1. Introduction

- Use AdS/CFT for high energy hadron scattering
- Study string scattering on a warped geometry
- Develop preceding work, Brower, Polchinski, Strassler and Tan [06] (BPST pomeron).

We study DVCS (Deeply Virtual Compton Scattering) in sphere level and large finite ‘t Hooft coupling.

and extract Generalized Parton Distribution (GPD), which is non-perturbative parton information.

\[ A_{\text{DVCS}}(x, \eta, t, q^2) \simeq C(\eta/x) \otimes H(x, \eta, t, q^2) \]

GPD

Kinematical parameters of DVCS

\[ p^\mu = \frac{1}{2}(p_1^\mu + p_2^\mu), \quad q^\mu = \frac{1}{2}(q_1^\mu + q_2^\mu), \quad \Delta^\mu = p_2^\mu - p_1^\mu = q_1^\mu - q_2^\mu \]
\[ x = \frac{-q^2}{2p \cdot q}, \quad \eta = \frac{-\Delta \cdot q}{2p \cdot q}, \quad t = -\Delta^2 \]

skewness

Forward case (PDF) and nonzero t case have been studied. (RN, Watari ’11)

We noticed that PDF/GPD shares qualitative properties of the real QCD.

Remaining problem: nonzero skewedness

2. Aspects from Field Theory

OPE can restrict the amplitude

\[ T^{\mu \nu} = i \int d^4x e^{-i p_2 \cdot x} \{ J^\mu(x/2) J^\nu(-x/2) \} h(p_1) \]

\[ i \int d^4x e^{-ip_2 \cdot x} \{ J^\mu(x/2) J^\nu(-x/2) \} = \sum_N C_N^{\mu \nu P_1 N}(q^2) C_{N}^{P_1 N}(0; q^2). \]

Twist-2 operators give dominant contributions

\[ G_{\mu}(\frac{q_1}{\hat{D}} \frac{q_2}{\hat{D}}) \ldots (\frac{q_1}{\hat{D}} \frac{q_j}{\hat{D}}) G_{\mu} \]

However, when skewness is nonzero, operators with total derivatives are also twist-2

\[ \partial^{\sigma_1} \ldots \partial^{\sigma_m} [G_{\mu}(\frac{q_1}{\hat{D}} \frac{q_2}{\hat{D}}) \ldots (\frac{q_1}{\hat{D}} \frac{q_j}{\hat{D}}) G_{\mu}] \]

Moreover, the anomalous dimension matrix mixes among operators with different number of total derivatives.

After diagonalizing of anomalous dimension, DVCS amplitude is given as

\[ T^{\mu \nu} \simeq \eta^{\mu \nu} \left[ \sum_j C_j(\eta/x) x^{-j} \left( \frac{\Lambda^2}{q^2} \right)^{\gamma(j)/2} H_j(\eta, t, \Lambda^2) \right] \]

H_j is the non-perturbative parton information which we want.

\[ H_j(\eta, t, \Lambda^2) = \sum_{k=0}^j \eta^k H_{j,k}(t, \Lambda^2) \]

H_j is related to the matrix element of the eigen-operators of anomalous dimension.

\[ \langle h(p_2) | \hat{O}_j^{+ \ldots +}(\mu^2) | h(p_1) \rangle = \sum_{k=0}^j (\Delta^+)^k (p^+)^{j-k} H_{j,k}(t, \mu^2) \]
3. Gravitational Description

In the case of zero-skewedness, BPST naively covariantized t-channel exchange amplitudes of N (excitation number) = j (spin) strings polarized in Minkowski Directions.

\[ A_{\text{flat}} \sim \sum_j (q^-)_j \frac{(\eta^-)_j}{t - \frac{\alpha'}{2} (j - 2)} (p^+)_j \]

AdS

\[ \sum_j (q^-)_j \frac{(g^-)_j}{\Delta_j - \frac{\alpha'}{2} (j - 2)} (p^+)_j \]

However, corresponding to operator mixing in RG flow, the string states may also mixes when skewedness is nonzero.

**Our prescription:** study in an effective field theory on warped spacetime.

1. We assume there is an action of string field theory whose bilinear terms are of the form:

\[ S_{\text{bilinear}} = \frac{\pm 1}{2} \int d^D x A^{M_1 \ldots M_j} (\partial^2 - M_N^2) A_{M_1 \ldots M_j} \]

for each component field A (different Fock states are not mixed, and derivative terms are simply d’Alembertian) as bosonic open string theory in Siegel gauge.

2. We assume arbitrary local interaction terms.

3. Covariantize the derivatives into one of AdS_5 space.

In this set-up, we studied what contributes as twist-2 (leading at large q^2).

a), t-channel exchange of what types of component fields?

b), What type of interaction?

c), t-channel exchange of what eigenmode of Laplacian in AdS?

**Our result**

the twist-2 contributions are given only from

a), N = j, symmetric fields

b), interaction terms of the form

\[ c_j \frac{(2\alpha')^{j/2}}{R^5} \frac{1}{2i} \int d^4 x dz \sqrt{-g} A_{m_1 \ldots m_j} \psi \nabla^{m_1} \ldots \nabla^{m_j} \psi. \]

(coupling constant is determined in flat limit)

c), transverse and traceless mode in AdS_5

\[ g^{m_1 m_2 A_{m_1 m_2 \ldots m_j}} = 0, \quad \nabla^{m_1} A_{m_1 \ldots m_j} = 0 \]

Eigenmodes which has nonzero z component also contribute.

Summary and Discussion

We provide a method to calculate H_j in gravity dual.

So far, analytic form for arbitrary j is very complicated.

Our result is consistent:

1), Our result approaches BPST’s amplitude in zero skewedness limit.

2), Our result has correctly the form which OPE predicts. (Eq.(*))