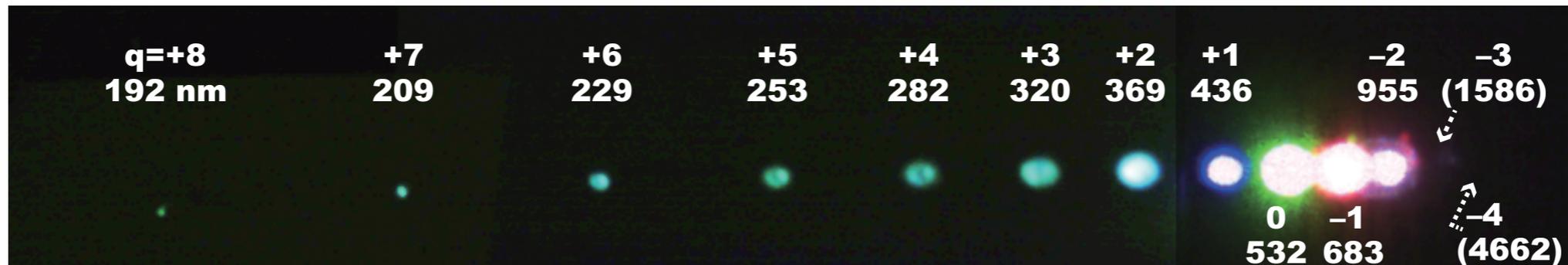


原子・分子過程による ニュートリノ物理

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大阪大学



素粒子物理学の進展2015@YITP, 京都, 2015/09/16

SPAN project

SPECTROSCOPY WITH ATOMIC NEUTRINO

Okayama U.

K. Kawaguchi, H. Hara, T. Masuda, Y. Miyamoto,
I. Nakano, N. Sasao, J. Tang, S. Uetake,
A. Yoshimi, K. Yoshimura, M. Yoshimura

Other institute

M. T. (Osaka), T. Wakabayashi (Kinki),
A. Fukumi (Kawasaki), S. Kuma (Riken),
C. Ohae (ECU), K. Nakajima (KEK), H. Nanjo (Kyoto)

INTRODUCTION

What we know about neutrino mass and mixing

Masses:

$$\Delta m_{21}^2 \simeq (8.66 \text{ meV})^2, \quad |\Delta m_{31(2)}^2| \simeq (49.6(5) \text{ meV})^2$$

$$\sum m_\nu \leq 0.23 \text{ eV} \quad \text{PLANCK 2013} \quad \text{NuFIT (2014)}$$

Mixing: $U = V_{\text{PMNS}} P$

$$V_{\text{PMNS}} =$$

$$\begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix}$$

$$P = \text{diag.}(1, e^{i\alpha}, e^{i\beta}) \quad \text{Majorana phases}$$

Bilenky, Hosek, Petcov; Doi, Kotani, Nishiura, Okuda, Takasugi; Schechter, Valle

$$\sin^2 \theta_{12} \simeq 0.30, \quad \sin^2 \theta_{23} \simeq 0.45(58), \quad \sin^2 \theta_{13} \simeq 0.022$$

NuFIT (2014)

Unknown properties of neutrinos

Absolute mass

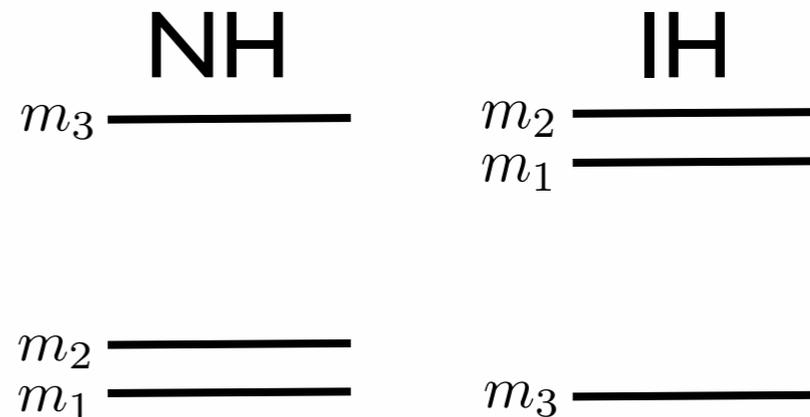
$$m_{1(3)} < 71(66) \text{ meV}, \quad 50 \text{ meV} < m_{3(2)} < 87(82) \text{ meV}$$

Mass type

Dirac or Majorana

Hierarchy pattern

normal or inverted



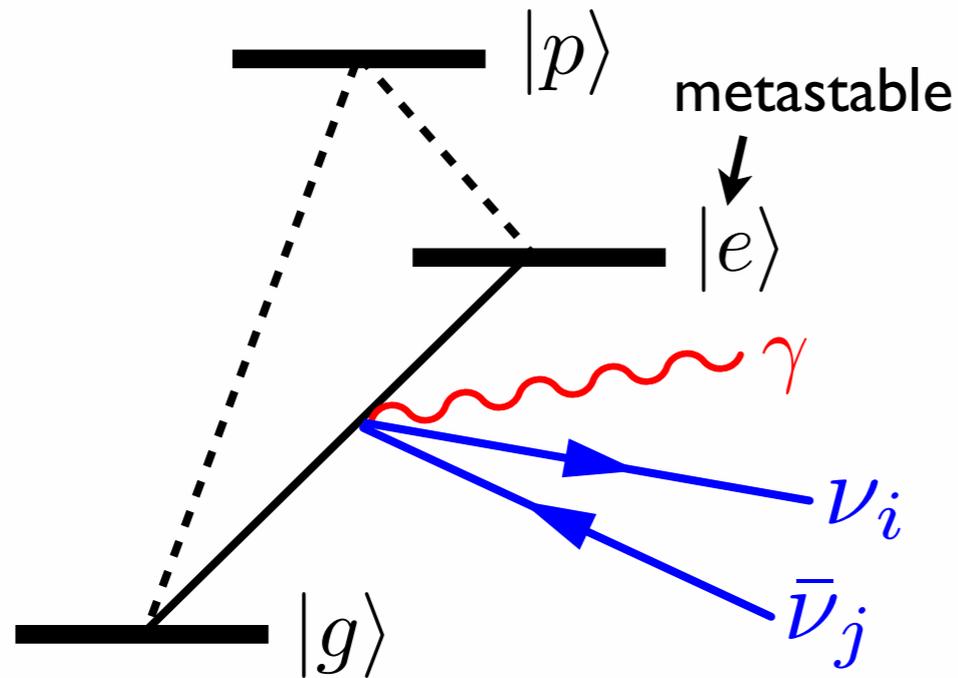
CP violation

one Dirac phase, two Majorana phases
 δ α, β

RENP

Radiative Emission of Neutrino Pair (RENPN)

A.Fukumi et al. PTEP (2012) 04D002, arXiv:1211.4904



$$|e\rangle \rightarrow |g\rangle + \gamma + \nu_i \bar{\nu}_j$$

Λ -type level structure

Ba, Xe, Ca⁺, Yb, ...

H₂, O₂, I₂, ...

Atomic/molecular energy scale \sim eV or less
close to the neutrino mass scale

cf. nuclear processes \sim MeV

$$\text{Rate} \sim \alpha G_F^2 E^5 \sim 1/(10^{33} \text{ s})$$

Enhancement mechanism?

Rate enhancement by coherence

R.H. Dicke,
Phys. Rev. 93, 99 (1954)

An ensemble of N atoms in a small volume L^3

$$L \ll \text{wave length} \implies e^{-ikx} \sim 1$$

Density matrix $\rho = \rho_{gg}|g\rangle\langle g| + \rho_{ee}|e\rangle\langle e| + \rho_{eg}|e\rangle\langle g| + \rho_{ge}|g\rangle\langle e|$

Fully excited state: $|e\rangle^N = |e\rangle \cdots |e\rangle$, $\rho_{eg} = 0$

deexcitation: $\left(\sum |g\rangle\langle e|\right) \prod |e\rangle$

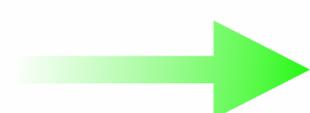
$$= |g\rangle|e\rangle \cdots |e\rangle + |e\rangle|g\rangle \cdots |e\rangle + \cdots + |e\rangle|e\rangle \cdots |g\rangle$$

 $\Gamma = N\Gamma_0$ **incoherent**

Fully coherent state: $\left[(|g\rangle + |e\rangle)/\sqrt{2} \right]^N$, $\rho_{eg} = 1/2$

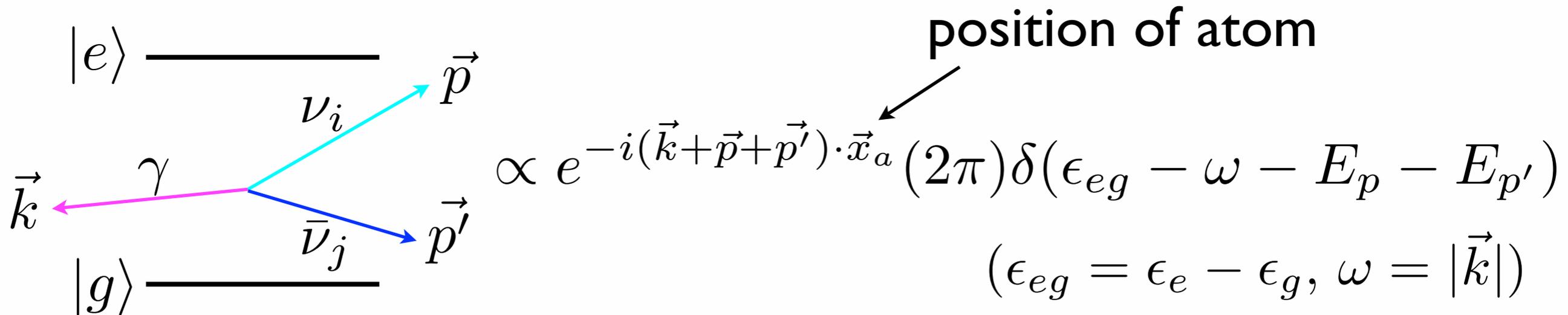
 $[|g\rangle(|g\rangle + |e\rangle) \cdots (|g\rangle + |e\rangle)$
deexcitation

$$+ (|g\rangle + |e\rangle)|g\rangle \cdots (|g\rangle + |e\rangle) + \cdots]/\sqrt{2^N}$$

 $\Gamma = N(N+1)\Gamma_0/4 \propto N^2$ **coherent**

Macrocoherence

Yoshimura et al. (2008)



Macroscopic target of N atoms, volume V ($n=N/V$)

$$\text{total amp.} \propto \sum_a e^{-i(\vec{k} + \vec{p} + \vec{p}') \cdot \vec{x}_a} \simeq \frac{N}{V} (2\pi)^3 \delta^3(\vec{k} + \vec{p} + \vec{p}')$$

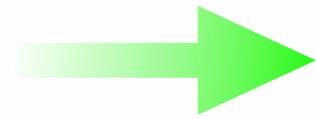
$$d\Gamma \propto n^2 V (2\pi)^4 \delta^4(q - p - p') \quad q^\mu = (\epsilon_{eg} - \omega, -\vec{k})$$

macrocoherent amplification

RENPs spectrum

D.N. Dinh, S.T. Petcov, N. Sasao, M.T., M. Yoshimura
PLB719(2013)154, arXiv:1209.4808

Energy-momentum conservation
due to the macrocoherence

 familiar 3-body decay kinematics

Six thresholds of the photon energy

$$\omega_{ij} = \frac{\epsilon_{eg}}{2} - \frac{(m_i + m_j)^2}{2\epsilon_{eg}} \quad i, j = 1, 2, 3$$

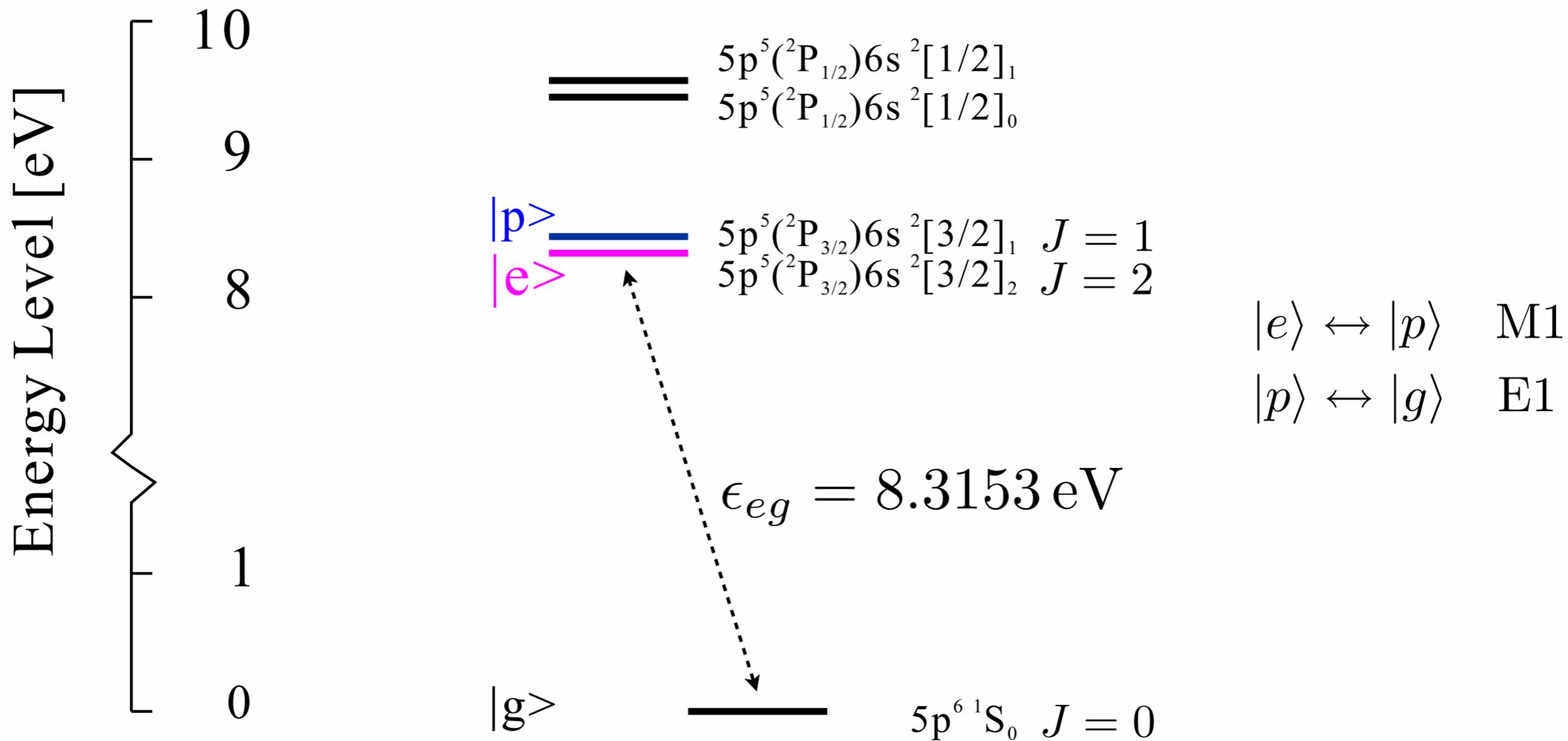
$$\epsilon_{eg} = \epsilon_e - \epsilon_g \quad \text{atomic energy diff.}$$

Required energy resolution $\sim O(10^{-6})$ eV

typical laser linewidth

$$\Delta\omega_{\text{trig.}} \lesssim 1 \text{ GHz} \sim O(10^{-6}) \text{ eV}$$

Xe



macro-coherence

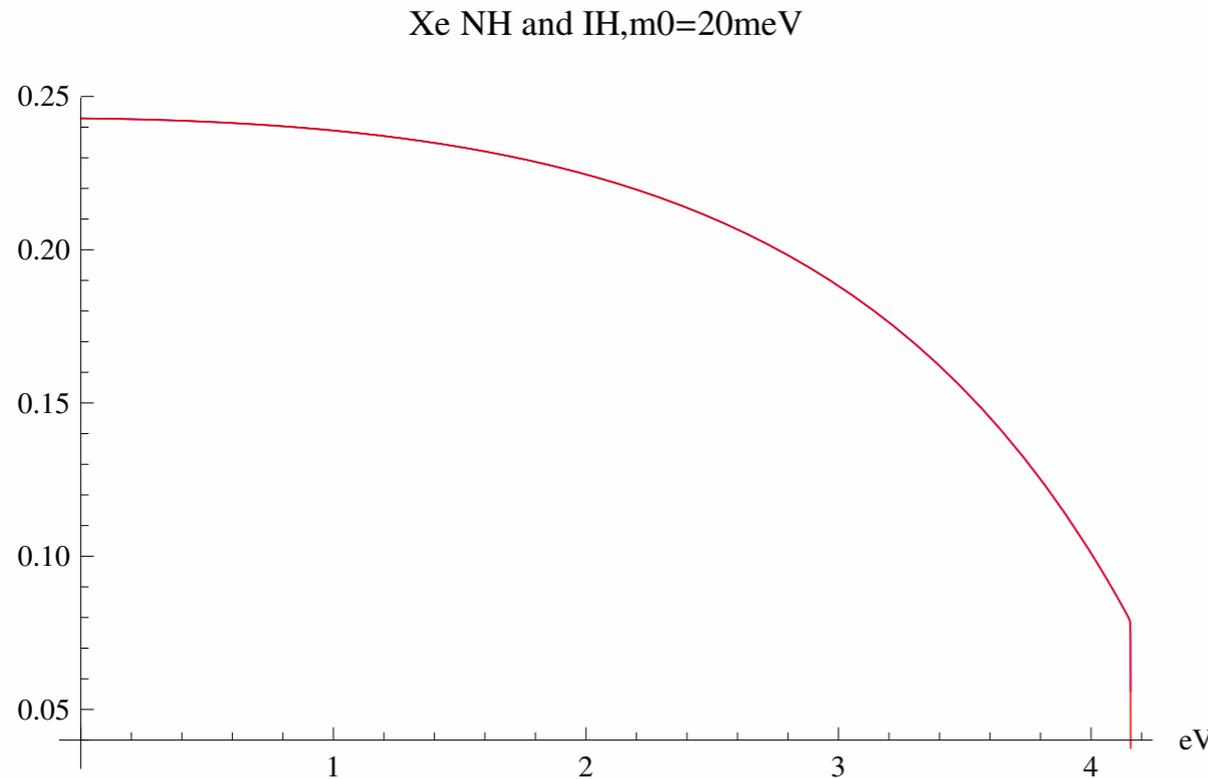
field energy density

$$\Gamma_0^{\text{SC}} \sim \frac{3n^2V G_F^2 \gamma_{pg} \epsilon_{eg} n}{2\epsilon_{pg}^3} \sim 1\text{ mHz} (n/10^{21}\text{ cm}^{-3})^3 (V/10^2\text{ cm}^3)$$

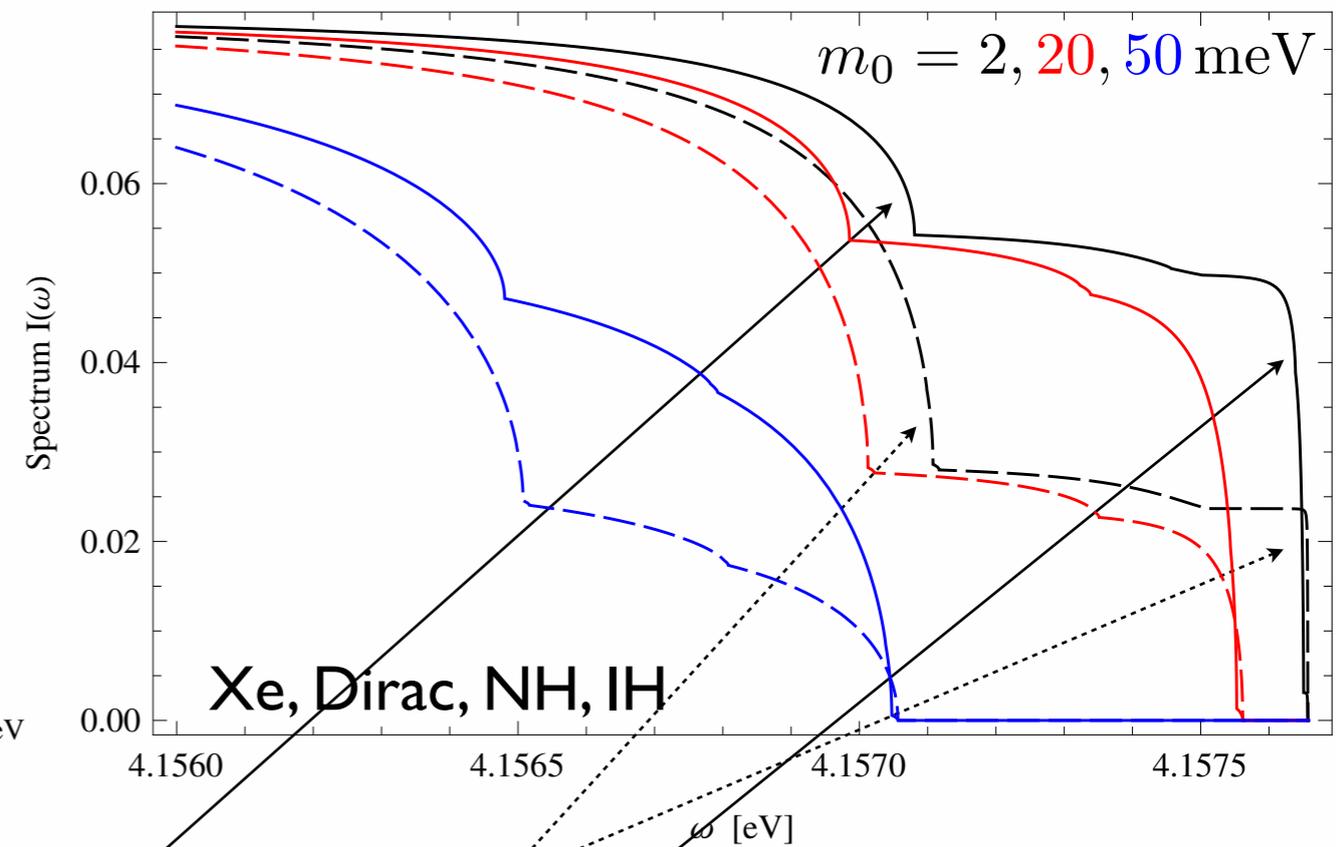
$\gamma_{pg} : |p\rangle \rightarrow |g\rangle$ rate

Photon spectrum (spin current)

Global shape



Threshold region



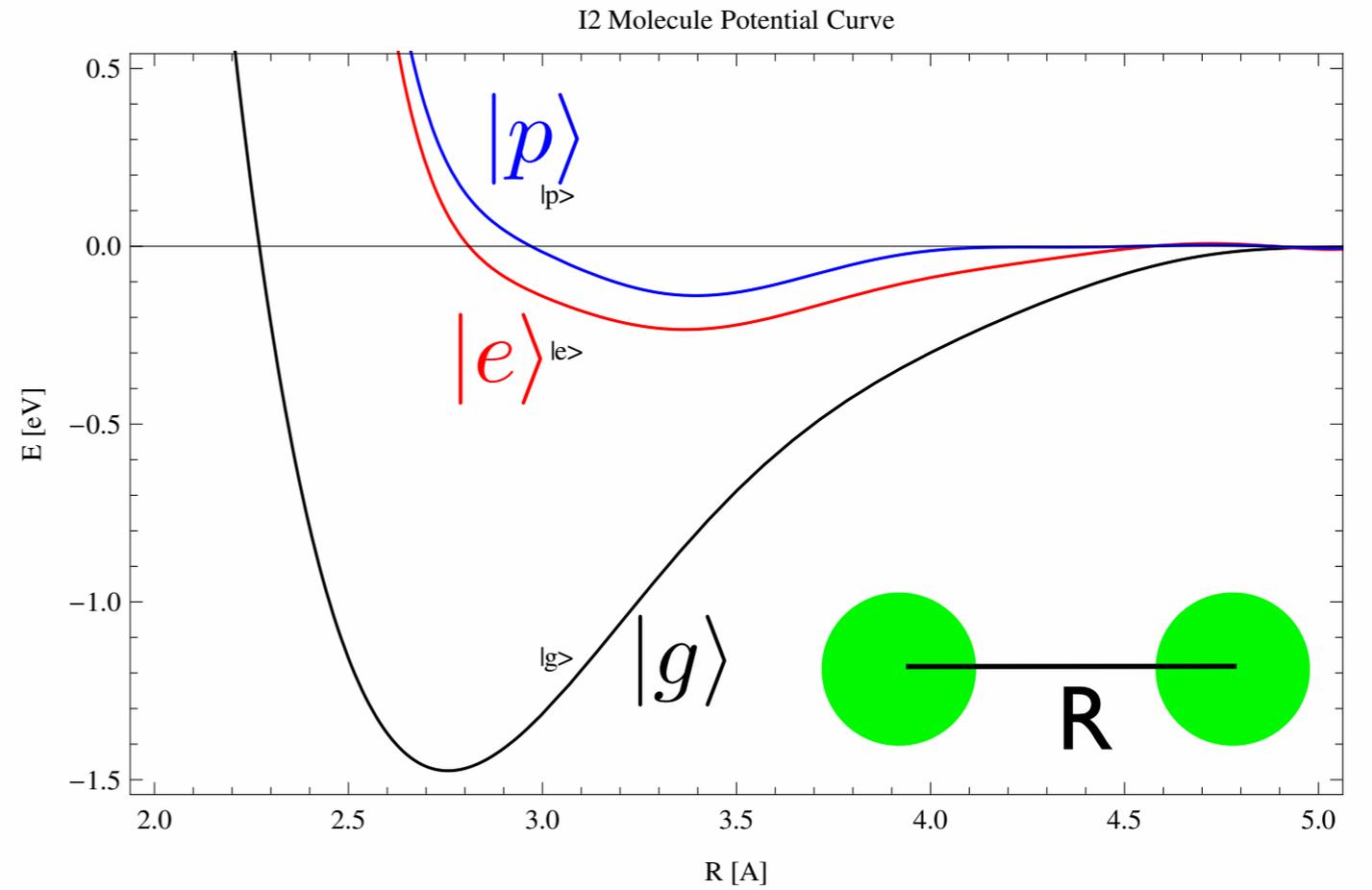
The threshold weight factors

B_{11}	B_{22}	B_{33}	$B_{12} + B_{21}$	$B_{23} + B_{32}$	$B_{31} + B_{13}$
$(c_{12}^2 c_{13}^2 - 1/2)^2$	$(s_{12}^2 c_{13}^2 - 1/2)^2$	$(s_{13}^2 - 1/2)^2$	$2c_{12}^2 s_{12}^2 c_{13}^4$	$2s_{12}^2 c_{13}^2 s_{13}^2$	$2c_{12}^2 c_{13}^2 s_{13}^2$
0.0311	0.0401	0.227	0.405	0.0144	0.0325

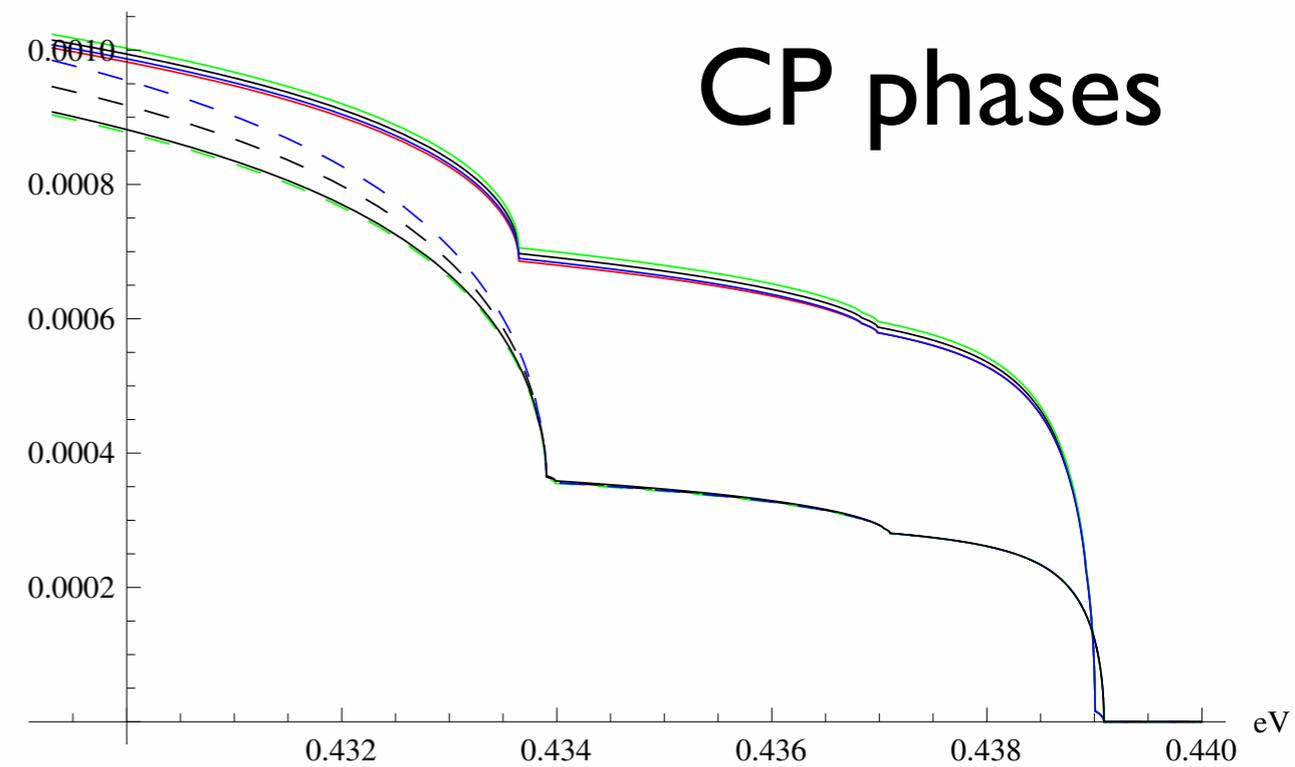
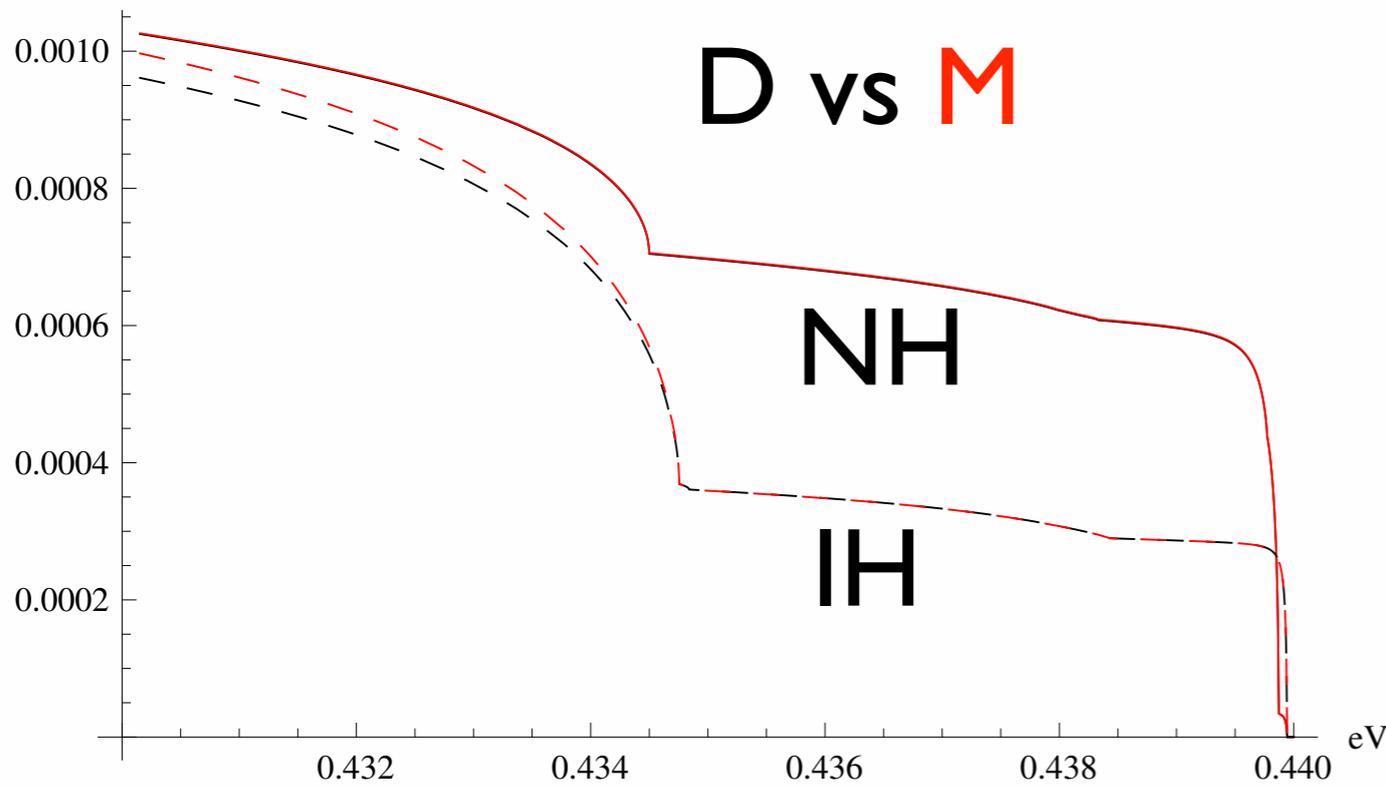
I2 molecule potential curves

$$\epsilon_{eg} \sim 1 \text{ eV}$$

I2 A'v=1 → Xv=15: m0=5meV



I2 A'v=1 → Xv=15: m0=20meV



D-M diff. < 10%

CNB

Cosmic Neutrino Background (CNB)

Big bang cosmology

Standard model
of particle physics



CNB

CNB at present: $f(\mathbf{p}) = [\exp(|\mathbf{p}|/T_\nu - \xi) + 1]^{-1}$

(not) Fermi-Dirac dist. $|\mathbf{p}| = \sqrt{E^2 - m_\nu^2}$

$$T_\nu = \left(\frac{4}{11}\right)^{1/3} T_\gamma \simeq 1.945 \text{ K} \simeq 0.17 \text{ meV}$$


$$n_\nu \simeq 6 \times 56 \text{ cm}^{-3}$$

Detection?

RENPN in CNB

M. Yoshimura, N. Sasao, MT,
PRD91, 063516 (2015); arXiv:1409.3648

$$|e\rangle \rightarrow |g\rangle + \gamma + \nu_i \bar{\nu}_j$$

Pauli exclusion

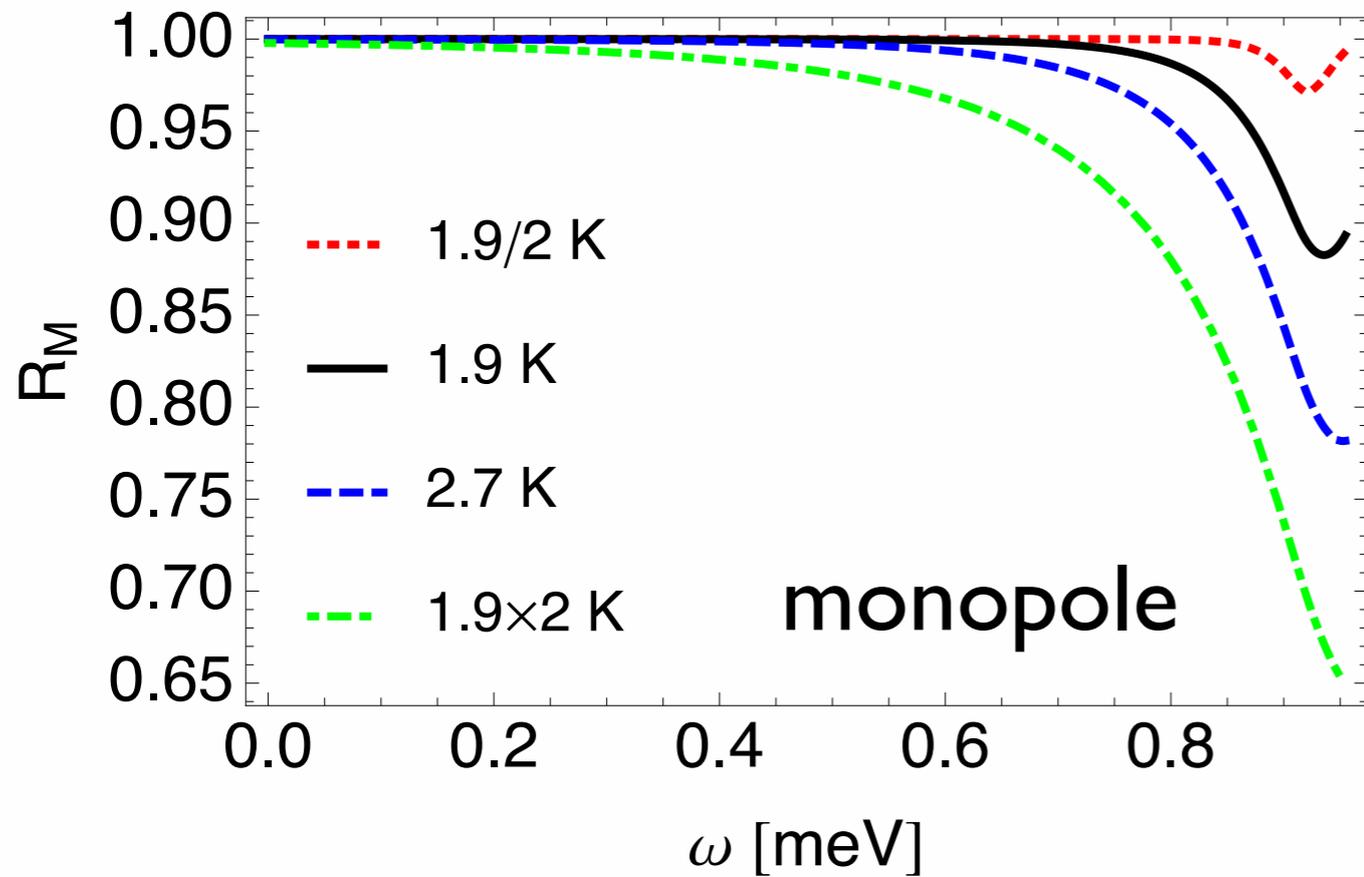
$$d\Gamma \propto |\mathcal{M}|^2 [1 - f_i(p)] [1 - \bar{f}_j(p')]$$

 spectral distortion

Distortion factor

$$R_X(\omega) \equiv \frac{\Gamma_X(\omega, T_\nu)}{\Gamma_X(\omega, 0)}$$

$$X = \begin{cases} M & \text{nuclear monopole} \\ S & \text{valence } e \text{ spin current} \end{cases} \quad \text{larger rate} \quad i = j$$



level splitting

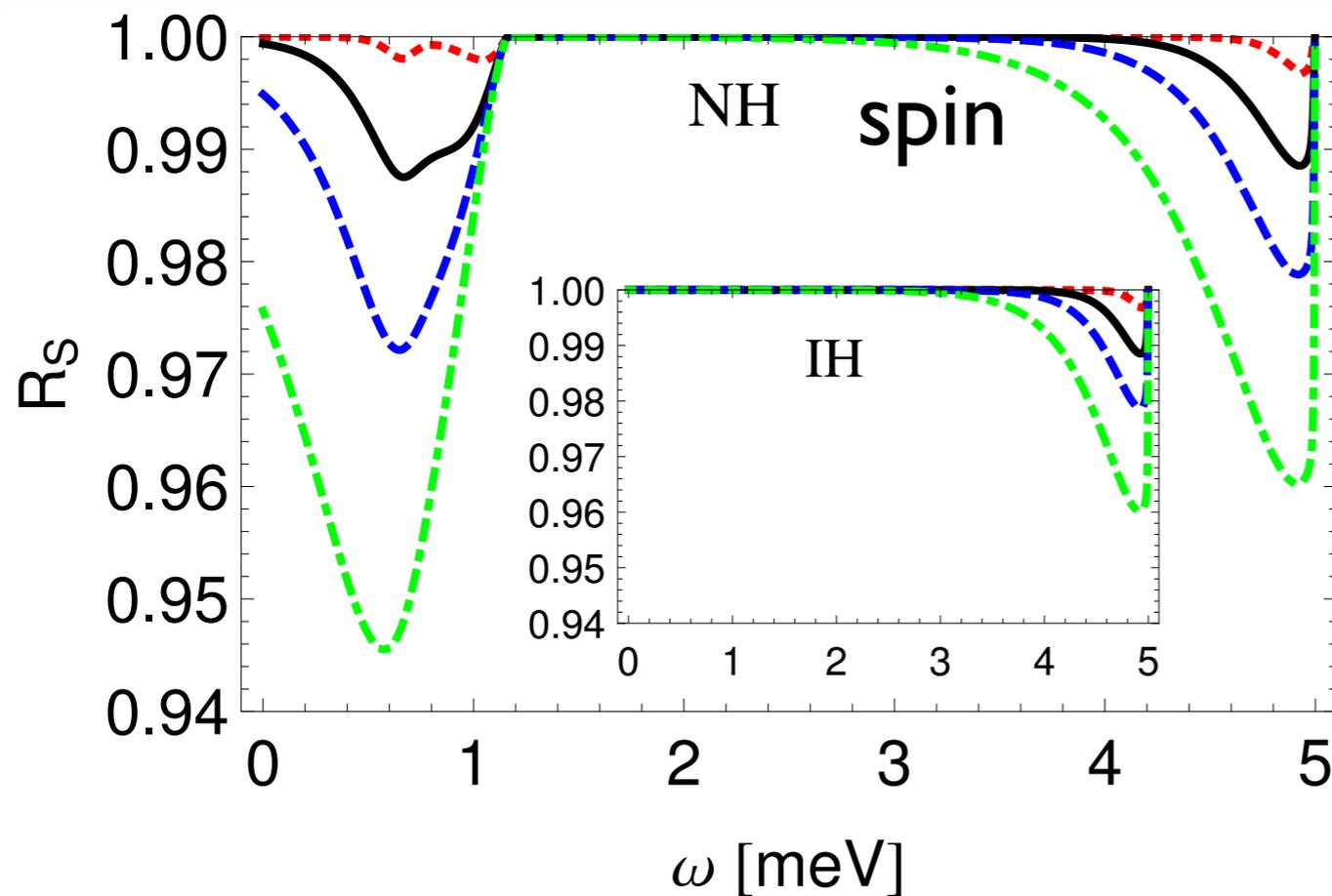
$$\epsilon_{eg} = 11 \text{ meV}$$

smallest neutrino mass

$$m_0 = 5 \text{ meV}$$

chemical potential

$$\xi_i \equiv \mu_i / T_\nu = 0$$



$$\epsilon_{eg} = 10 \text{ meV}$$

$$m_0 = 0.1 \text{ meV}$$

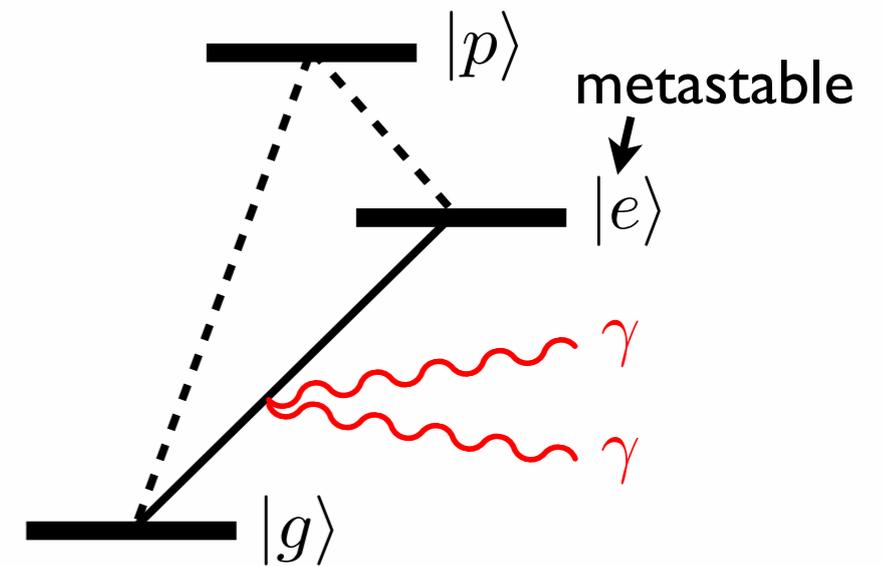
$$\xi_i = 0$$

PSR

Paired Super-Radiance (PSR)

M. Yoshimura, N. Sasao, MT, PRA86, 013812 (2012)

$$|e\rangle \rightarrow |g\rangle + \gamma + \gamma$$



Prototype for RENP

proof-of-concept for the **macrocoherence**

Preparation of **initial state** for RENP

coherence generation ρ_{eg}

dynamical factor $\eta_{\omega}(t)$

Theoretical description to be tested

Maxwell-Bloch equation

PSR with spatial gratings

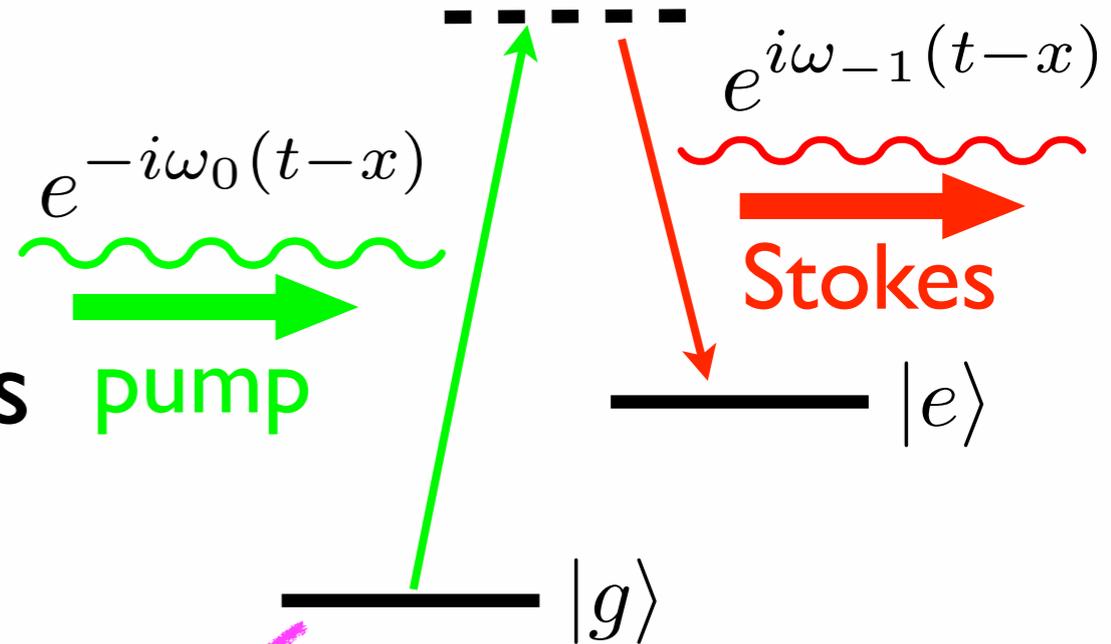
How to populate $|e\rangle$

Stimulated Raman process

$$\omega_0 - \omega_{-1} = \epsilon_{eg}$$

Generated coherence

$$\rho_{eg} = \rho_{eg}^{(0)} + \rho_{eg}^{(+)} e^{i\epsilon_{eg}x} + \rho_{eg}^{(-)} e^{-i\epsilon_{eg}x}$$



Stokes
pump



$$e^{i\omega_p(t-x)} e^{i\omega_{\bar{p}}(t-x)} = e^{i\epsilon_{eg}(t-x)}$$

$$\omega_p + \omega_{\bar{p}} = \epsilon_{eg}$$

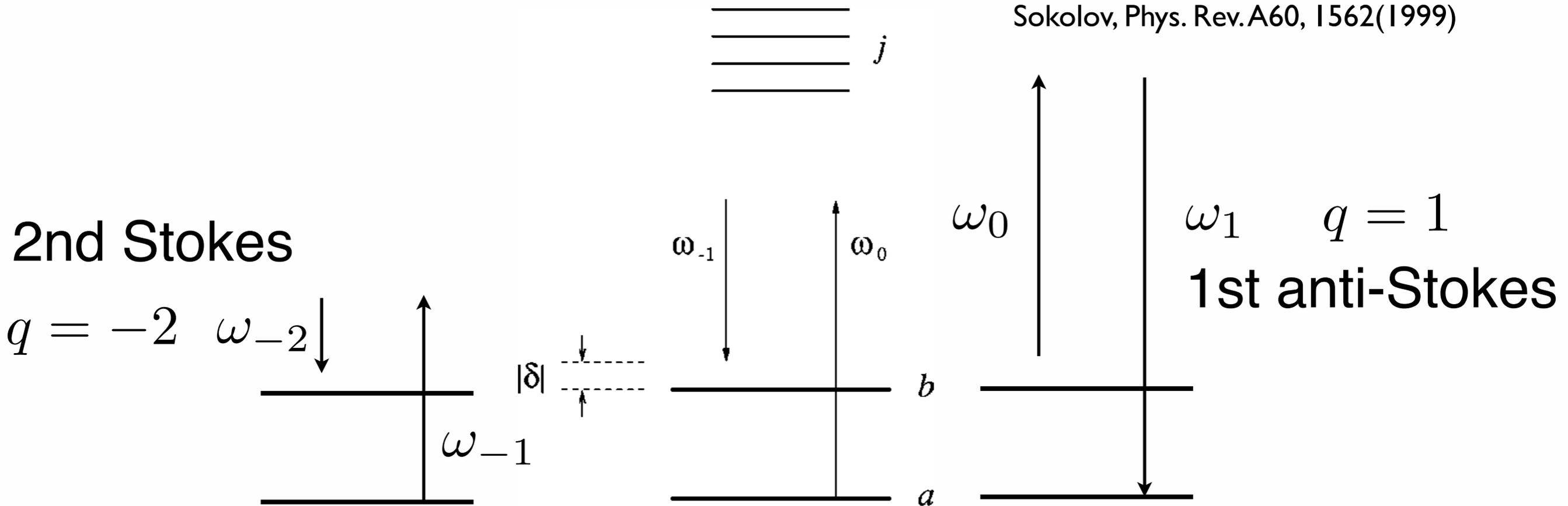
momentum conservation
in the macrocoherence

Unidirectional PSR

Raman sideband generation

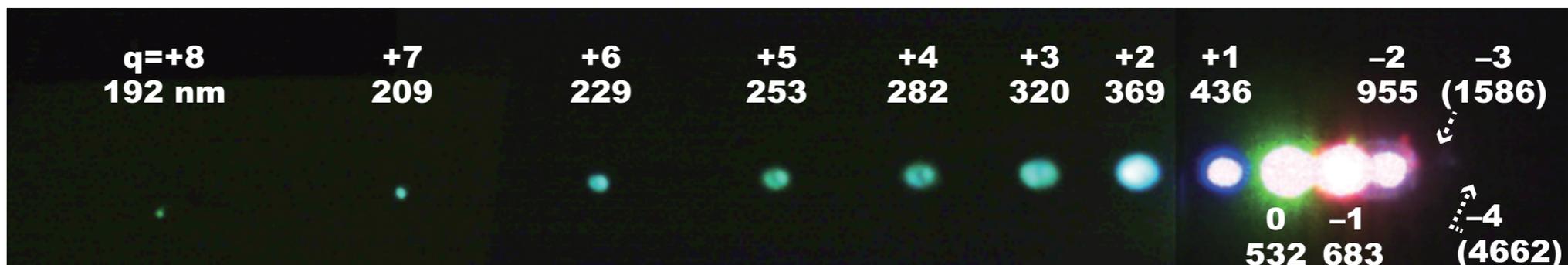
Harris, Sokolov, Phys. Rev. A55, R4019 (1997)

Kien, Liang, Katsuragawa, Ohtsuki, Hakuta, Sokolov, Phys. Rev. A60, 1562 (1999)



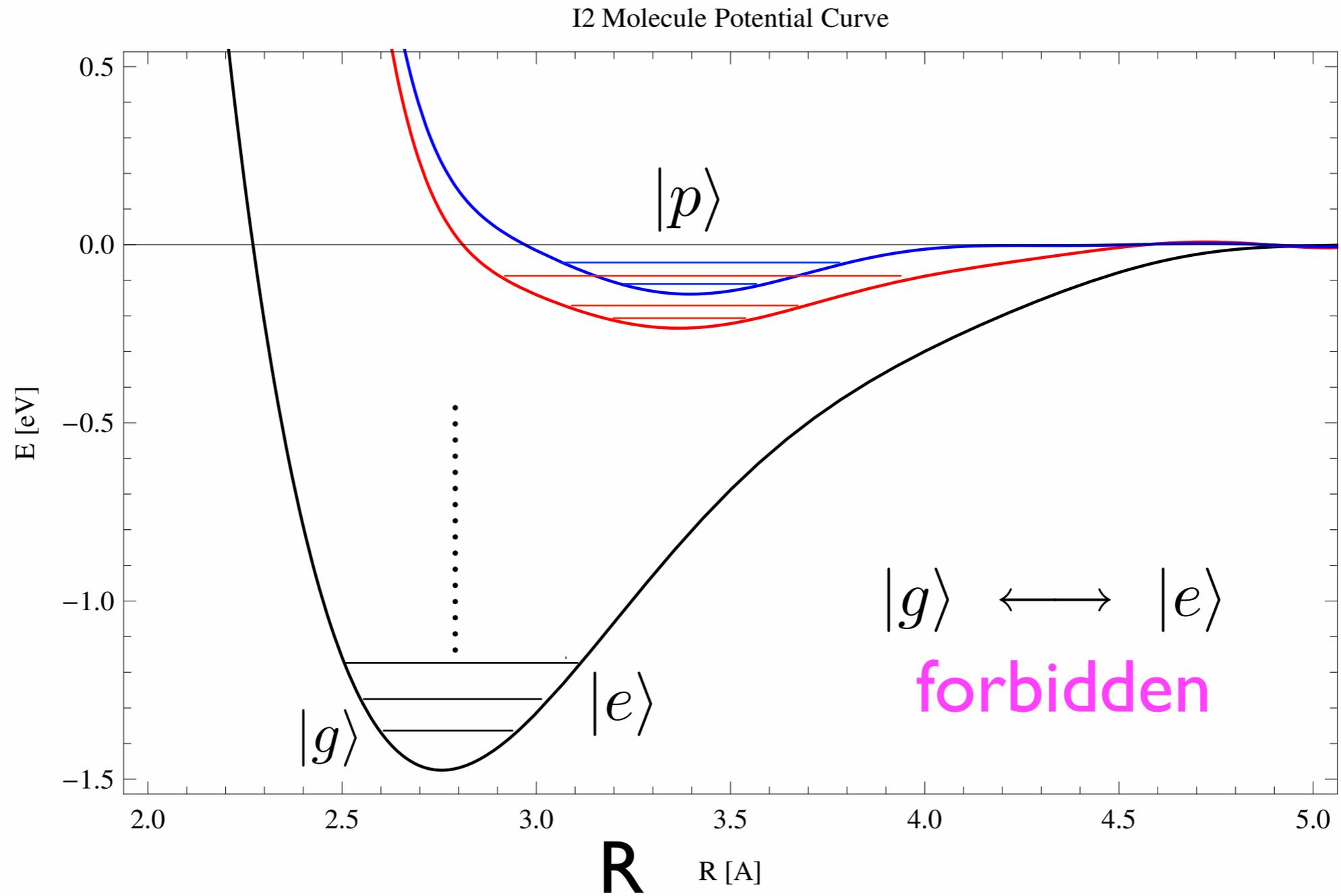
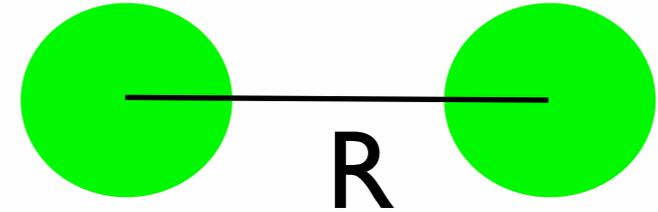
$$\omega_q = \omega_0 + q(\omega_b - \omega_a - \delta) = \omega_0 + q\omega_m$$

$q \geq q_{\min}$ the lowest Stokes



Homonuclear diatomic molecule

Potential curves



Para-hydrogen gas PSR experiment

@ Okayama U

Y. Miyamoto et al. PTEPI 13C01 (2014)

arXiv 1406.2198

vibrational transition of p-H₂

$$|e\rangle = |Xv = 1\rangle \longrightarrow |g\rangle = |Xv = 0\rangle$$

two-photon decay: $\tau_{2\gamma} \sim 10^{11}$ s

p-H₂: nuclear spin=singlet

smaller decoherence

$$1/T_2 \sim 130 \text{ MHz}$$

coherence production

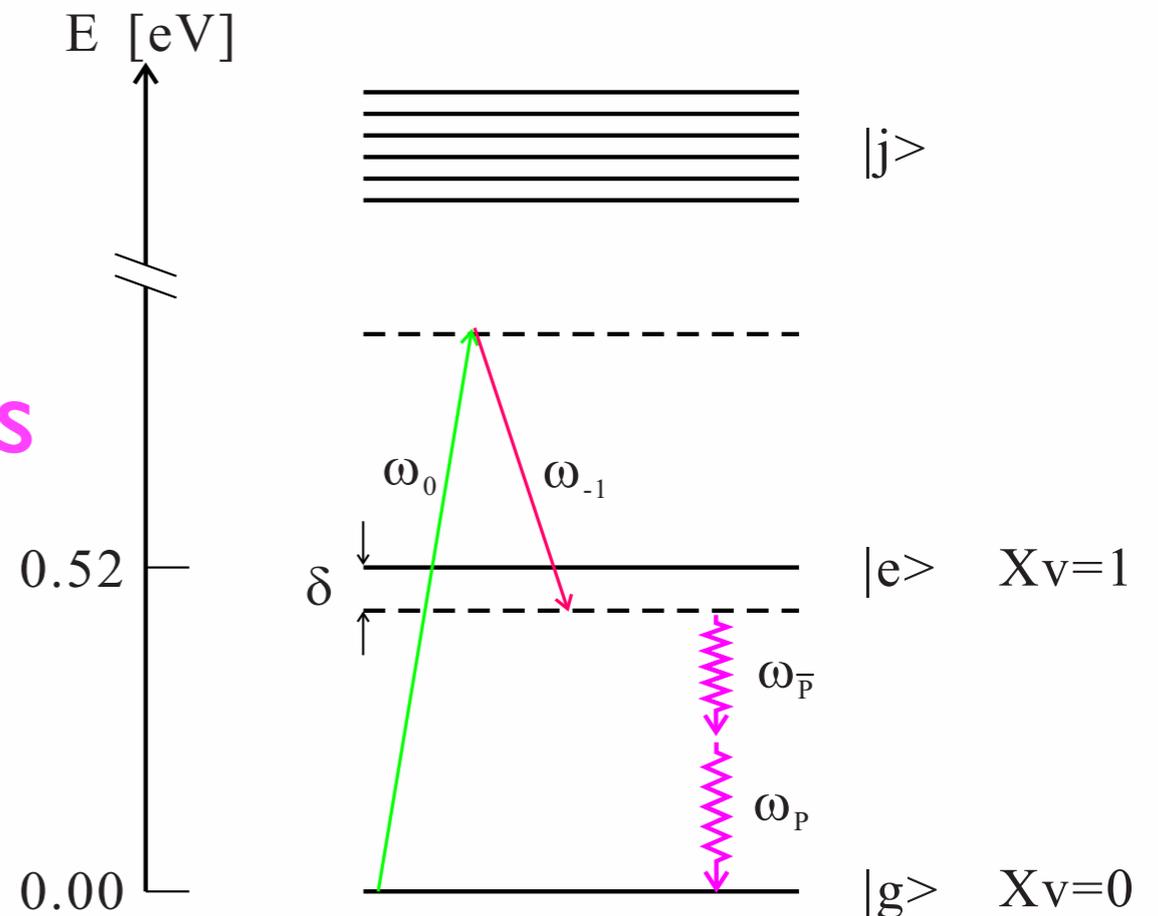
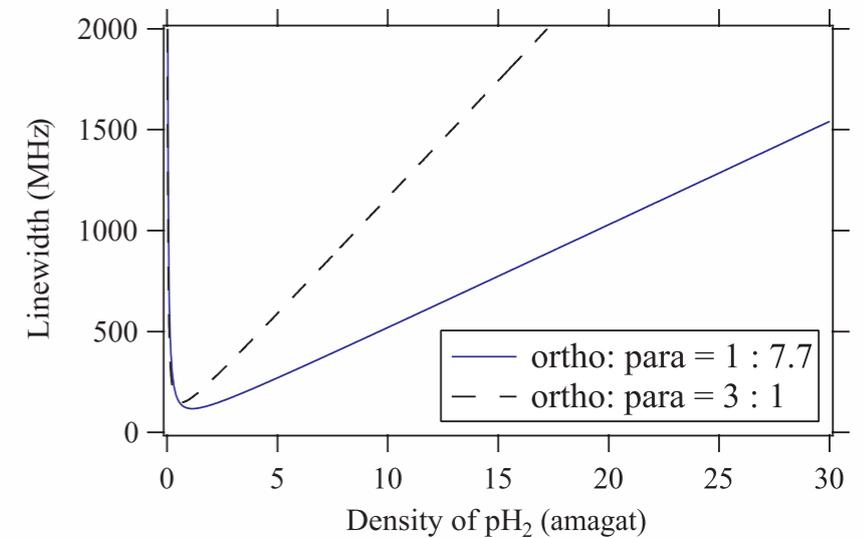
adiabatic Raman process

$$\Delta\omega = \omega_0 - \omega_{-1}$$

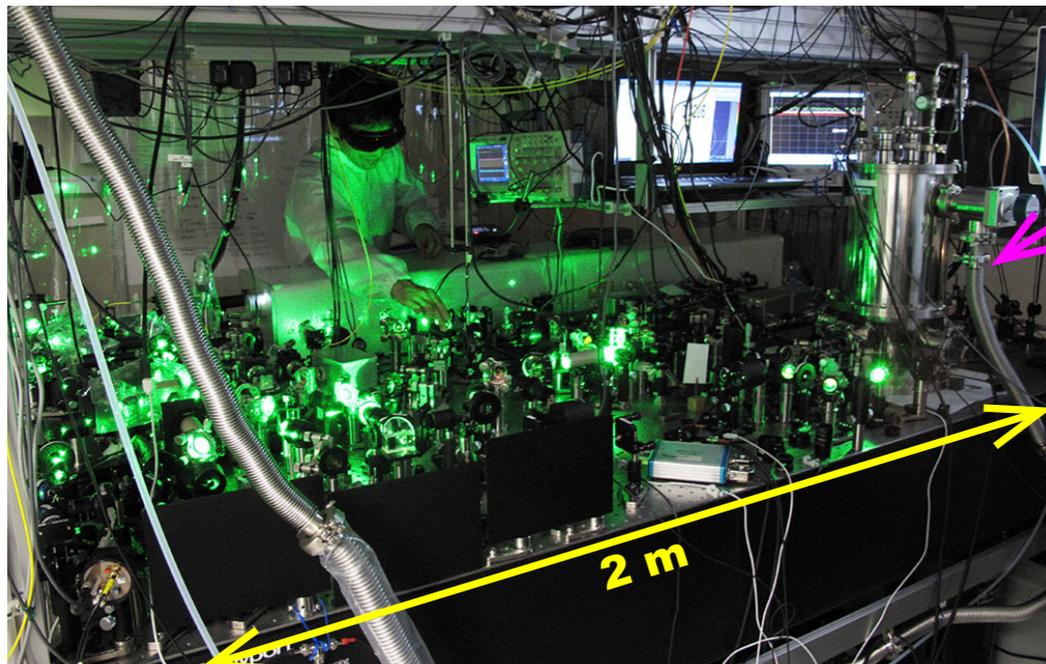
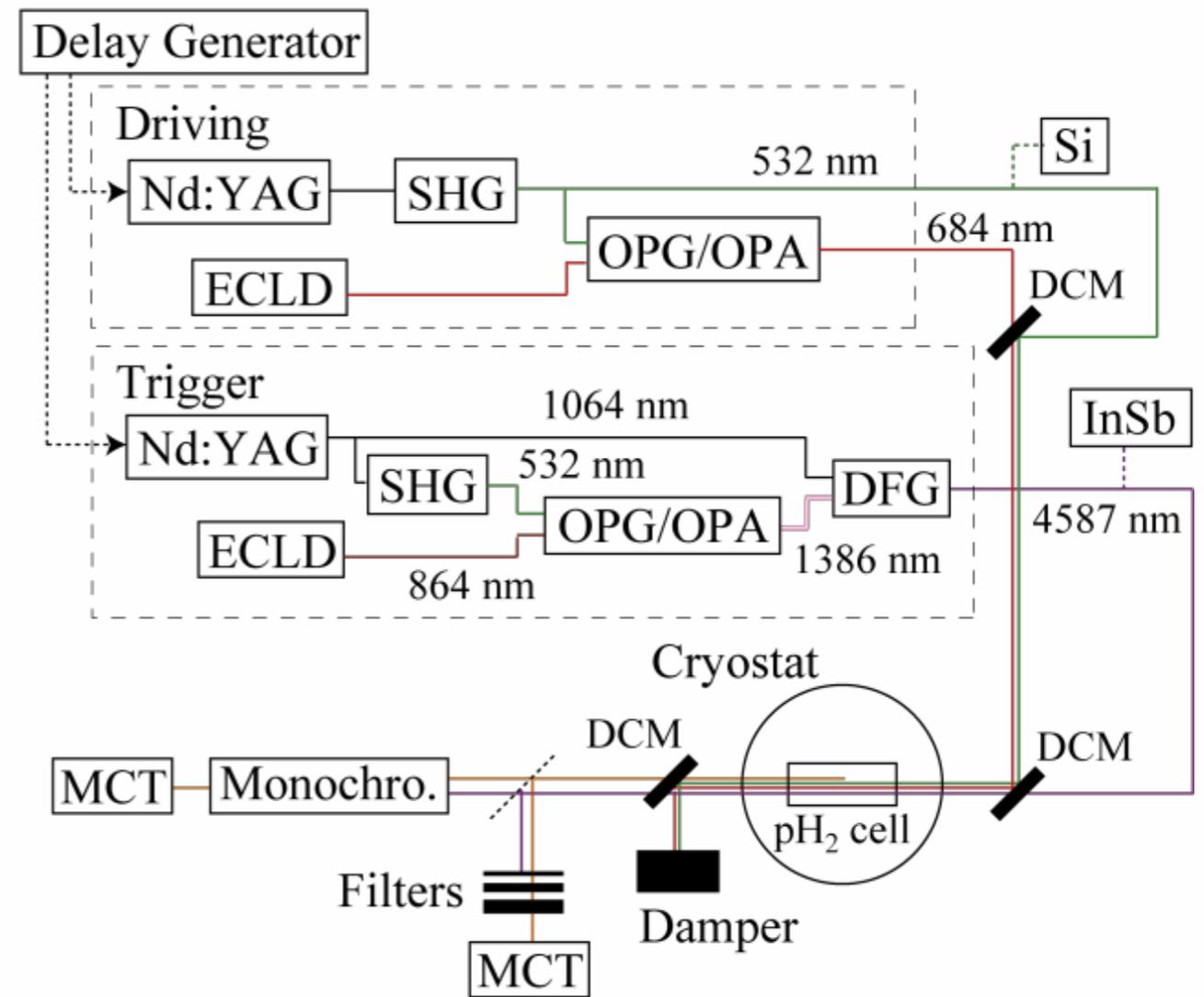
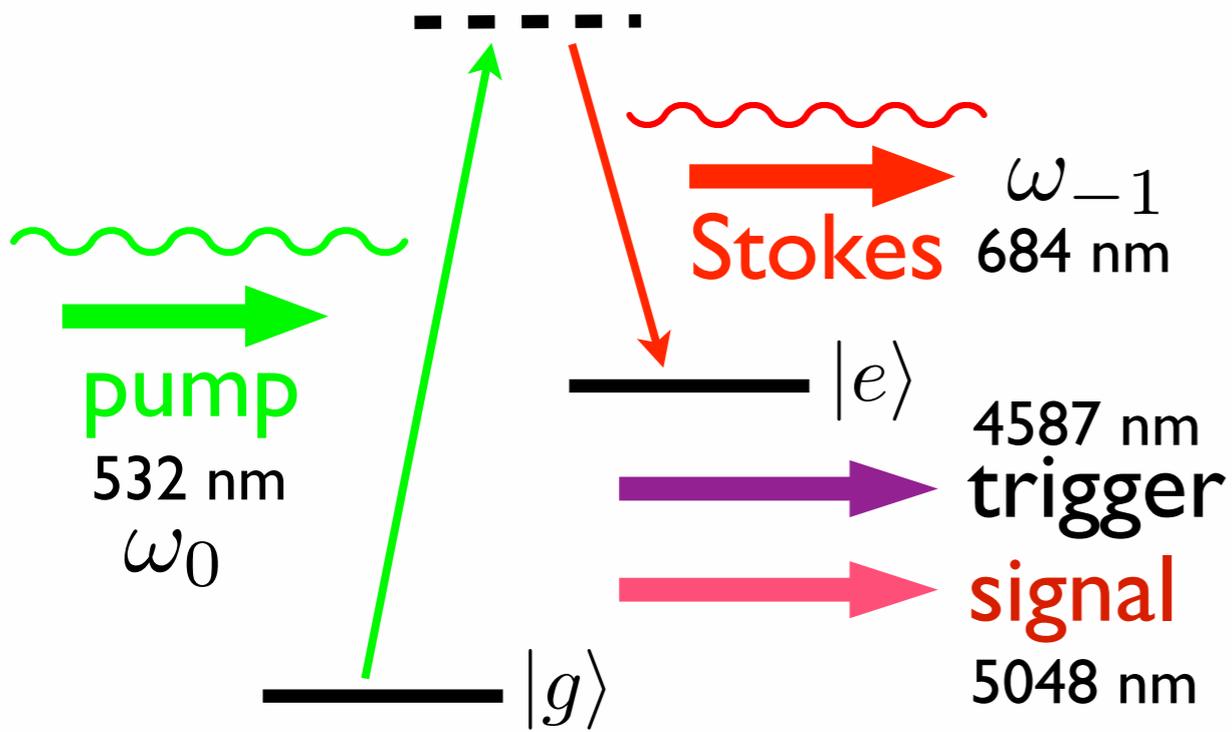
$$= \epsilon_{eg} - \delta$$

$$= \omega_p + \omega_{\bar{p}}$$

detuning



Experimental setup



Target cell: $L=15$ cm, $\Phi=2$ cm, 78 K, 60 kPa
 $n = 5.6 \times 10^{19}$ cm⁻³ $1/T_2 \sim 130$ MHz

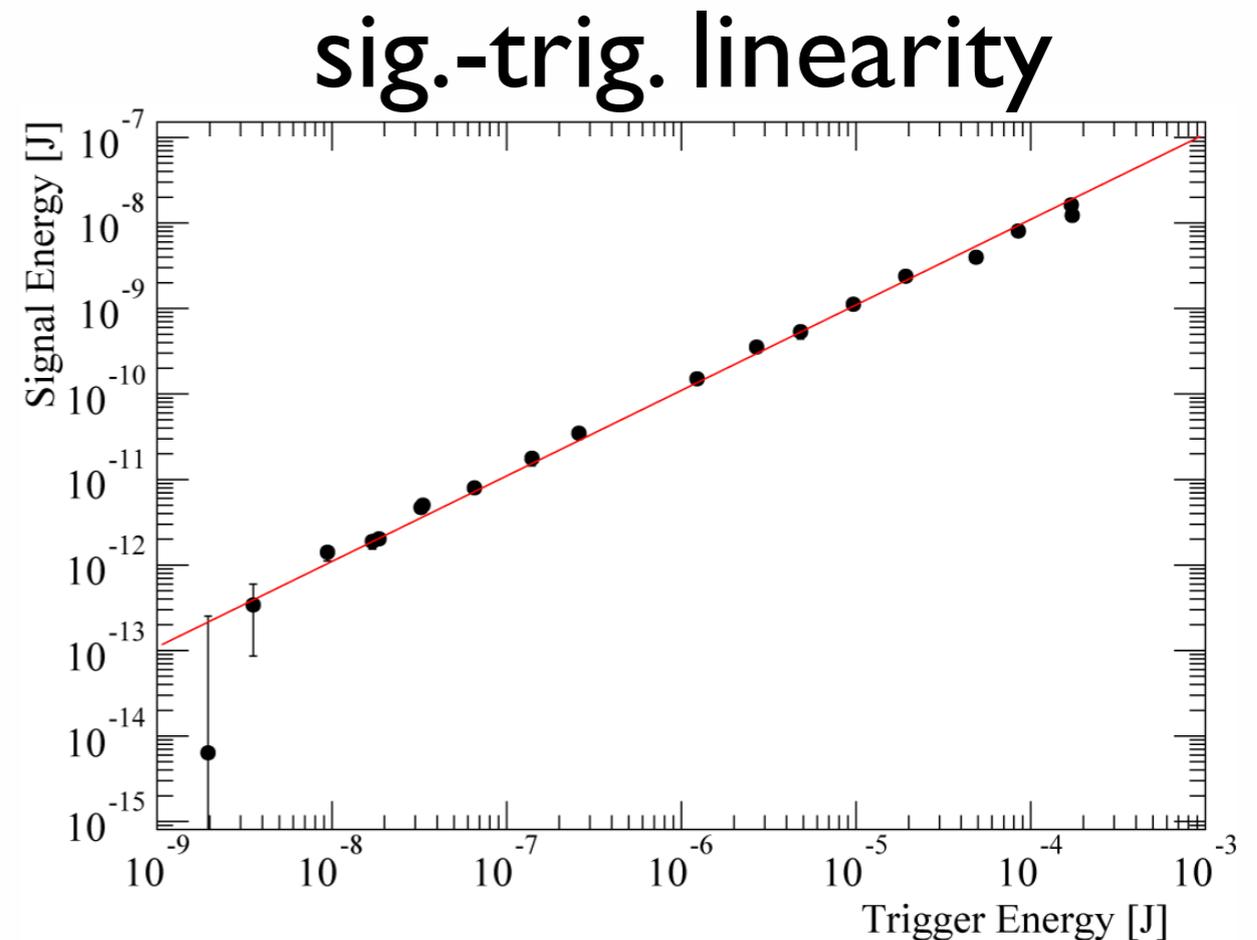
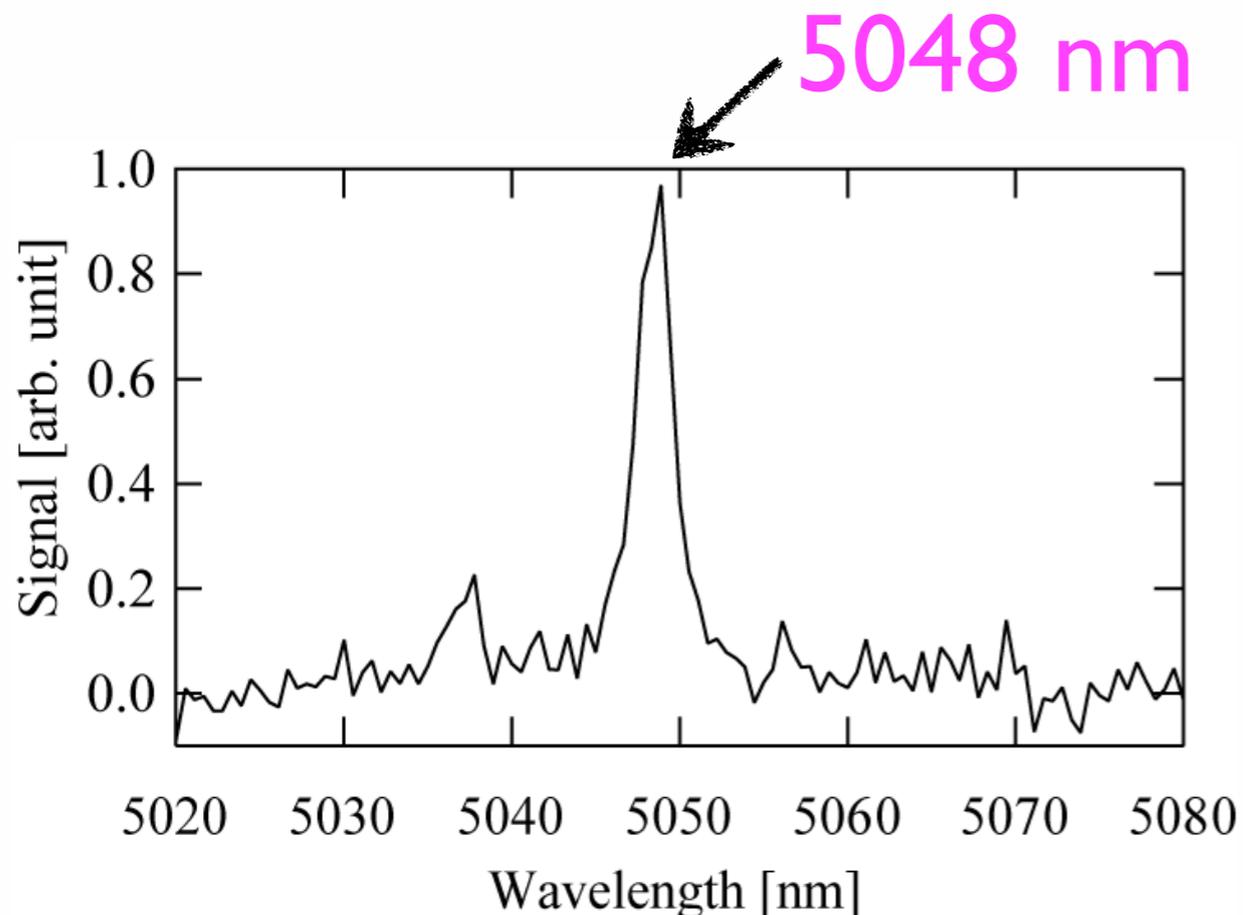
Driving lasers: 532, 684 nm
 5 mJ, 9, 6 ns, $w_0 = 100$ μ m (5 GW/cm²)

Trigger: 4587 nm
 150 μ J, 2 ns

Results

Estimated coherence (from sidebands)

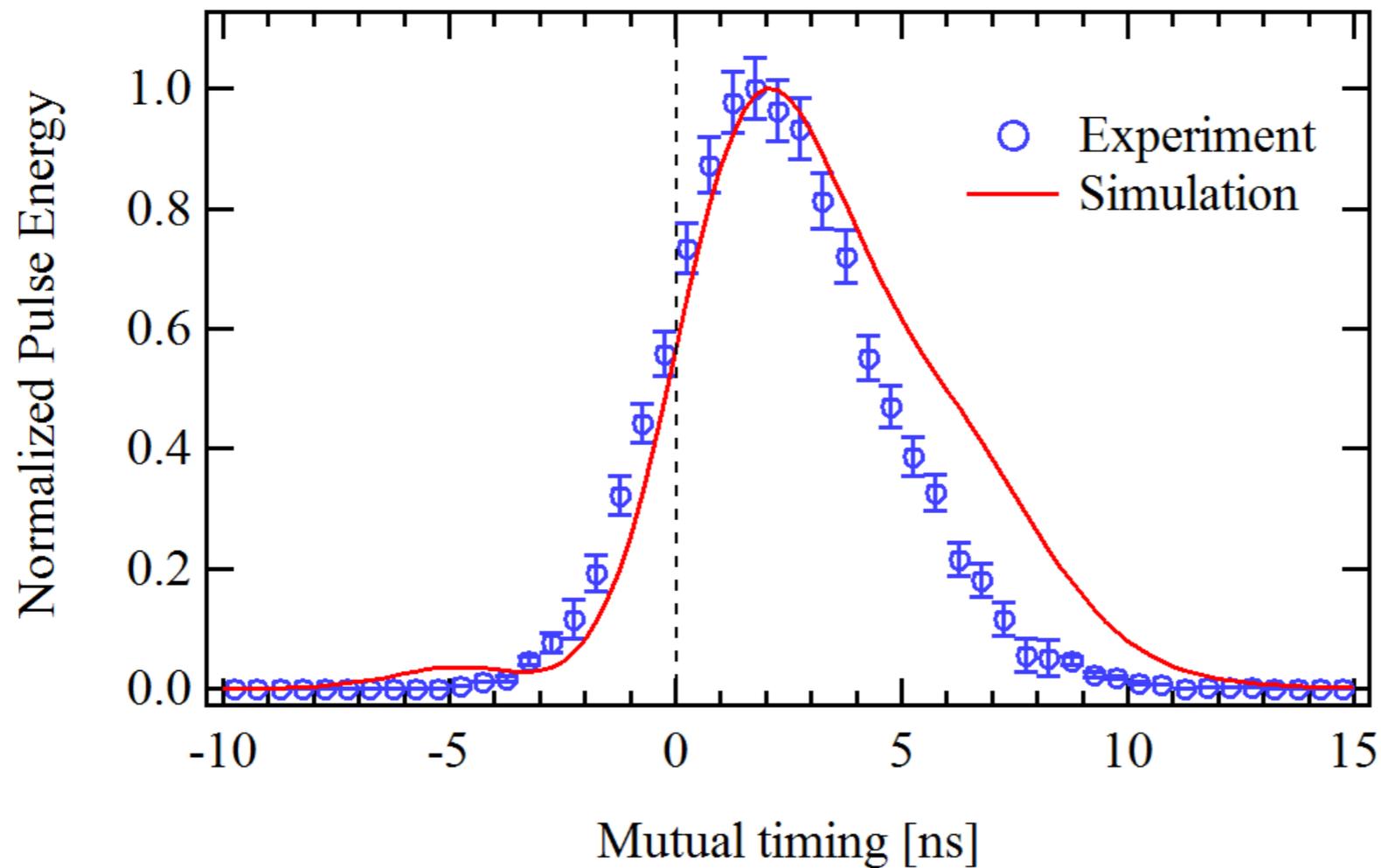
$$|\rho_{eg}| \sim 0.04 \quad (\delta = -160 \text{ MHz})$$



6×10^{11} photons/pulse
→ 10^{18} enhancement

weak field
low coherence

Trigger timing



trigger delay

Delayed coherence development in the target
less adiabatic, decoherence

SUMMARY

Neutrino Physics with Atoms/Molecules

- ★ **REN**P spectra are sensitive to unknown neutrino parameters.
Absolute mass, Dirac or Majorana, NH or IH, CP
- ★ **REN**P spectra are sensitive to the cosmic neutrino background.
- ★ **Macrocoherent** rate amplification is essential.
Demonstrated by a QED process, **PSR**.

- ★ **Background-free REN**P M. Yoshimura, N. Sasao, M. T. PTEP (2015) 053B06, arXiv:150105711
Waveguide (photonic crystals?)

A new approach to neutrino physics