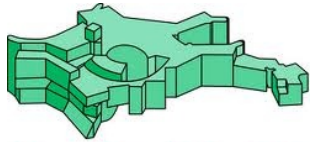


How to form a millisecond magnetar ?

Magnetic field amplification in protoneutron stars



Max-Planck-Institut
für Astrophysik

Jérôme Guilet
(MPA, Garching)



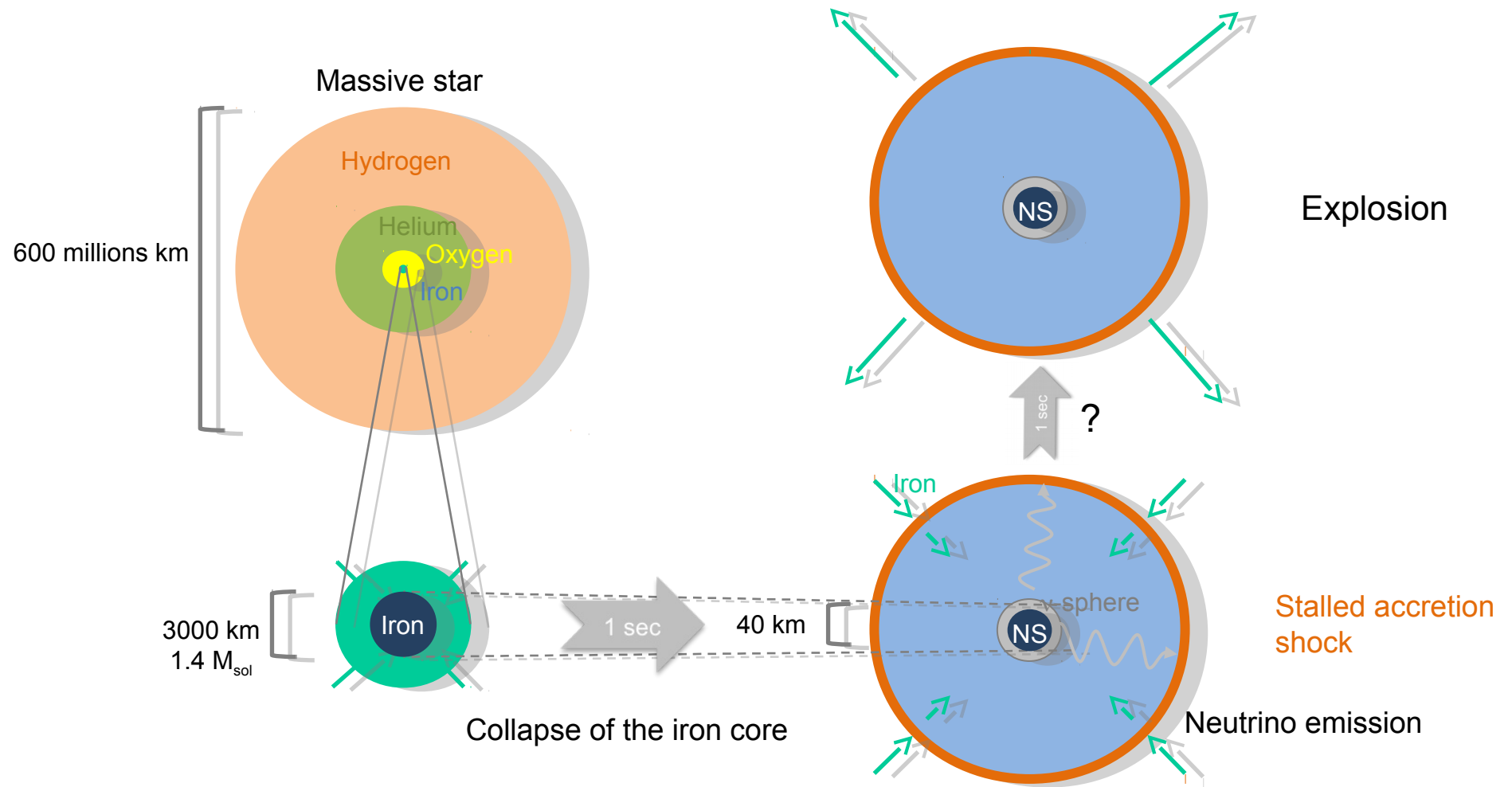
Max-Planck-Princeton Center
for plasma physics

collaborators Ewald Müller, Thomas Janka, Oliver Just (MPA Garching)
 Andreas Bauswein (Heidelberg)
 Tomasz Rembiasz, Martin Obergaulinger, Pablo Cerda-Duran,
 Miguel Angel Alloy (Valencia)

Plan of the talk

1. Introduction : Magnetic fields in core collapse supernovae
2. Can the magnetorotational instability grow ? Linear analysis
 - Effects of neutrino radiation
3. How strong is the final magnetic field ? Numerical simulations
 - Channel mode termination
 - Influence of buoyancy
 - Dependence on the magnetic Prandtl number
 - The dawn of global simulations
4. Conclusion & perspectives

Core collapse: formation of a neutron star

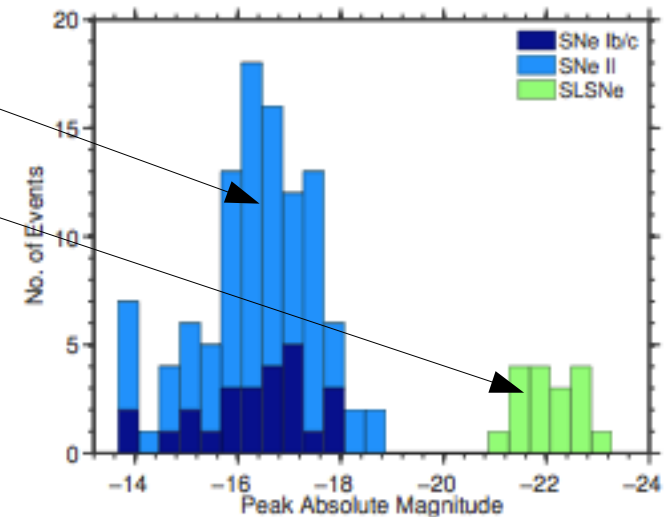


Explosion kinetic energy :

- Typical supernova 10^{51} ergs
- Rare hypernova (& GRB) 10^{52} ergs
- Neutrino driven explosions ?
e.g. Bruenn+14, Melson+15
- **Millisecond magnetar ?**
e.g. Burrows+07, Takiwaki+09,11
Bucciantini+09, Metzger+11

Total luminosity :

- Typical supernova 10^{49} ergs
- Superluminous supernovae 10^{51} ergs
- **Millisecond magnetar ?**
e.g. Woosley+10, Dessart+12,
Nicholl+13, Inserra+13



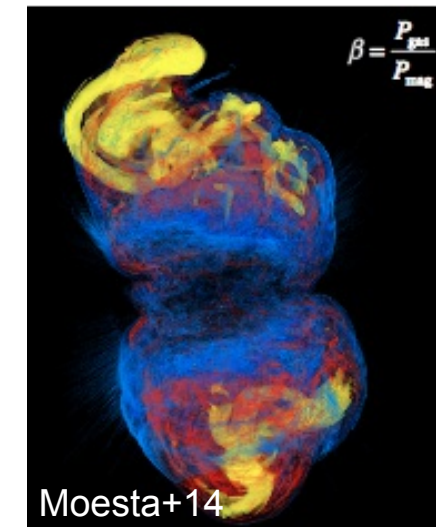
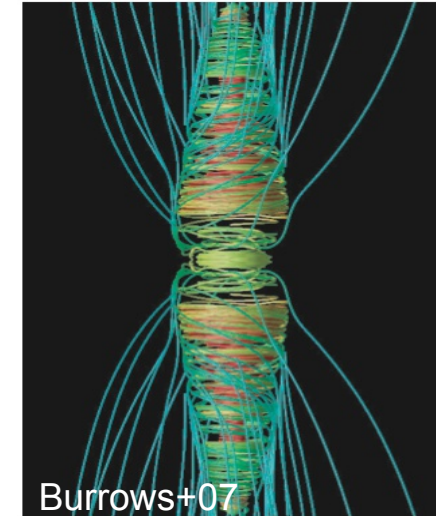
Strong magnetic field: $B \sim 10^{15}$ G
 + fast rotation (period of few milliseconds)

=> powerful jet-driven explosions !

e.g. Sibata+06, Burrows+07, Dessart+08,
 Takiwaki+09,11, Winteler+12

But in 3D, jets can be unstable to kink instability
 Moesta+2014

Open question:
 Can magnetic explosions explain hypernovae ?



Are millisecond magnetars powering superluminous supernovae ?

Delayed energy injection by magnetar spin-down on timescale of weeks-months

=> very high luminosity

Light curves can be fitted by:

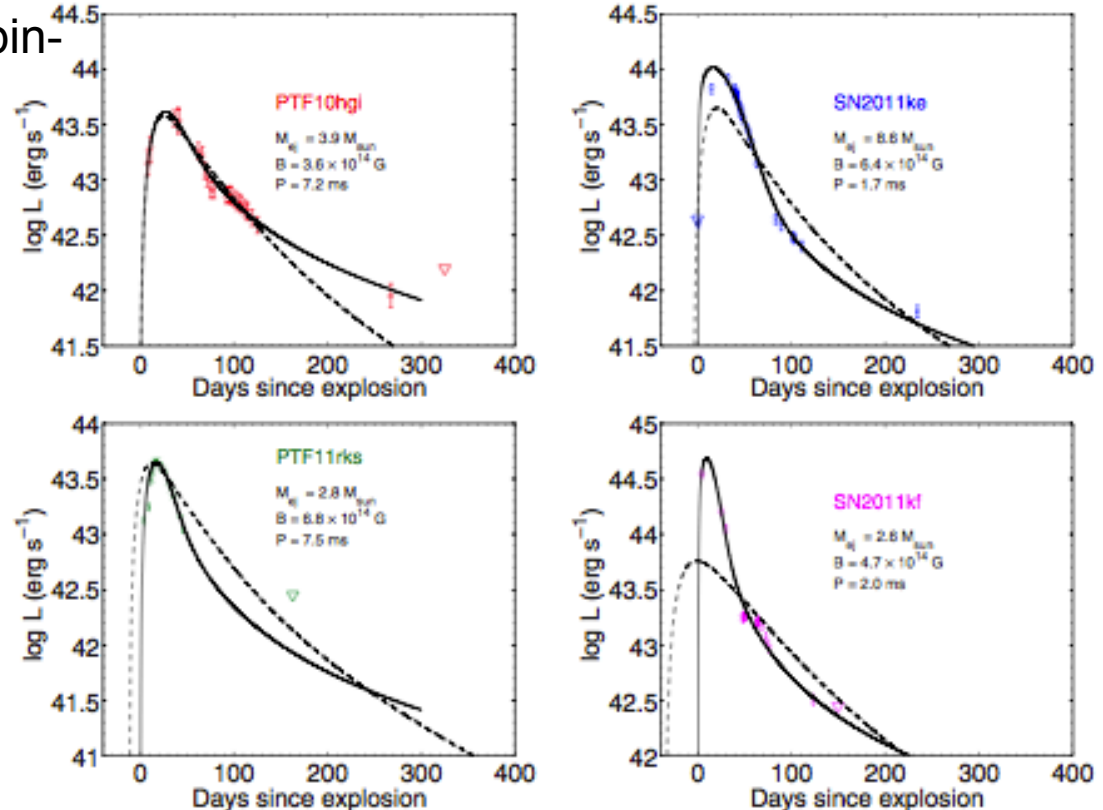
- strong dipole magnetic field:

$$B \sim 10^{14}\text{-}10^{15} \text{ G}$$

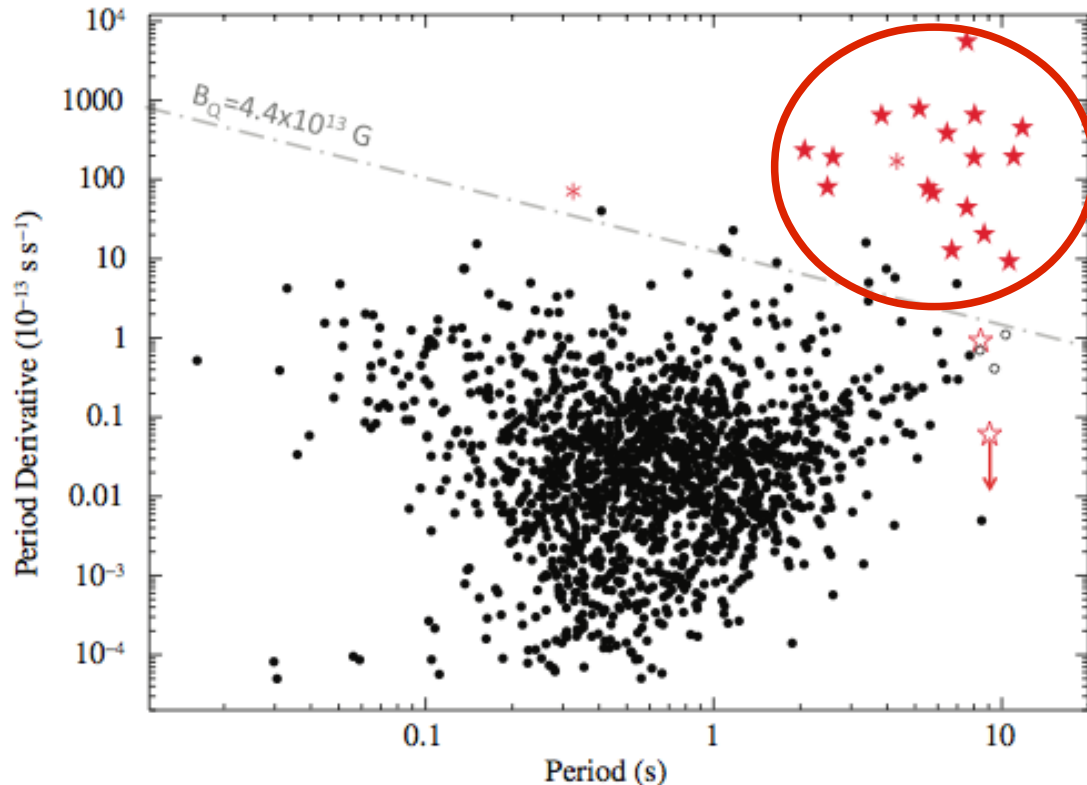
- fast rotation:

$$P \sim 1\text{-}10 \text{ ms}$$

Talk by Ken Chen last week



Inserra+2013



Magnetars:

Anomalous X-ray pulsars (AXP)

Soft gamma repeater (SGR)

Strong dipole magnetic field:

$$B \sim 10^{14}\text{-}10^{15} \text{ G}$$

Slow rotation:

$$P \sim 1\text{-}10 \text{ s}$$

Typical age:

$$10^4\text{-}10^5 \text{ years}$$

Talks by Michael Gabler & Pablo Cerda-Duran

Rotation at birth unknown: were some or all of them born as millisecond magnetars ?



Huge range of magnetic field strength :

- Initially « weak » magnetic field : $\lesssim 10^9 \text{ G} \text{ (?)}$
- After compression by the core-collapse: $\lesssim 10^{12} - 10^{13} \text{ G} \text{ (?)}$
- Magnetar strength : $\sim 10^{15} \text{ G}$

Amplification mechanism ?

Magnetorotational instability (MRI) ?

Similar to accretion disks

- application to protoneutron stars

Convective dynamo ?

Similar to solar & planetary dynamos

- need of numerical simulations for neutron stars

In ideal MHD (i.e. no resistivity or viscosity) :

Condition for MRI growth $\frac{d\Omega}{dr} < 0$

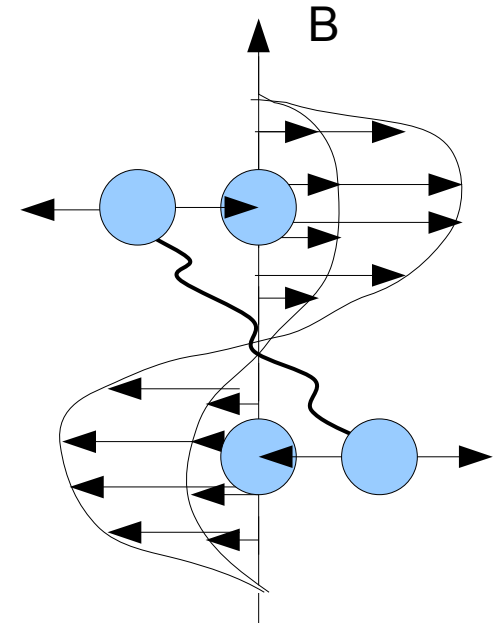
Growth rate : $\sigma = \frac{q}{2}\Omega$

with $\Omega \propto r^{-q}$

→ Fast growth for fast rotation

Wavelength : $\lambda \propto \frac{B}{\sqrt{\rho\Omega}}$

→ Short wavelength for weak magnetic field

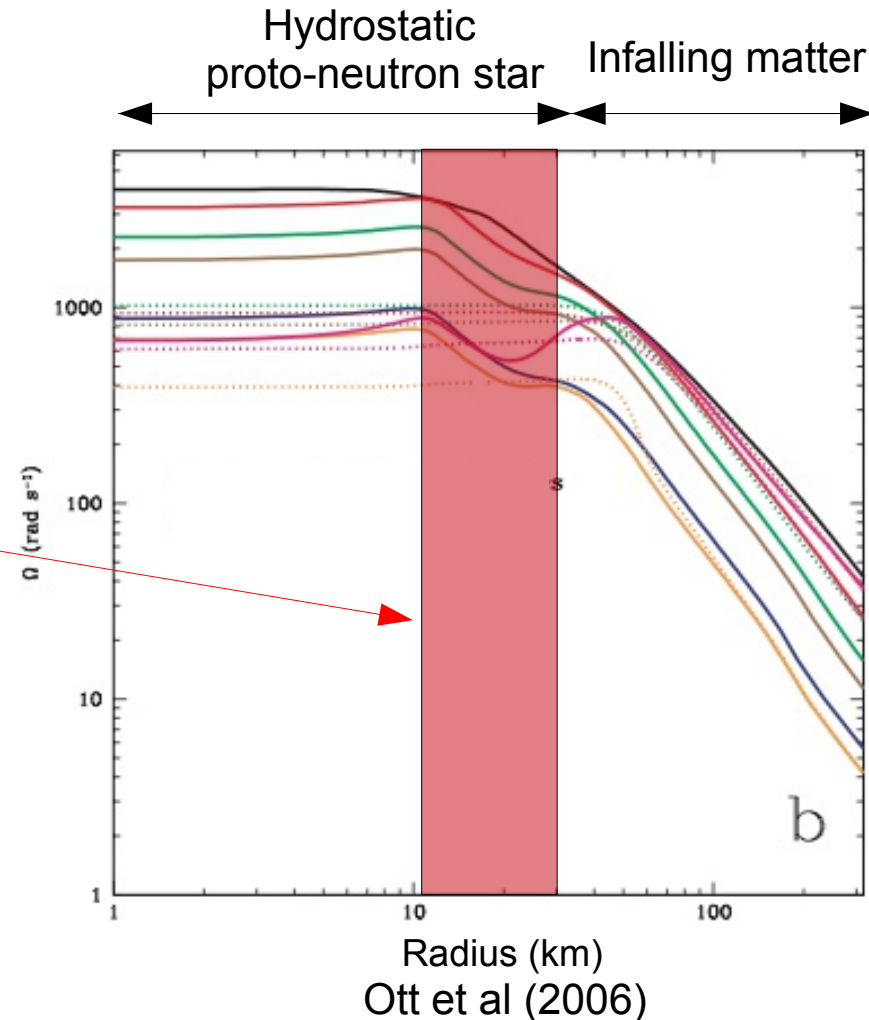


Rotation frequency profile :
 → Differential rotation at radii > 10 km

Rotation frequency decreases with
 radius : => **MRI unstable !**

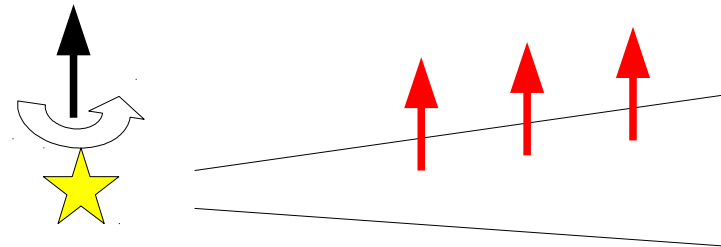
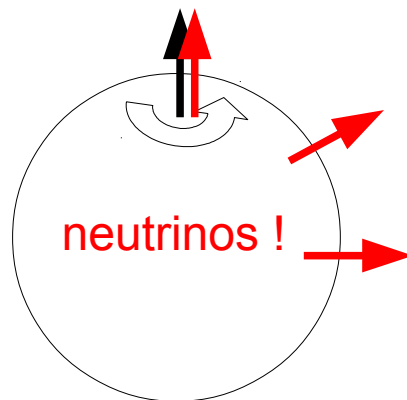
Akiyama et al (2003)

Obergaulinger et al (2009)



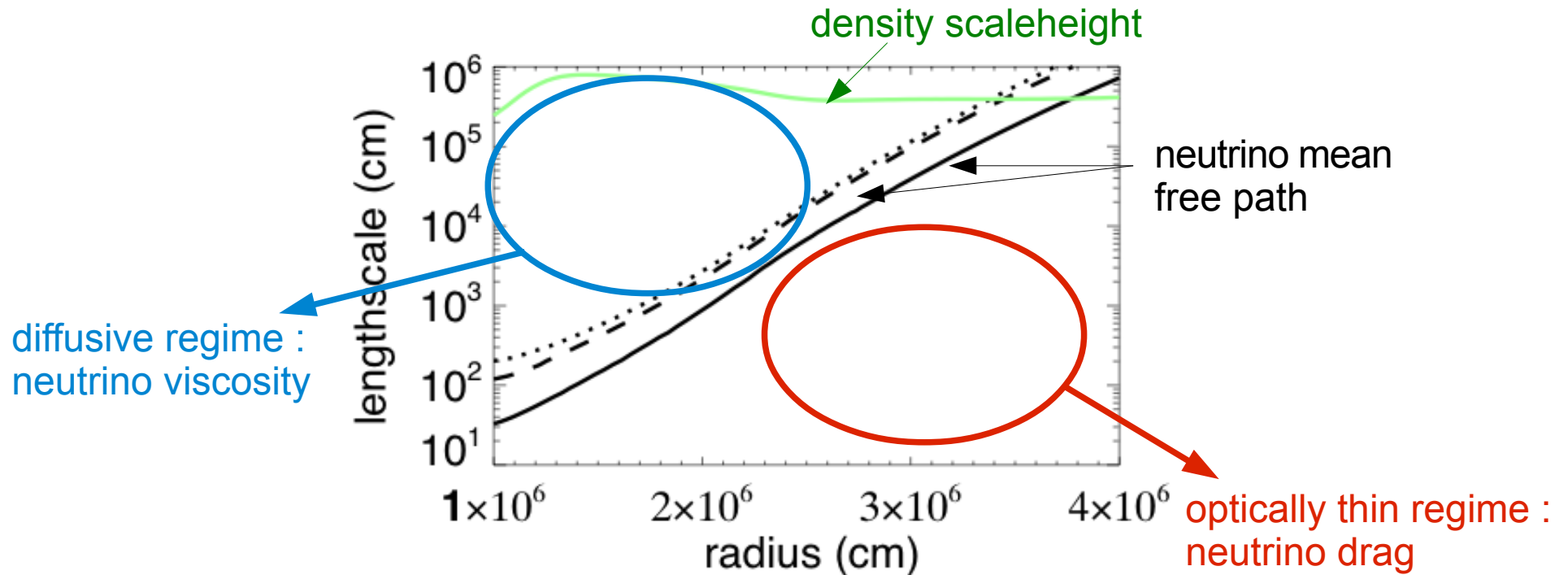
Main differences between proto-neutron stars and accretion disks:

- Neutrinos: viscosity and drag
 - Prevent MRI growth ?
- Buoyancy: radial entropy and composition gradients
 - Impact on magnetic field amplification by MRI ?
- Geometry: spherical vs thin disk
 - Help global coherence ?

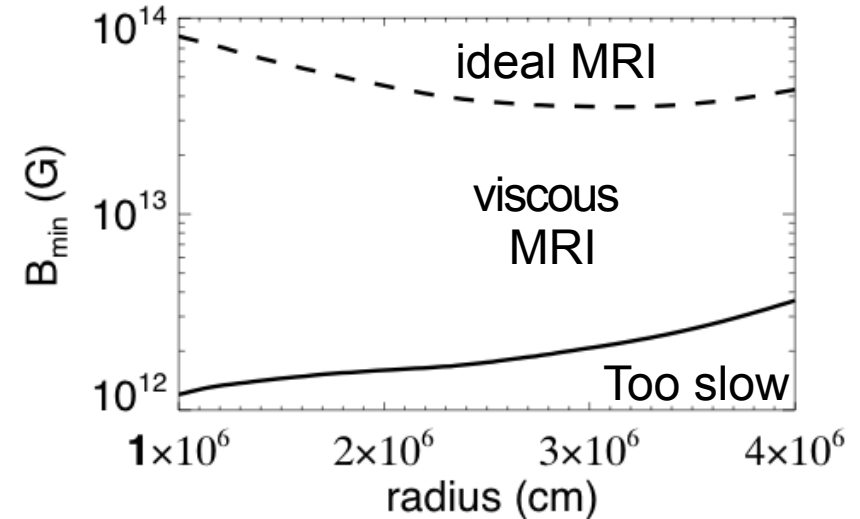
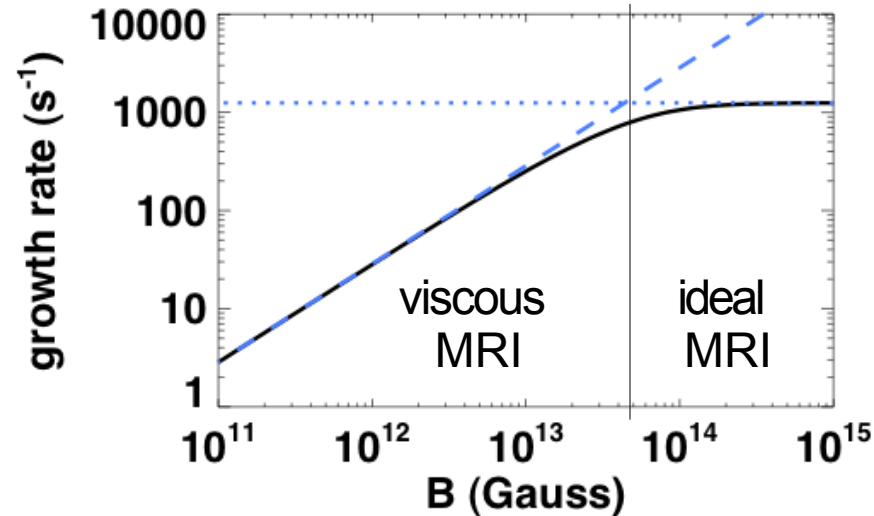


2. Can the magnetorotational instability (MRI) grow ?

Effects of neutrino radiation

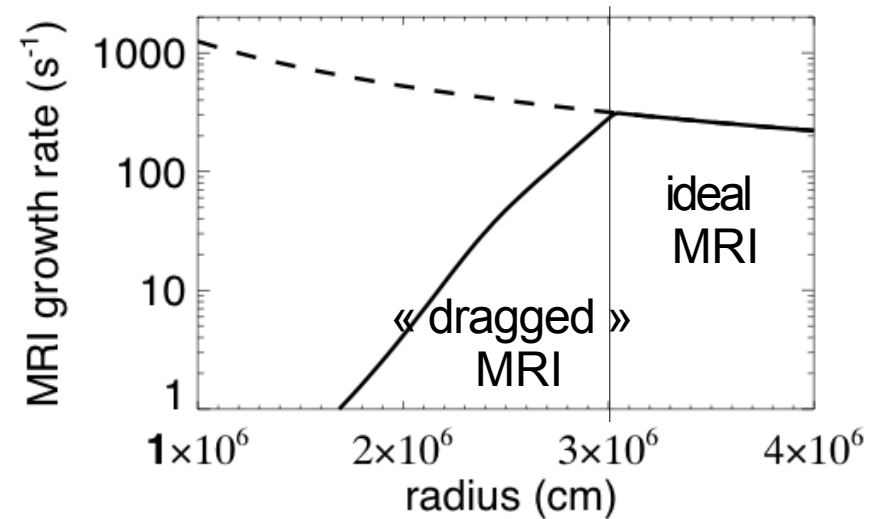
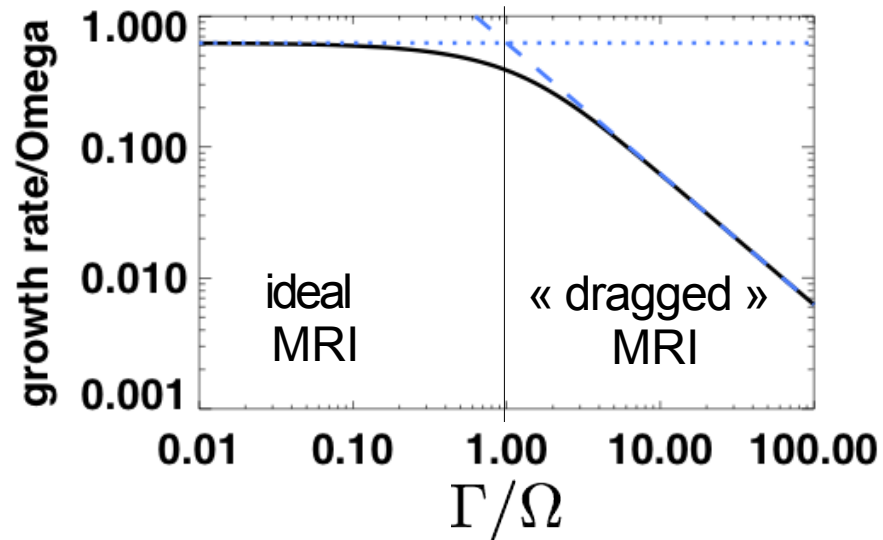


Neutron star structure from a simulation by Hanke et al (2013)



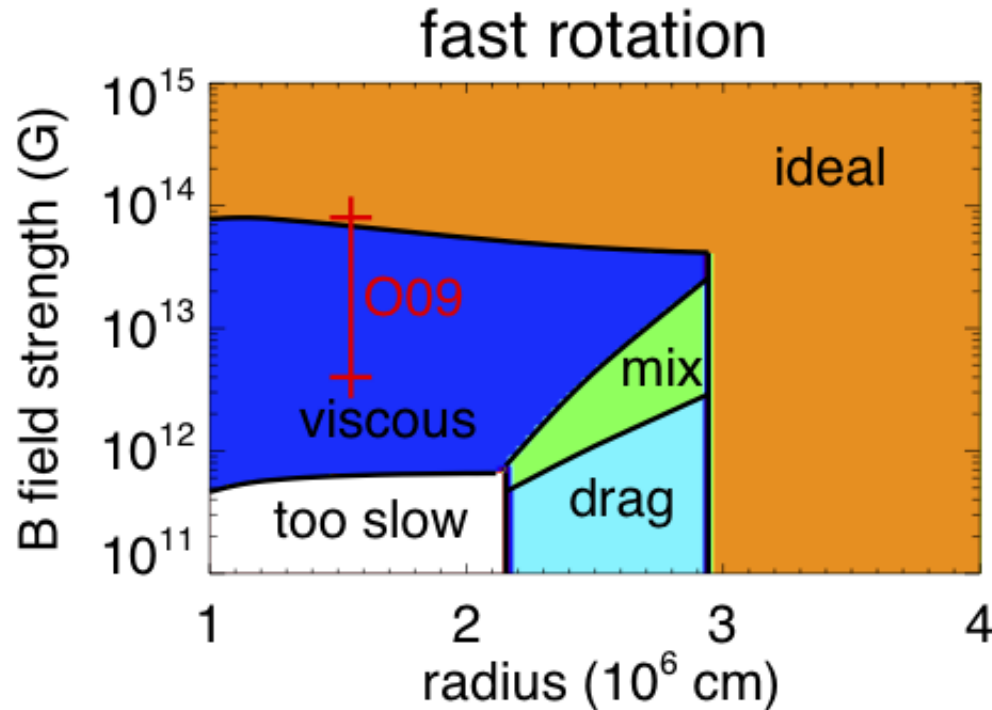
Dimensionless number : $E_\nu \equiv \frac{v_A^2}{\nu\Omega} \sim 0.02 \left(\frac{B}{10^{13} \text{ G}} \right)^2 \left(\frac{\rho}{10^{13} \text{ g.cm}^{-3}} \right)^{-1} \left(\frac{\Omega}{2000 \text{ s}^{-1}} \right)^{-1} \left(\frac{\nu}{2 \times 10^{10} \text{ cm}^2.\text{s}^{-1}} \right)^{-1}$
 e.g. Pessah & Chan (2008)

MRI growth requires a minimum initial magnetic field strength of $> 10^{12}$ G...

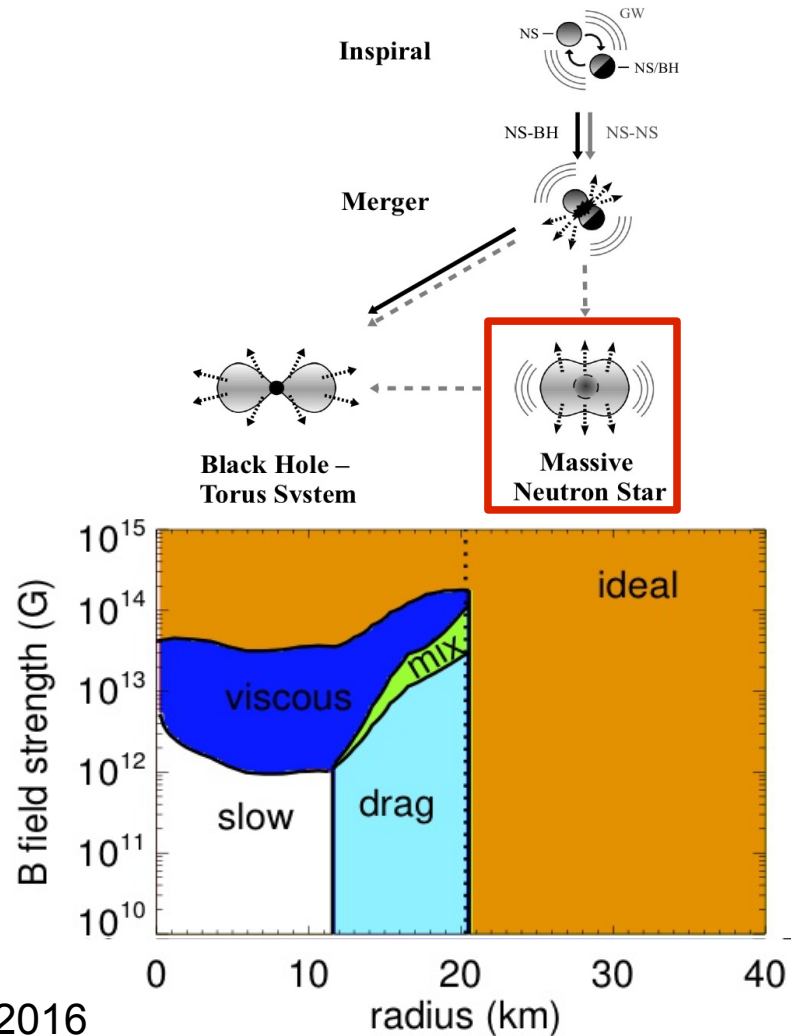


Neutrino drag : $-\Gamma \mathbf{v}$, with damping rate : $\Gamma = \frac{4}{3} \frac{E_\nu}{l_\nu \rho c}$

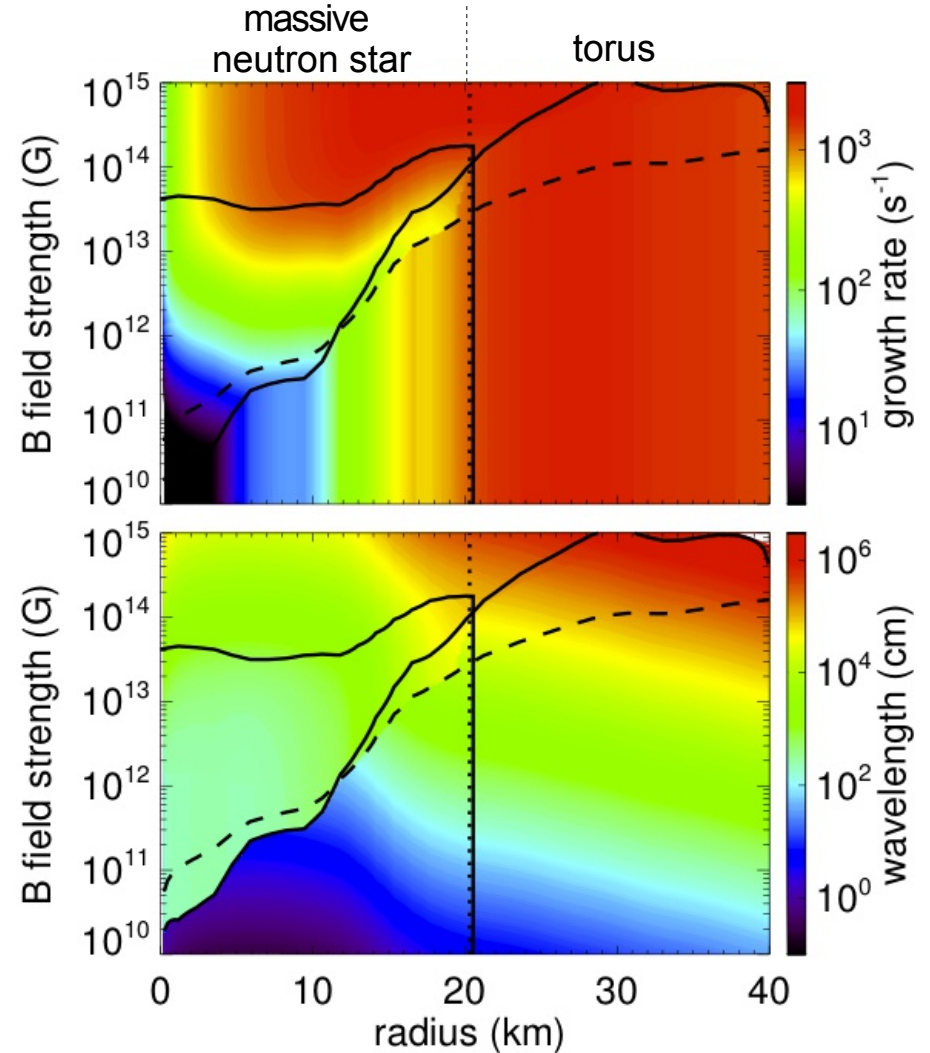
The MRI can grow near the PNS surface from any weak field strength !



Guilet et al (2015)



Guilet+2016



3. How strong is the final magnetic field ?

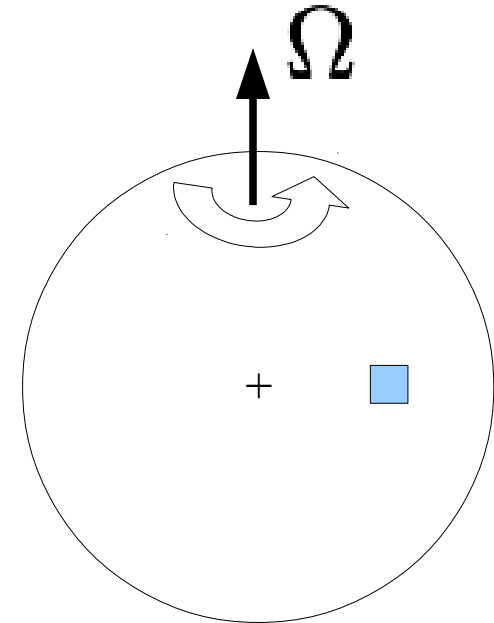
→ Channel mode termination

→ Influence of buoyancy

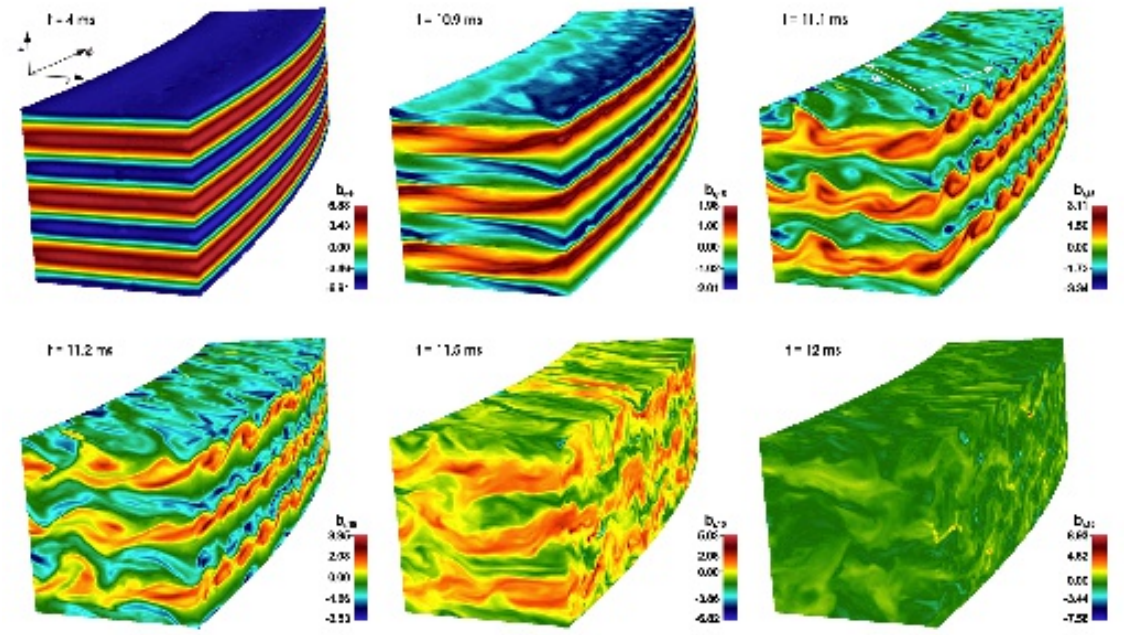
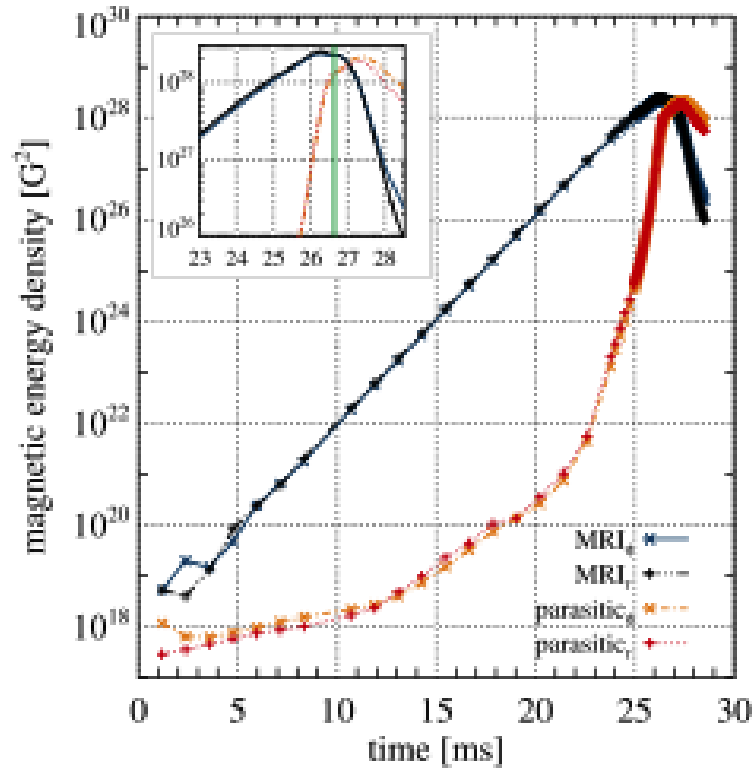
→ Dependence on the magnetic Prandtl number

→ The dawn of global simulations

- Small box : ~km size at a radius $r \sim 20\text{-}40$ km
- Differential rotation
=> shearing periodic boundary conditions
- Entropy/composition gradients
- Different numerical methods : spectral or finite volume
- Fully compressible or quasi-incompressible approximation



Obergaulinger+2009, Masada+2012,
Guilet+2015, Rembiasz+2016a,b



Rembiasz et al. 2016a&b

3. How strong is the final magnetic field ?

→ Channel mode termination

→ **Influence of buoyancy**

→ Dependence on the magnetic Prandtl number

→ The dawn of global simulations

Buoyancy from entropy and lepton fraction gradients

Brünt-Väisälä frequency :

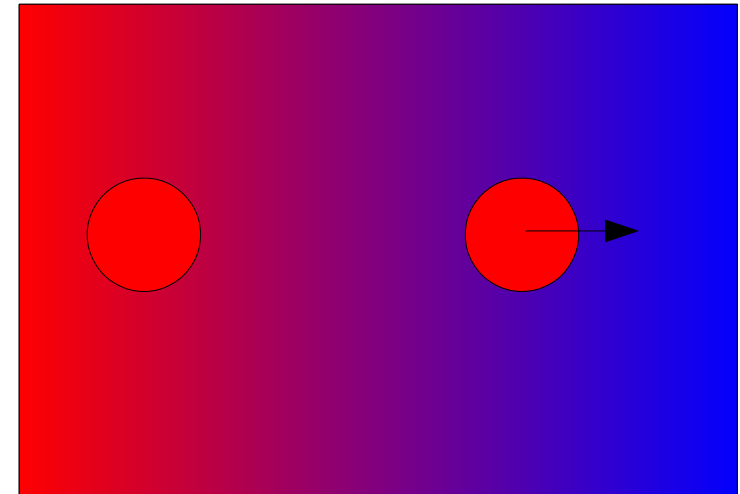
$$N^2 \equiv -\frac{g}{\rho} \left[\frac{\partial \rho}{\partial S} \Big|_{P, Y_e} \frac{dS}{dr} + \frac{\partial \rho}{\partial Y_e} \Big|_{P, S} \frac{dY_e}{dr} \right]$$

Linear analysis of MRI with buoyancy :

stable buoyancy can stabilise the MRI

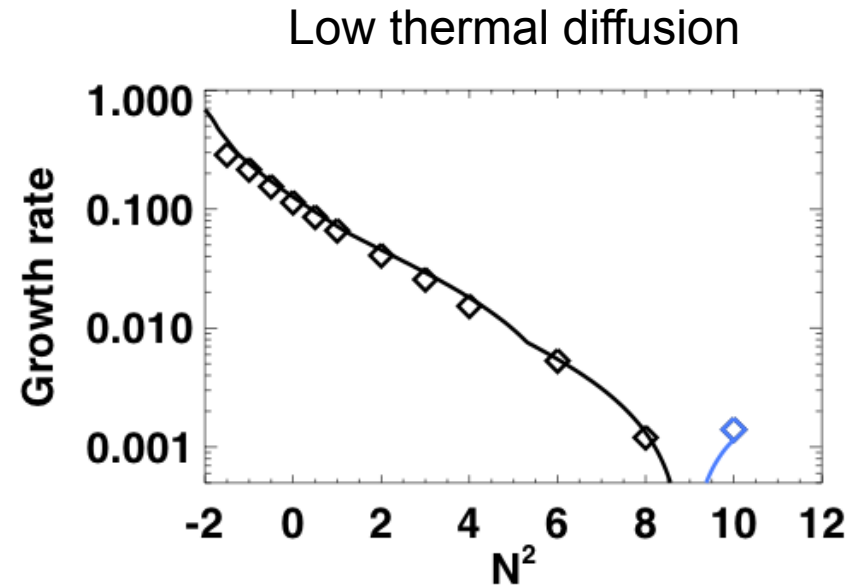
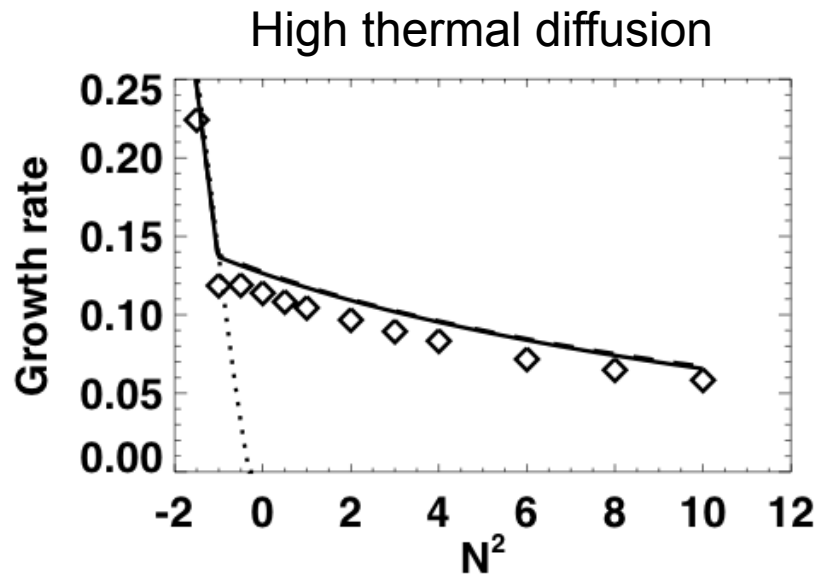
But : thermal diffusion allows the growth

Balbus & Hawley (1994), Menou et al (2003),
Masada et al (2007)



$$N^2 \gtrsim 0$$

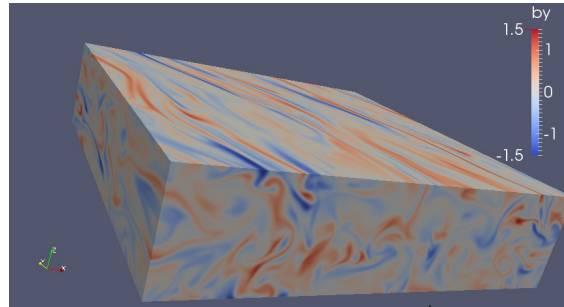
radial displacement suppressed



Confirms linear analysis :

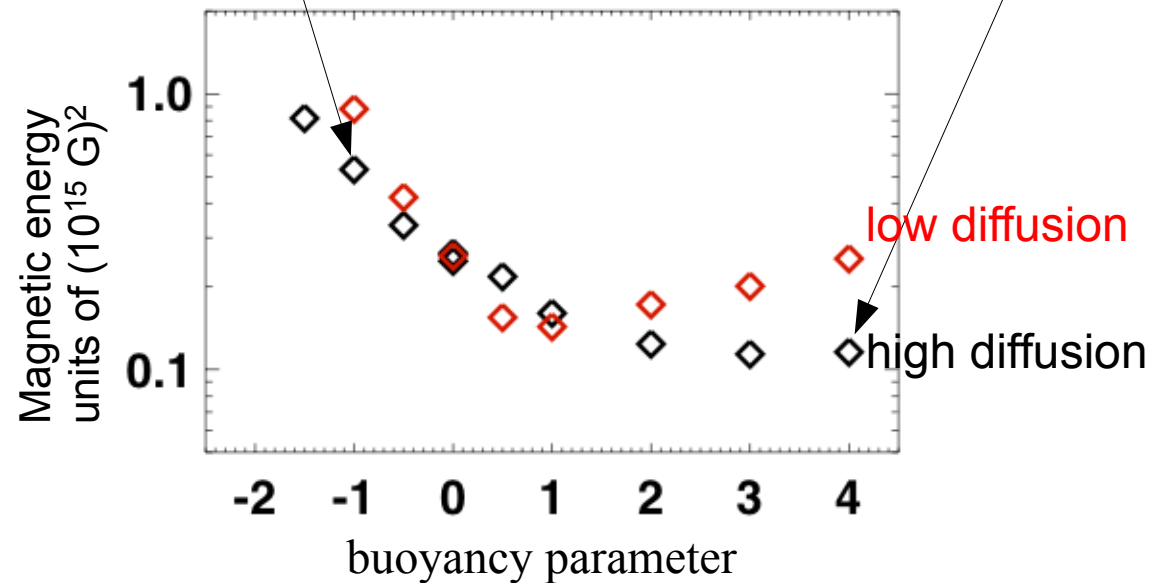
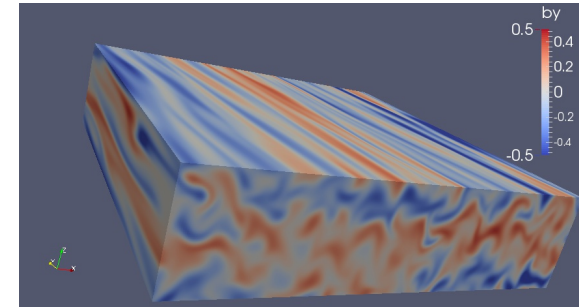
thermal diffusion by neutrinos allows fast MRI growth

unstable buoyancy



color: azimuthal
magnetic field

stable stratification



Guilet & Müller (2015)

3. How strong is the final magnetic field ?

→ Channel mode termination

→ Influence of buoyancy

→ Dependence on the magnetic Prandtl number

→ The dawn of global simulations

Neutrino viscosity : $\nu \sim 10^{10} \text{ cm}^2 \cdot \text{s}^{-1}$

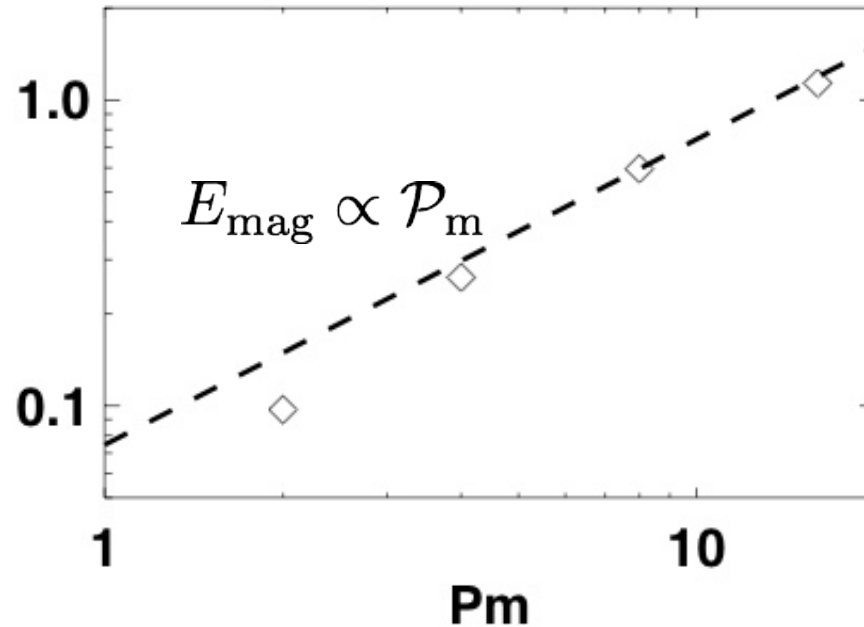
Resistivity : $\eta \sim 10^{-3} \text{ cm}^2 \cdot \text{s}^{-1}$

Magnetic Prandtl number : $\mathcal{P}_m \equiv \frac{\nu}{\eta} \simeq 10^{13}$

Previous simulations used : $\mathcal{P}_m = 4$

Behaviour at very large magnetic Prandtl number ?

Magnetic energy
units of $(10^{15} \text{ G})^2$



Behaviour at very large magnetic Prandtl number ?

3. How strong is the final magnetic field ?

→ Channel mode termination

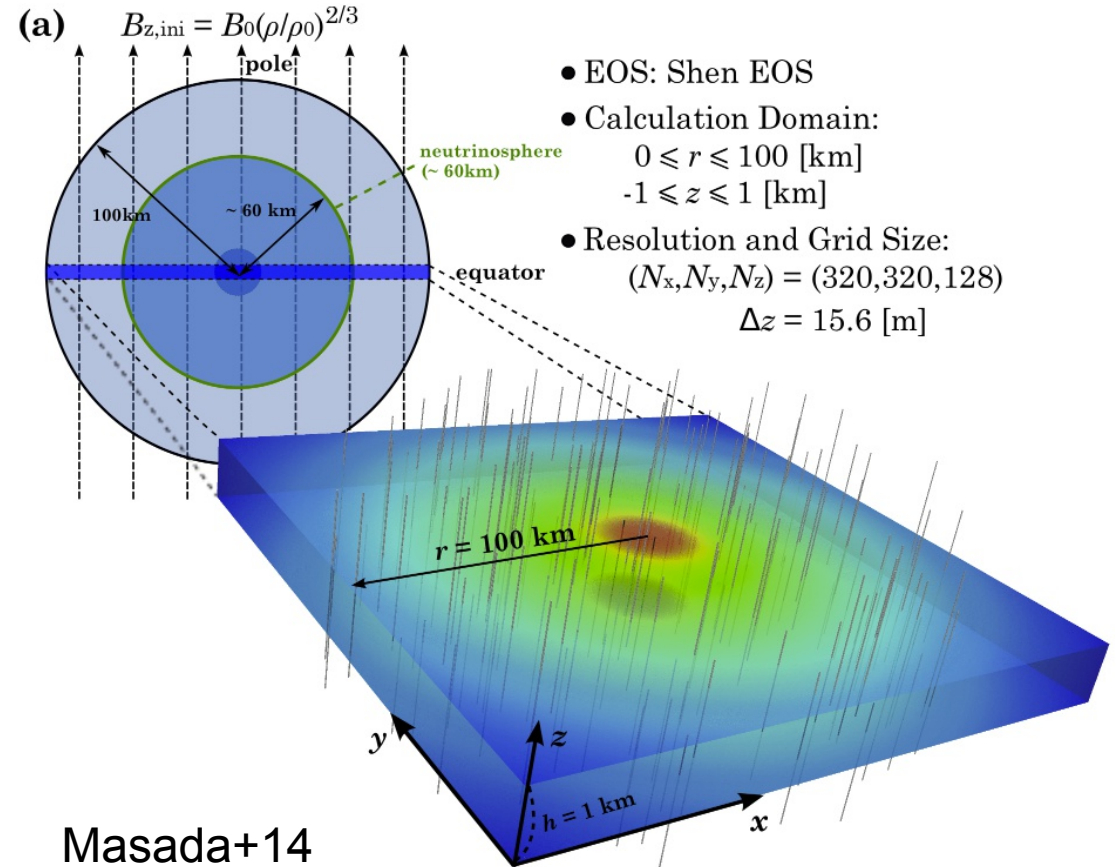
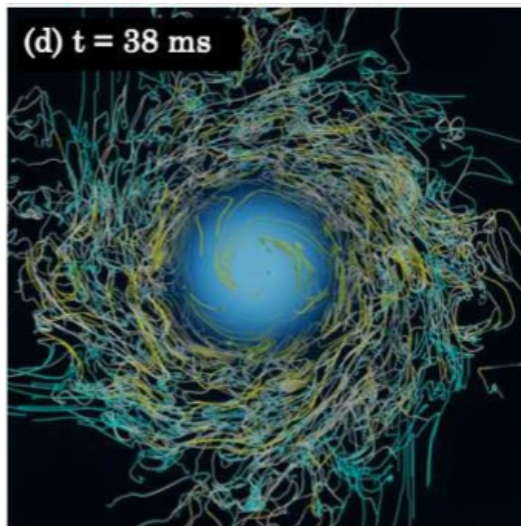
→ Influence of buoyancy

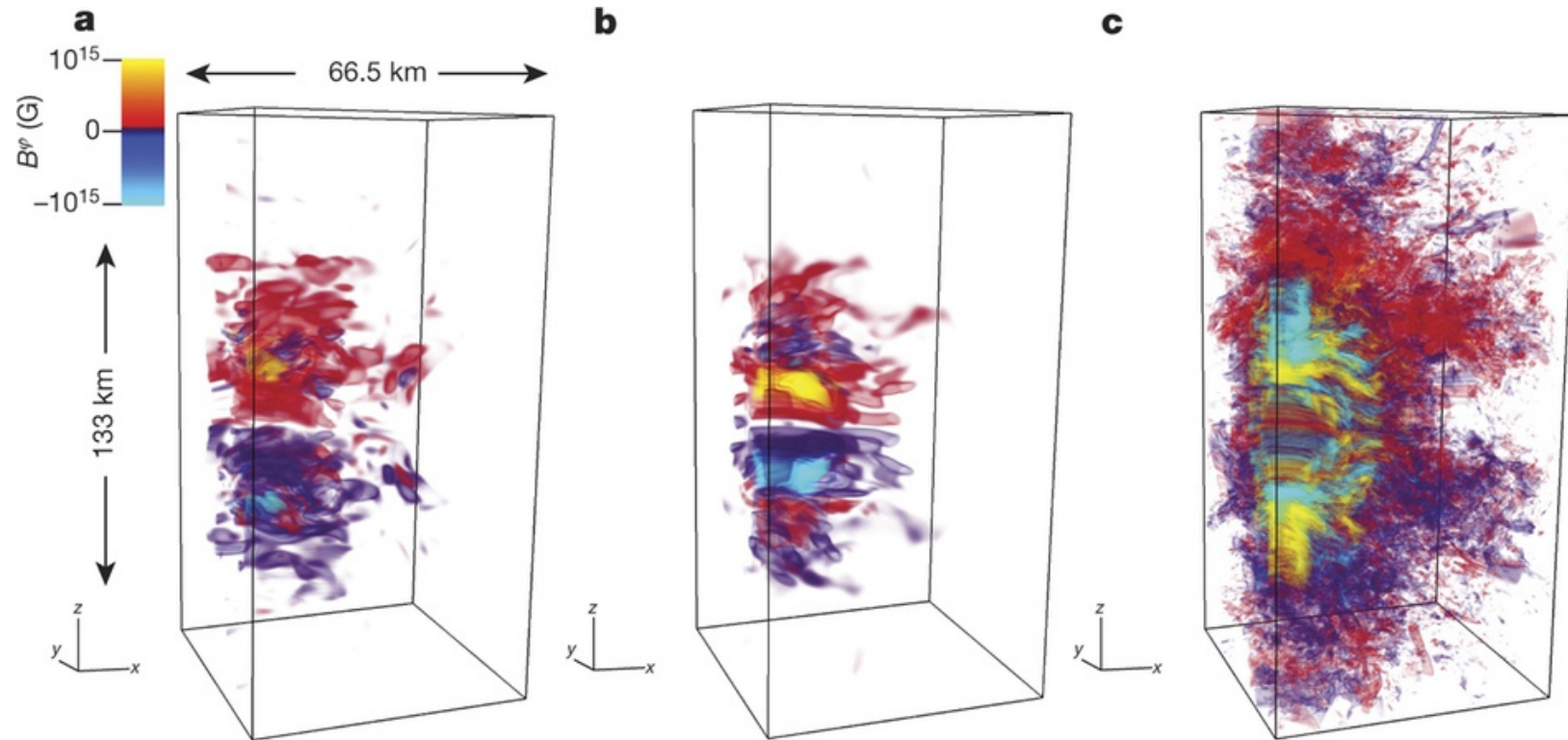
→ Dependence on the magnetic Prandtl number

→ The dawn of global simulations

Local in vertical direction
global in horizontal direction

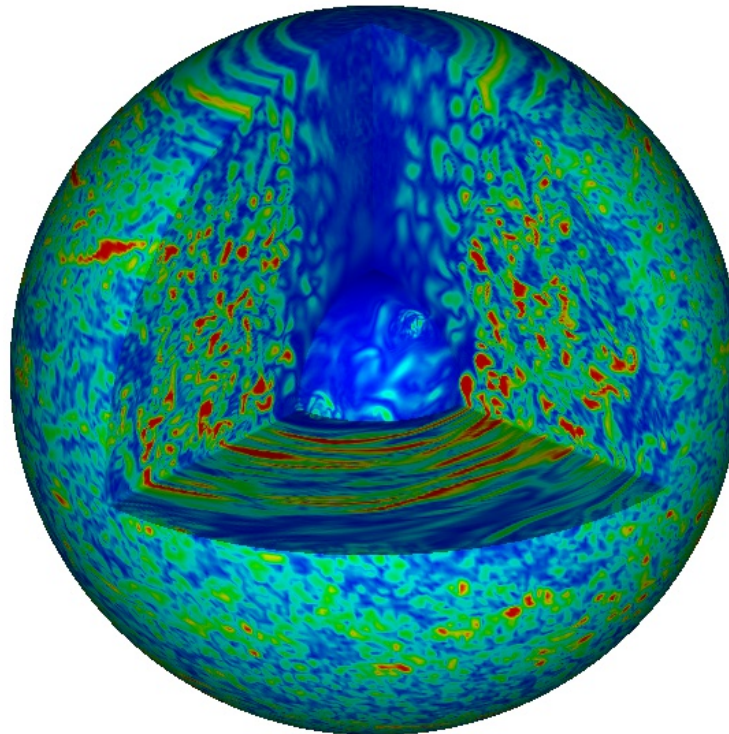
Good vertical resolution
but low horizontal resolution





Moesta+2015 : first simulation with large-scale magnetic field generation..
but started with magnetar strength dipolar field

- Preliminary** simulations of a simplified model of full neutron star
- incompressible approximation
 - start with a small-scale field of $\sim 5 \cdot 10^{14}$ G



1. The MRI can grow in two different regimes :

- Viscous regime deep inside the proto-neutron star :

 - requires a **minimum initial magnetic field** of $\sim 10^{12}$ G

- Neutrino drag near the surface of the proto-neutron star

2. Final magnetic field strength :

- Stratification matters : sub-magnetar strength in stable regions

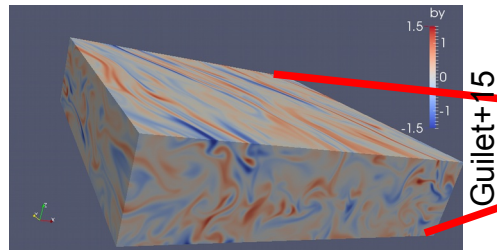
- Strong dependence on the magnetic Prandtl number

 - **MRI may be more efficient than simulations suggest !**

- Generation of a dipolar magnetic field is still an open question

Still a long way to go: from the small to the large scales

Step 1 : local MRI model

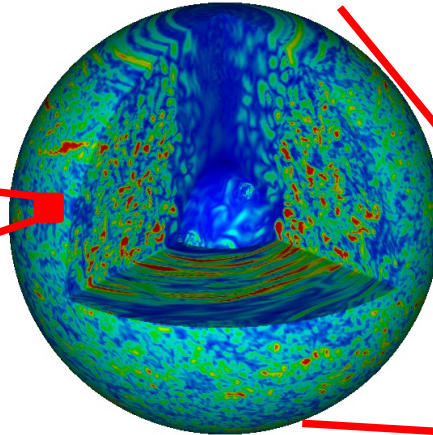


~ 1-5 km

High Pm regime ?

Neutrino drag regime ?

Step 2 : global simulations

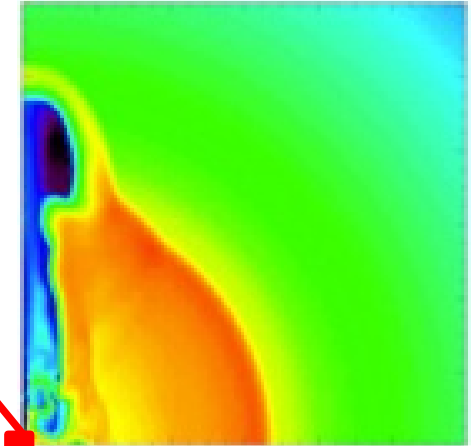


~ 10-50 km

Magnetic field geometry ?

MRI vs convective dynamo

Step 3 : hypernova & GRB jet



~ 10⁵-10⁶ km

Explosion diversity ?

Energy, jet properties,
nucleosynthesis,
luminosity etc..

Thanks !