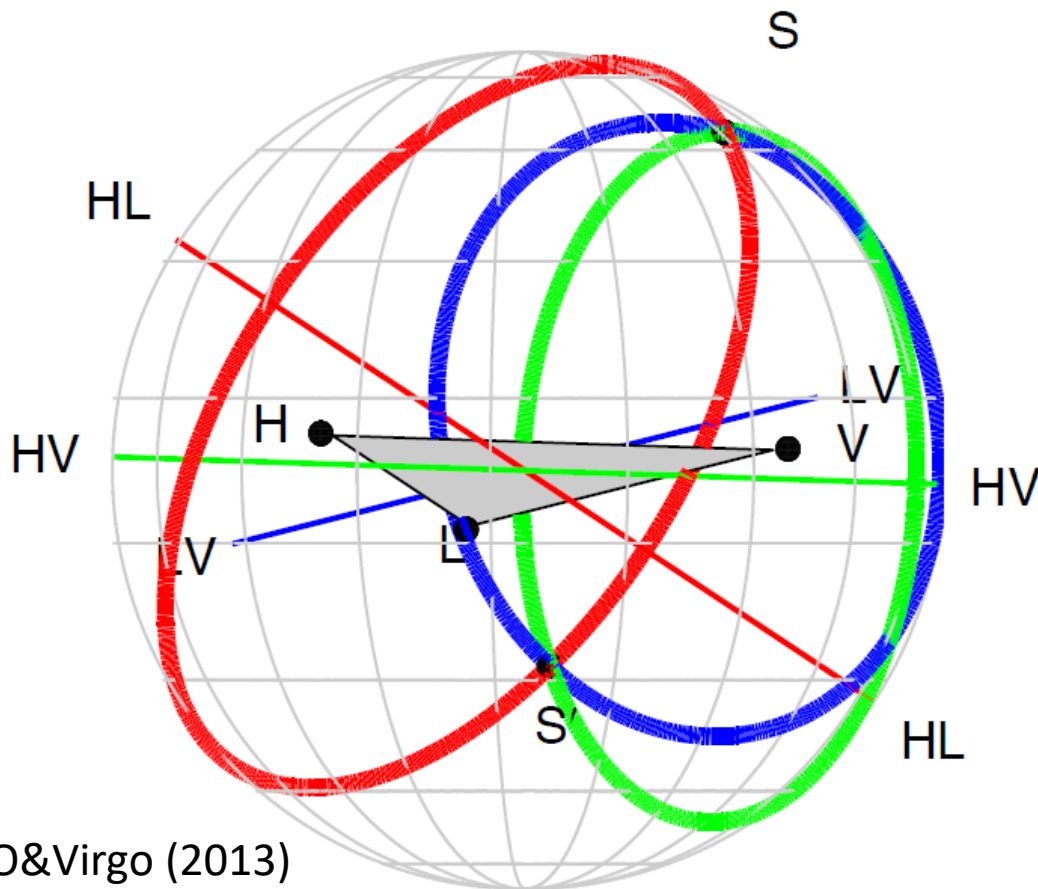
“Realistic”

Anyway - yearly detection may be expected

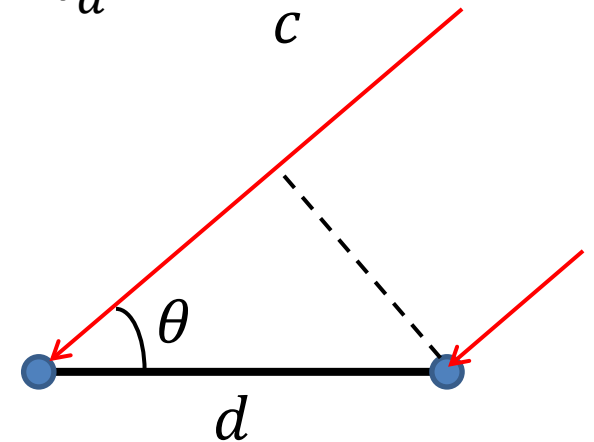
# Triangulation by a detector network

Determine the sky position from timing difference

$d \sim O(1000\text{km})$



$$t_d = \frac{d \cos \theta}{c}$$



LIGO&Virgo (2013)

# Dependence of peak luminosity/time

For spherical ejecta (Li-Paczynski 1998, also Arnett 1982)

The peak luminosity:  $L_{\text{peak}} \propto f \kappa^{-1/2} M^{1/2} v^{1/2}$

The peak time :  $t_{\text{peak}} \propto \kappa^{1/2} M^{1/2} v^{-1/2}$

Heating efficiency  $f$  and opacity  $\kappa$  – microphysics

important quantities, but not discussed today

Ejecta mass  $M$  and ejecta velocity  $v$  – macrophysics

hydrodynamic calculations can give answers

# Li-Paczynski model: macroscopic

Spherical ejecta with mass  $M$  and surface velocity  $v$

Homologous expansion w/ constant-density

$$R = vt, \quad \rho = \frac{3M}{4\pi R^3} = \frac{3M}{4\pi v^3 t^3}$$

Thermodynamic evolution for per-mass quantities

$$TdS = dE + PdV \rightarrow Tds = d\left(\frac{e}{\rho}\right) + Pd\left(\frac{1}{\rho}\right)$$

Nuclear heating and radiative cooling per mass

$$Tds/dt = \dot{\epsilon} - L/M$$

# Li-Paczynski model: microscopic

The ejecta should be radiation-dominated  $P = e/3$

Nuclear heating may obey a power-law

$$\dot{\epsilon} = \frac{f c^2}{t}$$

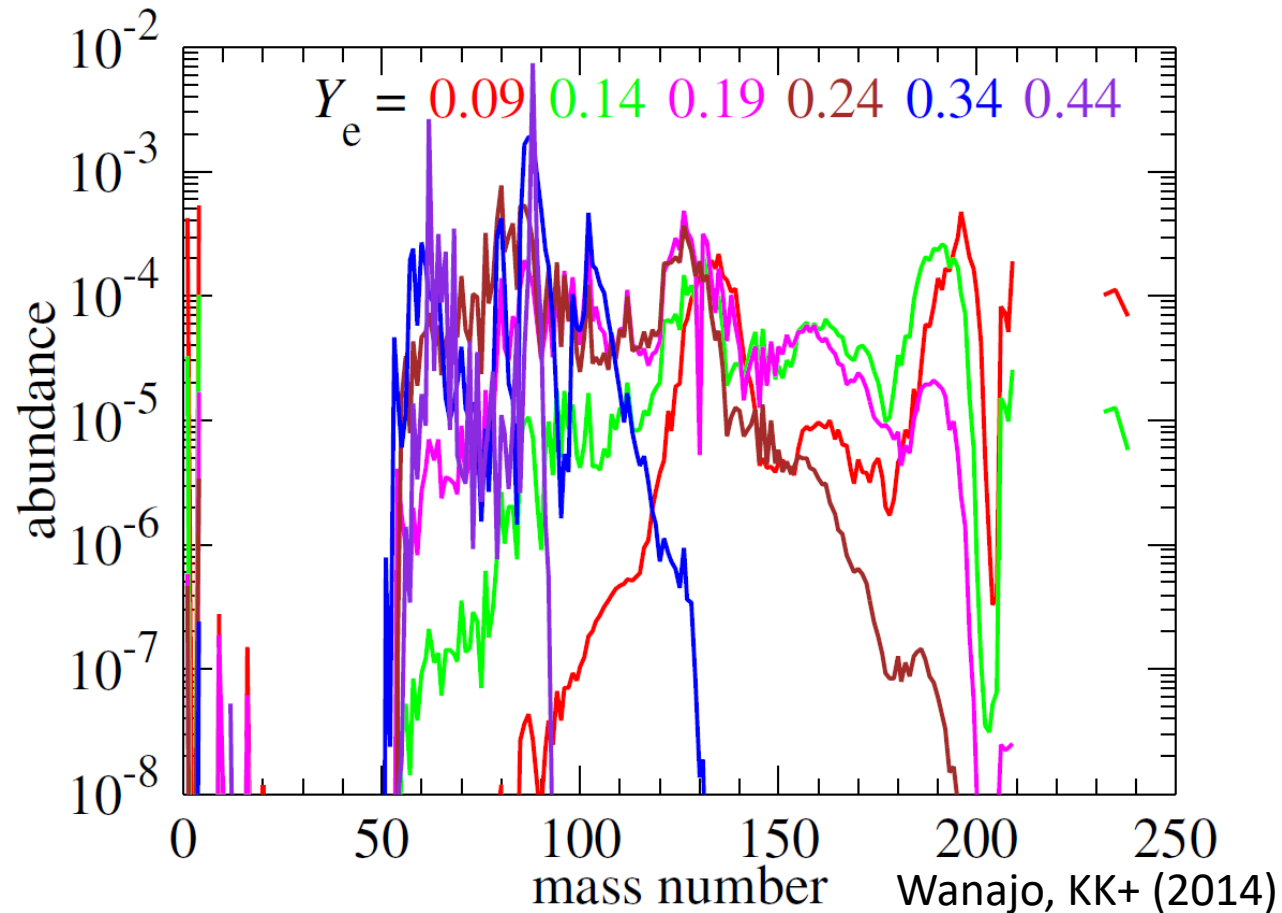
Radiative cooling is given by the diffusion approx.

$$L = 4\pi R^2 F, \quad F = \frac{c}{3\kappa\rho} \left( -\frac{dE}{dr} \right) \approx \frac{ceR^2}{\kappa\rho}$$

-> time evolution of  $e$  can be solved analytically  
the bolometric light curve is also derived

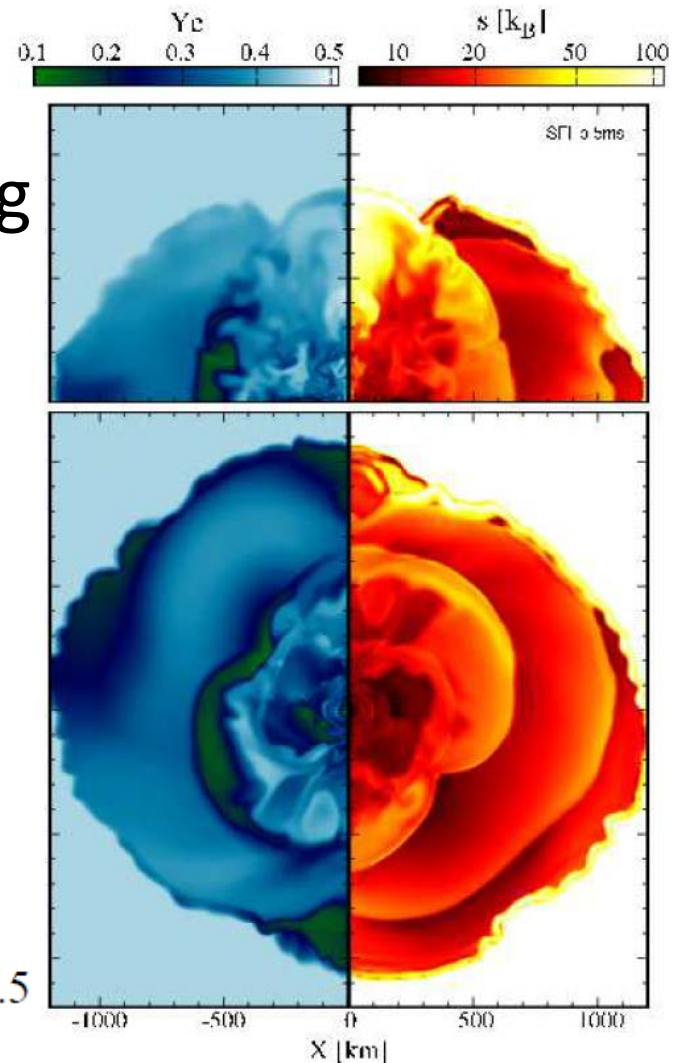
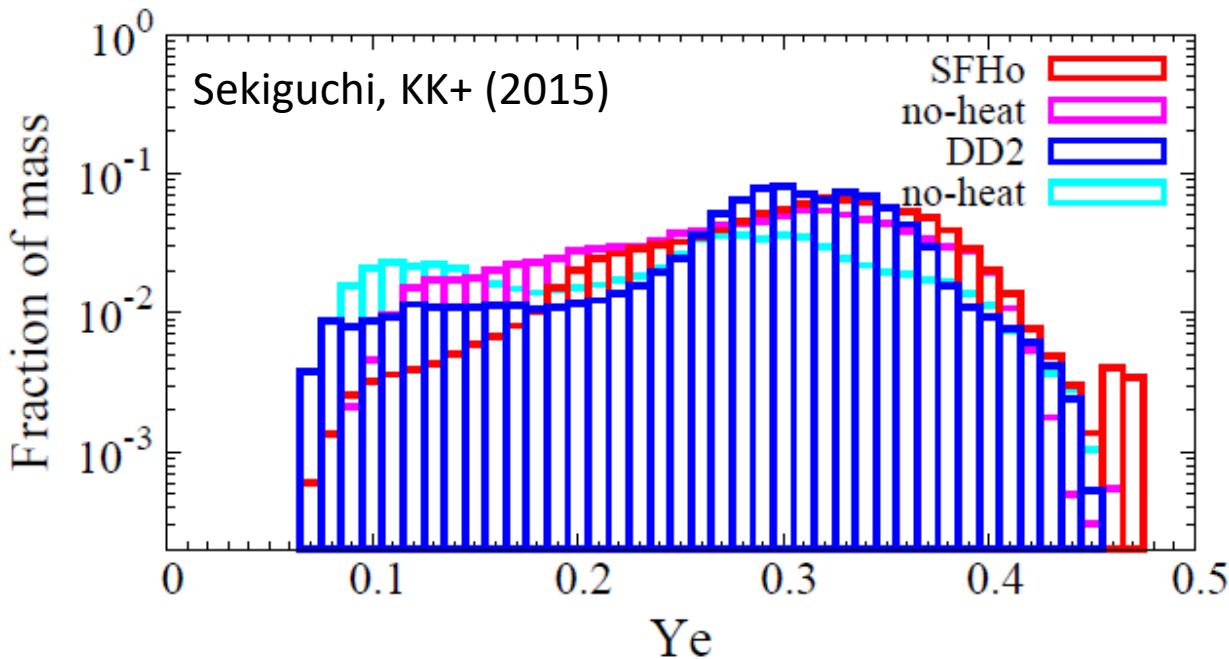
# Why successful r-process?

Broad distribution of electron fraction in full GR



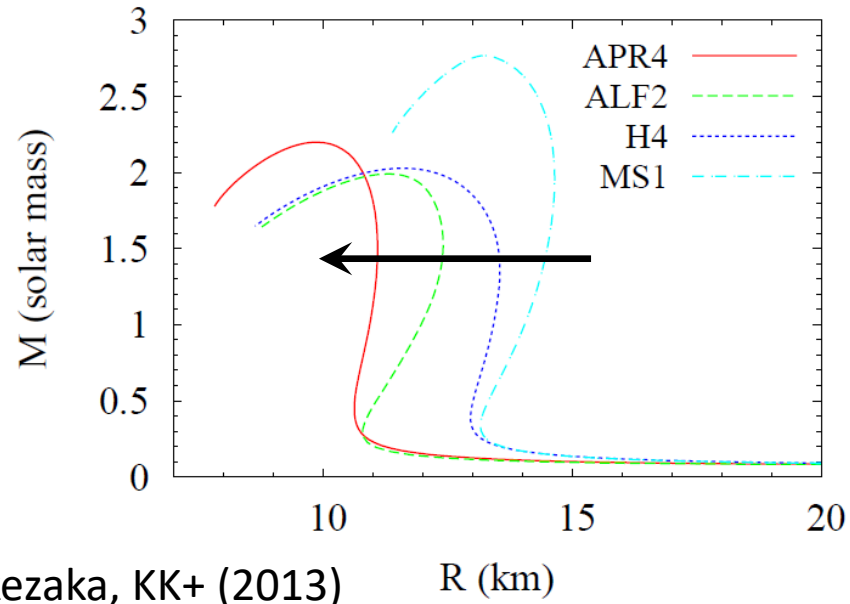
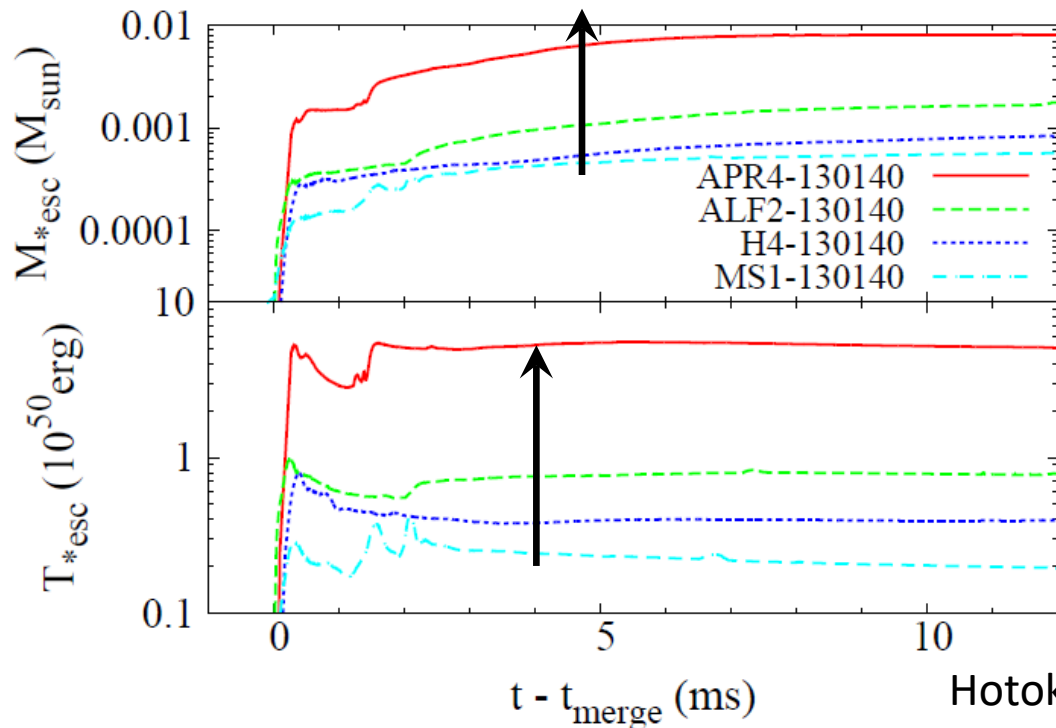
# GR NS-NS ejecta

The electron fraction can be increased by strong shock heating (and also neutrino irradiation)



# EOS dependence of NS-NS ejecta

Ejecta are massive when the NS radius is small due to violent activity of a compact remnant NS

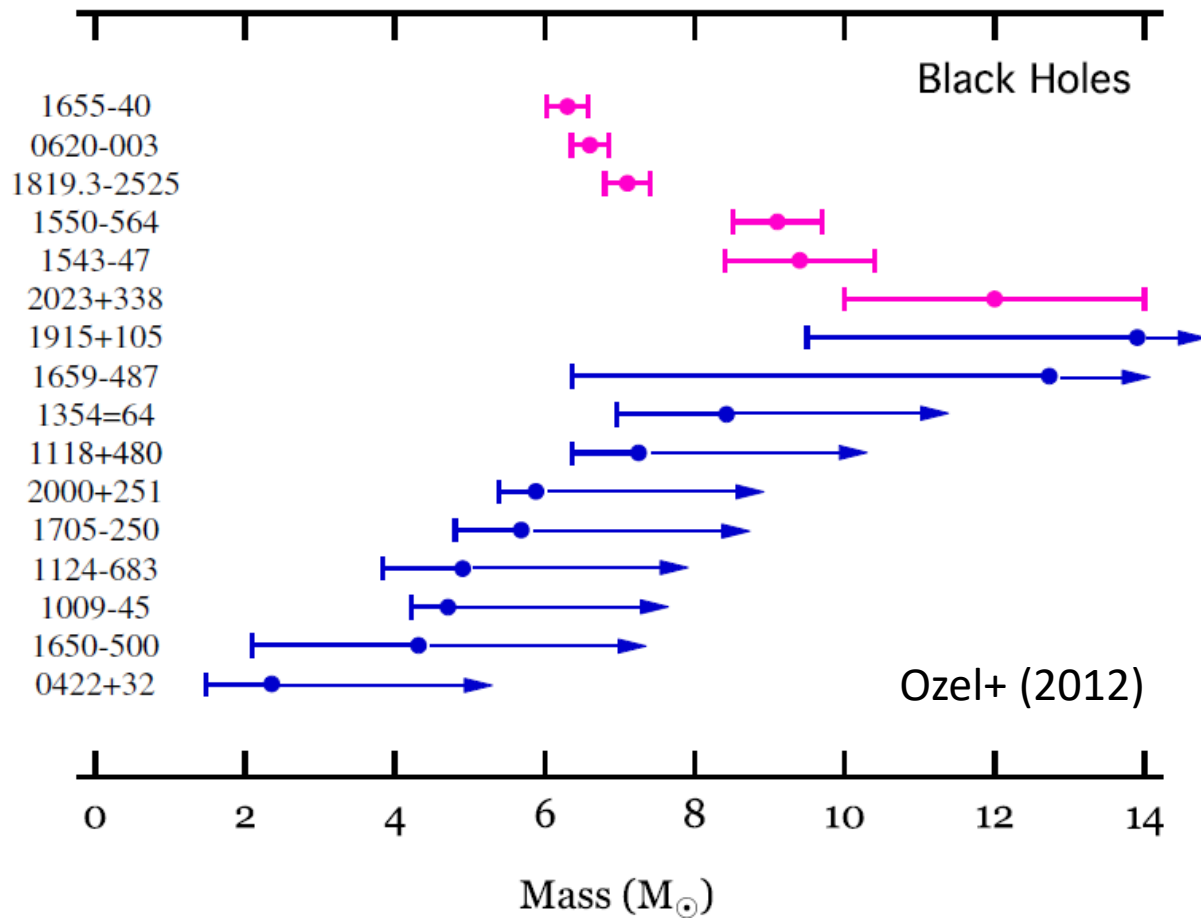


Hotokezaka, KK+ (2013)



# Black hole mass

Mass gap around  $3 - 5M_{\odot}$  is frequently debated



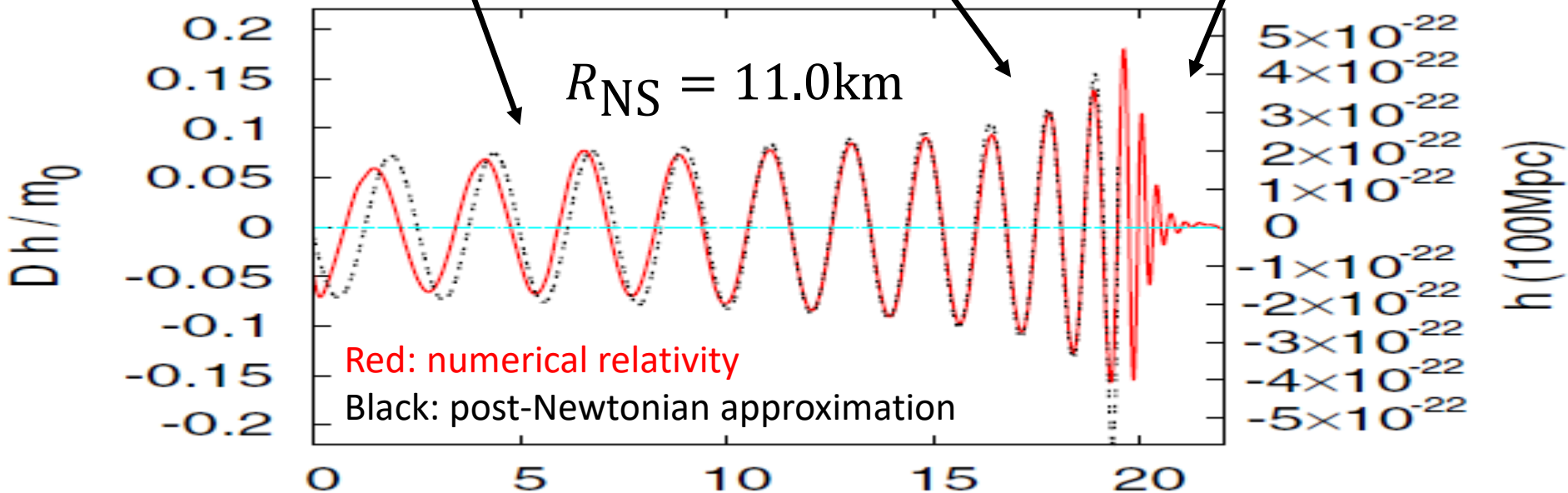
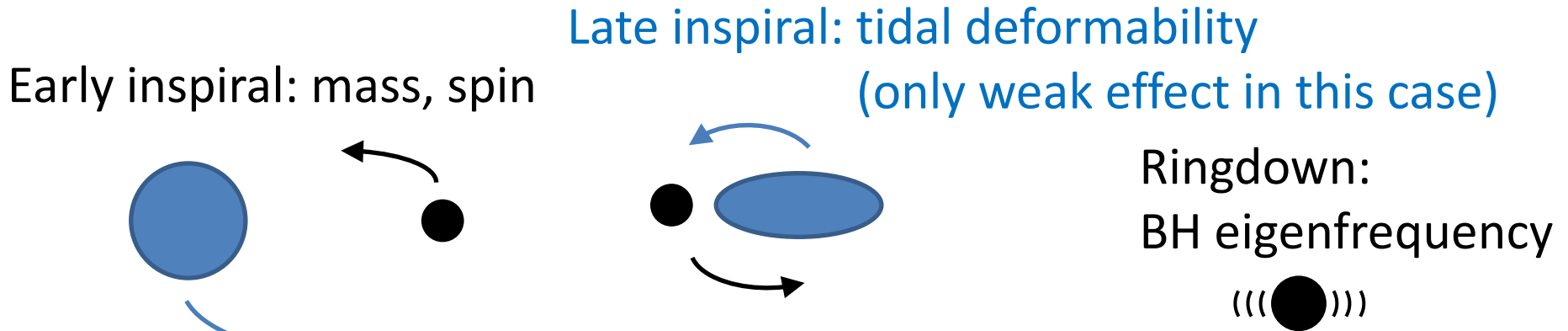
# Black hole spin

## Uncertain but no typical value exists?

McClintock+ (2014)

System	$a_*$	$M/M_\odot$	References
Persistent			
Cyg X-1	$> 0.95$	$14.8 \pm 1.0$	Gou et al. 2011; Orosz et al. 2011a
LMC X-1	$0.92^{+0.05}_{-0.07}$	$10.9 \pm 1.4$	Gou et al. 2009; Orosz et al. 2009
M33 X-7	$0.84 \pm 0.05$	$15.65 \pm 1.45$	Liu et al. 2008; Orosz et al. 2007
Transient			
GRS 1915+105	$> 0.95^b$	$10.1 \pm 0.6$	McClintock et al. 2006; Steeghs et al. 2013
4U 1543–47	$0.80 \pm 0.10^b$	$9.4 \pm 1.0$	Shafee et al. 2006; Orosz 2003
GRO J1655–40	$0.70 \pm 0.10^b$	$6.3 \pm 0.5$	Shafee et al. 2006; Greene et al. 2001
XTE J1550–564	$0.34^{+0.20}_{-0.28}$	$9.1 \pm 0.6$	Steiner et al. 2011; Orosz et al. 2011b
H1743–322	$0.2 \pm 0.3$	$\sim 8^c$	Steiner et al. 2012a
LMC X-3	$< 0.3^d$	$7.6 \pm 1.6$	Davis et al. 2006; Orosz 2003
A0620–00	$0.12 \pm 0.19$	$6.6 \pm 0.25$	Gou et al. 2010; Cantrell et al. 2010

# Gravitational waves without disruption

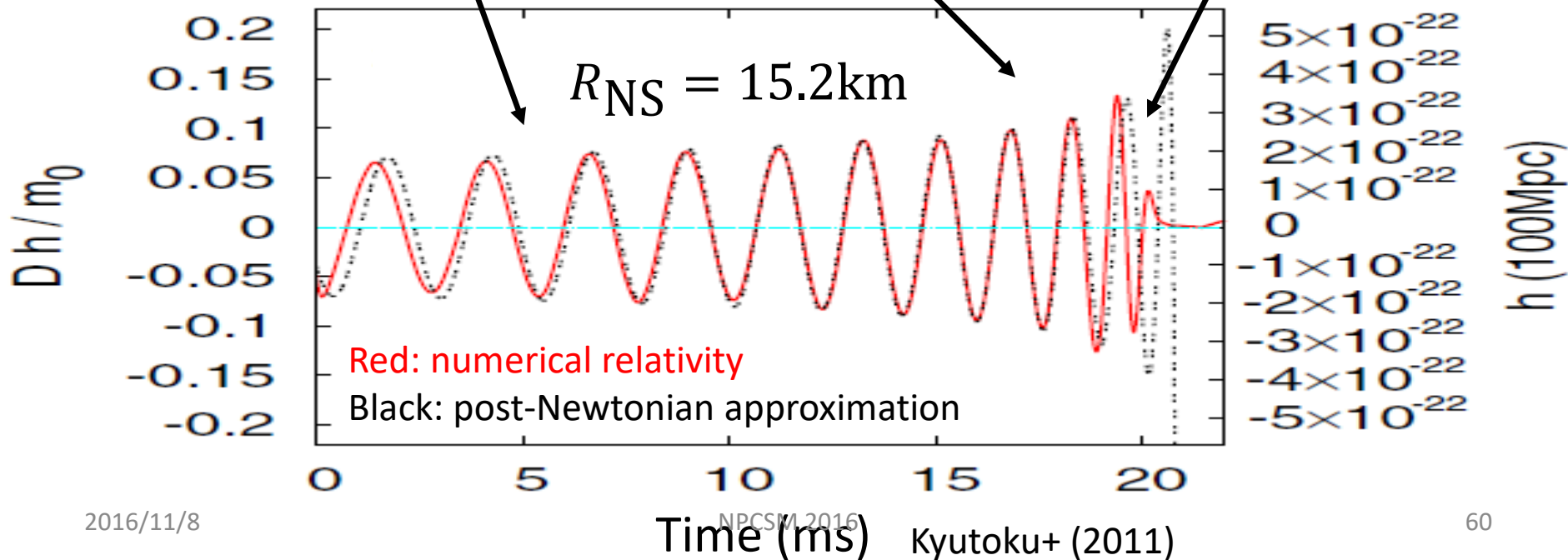
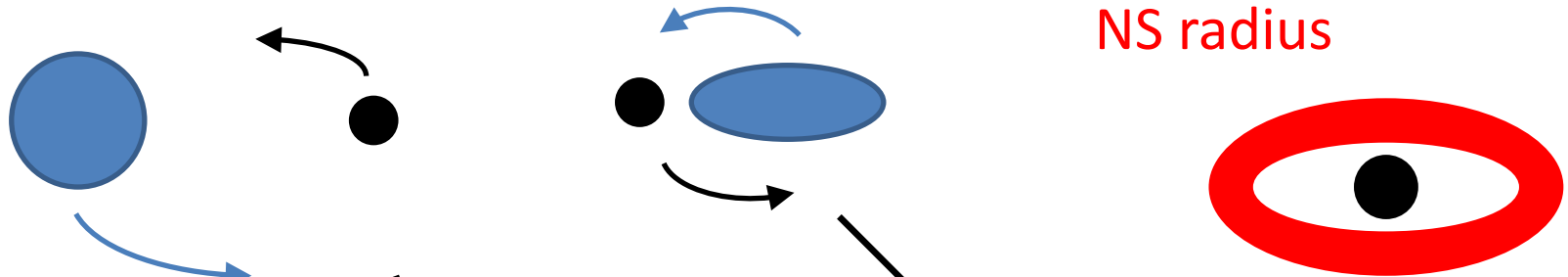


# Gravitational waves with disruption

Late inspiral: tidal deformability

Tidal disruption cutoff:  
NS radius

Early inspiral: mass, spin



# Numerical relativity

The Einstein equation

$$G_{ab} = 8\pi T_{ab}, \quad (G = c = 1)$$

Local energy-momentum conservation equation

$$\nabla_b T^{ab} = 0,$$

Rest-mass (or particle number) continuity equation

$$\nabla_a (\rho u^a) = 0$$

+ equation of state e.g.,  $P = P(\rho), P(\rho, T, Y_e) \dots$

also solve Magneto/Radiation-HD Eqs. if you want

# Numerical method

Initial data: LORENE (spectral method)  
quasiequilibrium states of BH-NS binaries

Dynamical simulation: SACRA (Yamamoto+ 2008)

- BSSN formalism of the Einstein equation

  - 4th order finite difference in time and space

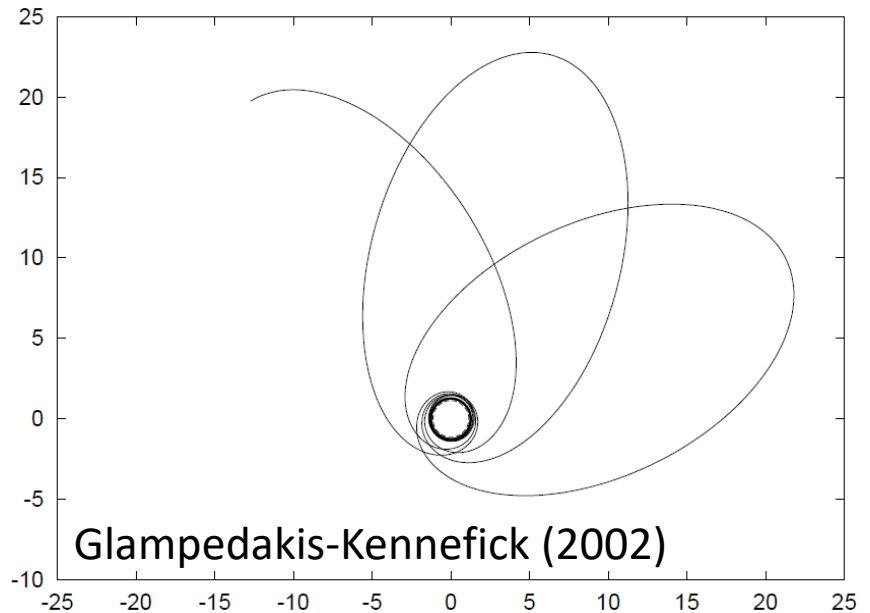
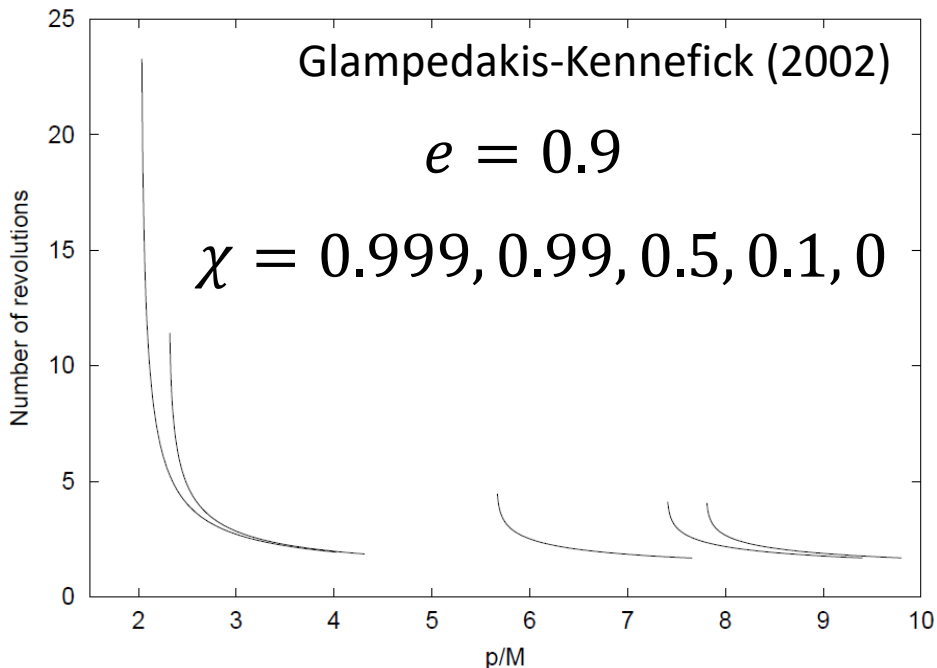
- ideal hydrodynamics

  - 3rd order PPM reconstruction + central scheme

- adaptive mesh refinement

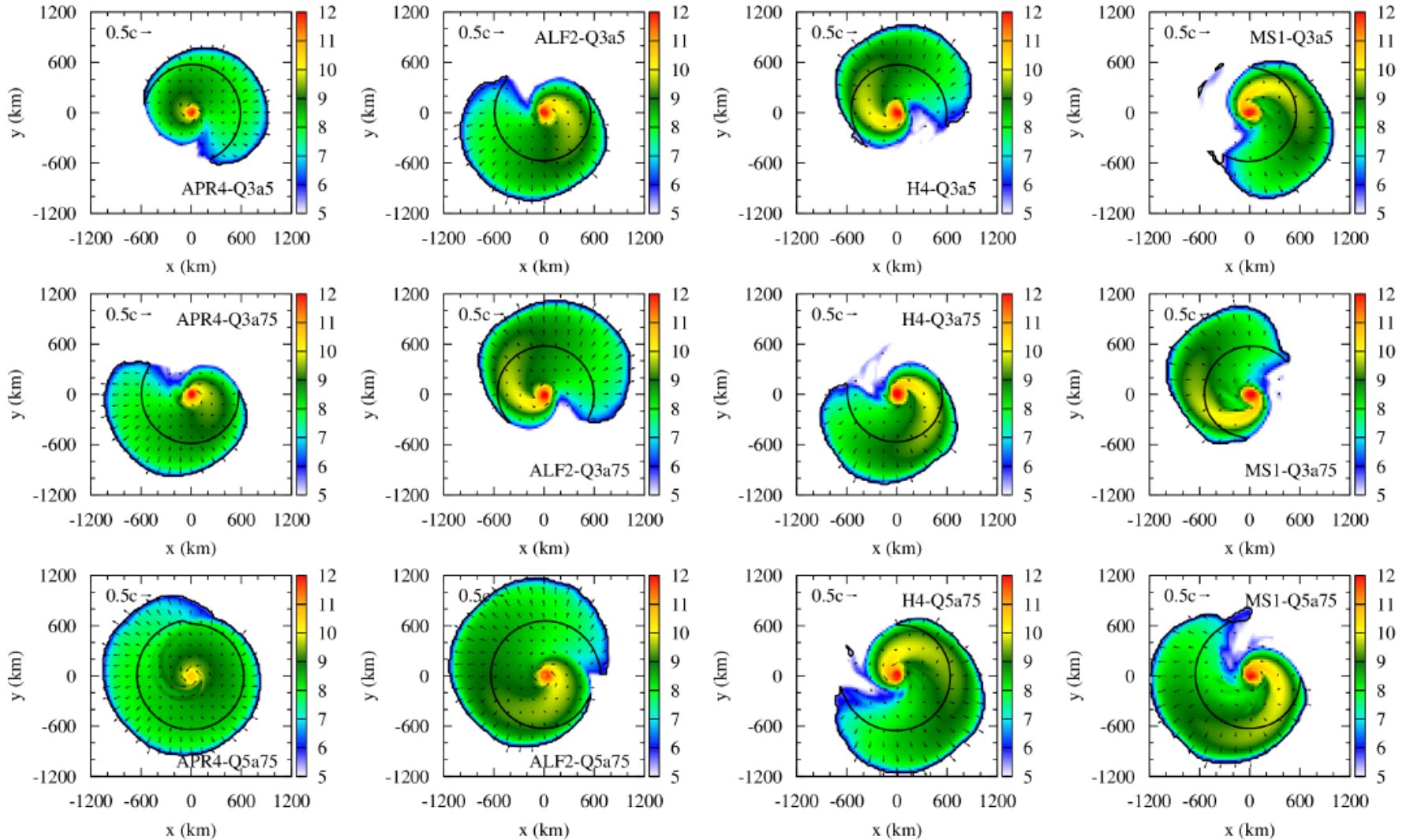
# Periastron advance: zoom-whirl

Eccentric orbits can experience many cycles near the last bound orbit



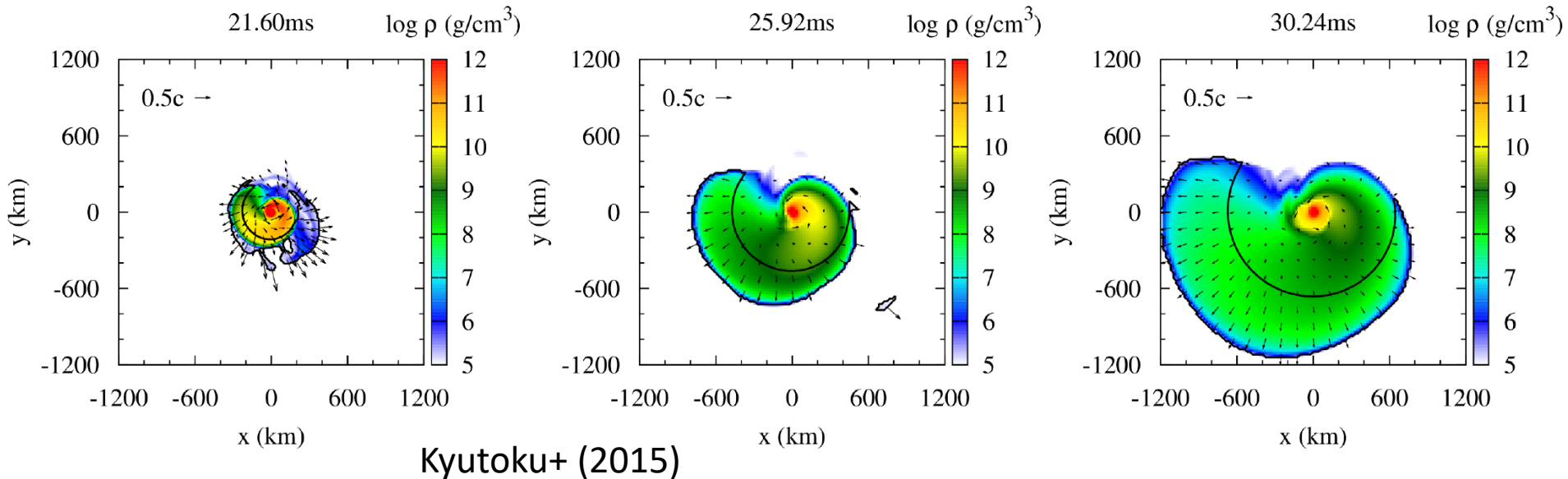
This “zoom-whirl” is an extreme example of periastron advance

# Various ejecta opening angle





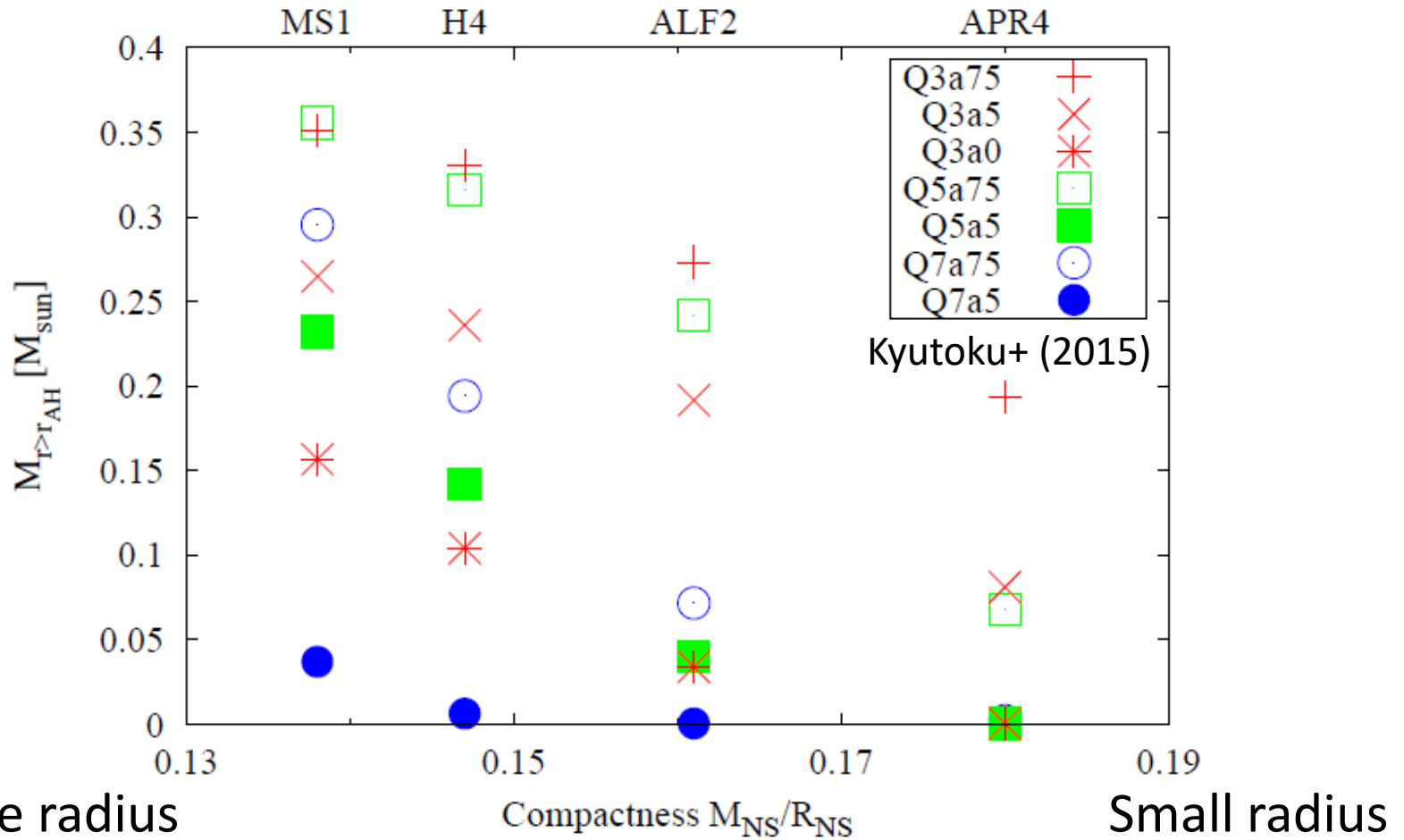
# Late-time evolution



- homologous evolution (crescent to half-disk)
- radial-motion dominated (angu. mom conserv.)

# Mass remaining outside the BH

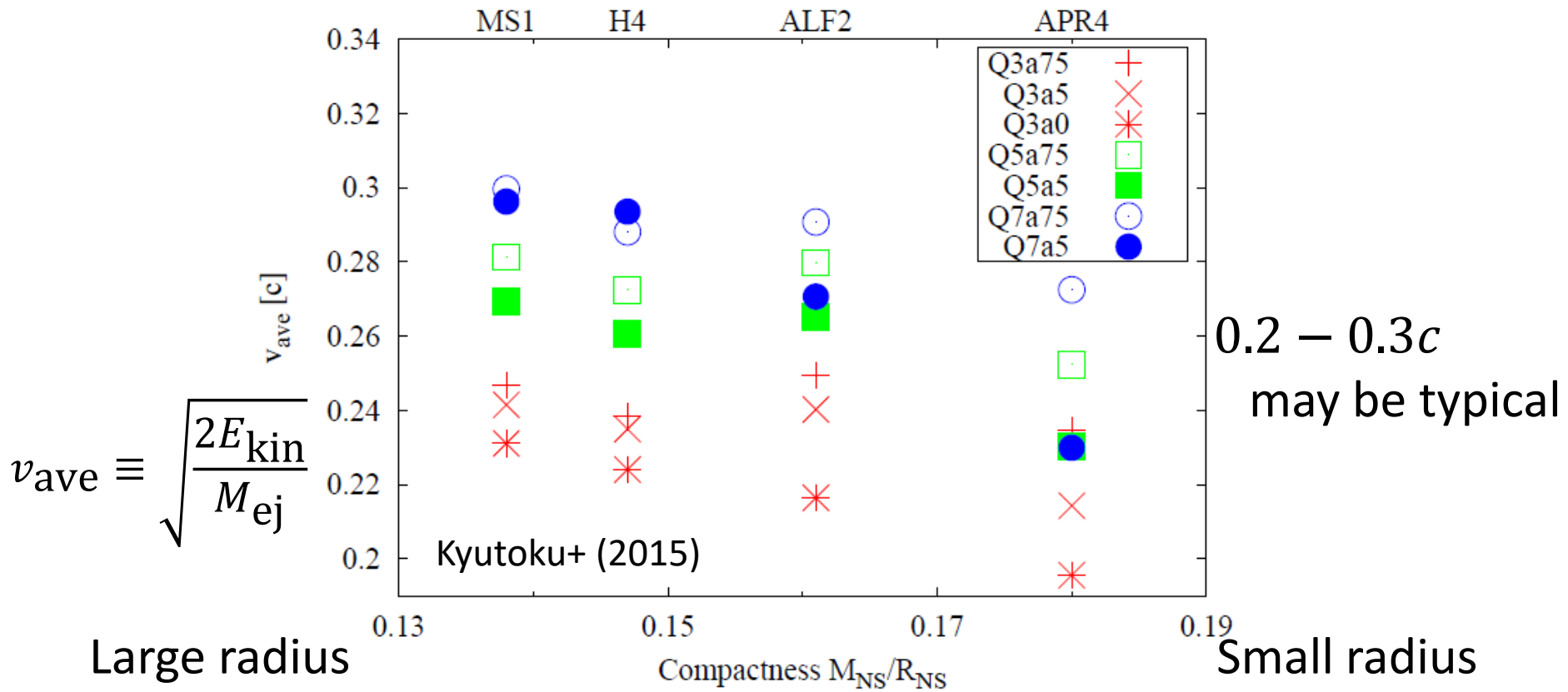
Nicely correlated with the NS compactness (radius)



# Average velocity of the ejecta

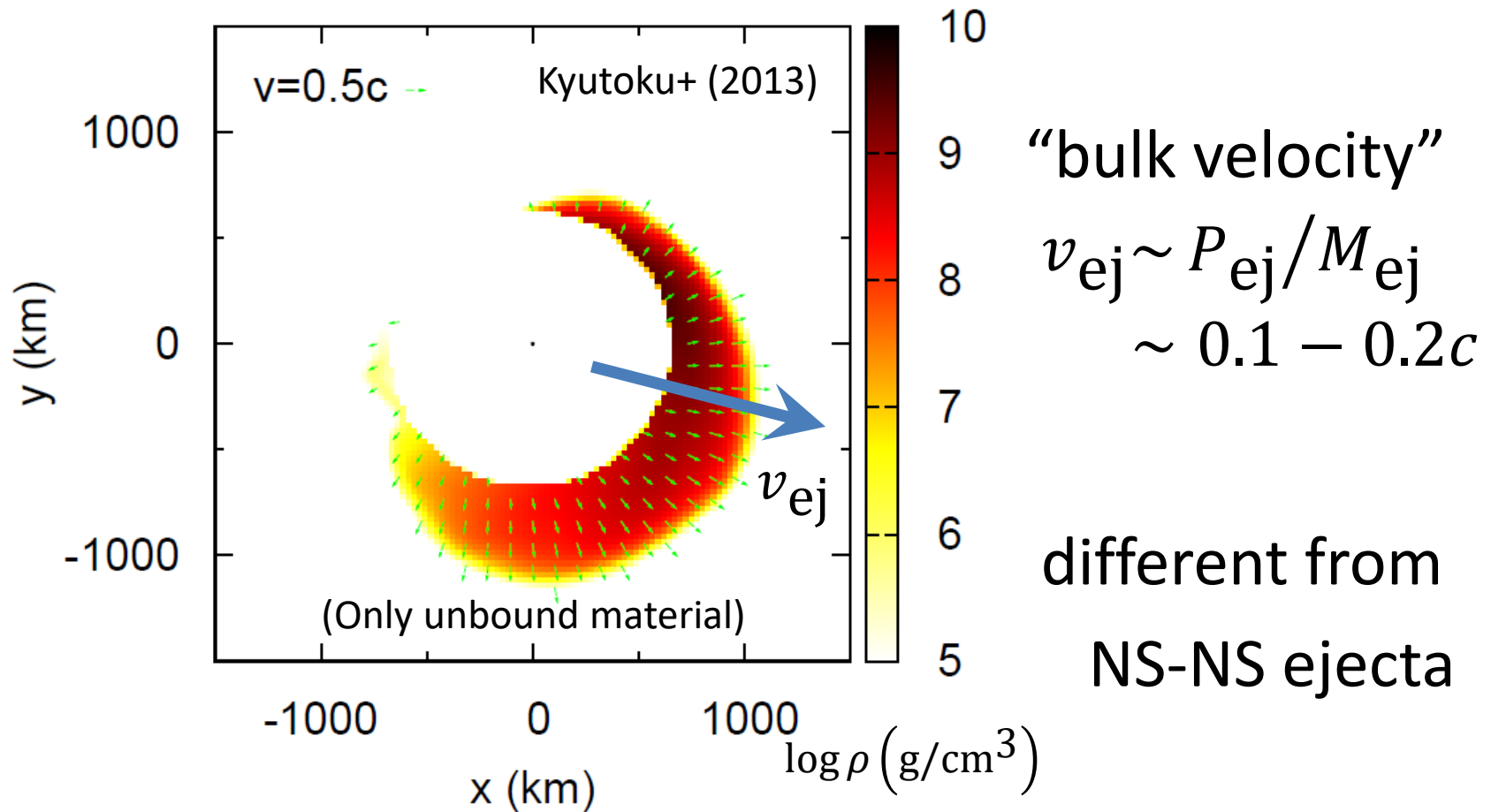
Also tends to increase as the mass ratio increases

-> the ejecta from a large  $Q$  binary is energetic



# Bulk velocity of the ejecta

The ejecta has a bulk linear momentum and velocity



# Kick velocity of the remnant BH

Two kinds of “kick velocity” of the remnant BH

- ejecta kick: large for strong disruption

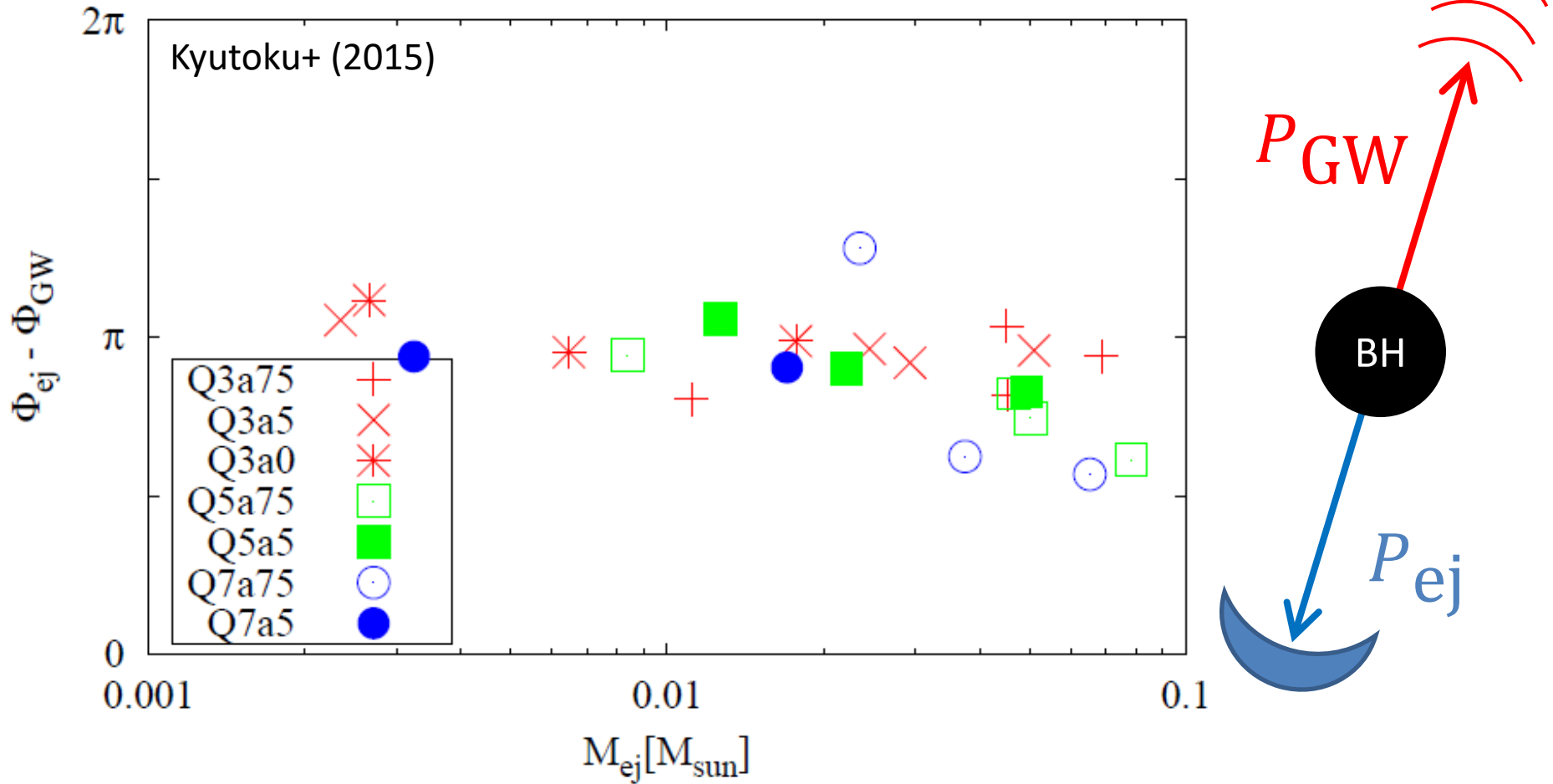
$$V_{ej} \approx \frac{P_{ej}}{M_{remnant}}$$

- gravitational-wave kick: large for weak disruption

$$V_{GW} \approx \frac{P_{GW}}{M_{remnant}}$$

# Anti-correlation of the kick direction

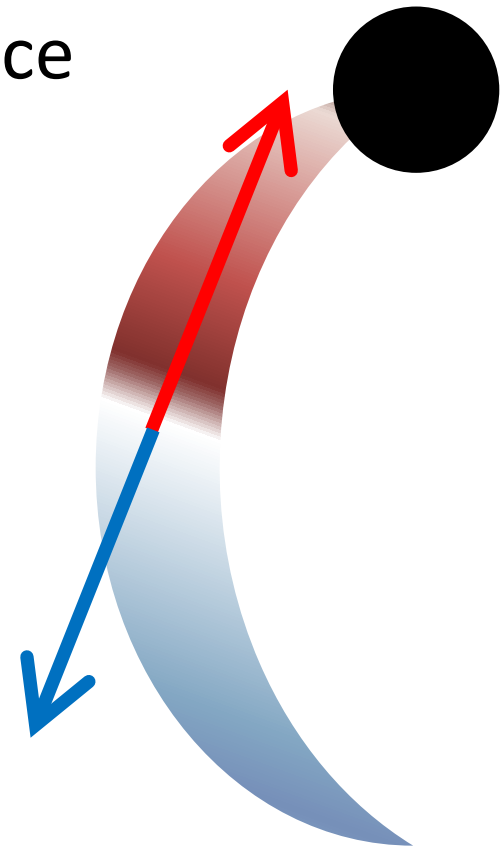
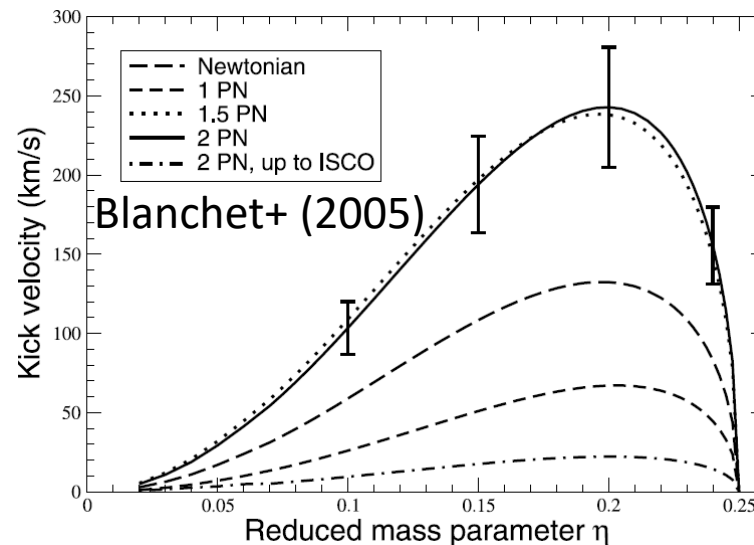
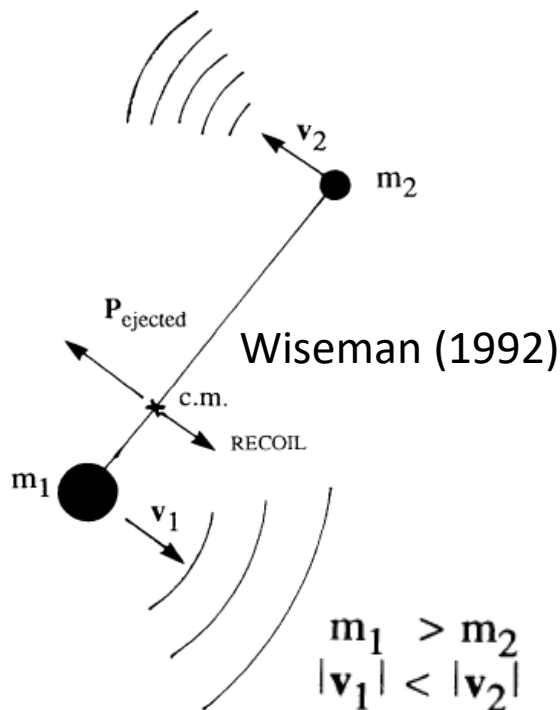
(direction of ejecta) – (direction of GW)  $\approx \pi$



# Possible explanation

Opposite motion of the ejecta  $\leftrightarrow$  plunge material

Plunge motion: fastest in the coalescence  
dominant to the recoil

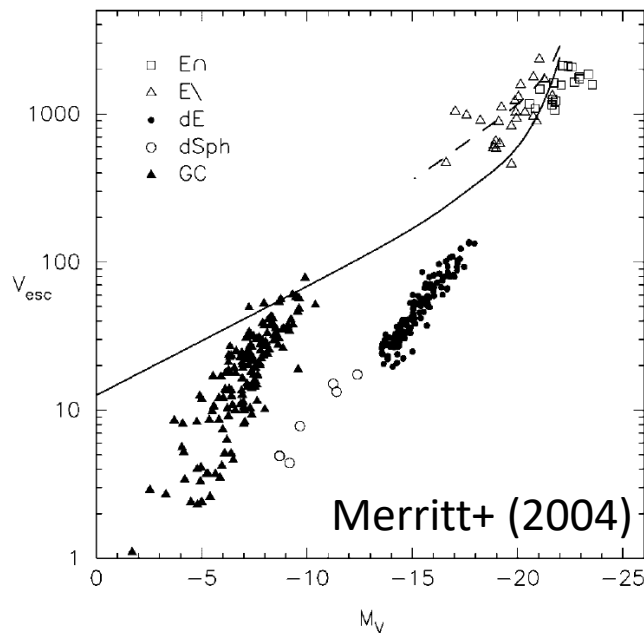


# Which of two kick velocities wins?

Change at  $M_{ej} \approx 0.01M_{\odot}$

The ejecta kick velocity could be as large as  $\sim 1000\text{km/s}$

Escape velocity of galaxies and globular clusters



Kyutoku+ (2015)

Model	$M_{ej}[M_{\odot}]$	$V_{ej} \text{ (km s}^{-1}\text{)}$	$V_{GW} \text{ (km s}^{-1}\text{)}$
APR4-Q3a75	0.01	100	90
ALF2-Q3a75	0.05	500	60
H4-Q3a75	0.05	500	60
MS1-Q3a75	0.07	800	20
APR4-Q3a5	$2 \times 10^{-3}$	20	70
ALF2-Q3a5	0.02	300	70
H4-Q3a5	0.03	300	50
MS1-Q3a5	0.05	600	50
APR4-Q3a0	$2 \times 10^{-5}$	< 1	60
ALF2-Q3a0	$3 \times 10^{-3}$	20	30
H4-Q3a0	$6 \times 10^{-3}$	70	40
MS1-Q3a0	0.02	200	40
APR4-Q5a75	$8 \times 10^{-3}$	30	20
ALF2-Q5a75	0.05	400	40
H4-Q5a75	0.05	400	70
MS1-Q5a75	0.08	700	50
APR4-Q5a5	$9 \times 10^{-5}$	< 1	30
ALF2-Q5a5	0.01	30	30
H4-Q5a5	0.02	200	50
MS1-Q5a5	0.05	400	50
APR4-Q7a75	$5 \times 10^{-4}$	< 1	40
ALF2-Q7a75	0.02	40	30
H4-Q7a75	0.04	200	40
MS1-Q7a75	0.07	400	30
APR4-Q7a5	$3 \times 10^{-6}$	< 1	30
ALF2-Q7a5	$2 \times 10^{-4}$	< 1	30
H4-Q7a5	$3 \times 10^{-3}$	6	20
MS1-Q7a5	0.02	30	20



# Reason of the power-law index 5/3

Rees 1988, Phinney 1989 for SMBH-MS disruption

Orbital period – semimajor axis – binding energy

$$P \propto a^{3/2} \propto |E|^{-3/2}$$

The fallback rate  $\sim$  the period distribution

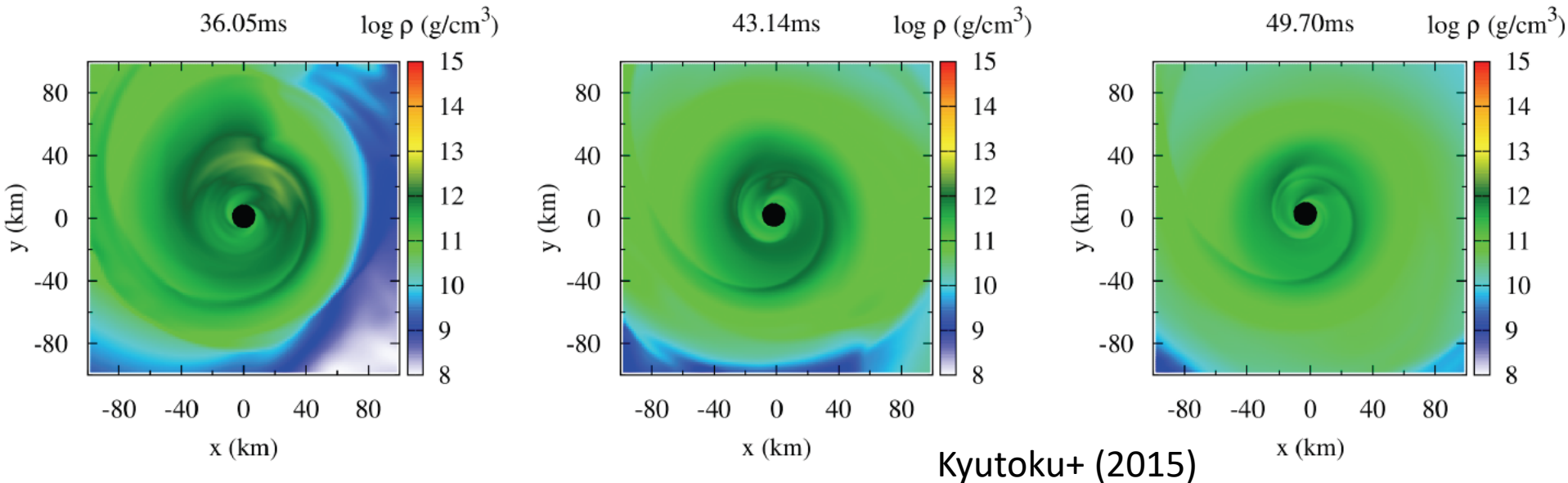
$$\dot{M} = \frac{dM}{dP} = \frac{dM}{dE} \frac{dE}{dP} \propto \frac{dM}{dE} P^{-5/3} = \frac{dM}{dE} t^{-5/3}$$

Why  $dM/dE$  is constant? Not fully understand yet

[e.g., Lodato+ 2009 for SMBH-MS]

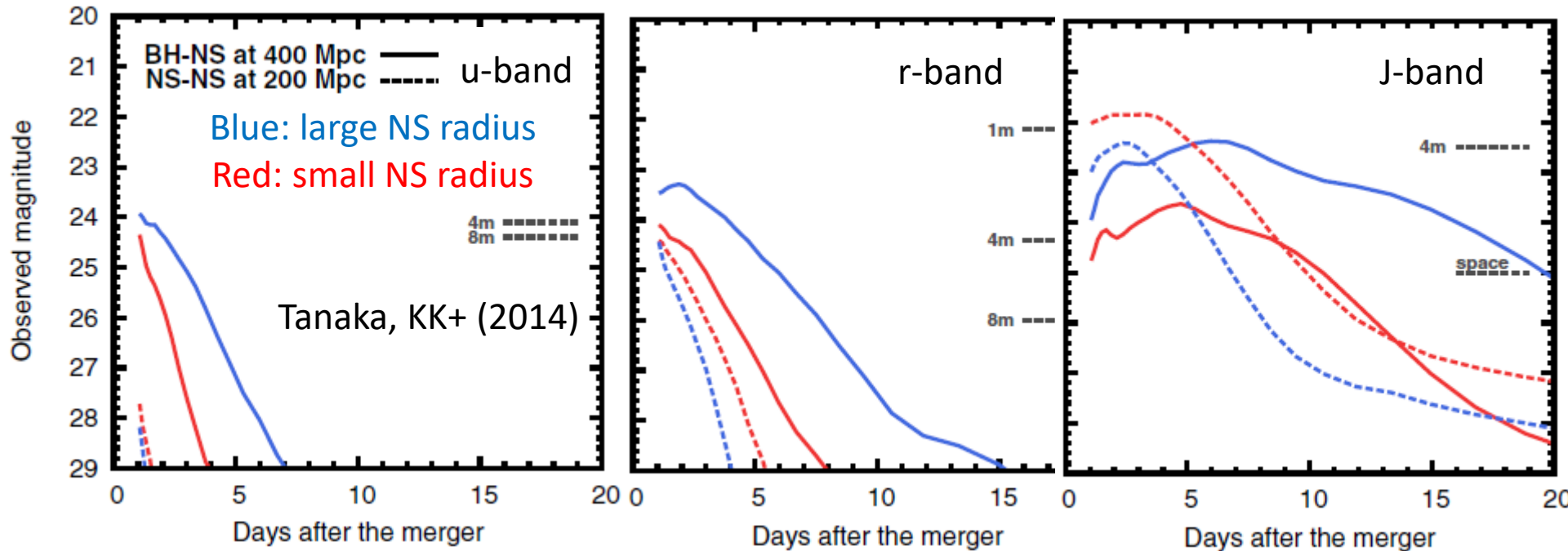
# Standing spiral shock in the disk

Formed as a result of the self-collision of tidal tail  
Drive mass accretion even for the perfect fluid



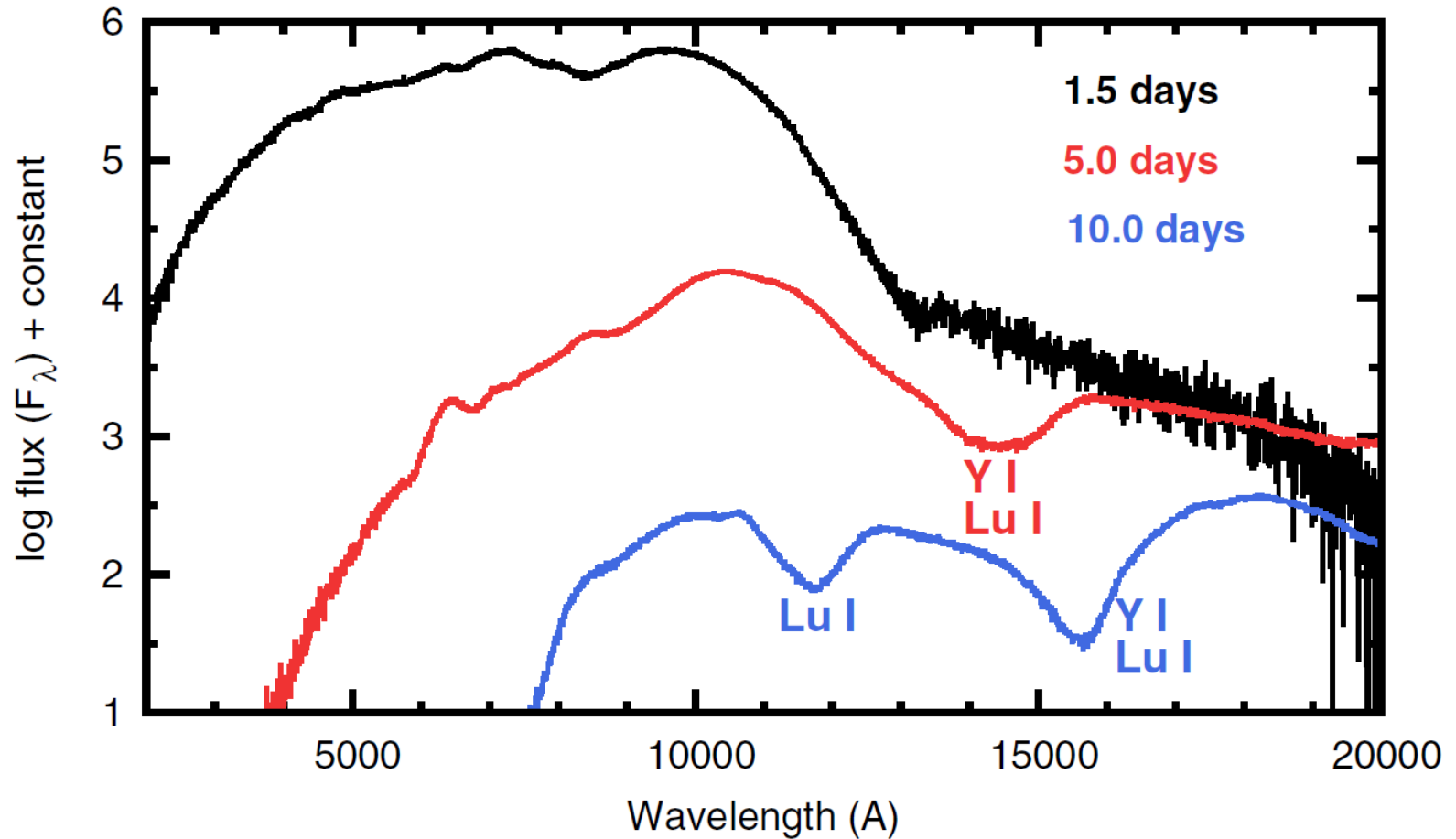
# Macronova/kilonova simulation

Red spectrum with opacity from r-process line lists



# Absence of r-process lines

No line may be found with all the r-process lines...



# Bright macronova/kilonova

For spherical ejecta (Li-Paczynski 1998)

The peak luminosity:  $L_{\text{peak}} \propto f \kappa^{-1/2} M^{1/2} v^{1/2}$

The peak time :  $t_{\text{peak}} \propto \kappa^{1/2} M^{1/2} v^{-1/2}$

Heating efficiency  $f$  and opacity  $\kappa$  – microphysics

important quantities, but are not discussed here

Ejecta mass  $M$  and ejecta velocity  $v$  – NR simulation

large ejecta mass -> bright and long emission

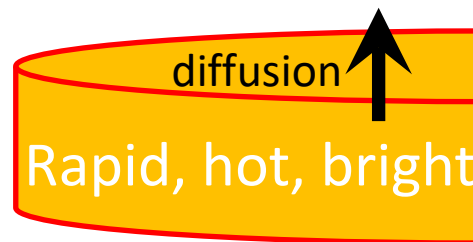
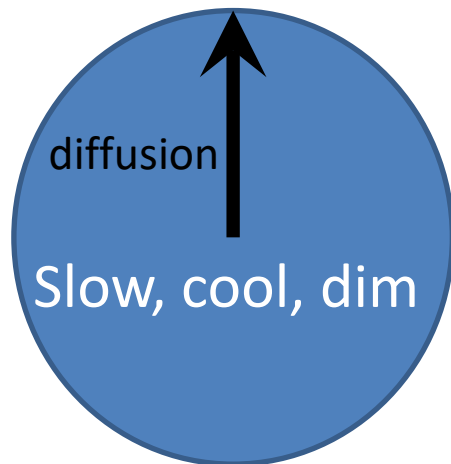
# Effect of anisotropy

Geometry determines the photon-diffusion direction

spherical ejecta

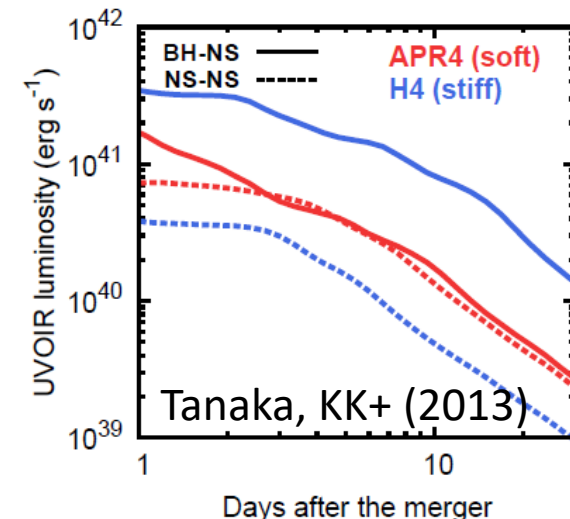
BH-NS crescent-like ejecta

$$\text{aspect ratio: } v_{\parallel}/v_{\perp} \sim 1/\theta_{ej} \sim 5$$



$$\text{NS-NS: } t_{\text{peak},s} \sim \left( 3\kappa M_{ej} / 4\pi c v \right)^{1/2} \sim 8 \text{ day}$$

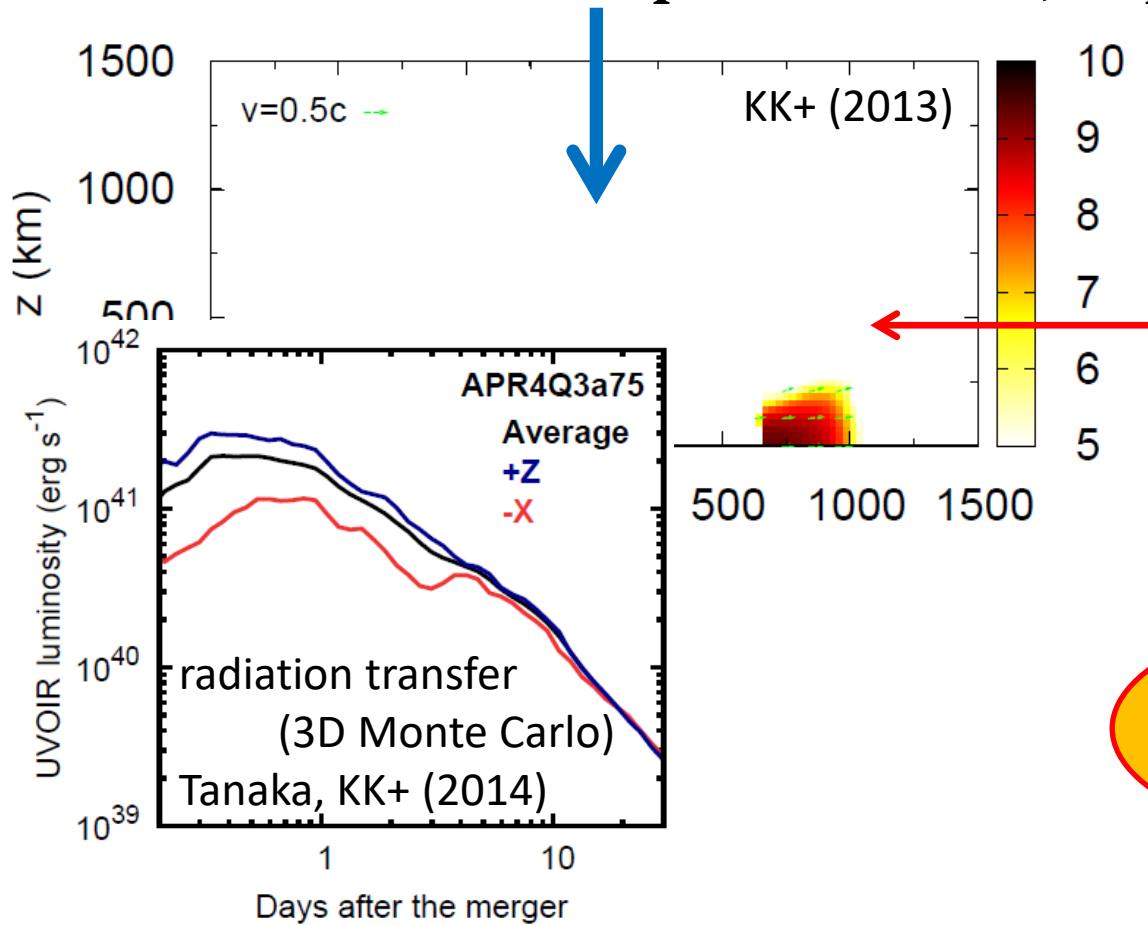
$$\text{BH-NS: } t_{\text{peak}} \sim \left( \kappa M_{ej} \theta_{ej} / c \varphi_{ej} v \right)^{1/2} \sim 4 \text{ day}$$



radiation transfer  
(3D Monte Carlo)

# Viewing-angle dependence

High luminosity  $L_{\text{peak}} \sim f M_{\text{ej}} / t_{\text{peak}} \sim 10^{41}$  erg/s



low luminosity

$$\sim \theta_{\text{ej}} L_{\text{peak}}$$

polarization?



# Synchrotron radio emission

Ejecta decelerate when accumulate  $M_{\text{ej}}$  from ISM

For a spherical ejecta (with  $n_{\text{H}} = 1\text{cm}^3$ )

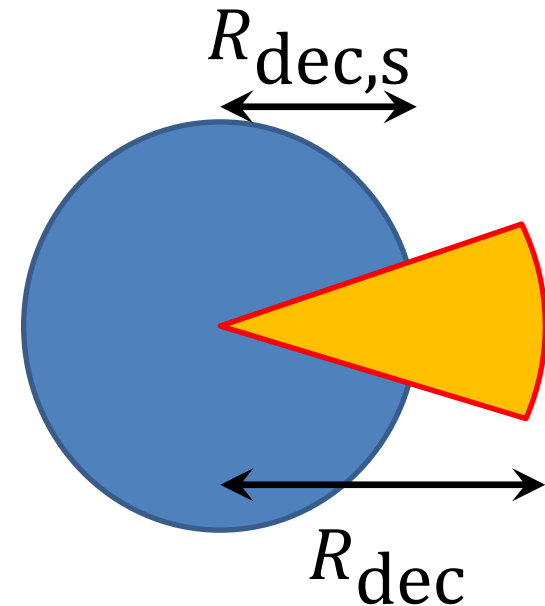
$$R_{\text{dec},s} \sim \left(3M_{\text{ej}}/4\pi m_{\text{p}} n_{\text{H}}\right)^{1/3} \sim 0.7\text{pc}$$

$$t_{\text{dec},s} \sim R_{\text{dec},s}/v \sim 7\text{yr}$$

For crescent-like BH-NS ejecta

$$R_{\text{dec}} \sim 1.7\text{pc} \theta_{\text{ej},1/5}^{-1/3} \varphi_{\text{ej},\pi}^{-1/3}$$

$$t_{\text{dec}} \sim 18\text{yr} \theta_{\text{ej},1/5}^{-1/3} \varphi_{\text{ej},\pi}^{-1/3}$$





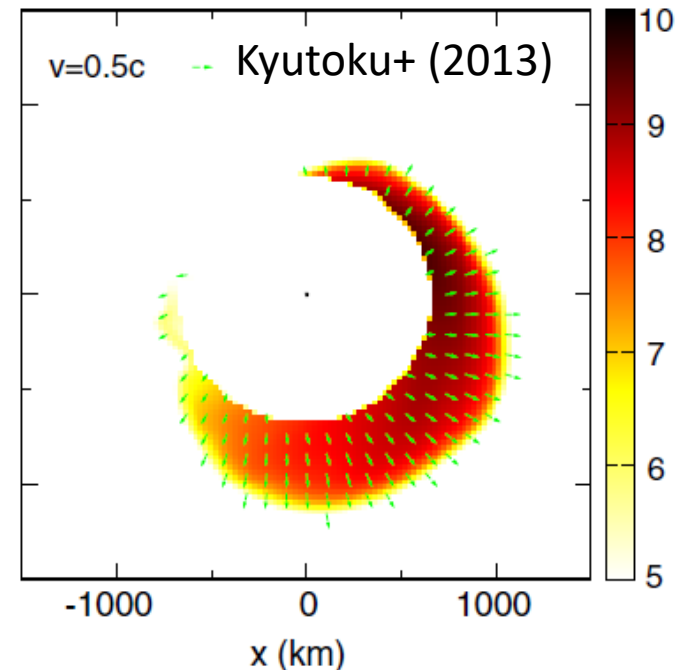
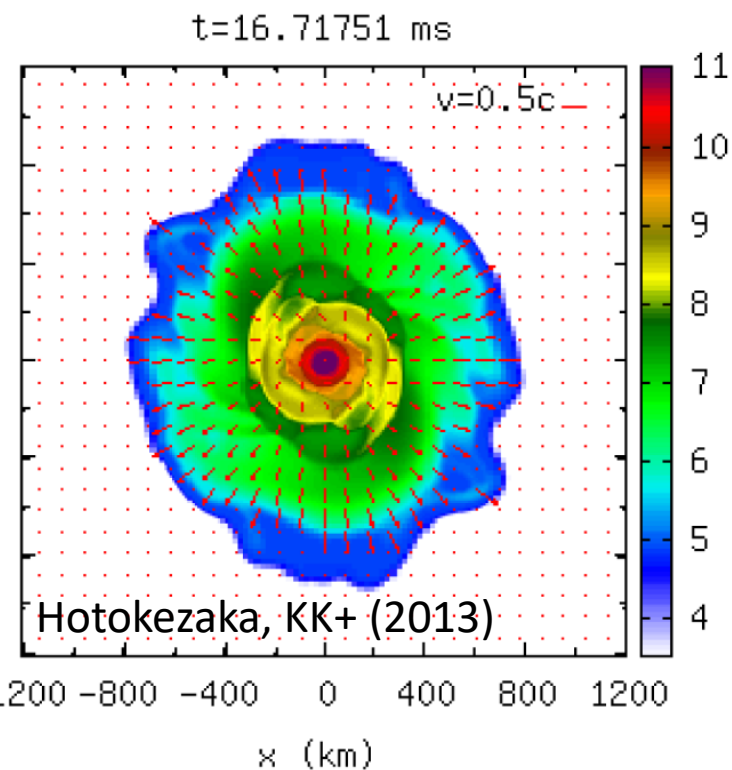
# Proper motion of radio images

Typical proper motion in terms of the angle

$$v_{\text{ej}} t_{\text{dec}} / D \sim 1 \text{pc} / 100 \text{Mpc} \sim 1 \text{mas}$$

resolvable by radio instruments?

both images  
expand in time  
but only BH-NS  
moves in time



# Heating rate

R-process elements decay back to beta-stability

- beta decay: releases about ~90% of energy

  - goes to electron -> totally thermalize the ejecta

  - neutrino -> totally escape

  - gamma-ray -> escape at the relevant epoch**

- (spontaneous) fission: releases about ~10%

  - nearly all the energy thermalize the material

This ratio is determined by detailed microphysics