

# Vertex operator approach for correlation functions of Belavin's $Z_n$ symmetric model

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In this talk I considered Belavin's  $(\mathbb{Z}/n\mathbb{Z})$ -symmetric model [1] on the basis of bosonization of vertex operators in the  $A_{n-1}^{(1)}$  model [2] and vertex-face transformation. This is  $sl(n)$ -generalization of Lashkevich-Pugai's construction [3], in which the integral formulae were presented for correlation functions of Baxter's eight-vertex model [4] using bosonization of vertex operators in the eight-vertex SOS model [5] and vertex-face transformation.

First I notice that the  $A_{n-1}^{(1)}$  model [6] is a restricted model, but in the present purpose, I should use unrestricted  $A_{n-1}^{(1)}$  model. Second I notice that the original vertex-face correspondence [6] maps the  $A_{n-1}^{(1)}$  model in regime III to  $(\mathbb{Z}/n\mathbb{Z})$ -symmetric model in the disordered phase. I should relate the former with  $(\mathbb{Z}/n\mathbb{Z})$ -symmetric model in the antiferroelectric phase.

I constructed a free field representation of the non-local operator  $\Lambda(u)$ , the unremovable tail of the intertwining vectors. The matrix element of  $\Lambda(u)$  can be expressed in terms of screening operators. Using this result and free field representations of  $\rho_{lk}^{(i)}$  and  $\Phi(u)_a^{a'}$ , the product of the corner transfer matrices and the vertex operators of the  $A_{n-1}^{(1)}$  model, integral formulae for correlation functions of  $(\mathbb{Z}/n\mathbb{Z})$ -symmetric model can be obtained. Furthermore, I showed that the spontaneous polarization of this model thus calculated reproduce the result by myself [7].

## 参考文献

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