

# LHC時代におけるフレーバーの物理

長井 稔 (KEK)

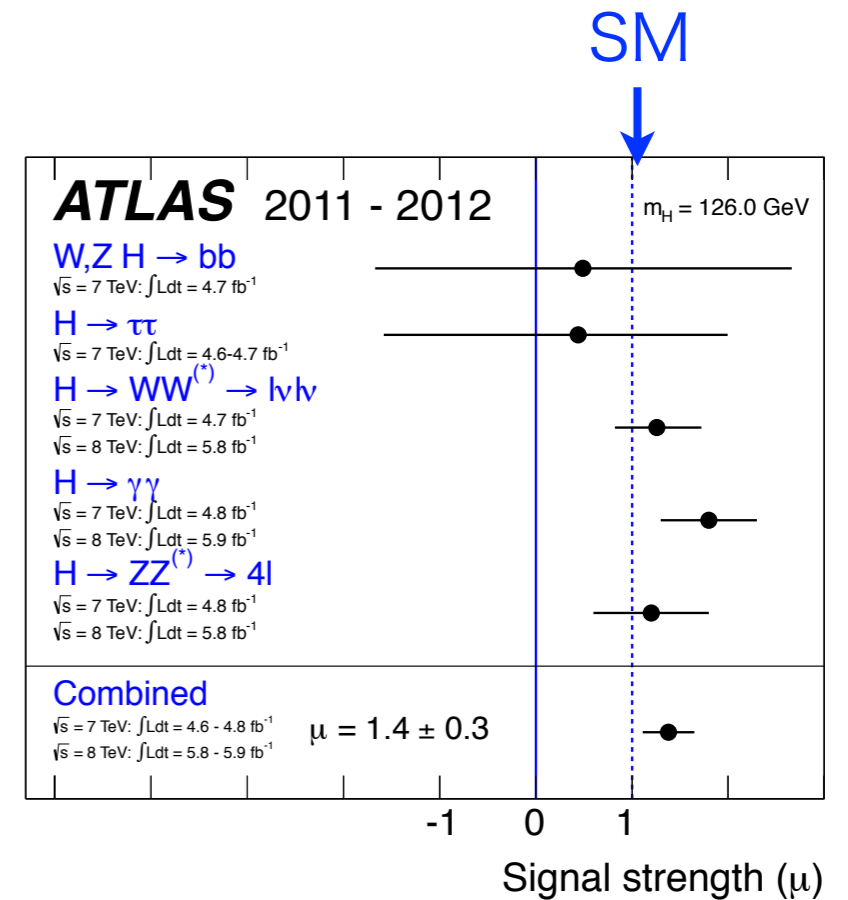
30 July, 2014

基研研究会 素粒子物理学の進展2014

# LHC7+8

- Discovery of 126 GeV Higgs

The last missing piece of the Standard Model (SM)!

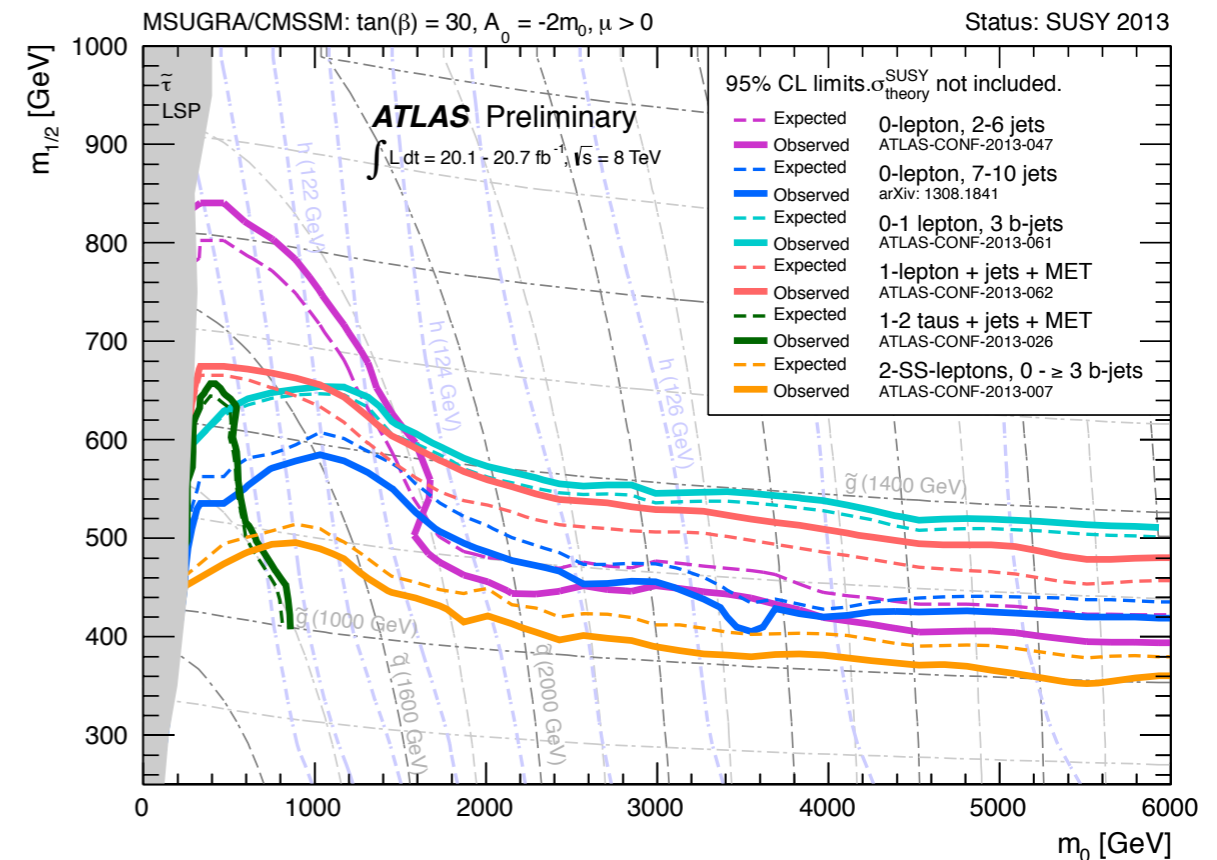


- Non-observation of NewPhysics (NP) signals

ex) CMSSM

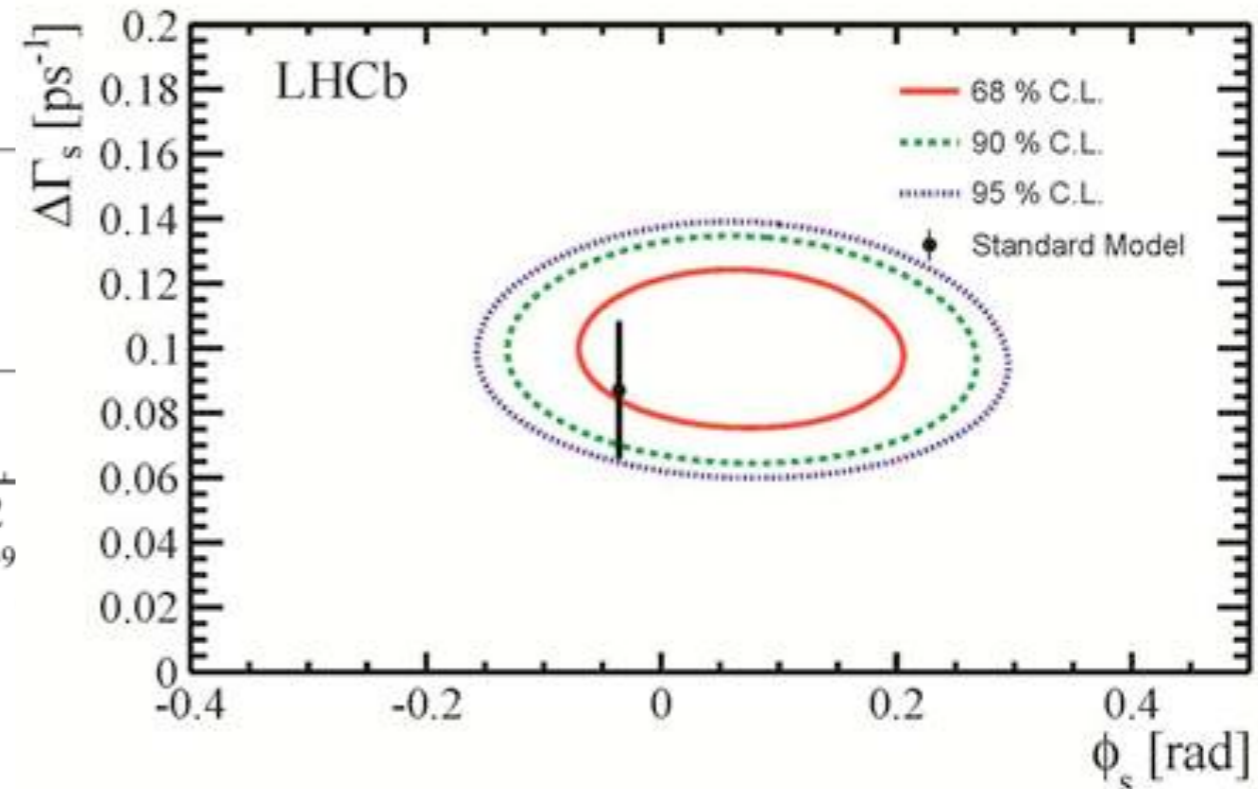
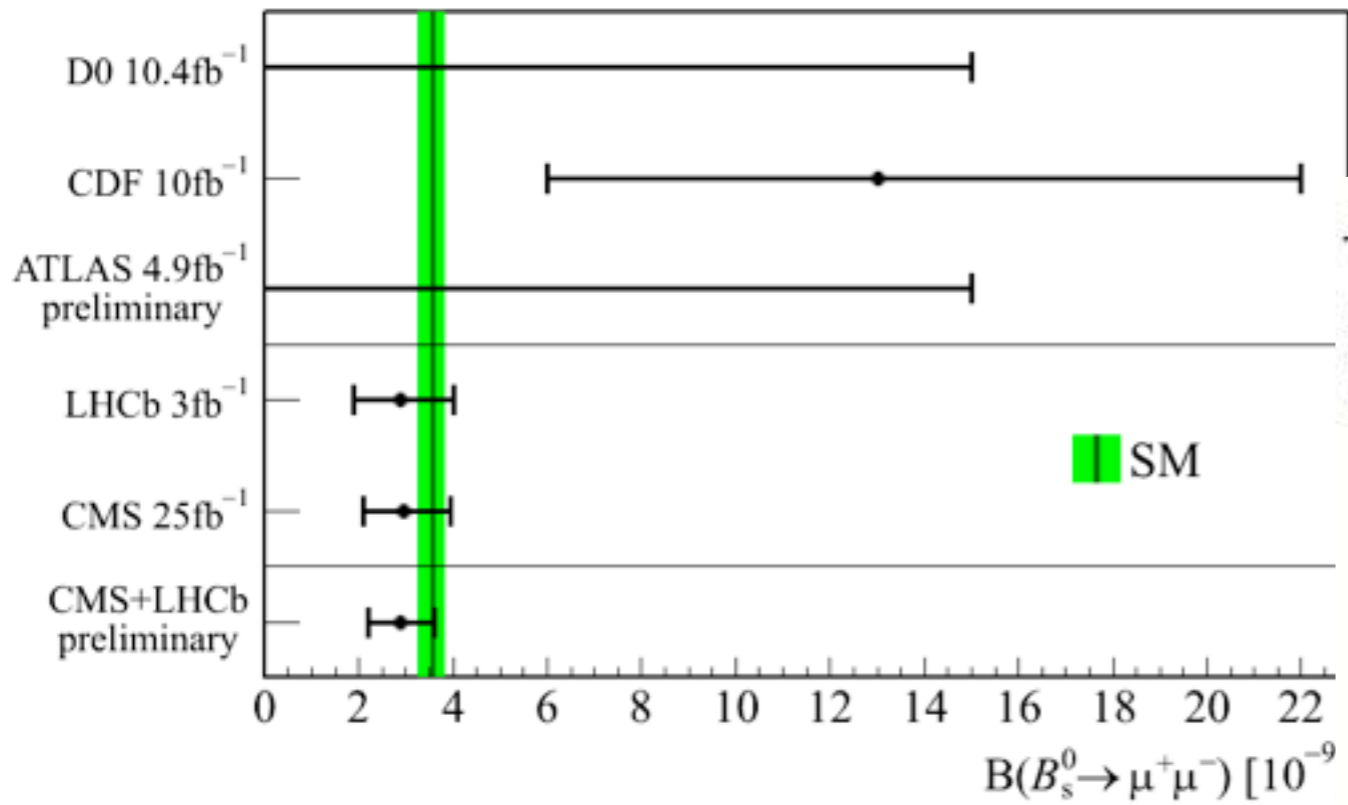
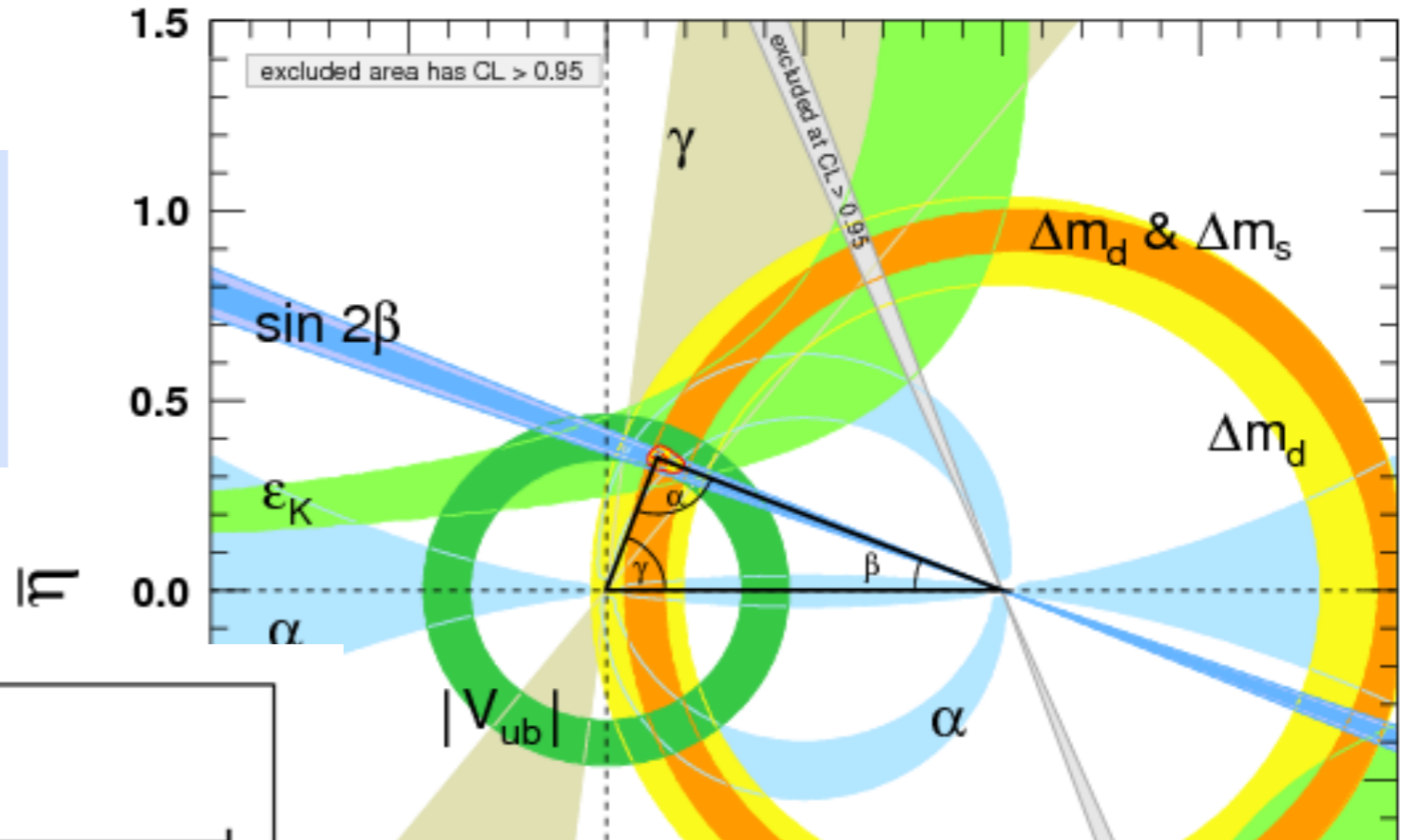
$$m_{\tilde{q}} \gtrsim 1.8 \text{ TeV}$$

$$M_{\tilde{g}} \gtrsim 1.4 \text{ TeV}$$



# Great successes of the SM in the flavor sector

SM looks to work very well.



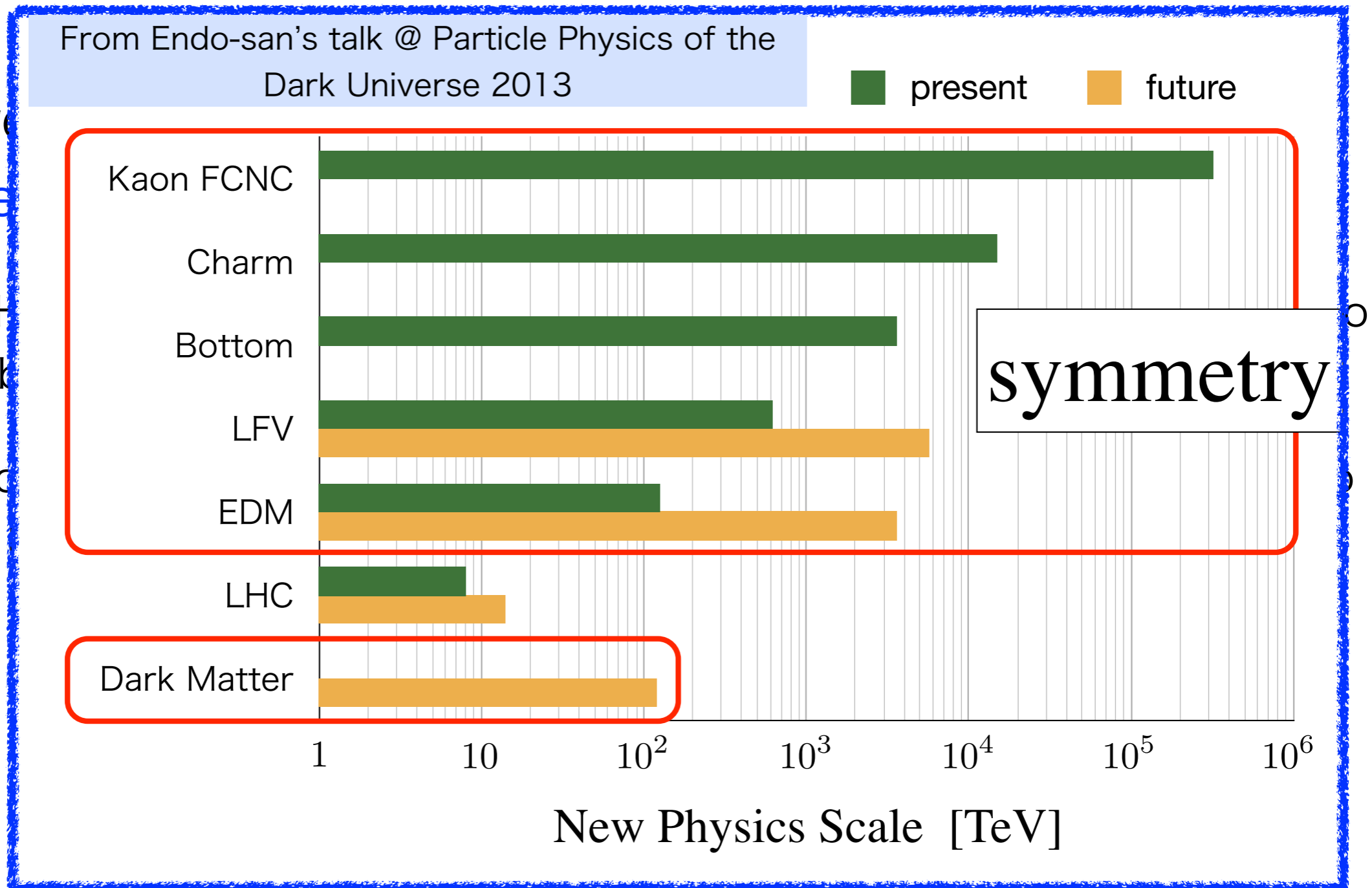
# Why flavor factories?

- In present, LHC experiments have not found any signals of **new physics (NP)** in the high-energy frontier.
  - If LHC finds some NP, flavor experiments play **complementary** roles to probe the flavor sector of the NP.
  - If not, flavor factories (and cosmology) may give the **unique access** to the NP in the high-luminosity frontier.



# Why flavor factories?

- In presence of new physics
  - If LHC probes new physics
  - If not, the



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In both of the situations, we need more observables and more precision!

SuperKEKB, LHCb, LFV, g-2, EDM, K, neutrino, ...

# NP search by the flavor observables

## Strategies

- For **hadronic observables that are SM consistent** but still have a lot of room for NP, such as  $B_q \rightarrow \mu^+ \mu^-$ ,  $\Delta M_q$ ,  $\Delta \Gamma_q$ ,  $a_{\text{sl}}^q$ ,  $\beta_s$  and  $\beta$ , both experimental and theoretical efforts are required to pin down the existence of NP. (Correlation and global analyses may help)
- Resolving and understanding of remaining **discrepancies**: muon  $g-2$ ,  $B \rightarrow D^{(*)} \tau \nu$ , dimuon asymmetry,  $V_{ub}$ ,  $B \rightarrow K^{(*)} \mu^+ \mu^-$ ,  $\beta$  ....
- In the SM background free experiment, such as **LFVs and EDMs**, just FIND THE SIGNAL.

## Implications on NP models

- Tendency of possible NP effects are constrained by precisely-measured flavor observables.
- Consider the NP models which explain existing anomalies.
- Consider (theoretically and/or experimentally) well-motivated models which predict flavor signals.

# Outline

1. Introduction

2. Comparison of experimental results and SM predictions

- Precise measurements and calculations in the flavor physics
- Remaining anomalies(?)

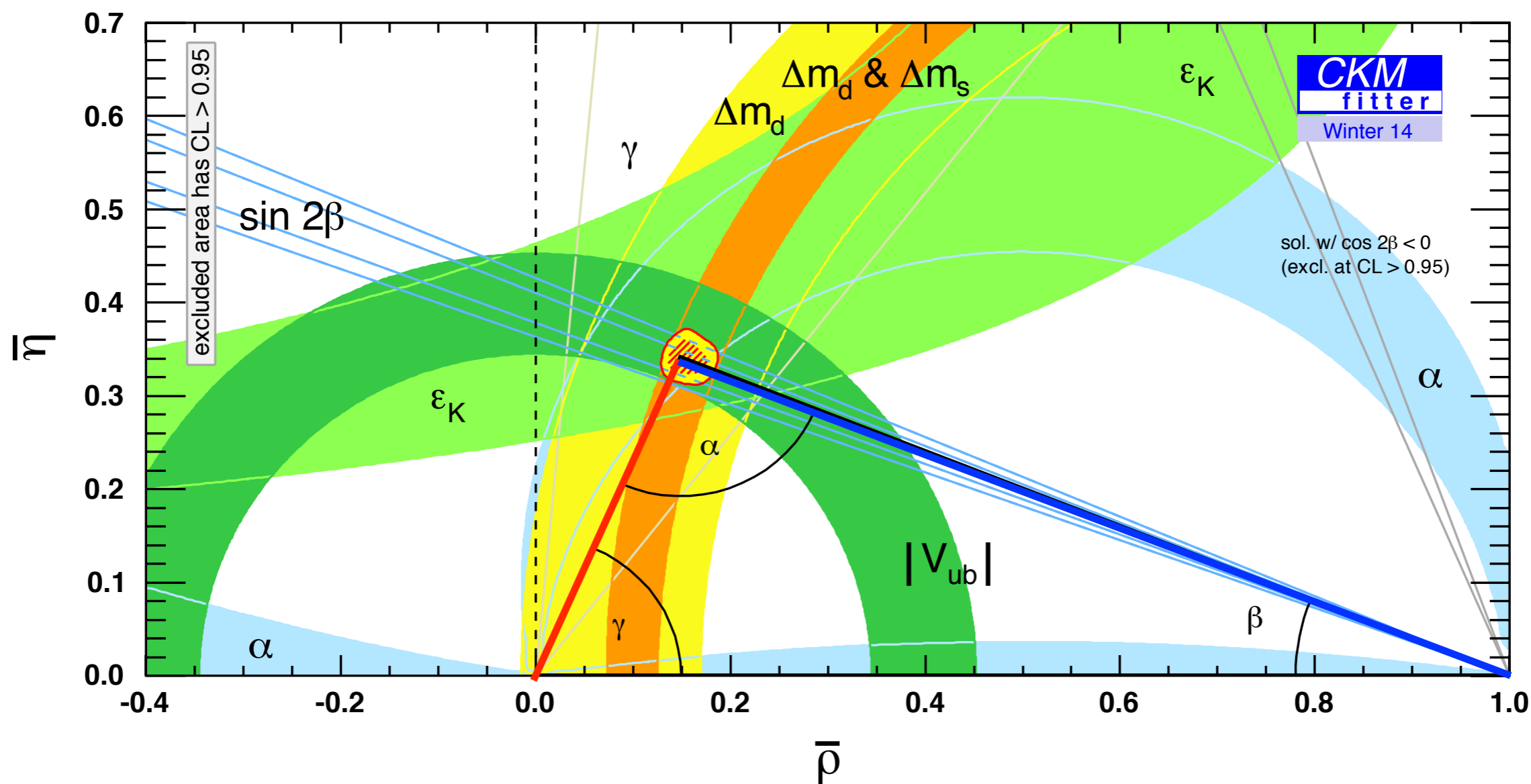
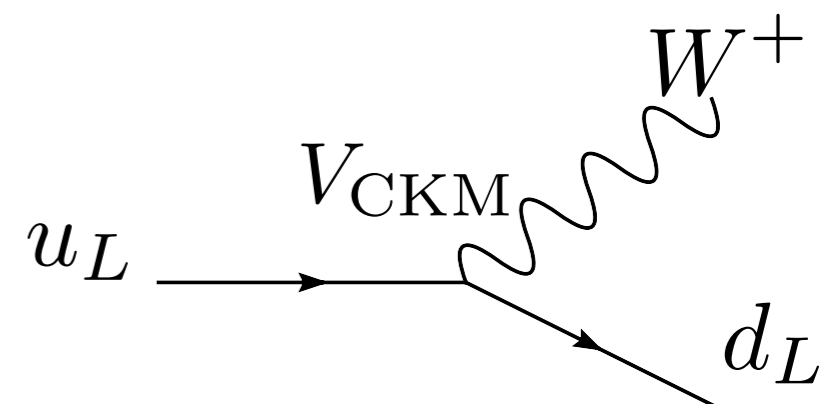
3. LFVs and EDMs

- Implications on SUSY search

4. Summary

まずはSMと実験がよく一致しているこれから

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



# Comparison btw SM and Exp (I)

- B meson mixing

$$\Delta M_d(\text{SM}) = (0.543 \pm 0.091) \text{ ps}^{-1}$$

$$\Delta M_d(\text{Exp}) = (0.510 \pm 0.004) \text{ ps}^{-1}$$

$$\Delta M_s(\text{SM}) = (17.3 \pm 2.6) \text{ ps}^{-1}$$

$$\Delta M_s(\text{Exp}) = (17.69 \pm 0.08) \text{ ps}^{-1}$$

$$\Delta\Gamma_s(\text{HQE}) = (0.087 \pm 0.021) \text{ ps}^{-1}$$

$$\Delta\Gamma_s(\text{Exp}) = (0.081 \pm 0.011) \text{ ps}^{-1}$$

$$\frac{\Delta\Gamma_d}{\Gamma_d}(\text{HQE}) = (0.42 \pm 0.08) \%$$

$$\frac{\Delta\Gamma_d}{\Gamma_d}(\text{HFAG}) = (1.5 \pm 1.8) \%$$

$$\frac{\Delta\Gamma_d}{\Gamma_d}(\text{D0}) = (0.5 \pm 1.38) \%$$

$$\frac{\Delta\Gamma_d}{\Gamma_d}(\text{LHCb}) = (-4.4 \pm 2.7) \%$$



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Lattice inputs

$$\Delta\Gamma_s(\text{HQE}) = (0.087 \pm 0.011) \text{ ps}^{-1}$$

$$F_q \sqrt{\hat{B}_q} = 216(16), 266(18) \text{ MeV}$$

$$\frac{\Delta\Gamma_d}{\Gamma_d}(\text{HQE}) = (0.42 \pm 0.18) \%$$

• central values    • errors

$$\frac{\Delta\Gamma_d}{\Gamma_d}(\text{D0}) = (0.5 \pm 1.38) \%$$

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Large NP room  
for  $\Delta \Gamma_d$

$$\frac{\Delta \Gamma_d}{\Gamma_d}(\text{LHCb}) = (-4.4 \pm 2.7) \%$$

# Comparison btw SM and Exp (II)

$$V_{ub}(\text{excl}) = 3.42(31) \times 10^{-3} \quad V_{ub}(\text{incl}) = 4.40(25) \times 10^{-3}$$

Buras and Girschbach (2013)

$ V_{ub}  \times 10^3$	3.1	3.4	3.7	4.0	4.3	Experiment
$ \varepsilon_K  \times 10^3$	1.76	1.91	2.05	2.19	2.33	2.228(11)
$\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau) \times 10^4$	0.58	0.70	0.83	0.97	1.12	1.14(22)
$(\sin 2\beta)_{\text{true}}$	0.619	0.671	0.720	0.766	0.808	0.679(20)
$S_{\psi\phi}$	0.032	0.035	0.038	0.042	0.046	<del>0.001(9)</del> $-(0.04^{+0.10}_{-0.13})$

SM predictions for  $\gamma = 68^\circ$

- $V_{ub}$ - $\varepsilon_K$ - $S_{\psi K_S}$  tension is relaxed

$$V_{ub}(\text{excl}) : 3.1 \rightarrow 3.4 \quad \longleftarrow \quad V_{ub}(\text{Belle 2013}) : 3.52$$

$$\mathcal{B}(B \rightarrow \tau\nu)(\text{exp}) : 1.73 \rightarrow 1.14 \quad \longleftarrow \quad \mathcal{B}(B \rightarrow \tau\nu)(\text{Belle 2012}) : 0.72$$

- $|S_{\psi\phi}(\text{NP})| < 0.2$  is still allowed

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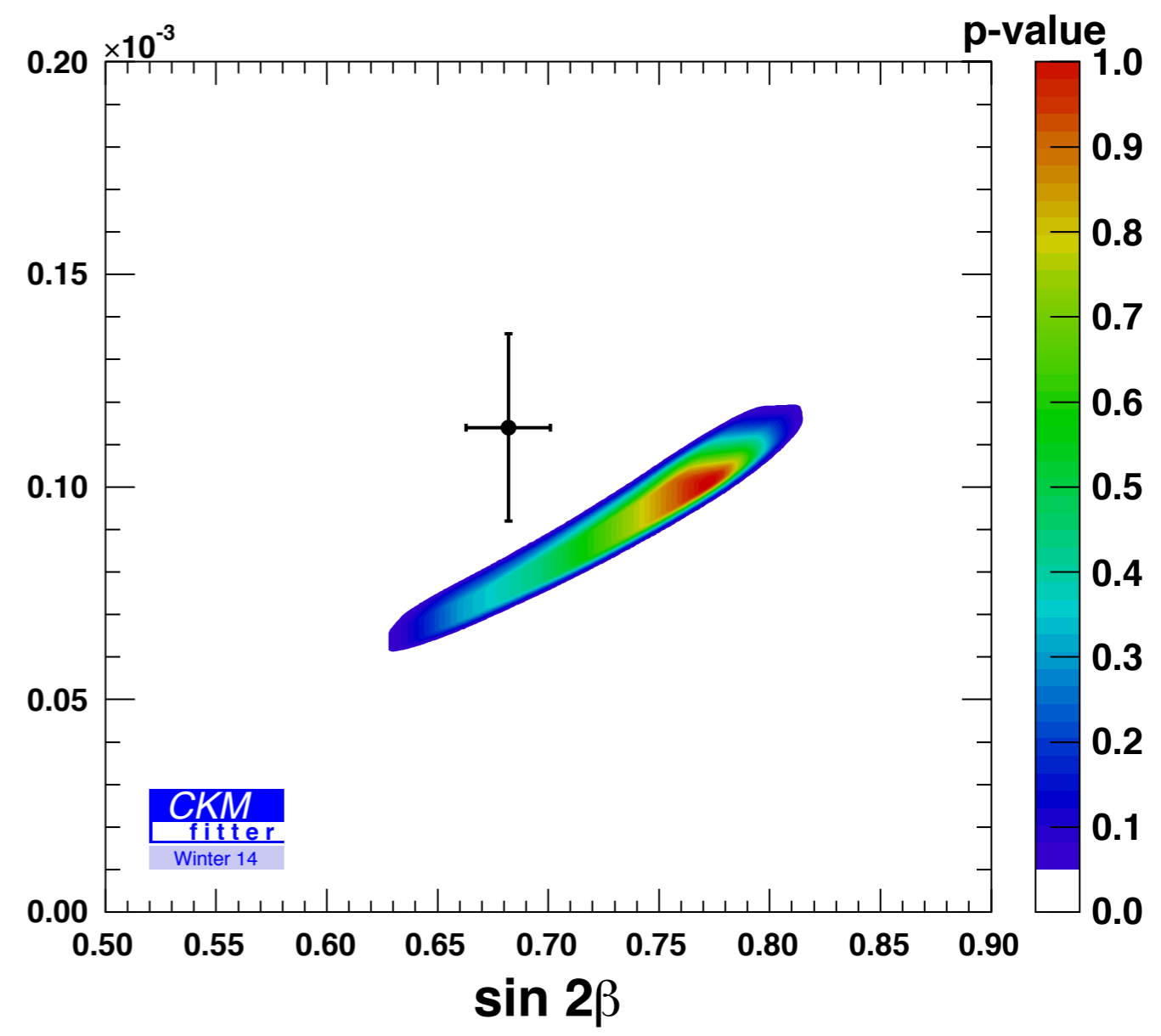
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SM prediction

**BR(B → τν)**



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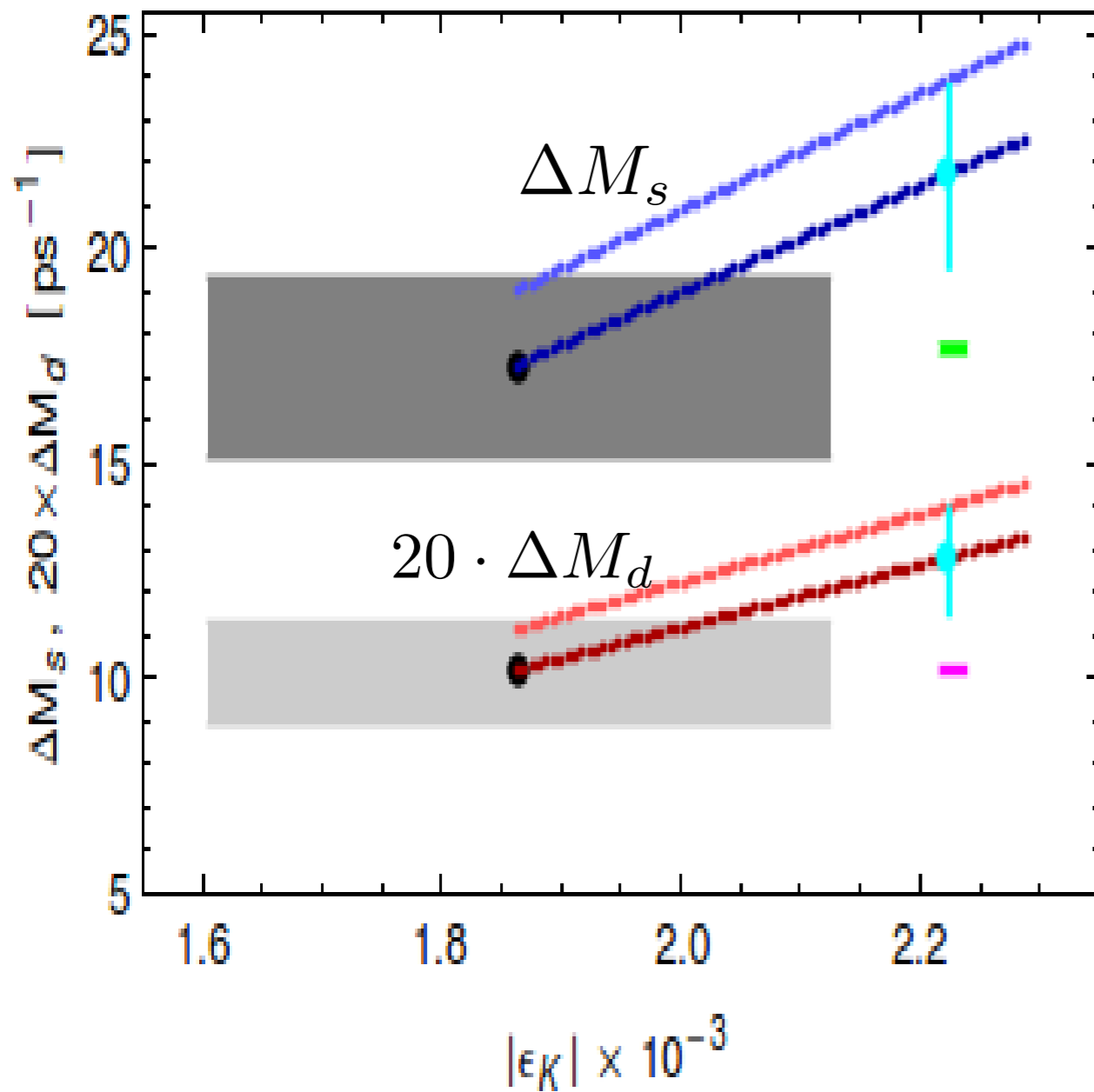
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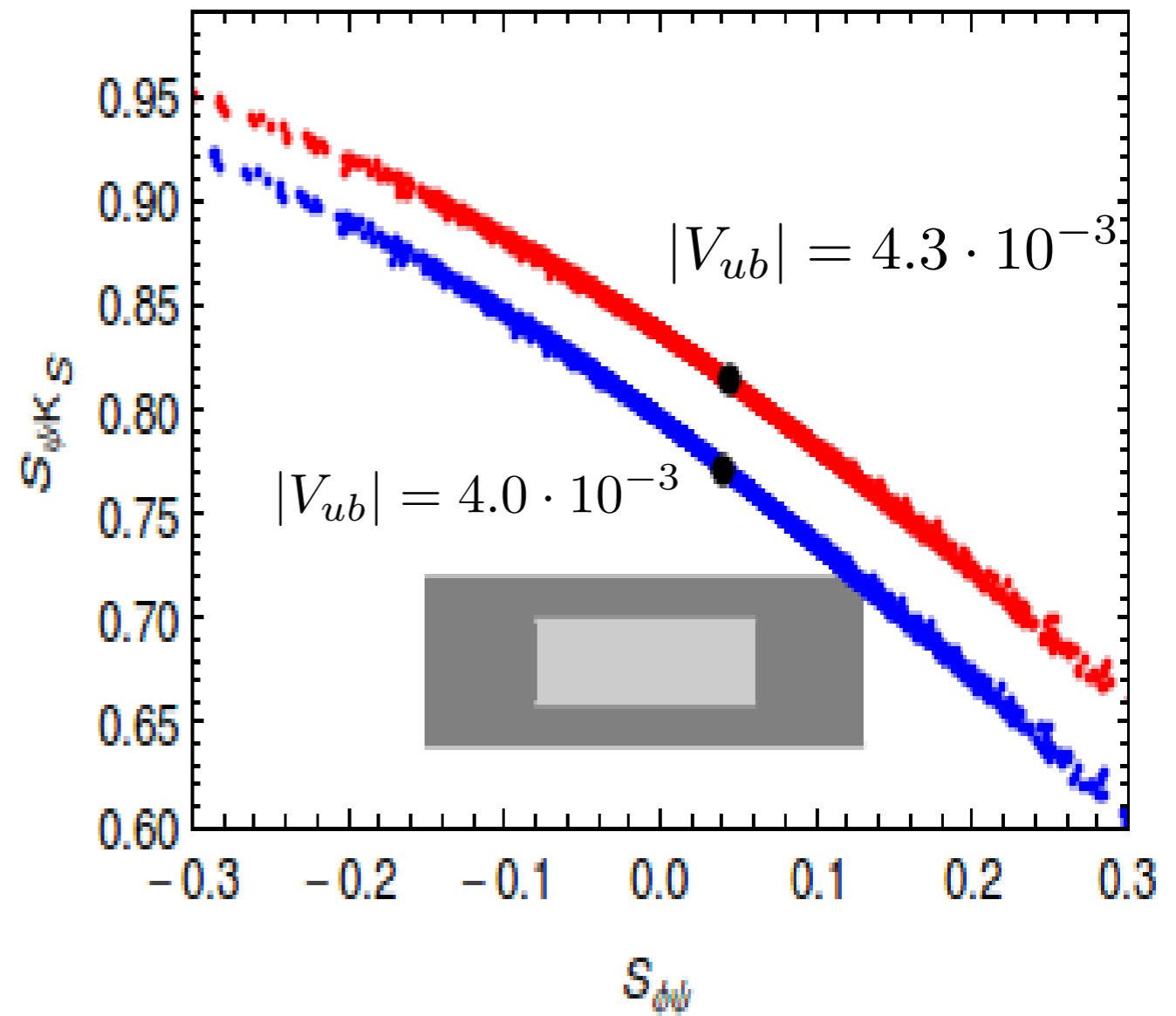
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# $\epsilon_K(\text{SM})$ がやや小さいのが気になる？

CMFV



2HDM<sub>MFV</sub>



See, Buras and Girschbach 1306.3775



# Comparison btw SM and Exp (III)

$$\bar{\mathcal{B}}(B_s \rightarrow \mu^+ \mu^-)(\text{SM}) = (3.65 \pm 0.23) \times 10^{-9}$$

$$\bar{\mathcal{B}}(B_d \rightarrow \mu^+ \mu^-)(\text{SM}) = (1.06 \pm 0.09) \times 10^{-10}$$

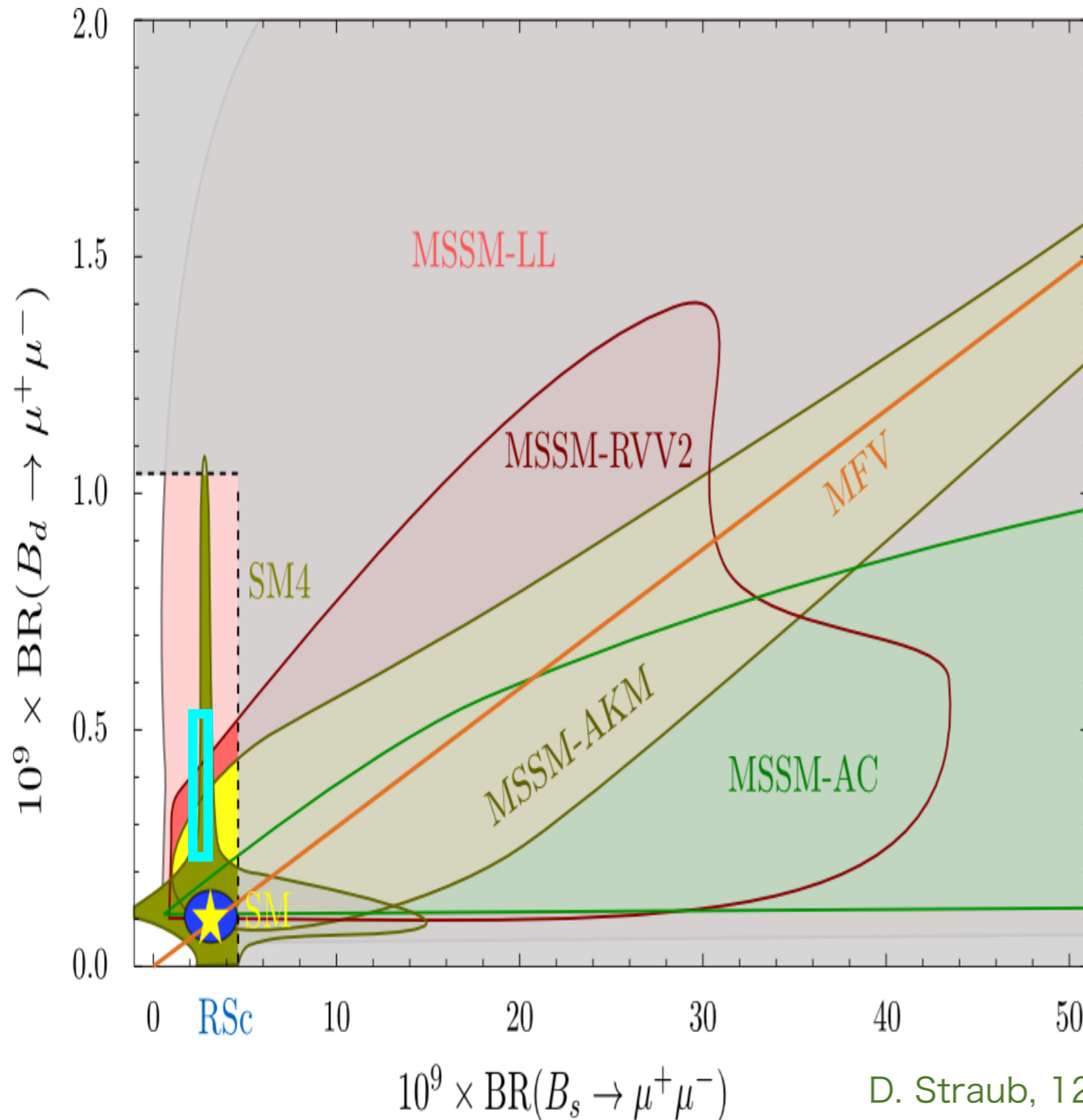
$$\bar{\mathcal{B}}(B_s \rightarrow \mu^+ \mu^-)(\text{Exp}) = (2.9 \pm 0.7) \times 10^{-9}$$

$$\bar{\mathcal{B}}(B_d \rightarrow \mu^+ \mu^-)(\text{Exp}) = (3.6_{-1.4}^{+1.6}) \times 10^{-10}$$

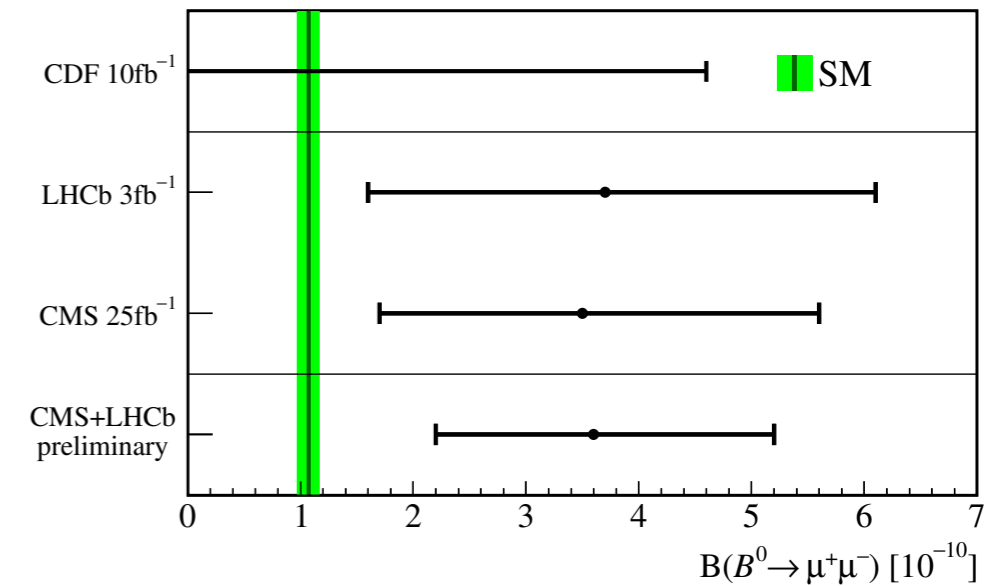
- NNLO-QCD & NLO EW corrections Bobeth et al (2014)
- Average time-integrated branching ratio de Bruyn et al (2012)

$$\bar{\mathcal{B}} = \frac{1 + A_q}{1 - y_q^2} \mathcal{B}^{[t=0]} \quad \text{where} \quad y_q = \frac{\Delta\Gamma_q}{2\Gamma_q} \quad A_q(\text{SM}) = y_q$$
$$y_s = 0.088 \pm 0.014$$

# Implications on NP models (I)



$$B_d \rightarrow \mu^+ \mu^-$$



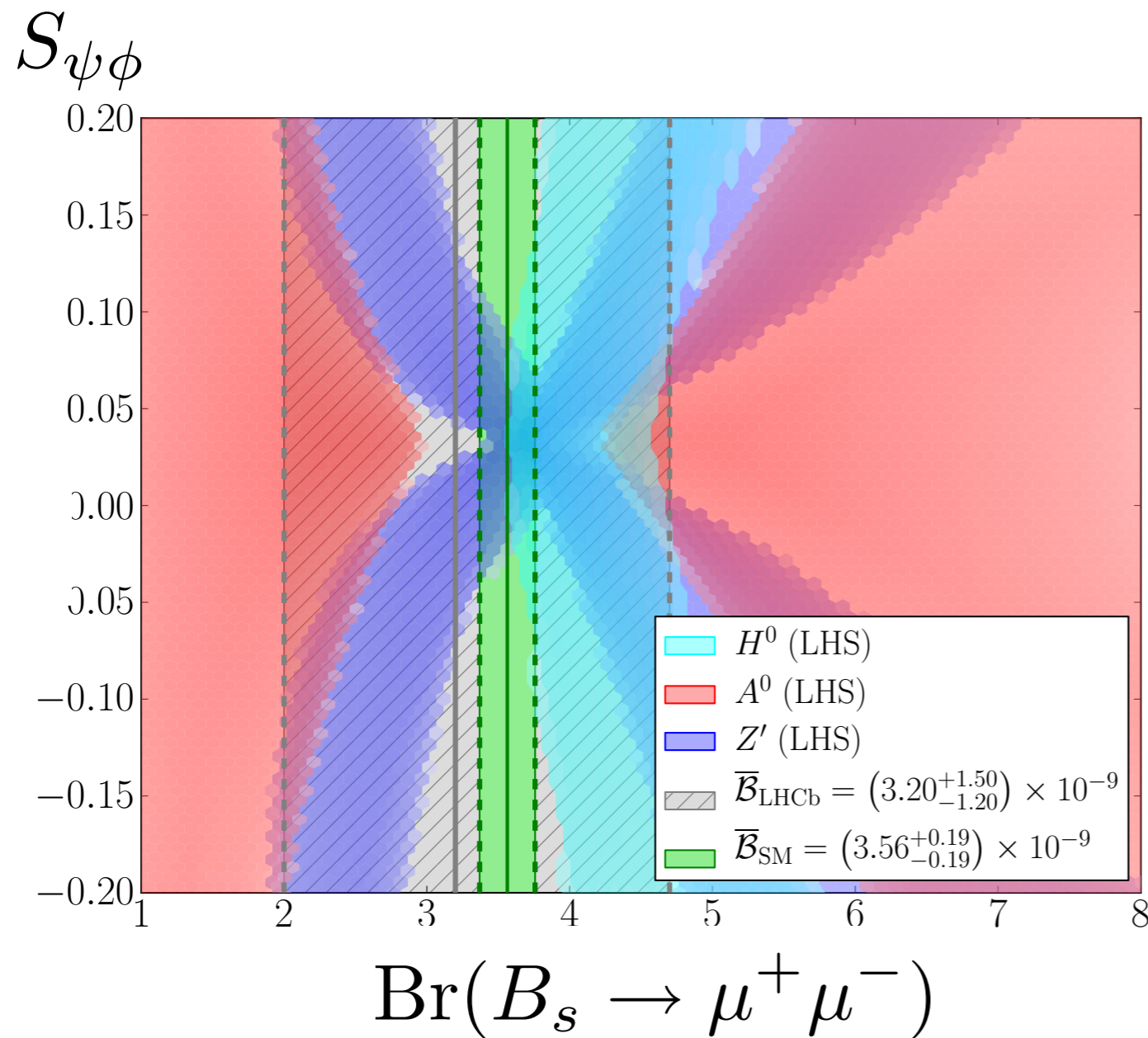
2.4  $\sigma$  above 0

1.6  $\sigma$  above the SM value

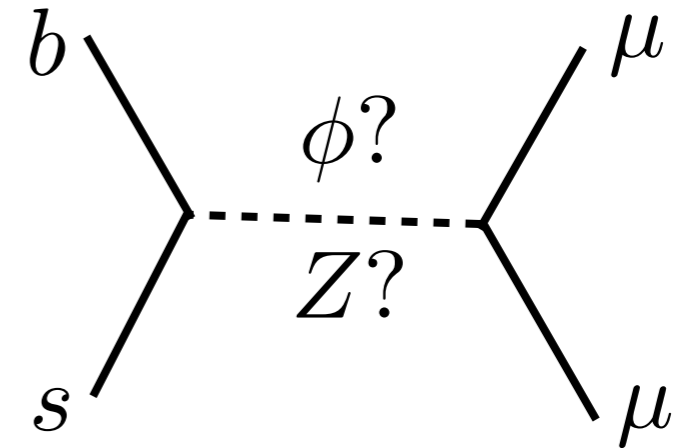
If confirmed,  
proof of non-MFV

D. Straub, 1205.6094

# Implications on NP models (II)



[Buras, Fazio, Girrbach, Kneijens and MN (2013)]



$$\mathcal{B} \sim |A + P|^2 + |S|^2$$

To obtain  $\text{Br} < \text{Br}(\text{SM})$ ,  
interference with SM  
amp. is required.

Note,

$h_{\text{SM}} + \text{FV } b\text{-}s \text{ coupling}$

→ 8 % increase at most  
+ P-scalar muon coupling

→  $\text{Br} < \text{Br}(\text{SM})$  is possible

# Remaining anomalies (?)

- muon  $g-2$
- $B \rightarrow D^{(*)} \tau \nu$
- Dimuon asymmetry
- $B \rightarrow K^{(*)} \mu^+ \mu^-$
- $V_{ub}$
- $\beta$

# Like-sign dimuon asymmetry (~2012)

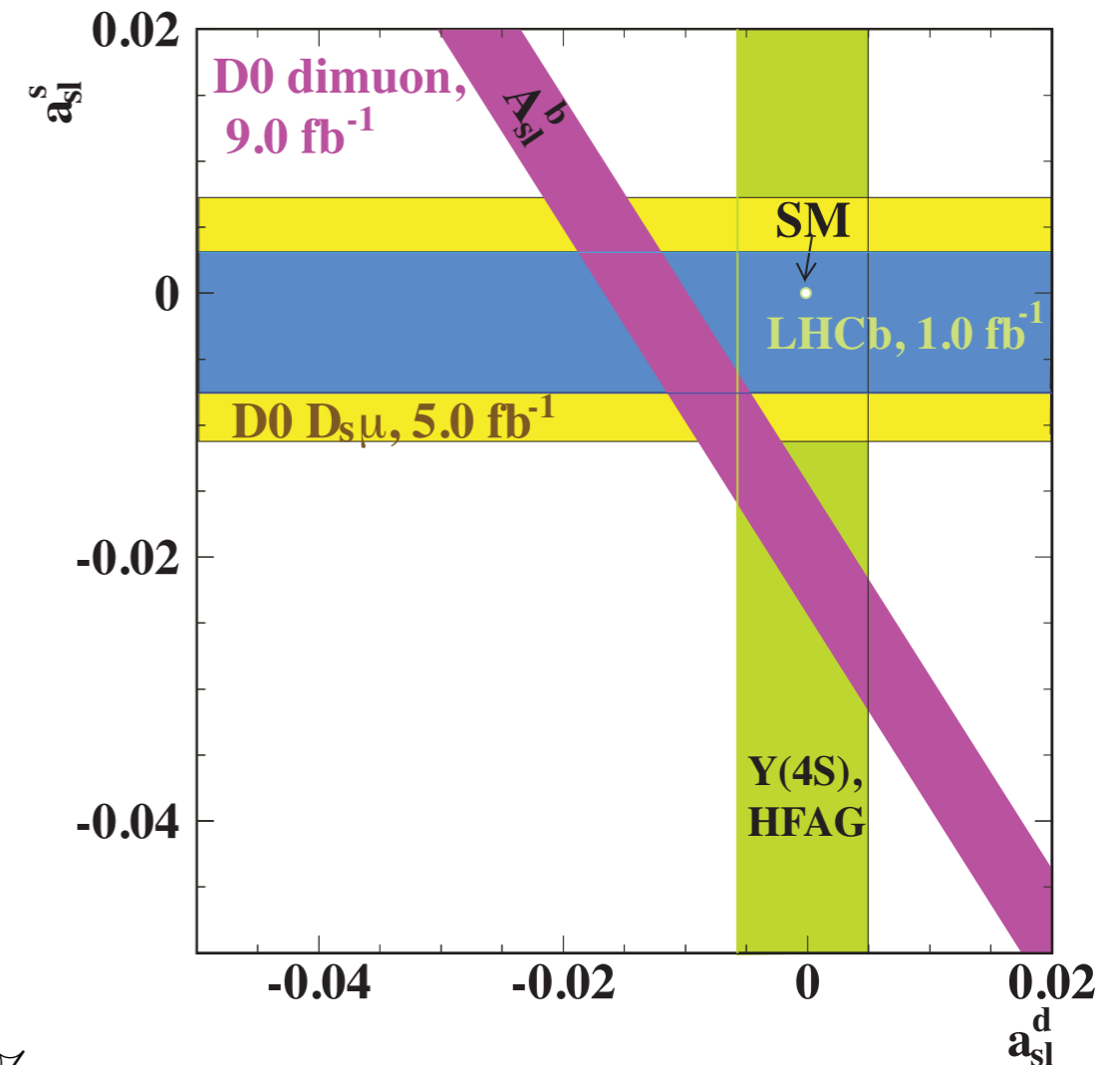
- D0 collaboration measured the like-sign dimuon asymmetry  $A_{CP}$ , which is interpreted as a **CP-violating effect in B meson mixing**.

$$A_{CP} \propto A_{sl}^b \equiv C_d a_{sl}^d + C_s a_{sl}^s$$

$$\begin{aligned} p\bar{p} &\rightarrow b\bar{b}X, \\ b &\rightarrow b \text{ hadron} \rightarrow \mu^- \text{ ("right-sign" } \mu), \\ \bar{b} &\rightarrow \underline{B_{(s)}^0} \rightarrow \bar{B}_{(s)}^0 \rightarrow \mu^- \text{ ("wrong-sign" } \mu); \end{aligned}$$

$$A_{sl}^b(\text{D0}, 9 \text{ fb}^{-1}) = (-0.787 \pm 0.172 \pm 0.093)\%$$

$$A_{sl}^b(\text{SM}) = (-0.028_{-0.006}^{+0.005})\% \quad \mathbf{3.9\sigma}$$



- LHCb confirmed SM consistent semi-leptonic asymmetry for  $B_s$  mesons.

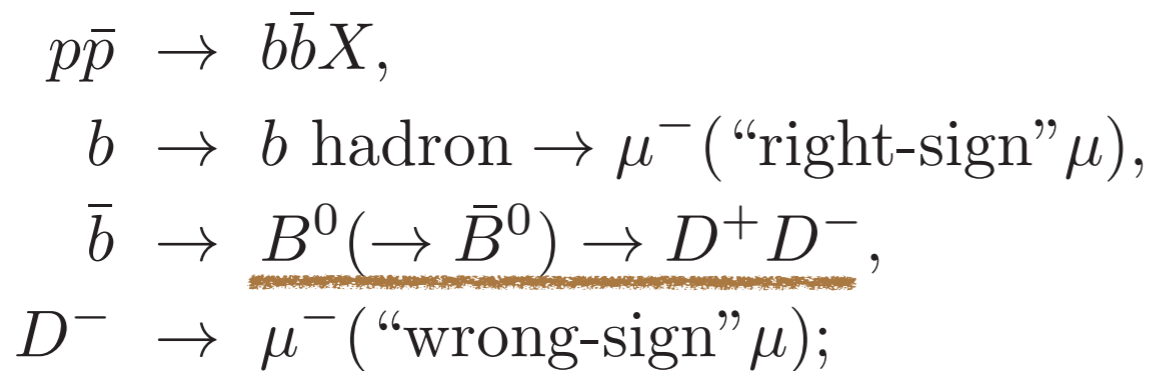
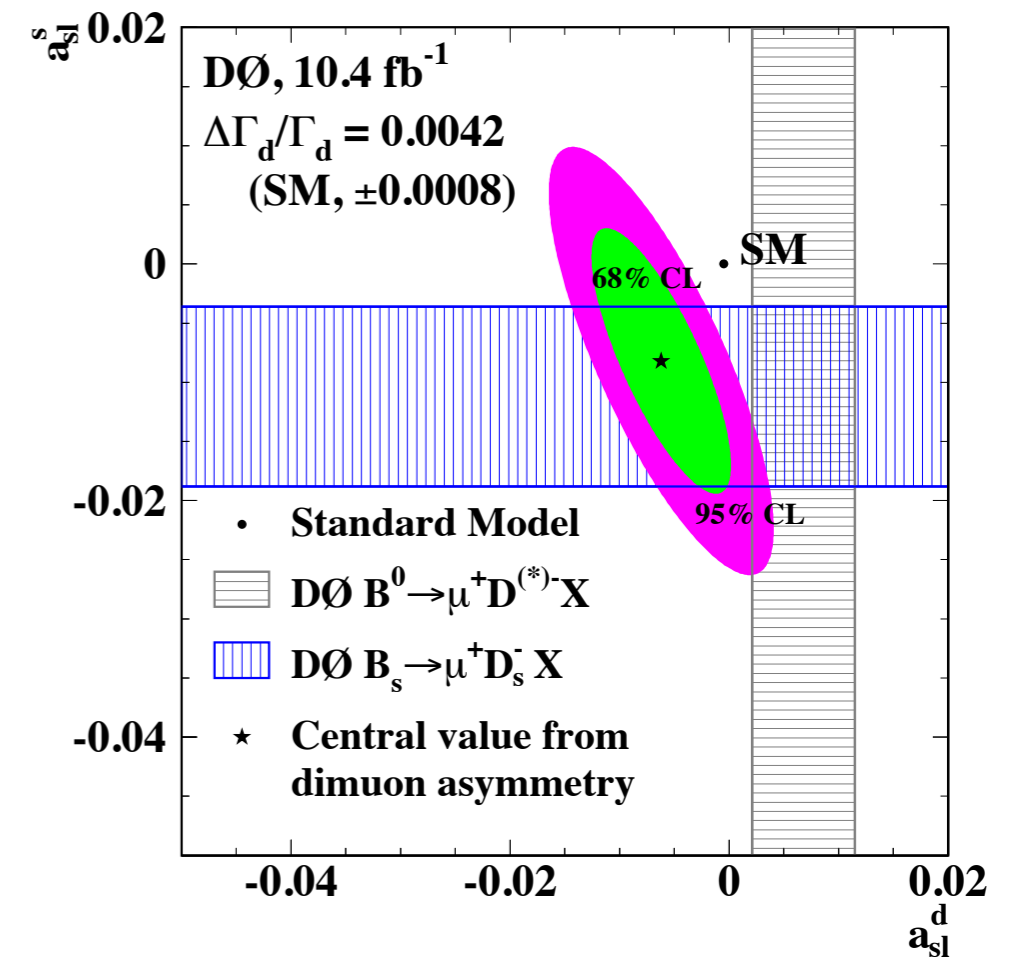
# Like-sign dimuon asymmetry (2013)

- New contributions proportional to decay rate differences were found.

$$A_{CP} \propto A_{sl}^b + C_{\Gamma_d} \frac{\Delta\Gamma_d}{\Gamma_d} + C_{\Gamma_s} \frac{\Delta\Gamma_s}{\Gamma_s}$$

CP violation in the interference of B meson decay amplitude with and without mixing.

Borissov and Hoeneisen (2013)



Assuming SM decay rate differences,

$$A_{sl}^b = (-0.496 \pm 0.153 \pm 0.072)\% \quad 2.8\sigma$$

3.4σ

Assuming SM semi-leptonic asymmetry,

$$\Delta\Gamma_d/\Gamma_d = (+2.63 \pm 0.66) \times 10^{-2} \quad 3.3\sigma$$

D0 collaboration (2013)

# New Physics in $\Delta \Gamma_d$

Bobeth, Haisch, Lenz, Pecjak, Tetlalmatzi-Xolocotzi (2013)

- D0 measurements may be explained by **possible NP contributions to  $\Delta \Gamma_d$** .
  - The SM prediction of  $\Delta \Gamma_s$  agrees quite well with the experimental value.
  - $\Delta \Gamma_d$  is triggered by the CKM-suppressed decay  $b \rightarrow ccd$  ( $\text{Br} \sim 1\%$ ). Thus, large modification of  $\Gamma(b \rightarrow ccd)$  can be hidden in the uncertainties of  $\Gamma_{\text{tot}}$ .
  - The SM contribution to  $\Delta \Gamma_d$  has a large cancellation between individual (charm and up) contributions. Then, NP effects can be easily enhanced compared to the SM one.
- Model-independent analysis:

$$\mathcal{H} = \frac{4G_F}{\sqrt{2}} \sum_{p,p'=u,c} V_{pd}^* V_{p'b} (C_1^{pp'} Q_1^{pp'} + C_2^{pp'} Q_2^{pp'}) \quad \left( C_i^{pp'} = C_i^{\text{SM}} + \Delta C_i^{pp'} \right)$$

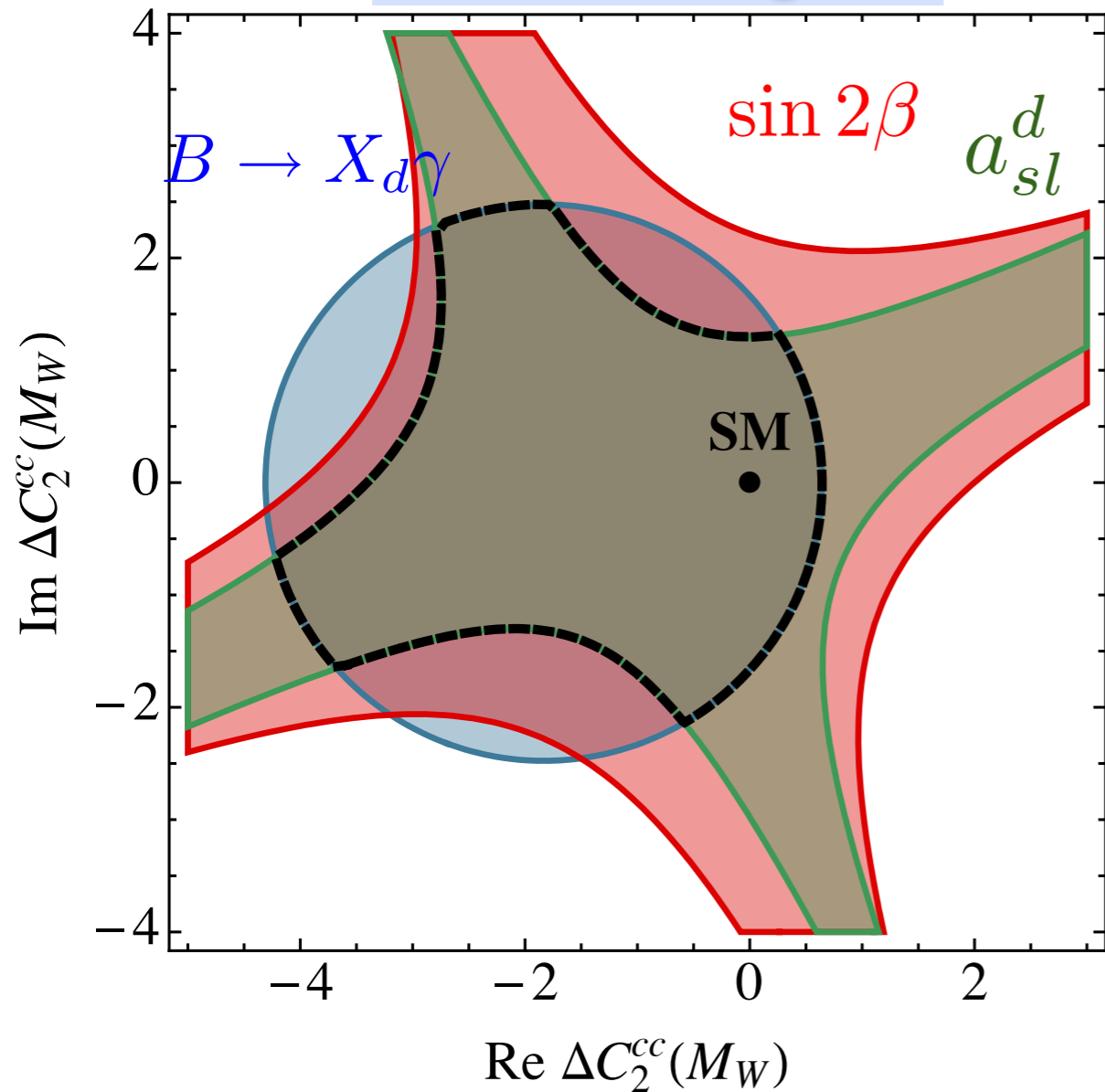
where

$$Q_1^{pp'} = (\bar{d}^\alpha \gamma^\mu P_L p^\beta) (\bar{p}'^\beta \gamma_\mu P_L b^\alpha)$$
$$Q_2^{pp'} = (\bar{d}^\alpha \gamma^\mu P_L p^\alpha) (\bar{p}'^\beta \gamma_\mu P_L b^\beta)$$

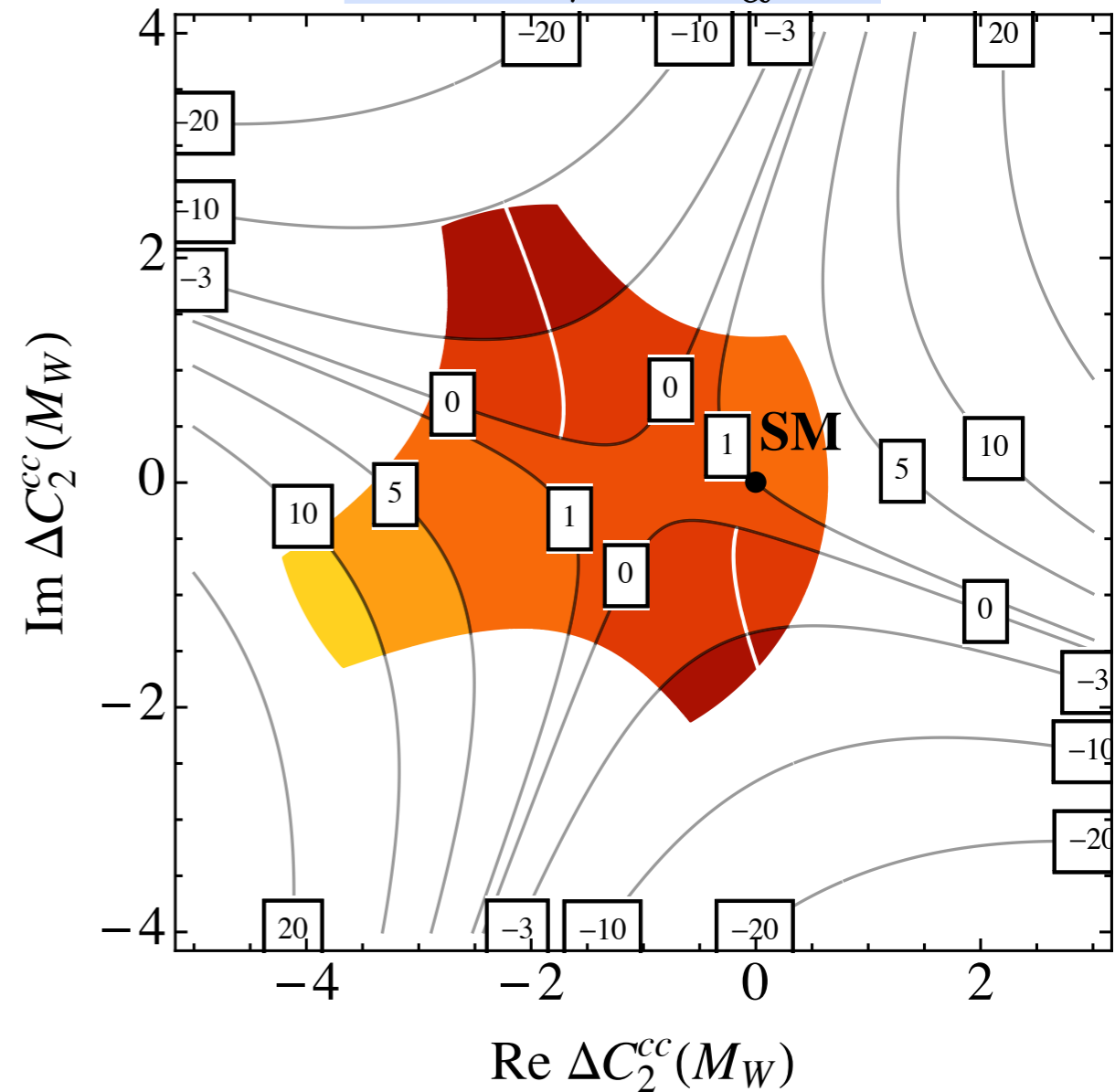


# New Physics in $\Delta \Gamma_d : b \rightarrow ccd$

Allowed region



$\Delta \Gamma_d / \Delta \Gamma_d^{\text{SM}}$

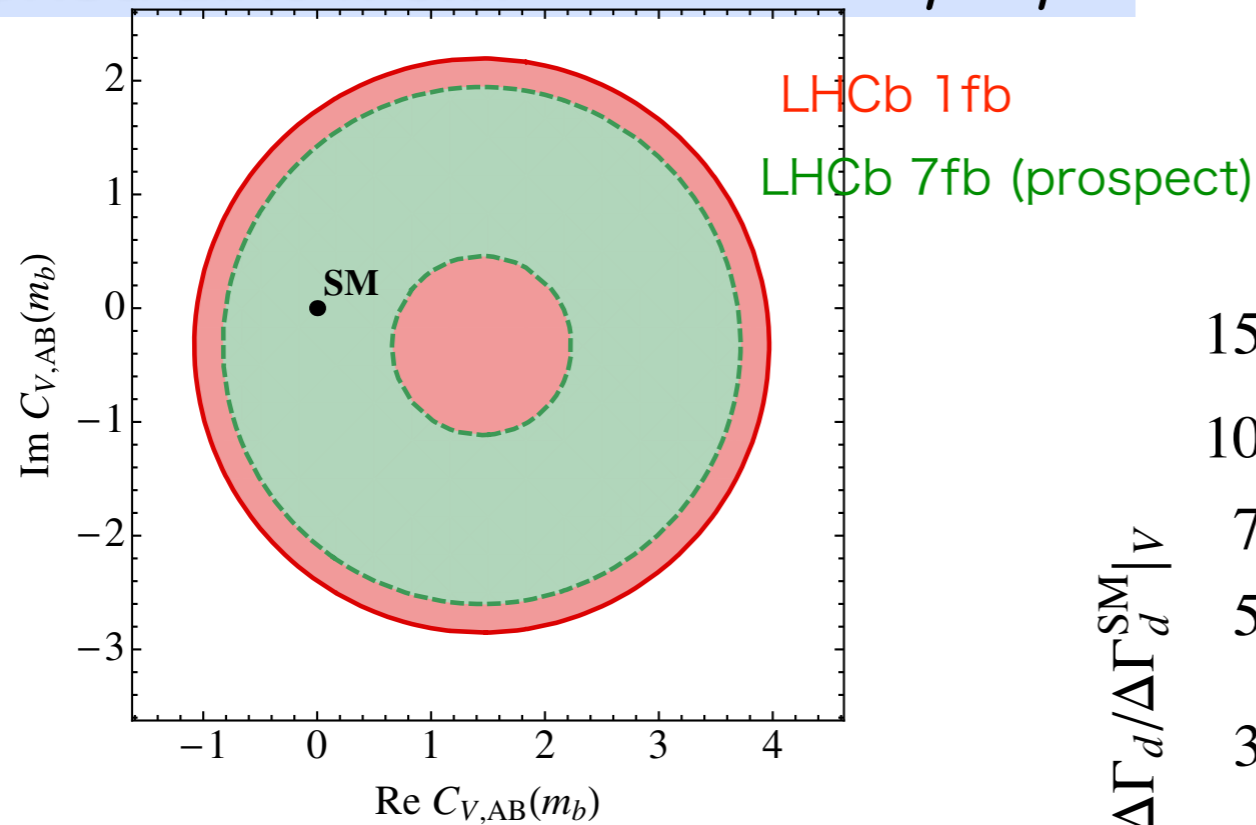


$\Delta \Gamma_d / \Delta \Gamma_d^{\text{SM}} \sim 5$  is possible

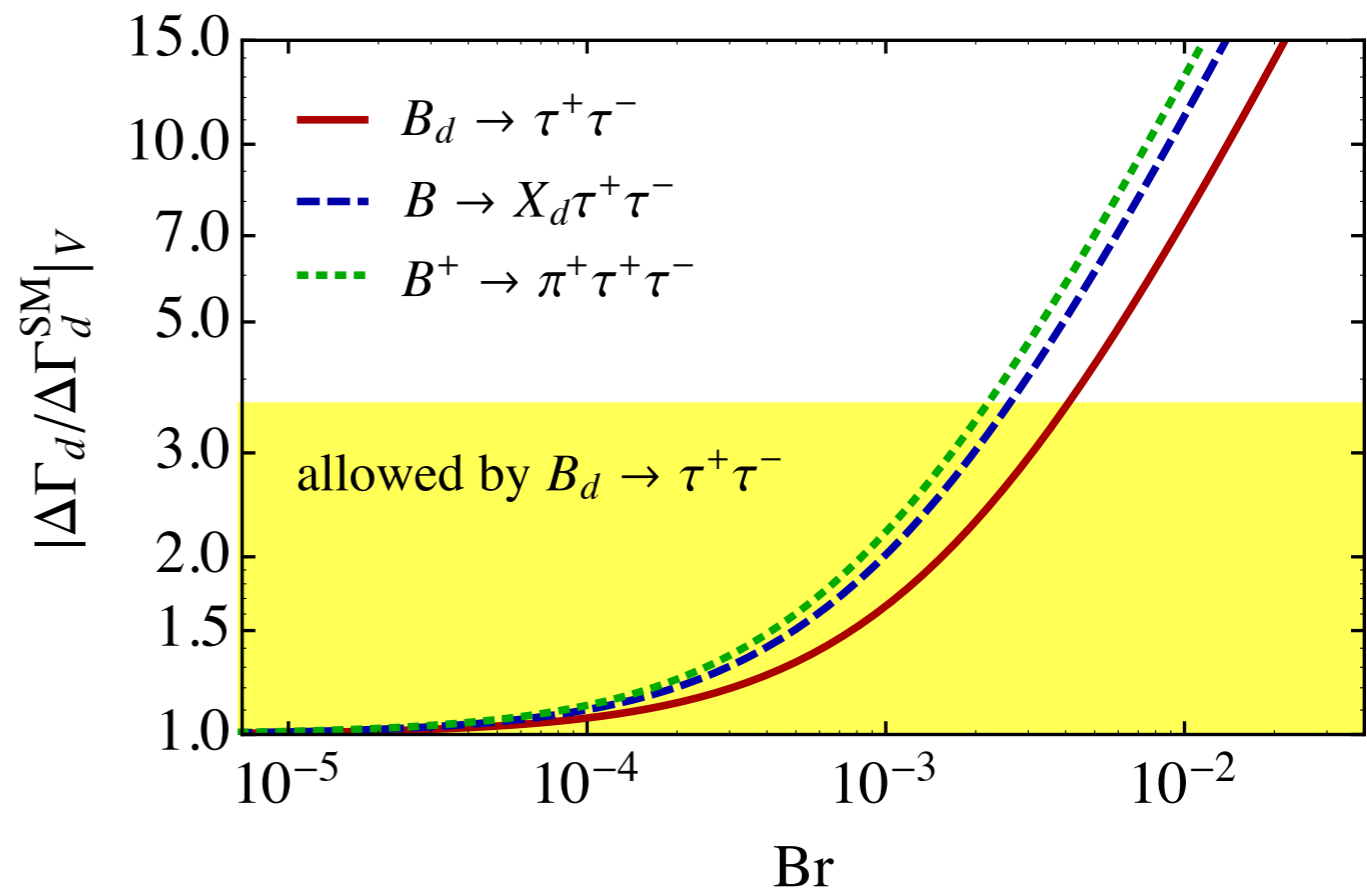
# New Physics in $\Delta \Gamma_d : b \rightarrow \tau \tau d$

Constraint from  $B^+ \rightarrow \pi^+ \mu^+ \mu^-$

(S, V, T operators)



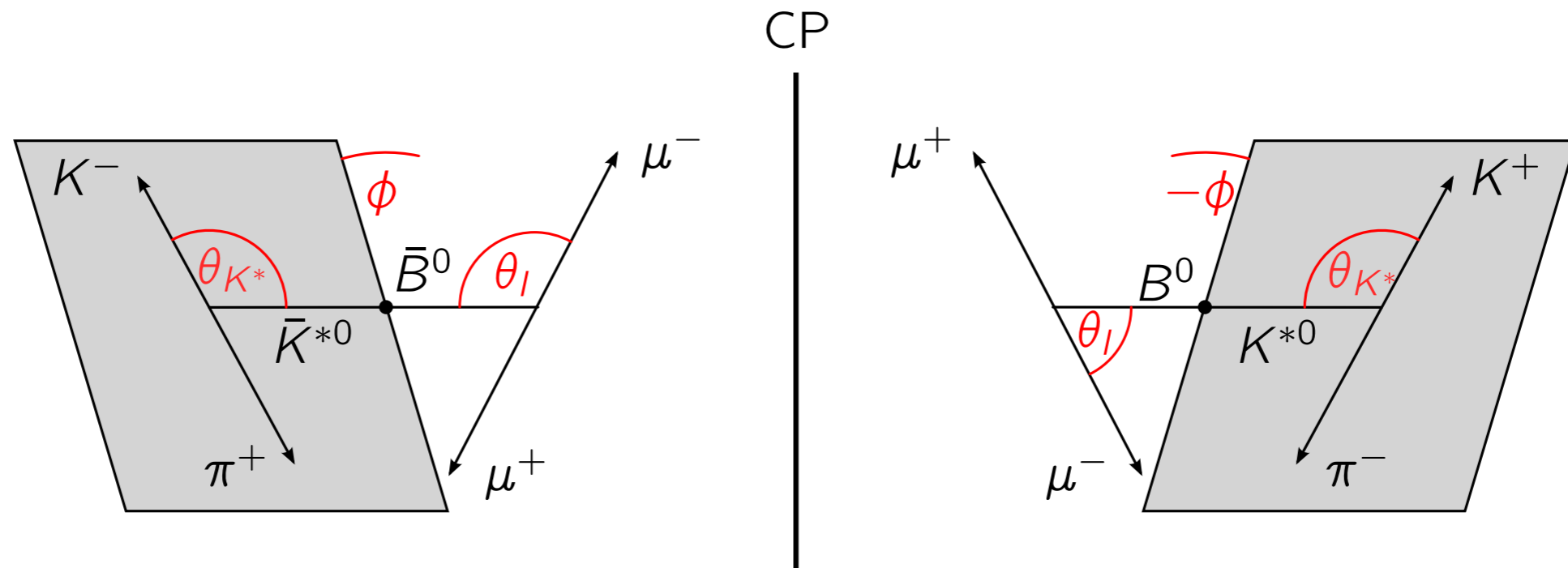
$$\Delta \Gamma_d / \Delta \Gamma_d^{\text{SM}}$$



Constraint	$ C_{V,AB}(m_b) $
$\text{Br}(B_d \rightarrow \tau^+ \tau^-)$	2.2
$\text{Br}(B \rightarrow X_d \tau^+ \tau^-)$	5.3
$\text{Br}(B^+ \rightarrow \pi^+ \tau^+ \tau^-)$	6.2
$\text{Br}(B \rightarrow X_d \gamma)$	—
$\text{Br}(B^+ \rightarrow \pi^+ \mu^+ \mu^-)$	4.0

$\Delta \Gamma_d / \Delta \Gamma_d^{\text{SM}} \sim 3$  is possible

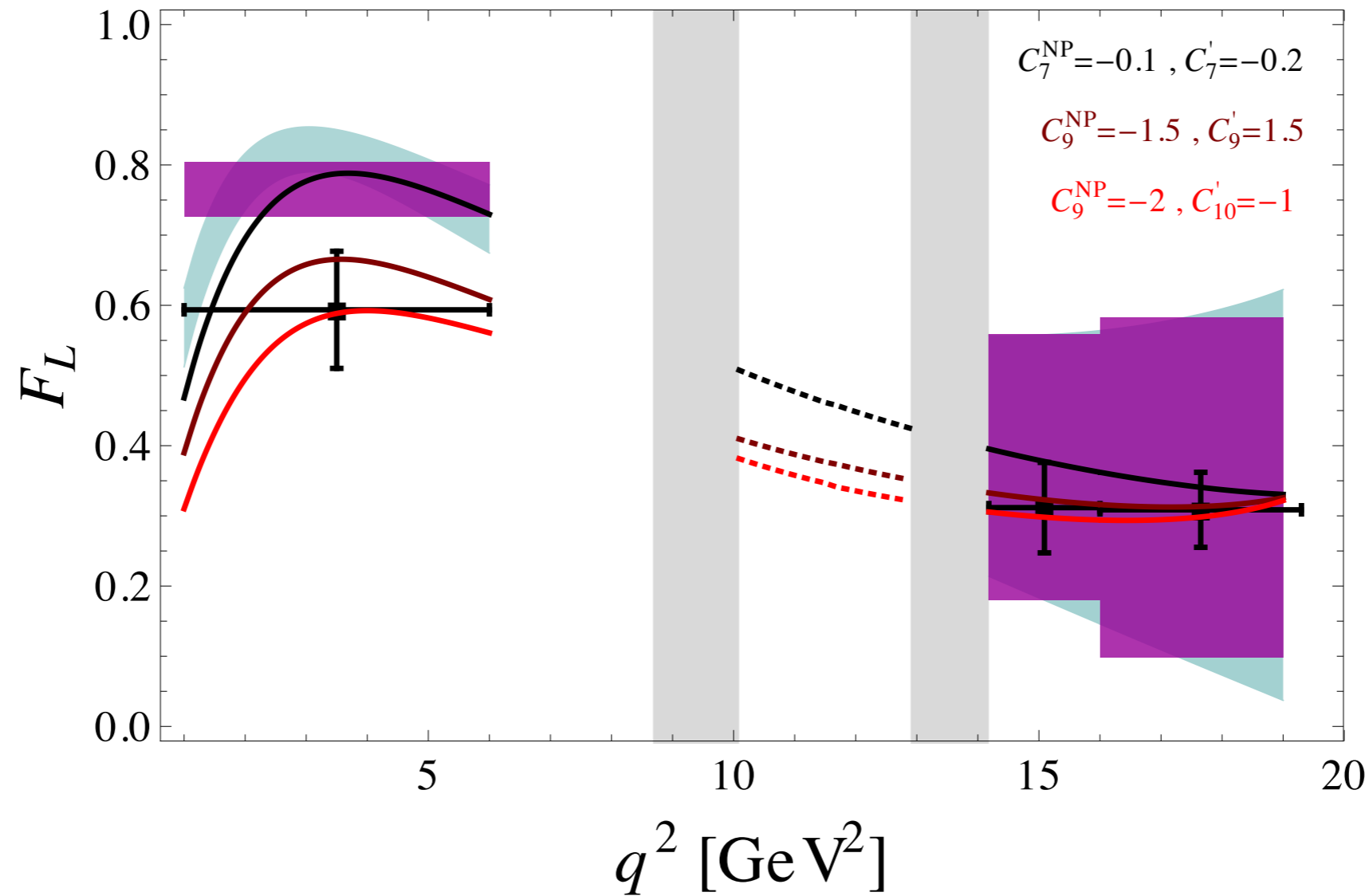
From slides by D. Straub @ KEK-FF2014

 $B \rightarrow K^* \mu^+ \mu^-$  angular observables

$$\frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d \cos \theta_I d \cos \theta_{K^*} d \phi} \sim \sum_i S_i(q^2) f_i(\theta_I, \theta_{K^*}, \phi)$$

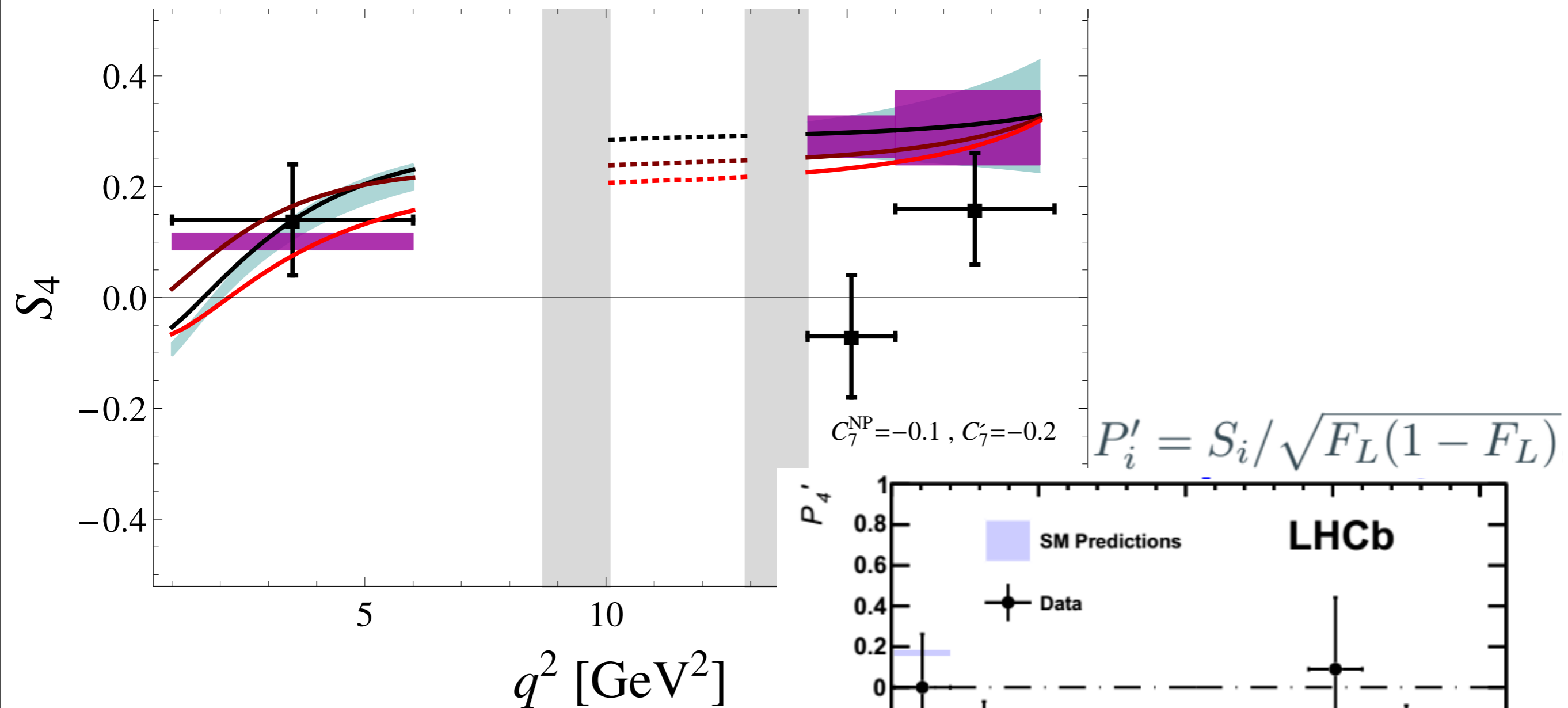
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# SM vs. data: $F_L$ [Altmannshofer and DS 1308.1501]

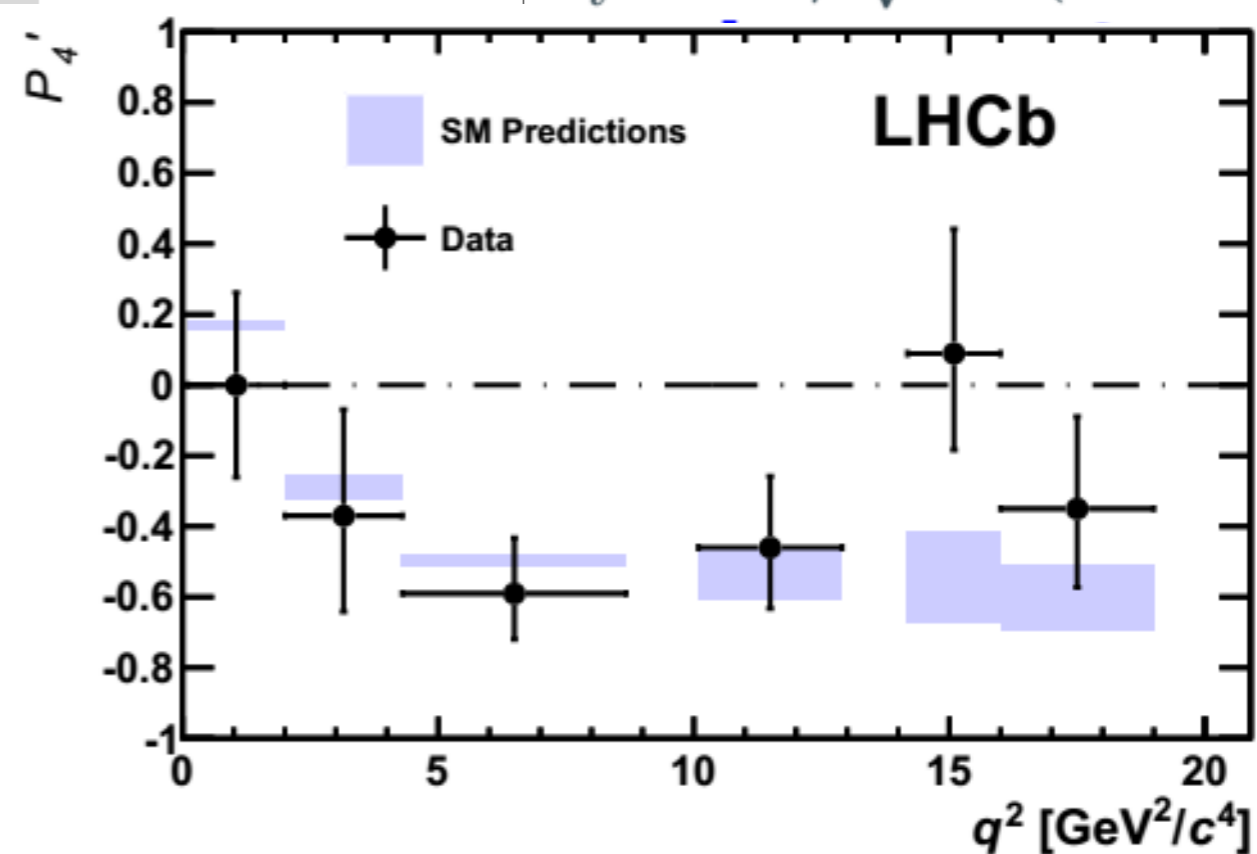


1.9 $\sigma$  tension at low  $q^2$  (driven by ATLAS and BaBar data)

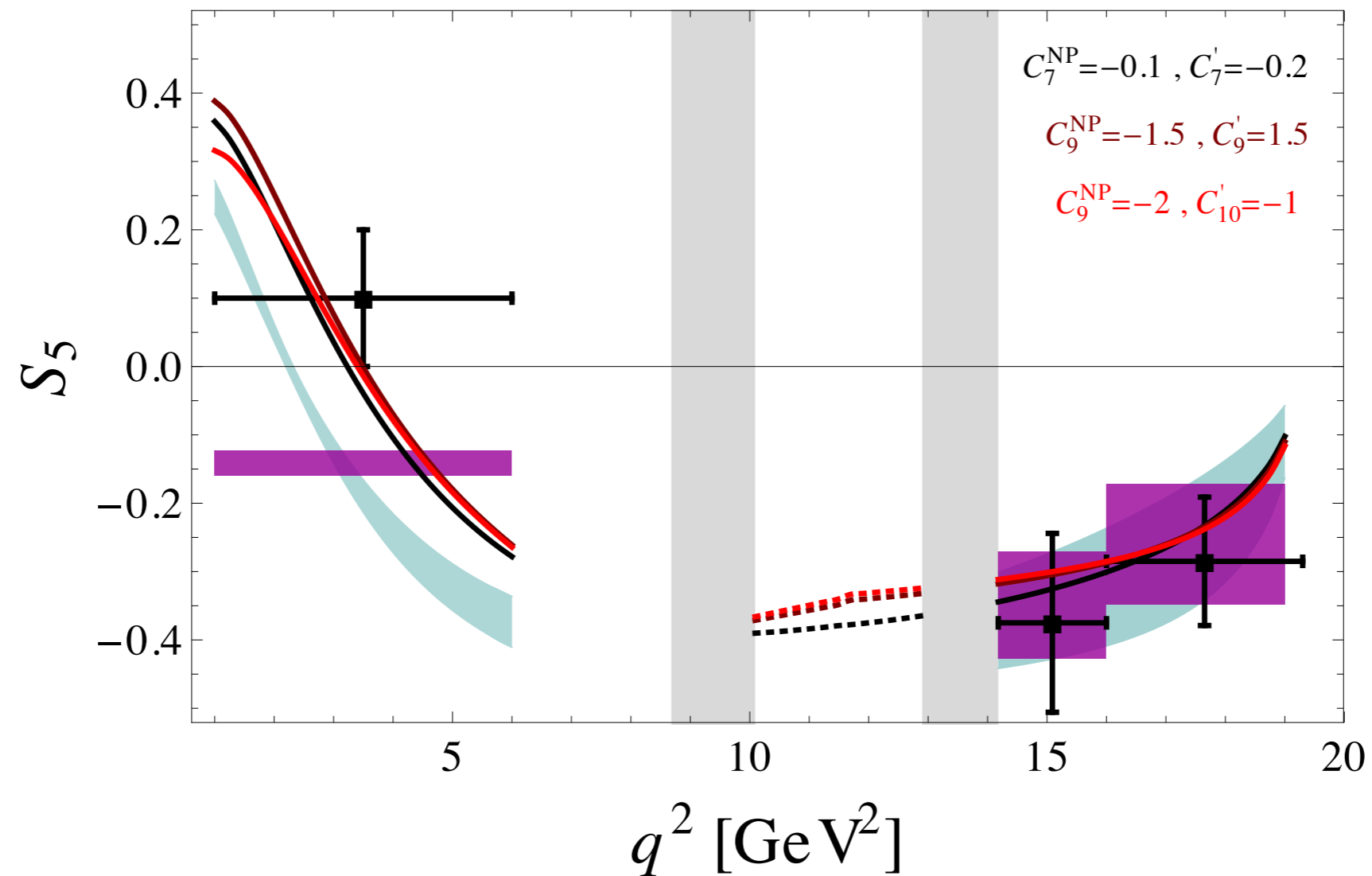
# SM vs. data: $S_4$ [Altmannshofer and DS 1308.1501]



2.8 $\sigma$  tension at high  $q^2$



# SM vs. data: $S_5$ [Altmannshofer and DS 1308.1501]

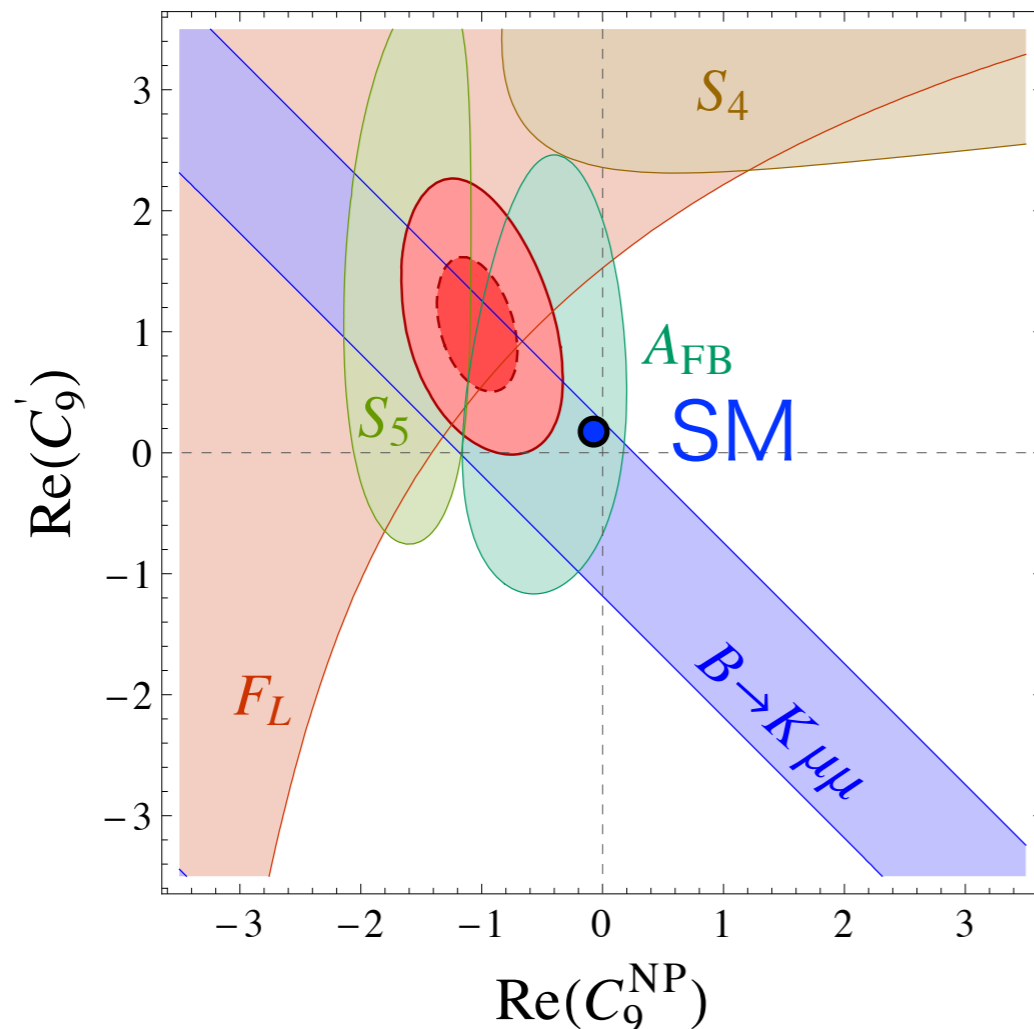


2.4 $\sigma$  tension at low  $q^2$

The “ $B \rightarrow K^* \mu\mu$  anomaly”

# Fitting $C_9$ and $C'_{9,10}$

[Altmannshofer and DS 1308.1501]



The are 2–3 $\sigma$  tensions in the observables  $F_L$ ,  $S_4$ ,  $S_5$ . Possible explanation

- ▶ Statistical **fluctuation** ...
- ▶ Underestimated **theory uncertainties** ( $\rightarrow$  see talk by Th. Feldmann!)
  - ▶ Non-factorizable corrections at low  $q^2$
  - ▶ Violation of quark-hadron duality at low and high  $q^2$
  - ▶ form factors
- ▶ **New physics?**
  - ▶ Can the tensions be removed by modifying  $C_i$  without upsetting other constraints?
  - ▶ The answer for the  $S_4$  tension is clearly “no”. What about the  $S_5$ ,  $F_L$  tensions?

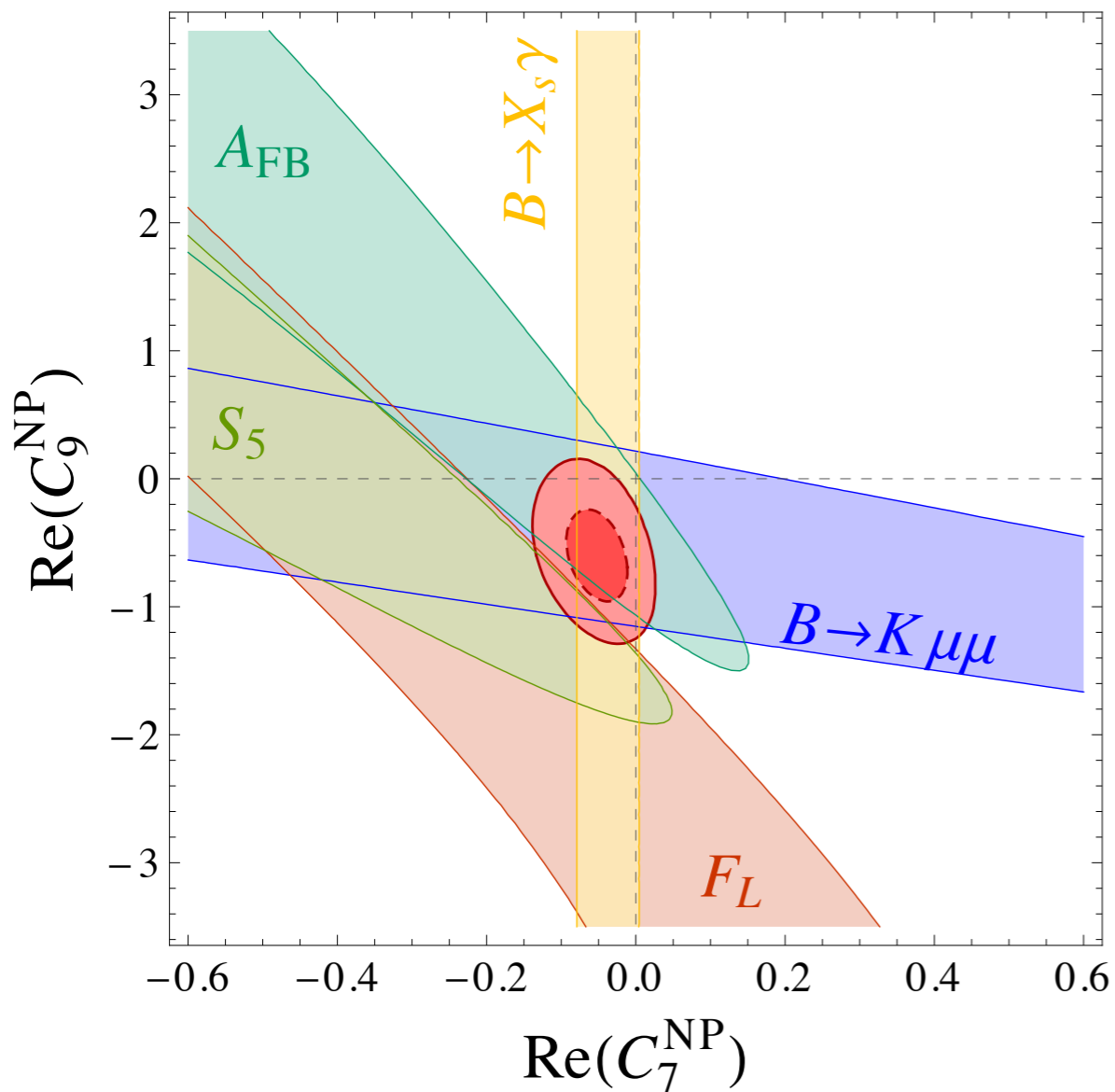
- ▶ Simultaneous NP effect in  $C_9$  and  $C'_9$  gives the best fit to the data
- ▶ As yet, only proposed model that can accomodate the effect:  
**flavour-violating  $Z'$**



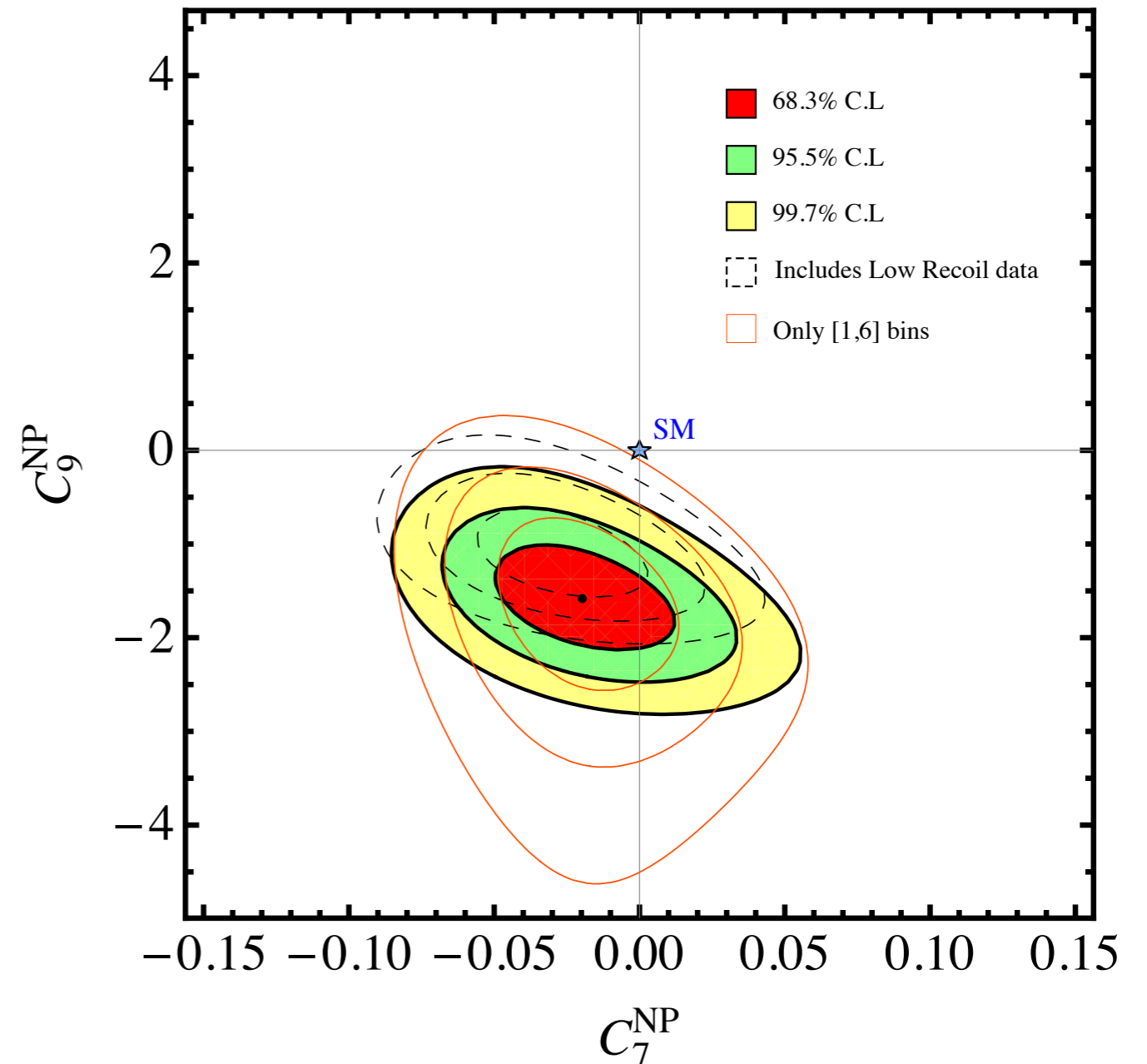
# Fitting $C_7$ and $C_9$

$$\begin{aligned} \mathcal{O}_7 &= e/(16\pi^2) m_b (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu}, \\ \mathcal{O}_9 &= e^2/(16\pi^2) (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell), \\ \mathcal{O}_{10} &= e^2/(16\pi^2) (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell), \end{aligned}$$

Altmannshofer and Straub (2013)



Descotes-Genon, Matias and Virto (2013)



# $R(D^{(*)})$

See, Hagiwara, nojiri and sakaki (2014)  
and references therein

Semi-leptonic decay

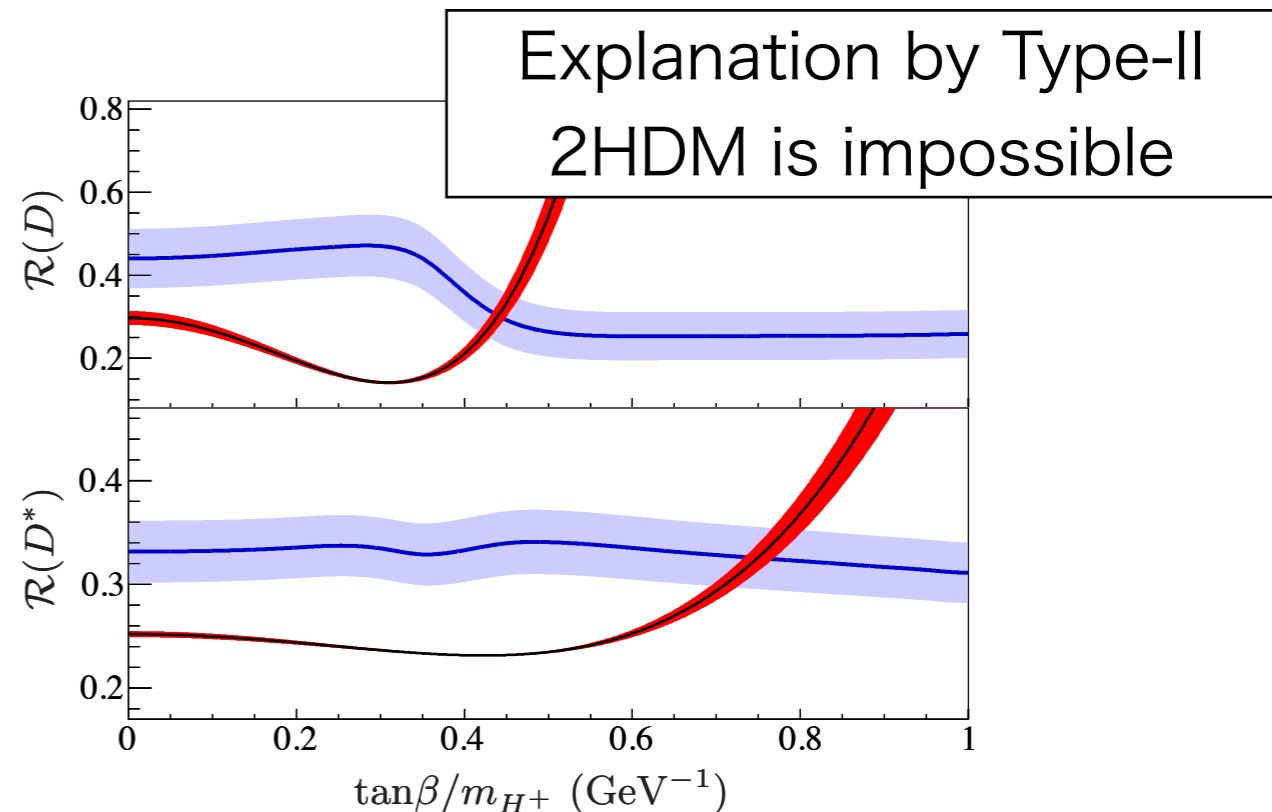
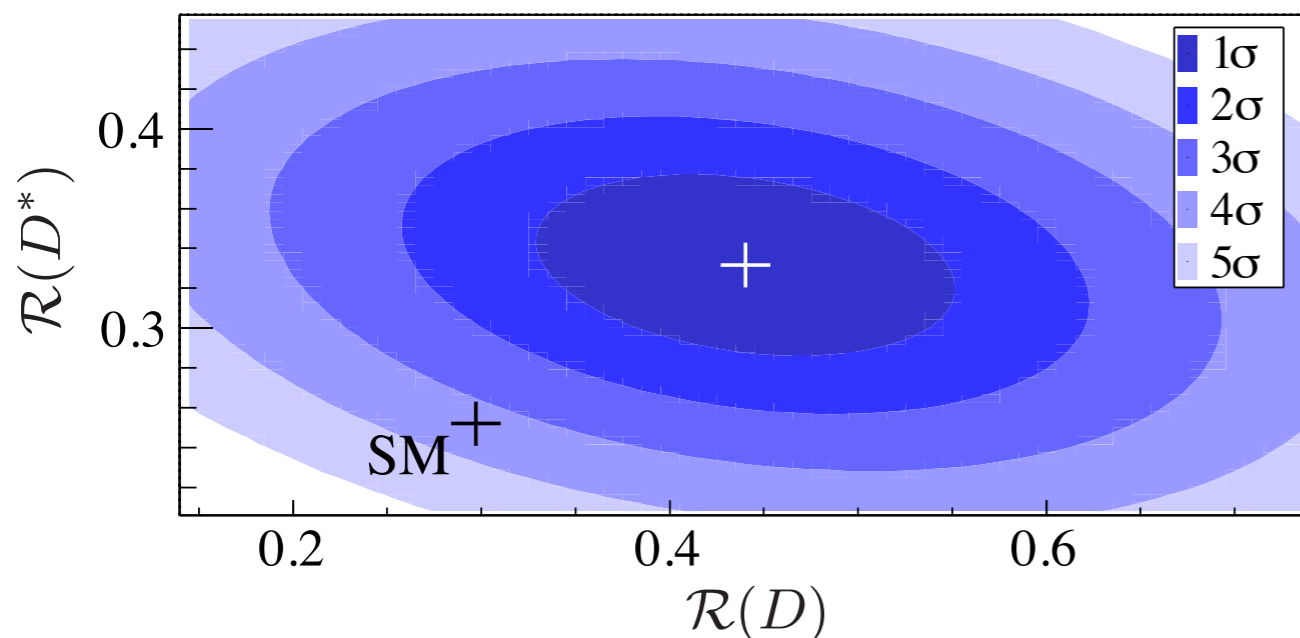
$$R(D^{(*)}) = \frac{\Gamma(B \rightarrow \bar{D}^{(*)} \tau^+ \nu_\tau)}{\Gamma(B \rightarrow \bar{D}^{(*)} l^+ \nu_l)}$$

$$R(D)_{\text{SM}} = 0.305 \pm 0.012, \quad R(D^*)_{\text{SM}} = 0.252 \pm 0.004.$$

$$R(D)_{\text{BaBar}} = 0.440 \pm 0.072, \quad R(D^*)_{\text{BaBar}} = 0.332 \pm 0.030,$$

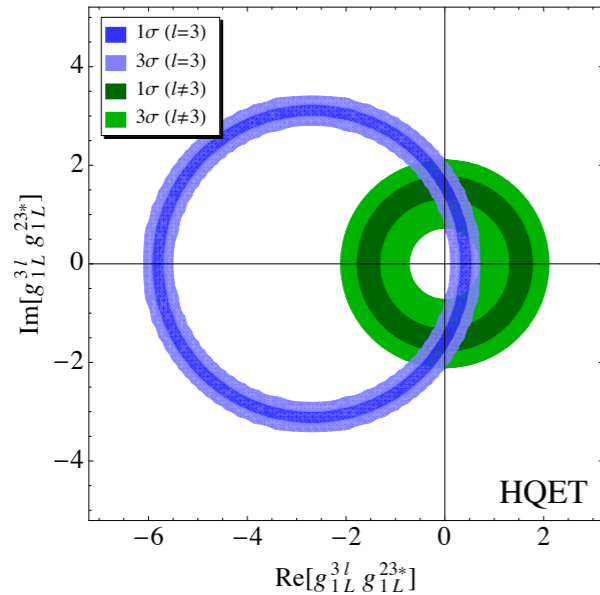
$$R(D)_{\text{Belle}} = 0.34 \pm 0.12, \quad R(D^*)_{\text{Belle}} = 0.43 \pm 0.08,$$

➔  $R(D)_{\text{exp}} = 0.42 \pm 0.06, \quad R(D^*)_{\text{exp}} = 0.34 \pm 0.03, \quad 3.8\sigma$

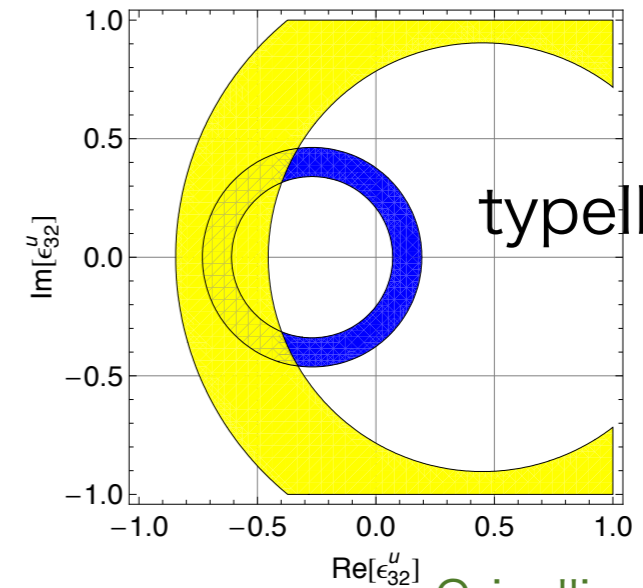


# NP explanations

- Explanations by Type-III 2HDM, lepto-quark model are possible

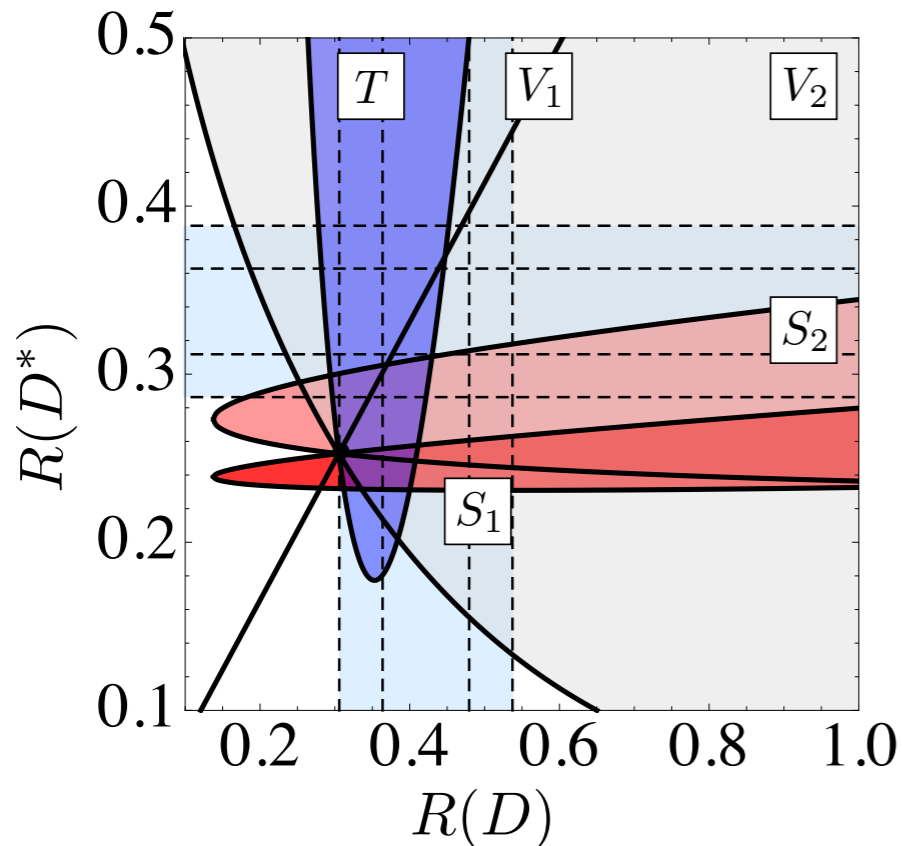


lepto-quark  
Sakaki et al (2013)



Crivellin et al (2012)

- Model-independent analysis



Tanaka et al (2012)

$$\mathcal{O}_{V_1} = (\bar{c}_L \gamma^\mu b_L) (\bar{\tau}_L \gamma_\mu \nu_{\tau L}),$$

$$\mathcal{O}_{V_2} = (\bar{c}_R \gamma^\mu b_R) (\bar{\tau}_L \gamma_\mu \nu_{\tau L}),$$

$$\mathcal{O}_{S_1} = (\bar{c}_L b_R) (\bar{\tau}_R \nu_{\tau L}),$$

$$\mathcal{O}_{S_2} = (\bar{c}_R b_L) (\bar{\tau}_R \nu_{\tau L}),$$

$$\mathcal{O}_T = (\bar{c}_R \sigma^{\mu\nu} b_L) (\bar{\tau}_R \sigma_{\mu\nu} \nu_{\tau L}).$$

# muon g-2

Magnetic Moment

$$\vec{\mu} = g_{\mu} \frac{e}{2m_{\mu}} \vec{S}$$

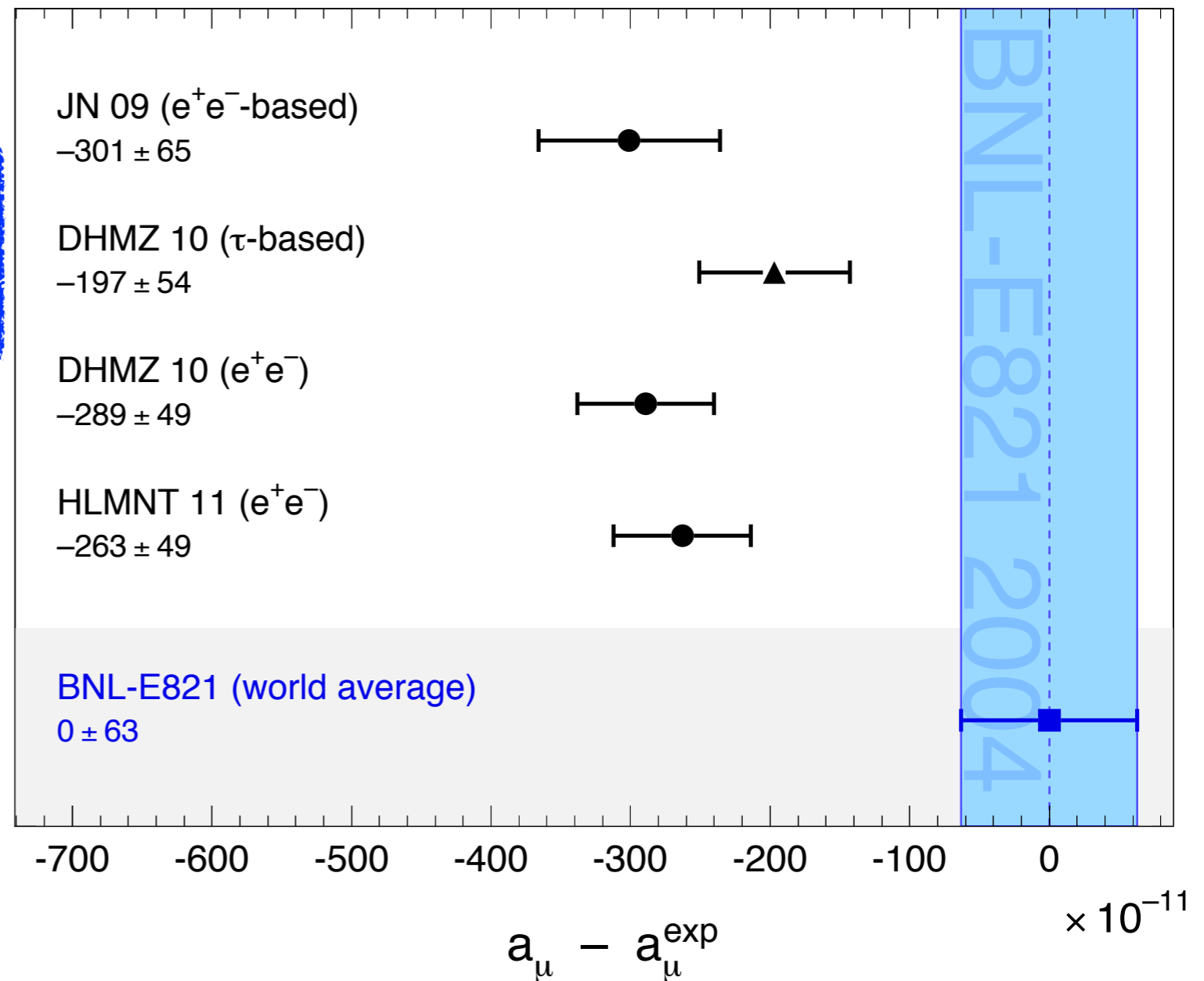
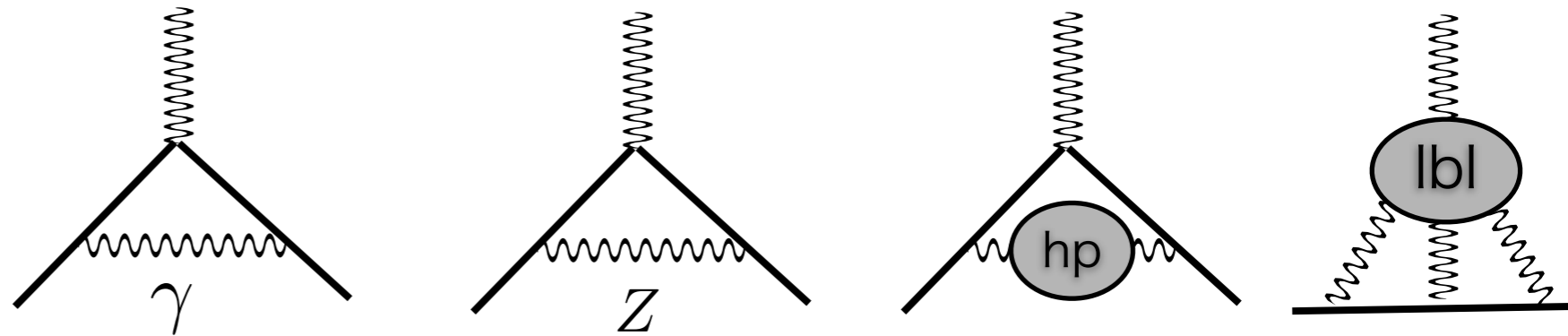
$$a_{\mu} \equiv \frac{g_{\mu} - 2}{2} \neq 0$$

Radiative corrections

$$\Delta a_{\mu} \equiv a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (28.8 \pm 80) \times 10^{-10}$$

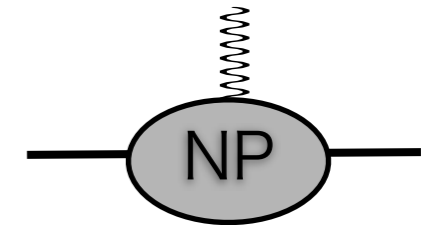
3.6  $\sigma$

$$a_{\mu}^{\text{EW}} = 15.4 \times 10^{-10}$$



# Implication on NP models

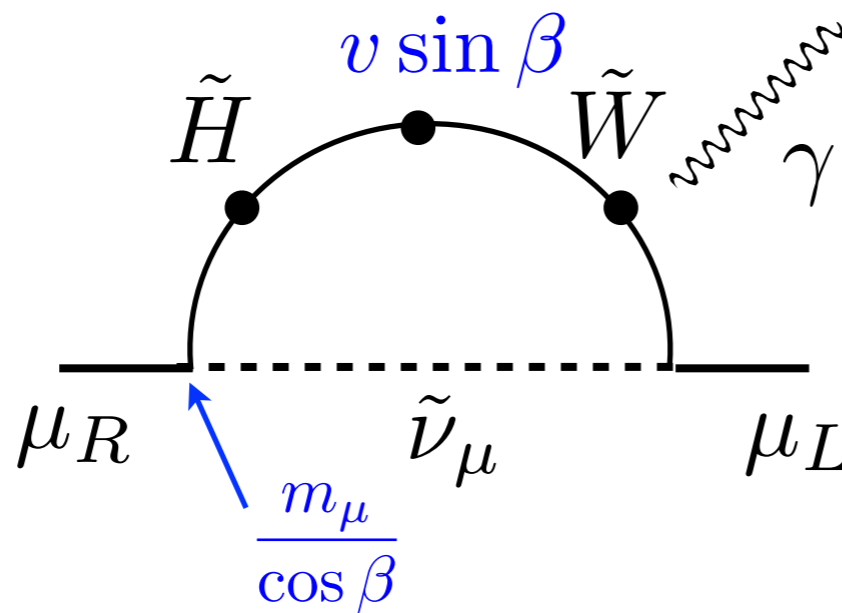
$$\Delta a_\mu \sim a_\mu^{\text{EW}} \sim \alpha_2 \frac{m_\mu^2}{m_W^2}$$



- light new particle
- heavy (<math>O(100 \text{ GeV})</math>) new particle  
+ enhancement factor

→ dark photon

→ SUSY, RS ...



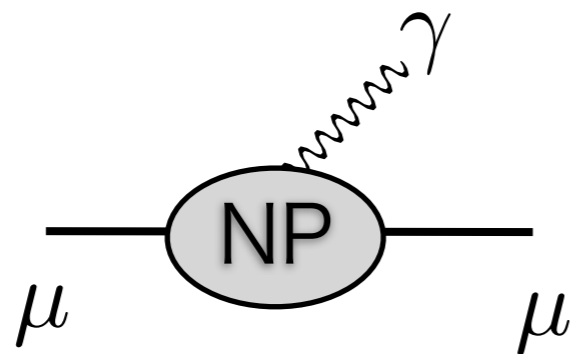
$$a_\mu^{\text{SUSY}} \sim \alpha_2 \frac{m_\mu^2}{m_{\text{SUSY}}^2} \tan \beta$$

Waiting for further experimental confirmations @Fermi and J-park.

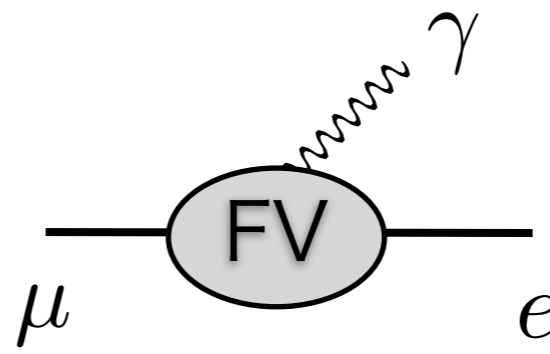
# LFVs and EDMs

- SM predictions are highly suppressed  
→ stringent constraints and/or strong tools to probe NP models
- Theoretically and/or Experimentally well-motivated models

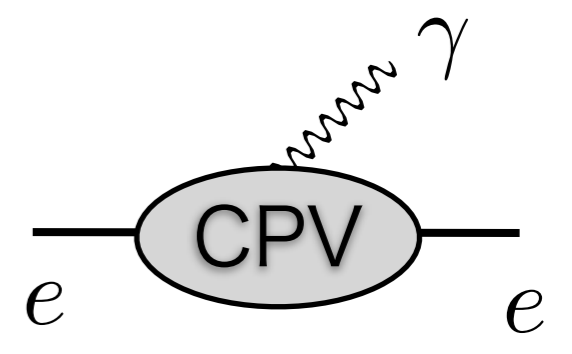
Similarity with **muon g-2**



muon g-2



LFV



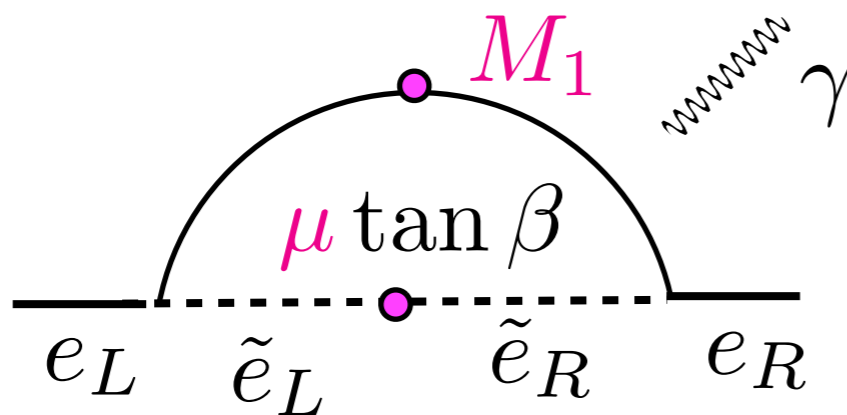
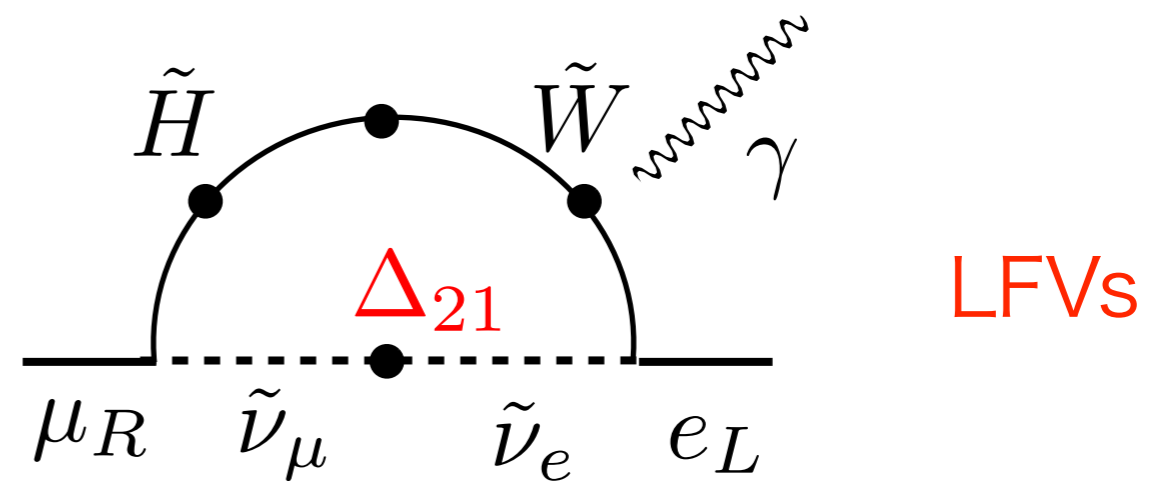
EDM

related with generation of  **$\nu$  masses?**

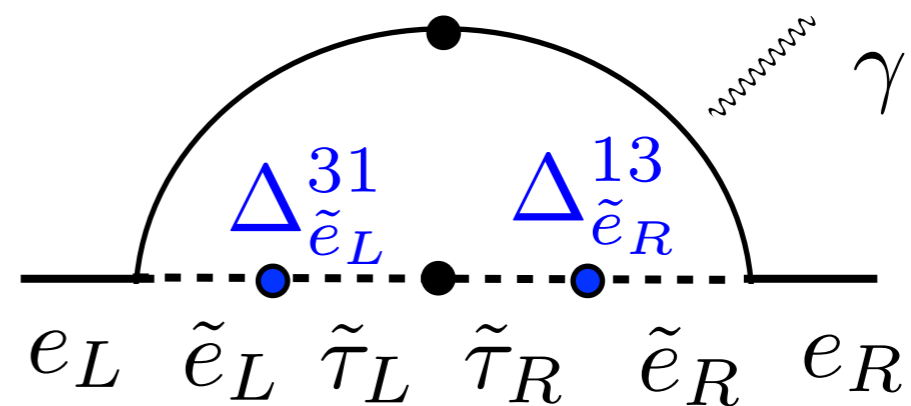
# TeV-scale SUSY models

Before the LHC run,  $O(0.1-1)\text{TeV}$  SUSY particles are expected.

- GUT
- Flavor & CP problem
- Dark Matter
- Collider signatures
- Naturalness
- Muon  $g-2$



“flavor-blind EDM”



“flavored EDM”



# LFV in SUSY flavor models

Lepton (& quark) flavor signals are discussed in some representative flavor models. [ Altmannshofer, Buras, Gori, Paradisi, Straub '09 ]

RVV2 model SU(3)

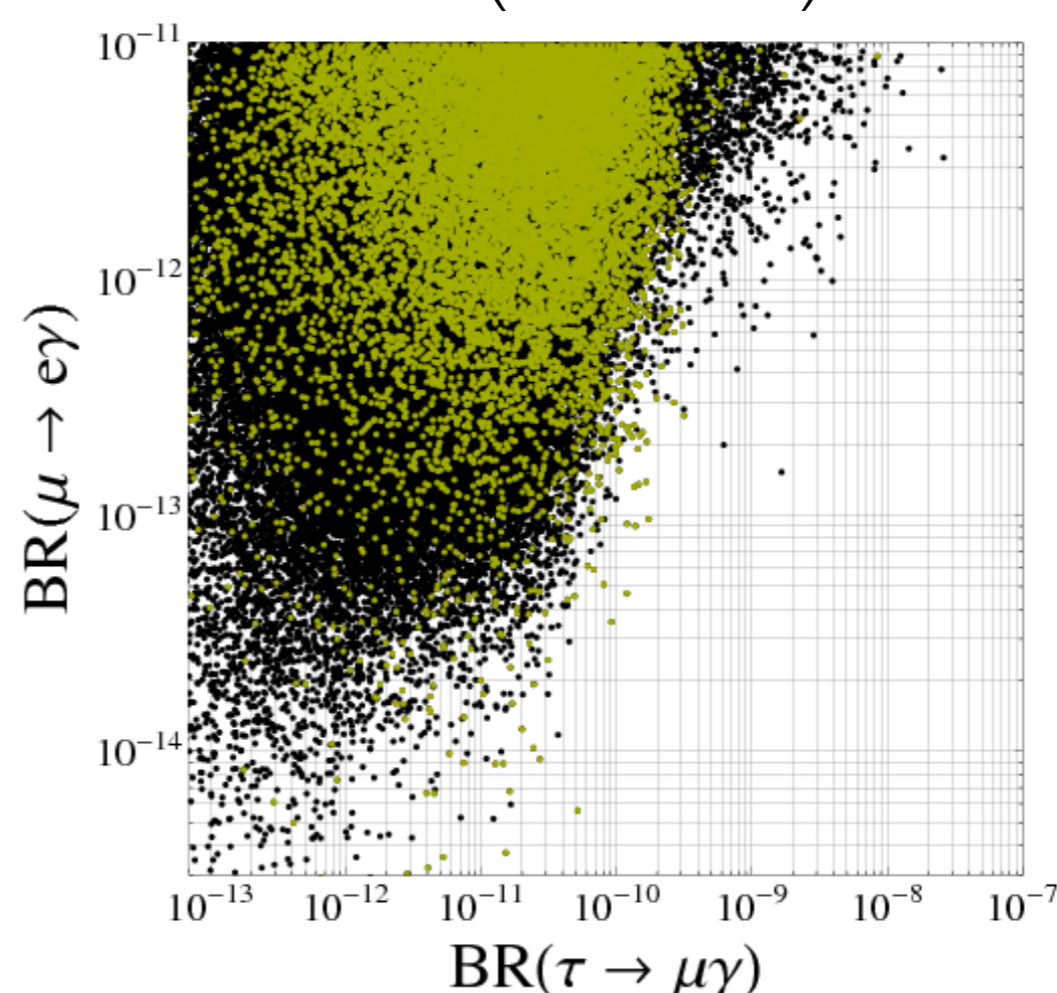
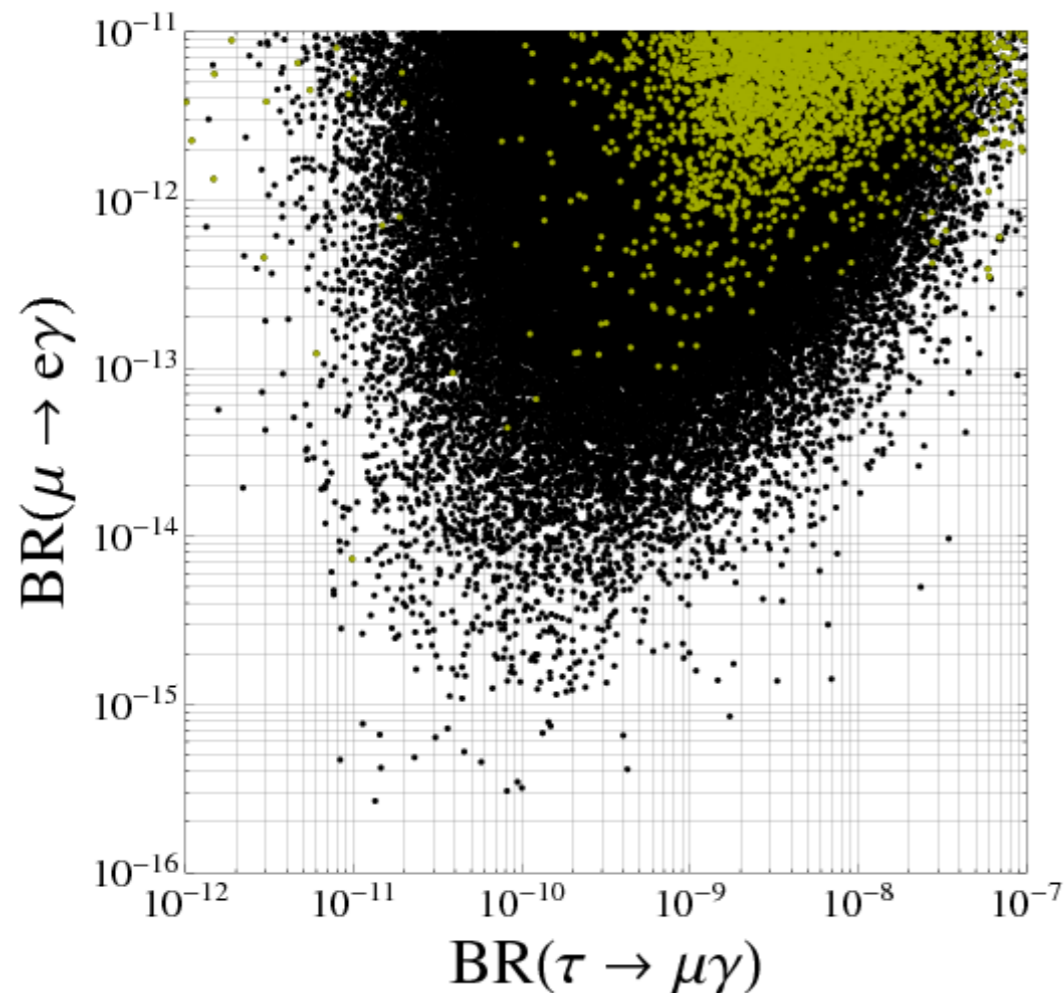
[Ross, Velasco-S, Vives ]

$$\delta_e^{LL} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \delta_e^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix}$$

AKM model SU(3)

[ Antusch, King, Malinsky ]

$$\delta_e^{LL} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix} \delta_e^{RR} \sim \begin{pmatrix} \cdot & \lambda^4 & \lambda^4 \\ \lambda^4 & \cdot & \lambda^2 \\ \lambda^4 & \lambda^2 & \cdot \end{pmatrix}$$

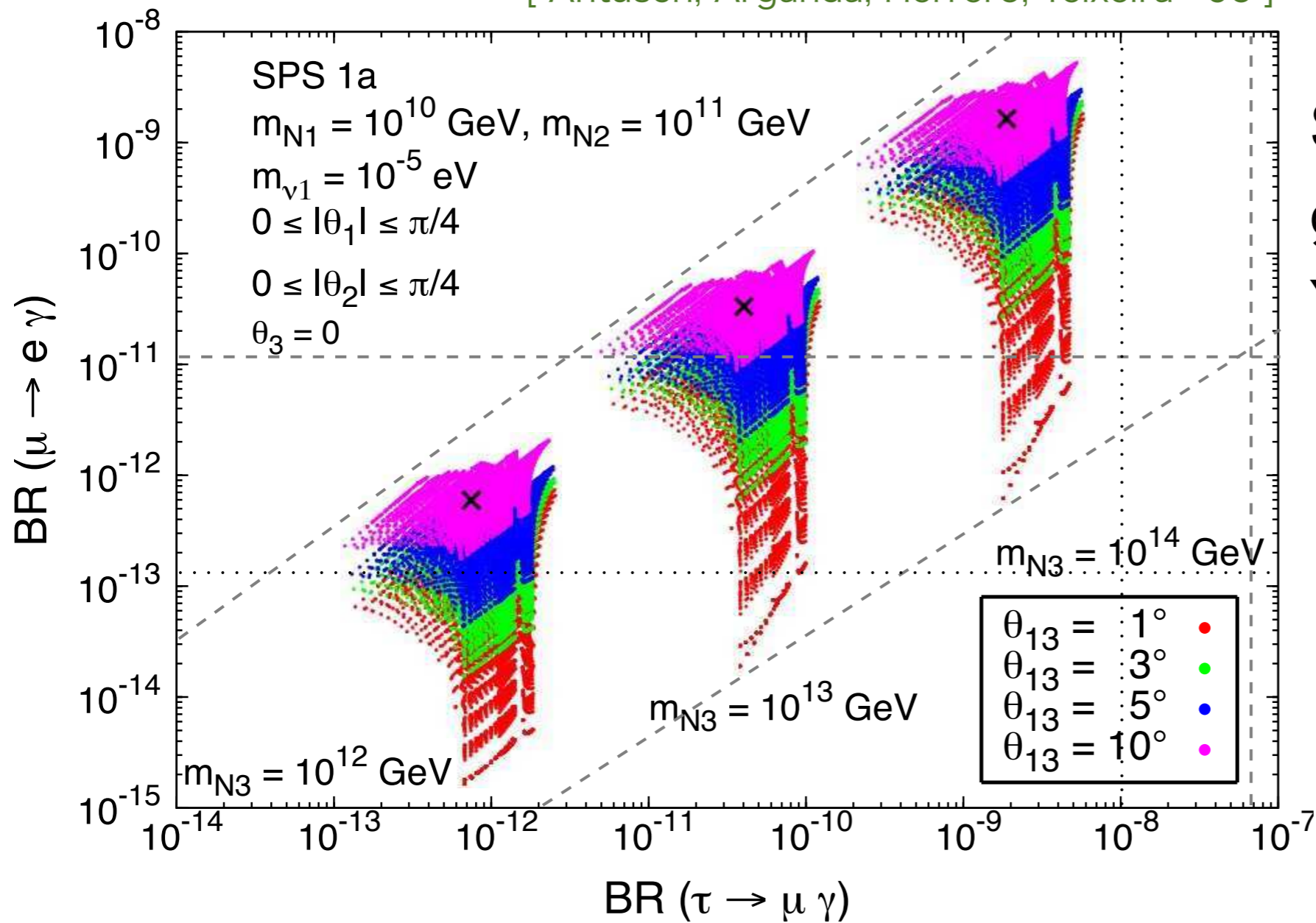


$$\Delta a_\mu > 10^{-9}$$



# LFV in SUSY models with RNs

[ Antusch, Arganda, Herrero, Teixeira '06 ]



Slepton mixings are generated by neutrino Yukawa couplings

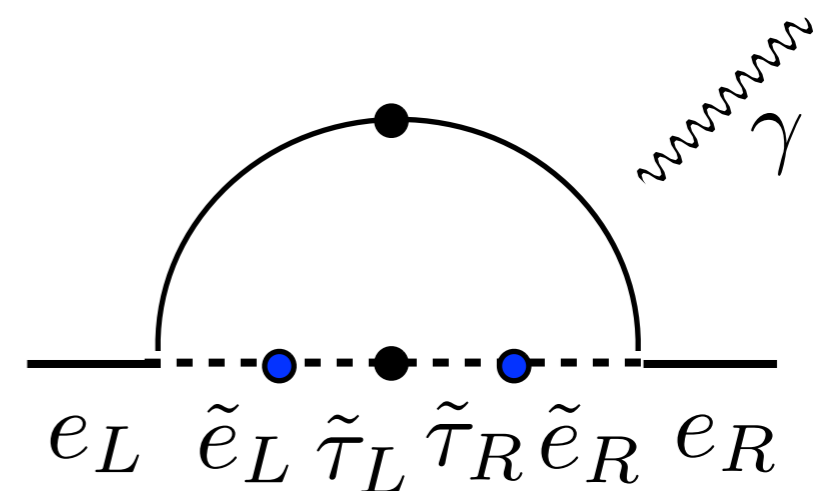
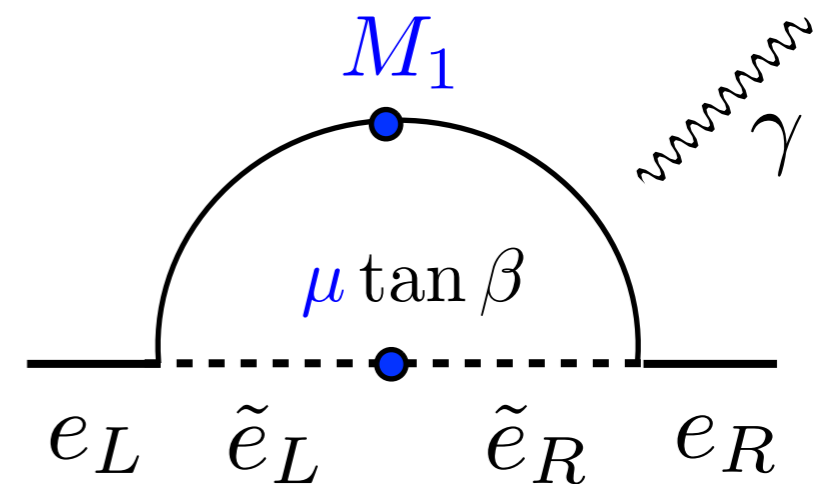
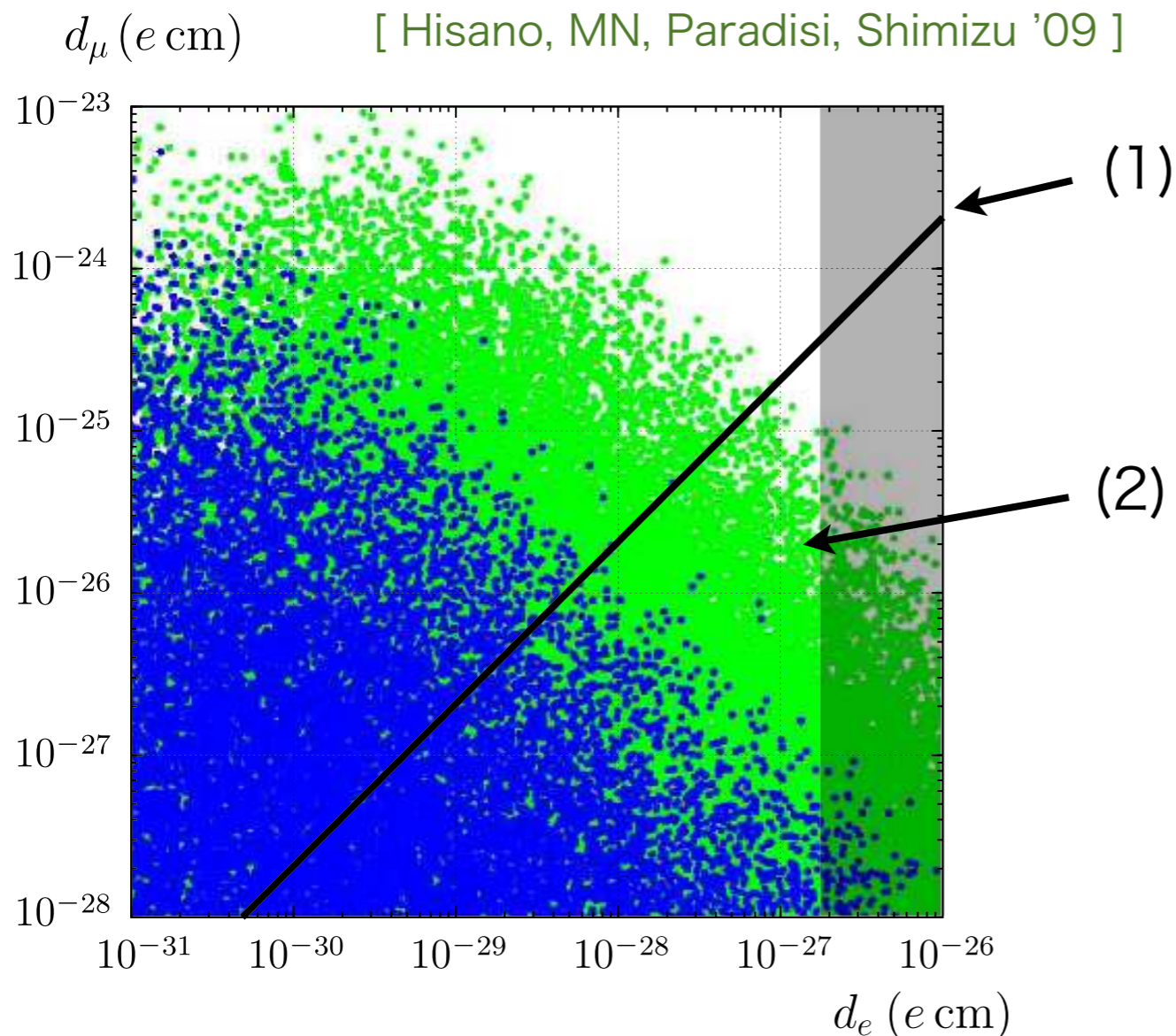


$\nu$  mass generation by see-saw mechanism

# Correlation with leptonic EDMs

## leptonic EDMs

CP violation comes from (1) gaugino masses and/or (2) slepton mixing terms



$$\text{Br}(\mu \rightarrow e\gamma) < 10^{-13}$$

$$\text{Br}(\mu \rightarrow e\gamma) < 10^{-11}$$

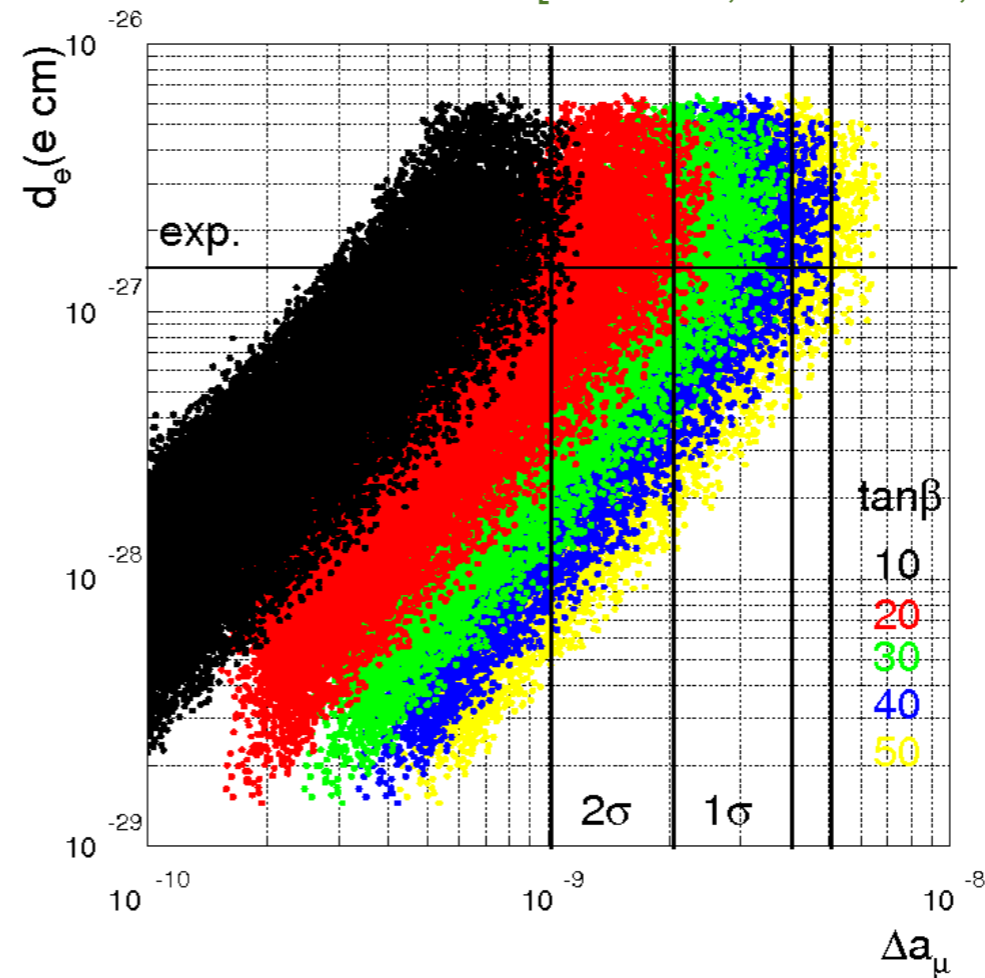
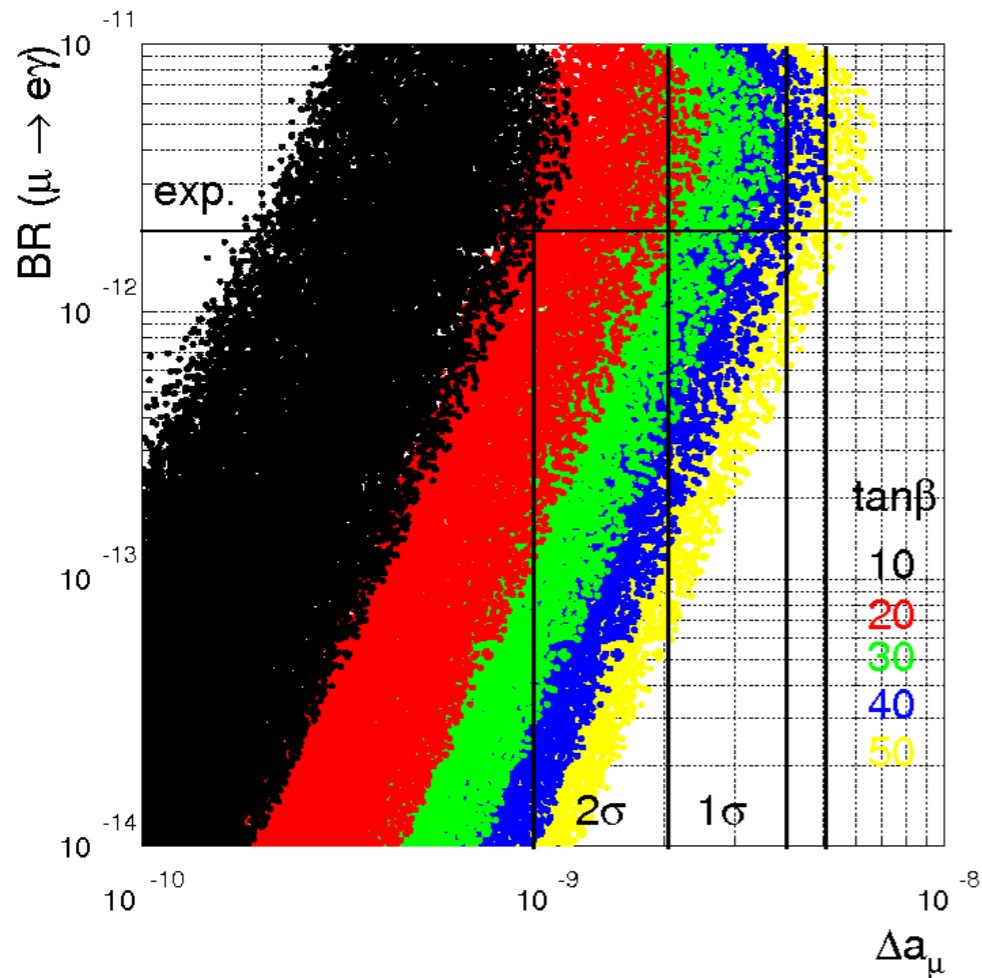
# LFV, muon g-2 and eEDM

- Distorted A terms scenario [Giudice, Isidori, Paradisi '12]

$$(\delta_{LR}^f)_{ij} \sim \frac{A_f \theta_{ij} m_{f_j}}{m_{\tilde{f}}^2} \quad f = u, d, e \quad \text{Sources of flavor \& CP violation}$$

LFV, eEDM : U(1), no tanbeta  
 muon g-2 : SU(2), tanbeta enhancement

[Giudice, Paradisi, Passera '12]



$$\theta_{ij} = \sqrt{m_i/m_j}$$

# LHC results pushed up SUSY scale!

- Non-observation of SUSY particles

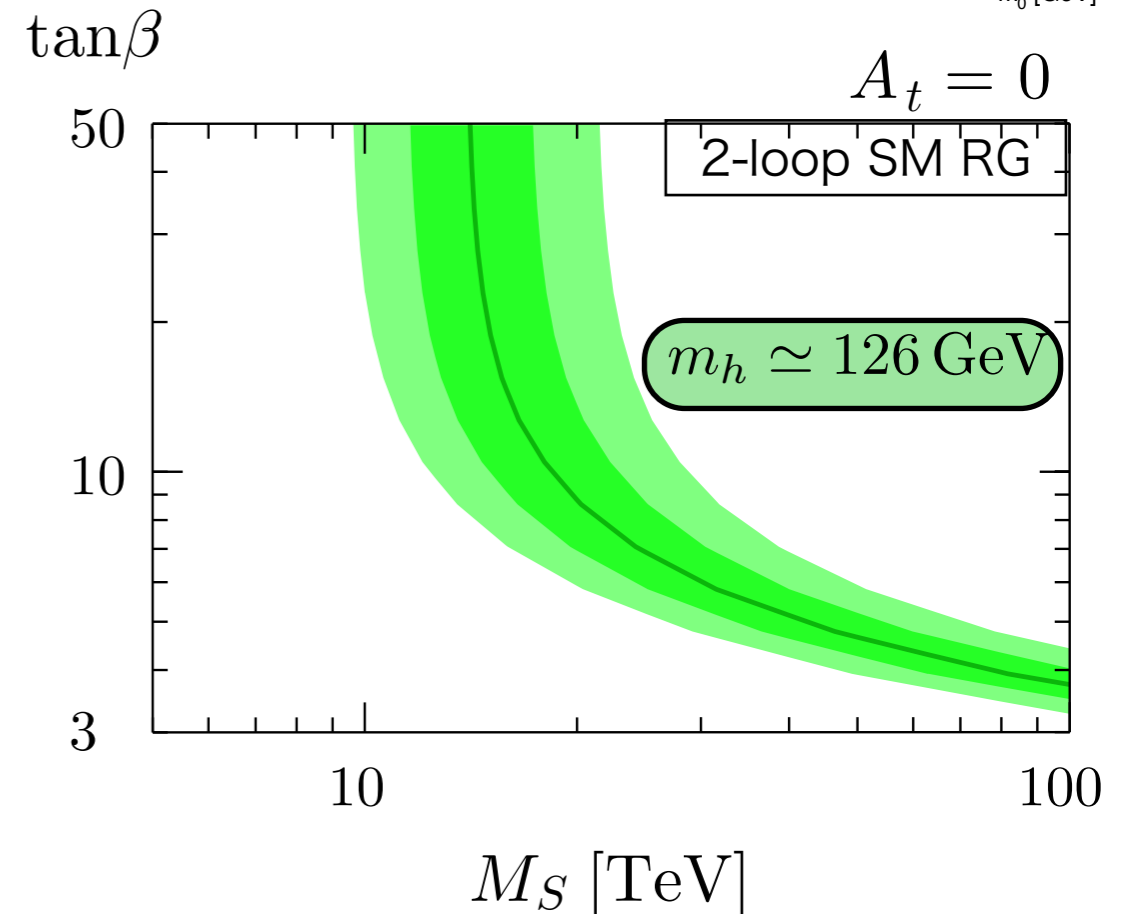
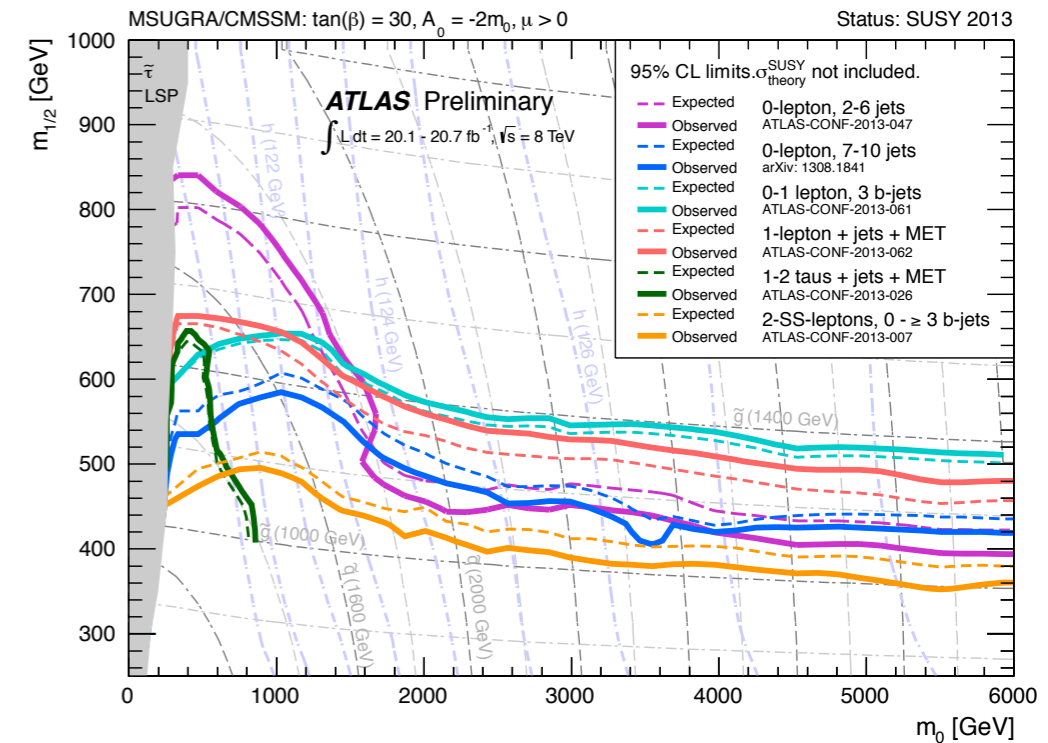
$$m_{\tilde{q}} \gtrsim 1.8 \text{ TeV} \quad M_{\tilde{g}} \gtrsim 1.4 \text{ TeV}$$

- Discovery of 126 GeV Higgs

MSSM

$$m_h^2 \simeq m_Z^2 \cos^2 2\beta + \frac{3m_t^4}{4\pi^2 v^2} \left[ \log \left( \frac{M_S^2}{m_t^2} \right) + \frac{A_t^2}{M_S^2} \left( 1 - \frac{A_t^2}{12M_S^2} \right) \right]$$

- Heavy stops ( O(10-100)TeV )
- Large A term
- Vector-quarks, U(1)' ...
- NMSSM





# High-scale SUSY models

126 GeV Higgs boson + Null result of SUSY search

➔  $O(10-100)\text{TeV}$  sfermions

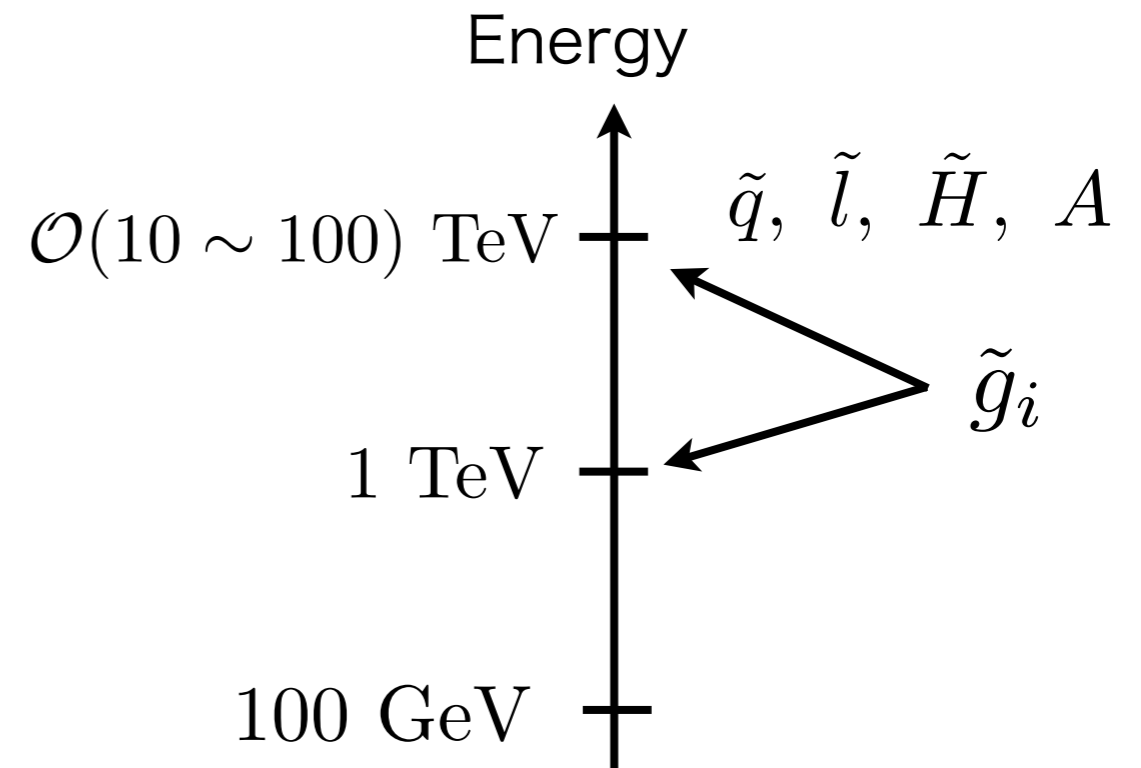
1) gaugino mass  $\sim$  sfermion mass

Heavy gaugino, mSUGRA

2) gaugino mass  $\ll$  sfermion mass

Anomaly-med

- GUT
- Flavor & CP problem
- Dark Matter
- Collider signatures
- Naturalness (0.1~0.001%)
- ~~Muon g-2~~

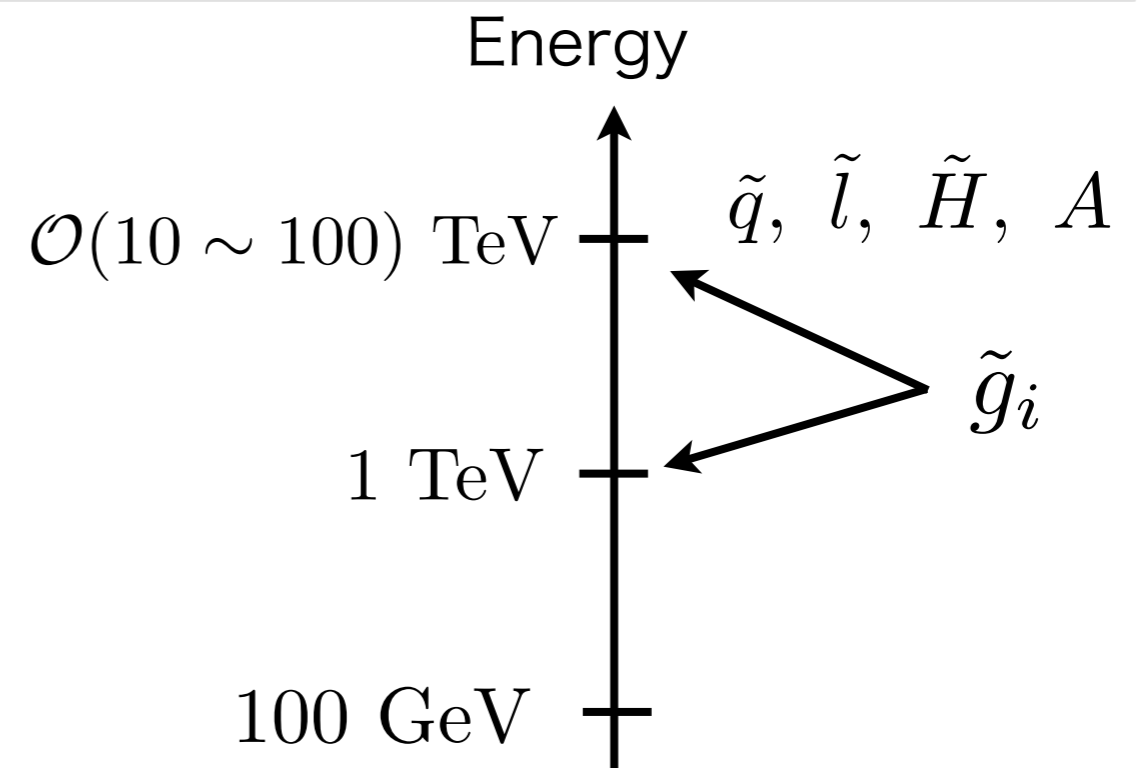


# High-scale SUSY models

126 GeV Higgs boson + Null result of SUSY search

Thanks to the automatic suppression by heavy masses, large flavor- and CP-violating parameters are allowed. In this situation, flavor observables are used to access such a high scale physics!

- GUT
- Flavor & CP ~~problem~~ **probe**
- Dark Matter
- Collider signatures
- Naturalness (0.1~0.001%)
- ~~Muon g-2~~



RA

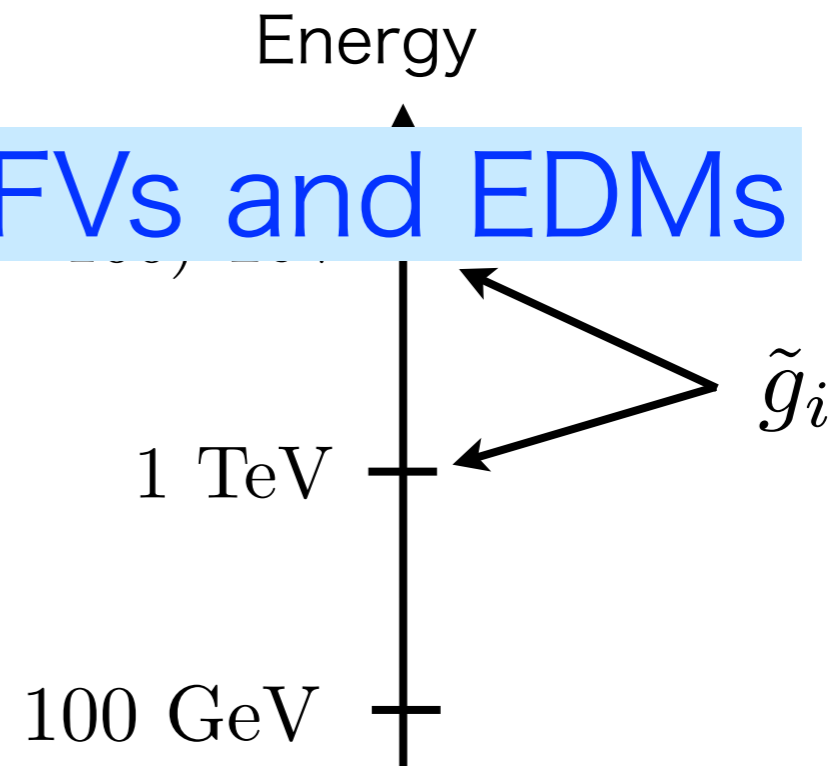
# High-scale SUSY models

126 GeV Higgs boson + Null result of SUSY search

Thanks to the automatic suppression by heavy masses, large flavor- and CP-violating parameters are allowed. In this situation, flavor observables are used to access such a high scale physics!

- GUT
- Flavor & CP ~~problem~~ <sup>probe</sup>
- Dark Matter
- Collider signatures
- Naturalness (0.1~0.001%)
- ~~Muon  $g-2$~~

$\epsilon_K$ , LFVs and EDMs  $A$



# Kaon mixing parameter

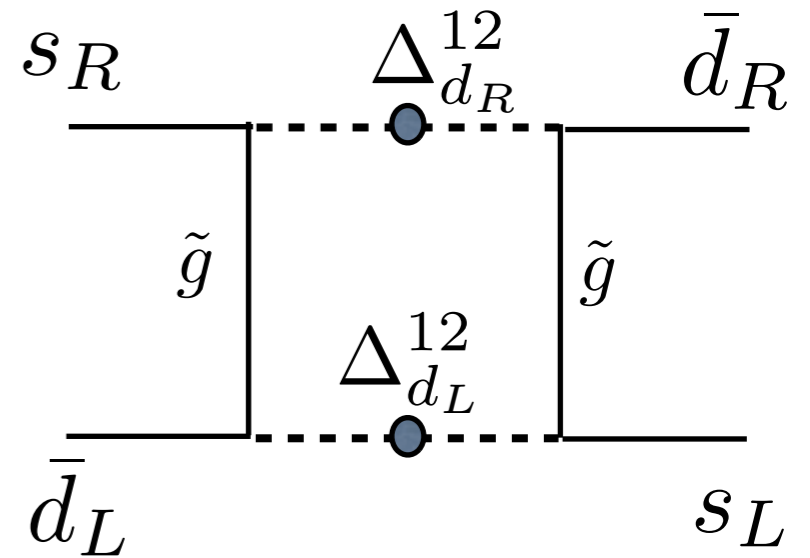
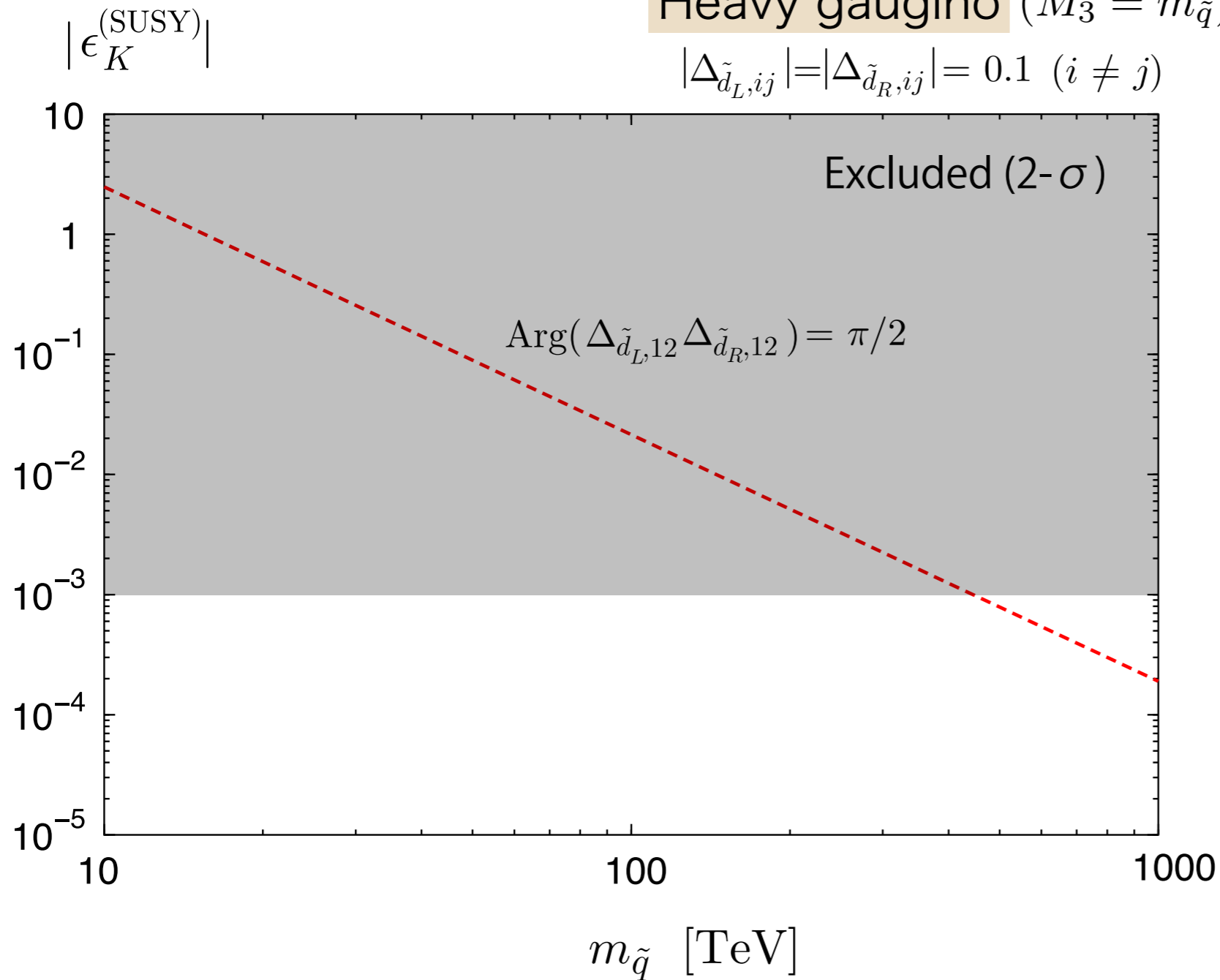
[Moroi and MN (2013)]

$$|\Delta_{ij}| = 0.1$$

maximal phase

Heavy gaugino ( $M_3 = m_{\tilde{q}}$ )

$$|\Delta_{\tilde{d}_L, ij}| = |\Delta_{\tilde{d}_R, ij}| = 0.1 \quad (i \neq j)$$



$$\epsilon_K \propto \frac{\text{Im}[\Delta_{d_R}^{12} \Delta_{d_L}^{12}]}{m_{\text{SUSY}}^2}$$

Suppressed If  
the phases are  
cancelled

symmetry?



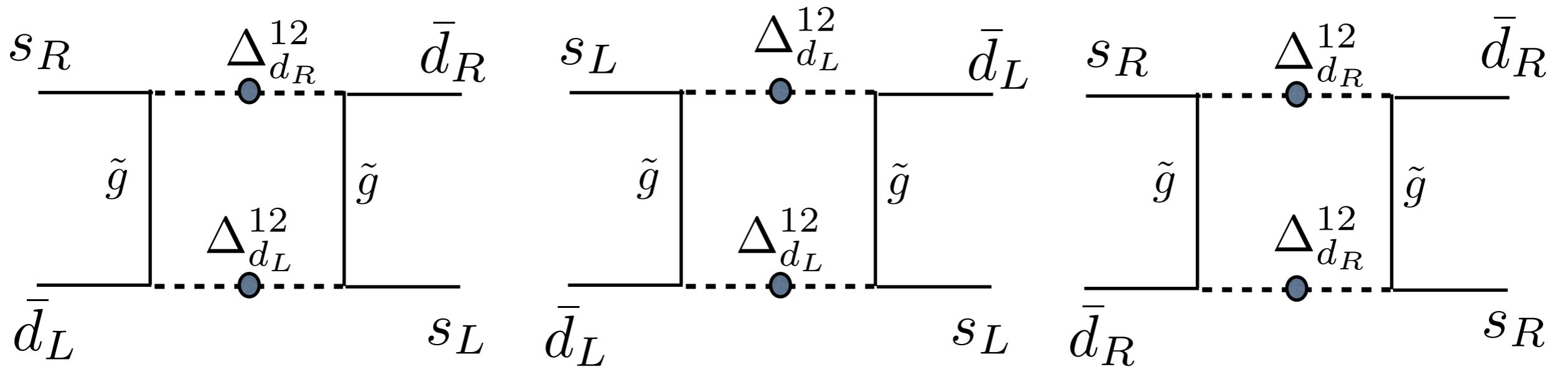
# SO(10) relation and C-invariance

$$m_{\tilde{d}_L, ij}^2 = m_{\tilde{d}_R, ij}^{2*}$$



C-inv. :  $d_L \leftrightarrow d_R^c$

→  $\epsilon_K^{\text{SUSY}}$  is suppressed



$$\text{Im}[\Delta_{d_R}^{12} \Delta_{d_L}^{12}] = 0$$

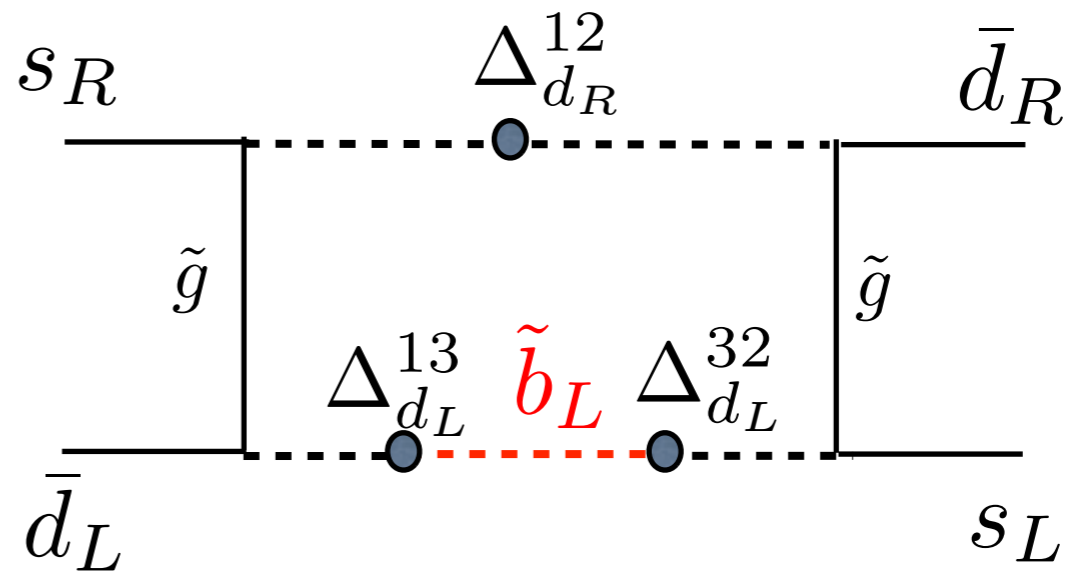
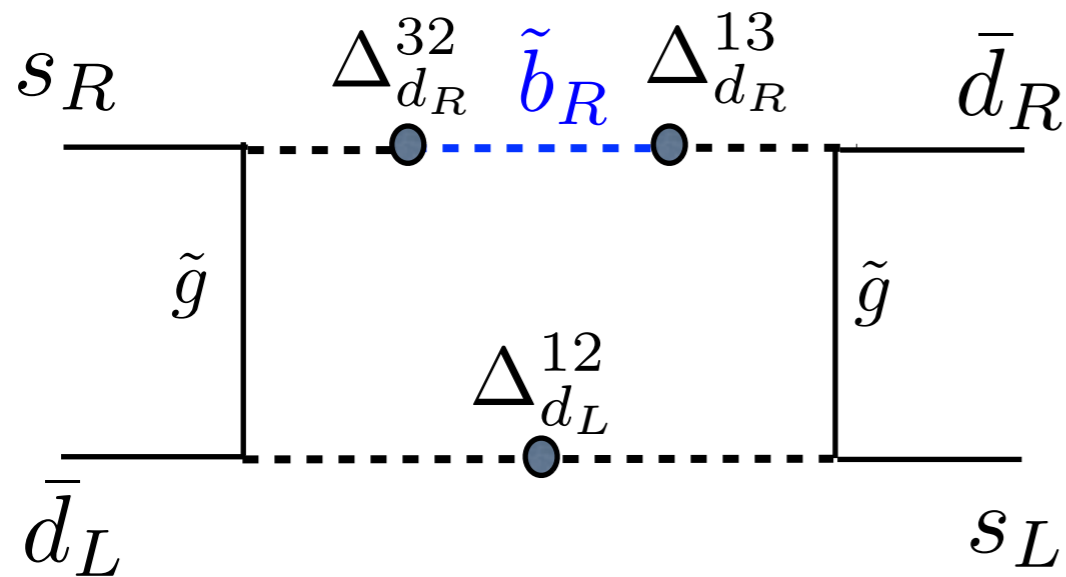
$$\text{Im}[\Delta_{d_L}^{12} \Delta_{d_L}^{12}] = -\text{Im}[\Delta_{d_R}^{12} \Delta_{d_R}^{12}]$$

Breaking of C-inv. : EW & Yukawa interactions

# Breaking of SO(10) relation

Dominant SUSY contribution comes from

$$m_{\tilde{d}_L,33}^2 \neq m_{\tilde{d}_R,33}^{2*} \quad (\text{RG effect through top Yukawa})$$



$$\epsilon_K^{SUSY} \sim \frac{\text{Im}[\Delta_{d_R}^{13} \Delta_{d_R}^{32} \Delta_{d_L}^{12}]}{m_{SUSY}^2} \frac{m_{\tilde{b}_R}^2 - m_{\tilde{b}_L}^2}{m_{SUSY}^2}$$

$\tan \beta$	$\Delta_{d_L,33}$	$\Delta_{d_R,33}$
10	0.7	1
30	0.7	0.8
50	0.5	0.5

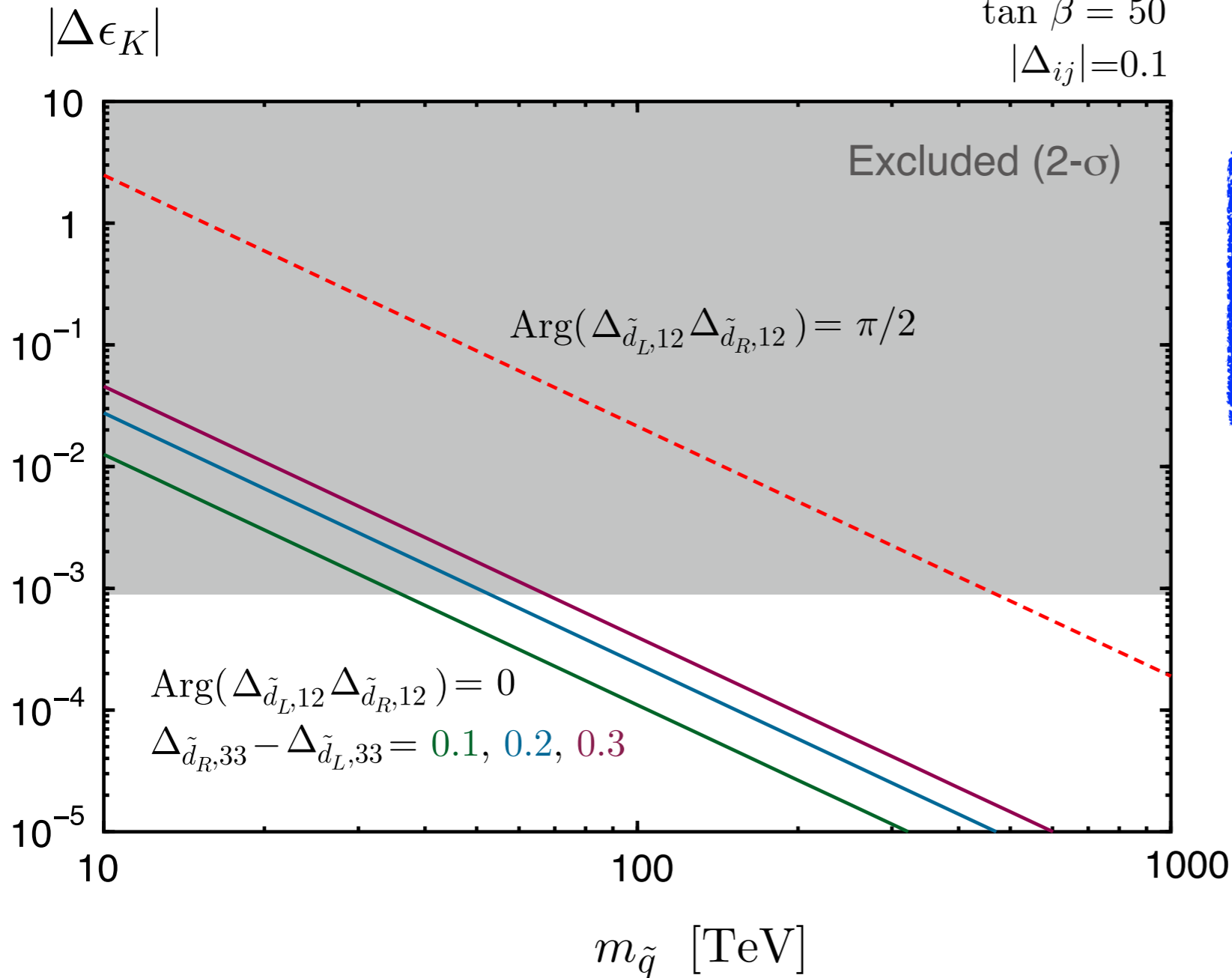
# Kaon mixing parameter

$$|\Delta_{ij}| = 0.1 \quad \text{maximal phase}$$

Heavy gaugino

$$\tan \beta = 50$$

$$|\Delta_{ij}| = 0.1$$



With SO(10) relation,  
 $\epsilon_K^{\text{SUSY}}$  is significantly  
 reduced

$$m_{\text{SUSY}} > \mathcal{O}(10) \text{ TeV}$$

Note,

$$\Delta M_K, D^0 \bar{D}^0 : \sim 30 \text{ TeV}$$

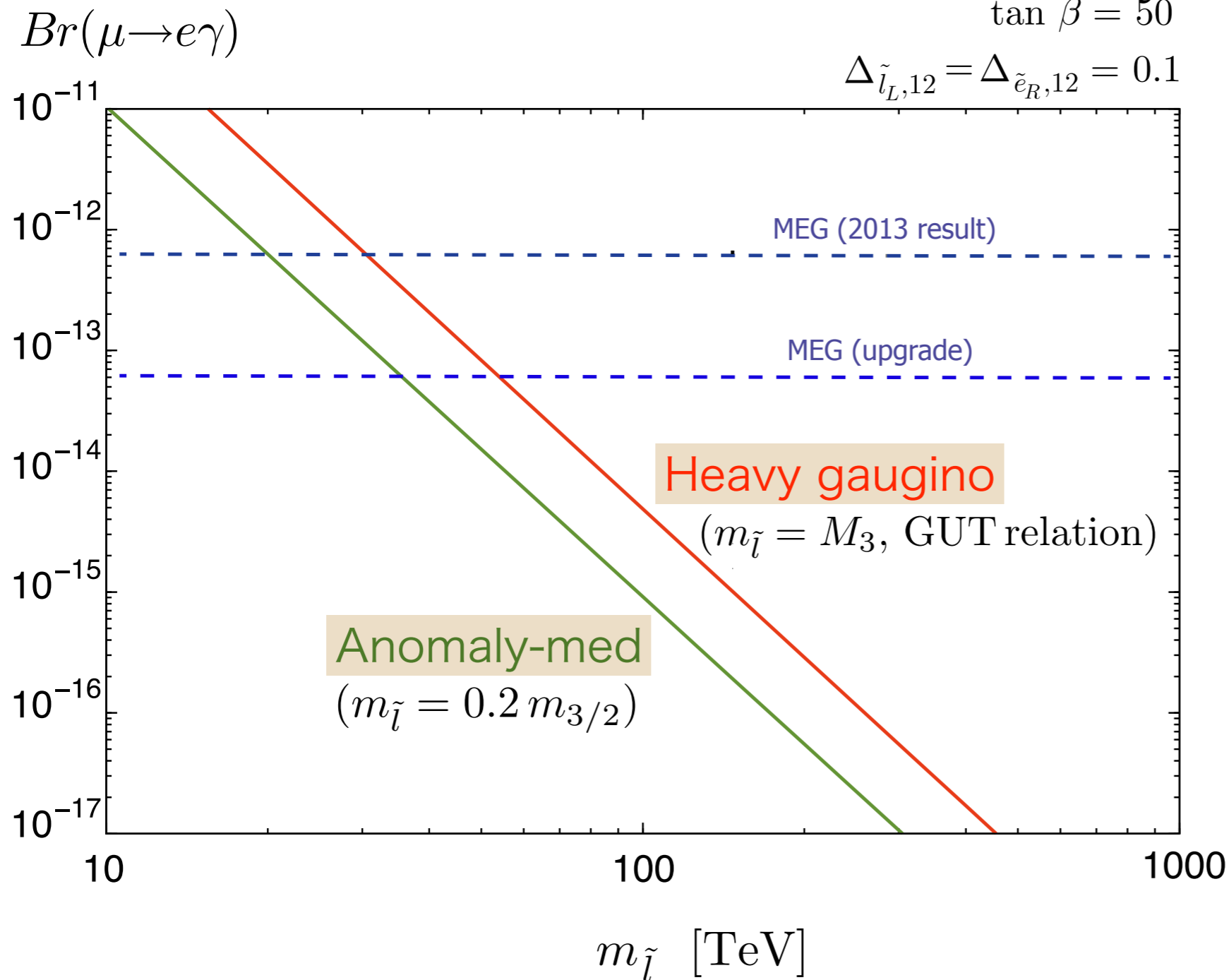
# LFV in High-scale SUSY models

$$|\Delta_{ij}| = 0.1$$

$$\mu = m_{\tilde{l}}$$

$$\tan \beta = 50$$

$$\Delta_{\tilde{l}_{L,12}} = \Delta_{\tilde{e}_{R,12}} = 0.1$$

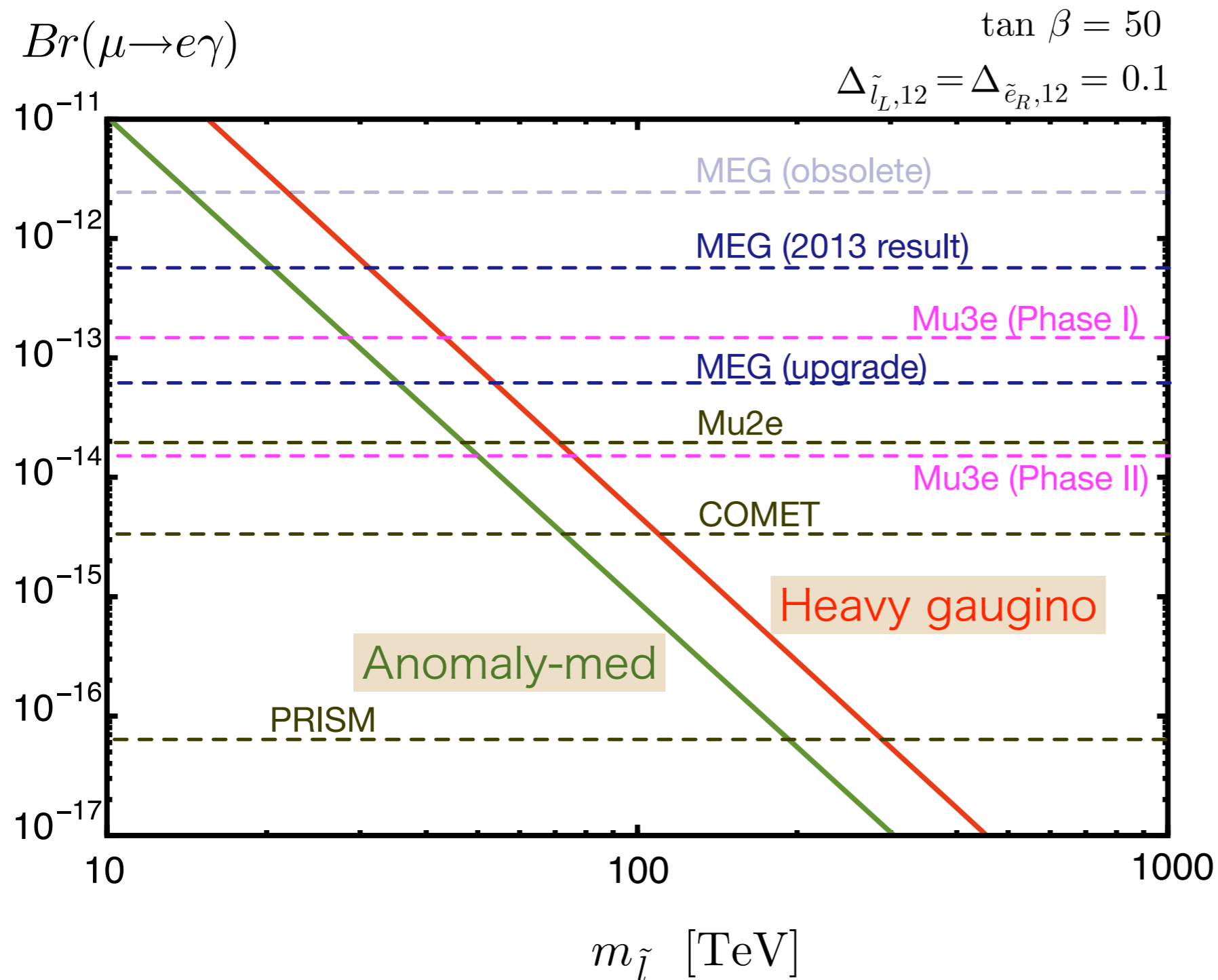


$$Br \propto \frac{\Delta^2}{m_{\tilde{l}}^4} \left( \frac{M_2 \mu t_\beta}{m_{\tilde{l}}^2} \right)^2$$

# LFV in High-scale SUSY models

In SUSY models, there is strong correlations btw  $Br(\mu \rightarrow e \gamma)$ ,  $Br(\mu \rightarrow eee)$  and  $R_{\mu e}$

Future experimental limits can be converted to that of  $Br(\mu \rightarrow e \gamma)$



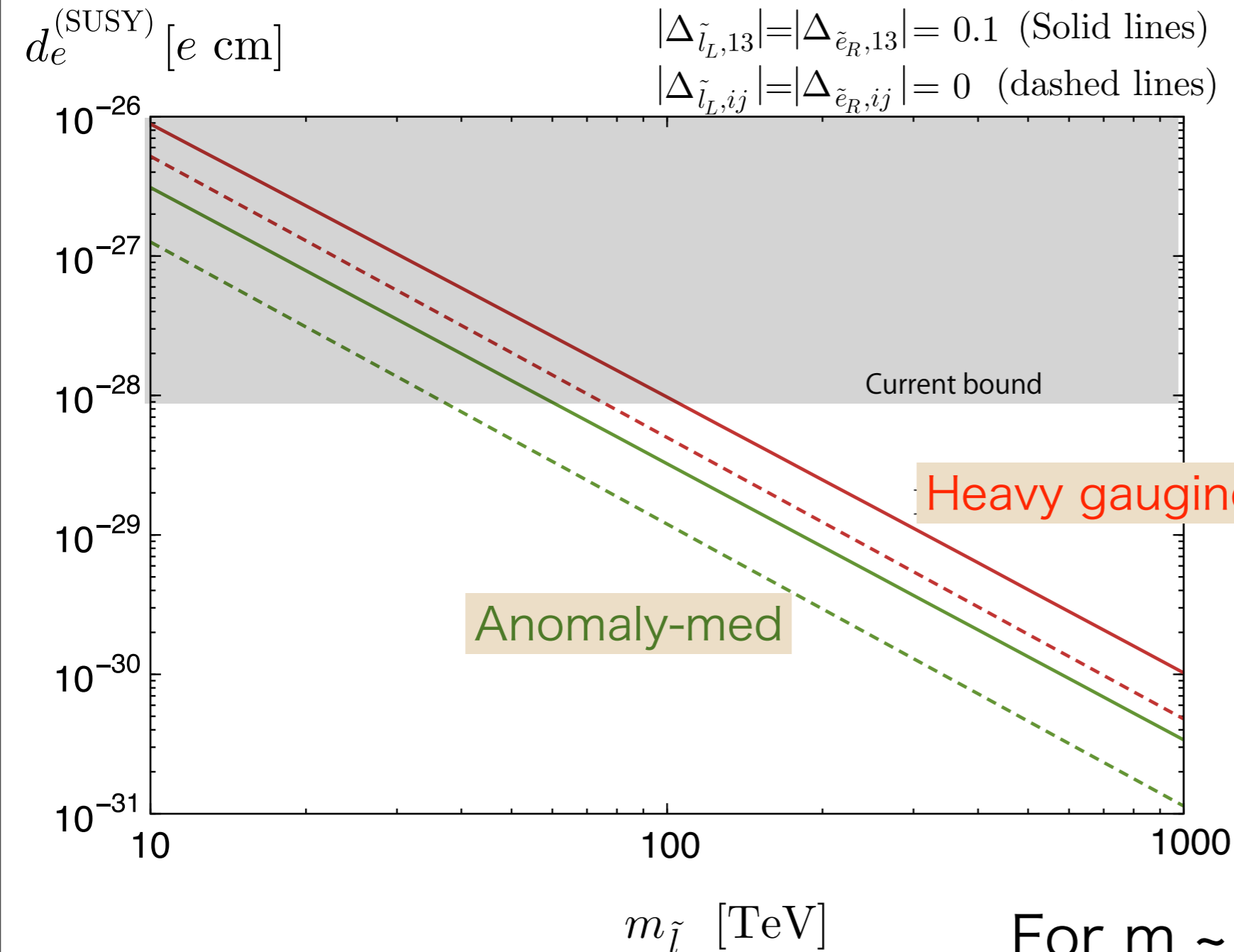
$$Br \propto \frac{\Delta^2}{m_{\text{SUSY}}^4}$$

# Electron EDM in High-scale SUSY models

$\tan \beta = 50$

$|\Delta_{\tilde{l}_L,13}| = |\Delta_{\tilde{e}_R,13}| = 0.1$  (Solid lines)

$|\Delta_{\tilde{l}_L,ij}| = |\Delta_{\tilde{e}_R,ij}| = 0$  (dashed lines)



— : flavored EDM  
 - - - : flavor-blind EDM

With  $\Delta \sim O(1)$ , flavored EDMs are much important because of the large enhancement by  $m_\tau/m_e$ .

$$d_e \propto \frac{\Delta^2}{m_{\tilde{l}}^2} \frac{M_1 \mu}{m_{\tilde{l}}^2} t_\beta$$

New Limit:  $d_e < 8.7 \times 10^{-29}$

ACME collaboration (2013)

For  $m \sim O(10)$  TeV, we need some mechanism to suppress the CP phases .

# Quark (C)EDMs

$$d_q^c \simeq \frac{\alpha_s}{4\pi} \frac{m_{q_3}}{m_{\tilde{q}}^2} \frac{M_3 X_q}{m_{\tilde{q}}^2} \text{Im}[\Delta_{13}^R \Delta_{31}^L] f(M_3^2/m_{\tilde{q}}^2)$$

$$f(x) \sim 3 \log x + \frac{59}{6} \quad (x \ll 1)$$

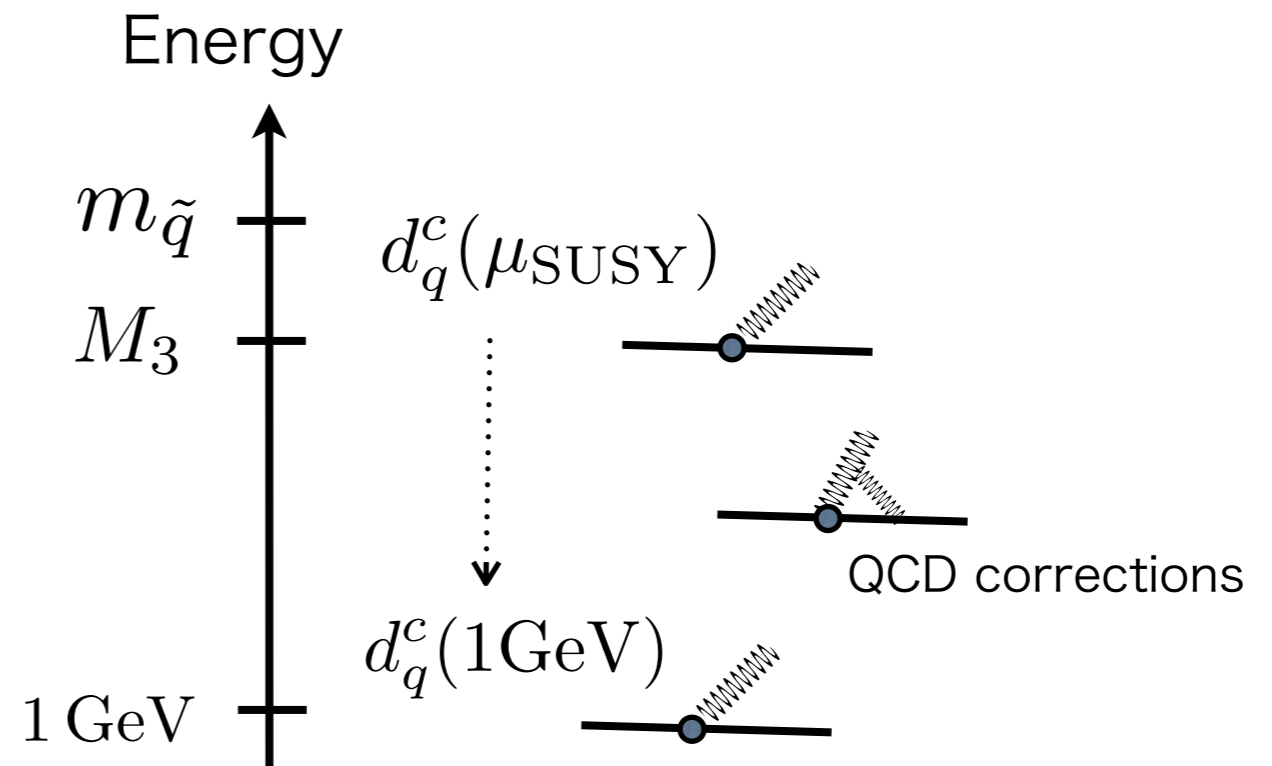
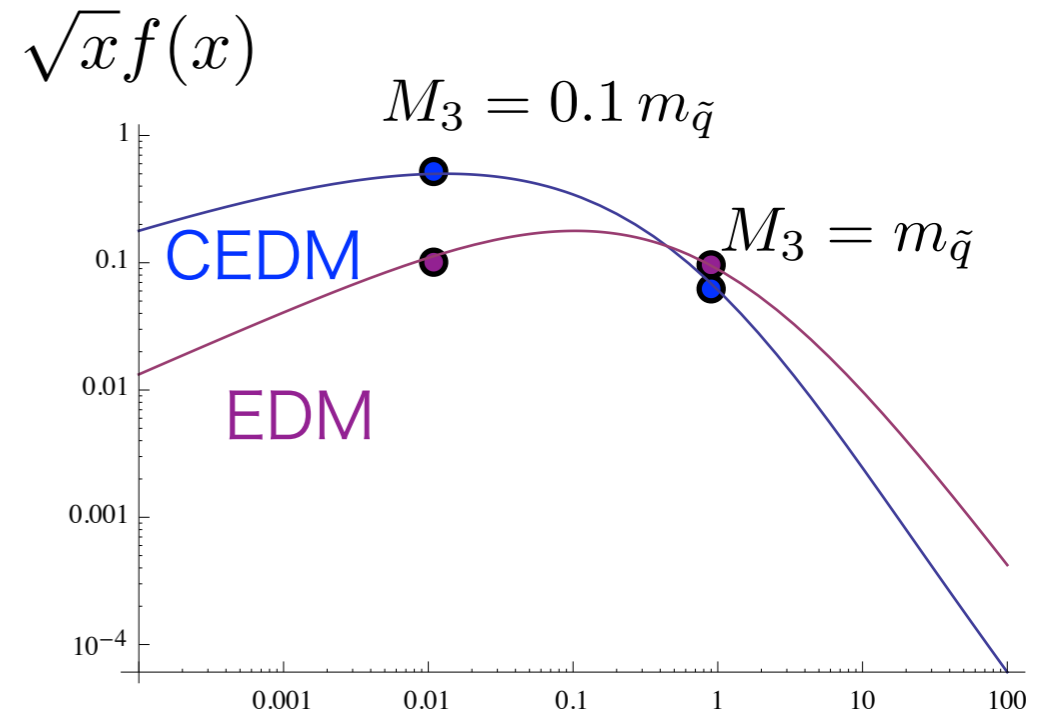
not suppressed so much even  
for lighter gauginos

Matching scale  $\mu_{\text{SUSY}}$ ?

$$\alpha_s(100\text{TeV})/\alpha_s(3\text{TeV}) \sim 0.82$$

$$M_3(100\text{TeV})/M_3(3\text{TeV}) \sim 0.69$$

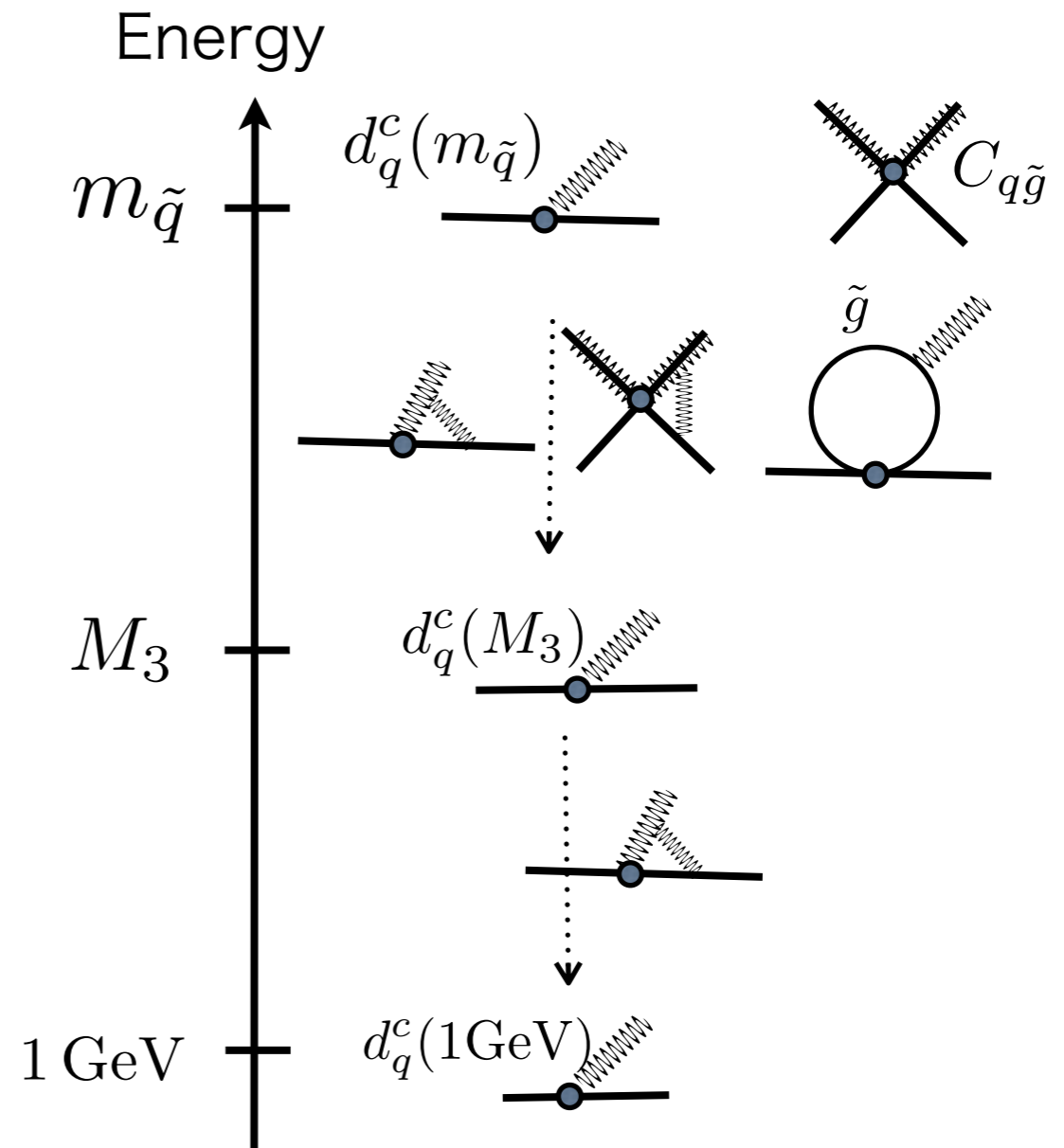
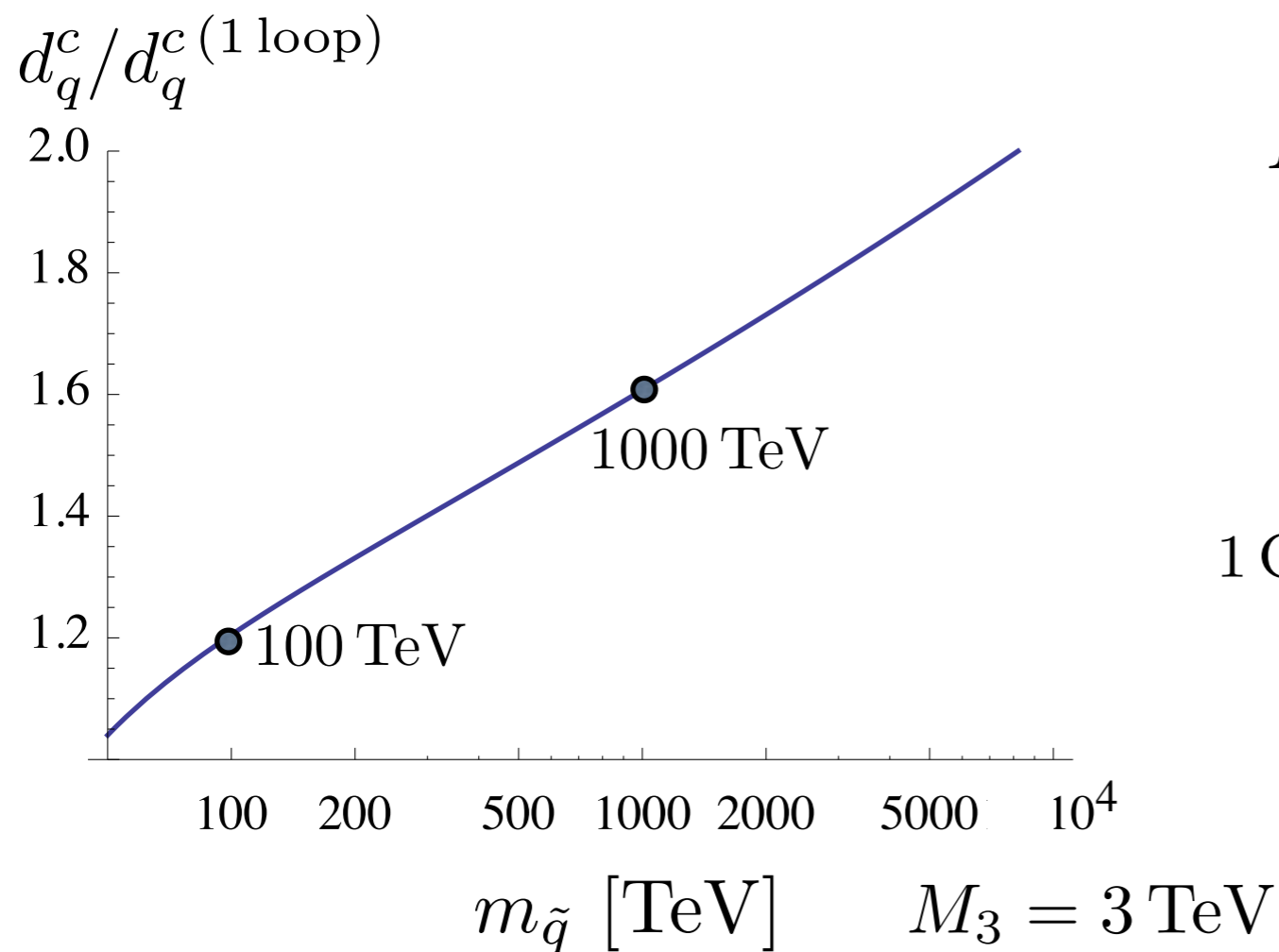
$$m_q(100\text{TeV})/m_q(3\text{TeV}) \sim 0.85$$



# QCD corrections to Quark (C)EDMs in high scale SUSY models

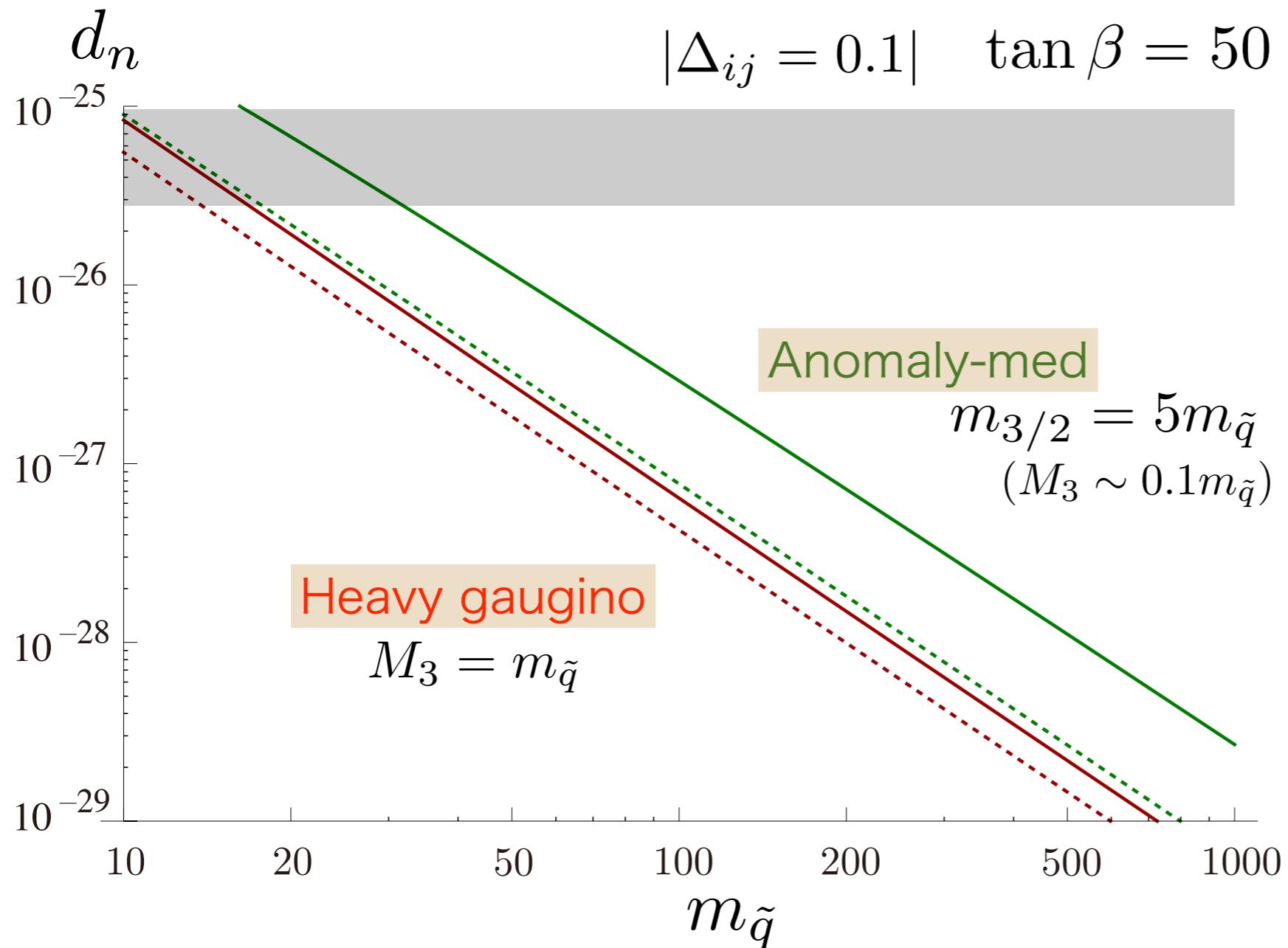
Altmannshofer, Harnik, Zupan (2013), Fuyuto, Hisano, Nagata, Tsumura (2013)

For  $M_3 \ll m_{\tilde{q}}$ , we need RG analysis to resum large logarithms.





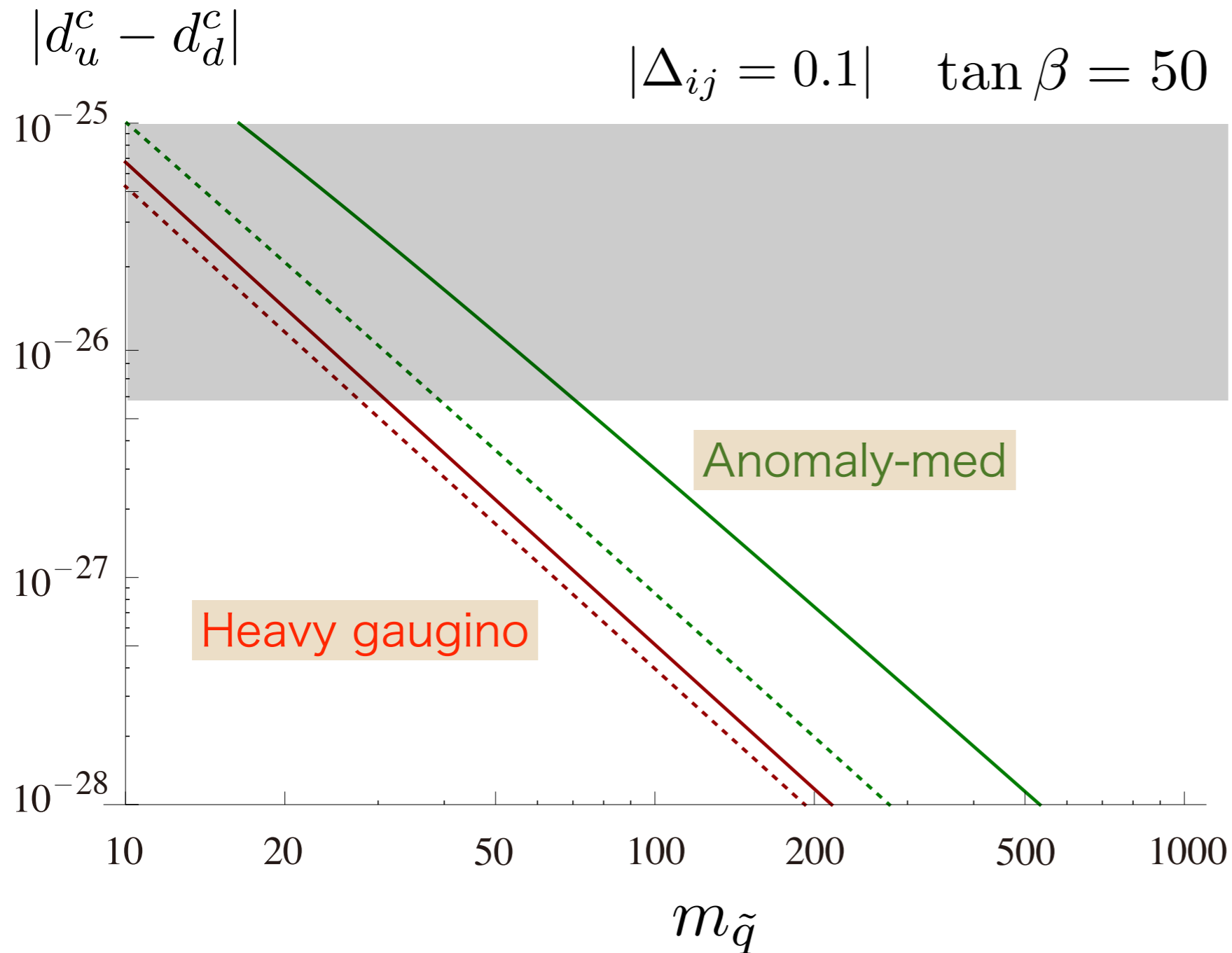
# nEDM in high scale SUSY models



— : flavored EDM  
 - - - : flavor-blind EDM

\* Thanks to logarithm terms, predicted EDMs are not changed so much for  $m_{3/2} = m_{\tilde{q}}$ . However, null result of gluino search put a bound,  $m_{\tilde{q}} > 40 \text{ TeV}$ , in that case.

# HgEDM in high scale SUSY models



— : flavored EDM  
 - - - : flavor-blind EDM

$|d_u^c - d_d^c| \lesssim 6 \times 10^{-27}$   
 from mercury EDM

Hadronic EDMs  
 are enhanced for  
 lighter gluino

# LFV in high-scale SUSY models with **universal** soft masses

[Moroi, MN, Ynagida (2013)]

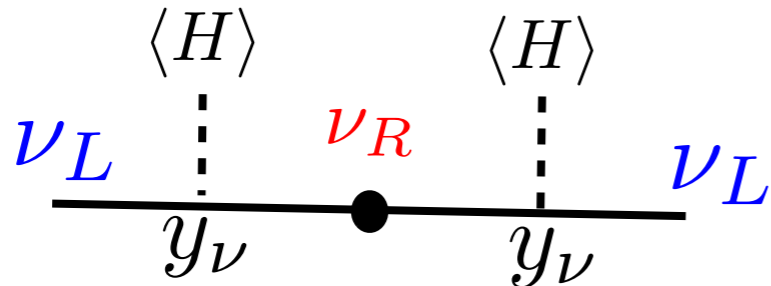
- Even with  $m \sim O(10-100)$  TeV,  $\epsilon_K$  and EDMs puts severe constraints on flavor- and CP-violating parameters.
- Sfermion mass matrices may have some **universal (degenerate)** structures at the tree-level to ameliorate these constraints even in high-scale SUSY models.

## Can we expect some flavor signals?

- Yes, flavor-mixing might be generated by radiative corrections.

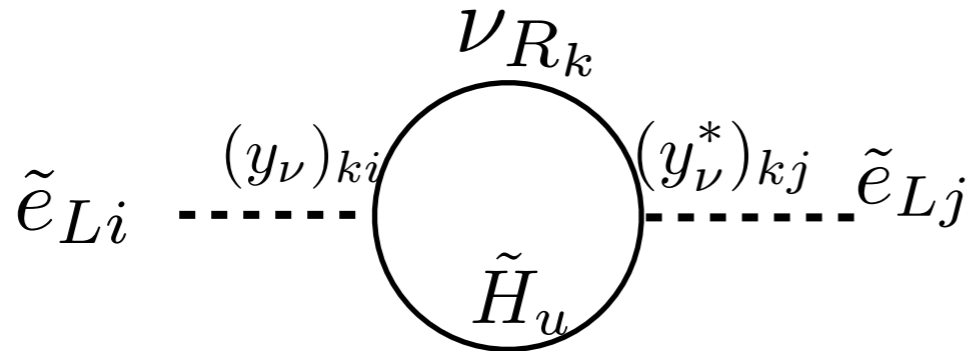
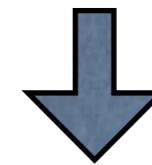
# Type-I SUSY see-saw model

Type-I See-saw model ... Introduction of heavy right-handed neutrinos (RNs)



$$\mathcal{L}_{\text{eff}} = \frac{1}{M_\nu} (l_L H_u)(l_L H_u) \quad m_\nu = \frac{y_\nu^2 v^2}{M_\nu}$$

For  $y_\nu \sim 1$ ,  $M_N \sim 10^{15} \text{ GeV}$

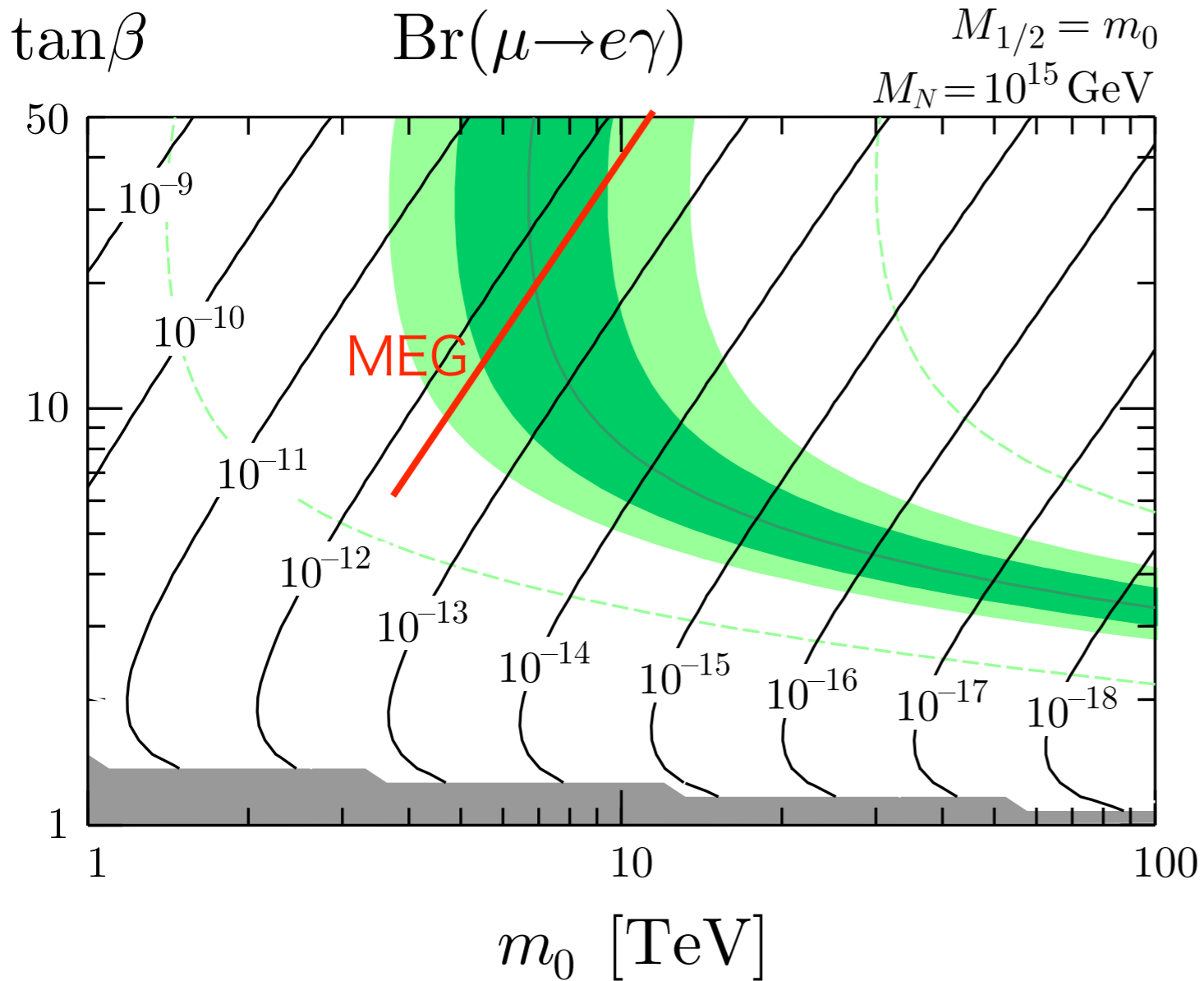


$$(\tilde{m}_L^2)_{ij} \sim (y_\nu^\dagger)_{ik} (y_\nu)_{kj} \log \frac{M_X}{M_{\nu_k}}$$

**Q** In the **SUSY see-saw model**, with keeping the explanation of Higgs mass, is it possible to detect the LFV signals?

# LFV in high scale SUSY models (universal)

mSUGRA



$m_0, M_{1/2}, \tan\beta, M_N(\text{or } y_\nu)$

$$y_\nu \rightarrow \Delta\tilde{e}_L$$

Flavored EDMs and epsilonK constraints are absent

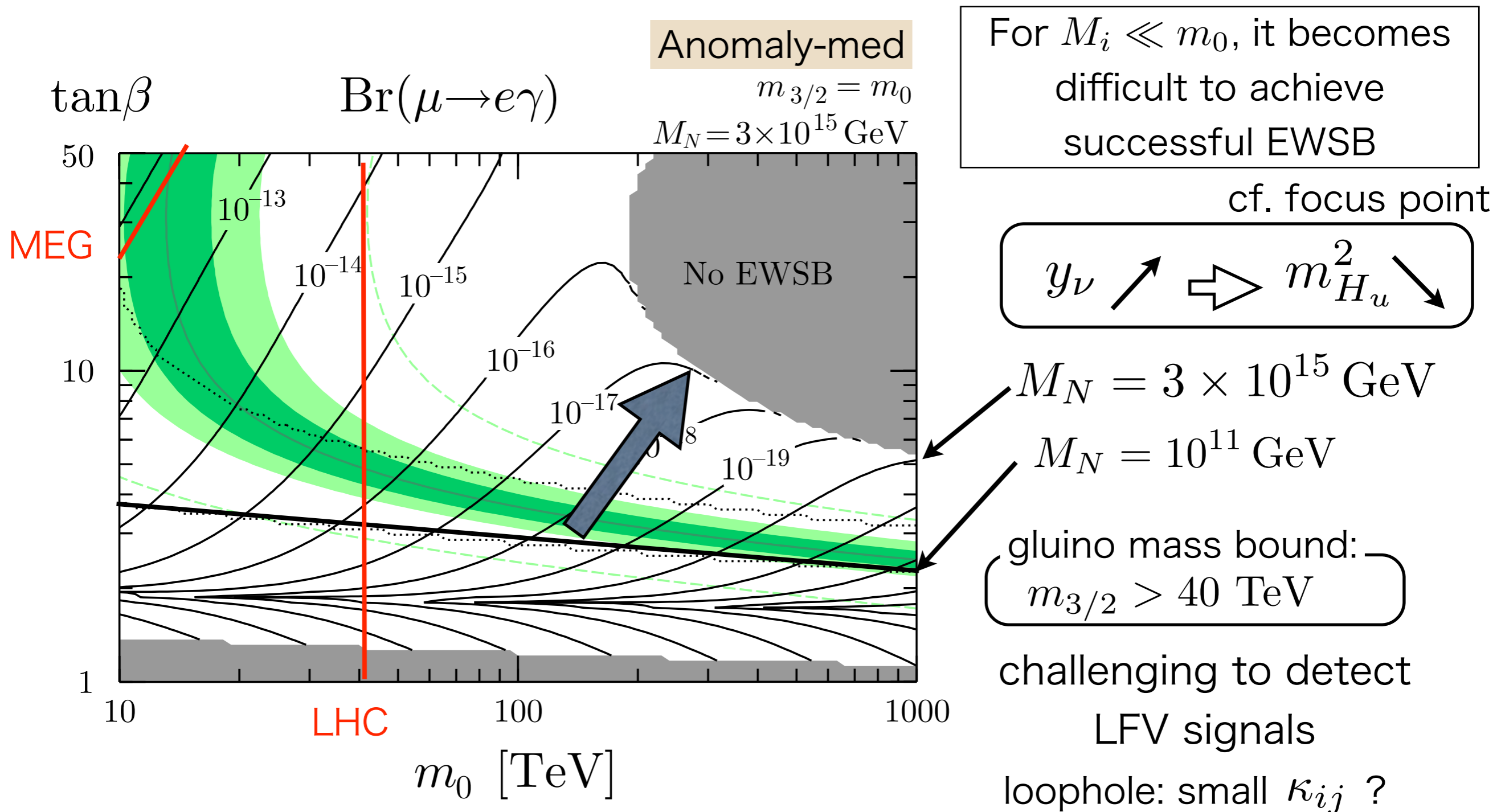
$$m_h \simeq 126 \text{ GeV}$$

$$M_N \sim 10^{15} \text{ GeV} \quad (y_\nu \sim 1)$$

➔ measurable LFV rates

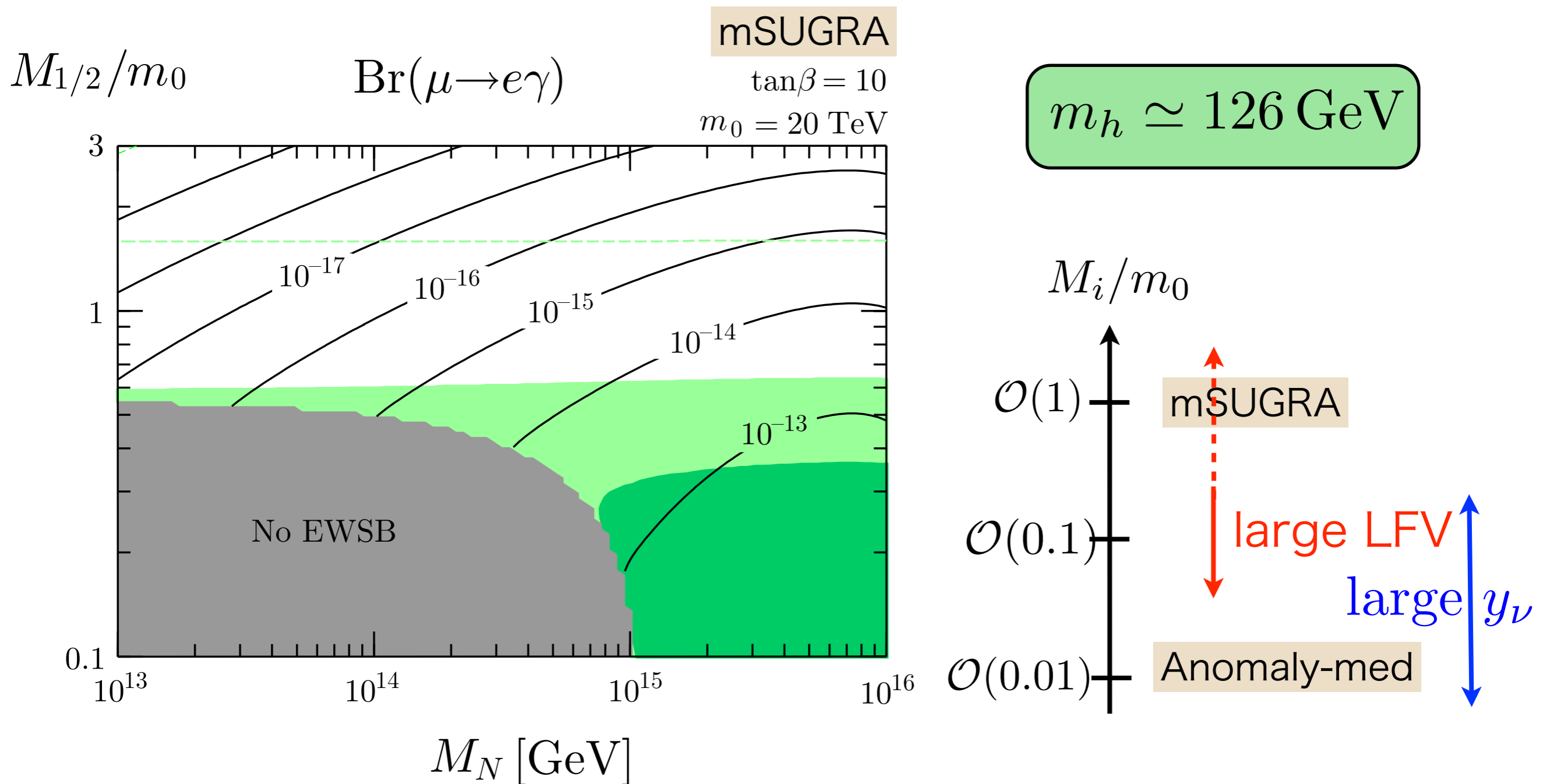
# LFV in high scale SUSY models (universal)

- Large neutrino Yukawa coupling is also useful to enlarge the parameter spaces with successful EWSB



# LFV in high scale SUSY models (universal)

- With lighter gaugino masses, a large neutrino Yukawa coupling is required, as long as universal soft masses are assumed.



# まとめ

- ✓ フレーバーの物理による新物理探索のためには、標準模型の予言と実験結果の精密な比較検証が必要。
  - 複数の観測量を考慮することにより現れる、新物理への示唆
  - 残っているアノマリー(?)の現状
- ✓ フレーバー観測量はLHC実験では直接探索できない高いエネルギースケールの物理を探ることが可能。
  - LFV & EDM による高エネルギー(10-100 TeV) 超対称模型の探索



# 宣伝

- KEK Theory Meeting on Particle Physics Phenomenology (KEK-PH 2014)

10/21-10/24

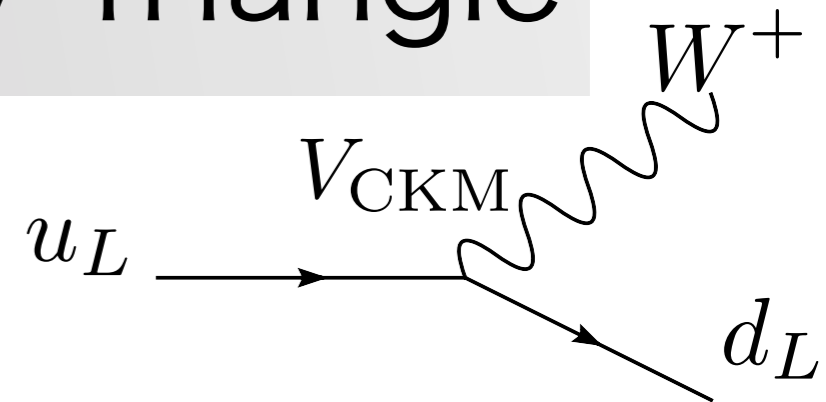
- KEK Flavor Factory Workshop (KEK-FF2014FALL)/ Belle II Theory Interface Platform (B2TiP) Meeting

10/28-10/31

<http://kds.kek.jp/conferenceDisplay.py?confId=15873>

# Back Up

# CKM matrix and Unitarity Triangle



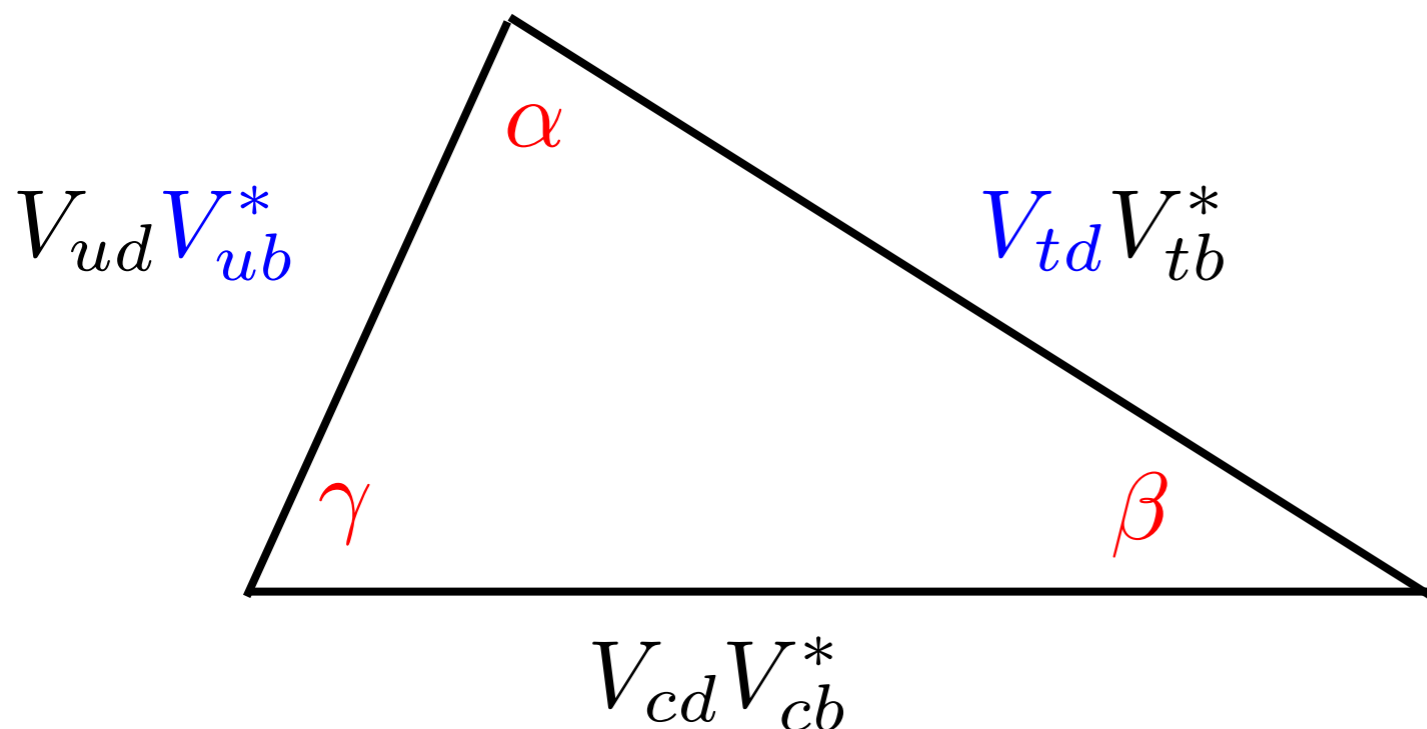
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Wolfenstein parametrization

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$|V_{us}| = 0.2252(9)$$

$$|V_{cb}| = (40.6 \pm 1.3) \times 10^{-3}$$

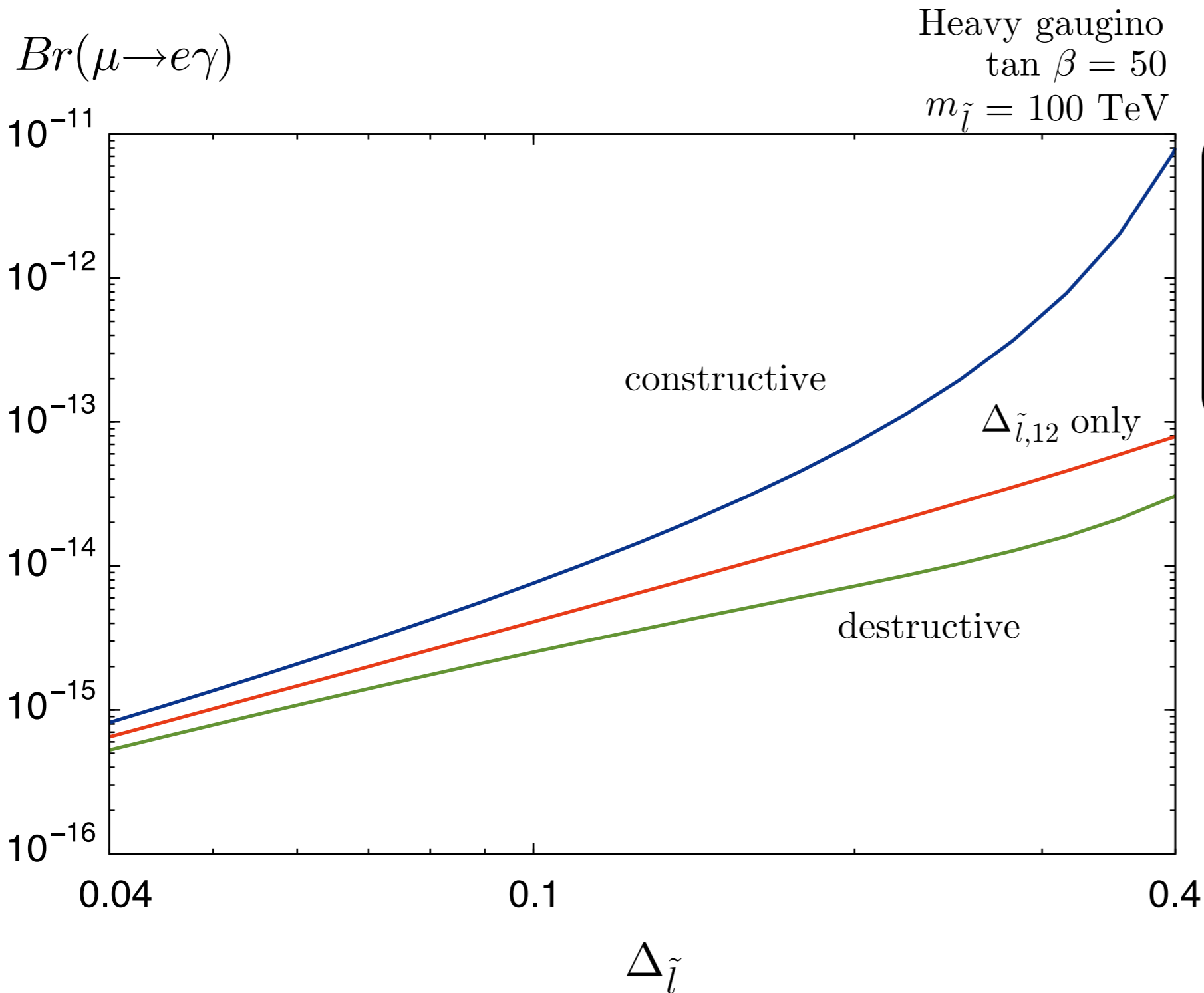


$$V_{td} = |V_{td}|e^{-i\beta}$$

$$V_{ub} = |V_{ub}|e^{-i\gamma}$$

$$V_{ts} = -|V_{ts}|e^{-i\beta_s}$$

# Importance of double-mass insertion in high-scale SUSY models (Anarchy)



$$\alpha_2 \Delta_{e_L}^{12}$$

vs

$$\alpha_Y \Delta_{e_L}^{13} \Delta_{e_R}^{32} m_\tau / m_\mu$$

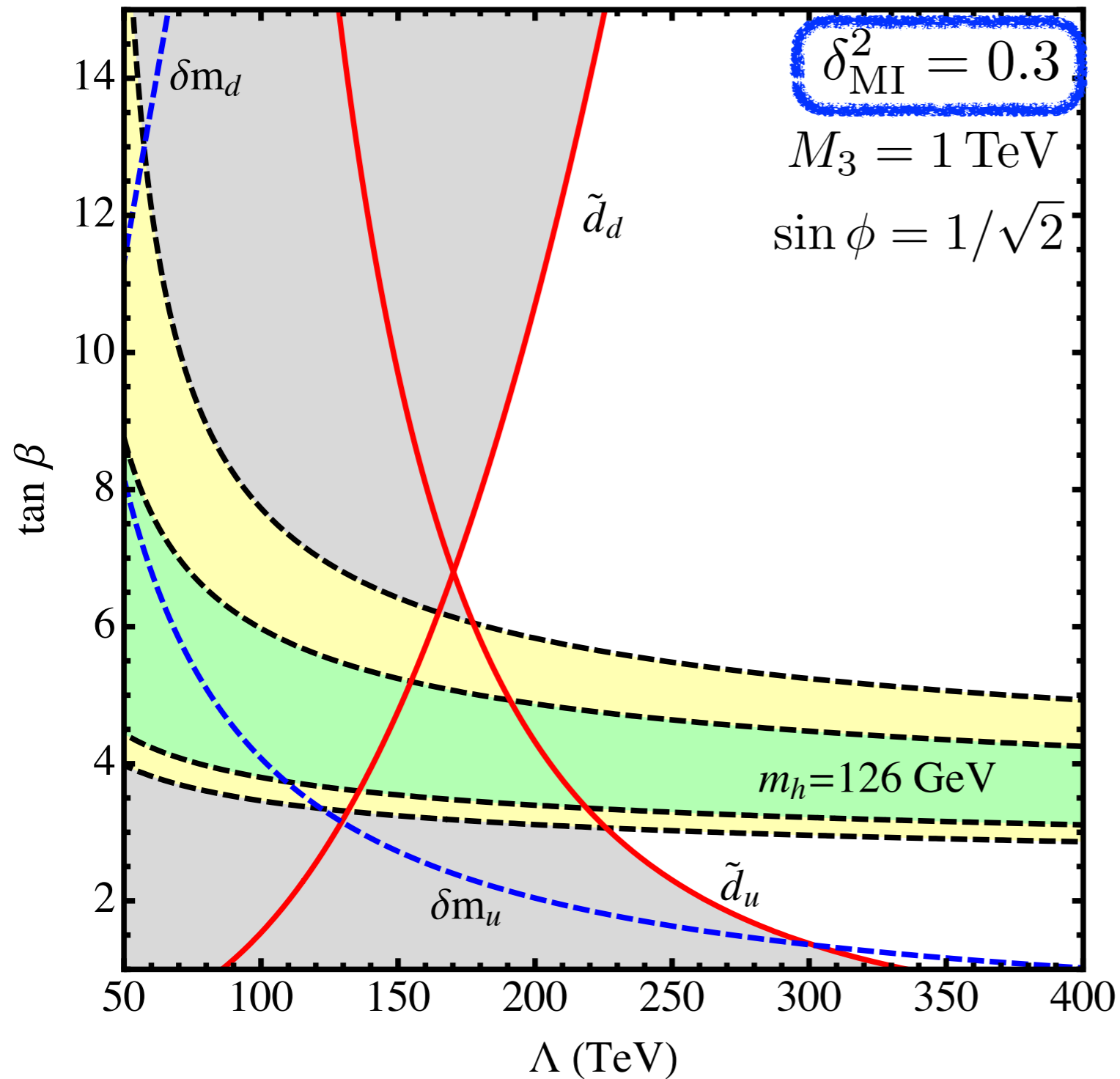
single mass insertion

$$Br \propto \frac{\Delta^2}{m_{\text{SUSY}}^4}$$

double mass insertion

$$Br \propto \frac{\Delta^4}{m_{\text{SUSY}}^4}$$

# Summary of flavor constraints (i)



$$|\tilde{d}_u - \tilde{d}_d| < 6 \times 10^{-27} \text{ cm}$$

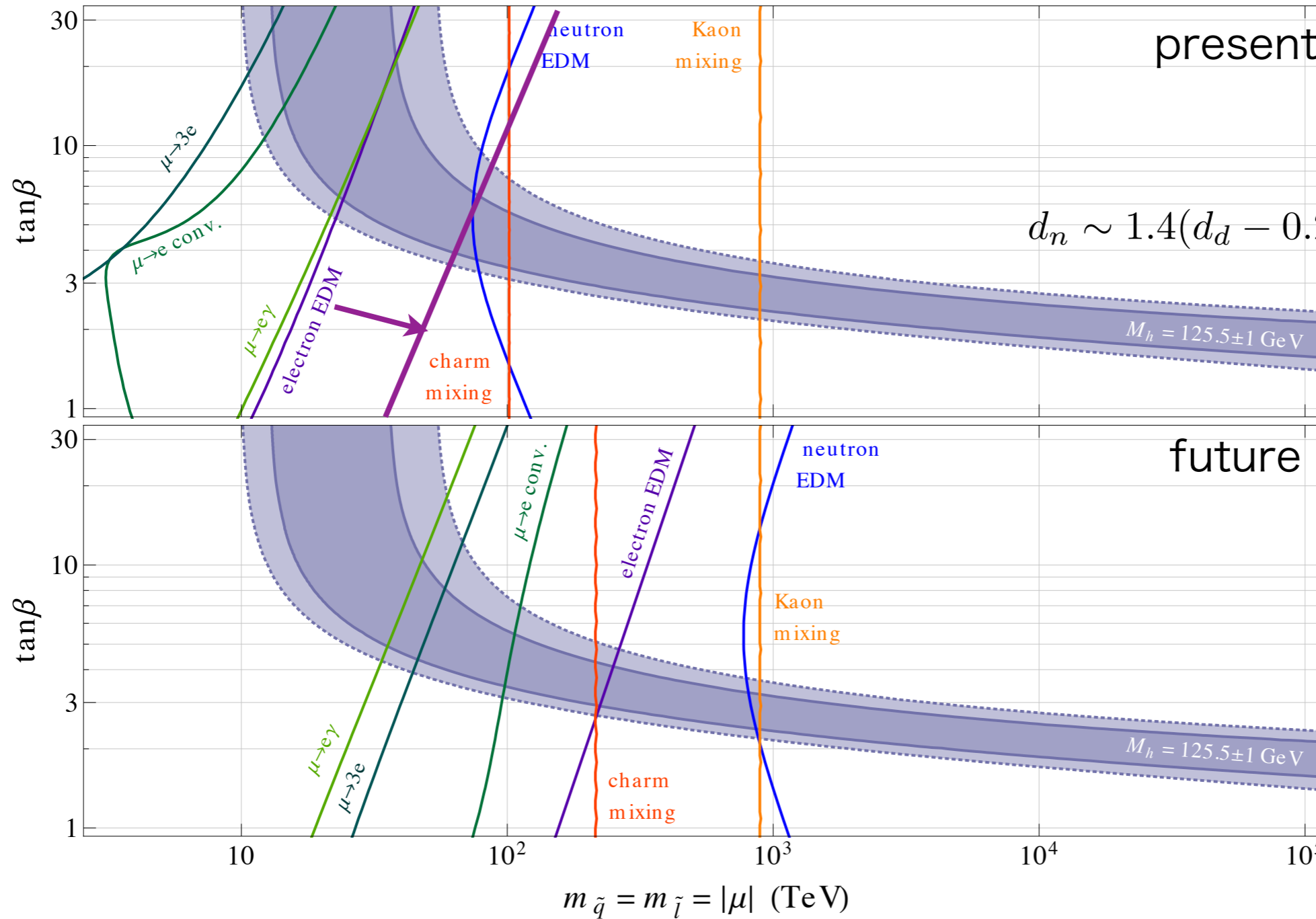
from mercury EDM

McKeen, Pospelov and Ritz (2013)

# Summary of flavor constraints (ii)

Altmannshofer, Harnik, Zupan (2013)

$$|m_{\tilde{B}}| = |m_{\tilde{W}}| = 3 \text{ TeV}, |m_{\tilde{g}}| = 10 \text{ TeV}$$

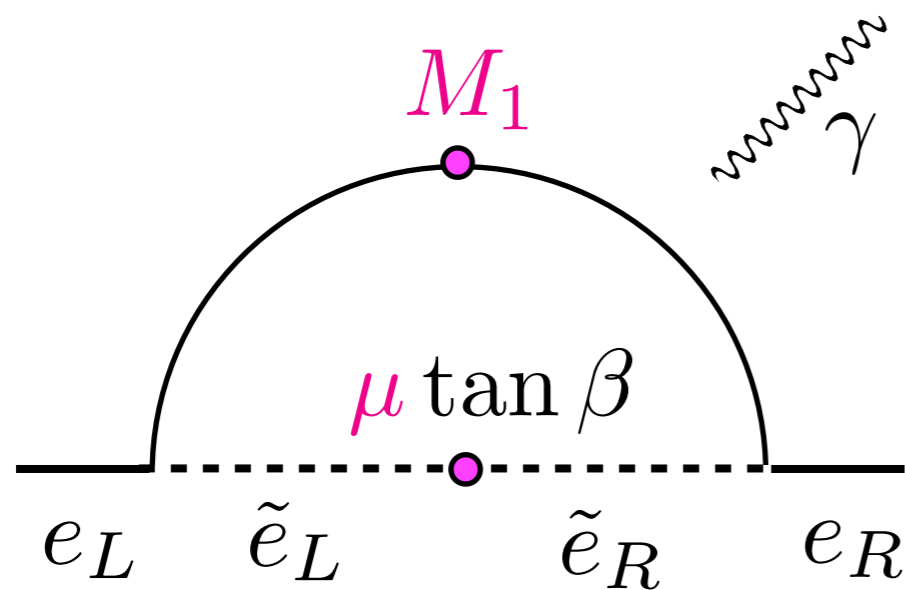


$$\delta_{\text{MI}} = 0.3$$

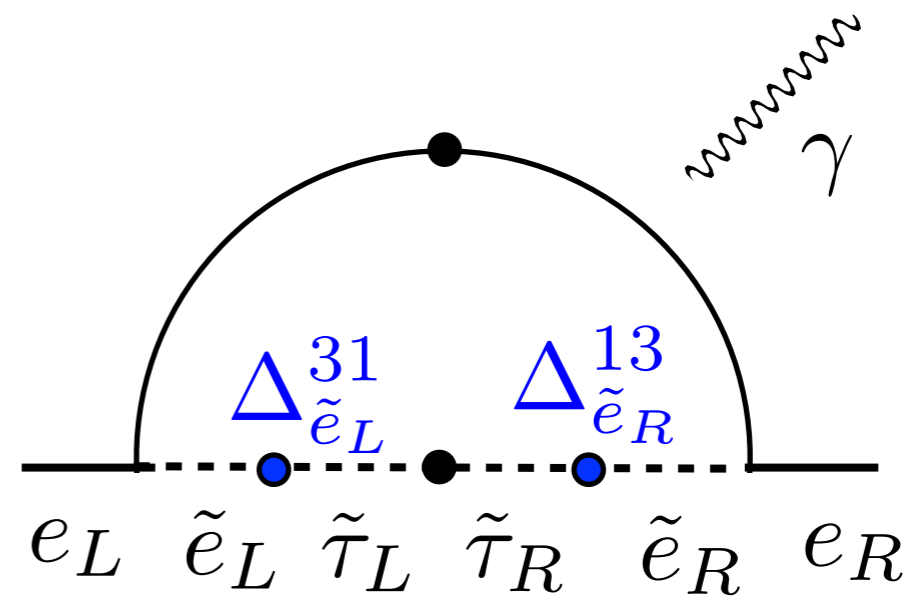
$$d_n \sim 1.4(d_d - 0.25d_u) + 1.1e(d_d^c + 0.5d_u^c) < 2.9 \times 10^{-26} e \text{ cm}$$

# Electron EDM in SUSY models

CP violating phases can appear in **flavor-blind** and/or **flavor-violating** mass terms.



“flavor-blind EDM”



“flavored EDM”

For  $\Delta \sim O(1)$ , flavored EDMs are much important because of the large enhancement by  $m_\tau/m_e$ .