

09/02/2020

Progress of Particle Physics

# Physics beyond the standard model from Higgs Parity

Keisuke Harigaya

(Institute for Advanced Study)

Hall and KH :[1803.08119](#), [1905.12722](#)

Dunsky, Hall and KH :[1902.07726](#), [1908.02756](#)

# Particle physics

is trying to answer questions such as

- \* What are **the fundamental laws** of physics?

Particles, interactions among them, ...

- \* How did our **universe** begin and evolve?

Inflation, cosmic perturbations,  
baryon asymmetry, dark matter, ...

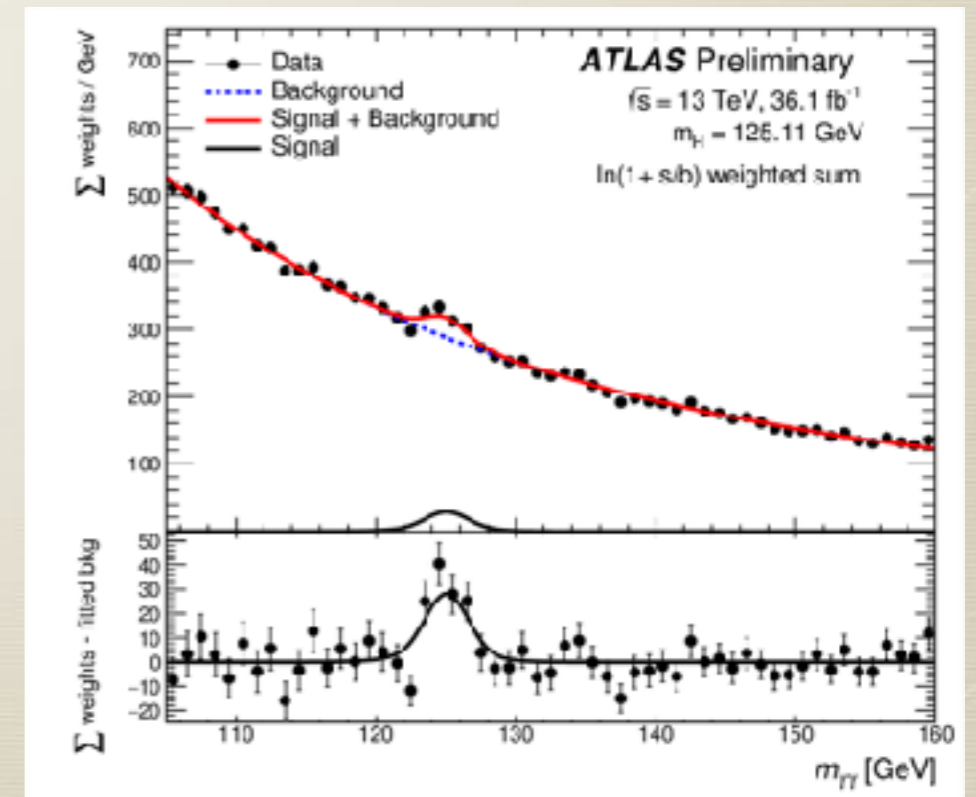
# Standard Model

	1st	2nd	3rd	
<b>Quarks</b>	$u$ up	$C$ charm	$t$ top	<b>Gauge Bosons</b>
	$d$ down	$S$ strange	$b$ beauty	
	$e$ electron	$\mu$ muon	$\tau$ tau	
<b>Leptons</b>	$\nu_e$ neutrino electron	$\nu_\mu$ neutrino muon	$\nu_\tau$ neutrino tau	
				$W^\pm$ W boson
				$Z^0$ Z boson
			$g$ gluon	
			$H$ Higgs Boson	

figure from [www.physik.uzh.ch](http://www.physik.uzh.ch)



Events



Invariant mass

# Precise measurements

- \* Higgs mass  $m_h = 125.18 \pm 0.16$  GeV
- \* Top quark mass  $m_t = 173.1 \pm 0.4$  GeV
- \* Strong coupling constant  $\alpha_s(m_Z) = 0.1184 \pm 0.0011$
- \* ...

Can we learn something beyond the Standard Model ?

nature of dark matter, mass of new particles, rare decays, etc.

# Precise measurement and new physics

Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)

New symmetry  
Higgs Parity

- \* is part of a grand unified gauge symmetry
- \* solves the strong CP problem
- \* gives a dark matter candidate

# Precise measurement and new physics

Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)

top quark mass  
Higgs mass  
strong coupling constant



Higgs Parity  
symmetry  
breaking scale

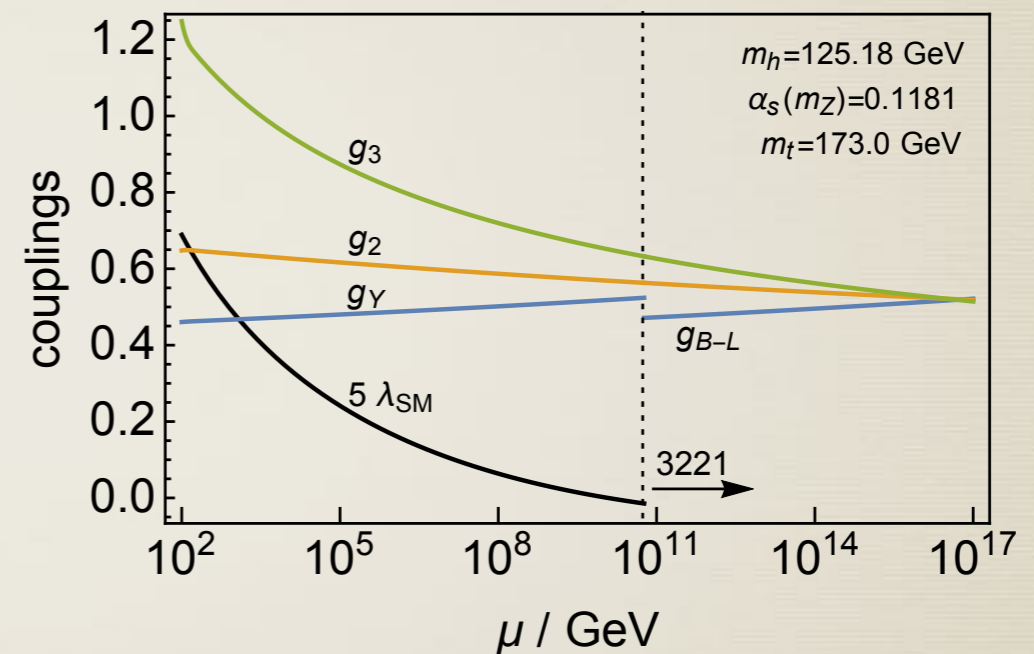
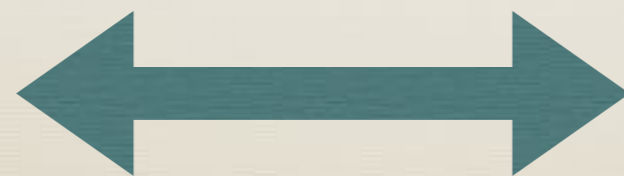
# Precise measurement and new physics

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top quark mass  
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Higgs Parity  
symmetry  
breaking scale



UV physics,  
experimental signatures  
Grand unification, proton decay

Dark matter detection rate, neutron EDM,  
gravitational waves, dark radiation, warm dark matter, ...

# Outline

- \* Introduction (continued)
- \* Higgs Parity
- \* Grand unification and proton decay
- \* Summary and outlook



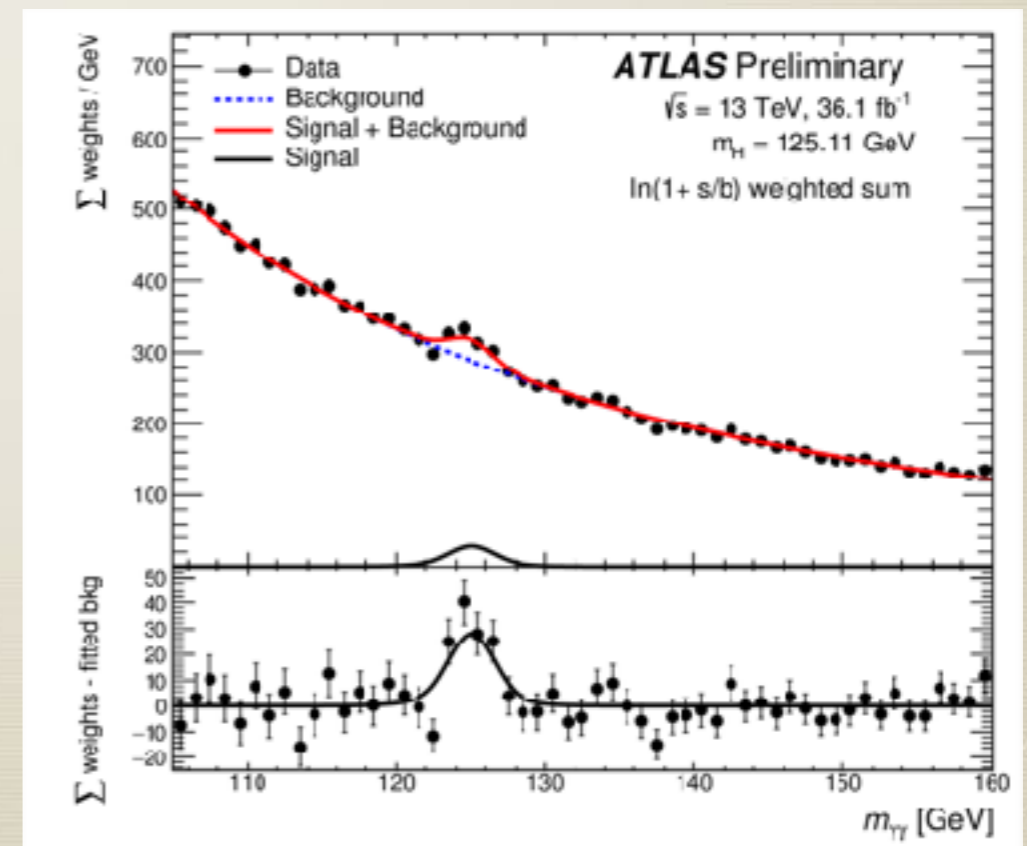
# Introduction

# Standard Model

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				$\gamma$ photon
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			$Z^0$ Z boson	
			$g$ gluon	
			$H$ Higgs Boson	



figure from [www.physik.uzh.ch](http://www.physik.uzh.ch)



CERN, 2013

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + \bar{\psi} \not{D} \psi + \text{h.c.} \\ & + \frac{1}{2} g_{ij} \psi_i \psi_j + \text{h.c.} \\ & + \frac{1}{2} (D_\mu \phi)^2 - V(\phi) \end{aligned}$$

Picture from Recondito.org

CERN, 2013

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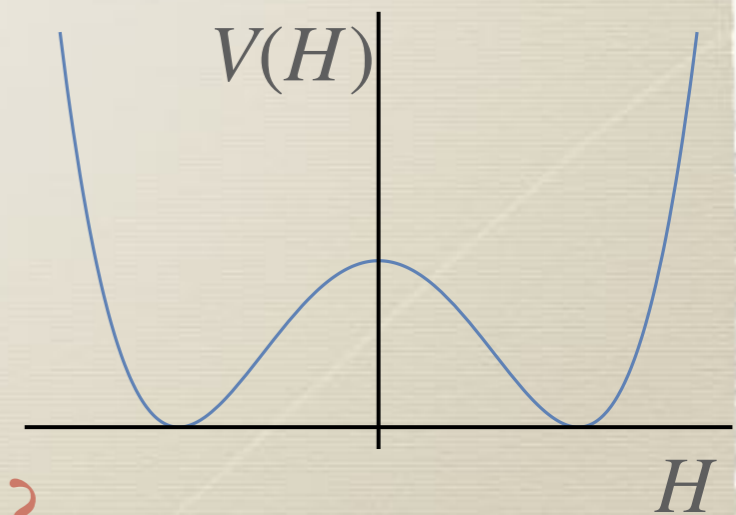
Picture from Recondito.org

# We are far away from the goal

- \* What is dark matter?
- \* How did cosmic inflation occur?
- \* How was the baryon asymmetry of the universe created?
- \* Why does QCD preserve CP symmetry?
- \* What sets the Higgs potential parameters?

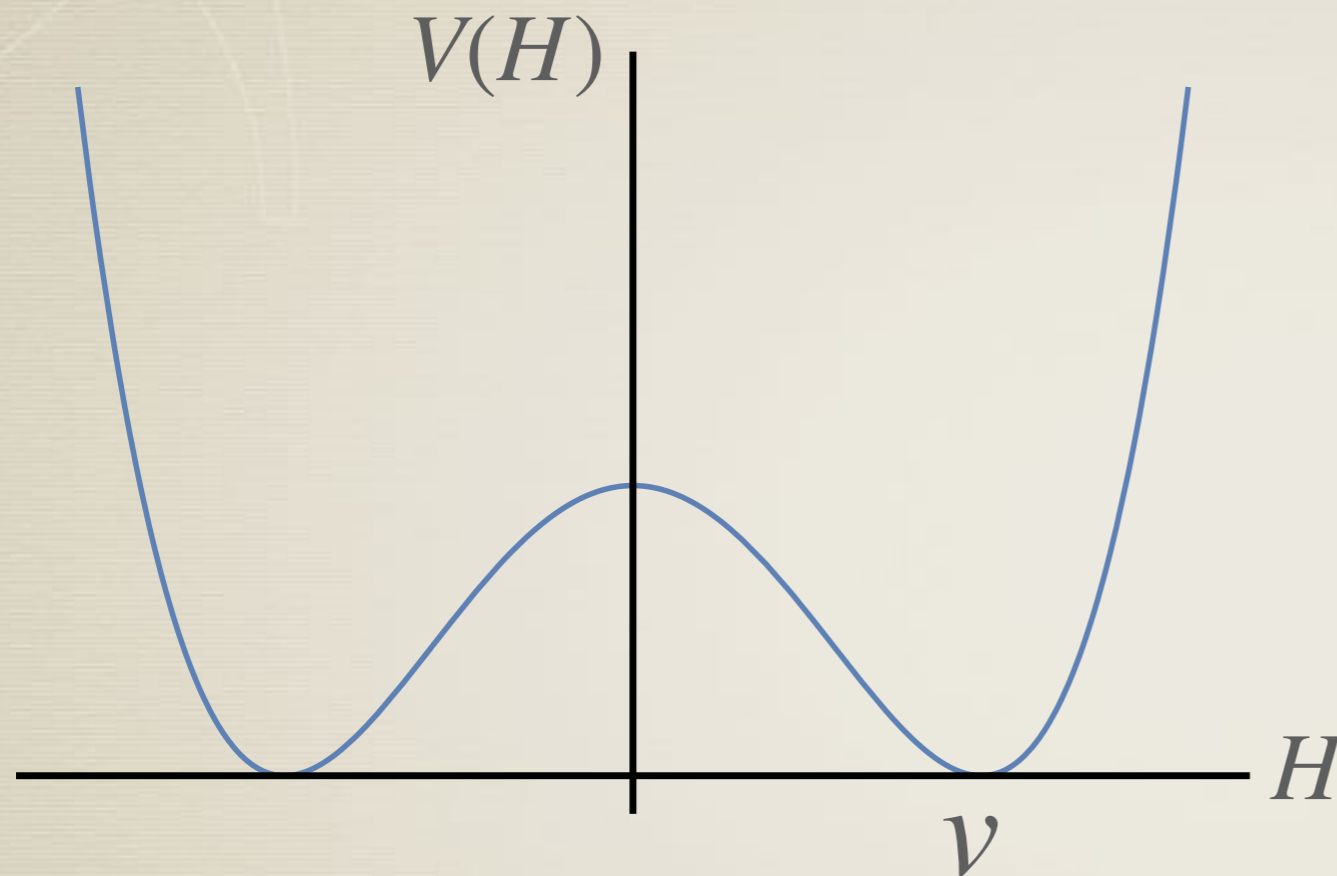
# We are far away from the goal

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$$V(H) = \lambda_{\text{SM}} \left( |H|^2 - v^2 \right)^2$$

# Higgs potential



$$V(H) = \lambda_{\text{SM}} \left( |H|^2 - v^2 \right)^2$$

A question of few decades:

What sets the mass scale of Higgs?

$v = 173 \text{ GeV} \ll (\text{Planck scale, GUT scale})$

**Hierarchy problem**

# Higgs potential

What sets the small mass scale of Higgs?

Ex. Supersymmetry, composite Higgs

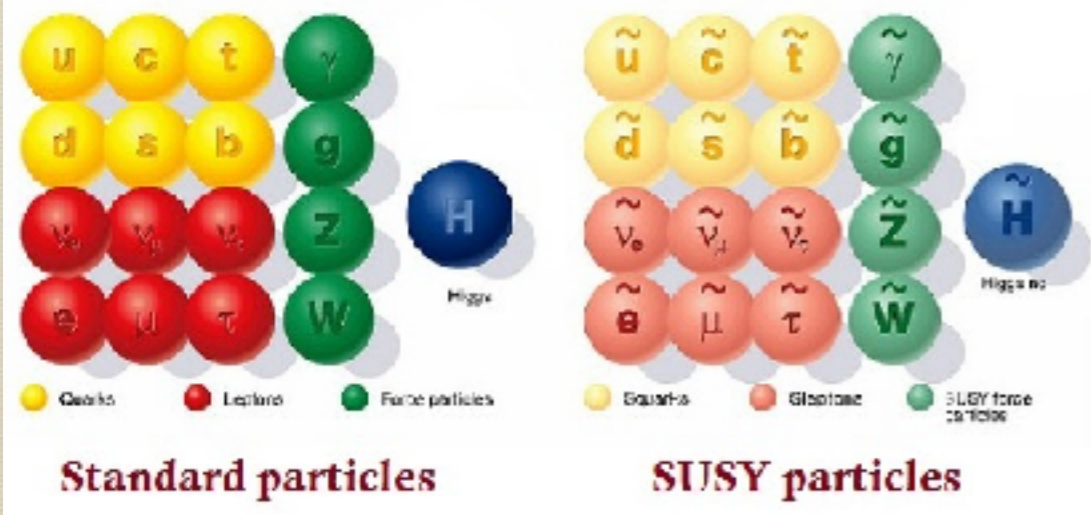
Higgs mass scale is naturally much smaller than the Planck scale

Maiani (1979), Veltman (1979), Witten (1981),  
Kaul (1982), Kaplan and Georgi (1984)  
Kaplan, Georgi and Dimopoulos (1984)

$$m_{\text{SUSY}}, m_{\text{composite}} \propto \exp\left(-\frac{8\pi^2}{g^2}\right)$$

predict new particles with masses around 100 GeV

## SUPERSYMMETRY



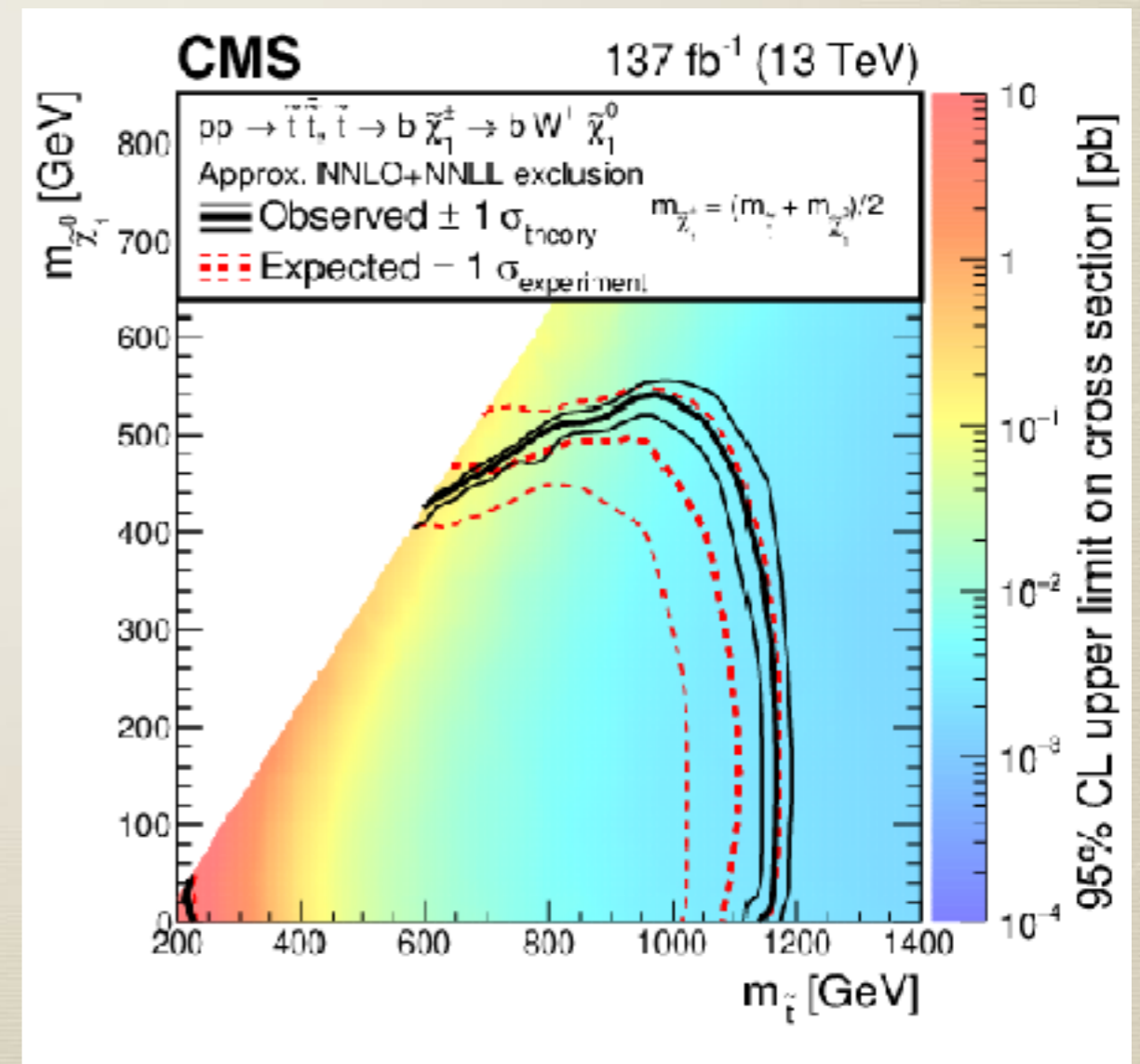
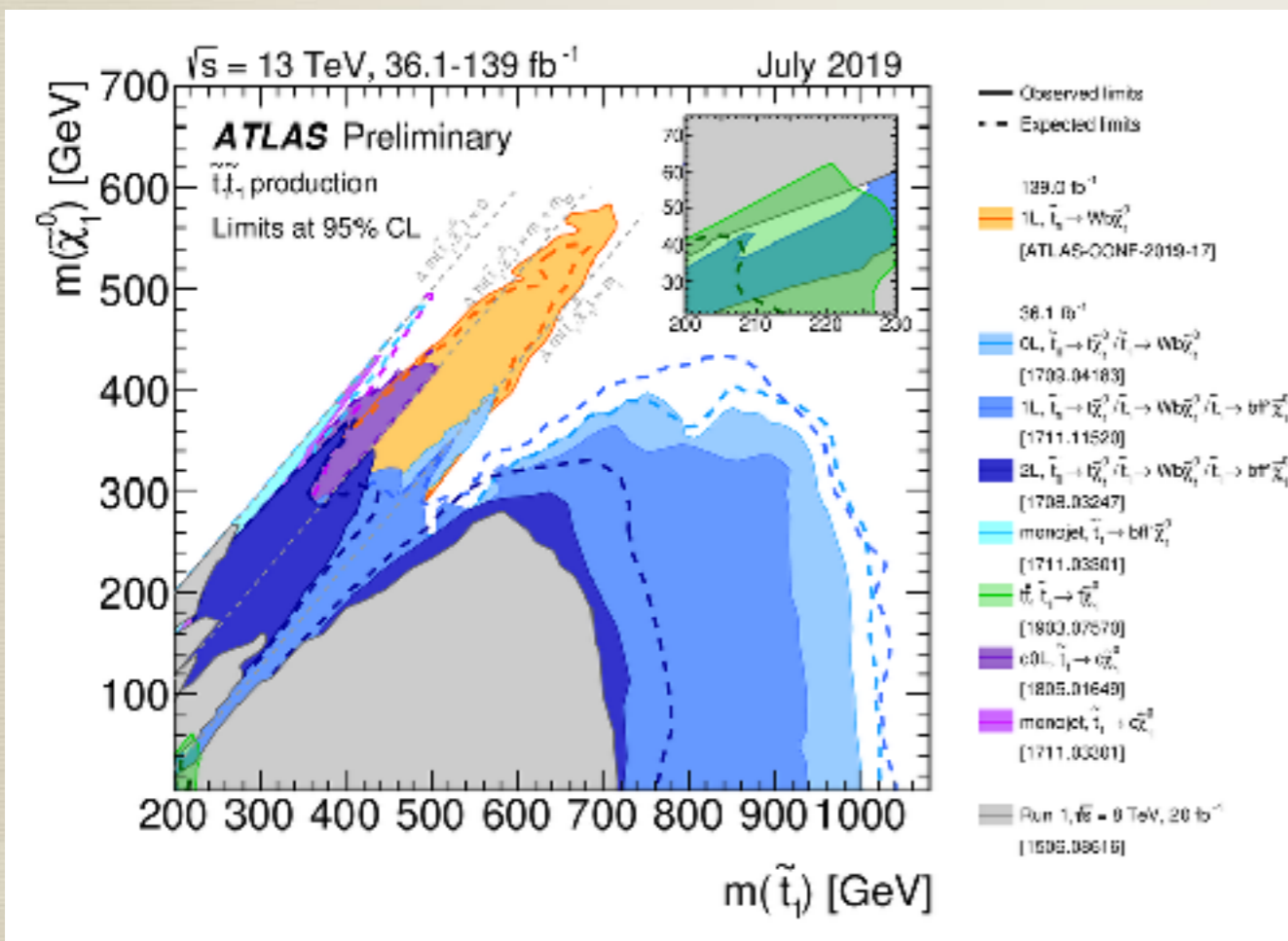
CERN & IES de SAR



# 100 GeV scale new physics

New particles have not been found so far

Ex. Constraints on stop and neutralino masses in MSSM



# Fine-tuned Higgs mass?

$$V(H) = \lambda_{\text{SM}} \left( |H|^2 - \textcircled{v^2} \right)^2$$

We are not sure if the small Higgs mass is a guiding principle to look for new physics

The small Higgs mass may be explained by theoretical ideas which are difficult to probe experimentally

Ex. **Multiverse and anthropic selection**

Weinberg (1987), Susskind (2003), Agrawal, Barr, Donoghue and Seckel (1998), Clavelli and White (2006), Hall, Pinner and Ruderman (2014), D'Amico, Strumia, Urbano and Xue (2019), ...

# Fine-tuned Higgs mass?


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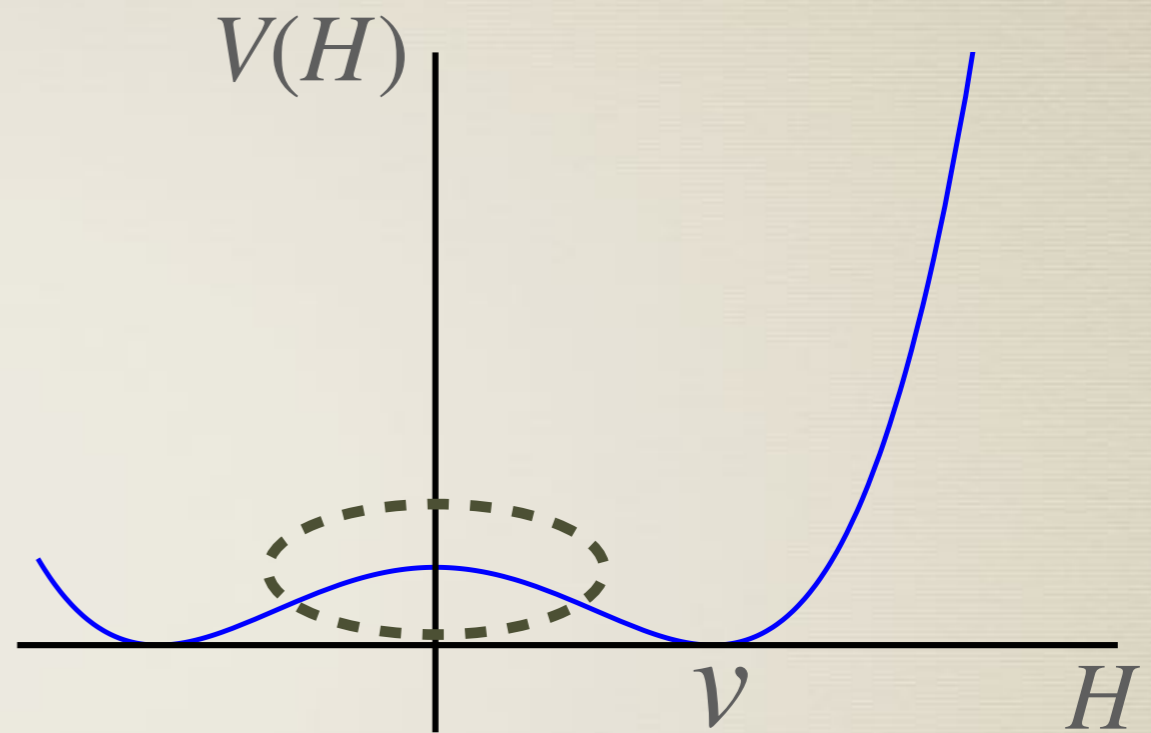
I will postulate fine-tuned Higgs mass and look for another clue

# Higgs mass

$$V(H) = \lambda_{\text{SM}} \left( |H|^2 - v^2 \right)^2$$



$(173\text{GeV})^2$

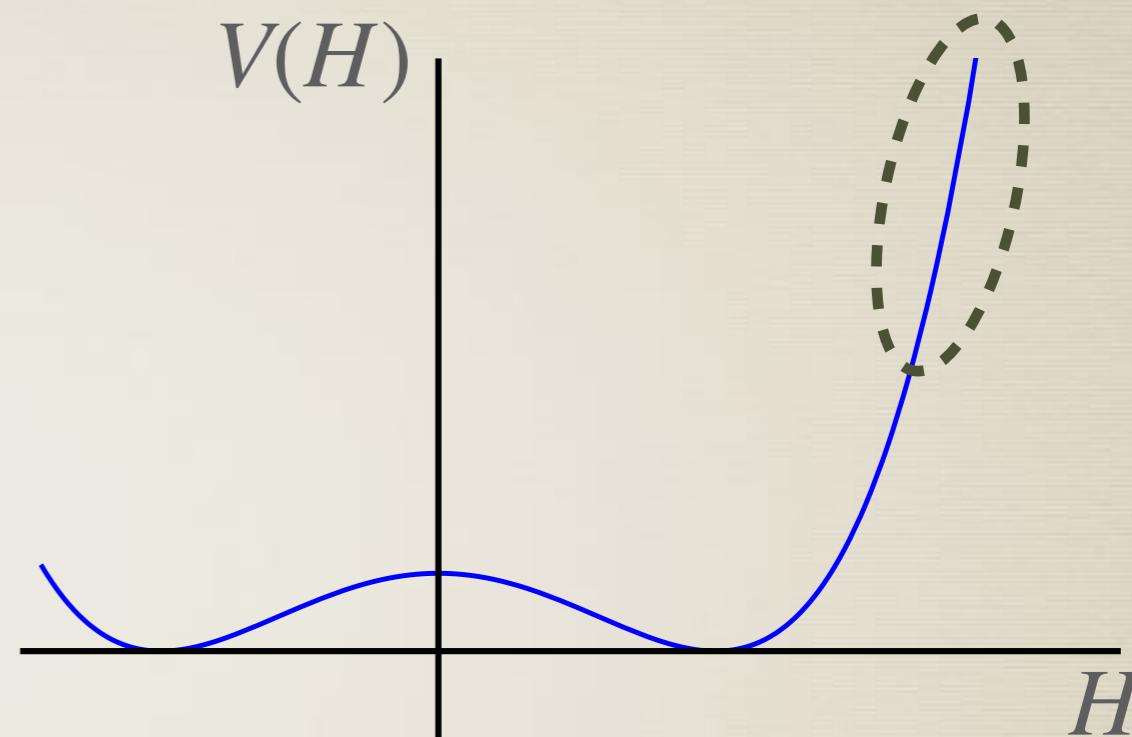


# Higgs self-interaction?

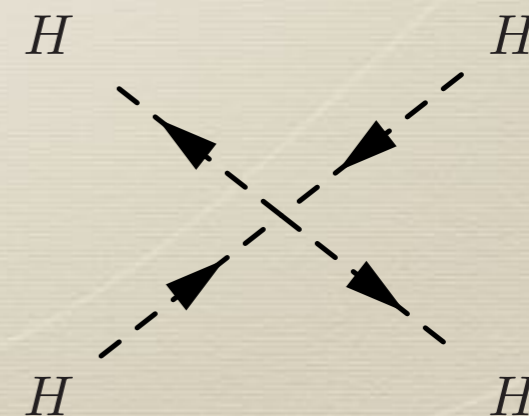
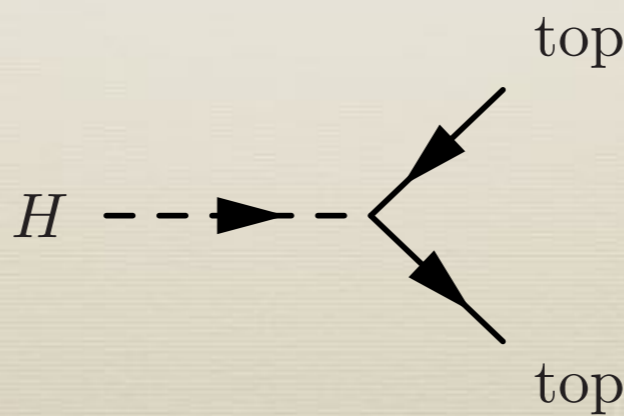
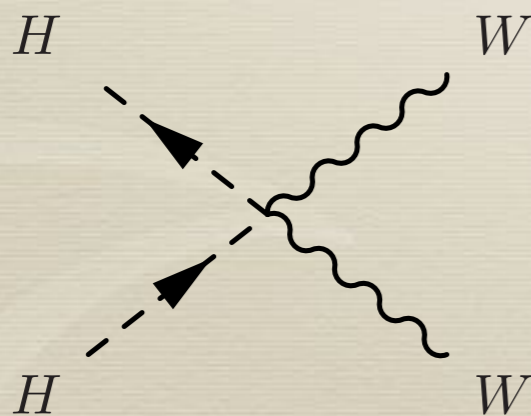
$$V(H) = \lambda_{\text{SM}} \left( |H|^2 - v^2 \right)^2$$



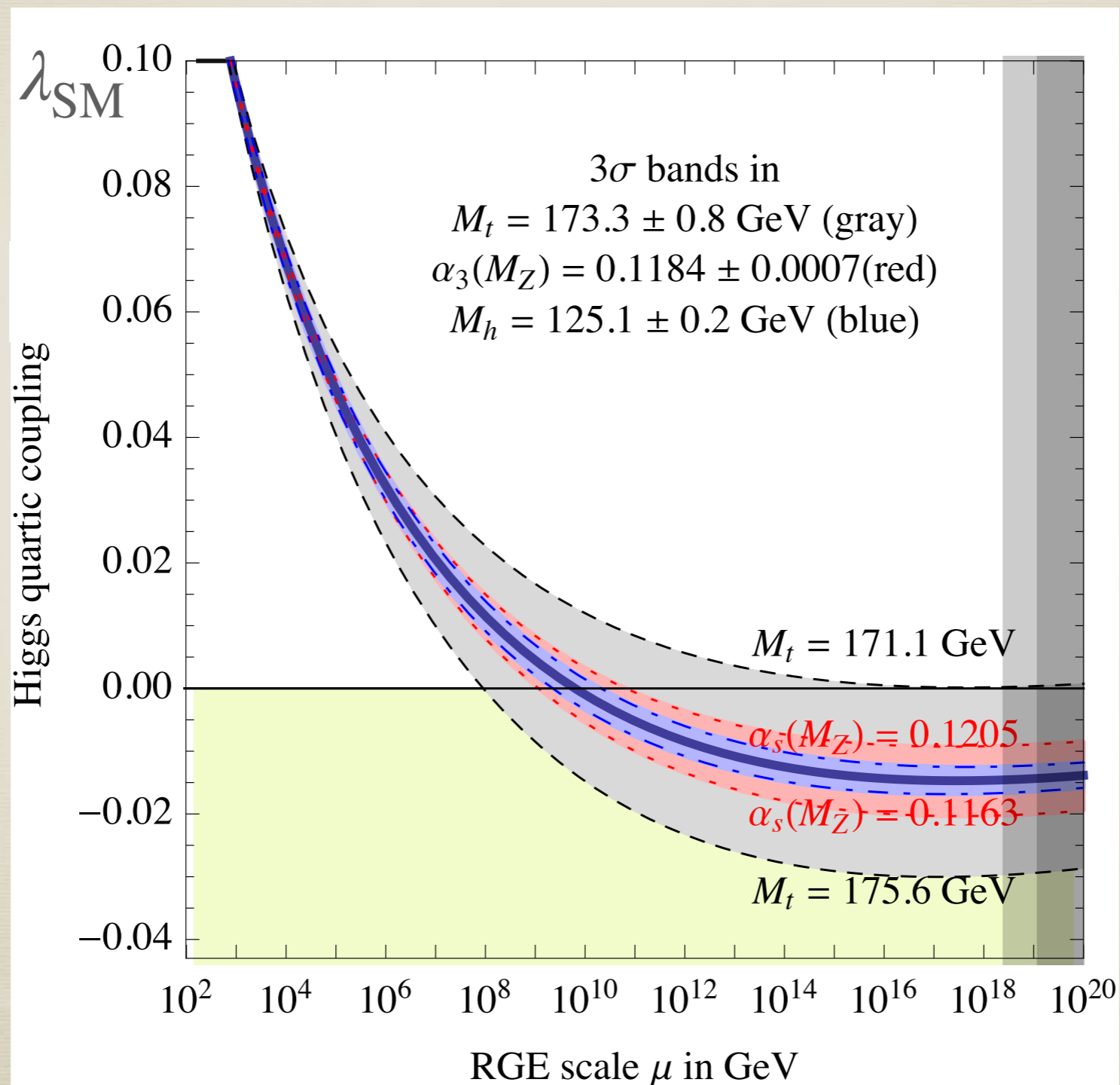
$$m_h^2 / (4v^2) \simeq 0.13$$



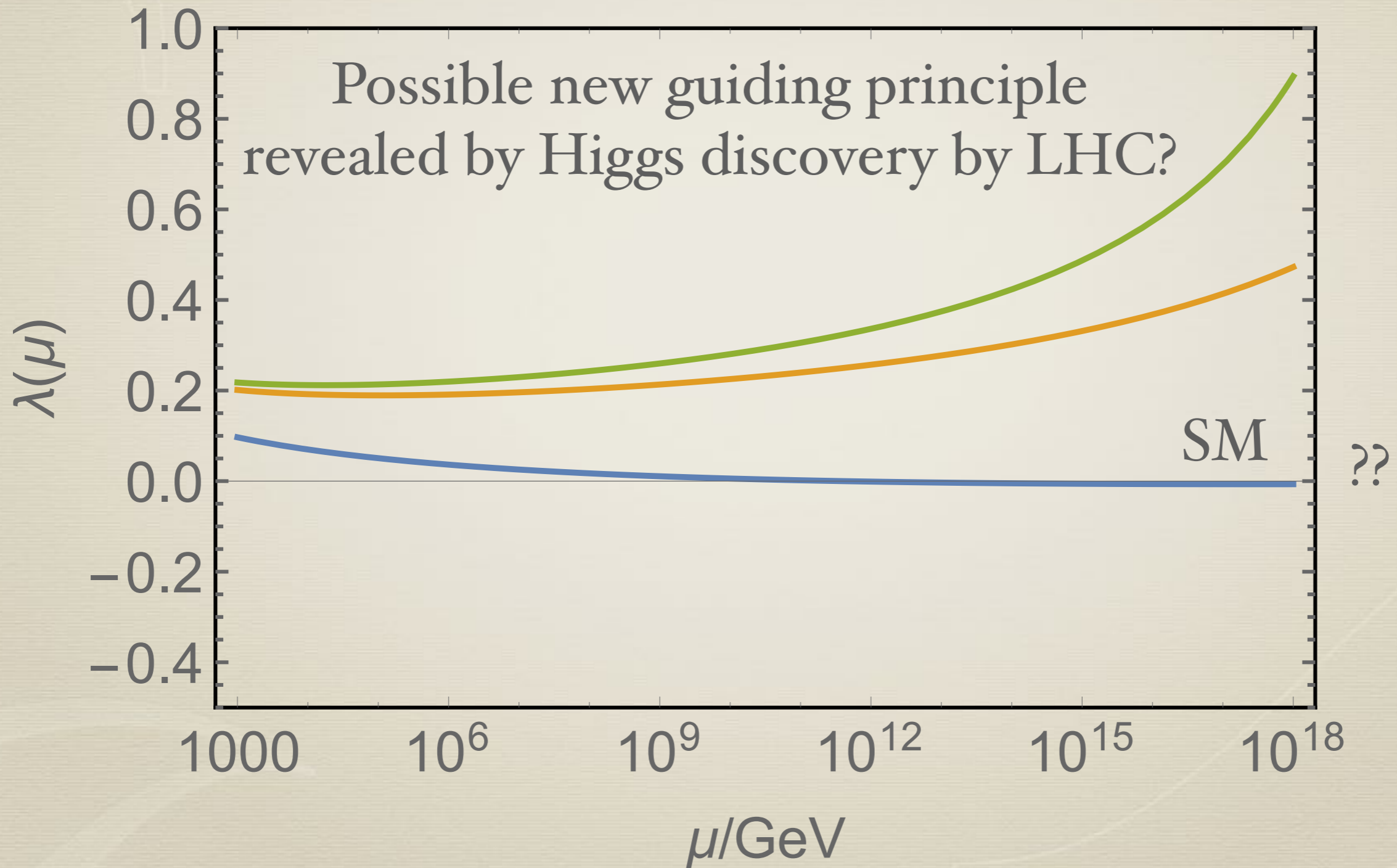
Let us examine the quartic coupling,  
assuming that the standard model is valid up to high energy scales,  
including quantum corrections



# Small quartic coupling

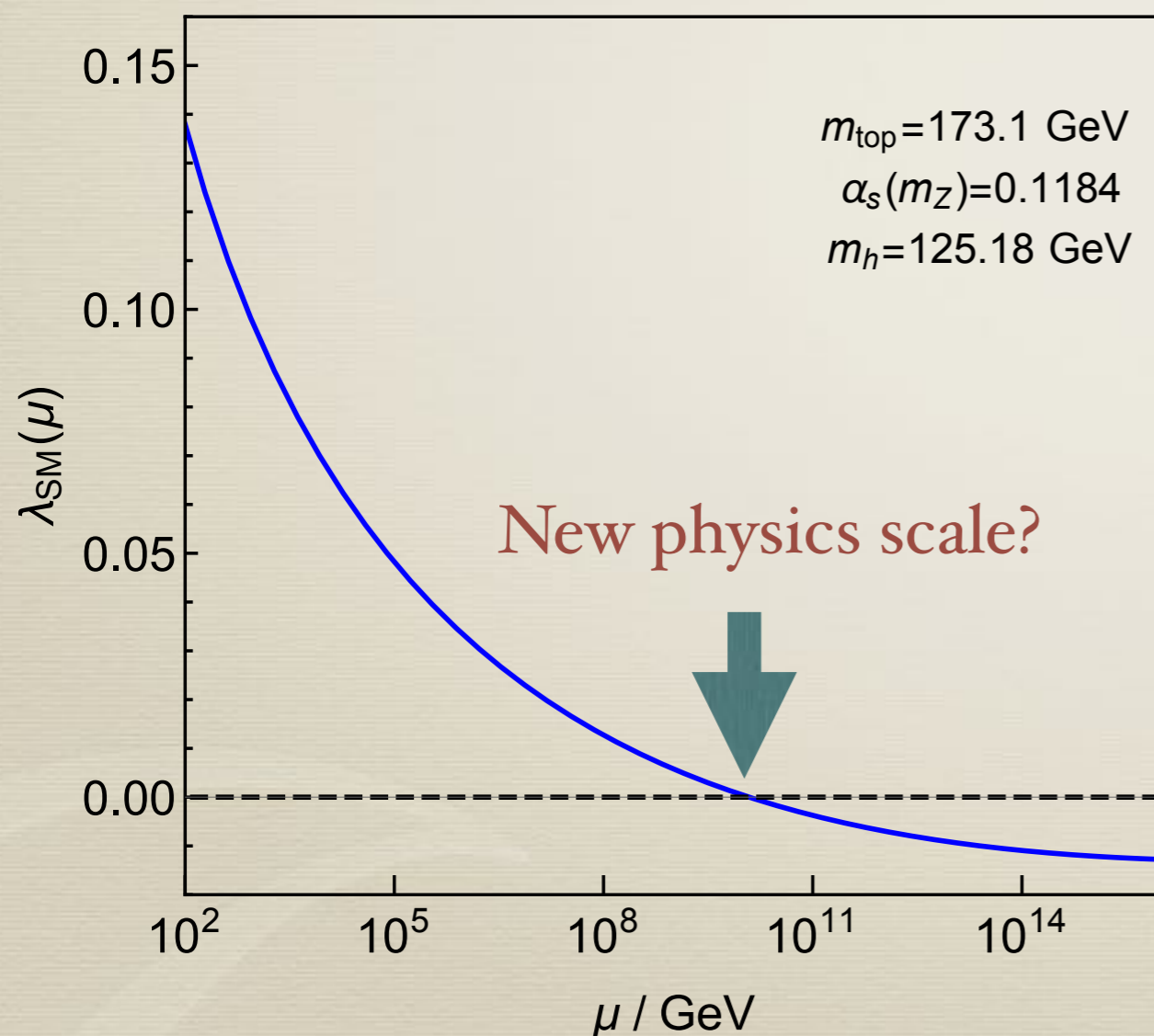


# Small quartic coupling



# New physics?

Conjecture : some new physics which couples to Higgs sets  $\lambda_{\text{SM}} \simeq 0$  at a high energy scale



PQ symmetry?

Redi and Strumia (2012)

Supersymmetry?

Hall and Nomura (2013),

Ibe, Matsumoto and Yanagida (2013)

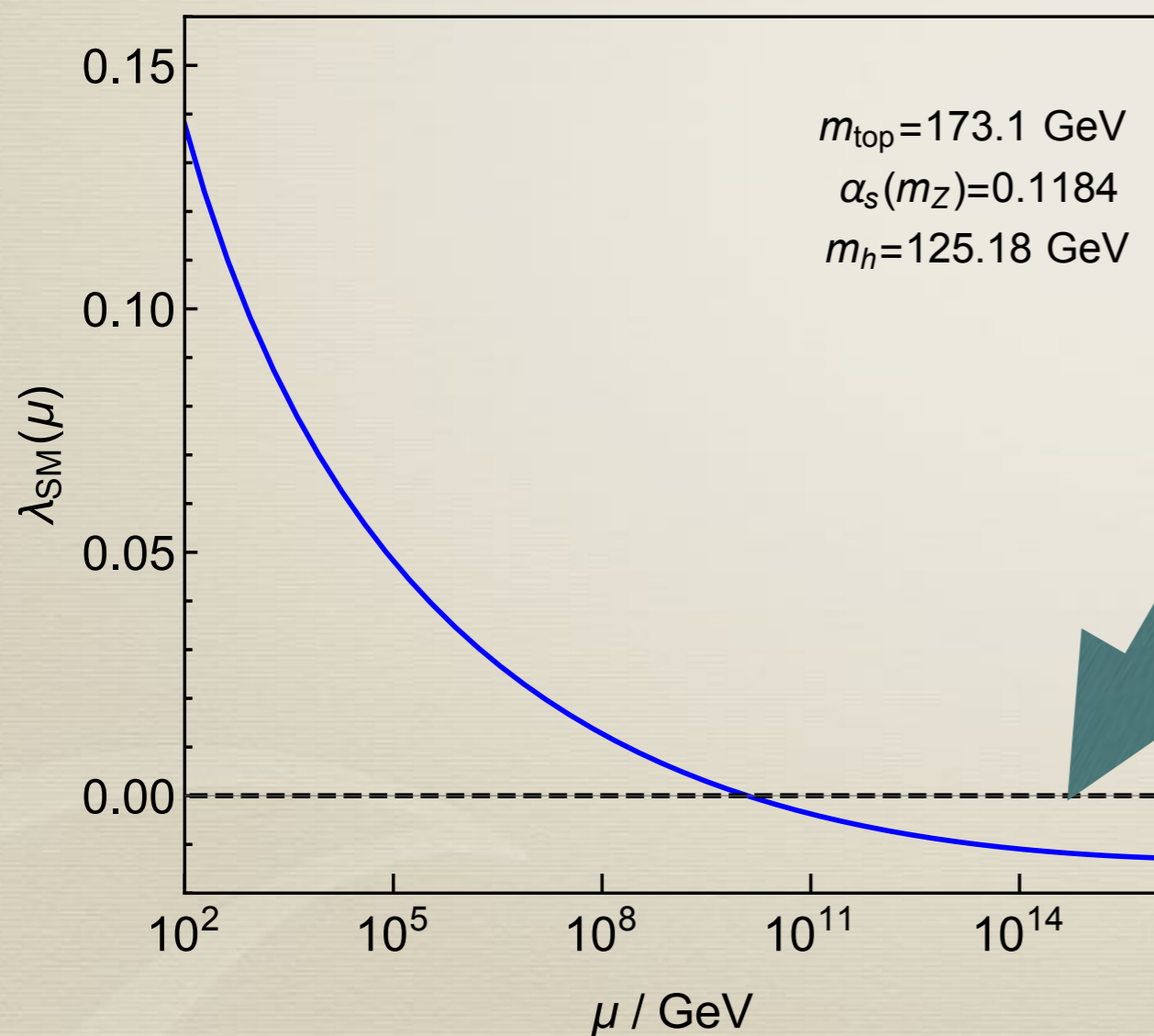
Gauge-Higgs unification?

Gogoladze, Okada and Shafi (2007)

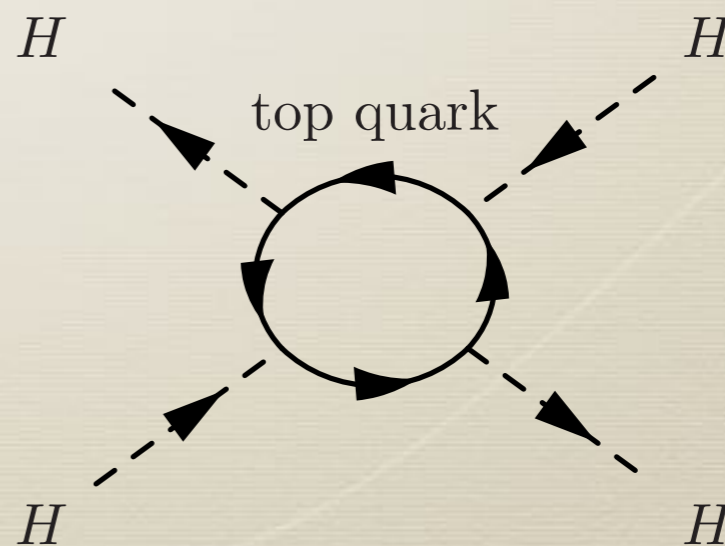


# New physics?

Conjecture : some new physics which couples to Higgs sets  $\lambda_{\text{SM}} \simeq 0$  at a high energy scale



quartic coupling assuming  
Standard Model remains small  
due to small yukawa  
coupling at high energy



# Precise measurement and new physics?

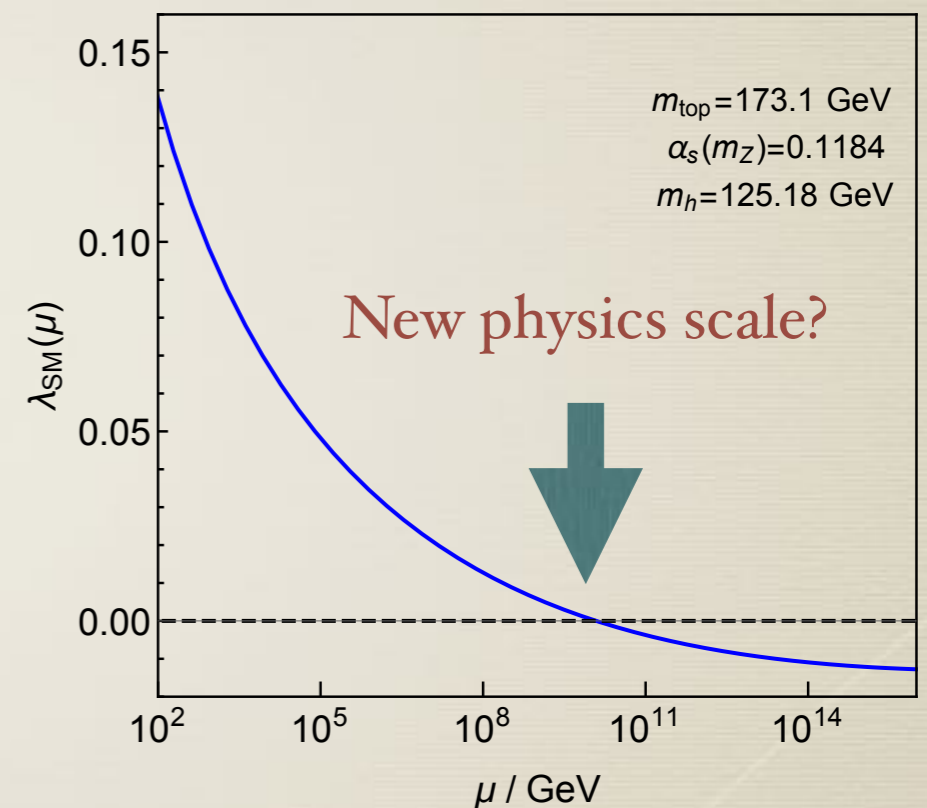
top quark mass  
Higgs mass  
strong coupling constant



scale of the new physics



further UV physics,  
experimental signals?



# Precise measurement and new physics

Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)

top quark mass  
Higgs mass  
strong coupling constant

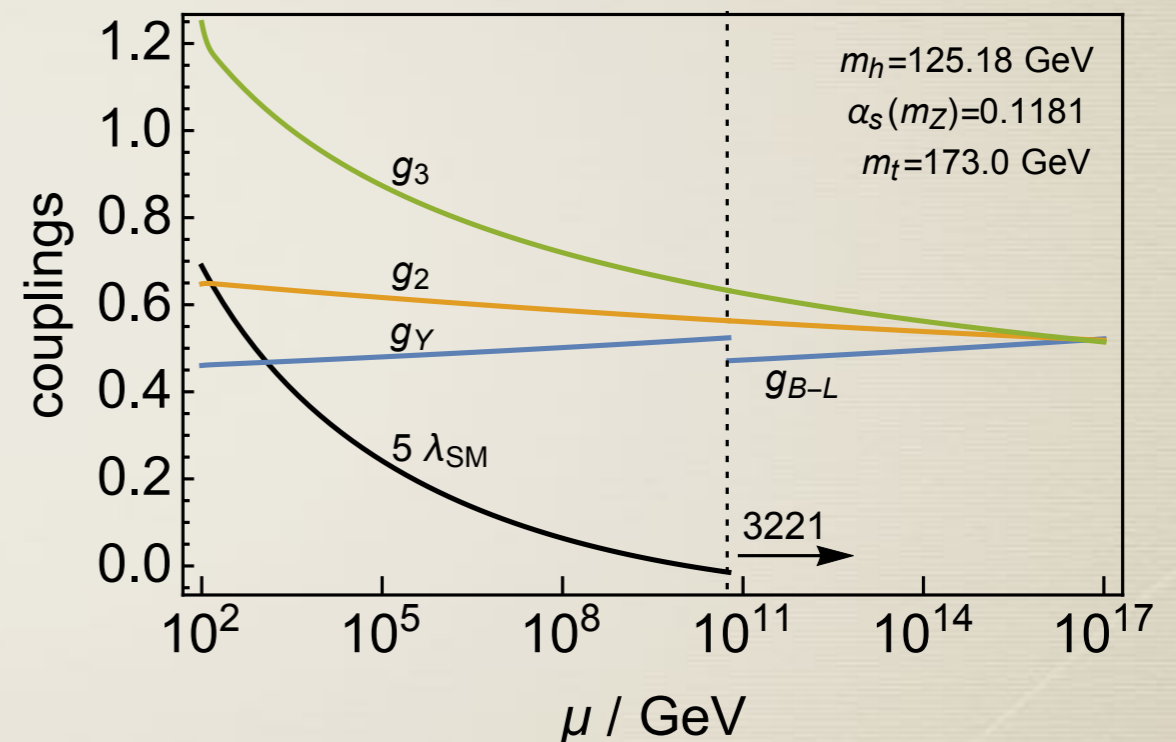


New symmetry  
(Higgs Parity)  
breaking scale




Grand unification  
proton decay

Dark matter detection rate, neutron EDM,  
gravitational waves, dark radiation, warm dark matter, ...



# Outline

- \* Introduction
- \* **Higgs Parity** 
- \* Grand unification and proton decay
- \* Summary and outlook

# Symmetry

Symmetry has been playing the central role in physics

Dictate **relations** among masses  
and interaction rates of particles

Ex. Symmetry of hadrons


Explain why the proton mass is similar to the neutron mass

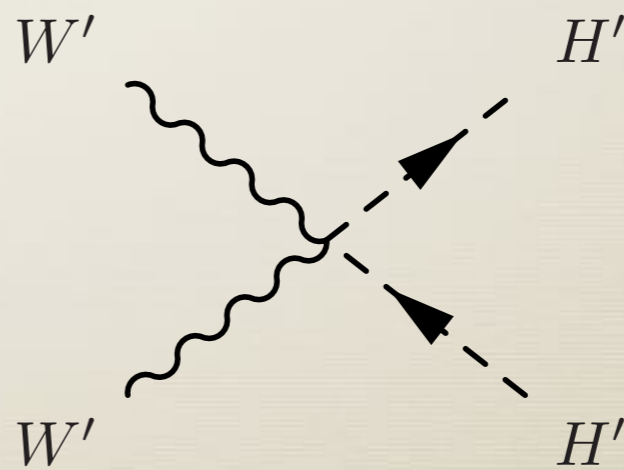
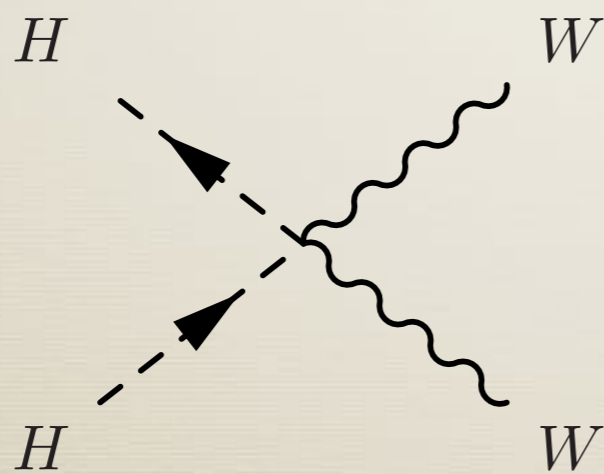
938.27 MeV

939.57 MeV

# $Z_2$ symmetry

Higgs  
 $H$   Higgs'  
 $H'$

Weak gauge boson  
 $W$   
 $SU(2)$   Weak gauge boson'  
 $W'$   
 $SU(2)'$



# $Z_2$ symmetry

Higgs  $H$   $\longleftrightarrow$  Higgs'  $H'$

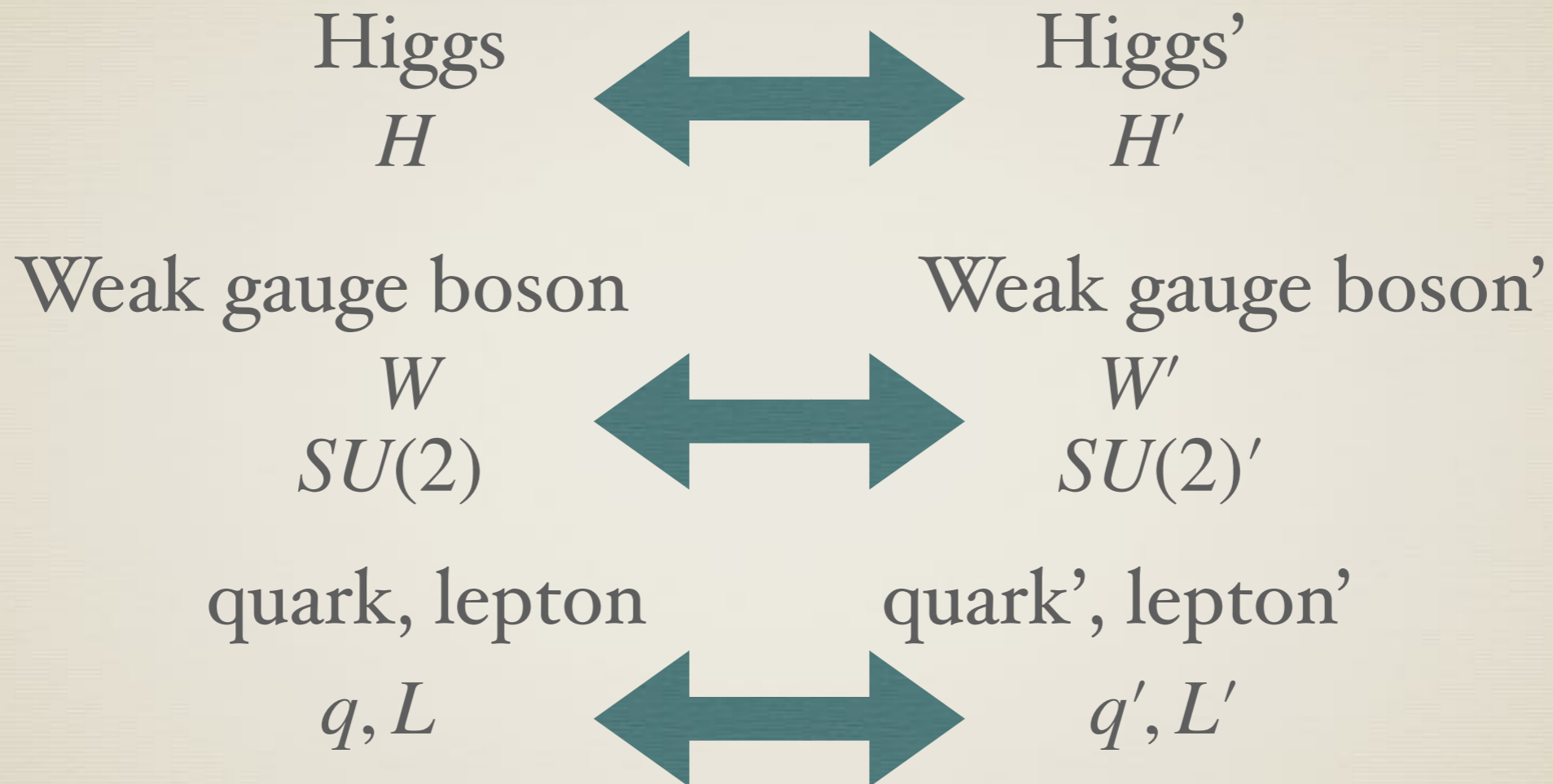
Weak gauge boson  $W$   $SU(2)$   $\longleftrightarrow$  Weak gauge boson'  $W'$   $SU(2)'$

quark, lepton  $q, L$   $\longleftrightarrow$  quark', lepton'  $q', L'$

(photon, gluon : several options)

- \* is part of a grand unified gauge symmetry
- \* solves the strong CP problem
- \* (gives a dark matter candidate)

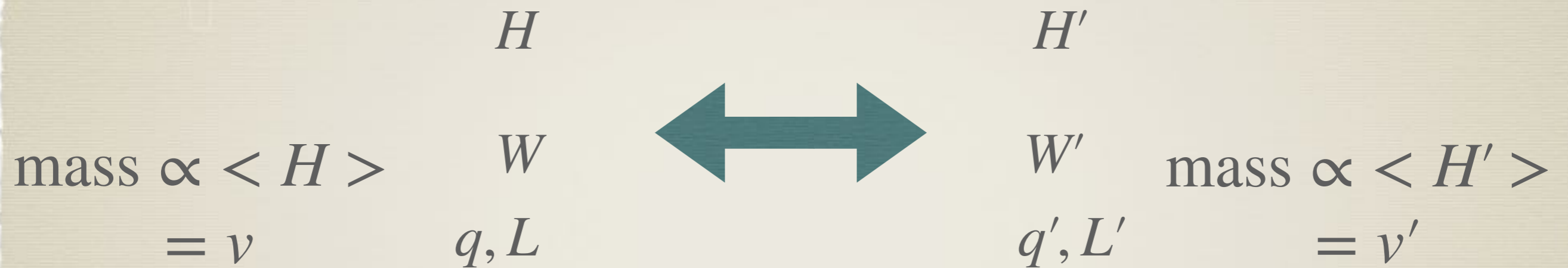
# $Z_2$ symmetry



Higgs Parity (HP)



# Spontaneously broken Higgs Parity



In well-motivated theories (explained later),  
 $W'$ ,  $q'$  or  $L'$  interact with Standard Model particles with  
 $O(1)$  couplings

unbroken  $Z_2$   $\langle H \rangle = \langle H' \rangle$  is experimentally excluded

symmetry breaking  $\langle H \rangle \ll \langle H' \rangle$  is required

# Small quartic

Hall, KH (2018)

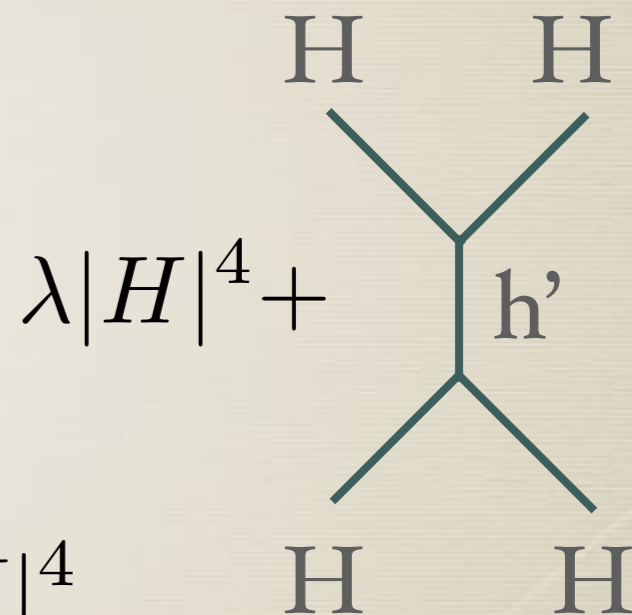
$$V(H, H') = \lambda(|H|^2 + |H'|^2)^2 + \lambda'|H|^2|H'|^2 - m^2(|H|^2 + |H'|^2)$$

$$\langle H' \rangle^2 = \frac{m^2}{2\lambda} \equiv v'^2$$

Integrate out heavy d.o.f.

$$V_{\text{eff}} \simeq \underbrace{\lambda' v'^2}_{|\lambda'| \ll 1} |H|^2 - \lambda' \left(1 + \frac{\lambda'}{4\lambda}\right) |H|^4$$

$$\lambda_{\text{SM}}(v') = 0$$



Threshold correction:  $\lambda_{\text{SM}}(v') \sim -\frac{y_t^4}{16\pi^2} \sim -10^{-3}$

# pseudo-NGB Higgs

Hall, KH (2018)

$$V(H, H') = \lambda(|H|^2 + |H'|^2)^2 + \cancel{\lambda'|H|^2|H'|^2} - m^2(|H|^2 + |H'|^2)$$

Accidentally  $U(4)$  symmetric      $4 = (H, H')$

$U(4) \rightarrow U(3)$  by  $H'$

$$16 - 9 = 7 = 4 + 3$$

$W', Z'$

SM Higgs is a pseudo Nambu-Goldstone boson

$$\lambda_{\text{SM}}(v') = 0$$

# Prediction on symmetry breaking scale

Hall, KH (2018)

Higgs Parity

$$H \longleftrightarrow H'$$

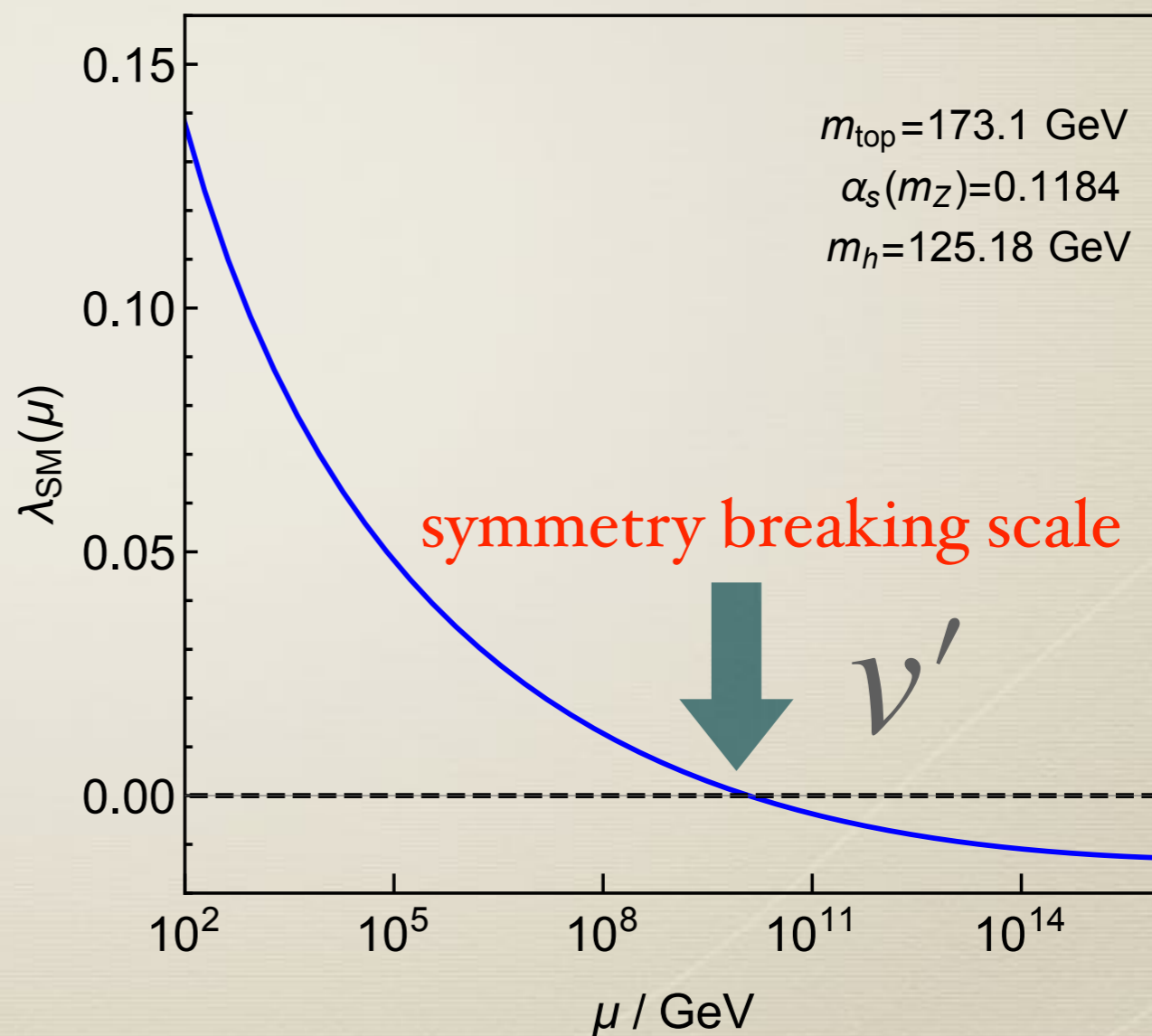
is broken by

$$\langle H \rangle \ll \langle H' \rangle$$

$$v \ll v'$$

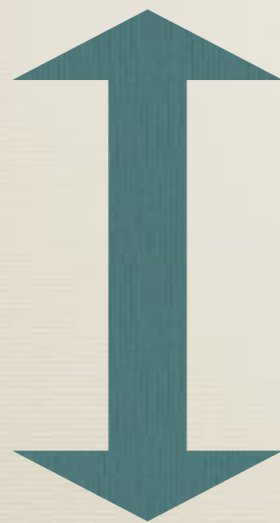


$$\lambda_{\text{SM}}(v') \simeq 0$$



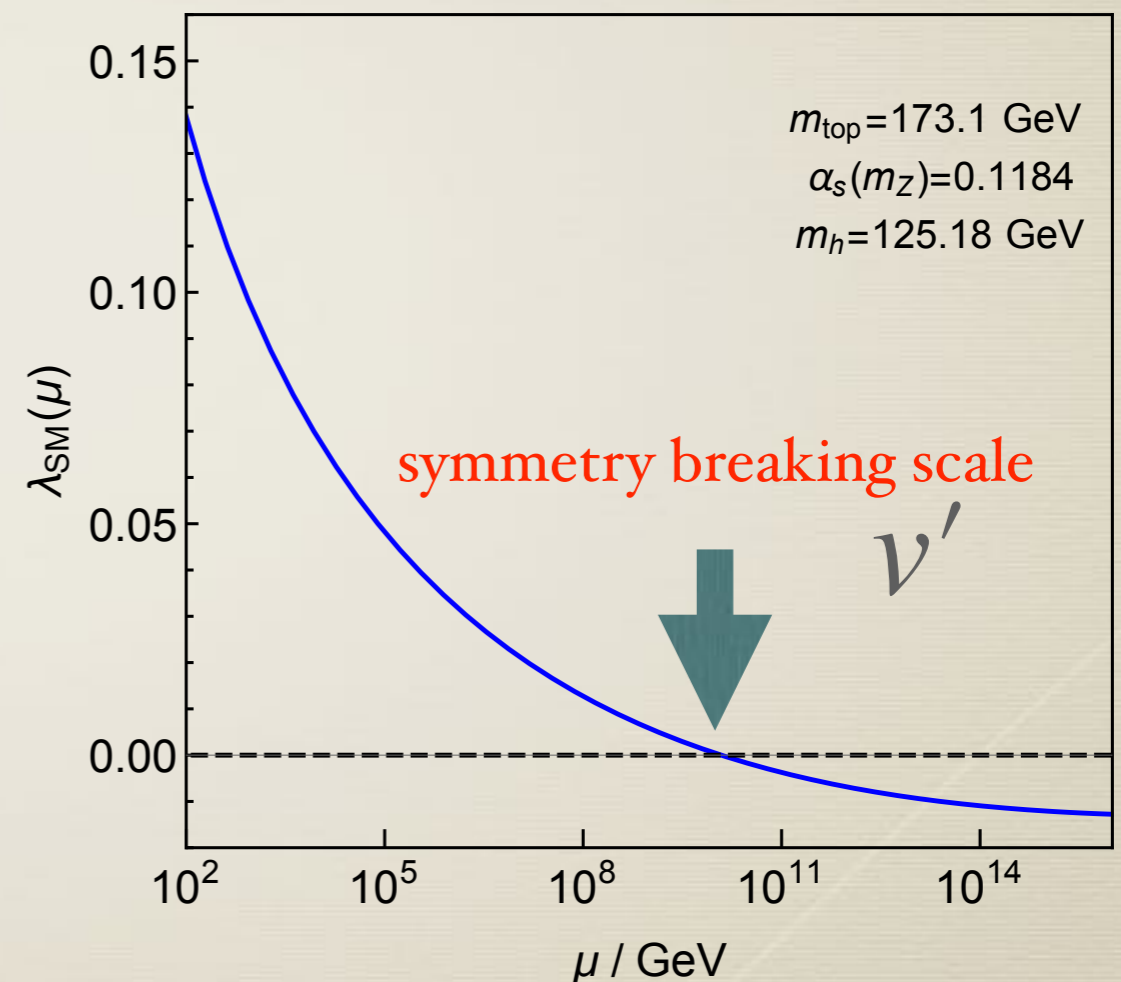
# Precise measurement and new physics

top quark mass  
Higgs mass  
strong coupling constant



**Higgs Parity (HP)**  
symmetry breaking scale


Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)



Experimental signatures

# Fine-tuning

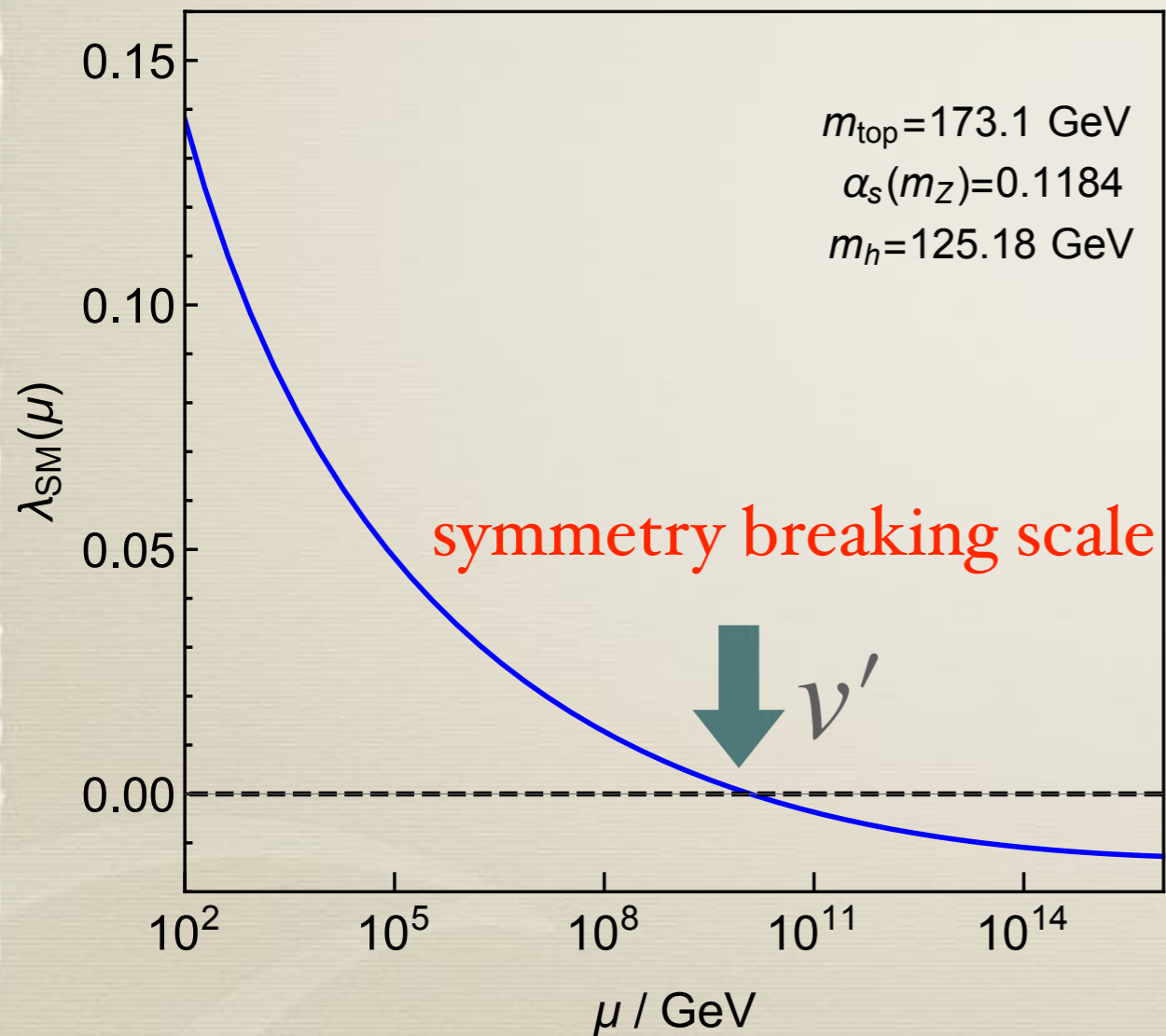
$$V(H, H') = \lambda(|H|^2 + |H'|^2)^2 + \lambda'|H|^2|H'|^2 - m^2(|H|^2 + |H'|^2)$$


$$\frac{v^2}{v'^2} \times \frac{v'^2}{\Lambda_{\text{cut}}^2} = \frac{v^2}{\Lambda_{\text{cut}}^2}$$

Despite the intermediate scale  $v'$ ,  
same as that of standard model

# Quiz 1

If the Higgs mass is larger,  $v'$  is



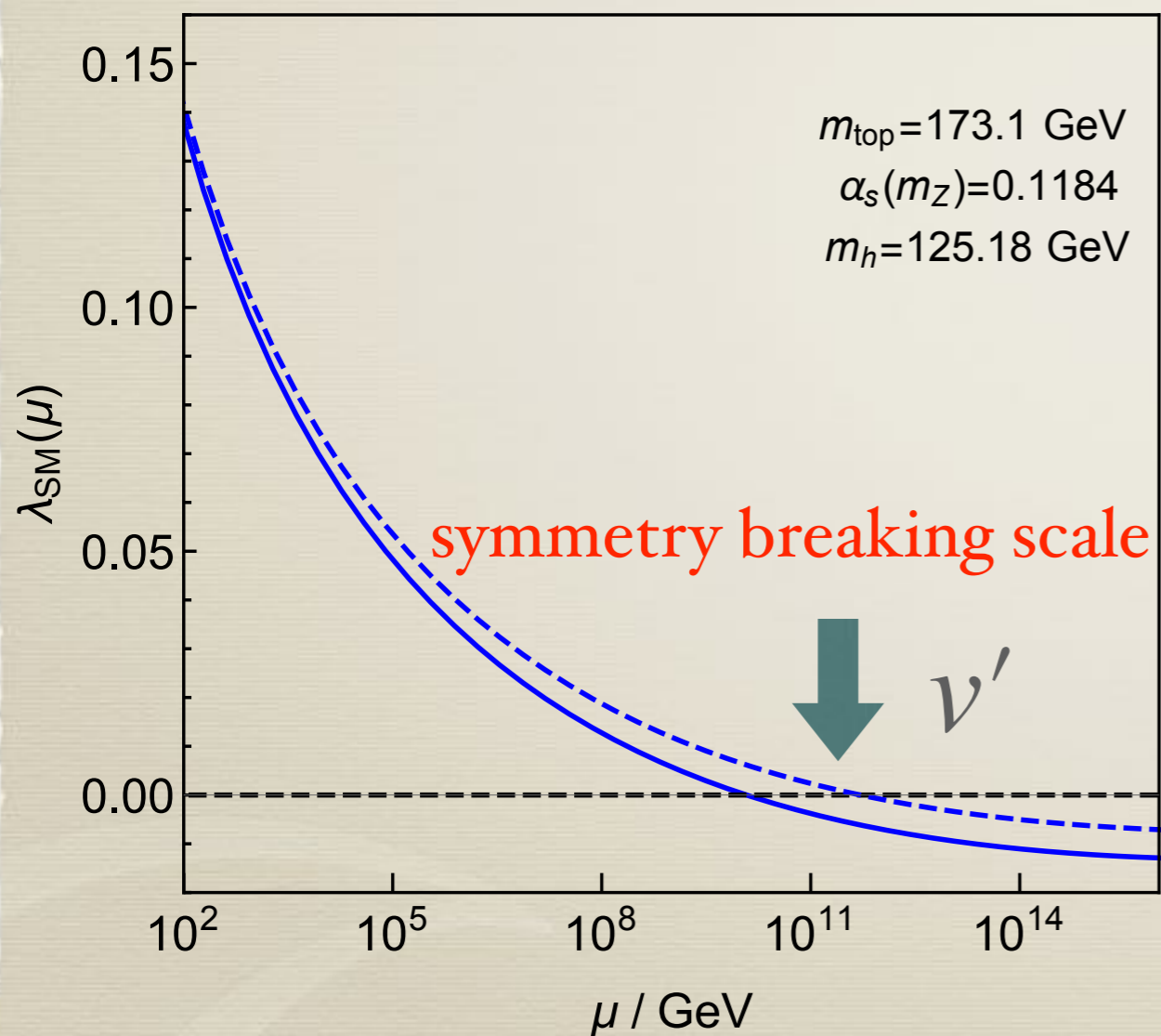
A : Larger  
B : Smaller

Hint: Higgs mass

$$m_h \propto \lambda_{\text{SM}}^{1/2}(\mu = \text{EW scale})$$

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If the Higgs mass is larger,  $v'$  is



A : Larger

B : Smaller

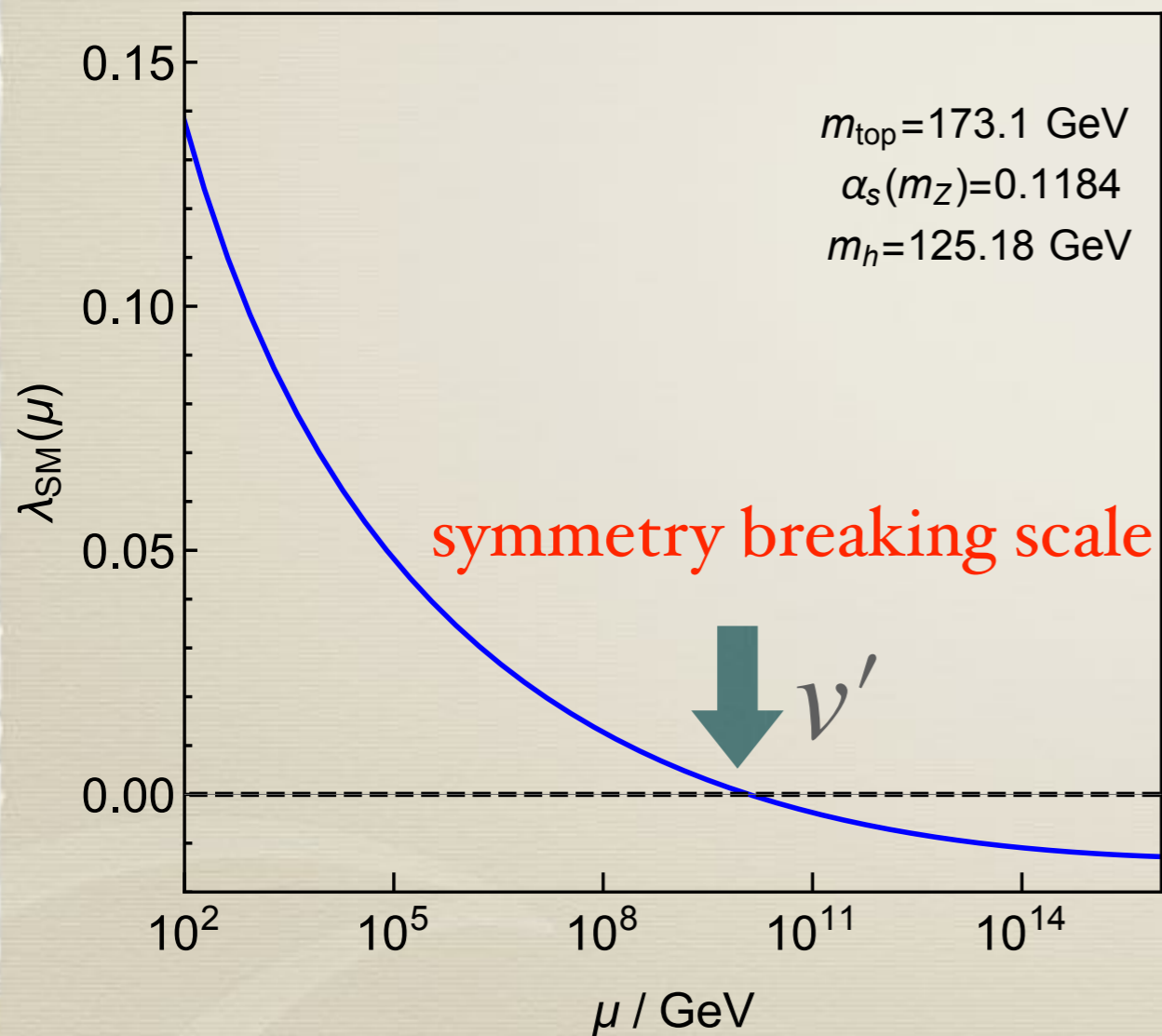
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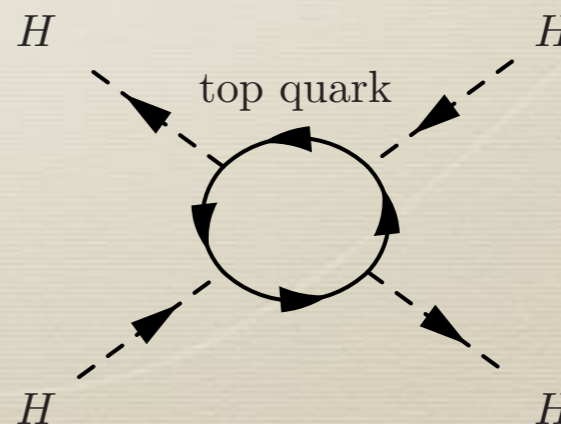
# Quiz 2

If the top quark mass is larger,  $v'$  is



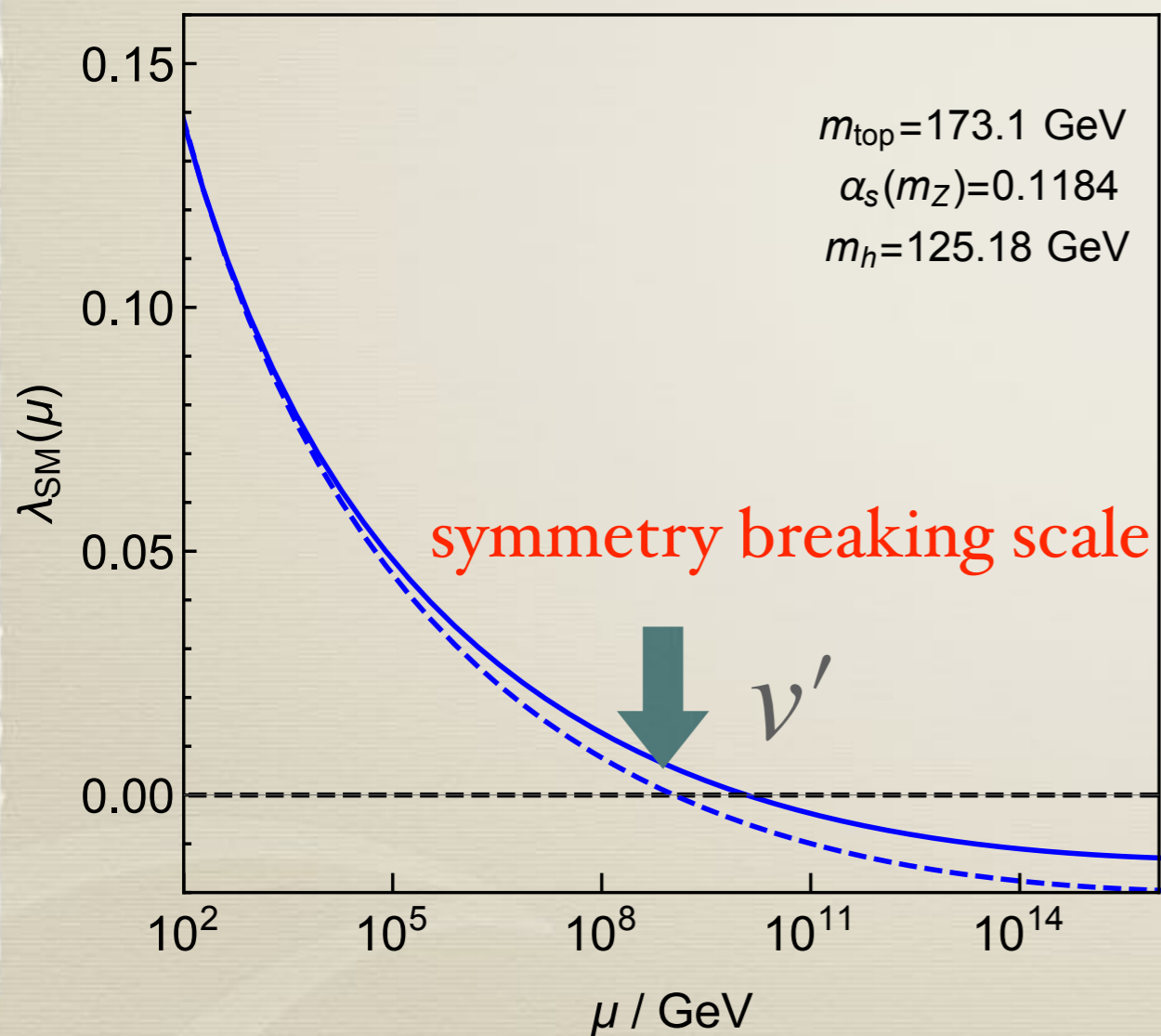
A : Larger  
B : Smaller

Hint: the quartic coupling becomes smaller because of the top quark yukawa



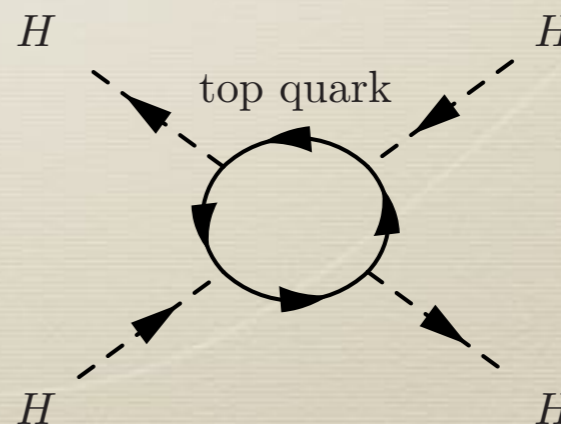
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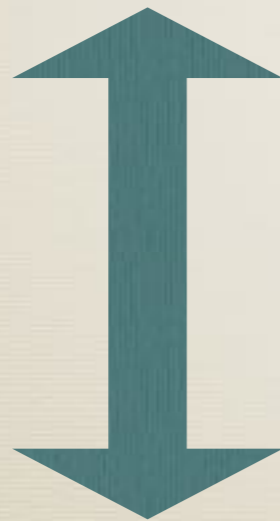
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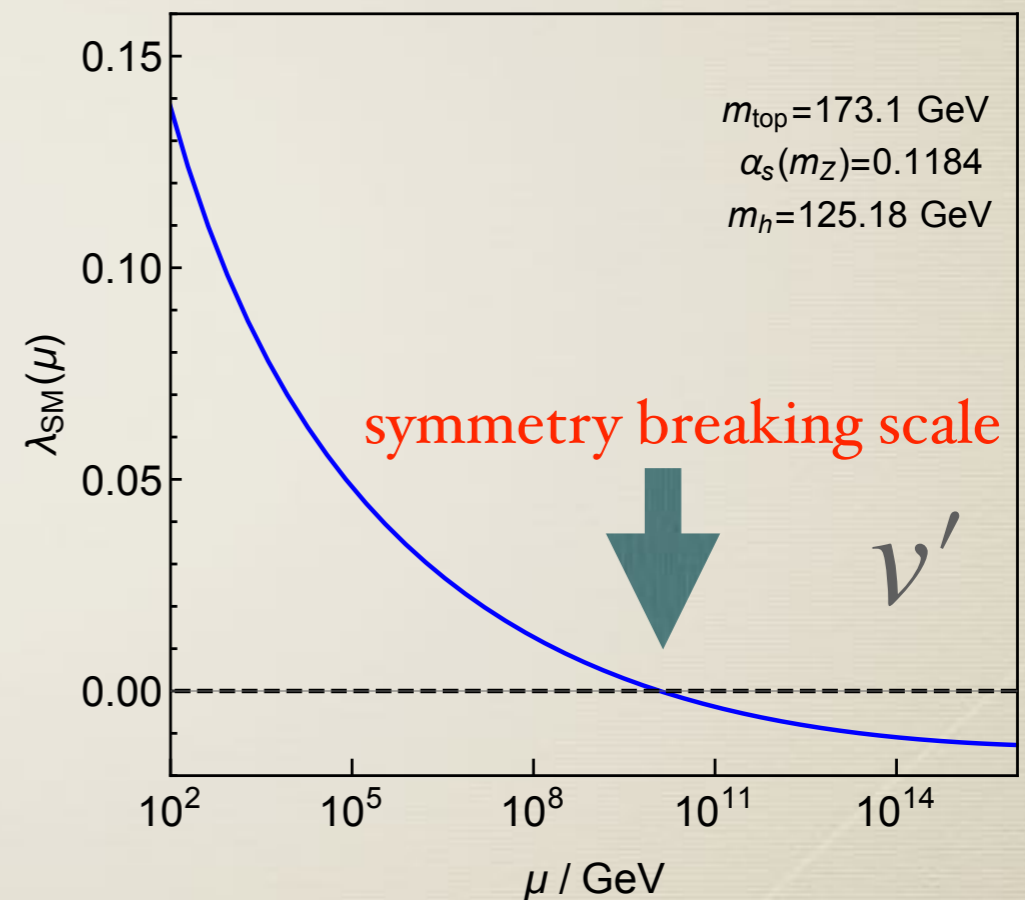
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**Higgs Parity (HP)**  
symmetry breaking scale

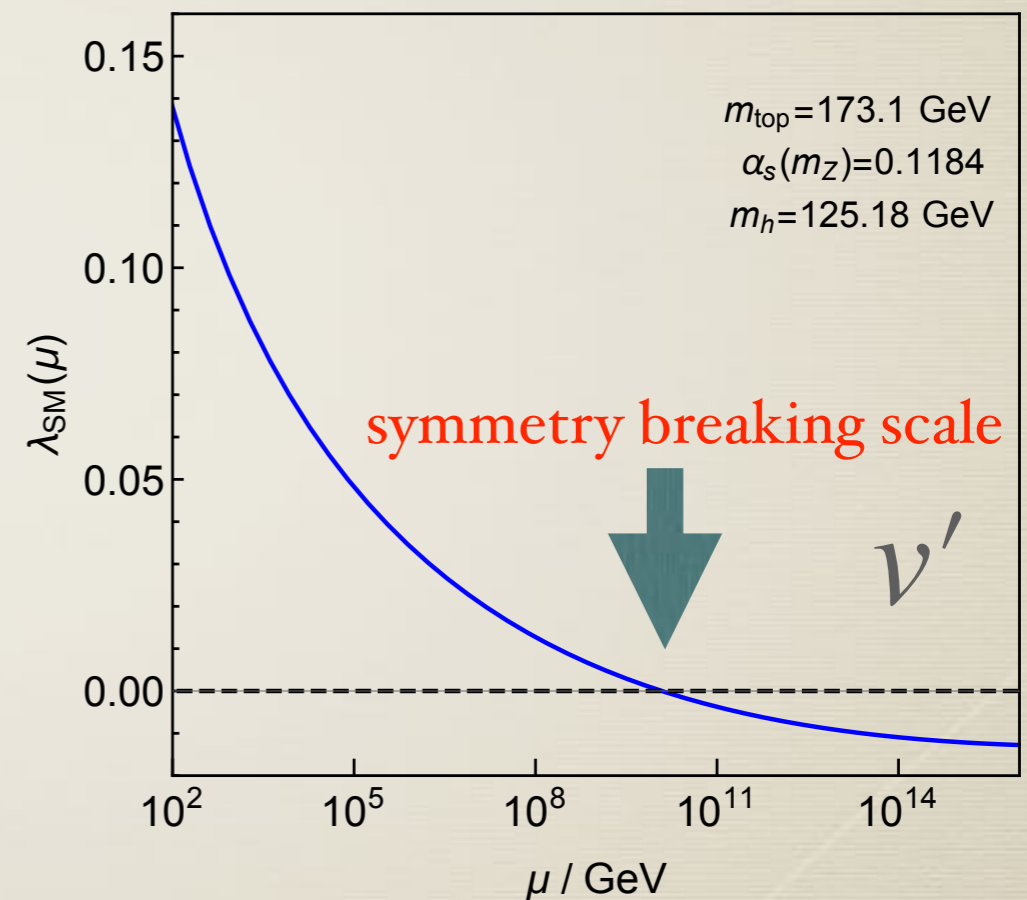
Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)



# Precise measurement and new physics

top quark mass  
Higgs mass  
strong coupling constant

Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)



Higgs Parity (HP)  
symmetry breaking scale



further UV physics,  
experimental signatures

# Outline

- \* Introduction
- \* Higgs Parity
- \* Grand unification and proton decay
- \* Summary and outlook



# Precise measurement and Grand Unification

Hall and KH (2018, 2019)

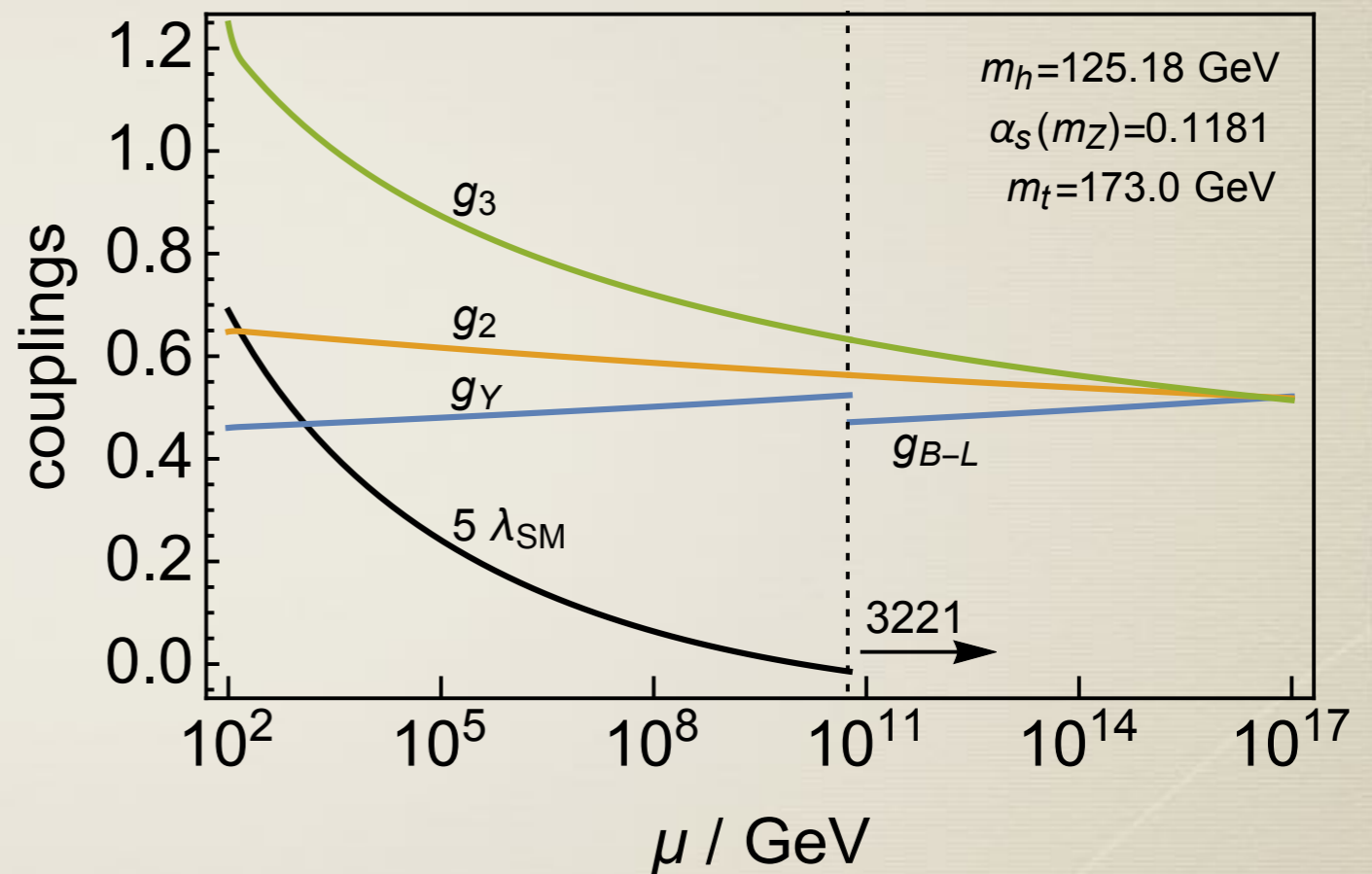
top quark mass  
Higgs mass  
strong coupling constant



Higgs Parity  
symmetry breaking scale



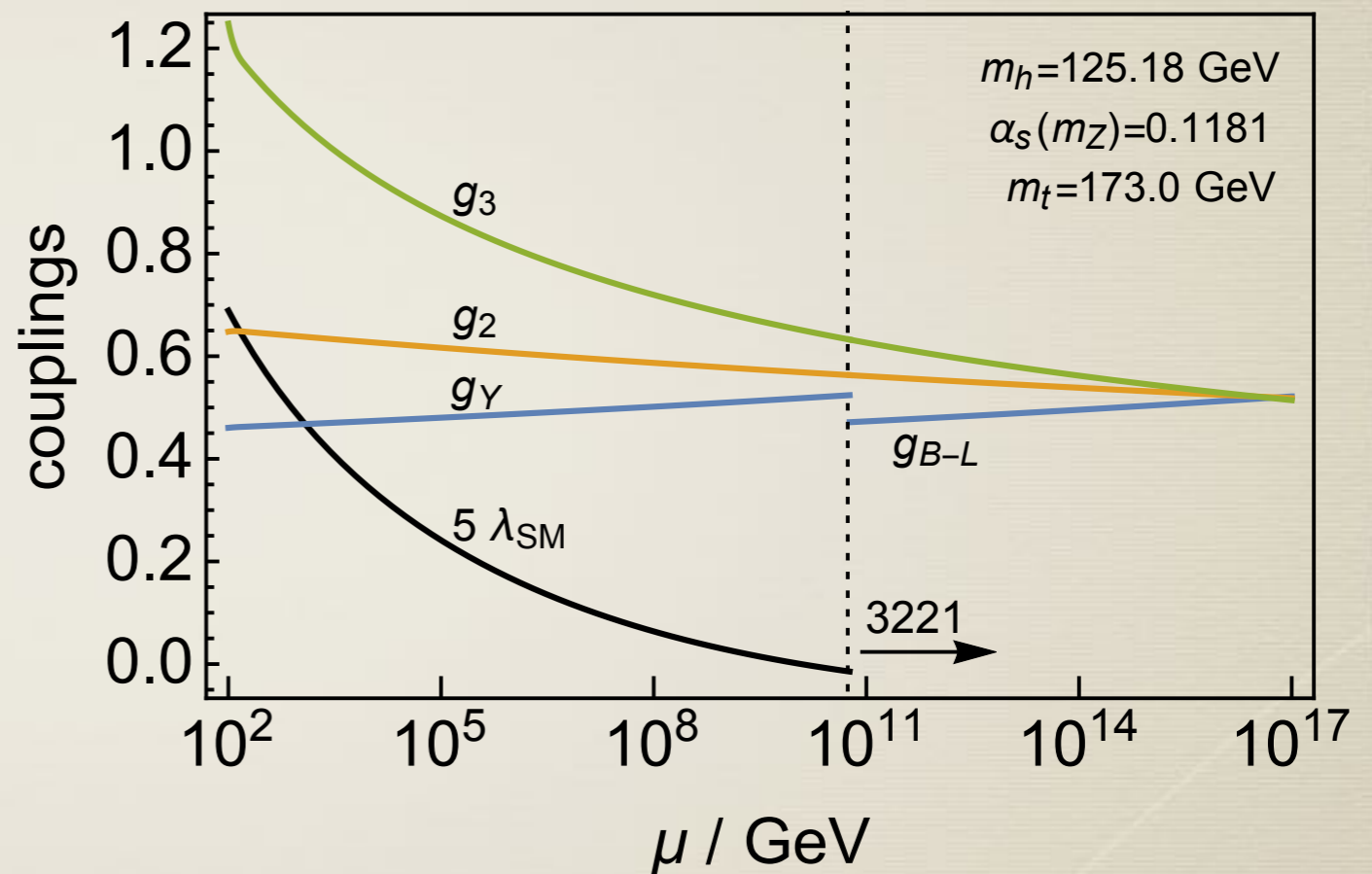
Grand Unification  
Proton decay



# Precise measurement and Grand Unification

Hall and KH (2018, 2019)

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 Higgs mass  
 strong coupling constant

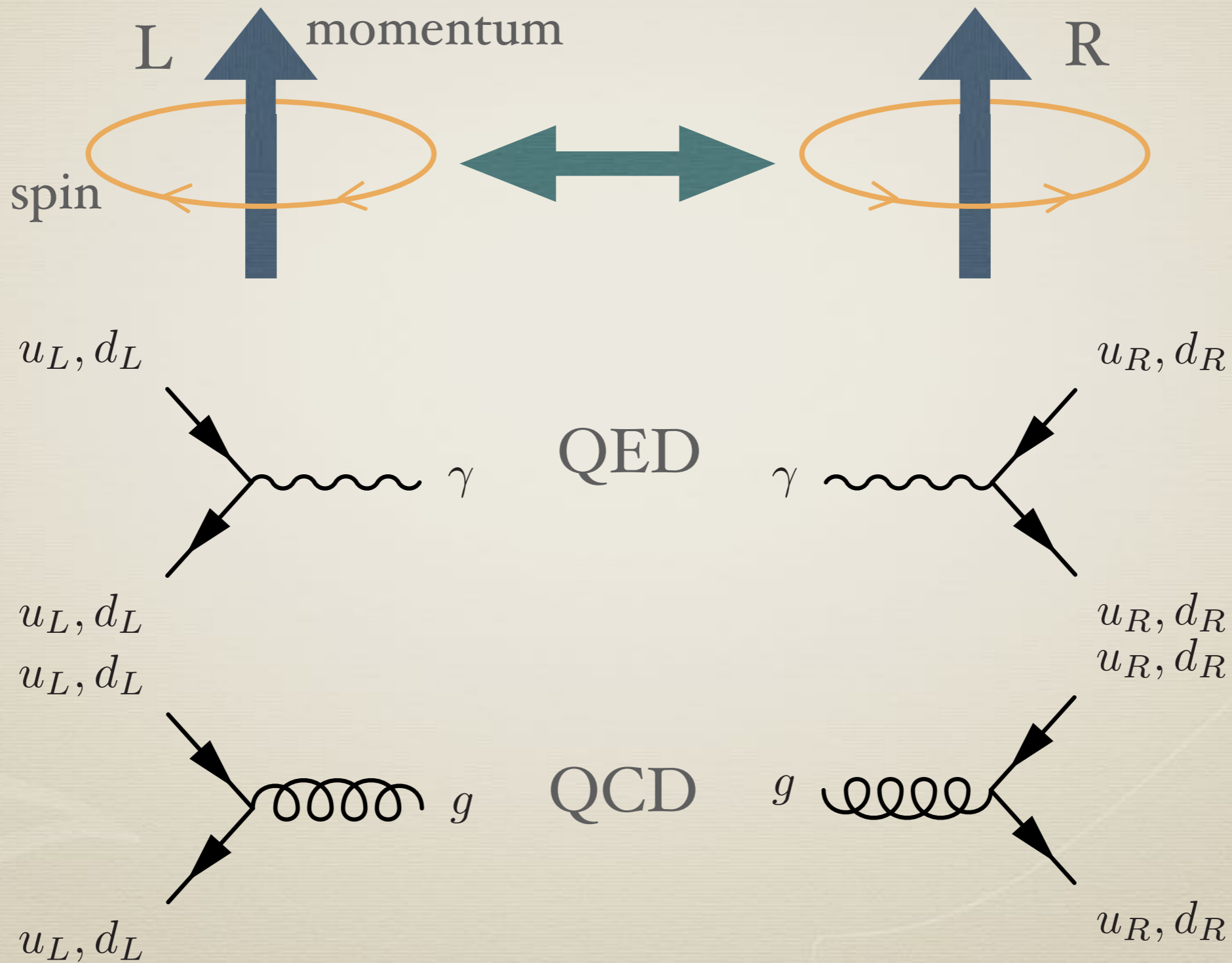


Left-Right  
 Higgs Parity  
 symmetry breaking scale



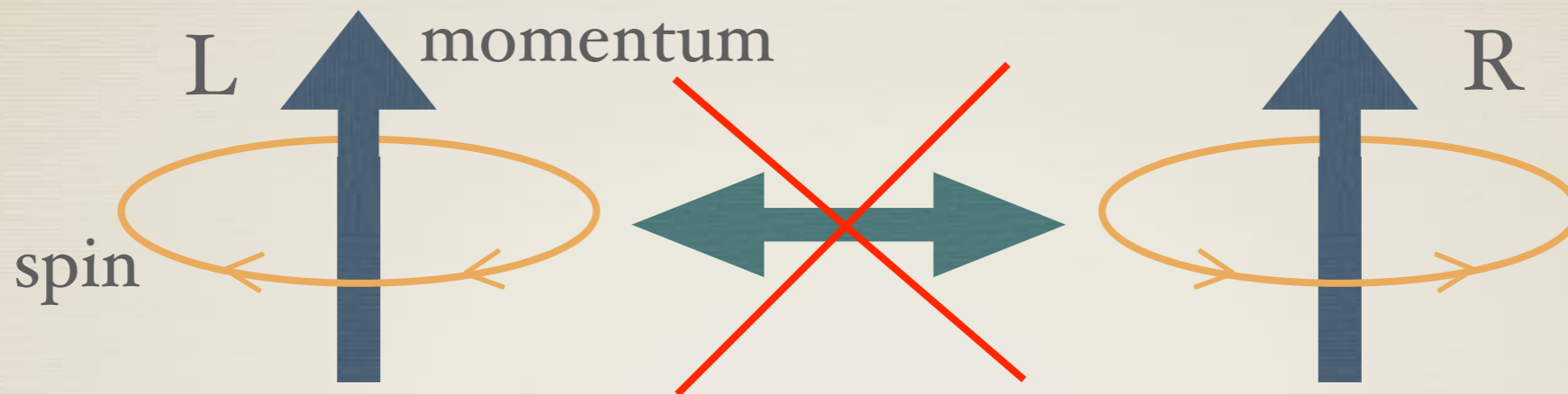
Grand Unification  
 Proton decay

# Left-Right symmetry

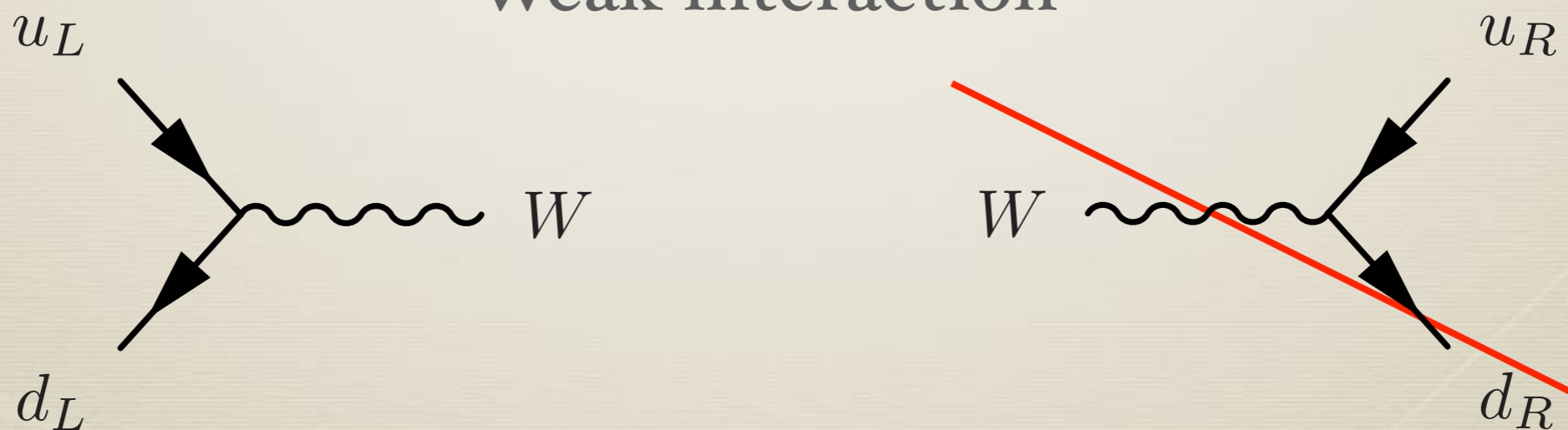




# Left-Right symmetry

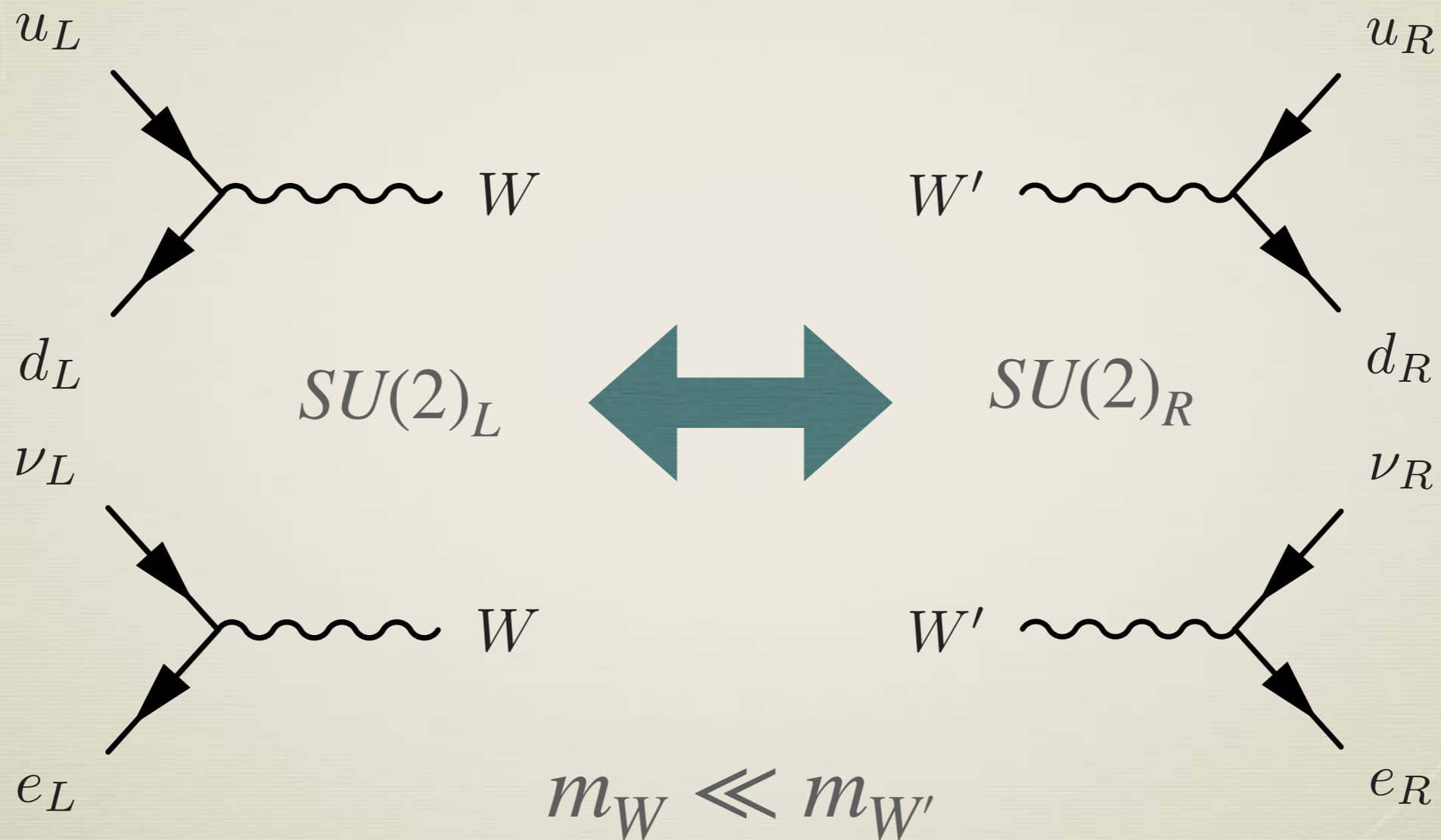


## Weak interaction



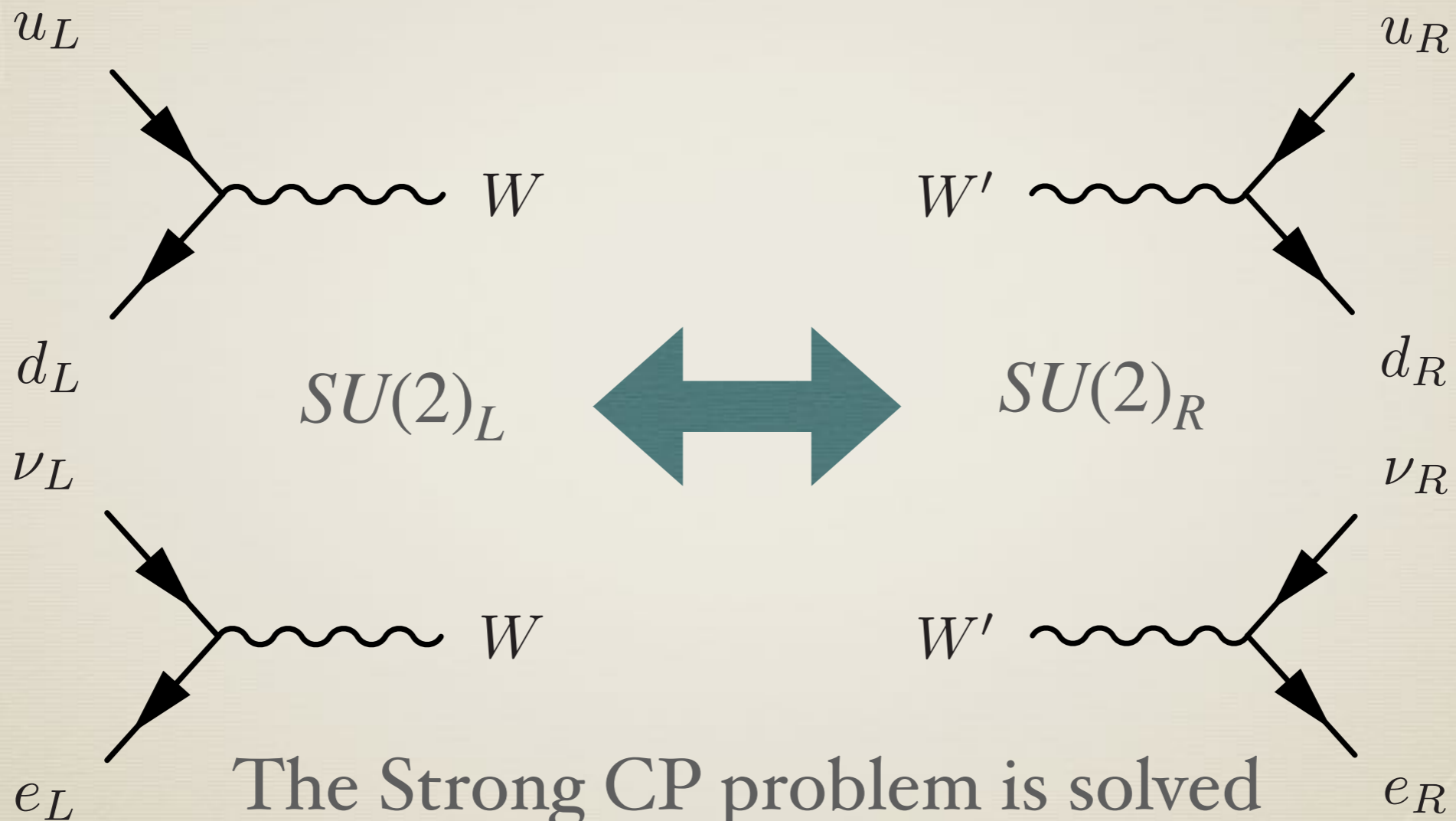
Lee and Yang (1956), Wu (1957)

# Spontaneously broken Left-Right symmetry



Lee (1973), Pati and Salam (1975),  
Moahapatra and Pati (1975), Senjanovic and Mohapatra (1975)

# Spontaneously broken Left-Right symmetry



The Strong CP problem is solved  
via space-time parity

~~$$H = d_n \vec{E} \cdot \vec{S}$$~~

Mohapatra and Senjanovic (1978), Beg and Tsao (1978),  
Babu and Mohapatra (1989), Hall and KH (2018)

# Left-Right Higgs Parity

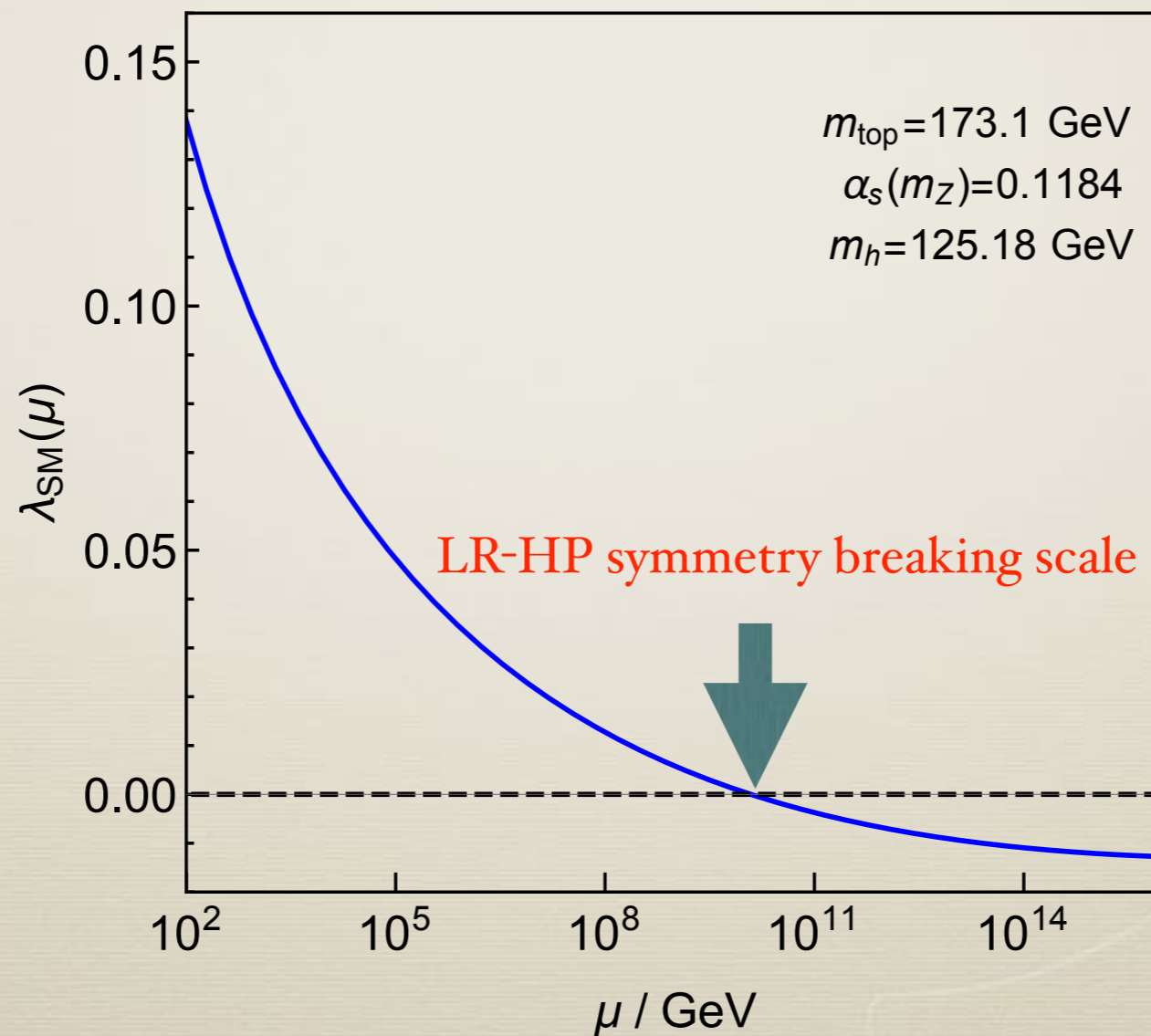
Higgs  $H$   $\longleftrightarrow$  Higgs'  $H'$

Weak gauge boson  $W$   $\longleftrightarrow$  Weak gauge boson'  $W'$   
 $SU(2)_L$   $SU(2)_R$

left-handed quark, lepton  $q_L, L_L$   $\longleftrightarrow$  right-handed quark, lepton  $q', L' = q_R, L_R$

$$SU(3)_c \times SU(2)_L \times \frac{SU(2)_R \times U(1)}{\langle H' \rangle} \rightarrow U(1)_Y$$

# Left-Right Higgs Parity



# Left-Right symmetry and Grand Unified Theory

Grand Unification  
 $SO(10)$



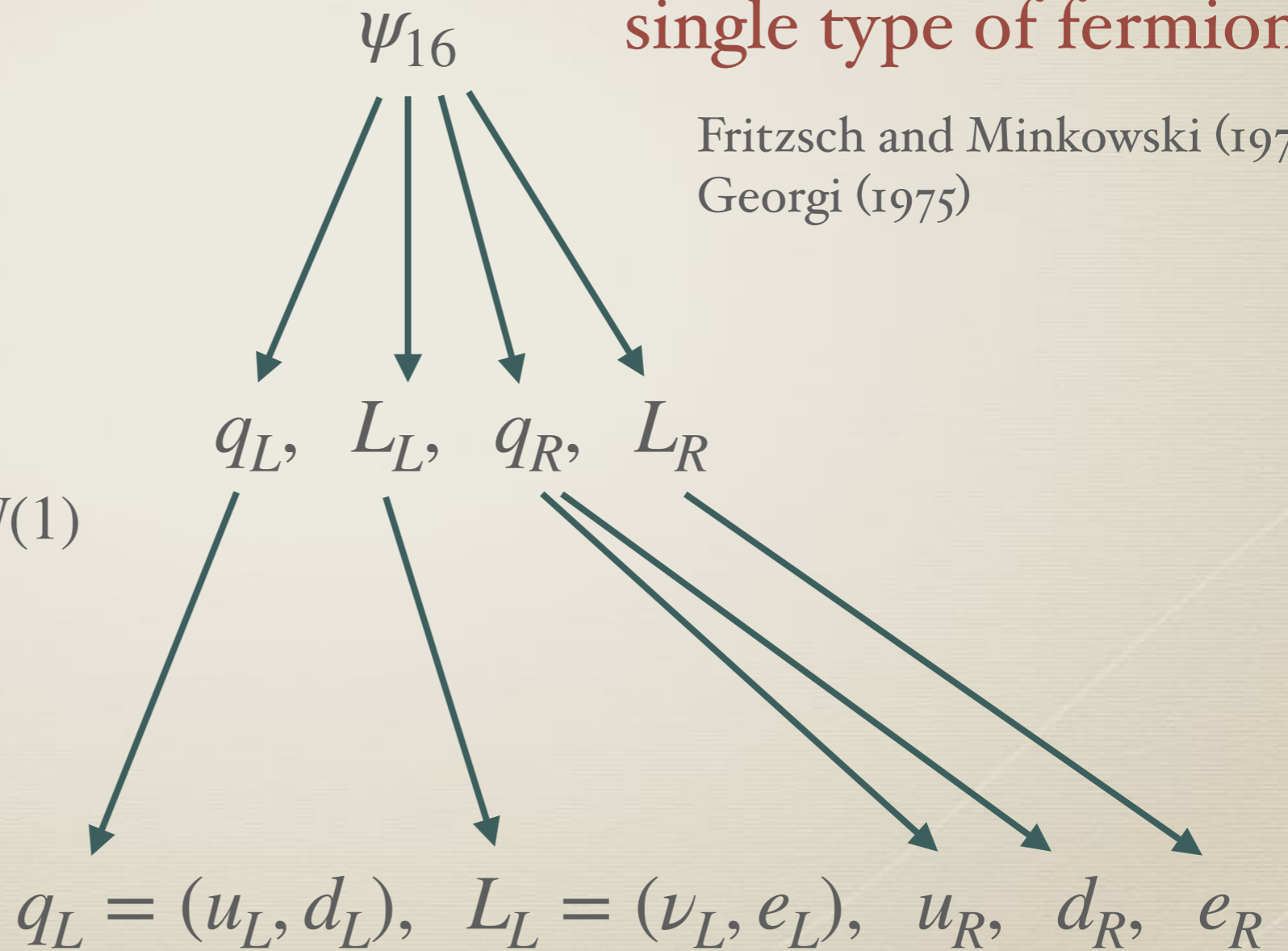
Left-Right Symmetry  
 $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)$



Standard Model  
 $SU(3)_c \times SU(2)_L \times U(1)_Y$

Single gauge group,  
single type of fermions

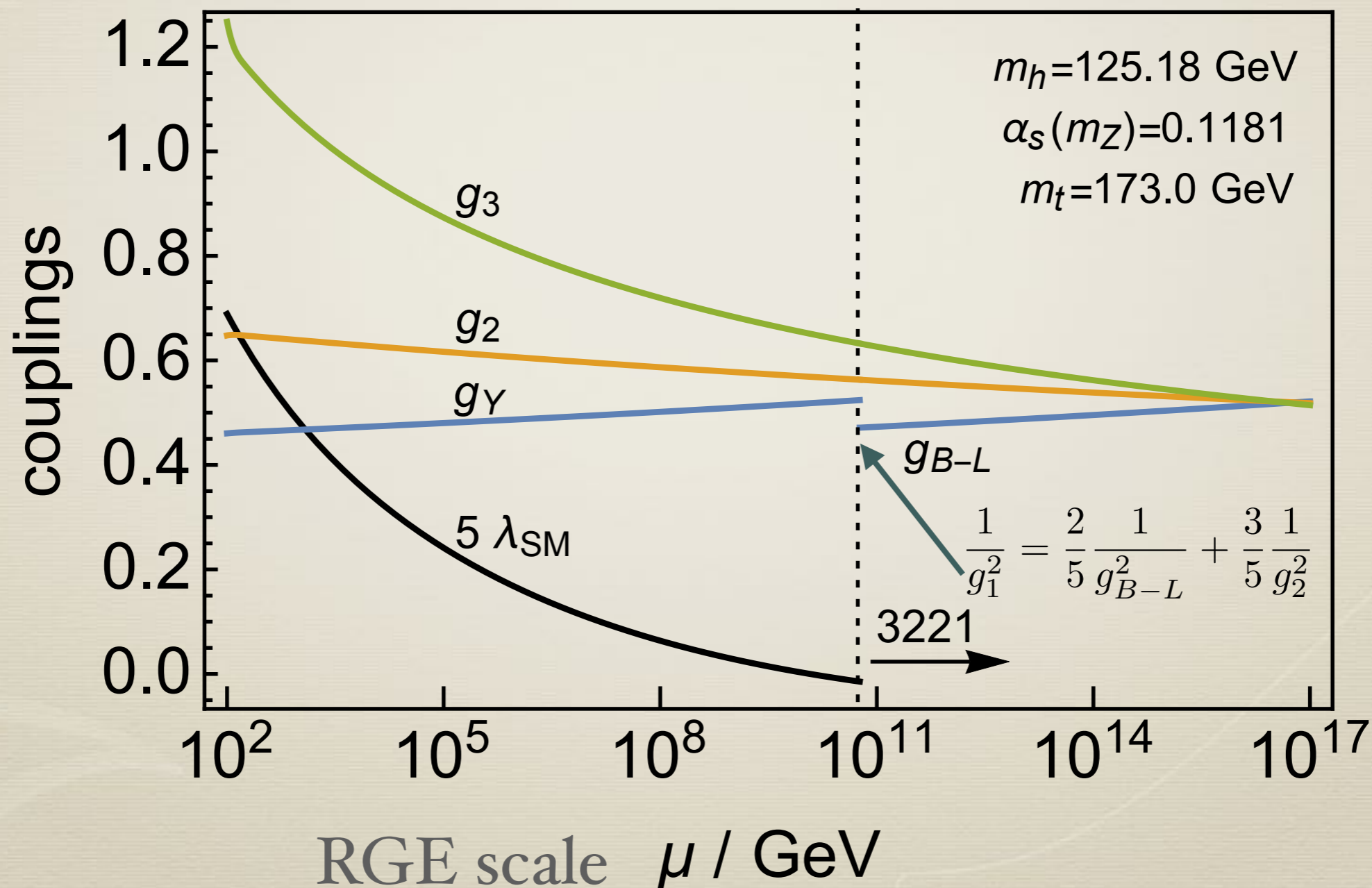
Fritzsch and Minkowski (1975),  
Georgi (1975)



# Coupling unification

Hall, KH (2018, 2019)

energy-dependent couplings

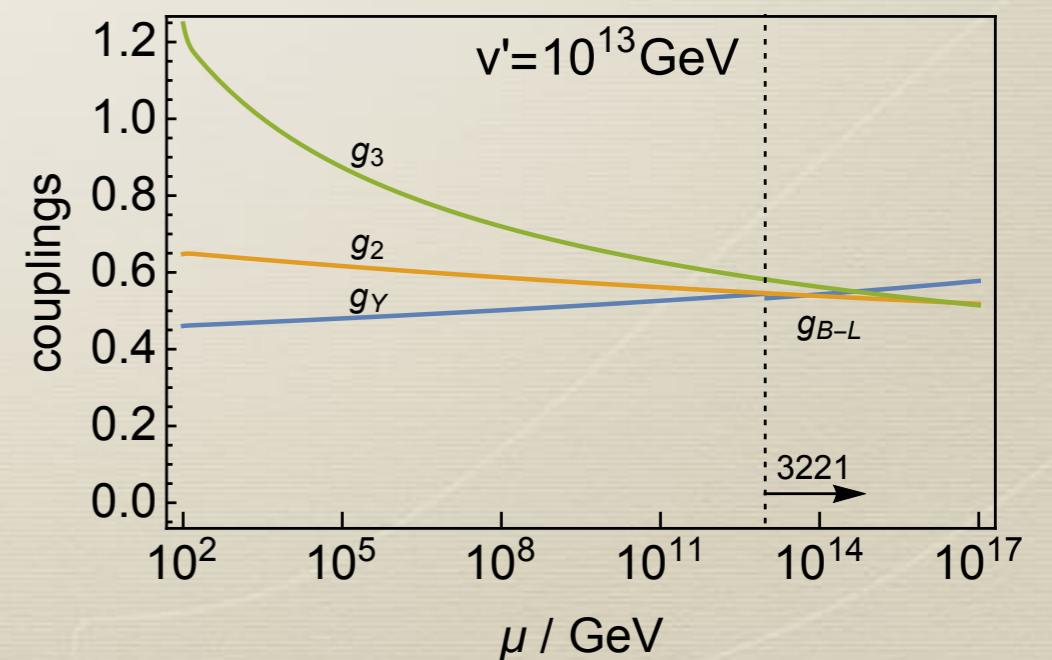
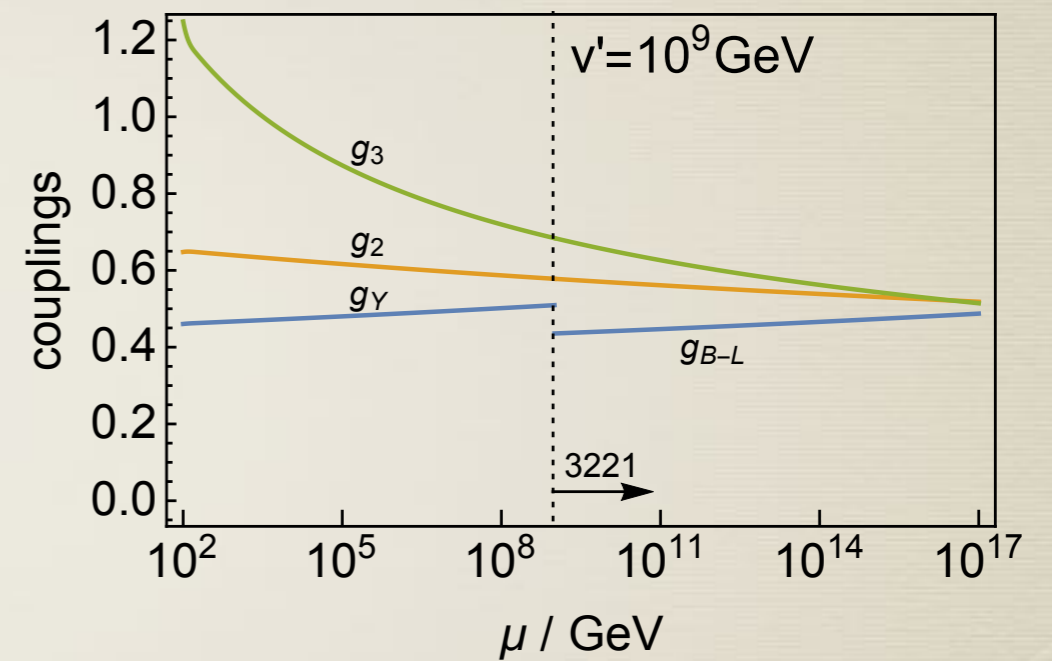
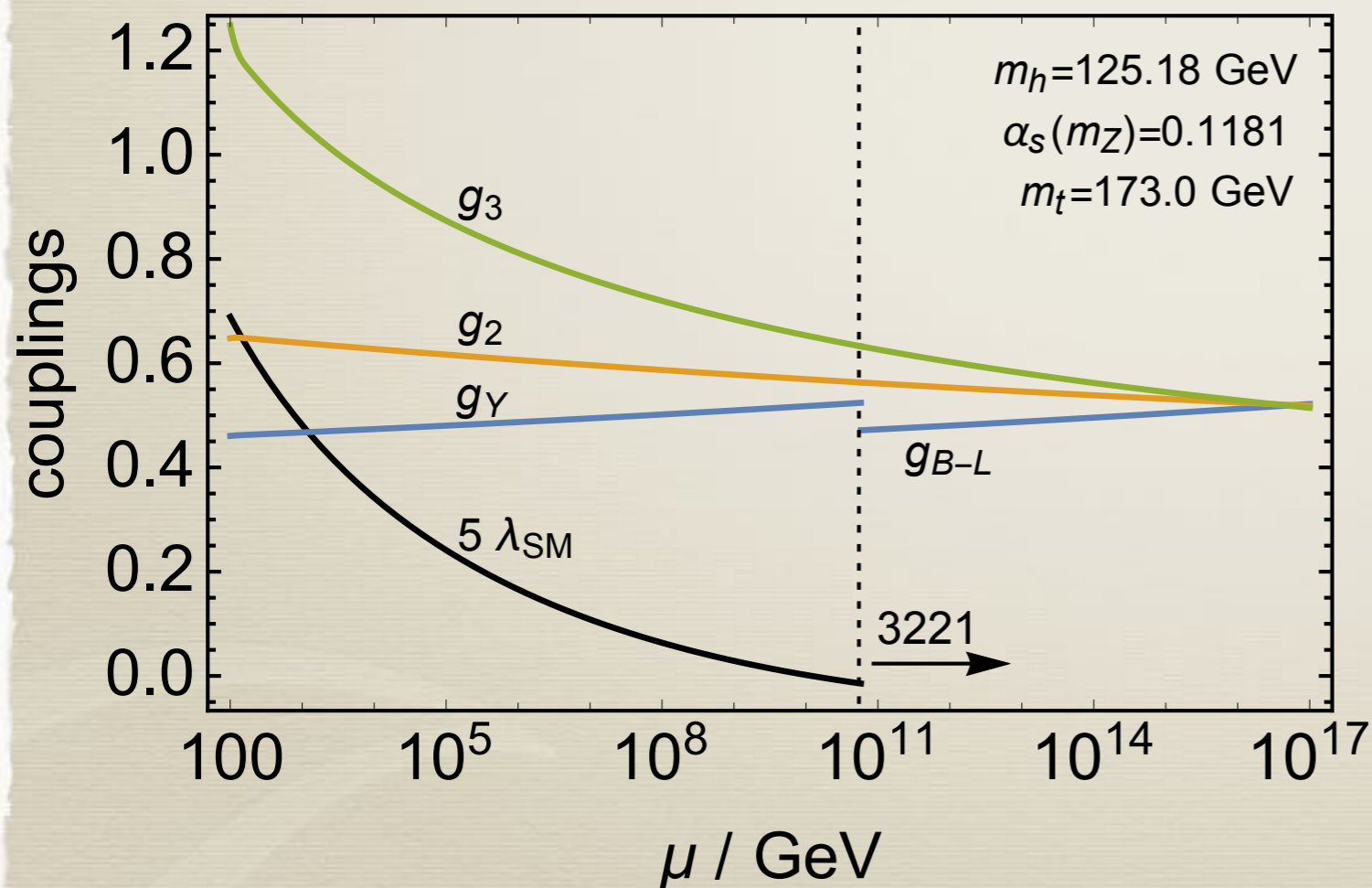


# Coupling unification

Hall, KH (2018, 2019)

Other  $\nu'$

$\nu'$  determined by Higgs Parity

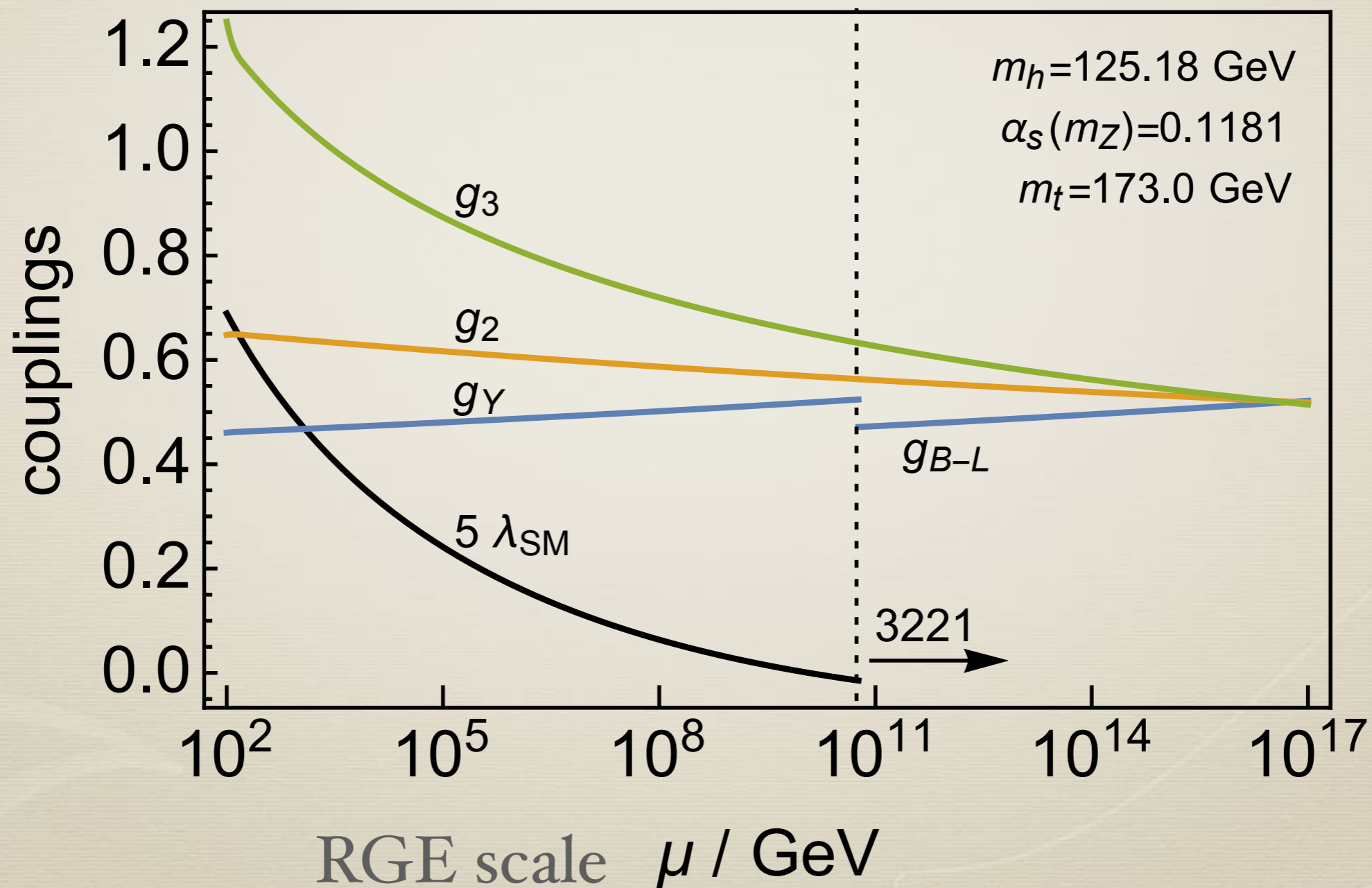




# Higgs Parity GUT

Hall, KH (2018, 2019)

energy-dependent couplings



# Higgs Parity GUT

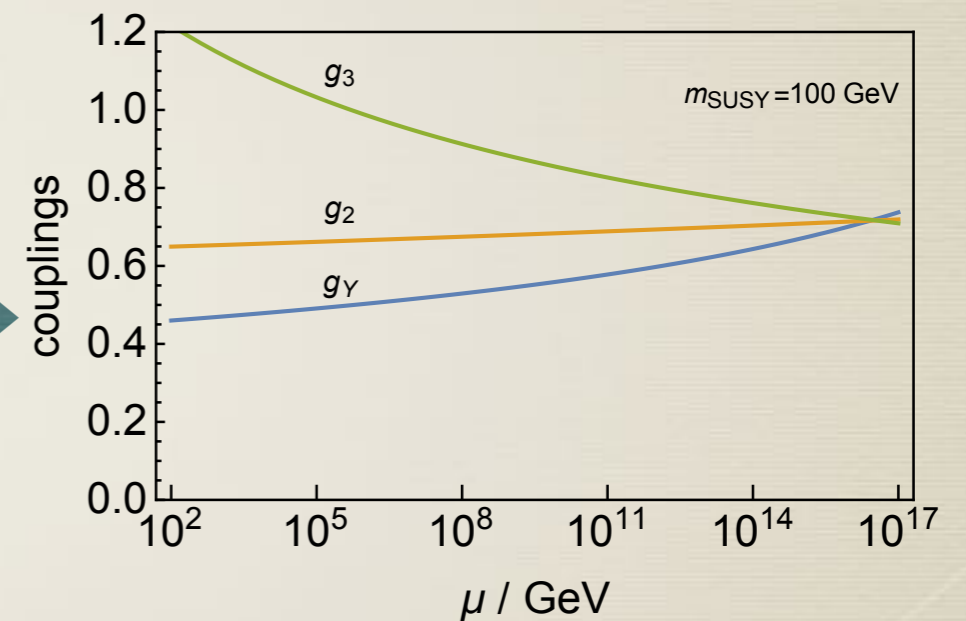
Hall, KH (2018, 2019)

weak scale  $10^2$  GeV

GUT scale  $10^{16}$  GeV

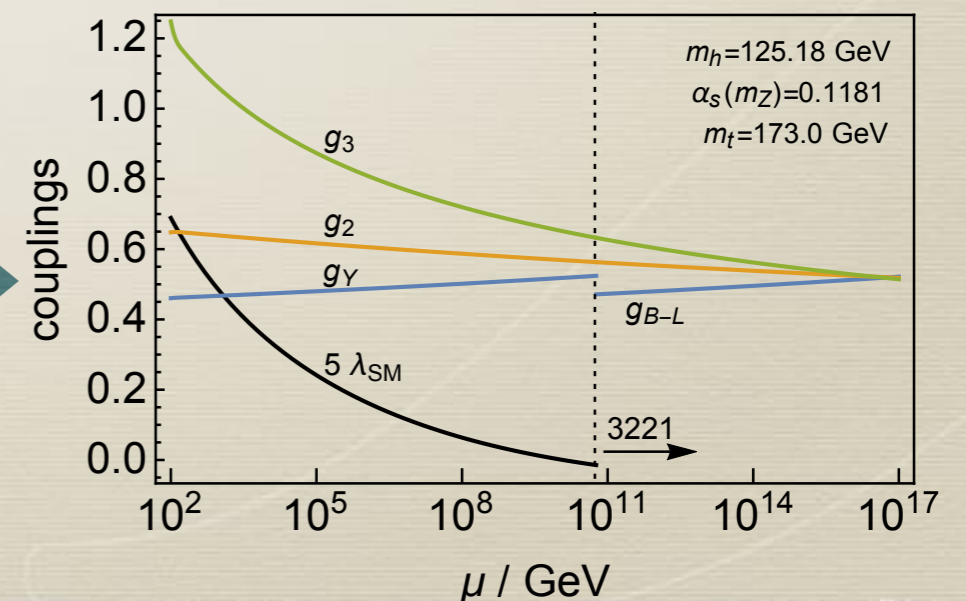
gauge coupling constants  
(LEP, ...)

SUSY GUT

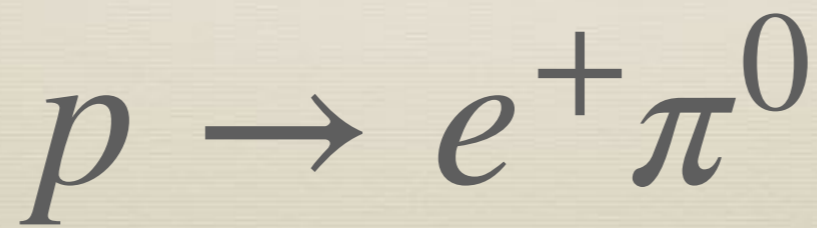
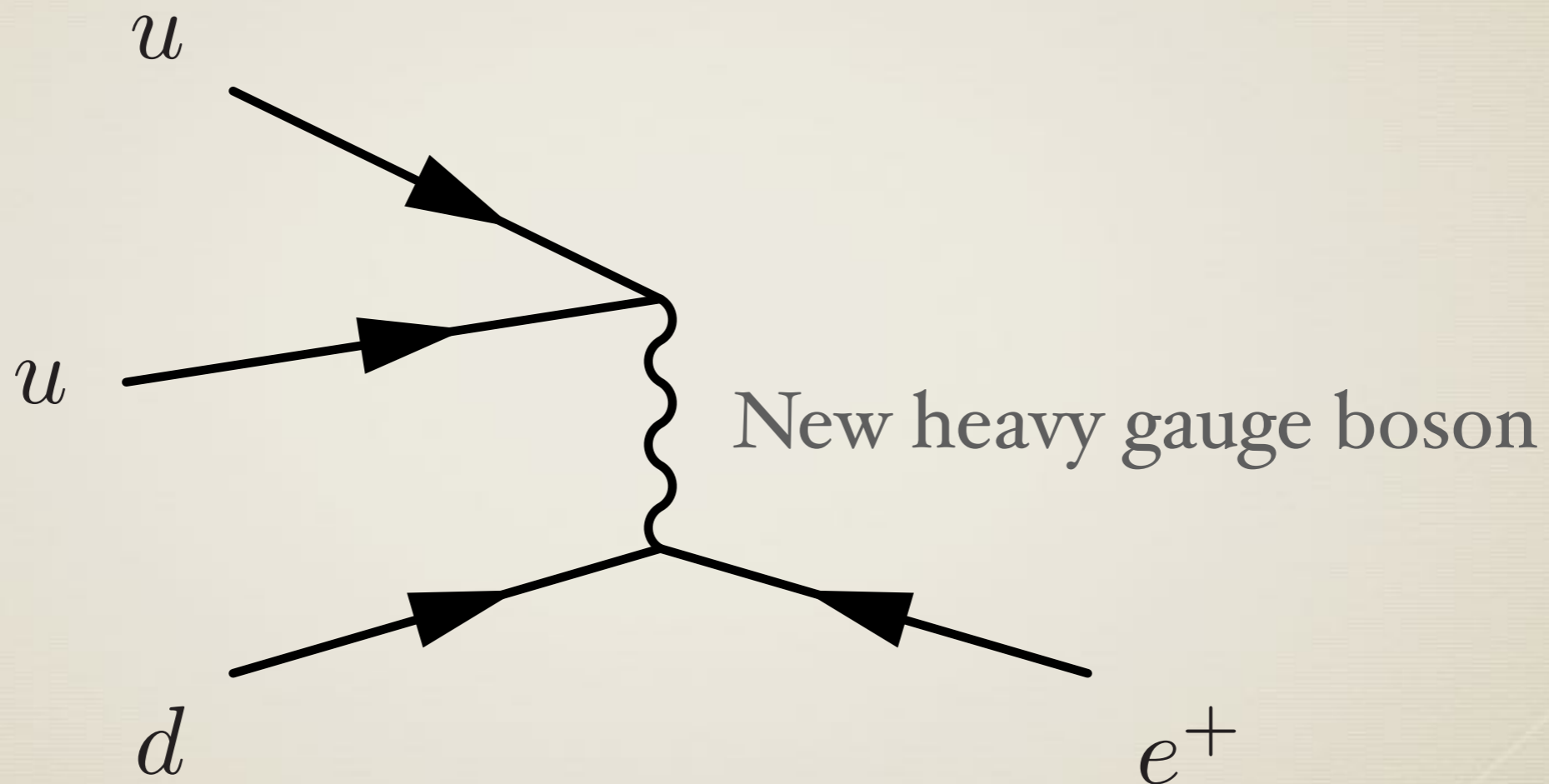


gauge coupling constants  
top quark mass  
Higgs mass  
(LHC, lattice, future colliders, ...)

HP GUT



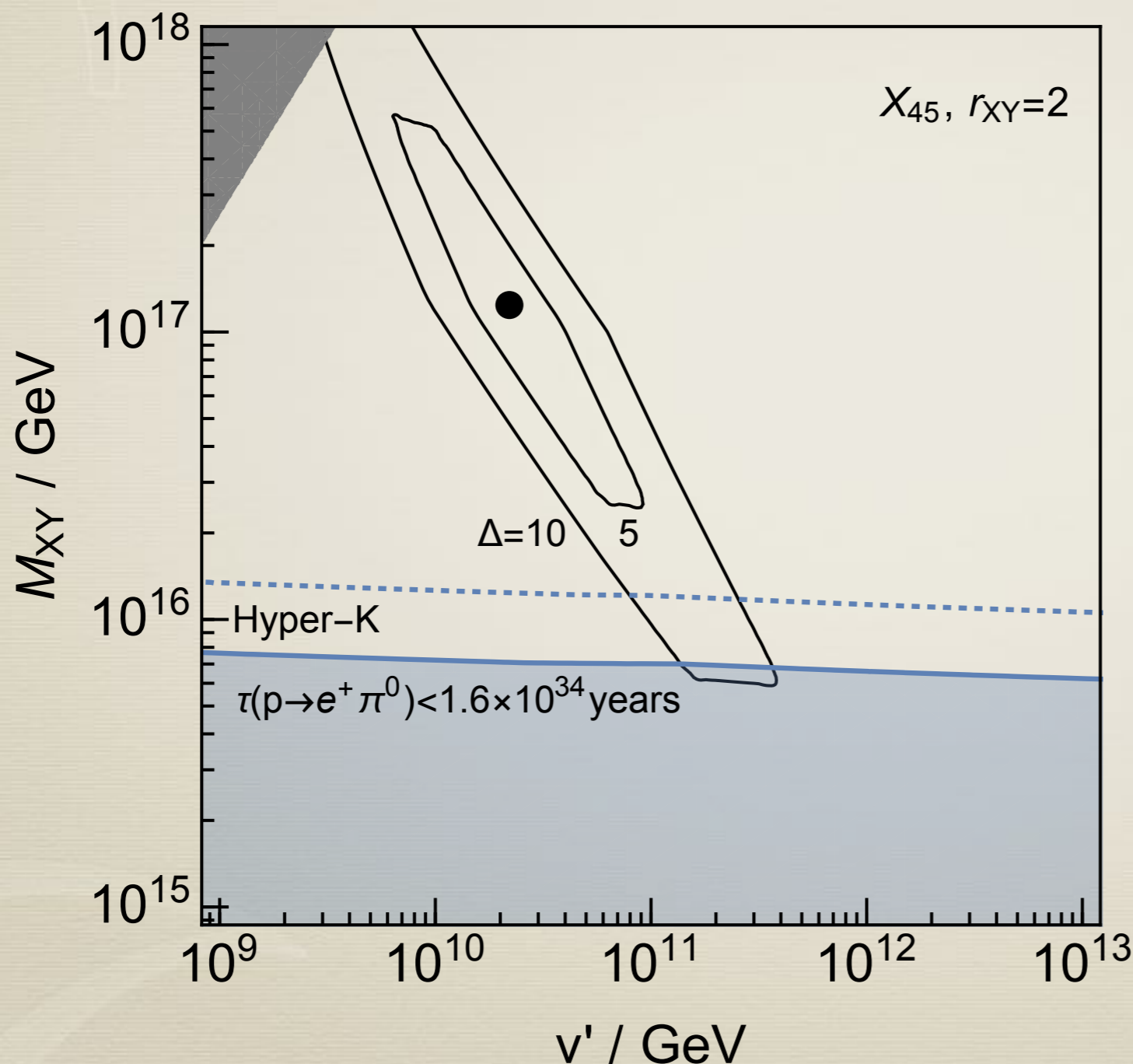
# Proton decay



# Quantify unification

Hall, KH (2019)

mass of new gauge boson  
mediating proton decay



There can be quantum corrections from heavy particles around the GUT scale

$$\Delta = \max_{i,j} \left| \frac{8\pi^2}{g_i^2} - \frac{8\pi^2}{g_j^2} \right|$$

typically

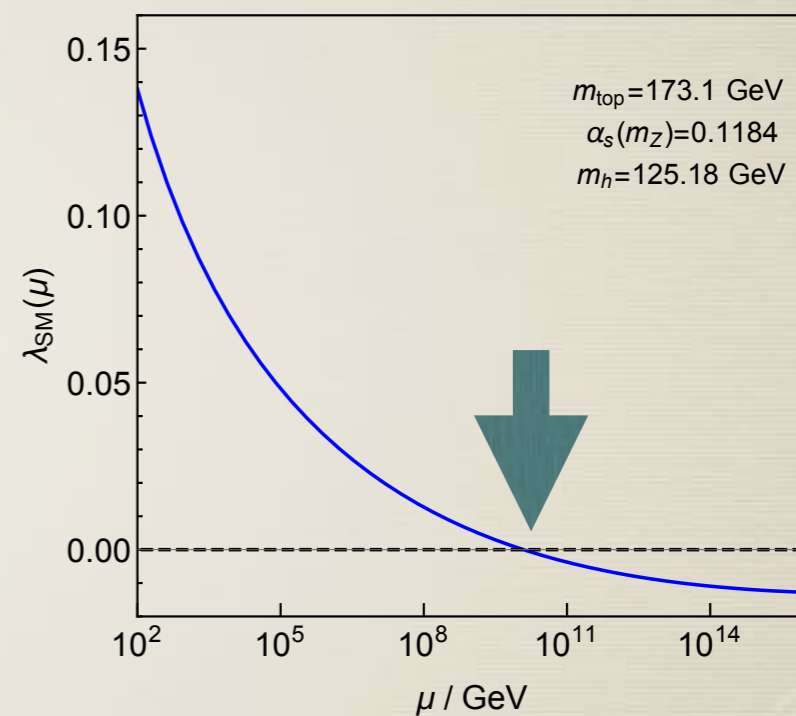
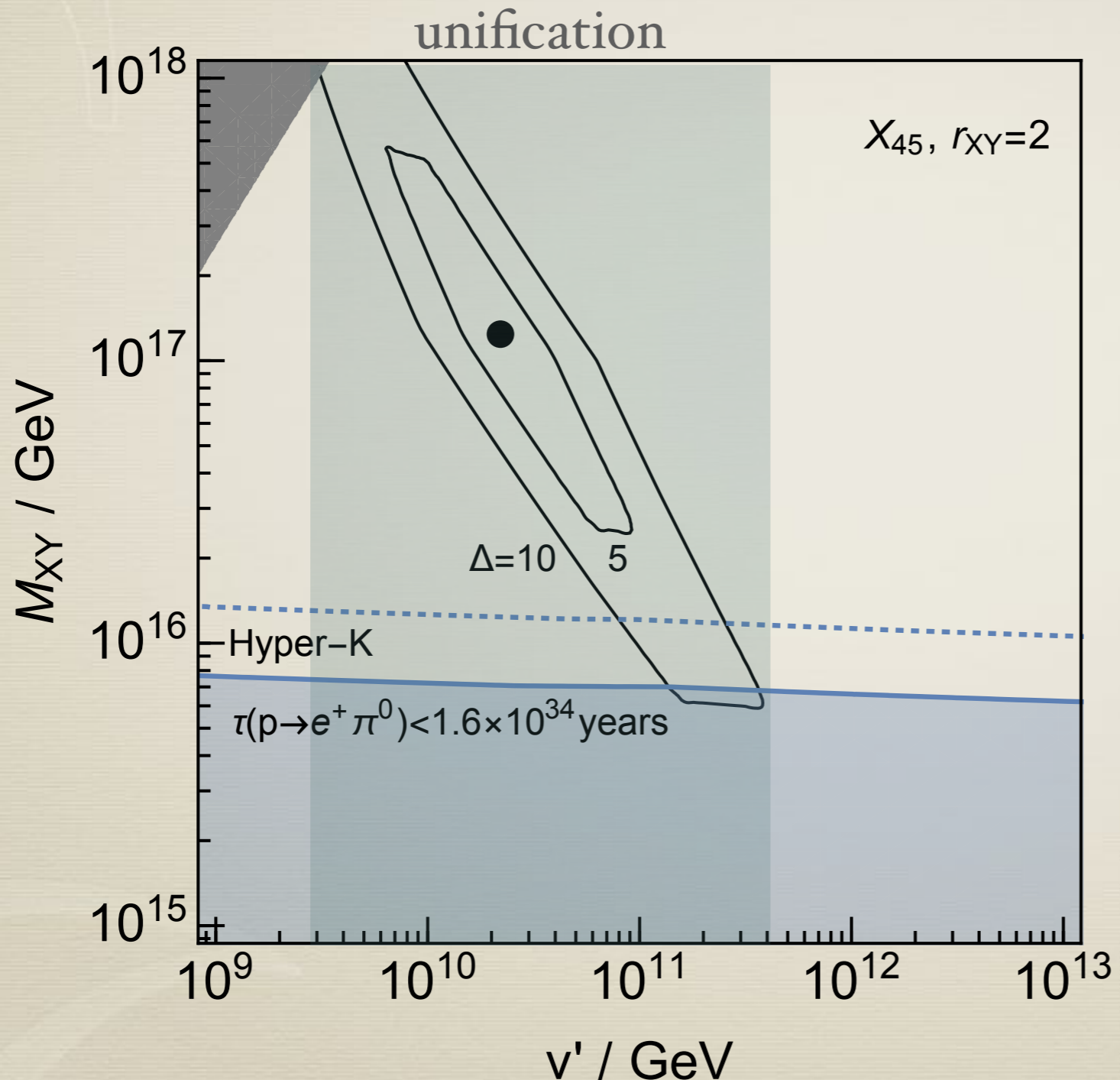
$$\Delta = \text{few} - 10$$

(smaller than SUSY GUT)

# Quantify unification

Hall, KH (2019)

mass of new gauge boson  
mediating proton decay

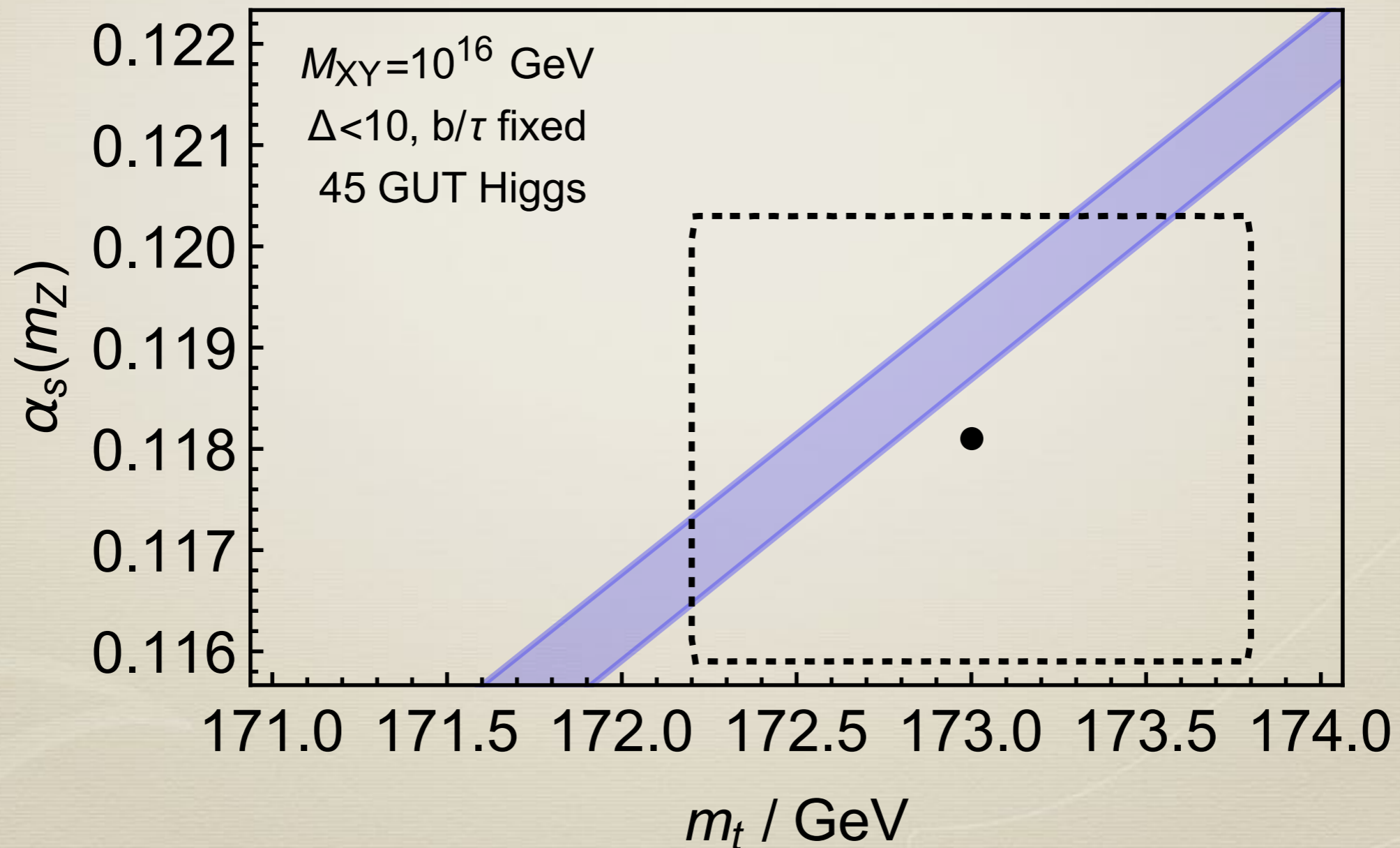


typically  
 $\Delta = \text{few} - 10$   
(smaller than SUSY GUT)

# Proton decay

Hall, KH (2019)

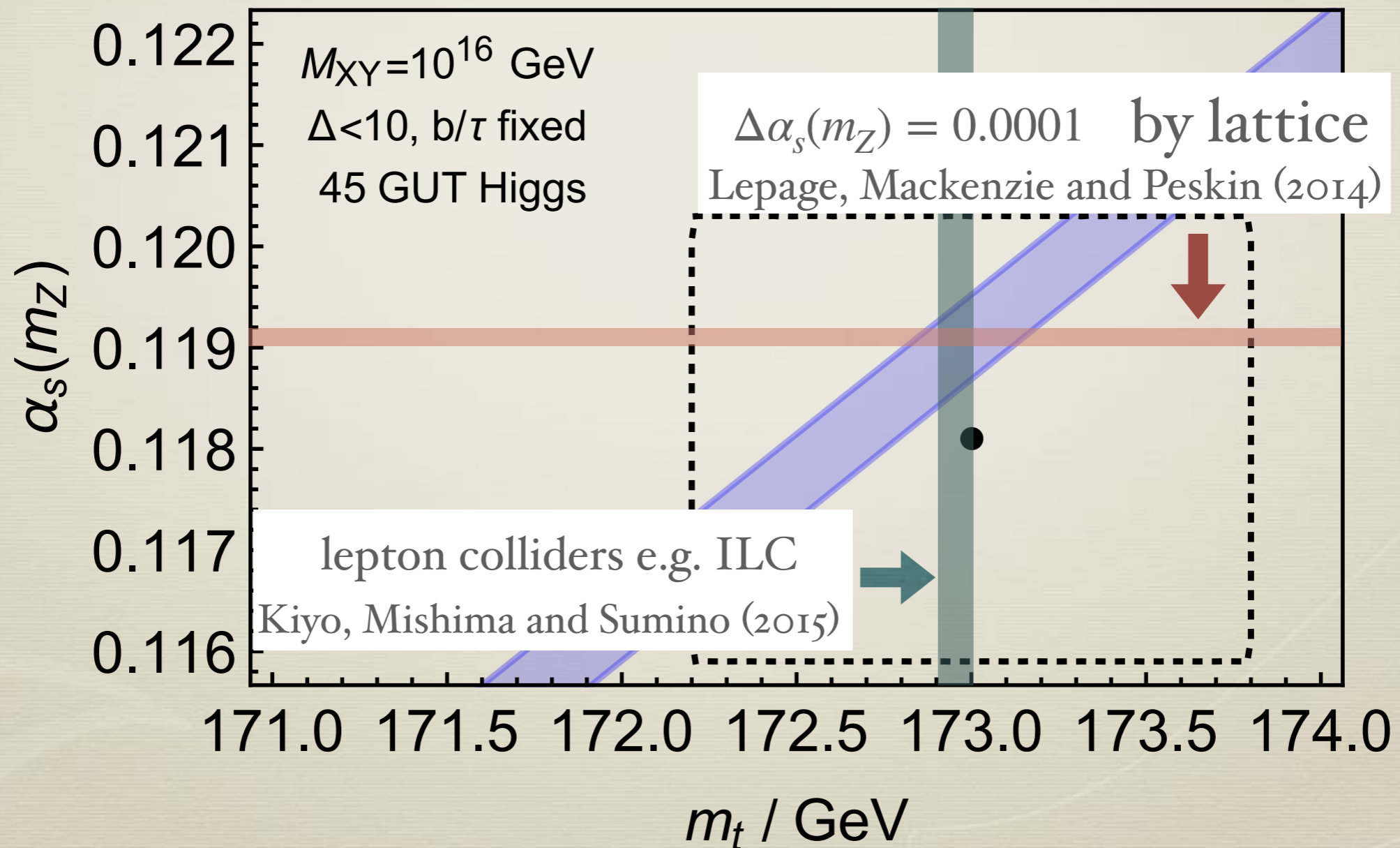
Suppose proton decay is observed at Hyper-K (2027-)



# Proton decay

Hall, KH (2019)

Suppose proton decay is observed at Hyper-K (2027-)



# Intermediate Pati-Salam

Grand Unification  
 $SO(10)$

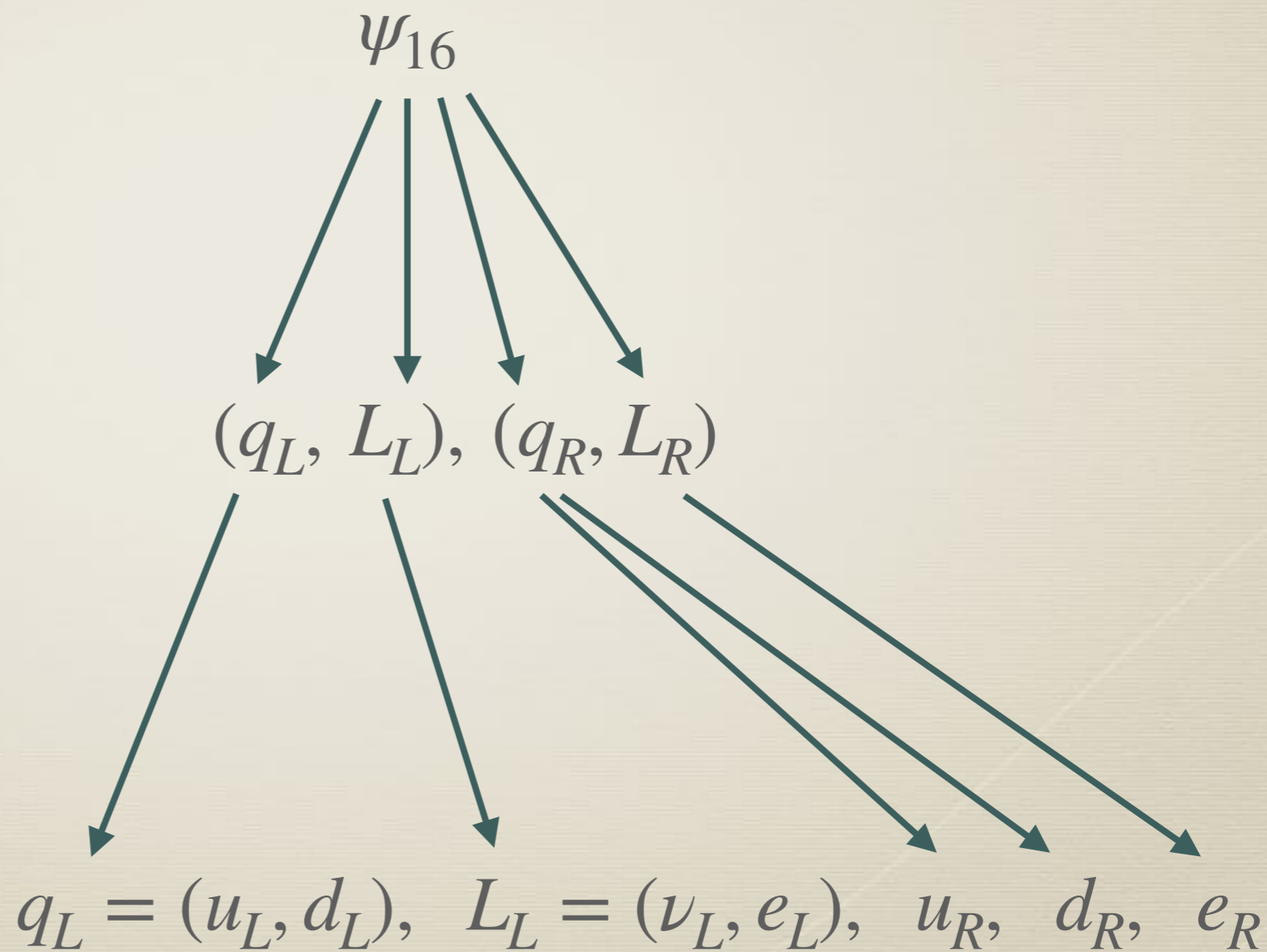


Pati-Salam group  
 $SU(4) \times SU(2)_L \times SU(2)_R$



$\langle H' \rangle \neq 0$

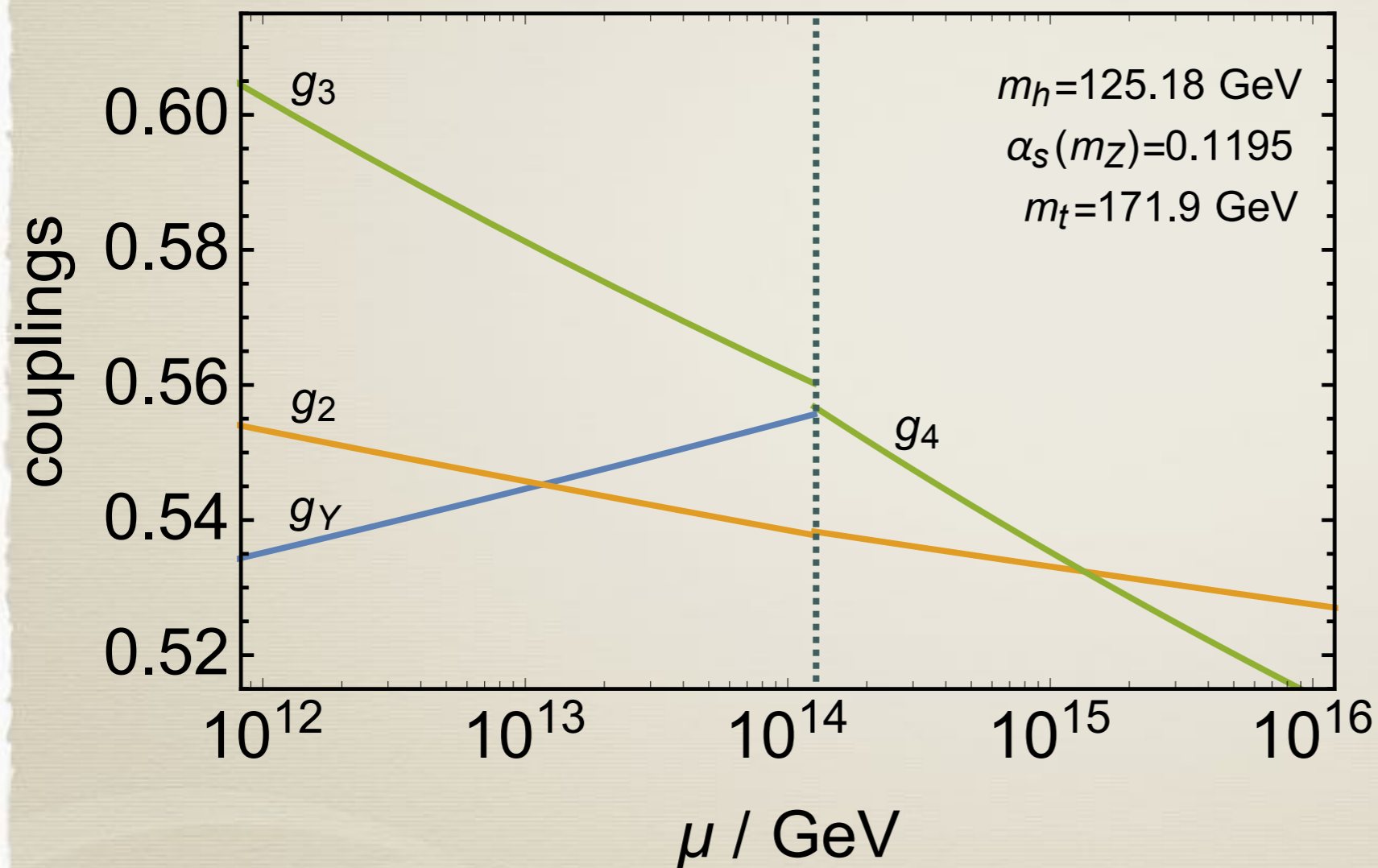
Standard Model  
 $SU(3)_c \times SU(2)_L \times U(1)_Y$





# Intermediate Pati-Salam

Hall, KH (2018, 2019)

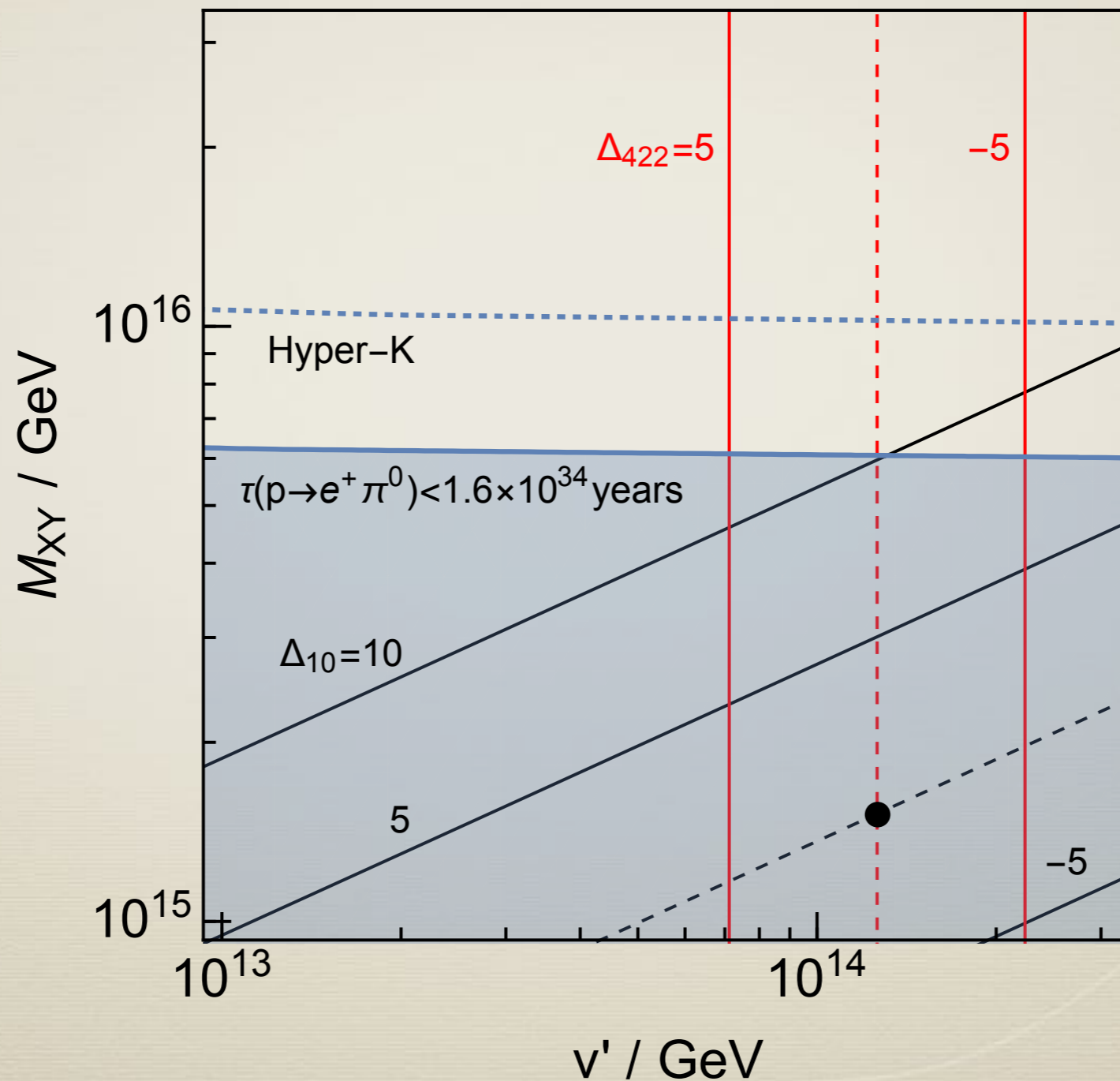


$SU(4) \times SU(2)_L \times SU(2)_R$   
 2 couplings

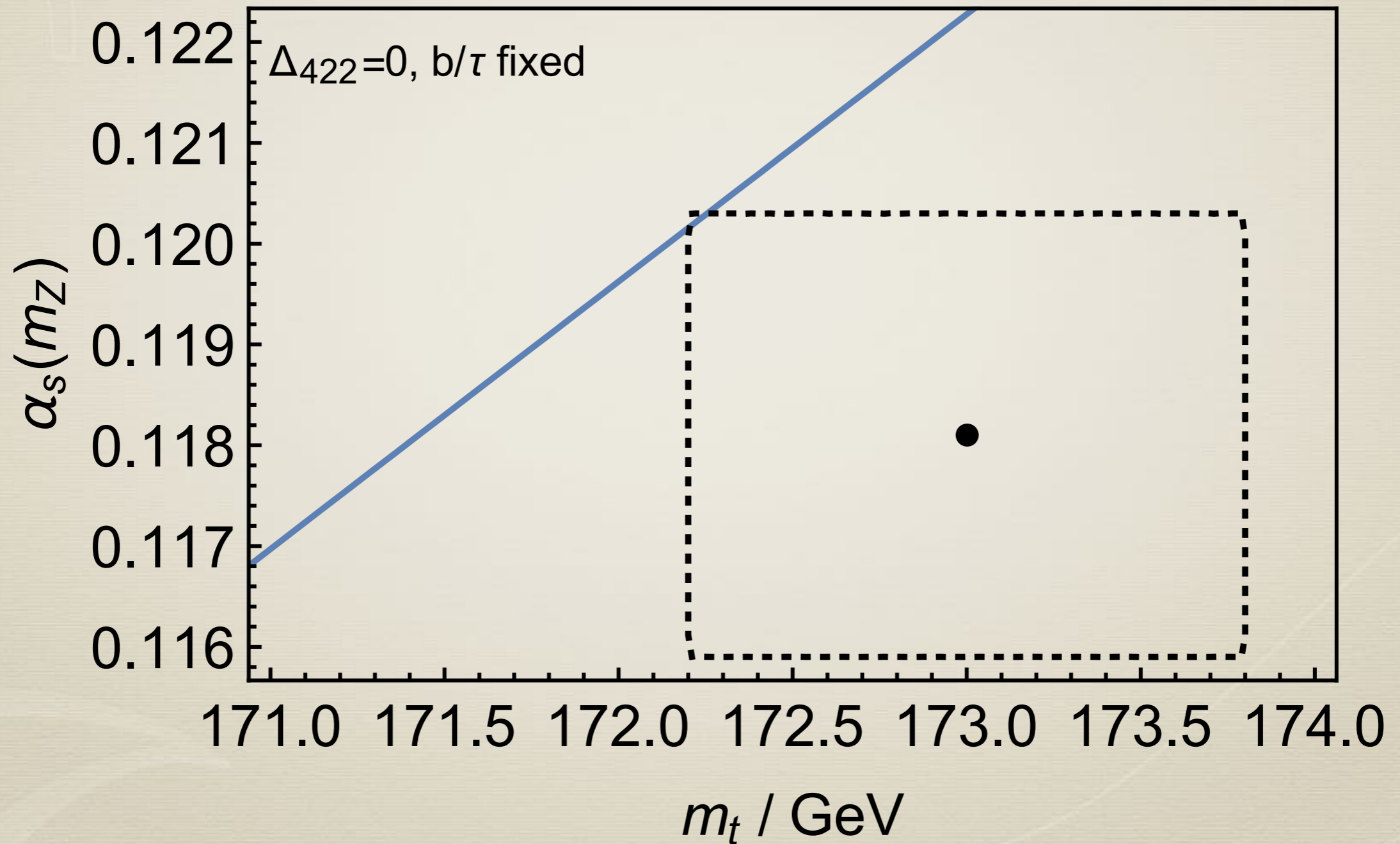
Pati-Salam scale is  
 fixed by coupling unification

$$\frac{1}{g_1^2} \simeq \frac{2}{5} \frac{1}{g_4^2} + \frac{3}{5} \frac{1}{g_2^2}$$

# Pati-Salam



# Pati-Salam

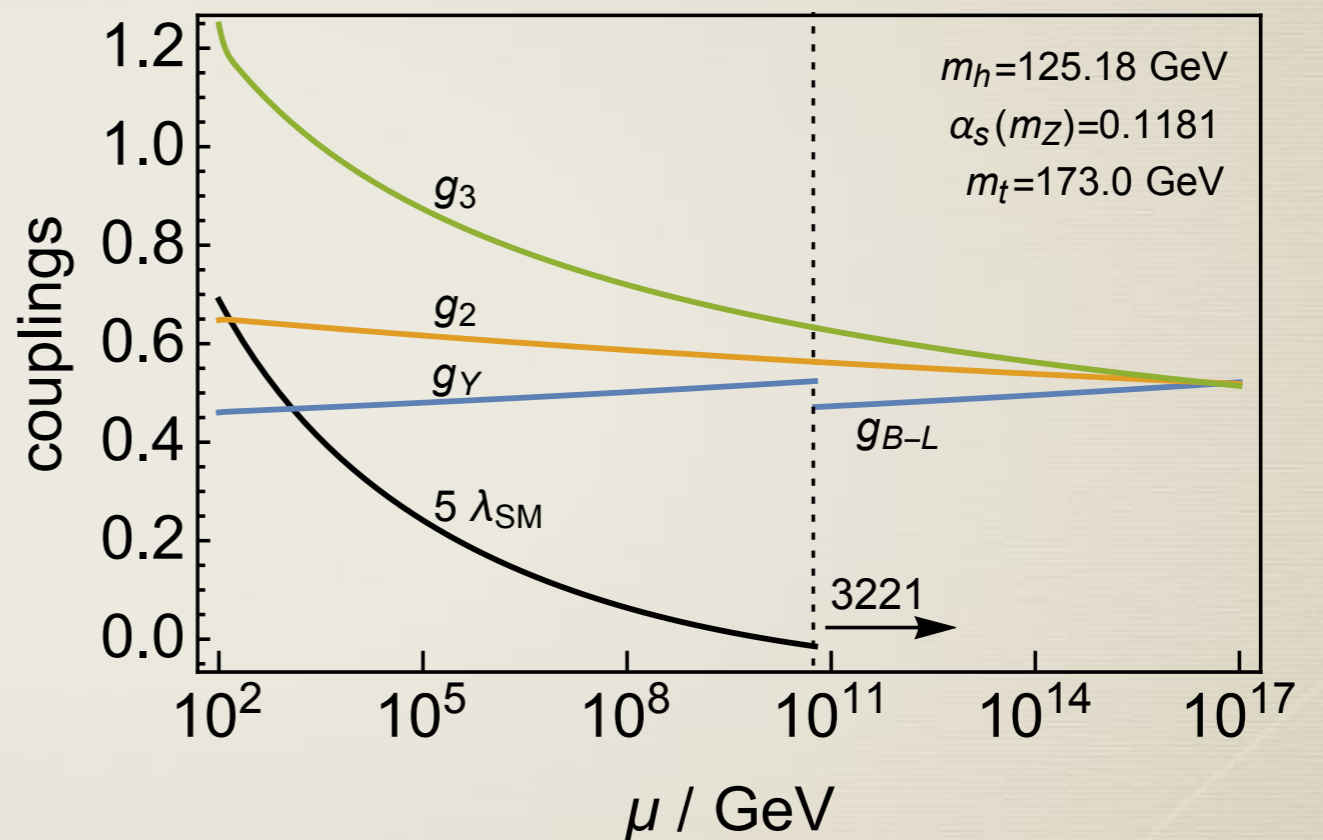


# Summary and outlook

# Higgs Parity

Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)

top quark mass  
Higgs mass  
strong coupling constant



Higgs Parity  
symmetry breaking scale



Grand unification  
proton decay

(dark matter detection, gravitational waves,  
dark radiation, warm dark matter, neutron EDM, axion, ...)

# Other models with Higgs Parity

\*  $SU(3)_c \times SU(2)_L \times SU(2)' \times U(1)_Y \times U(1)'_Y$

Dunsky, Hall and KH, [1902.07726](#)

Dark matter direct detection rate is predicted from  
the SM parameters

[backup](#)

\* A model with a mirror copy of the SM

Dunsky, Hall and KH, [1908.02756](#)

Dark radiation and gravitational wave abundance are  
predicted from SM parameters

[backup](#)

\* A model with a sterile neutrino DM and leptogenesis

Dror, Dunsky, Hall and KH, [2004.09511](#)

Dunsky, Hall and KH, [2007.12711](#)

Strong CP problem is solved via parity. Possible range  
of sterile neutrino DM mass and warmness is  
predicted from SM parameters

# Future of colliders

We should maximize the impact of future colliders



\* Searches for new particles

\* Searches for deviation from the standard model predictions

$$N_{\text{events}} = N_{\text{SM prediction}} ?$$

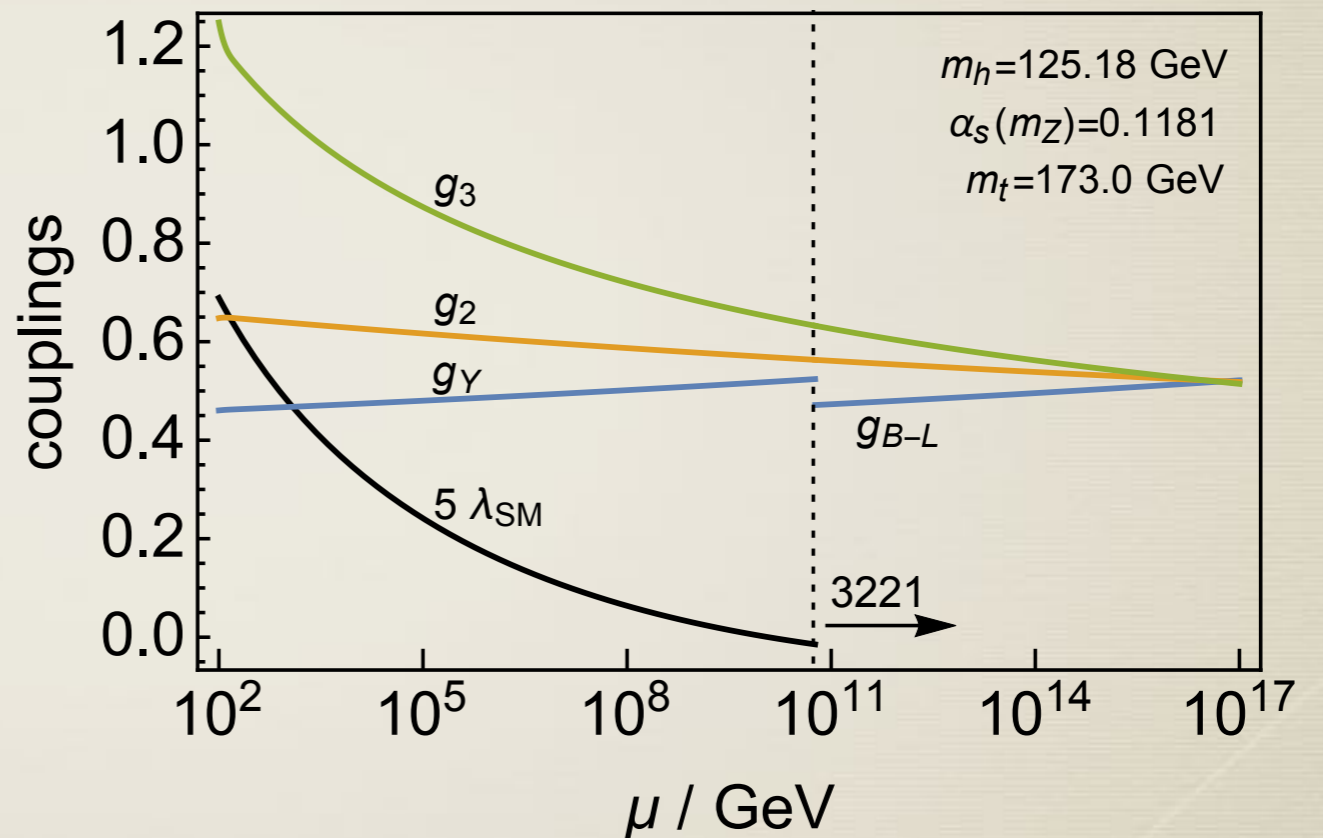
\* **Precise measurement of the standard model parameters**  
top quark mass,  
strong coupling constant,  
Higgs mass, etc.

Any other new physics models  
impacted by precise measurements?

# Higgs Parity

Hall and KH (2018, 2019)  
Dunsky, Hall and KH (2019)

top quark mass  
Higgs mass  
strong coupling constant



Higgs Parity  
symmetry breaking scale



Grand unification  
proton decay

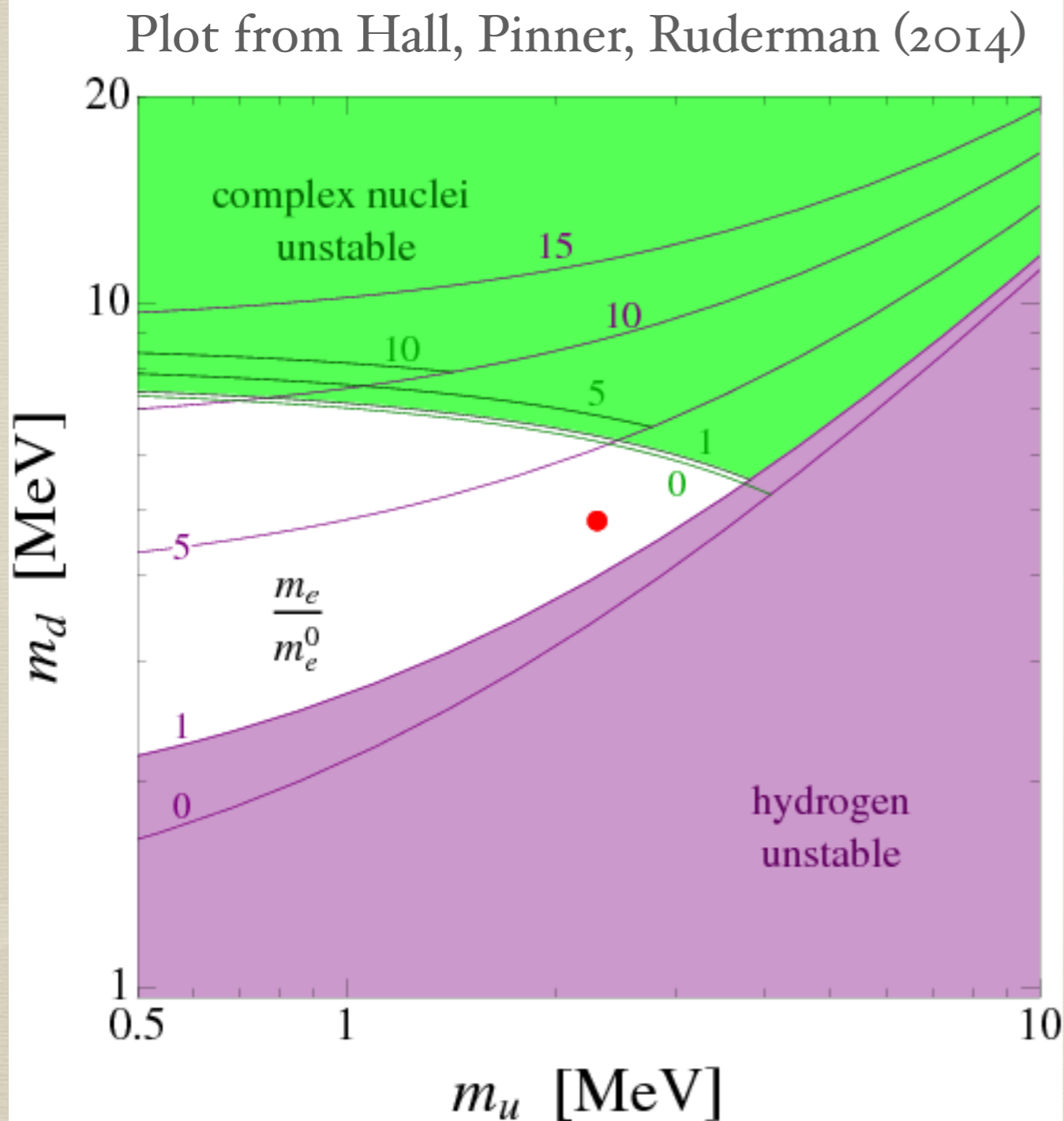
(dark matter detection, gravitational waves,  
dark radiation, warm dark matter, neutron EDM, axion, ...)



Back up

# On fine-tuning

# Stability of nuclei



We need smaller yukawa to compensate large  $\nu$

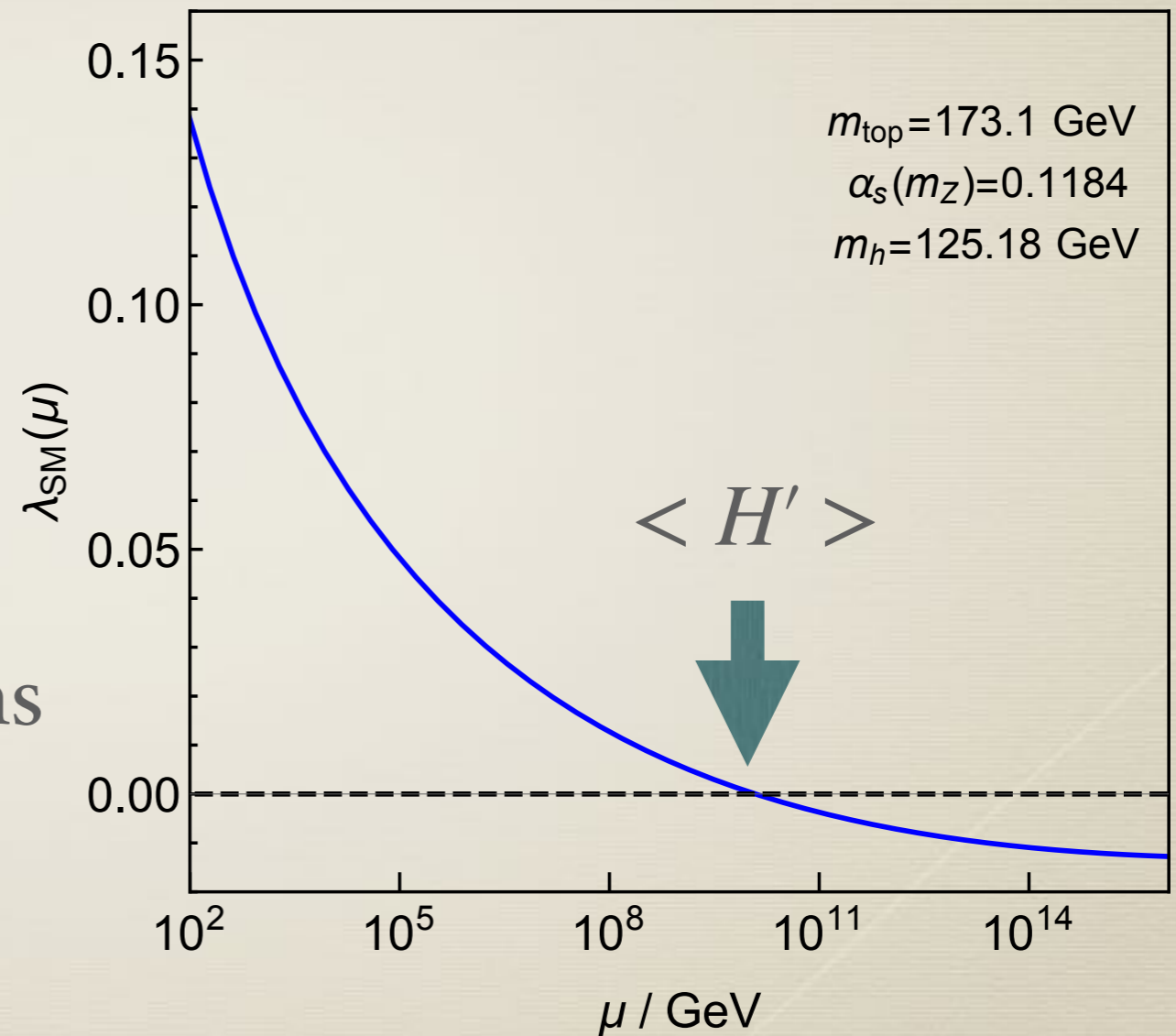
Detail about Small quartic

# HP symmetry breaking scale

I will show that

$$\lambda_{\text{SM}}(\langle H' \rangle) \simeq 0$$

because Higgs Parity constrains  
the potential of H and H'



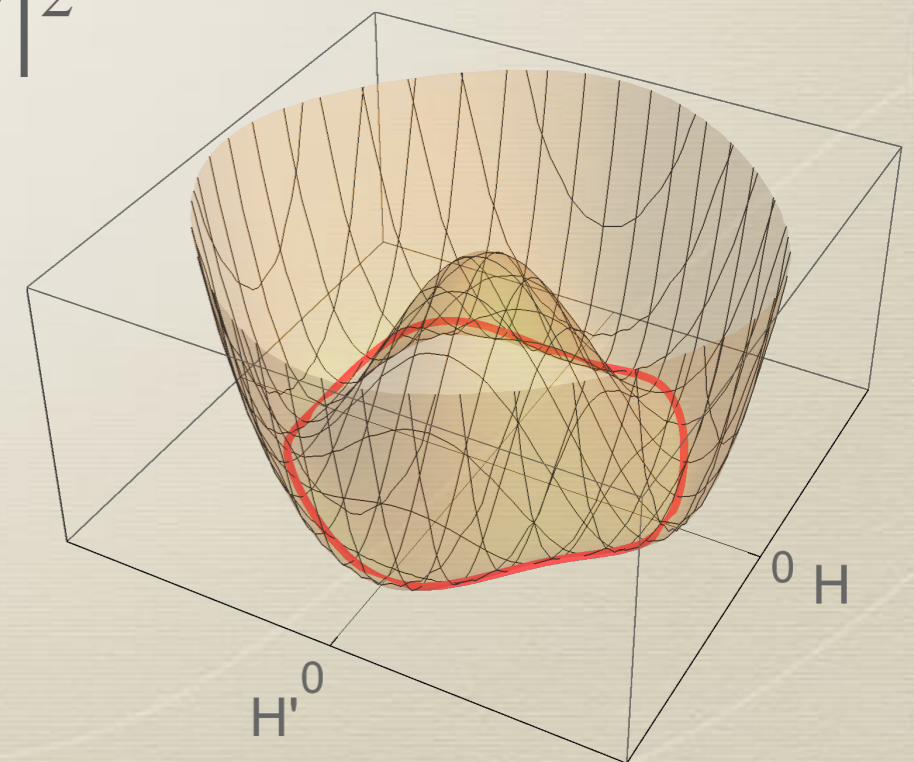
# Higgs potential



$$\begin{aligned}
 V &= \left( \lambda |H|^4 - m^2 |H|^2 \right) + \left( \lambda |H'|^4 - m^2 |H'|^2 \right) + \tilde{y} |H|^2 |H'|^2 \\
 &= \lambda \left( |H|^2 + |H'|^2 - v'^2 \right)^2 + y |H|^2 |H'|^2
 \end{aligned}$$

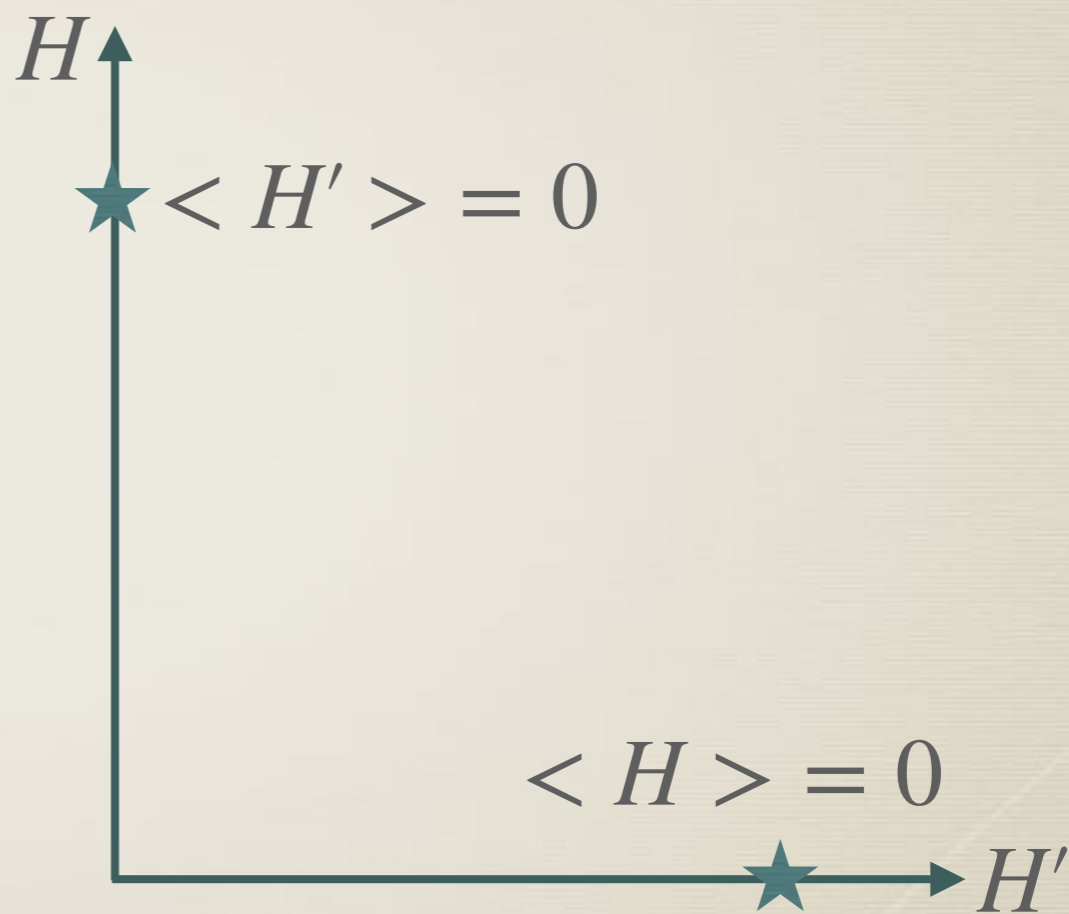
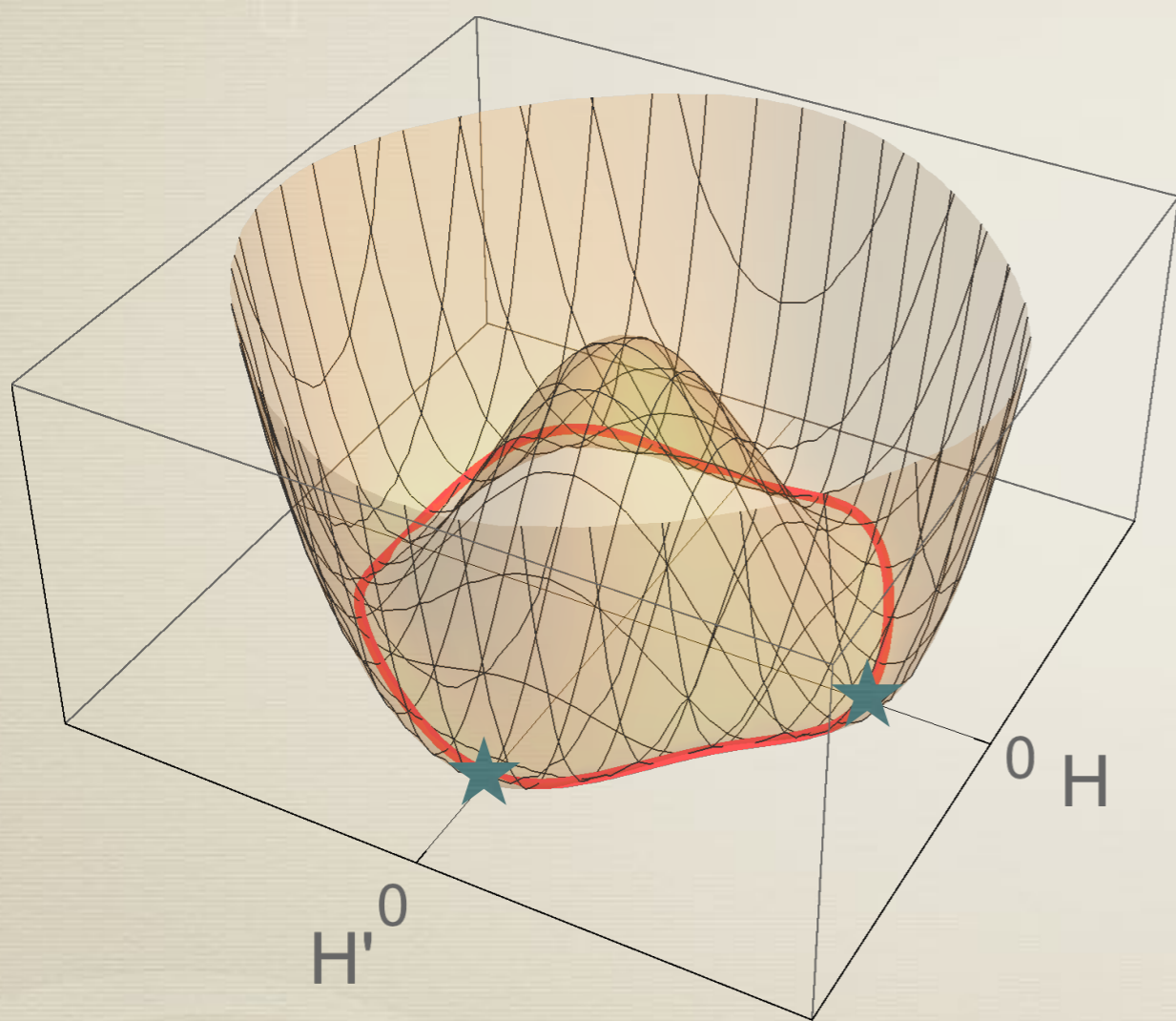
Can we find the minimum with

$$\langle H \rangle \ll \langle H' \rangle ?$$



$$y > 0$$

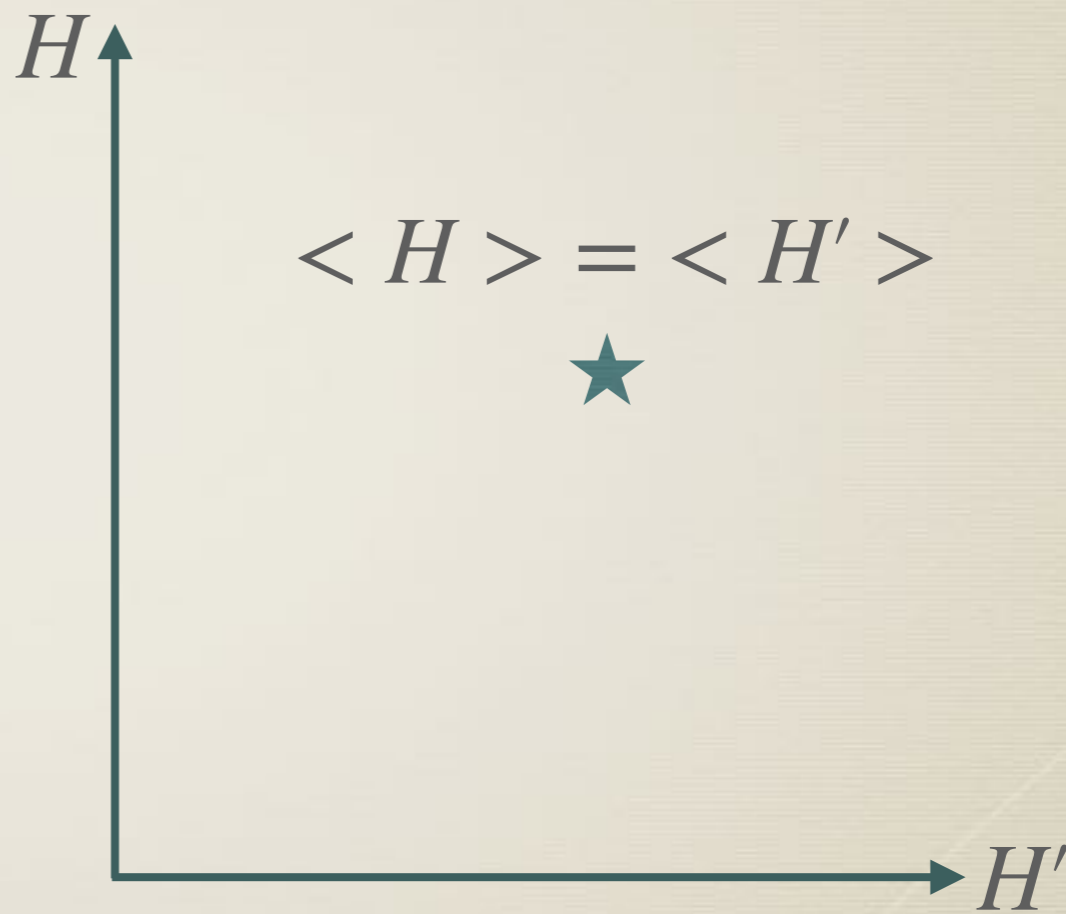
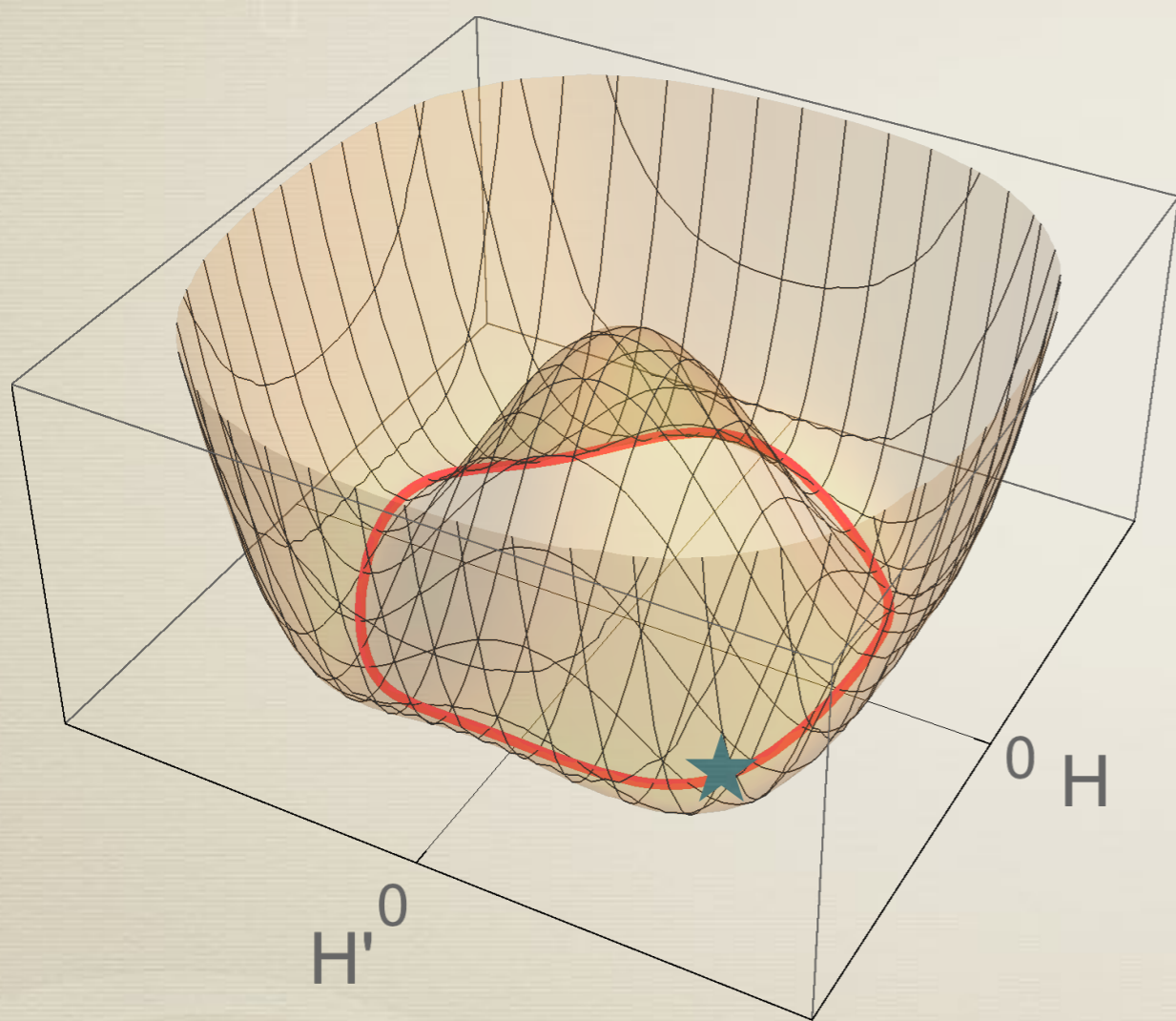
$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$



$$0 \neq \langle H \rangle \ll \langle H' \rangle$$

$$y < 0$$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$



$$\langle H \rangle = \langle H' \rangle$$

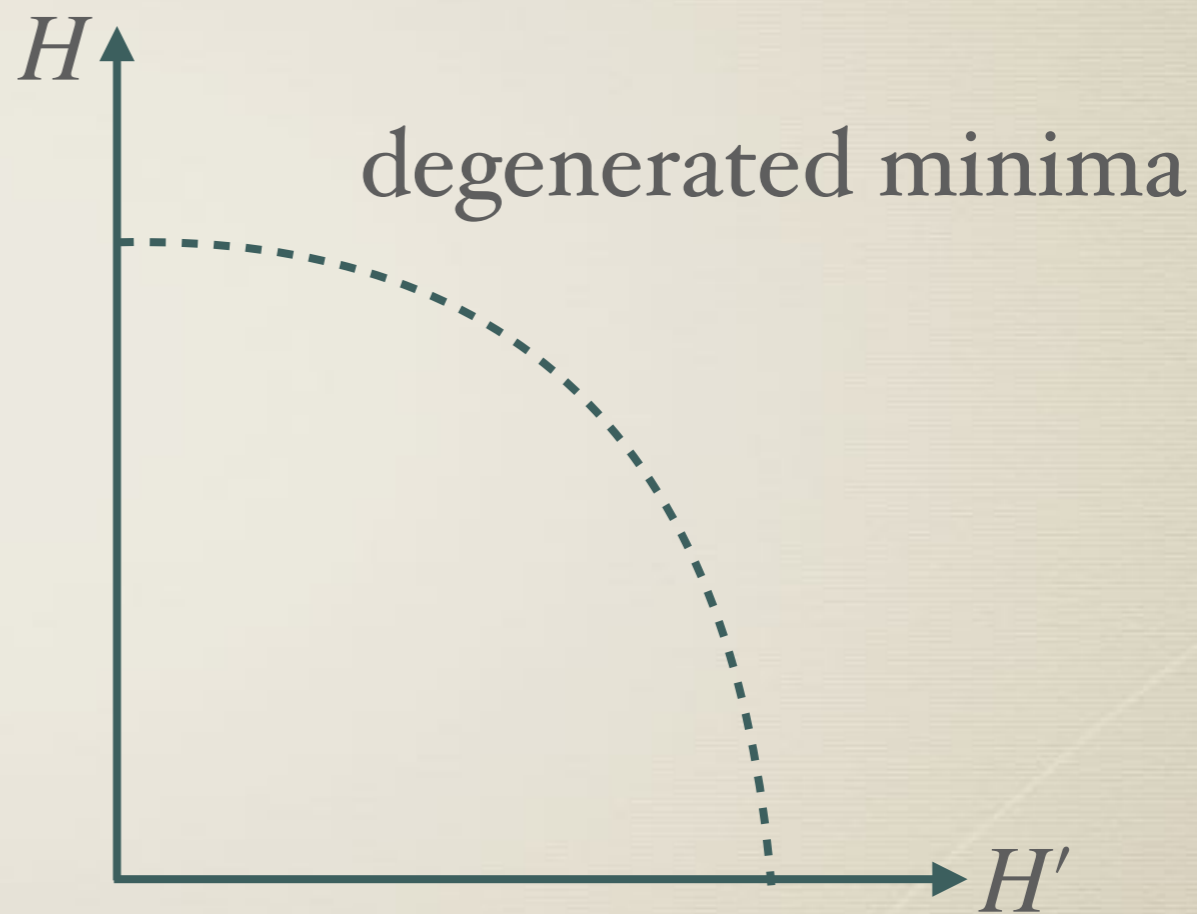
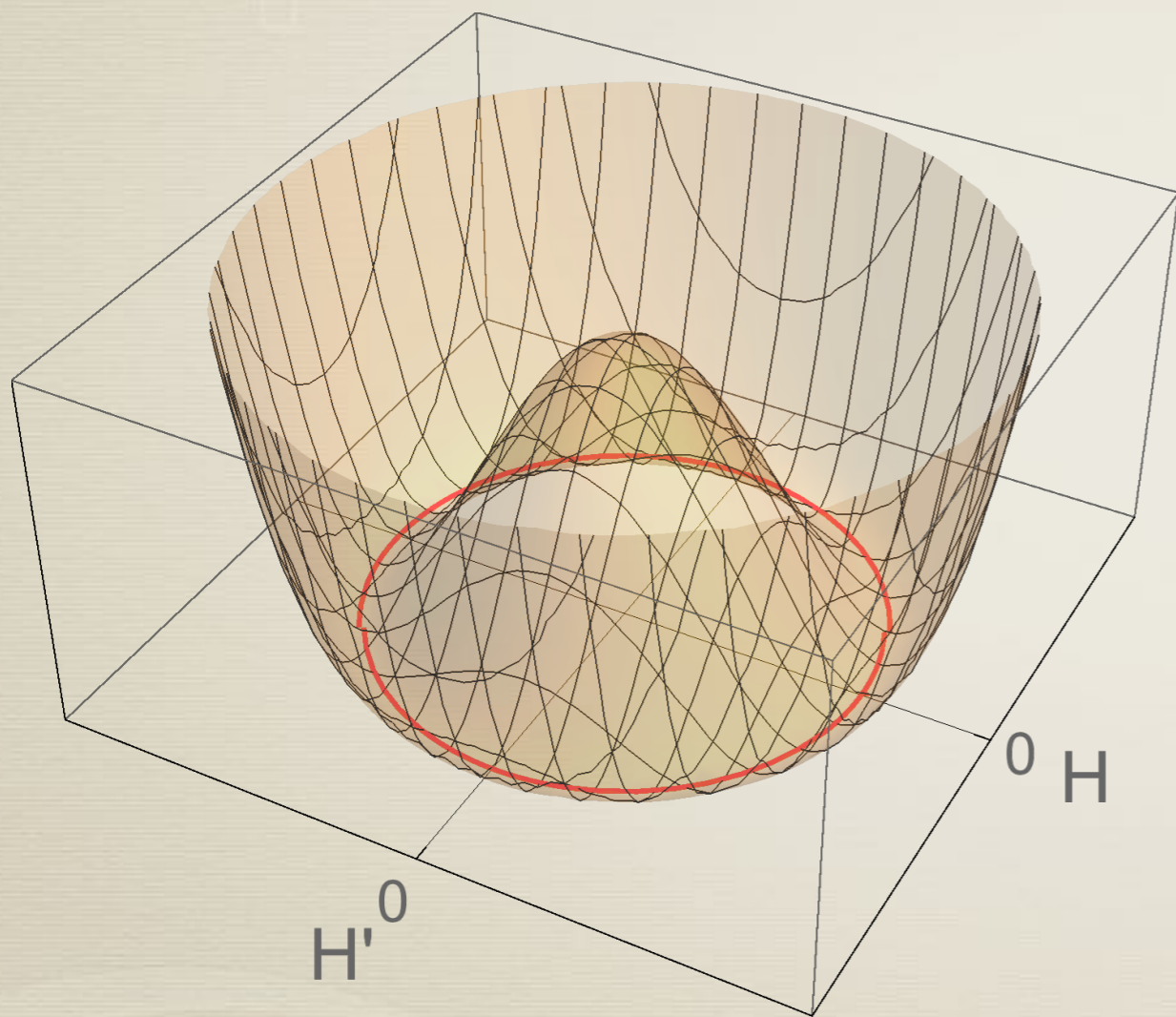


~~$$\langle H \rangle \ll \langle H' \rangle$$~~



$$y \simeq 0$$

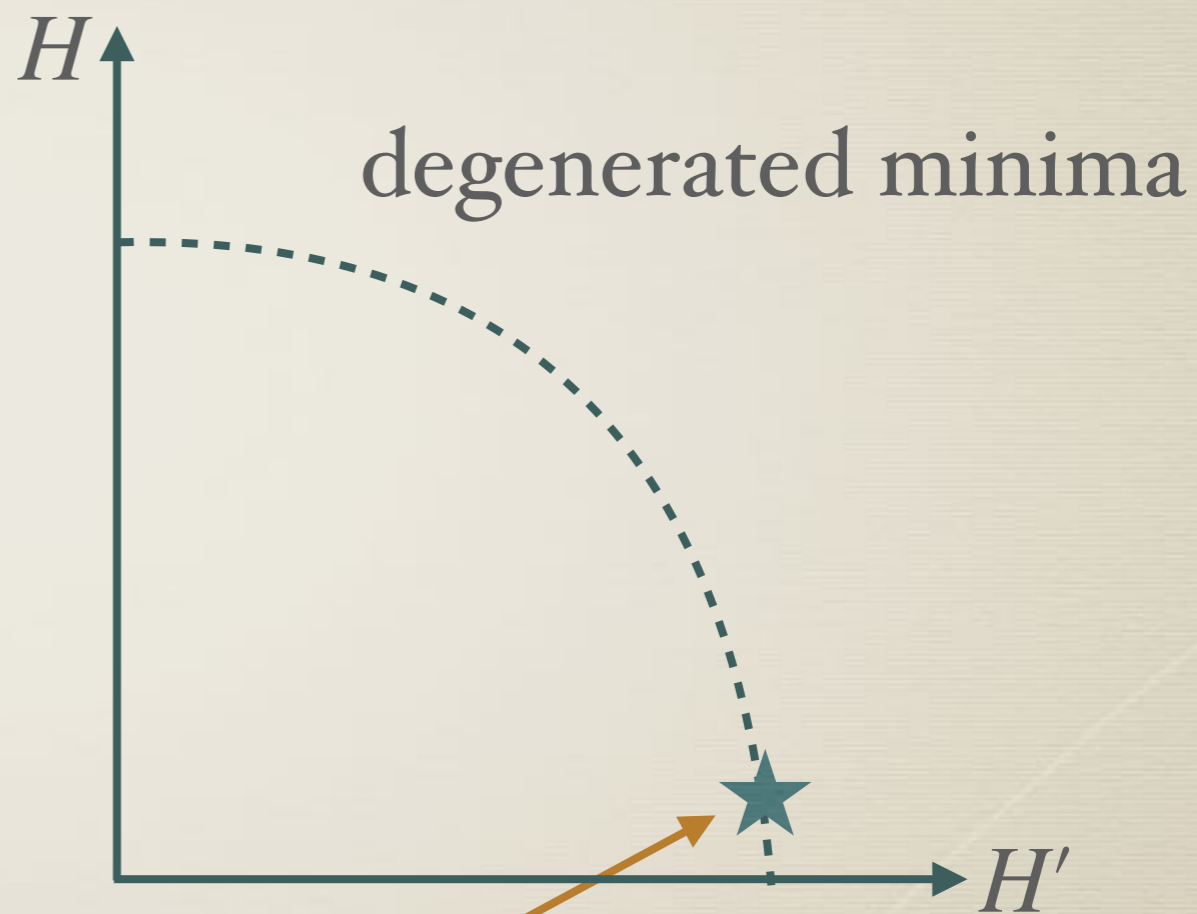
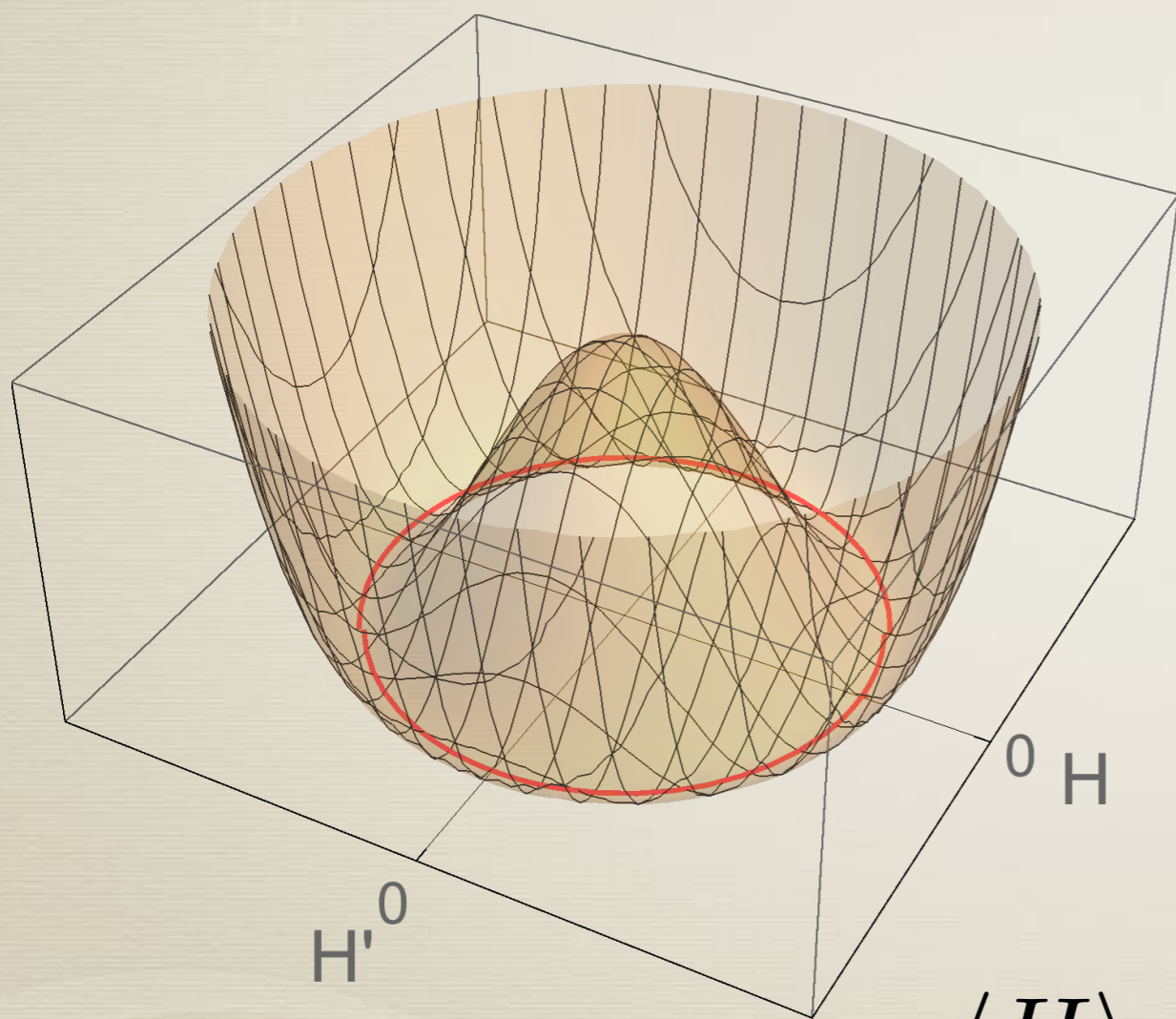
$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$



symmetry rotating the vector  
 $(H, H')$

$$y \simeq 0$$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$

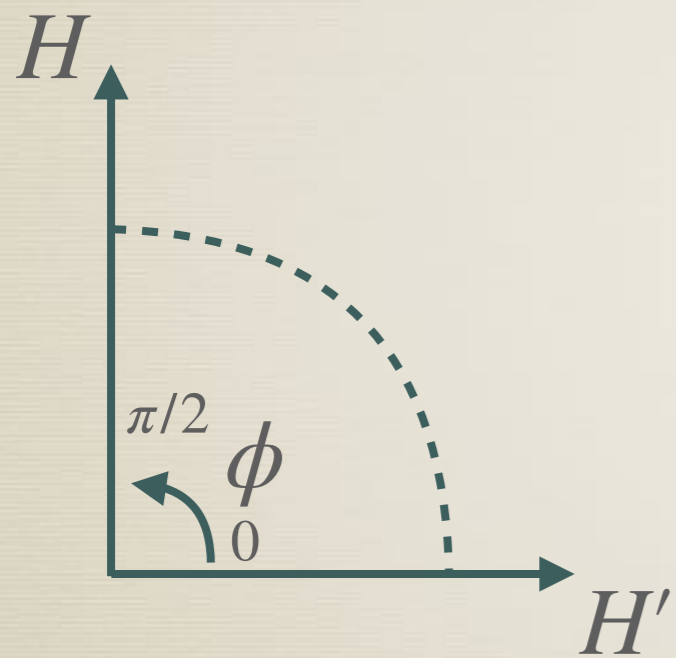


$$\langle H \rangle \ll \langle H' \rangle ?$$

Degeneracy is resolved by quantum corrections

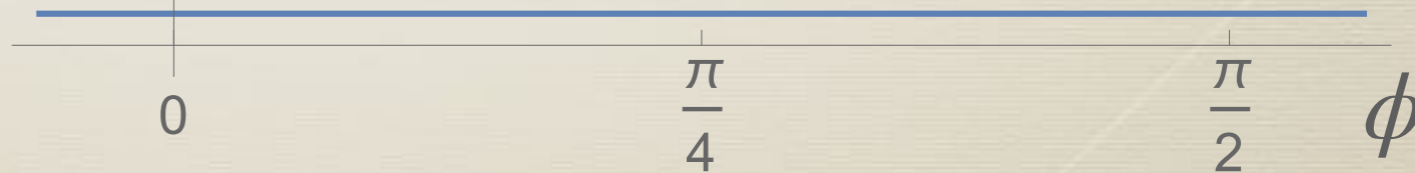
$$y \simeq 0$$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2$$



angular direction  $\phi$

$V(\phi)$   $y = 0$ , tree level

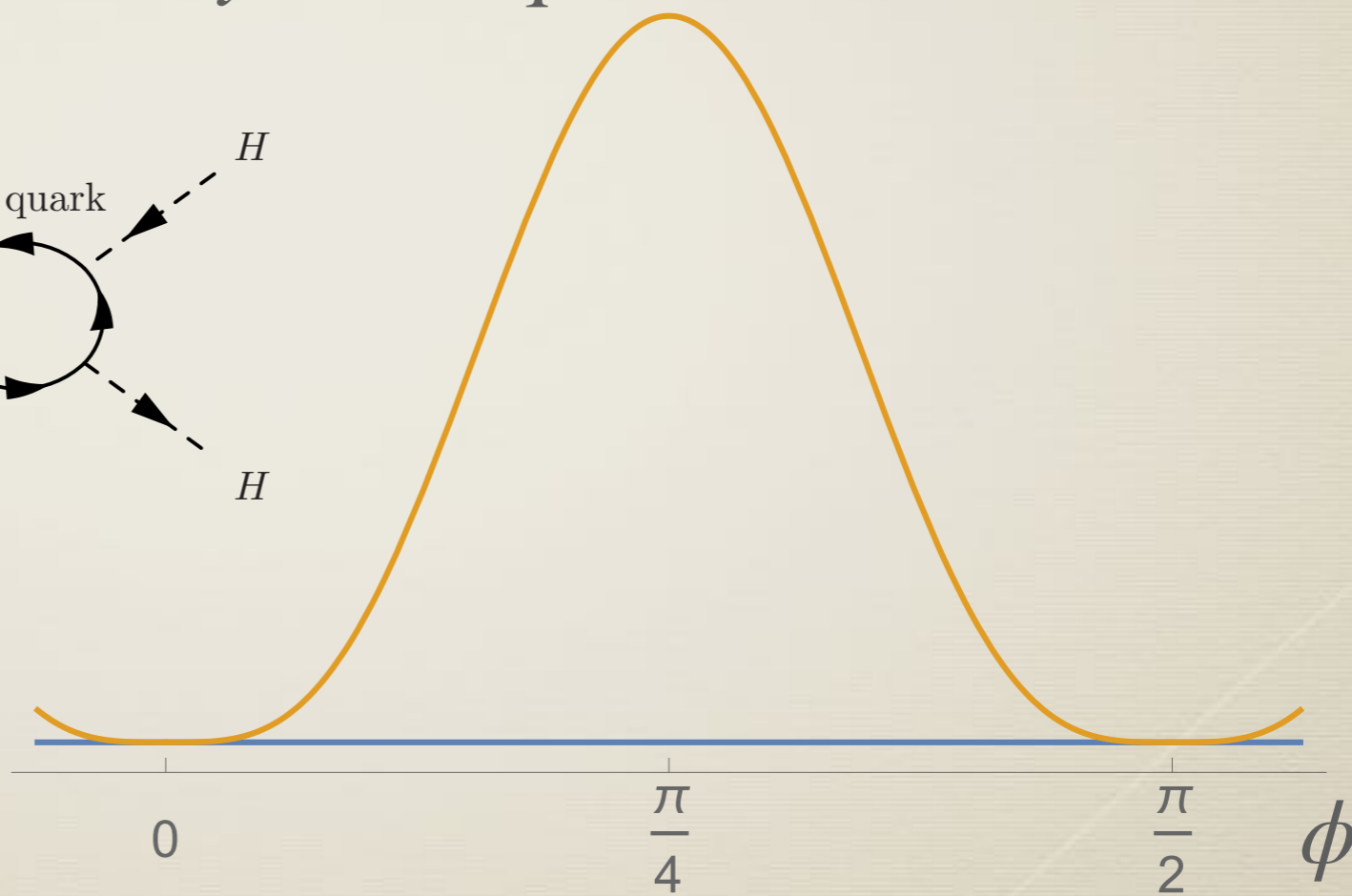
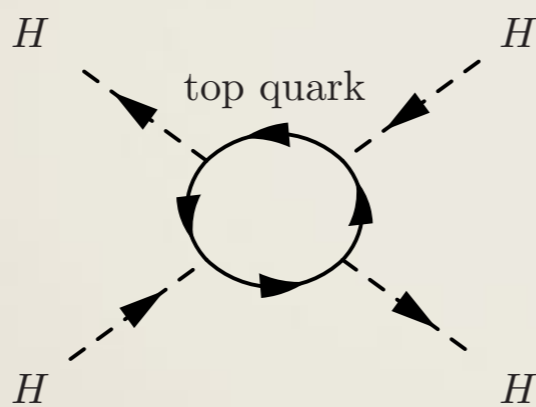
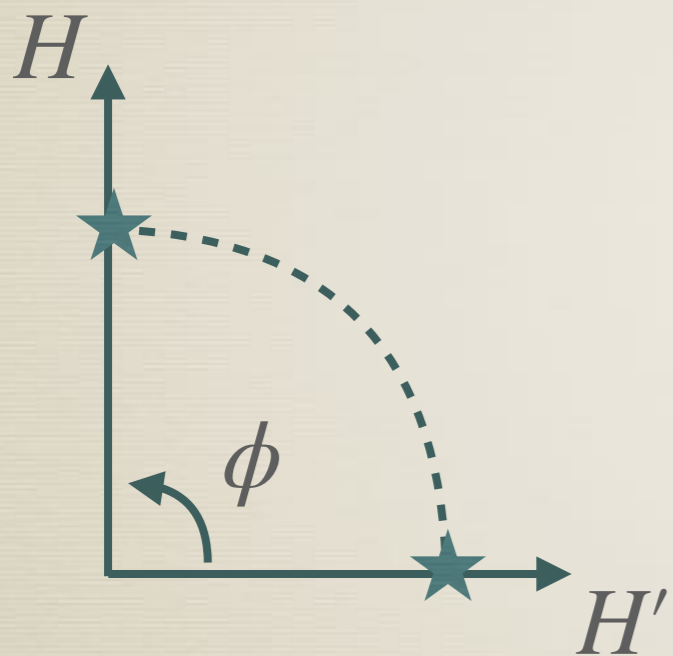


$$y \simeq 0$$

Colemann-Weinberg potential

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + V_{\text{quantum}}(H, H')$$

$y = 0$ , quantum correction



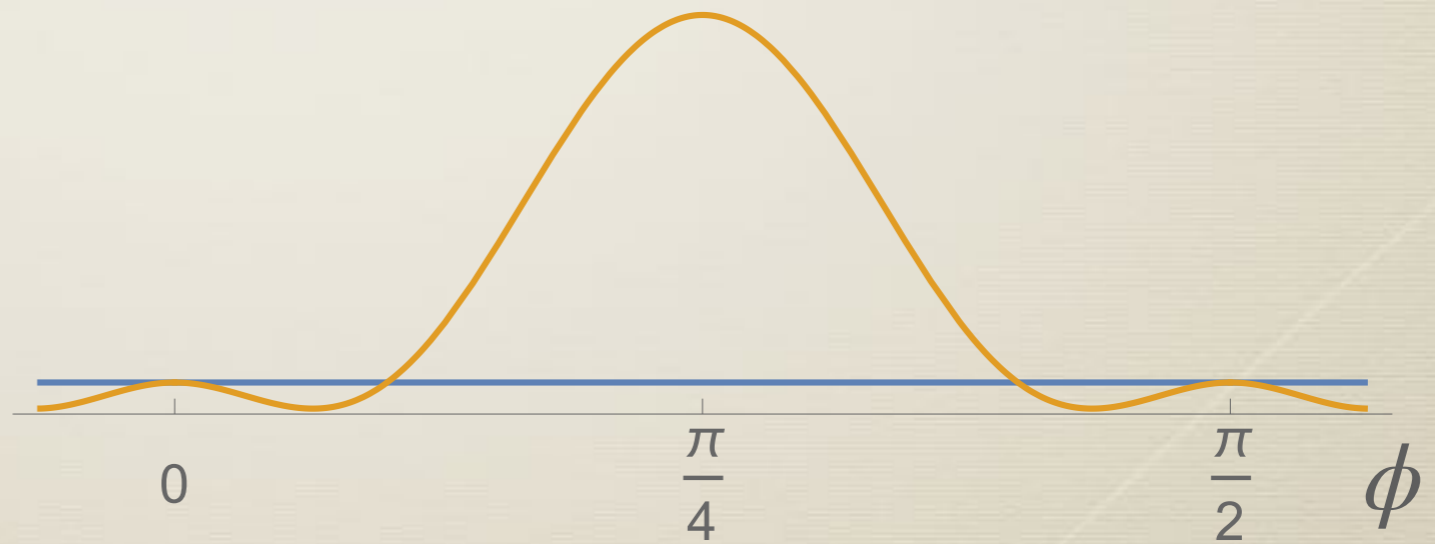
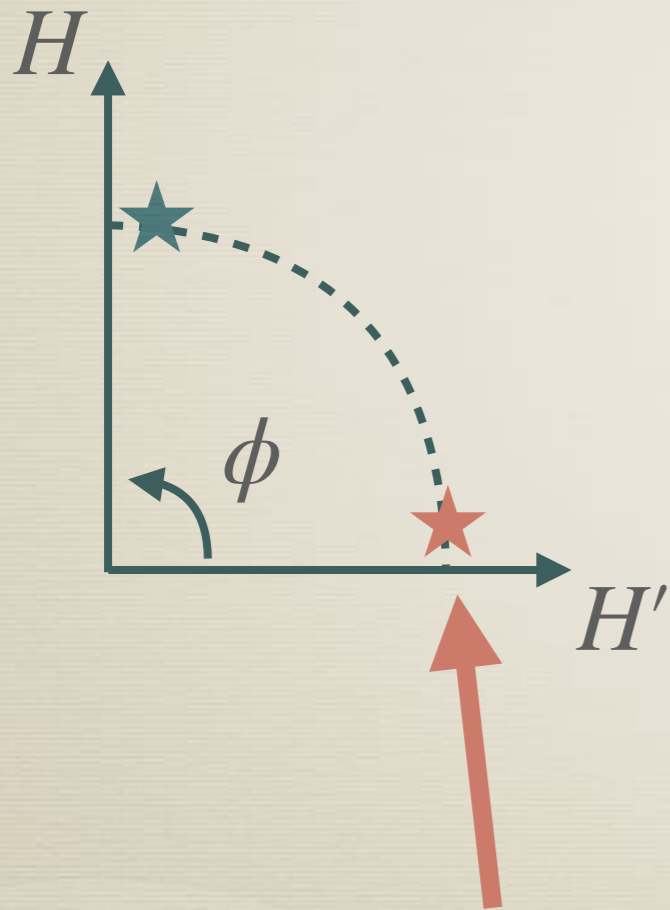
$$y \simeq 0$$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + V_{\text{quantum}}(H, H') + y|H|^2|H'|^2$$

$$y \simeq -\frac{v^2}{v'^2}, \text{ quantum correction}$$



(fine-tuned Higgs mass)



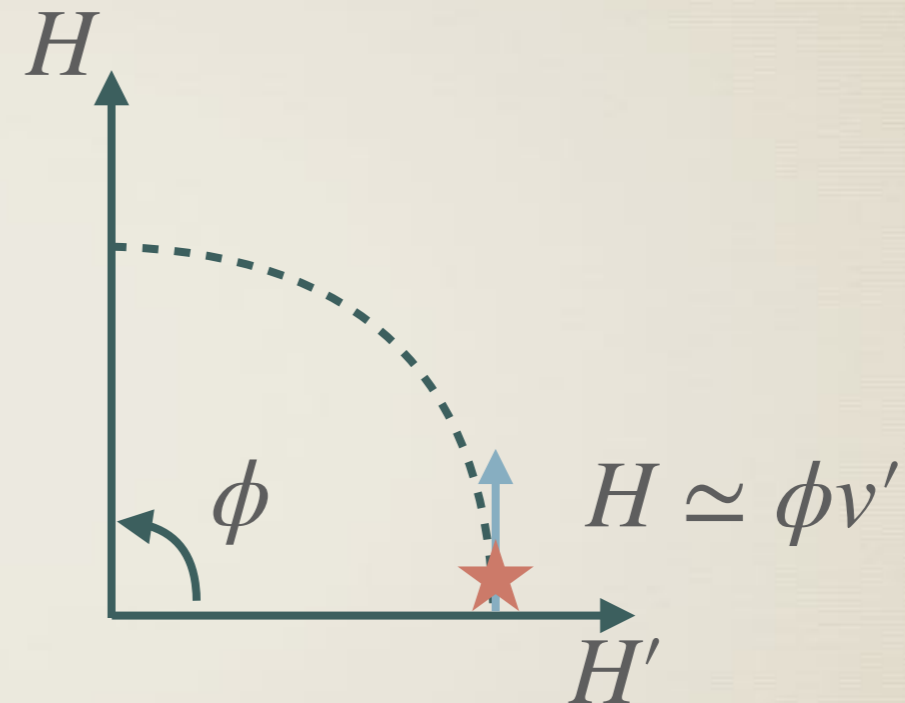
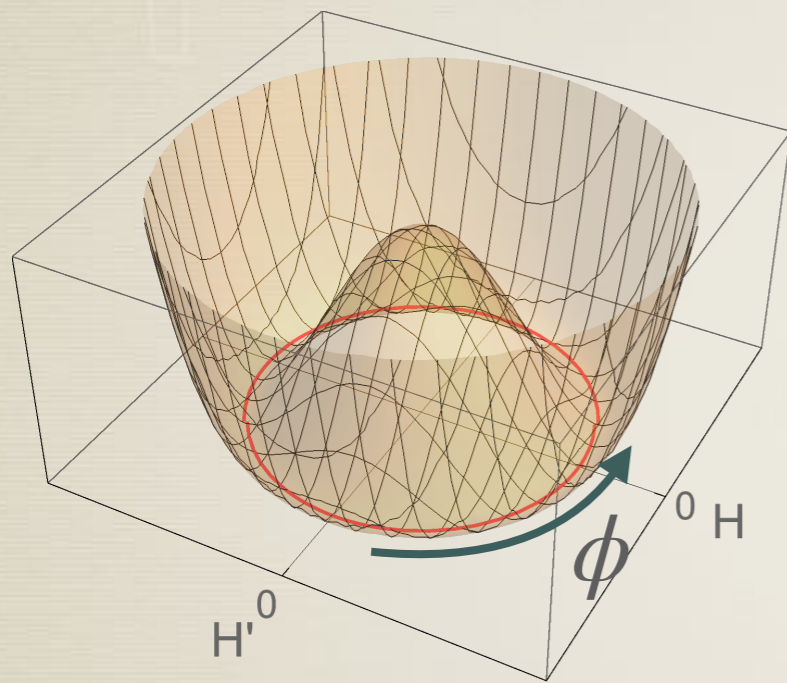
$\langle H \rangle \ll \langle H' \rangle$  is achieved!

Hall, KH (2018)

# Prediction on the quartic coupling

Hall, KH (2018)

$$V \simeq \lambda(|H|^2 + |H'|^2 - v'^2)^2 + \text{small corrections}$$



symmetry rotating the vector  $(H, H')$

Standard Model Higgs is a (pseudo) Nambu-Goldstone boson associated with symmetry breaking by  $\langle H' \rangle = v'$

$$\lambda_{\text{SM}}(v') \simeq 0$$

(up to calculable threshold correction)

# Dark Matter

# Precise measurement and dark matter

Dunsky, Hall and KH (2019)

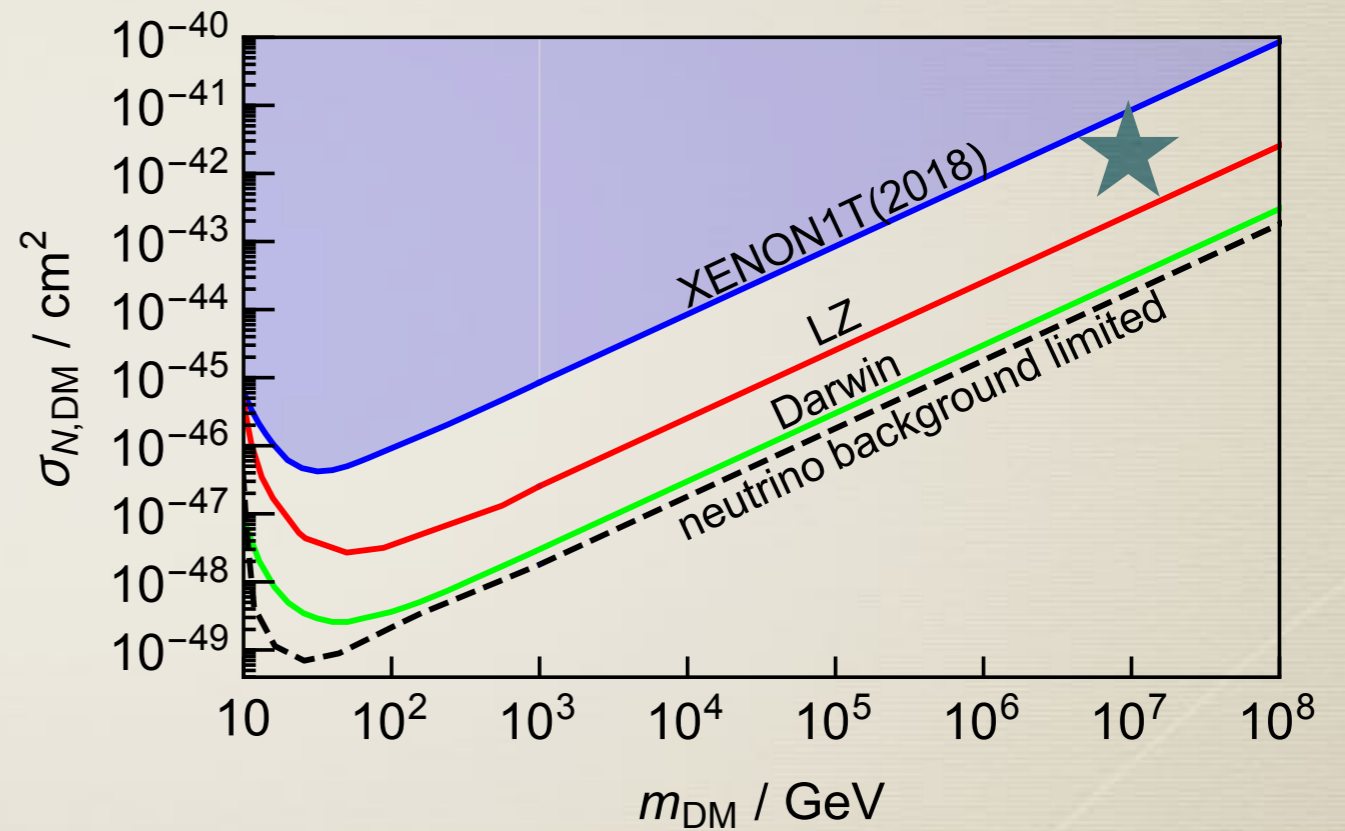
top quark mass  
Higgs mass  
strong coupling constant



Higgs Parity  
symmetry breaking scale



Dark matter direct  
detection rate





# Mirrored electroweak theory

SM particles

quark  $q, u, d$

lepton  $L, e$

Higgs  $H$

gauge bosons  $W, Z, \gamma$

New particles

$q', u', d'$

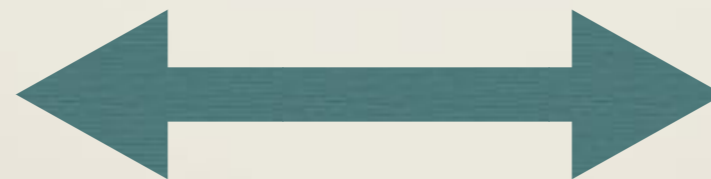
$L', e'$

$H'$

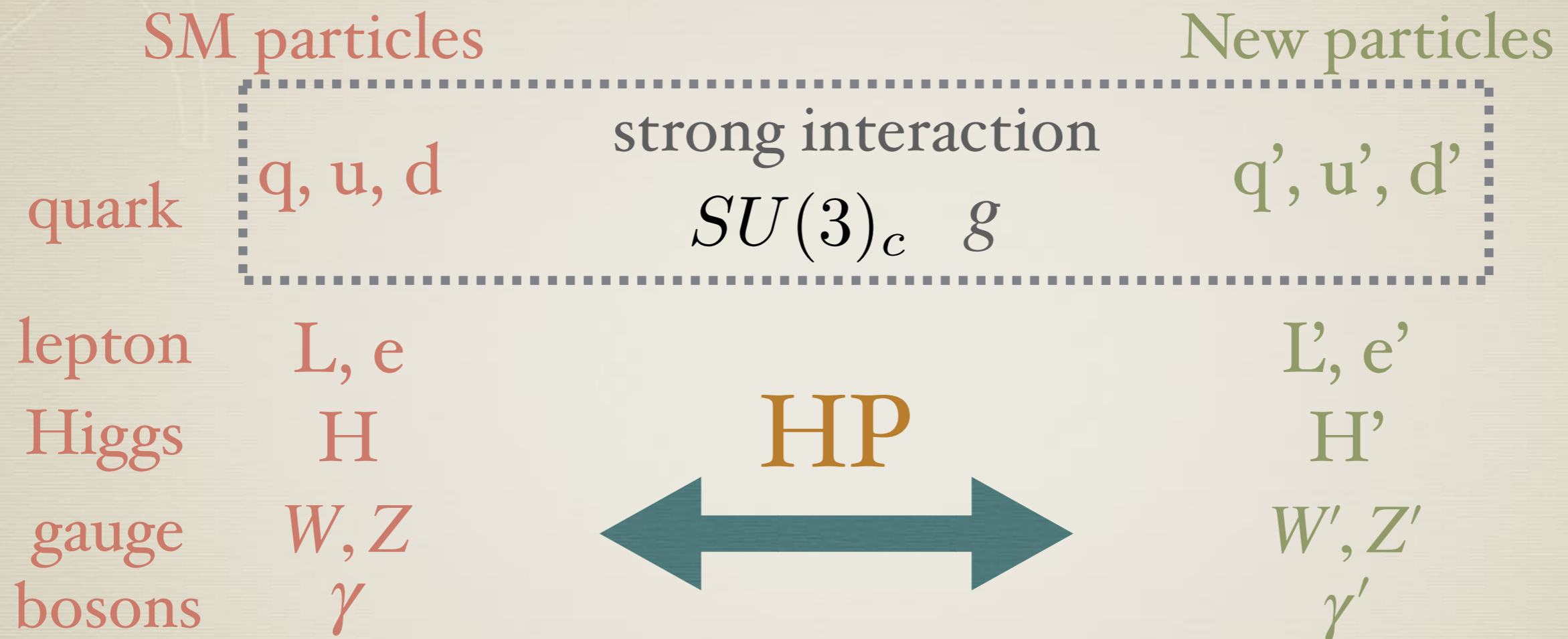
$W', Z'$

$\gamma'$

HP

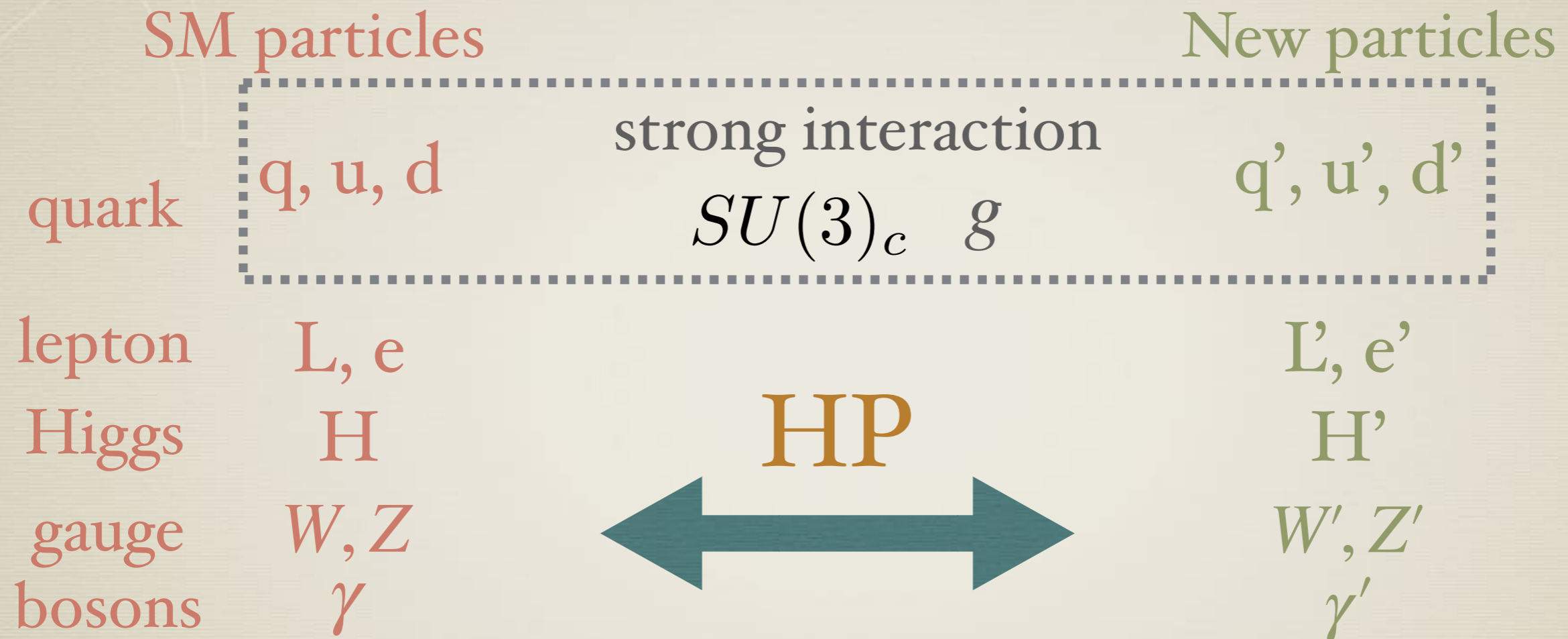


# Mirrored electroweak theory



Motivated from the **Strong CP problem**  
in the Standard Model

# Mirrored electroweak theory



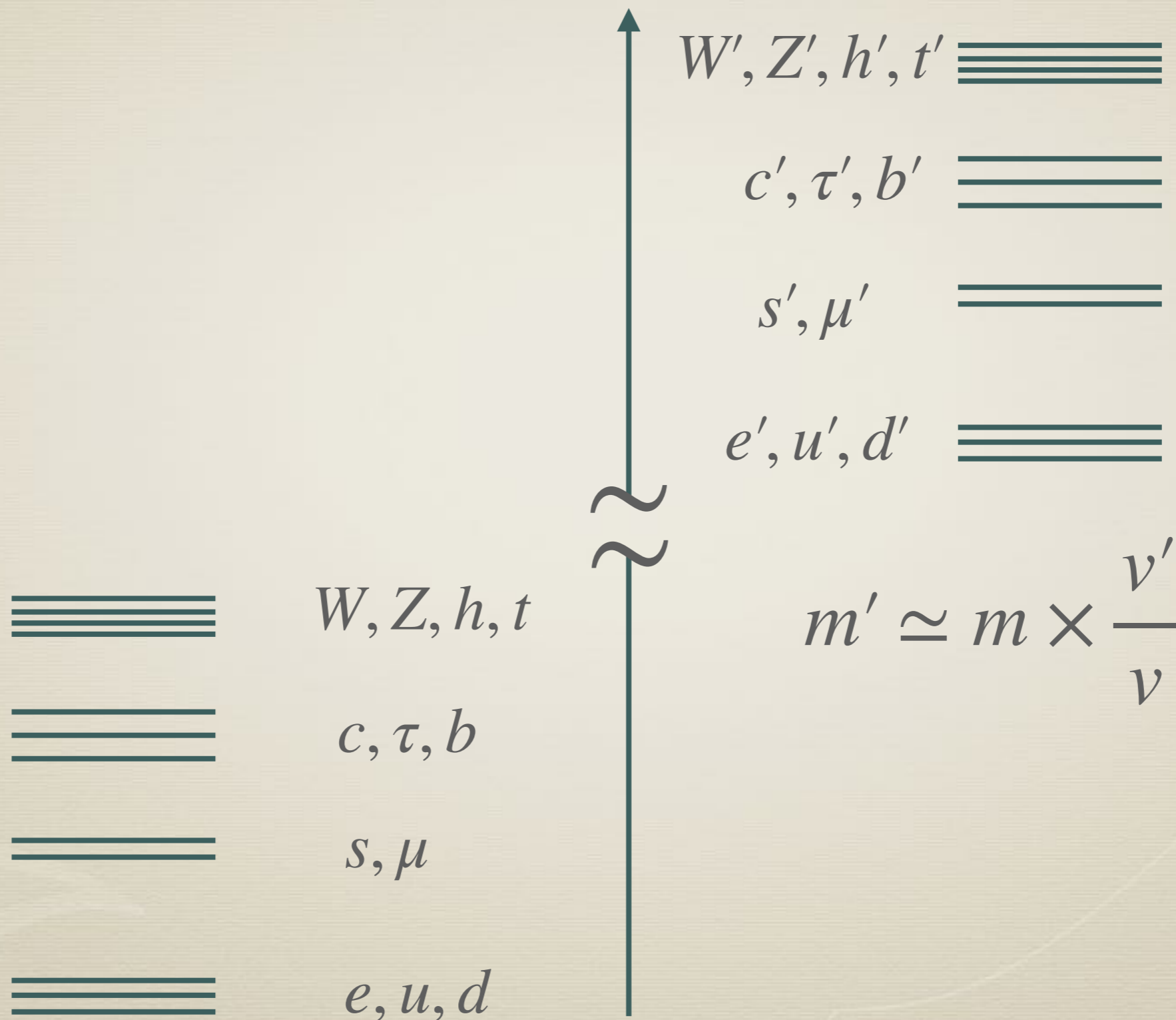
HP with space-time parity forbids the neutron EDM

~~$$H = d_n \vec{E} \cdot \vec{S}$$~~

Mohapatra and Senjanovic (1978), Beg and Tsao (1978),  
 Babu and Mohapatra (1989), Barr, Chang and Senjanovic (1991)  
 Dunsky, Hall and KH (2019)

(a quick explanation for experts: q and q' have masses with opposite phases)

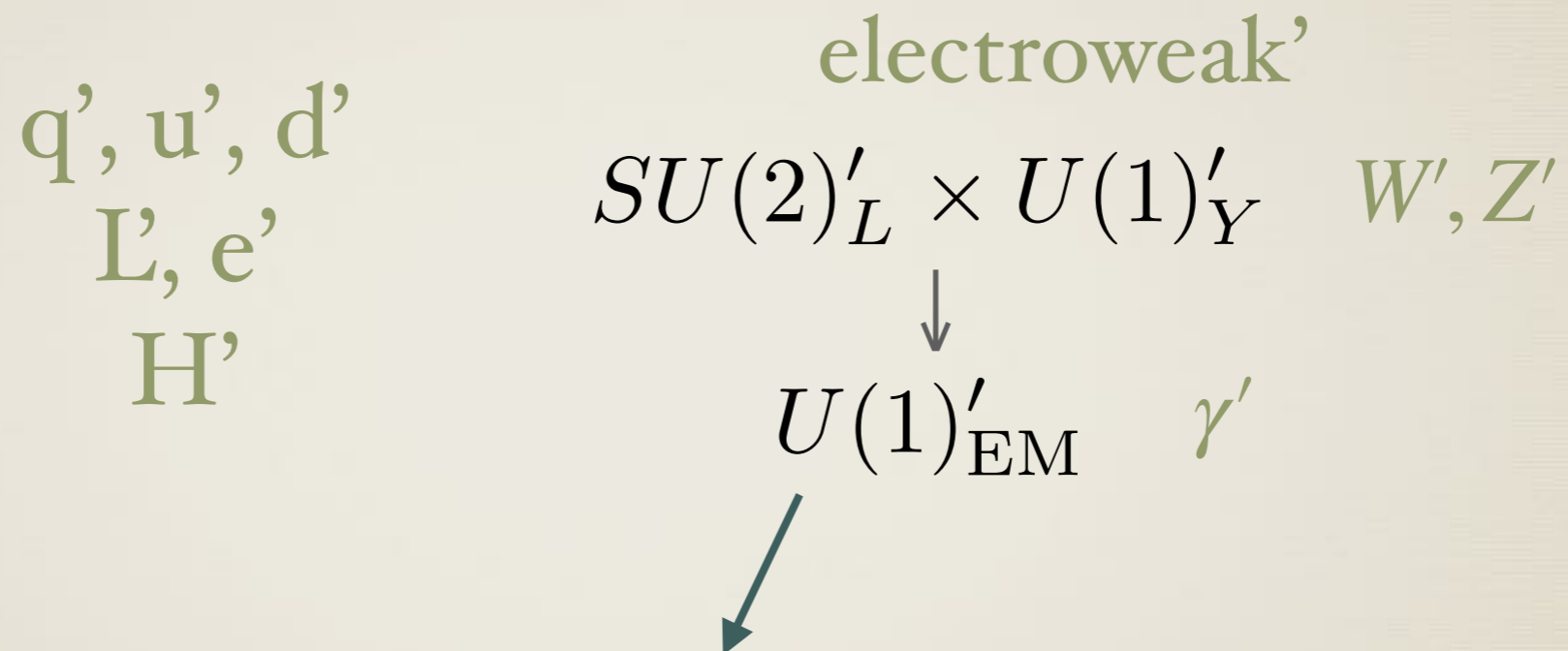
# Mass spectrum



# Mirror dark matter

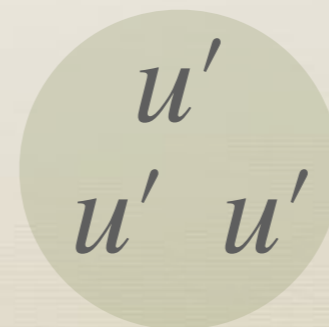
New particles

Dunsky, Hall, KH (2019)



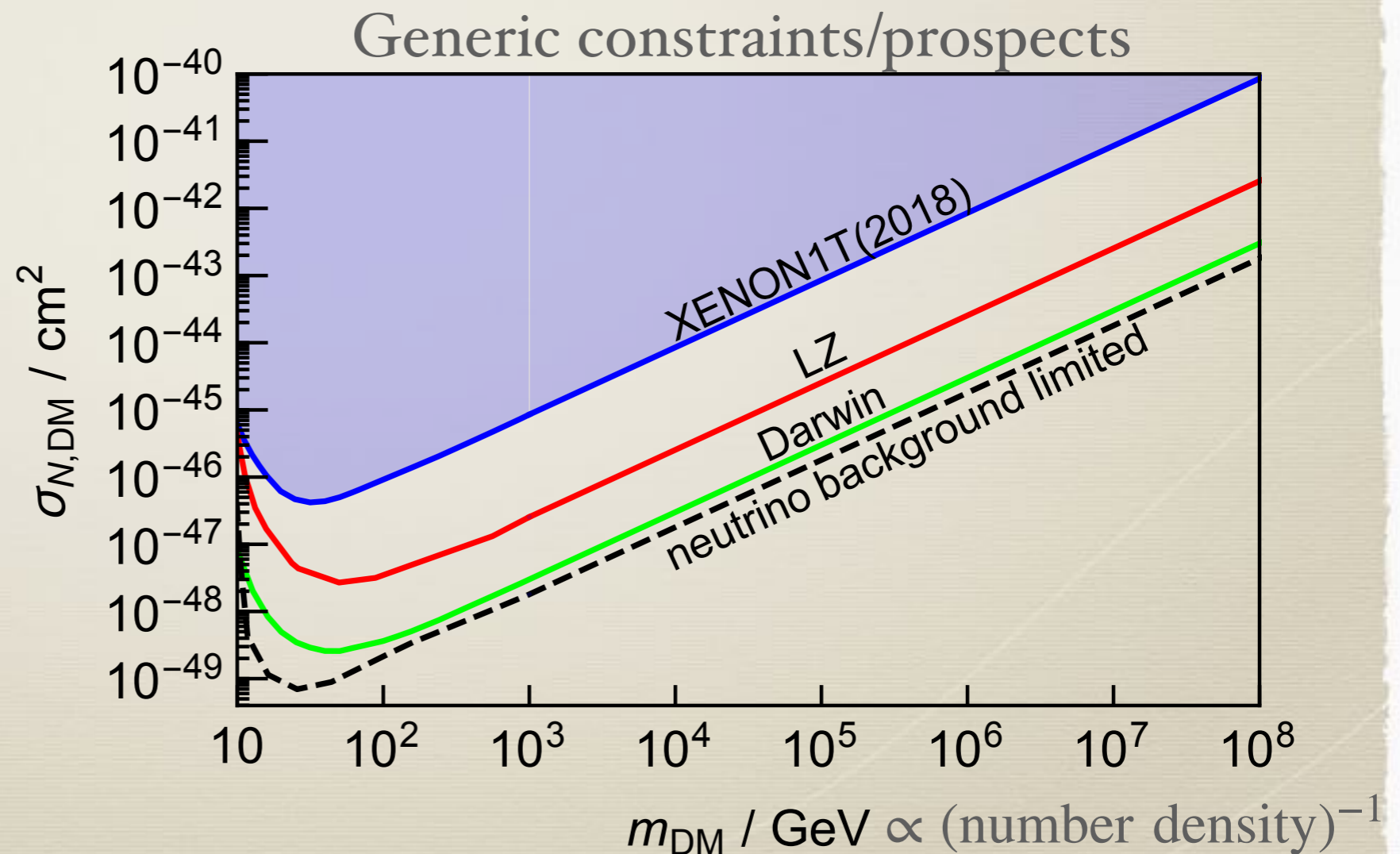
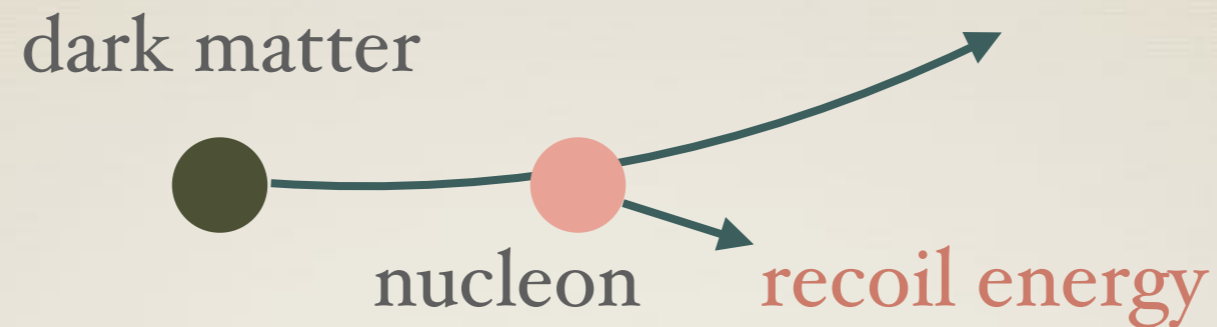
The mirror electron and the lightest mirror baryon are stable

$e'$

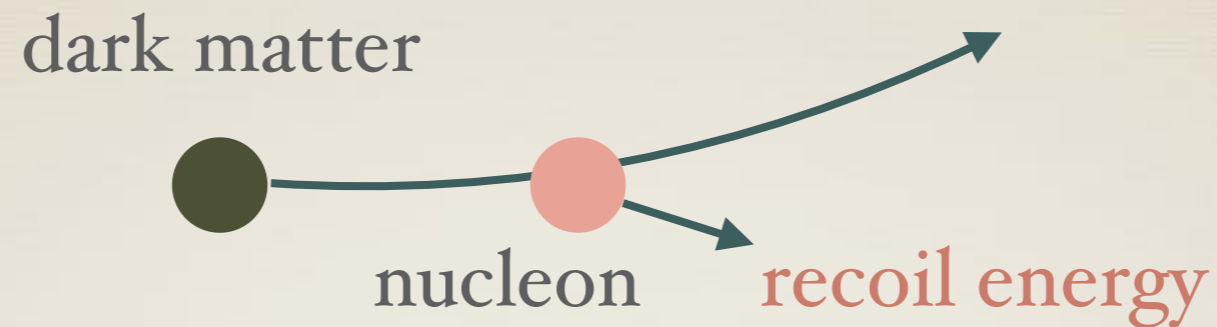


I assume that they comprise all of dark matter

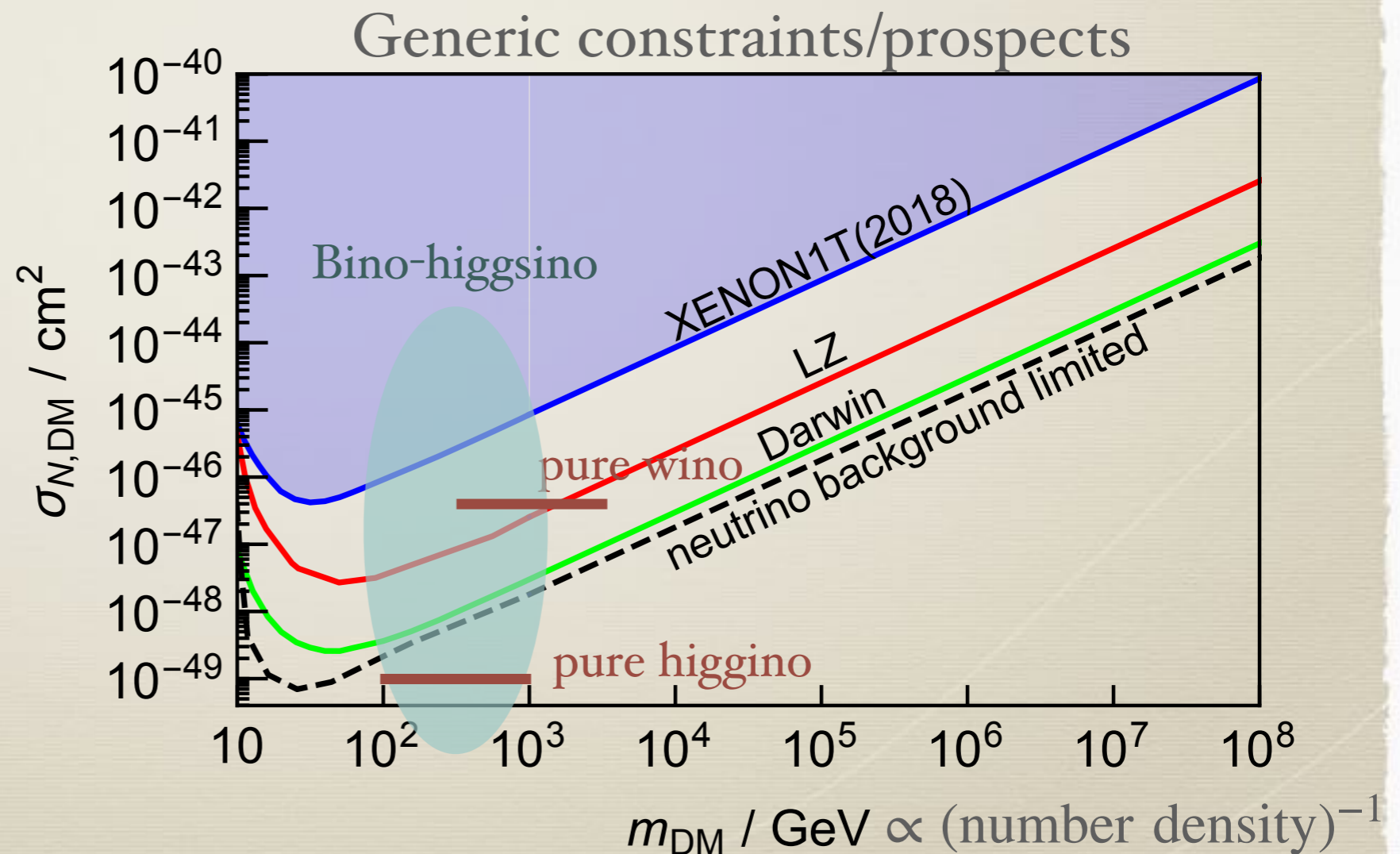
# Direct detection of dark matter



# Direct detection of dark matter



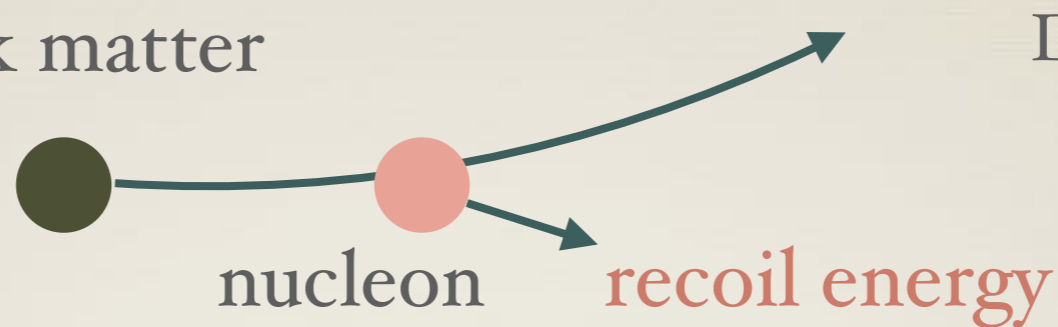
ex.  
Dark matter in  
supersymmetric  
theories



# Direct detection of dark matter

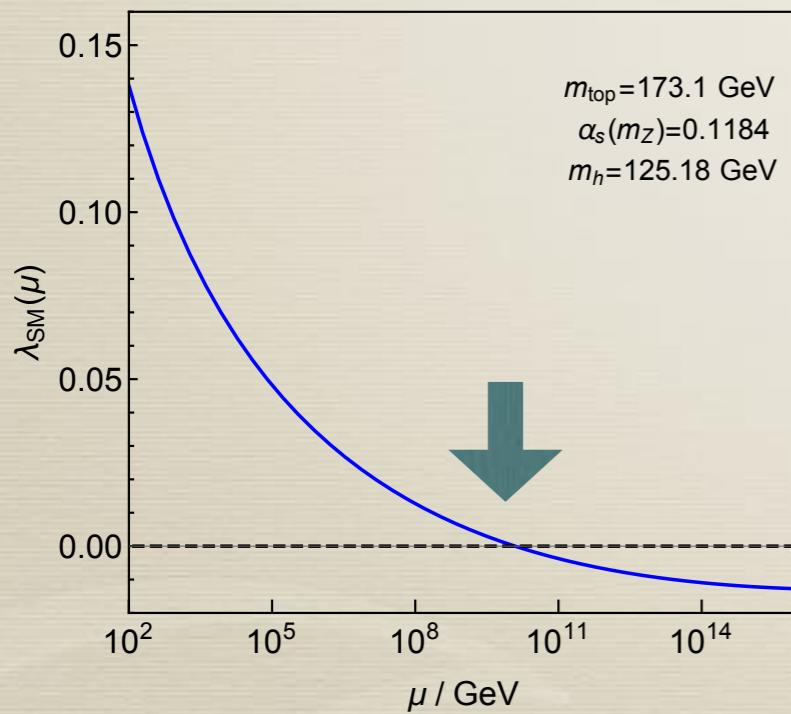
dark matter

Dunsky, Hall, KH (2019)



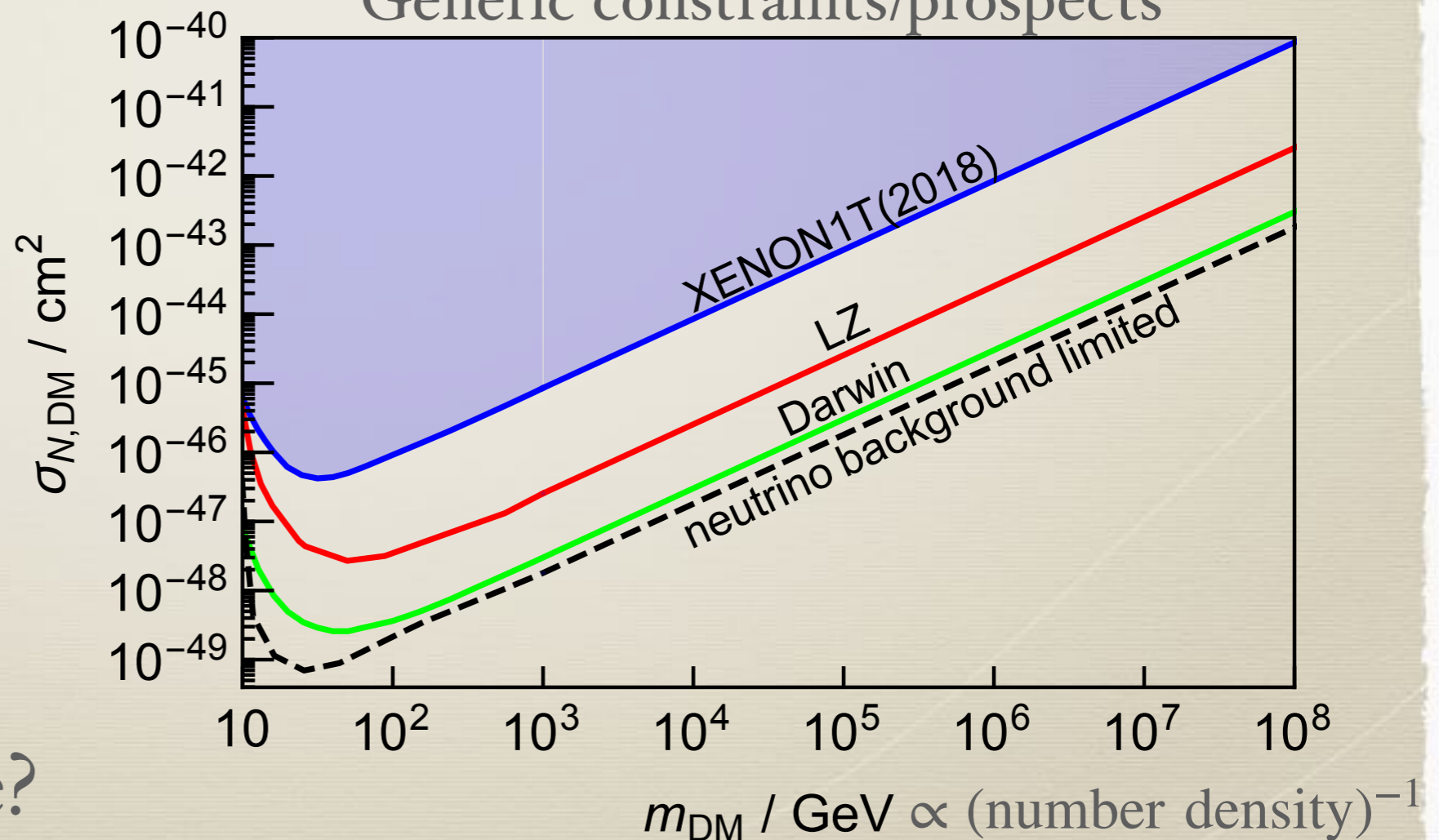
## Higgs Parity

$$m_{e'} = y_e v'$$



Interaction rate?

Generic constraints/prospects

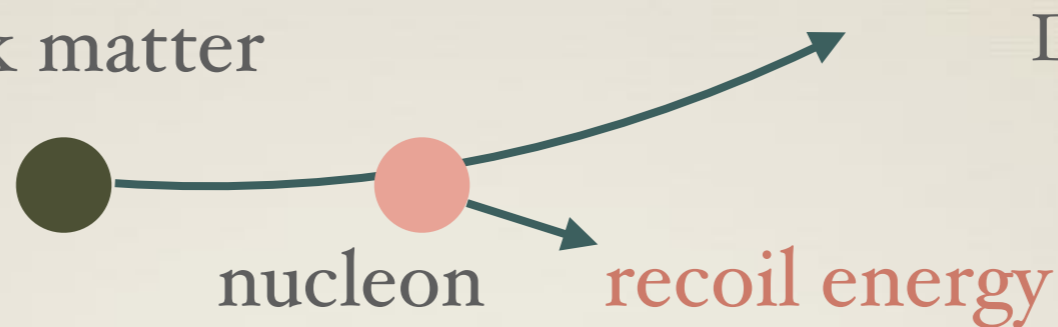




# Direct detection of dark matter

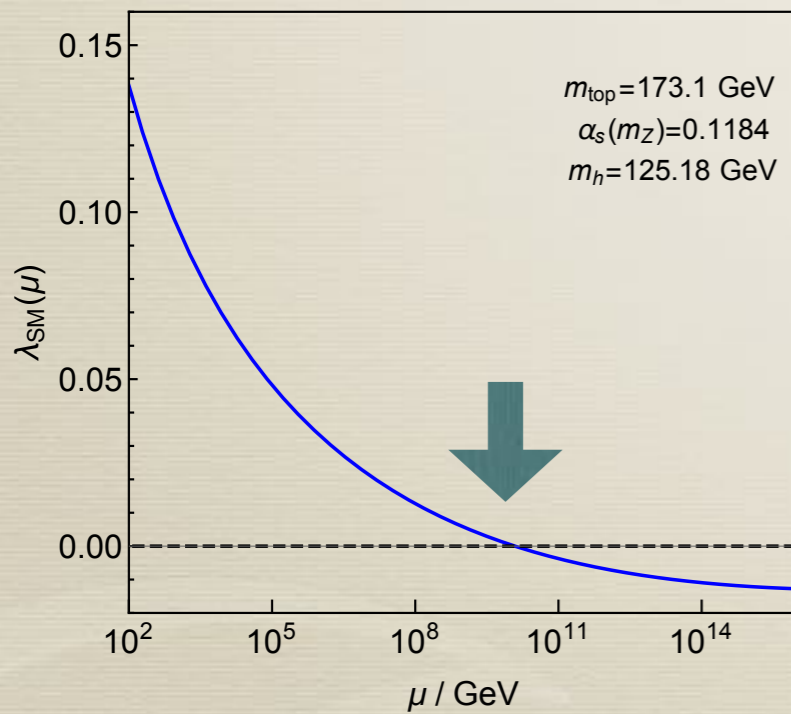
dark matter

Dunsky, Hall, KH (2019)



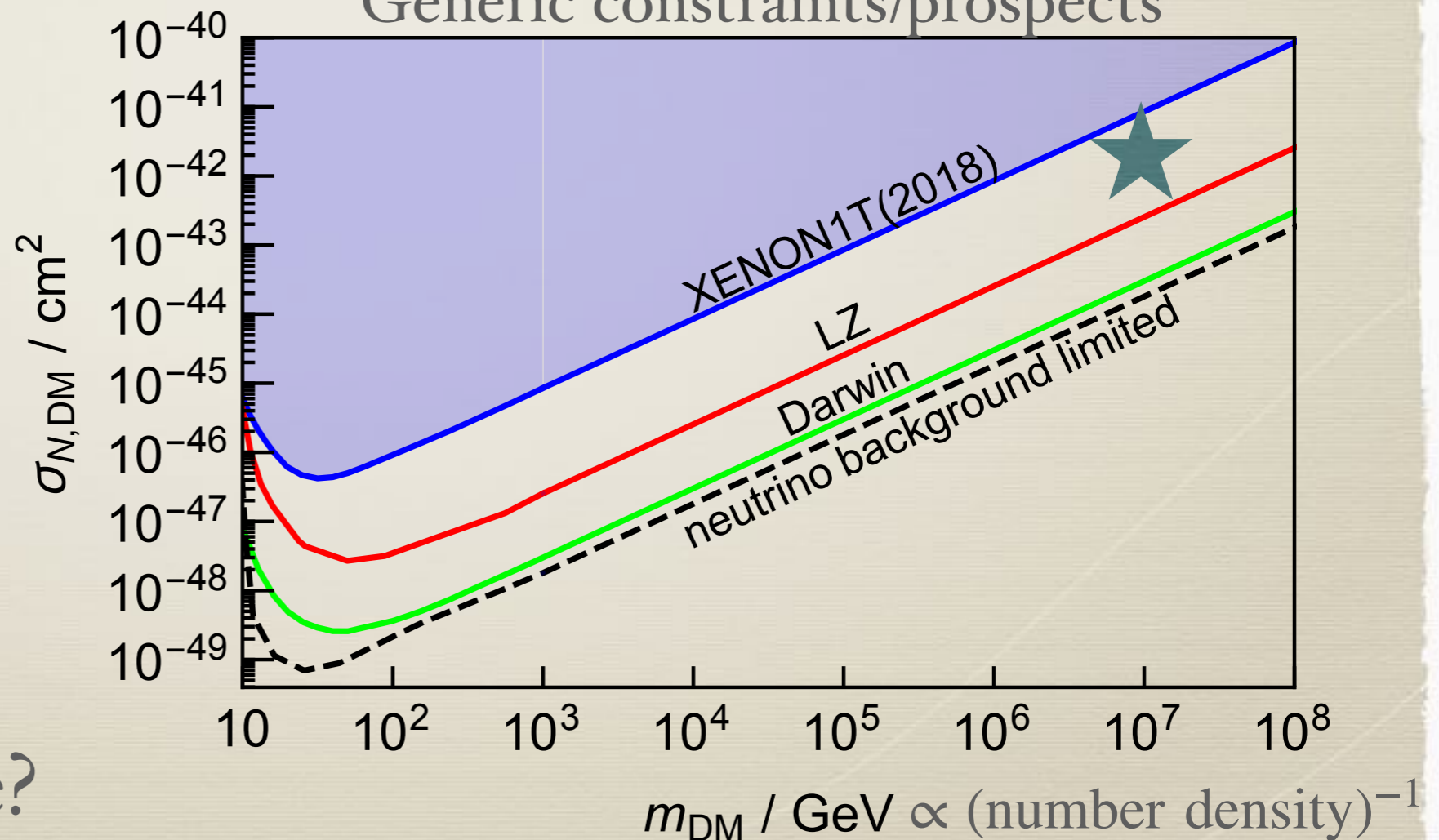
Higgs Parity

$$m_{e'} = y_e v'$$



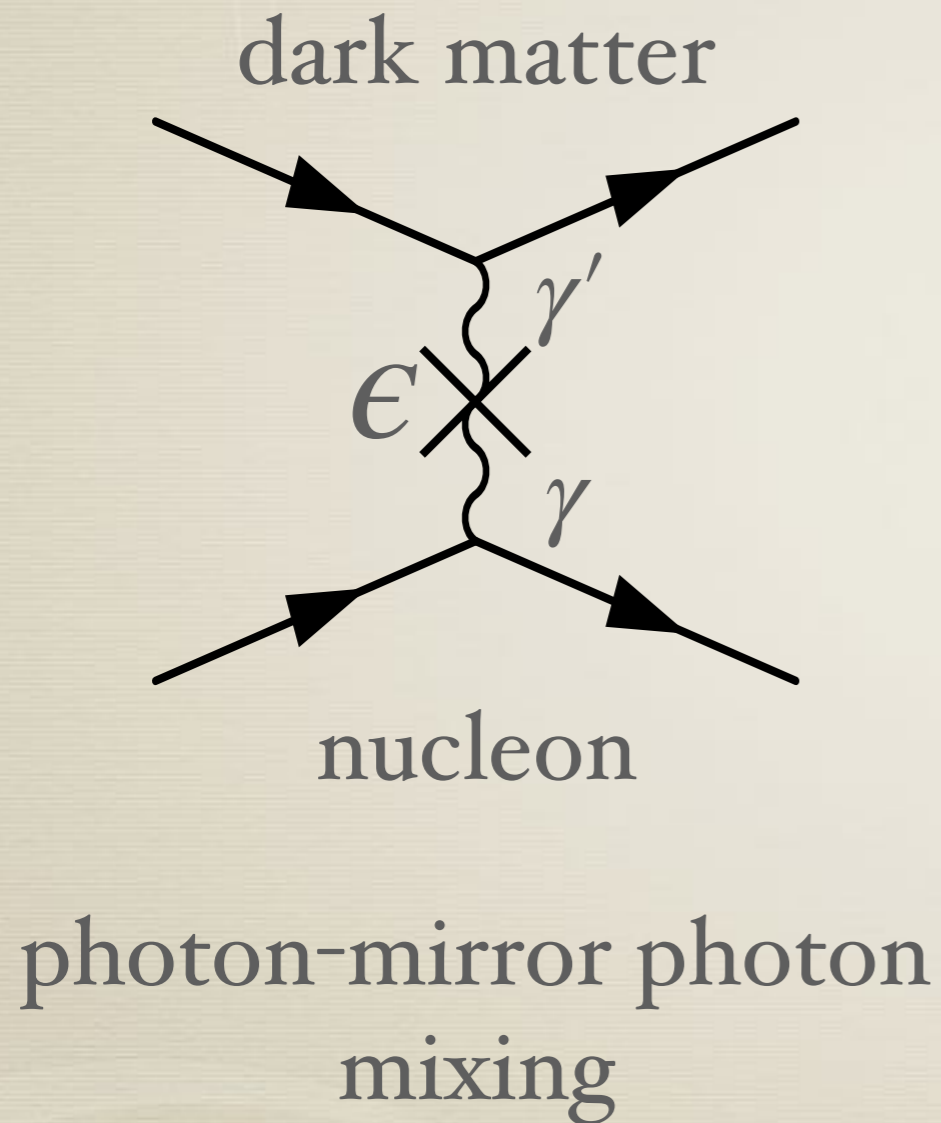
Interaction rate?

Generic constraints/prospects

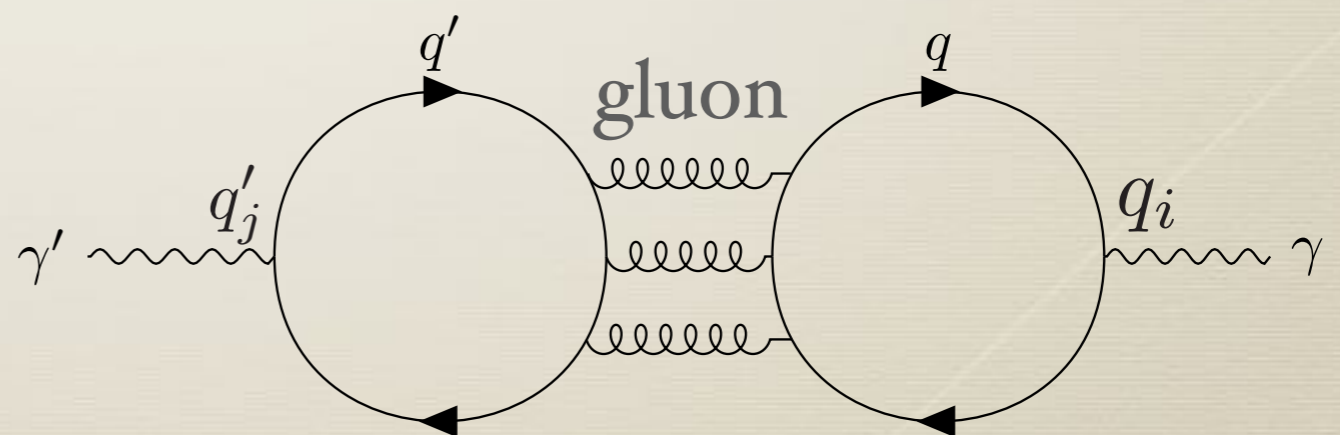


# Prediction on interaction

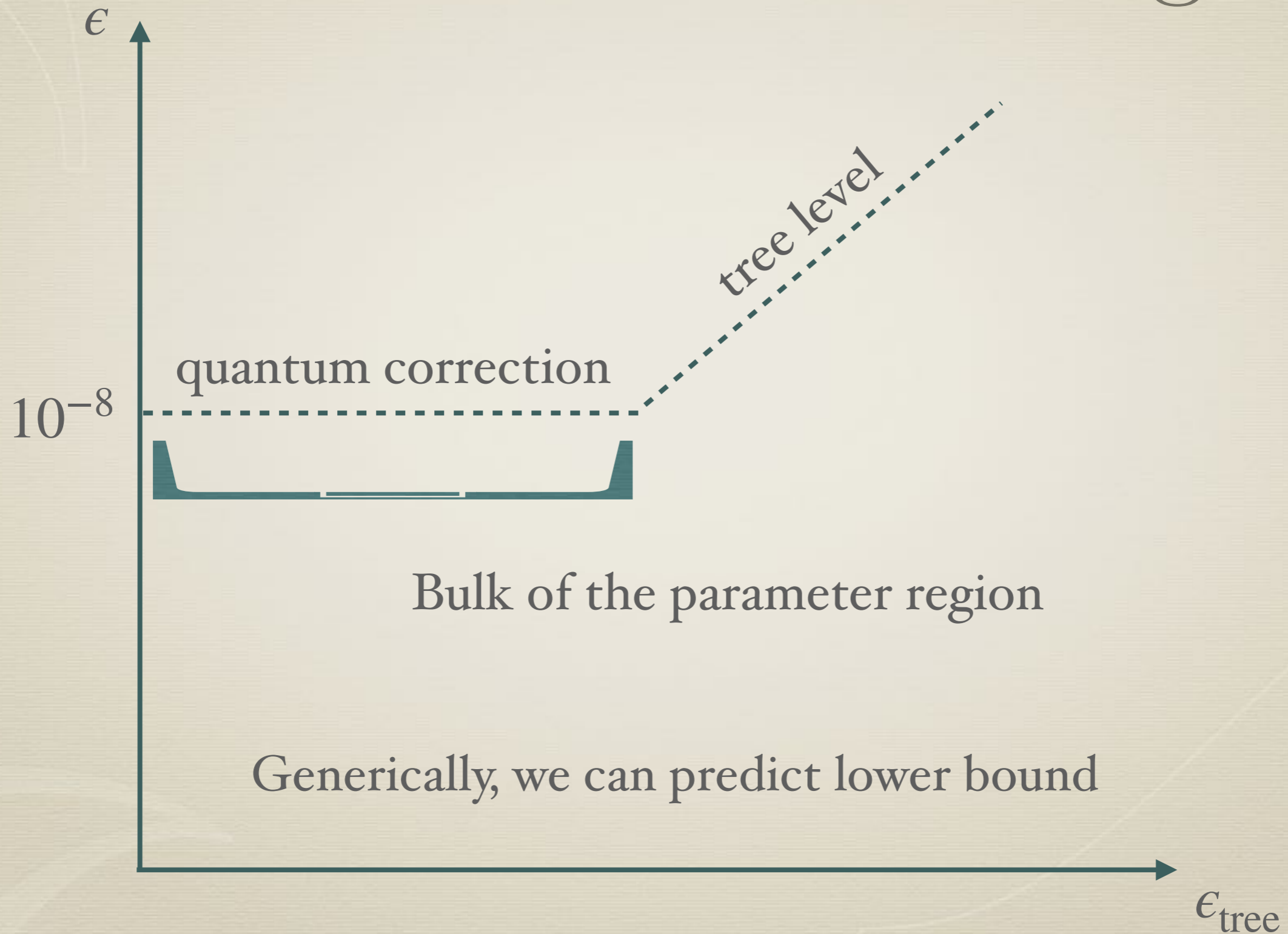
Dunsky, Hall, KH (2019)



$$\epsilon = \epsilon_{\text{tree}} + \epsilon_{\text{quantum correction}}$$



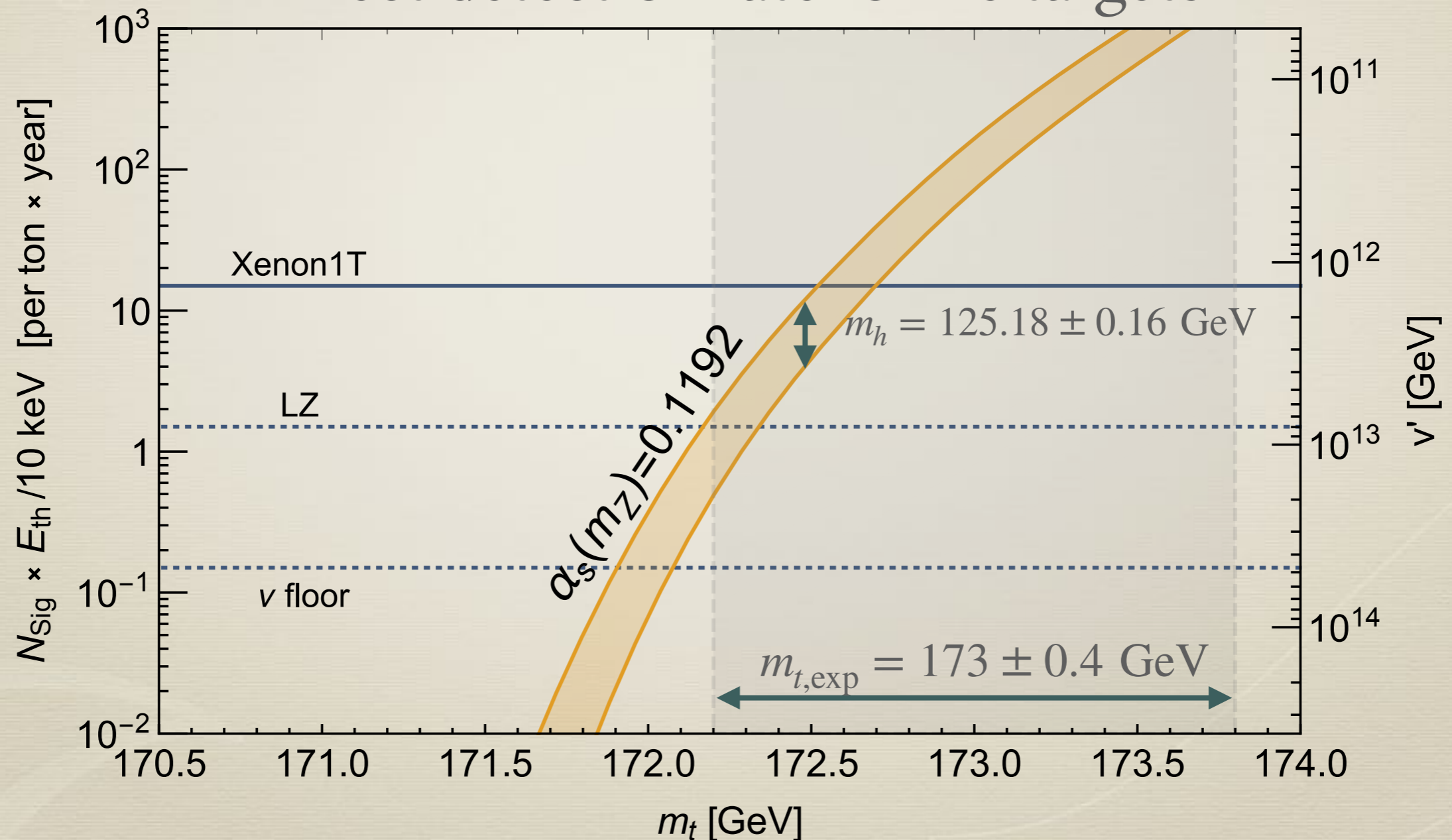
# Prediction on mixing



# SM parameters and DM

Dunsky, Hall, KH (2019)

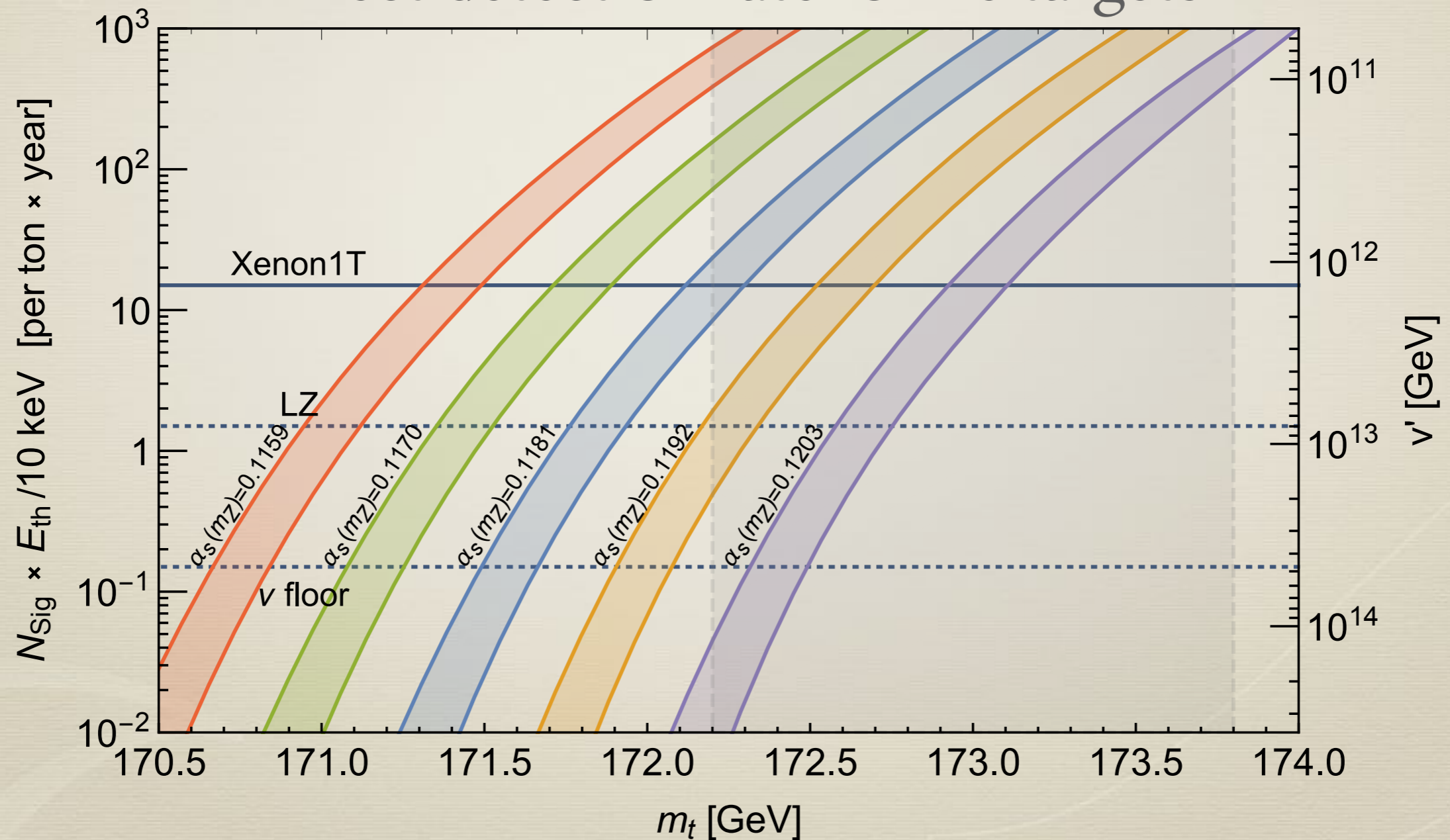
## Direct detection rate for Xe targets



# SM parameters and DM

Dunsky, Hall, KH (2019)

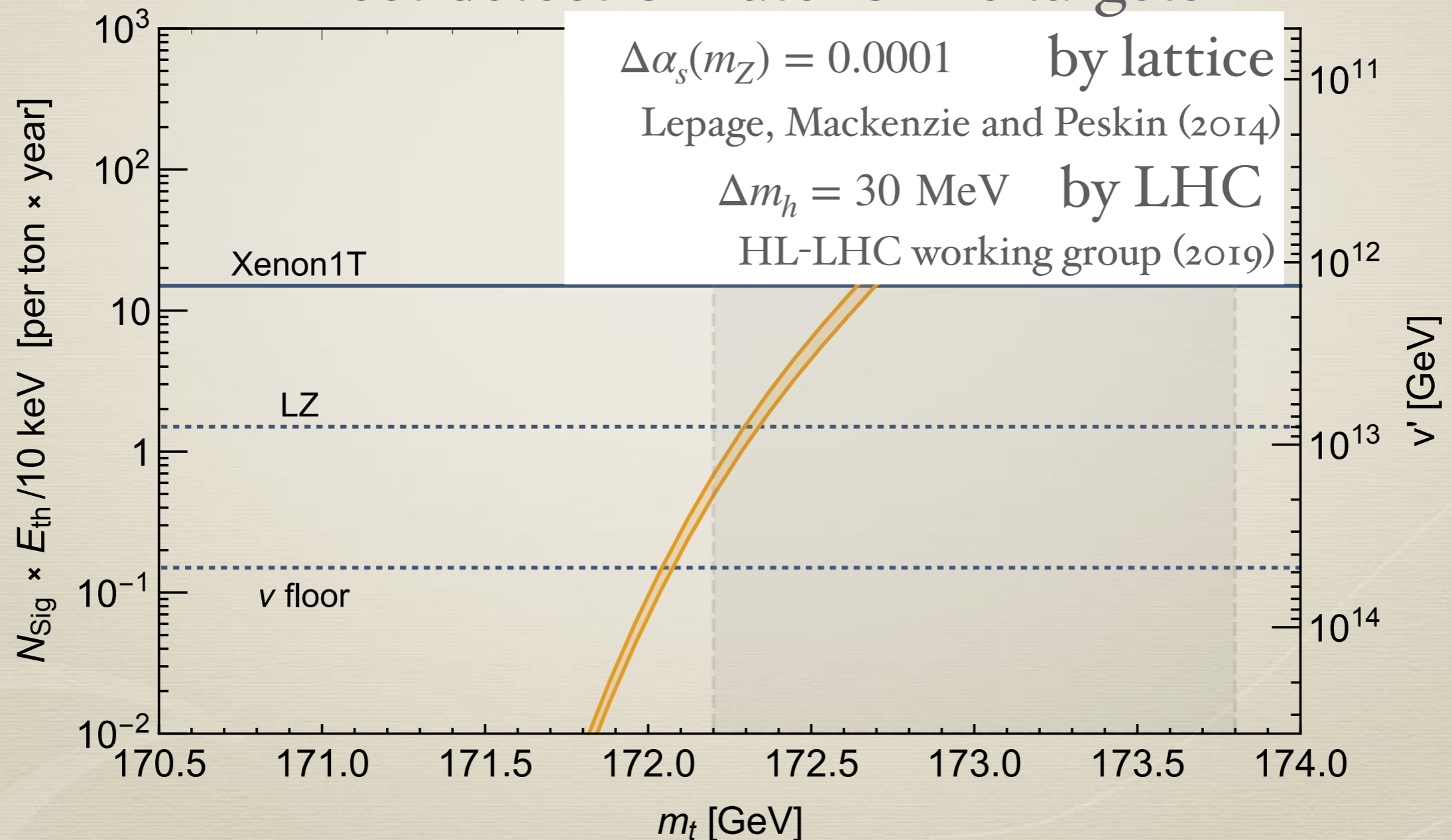
## Direct detection rate for Xe targets



# SM parameters and DM

Dunsky, Hall, KH (2019)

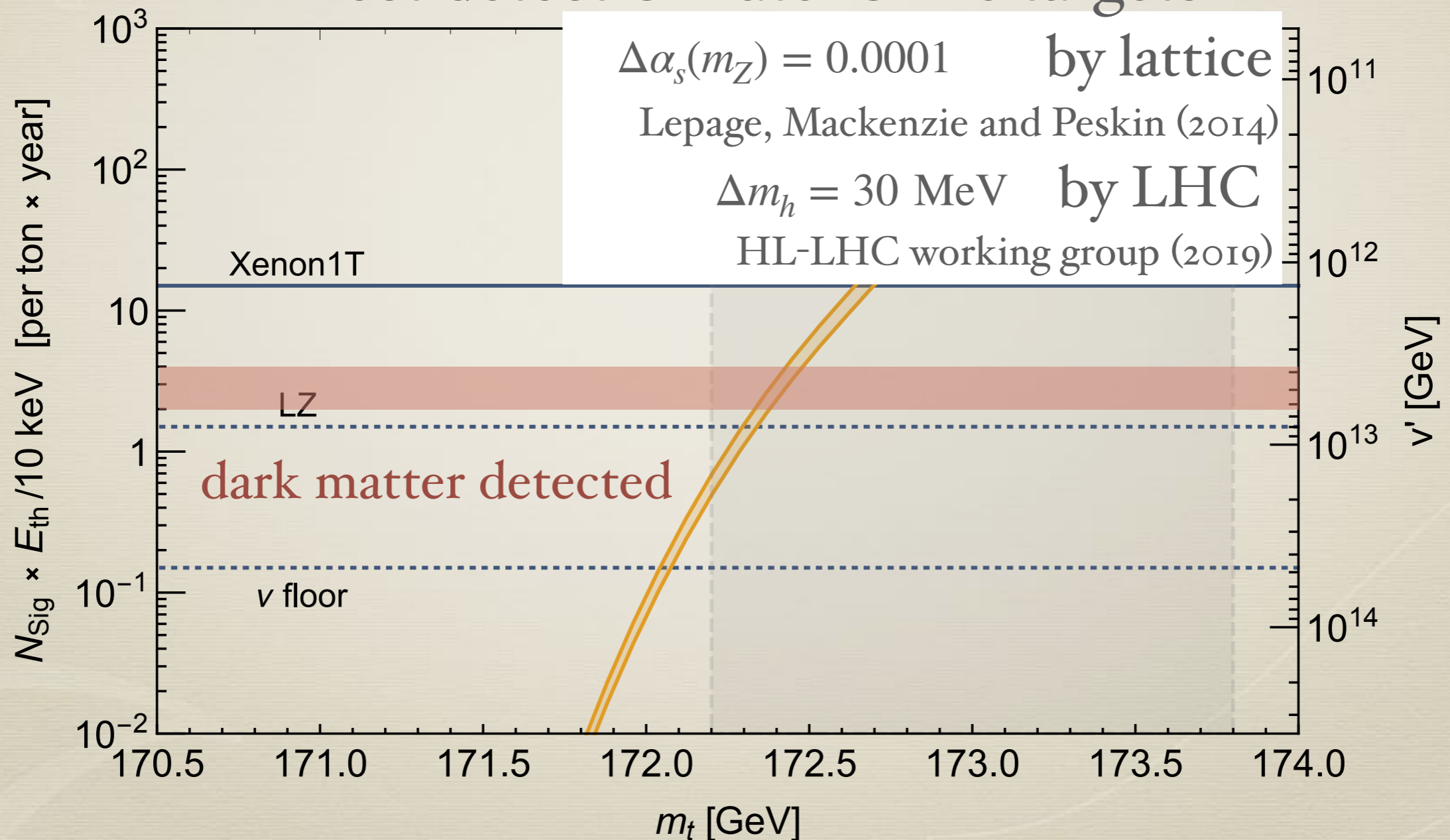
## Direct detection rate for Xe targets



# SM parameters and DM

Dunsky, Hall, KH (2019)

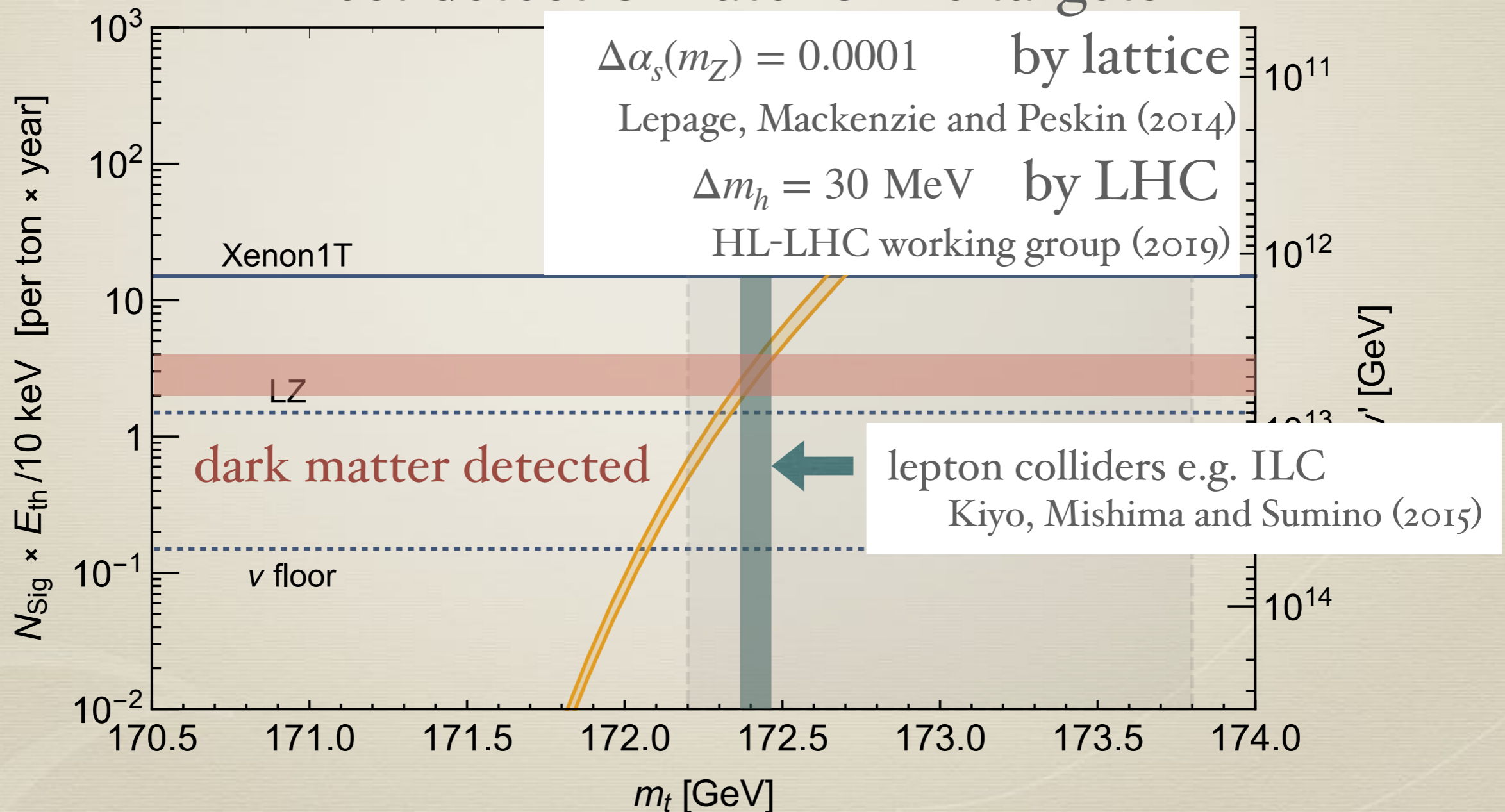
## Direct detection rate for Xe targets



# SM parameters and DM

Dunsky, Hall, KH (2019)

## Direct detection rate for Xe targets





# $u'u'u'$ DM?

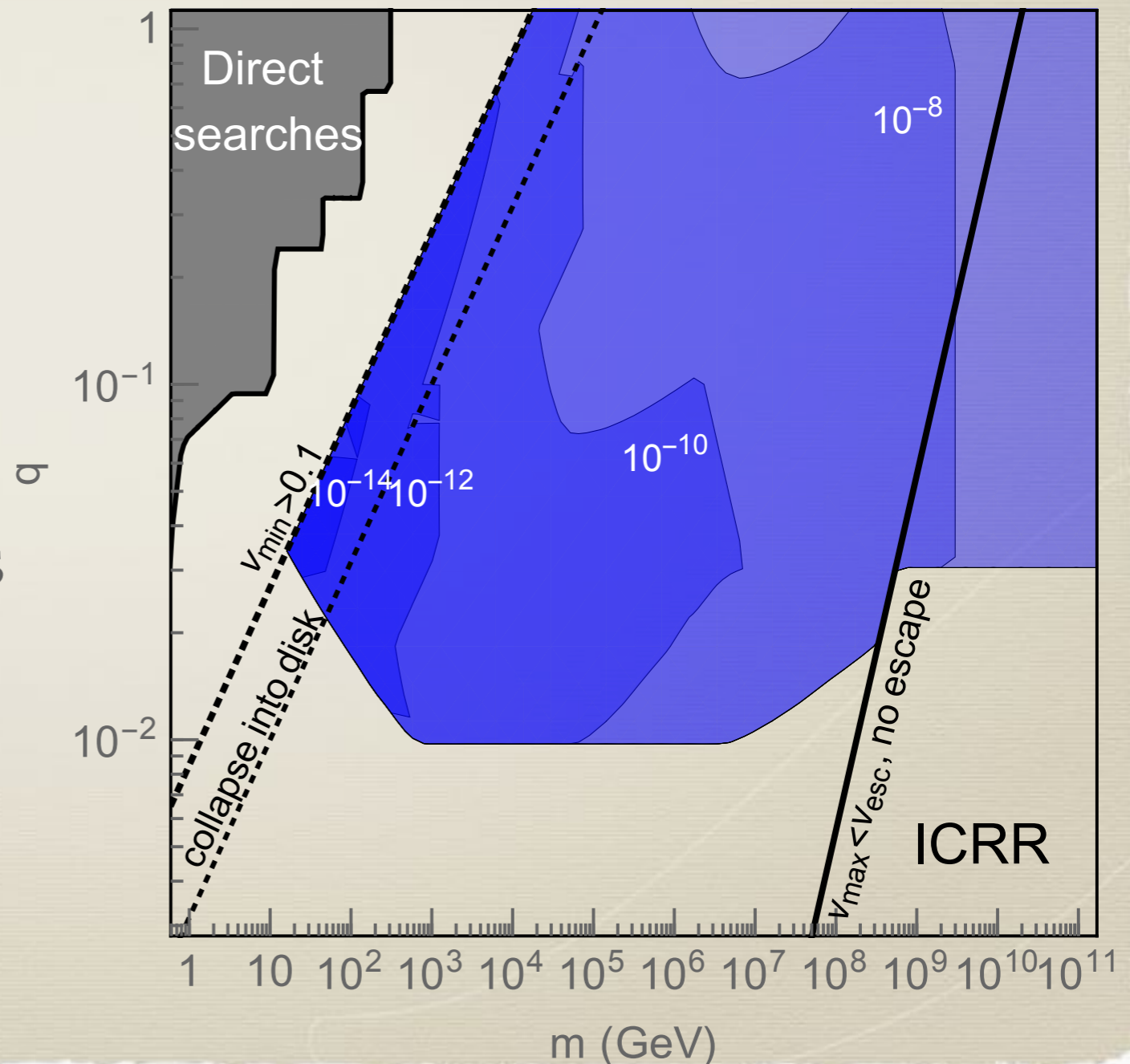
$u'qq$ ,  $u'q\bar{q}$  are necessarily produced after the QCD phase transition

Dunsky, Hall, KH (2018)

Upper bound on

$$\frac{\Omega_{u'\bar{u}}}{\Omega_{\text{DM}}}$$

by ionizing particle searches



# $u'u'u'$ DM?

Dunsky, Hall, KH (2019)

Y of colour neutral states

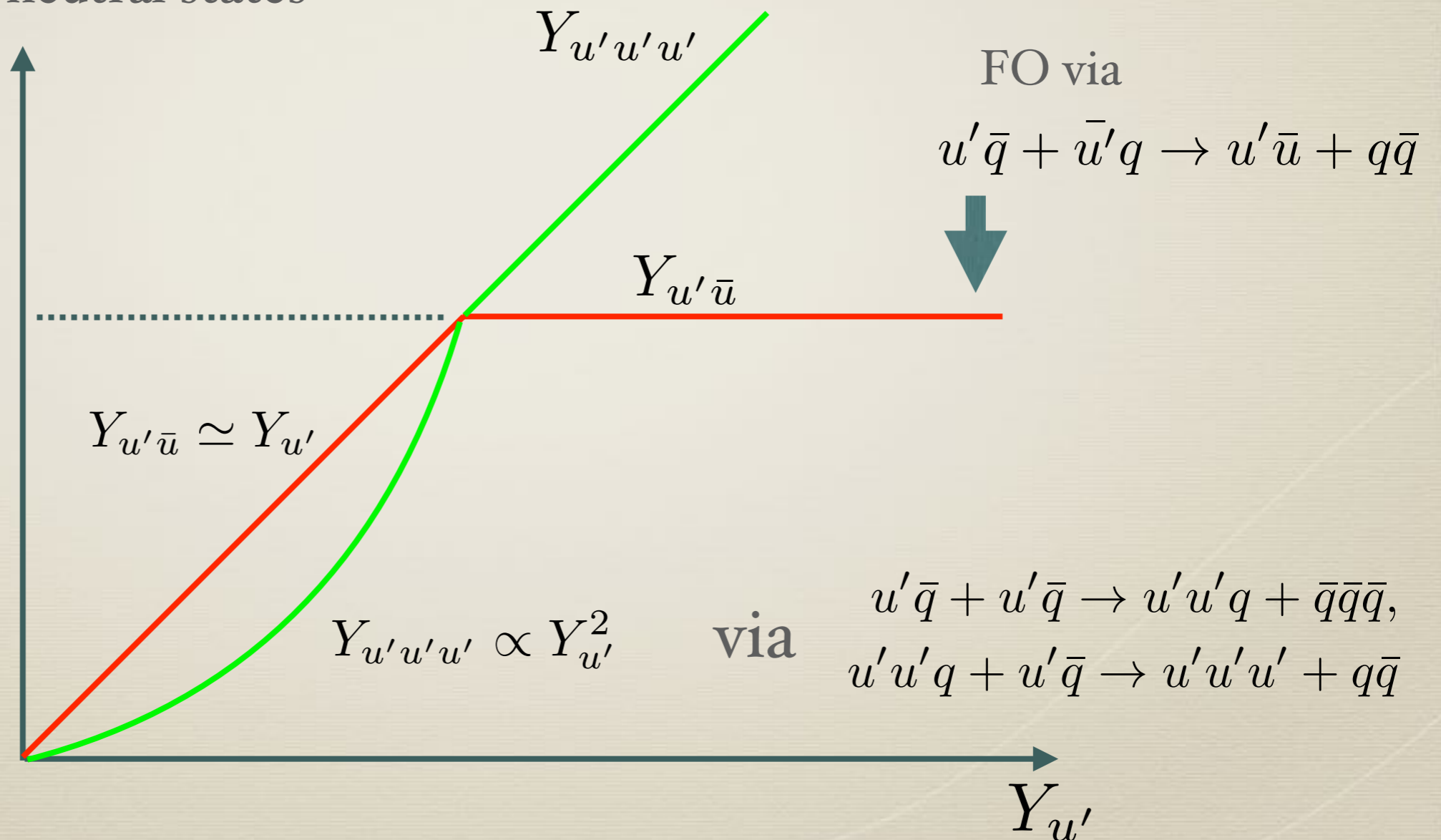
At the smallest

$$\frac{\Lambda_{\text{QCD}}}{M_{pl}} \sim 10^{-18}$$

Likely to be larger

Arvanitaki et.al (2005)

De Luca et.al (2018)



# $e'$ without $u'$

$$T \ll m_{u'} \text{ and}$$

Dunsky, Hall, KH (2019)

Inflaton  $\rightarrow e'e\bar{a}'$ ,  ~~$u'u\bar{a}'$~~

e.g. by

$$2m_{e'} < \phi < 2m_{u'}$$

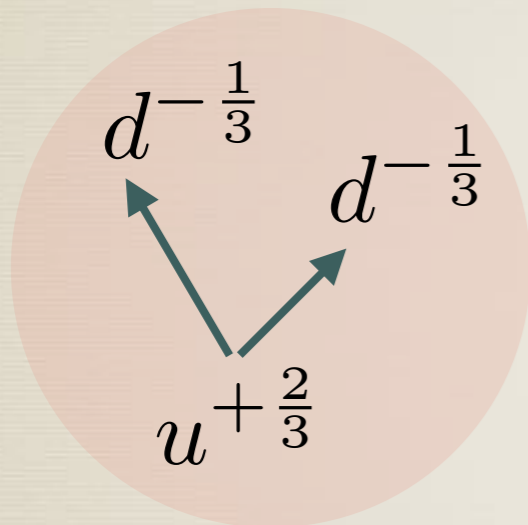
Other possibilities?

Baryogenesis for low temperature?

Higgs Parity can solve  
Strong CP problem

# QCD seems to preserve CP

Naively, neutrons will have electric dipole moments



$$d_n/e \sim 0.1 \text{ fm} \sim 10^{-14} \text{ cm} ?$$



$$H = d_n \vec{E} \cdot \vec{S} \quad \text{Electric field-spin interaction}$$

However,

$$d_n/e < 2.9 \times 10^{-26} \text{ cm} \quad \text{Baker et.al (2006)}$$

Suggests CP symmetry

$$d_n \vec{E} \cdot \vec{S} \xrightarrow{\text{CP=T}} -d_n \vec{E} \cdot \vec{S} \quad \rightarrow \quad d_n = 0$$

# CP is not preserved in SM

$$\mathcal{L} = y_{ij}^u H^\dagger q_i \bar{u}_j + y_{ij}^d H q_i \bar{d}_j + \frac{\theta_{\text{QCD}}}{8\pi^2} \mathbf{E}^a \cdot \mathbf{B}^a$$

CP violation

observed  $\theta_{\text{CKM}} = O(1)$   $\Rightarrow$   $y^{u,d}$  must have complex phases  $\Rightarrow$  CP is violated

$$d_n/e \simeq 5 \times 10^{-16} \bar{\theta} \text{ cm} \quad \text{Crewther, Vecchia and Witten (1979)}$$

$$\bar{\theta} = \text{argdet}(y^u y^d) + \theta_{\text{QCD}} < 10^{-10}$$

The strong CP problem

# Known Solutions

- \* QCD axion
- \* Spontaneously broken CP
- \* Spontaneously broken parity

# Known Solutions

\* **QCD axion**

Peccei and Quinn (1977)

Weinberg (1978), Wilczek (1978)

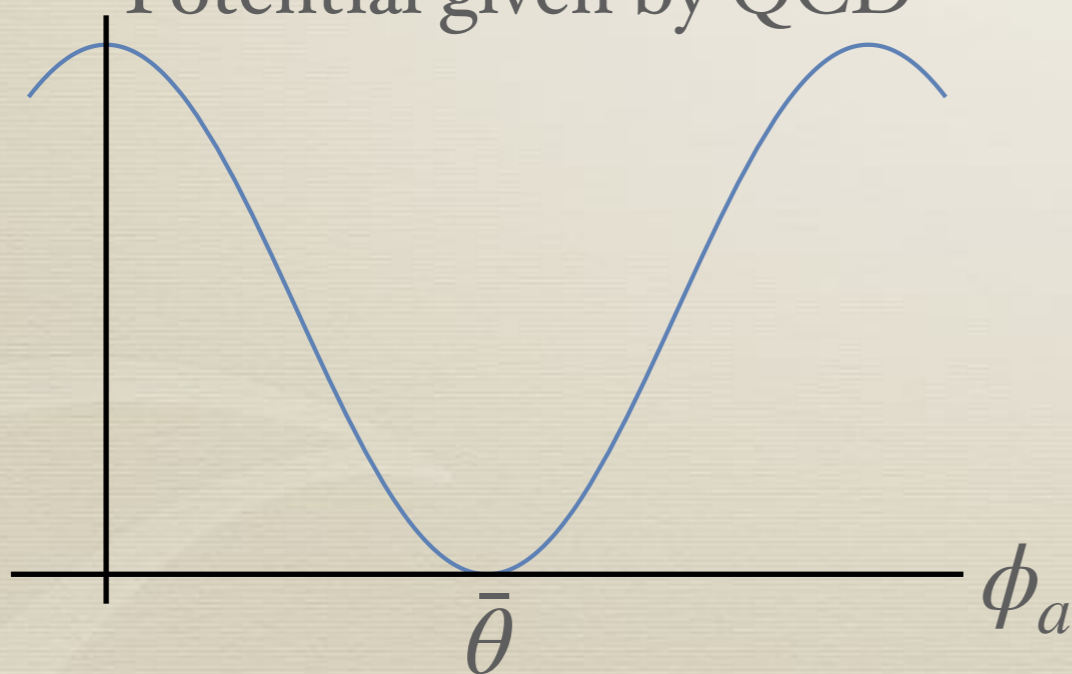
\* Spontaneously broken CP

\* Spontaneously broken parity

$$\bar{\theta} \rightarrow \bar{\theta} - \phi_a(x)$$

Axion is a dark matter candidate

Potential given by QCD



Abbott and Sikivie (1983), Dine and Fischler (1983), Preskill, Wise and Wilczek (1983), Davis (1986), Co, Hall and KH (2017, 2019), KH and Leedom (2019)

can produce baryon asymmetry of the universe (axiogenesis)

Co and KH (2019)



# Known Solutions

- \* QCD axion
- \* **Spontaneously broken CP**
- \* Spontaneously broken parity

$$\text{CP} \rightarrow \bar{\theta} = 0, d_n = 0$$

CP symmetry is spontaneously broken  complex yukawa  $y^{u,d}$

but in a sophisticated way so that  $\bar{\theta}$  remains zero

Nelson (1984), Barr (1984)

# Known Solutions

\* QCD axion

Mohapatra and Senjanovic (1978)

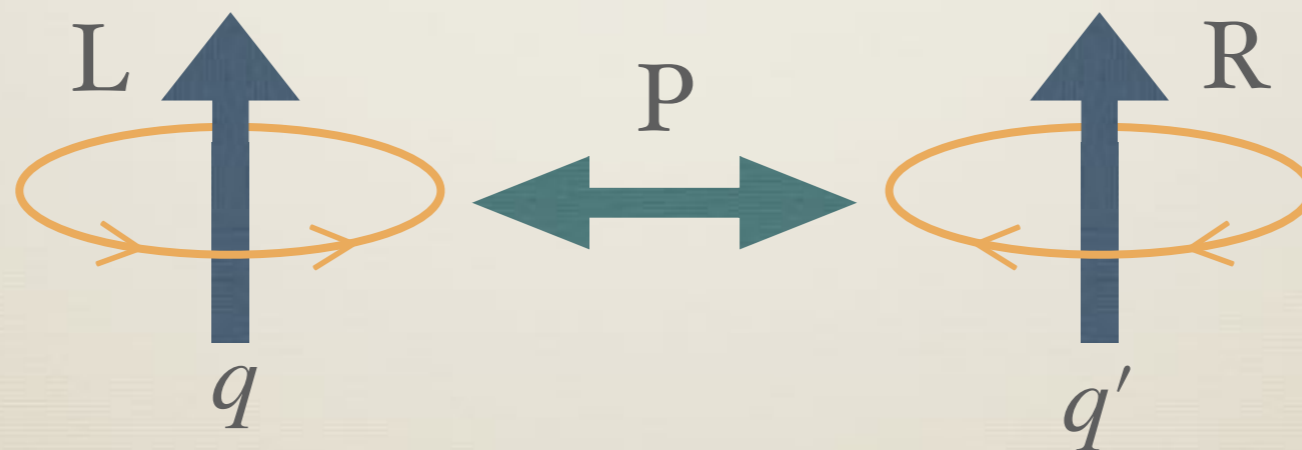
Beg and Tsao (1978)

Babu and Mohapatra (1989)

\* Spontaneously broken CP

Barr, Chang and Senjanovic (1991)

\* Spontaneously broken parity



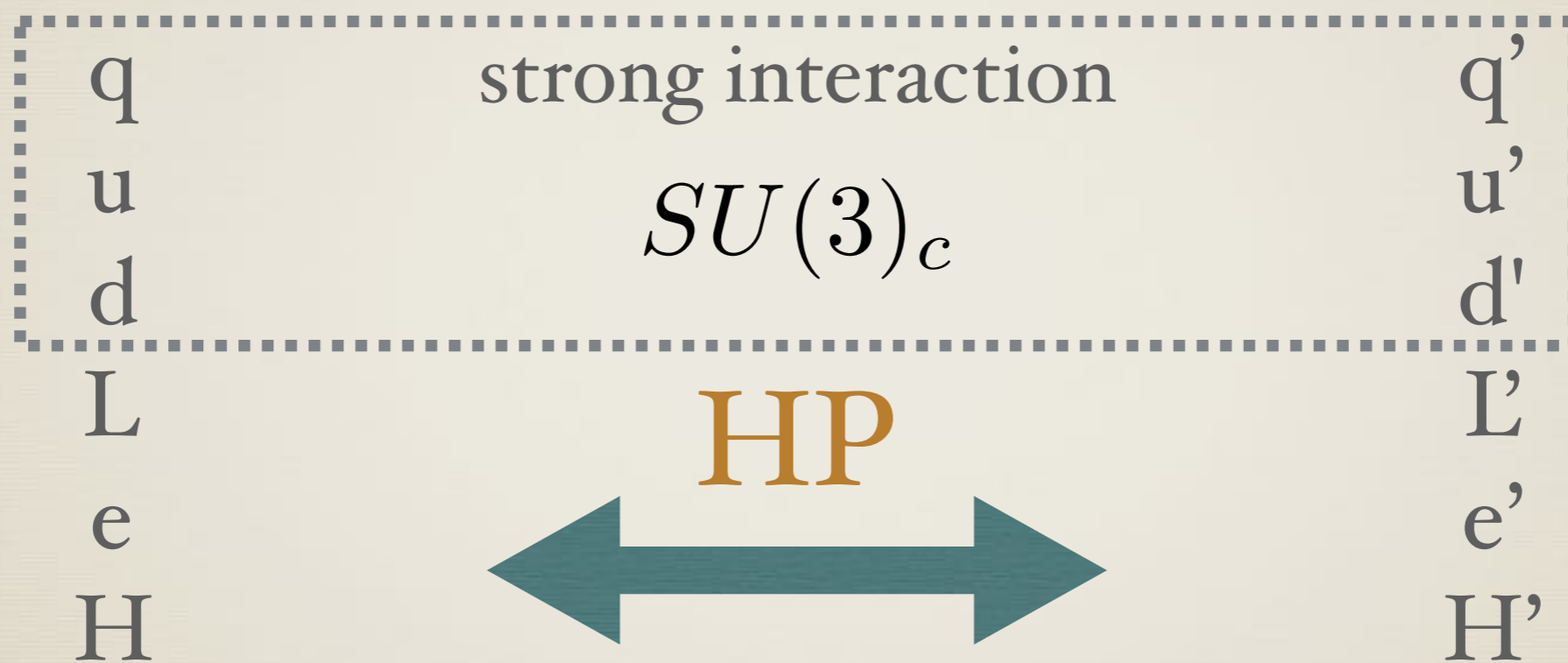
How the strong CP problem is solved depends on what  $q'$  is.

( $q'$  = antiparticle of  $q$  : P is CP)

# Mirrored electroweak theory

SM particles

New particles



electroweak

electroweak'

$W, Z \quad SU(2)_L \times U(1)_Y$

$W', Z' \quad SU(2)'_L \times U(1)'_Y$

$\gamma \quad U(1)_{EM}$

$\gamma' \quad U(1)'_{EM}$

# Strong CP problem solved

Barr, Chang and Senjanovic (1991)

HP

$$\mathcal{L} = yq\bar{u}H^\dagger + yq'^\dagger\bar{u}'^\dagger H' + y^*q^\dagger\bar{u}^\dagger H + y^*q'\bar{u}'H'^\dagger$$

$$\Delta\bar{\theta}_q$$

$$\Delta\bar{\theta}_{q'} = -\Delta\bar{\theta}_q$$

$$\bar{\theta} = \Delta\bar{\theta}_q + (-\Delta\bar{\theta}_q) = 0$$

cancel with each other

HP

$$+\frac{\theta_{\text{QCD}}}{8\pi^2}\mathbf{E}^a \cdot \mathbf{B}^a$$

Neutron  
electric dipole moment

# Space-time parity and neutron EDM

The neutron EDM vanishes in the parity symmetric limit

$$~~H = d_n \vec{E} \cdot \vec{S}~~$$

$\langle H \rangle \ll \langle H' \rangle$  spontaneously breaks the parity

We expect non-zero neutron EDM at some level

# Non-zero CP violation

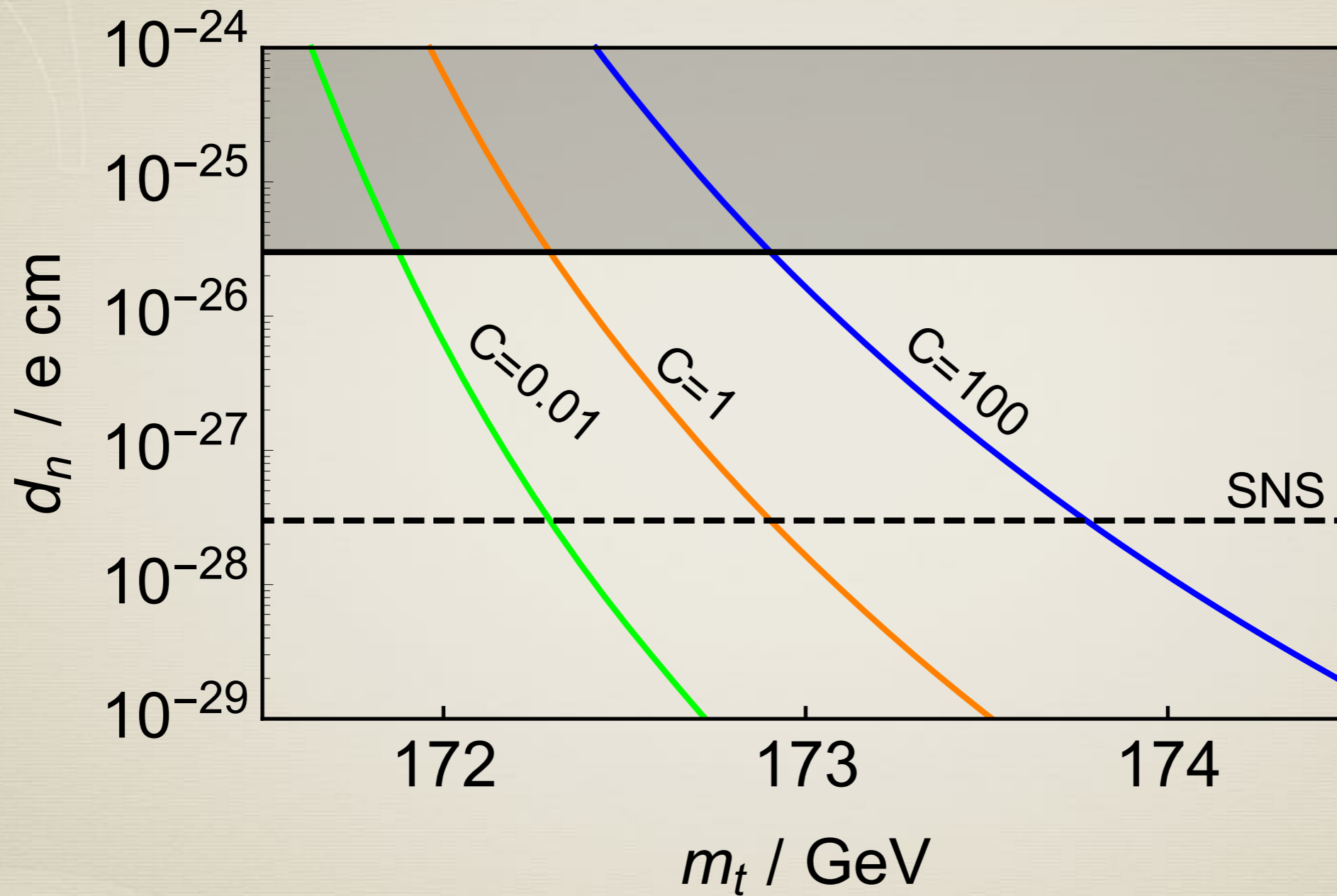
$$\frac{C}{M_{\text{pl}}^2} \left( |H|^2 - |H'|^2 \right) \underline{\mathbf{E} \cdot \mathbf{B}}$$

Electric and magnetic  
fields of gluon

$$d_n \simeq 10^{-26} e \text{ cm} \times C \left( \frac{v'}{10^{12} \text{ GeV}} \right)^2$$

- \* Present limit  $d_n < 2.9 \times 10^{-26} e \text{ cm}$  Baker et.al (2006)
- \* PSI  $d_n < 5 \times 10^{-27} e \text{ cm}$  Baker et.al (2011)
- \* SNS  $d_n < 3 \times 10^{-28} e \text{ cm}$  Tsentalovich (2014)

# Neutron EDM



$$\frac{C}{M_{\text{pl}}^2} \left( |H|^2 - |H'|^2 \right) \mathbf{E} \cdot \mathbf{B}$$



# Experimental program

Dunsky, Hall and KH (2019)

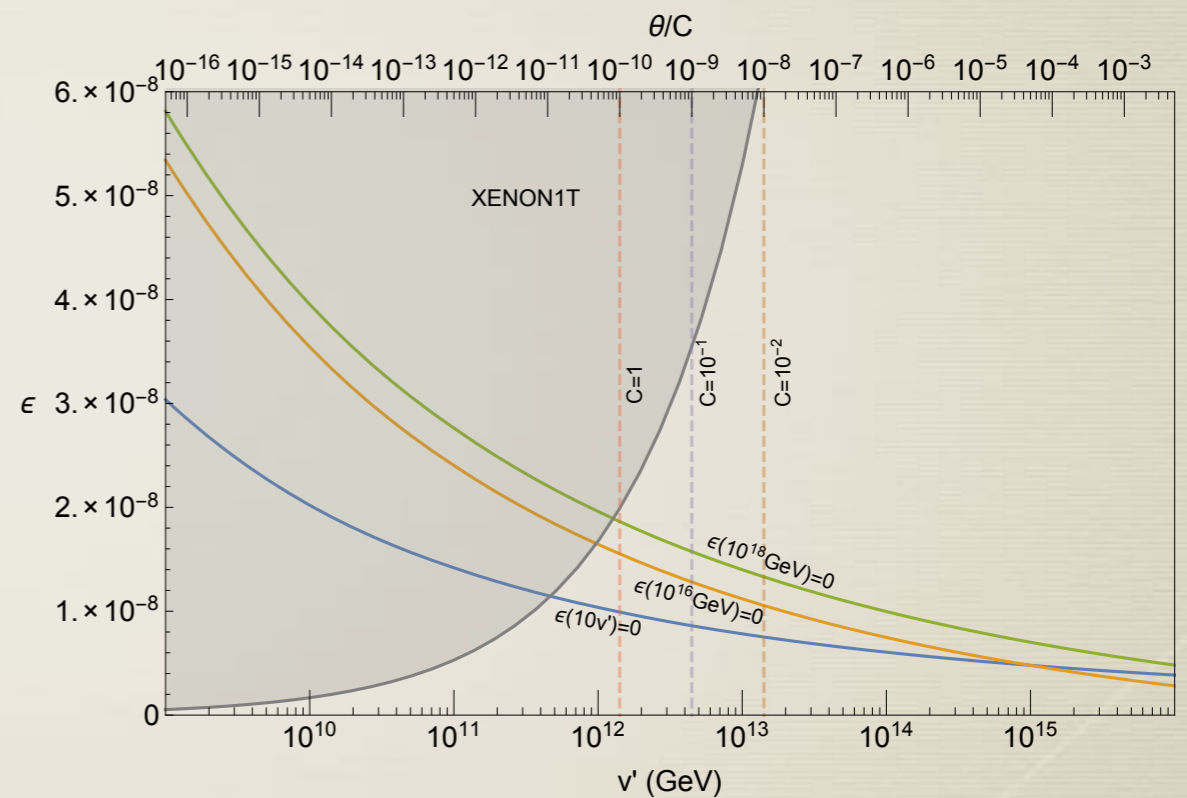
Top quark yukawa  
Higgs mass  
Strong coupling constant



Higgs Parity  
symmetry breaking scale



Dark matter detection  
Neutron EDM

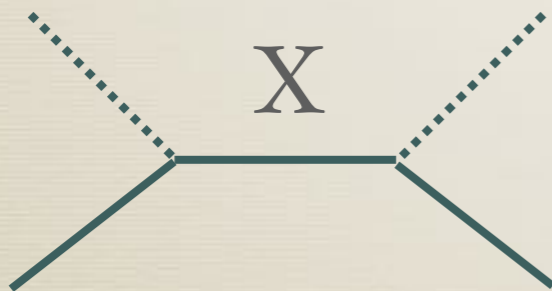


GUT

# Yukawa interaction

No gauge invariant renormalizable coupling

$$\frac{c_{ij}}{M} H H' q_L \bar{q}_R$$



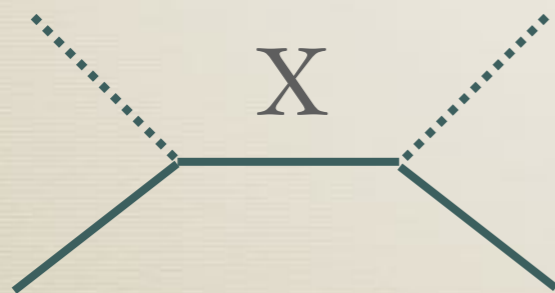
# Strong CP problem solved

Babu and Mohapatra (1989)

Hall and KH (2018)

No gauge invariant renormalizable coupling

$$\frac{c_{ij}}{M} HH' q_L \bar{q}_R$$



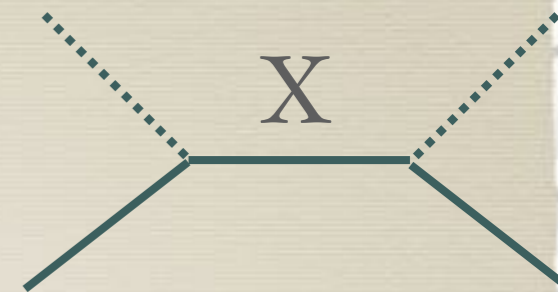
$$q_L(t, x) \stackrel{\text{HP}}{\leftrightarrow} q_R(t, -x)$$



$$c = c^\dagger, \arg(\det[c]) = 0$$

# Yukawa couplings

Small enough not to blow up the gauge coupling



	$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)$	$SU(4)$	$SO(10)$	coupling
up	<b>3</b>	<b>1</b>	<b>1</b>	$2/3$	<b>15</b>	<b>45</b>	$\bar{X}_q H^\dagger + X_{q'} H'^\dagger$
	<b>3</b>	<b>2</b>	<b>2</b>	$-1/3$	$6/10$	<b>45, 54, 210/210</b>	$\bar{X}_q H'^\dagger + X_{q'} H^\dagger$
down	<b>3</b>	<b>1</b>	<b>1</b>	$-1/3$	$6/10$	<b>10, 126/120</b>	$\bar{X}_q H + X_{q'} H'$
	<b>3</b>	<b>2</b>	<b>2</b>	$2/3$	<b>15</b>	<b>120, 126</b>	$\bar{X}_q H' + X_{q'} H$
electron	<b>1</b>	<b>1</b>	<b>1</b>	$-1$	<b>10</b>	<b>120</b>	$\bar{X}_l H + X_{l'} H'$
	<b>1</b>	<b>2</b>	<b>2</b>	$0$	$1/15$	<b>10, 120/120, 126</b>	$X_l H' + X_{l'} H$
neutrino	<b>1</b>	<b>1</b>	<b>1</b>	$0$	$1/15$	<b>1, 54, 210/45, 210</b>	$X(\ell H^\dagger + \ell' H'^\dagger)$
	<b>1</b>	<b>2</b>	<b>2</b>	$-1$	<b>10</b>	<b>210</b>	$\bar{X}_l H'^\dagger + X_{l'} H^\dagger$
	<b>1</b>	<b>3</b>	<b>1</b>	$0$	<b>1</b>	<b>45</b>	$X_l H^\dagger$
	<b>1</b>	<b>1</b>	<b>3</b>	$0$	<b>1</b>	<b>45</b>	$X_{l'} H'^\dagger$

# SO(10) embedding

$$q, \ell, q', \ell' = 16$$

Hall, KH (2018)

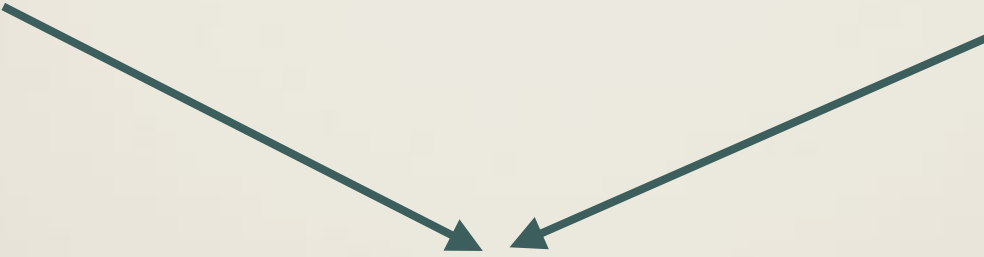
$$H, H' \subset 16_H$$

$$q(t, x) \leftrightarrow \bar{q}'(t, x)$$

C: Part of SO(10)

$$q(t, x) \leftrightarrow i\sigma_2 q^*(t, -x)$$

CP


$$q(t, x) \leftrightarrow i\sigma_2 \bar{q}'^*(t, -x)$$

$$SO(10) \times CP \xrightarrow{\phi_{45}^-} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times P_{LR}$$

# CKM phase

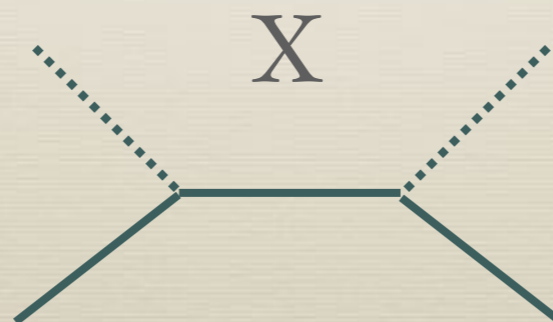
$$SO(10) \times CP \xrightarrow{\phi_{45}^-} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times P_{LR}$$

Real yukawas, without CP symmetry breaking...

A simple renormalizable example to obtain CP phases

$$\mathcal{L} = (M^{ij} + i\lambda^{ij} \phi_{45}) X_{10,i} X_{10,j}$$

$$\frac{c_{ij}}{M} H H' q_i q'_j$$



# Top-down perspective

## SUSY GUT

3 parameters

$g_{\text{GUT}}, M_{\text{GUT}}, m_{\text{SUSY}}$



4 parameters

$g_1, g_2, g_3, v_{\text{EW}}$   
(or more, e.g.  $\Omega_{\text{DM}}$ )

## Similar structures

## Parity GUT

4 parameters

$g_{\text{GUT}}, M_{\text{GUT}}, v', y_t$



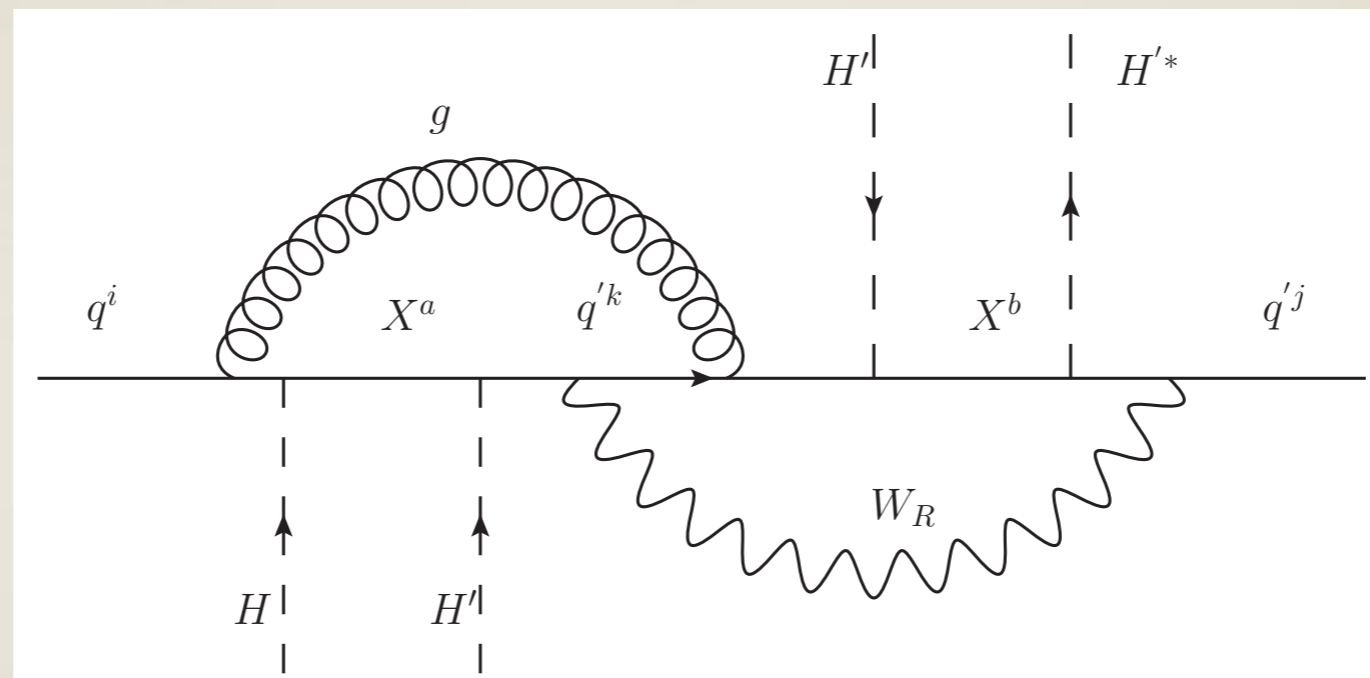
5 parameters

$g_1, g_2, g_3, y_t, \lambda_{\text{higgs}}$



# Non-zero CPV

Hall, KH (2018)



$$\delta\theta \sim 10^{-11} \frac{\theta_{23}^u \theta_{23}^d}{V_{cb}^2}$$

Suppressed by loop factors, flavor mixing

# Correction to the gauge coupling unification by high dimensional operator

$$SO(10) \xrightarrow{\phi_{210}} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times C_{LR}$$

$$\frac{210^{abcd}}{M_*} F_{10}^{ab} F_{10}^{cd} \quad \Delta \left( \frac{2\pi}{\alpha} \right) \lesssim 10$$

$$SO(10) \times CP \xrightarrow{\phi_{45}} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times P_{LR}$$

$$\frac{45^{ac}}{M_*} \frac{45^{bd}}{M_*} F_{10}^{ab} F_{10}^{cd} \quad \Delta \left( \frac{2\pi}{\alpha} \right) \lesssim 1$$

# Correction to the gauge coupling unification by high dimensional operator

$$SO(10) \xrightarrow{\phi_{54}} SU(4) \times SU(2)_L \times SU(2)_R \times C_{LR}$$

$$\frac{54^{ab}}{M_*} F_{10}^{ac} F_{10}^{bc} \quad \Delta \left( \frac{2\pi}{\alpha} \right) \lesssim 1$$

$$SO(10) \times CP \xrightarrow{\phi_{210}} SU(4) \times SU(2)_L \times SU(2)_R \times P_{LR}$$

$$\frac{210}{M_*} \frac{210}{M_*} F_{10} F_{10} \quad \Delta \left( \frac{2\pi}{\alpha} \right) \ll 1$$

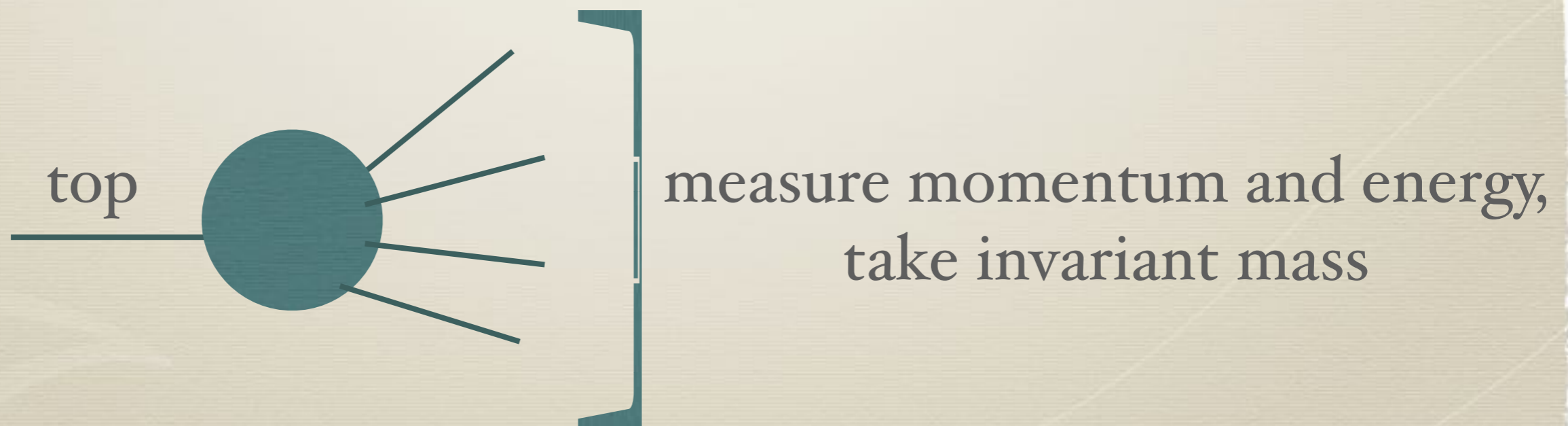
SM parameters

# “top quark mass”

pole mass  $172.9 \pm 0.4 \text{ GeV}$

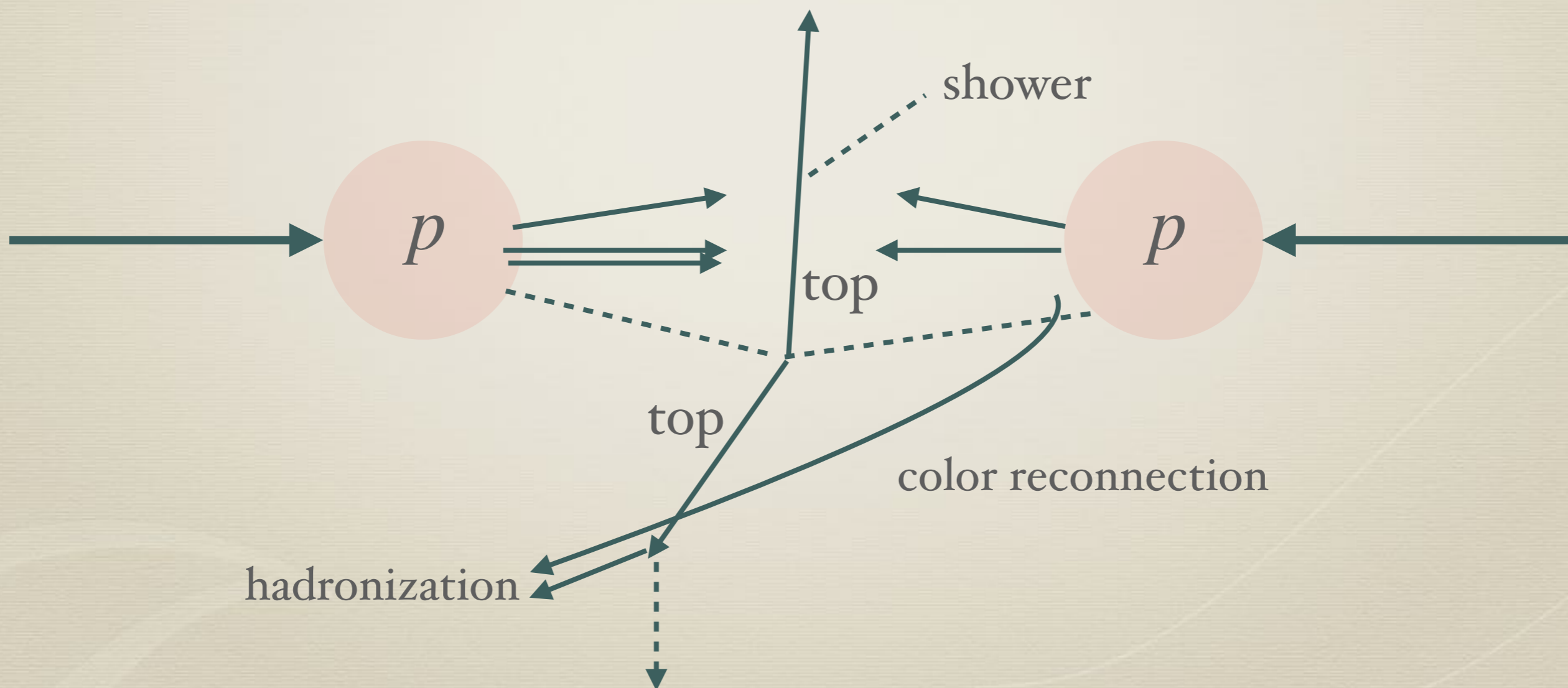
Particle Data Group

if top were colorless, isolated objects



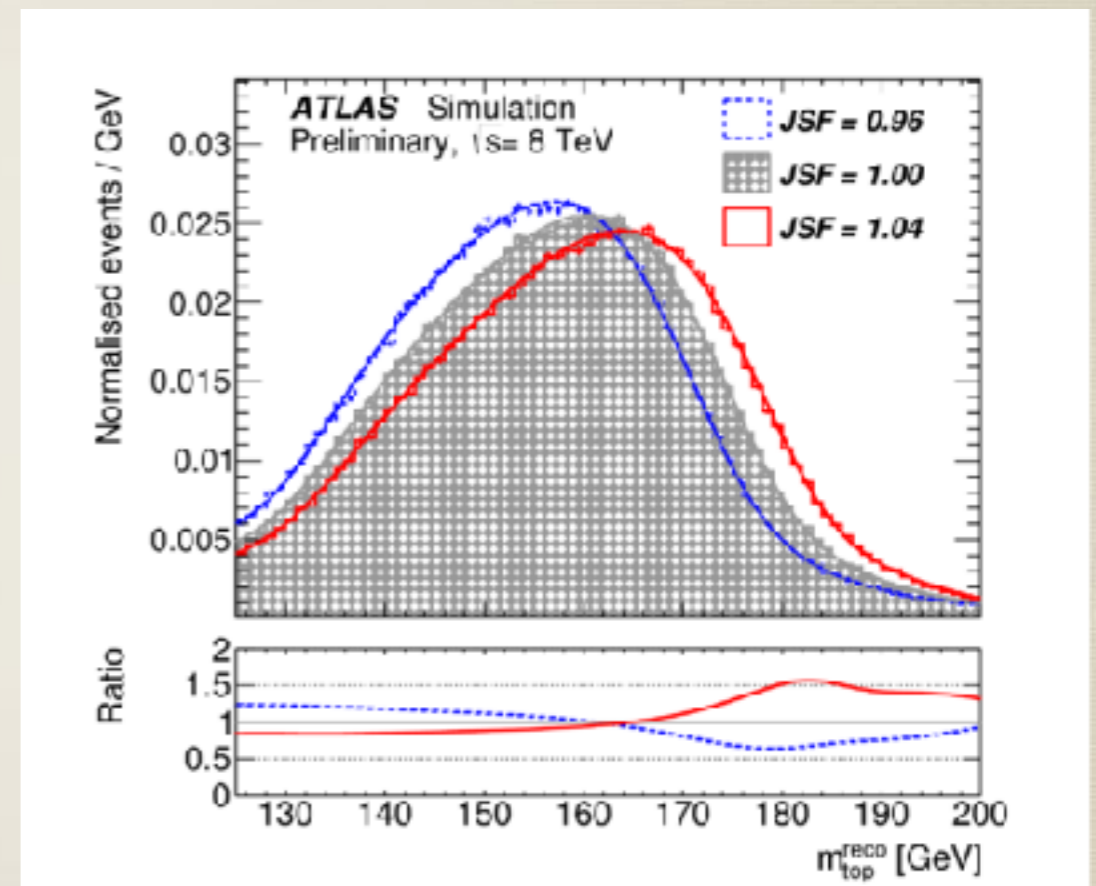
# “top quark mass”

but of course top is colored and is not isolated



# “top quark mass”

templates of distribution of kinematical observables



fitting the templates, combining results,

$$172.9 \pm 0.4 \text{ GeV}$$

Uncertainty from non-perturbative QCD  $\Delta m_t \gtrsim \Lambda_{\text{QCD}}$

# $\overline{MS}$ quantity

pole mass

$$y_{t,\overline{MS}}(m_t) = 0.93690 + 0.005556\left(\frac{m_t}{\text{GeV}} - 173.34\right) - 0.00042\frac{\alpha_s(m_Z) - 0.1184}{0.0007}$$

Buttazzo et.al. (2013)

\* NNNLO QCD corrections included

\* Uncertainty from non-perturbative nature of QCD

$$\Delta m_t \sim \Lambda_{\text{QCD}}$$

Bigi, Shifman, Uraltsev and Vainshtein (1994)

Benek and Braun (1994)

Eventually, we should directly determine  $\overline{MS}$  quantity by

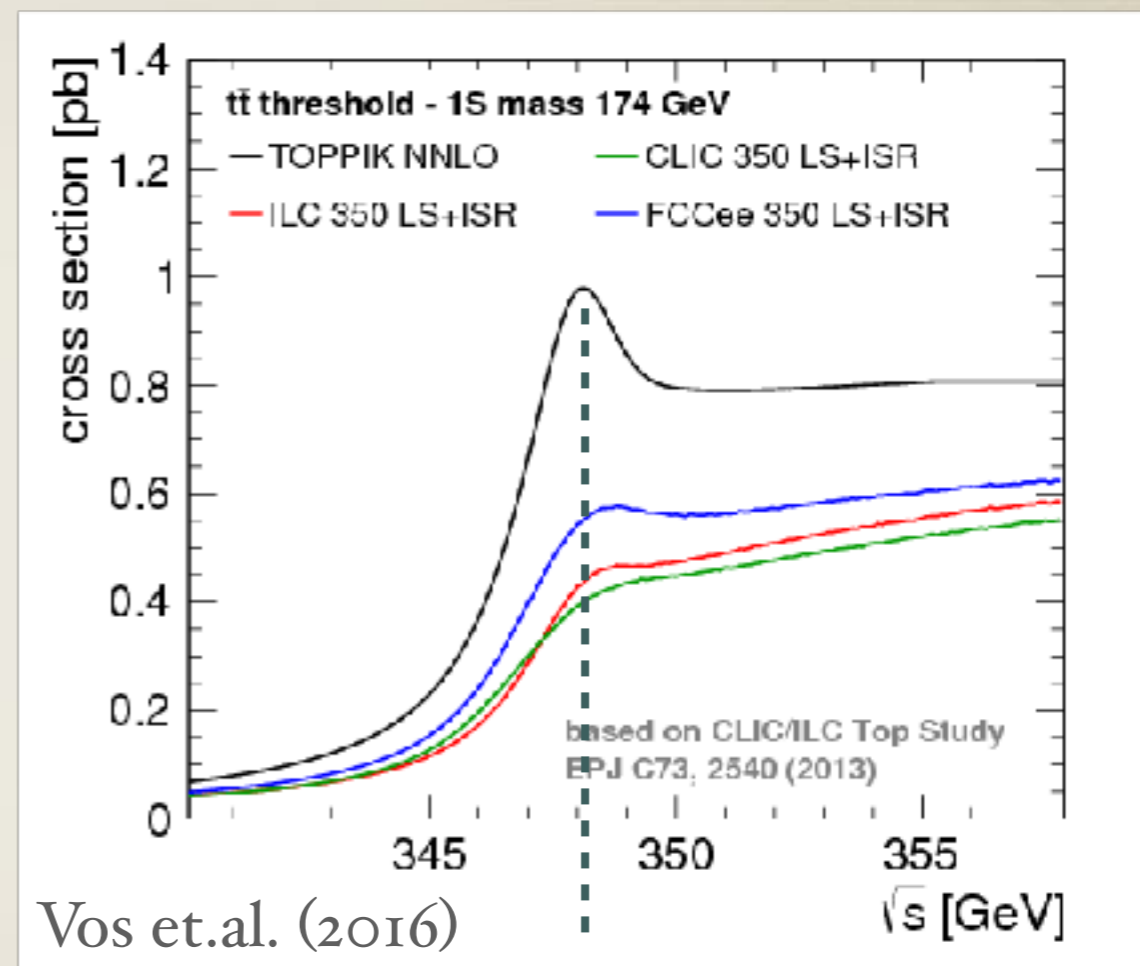
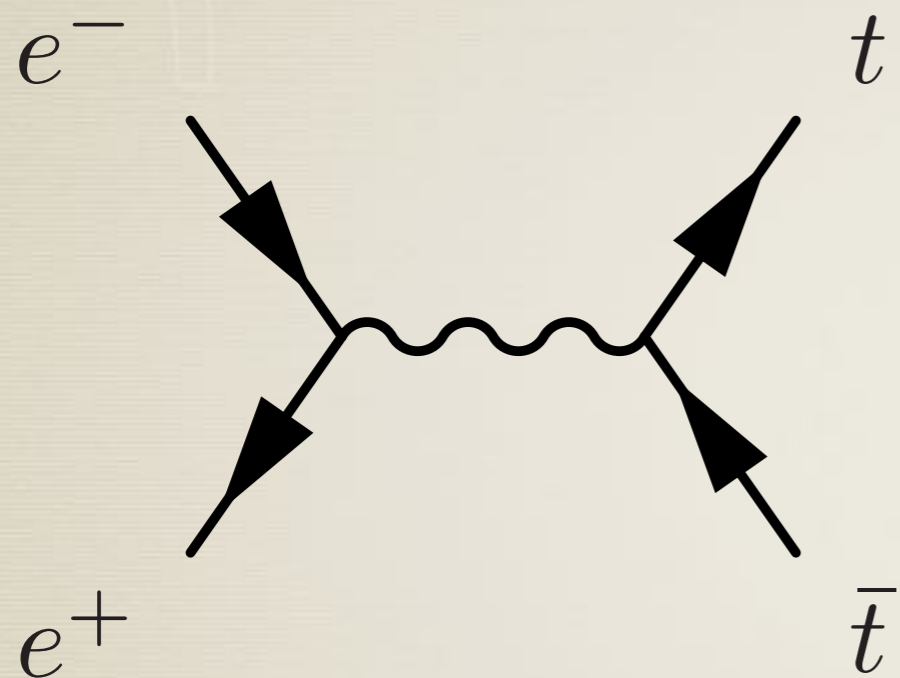
$\overline{MS}$  quantity



observables



# Lepton colliders



Vos et.al. (2016)

$$M_{t\bar{t}}(1S)$$

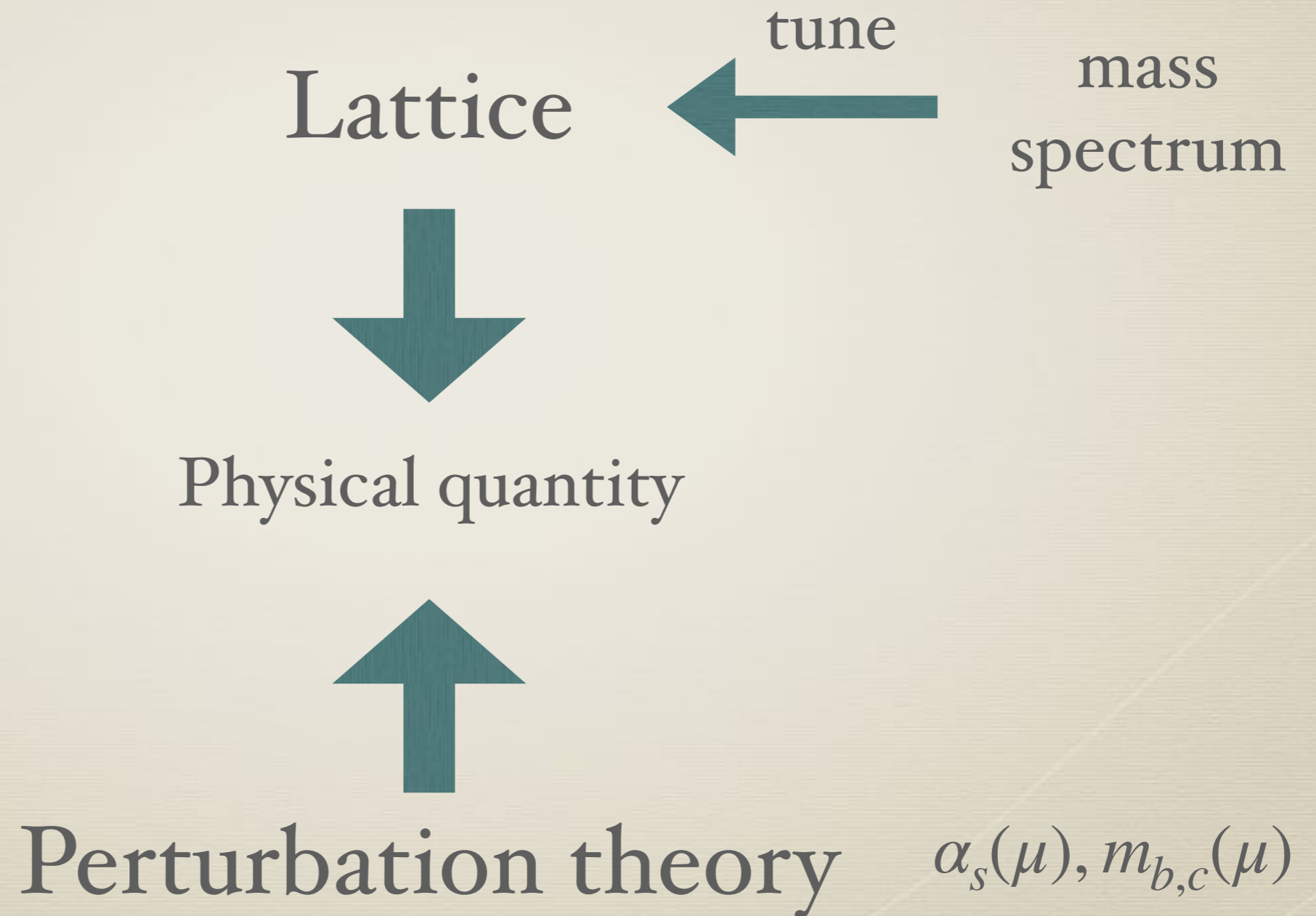
$$M_{t\bar{t}}(1S) = 2(165 + 7.20 + 1.20 + 0.216 + 0.0077 + \dots) \text{ GeV}$$

Kiyo, Mishima and Sumino (2015)

$$\Delta m_{t,\overline{MS}} \simeq \text{few tens MeV}$$

# Strong coupling constant

e.g. HPQCD collaboration (2008)



# Gravitational waves and dark radiation

# Mirror Higgs Parity

SM particles

New particles

quark q, u, d

lepton L, e

Higgs H

W, Z

$\gamma$

g

$SU(3) \times SU(2) \times U(1)$

q', u', d'

L', e'

H'

W', Z'

$\gamma'$

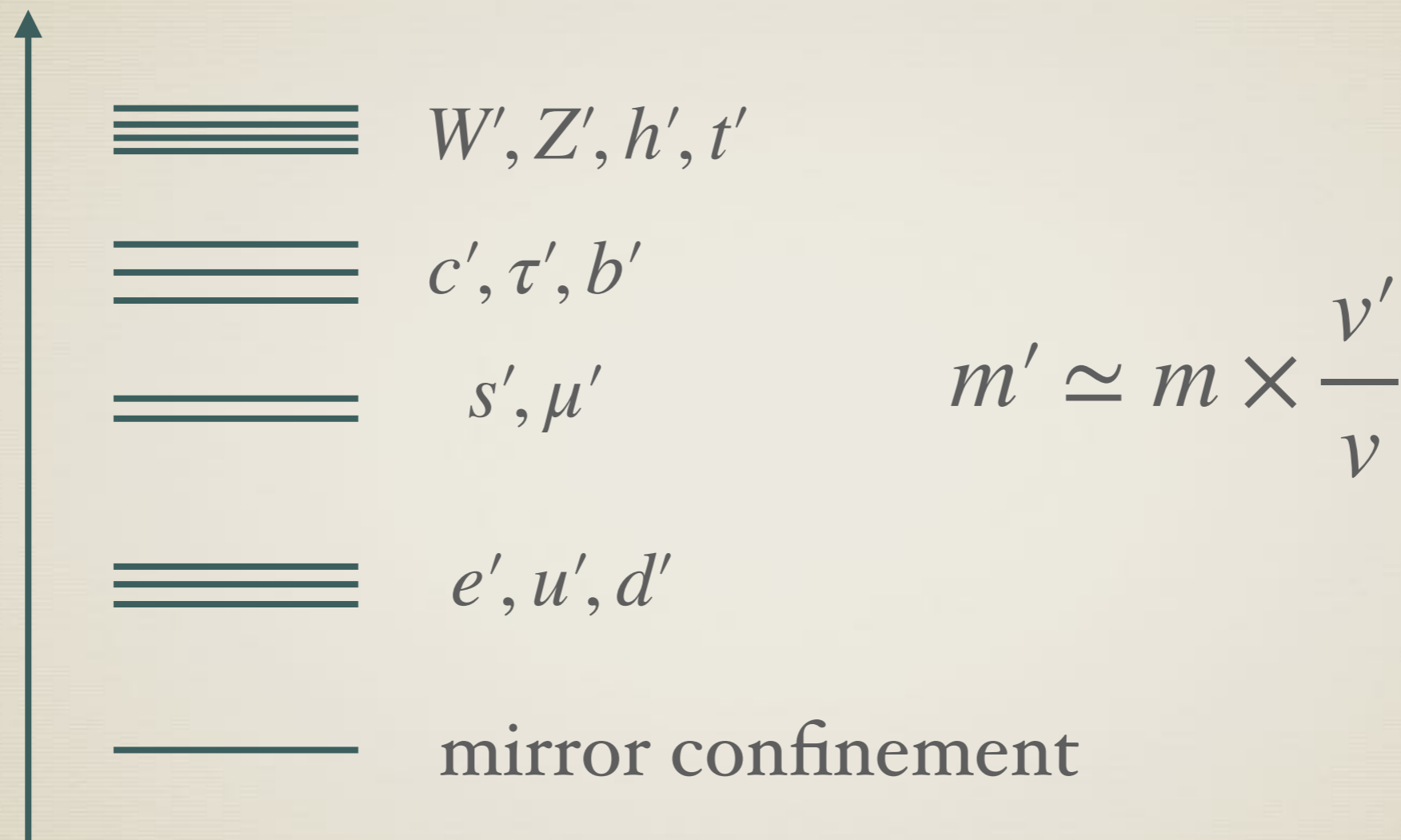
g'

$SU(3)' \times SU(2)' \times U(1)'$

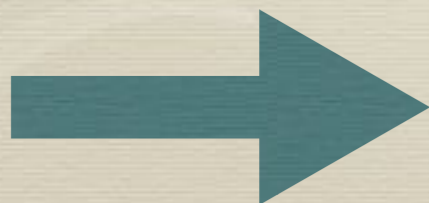
HP



# Mirror confinement



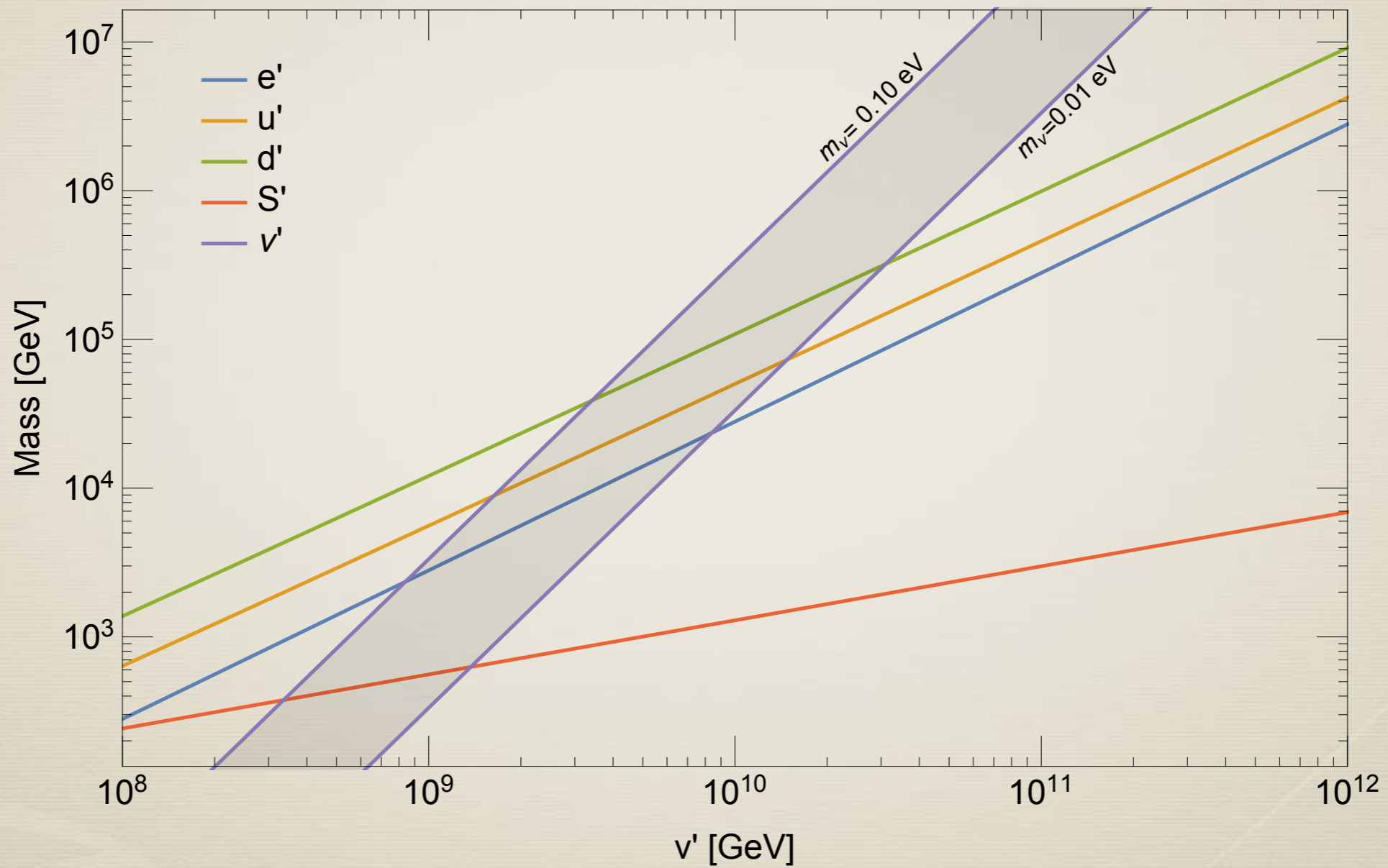
The confining occurs as a first order phase transition



Gravitational waves

# Dilution

## Mirror Spectrum

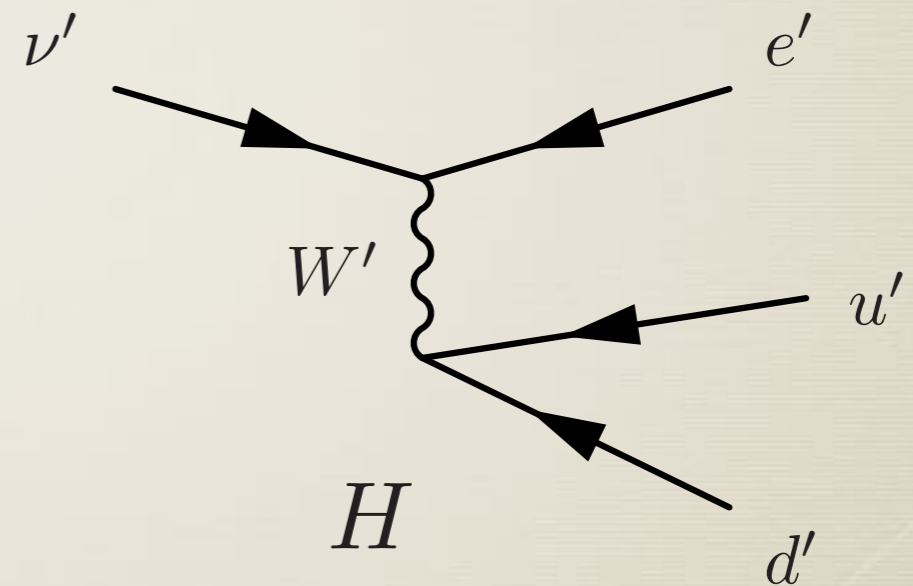


Mirror leptons and baryons overproduced, dilution required

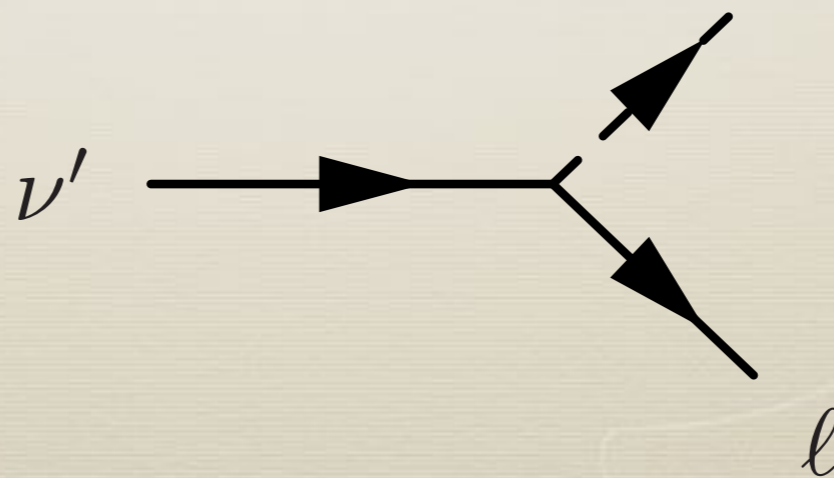
# Dilution

Mirror neutrino can be long-lived

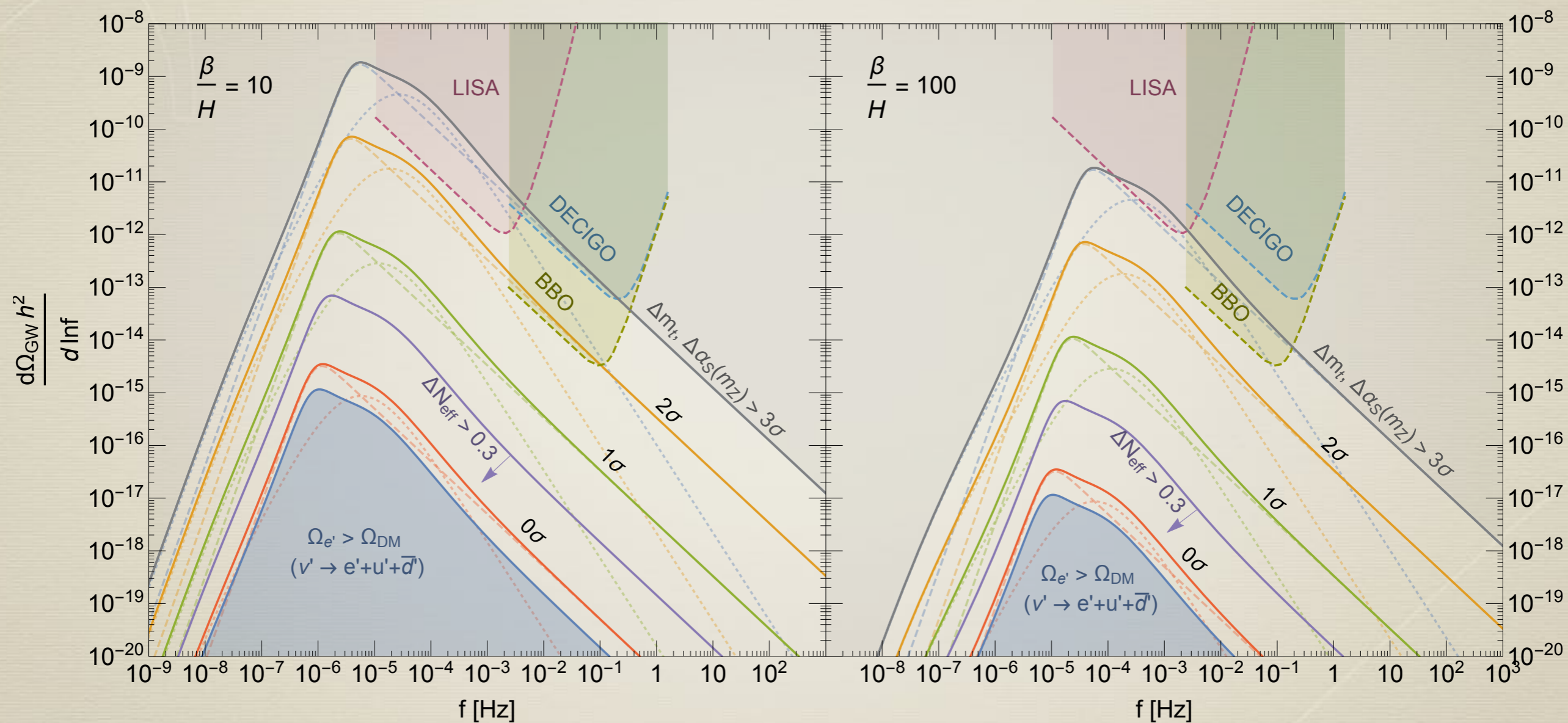
$$m'_{\nu} = m_{\nu} \left( \frac{v'}{v} \right)^2 < m'_e + m'_u + m'_d \propto v'$$



Dilution from



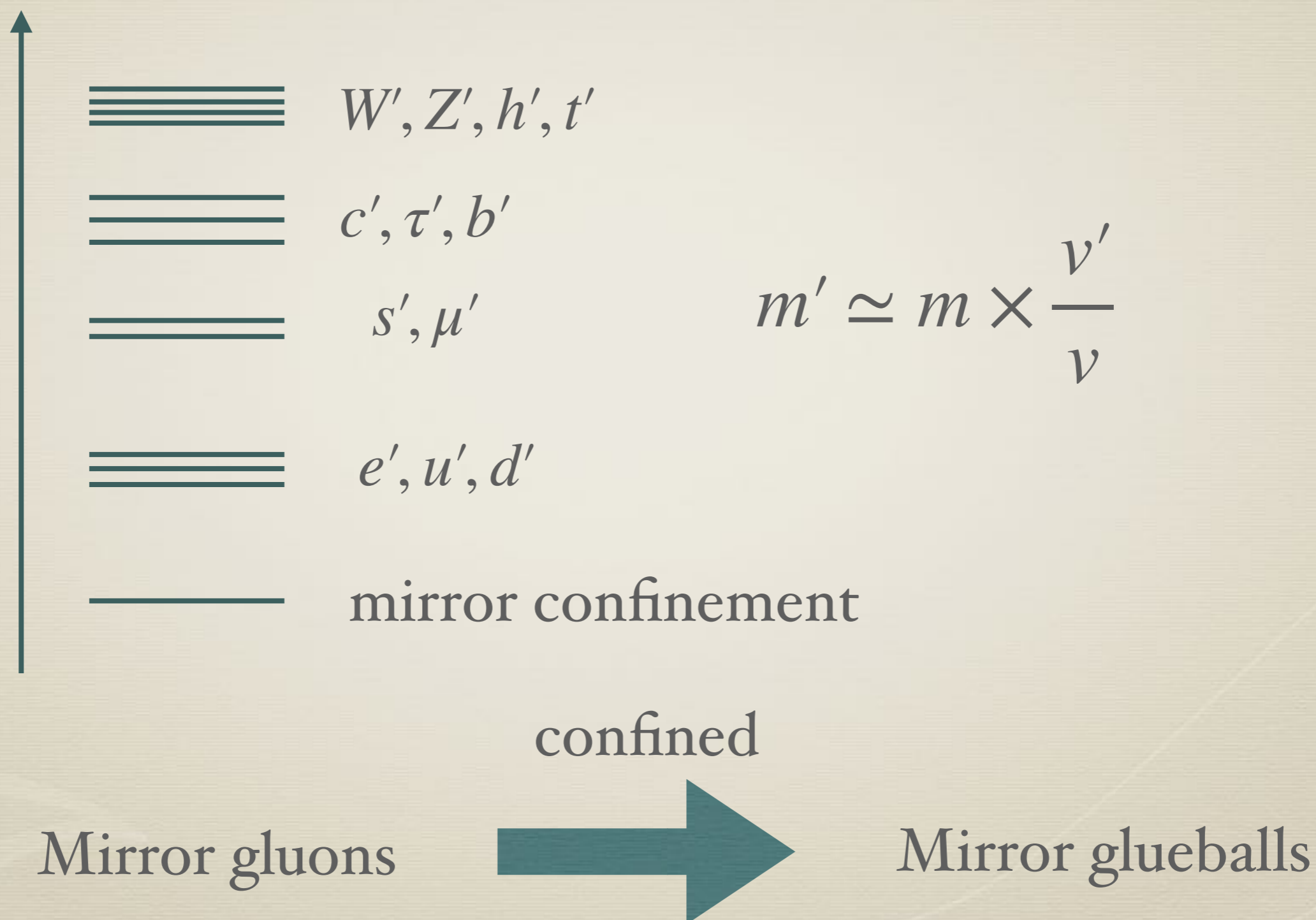
# Gravitational waves



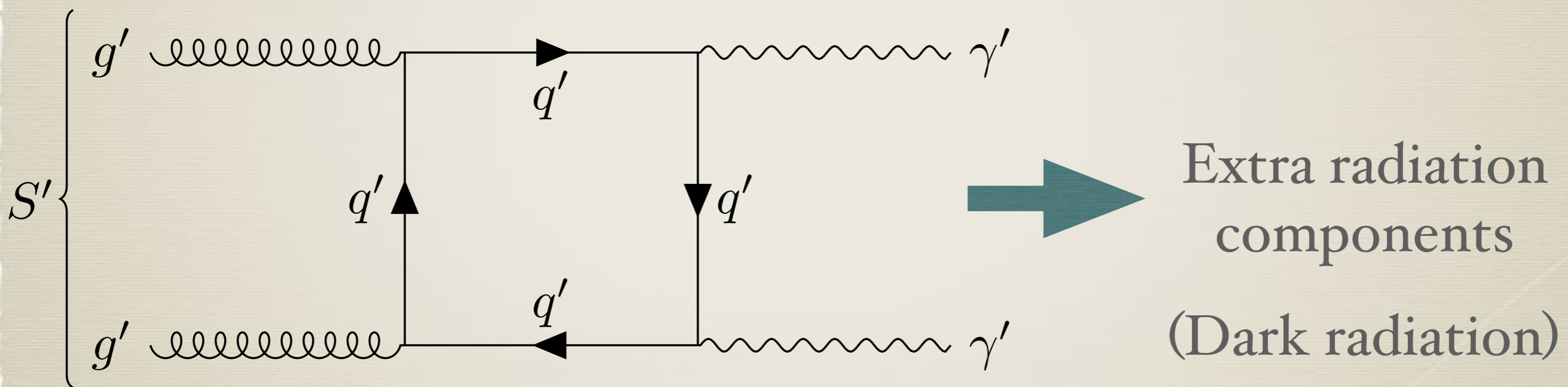
Nature of the phase transition needs to be better understood



# Mirror glueball



# Long-lived mirror glueball



$$m'_q \simeq m_q \times \frac{v'}{v}$$

