

Test of the $R(D^{(*)})$ anomaly in the LHC experiment

Syuhei Iguro (Nagoya-U)



Based on

work in progress w/ Y. Omura(KMI), M. Takeuchi(IPMU)

Nucl.Phys. B925 (2017) 560-606 w/ K. Tobe(KMI,Nagoya-U),

Let me introduce myself in 2 min

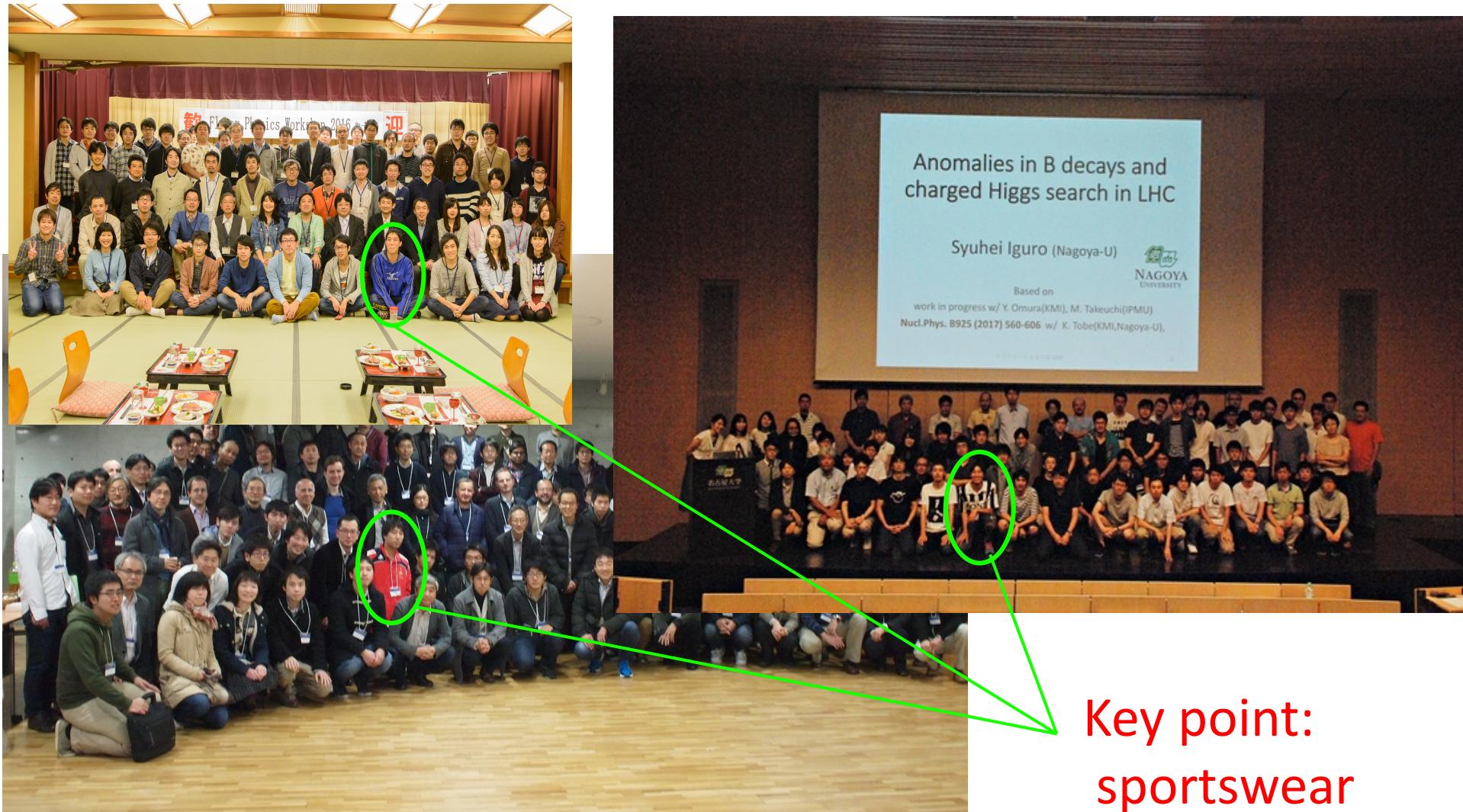
- Name: Syuhei Iguro (井黒 就平)
 - Position: D1 student
 - Birth place: Japan, Tokyo
 - Interests: Flavor, Collider, Dark Matter, Neutrino...
 - Ambition: 10 papers by 24/7/2020
 - I love football,
most aggressive student in theoretical group (E-lab)
 - For more info: <http://www.eken.phvs.nagoya-u.ac.jp/~iguro/IGURO.html>



The easiest way to find me



The easiest way to find me



Key point:
sportswear
and vivid color

What I do today

I interplay $R(D^{(*)})$ anomaly and $\tau\nu$
resonance search in LHC within a
General Two Higgs Doublet Model
(G2HDM)

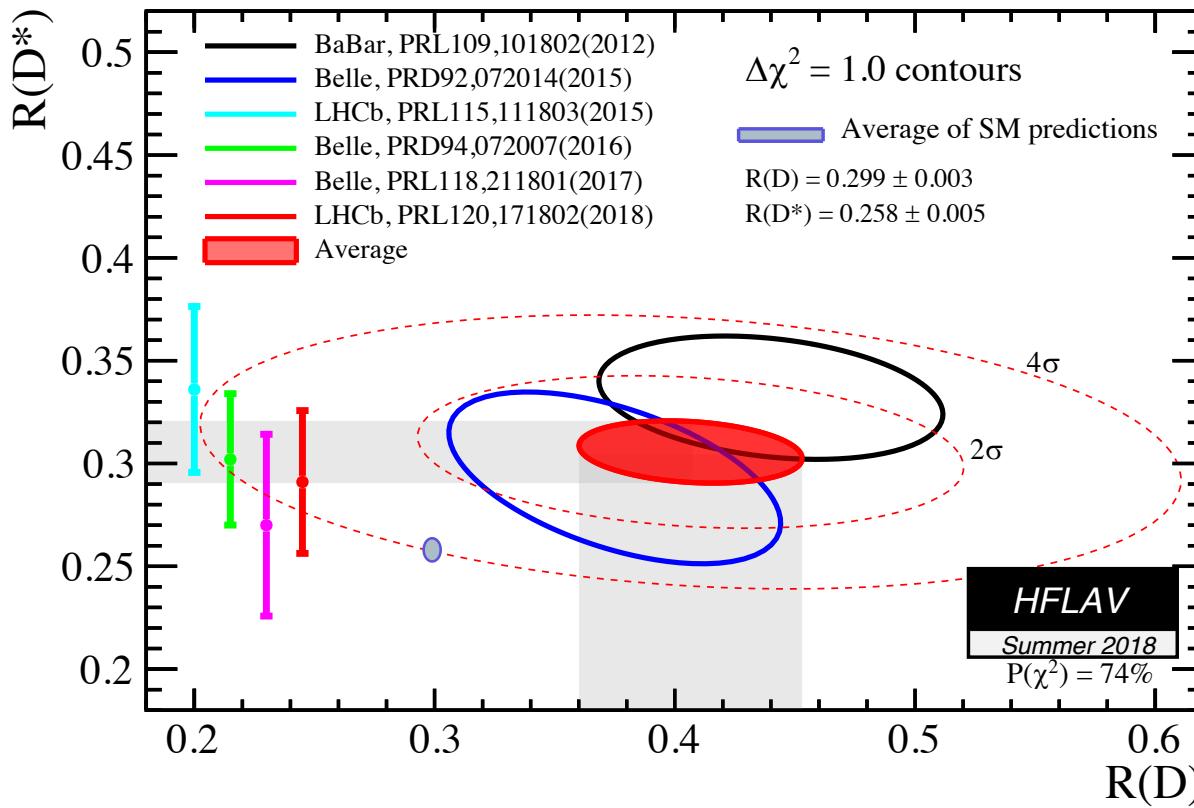
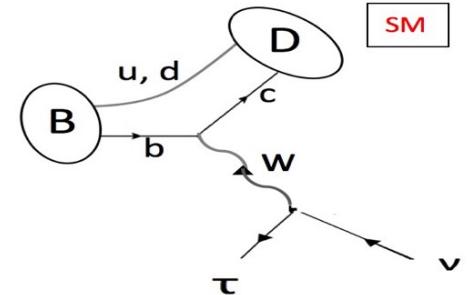
Menu

- $R(D^{(*)})$ anomaly
- Introduction of G2HDM
- Collider search
- Summary

Current status of $R(D^{(*)})$ anomaly

$$R(D^{(*)}) \equiv \frac{BR(B \rightarrow D^{(*)}\tau\nu)}{BR(B \rightarrow D^{(*)}l\nu)}, \quad l = \mu, e$$

3.9 σ discrepancy



ICHEP 2018

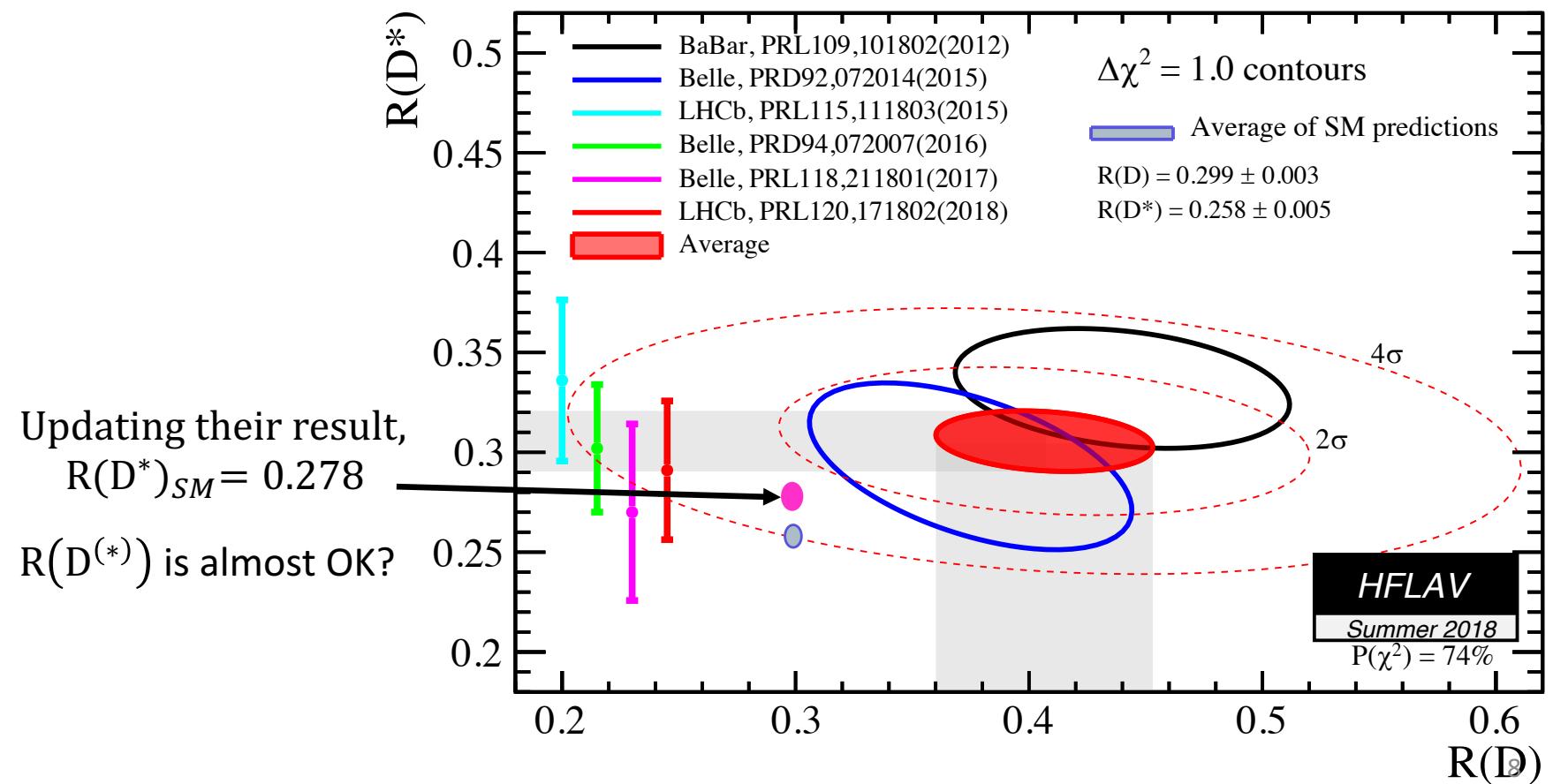
No new result but
minor change from last year

$$R(D^*)_{SM} = 0.252$$

$$\downarrow$$

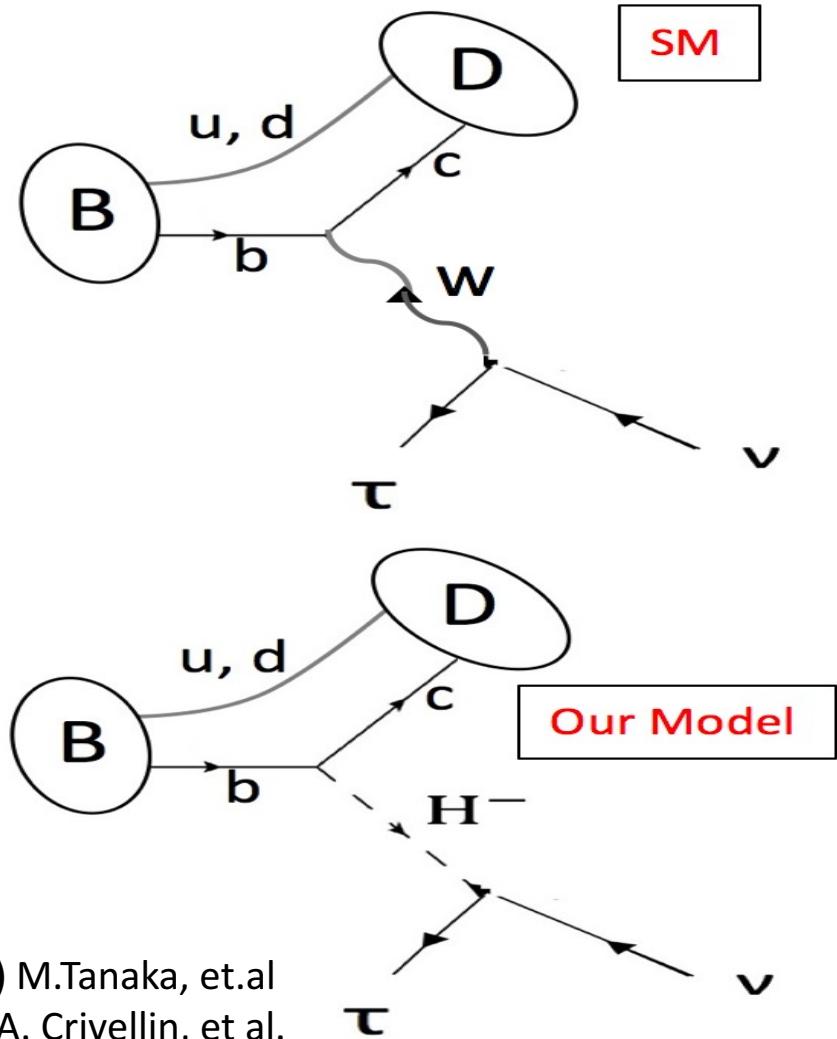
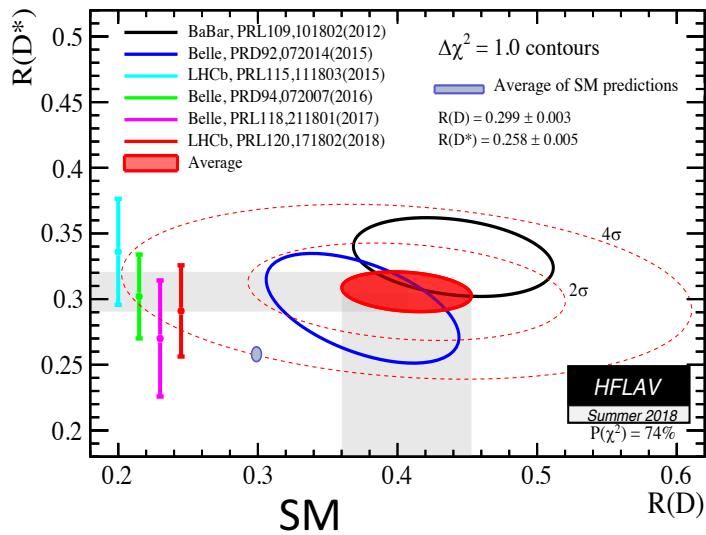
$$R(D^*)_{SM} = 0.258$$

Recently by taking into account the phase space
 in $D^* \rightarrow D\pi$, the mode a D^* is observed,
 $R(D^*)_{SM} = 0.272$. This is consistent with 4 body decay
 Belle and LHCb. J. E. Chavez-Saab et al. 1806.06997



Naively, H^- is a good candidate.

$$R(D^{(*)}) = \frac{BR(B \rightarrow D^{(*)}\tau\nu)}{BR(B \rightarrow D^{(*)}l\nu)}$$



Phys. Rev. D 82, 034027 (2010) M.Tanaka, et.al

Phys.Rev. D86 (2012) 054014 A. Crivellin, et al.

Nucl.Phys. B925 (2017) 560-606 SI, K. Tobe

Motivation

Why I work on Higgs physics?

Guiding principles

- Simplicity of the model.
- Electroweak precision test
- Extending Higgs sector keeps the gauge anomaly-free condition



General Two Higgs Doublet Model (G2HDM)

- SM Higgs exist!
- Simple extension of scalar sector
- STU parameter is controllable
- Flavor violating Yukawa could exist



Rich flavor phenomenology

Motivation

Guiding principle

- Simplicity of
- Electroweak
- Extending Higgs condition

may explain the discrepancies in flavor physics

- $R(D^{(*)}) = BR(B \rightarrow D^{(*)}\tau\nu)/BR(B \rightarrow D^{(*)}l\nu)$ today
- muon g-2 Omura, Senaha, Tobe: **JHEP 1505 (2015) 028**
- P'_5 : angular observable in $B \rightarrow K^*\mu\mu$ If time allows
- $R(K^{(*)}) = BR(B \rightarrow K^{(*)}\mu\mu)/BR(B \rightarrow K^{(*)}ee)$

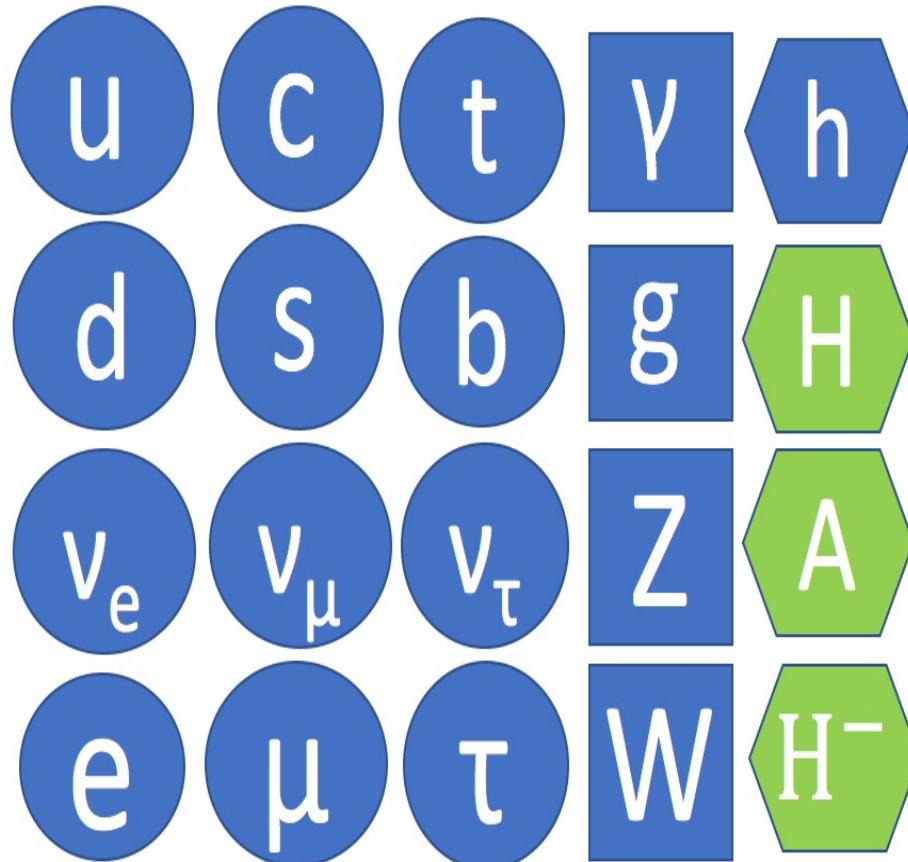
for a combination of them, see **JHEP 1805 (2018) 173** SI, Y. Omura

- SM Higgs exists
- Simple extension of scalar sector
- STU parameter is controllable
- Flavor violating Yukawa could exist

Rich flavor phenomenology

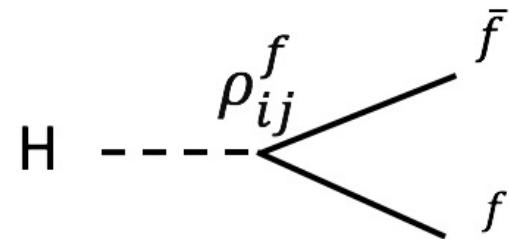
Our Model

Particle set in **G2HDM**



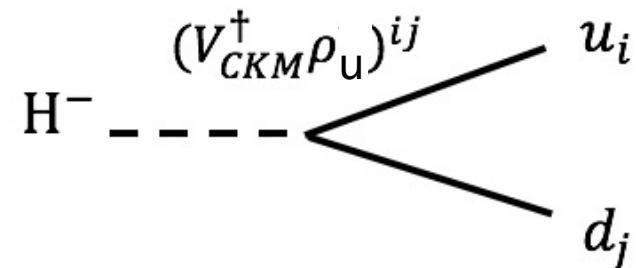
Neutral Scalar

$$\frac{1}{\sqrt{2}} \rho_f^{ij} H \bar{f}_L^i f_R^j \quad (f = u, d, e, \nu)$$



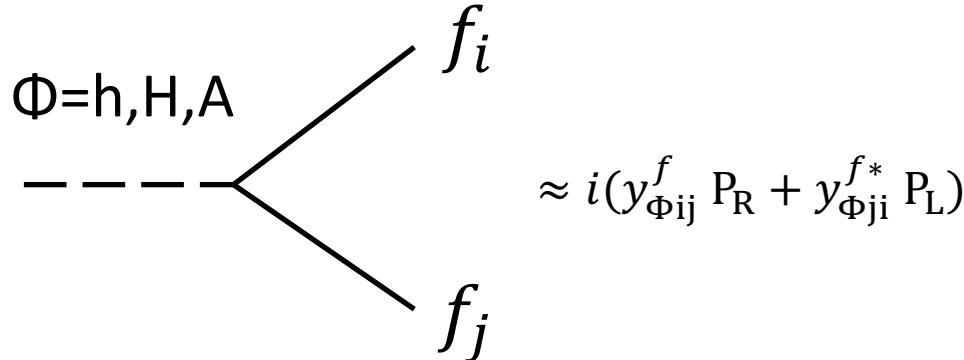
Charged Scalar

$$(V_{CKM} \rho_d)^{ij} H^- \bar{u}_L^i d_R^j + (V_{CKM}^\dagger \rho_u)^{ij} H^- \bar{d}_L^i u_R^j$$



Model: G2HDM

Yukawa couplings between a neutral scalar and fermions

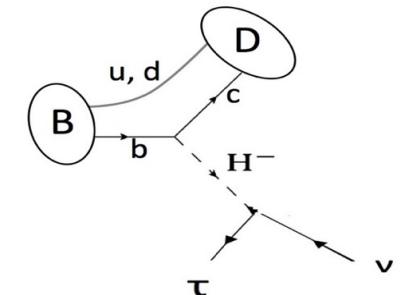
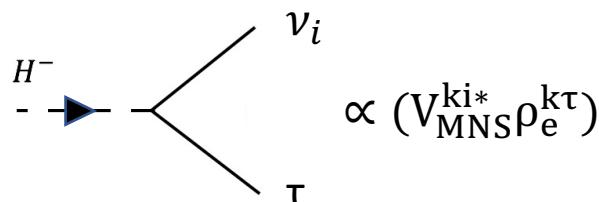
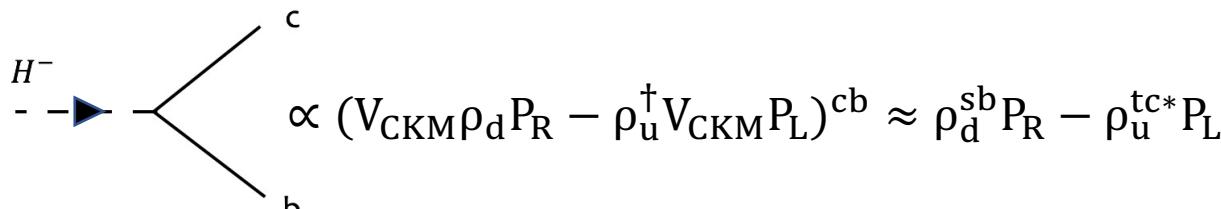


$$y_{hij}^f = \frac{m_f^i}{v} s_{\beta\alpha} \delta_{ij} + \frac{\rho_f^{ij}}{\sqrt{2}} c_{\beta\alpha},$$

$$y_{Aij}^f = \begin{cases} -\frac{i\rho_f^{ij}}{\sqrt{2}} & \text{for } f = u \\ +\frac{i\rho_f^{ij}}{\sqrt{2}} & \text{for } f = d, e, \end{cases}$$

$$y_{Hij}^f = \frac{m_f^i}{v} c_{\beta\alpha} \delta_{ij} - \frac{\rho_f^{ij}}{\sqrt{2}} s_{\beta\alpha}$$

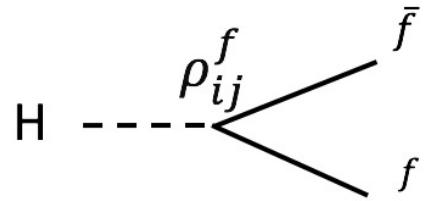
Yukawa interactions relevant to $R(D^{(*)})$



Yukawa interactions relevant to $R(D^{(*)})$

$(\rho_u^{tc}, \rho_d^{sb}) \times (\rho_e^{e\tau}, \rho_e^{\mu\tau}, \rho_e^{\tau\tau})$

Yukawa couplings



Without discrete symmetry like Z_2 symmetry,
G2HDM has **flavor violating interactions at tree level.**

Experimentally, Yukawa couplings to use are limited

e.g. Stringent bounds come from

- meson mixing
- $b \rightarrow s\gamma$
- $B \rightarrow \tau\nu \dots$

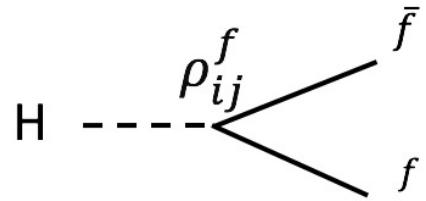


$\rho_d^{sb} \ll 1$, but
 ρ_u^{tc} can be $O(1)$

We turn others off for simplicity and clarify how G2HDM can explain $R(D^{(*)})$ anomalies

For the top down approach of this model e.g. Cheng et al. 1507.04354

Yukawa couplings



Without discrete symmetry like Z_2 symmetry,
G2HDM has flavor violating interactions at tree level.

Experimentally, Yukawa couplings to use are limited

e.g. Stringent bounds come from

- meson mixing
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$$\rho_d^{sb} \ll 1, \text{ but}$$

15:45～ 重神さん

halies

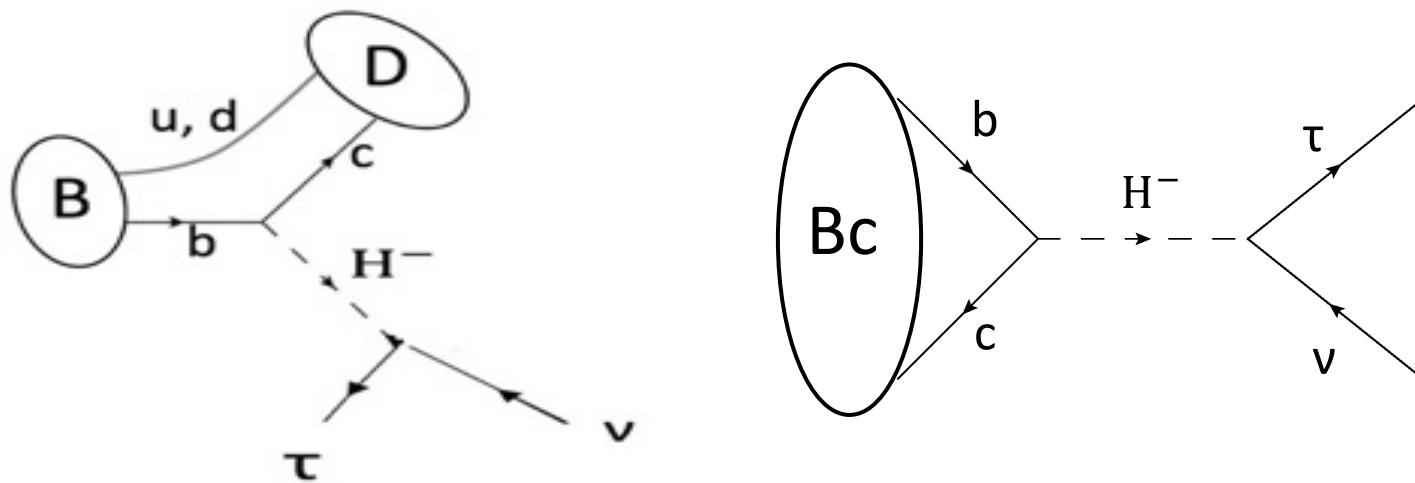
We turn others off for

For the top down



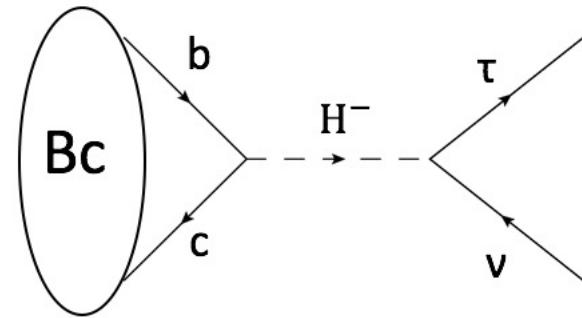
Stringent bound from $\text{BR}(B_c^- \rightarrow \tau \bar{\nu})$

Diagram for $R(D^{(*)})$ automatically contributes to $(B_c^- \rightarrow \tau \bar{\nu})$



- $L_{eff} = -\frac{4G_F}{\sqrt{2}} V_{cb} [(\bar{\tau} \gamma_\mu P_L \nu)(\bar{c} \gamma^\mu P_L b) + S_L (\bar{\tau} P_L \nu)(\bar{c} P_L b) + S_R (\bar{\tau} P_L \nu)(\bar{c} P_R b)] + \text{h.c.}$

Stringent bound from BR($B_c^- \rightarrow \tau \bar{\nu}$)



- $L_{eff} = -\frac{4G_F}{\sqrt{2}} V_{cb} [(\bar{\tau}\gamma_\mu P_L \nu)(\bar{c}\gamma^\mu P_L b) + S_L (\bar{\tau}P_L \nu)(\bar{c}P_L b) + S_R (\bar{\tau}P_L \nu)(\bar{c}P_R b)] + h.c.$



Scalar operators have a large coefficient

$$\text{BR}(B_c^- \rightarrow \tau \bar{\nu}) =$$

$$\text{BR}(B_c^- \rightarrow \tau \bar{\nu})_{\text{SM}} \times \left| 1 + \frac{m_{B_c}^2}{m_\tau(m_b + m_c)} (S_R - S_L) \right|^2$$

$$\text{BR}(B_c^- \rightarrow \tau \bar{\nu})_{\text{SM}} = 2\%$$

Indirect upper bounds on $\text{BR}(B_c^- \rightarrow \tau\bar{\nu})$

$\text{BR}(B_c^- \rightarrow \tau\bar{\nu}) = 1 - \text{Br}(\text{Bc the other decay}) < 30\%$ R.Alonso et al. 1611.06676



Substituting a SM calculation

Combining LEP data with inputs obtained in LHCb

< 10% A.G.Akeroyd.et al. 1708.04072

LEP has an upper limit on $B_c \rightarrow \tau\bar{\nu} + B \rightarrow \tau\bar{\nu}$. Combining recent result of LHCb, they got an upper limit on $\text{BR}(B_c^- \rightarrow \tau\bar{\nu})$.

comment: they used $\text{BR}(B_c \rightarrow J/\psi l\nu)_{\text{SM}}$ as an input.

$$\begin{aligned}\mathcal{H}_{eff} = & C_{LL}^V (\overline{b_L} \gamma_\mu c_L) (\overline{\nu_L} \gamma^\mu \tau_L) + C_{RL}^V (\overline{b_R} \gamma_\mu c_R) (\overline{\nu_L} \gamma^\mu \tau_L) \\ & + C_{LR}^V (\overline{b_L} \gamma_\mu c_L) (\overline{\nu_R} \gamma^\mu \tau_R) + C_{RR}^V (\overline{b_R} \gamma_\mu c_R) (\overline{\nu_R} \gamma^\mu \tau_R) \\ & + \underline{C_L^S (\overline{b_R} c_L) (\overline{\nu_L} \tau_R)} + \underline{C_R^S (\overline{b_L} c_R) (\overline{\nu_L} \tau_R)} + h.c..\end{aligned}$$

$$\begin{aligned}R(D) \simeq R(D)_{SM} \Bigg\{ & |1 + C_{LL}^V + C_{RL}^V|^2 + |C_{RR}^V + C_{LR}^V|^2 + 0.99 |\underline{C_L^S + C_R^S}|^2 \\ & + 1.47 \text{Re} \left[(1 + C_{LL}^V + C_{RL}^V) (\underline{C_L^{S*} + C_R^{S*}}) \right] \Bigg\},\end{aligned}$$

$$\begin{aligned}R(D^*) \simeq R(D^*)_{SM} \Bigg\{ & |1 + C_{LL}^V|^2 + |C_{RL}^V|^2 + |C_{RR}^V|^2 + |C_{LR}^V|^2 + 0.02 |\underline{C_L^S - C_R^S}|^2 \\ & - 1.77 \text{Re} \left[(1 + C_{LL}^V) (C_{RL}^{V*}) + (C_{RR}^V) (C_{LR}^{V*}) \right] + 0.09 \text{Re} \left[(1 + C_{LL}^V - C_{RL}^V) (\underline{C_L^{S*} - C_R^{S*}}) \right] \Bigg\}\end{aligned}$$

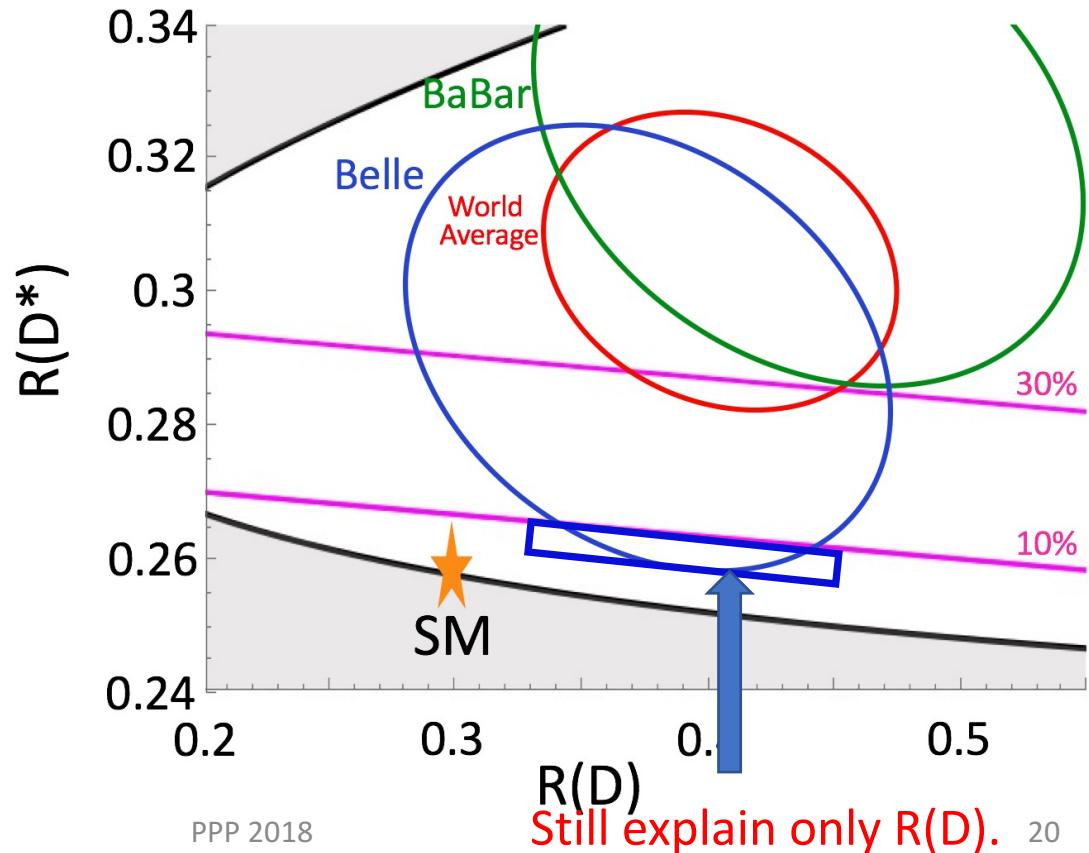
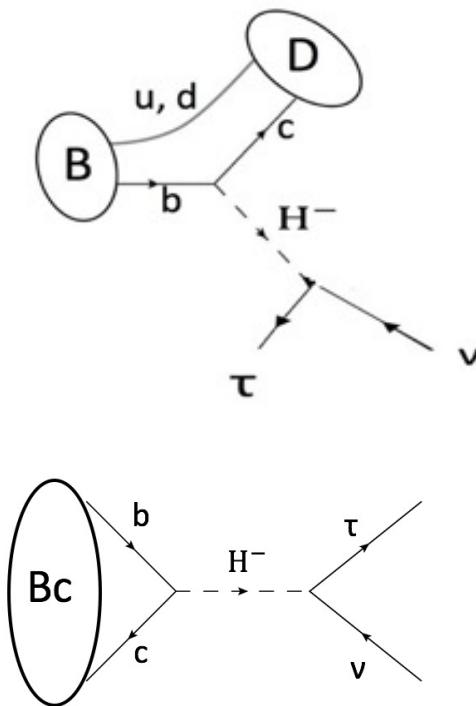
$$\rho_d^{sb} \ll 1 \rightarrow C_L^S \ll 1$$

P. Asadi ,et at.1804.04135

Stringent bound from $\text{BR}(B_c^- \rightarrow \tau \bar{\nu})$

R.Alonso et al. 1611.06676, A.G.Akeroyd et al. 1708.04072

Diagram for $R(D^{(*)})$ automatically contributes to $\text{Br}(B_c^- \rightarrow \tau \bar{\nu})$



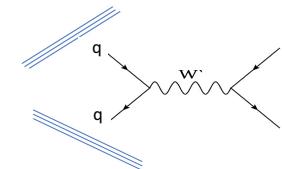
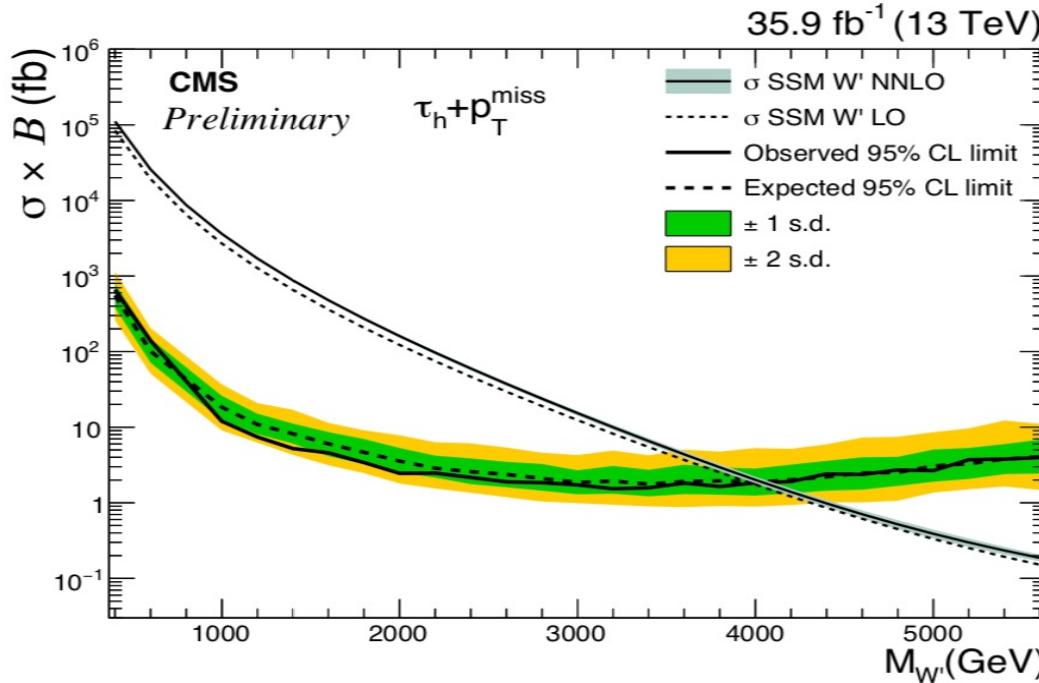
Collider study

Any direct limit from collider experiment right now?

$\tau\nu$ resonance search

$\tau\nu$ resonance (+j) search in CMS can give a stringent limit.

But, the limit is for W' . CMS-PAS-EXO-17-008

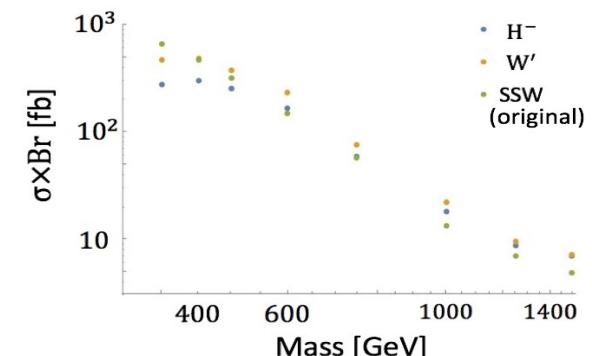


Need to reinterpret
this limit for H^- .

We calculated an
efficiency for H^-
and obtained the limit.

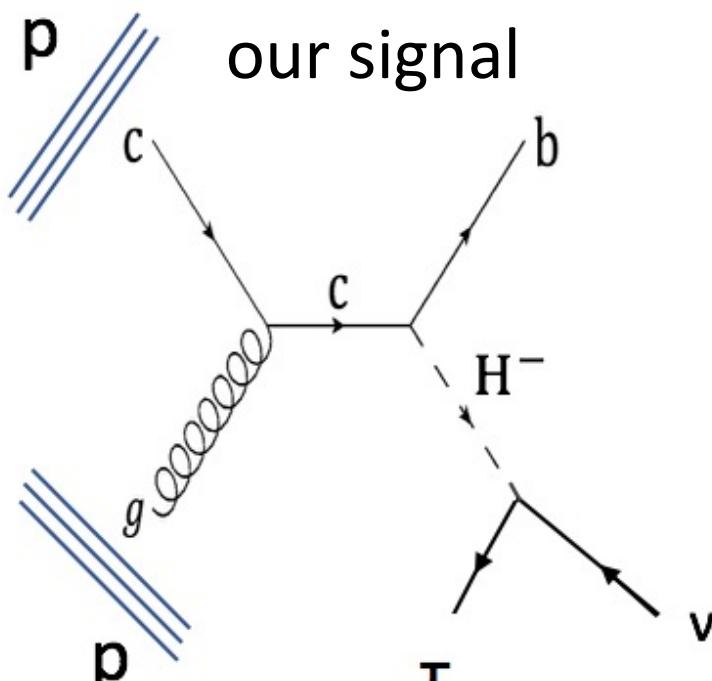
Upper bounds on
 $\sigma \times \text{Br}$

Experiment:arXiv	$\sqrt{s} [\text{TeV}]$	$L [\text{fb}^{-1}]$	Range $M_{W'} [\text{TeV}]$
CMS:1508.04308	7,8	19.7	0.3–4
CMS:CMS-PAS-EXO-16-006	13	2.3	1–5.8
ATLAS:1801.06992	13	36.1	0.5–5
CMS:CMS-PAS-EXO-17-008	13	35.9	0.4–4



$\tau\nu$ resonance search on H^-

Why no study so far?

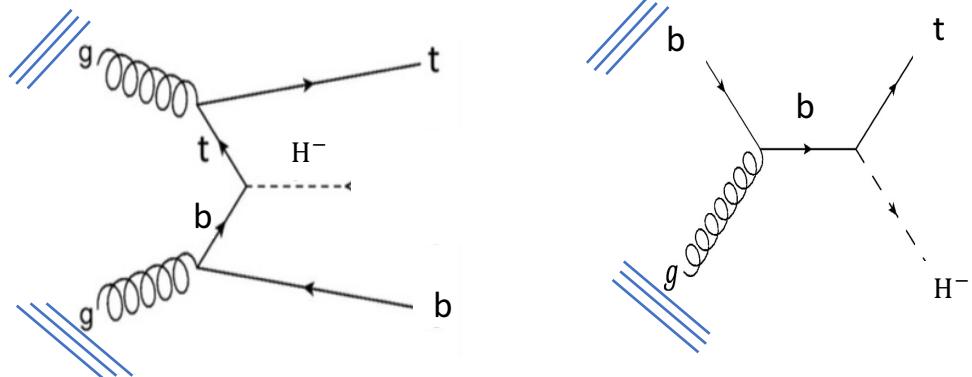


H^- in Type II 2HDM mainly couple to $bt, \tau\nu$.

No top quark in proton PDF.

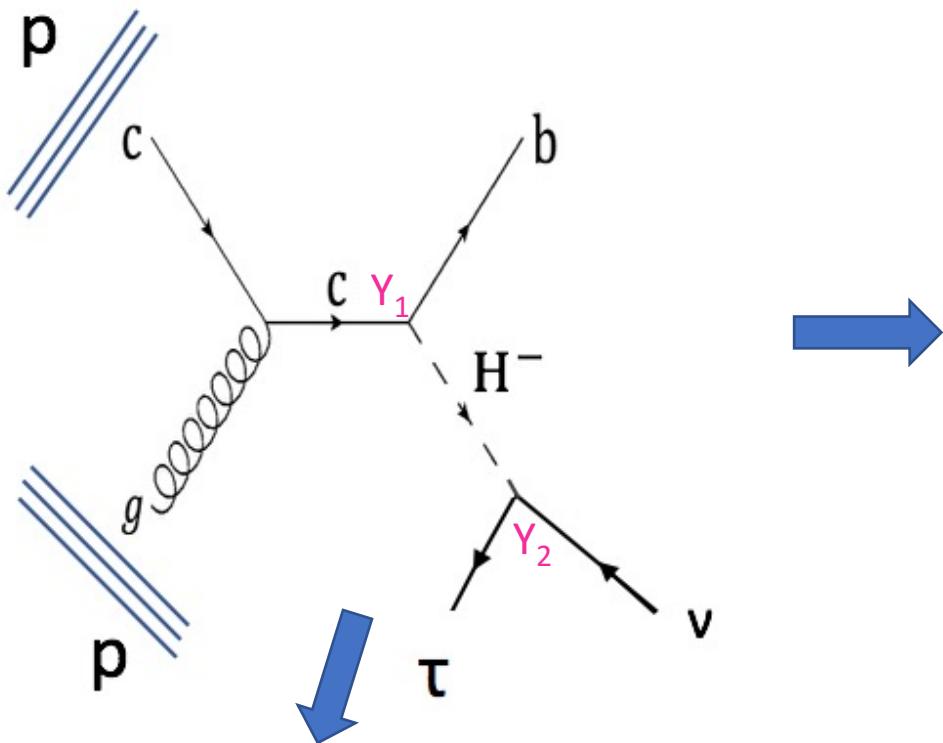


H^- is produced with top quark

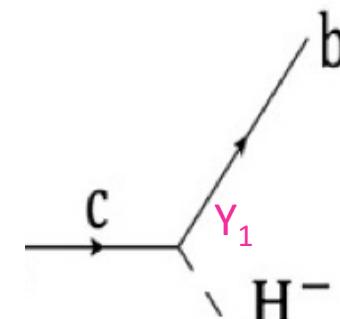


Exotic process for H^-

We assume our H^- interacts only with bc or $\tau\nu$ for simplicity.

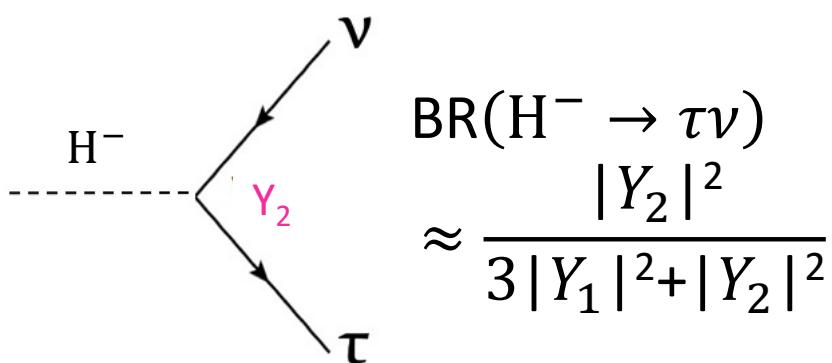


Production



depending on H^- mass
 $\sigma = X_{H^-} |Y_1|^2$

Branching ratio



$$BR(H^- \rightarrow \tau\nu) \approx \frac{|Y_2|^2}{3|Y_1|^2 + |Y_2|^2}$$

$$\sigma \times BR = \frac{X_{H^-} |Y_1|^2 |Y_2|^2}{3|Y_1|^2 + |Y_2|^2}$$

To fit $R(D^{(*)})$ data,
 $Y_1 Y_2 \equiv \alpha$ is sizable.

We set $|Y_1|, |Y_2| < 1$: narrow resonance $\tau\nu$ search.

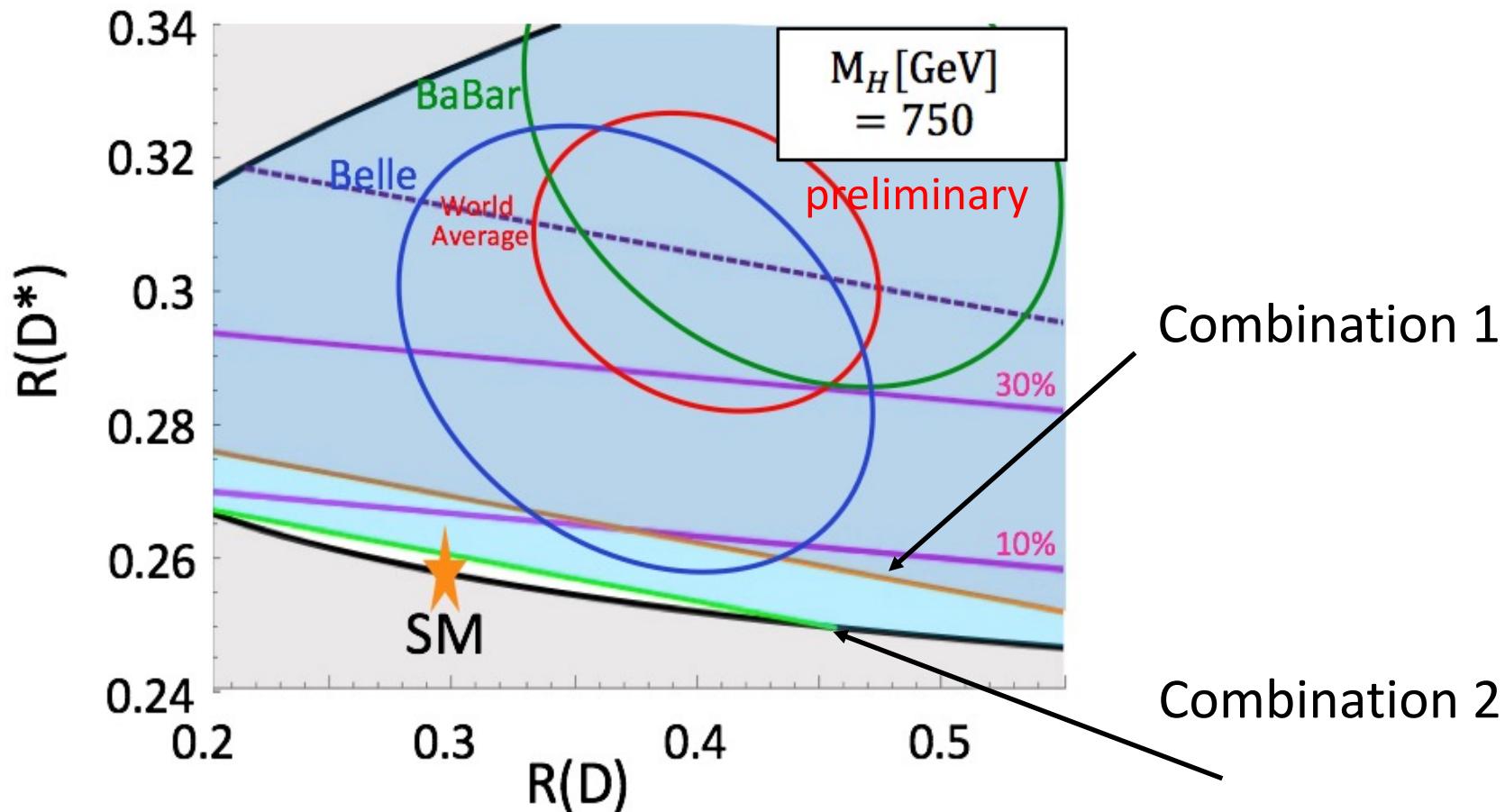
$$\Gamma/m_H - < 0.1$$

$$\sigma \times \text{BR} = \frac{X_H - |Y_1|^2 |Y_2|^2}{3|Y_1|^2 + |Y_2|^2}$$

Combination 1 : $Y_1 = 1$, maximizing denominator.
weaker constraint.

Combination 2 : $Y_2 = \sqrt{3}Y_1$, minimizing denominator.
severe constraint.

Result

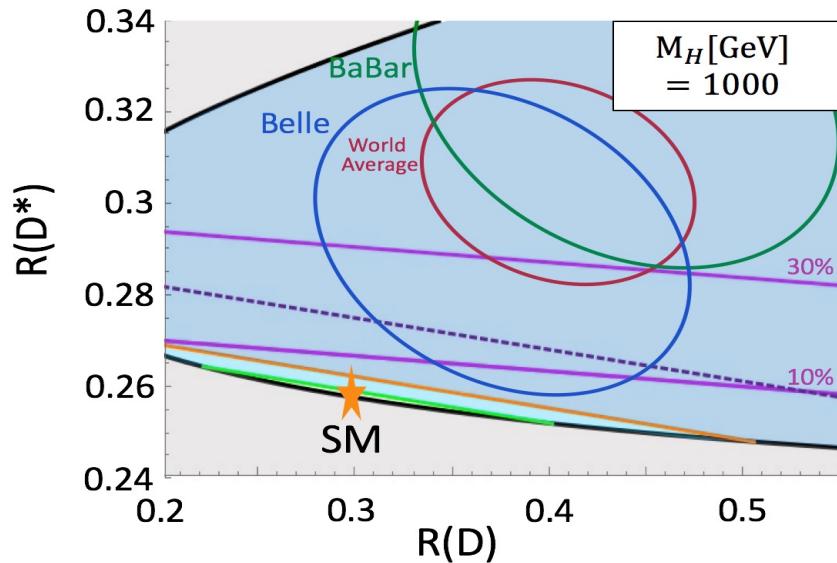


Comparable or more stringent constraint than $B_c^- \rightarrow \tau \bar{\nu}$

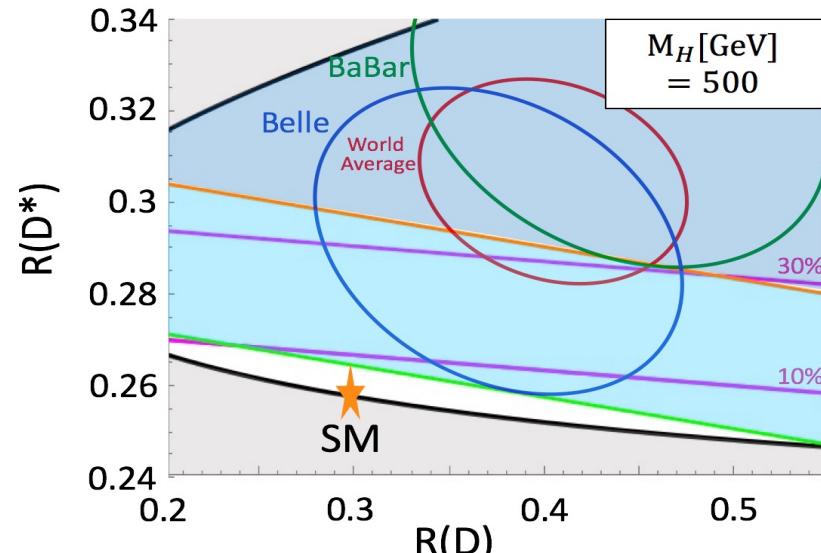
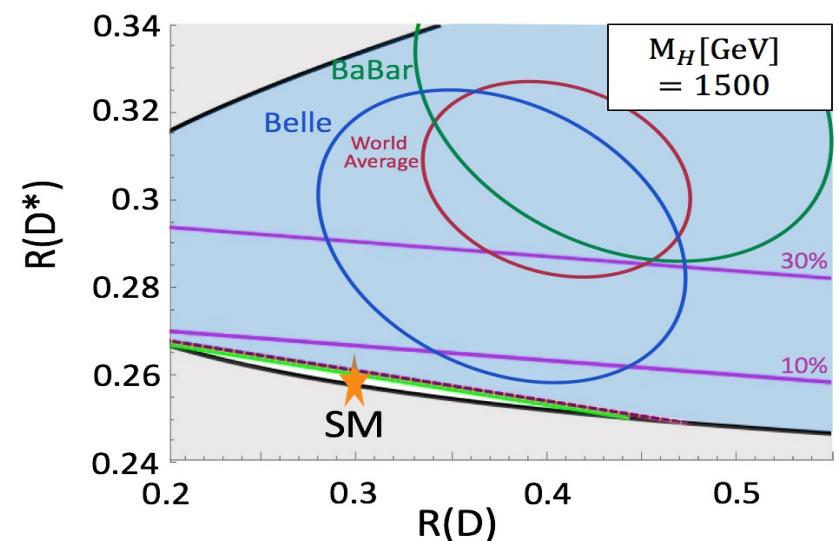
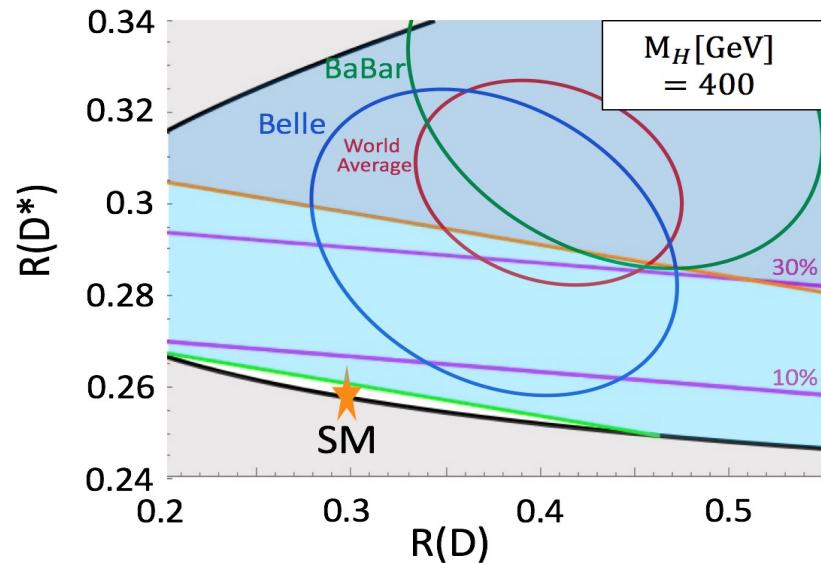
Result

preliminary heavier

Heavier H^- , more severe constraint.



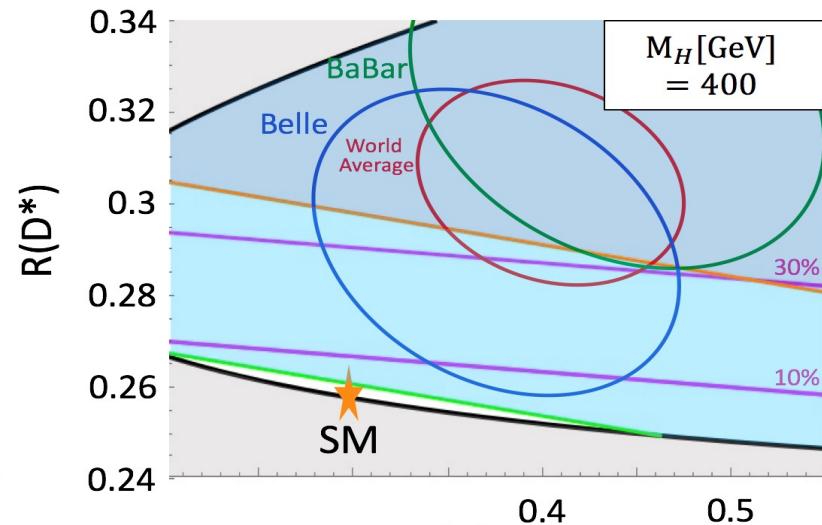
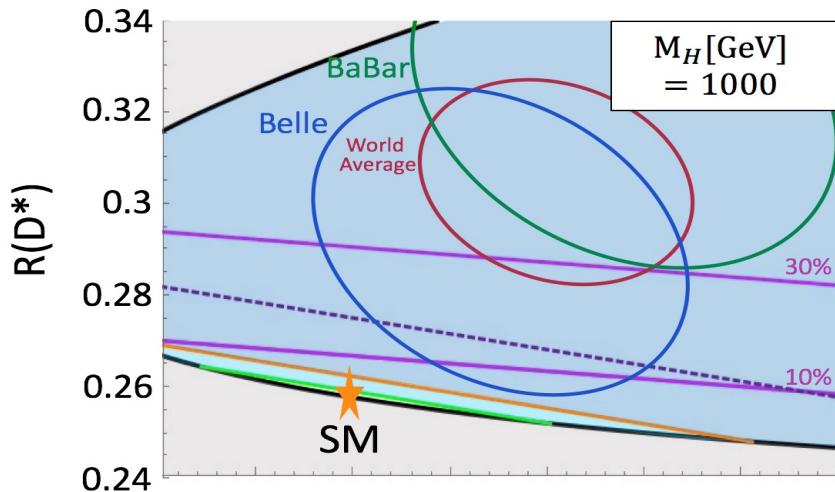
lighter



Result

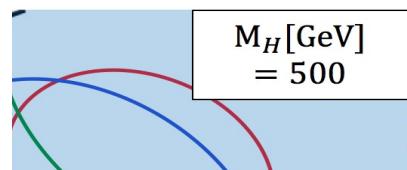
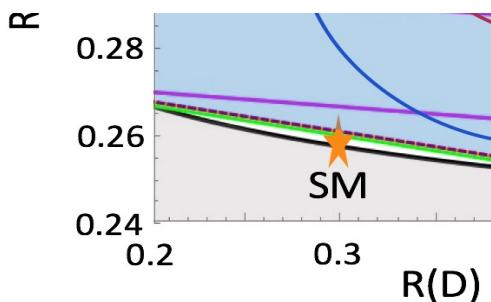
preliminary heavier

Heavier H^- , more severe constraint.



Better sensitivity for heavy $\tau\nu$ resonance:

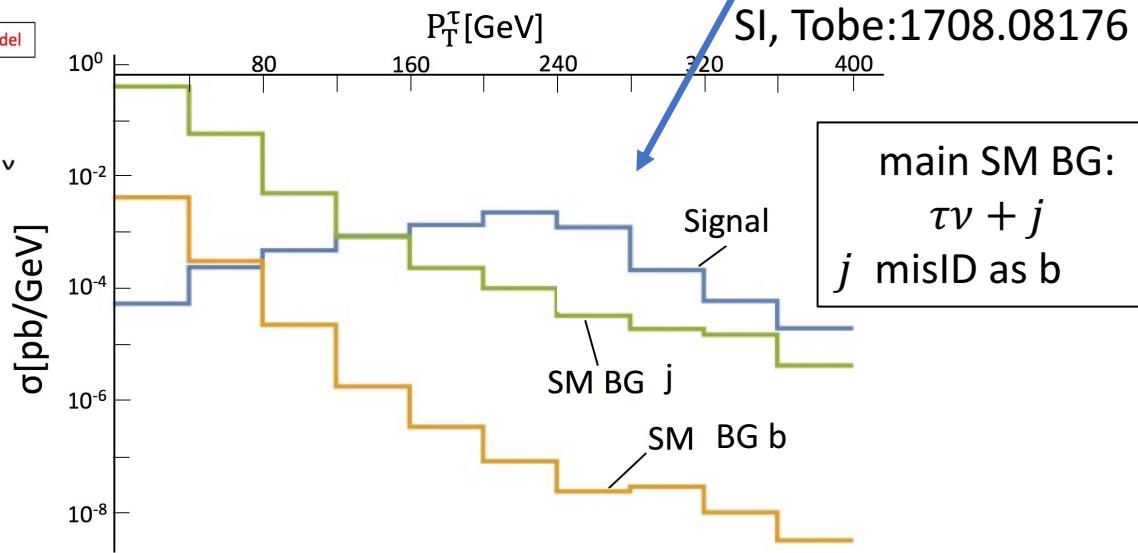
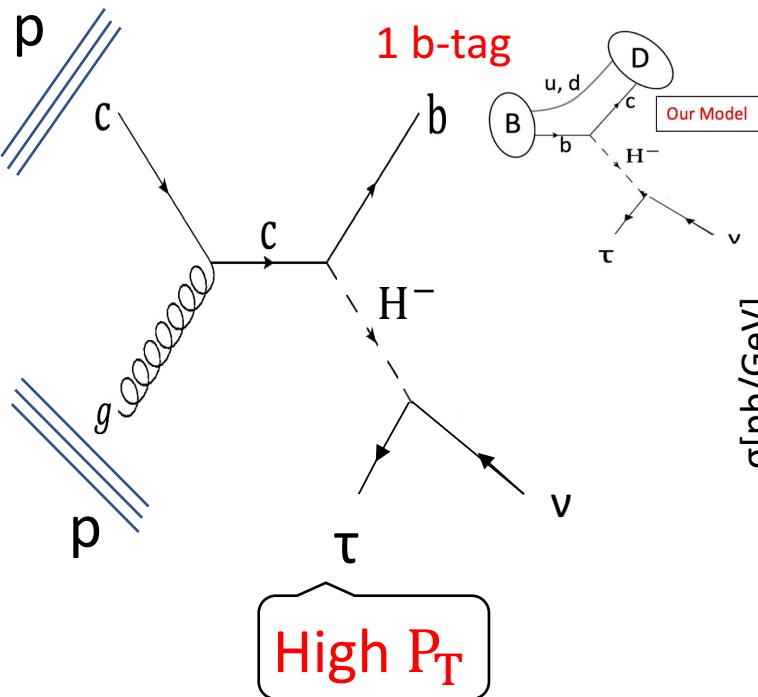
low background from $W \rightarrow \tau\nu$.



Experiment:arXiv	$\sqrt{s} [\text{TeV}]$	$L [\text{fb}^{-1}]$	Range $M_{W'} [\text{TeV}]$
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Implications for LHC

Enhancing $R(D^{(*)})$ needs a large effective coupling $\bar{c}b\bar{\tau}\nu$ mediated by charged Higgs and generates an energetic tau lepton as a final state in LHC. (A.Soni, et al. arXiv:1704.06659)



This process looks promising, but not measured yet

Summary

G2HDM can still explain R(D).

$\tau\nu$ resonance search can test it.

$\tau\nu$ resonance can give more stringent constraints
than $\text{Br}(B_c^- \rightarrow \tau\bar{\nu})$.

An interplay between flavor physics and collider physics
is important.

Back up

Menu

- W' case
- P'_5 anomaly and H⁻
-

Constraint for W'

See also M. Abdullah, et al.1805.01869

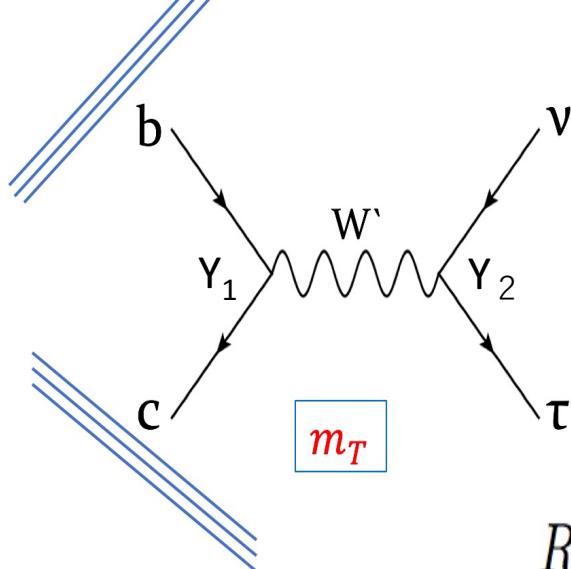
Vector (couple to left handed or right handed quarks)

We assume following operators.

A. Celis,et al. 1604.03088

G. Isidori,et al. 1506.01705....

$$L_{eff} = -2\sqrt{2}G_F V_{cb} \left((\delta_{l\tau} + C_{v1}^l) O_{v1}^l + C_{v2}^l O_{v2}^l \right)$$



left handed case

$$\frac{R(D)}{R(D)_{SM}} = \frac{R(D^*)}{R(D^*)_{SM}} = 1 + 2Re\{C_{v1}^\tau\} + |C_{v1}^\tau|^2 + |C_{v1}^\mu|^2 + |C_{v1}^e|^2$$

Left handed vector charged current

$$\frac{R(D)}{R(D)_{SM}} = \frac{R(D^*)}{R(D^*)_{SM}} = 1 + 2\text{Re}\{C_{v1}^\tau\} + |C_{v1}^\tau|^2 + |C_{v1}^\mu|^2 + |C_{v1}^e|^2$$

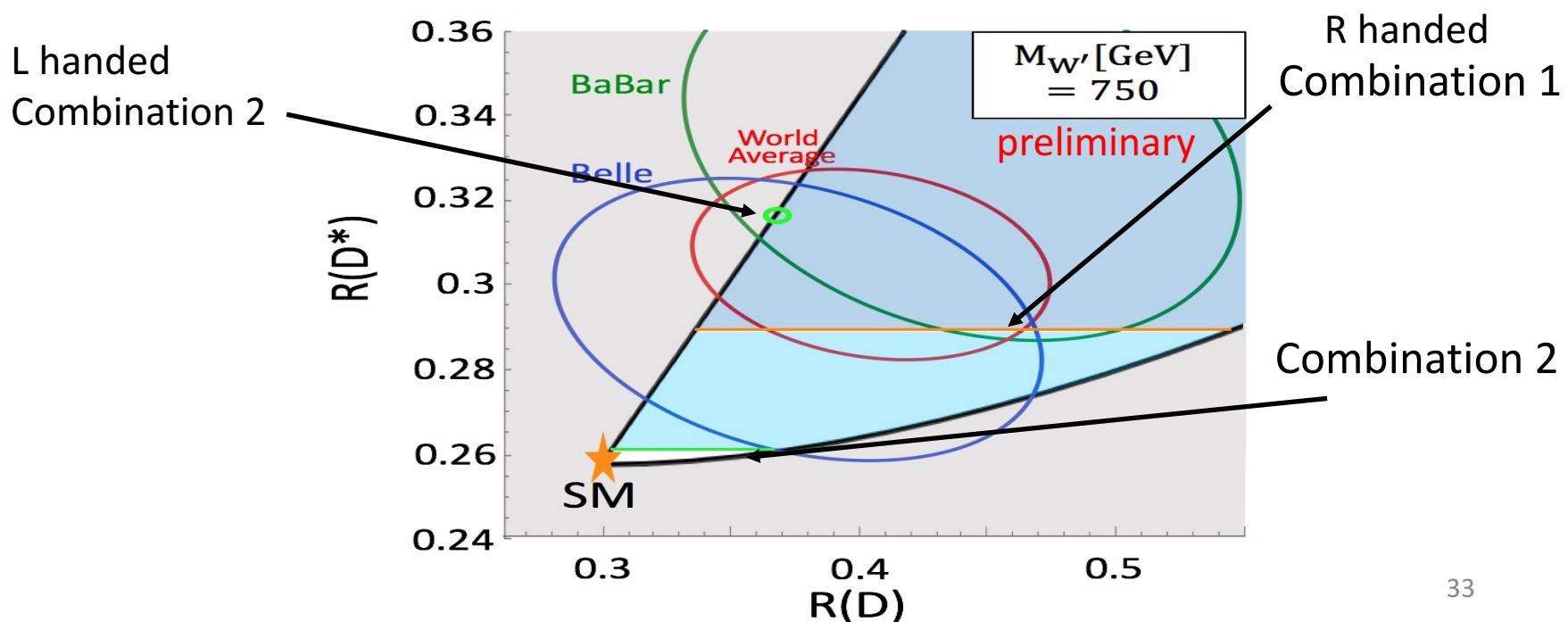
Right handed vector charged current

$$\frac{R(D)}{R(D)_{SM}} = 1 + 2\text{Re}\{C_{v1}^\tau\} + |C_{v1}^\tau|^2 + |C_{v1}^\mu|^2 + |C_{v1}^e|^2$$

$$\frac{R(D^*)}{R(D^*)_{SM}} = 1 + |C_{v1}^\tau|^2 + |C_{v1}^\mu|^2 + |C_{v1}^e|^2$$

This behavior comes from meson properties

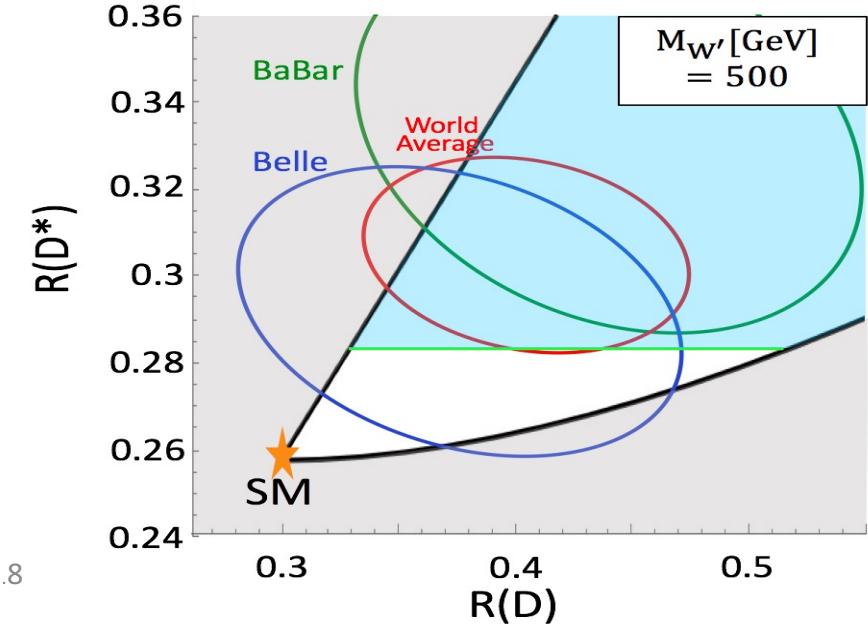
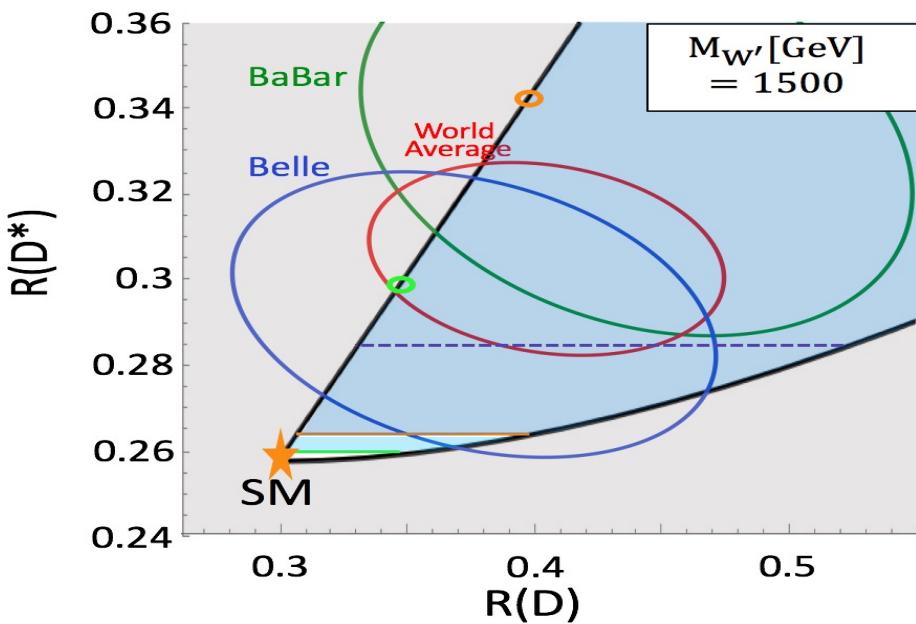
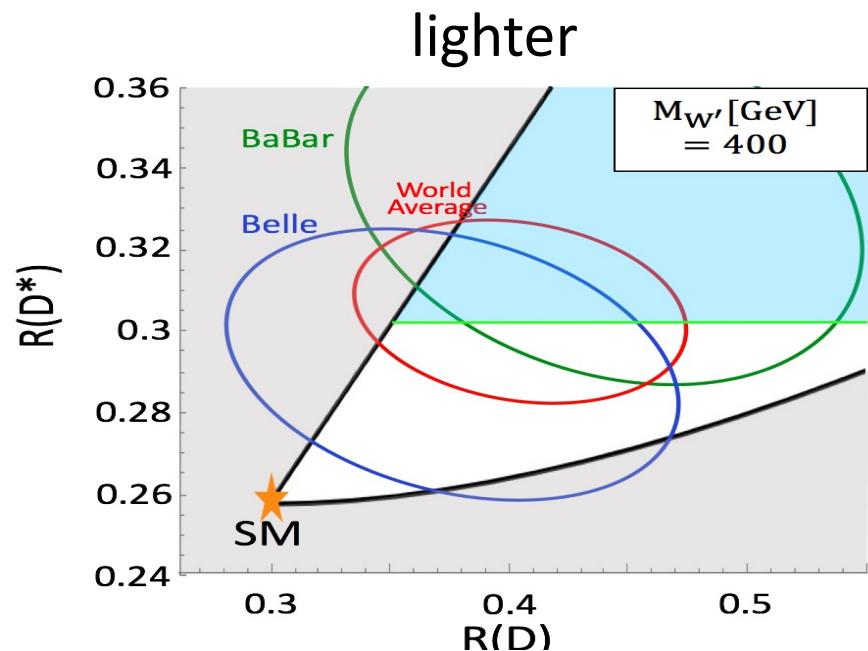
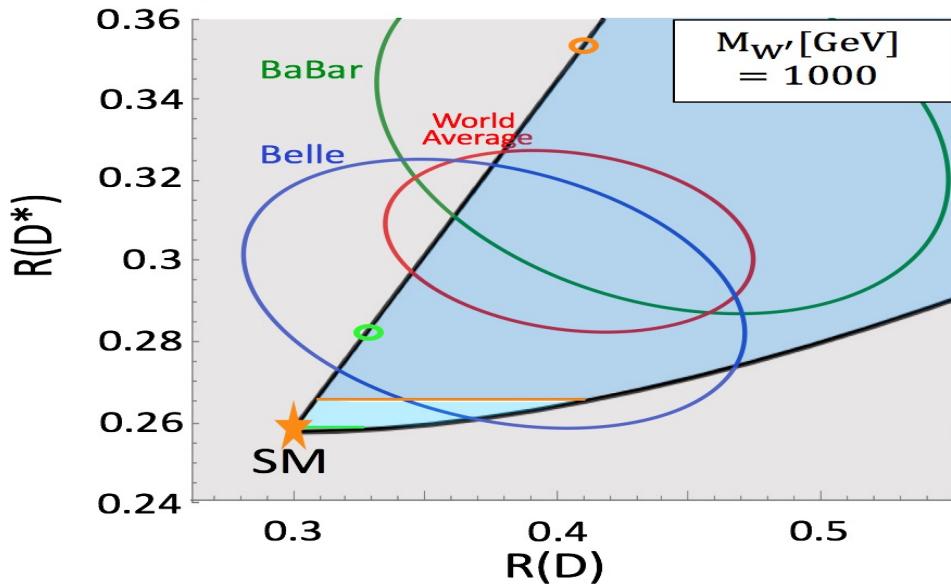
D: pseudo scalar, D*:vector meson.



Result

preliminary heavier

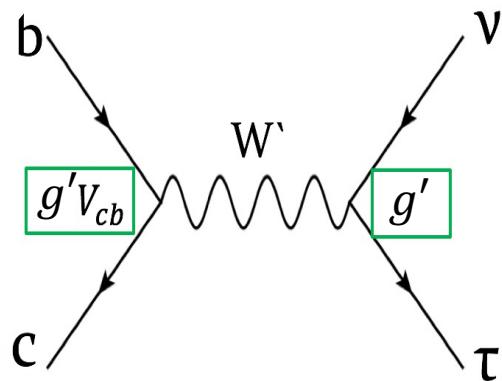
the heavier W' , the more severe constraint.



discussion

W' : difficulty for building models

SM like flavor structure is not favored. See left fig.



$V_{cb}=0.04$ suppression exists and requires large g'

T-parameter requires Z' with $m_{W'} \approx m_{Z'}$.

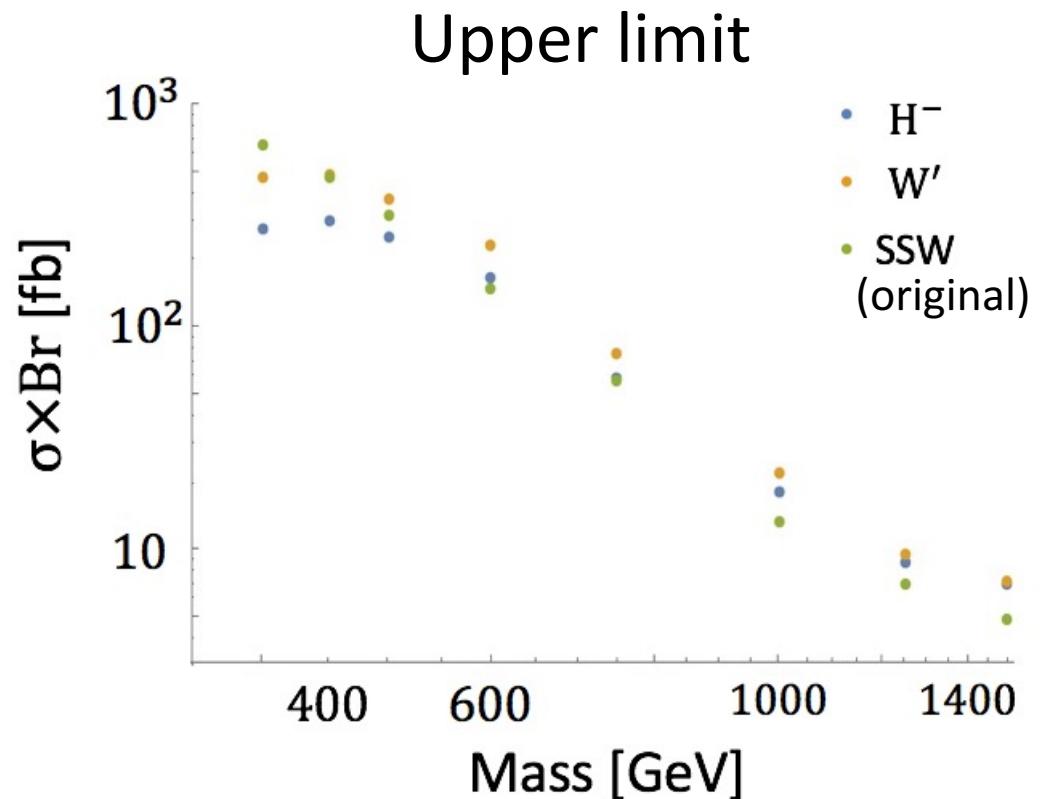
Then, there should be V_{cb} unsuppressed
 $pp \rightarrow bb \rightarrow Z' \rightarrow \tau\tau$ A.Greljo,et al:1609.07138

$500\text{GeV} > m_{W'} \text{ R}(D^{(*)})$ at that time.

We need extended gauge bosons with
an exotic flavor structure and lighter mass.

reinterpretation

Comparing their efficiencies by generating events with SSW, H^- and W' .

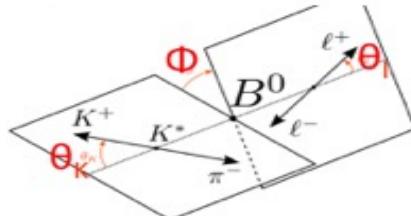


Cut

$P_T^\tau \geq 80\text{GeV}$, $|\eta| \leq 2.4$. $E_{miss} \geq 200\text{GeV}$. No e ($P_T^e \geq 20\text{GeV}$, $|\eta| \leq 2.5$) nor μ ($P_T^\mu \geq 20\text{GeV}$, $|\eta| \leq 2.4$). $0.7 \leq P_T^\tau/E_{miss} \leq 1.3$, azimuthal angle b/w τ and E_{miss} : $\Delta\phi \geq 2.4$.

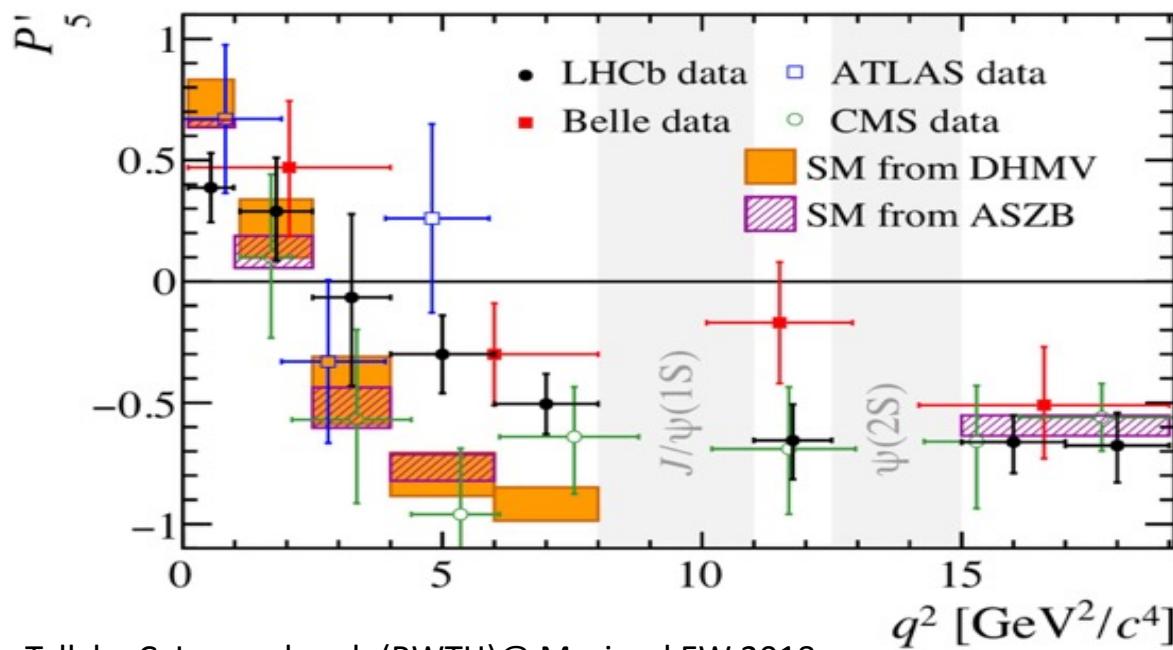
P'_5 anomaly in G2HDM

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell \, d\cos\theta_K \, d\phi \, dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2\theta_K + F_L \cos^2\theta_K \right.$$


 $\left. + \frac{1}{4}(1 - F_L) \sin^2\theta_K \cos 2\theta_\ell \right.$
 $- F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi$
 $+ S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi$
 $+ S_6 \sin^2\theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi$
 $+ S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right]$

Optimized observable

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}},$$



Talk by C. Langenbruch (RWTH)@ Moriond EW 2018

$b \rightarrow s$ transition

P'_5 : angular observable
in $B \rightarrow K^* \mu\mu$

P'_5 anomalies

$$\mathcal{H}_{B_s} = -g_{\text{SM}} \left\{ C_9^l (\bar{s}_L \gamma_\mu b_L) (\bar{l} \gamma^\mu l) + C_{10}^l (\bar{s}_L \gamma_\mu b_L) (\bar{l} \gamma^\mu \gamma_5 l) + h.c. \right\},$$

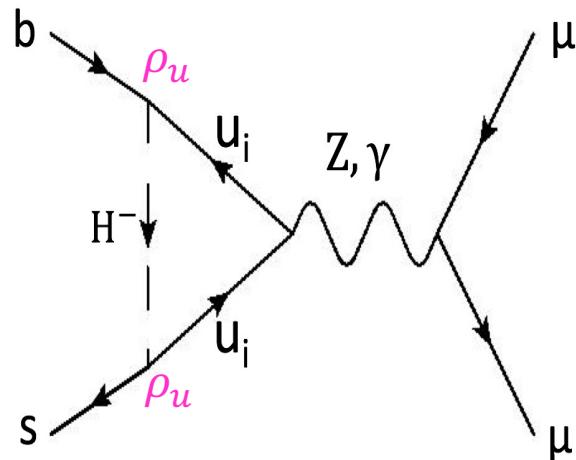
$$g_{\text{SM}} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2}.$$

ρ_u^{tc} generates charm rotating diagrams : $u_i = c$

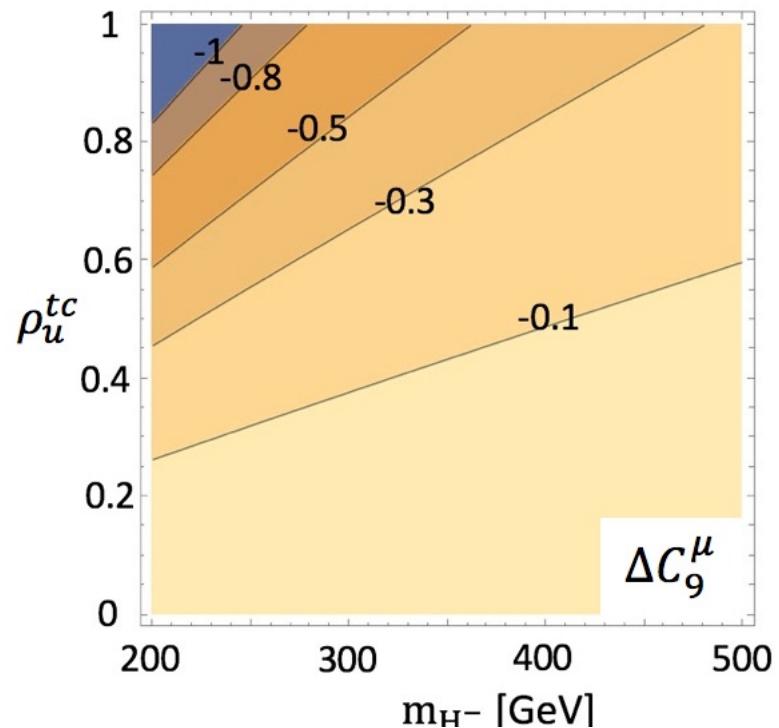
P'_5

$$\Delta C_9^\mu \approx -1 \text{ or } \Delta C_9^\mu = -\Delta C_{10}^\mu \approx -0.5$$

is favored G. D' Amico et al. 1704.05438



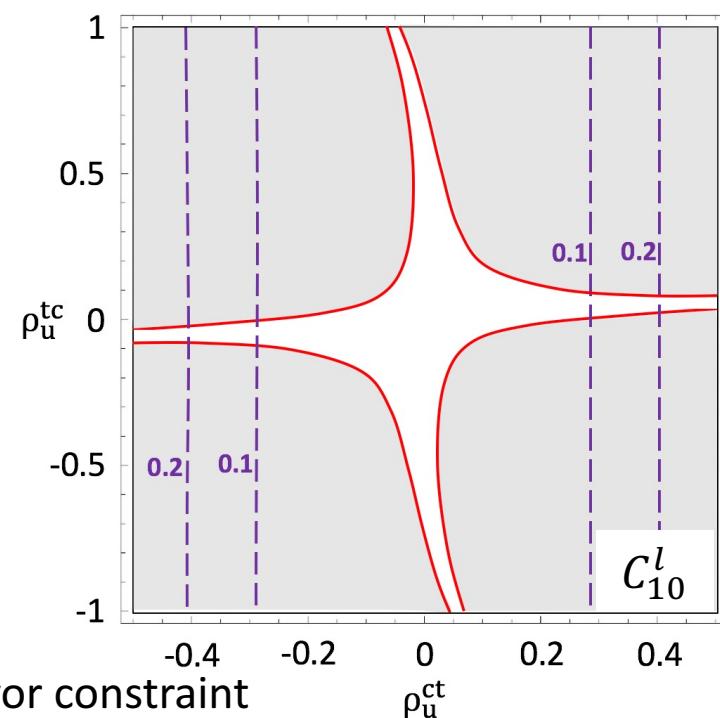
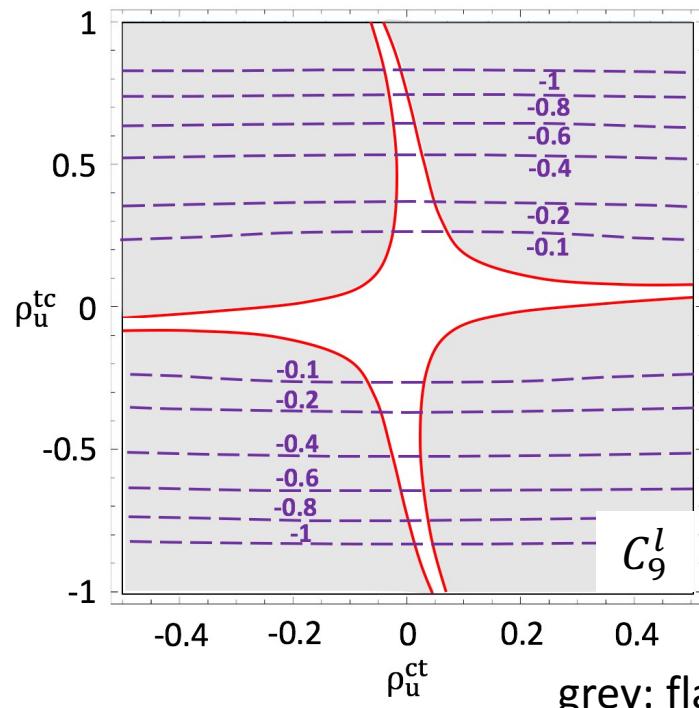
This γ penguin contribution has a dimensionless $\log \frac{m_c}{m_{H^-}}$ enhancement



Other prediction

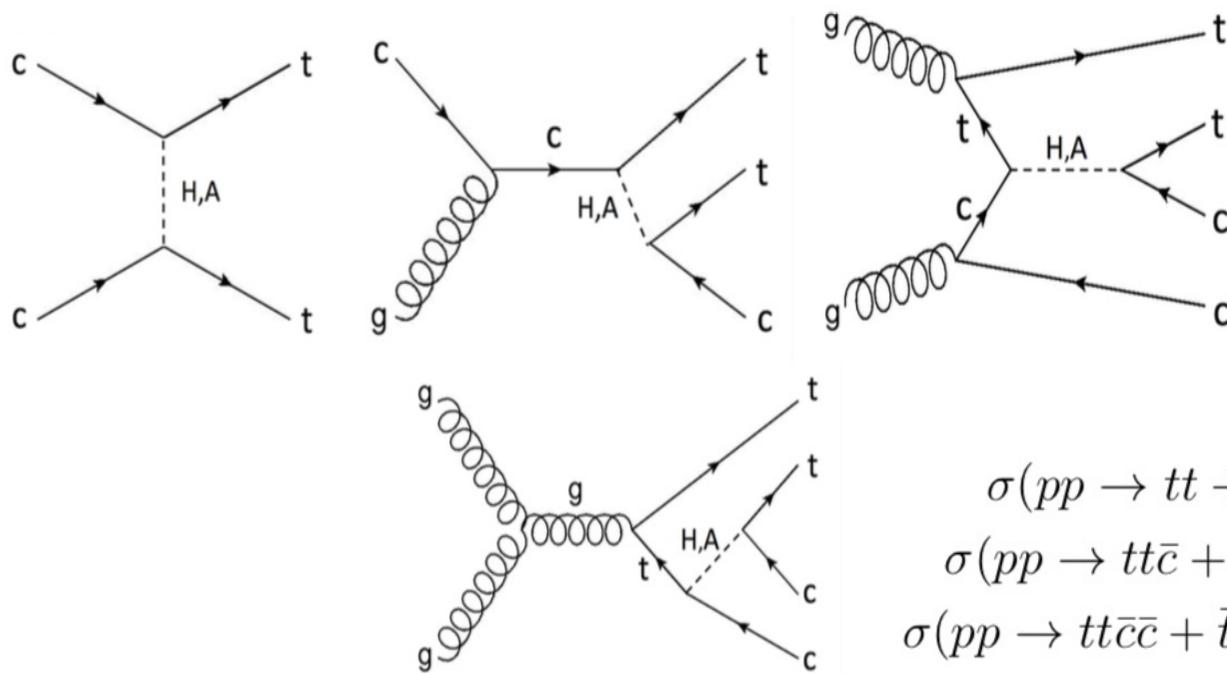
ρ_u^{tc} which generates a large contribution to C_9^l via γ penguin diagram, do not change $\text{Br}(B_s \rightarrow \mu\mu)$.

$$\frac{\text{Br}(B_s \rightarrow \mu\mu)}{\text{Br}(B_s \rightarrow \mu\mu)_{\text{SM}}} = |1 - 0.24C_{10}^\mu|^2$$



Collider signal

Same sign top is most striking



$$\sigma(pp \rightarrow tt + \bar{t}\bar{t}) = 4.23 \times 10^{-3} |\rho_u^{tc}|^4$$

$$\sigma(pp \rightarrow tt\bar{c} + \bar{t}\bar{t}c) = 4.13 \times 10^{-1} |\rho_u^{tc}|^4$$

$$\sigma(pp \rightarrow tt\bar{c}\bar{c} + \bar{t}\bar{t}cc) = 1.14 \times 10^{-1} |\rho_u^{tc}|^4$$

$$\text{for } (m_A, m_H) = (200, 250) \text{ GeV}$$

$m_A = m_H$ suppresses the signal.

Upper bound on $\sigma(\text{same sign top})=1.2$ [Pb] CMS:1704.07323 is still weak

For recent progress see 1808.00333.

G2HDM

We take so called Higgs base : a doublet acquires VEV

$$H_1 = \begin{pmatrix} G^+ \\ v + \Phi_1 + iG \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ \Phi_2 + iA \end{pmatrix}$$

G^+, G : N-G boson, H^+ :charged Higgs, A : CP odd Higgs

Linear transformation to mass base of CP even scalars

$$\begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{\beta\alpha} & \sin \theta_{\beta\alpha} \\ -\sin \theta_{\beta\alpha} & \cos \theta_{\beta\alpha} \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}$$

Yukawa terms

$$\begin{aligned} L_{CC} = & - \sum_{f=u,d,e} \sum_{\Phi=h,H,A} y_{\Phi ij}^f \bar{f}_{Li} \Phi f_{Rj} + \text{h.c.} \\ & - \bar{v}_{Li} (V_{MNS}^\dagger \rho_e)^{ij} H^+ e_{Rj} + \text{h.c.} \\ & - \bar{u}_i (V_{CKM} \rho_d P_R - \rho_u^\dagger V_{CKM} P_L)^{ij} H^+ d_j + \text{h.c.}, \end{aligned}$$

$$y_{hij}^f = \frac{m_f^i}{v} s_{\beta\alpha} \delta_{ij} + \frac{\rho_f^{ij}}{\sqrt{2}} c_{\beta\alpha}, \quad y_{Aij}^f = \begin{cases} -\frac{i\rho_f^{ij}}{\sqrt{2}} & \text{for } f = u \\ +\frac{i\rho_f^{ij}}{\sqrt{2}} & \text{for } f = d, e, \end{cases} \quad y_{Hij}^f = \frac{m_f^i}{v} c_{\beta\alpha} \delta_{ij} - \frac{\rho_f^{ij}}{\sqrt{2}} s_{\beta\alpha}$$

Result2

compatibility

	$R(K^{(*)})$	P'_5	$R(D)$	$R(D^*)$	$\delta\alpha_\mu$
(B) $\rho_e \neq 0, \rho_\nu = 0$					
ρ_u^{tt}	×	×	×	×	○
ρ_u^{tc}	×	○	○	×	×
ρ_u^{ct}	×	×	×	×	○

○: within 1σ

or XXOXO

JHEP 1805 (2018) 173 SI, Y. Omura