

# Classification of simple heavy vector triplet models

Ryo Nagai

( Nagoya U. )

based on

RN and T. Abe arXiv: 1607.03706 [hep-ph]

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# Extra spin-1 particles ( $V'$ )

## Well-motivated

- Various BSM predict them.
  - \* Extension of gauge sym  $\rightarrow$   $W'/Z'$  boson
  - \* New dynamics  $\rightarrow$   $\rho'$  resonance
- Their mass scale is expected to be around TeV scale.

# Extra spin-1 particles (V')

## There are many models



- Radindra-Mohapatra-Pati (1974)
- Mohapatra-Pati (1974)
- Barger-Keung-Ma (1980)
- Mohapatra-Senjanovic (1980)
- Bando-Kugo-Yamawaki (1987)
- Agashe-Davoudiasl-Gopalakrishna-Han-Huang-Perez-Si-Soni (2007)
- Agashe-Gopalakrishna-Han-Huang-Soni (2009)
- Agache-Azatov-Han-Li-Si-ZHu (2010)
- Contino-Pappadopulo-Marzocca-Rattazzi (2011)
- Abe-Kitano (2013)

## Ryo Nagai (Nagoya U.)

# Extra spin-1 particles ( $V'$ )

## There are many models



## Can we identify the $V'$ model if $V'$ is discovered in the future ?

## The classification of $V'$ models is important.

Ryo Nagai (Nagoya U.)

# Contents

- ❖ Introduction
- ❖ Classification of  $V'$  models
- ❖ Explicit models
- ❖ Summary

# Our strategy

We focus on the ratio:

$$R = \frac{\Gamma(V' \rightarrow ff)}{\Gamma(V' \rightarrow VV)}$$

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$$R = \frac{\Gamma(V' \rightarrow ff)}{\Gamma(V' \rightarrow VV)} \simeq 4N_c \frac{\tilde{\zeta}_f^2}{\tilde{\zeta}_V^2}$$

Two important parameters:

$$g_{V'ff} = -\tilde{\zeta}_f g_{Vff} \qquad g_{V'VV} = \tilde{\zeta}_V g_{VVV} \frac{m_V^2}{m_{V'}^2}$$

$V'ff$  coupling

$V'VV$  coupling

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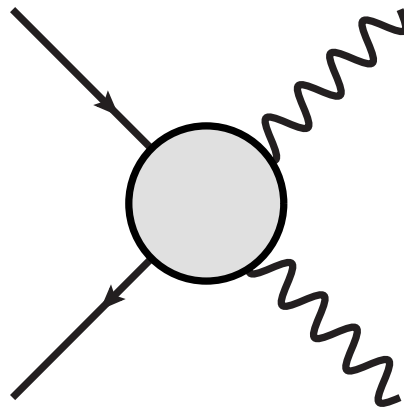
$$g_{V'ff} = -\tilde{\zeta}_f g_{Vff} \quad g_{V'VV} = \tilde{\zeta}_V g_{VVV} \frac{m_V^2}{m_{V'}^2}$$

Let us impose perturbative unitarity and custodial symmetry  
in the  $V'$  models.



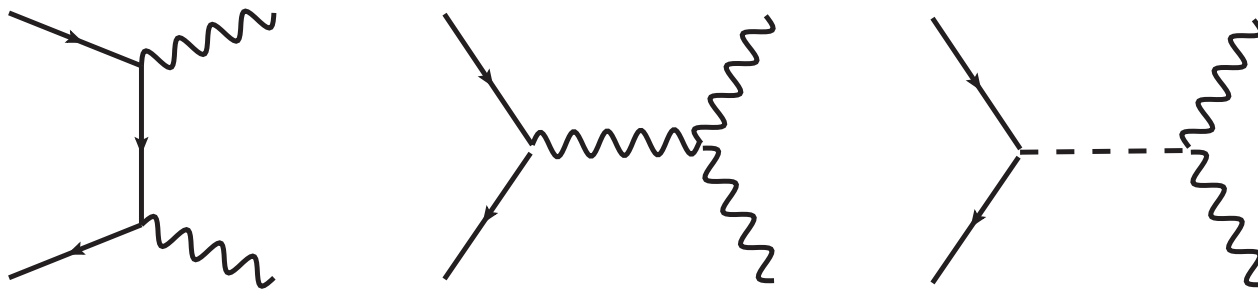
# $V'$ and perturbative unitarity

Let us focus on vector / fermion scattering



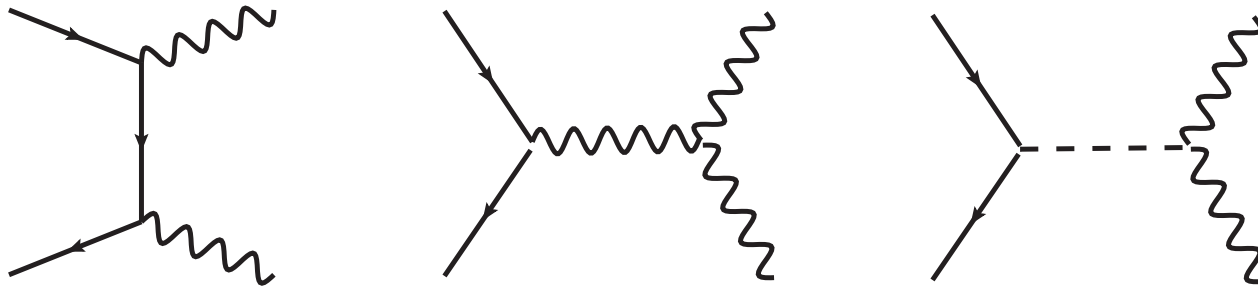
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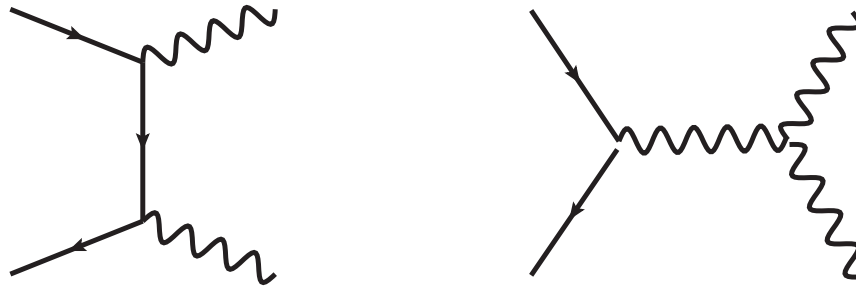
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$$\mathcal{M} \simeq A \frac{E^2}{m^2} + B \frac{E}{m}$$

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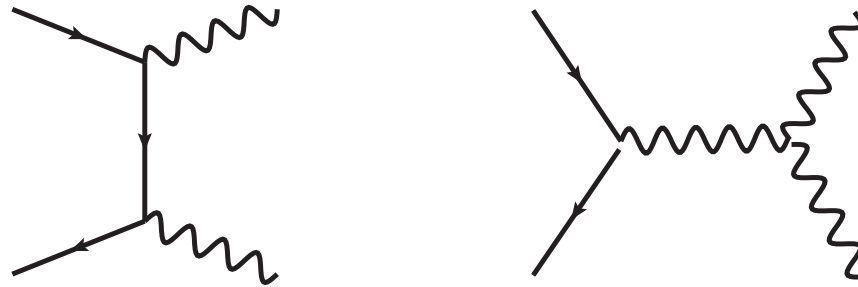


Requiring  $A = 0$  in  $ff \rightarrow VV$ , we obtain

$$g_{Vff}^2 = g_{Vff}g_{VVV} + g_{V'ff}g_{V'VV}$$

# V' and perturbative unitarity

Let us focus on vector / fermion scattering  $\mathcal{M} \simeq A \frac{E^2}{m^2} + B \frac{E}{m}$



Requiring  $A = 0$  in  $ff \rightarrow VV, VV', V'V'$ , we obtain

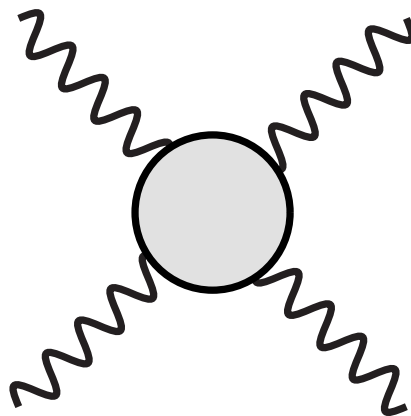
$$\zeta_V = \frac{1}{\zeta_f} \frac{g_{VVV} - g_{Vff} \frac{m_{V'}^2}{m_V^2}}{g_{VVV}} \quad \begin{aligned} g_{V'ff} &= -\zeta_f g_{Vff} \\ g_{V'VV} &= \zeta_V g_{VVV} \frac{m_V^2}{m_{V'}^2} \end{aligned}$$

$\nearrow$   $\zeta_V$   $\swarrow$ 
 $\zeta_f$   $\nwarrow$

$V'VV$  coupling
 $V'ff$  coupling

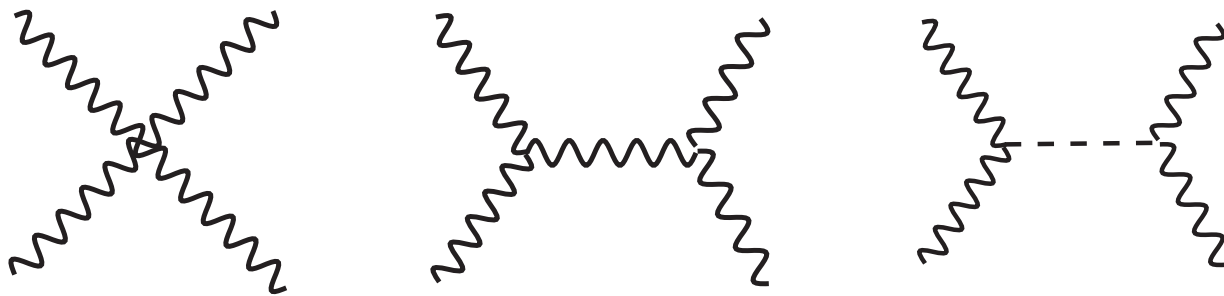
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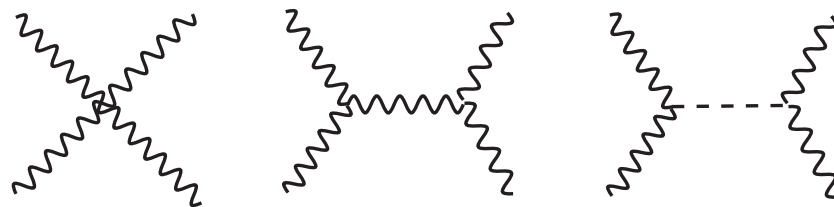
Let us next focus on vector scattering



$$\mathcal{M} \simeq C \frac{E^4}{m^4} + D \frac{E^2}{m^2}$$

# $V'$ and perturbative unitarity

Let us next focus on vector scattering



The image shows three Feynman diagrams for vector scattering. The first diagram is a contact interaction where four wavy lines meet at a central point. The second diagram is a t-channel exchange where two wavy lines enter from the left and two exit to the right, connected by a wavy line in the middle. The third diagram is a t-channel exchange where two wavy lines enter from the left and two exit to the right, connected by a dashed line in the middle. To the right of these diagrams is the equation  $\simeq C \frac{E^4}{m^4} + D \frac{E^2}{m^2}$ .

- “D” in  $VV \rightarrow VV, VV', V'V'$  depend on Higgs couplings.
- From  $D = 0$  in  $VV \rightarrow V'V'$ , we find some relations which are independent from custodial singlet Higgs coupling.



# $V'$ and perturbative unitarity

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$$\tilde{\zeta}_V^- = -\frac{1}{\tilde{\zeta}_f} \left[ 1 - (1 - \tilde{\zeta}_f^{-2}) \frac{m_V^2}{m_{V'}^2} \right]^{-1}$$

$$g_{V'ff} = -\tilde{\zeta}_f g_{Vff} \quad g_{V'VV} = \tilde{\zeta}_V g_{VVV} \frac{m_V^2}{m_{V'}^2}$$

\* Here we assume there is no scalars other than custodial singlets

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$$R \simeq 4N_c^2$$

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$V'$  mainly decays into  
Fermion  
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Boson  
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# Summary so far

What we found:

- $V'$  models are classified into 2 categories

This is only based on the unitarity argument,  
not rely on specific models.

$$\xi_V^+ = \xi_f \left[ 1 - (1 - \xi_f^2) \frac{m_V^2}{m_{V'}^2} \right]^{-1}$$

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$$\xi_V^- = -\frac{1}{\xi_f} \left[ 1 - (1 - \xi_f^{-2}) \frac{m_V^2}{m_{V'}^2} \right]^{-1}$$

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Boson  
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# Summary so far

What we found:

- $V'$  models are classified into 2 categories

This is only based on the unitarity argument,  
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Next to do:

- To find bench-mark models in each categories

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# Strategy

We focus on

- $SU(2)_0 \times SU(2)_1 \times U(1)_2$  gauge model
- Renormalizable
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The models contains at least two scales (two VEVs)

- Models with two VEVs

# Model 1

$$SU(2)_0 \times SU(2)_1 \times U(1)_2 \rightarrow U(1)_{EM}$$

	$SU(2)_0$	$SU(2)_1$	$U(1)_2$
$q_L$	<b>1</b>	<b>2</b>	1/6
$u_R$	<b>1</b>	<b>1</b>	2/3
$d_R$	<b>1</b>	<b>1</b>	- 1/3
$l_L$	<b>1</b>	<b>2</b>	- 1/2
$e_R$	<b>1</b>	<b>1</b>	- 1
$H_1$	<b>2</b>	<b>2</b>	0
$H_2$	<b>1</b>	<b>2</b>	1/2

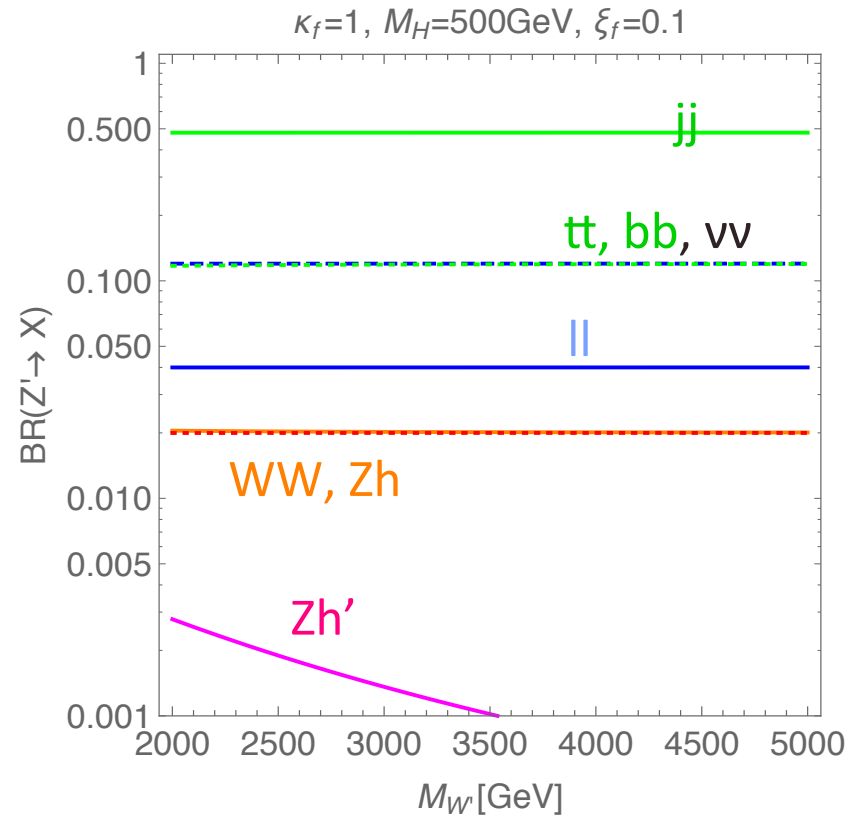
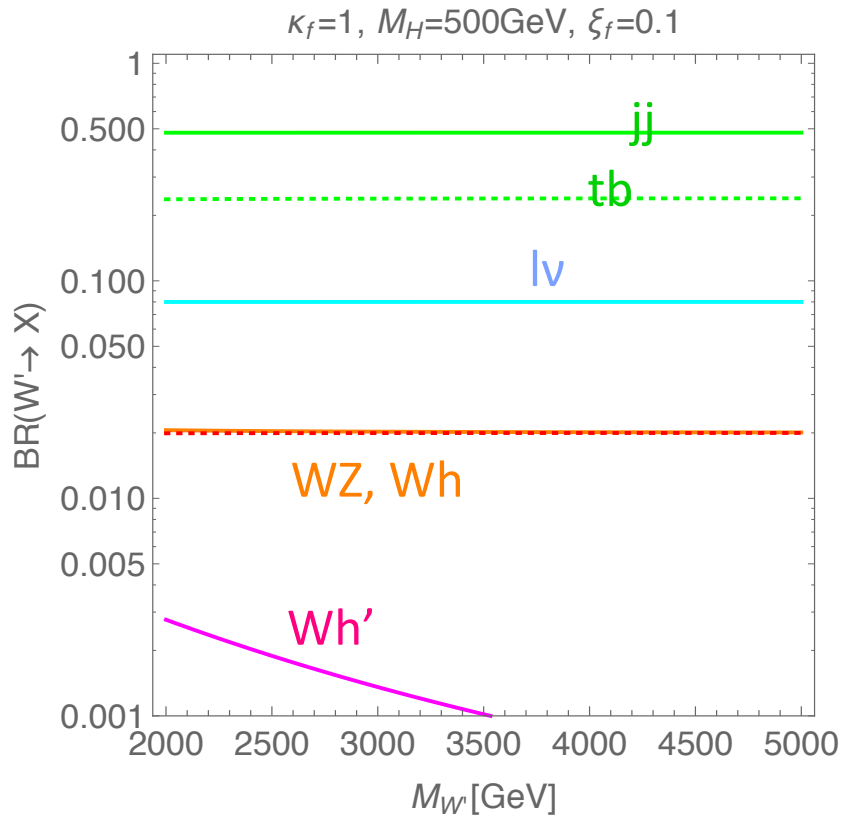
Barger-Keung-Ma (1980)  
Pappadopulo-Thamm-Torre-Wulzer (2014)

- New particles
  - One CP-even scalar:  $h'$
  - New vectors:  $W', Z'$
- $V'VH$  coupling is suppressed

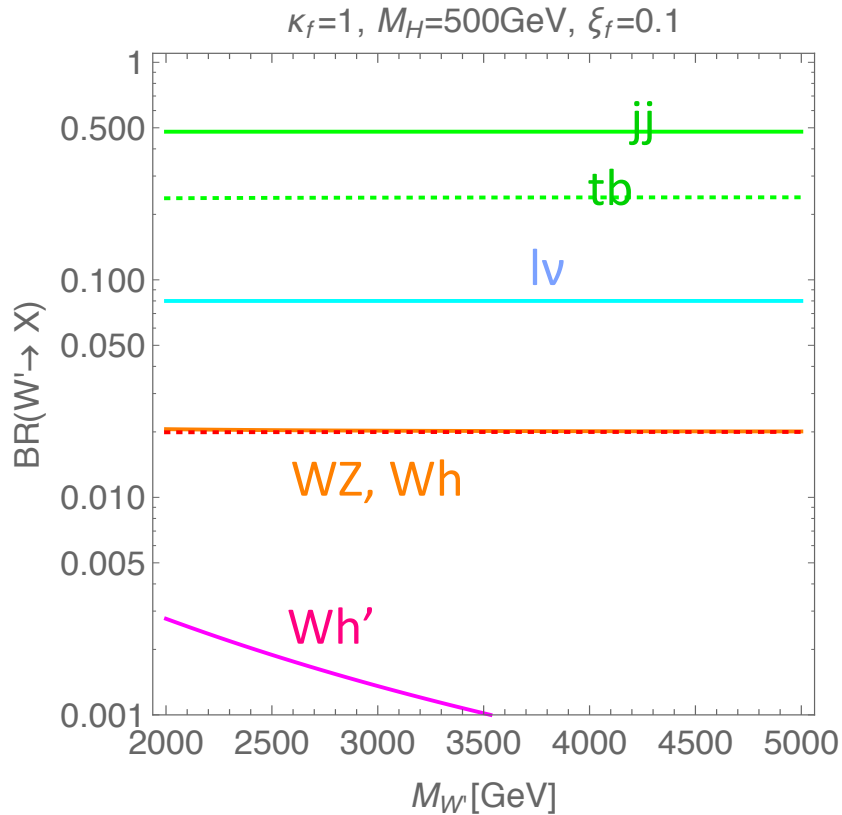
$$\left| \frac{g_{W'Wh'}}{g_{WWH}} \right| \sim \mathcal{O}(0.01)$$

- $BR(V' \rightarrow VH)$  is suppressed even for  $m_H < m_{V'}$

# BR of $W'/Z'$



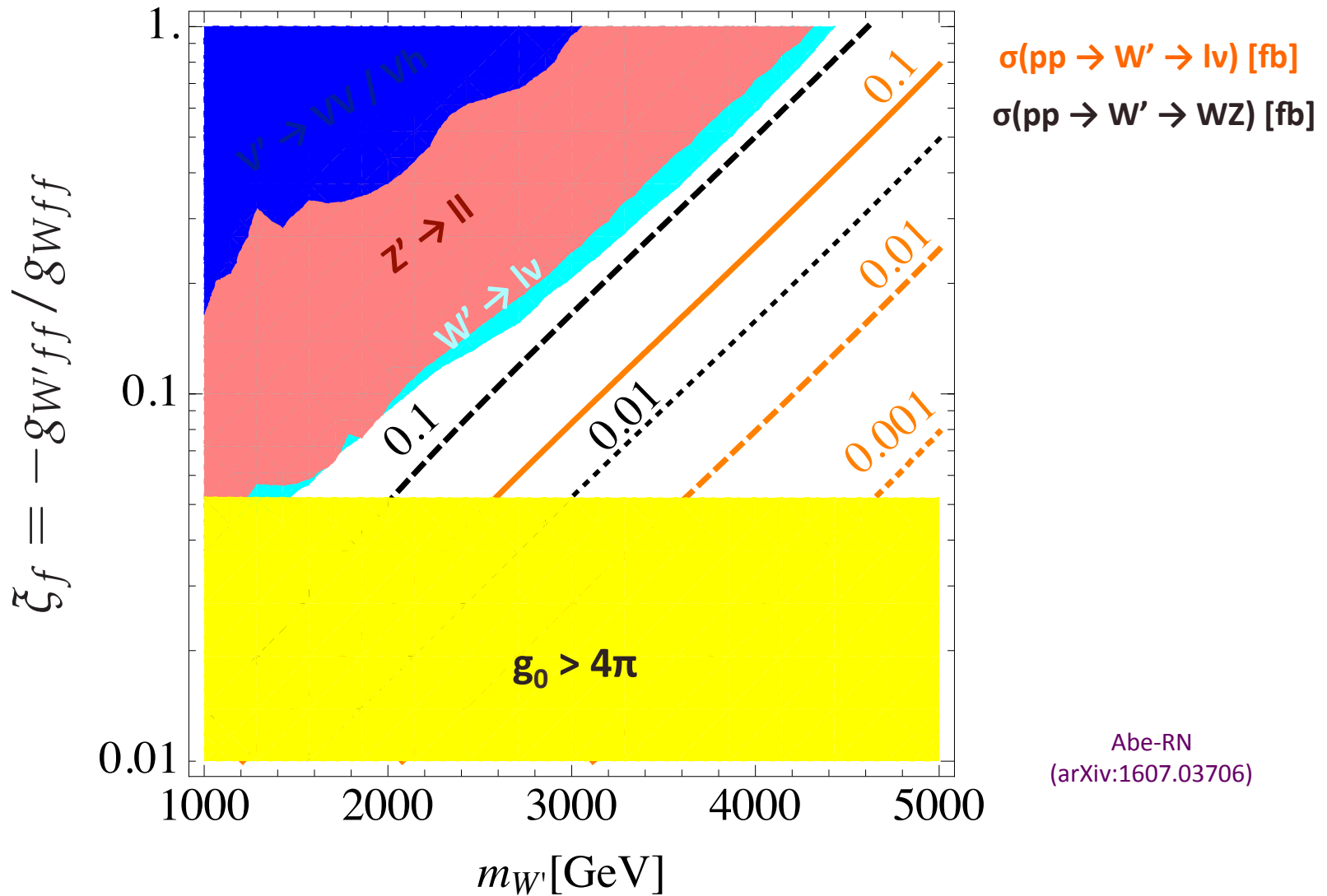
# BR of $W'/Z'$



This model falls into  
type-F

- $V'$  mainly decays into fermions

# LHC constraint



Abe-RN  
(arXiv:1607.03706)

# Strategy

We focus on

- $SU(2)_0 \times SU(2)_1 \times U(1)_2$  gauge model
- Renormalizable
- without extra fermions

The models contains at least two scales (two VEVs)

- Models with two VEVs
- Models with three VEVs

# Model 2

$$SU(2)_0 \times SU(2)_1 \times U(1)_2 \rightarrow U(1)_{EM}$$

	$SU(2)_0$	$SU(2)_1$	$U(1)_2$
$q_L$	<b>2</b>	<b>1</b>	1/6
$u_R$	<b>1</b>	<b>1</b>	2/3
$d_R$	<b>1</b>	<b>1</b>	- 1/3
$l_L$	<b>2</b>	<b>1</b>	- 1/2
$e_R$	<b>1</b>	<b>1</b>	- 1
$H_1$	<b>2</b>	<b>2</b>	0
$H_2$	<b>1</b>	<b>2</b>	1/2
$H_3$	<b>2</b>	<b>1</b>	1/2

Abe-Kitano (2013)

- New particles:

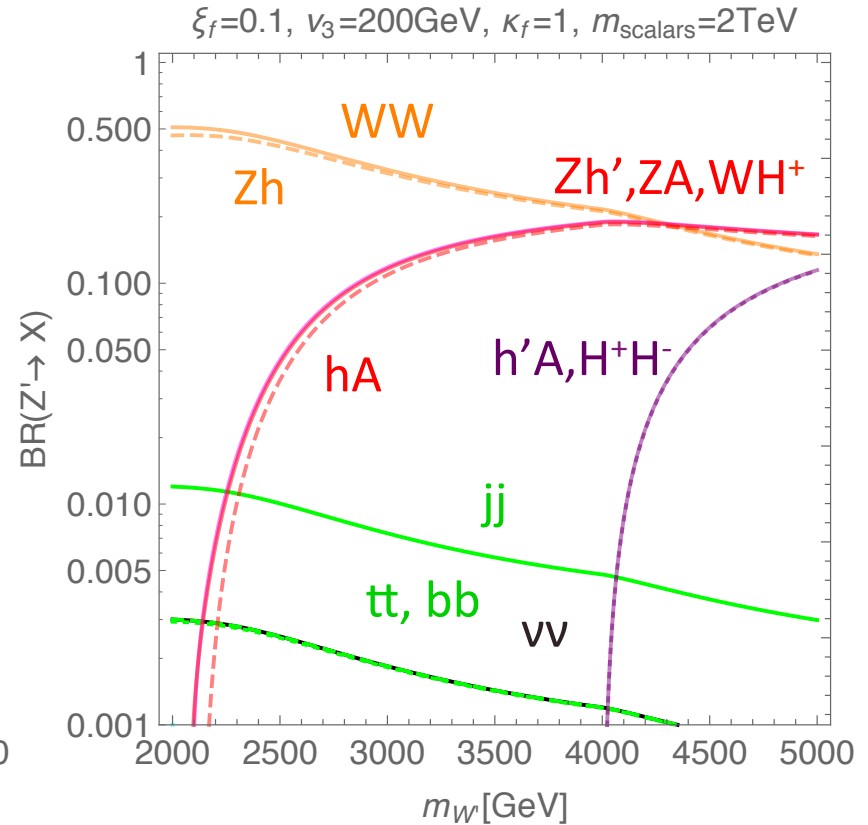
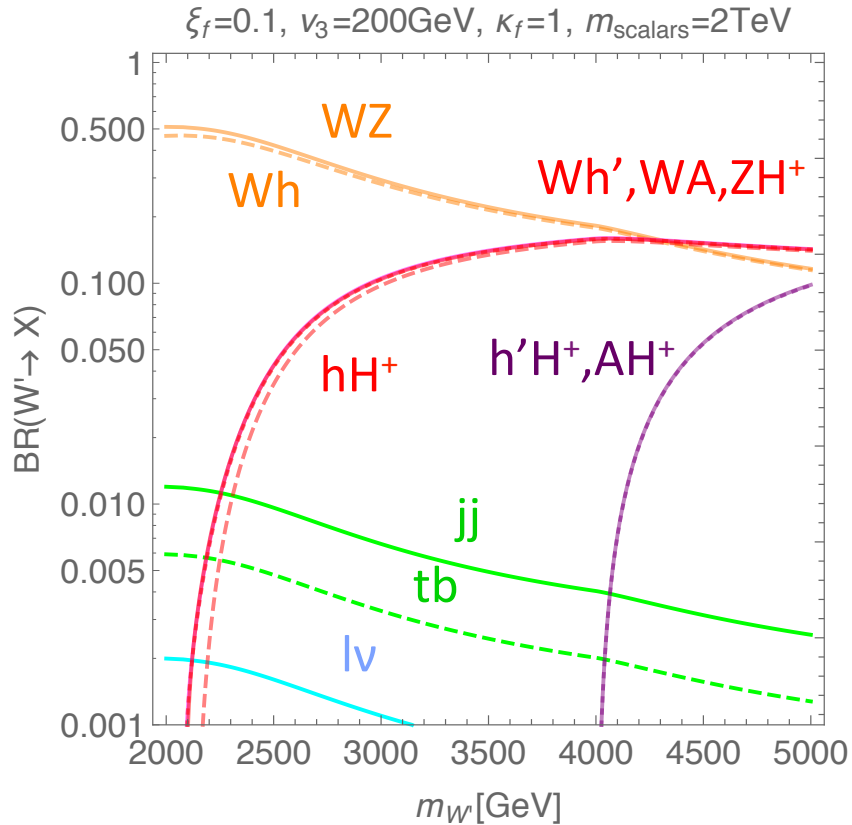
- Two CP-even scalars:  $h', h''$
- One CP-odd scalar:  $A$
- One charged scalar:  $H^\pm$
- New vectors:  $W', Z'$

- $V'VX$  ( $X$ : heavy scalars) couplings are not suppressed

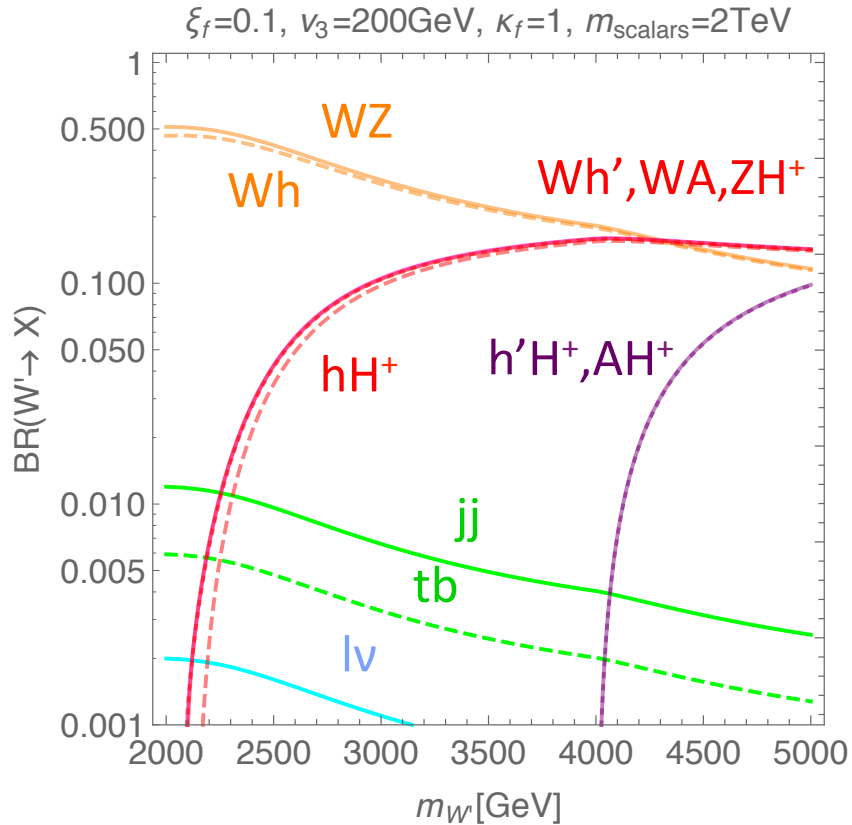
$$\left| \frac{g_{W'Wh'}}{g_{WWh}} \right| \sim 5$$



# BR of $W'/Z'$



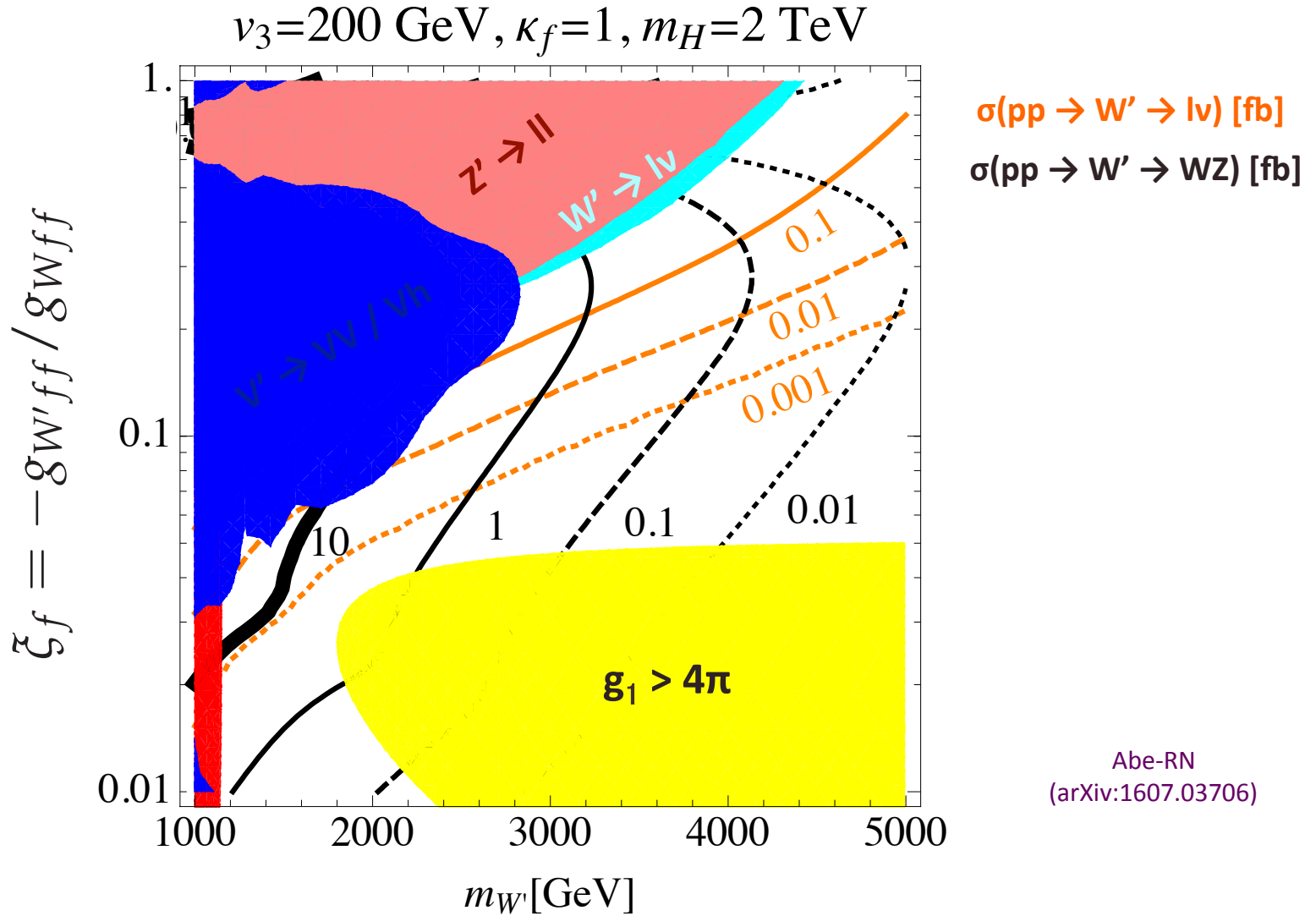
# BR of $W'/Z'$



This model falls into  
type-B

- $V'$  mainly decays into bosons

# LHC constraint



Abe-RN  
(arXiv:1607.03706)

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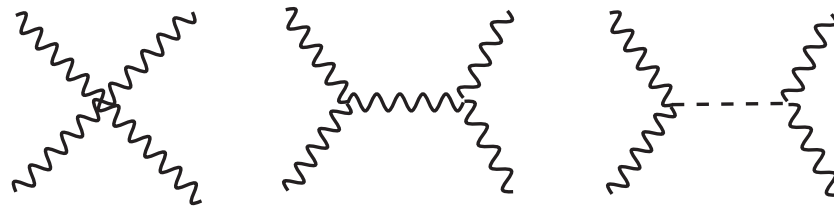
# Summary

- We classify  $V'$  models in model-independent manner.  
focusing on their dominant decay mode
- We find two categories, Type-F ( $V'$  mainly decays into fermions) and Type-B ( $V'$  mainly decays into bosons).
- Scalars other than custodial singlets are needed for renormalizable type-B models.

BACK UP SLIDES

# V' and perturbative unitarity

Let us next focus on vector scattering



$$\simeq C \frac{E^4}{m^4} + D \frac{E^2}{m^2}$$

- Requiring  $D = 0$  in  $VV \rightarrow VV, VV', V'V'$ , we find some relations which are **independent from custodial singlet Higgs coupling**.

$$\frac{(m_V^2 - m_{V'}^2)^2}{m_V^2} g_{V'VV}^2 + \frac{(m_V^2 - m_{V'}^2)^2}{m_{V'}^2} g_{V'V'V}^2 - m_V^2 (g_{V'VV}^2 - g_{VVV} g_{V'V'V}) - m_{V'}^2 (g_{V'V'V}^2 - g_{V'VV} g_{V'V'V'}) = - \sum_{\Delta} g_{VV'\Delta}^2$$

# Classification of $V'$

We find two solutions.

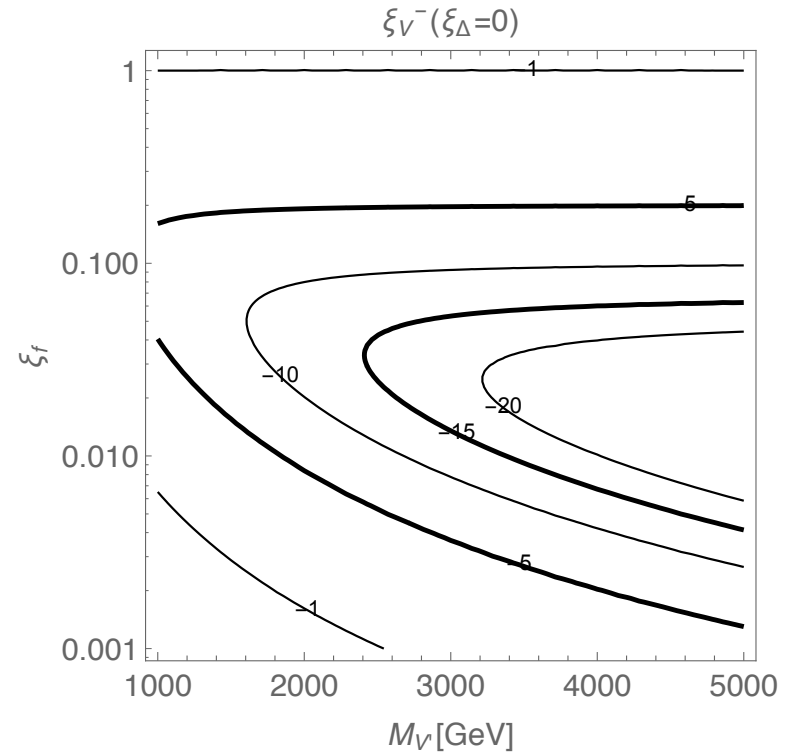
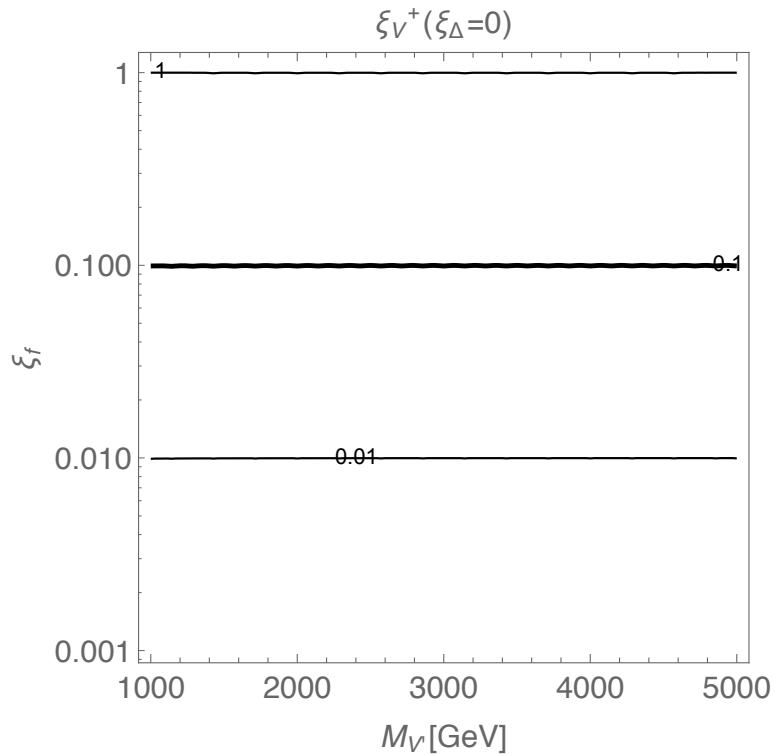
$$\tilde{\zeta}_V^\pm = -\tilde{\zeta}_f \frac{\left( 2(1-r^2)(1-2r^2)(1-\tilde{\zeta}_f^2) - \frac{r^2\tilde{\zeta}_f^2(1+\tilde{\zeta}_f^2)^2\tilde{\zeta}_\Delta^2}{r^2+\tilde{\zeta}_f^2} \right) \pm \left( -2(1-r^2)(1+\tilde{\zeta}_f^2)\sqrt{1-\tilde{\zeta}_\Delta^2} \right)}{4(1-r^2)(\tilde{\zeta}_f^2 + r^2(1-r^2)(1-\tilde{\zeta}_f^2)^2) + \frac{r^4\tilde{\zeta}_f^4(1+\tilde{\zeta}_f^2)^2\tilde{\zeta}_\Delta^2}{r^2+\tilde{\zeta}_f^2}}$$

where

$$r = \frac{m_V^2}{m_{V'}^2} \quad \text{and} \quad \sum_{\Delta} g_{VV'\Delta}^2 = \frac{1}{4} g_{Vff}^2 \frac{m_V^2 m_{V'}^2}{m_V^2 + m_{V'}^2 \tilde{\zeta}_f^2} (1 + \tilde{\zeta}_f^2)^2 \tilde{\zeta}_\Delta^2$$

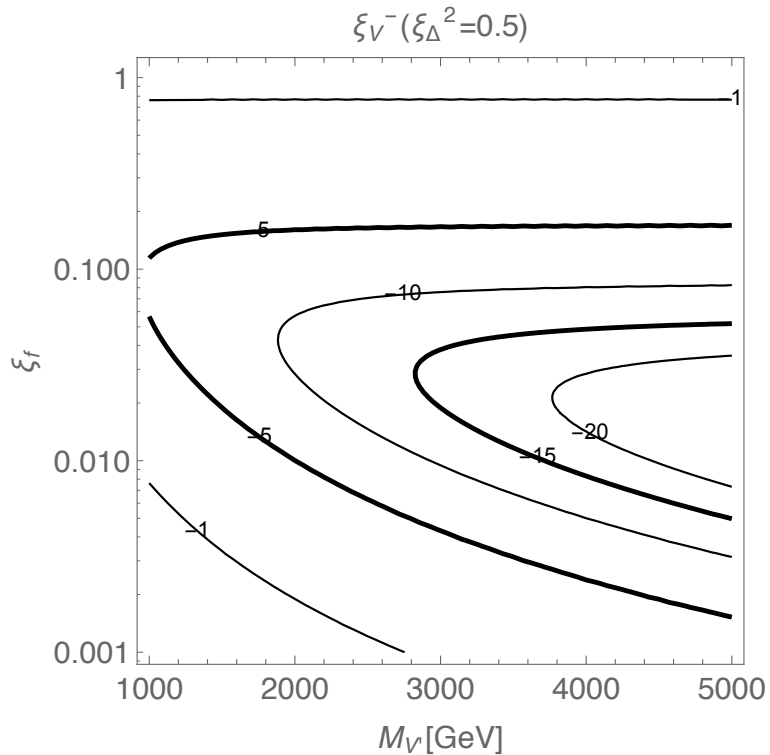
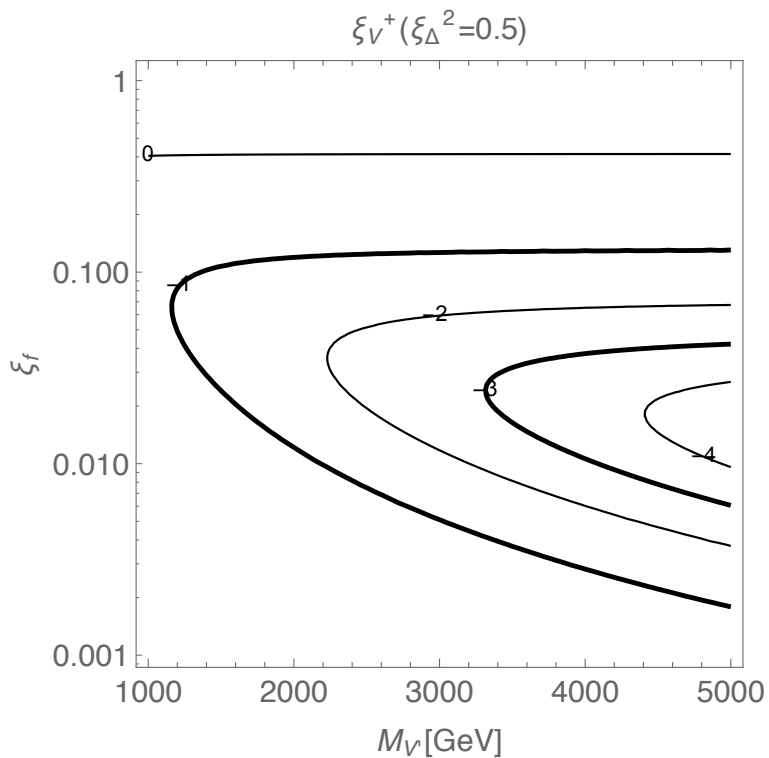


# Classification of $V'$



$\xi_{\Delta}$  :  $V'V\Delta$  coupling ( $|\xi_{\Delta}| \leq 1$ )

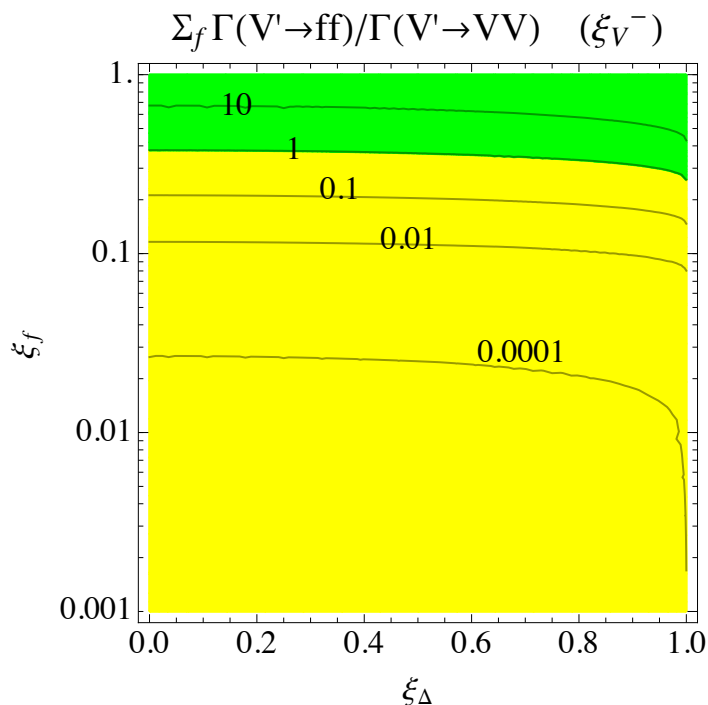
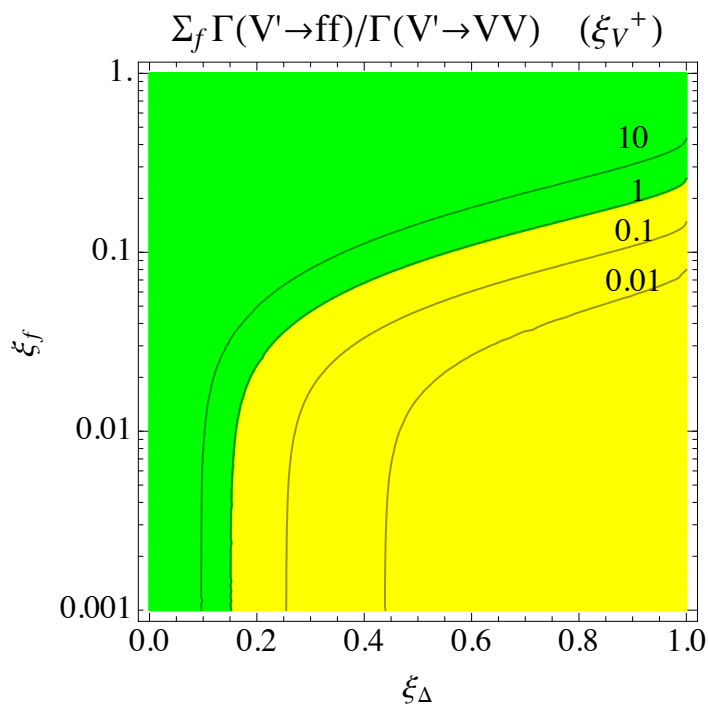
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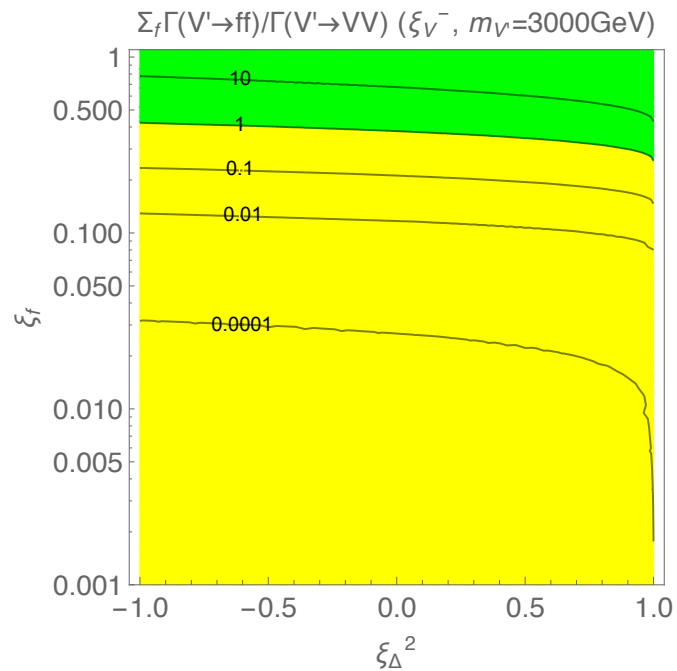
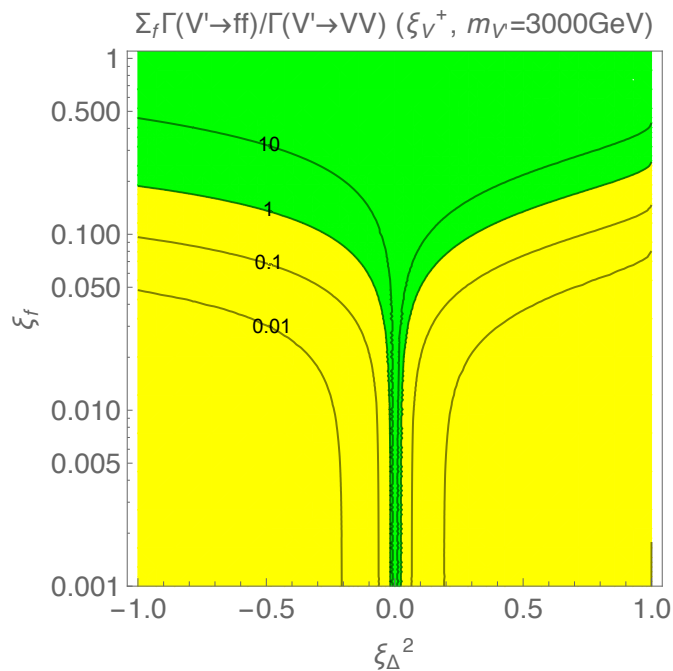
Remark If triplets ( $\Delta$ ) exist,  $\xi_V$  depends on  $V'V\Delta$  coupling



- If  $\xi_\Delta$  is non-zero, our classification still valid.  $\xi_\Delta$  :  $V'V\Delta$  coupling ( $|\xi_\Delta| \leq 1$ )

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