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# Triple alpha reaction rate under extreme conditions

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T. Kawabata  
Department of Physics, Osaka University

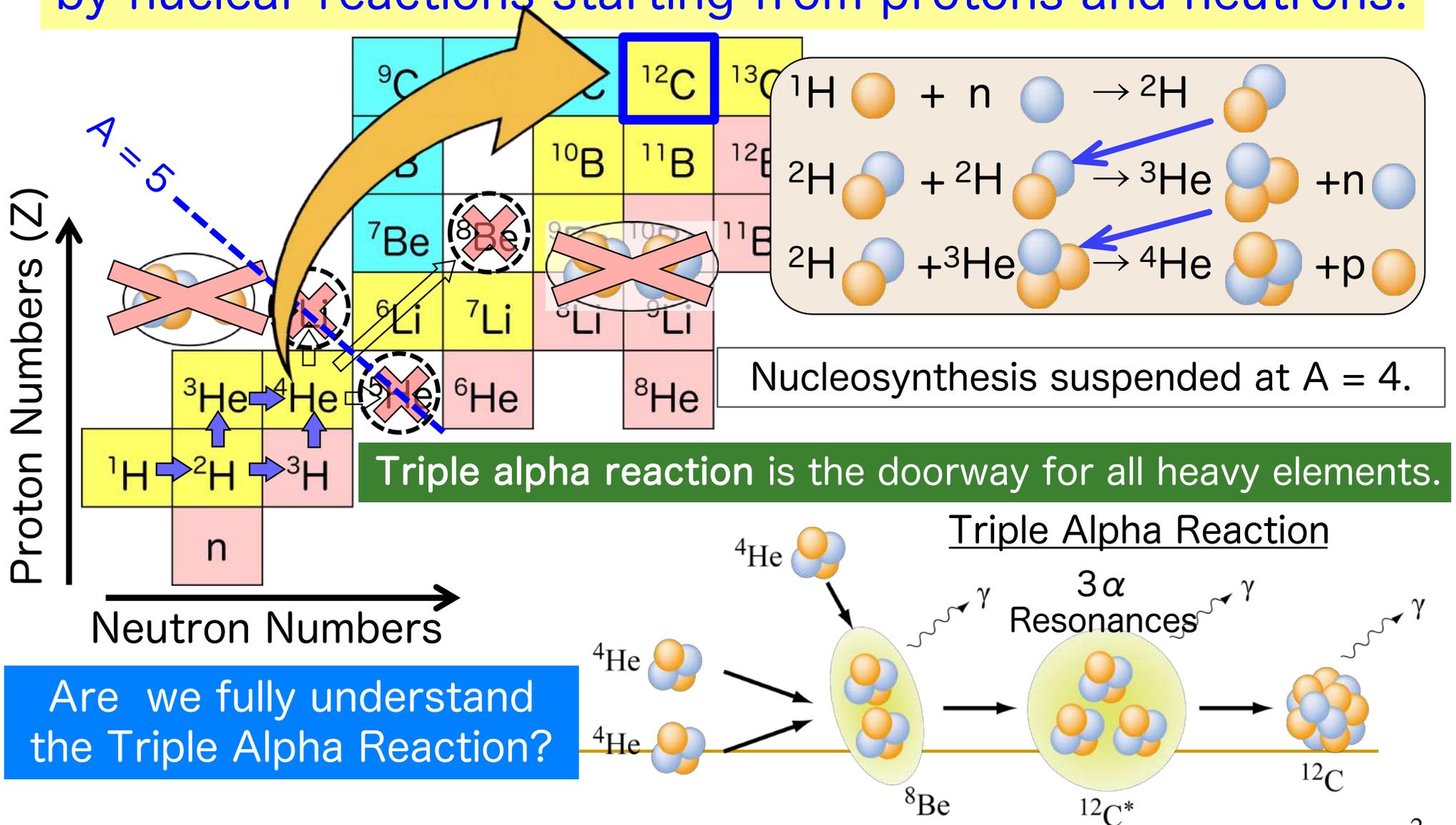
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# Nucleosynthesis in the Universe

All chemical elements were synthesized by nuclear reactions starting from protons and neutrons.



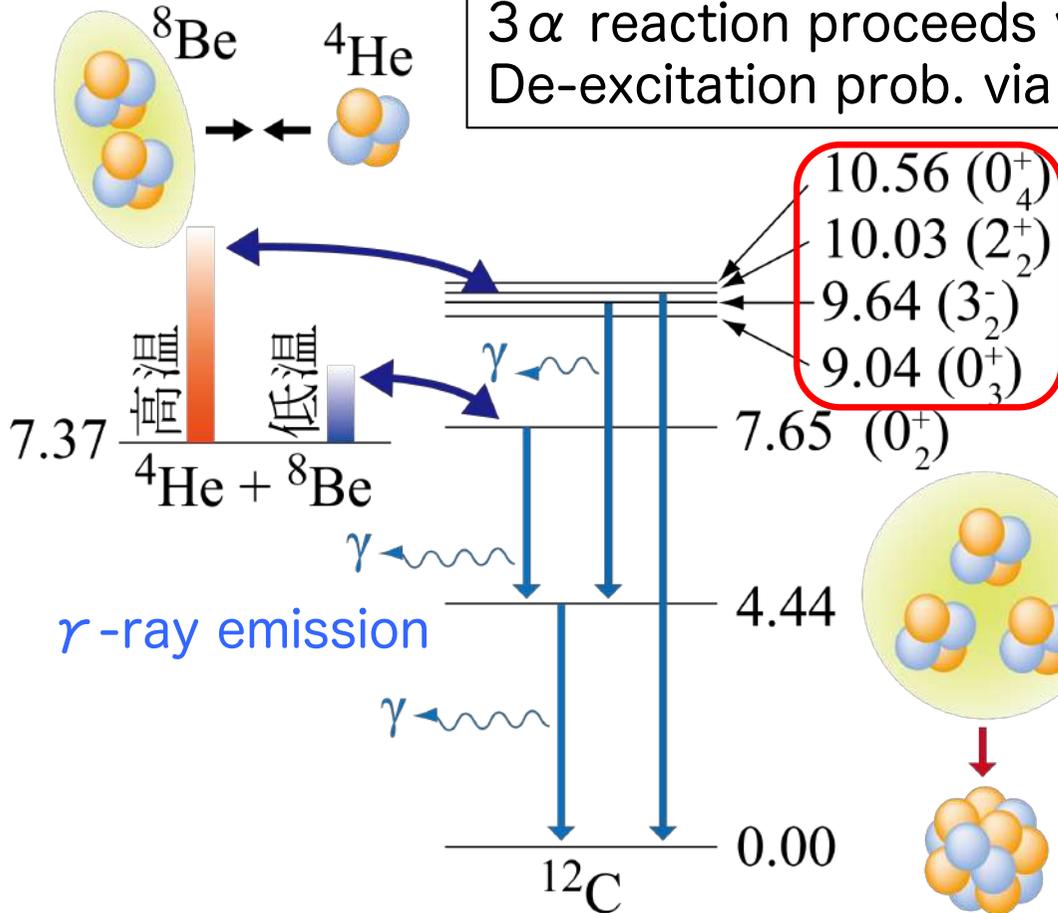
# Triple Alpha Rate and De-Excitation Prob.

Most of  $3\alpha$  states decay back to  $3\alpha$  particles,  
but rarely de-excite into  $^{12}\text{C}$

De-excitation probability  
determines the  $3\alpha$  rate

Normal Stellar Environments ( $\rho \sim 10^3\text{--}5 \text{ g/cm}^3$ ,  $T \sim 10^8 \text{ K}$ )

$3\alpha$  reaction proceeds via the  $0^+_2$  state at  $E_x = 7.65 \text{ MeV}$   
De-excitation prob. via the  $\gamma$  decay is known [ $4.4(5) \times 10^{-4}$ ].



## High Temp. ( $T > 10^9 \text{ K}$ )

High-lying  $3\alpha$  resonances  
( $2^+_2$ ,  $3^-_1$ ,  $0^+_3$ ,  $0^+_4$ ) are important.  
De-excitation by  $\gamma$  decays.  
 $\gamma$ -decay prob. are unknown.

Scattering with BG particles

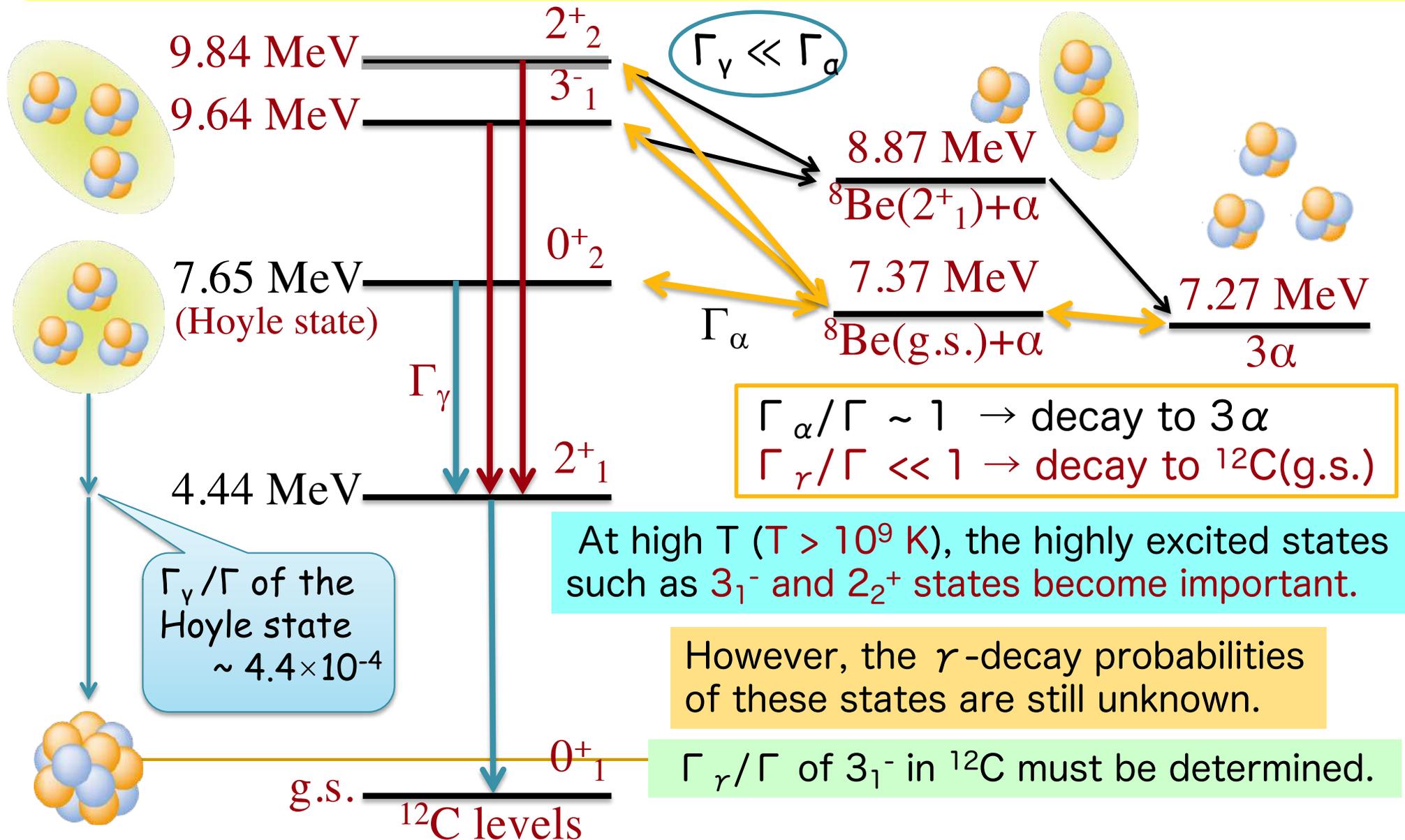
## High Density ( $\rho > 10^6 \text{ g/cm}^3$ )

Scattering with BG particles  
Cross sections are unknown.

$3\alpha$  reaction under extreme conditions (High  $T$  and  $\rho$ )  
has never been fully understood.

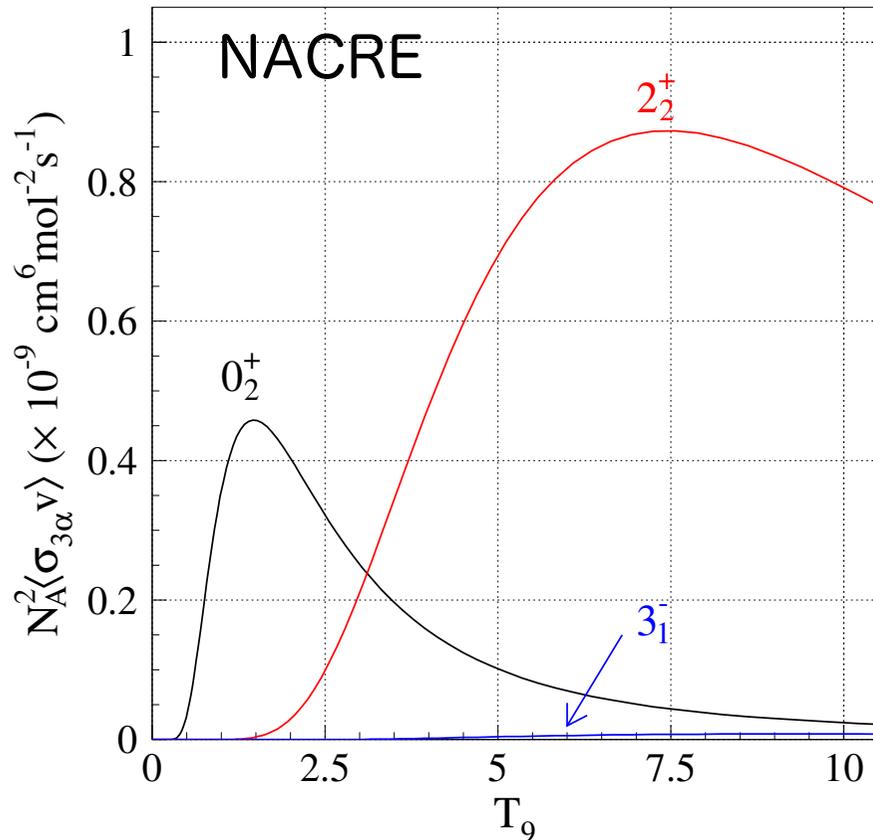
# 3 $\alpha$ Reaction and $\gamma$ -decay Probability

The 3 $\alpha$  reaction rate strongly depends on  $\gamma$ -decay probability.



# Triple alpha reaction rate

First star is massive and temperature reaches  $T_9 \sim 5$ .



C. Angulo et al., Nucl. Phys. A **656** 3—187 (1999).

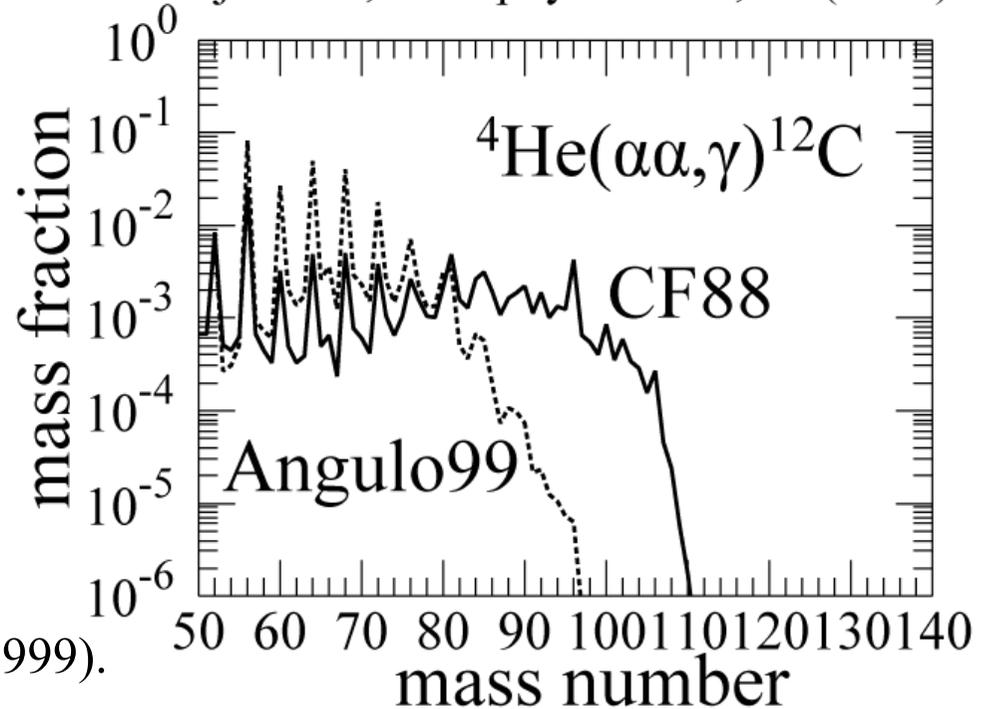
Large Impact on Heavy element abundance by  $\nu p$  process

Angulo99: Include  $3_1^-$  and  $2_2^+$ \*

CF88:  $0_2^+$  and  $3_1^-$ \*

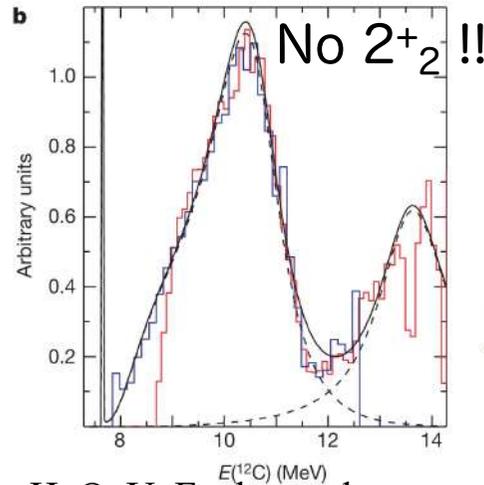
\*Not experimental information

S. Wanajo et al., Astrophys. J. **729**, 46 (2011).

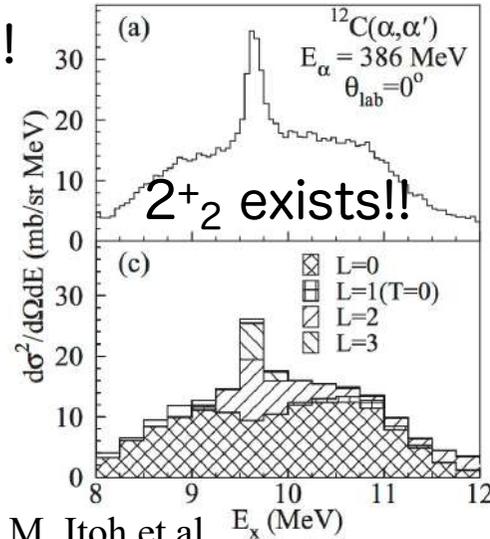


# Recent Update

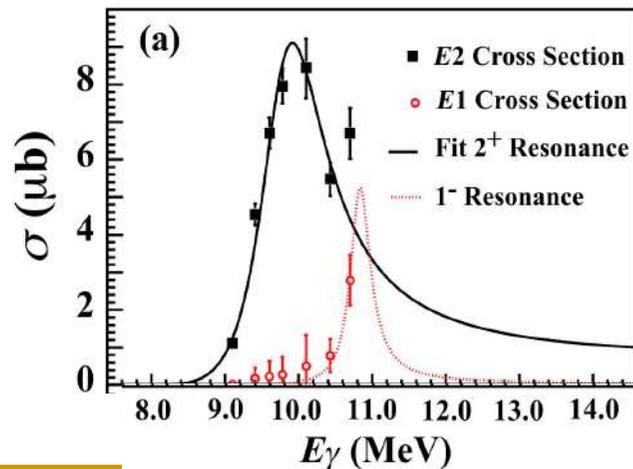
New data on the  $2^+_2$  were published.



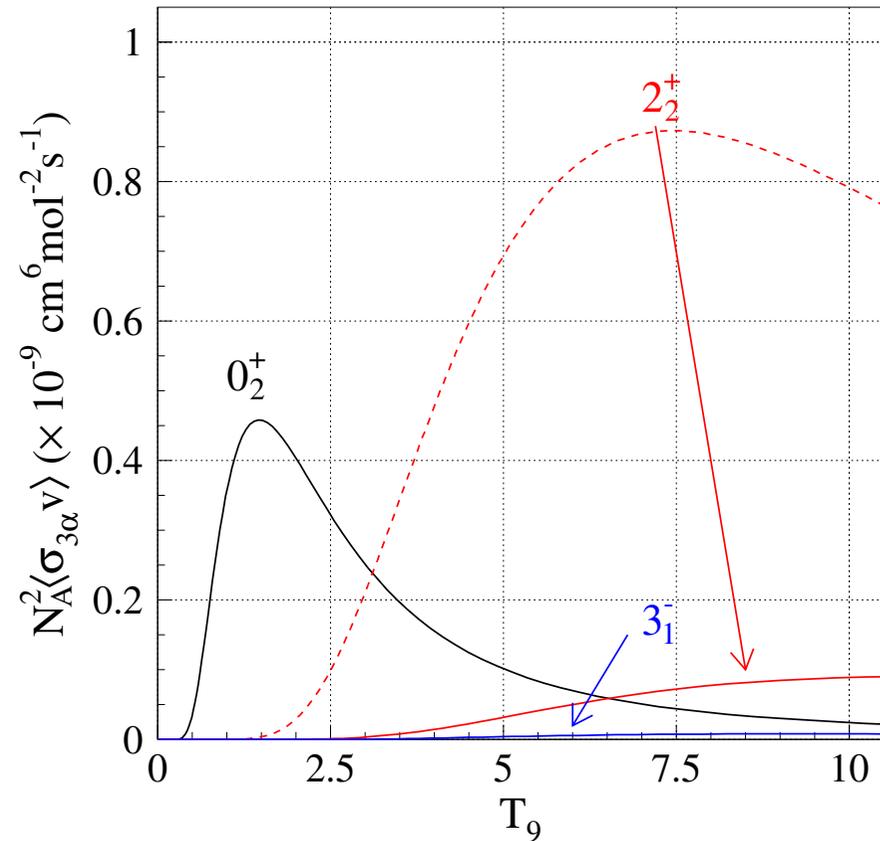
H. O. U. Fynbo et al.,  
Nature **433**, 136 (2005).



M. Itoh et al.,  
Phys. Rev. C **84**, 054308 (2011).



W. R. Zimmerman et al., Phys. Rev. Lett. **110**, 152502 (2013).



$3\alpha$  rate significantly suppressed at high  $T$ .

How about the  $3^-_1$  state ?

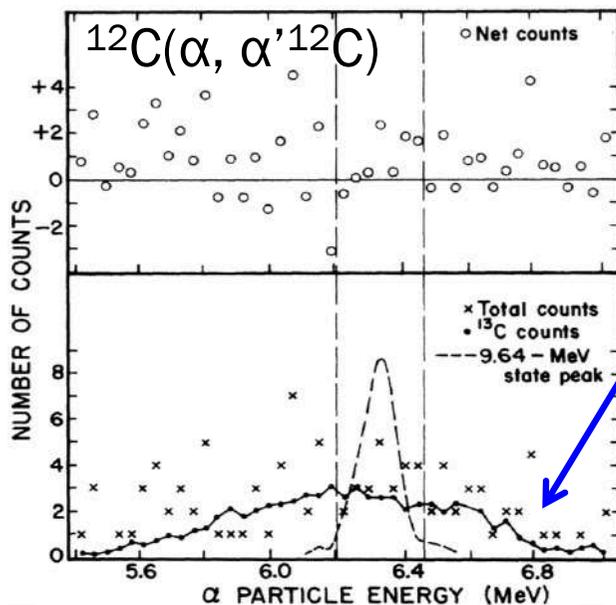
# $\gamma$ -decay probability of the $3_1^-$ state

Difficult to measure the  $\Gamma_\gamma/\Gamma$  of the  $3_1^-$  state because it is very small.

$3_1^-$ in $^{12}\text{C}$	Total width $\Gamma$	$\gamma$ -decay width $\Gamma_\gamma$	$\gamma$ -decay probability $\Gamma_\gamma/\Gamma$
Lower limit	34(5) keV	0.31(4) meV	$9.1 \times 10^{-9}$
Upper limit		28 meV (2 $\sigma$ C. L.)	$4.1 \times 10^{-7}$

Direct  $\gamma$ -decay to the g. s. taken from (e,e')

## Previous experiment

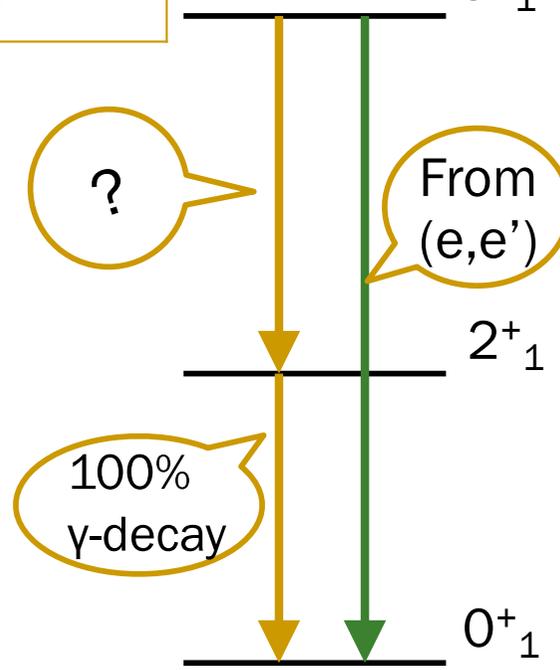


Difficult to measure!!

Background due to  $^{13}\text{C}$  contaminants

Use  $^{12}\text{C}$  beam not  $^{12}\text{C}$  Target!

No  $^{13}\text{C}$  contaminants in  $^{12}\text{C}$  beam!!



[D. Camberlin et al., Phys. Rev. C **10**, 2 (1974).]

# Experimental procedure

Using the inverse kinematic reaction  $H(^{12}\text{C}, ^{12}\text{C} p)$ , recoil protons and scattered  $^{12}\text{C}$  will be measured simultaneously instead of  $\gamma$ -rays.

$\gamma$ -decay probability  $\Gamma_\gamma / \Gamma$

$$\frac{\Gamma_\gamma}{\Gamma} = \frac{\text{Number of } \gamma\text{-decay events}}{\text{Number of all excited events}}$$

Number of all excited events

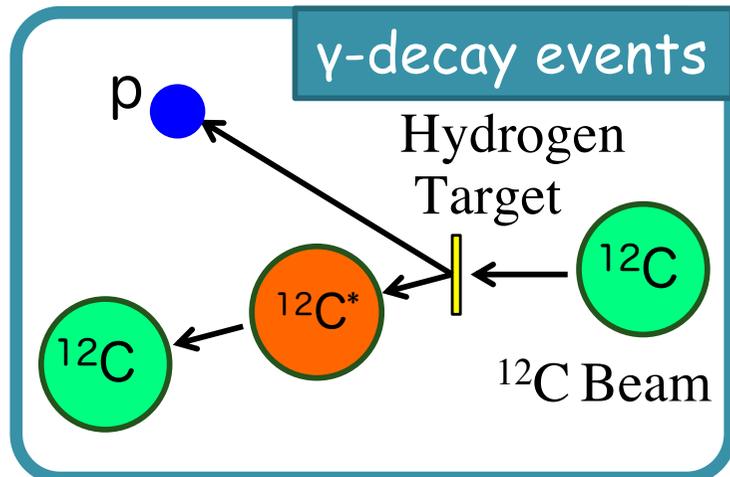
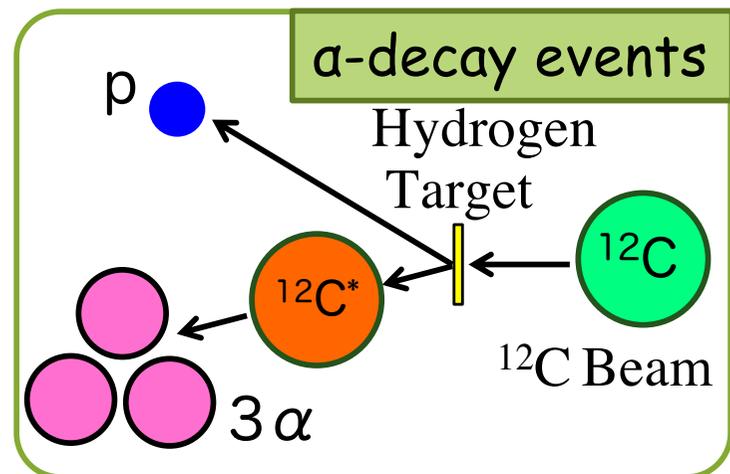
$E_x$  in  $^{12}\text{C}$  is determined from the energy and angle of **the recoiled proton**.

Number of  $\gamma$ -decay events

The scattered  $^{12}\text{C}$  should be detected in coincidence with the recoiled proton.

- Thin solid hydrogen target.
- Recoil proton detector.

All excited events



# Experimental Setup

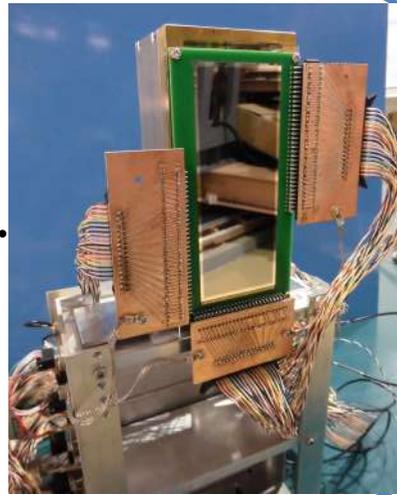
The experiment was performed at the cyclotron facility in RCNP.

## Recoil proton detector

Particle-identified by **Gion** (Si+GAGG telescope).

→  $E_x$  of the scattered  $^{12}\text{C}$

Count the excited events

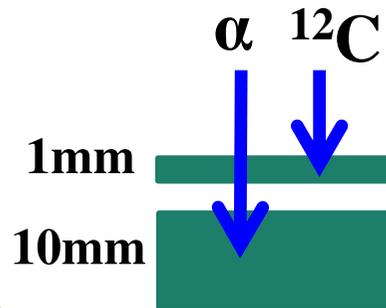


## Solid Hydrogen Target

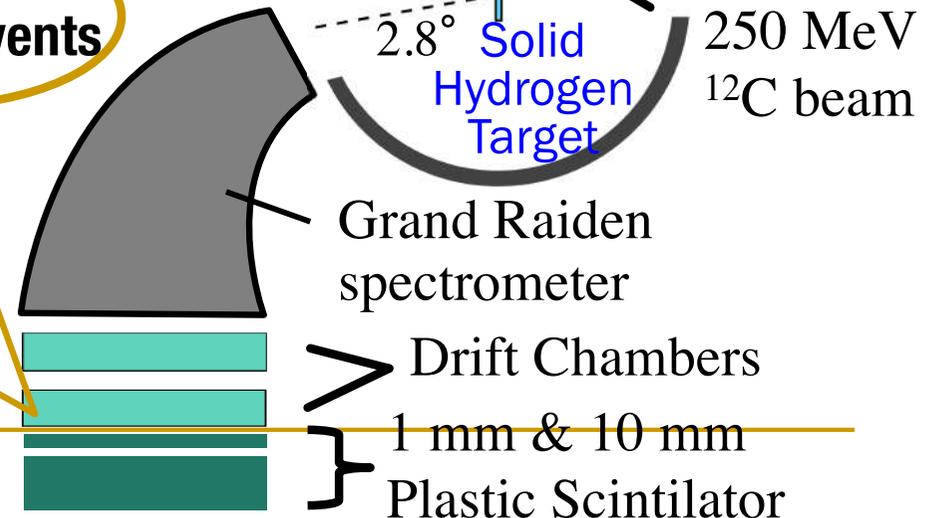


Select  $\gamma$ -decay events

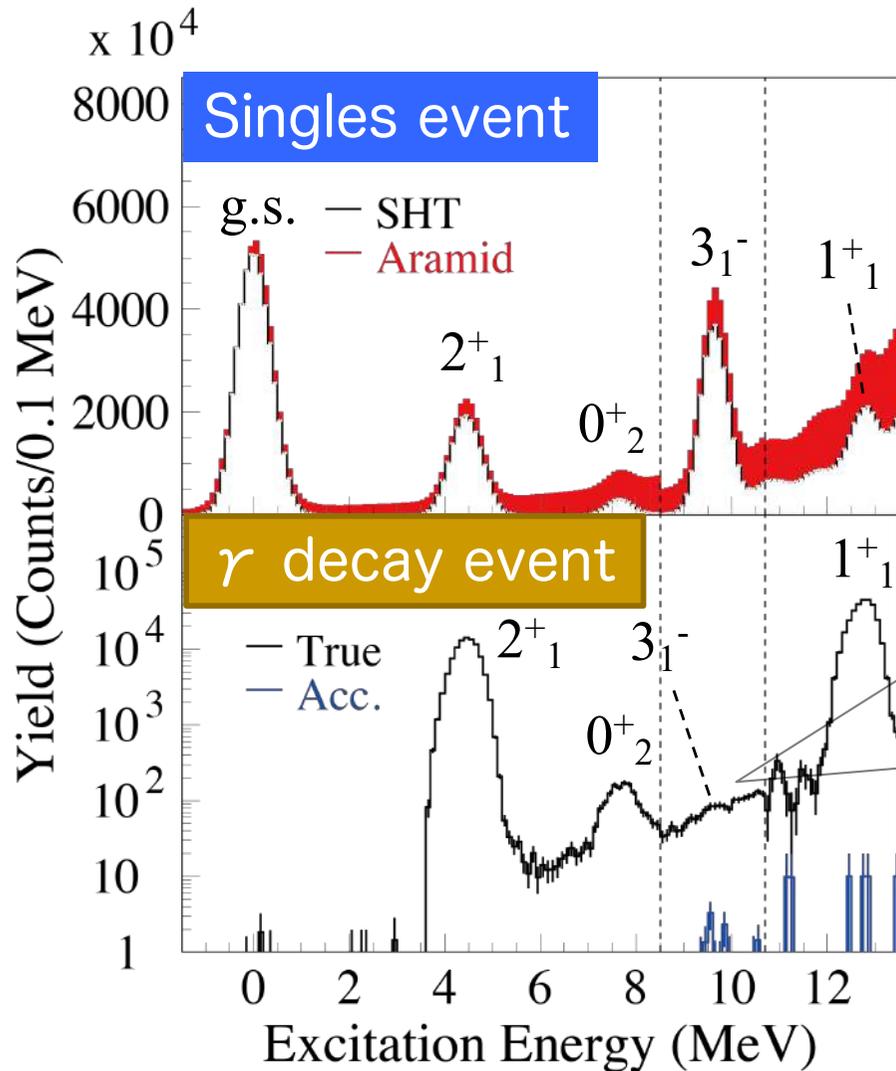
## Scattered $^{12}\text{C}$ detector



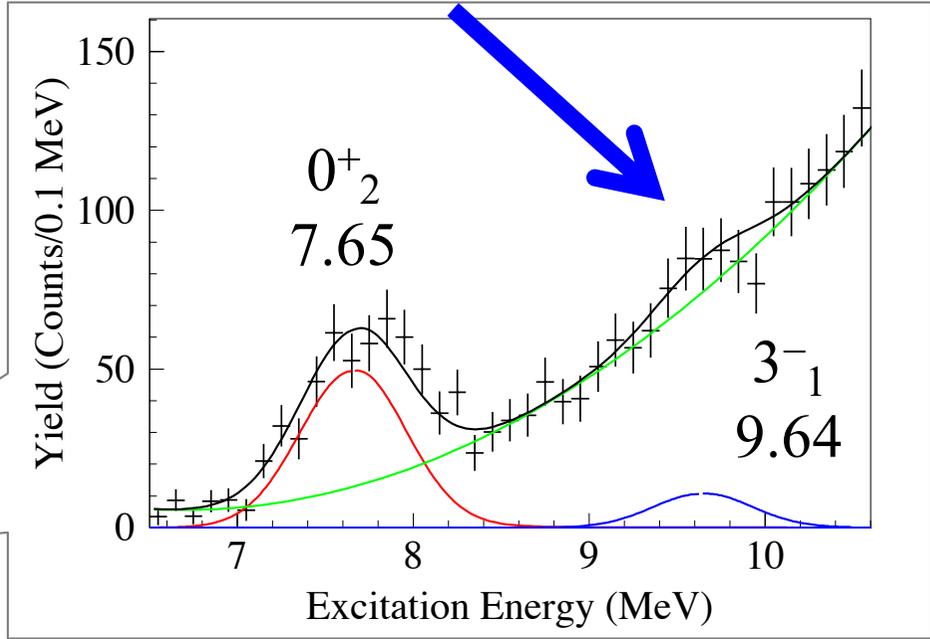
Anti-coinc between 2 scintillators  
→  $^{12}\text{C}$  trigger



# Results



γ-decay from 3<sup>-</sup><sub>1</sub> was observed !



Peak significance: 91%

# Gamma Decay Probability

$\gamma$ -decay probability is given by

$$\frac{\Gamma_{\gamma}}{\Gamma} = \frac{\# \text{ of } \gamma \text{ decay events}}{\# \text{ of singles events}} \times \frac{1}{\text{geo. eff.}}$$

Geometrical efficiency should be estimated by MC calculation.

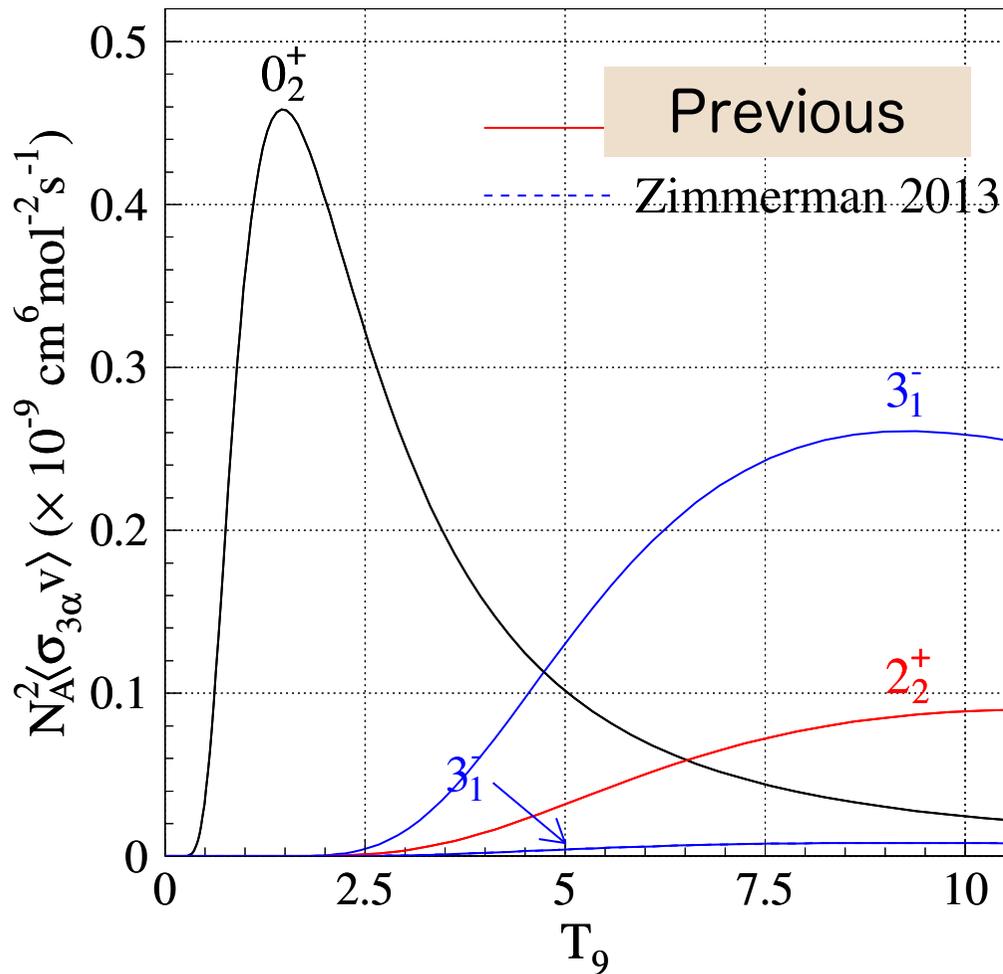
	$0^+_2$	$1^+_1$	$3^-_1$
Geo. Efficiency	0.117(2)	0.186(9)	0.229(3)
$\Gamma_{\gamma}/\Gamma$ Previous	$4.16(11) \times 10^{-4}$ <del><math>6.2(6) \times 10^{-4}</math></del>	$2.21(7) \times 10^{-2}$	Unknown
$\Gamma_{\gamma}/\Gamma$ Present	$4.3(8) \times 10^{-4}$	$2.6(7) \times 10^{-2}$	$1.3(8) \times 10^{-6}$

The present results are consistent with the previous result on the  $0^+_2$  and  $1^+_1$  states, but not with the recent report for the  $0^+_2$  state by Kibedi et al.

$\Gamma_{\gamma}$  for the  $3^-_1$  state is larger than the previous upper limit [ $8.2 \times 10^{-7}$  ( $2\sigma$ )].

# Triple Alpha Reaction Rate

Triple reaction rate was calculated using the measured  $\Gamma_r/\Gamma$

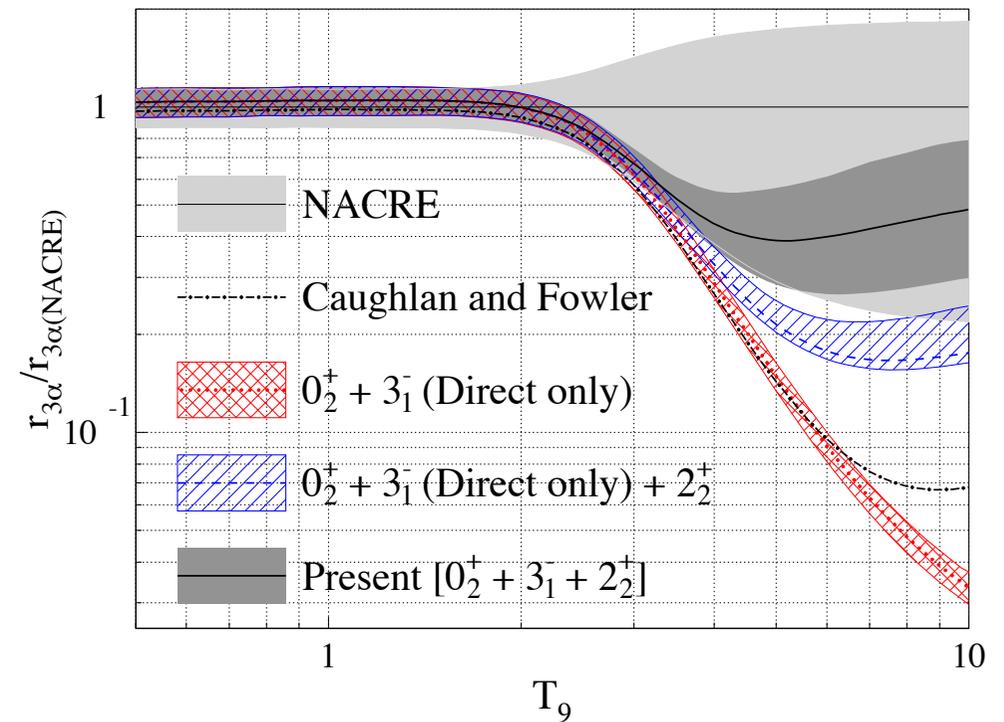


NACRE

$3_1^-$   
 $\Gamma_r = 2 \text{ meV}$

Present

$3_1^-$   
 $\Gamma_r = 44 \text{ meV}$



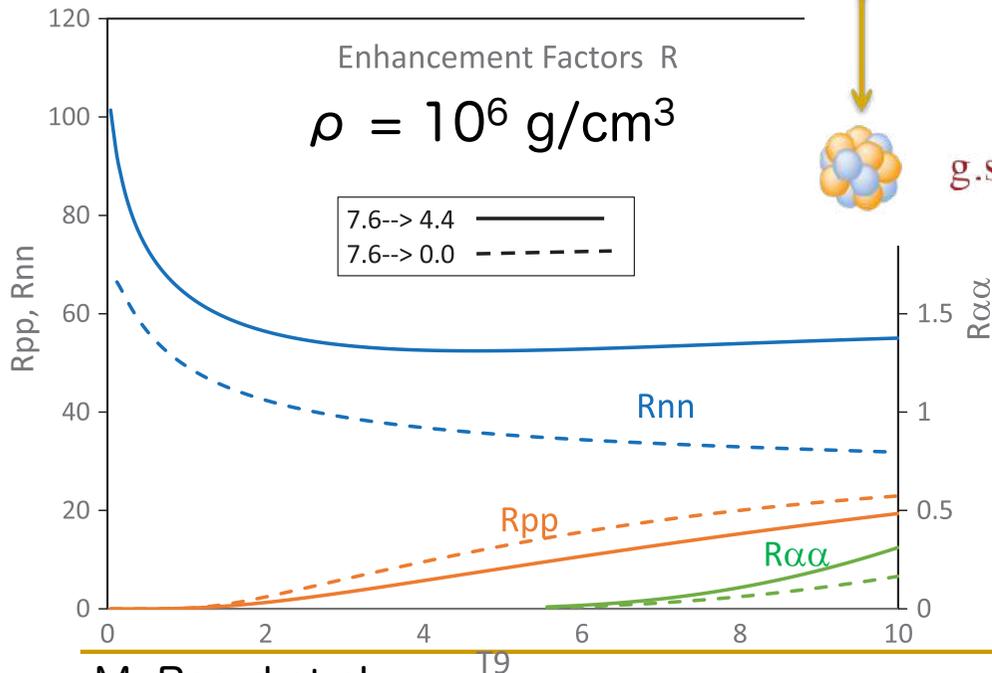
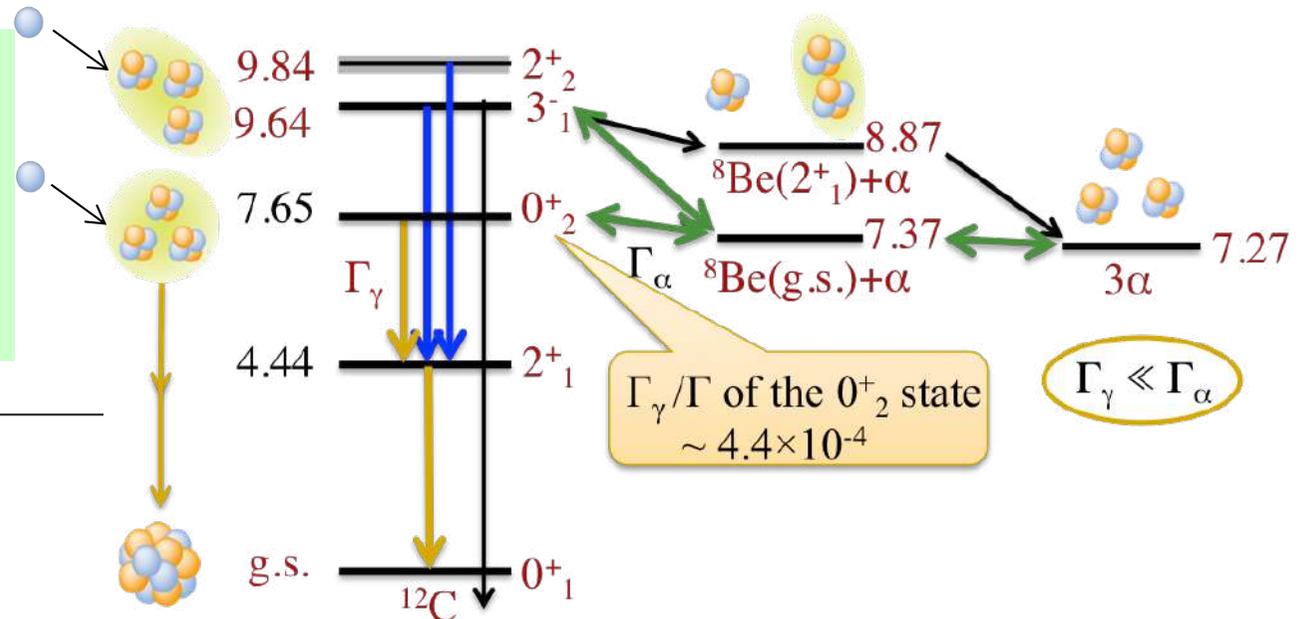
The  $3\alpha$  rate is partially restored, and consistent with NACRE...

Recently published in M. Tsumura, T. K. et al., Phys. Lett. B 817, 136283 (2021).

# Triple Alpha Reaction Rate at high $\rho$

Only de-excitation by gamma decay was considered so far.

Exothermic inelastic scattering with background particles should be considered at high density environment.



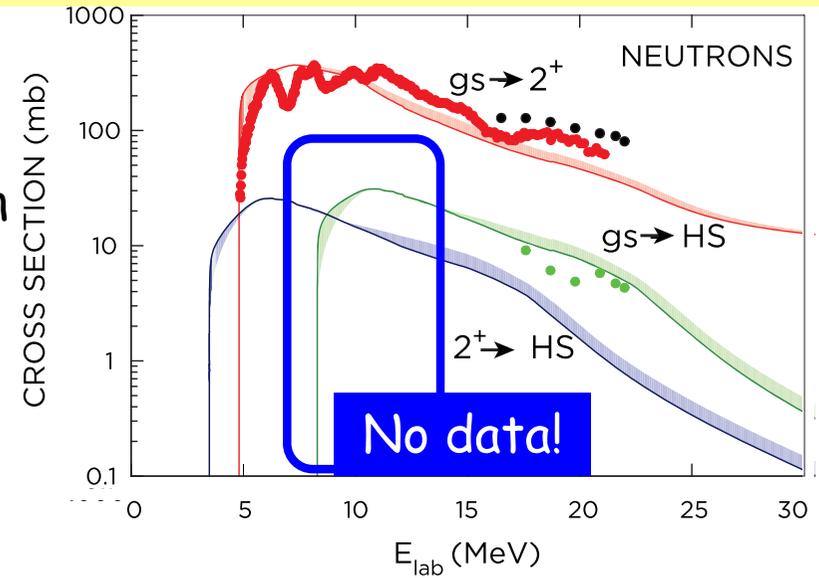
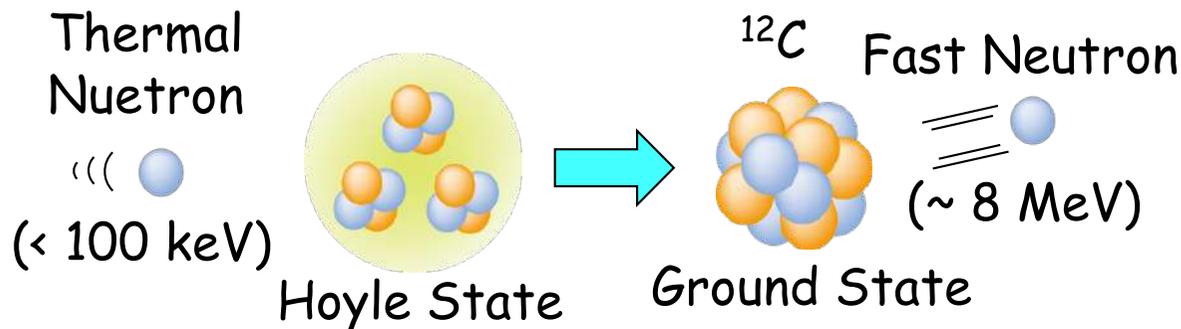
$^{12}\text{C}(\text{Hoyle})(n,n')^{12}\text{C}(\text{g.s.})$  might enhance the triple alpha reaction rate by a factor of 60—100.

Need to determine the cross sections.

# Time Inverse Reaction

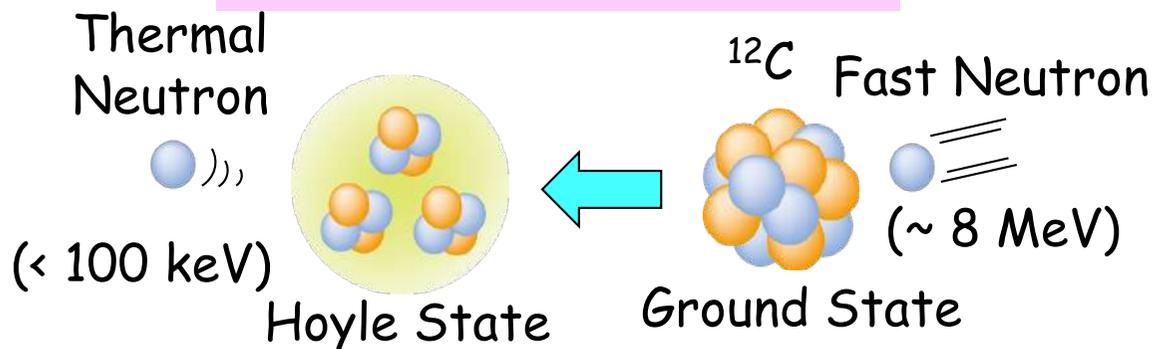
Direct measurement of  $^{12}\text{C}(\text{Hoyle})(n,n')^{12}\text{C}(\text{g.s.})$  is impossible.  
 → Time inverse reaction should be measured.

## Astrophysical Reaction



M. Beard et al., PRL 119, 112701 (2017).

## Time Inverse Reaction

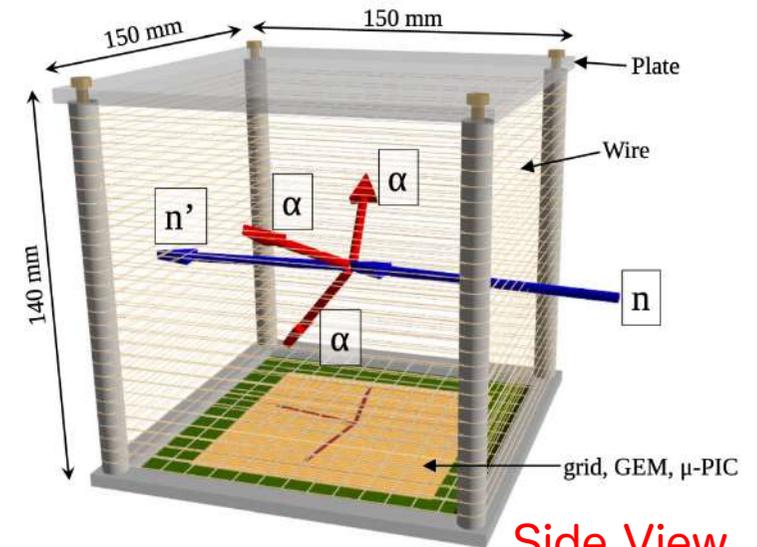


However, measurements of low-E neutrons or alpha particles are not easy.  
 → MAIKo Active Target

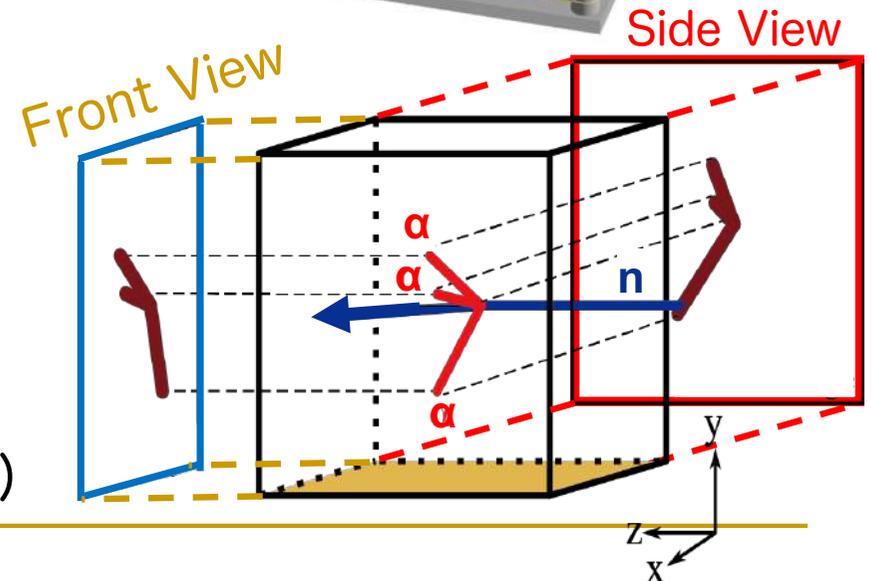
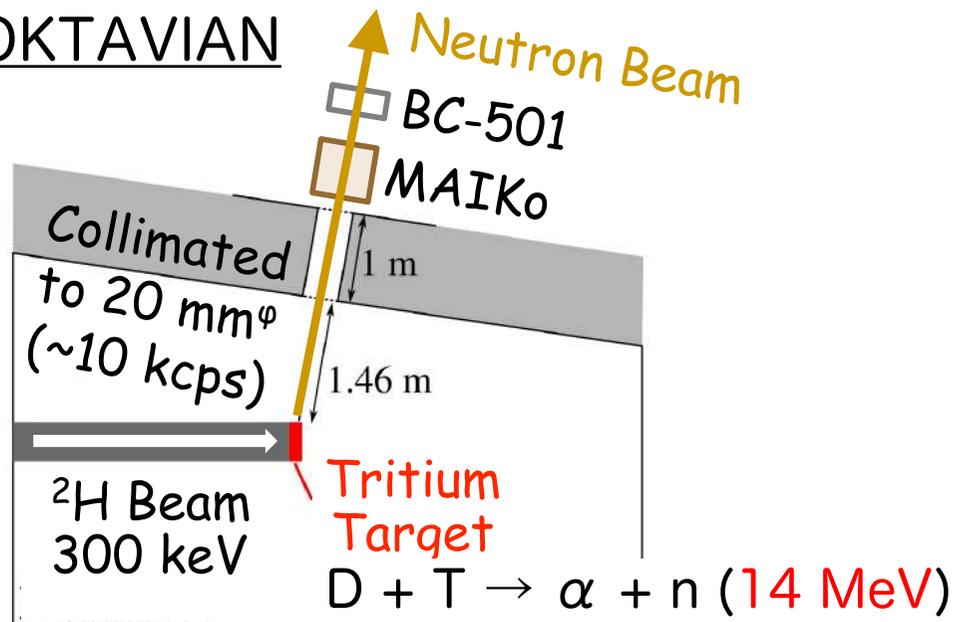
# Test Measurement with MAIKo

Test measurement was carried out at OKTAVIAN, Osaka.

- MAIKo TPC
  - ✓ Two images of 2D-projected trajectories.
  - ✓ Detect low-E particles over large  $\Omega$
  - ✓  $iC_4H_{10}(10\%) + H_2$  or He @100, 450 hPa
- BC-501 Liquid Scintillator
  - ✓ Determine the neutron flux.



OKTAVIAN



T. Doi, Master Thesis, Kyoto University (2020).

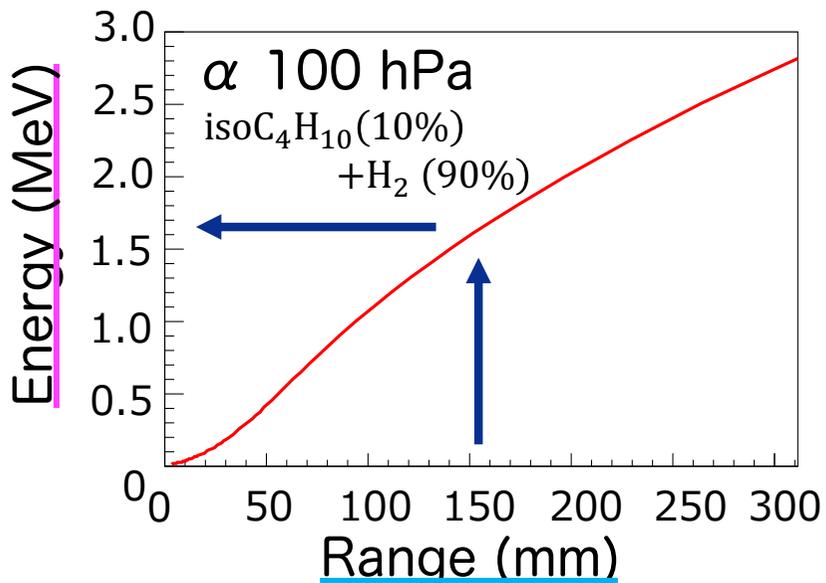
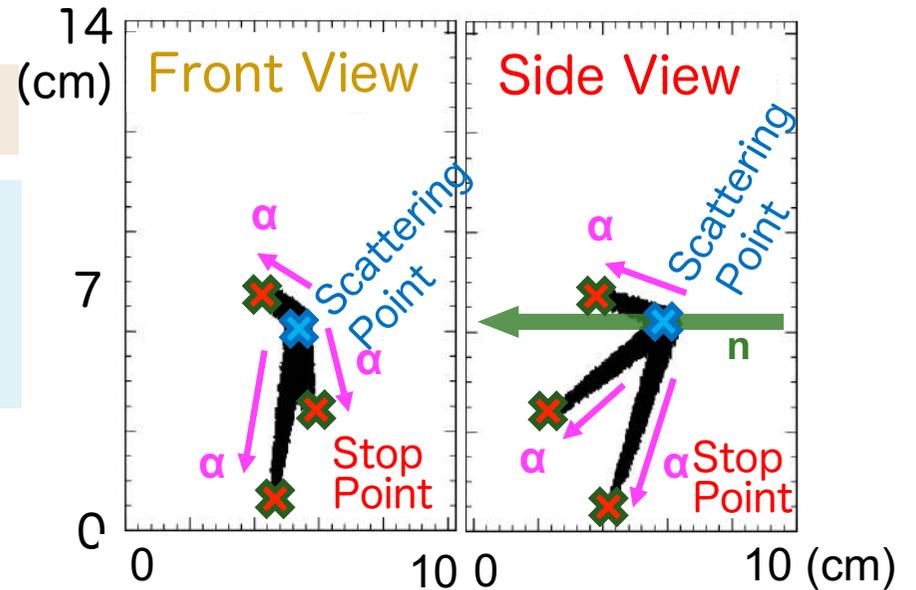
# Eye-Scan Analysis

Two track images were analyzed by human eyes.



60K events by 11 people

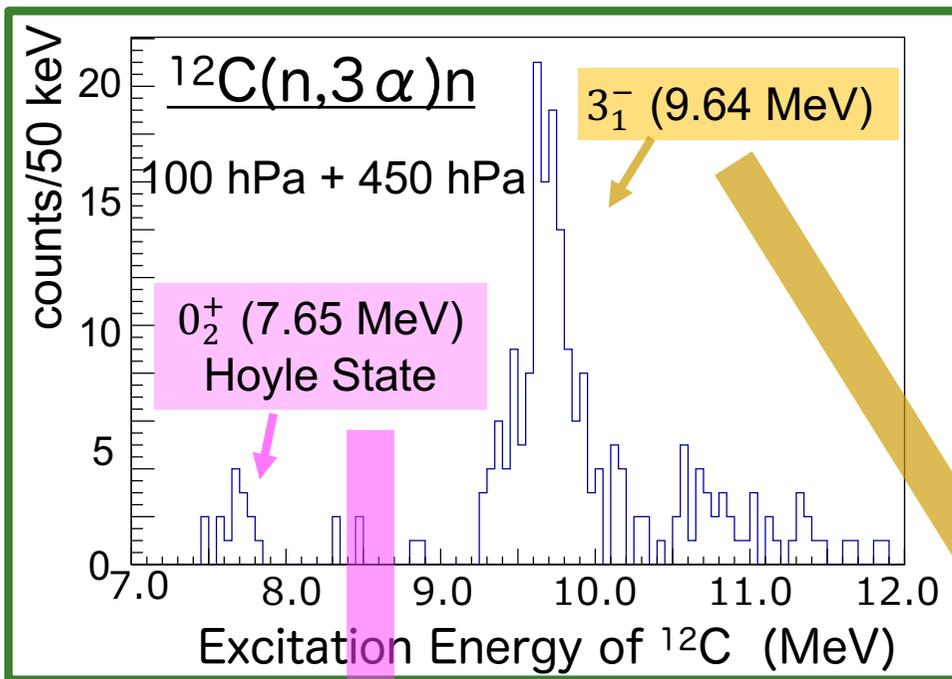
- ✓ Number of trajectories
- ✓ Scattering point
- ✓ Stop positions



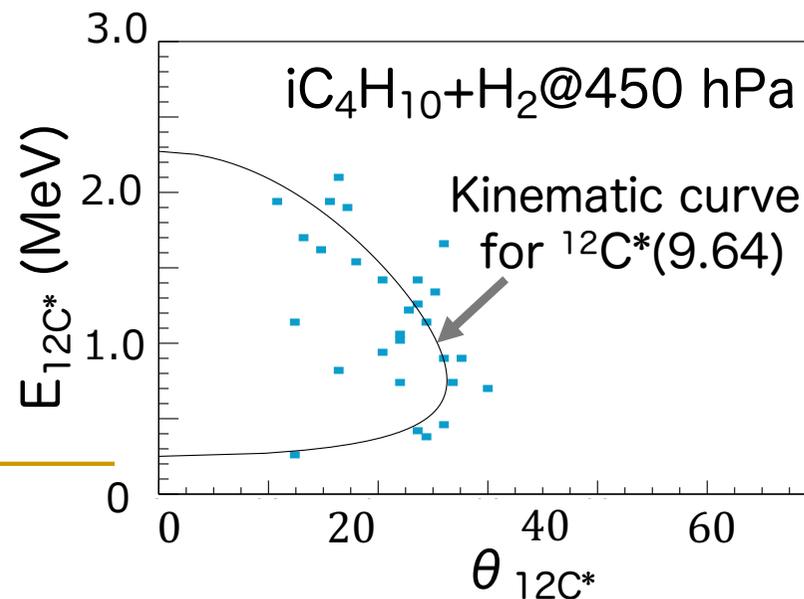
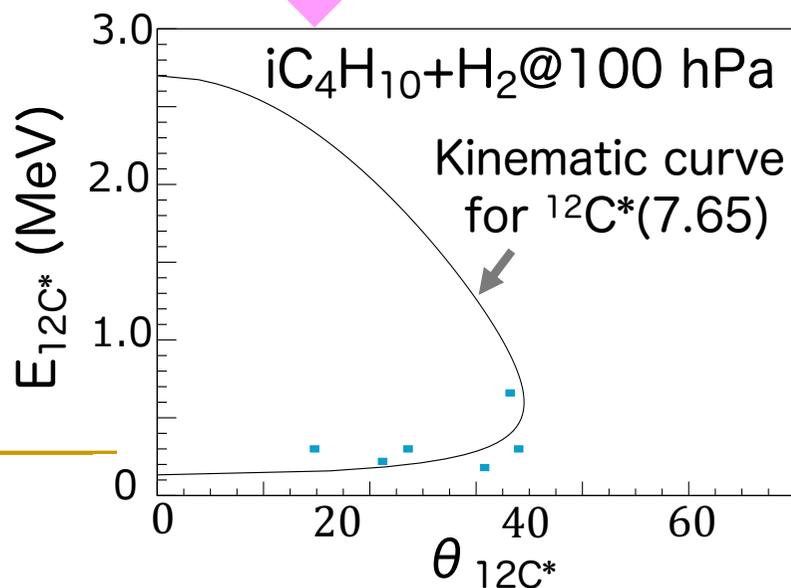
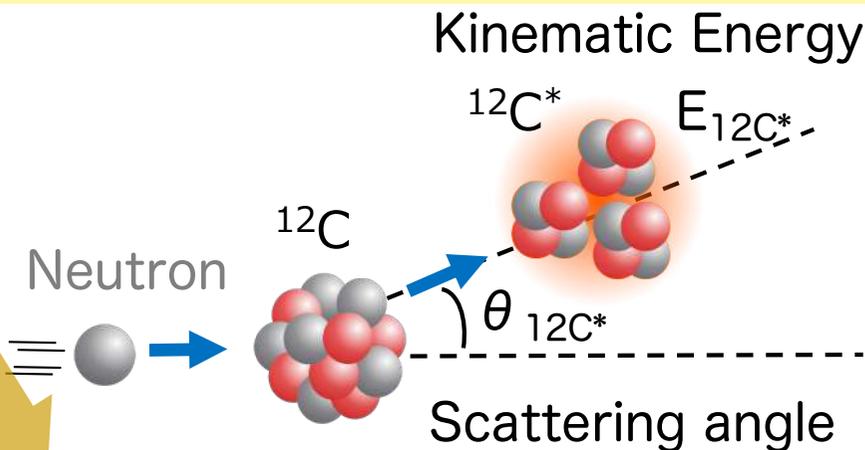
- ✓ Reconstruct 3D trajectories
  - Ranges → Kinematic energies
  - Emission angles

- ✓ Invariant mass spectroscopy of  $^{12}\text{C}$ .

# Event Reconstruction



Two peaks at 7.65 MeV and 9.64 MeV were successfully identified.



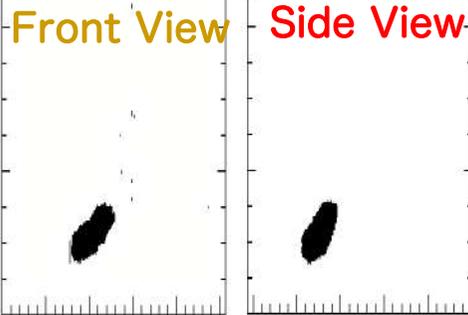
# Reconstruction Efficiency

Requirements:

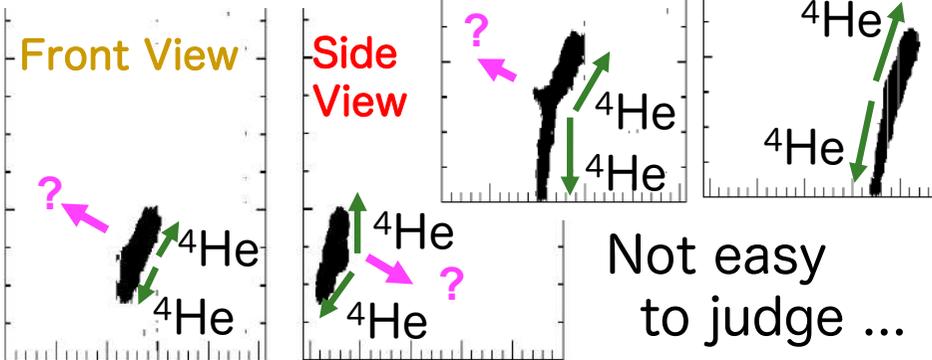
- ✓ 3  $\alpha$ s stopped in the sensitive volume.
- ✓ Human eyes can find 3 tracks.

## Track examples

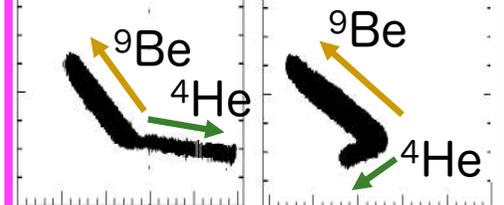
1 track  ${}^4\text{He}(n, n'){}^4\text{He}$



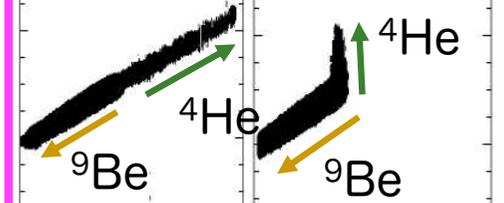
3 or 2 tracks ?  
3  $\alpha$  ( ${}^4\text{He}$ ) ?



Front View Side View



Front View Side View



2 tracks  ${}^{12}\text{C} + n \rightarrow {}^{13}\text{C}^* \rightarrow {}^9\text{Be} + {}^4\text{He}$

- ✓ Test images were generated by Simulation.  
→ BG events were randomly mixed.
- ✓ **Eye-scan analysis** was carried out to estimate the reconstruction efficiency.

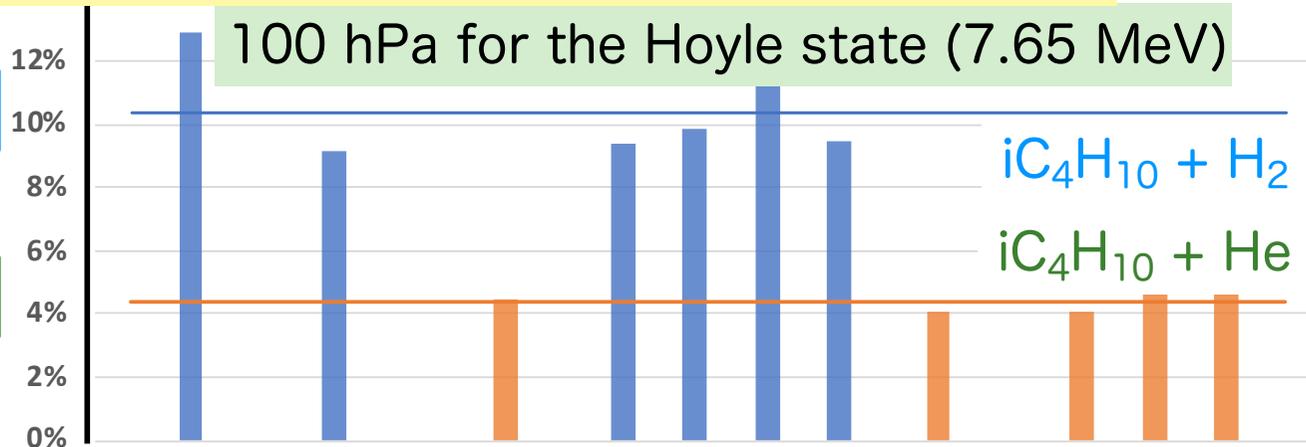
K. Himi, Bachelor Thesis, Osaka University (2021).

# Eye-Scan Analysis, again

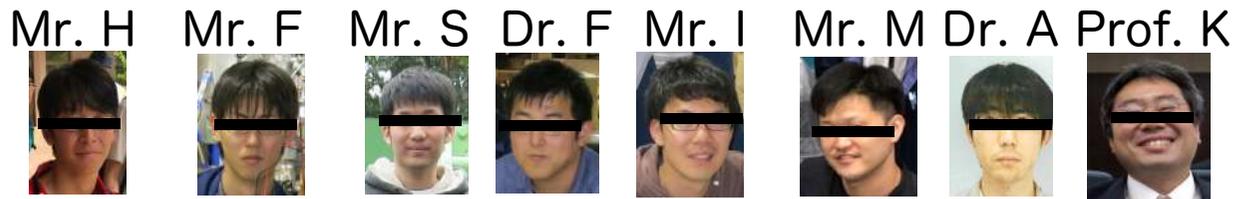
8 scanners analyzed the simulated data.

Ave.  $10 \pm 1.4\%$

Ave.  $4.4 \pm 0.32\%$

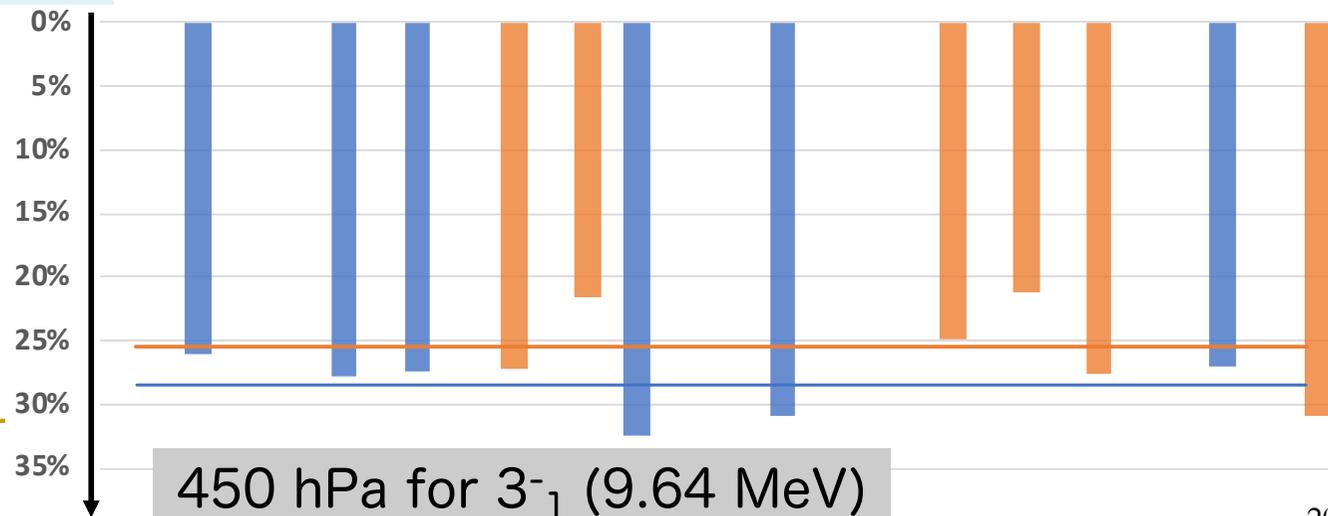


$iC_4H_{10} + H_2$  works better than  $iC_4H_{10} + He$  as the detection gas.



Ave.  $26 \pm 3.4\%$

Ave.  $29 \pm 2.3\%$



# Measured Cross Section

$$\sigma(\text{mb}) = \frac{Y}{N_t N_{beam} \epsilon}$$

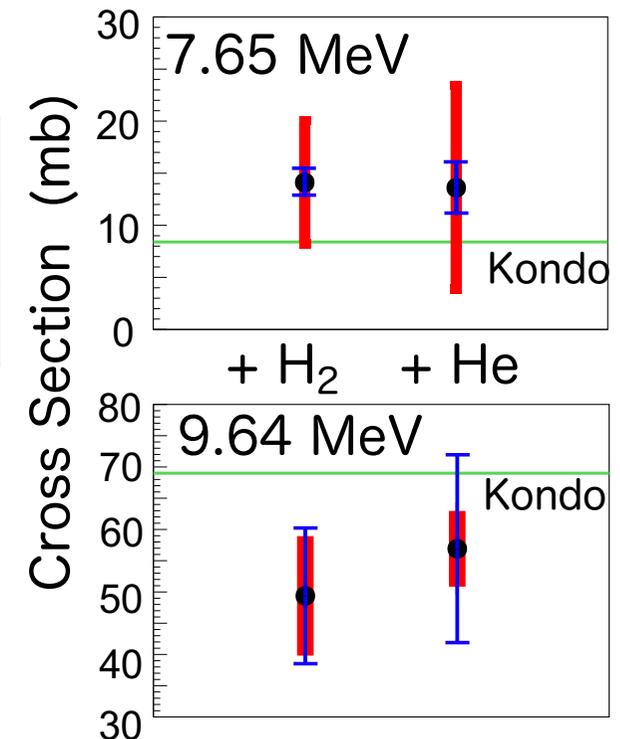
$Y$  ... Yield  
 $N_t$  ... Target Area Density ( $\text{cm}^{-2}$ )  
 $N_{beam}$  ... Number of incident neutrons  
 $\epsilon$  ... Efficiency

100 hPa Hoyle state (7.65 MeV)

	Y	$\epsilon$	$\sigma$ (mb)	$\Delta \sigma_{sta}$ (mb)	$\Delta \sigma_{sys}$ (mb)
+ H <sub>2</sub>	6	0.10	14	5.8	1.2
+ He	2	0.044	14	9.6	2.4

450 hPa 3<sub>1</sub><sup>-</sup> (9.64 MeV)

	Y	$\epsilon$	$\sigma$ (mb)	$\Delta \sigma_{sta}$ (mb)	$\Delta \sigma_{sys}$ (mb)
+ H <sub>2</sub>	28	0.29	49	9.6	11
+ He	111	0.26	57	6.1	15



Consistent with the previous data by K. Kondo et al. [J. Nucl. sci. Tech. 45, 103 (2008).]

8.4 mb for 7.65 MeV, 69 mb for 9.64 MeV

→ Experimental feasibility has been confirmed.

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# Summary

- Triple alpha reaction rates under extreme conditions were measured.
    - Measurement of the  $\gamma$ -decay probability of the  $3_1^-$  state in  $^{12}\text{C}$ 
      - Triple alpha reaction rate at high T has been updated.
    - New measurement of the cross sections for the  $^{12}\text{C}(n,n')^{12}\text{C}^*$  reaction is in progress.
      - Triple alpha reaction rate at high  $\rho$ .
      - Experimental feasibility has been confirmed.
      - Upgrade of MAIKo is now ongoing.  
(Sensitive volume  $10 \times 10 \times 10 \text{ cm}^3 \rightarrow 30 \times 30 \times 30 \text{ cm}^3$ )
-