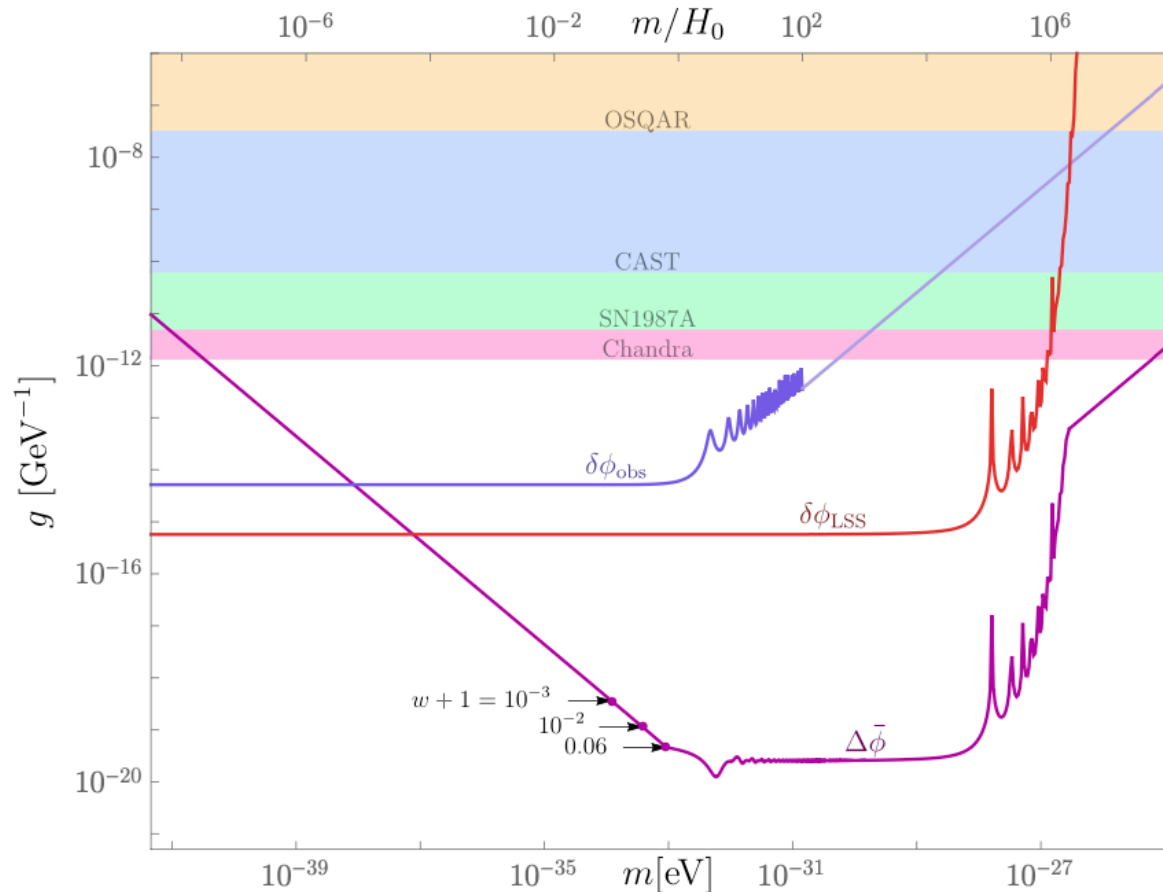


Probing Axion-like Particles via CMB Polarization



Collaborators: Tomohiro Fujita, Yuto Minami, Kai Murai,
[arxiv:2008.02473](https://arxiv.org/abs/2008.02473)



Speaker:
 Hiromasa Nakatsuka
 ICRR, The University of Tokyo
 2nd year PhD student



Axion

■ QCD axion

- Strong CP problem:

C. A. Baker, et al. (2006)

$$\mathcal{L}_{\theta_{QCD}} = \frac{\theta_{QCD}}{32\pi^2} \text{Tr} G_{\mu\nu} \tilde{G}^{\mu\nu}, \quad \theta_{QCD} \lesssim 10^{-10} \quad \text{by the electric dipole moment of neutron}$$

- One of solutions is QCD axion:

$$\mathcal{L}_{\theta_{QCD}} \rightarrow \left(\theta_{QCD} + \frac{\phi}{f} \right) \frac{1}{32\pi^2} \text{Tr} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

■ Axion-like particles by String Axiverse

A. Arvanitaki, et al. (2009)

“String theory suggests the simultaneous presence of many ultralight axions”

- Axions have mass nonperturbatively, which is exponentially suppressed:

$$m_{\phi}^2 \propto \left(\frac{\mu^4}{f^2} \right) e^{-S_{\text{inst}}}$$

David J. E. Marsh (2015)

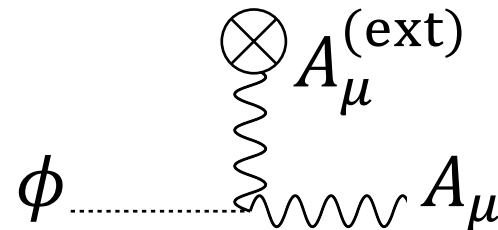
- Axion as Dark Matter: $10^{-22} \text{eV} \lesssim m$
- Axion as Dark Energy: $m \lesssim H_0 \sim 10^{-33} \text{eV}$

Axion-like Particles

Axion-Photon coupling

$$\mathcal{L} = -\frac{1}{2}\partial^\mu\phi\partial_\mu\phi - V(\phi) - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{4}g\phi F_{\mu\nu}\tilde{F}^{\mu\nu}, \quad \phi:\text{axion(ALP)}$$

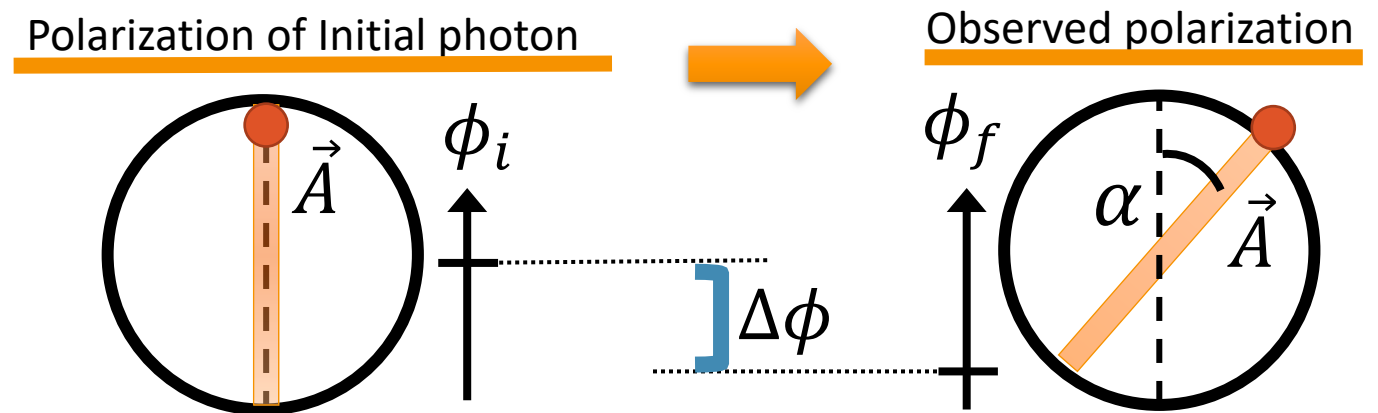
- Axion-photon conversion
By background B field:



- Rotation of polarization angle

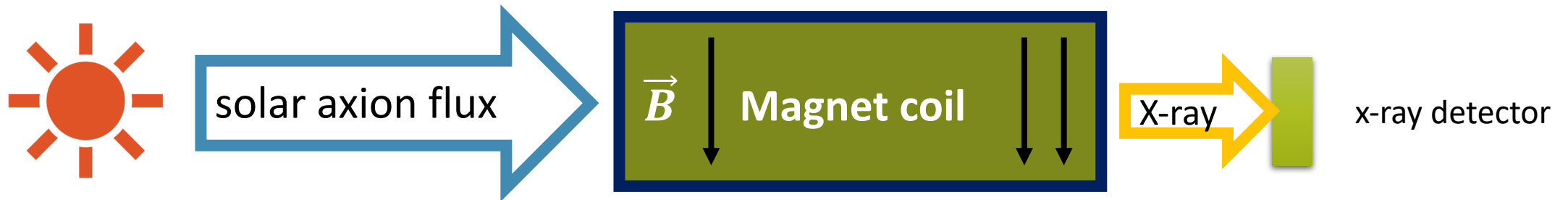
$$\alpha = \frac{g}{2}\Delta\phi = \frac{g}{2}(\phi_f - \phi_i)$$

D.Harari&P.Sikivie (1992)



Axion-photon conversion

■ Axion Helioscope (e.g., CAST, CAST Collaboration (2005))



■ Axion Dark Matter eXperiment (ADMX) for Axion DM

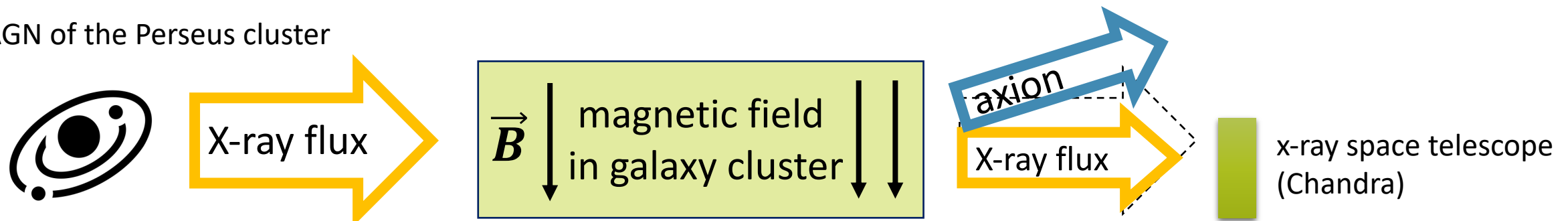
S.J. Asztalos, et al. (2009)

- The microwave cavity for resonant conversion

■ X-ray space telescope: Chandra observatory

M. Berg, et al. (2016)

AGN of the Perseus cluster



Polarization rotation

■ Ground-based experiment: Laser technique

- The background axion DM rotates the polarization angle of laser.
- Laser cavity can detect the small rotation angle.

H. Liu, et al. (2018), I. Obata, et al. (2018), K. Nagano, et al. (2019)

■ Astronomical source (e.g. proto-planetary disc)

- Flattened gaseous object surrounding a young star
- The background axion DM rotates the direction of scattering polarization.

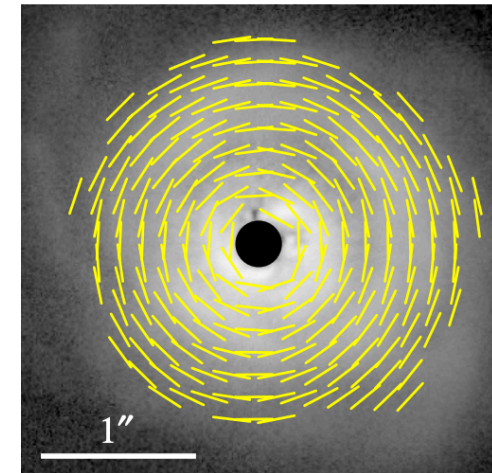
J. Hashimoto, et al. (2011), T. Fujita, et al. (2018), S. Chigusa et al. (2019)

■ Cosmological source: CMB

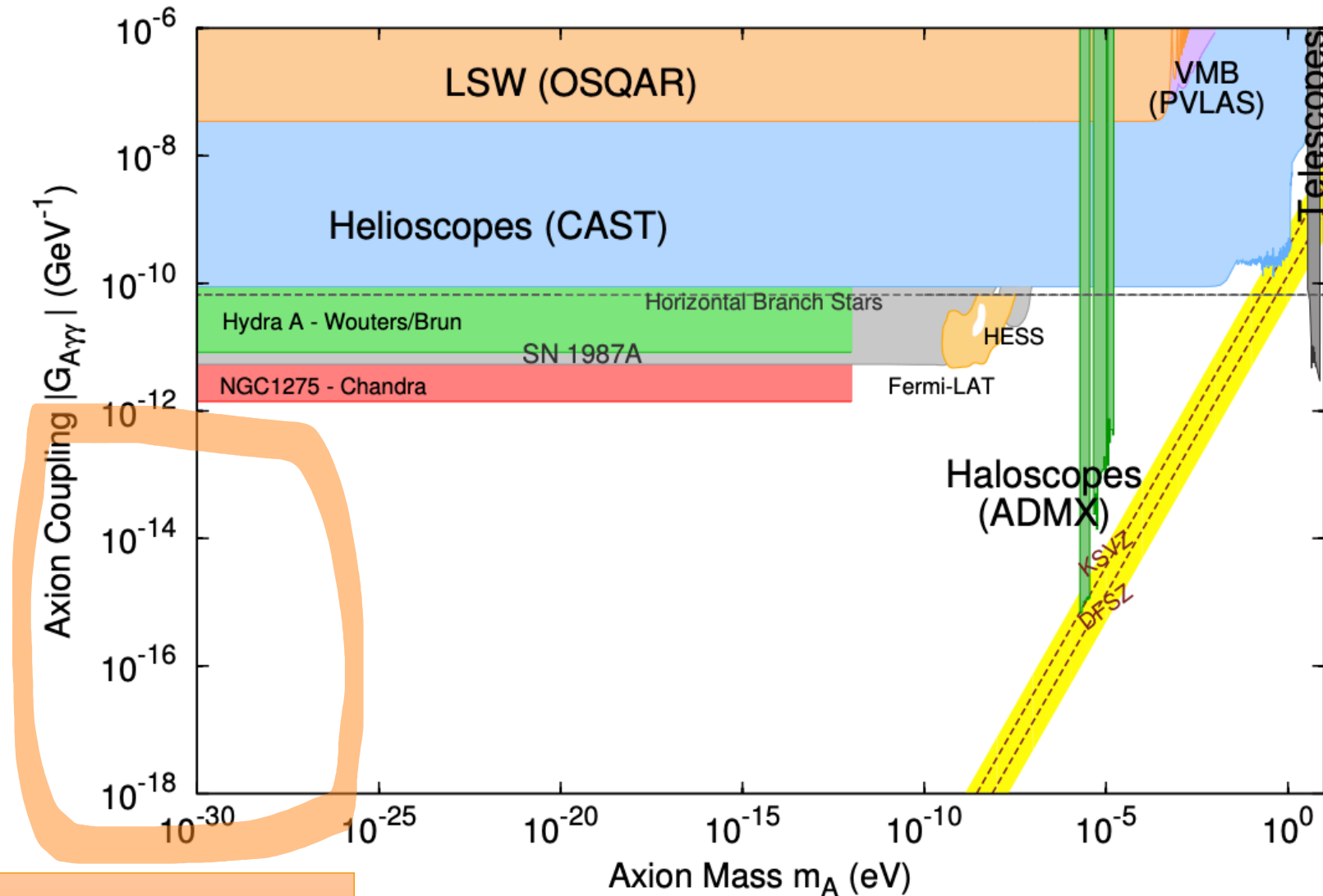
S. M. Carroll (1998), A. Lue, et al. (1999), M. A. Fedderke, et al. (2019), G. Sigl&P. Trivedi (2018)

- and This work

J.Hashimoto, et al. (2011),



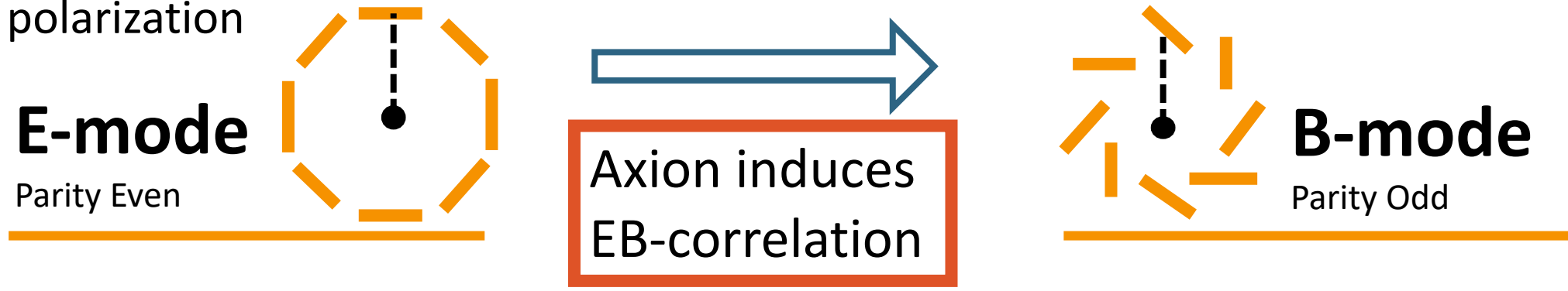
The constraints of axion-photon coupling



This work

Cosmic Birefringence

■ CMB polarization

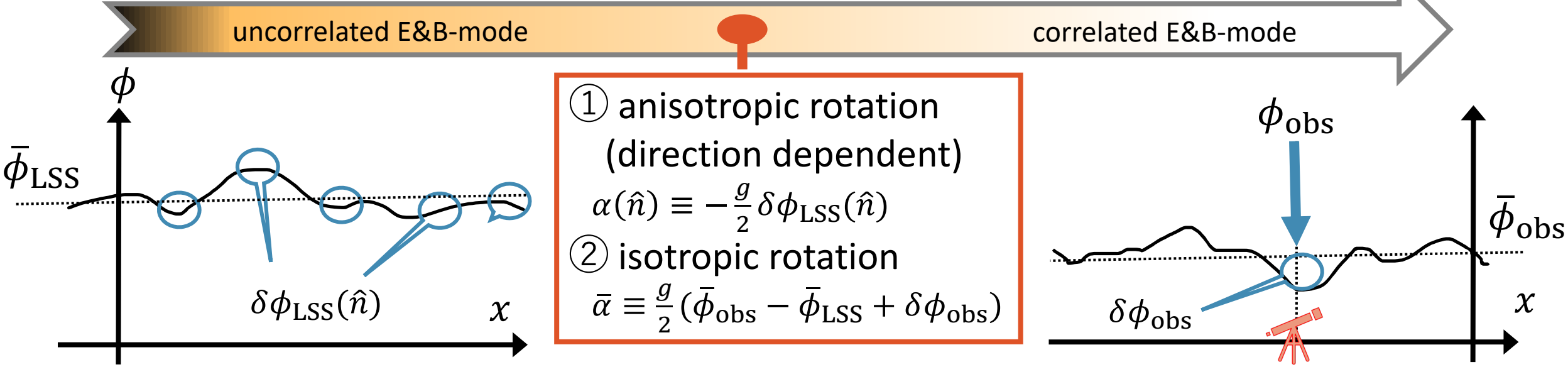


■ Cosmic Birefringence

● Last Scattering Surface(LSS): $t_{LSS} \sim 3.8 \times 10^5 \text{ yr}$

● Observer: $t_0 \sim 13.8 \times 10^9 \text{ yr}$

S.M.Carroll (1998), A. Lue, et.al. (1999)



- ① anisotropic rotation (direction dependent)
 $\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{LSS}(\hat{n})$
- ② isotropic rotation
 $\bar{\alpha} \equiv \frac{g}{2} (\bar{\phi}_{obs} - \bar{\phi}_{LSS} + \delta\phi_{obs})$

Field Dynamics

■ Birefringence by $\Delta\bar{\phi}$, $\delta\phi_{\text{obs}}$ and $\delta\phi_{\text{LSS}}$

- Potential term : $V(\phi) = \frac{1}{2}m^2\phi^2$
- Background motion : $\Delta\bar{\phi} \equiv \bar{\phi}(t_0) - \bar{\phi}(t_{\text{LSS}})$,

- Dynamics : $\bar{\phi}(t) \propto \begin{cases} \text{constant} & (m < H(t)) \\ a(t)^{-\frac{3}{2}} \sin(mt) & (H(t) < m) \end{cases}$

- Amplitude : $|\bar{\phi}| \propto \Omega_\phi^{1/2}$, $\Omega_\phi \sim \begin{cases} 0.7 & (m \lesssim H_0) \\ 0.01 & (H_0 \lesssim m \lesssim 10^{-25} \text{eV}) \end{cases}$ R.Hlozek, et.al.(2015)

- Perturbation: $\delta\phi_{\text{obs}}$ & $\delta\phi_{\text{LSS}}$

- $\mathcal{P}_\phi^{\text{inf}} = \left(\frac{H_I}{2\pi}\right)^2 = \frac{M_{\text{pl}}^2}{8\pi} \mathcal{P}_\zeta \times r$, $\mathcal{P}_\zeta \simeq 2 \times 10^{-9}$, r : tensor to scalar ratio, we use $r = 0.06$

① anisotropic rotation (direction dependent) : $\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{\text{LSS}}(\hat{n})$

② isotropic rotation : $\bar{\alpha} \equiv \frac{g}{2} (\Delta\bar{\phi} + \delta\phi_{\text{obs}})$

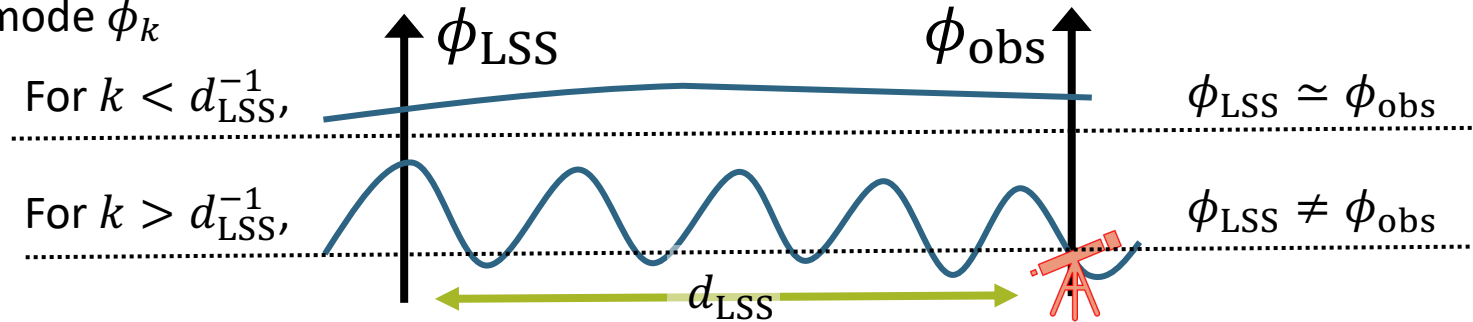
$$\cdot \begin{cases} \phi_{\text{LSS}} = \bar{\phi}(t_{\text{LSS}}) + \delta\phi_{\text{LSS}}(t_{\text{LSS}}, \hat{n}) \\ \phi_{\text{obs}} = \bar{\phi}(t_0) + \delta\phi_{\text{obs}}(t_0, x=0) \end{cases}$$

• H_0 : (current Hubble parameter)

Field Dynamics

Fluctuation at observer: $\delta\phi_{\text{obs}}$

- The Fourier mode $\tilde{\phi}_k$



- $$\langle \delta\phi_{\text{obs}}^2 \rangle = \int_{d_{\text{LSS}}^{-1}}^{\infty} \int_{d_{\text{LSS}}^{-1}}^{\infty} \frac{d^3k d^3p}{(2\pi)^6} \langle \phi_{\mathbf{k}}(\eta_0) \phi_{\mathbf{p}}(\eta_0) \rangle$$

Damping effect by the width of LSS

- Last Scattering Surface(LSS): $t_{\text{LSS}} \sim 3.8 \times 10^5 \text{yr}$

- Observer: $t_0 \sim 13.8 \times 10^9 \text{yr}$



- For $m > 10^{-28} \text{eV}$, ϕ oscillates at LSS:

$$\langle \bar{\phi} \rangle_{\text{LSS}} = \int dT g(T) \bar{\phi}(t(T)) \quad , \text{visibility function: } g(T) \simeq \frac{1}{\sqrt{2\pi}\sigma_T} \exp\left[-\frac{(T - T_L)^2}{2\sigma_T^2}\right]$$

Sensitivity

■ Current sensitivity from Planck, SPTpol & ACTPol

N. Aghanim, et al. (2016), F. Bianchini, et al. (2020), T. Namikawa, et al. (2020)

① anisotropic rotation (direction dependent) : $\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{\text{LSS}}(\hat{n})$

$$C_L^{\alpha\alpha} \equiv \frac{1}{2L+1} \sum_M a_{(\alpha)LM} a_{(\alpha)LM}^*, \quad a_{(\alpha)Lm} \equiv \int d\Omega \alpha(\hat{n}) Y_L^{m*}(\hat{n})$$

- For flat power spectrum,

$$A_\alpha \equiv \frac{L(1+L)C_L^{\alpha\alpha}}{2\pi}$$

- SPTpol & ACTPol 2020:

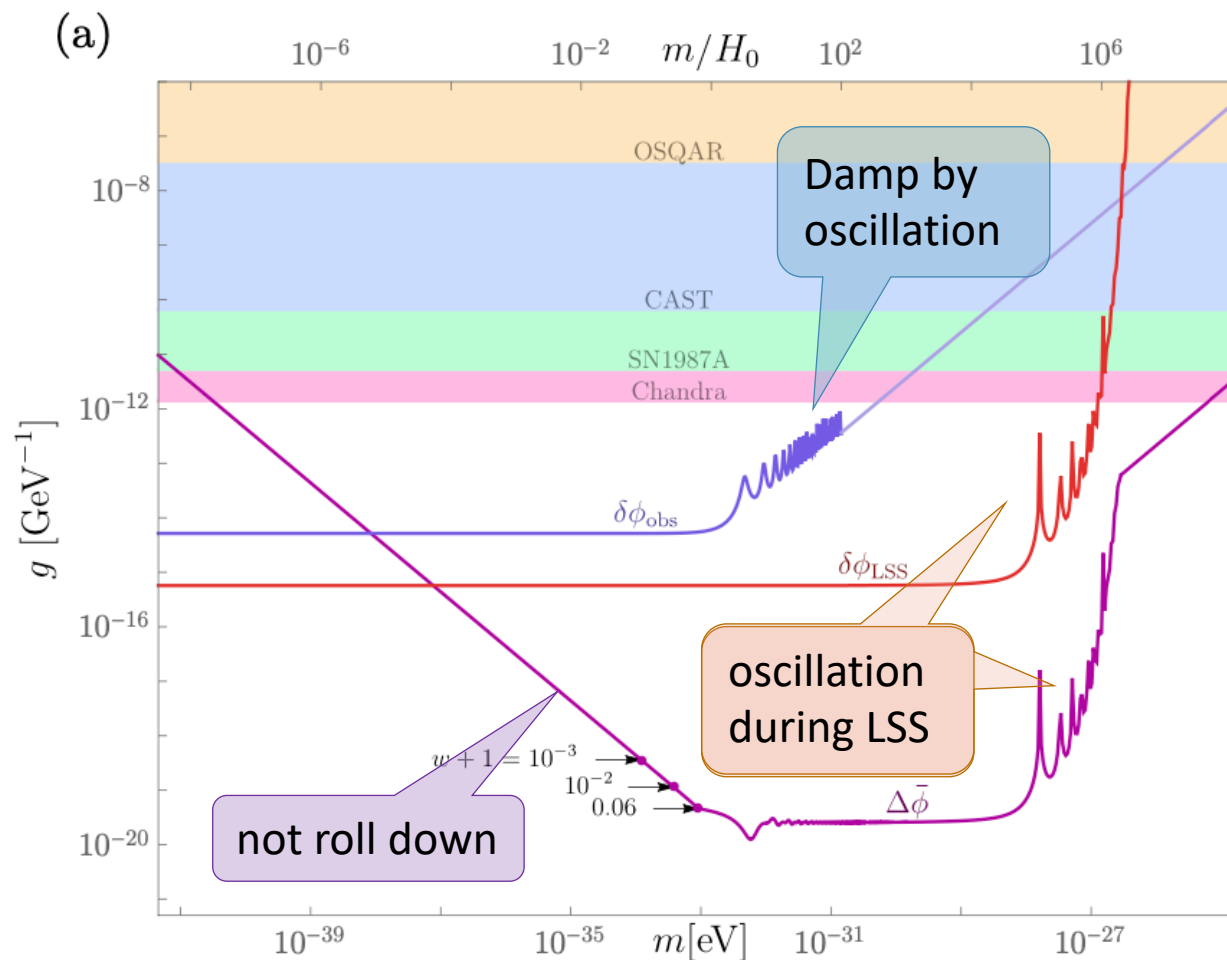
$$A_\alpha < 8.3 \times 10^{-3} \text{ deg}^2 \quad (68\% \text{CL})$$

② isotropic rotation : $\bar{\alpha} \equiv \frac{g}{2} (\Delta\bar{\phi} + \delta\phi_{\text{obs}})$

- Planck2016: $|\bar{\alpha}| < 0.6^\circ \quad (68\% \text{CL})$

Sensitivity

H_0 : (current Hubble parameter)



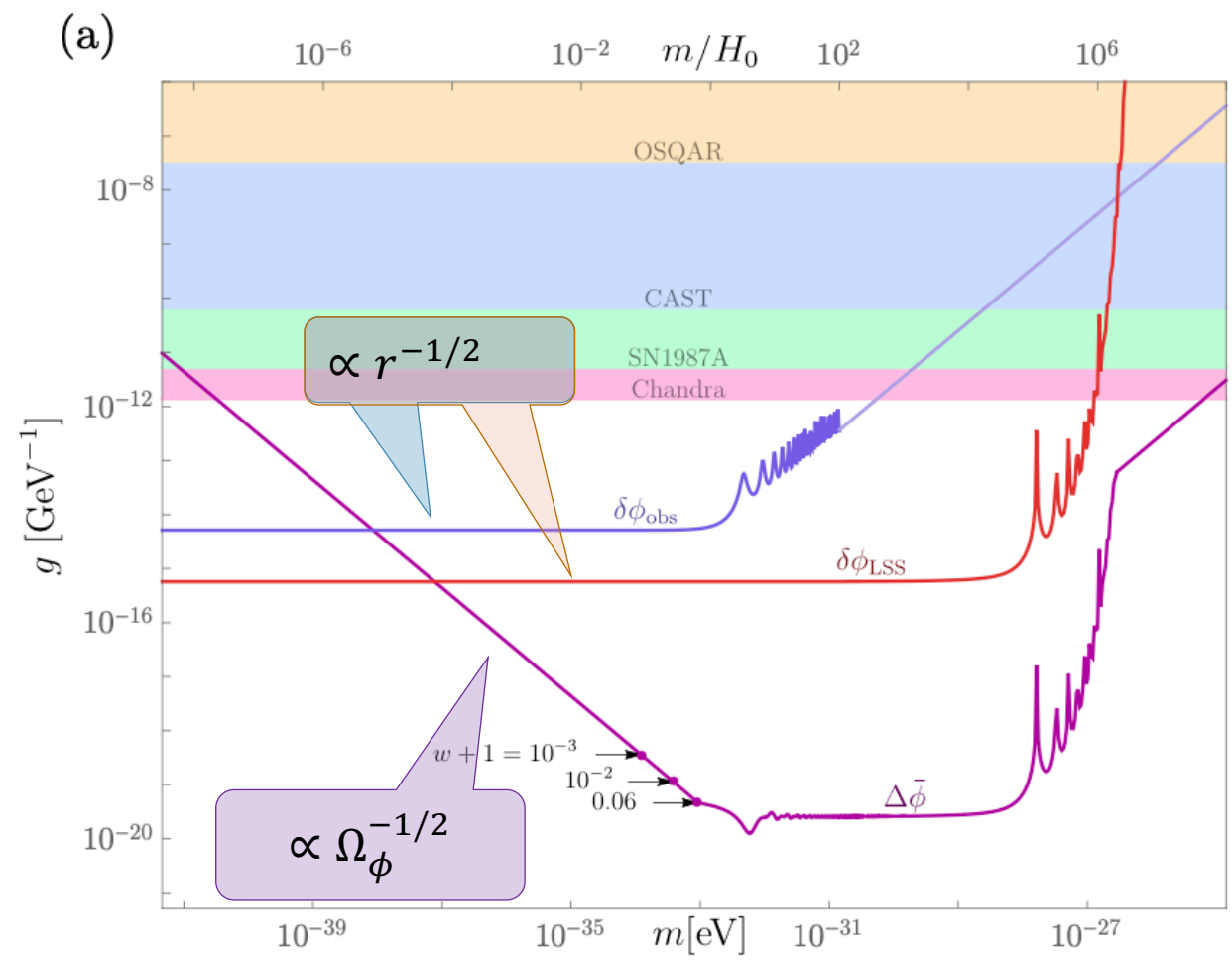
Current sensitivity from Planck & SPTpol

N. Aghanim et al. 2016, F. Bianchini et al. 2020, T. Namikawa et al. 2020

- **Red line** by $\delta\phi_{\text{LSS}}$
 For $10^{-28} \text{eV} < m$, ϕ oscillates during LSS, and the averaged rotation angle damps.
- **Purple line** by $\Delta\bar{\phi}$
 For $m < H_0$, $\bar{\phi}$ does not roll down the potential, and $\Delta\bar{\phi} \propto (m/H_0)$
- **Blue line** by $\delta\phi_{\text{obs}}$
 For $H_0 < m$, $\delta\phi_{\text{obs}}$ starts oscillating and damps.

Sensitivity

H_0 : (current Hubble parameter)



Current sensitivity from Planck & SPTpol

• Even if no BG axion $\Omega_\phi \rightarrow 0$, we ubiquitously have $\delta\phi_{\text{LSS}}$ & $\delta\phi_{\text{obs}}$ from inflation.

- $\delta\phi_{\text{LSS}}$: anisotropic birefringence
- $\delta\phi_{\text{obs}}$: isotropic birefringence

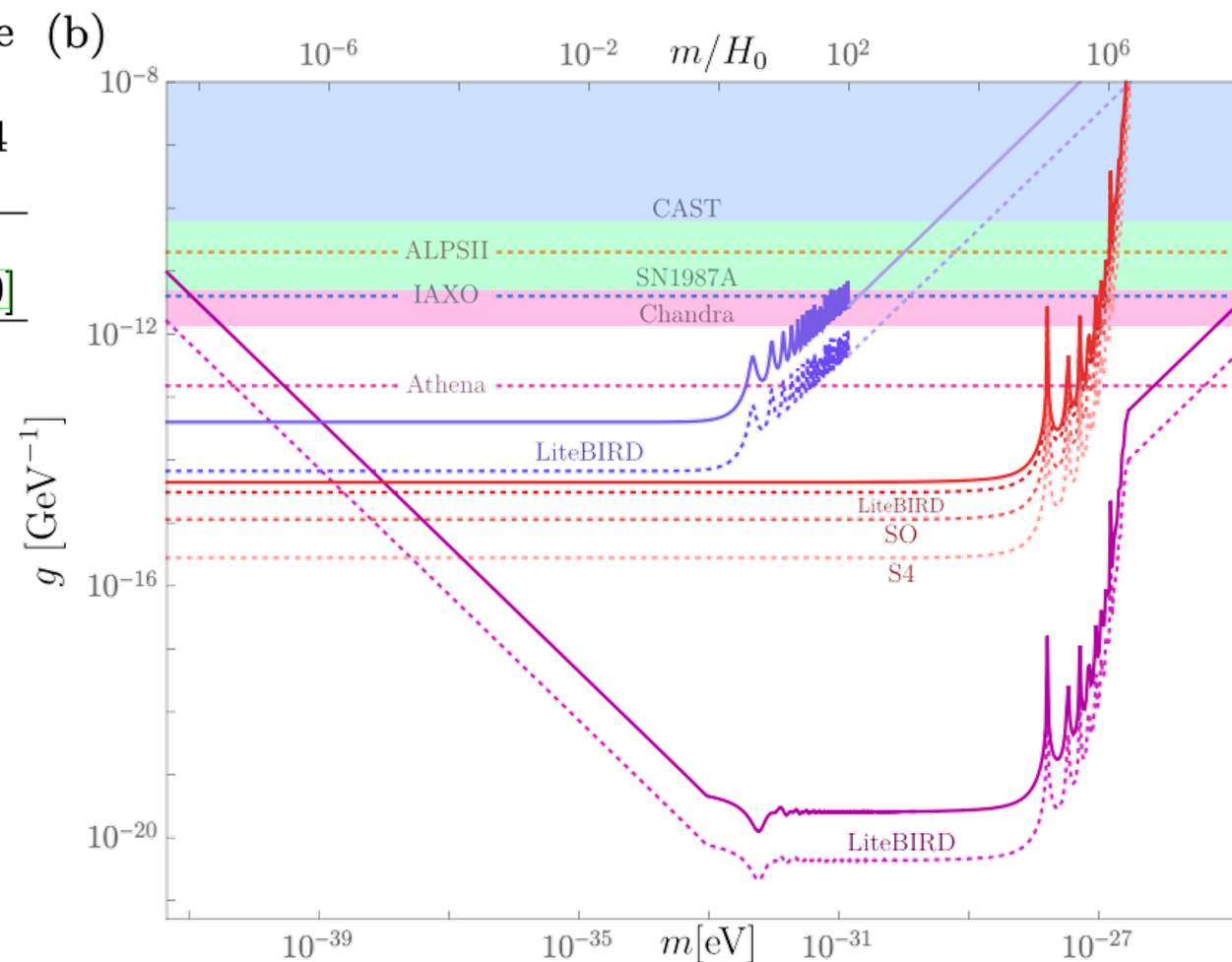
Future sensitivity

TABLE I. Current bounds and projected sensitivities to the polarization rotation parameters. (b)

	Current	LiteBIRD	SO	CMB-S4 like
$ \bar{\alpha} $ ($^\circ$)	< 0.6 [46]	0.1 [47]	-	-
A_α (10^{-3} deg^2)	< 8.3 [48, 49]	4.0 [50]	0.55 [50]	0.033 [50]

[Table in our paper, arxiv:2008.02473](#)

- Here, $r = 10^{-3}$ in the reach of LiteBIRD



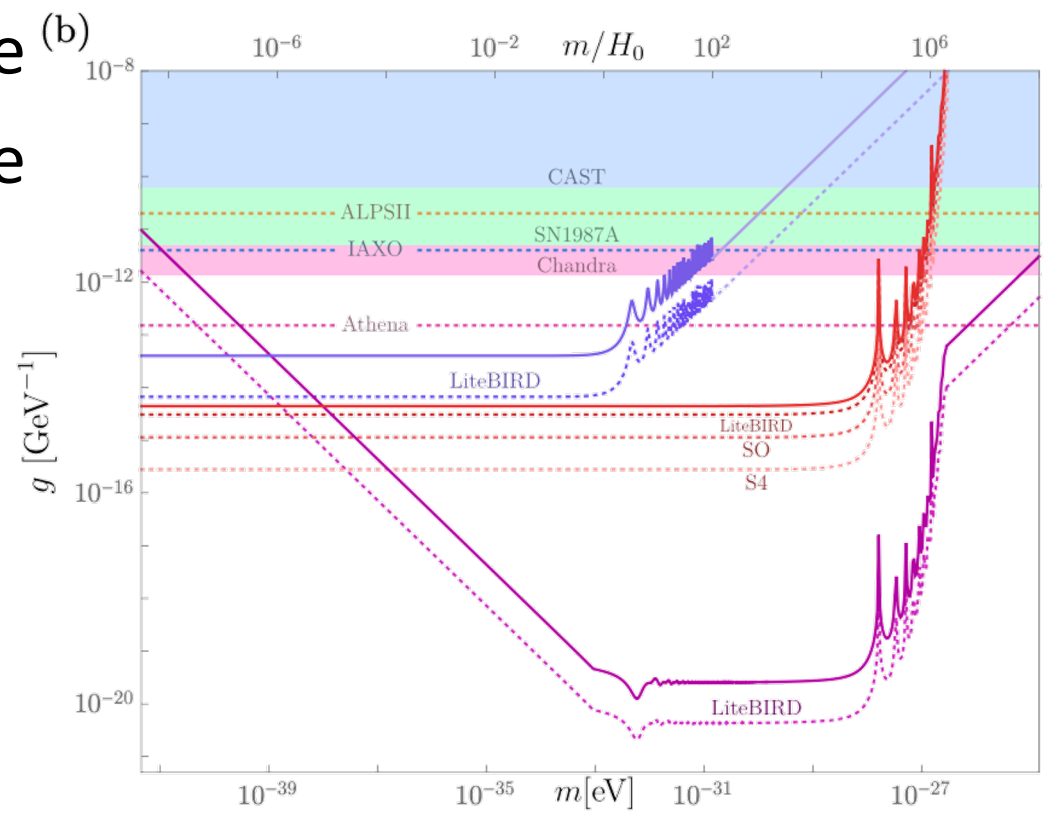
Discussion

What if we detect ... ?

- ① anisotropic birefringence
- ② Only isotropic (no anisotropic) birefringence
- ③ Only anisotropic (no isotropic) birefringence

$$\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{LSS}(\hat{n})$$

$$\bar{\alpha} \equiv \frac{g}{2} (\Delta\bar{\phi} + \delta\phi_{obs})$$



Discussion

What if we detect ... ?

① anisotropic birefringence by $\delta\phi_{LSS} \propto \left(\frac{H_I}{2\pi}\right)$

- we can fix “ $g^2 \times r$ ”,

$$\left(\frac{A_\alpha^{CMB}}{8.3 \times 10^{-3} \text{ deg}^2}\right) = \left(\frac{g}{4.4 \times 10^{-15} \text{ GeV}^{-1}}\right)^2 \left(\frac{r}{10^{-3}}\right)$$

Observable

upper bound (e.g. Chandra)

$$g < g_{\text{max}}$$

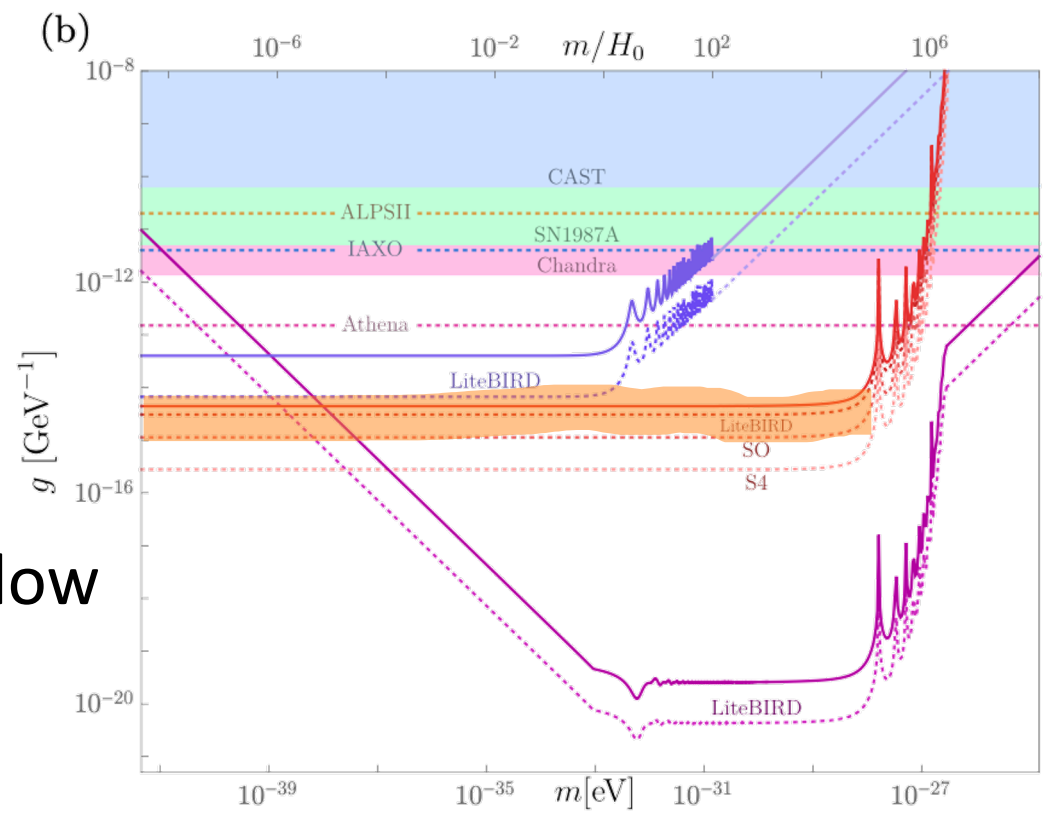
$$\Rightarrow r > 5 \times 10^{-9} \left(\frac{A_\alpha^{CMB}}{4 \times 10^{-3} \text{ deg}^2}\right)$$

✓ CMB experiments can investigate r from below by Birefringence!

(and from above by the primordial GW)

$$\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{LSS}(\hat{n})$$

$$\bar{\alpha} \equiv \frac{g}{2} (\Delta\bar{\phi} + \delta\phi_{\text{obs}})$$



Discussion

What if we detect ... ?

② Only isotropic birefringence by $\delta\phi_{\text{obs}}$ or $\Delta\bar{\phi}$

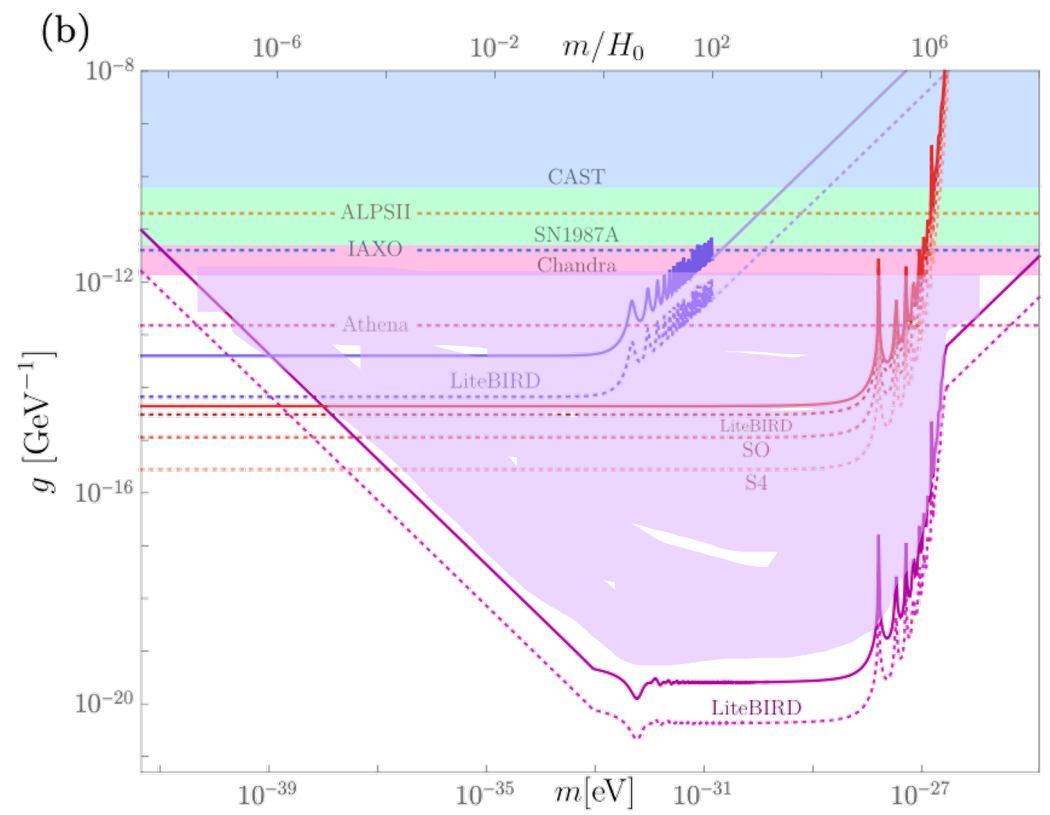
• Non-detection of $\delta\phi_{\text{LSS}}$ means $\Delta\bar{\phi}$, not $\delta\phi_{\text{obs}}$

• g has upper bound, then

$$10^{-8} \left(\frac{|\bar{\alpha}|}{0.3^\circ} \right) < \frac{m}{H_0} < 10^8 \left(\frac{|\bar{\alpha}|}{0.3^\circ} \right)$$

✓ We can investigate the mass of axion DE, including very small Equation of State w !

$$\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{\text{LSS}}(\hat{n})$$
$$\bar{\alpha} \equiv \frac{g}{2} (\Delta\bar{\phi} + \delta\phi_{\text{obs}})$$



Discussion

What if we detect ... ?

③ Only anisotropic birefringence

- Non-detection of $\delta\phi_{\text{obs}}$ means

$$1 \lesssim \frac{m}{H_0}$$

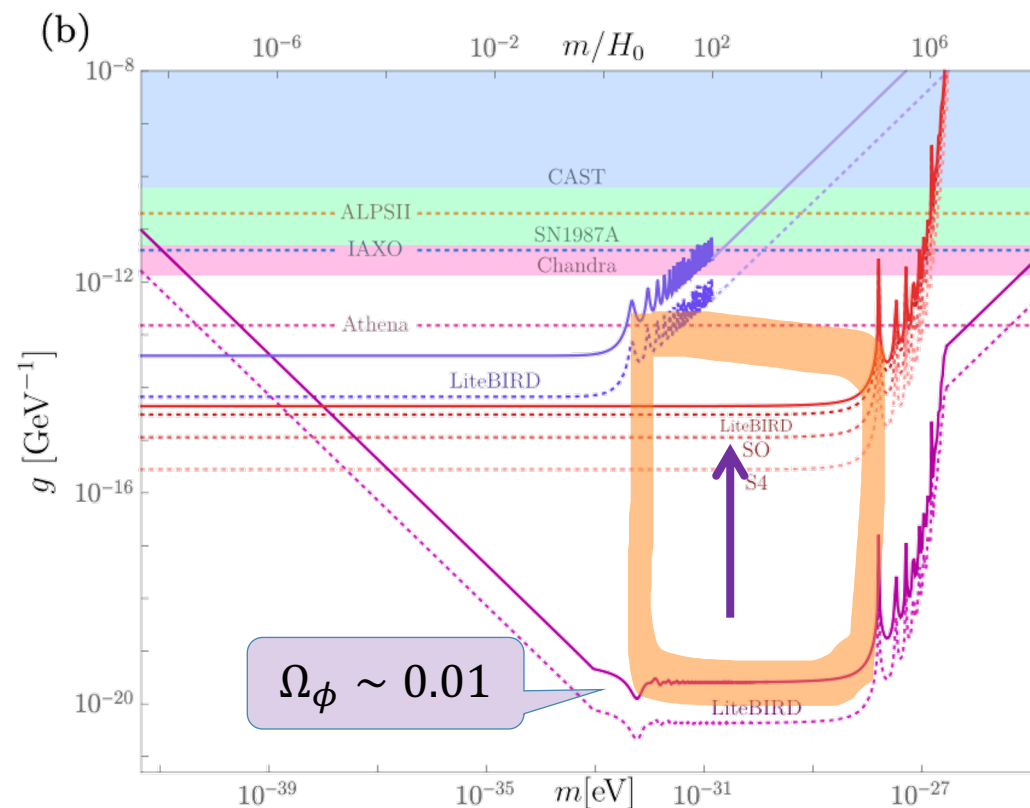
- Non-detection of $\Delta\bar{\phi}$ means

$$\Omega_\phi h^2 \lesssim 2 \times 10^{-13} \left(\frac{|\bar{\alpha}|}{0.05^\circ} \right)^2 \left(\frac{A_\alpha^{\text{CMB}}}{4 \times 10^{-3} \text{deg}^2} \right)^{-1} \left(\frac{r}{0.06} \right)$$

- ✓ We can put a stringent constraint on the energy fraction of the axion!

$$\alpha(\hat{n}) \equiv -\frac{g}{2} \delta\phi_{\text{LSS}}(\hat{n})$$

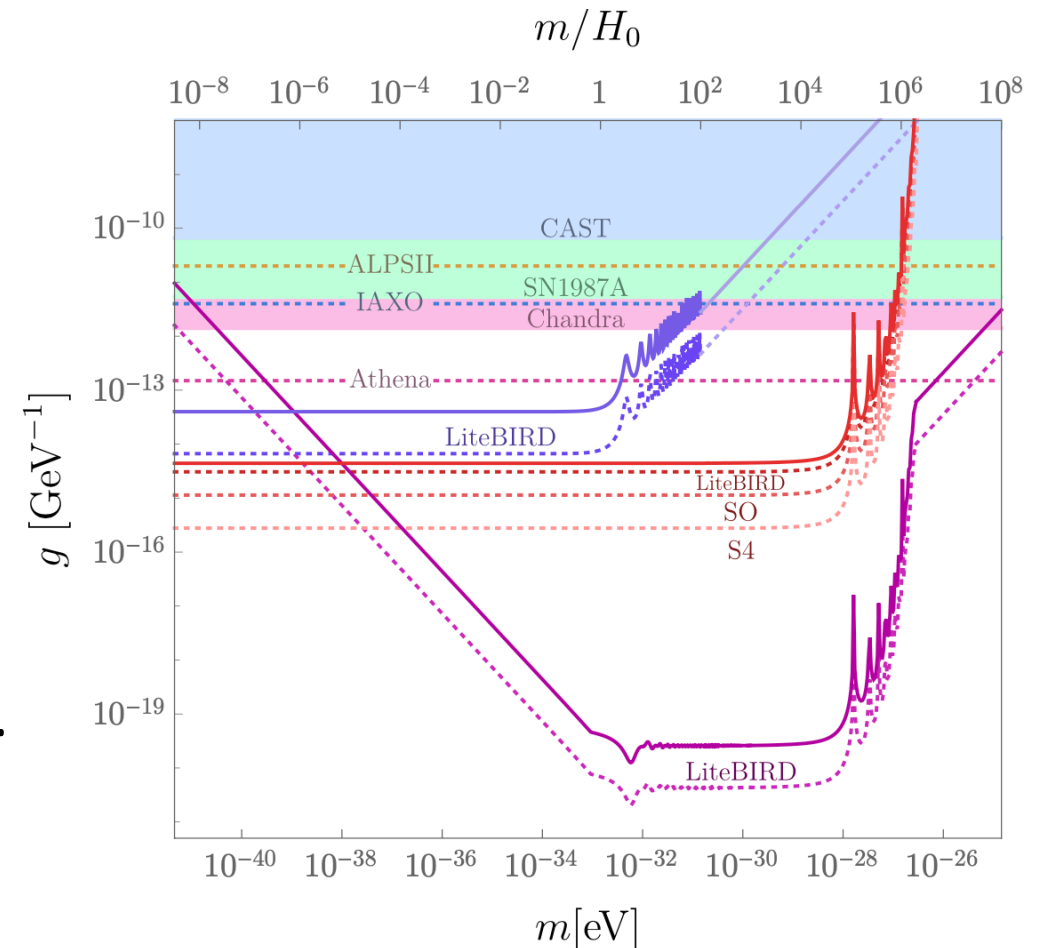
$$\bar{\alpha} \equiv \frac{g}{2} (\Delta\bar{\phi} + \delta\phi_{\text{obs}})$$



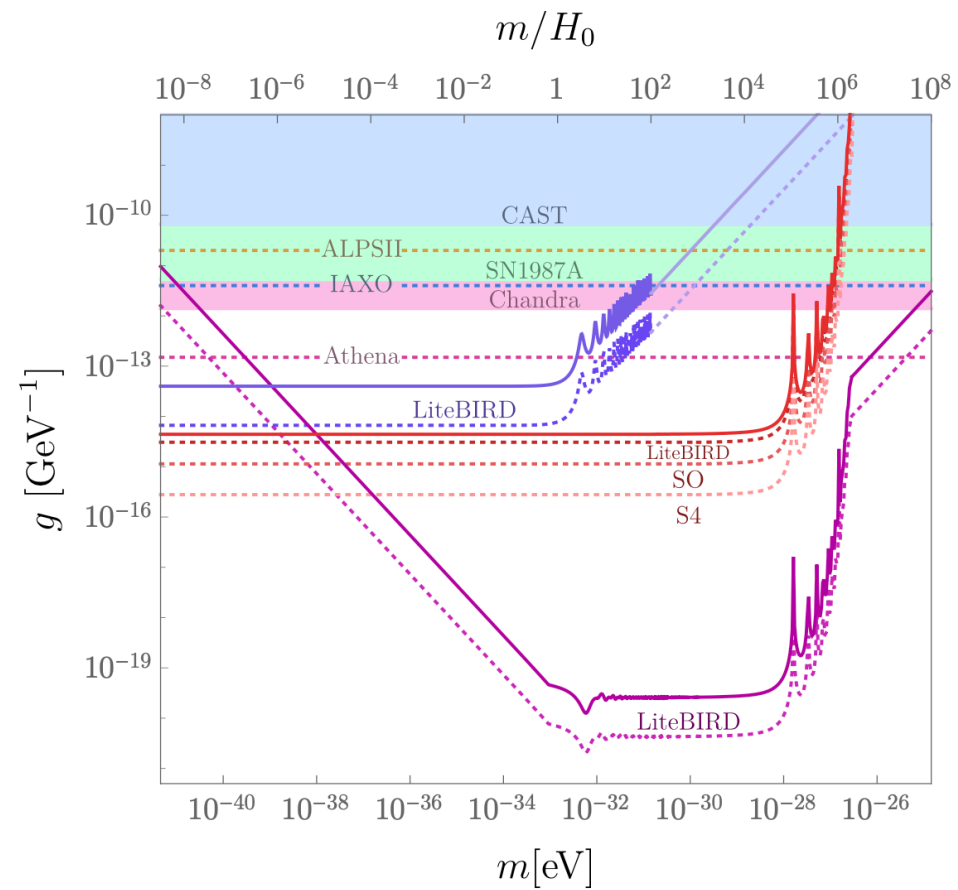
Conclusion

- Future CMB experiments investigate the broad range of axion-photon coupling, including
 - dark energy axion
 - axion with tiny energy fraction
- Detection of birefringence provides valuable information;
 - through anisotropic birefringence, we can search small-scale inflation with $r > 5 \times 10^{-9}$.
 - through isotropic rotation, we can search tiny energy fraction of axion with $\Omega_\phi h^2 \lesssim 2 \times 10^{-13}$.

[Detailed calculations in arxiv:2008.02473](https://arxiv.org/abs/2008.02473)



Backup



About CMB observation

$$\langle C^{EB,o} \rangle = \frac{\tan(4\alpha_s)}{2} (\langle C^{EE,o} \rangle - \langle C^{BB,o} \rangle) + \frac{\sin(4\alpha)}{2\cos(4\alpha_s)} (\langle C^{EE,CMB} \rangle - \langle C^{BB,CMB} \rangle)$$

α_s : rotation of polarization sensitive detector

α : cosmic birefringence

Y.Minami, et.al.(2019)