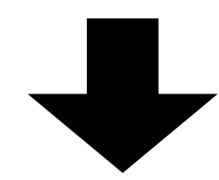
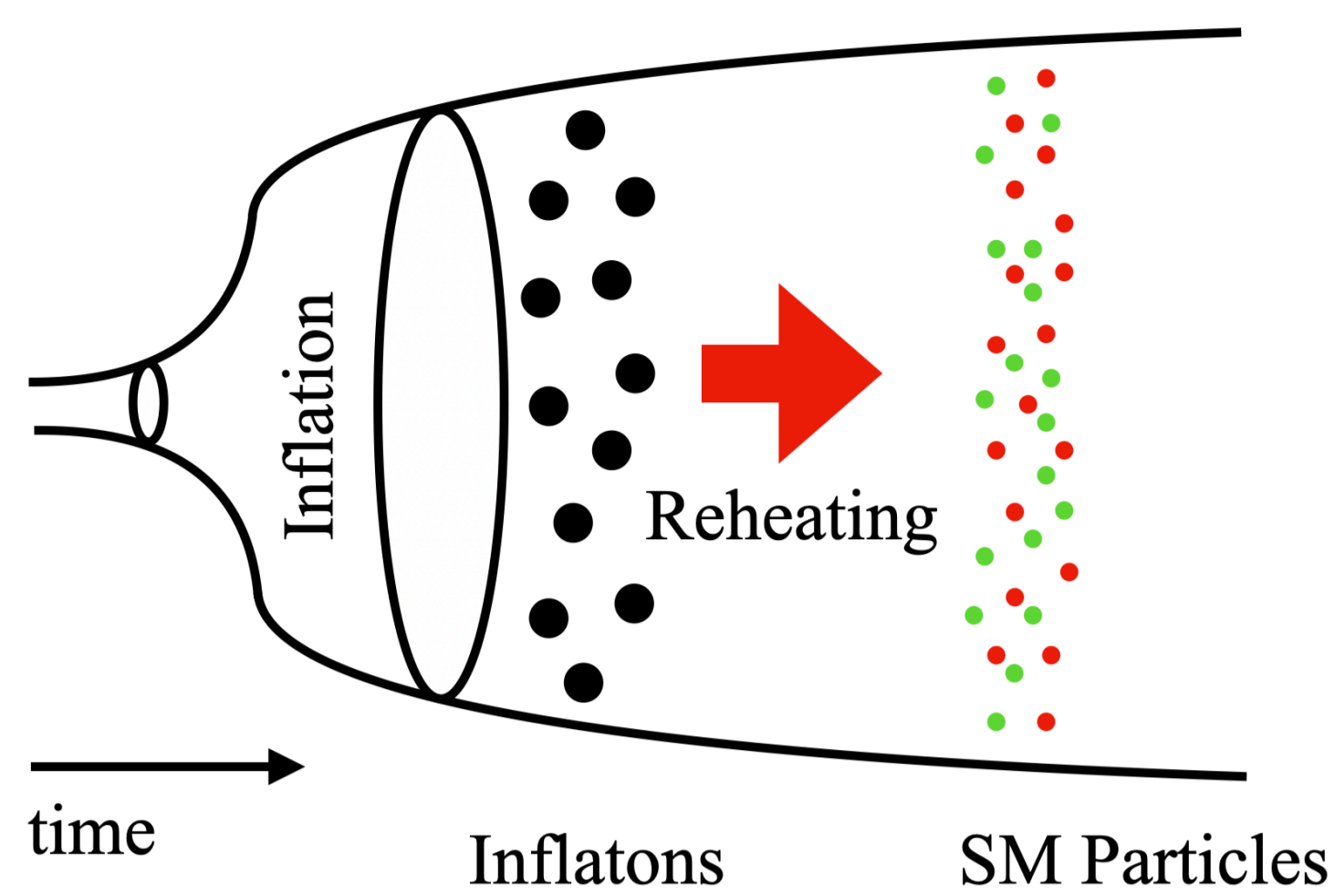


1. Introduction

To achieve a successful reheating after inflation, the inflaton must interact with Standard Model particles.



We consider a coupling to **gluon Chern-Simons term**:



$$\phi G \tilde{G}. \quad (\phi : \text{inflaton}, G : \text{gluon field strength})$$

This is a natural possibility if ϕ is an axion.

The QCD axion is needed to solve the Strong CP problem through the coupling with gluons as

$$a G \tilde{G}. \quad (a : \text{QCD axion})$$

✓ **The QCD axion can mix with the inflaton** if the Hubble parameter below the QCD scale.

✓ It is one of the candidates for Dark Matter(DM).

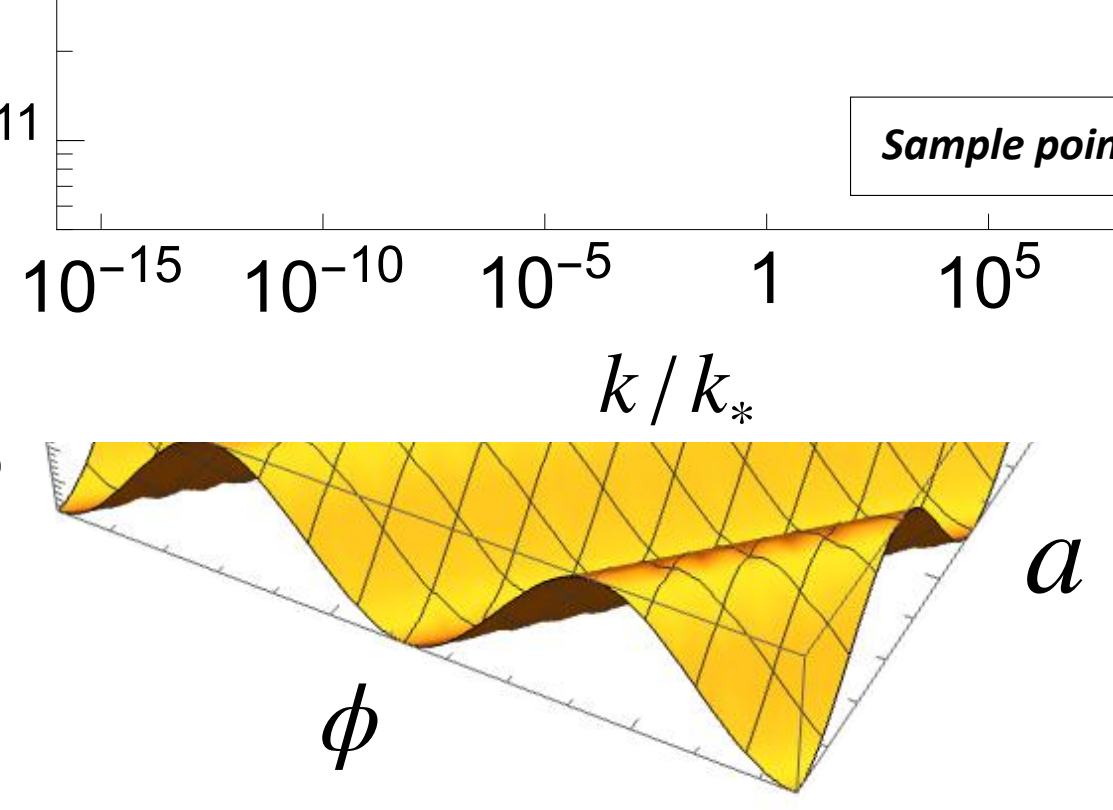
2. Setup in our model

Let us introduce an Axion-Like Particle (ALP) ϕ , which is coupled to gluons in the similar way to the QCD axion a ,

$$\mathcal{L} \supset \frac{\alpha_{st}}{8\pi} \left(\frac{a}{f_a} - n_{mix} \frac{\phi}{f_\phi} \right) G \tilde{G},$$

where n_{mix} is an integer.

Through this coupling, they acquire the QCD potential :

$$V_{\text{QCD}}(a, \phi) = \chi_0 \left[1 - \cos \left(\frac{a}{f_a} - n_{mix} \frac{\phi}{f_\phi} \right) \right], \quad V_{\text{QCD}}$$


where $\chi_0 \simeq (75.6 \text{MeV})^4$.

We also consider that the ALP has its own potential with a periodicity of $2\pi f_\phi$:

$$V_\phi(\phi) = V_\phi(\phi + 2\pi f_\phi).$$

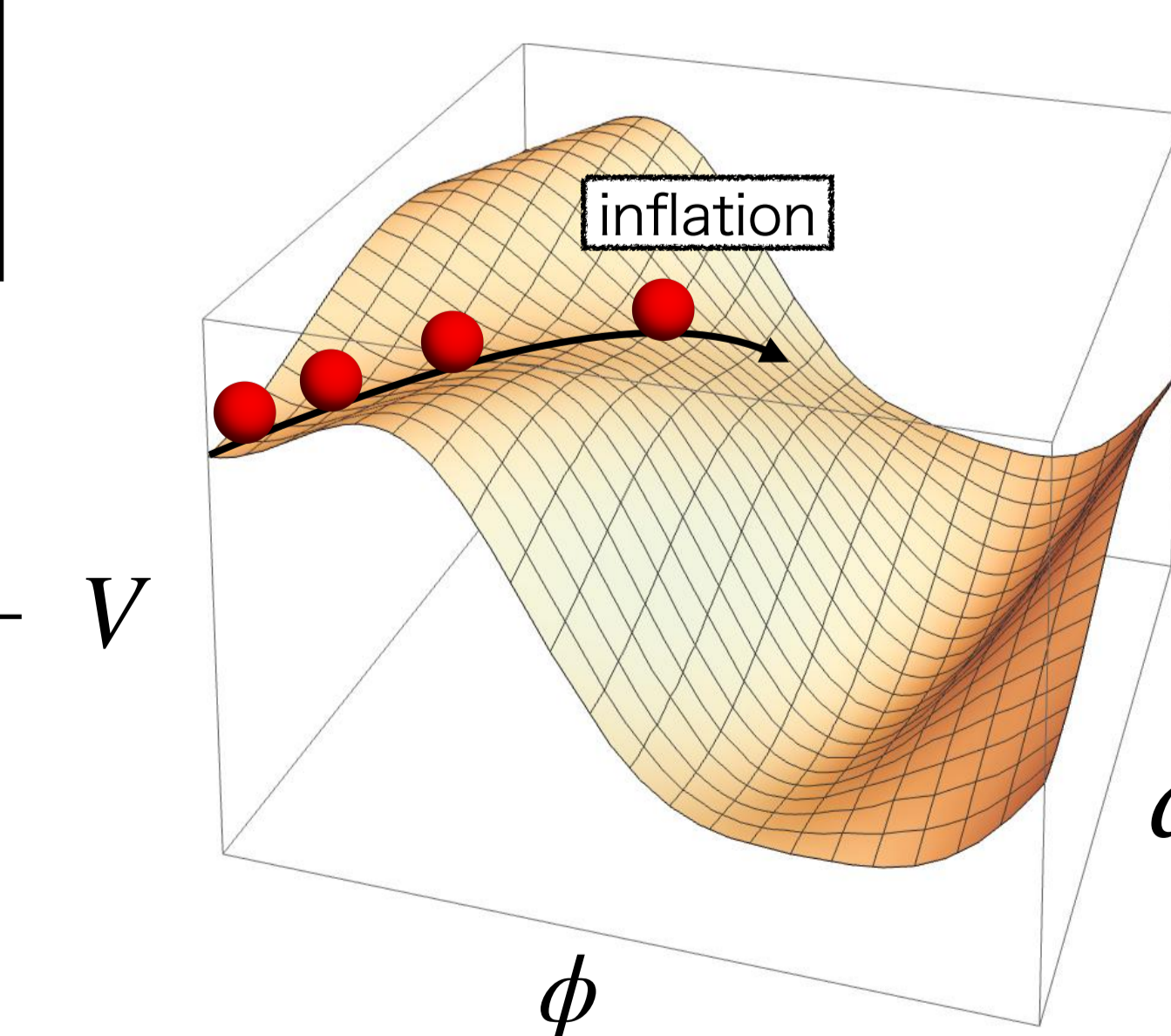
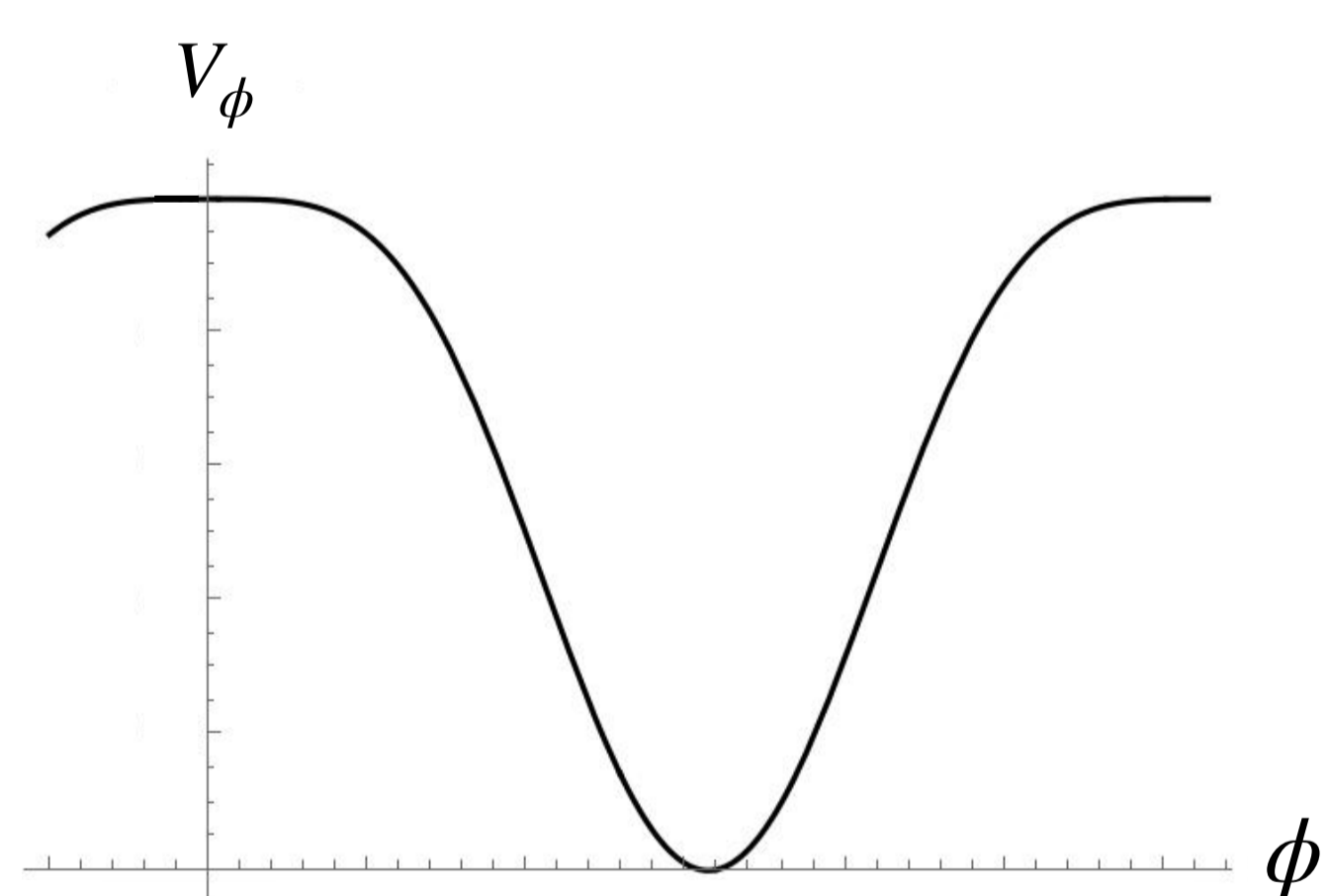
We focus on

$$V_\phi(\phi) = \Lambda^4 \left[\cos \left(\frac{\phi}{f_\phi} \right) - \frac{1}{n^2} \cos \left(n \frac{\phi}{f_\phi} \right) \right] + \text{const.},$$

where $n (> 1)$ is an even integer.

Then, the total potential is given by

$$V(a, \phi) = V_{\text{QCD}}(a, \phi) + V_\phi(\phi).$$



3. Calculation Results

We find the following parameters:

$$f_a = 5 \times 10^9 \text{GeV}, f_\phi \approx 2 \times 10^7 \text{GeV}, \Lambda \approx 18 \text{TeV}, n = 2, n_{mix} = 1,$$

which are consistent with the CMB observations.

This parameter set also explain the QCD axion DM.

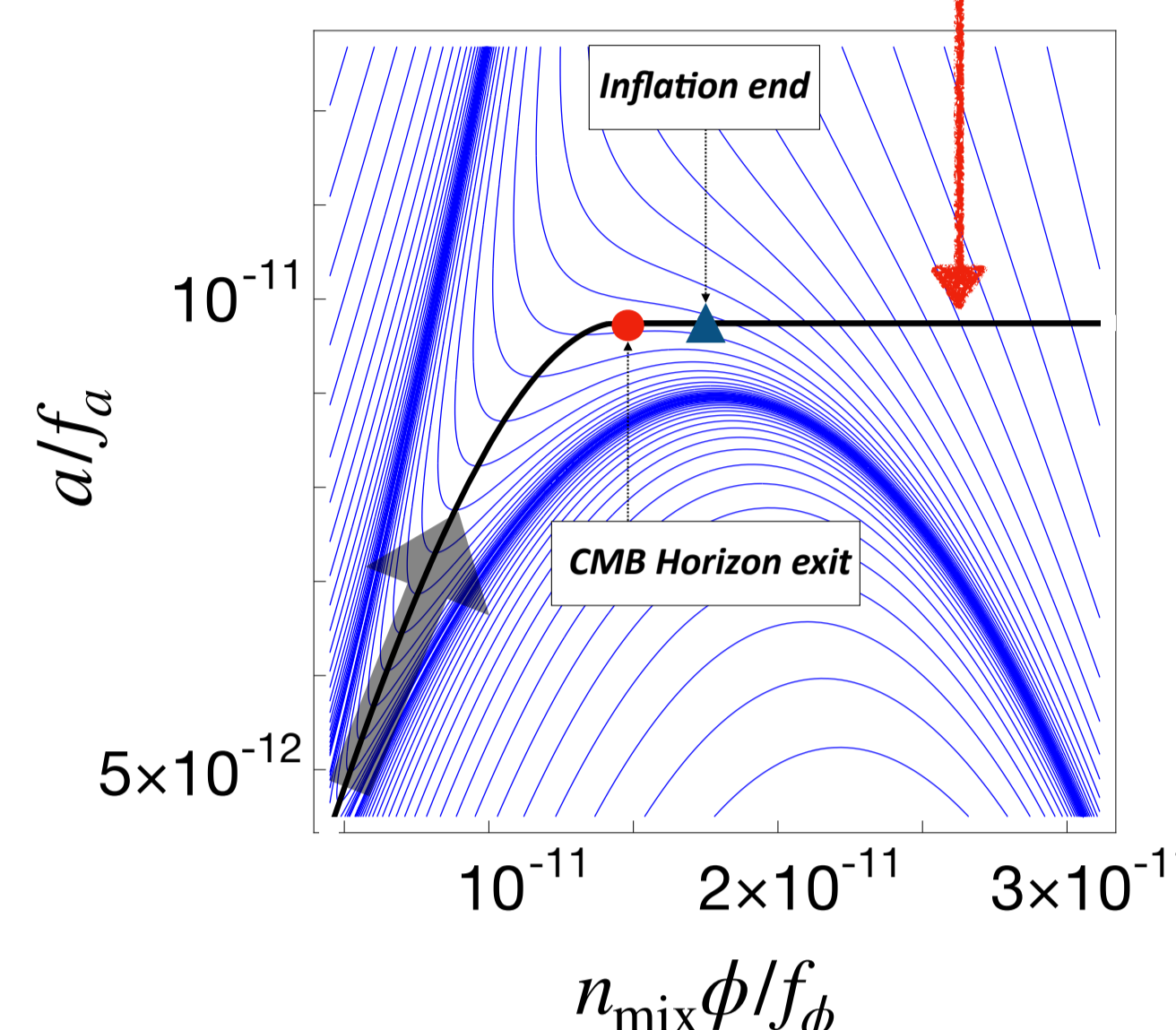
Hubble parameter

$$H_{\text{inf}} \approx 0.1 \text{eV} < \Lambda_{\text{QCD}}$$

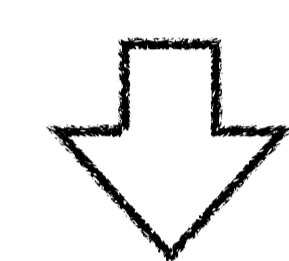
Inflationary dynamics

Trajectory

The field value of the QCD axion is frozen after inflation.



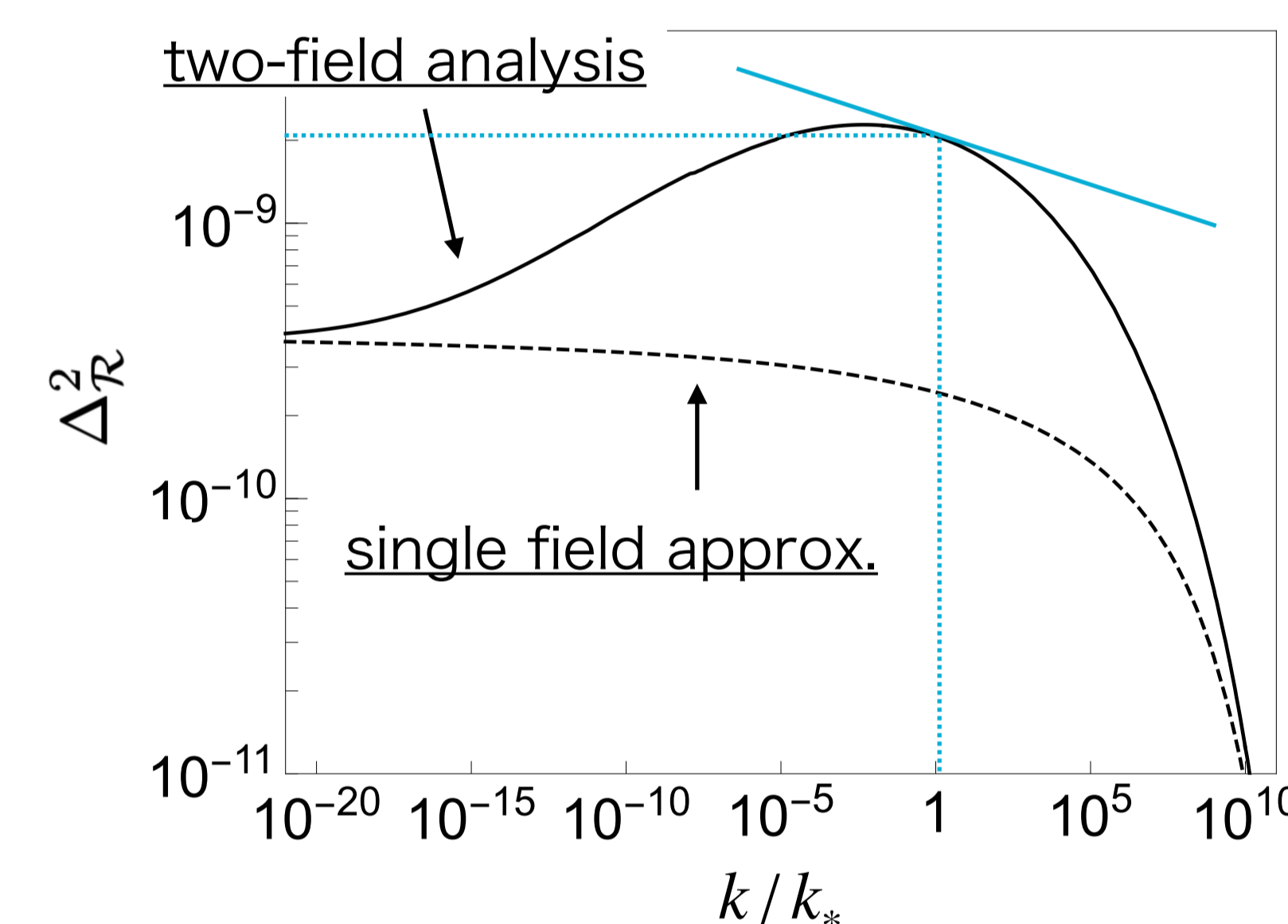
- The QCD axion drives the inflation at an early stage.
- Both mass eigenvalues are lighter than H_{inf} .



We need to consider the two-field effect.

🔍 We numerically calculate the time evolution of the both fluctuations.

Power spectrum of curvature perturbation



CMB normalization is $\Delta_R^2(k_*) \simeq 2.1 \times 10^{-9}$.

The observed spectral index is

$$n_s(k_*) \simeq 0.965.$$

- The fluctuations of both scalars affect on the power spectrum.
- This result can successfully explain the CMB data!

QCD axion abundance and DM

The QCD axion abundance generated by the misalignment mechanism is given by

$$\Omega_a h^2 \simeq 0.0092 F(\theta_i) \theta_i^2 \left(\frac{f_a}{10^{11} \text{GeV}} \right)^{1.17}, \quad \theta_i \equiv \frac{|a_i - a_{\text{min}}|}{f_a},$$

a_i is fixed!

where the function $F(\theta_i)$ is

$$F(\theta_i) \equiv \left[\log \left(\frac{e}{1 - \theta_i^2/\pi^2} \right) \right]^{1.17},$$

In this case, $f_a = 5 \times 10^9 \text{GeV}$, $a_{\text{min}} = \pi$, and $\theta_i \sim \pi - 10^{-11}$.

So, we can estimate the QCD axion abundance: $\Omega_a h^2 \sim 0.12$.

➡ The QCD axion explains all DM!

Summary

- Through the detailed analysis of the two axion fields, we have identified the viable parameters and shown that the QCD axion can be not only the inflaton but also DM.
- This scenario can be probed in the axion direct search experiments such as IAXO, and in future CMB and BAO experiments.
- Also, The ALP ϕ may probed by future accelerator experiments.
- Interestingly, we can solve the quality problem of Peccei-Quinn symmetry by the requirement of successful inflation and the axion DM bound.