

The equation of state after Inflation



MAX-PLANCK-GESELLSCHAFT

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Outline

1.) The equation of state after inflation **KL** and M. Amin (2016,17,19)

2.) Oscillons and baryogenesis **KL** and M. Amin (2014)

3.) Gauge fields, inflation and reheating **KL** and M. Amin (2016)
KL, A. Maleknejad and E. Komatsu (2018)
L. Mirzagoli, A. Maleknejad and **KL** (2019)

4.) Cosmology of fine-tuning (in particle physics)
M. Amin, J. Fan, **KL** and M. Reece (2019)

The equation of state after inflation

KL and M. Amin, arXiv:1902.06736

KL and M. Amin, PRD 97 023533 (2017)

KL and M. Amin, PRL 119 061301 (2016)

What is w after inflation?

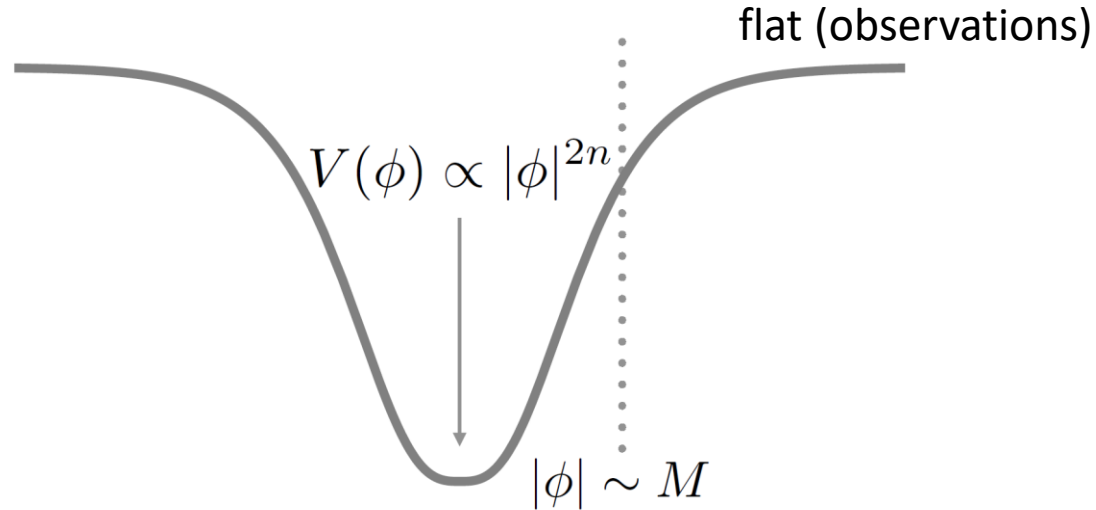
$$w = \frac{\text{pressure}}{\text{energy density}}$$

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) \right]$$

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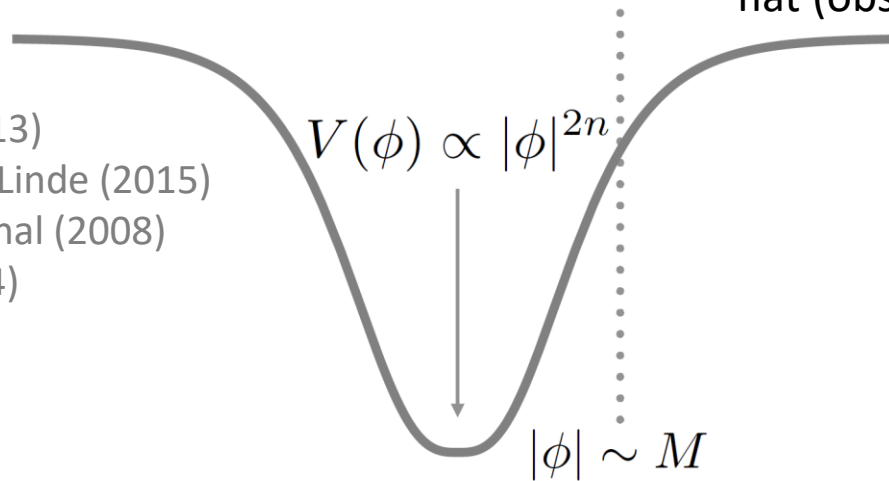
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flat (observations)

$$V(\phi) \propto |\phi|^{2n}$$

$$|\phi| \sim M$$

Kallosch and Linde (2013)
Carrasco, Kallosch and Linde (2015)
Silverstein and Westphal (2008)
McAllister, et al. (2014)

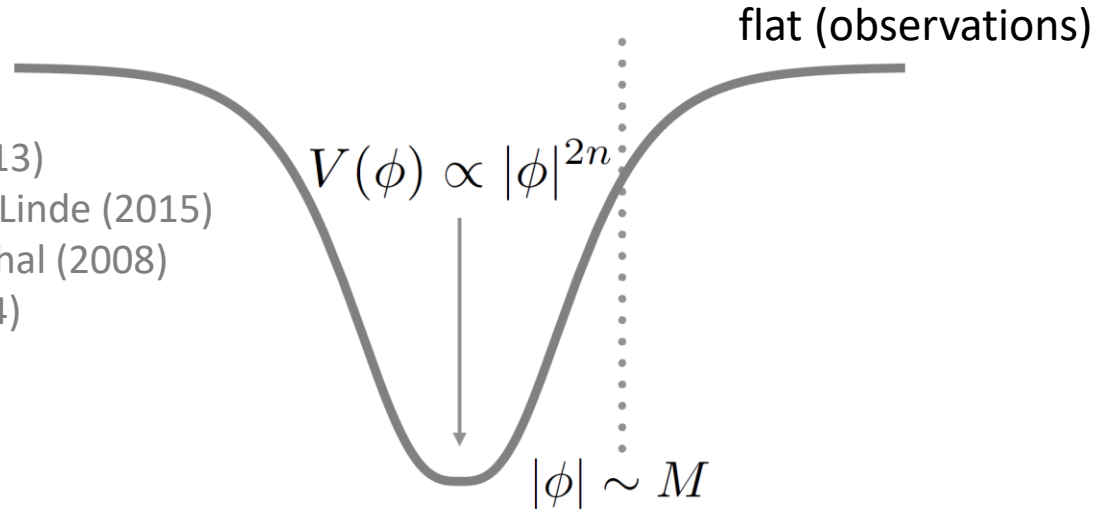


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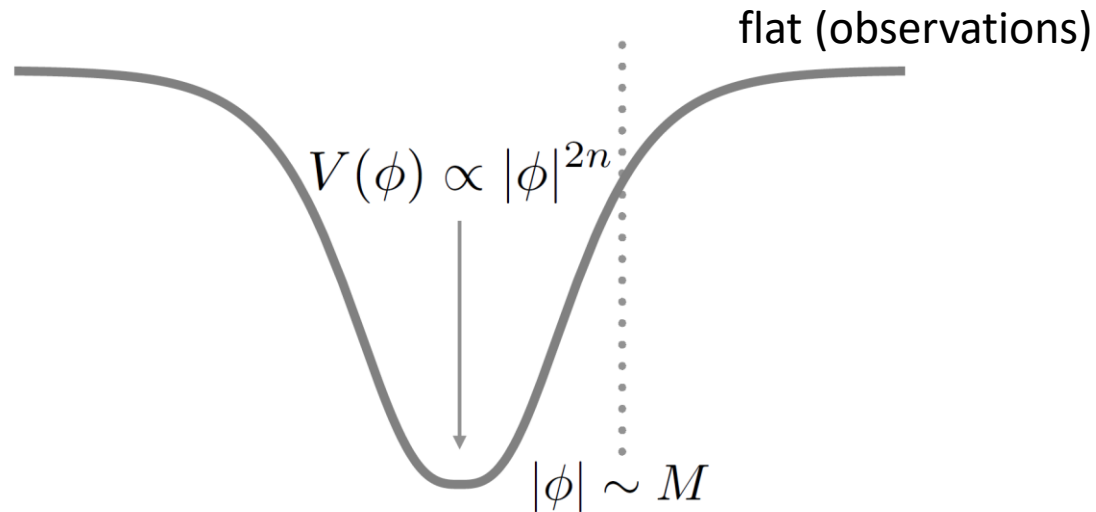
assumption: self-couplings dominate over others

What is w after inflation?

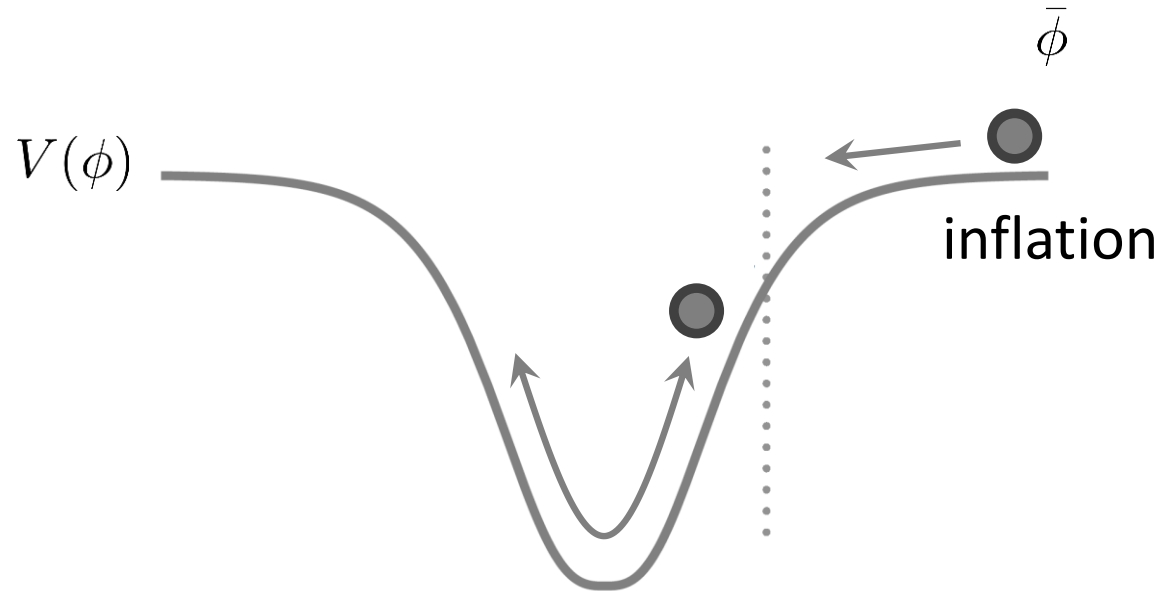
at sufficiently late times:

$$w = \begin{cases} 0 & \text{if } n = 1 \\ 1/3 & \text{if } n > 1 \end{cases}$$

(even without couplings to other fields!)

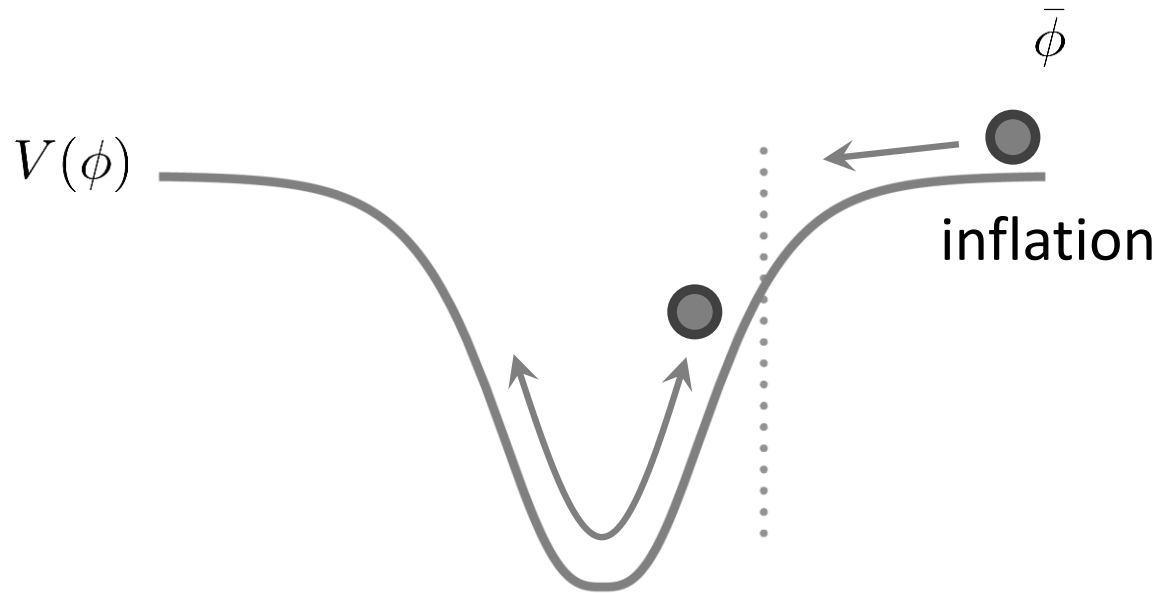


Inflaton dynamics



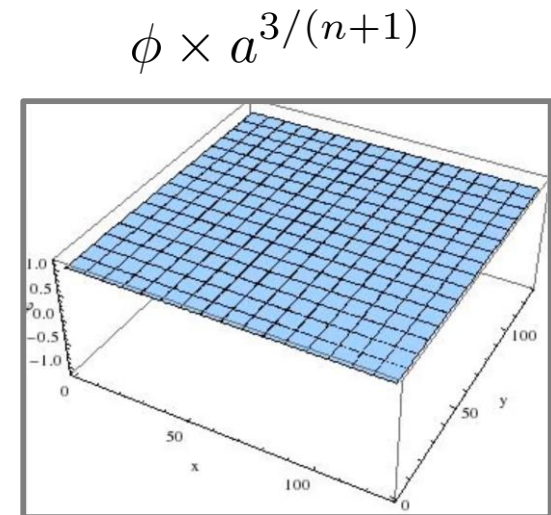
inflation ends:
oscillatory phase

Inflaton (homogeneous) dynamics

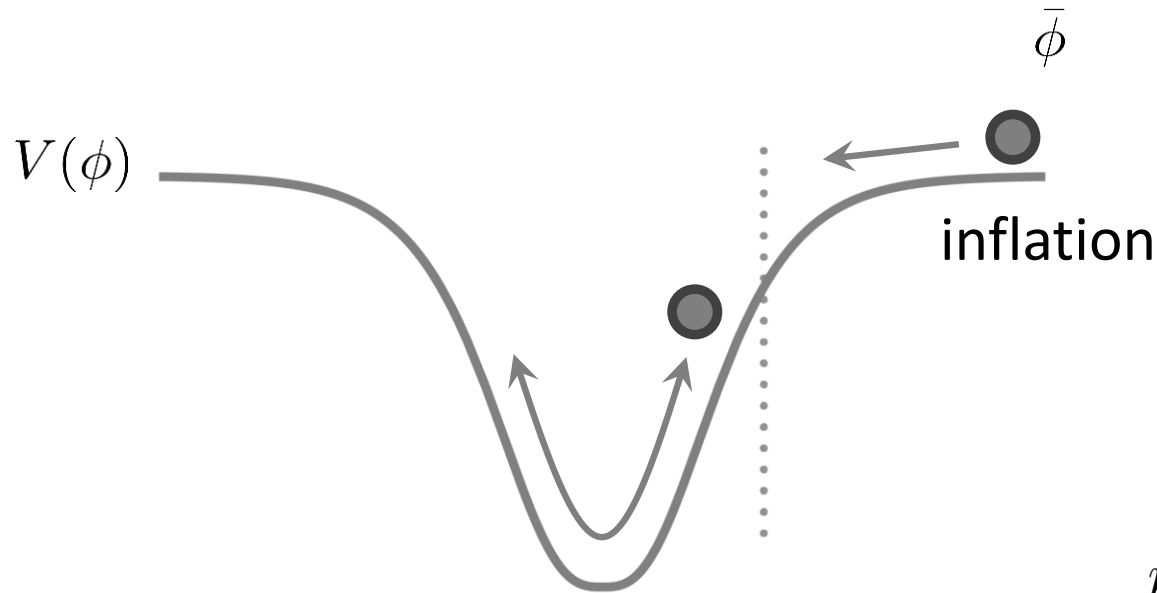


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$$\bar{\phi}(t) \propto a(t)^{-3/(n+1)}$$



Inflaton (homogeneous) dynamics

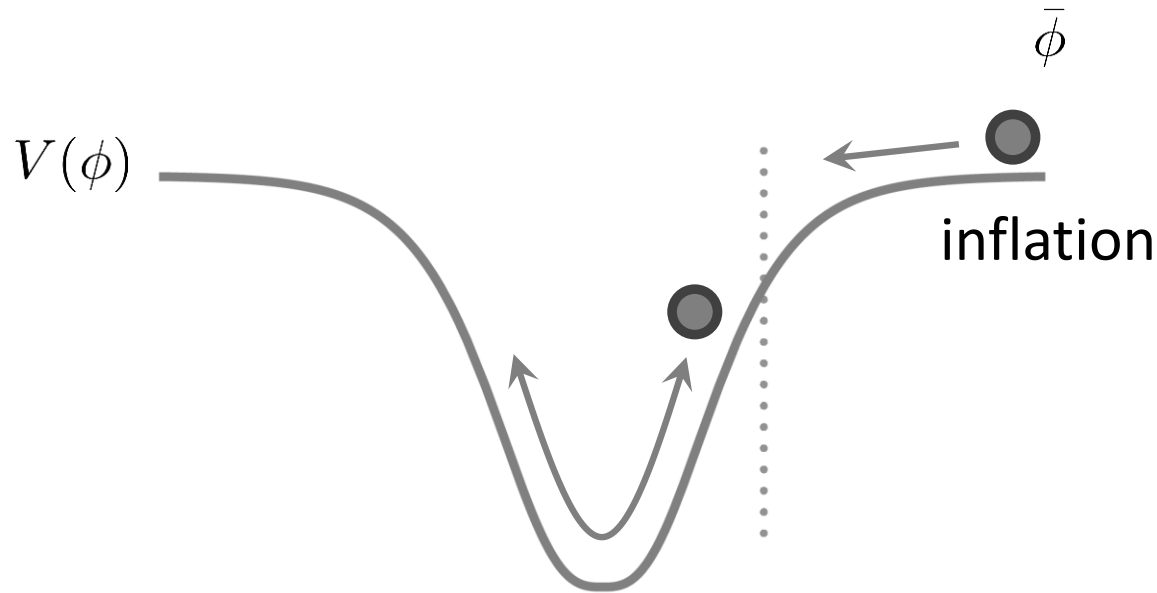


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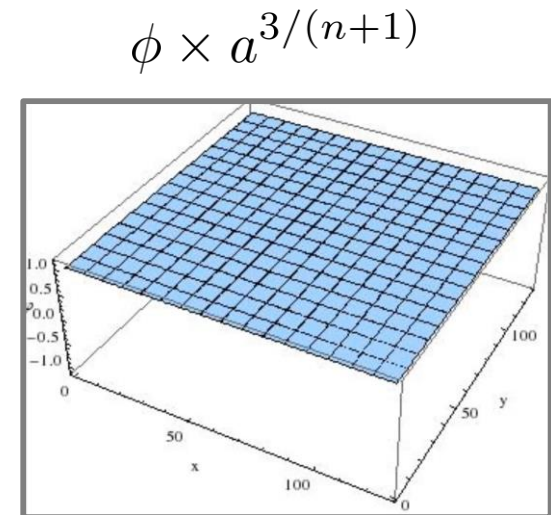
$$w \equiv \frac{p}{\rho} = \frac{\dot{\phi}^2/2 - (\nabla\phi)^2/6 - V(\phi)}{\dot{\phi}^2/2 + (\nabla\phi)^2/2 + V(\phi)}$$

Inflaton (homogeneous) dynamics



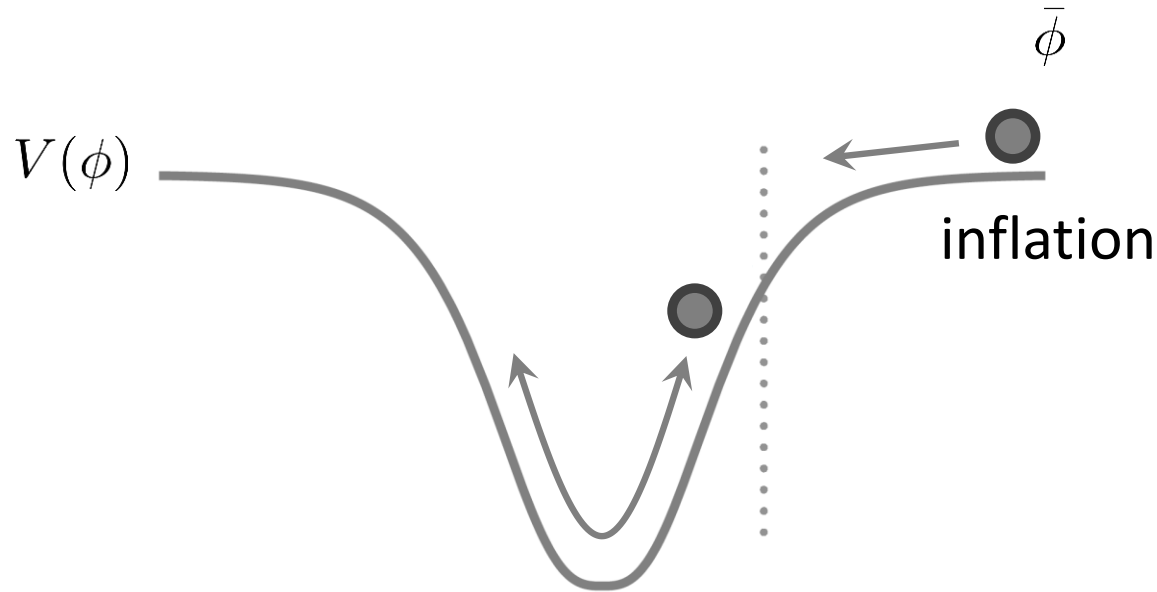
inflation ends:
oscillatory phase

$$w_{\text{hom}} = \frac{n-1}{n+1}$$



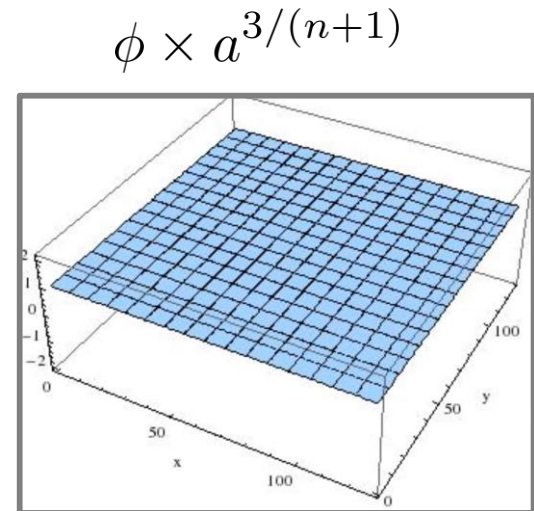
Turner (1983)

Inflaton (actual) dynamics



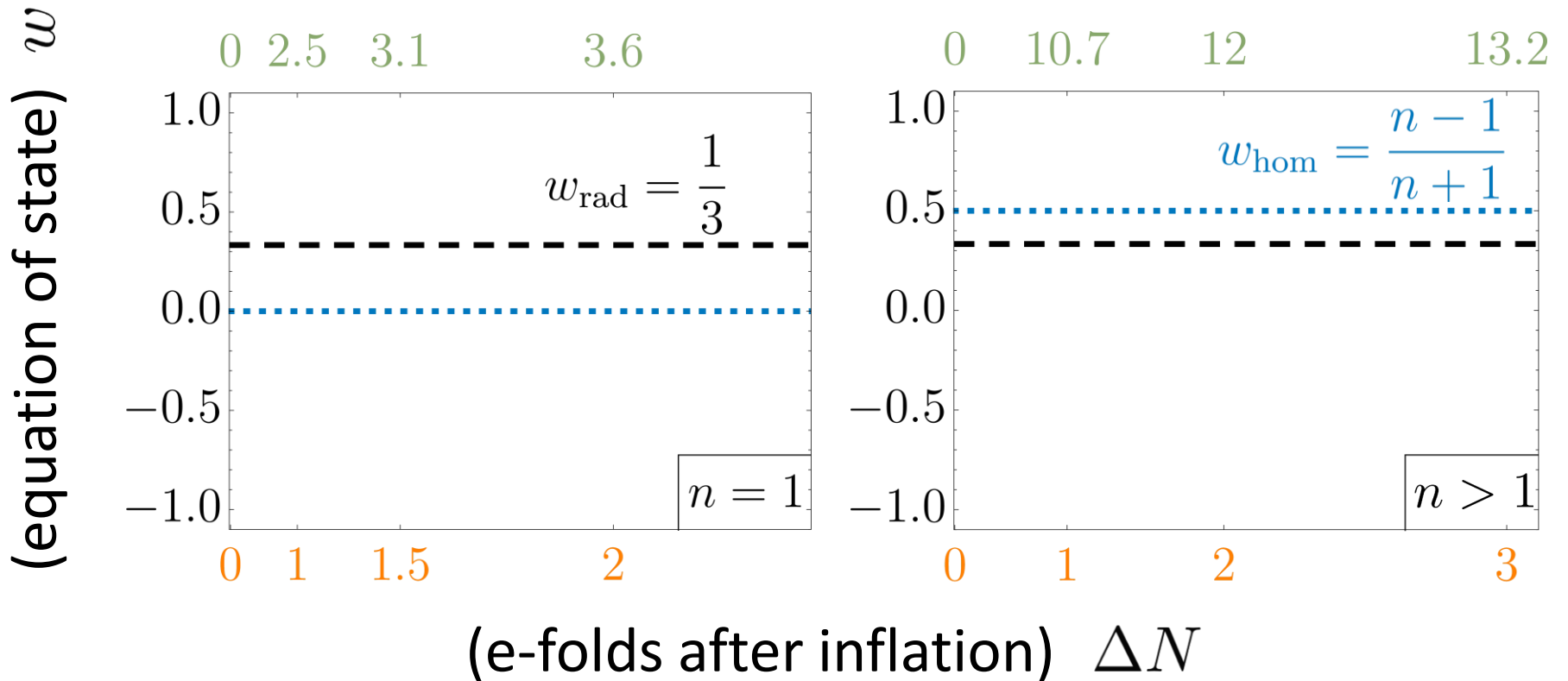
inflation ends:
oscillatory phase

- parametric resonance of $\delta\phi(t, \mathbf{x})$
- $\bar{\phi}$ fragments



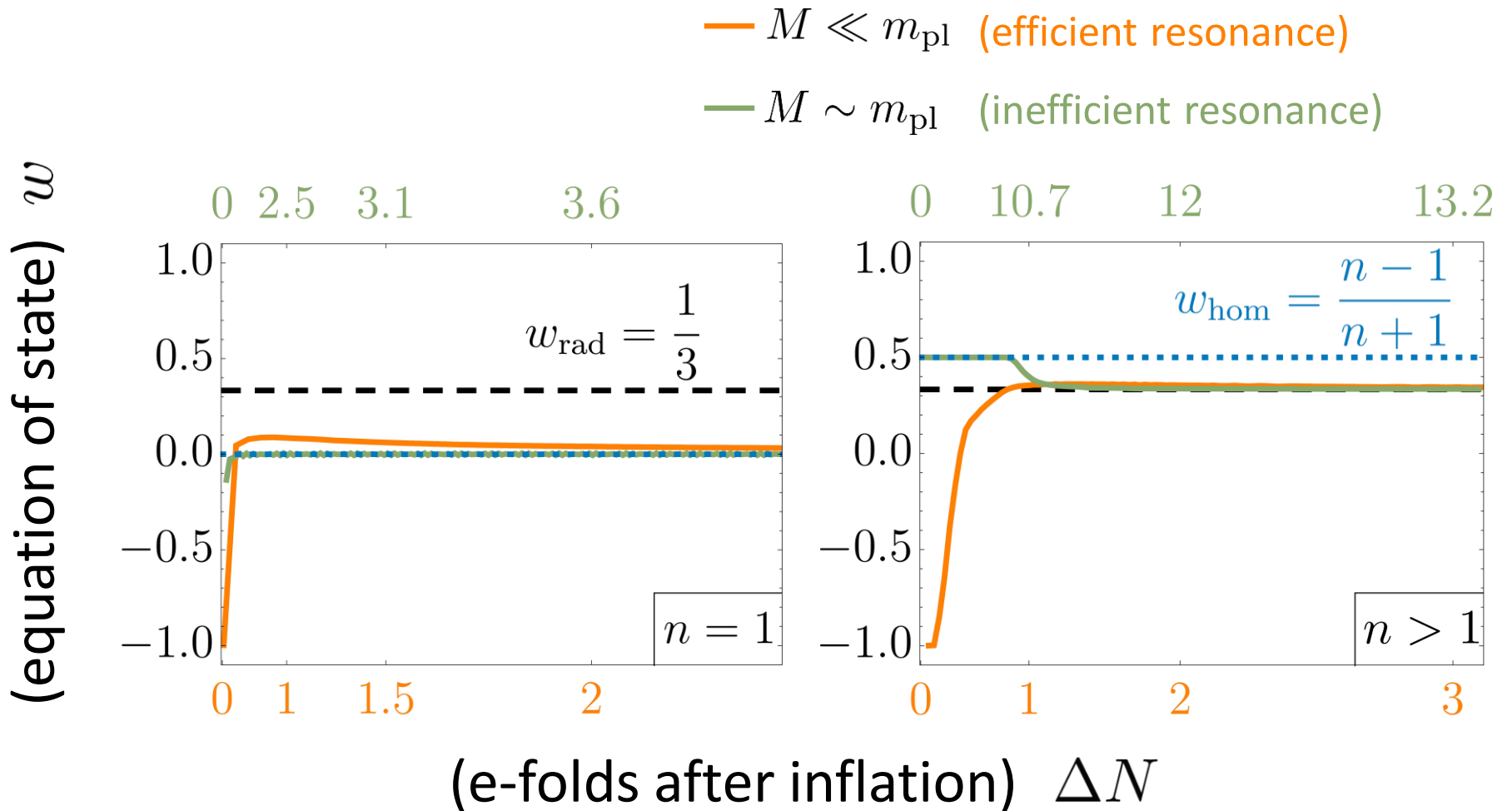
KL and M. Amin (2016)
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Equation of state



$$\Delta N \equiv \int_{a_{\text{end}}}^a d \ln a$$

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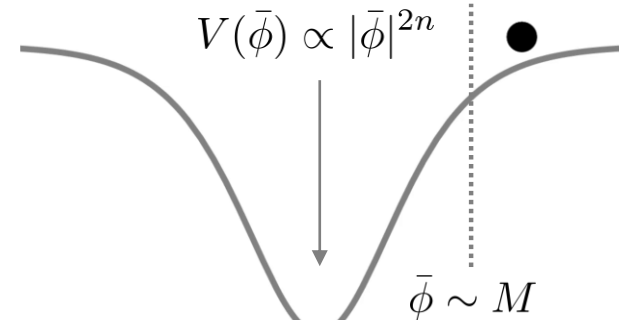
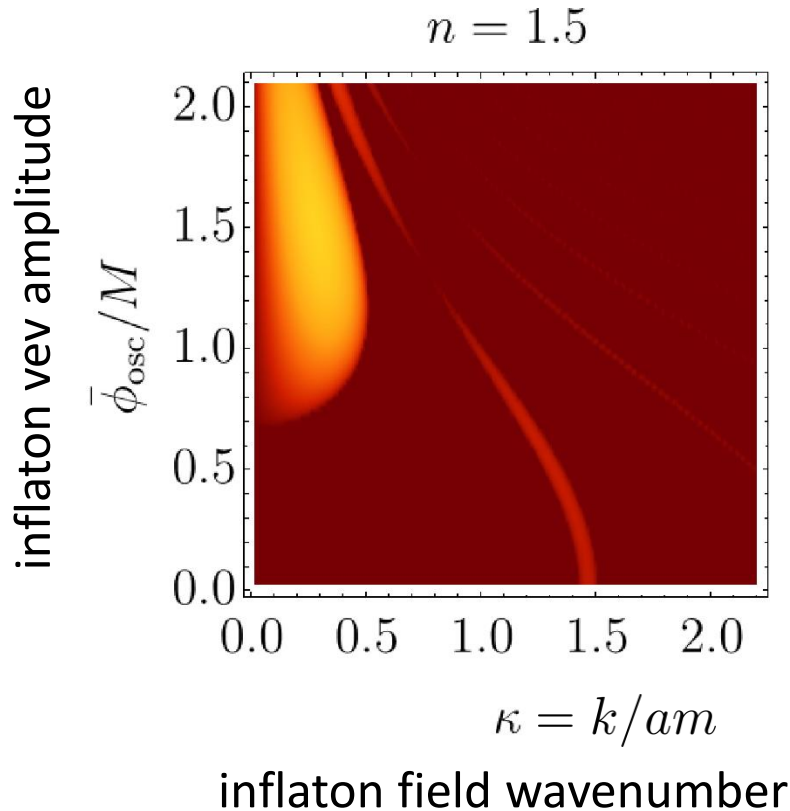
Towards radiation domination

$$n > 1$$

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Non-perturbative decay (parametric self-resonance)



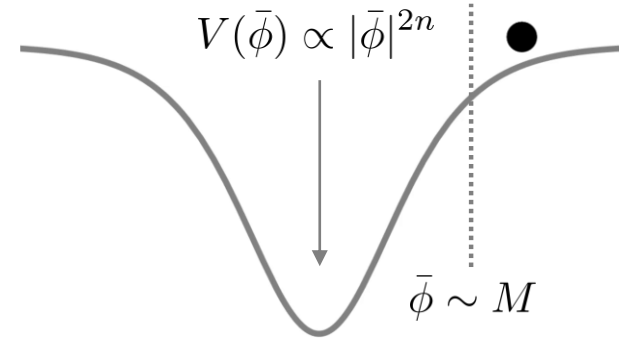
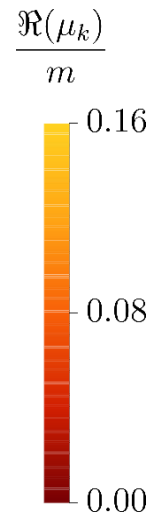
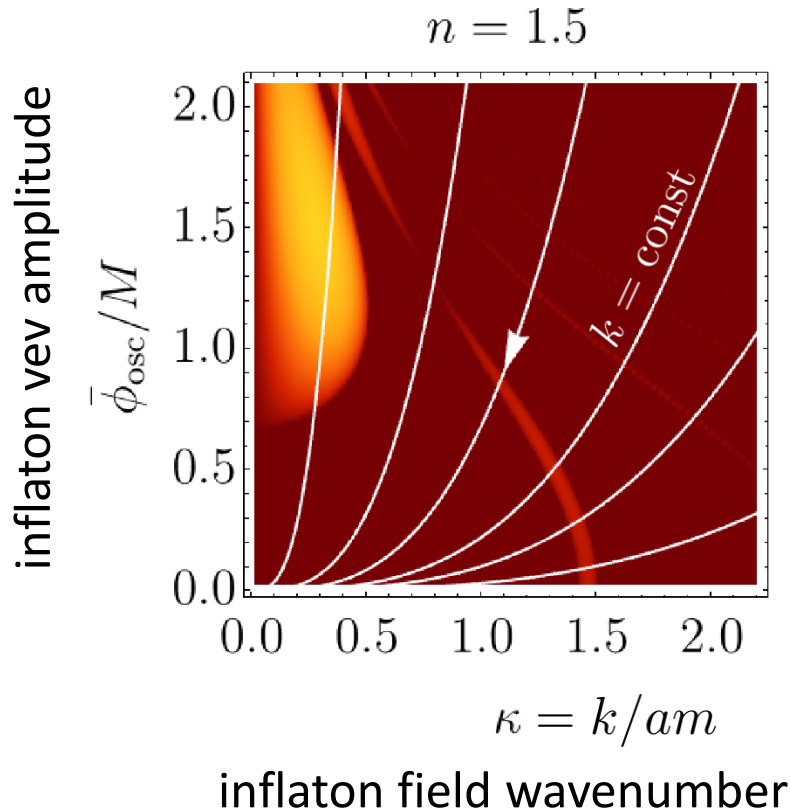
$$\delta\phi_k \propto \exp(\pm\mu_k t)$$

$$m^2 \equiv V'(\bar{\phi}_{\text{osc}})/\bar{\phi}_{\text{osc}}$$

Towards radiation domination

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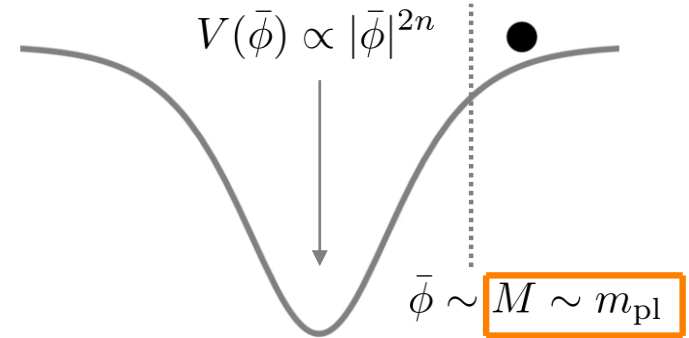
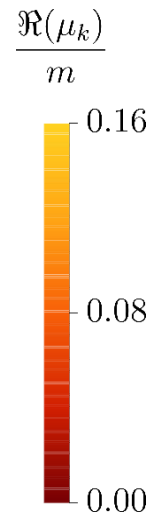
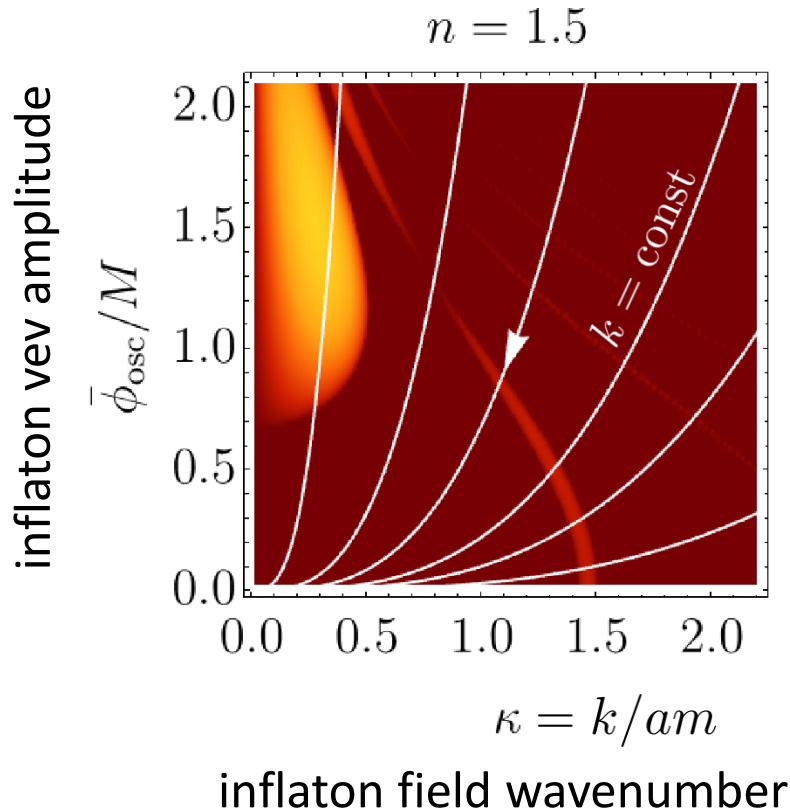
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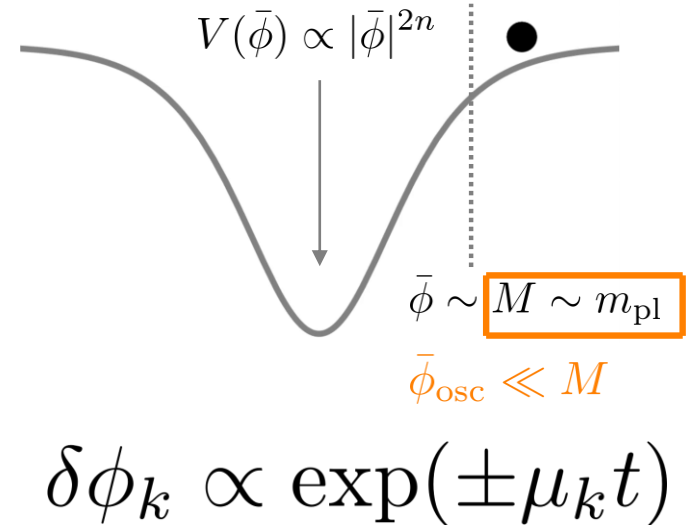
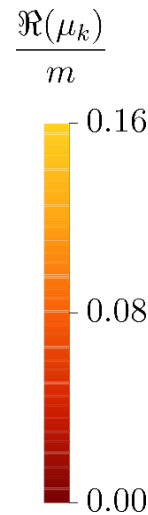
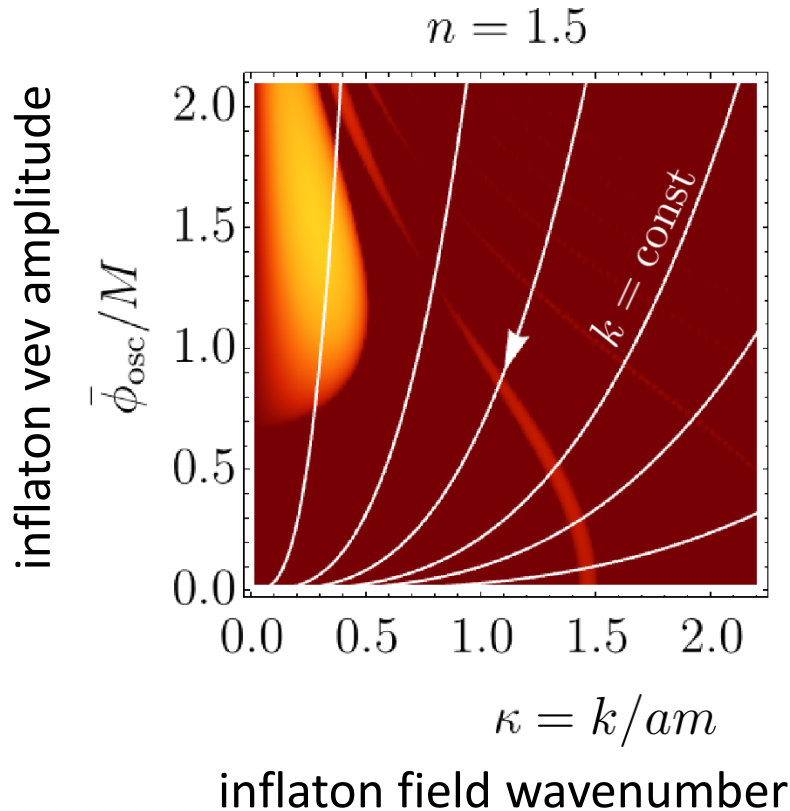
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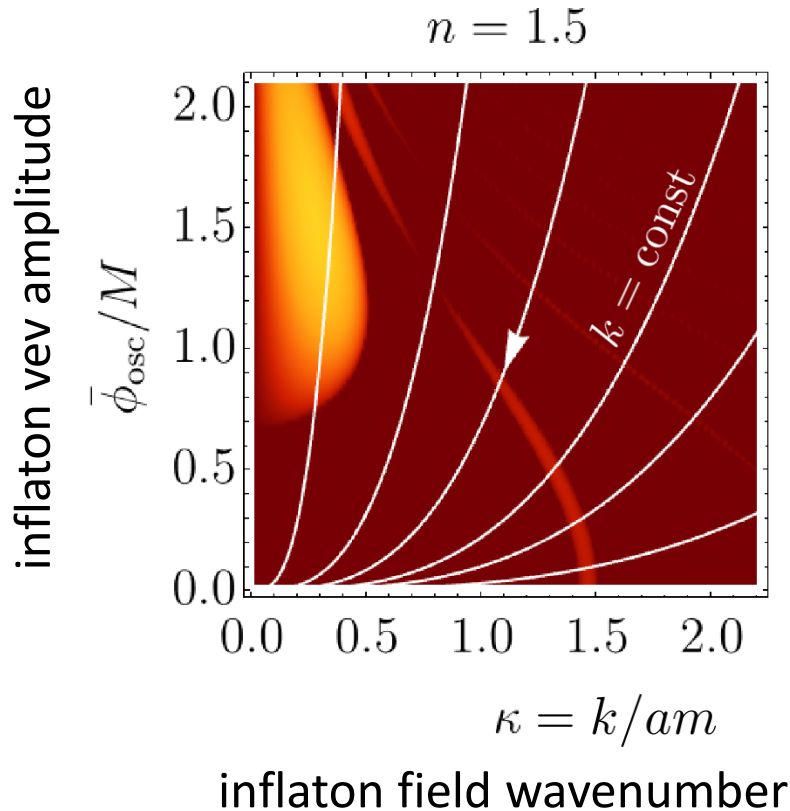


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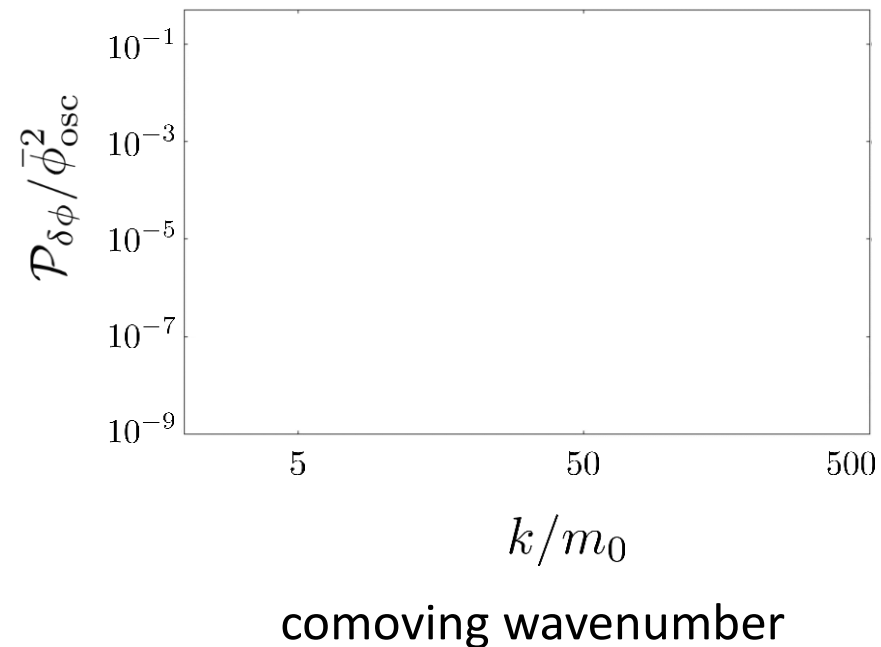
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Non-perturbative decay (parametric self-resonance)



Power spectrum:

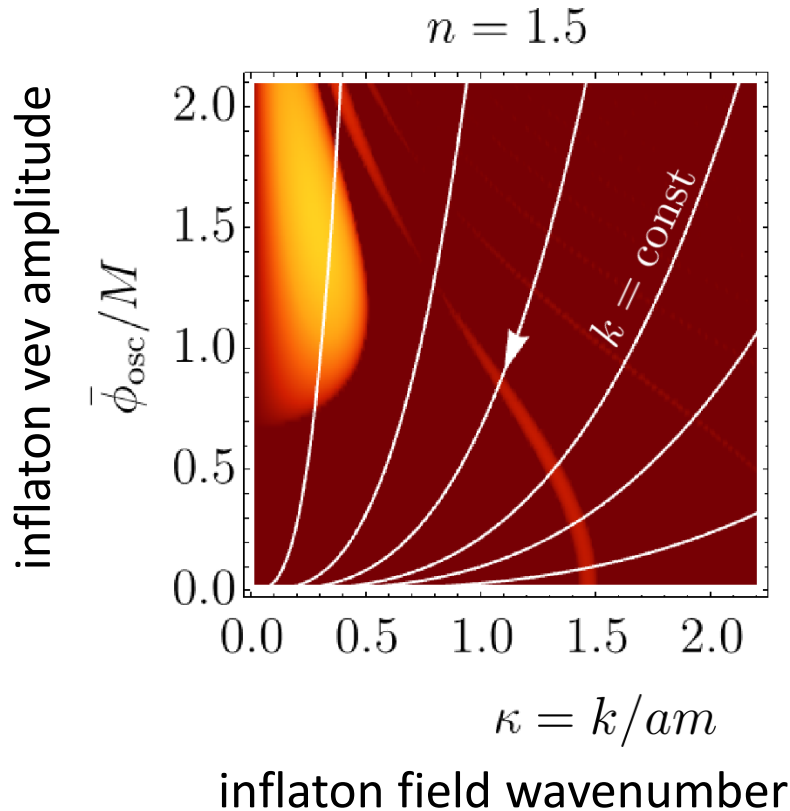
$$\langle \delta\phi(x)^2 \rangle \equiv \int \mathcal{P}_{\delta\phi} d \ln k$$



Towards radiation domination

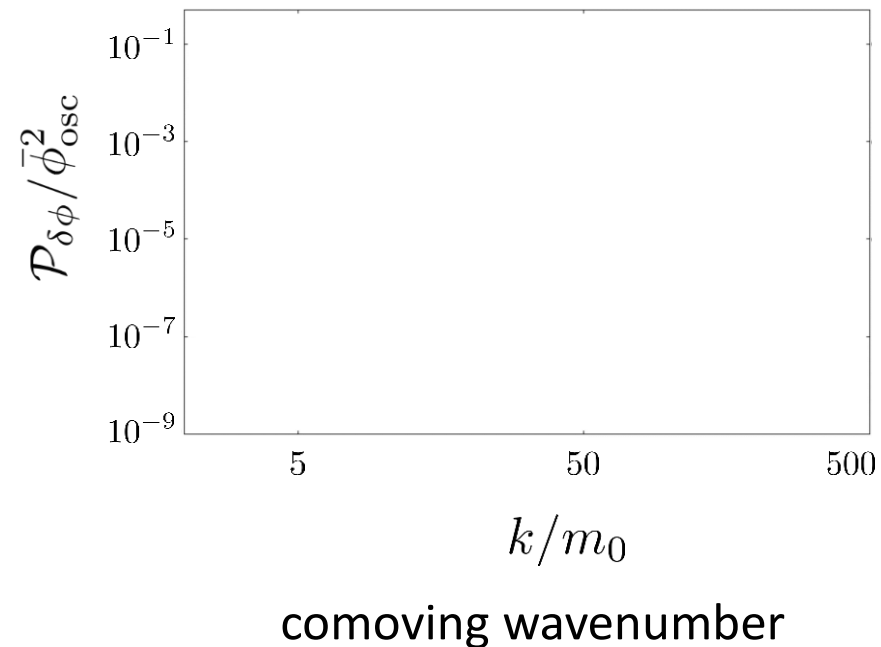
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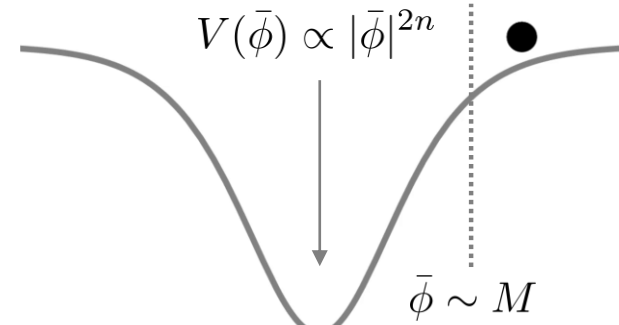
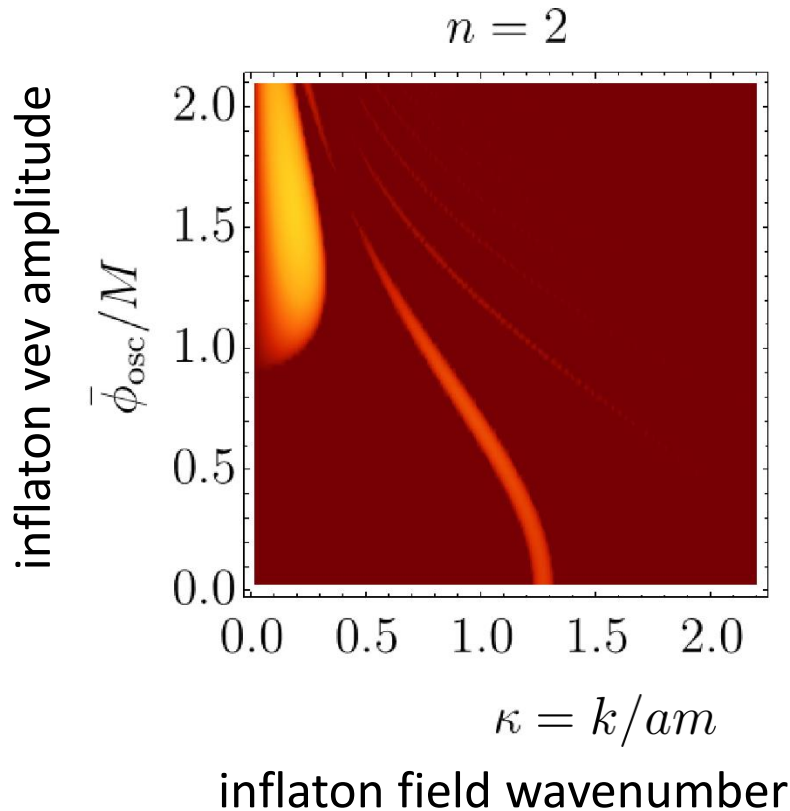
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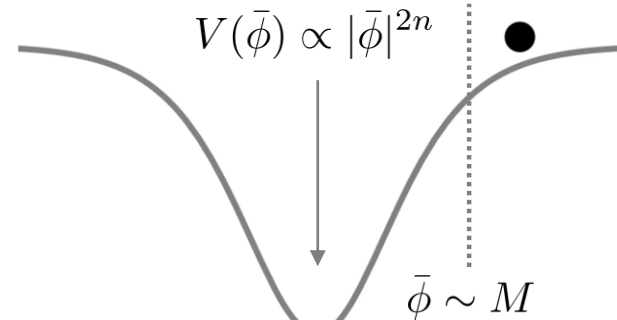
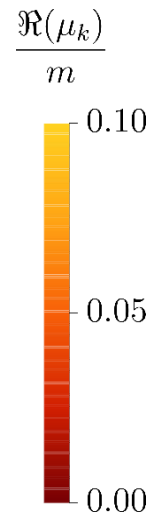
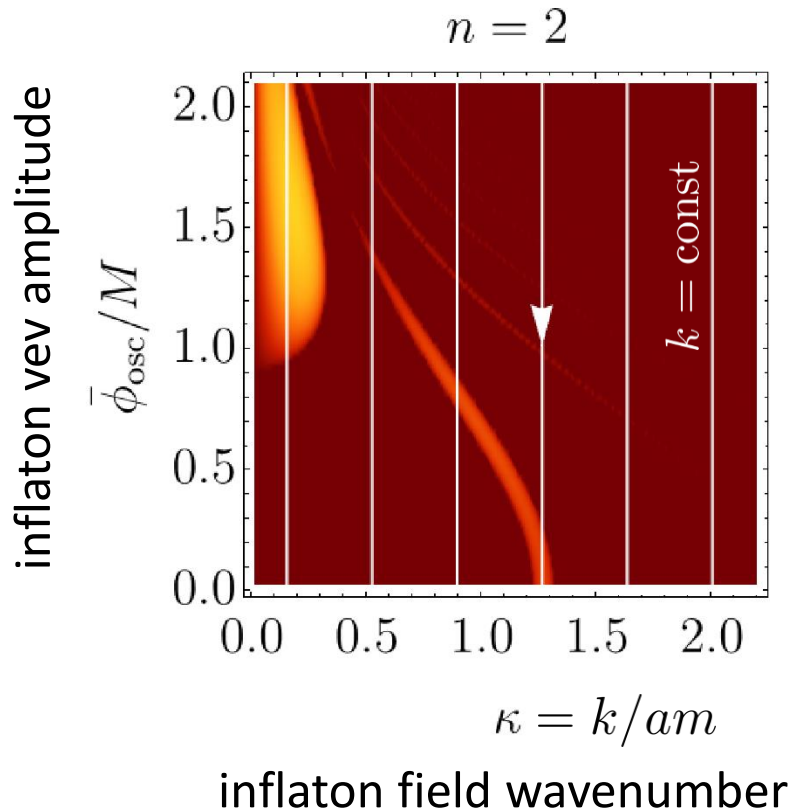
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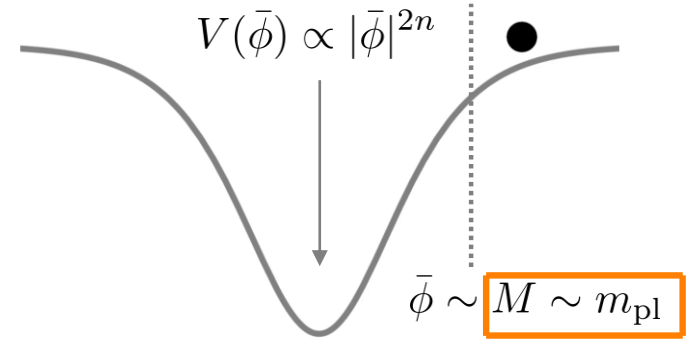
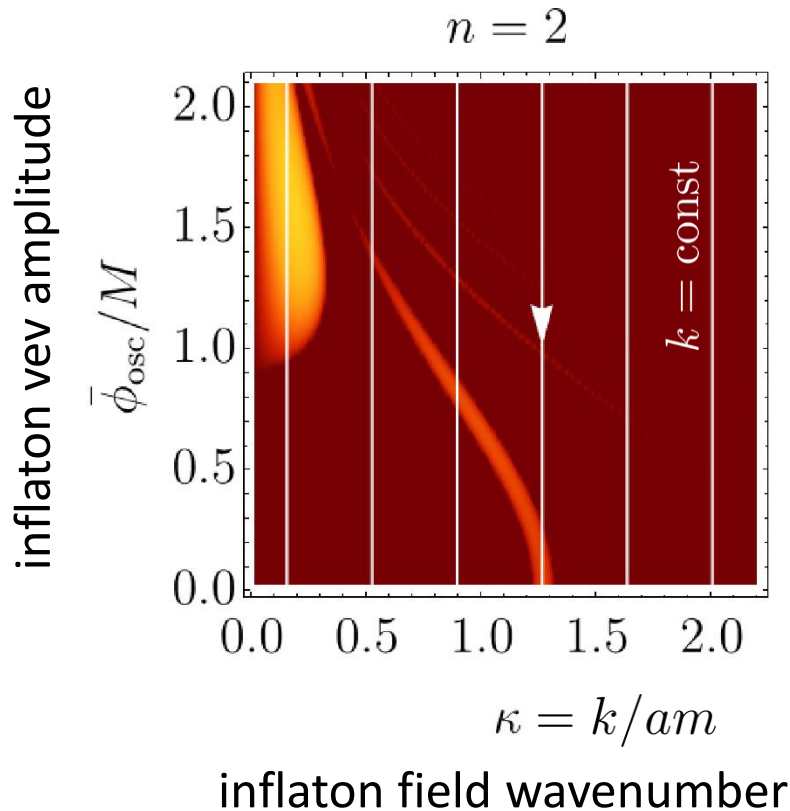
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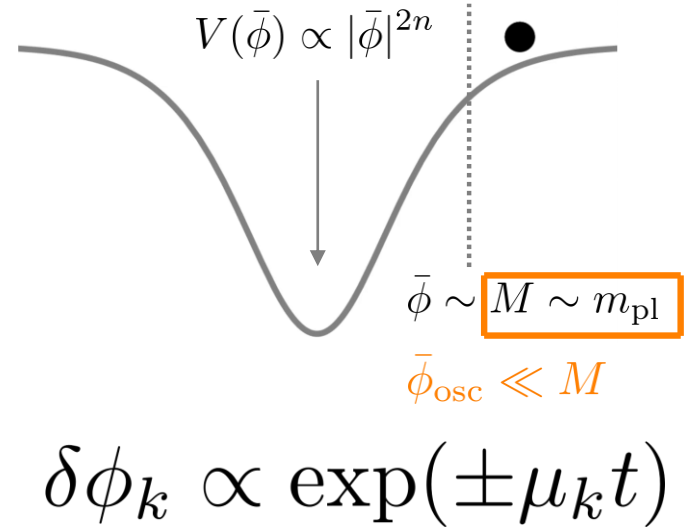
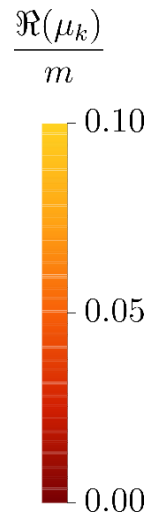
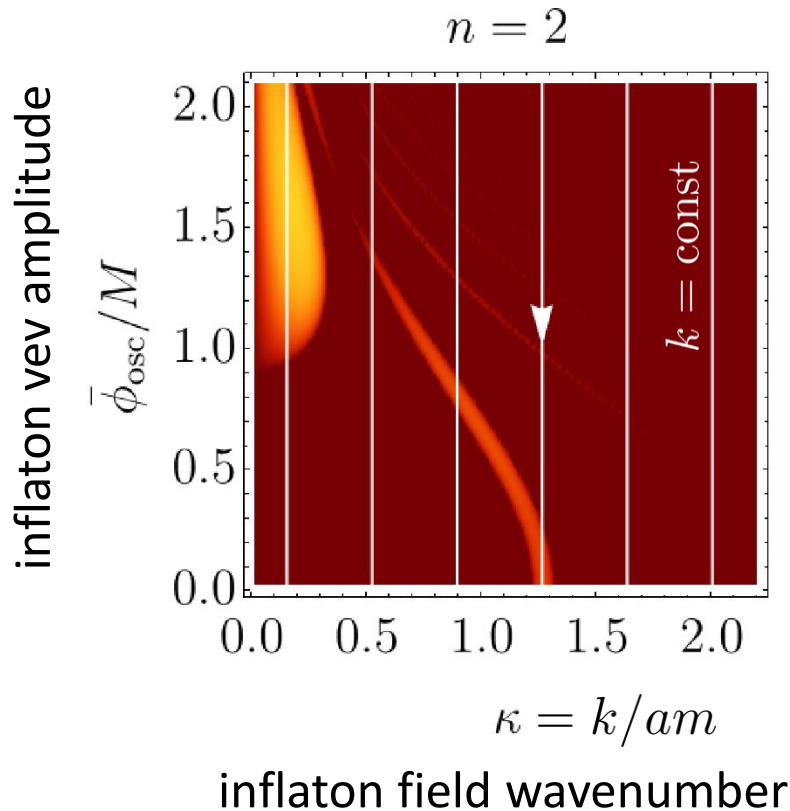
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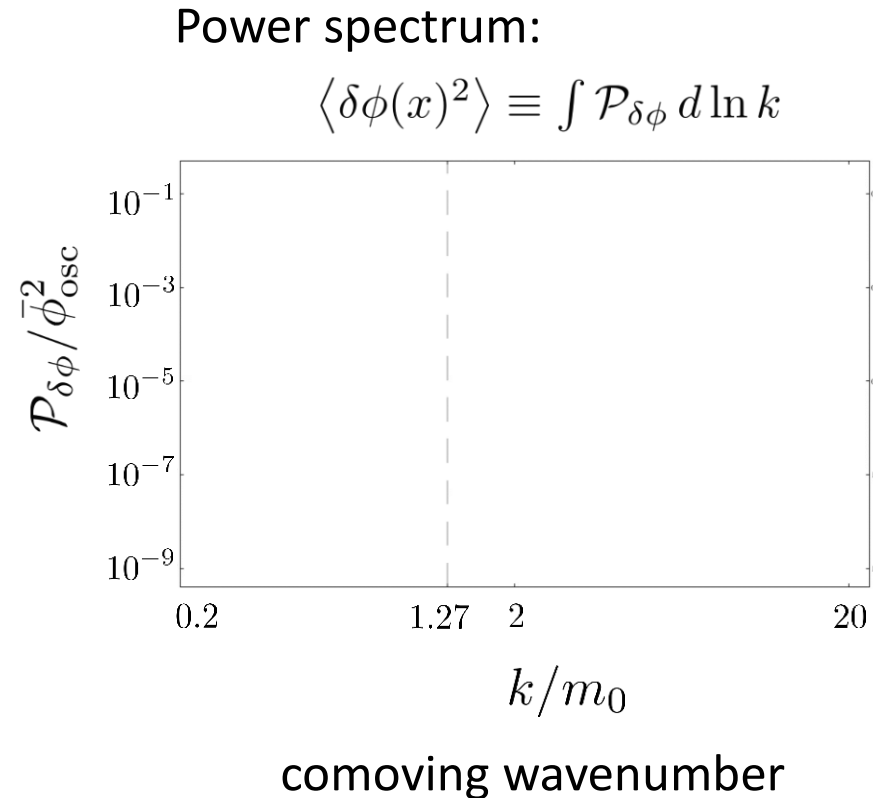
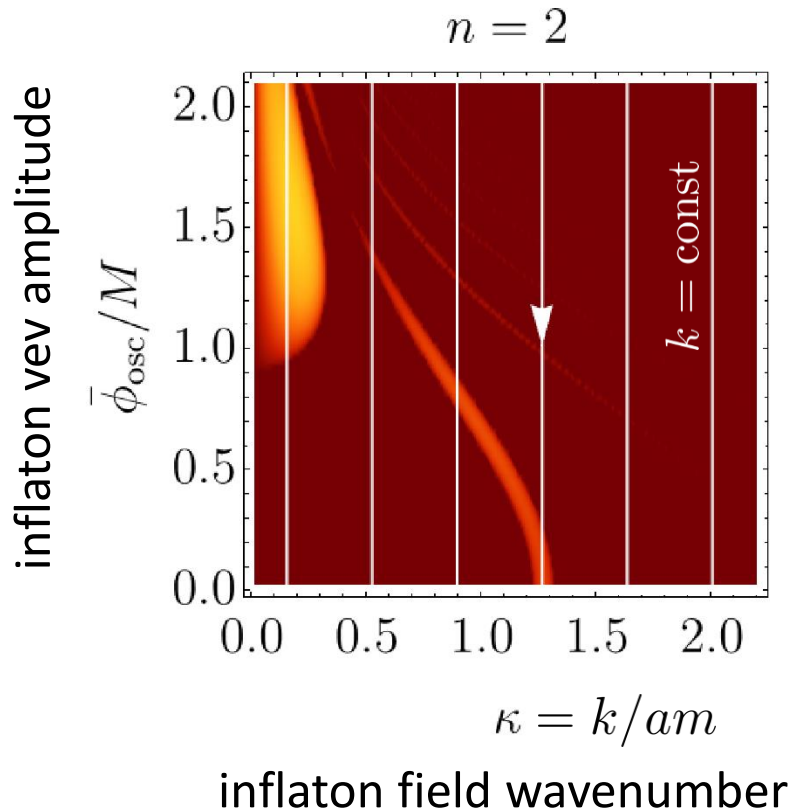


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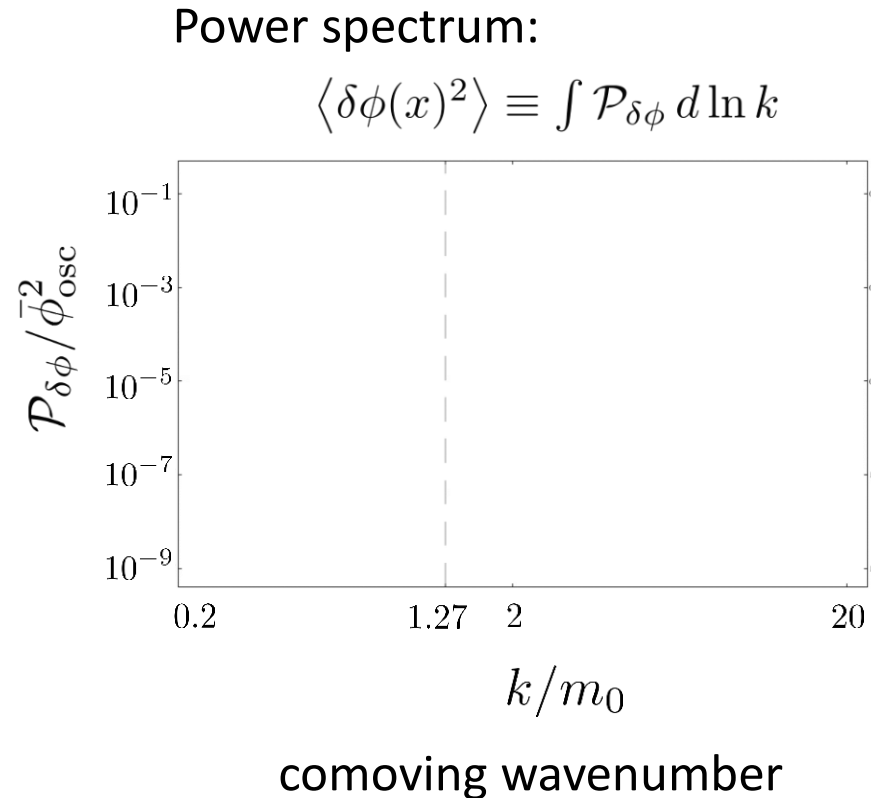
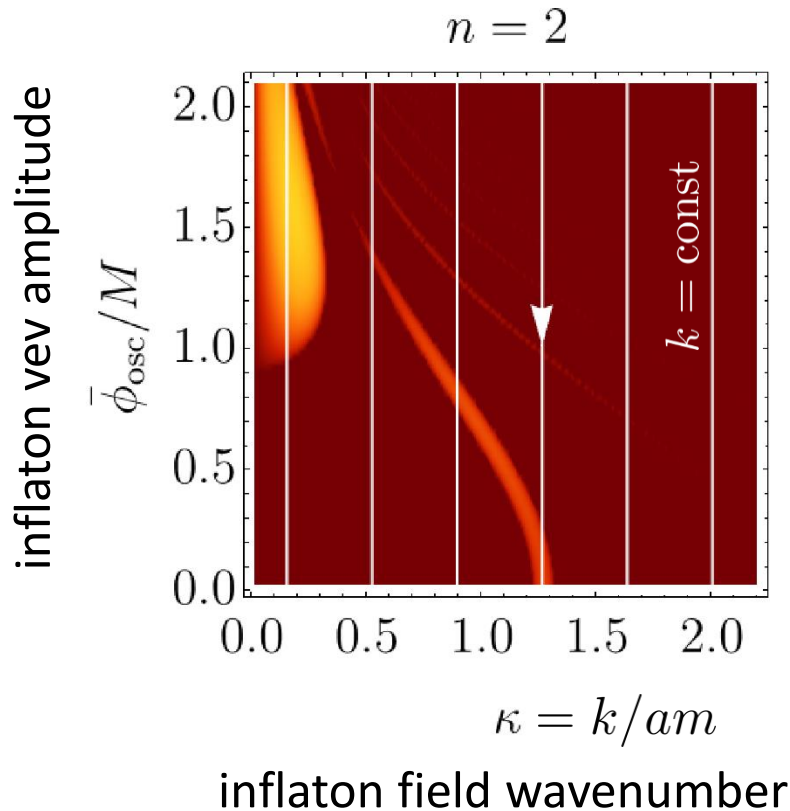
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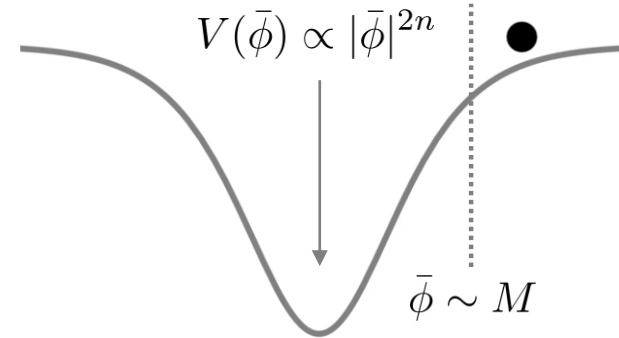
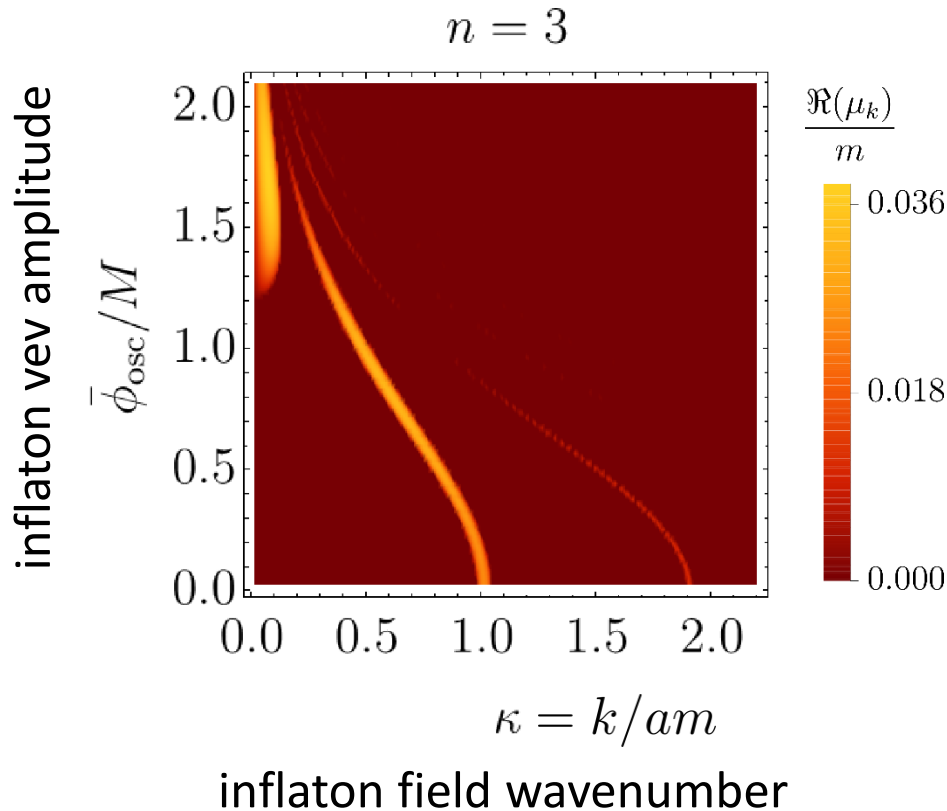
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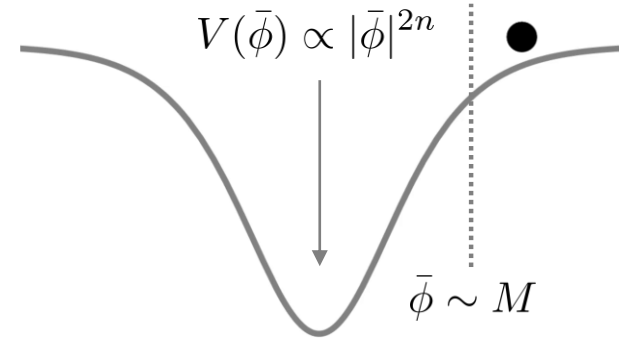
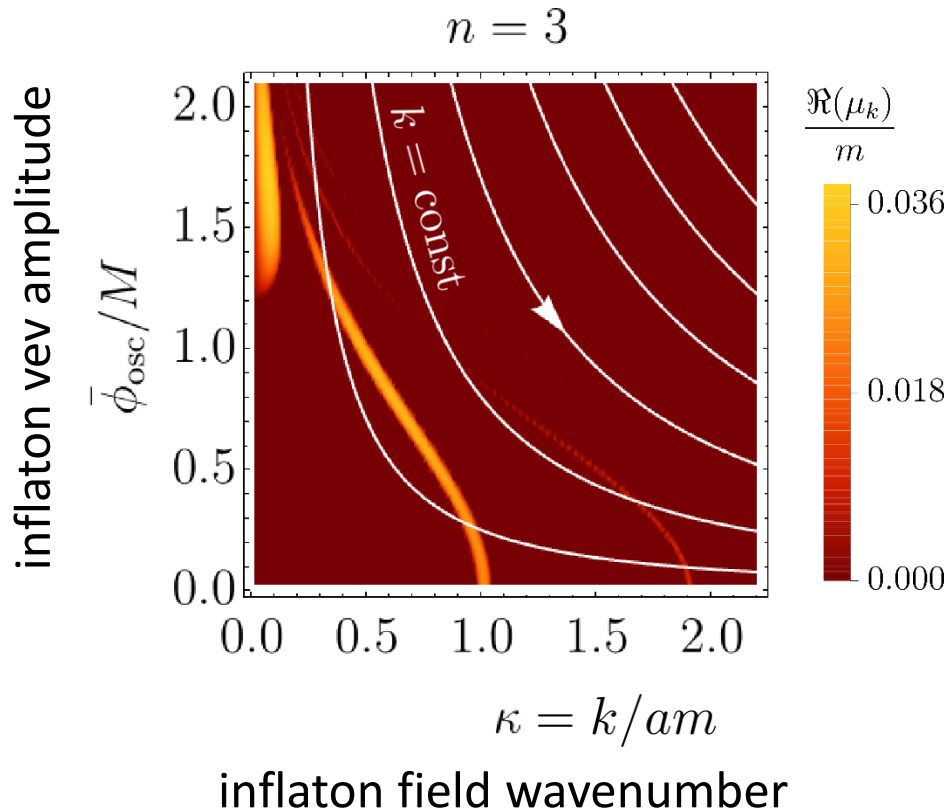
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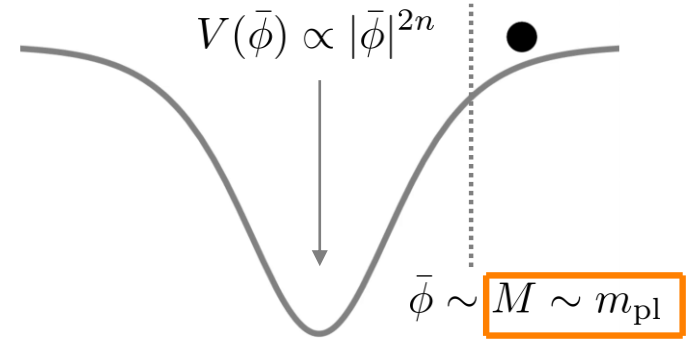
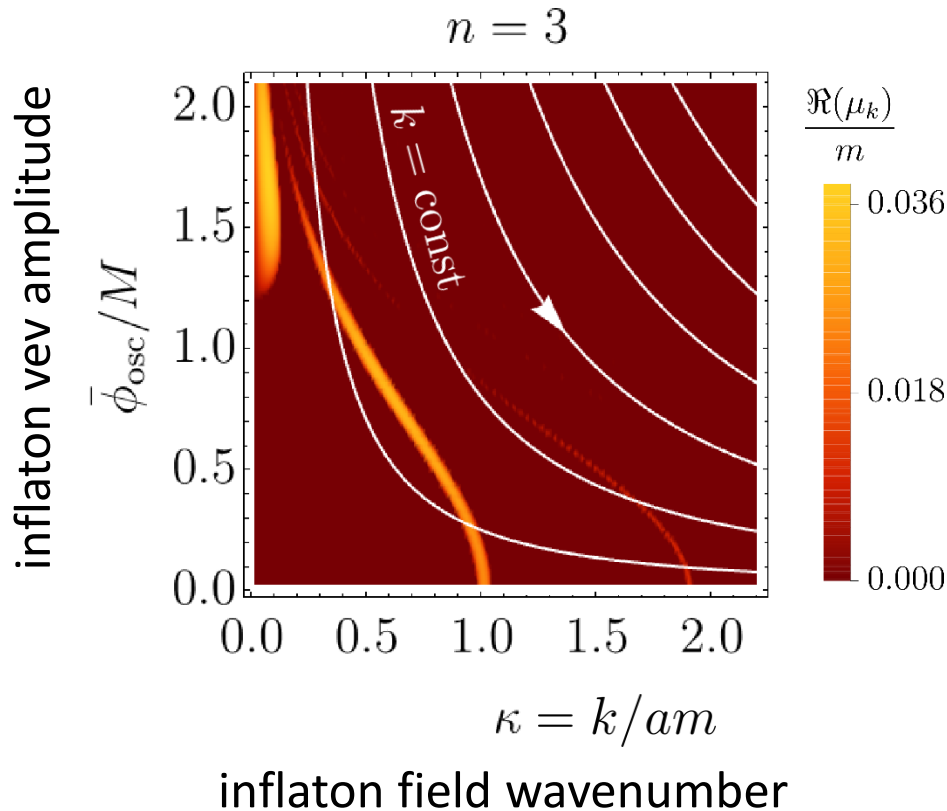
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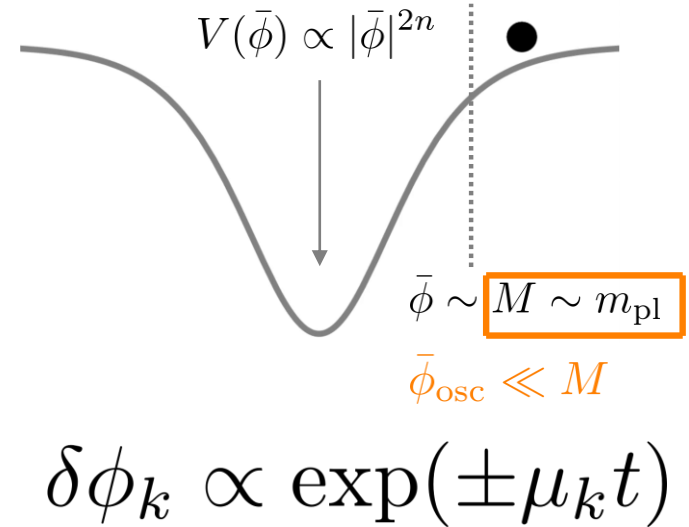
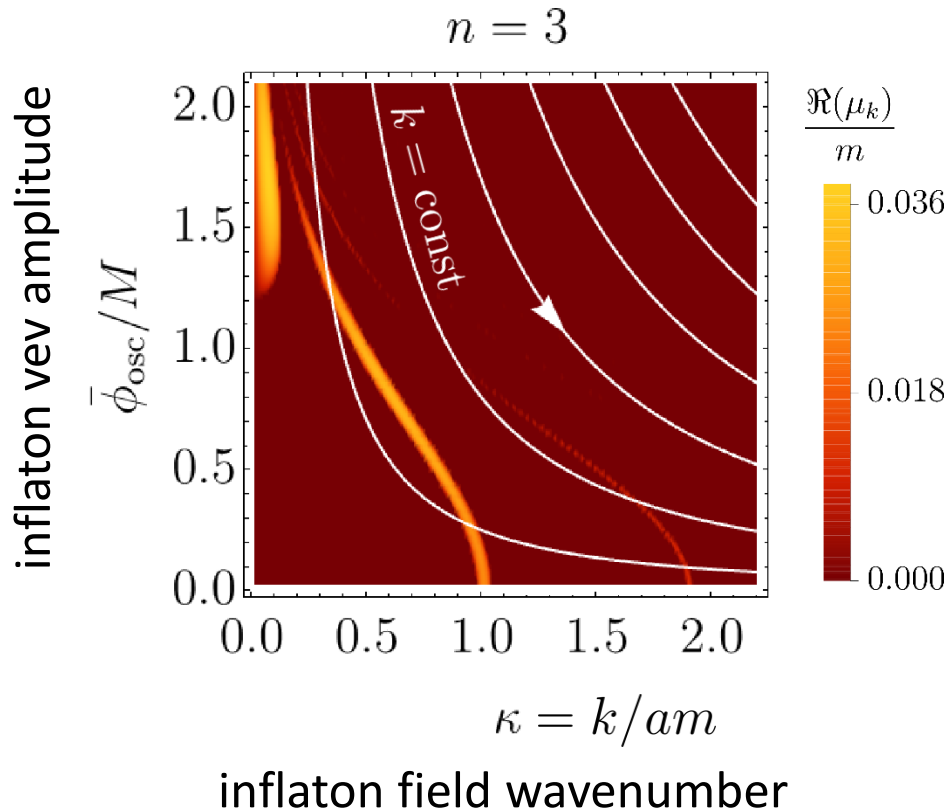
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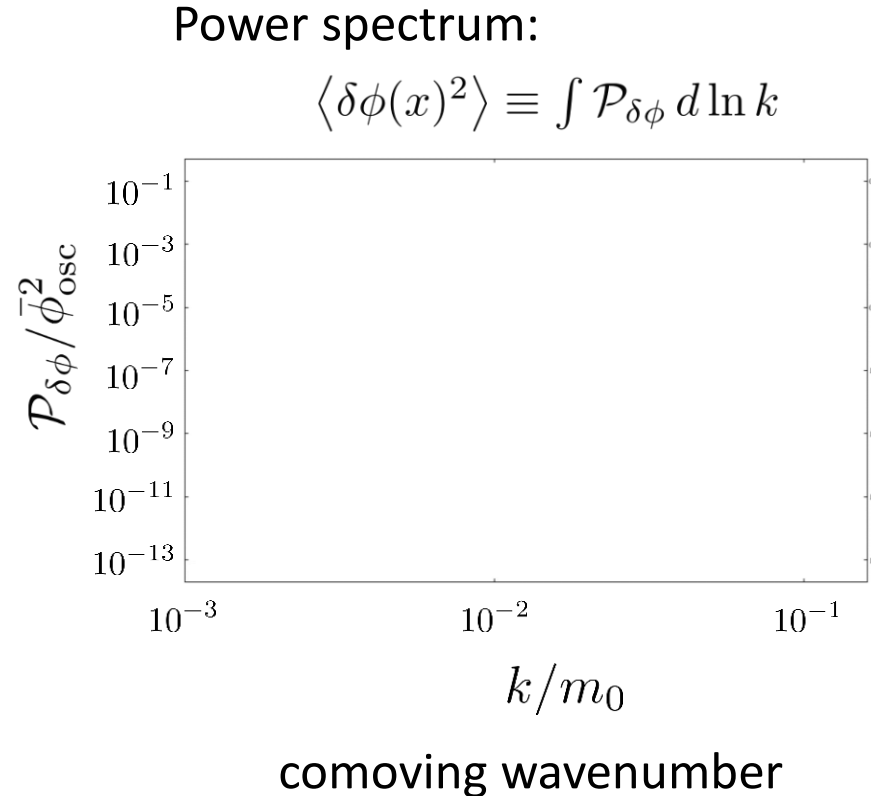
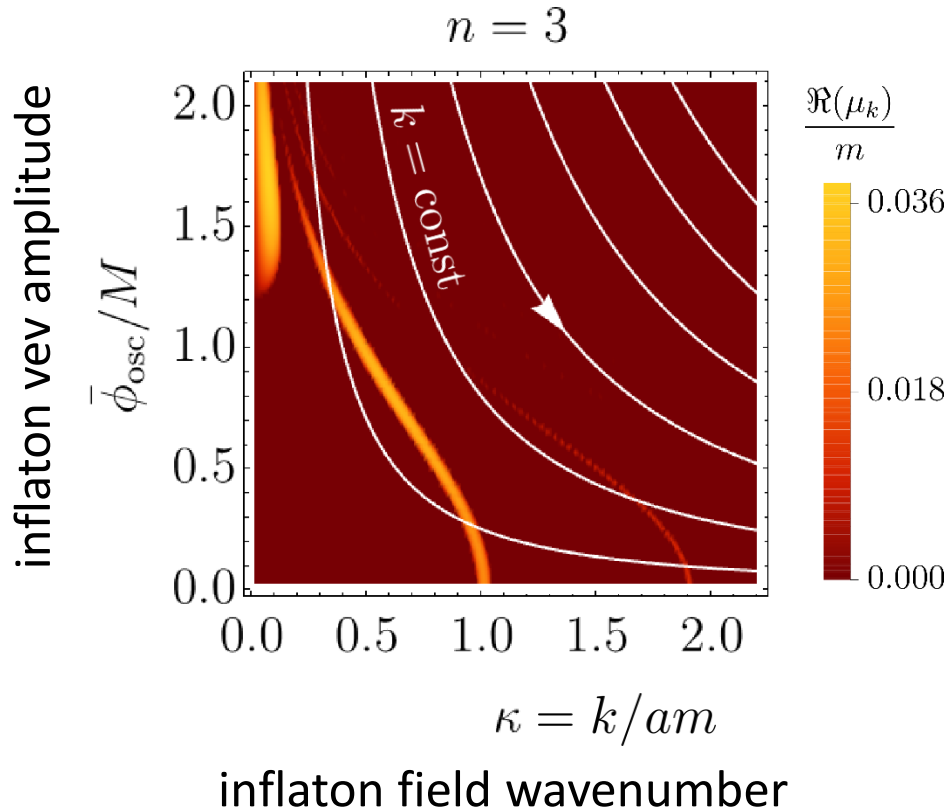


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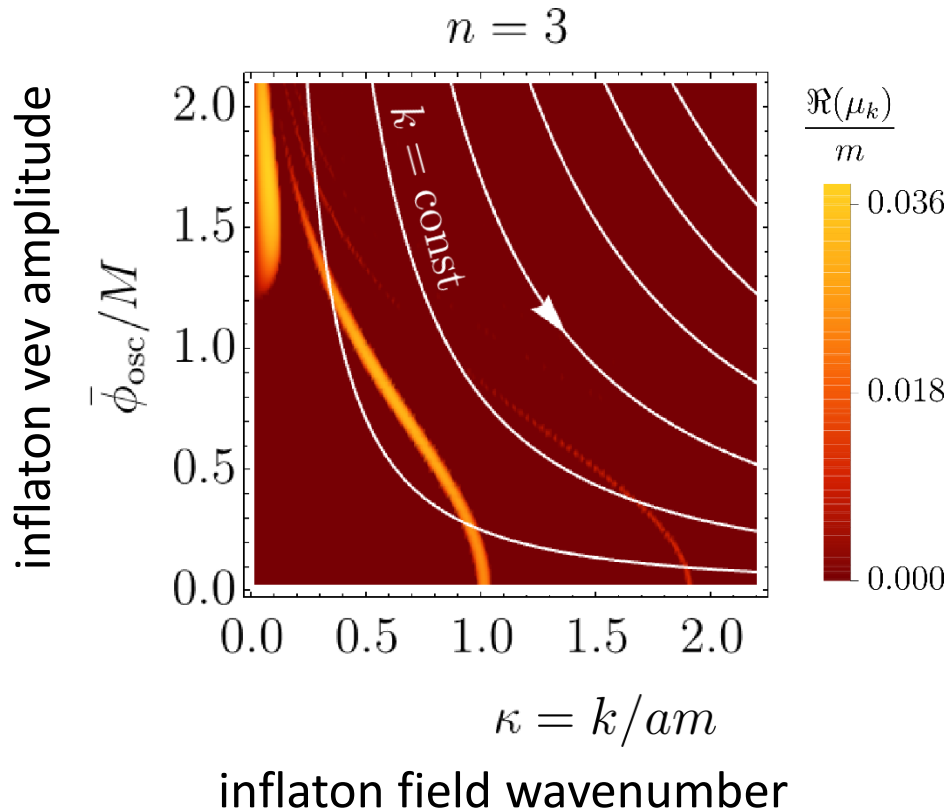
Non-perturbative decay (parametric self-resonance)



Towards radiation domination

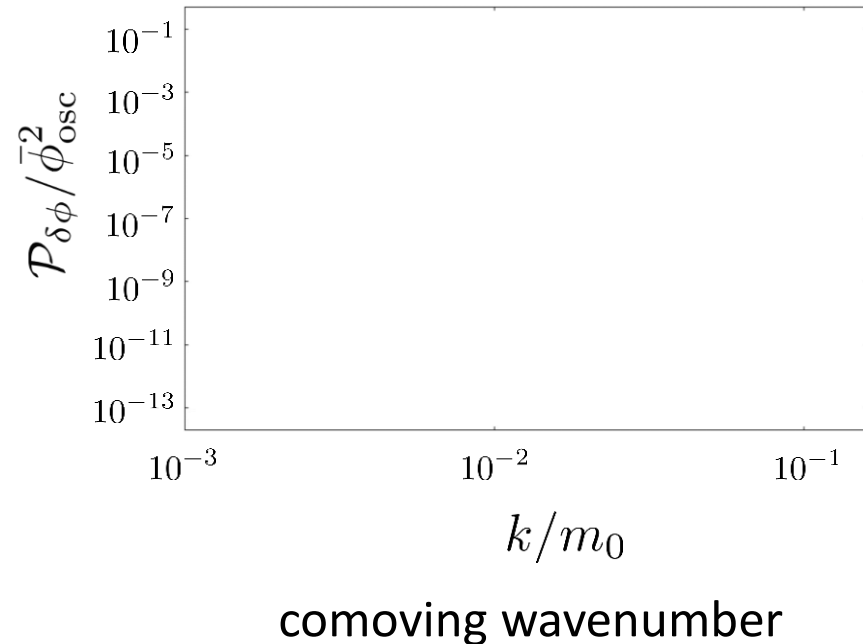
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Power spectrum:

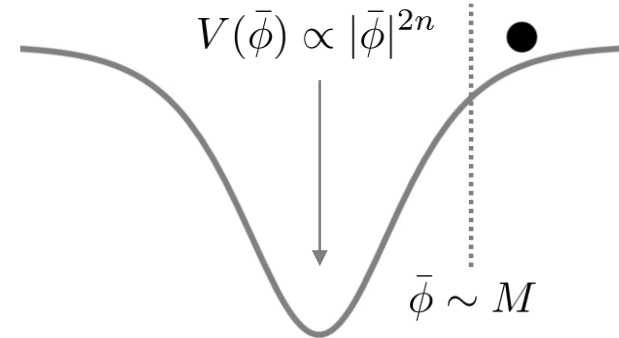
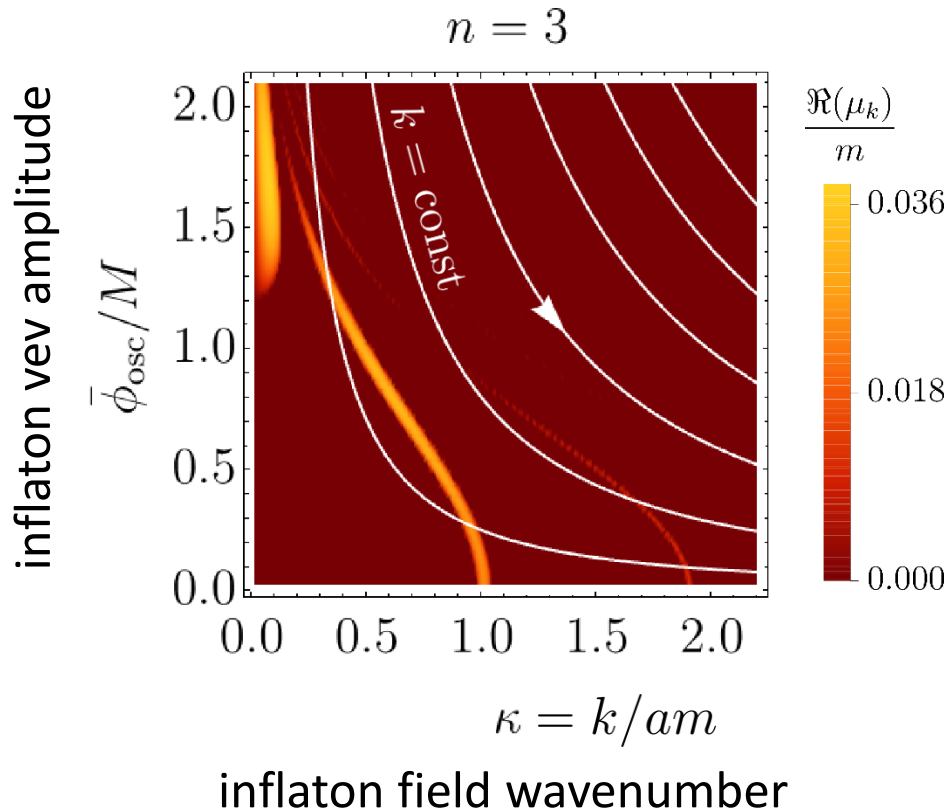
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Towards radiation domination

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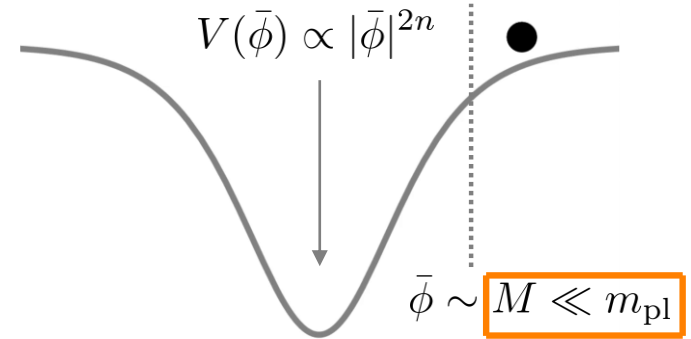
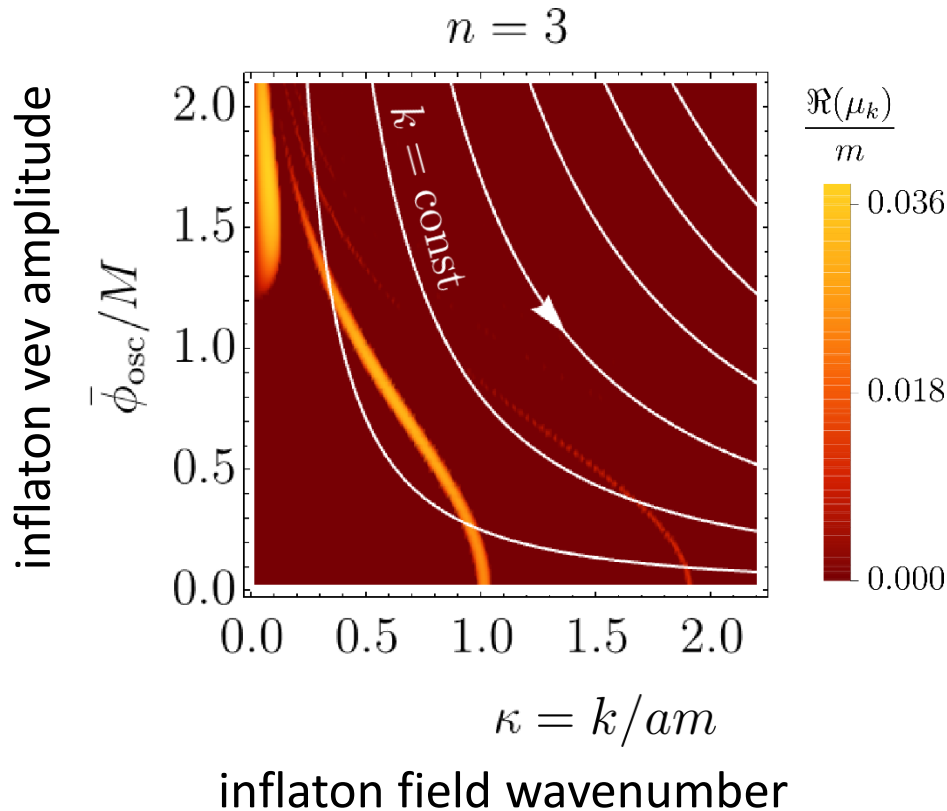
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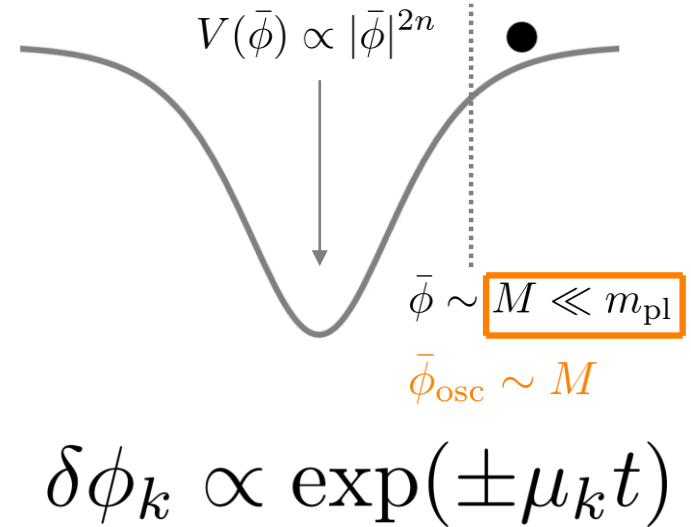
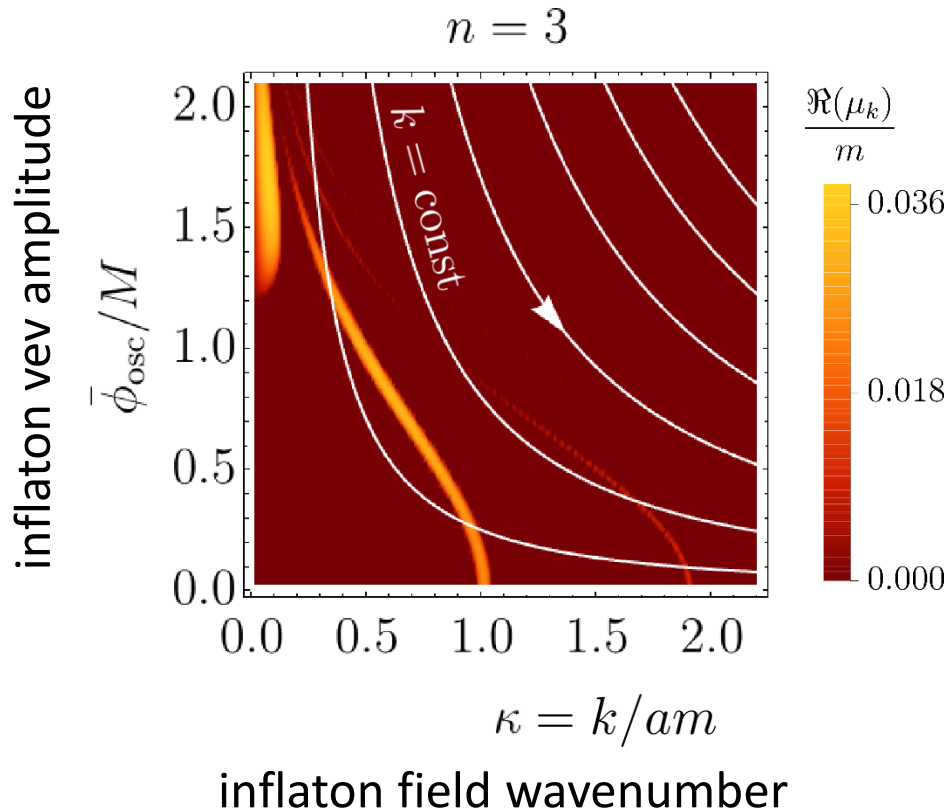
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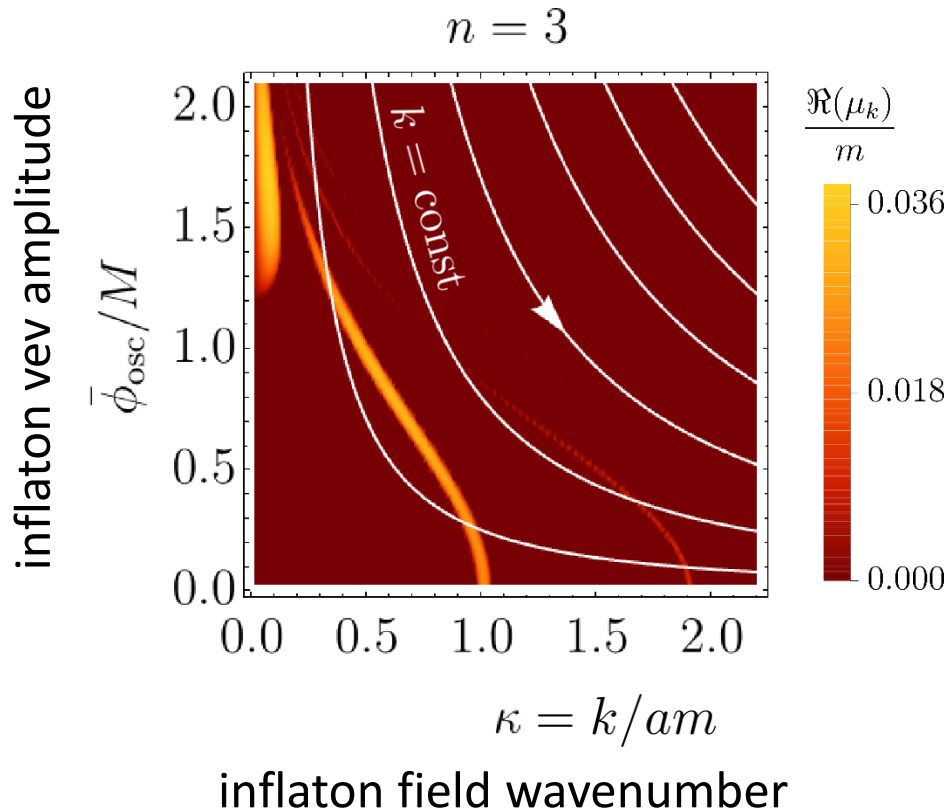


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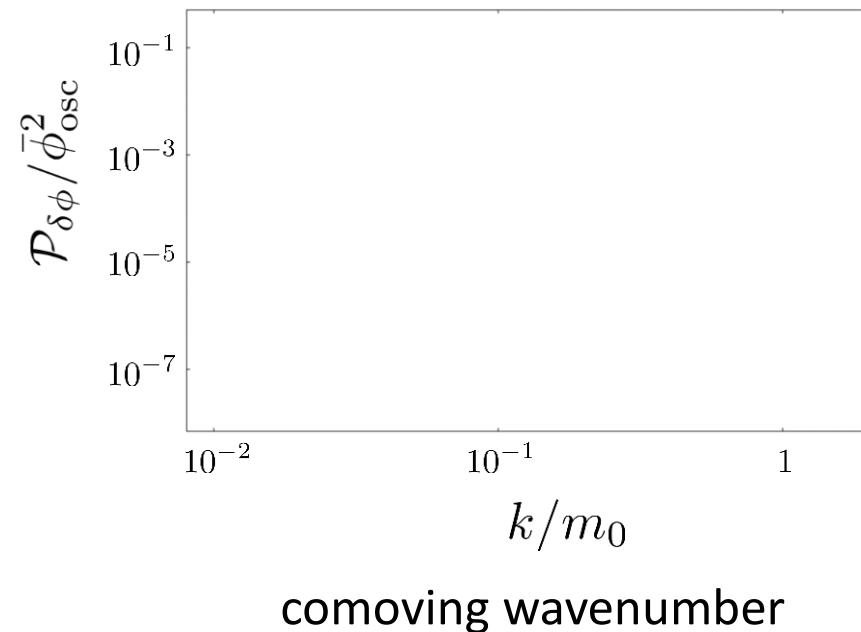
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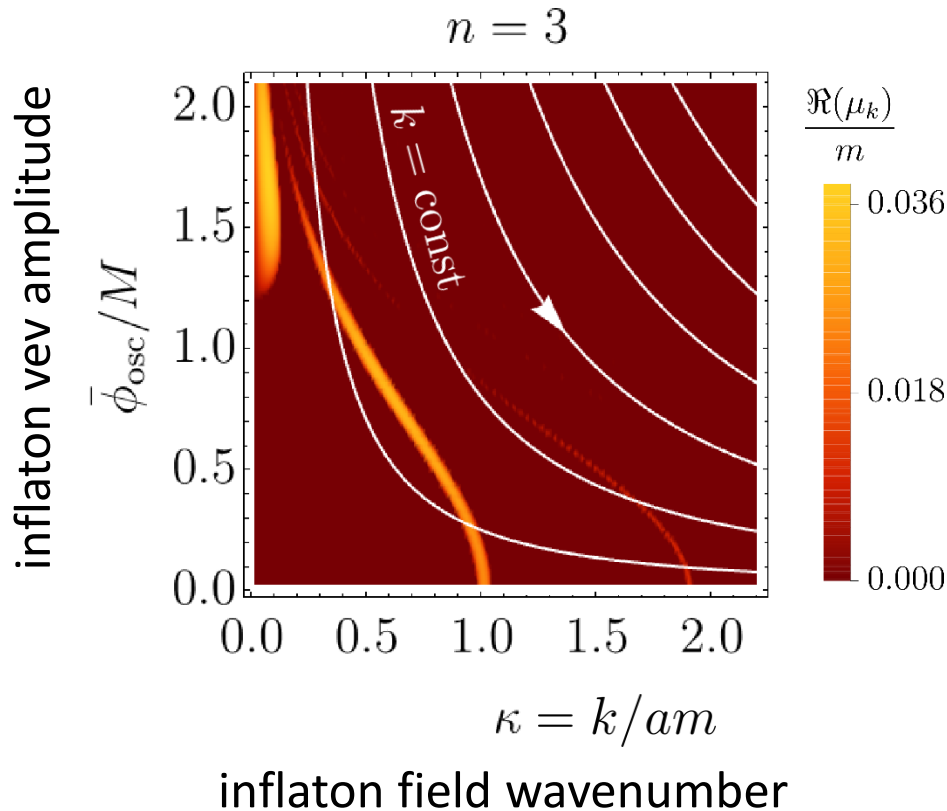
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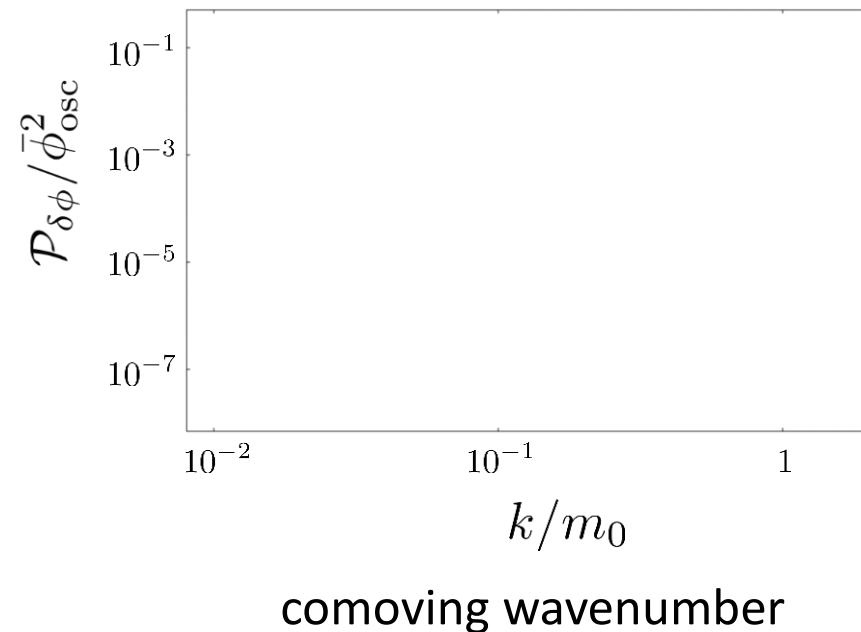
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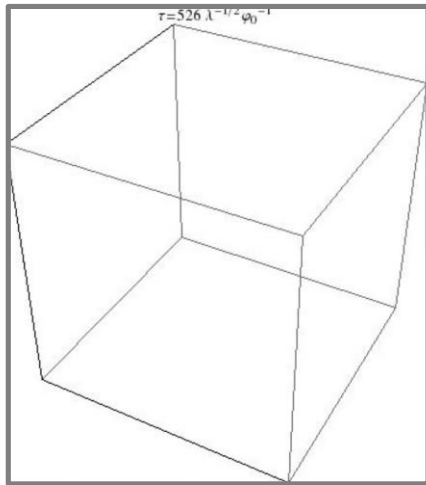


Towards radiation domination

$$M \ll m_{\text{pl}}$$

$$n > 1$$

$$M \sim m_{\text{pl}}$$



- $\bar{\phi}$ fragments quickly

- slow production of $\delta\phi(t, \mathbf{x})$
- $\bar{\phi}$ fragments gradually

$$\Delta N_{\text{fr}} \approx \frac{n+1}{3} \ln \left(10^3 \frac{M}{m_{\text{pl}}} \right)$$

at sufficiently late times:

$$\phi \text{ virialized + turbulent} \rightarrow w = \frac{1}{3}$$

Expansion history effects

Expansion history effects

Spectral index: n_s

Tensor-to-scalar ratio: r

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

Tensor-to-scalar ratio: $r = r(M, n, N_*)$

Expansion history effects

Spectral index: $n_s = n_s(M, n, \textcircled{N_*})$

Tensor-to-scalar ratio: $r = r(M, n, \textcircled{N_*})??$

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

Tensor-to-scalar ratio: $r = r(M, n, N_*)??$

$$50 \leq N_* \leq 60$$

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

Tensor-to-scalar ratio: $r = r(M, n, N_*)$ ✓

$$\cancel{50 \leq N_* \leq 60}$$

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

Tensor-to-scalar ratio: $r = r(M, n, N_*)$ ✓

$$N_* = 66.89 - \frac{1}{12} \ln g_{\text{th}} + \frac{1}{4} \ln \frac{V_*^4}{m_{\text{pl}}^4 \rho_{\text{end}}} - \ln \frac{k_*}{a_0 H_0} + \frac{3\bar{w}_{\text{int}} - 1}{4} \Delta N_{\text{rad}}$$

$$\Delta N_{\text{rad}} \equiv \int_{a_{\text{end}}}^{a_{\text{rad}}} d \ln a$$

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

Tensor-to-scalar ratio: $r = r(M, n, N_*)$ ✓

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reheating

$$\Delta N_{\text{rad}} \equiv \int_{a_{\text{end}}}^{a_{\text{rad}}} d \ln a$$

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

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$$\Delta N_{\text{fr}} = \begin{cases} 1 & \text{if } M \ll m_{\text{pl}} \\ \frac{n+1}{3} \ln \left(10 \frac{\kappa}{\Delta \kappa} \frac{M}{m_{\text{pl}}} \right) & \text{if } M \sim m_{\text{pl}} \end{cases}$$

$$\Delta N_{\text{rad}} \equiv \int_{a_{\text{end}}}^{a_{\text{rad}}} d \ln a$$

Expansion history effects

Spectral index: $n_s = n_s(M, n, N_*)$

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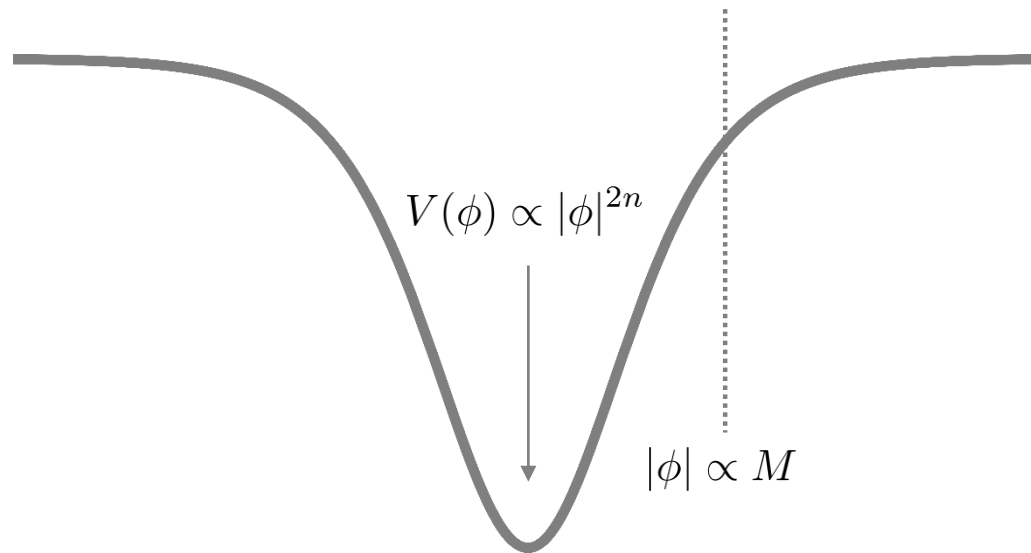
$$w_{\text{int}}(\Delta N) = \begin{cases} \frac{n-1}{n+1} & \text{if } 0 < \Delta N < \Delta N_{\text{rad}} \\ \frac{1}{3} & \text{if } \Delta N > \Delta N_{\text{rad}} \end{cases}$$

$$\Delta N_{\text{rad}} \equiv \int_{a_{\text{end}}}^{a_{\text{rad}}} d \ln a$$

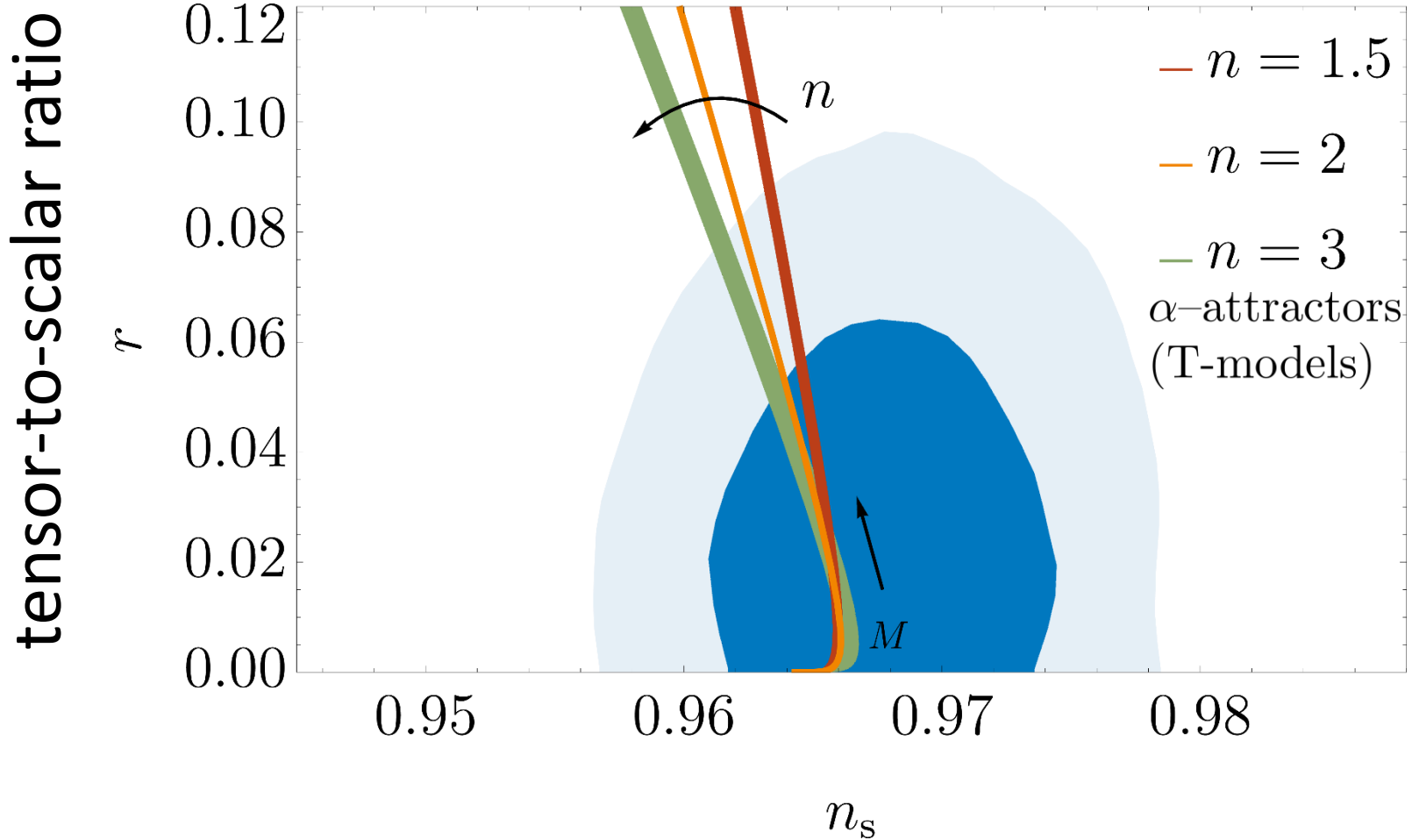
Expansion history effects

$$V(\phi) \propto \tanh^{2n} \left(\frac{|\phi|}{M} \right)$$

α -attractors
(T-models)



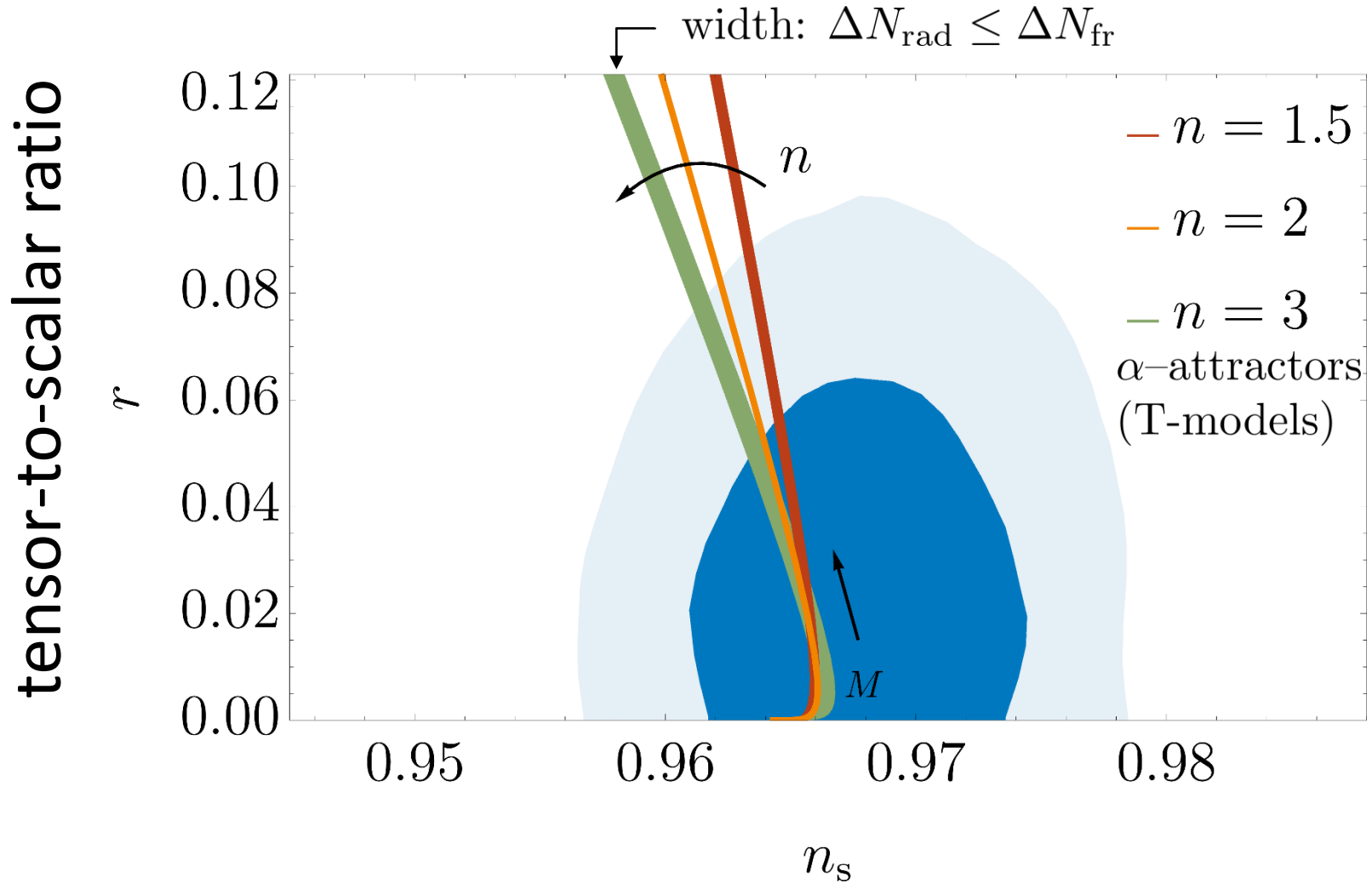
Expansion history effects



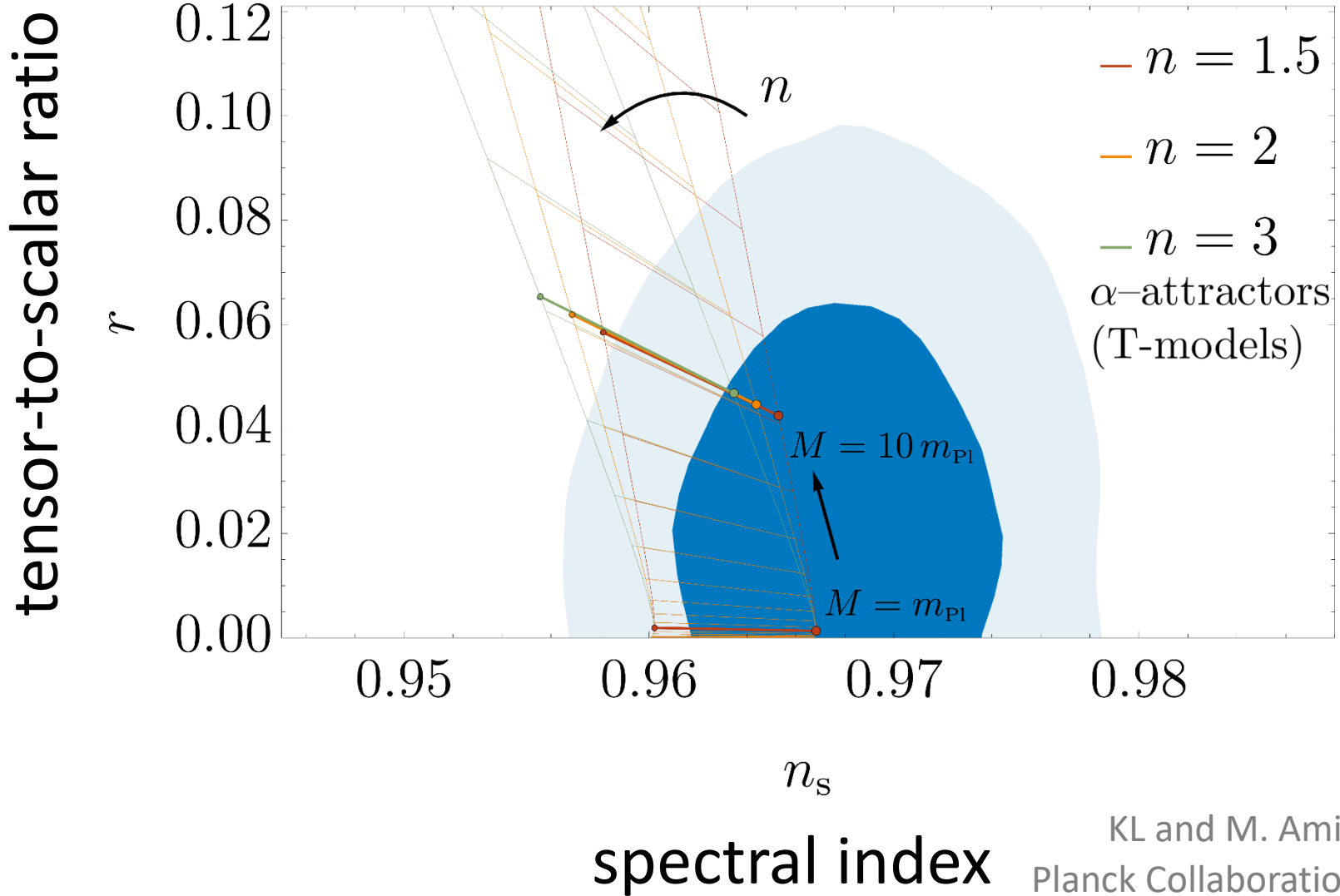
spectral index

KL and M. Amin (2016)
Planck Collaboration (2015)

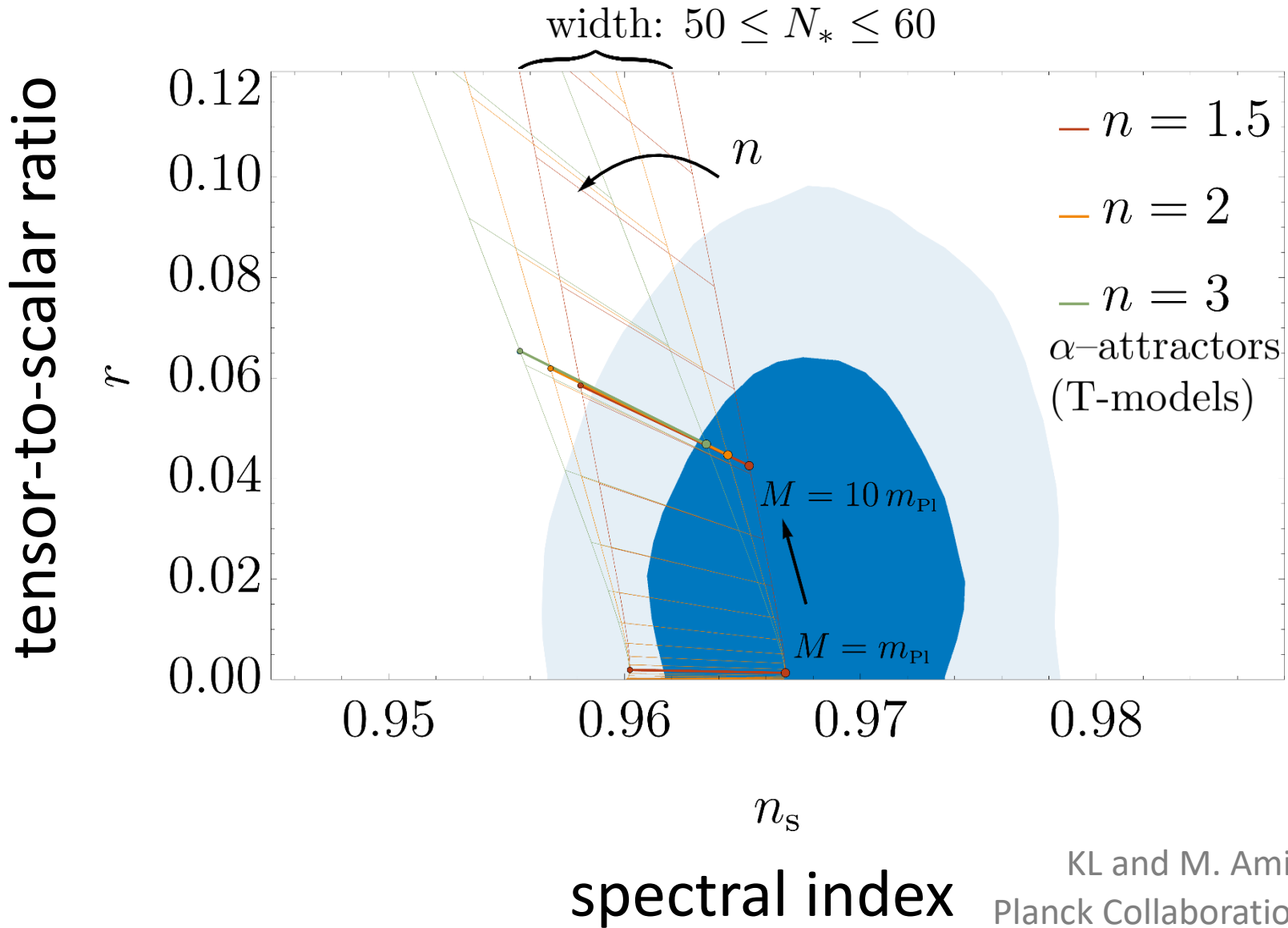
Expansion history effects



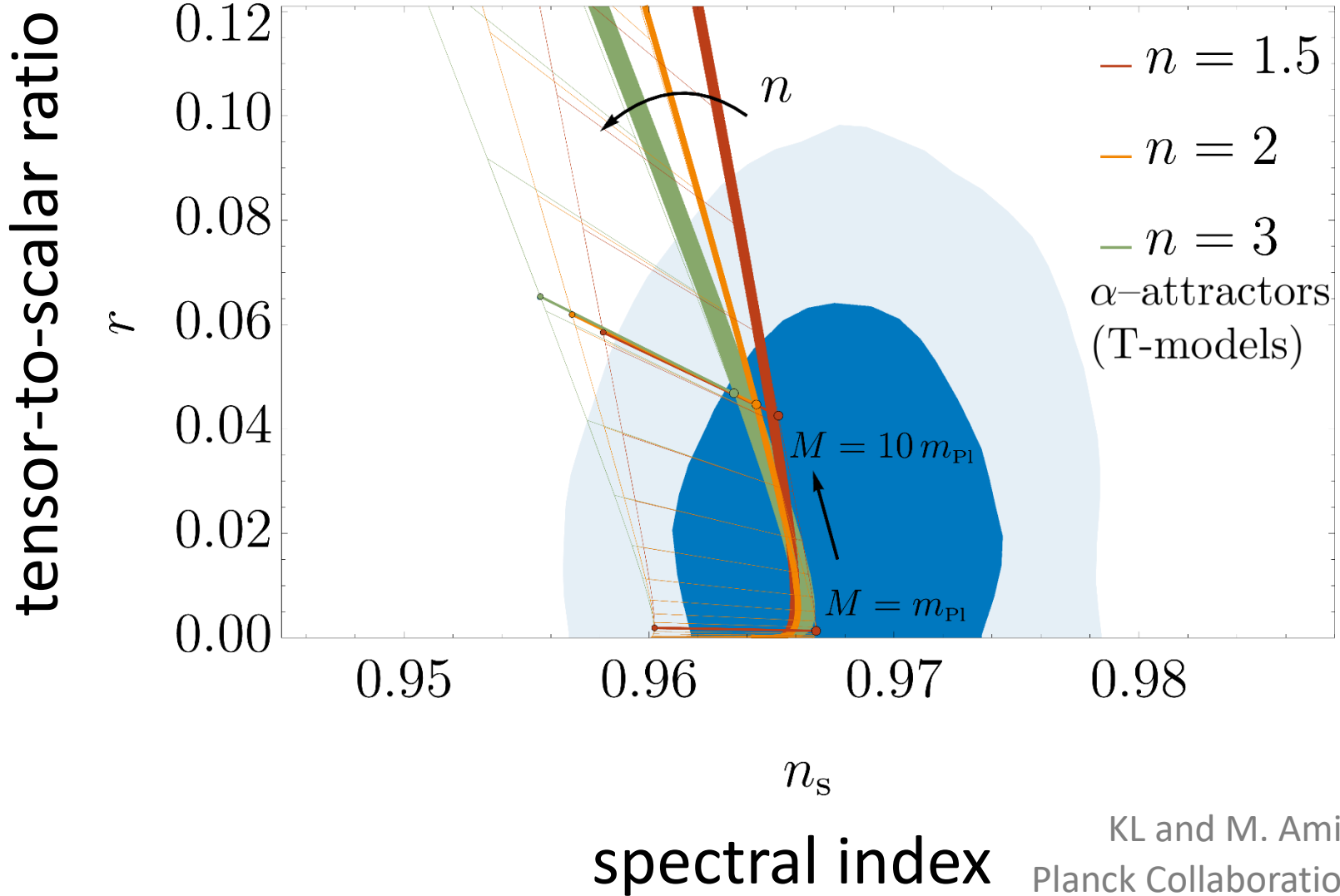
Expansion history effects



Expansion history effects



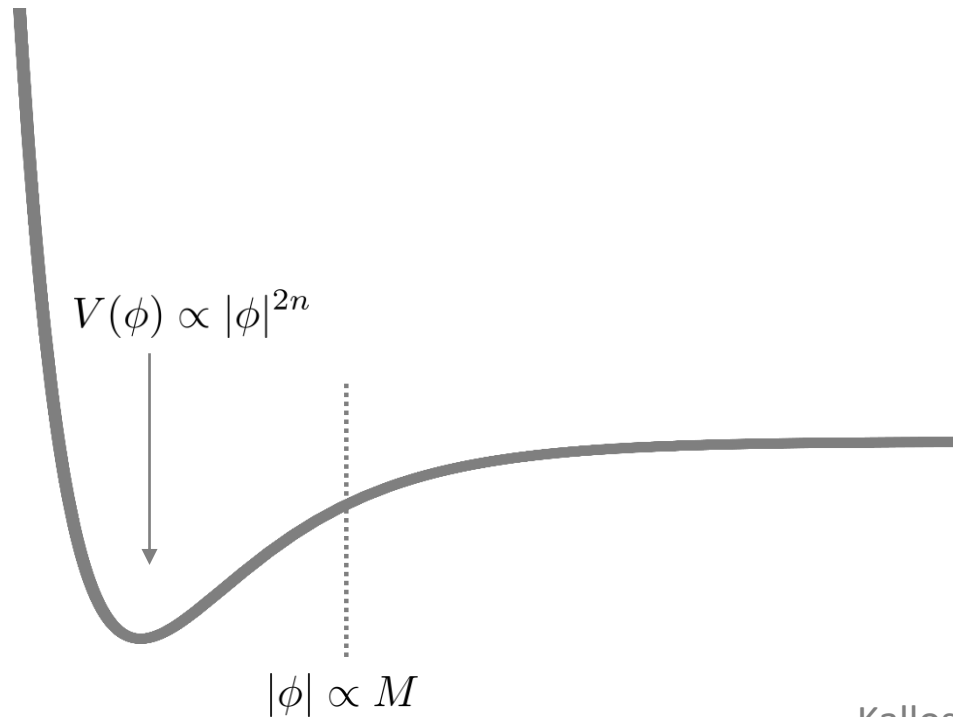
Expansion history effects



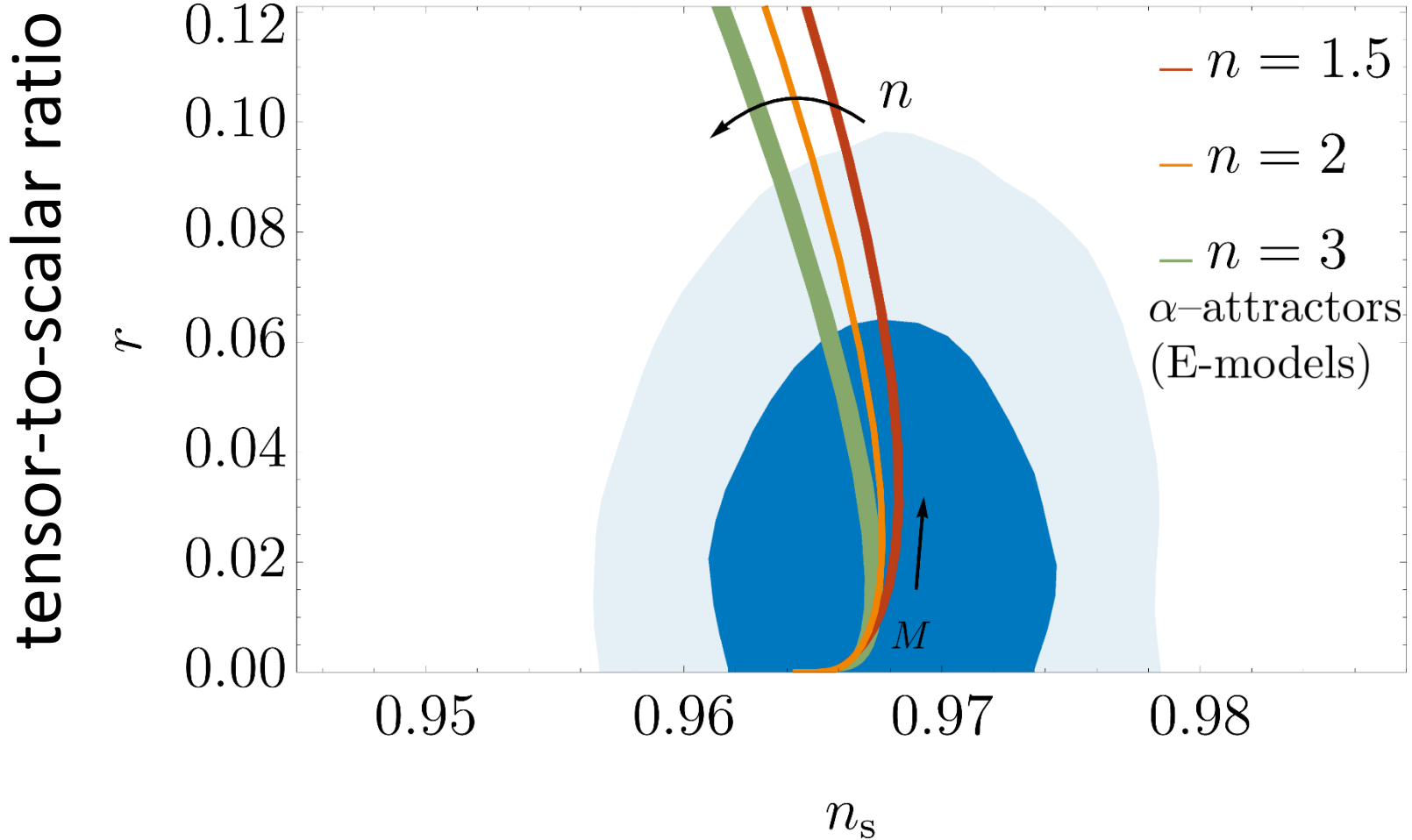
Expansion history effects

$$V(\phi) \propto \left| 1 - e^{-\phi/M} \right|^{2n}$$

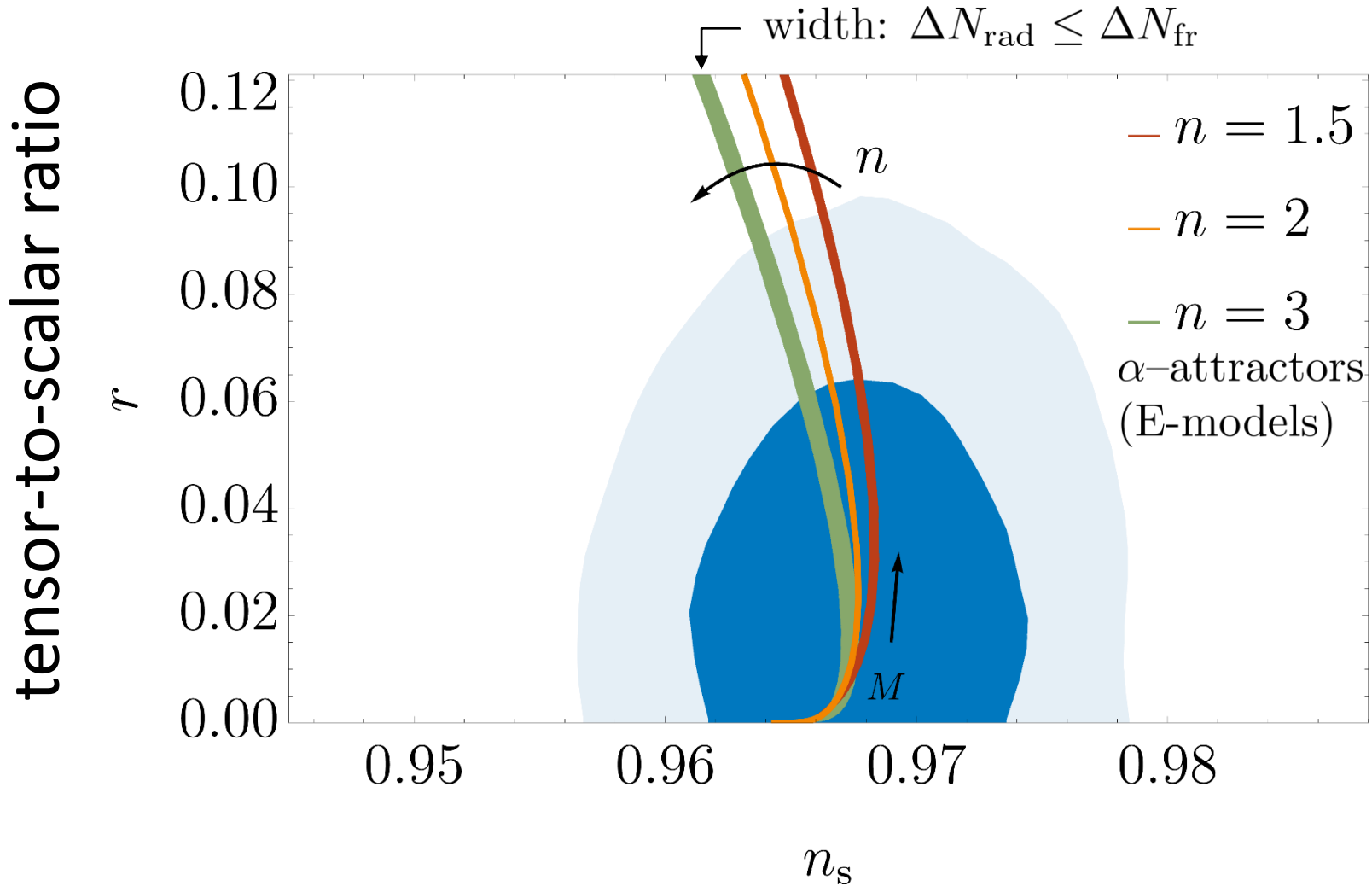
α -attractors
(E-models)



Expansion history effects



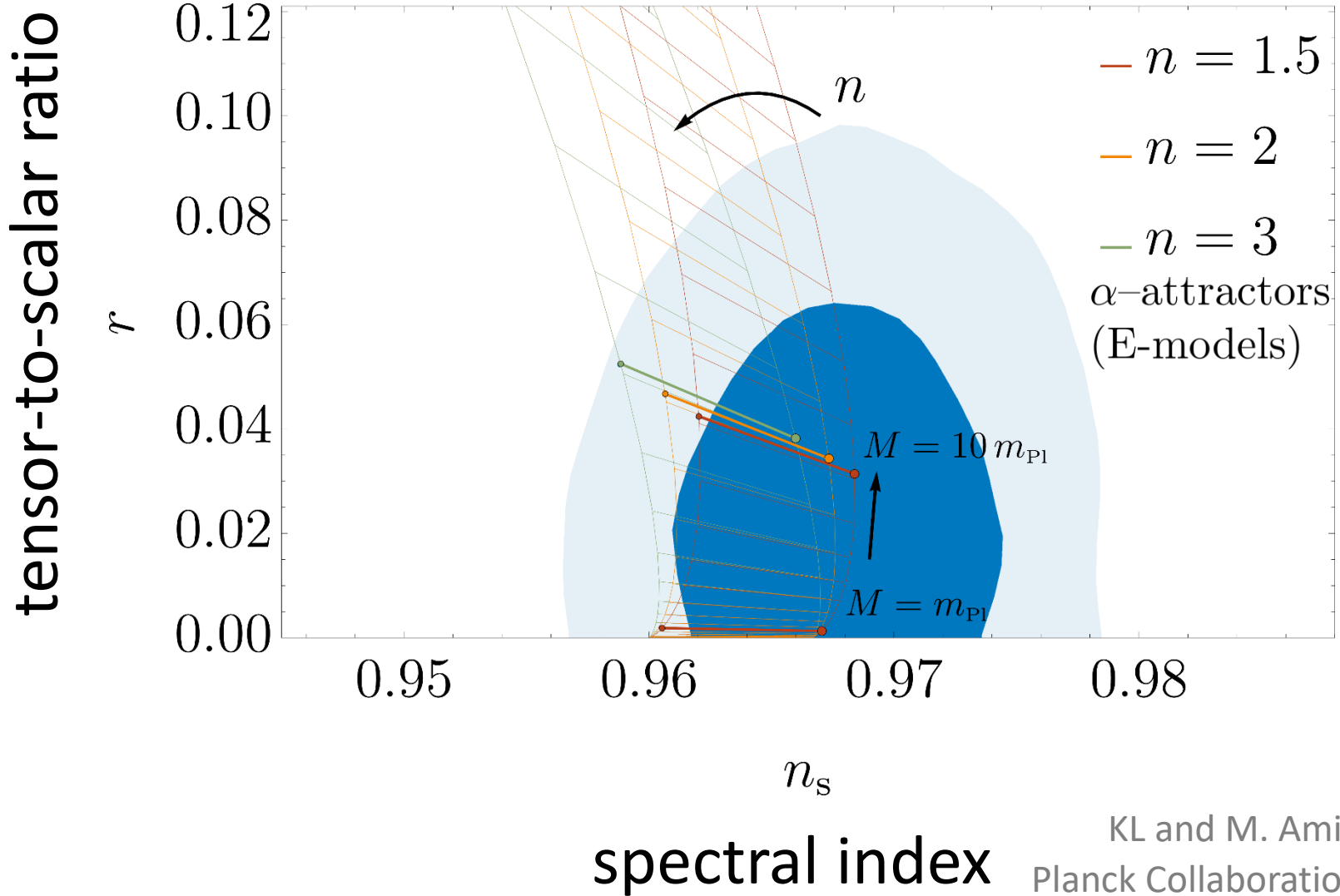
Expansion history effects



spectral index

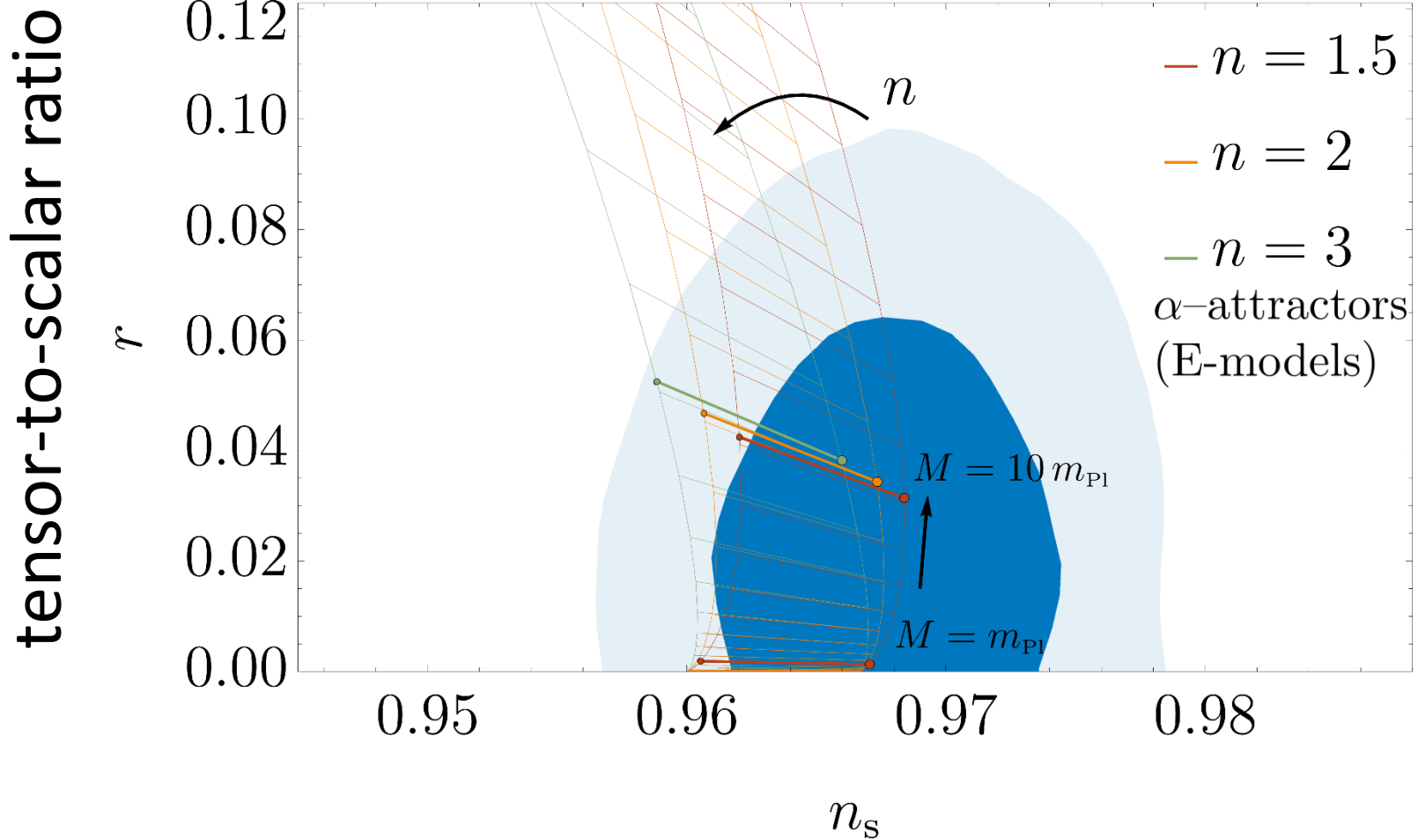
KL and M. Amin (2016)
Planck Collaboration (2015)

Expansion history effects



Expansion history effects

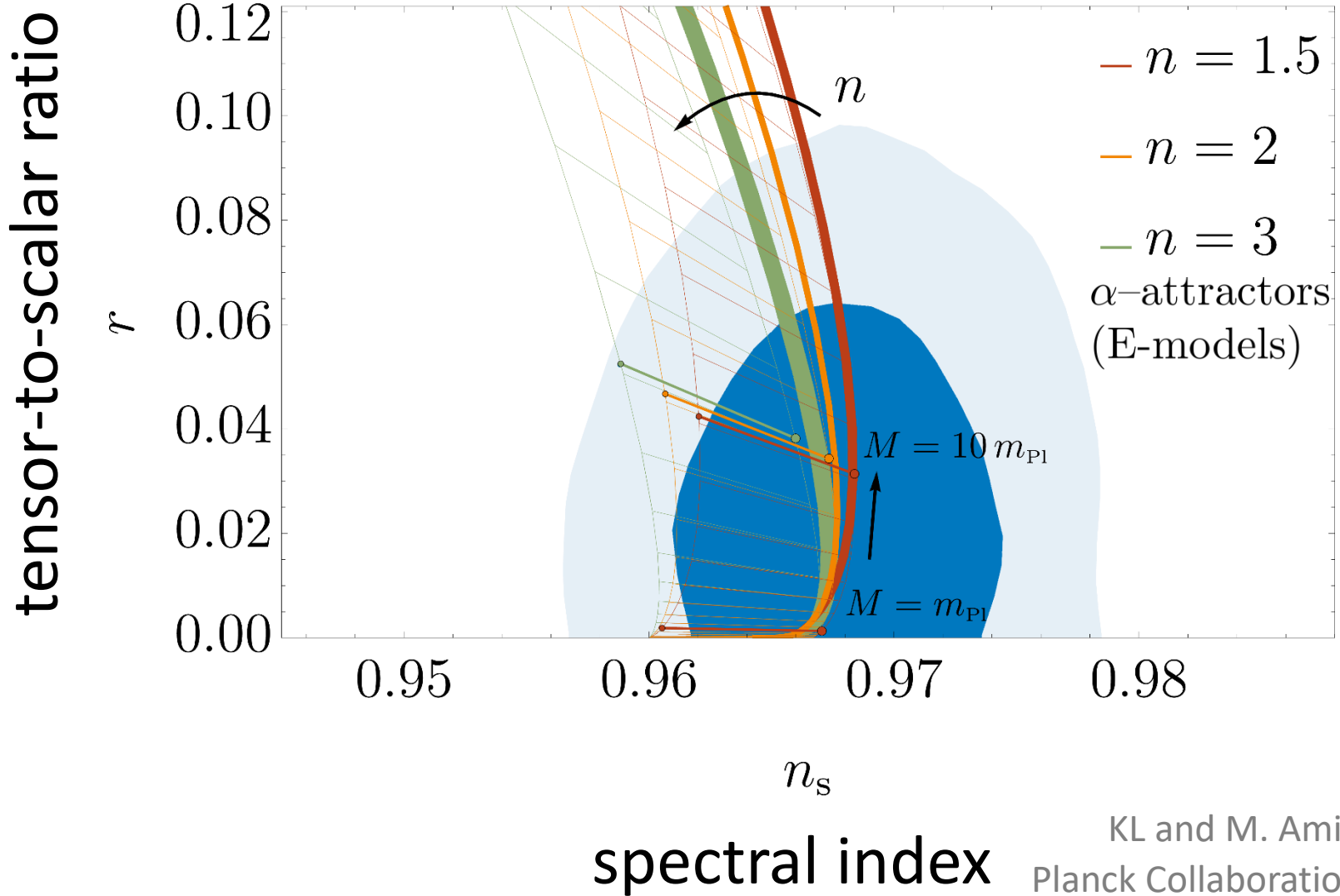
width: $50 \leq N_* \leq 60$



spectral index

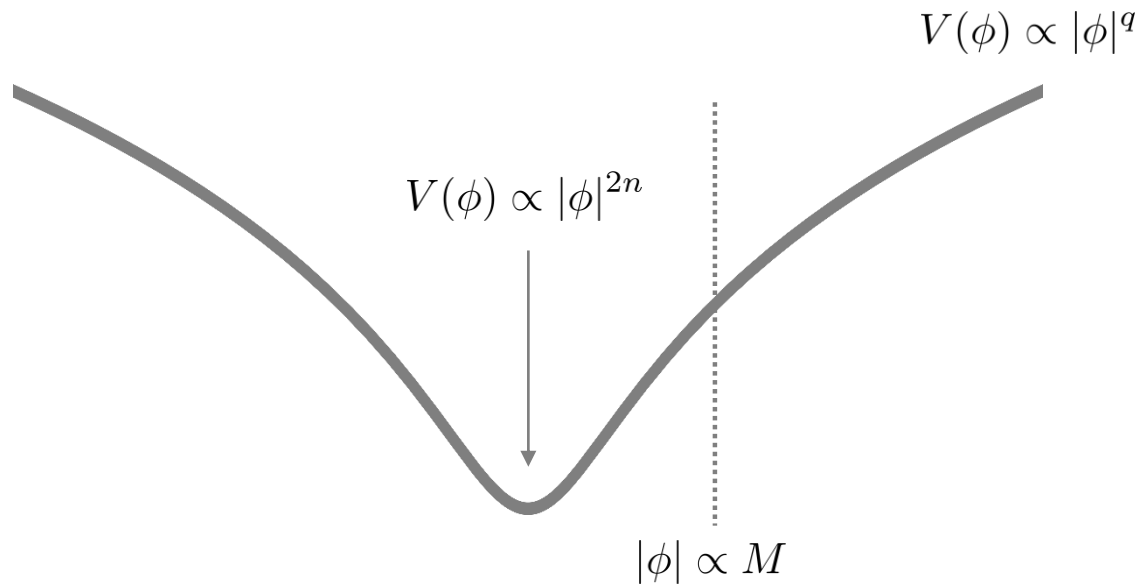
KL and M. Amin (2016)
Planck Collaboration (2015)

Expansion history effects



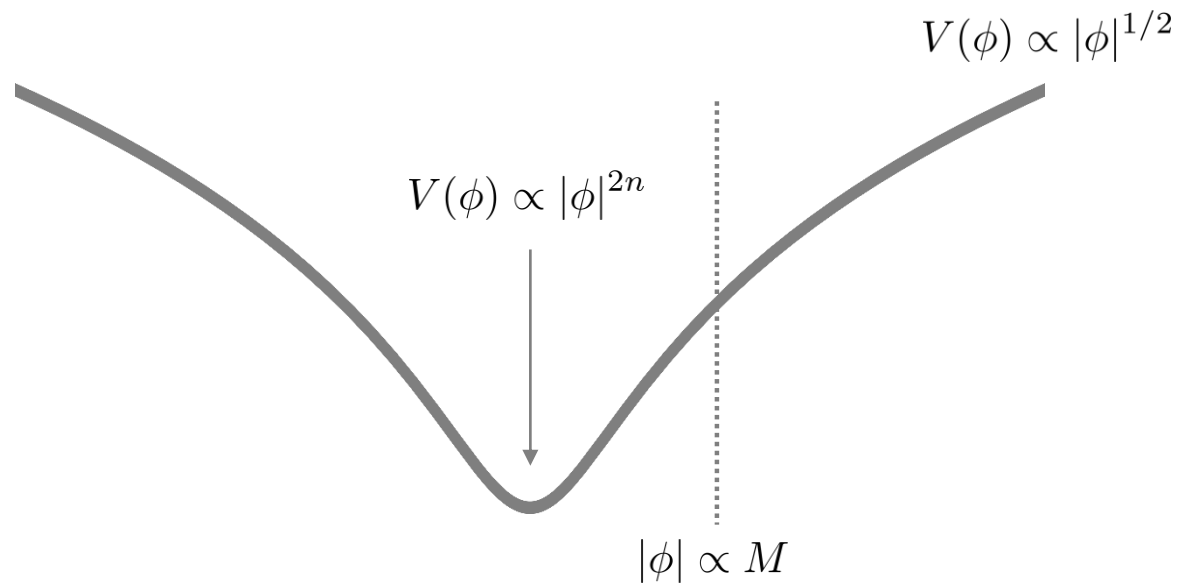
Expansion history effects

$$V(\phi) \propto \left[1 + \left| \frac{\phi}{M} \right|^{2n} \right]^{\frac{q}{2n}} - 1 \quad \text{Monodromy}$$

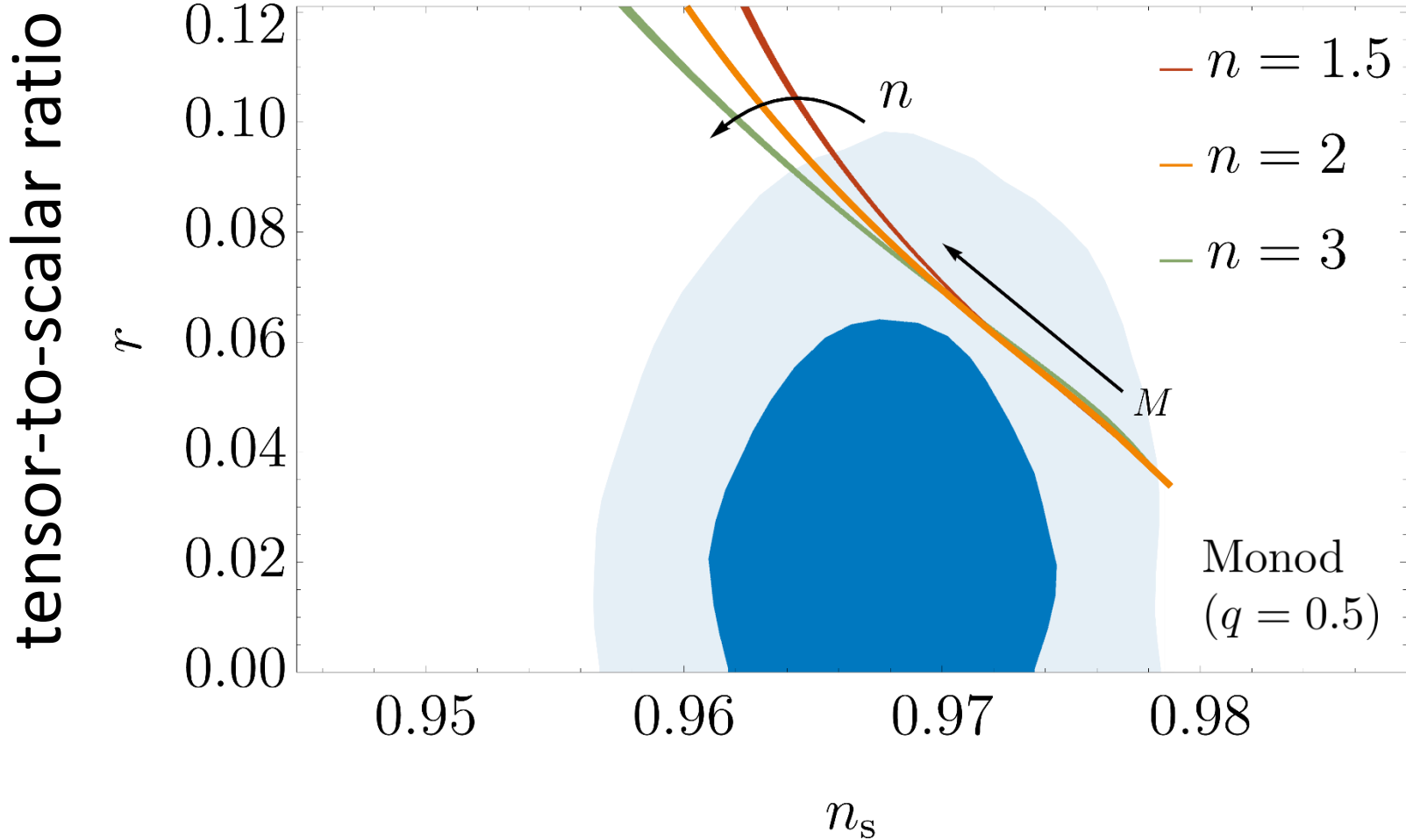


Expansion history effects

$$V(\phi) \propto \left[1 + \left| \frac{\phi}{M} \right|^{2n} \right]^{\frac{1}{4n}} - 1 \quad \text{Monodromy} \\ q = 1/2$$



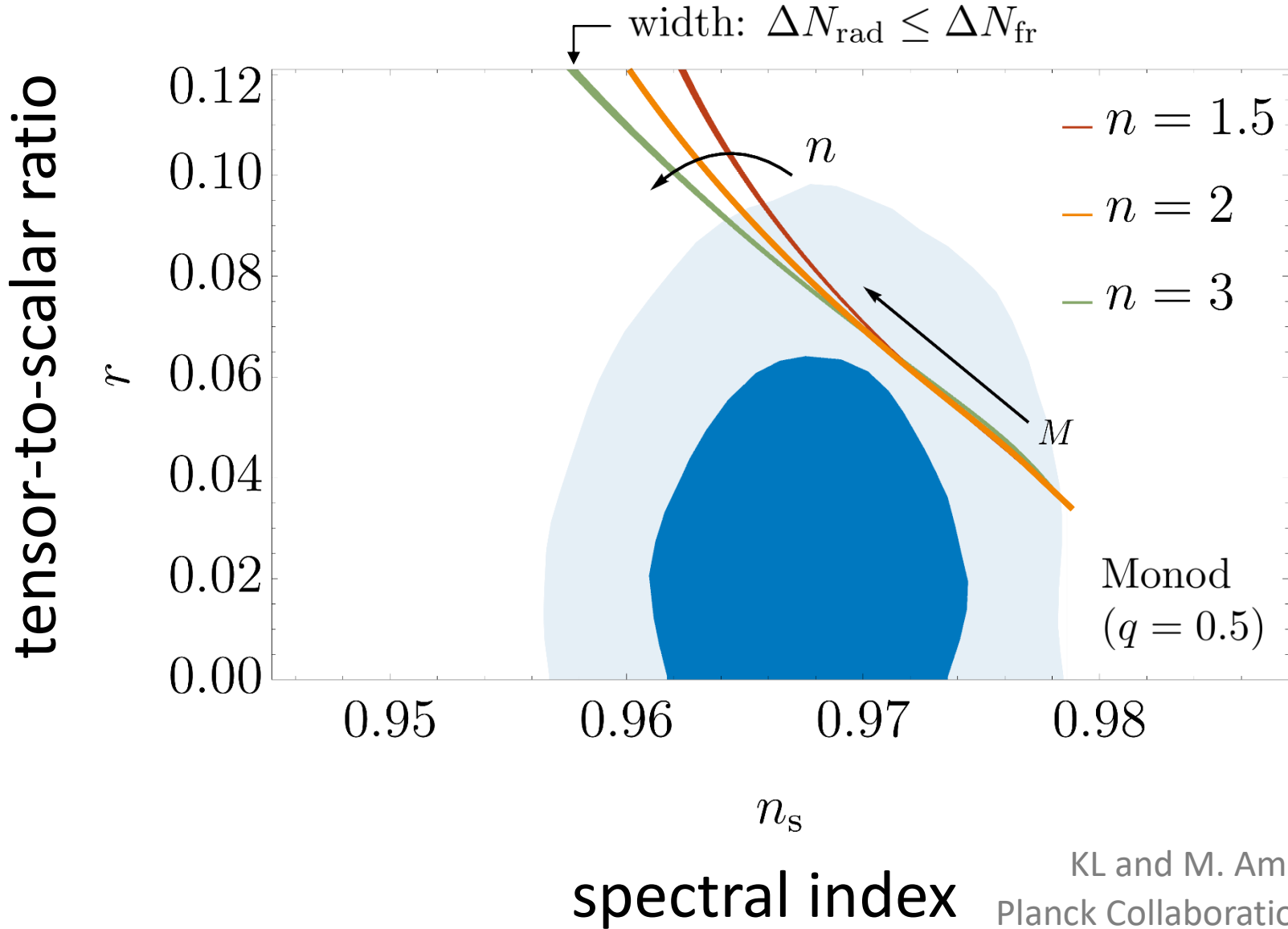
Expansion history effects



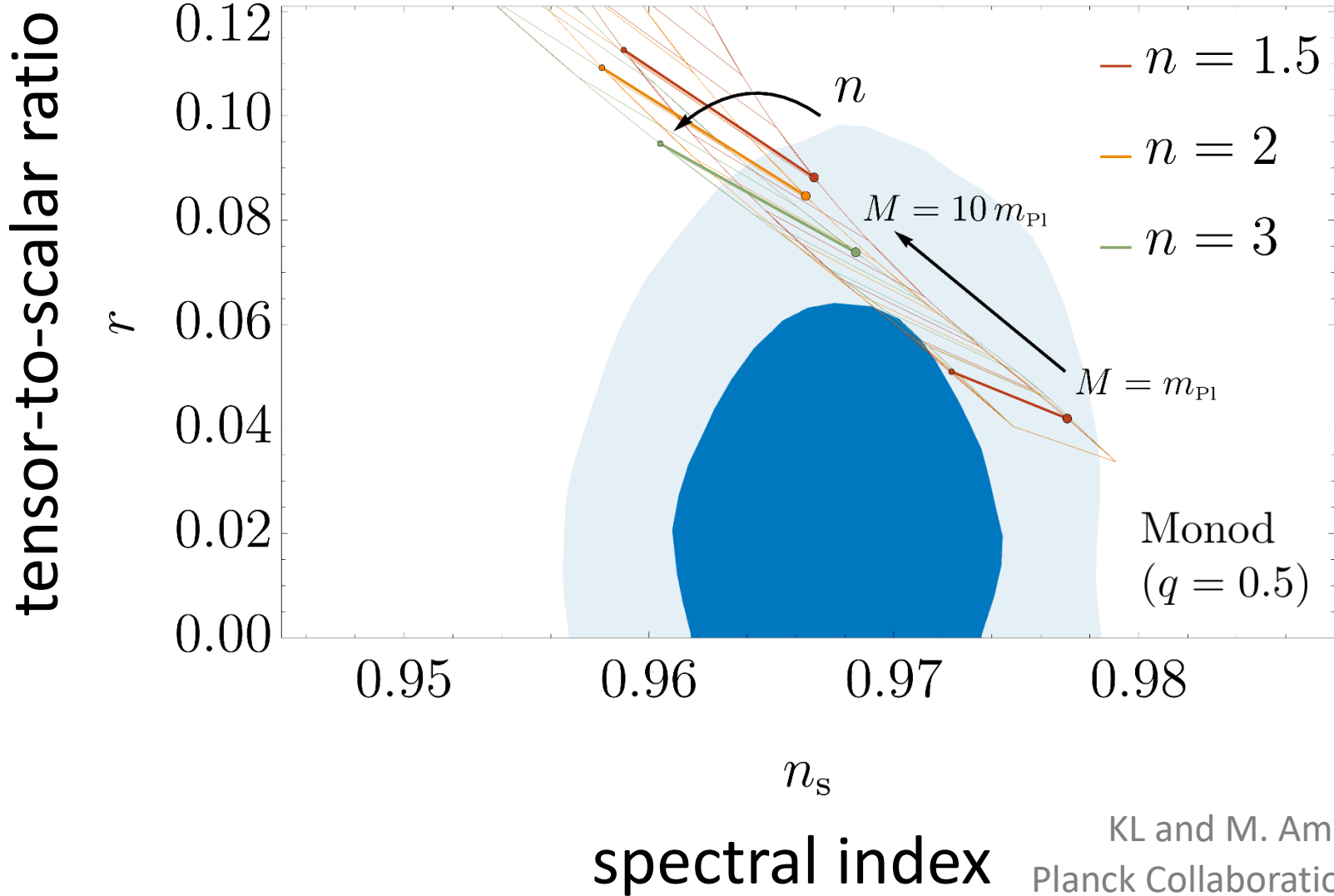
spectral index

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Planck Collaboration (2015)

Expansion history effects

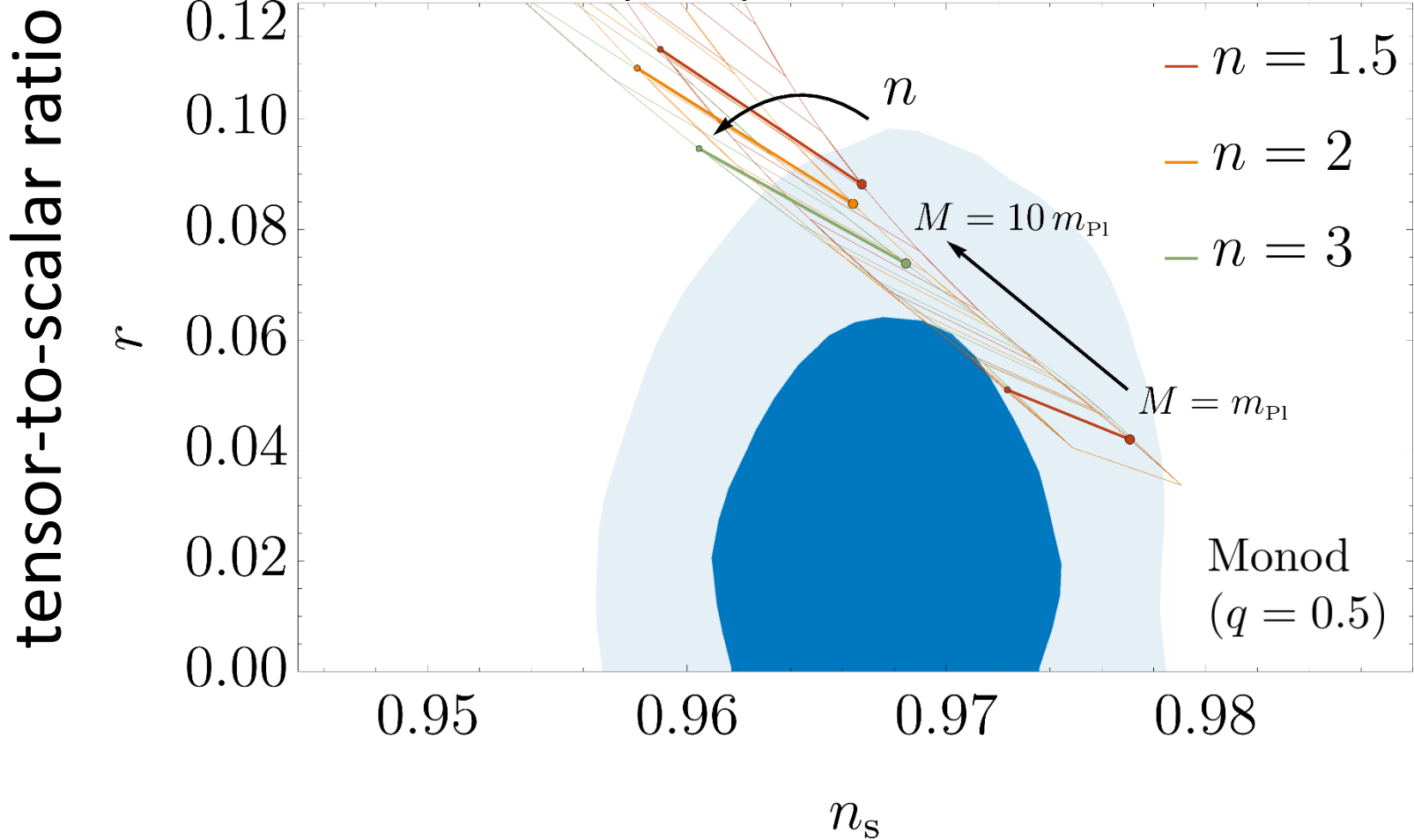


Expansion history effects



Expansion history effects

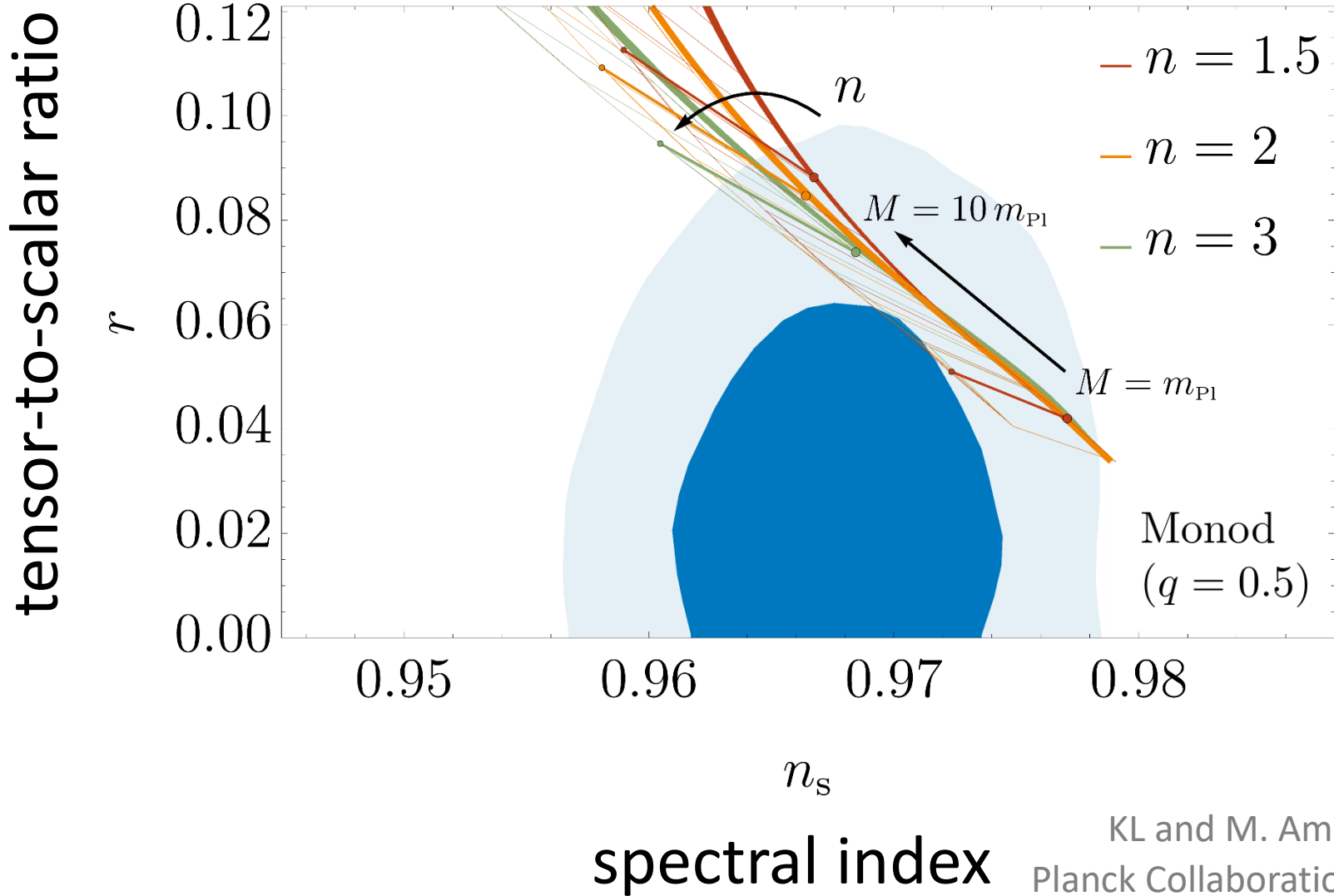
width: $50 \leq N_* \leq 60$



spectral index

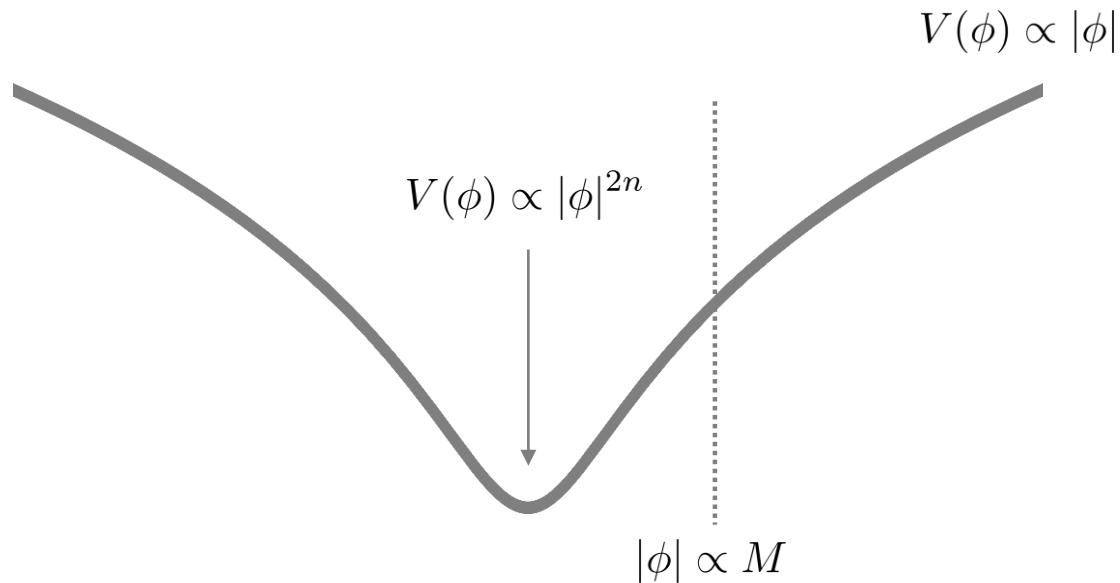
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Expansion history effects

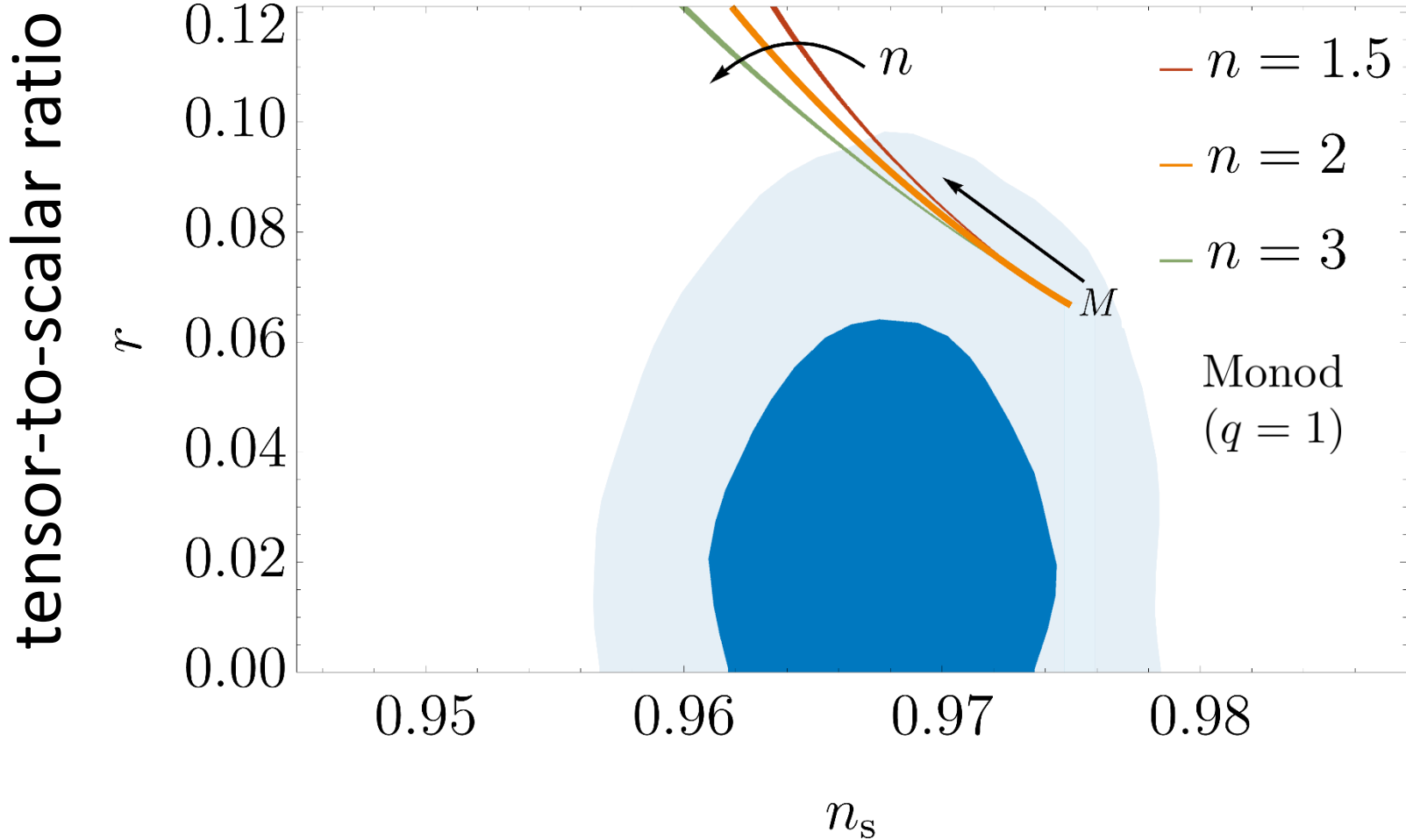


Expansion history effects

$$V(\phi) \propto \left[1 + \left| \frac{\phi}{M} \right|^{2n} \right]^{\frac{1}{2n}} - 1 \quad \text{Monodromy } q = 1$$



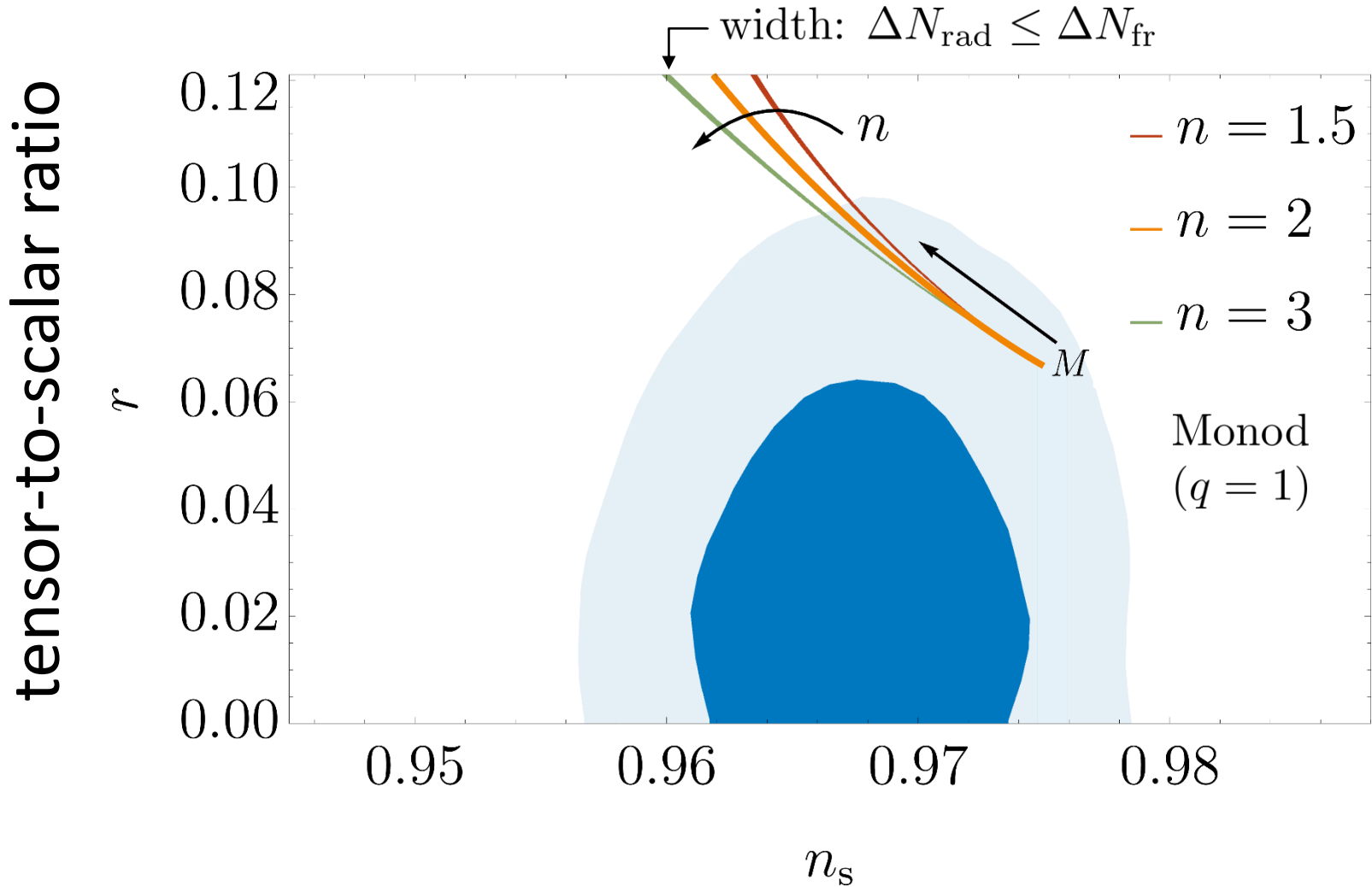
Expansion history effects



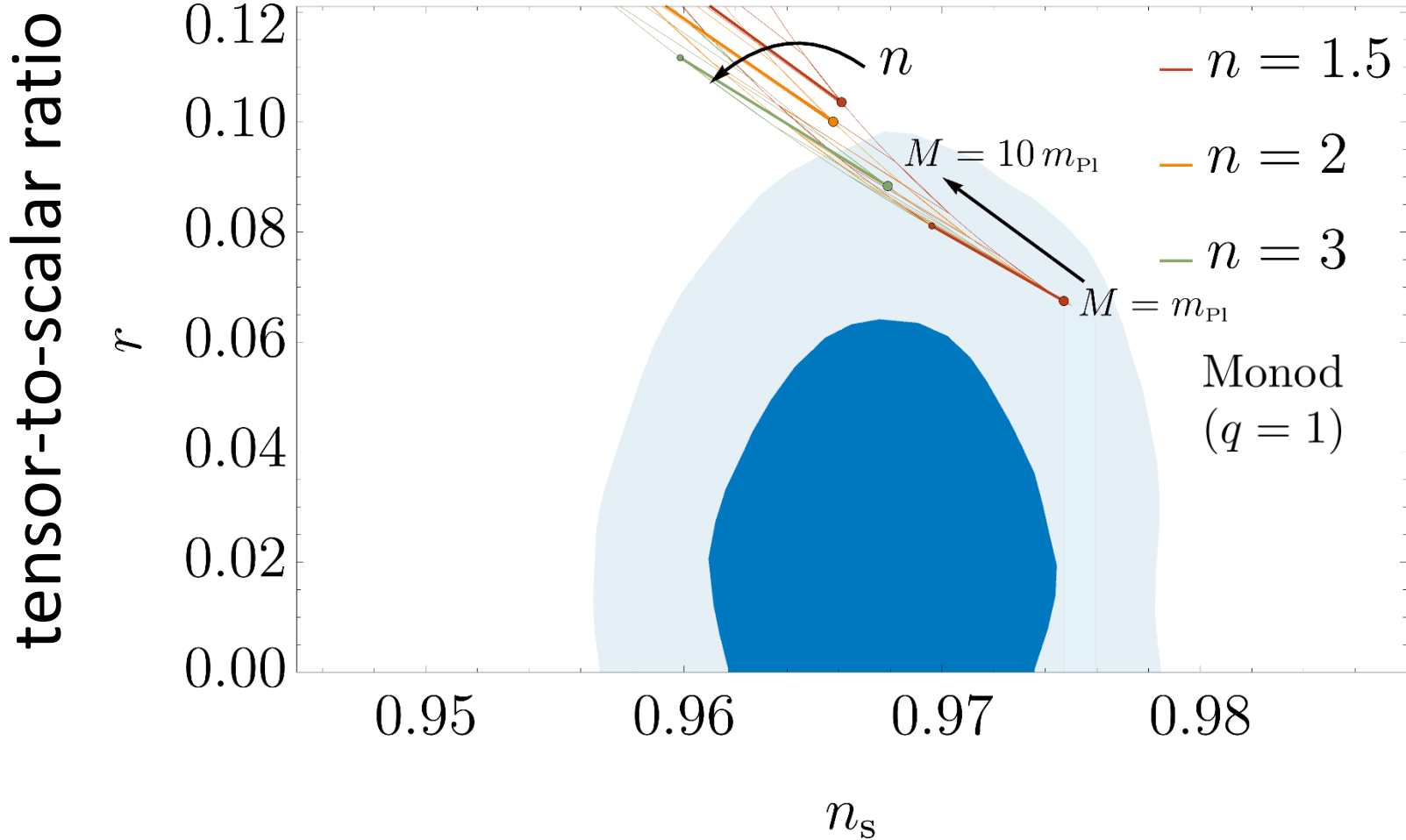
spectral index

KL and M. Amin (2016)
Planck Collaboration (2015)

Expansion history effects



Expansion history effects

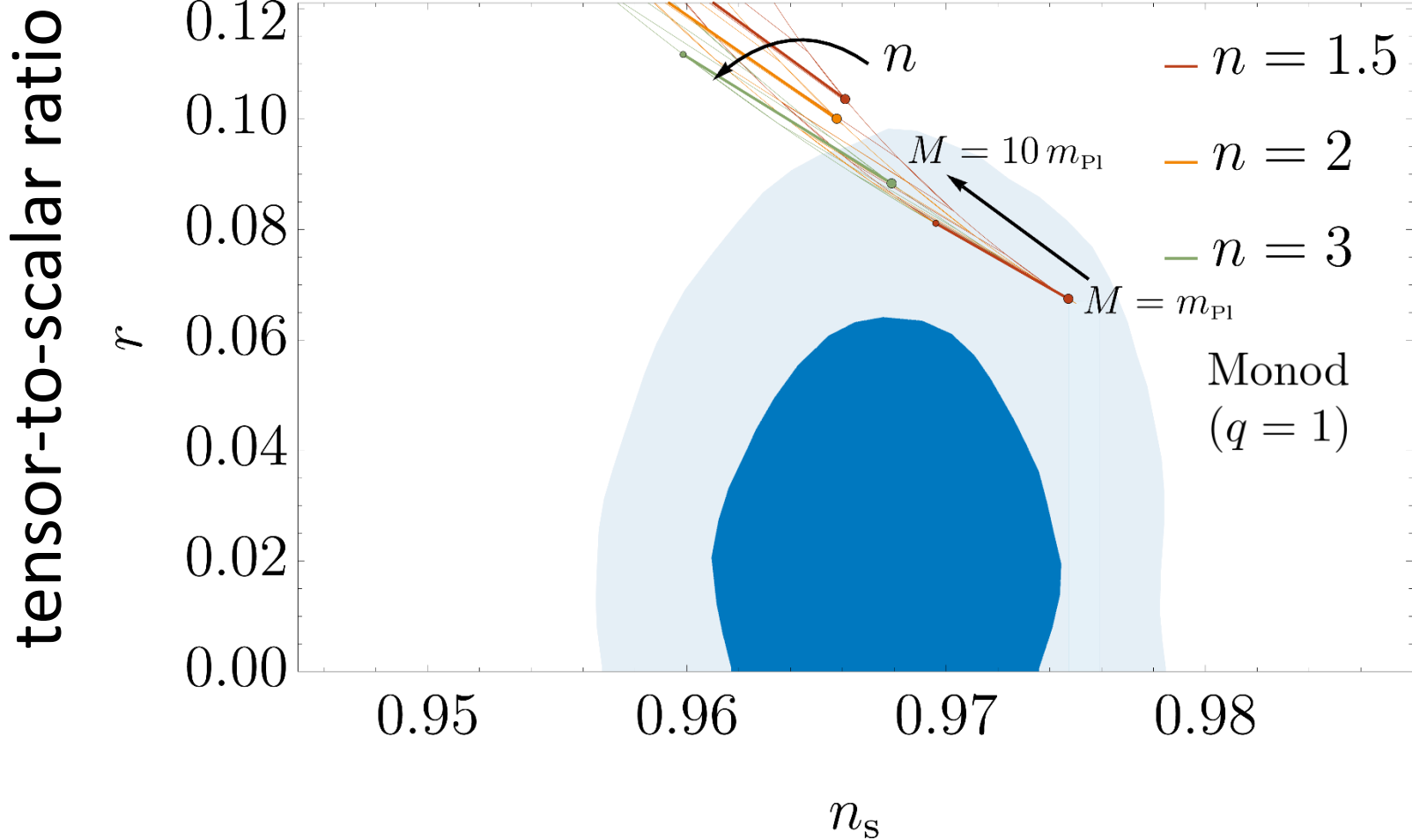


spectral index

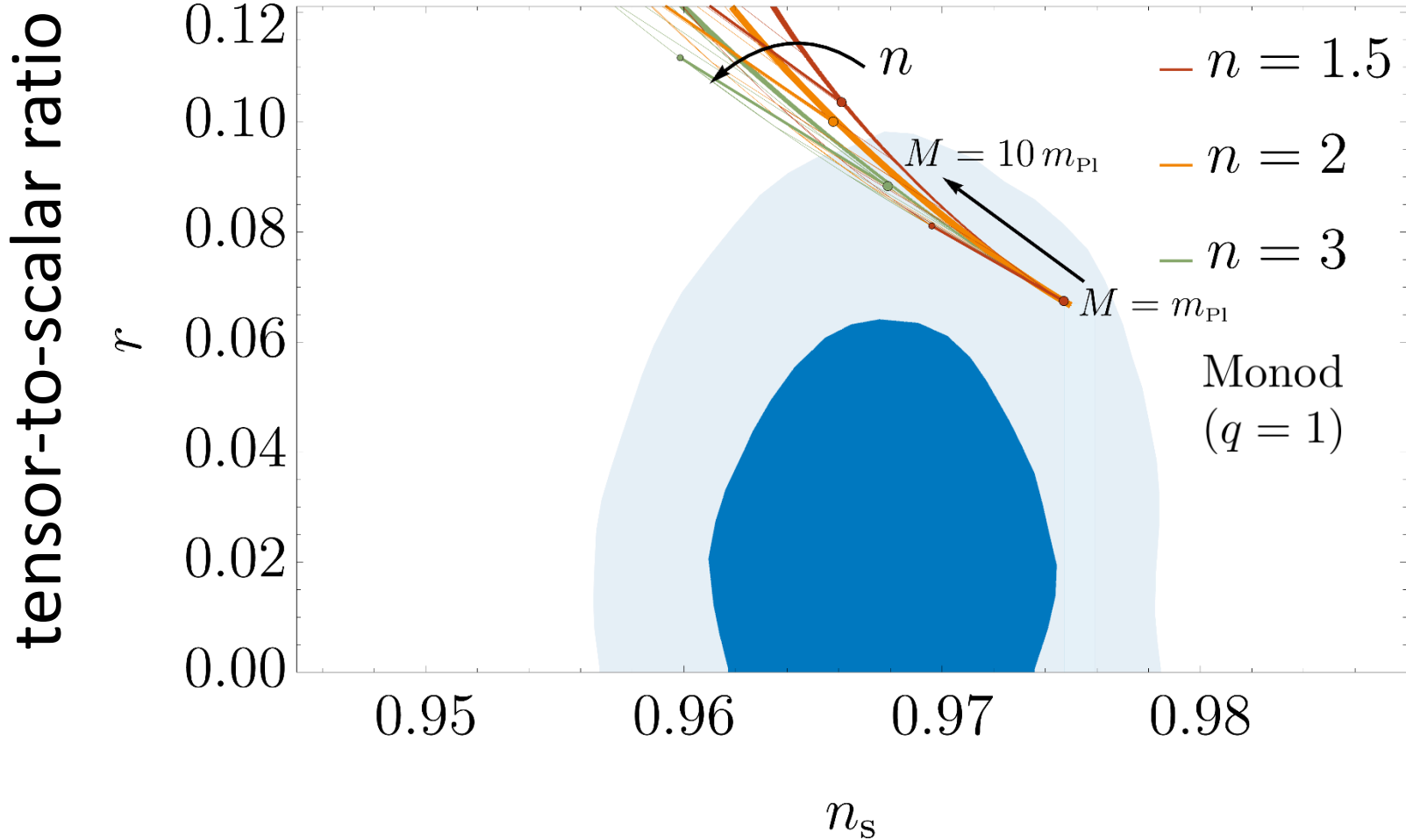
KL and M. Amin (2016)
Planck Collaboration (2015)

Expansion history effects

width: $50 \leq N_* \leq 60$



Expansion history effects

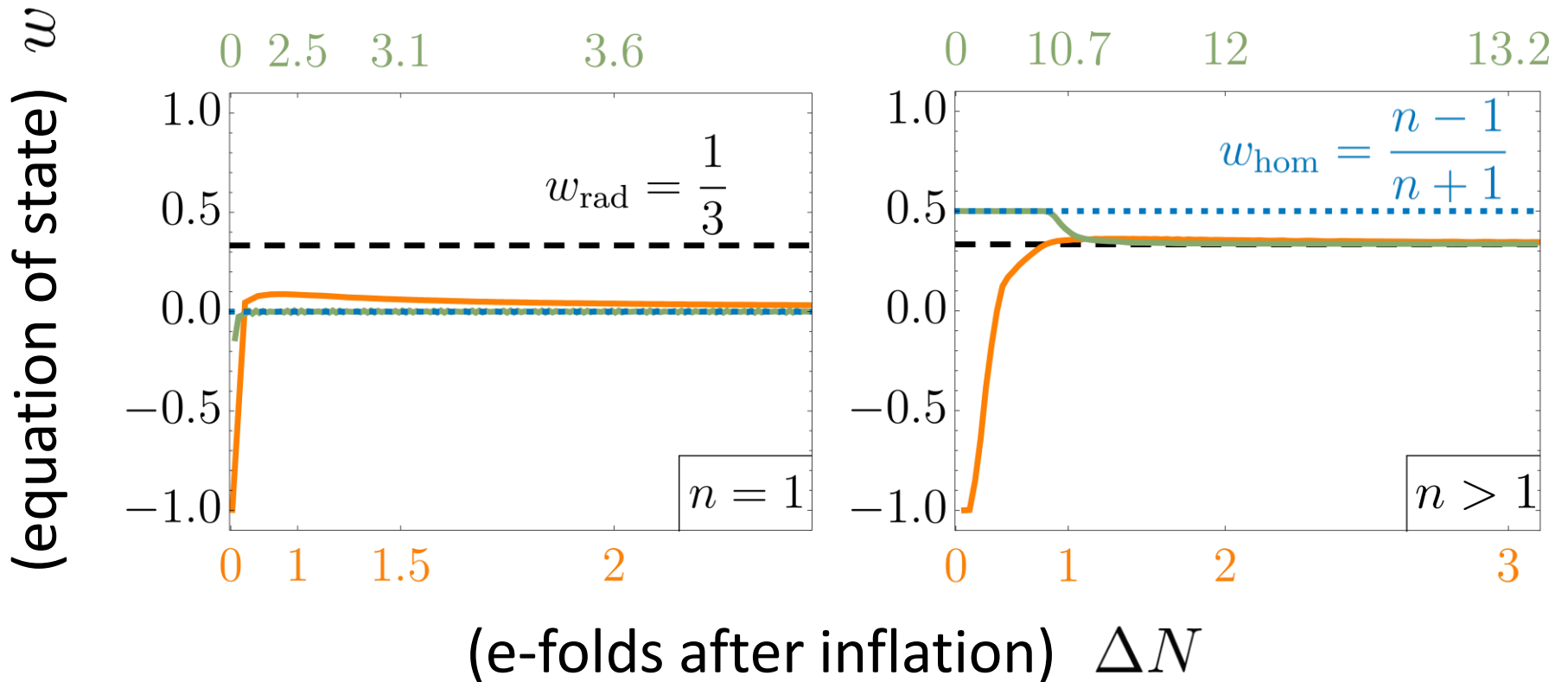


spectral index

Equation of state

— $M \ll m_{\text{pl}}$ (efficient resonance)

— $M \sim m_{\text{pl}}$ (inefficient resonance)



$$\Delta N \equiv \int_{a_{\text{end}}}^a d \ln a$$

Matter domination?

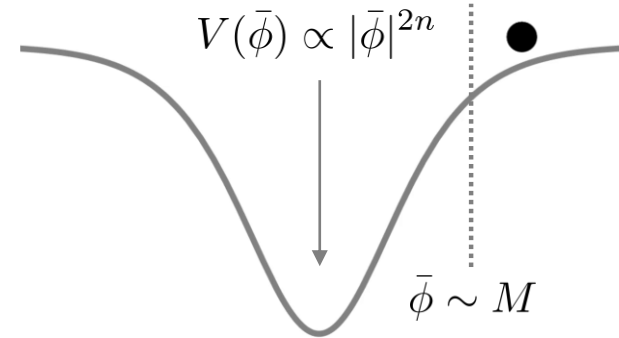
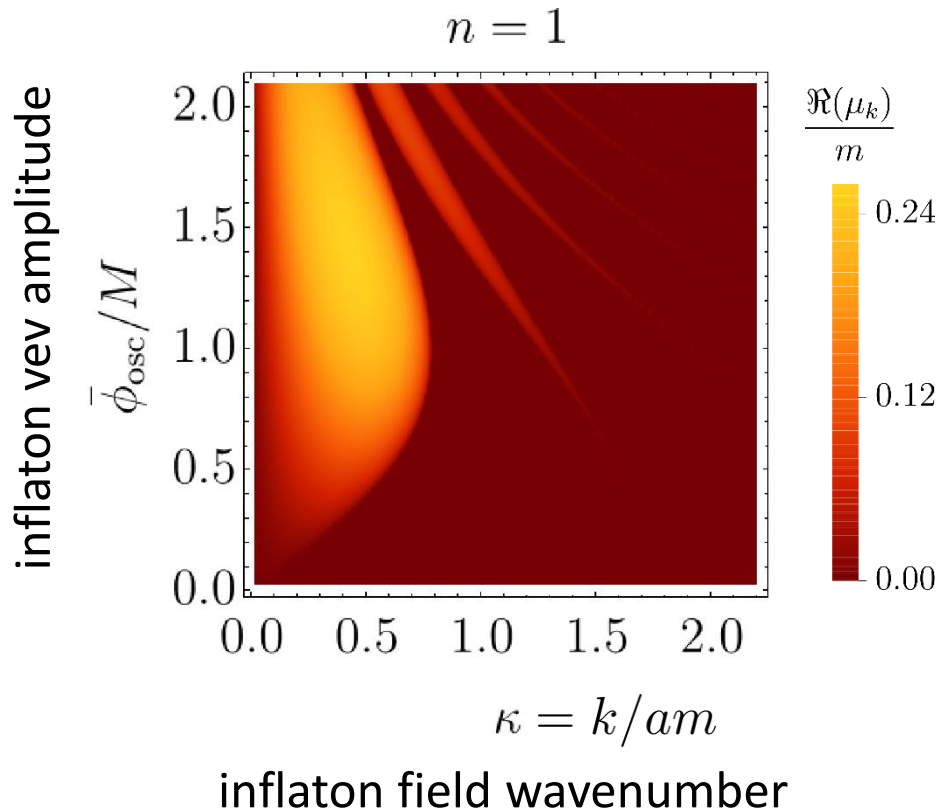
$$n = 1$$

Matter domination?

$$n = 1$$

KL and M. Amin (2016)

Non-perturbative decay (parametric self-resonance)



$$\delta\phi_k \propto \exp(\pm\mu_k t)$$

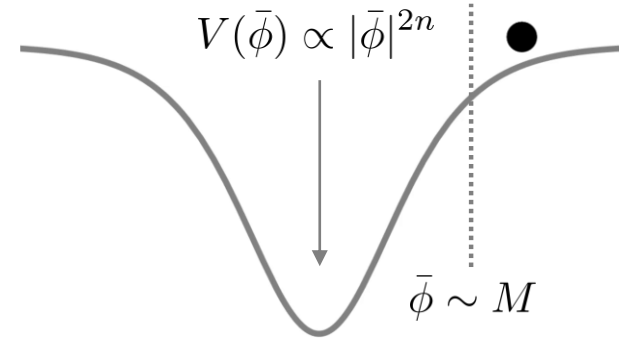
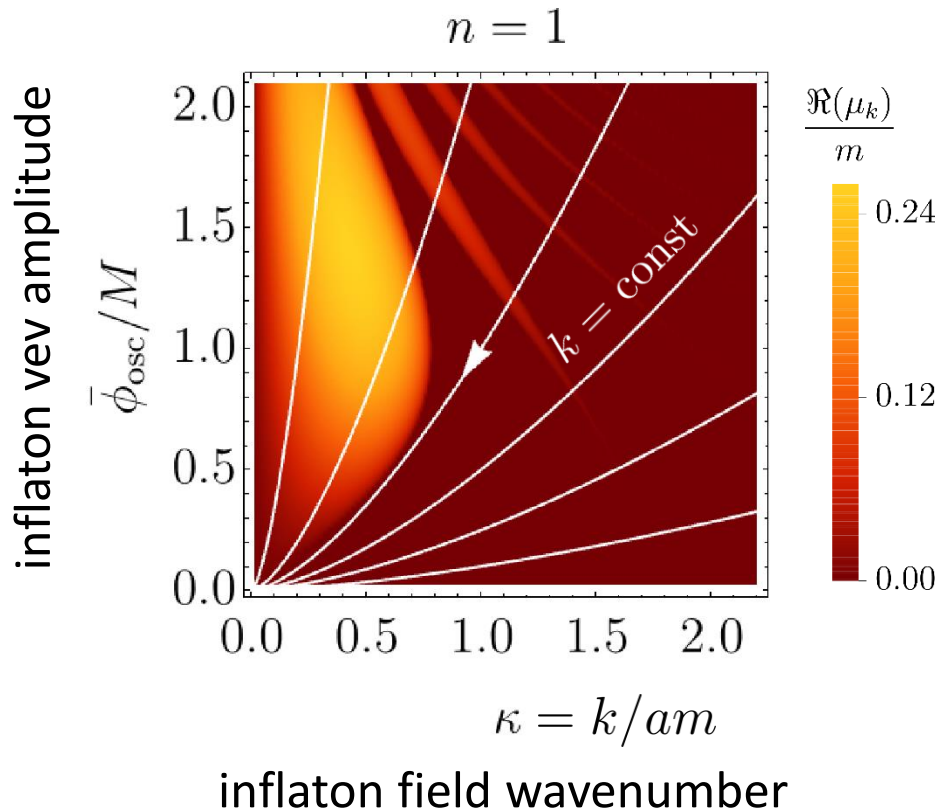
See also Amin, Hertzberg + (2011), Fukunaga, Kitajima and Urakawa (2019) $m^2 \equiv V'(\bar{\phi}_{\text{osc}})/\bar{\phi}_{\text{osc}}$

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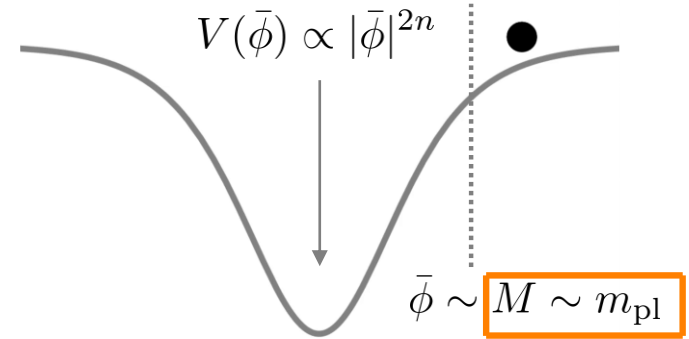
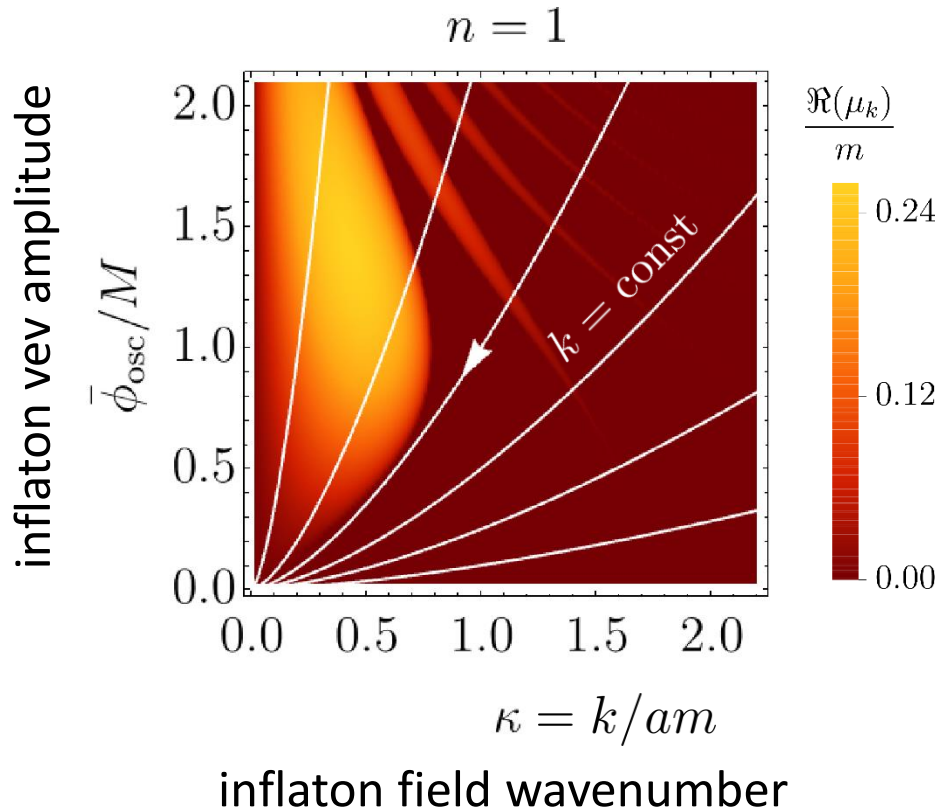
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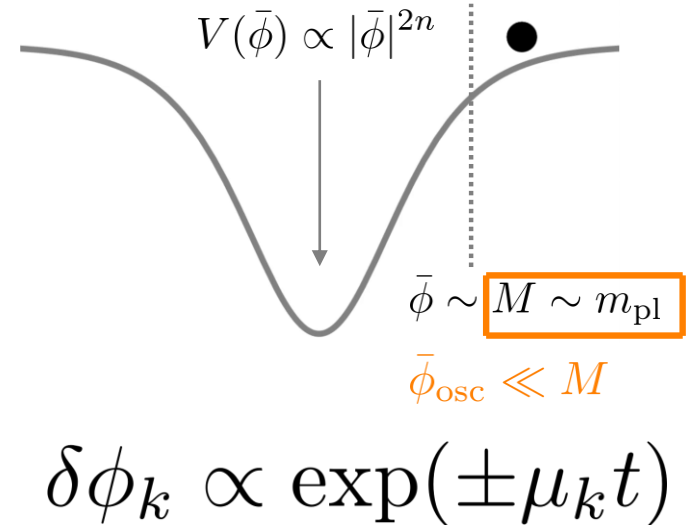
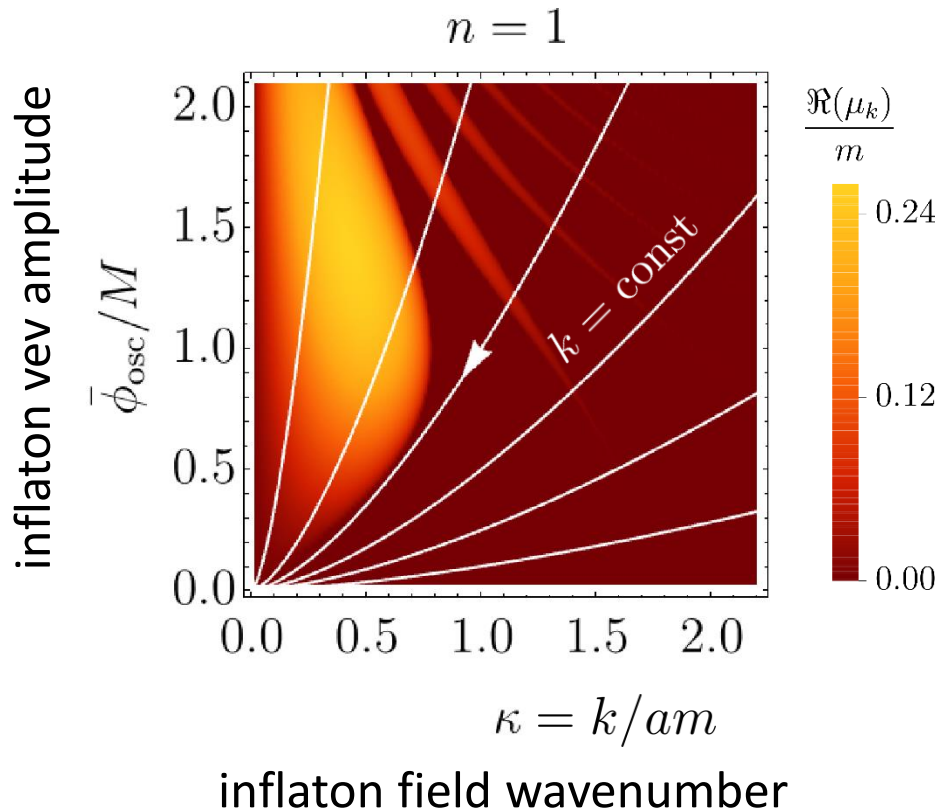
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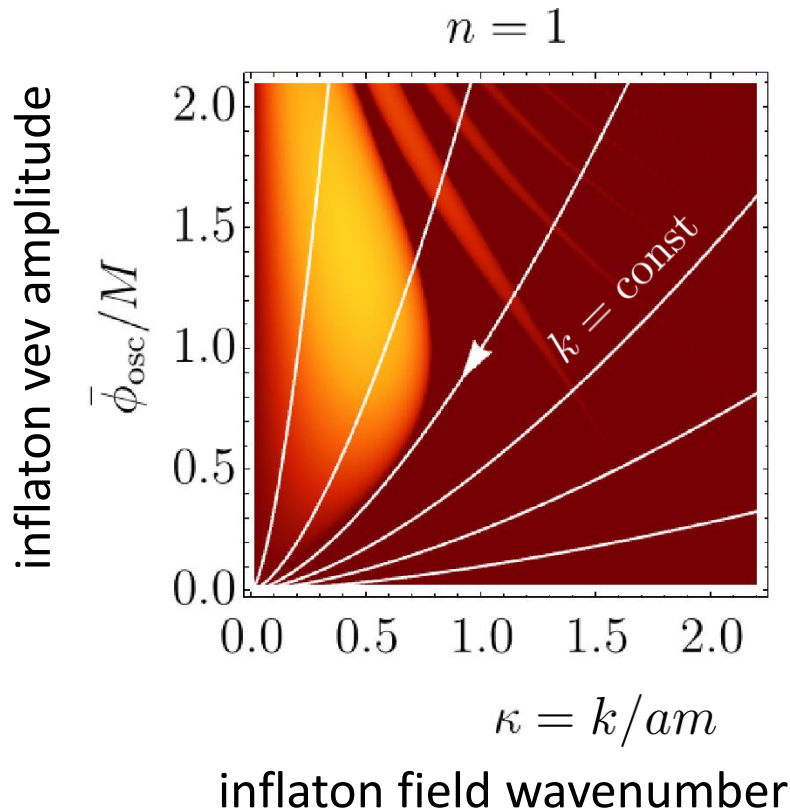
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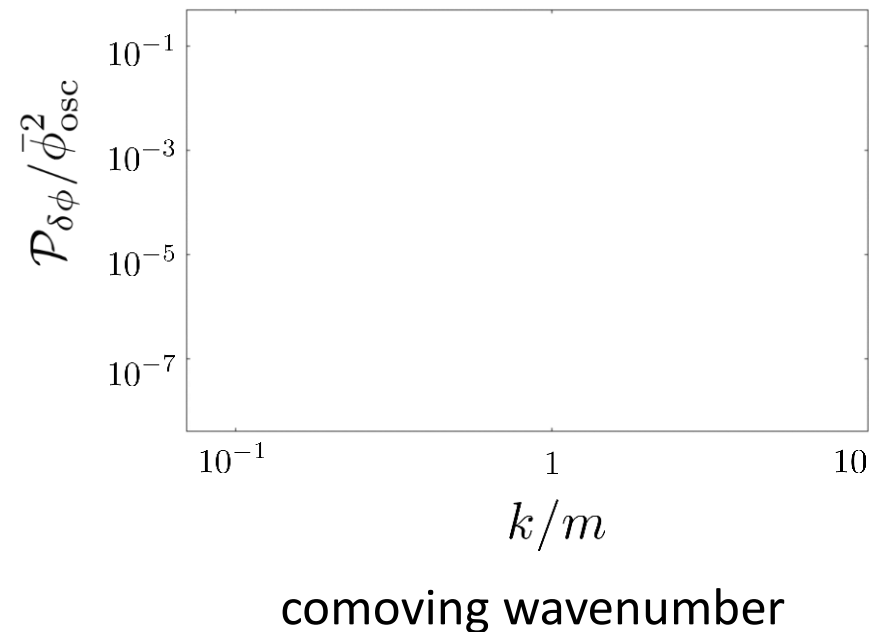
KL and M. Amin (2016)

Non-perturbative decay (parametric self-resonance)



Power spectrum:

$$\langle \delta\phi(x)^2 \rangle \equiv \int \mathcal{P}_{\delta\phi} d \ln k$$

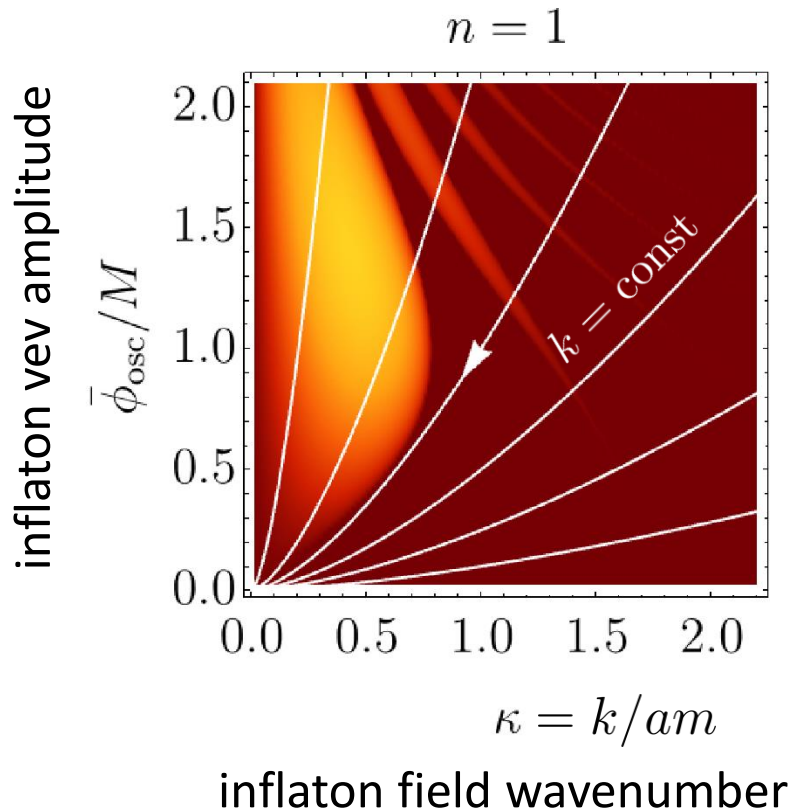


Matter domination?

$$n = 1$$

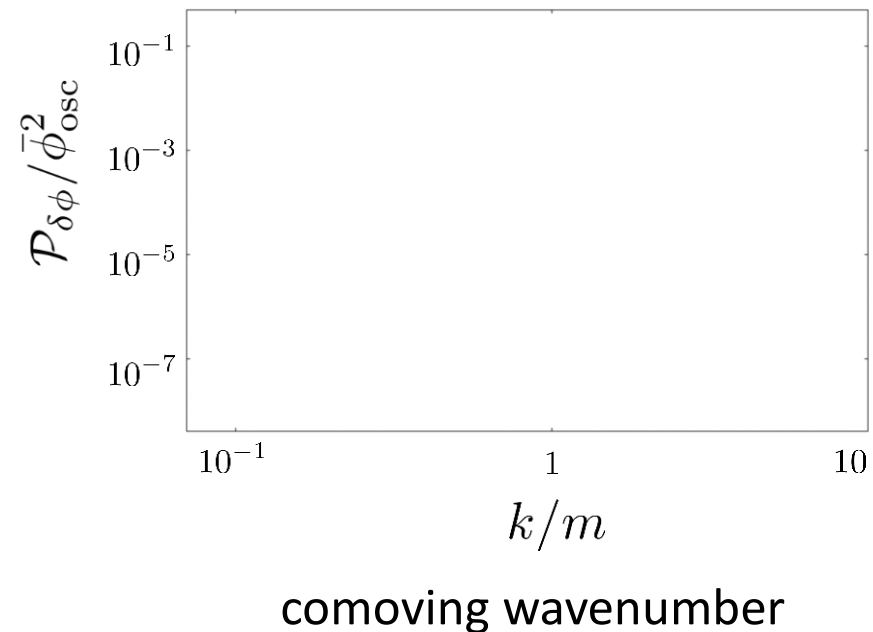
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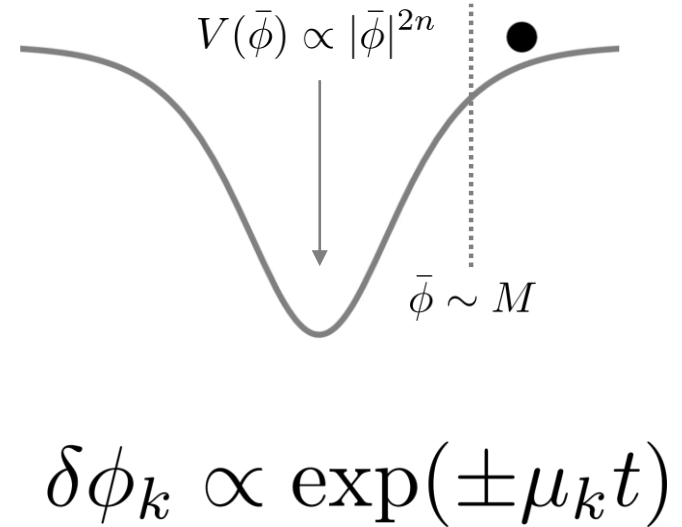
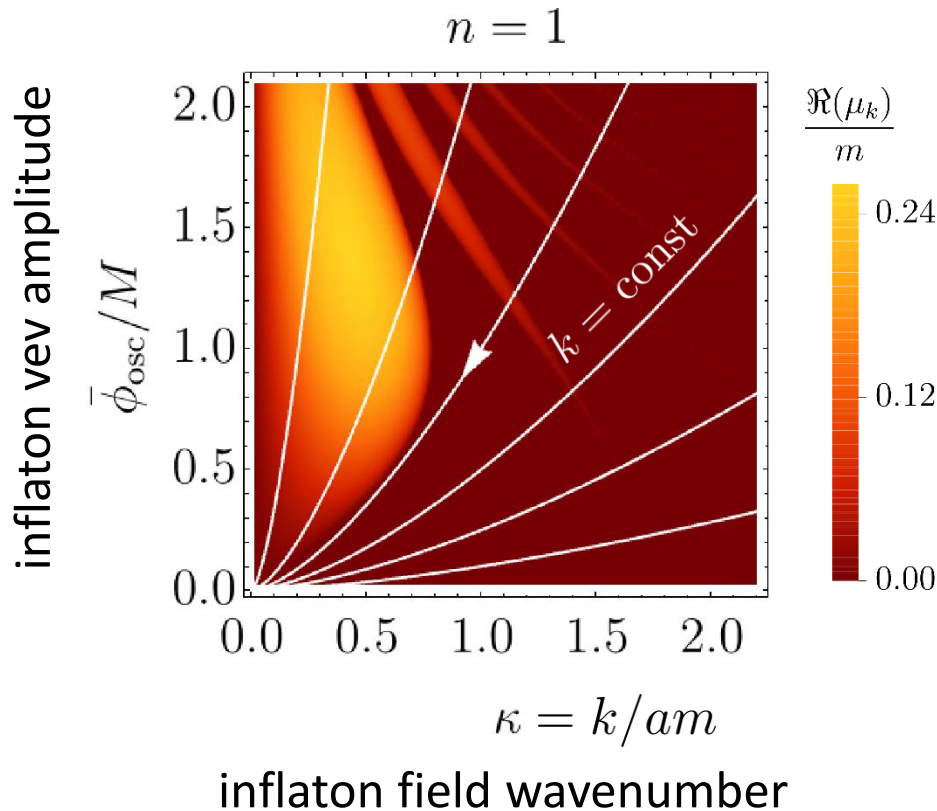


Matter domination?

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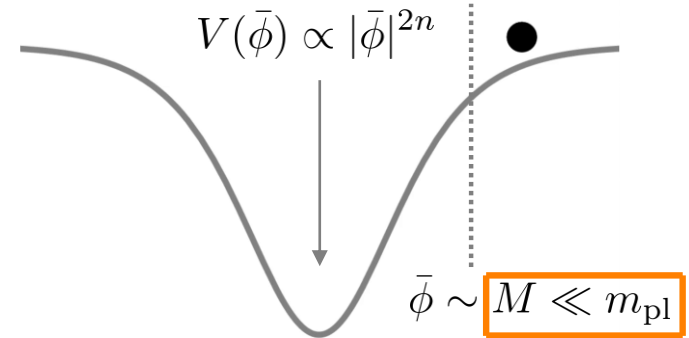
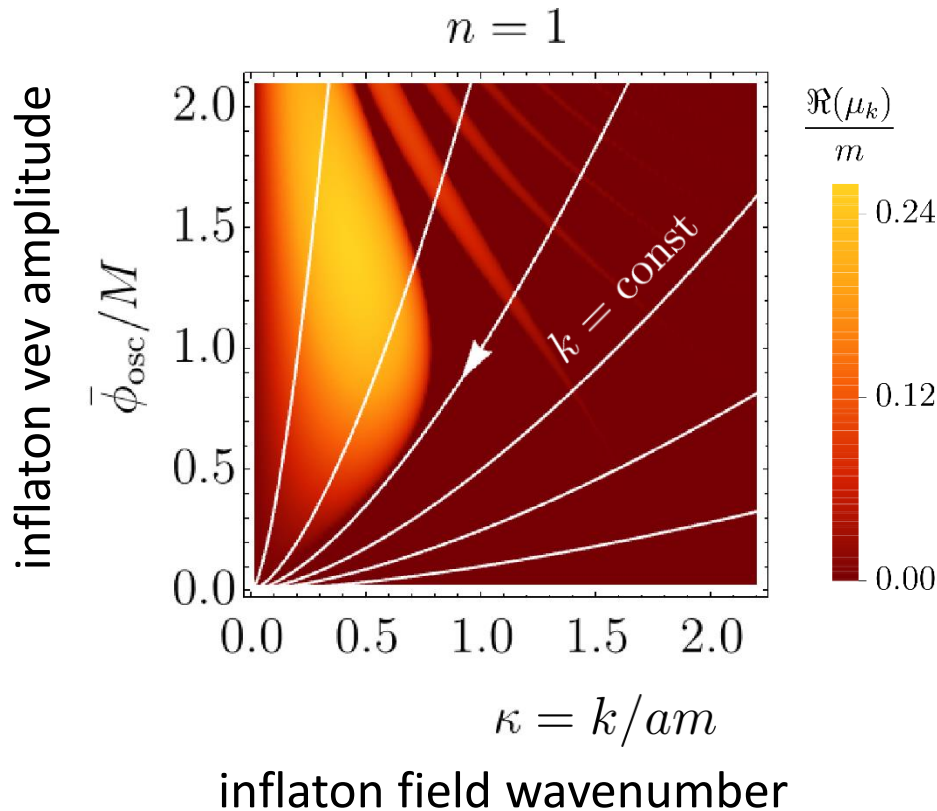
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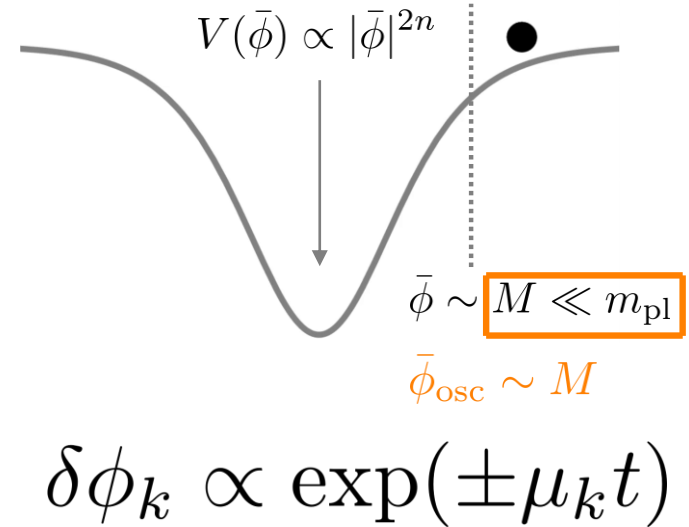
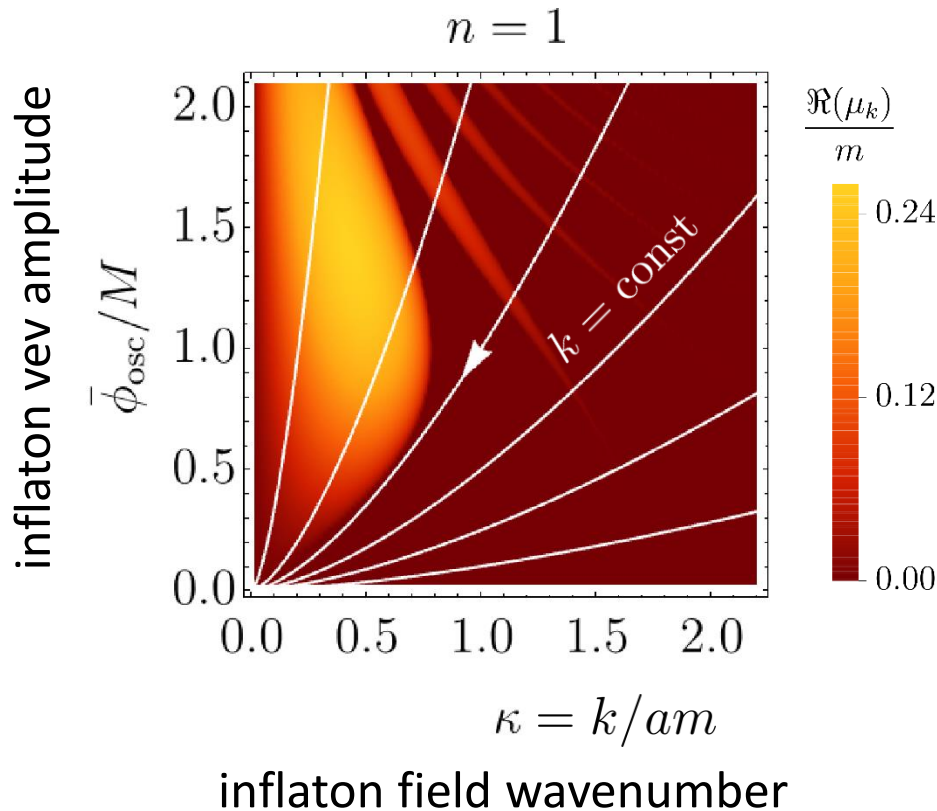
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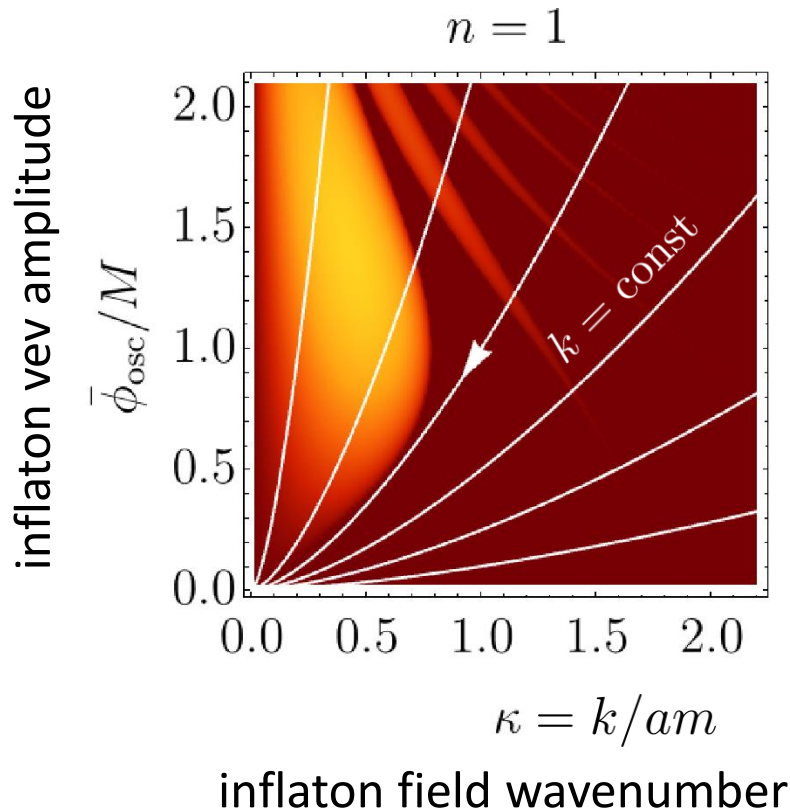
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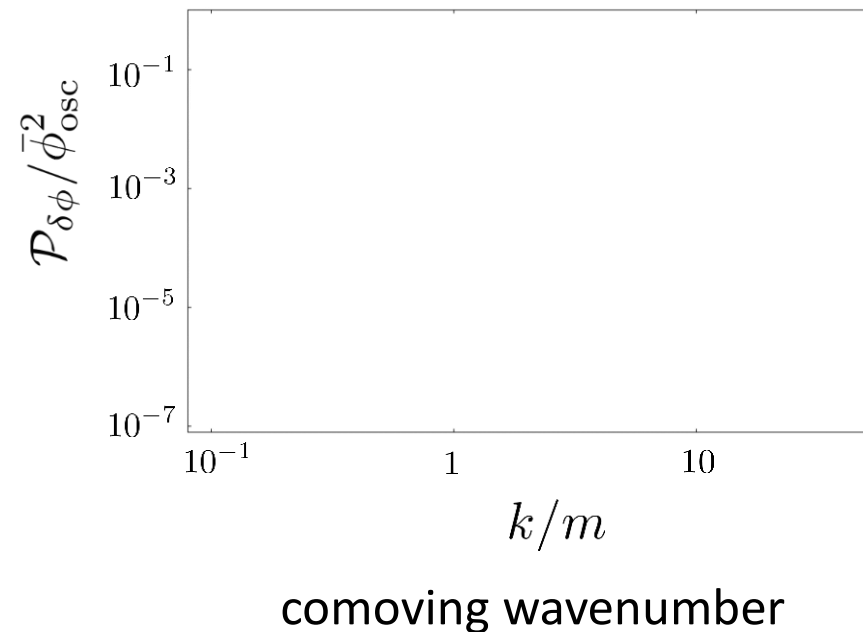
KL and M. Amin (2016)

Non-perturbative decay (parametric self-resonance)



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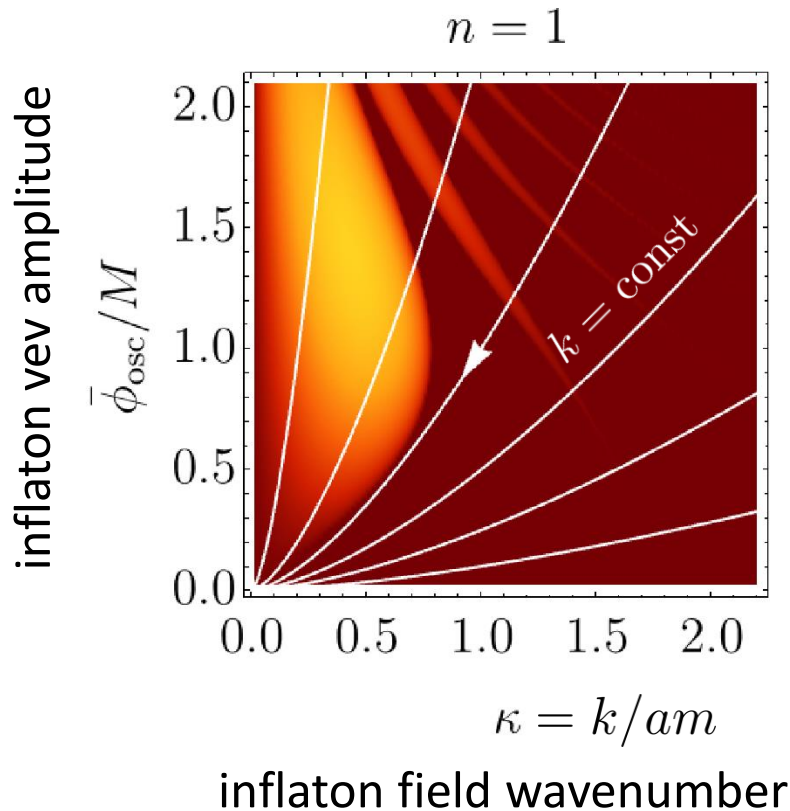


Matter domination?

$$n = 1$$

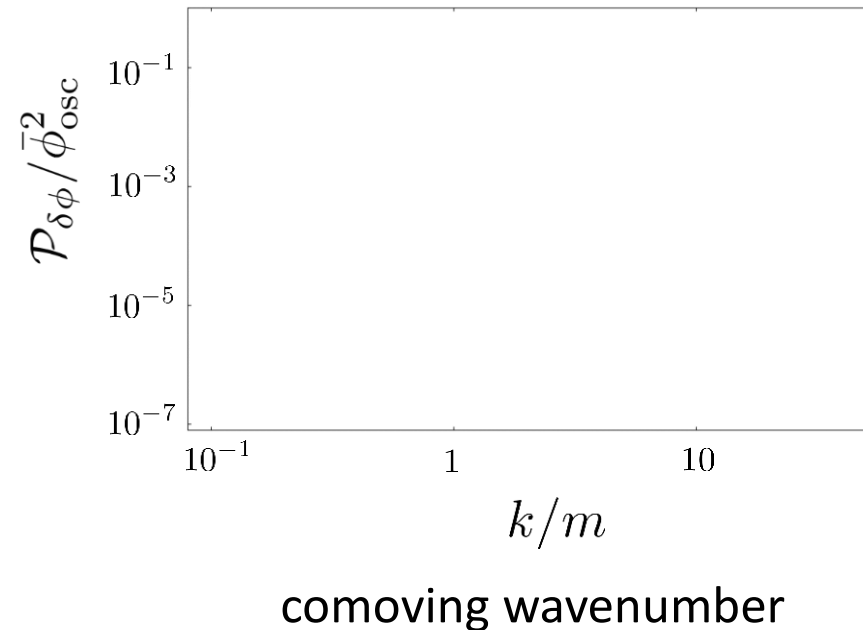
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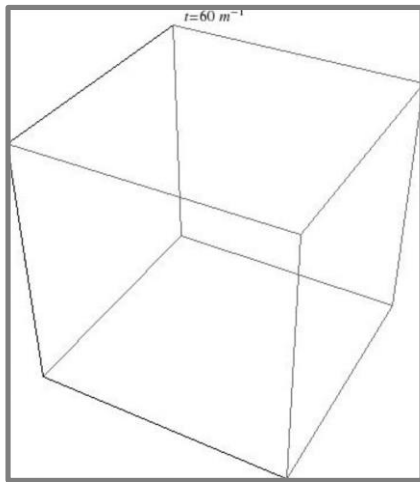


Matter domination?

$$M \ll m_{\text{pl}}$$

$$n = 1$$

$$M \sim m_{\text{pl}}$$



- $\delta\phi(t, \mathbf{x})$ production shut off
- $\bar{\phi}_{\text{osc}}(t) = \text{pressureless dust}$

- $\bar{\phi}$ forms oscillons (stable)

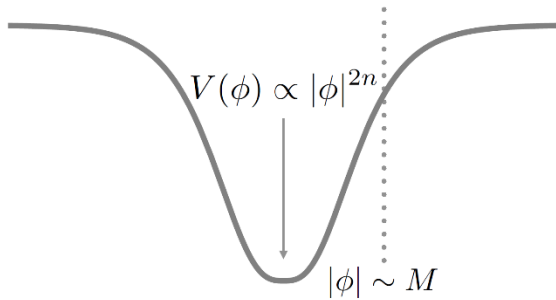
See also Amin, Hertzberg et al (2011),
Urakawa's talk, Kitajima's talk, Torrenti's talk

matter-like eos: $w = 0$

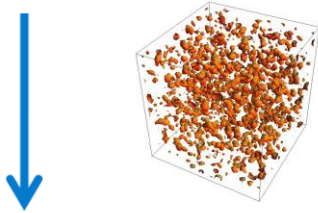
couplings to other fields?

See also Hertzberg (2010), Adshead et al (2015)

Summary



observationally
favored $V(\phi)$

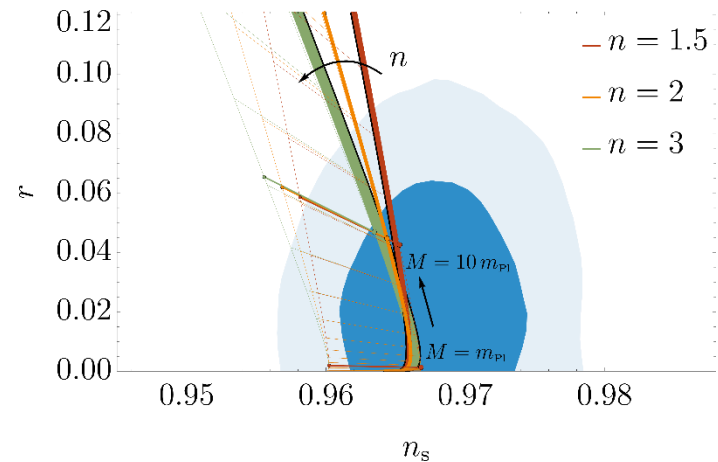


simple result

$$w = \begin{cases} 0 & \text{if } n = 1 \\ 1/3 & \text{if } n > 1 \end{cases} \quad (\text{even without couplings to other fields!})$$

(at sufficiently late times)

KL and M. Amin, PRD 97 023533 (2017)
KL and M. Amin, PRL 119 061301 (2016)



**Reduction in
theoretical uncertainty of
inflationary models**

Other connections ...

Other connections ...

- stochastic GWs from fragmentation

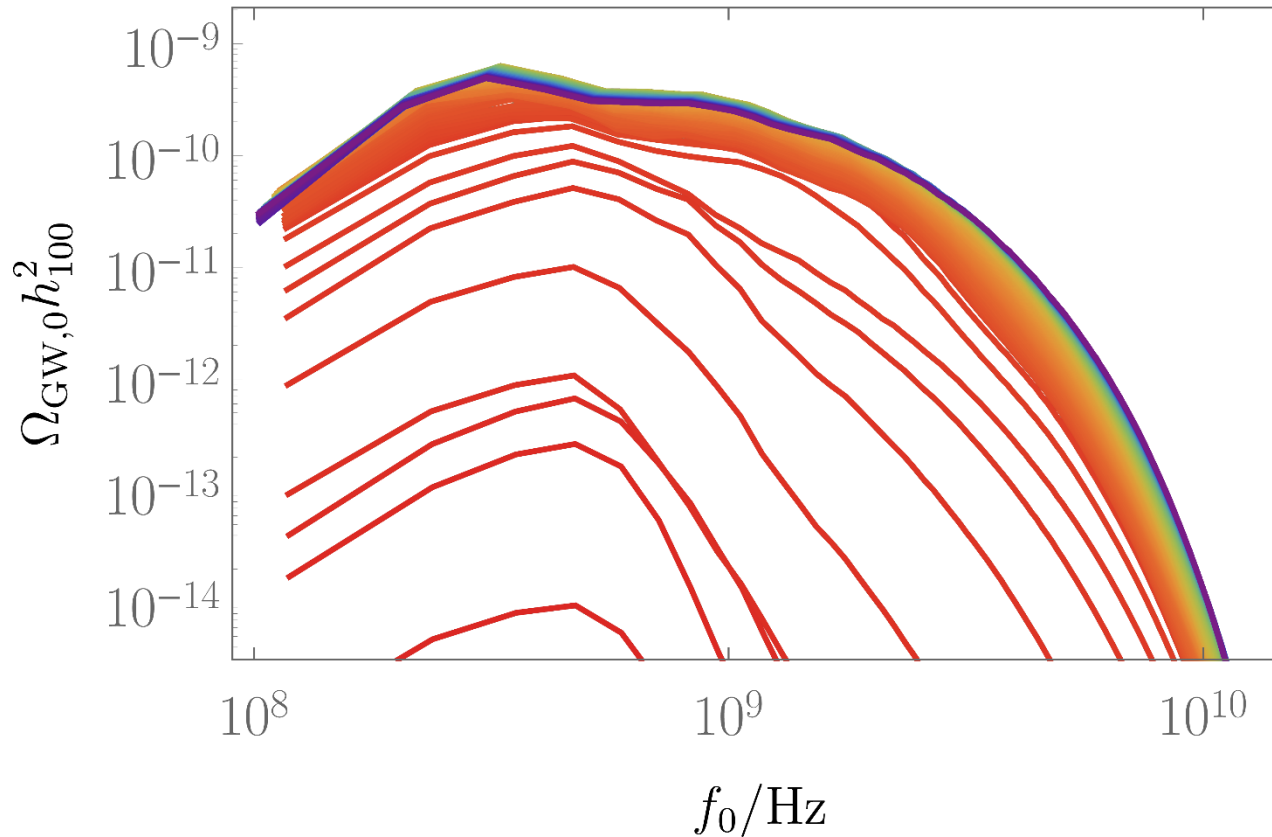
KL and M. Amin (2019)

Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

Oscillons

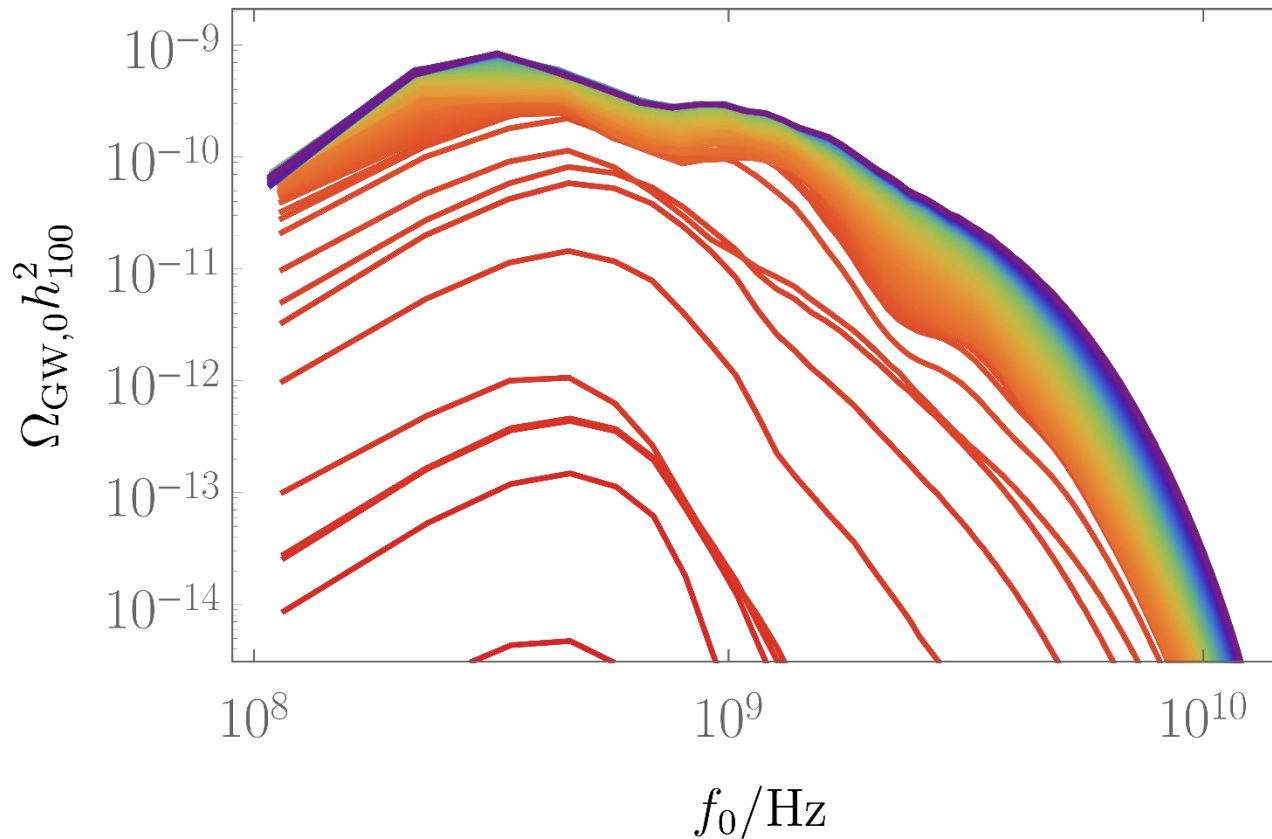


Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

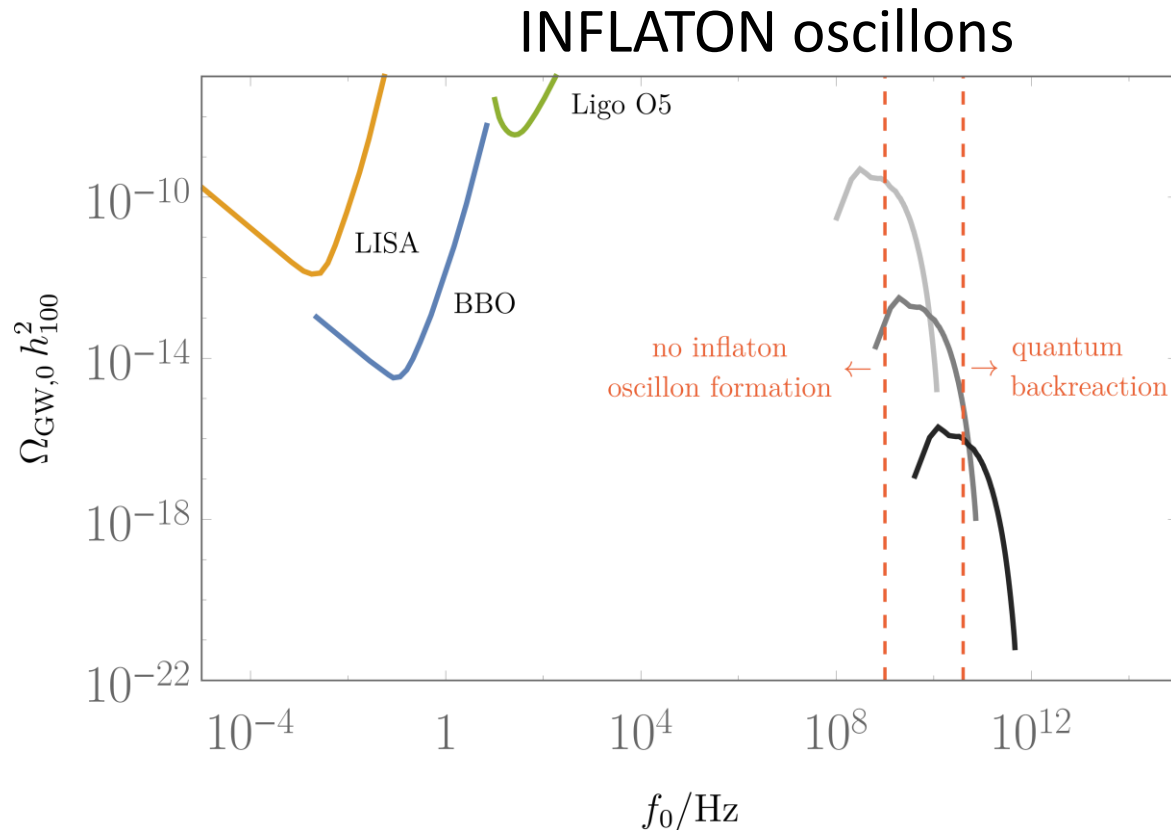
Transients



Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

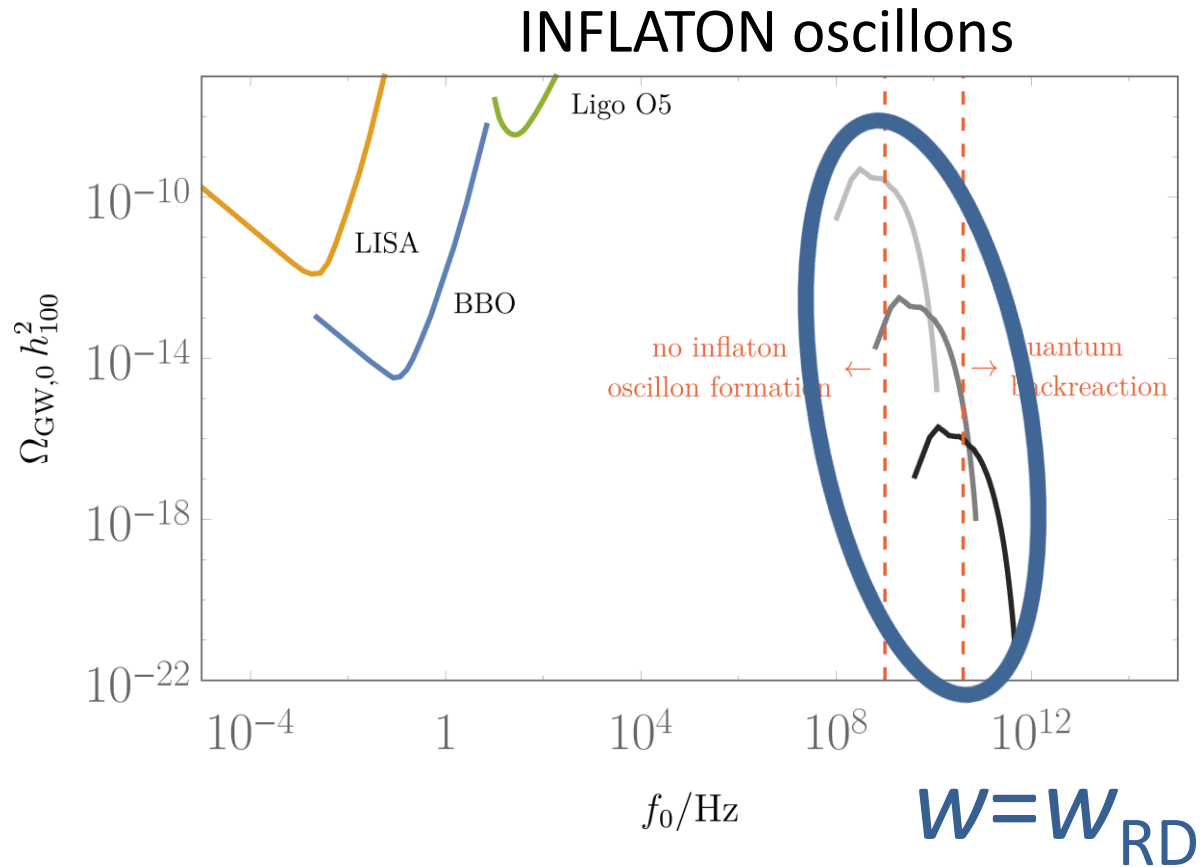


See also Antusch et al (2016), Soda and Urakawa (2017), Kitajima, Soda and Urakawa (2018)

Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

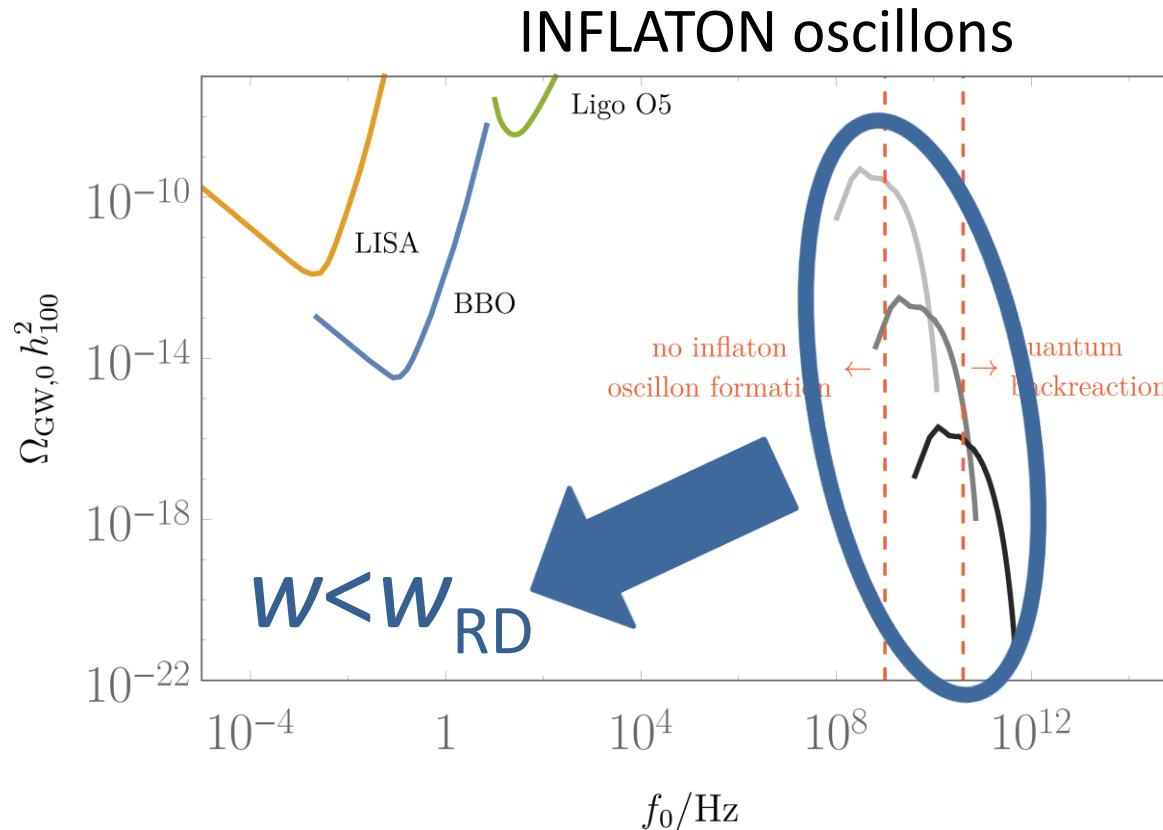


See also Antusch et al (2016), Soda and Urakawa (2017), Kitajima, Soda and Urakawa (2018)

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KL and M. Amin (2019)

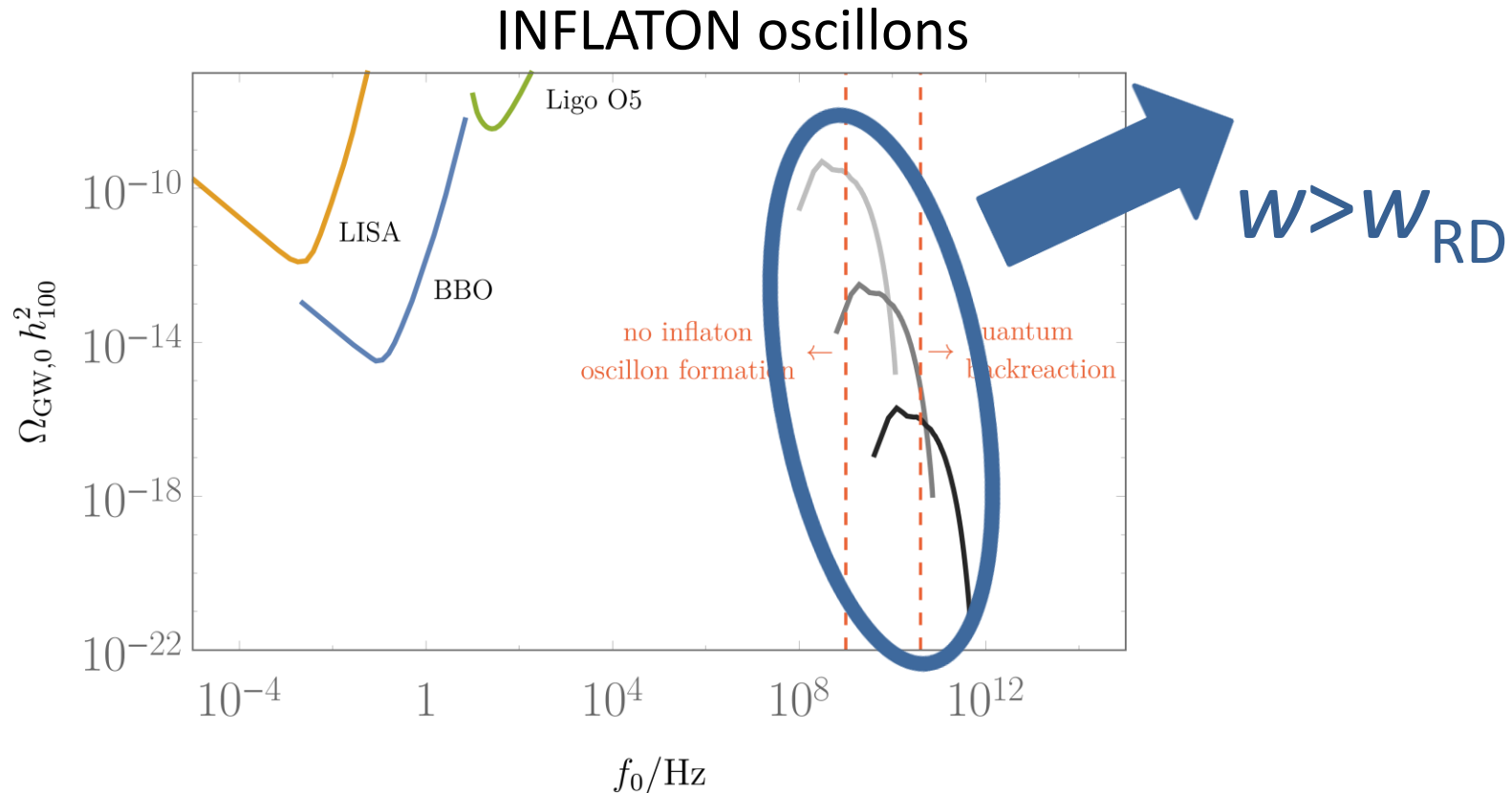


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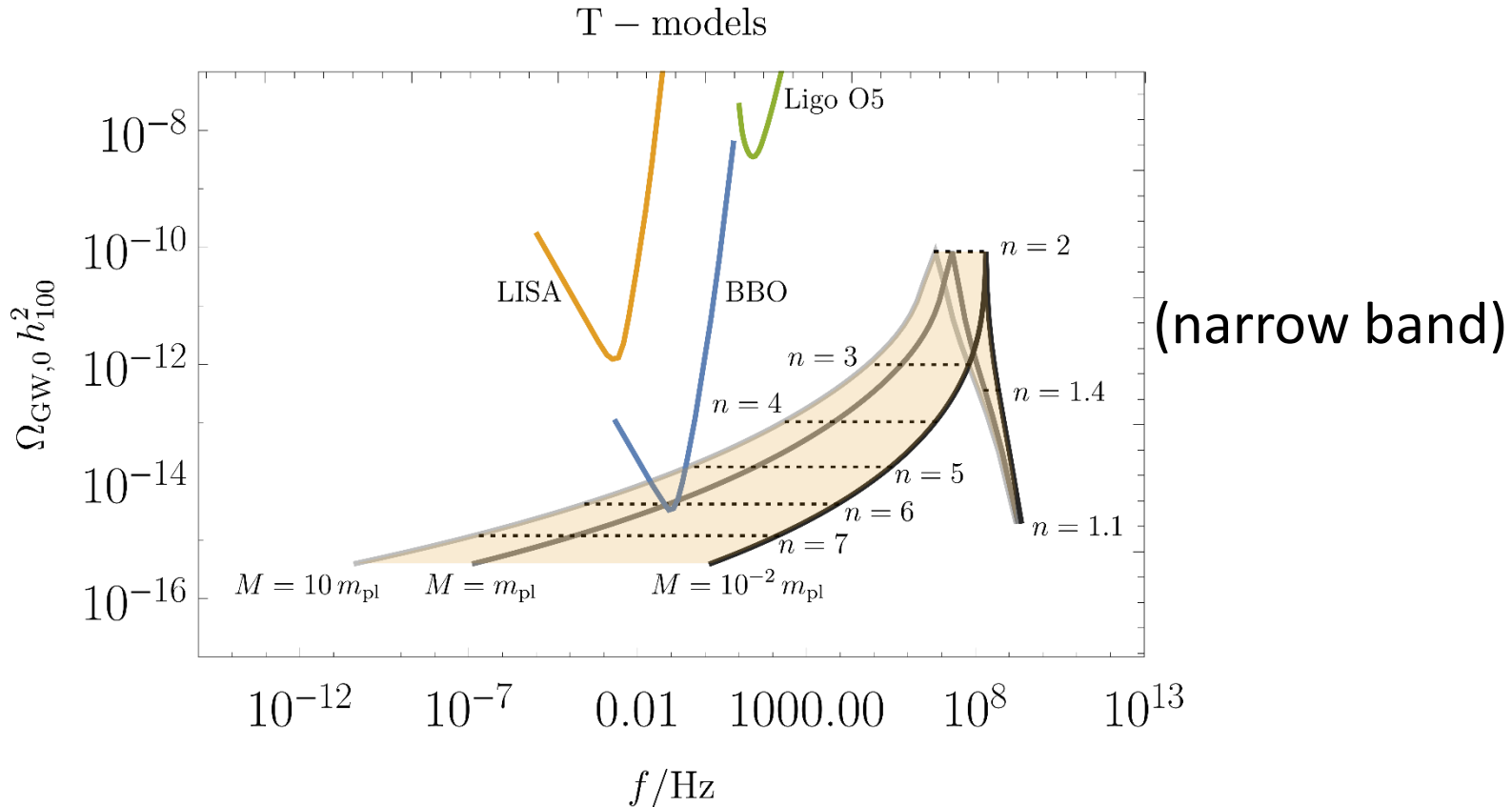


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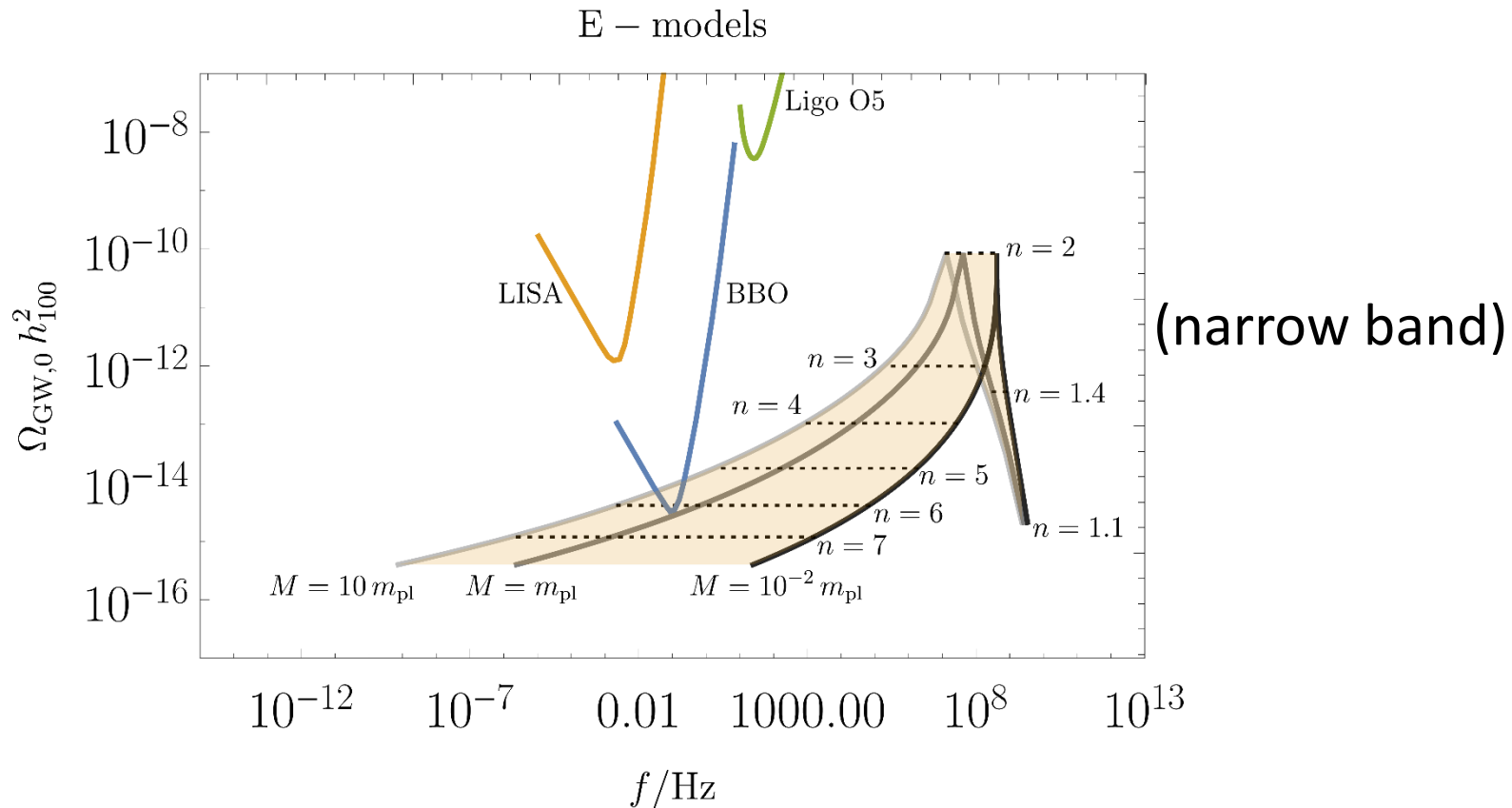
KL and M. Amin (2019)



Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

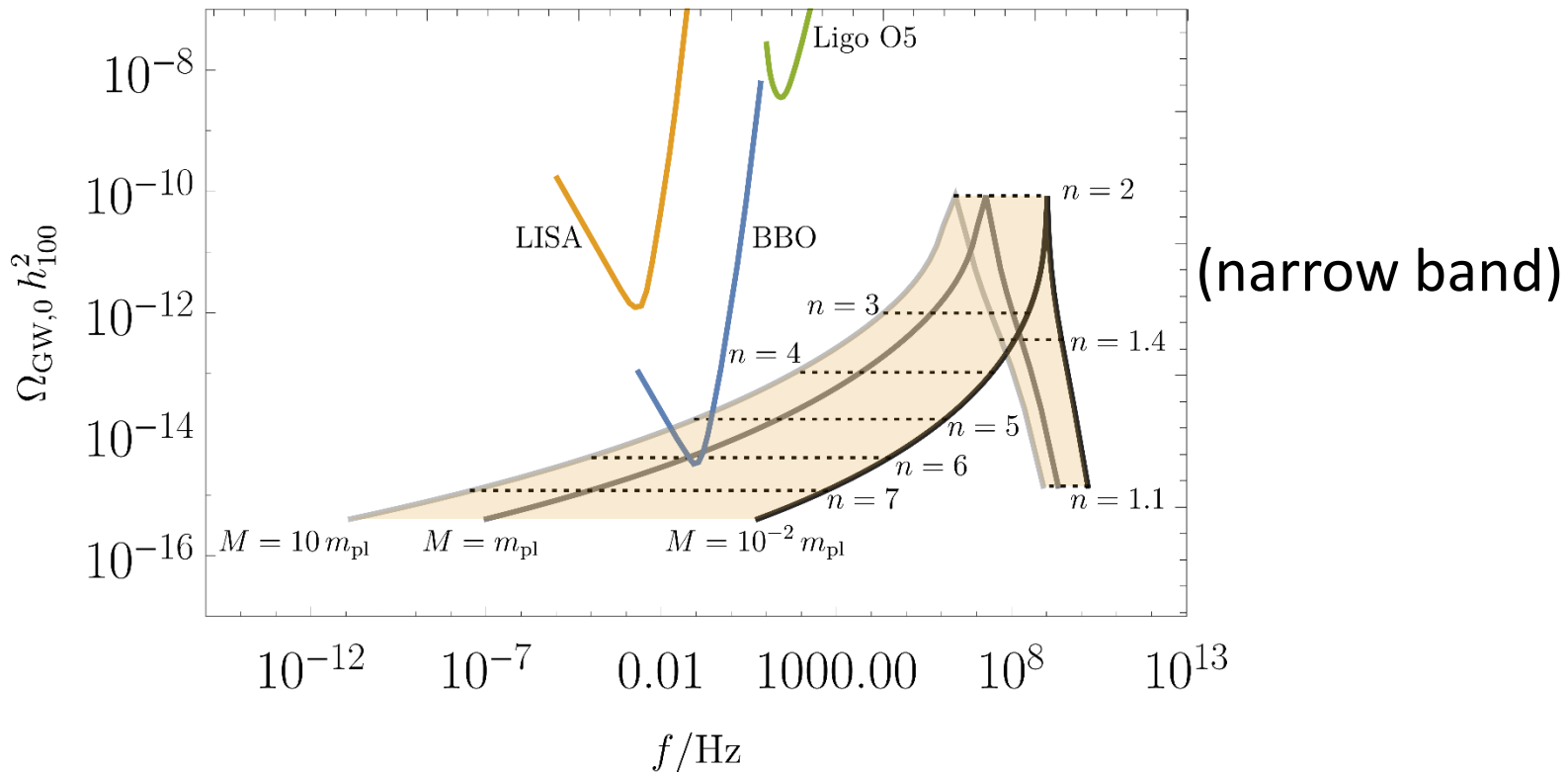


Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

Monodromy $q = 0.5$

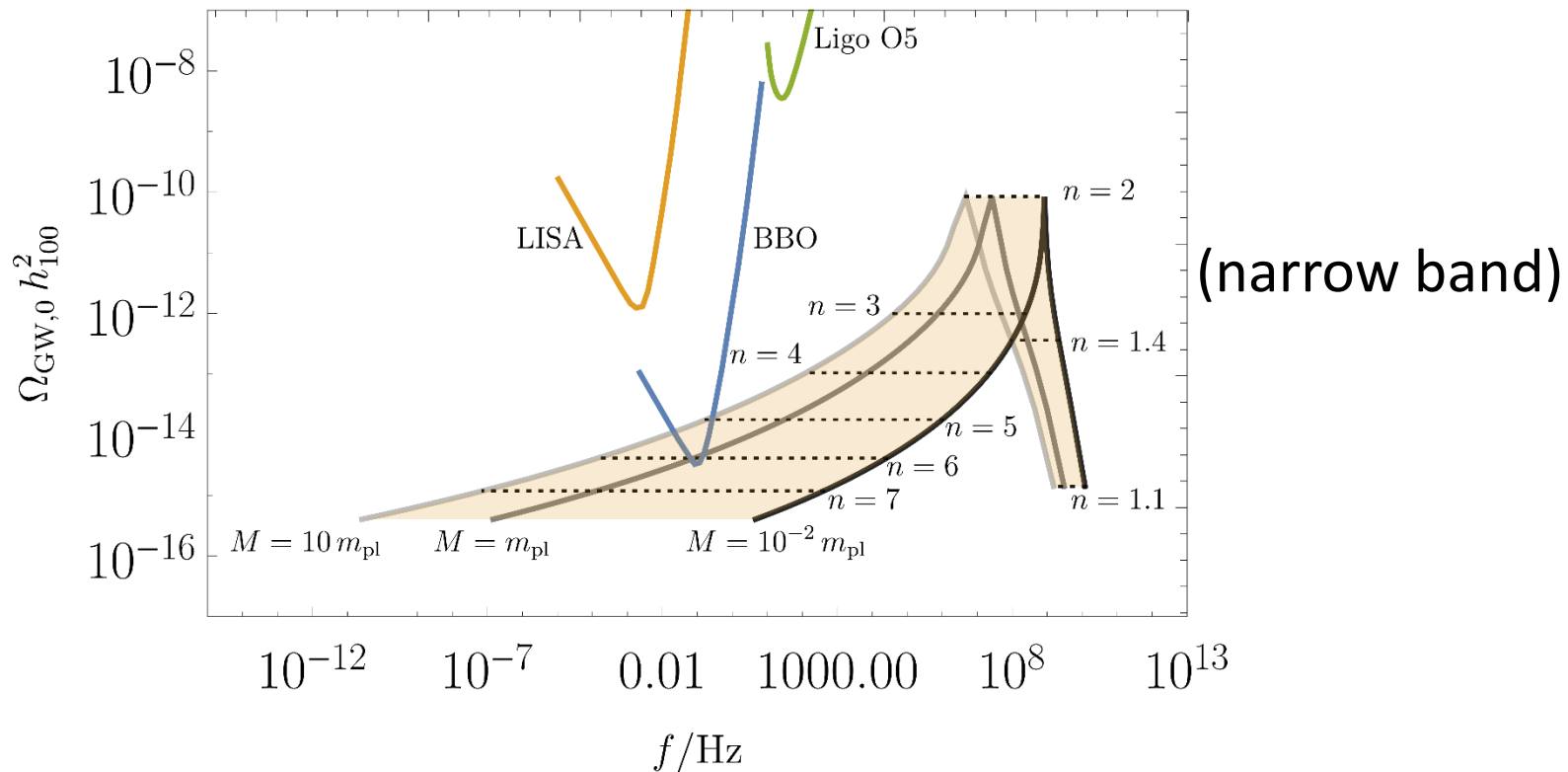


Other connections ...

- stochastic GWs from fragmentation

KL and M. Amin (2019)

Monodromy $q = 1$



Other connections ...

- stochastic GWs from fragmentation KL and M. Amin (2019)
- dark energy P. Agrawal, L. Randall, et al (2019)

Other connections ...

- stochastic GWs from fragmentation KL and M. Amin (2019)
- dark energy P. Agrawal, L. Randall, et al (2019)
- dark matter

Other connections ...

- stochastic GWs from fragmentation KL and M. Amin (2019)
- dark energy P. Agrawal, L. Randall, et al (2019)
- dark matter
- matter-antimatter asymmetry... KL and M. Amin (2014)

Oscillons and matter-antimatter asymmetry

KL and M. Amin, PRD 90, 083528 (2014)

Main idea

complex
inflaton ϕ
+ ~~U(1)~~



dynamics at the end of inflation

inflaton/anti-inflaton
asymmetry



decay

matter-antimatter
asymmetry

$$\eta \approx 6 \times 10^{-10}$$

The model

A variation of the Affleck-Dine Mechanism (1985)
Hertzberg & Karouby (2013, 2014)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} + |\partial\phi|^2 - V(\phi, \phi^*) \right]$$

$$V(\phi, \phi^*) = V_s(|\phi|) + V_b(\phi, \phi^*)$$



respects U(1) symmetry

responsible for inflation



breaks U(1) symmetry

responsible for generating
inflaton/antiinflaton asymmetry

$$V_b(\phi, \phi^*) = \frac{c_n}{n} (\phi^n + \phi^{*n})$$

“small” symmetry breaking

- technically natural
- small during inflation
- small long after inflation

Inflaton asymmetry – baryon asymmetry

$$\Delta N_\phi = N_\phi - N_{\bar{\phi}} = i \int d^3x a^3 (\phi^* \dot{\phi} - \dot{\phi}^* \phi)$$

inflaton number (**not conserved!**)

- generated at end of inflation

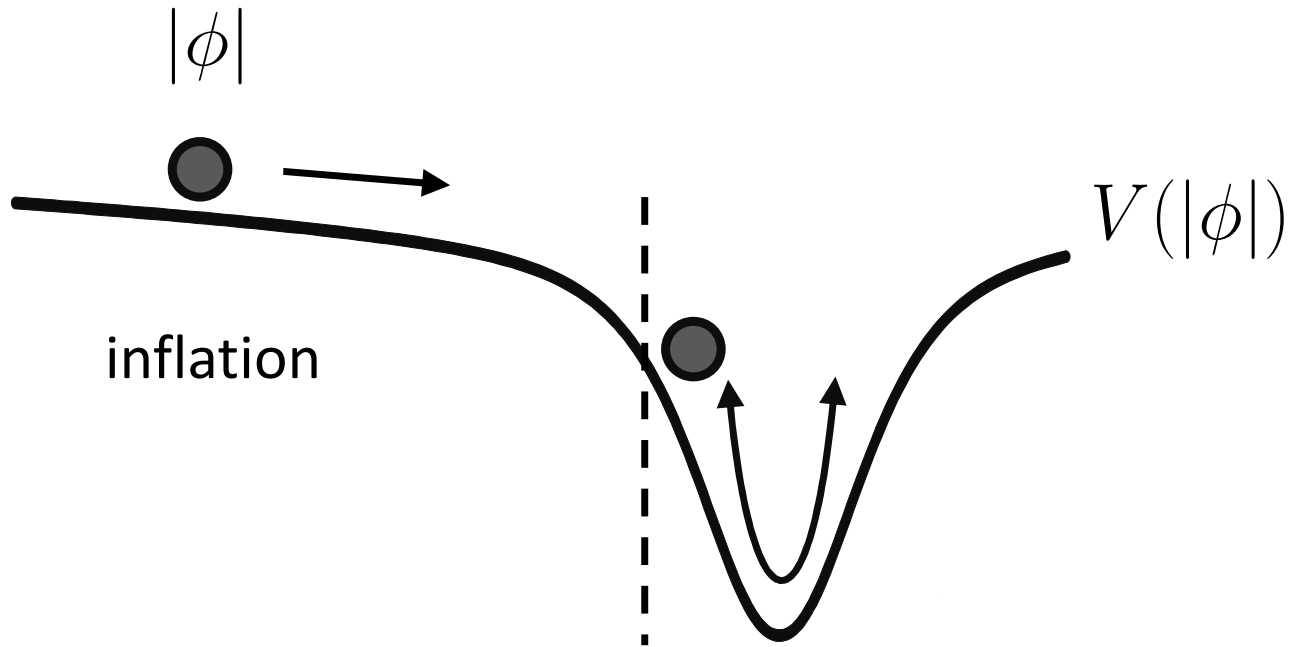
$$\phi \rightarrow b$$

decay

$$N_b - N_{\bar{b}} = b_\phi (N_\phi - N_{\bar{\phi}})$$

baryon number

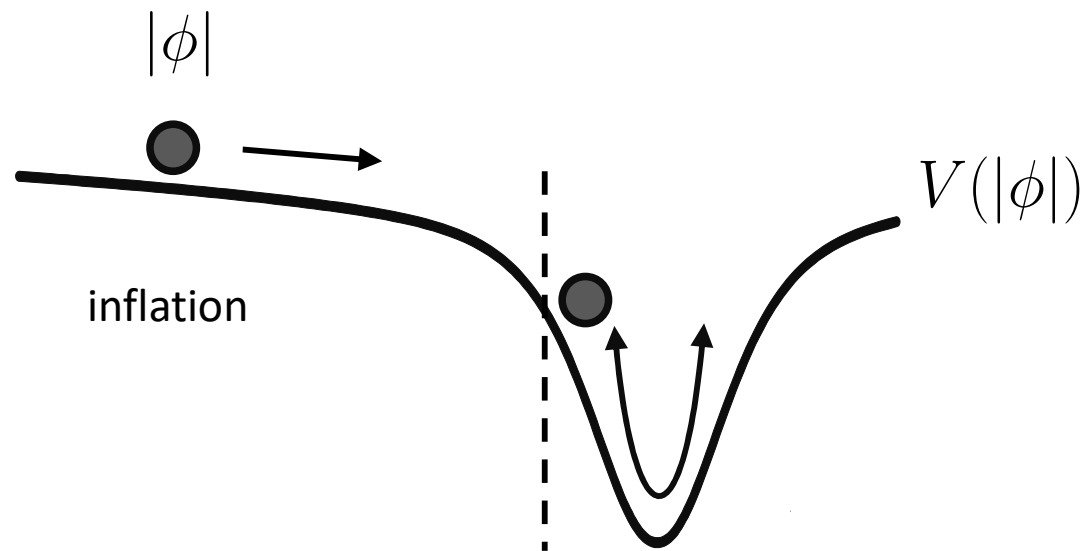
Inflaton dynamics



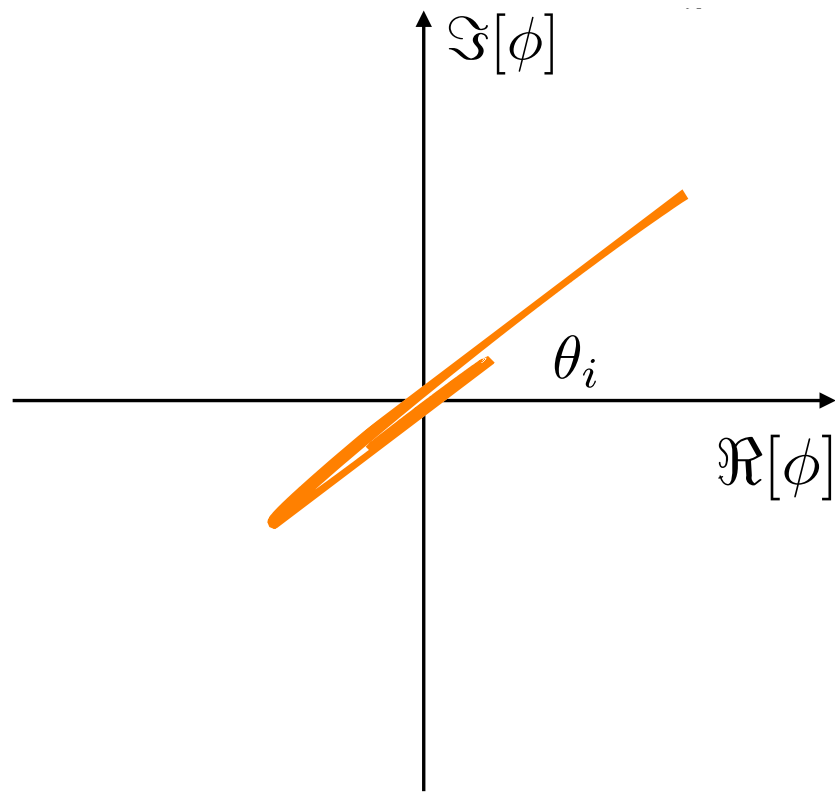
inflation

inflation ends:
oscillatory phase

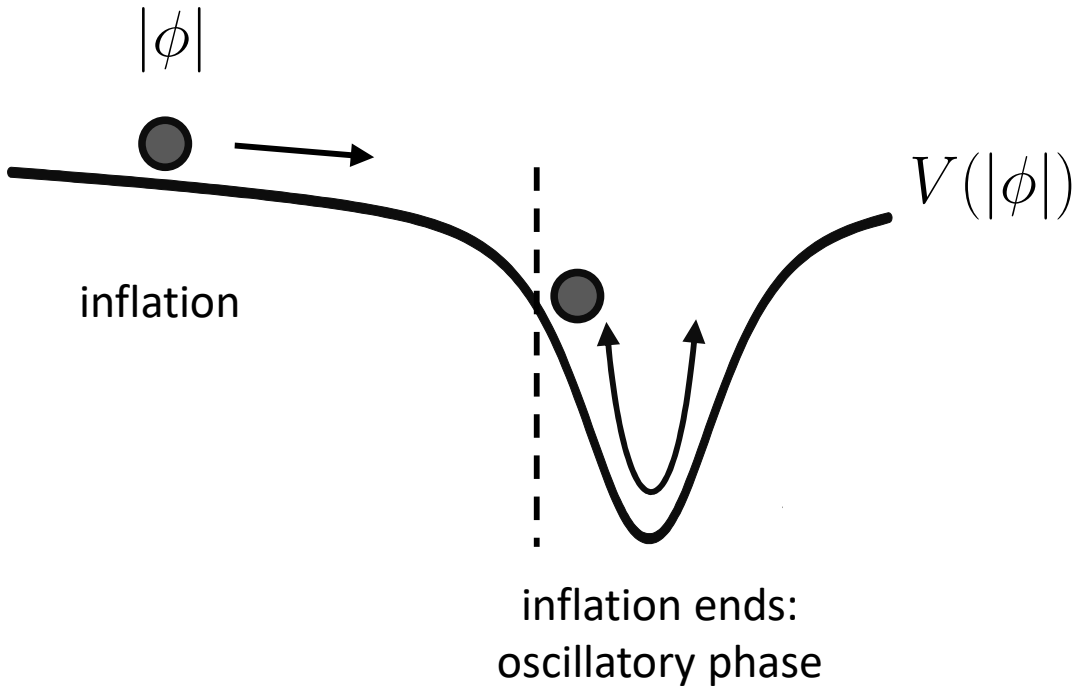
Inflaton (homogeneous) dynamics



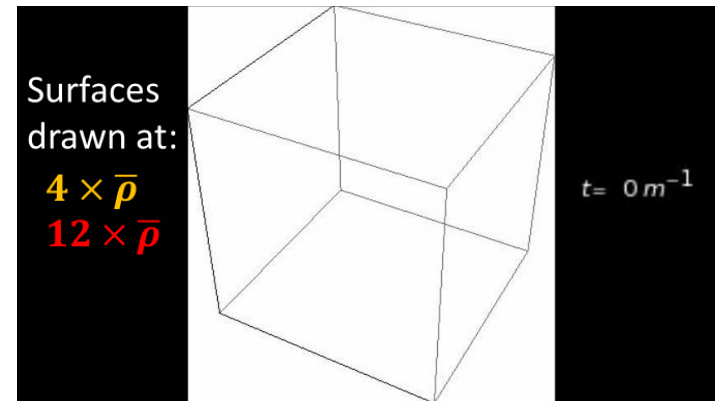
$$|\phi(t)| \approx \frac{|\phi_0|}{a(t)^{3/2}} \sin(mt)$$



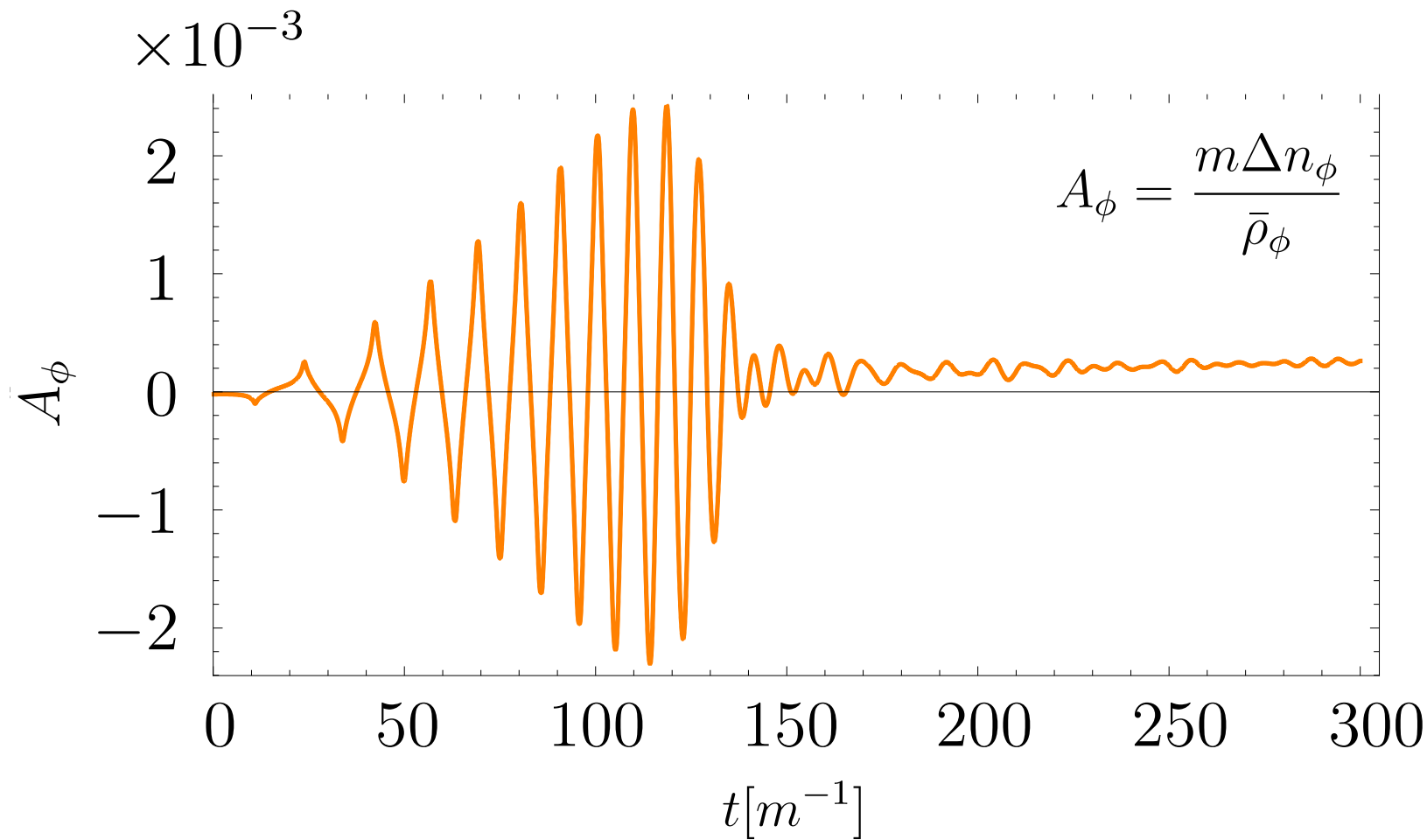
Inflaton (actual) dynamics



- parametric resonance of $\delta\phi$
- ϕ fragments
- forms oscillons

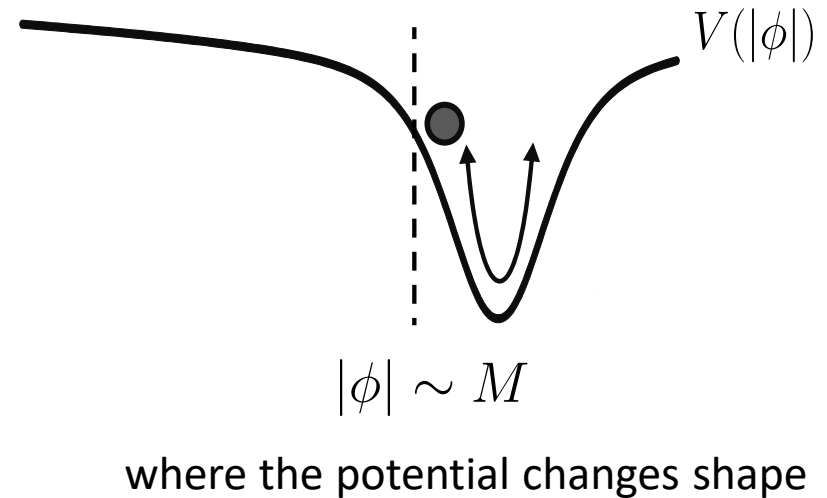
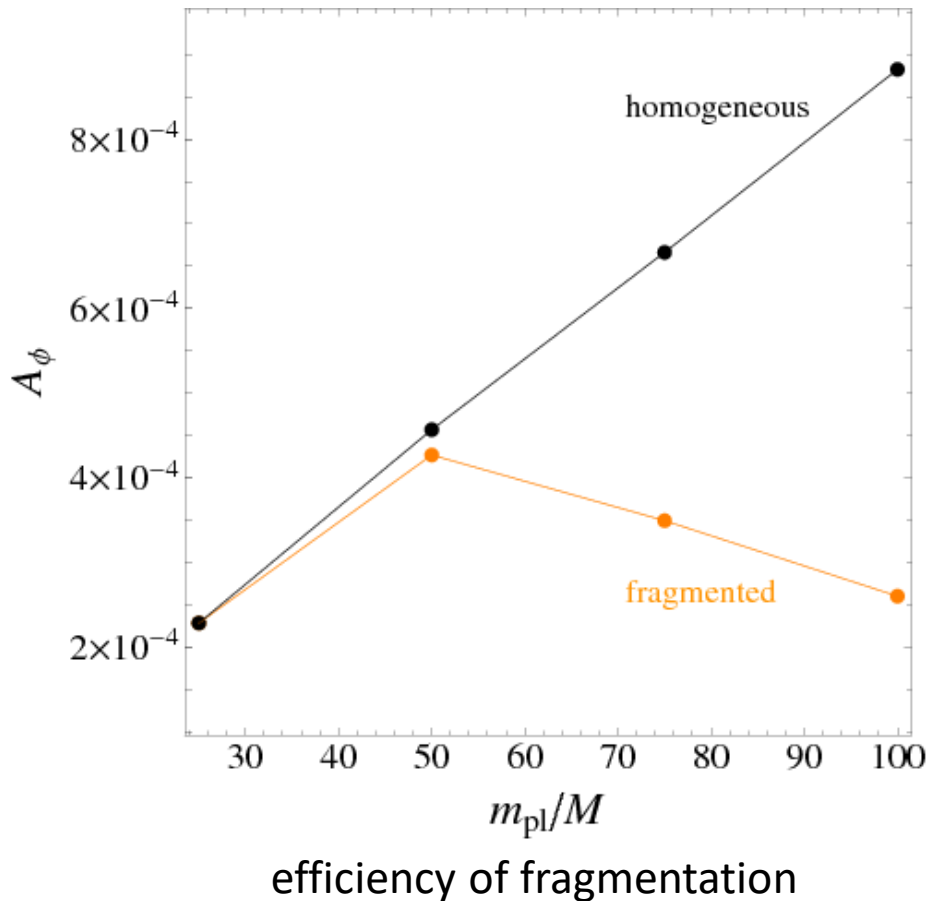


Inflaton asymmetry

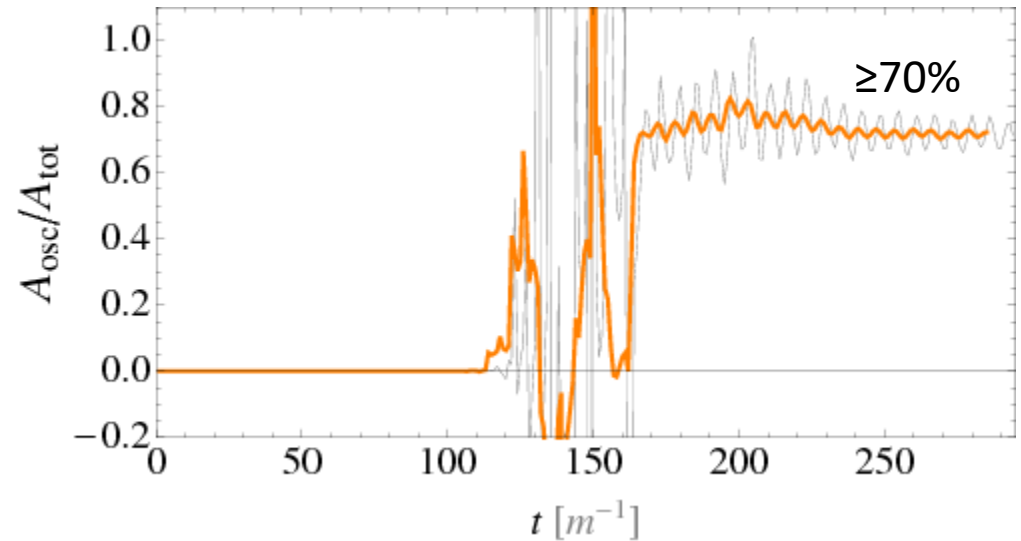
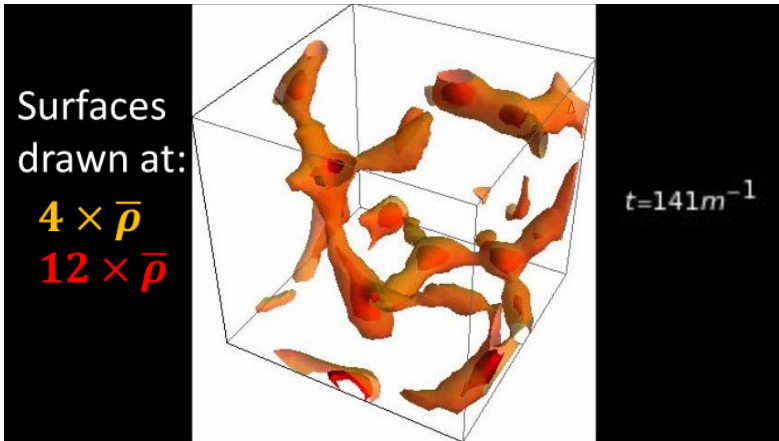


Asymmetry-fragmentation

Non-linear structures DO AFFECT inflaton/anti-inflaton ASYMMETRY!



Where is the inflaton/anti-inflaton ASYMMETRY?

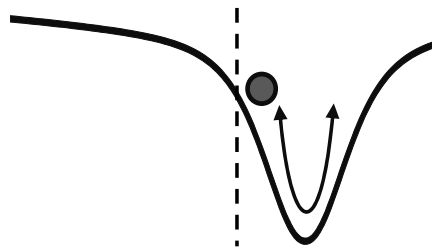


More than 70% of ASYMMETRY locked in oscillons!

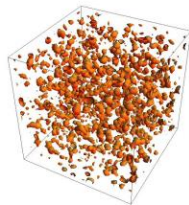
Inflaton asymmetry – parameter dependence

$$A_\phi \sim \mathcal{O}(10^2) \times \left(\frac{M}{m_{\text{Pl}}} \right) c_3^2 \sin 3\theta_i$$

(inverse) strength of instability



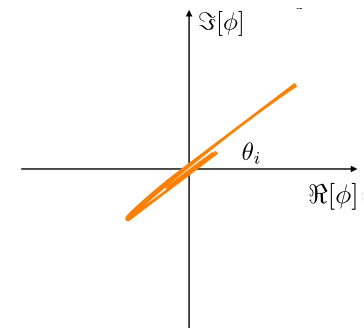
$$|\phi| \sim M$$



symmetry breaking

$$V_b(\phi, \phi^*) = \frac{c_3}{3} (\phi^3 + \phi^{*3})$$

initial conditions-inflation



$$c_3 \ll 1, M \ll m_{\text{Pl}}$$

Inflaton to baryons (qualitative)

$$\eta \sim \mathcal{O}(10^2) \times A_\phi \left(\frac{T_{\text{reh}}}{m} \right)$$

from end of inflation

decay rate to baryons

caveats: uncertainty here!! particle physics details, inhomogeneous decay...

Inflaton to baryons (qualitative)

$$\eta \sim \mathcal{O}(10^2) \times A_\phi \left(\frac{T_{\text{reh}}}{m} \right) \sim 10^{-9}$$

from end of inflation

decay rate to baryons

sample numbers: $A_\phi \sim 10^{-4}$, $T_{\text{reh}} \sim 10^7 \text{ GeV}$, $m \sim 10^{14} \text{ GeV}$

caveats: uncertainty here!! particle physics details, inhomogeneous decay...

Summary

KL and M. Amin, PRD 90, 083528 (2014)

complex
inflaton ϕ
+ ~~$U(1)$~~



dynamics at the end of inflation

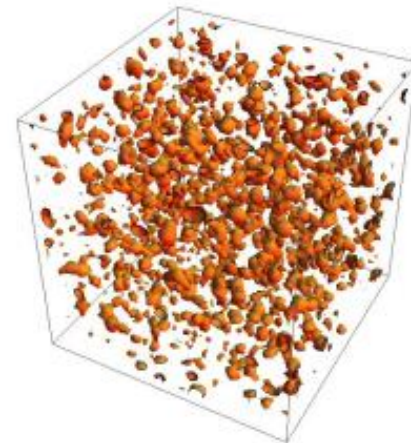
inflaton/anti-inflaton
asymmetry



decay

matter-antimatter
asymmetry

$$\eta \approx 6 \times 10^{-10}$$



very different dynamics from homogeneous case!

Gauge fields, inflation & reheating

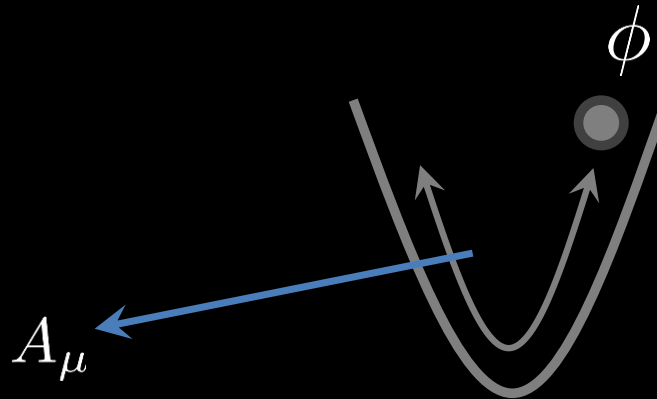
KL and M. Amin, JCAP 1606 032 (2016)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - (D_\mu \phi)^\dagger D^\mu \phi - V(|\phi|) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} \right]$$

Gauge fields, inflation & reheating

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Gauge fields, inflation & reheating

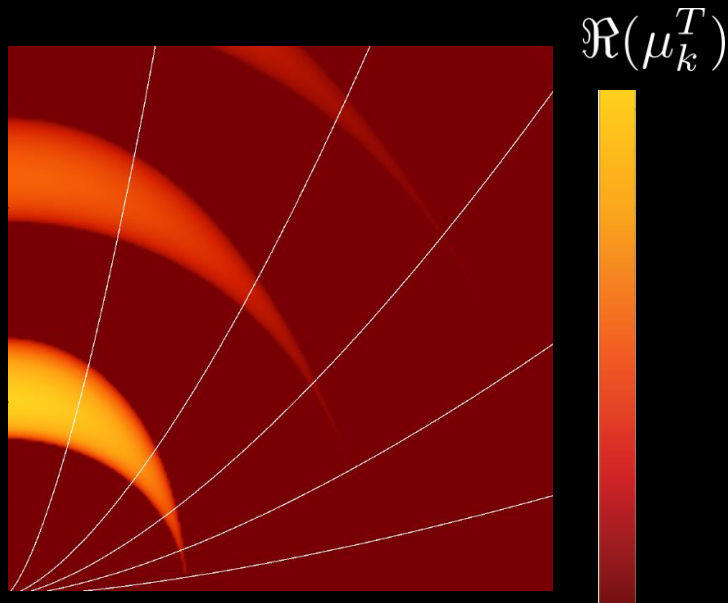
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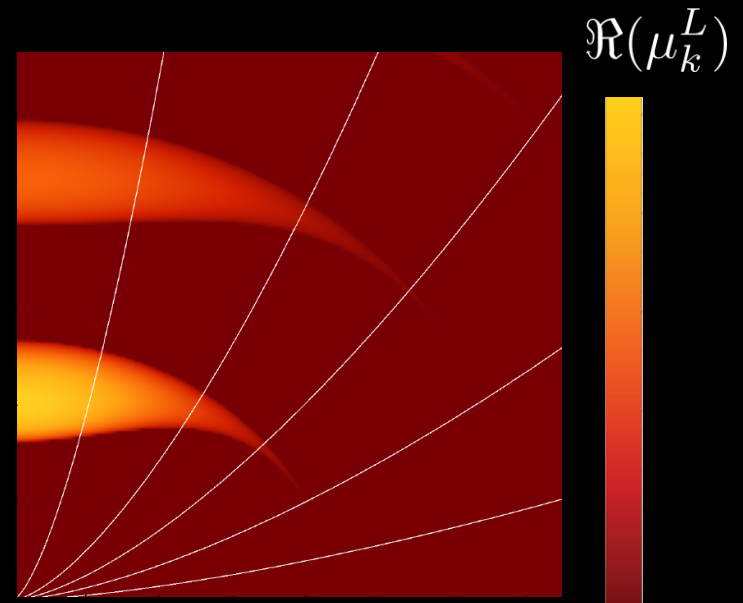
$$A_k^T \propto \exp(\pm \mu_k^T t)$$

$$A_k^L \propto \exp(\pm \mu_k^L t)$$

inflaton amplitude



wavenumber



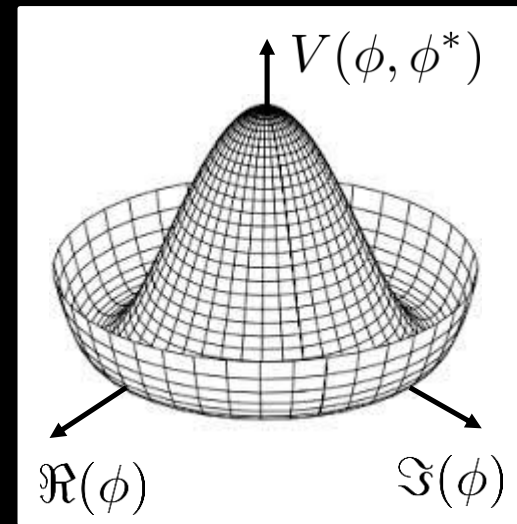
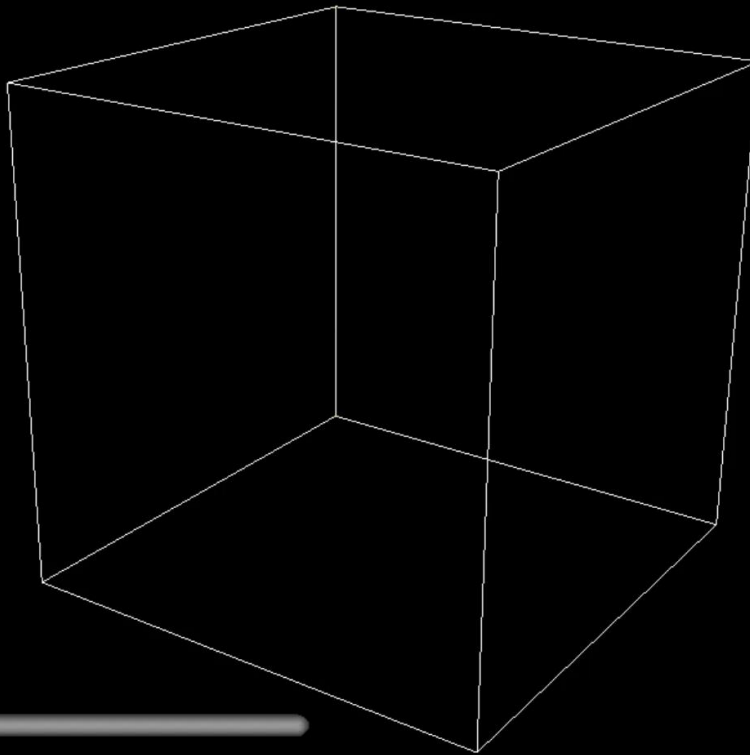
wavenumber

Gauge fields, inflation & reheating

KL and M. Amin, JCAP 1606 032 (2016),
see also Yamaguchi's and Torrenti's talks

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - (D_\mu \phi)^\dagger D^\mu \phi - V(|\phi|) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} \right]$$

(in progress)



with Eiichiro Komatsu and Mustafa Amin

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} - \frac{\phi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \right]$$

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} - \frac{\phi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \right]$$

Non-trivial vevs:

Gauge fields, inflation & reheating

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Non-trivial vevs:

$$\bar{\phi}(t)$$

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Non-trivial vevs:

$$\begin{aligned} & \bar{\phi}(t) \\ \bar{A}_i^b(t) &= a(t) Q(t) \delta_i^b \end{aligned}$$

See also Maleknejad (2011)

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} - \frac{\phi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \right]$$

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Drive inflation

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Drive inflation
(+extensions)

Adshead et al (2016, 2017)

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Drive inflation
(+extensions)

Spectator sector

Adshead et al (2016, 2017)

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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See also Maleknejad (2011)

Drive inflation
(+extensions)

Adshead et al (2016, 2017)

Spectator sector

Dimastrogiovanni et al (2016)

Maleknejad (2016, 2018)

Adshead et al (2017)

Agrawal, Komatsu et al (2017, 2018)

Soda and Urakawa (2017)

Kitajima et al (2018)

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Linear coupling between Gauge Fields and GWs!

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Linear coupling between Gauge Fields and GWs!

$$\delta A_i^b$$

Gauge fields, inflation & reheating

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Linear coupling between Gauge Fields and GWs!

$$\delta A_i^b \quad \text{and}$$

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Non-trivial vevs:

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Linear coupling between Gauge Fields and GWs!

$$\delta A_i^b \quad \text{and} \quad h_{ij}$$

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

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Non-trivial vevs:

$$\overline{\phi}(t)$$

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Linear coupling between Gauge Fields and GWs!

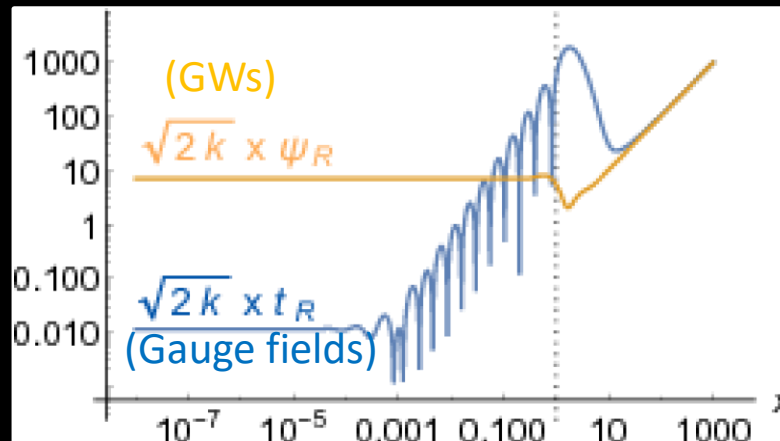


Figure from
Dimastrogiovanni et al.
arXiv:1608.04216

Gauge fields, inflation & reheating

Adshead and Wyman (2012)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} - \frac{\phi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \right]$$

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Linear coupling between Gauge Fields and GWs!

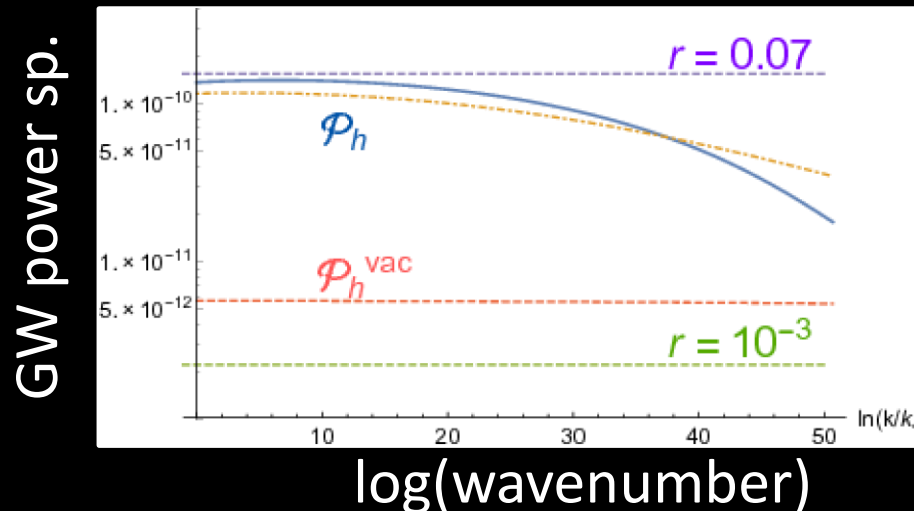


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Gauge fields, inflation & reheating

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$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} \mathcal{R} - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} - \frac{\phi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \right]$$

Non-trivial vevs:

$$\begin{aligned} \overline{\phi}(t) \\ \overline{A}_i^b(t) = a(t) Q(t) \delta_i^b \end{aligned}$$

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See also Domcke et al (2018), Adshead et al (2015, 2018, 2019)

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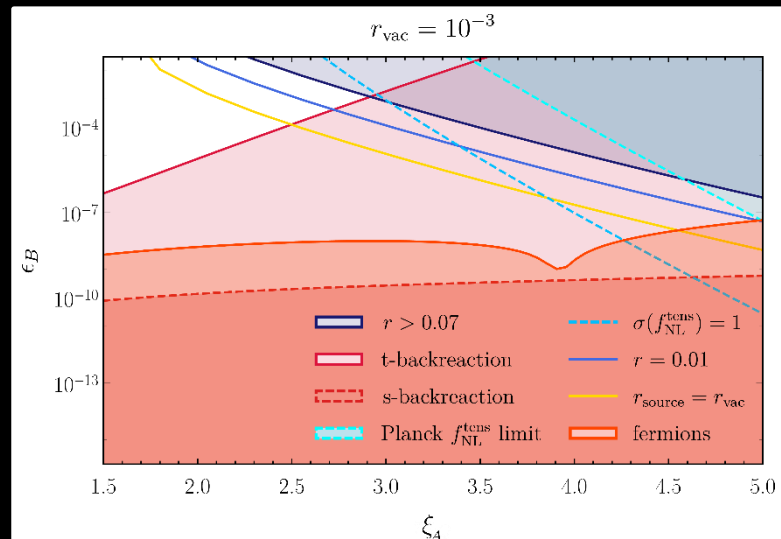
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Fraction of energy
in Gauge Fields



Gauge field coupling strength

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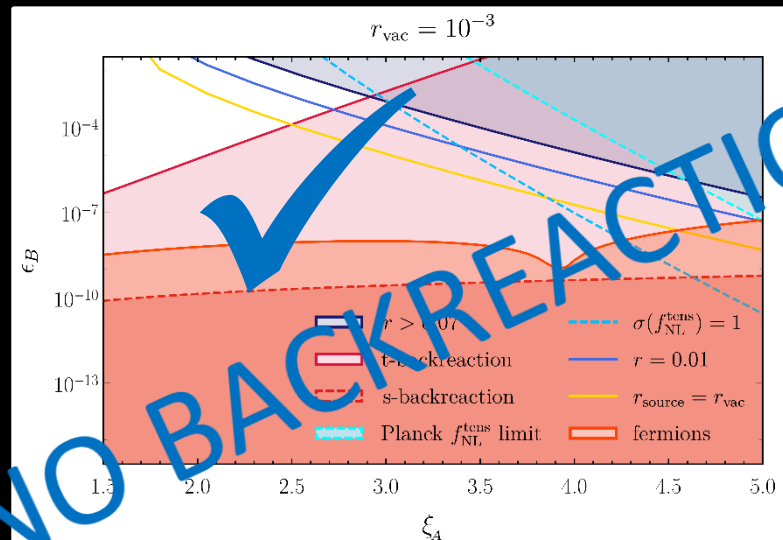
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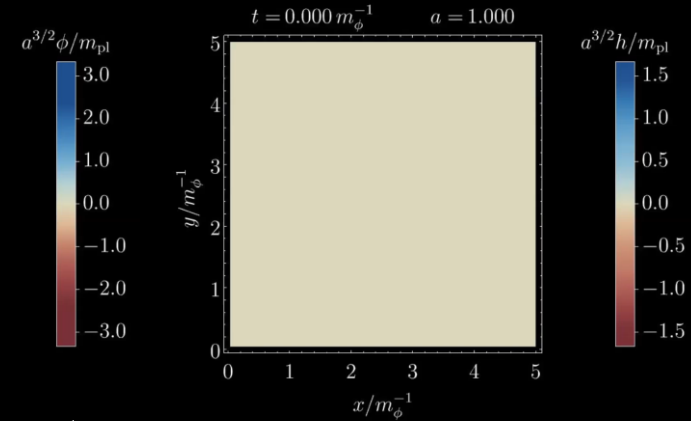
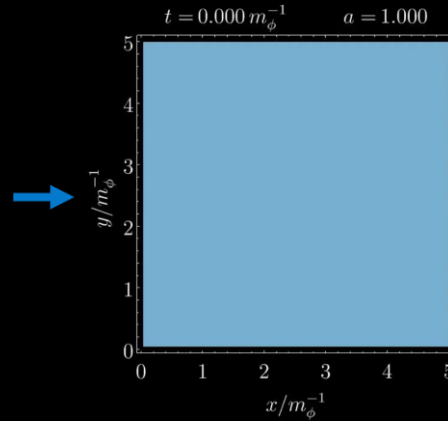
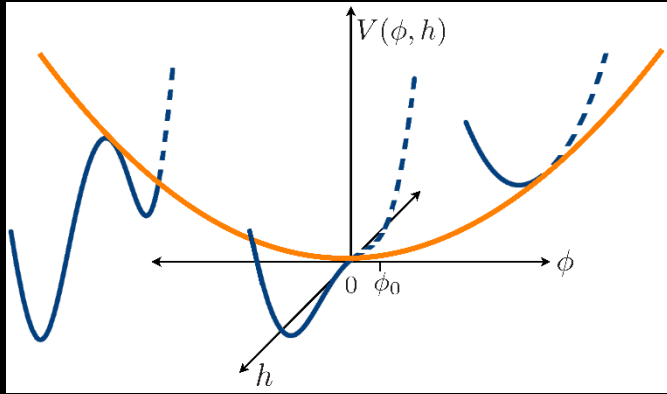
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Cosmology of a Fine-Tuned Higgs

Mustafa Amin, Jiji Fan, KL and Matthew Reece, PRD 99 035008 (2019)



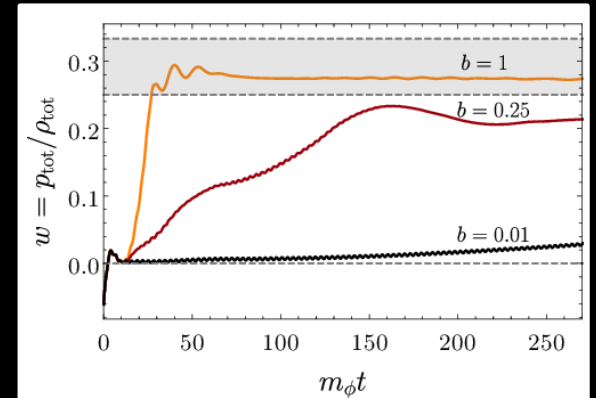
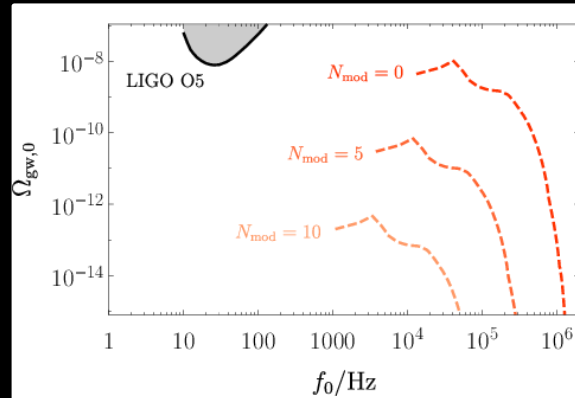
$$\frac{1}{2}m_\phi^2\phi^2 + \frac{M^2}{f}(\phi - \phi_0)\left(h^\dagger h - \frac{v^2}{2}\right) + \lambda(h^\dagger h)^2$$

$$b \equiv \frac{M^4}{2\lambda f^2 m_\phi^2} \rightarrow 1 \Leftrightarrow \text{rapid fragmentation}$$

$$\text{fine tuning} \Leftrightarrow \frac{\phi_0}{f} \ll 1$$

stochastic gravitational waves

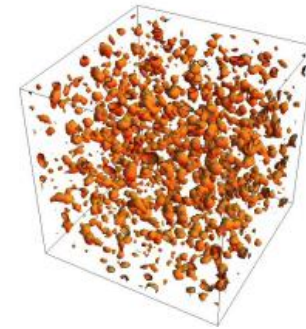
non-trivial eq. of state



Conclusions

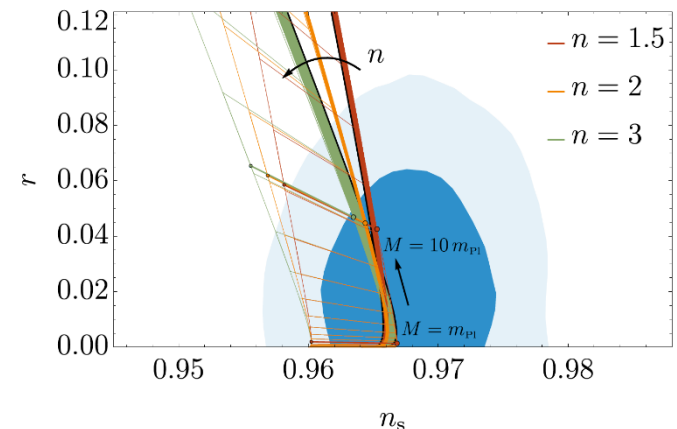
Reheating at the end of inflation:

- very rich dynamics



Future plans:

- more realistic models (e.g. gauge fields)
- observational signatures
 - expansion history, relics, GWs



Strings

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