# Long-term dynamics of cosmological axion strings

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05/09/2019@"Resonant instabilities in cosmology and their observational consequences"

Masahiro Kawasaki, Toyokazu Sekiguchi, MY, Jun'ichi Yokoyama 1806.05566, PTEP 2018 (2018) 091E01 "with preliminary update"

(Hiramatsu, Kawasaki, Sekiguchi, MY, Yokoyama, 1012.5502, PRD 83, 123501(2011). MY, Kawasaki, Yokoyama, hep-ph/9811311, PRL 82, 4578(1999). )

 $c = \hbar = M_G^2 = 1/(8\pi G) = 1$ 

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### Introduction

What is a DM? What is an axion?

### • Axion abundances

(Axion) string dynamics

Spectrum of axions radiated from strings.

• Discussion and conclusions

Introduction

### **Evidences of the presence of (cold) DM**



http://personal.psu.edu/mxe17/A020S/pages/darkmatter.html

Abell 2218, z = 0.175



HST

ISA. A. Fruchter and the ERO Team (STScI, ST-ECF) • STScI-PRC00-08

#### **Bullet Cluster**



Optical: NASA/STScI; Magellan/U.Arizona/D.Clowe et al.

X-ray: NASA/CXC/CfA/ M.Markevitch et al.; Lensing Map: NASA/STScI; ESO WFI; Magellan/U.Arizona/ D.Clowe et al





All of these data suggest the presence of CDM.

PLANCK

# **Candidates of DM**



Gardner & Fuller, 1303.4758 Prog. Part. Nucl. Phys. 71 (2013) 167

# What's an axion ?

#### • Strong CP problem in QCD



Theoretically, all of  $\overline{\theta}$  ( $0 \le \overline{\theta} < 2\pi$ ) are equivalent.

#### But, a neutron electric dipole moment:

$$d_N = (5.2 \times 10^{-16} e \,\mathrm{cm}) \,\overline{\theta} < 2.9 \times 10^{-26} e \,\mathrm{cm}$$

 $\overline{\theta} < 10^{-10}$  Why so small ?

**Peccei-Quinn (anomalous)** U(1)PQ symmetry Effectively makes the parameter  $\overline{\theta}$  dynamical Such a dynamical field : Axion, a(x) • **Observable:**  $\theta(x) = \overline{\theta} - a(x)/f_a$ **Dynamically**  $\overline{\theta} \to \mathbf{0}$ .  $V(\overline{\theta}, a) = F_{\pi}^2 m_{\pi}^2 \left[ 1 - \cos\left(\overline{\theta} - \frac{a(x)}{f_a}\right) \right]$ **Peccei & Quinn: introduce a global U(1) symmetry** spontaneously broken **Axion is identified with NG boson of U(1)**<sub>PQ</sub> symmetry

# **Constraints on** fa



Strength of a coupling of an axion

 $\propto rac{1}{f_a} \propto m_a$ 

**Lower** bounds on fa come from astrophysical objects:

 $f_a \gtrsim 4 \times 10^8 \,\, {
m GeV} \,\, ({
m SN} \, 1987{
m A})$ 

On the other hand, upper bound comes from the (over)closure condition.

# **Production mechanism of axions**

**Potential of Peccei-Quinn scalar** 

fa

 $\mathbf{O}$ 

 $\mathcal{O}_{\ell}$ 

 $2\pi f_a$ 

(i) U(1) symmetry breaking => strings

**Axions are emitted from strings.** 



In this talk, we concentrate on this abundance.

(ii) After QCD phase transition => string-wall system

Axions are emitted from such wall system.

In addition, coherent oscillation of an axion contributes the energy density of the Universe.

(In case the PQ symmetry is broken only before inflation, only the last contributes.)

# **Axion strings**

**Cosmic strings are formed after the U(1) symmetry breaking.** 



Axions are emitted from such axion strings.

#### **Abundance of axions emitted from axion strings**

In order to estimate the abundance of these axions, we need the following information:

- i) How many axion strings exist at each time ?⇔ How much energy is stored in axion strings ?
- ii) How many axions are emitted from a string ?(spectrum ⇔ average energy of emitted axion)
  - These issues have had long history and debates, and still have.
  - (My 1999 paper gave almost conclusive results, but ...)

# i) How many axion strings exist at each time ?

**Scaling property** (evolution of cosmic strings in an expanding Universe)

The number of long string per horizon is constant irrespective of cosmic time.



**This number is constant**, ξ. (this constant number depends on the background dynamics.)

$$\rho_{\rm S} = \frac{\xi \cdot \mu \cdot t}{t^3} = \xi \frac{\mu}{t^2} \propto t^{-2} \propto a^{-4} ({\rm RD}), \ a^{-3} ({\rm MD})$$

μ: tension (energy per unit length of a string)

How can we understand this property intuitively ?

### **Intuitive understanding of scaling property**



 Tension works only inside horizon, then a string configuration is random beyond horizon.

# Intercommutation



# **One scale model**

(Kibble, many others)

 $\dot{\rho}_{\infty} = -2H\left(1 + \langle v^2 \rangle\right)\rho_{\infty}$  = **EOM** from NG action **↑ ↑** cosmic expansion random walk We assume the presence of typical scale L(t) characterizing the system:  $\rho_{\infty} = \frac{\mu}{L(t)^2}$  (a string with its length L in the box L<sup>3</sup>) By taking into account of the intercommutation effect,  $\dot{\rho}_{\infty \to |000} = c \frac{\rho_{\infty}}{\tau}$  $\Rightarrow \dot{\rho}_{\infty} = -2H\left(1 + \langle v^2 \rangle\right)\rho_{\infty} - c\frac{\rho_{\infty}}{\tau}$  $L(t) \equiv \gamma(t) \cdot t$  $\frac{\dot{\gamma}}{\gamma} = -\frac{1}{2t} \left[ \left( 1 - \langle v^2 \rangle \right) - \frac{c}{\gamma} \right] \implies \gamma_{\text{fix}} = \frac{c}{1 - \langle v^2 \rangle} \text{ : stable fixed point}$ 

#### Local string (based on gauge symmetry breaking)

Gradient energy around a string core is cancelled by gauge field. String is thin (energy is stored mostly in the core) and can be well approximated by Nambu-Goto action. Albrecht & Turok

Scaling is confirmed  $\Rightarrow \xi \sim 10$ 

Albrecht & Turok Bennet & Bouchet Allen & Shellard Hindmarsh et al. Hiramatsu et al.

#### **OGlobal string** (based on global symmetry breaking)

Gradient energy around a string core apparently diverges, but has a cutoff given by a neighborhood string.

$$\mu \sim \int d^2 r |\nabla \Phi|^2 = 2\pi \int dr r \left| \frac{1}{r} \frac{\partial \Phi}{\partial \theta} \right|^2 = 2\pi f_a^2 \ln \frac{r_{\text{cut}}}{\delta} \qquad \text{distance}$$
 core radius

A force proportional to the inverse separation works between strings. Try to confirm the scaling property by solving the dynamics of complex scalar fields.

# **Numerical simulations**



Solve the EOMs of a complex scalar field in the expanding Universe and follow the formation and evolution of strings. (The string width is fixed, not fat string) A big obstacle is how to identify a string.

(MY & Yokoyama 2002, Hiramatsu et al. 2011)

4096<sup>3</sup> lattices in this work (256<sup>3</sup> in 1999 paper)



String core is identified with the intersect of two planes with  $\text{Re}\Phi=0$  and  $\text{Im}\Phi=0$ , which enables to evaluate the exact position.

We can follow the dynamics of strings, and hence evaluate their velocities.

$$egin{aligned} & egin{aligned} & egi$$

### **Identification of strings**

#### **Identification of strings — non-trivial due to discrete nature of lattice**



 $\lesssim (d^2 t)^{\frac{1}{3}}$ 

#### Separation of loop and infinite strings

- Grouping string points via Friends-of-Friends algorithm.
- A group of string points with  $L < 2 \pi$  t is regarded as a loop; otherwise as an infinite string.
- Loops/infinite strings are separated automatically in field theoretic simulation of axion strings.

# Is the scaling property confirmed ?



The initial state is a thermal equilibrium and phase transition happened.

Scaling is almost confirmed

<<

10



# Update



#### We observe the log-dependence of ξ !!!

Scaling property might be slightly broken due to the logarithmic dependence. c.f. Fleury et al. 1509.00026 Klaer & Moore 1707.05566 Klaer & Moore 1708.07521 Gorghetto et al.1806.04677 Vaquero et al. 1809.09241

# **String velocities**



Initially, rms of velocity ~ 0.7 consistent with previous works, However, as time advances, it decreases gradually and reads around 0.5 at the later time of the simulation.

This is substantially smaller compared to the velocity estimated from simulation of local-string based on the Nambu-Goto action, but consistent with field-theoretic simulation of local strings.

At this moment, we are unable to tell if the velocity has settled down already within the simulation time or continues to decrease subsequently.

# **Present abundance of axions** (radiated from axion string)

#### The dynamics of (long) axion strings

(Loops finally disappear by emitting axions)

**Energy density of radiated axions** (axions are relativistic at emission)

Spectrum, average energy

**Current number density** 

(Axions are now non-relativistic.)

Multiplying its mass leads to the current energy density.



#### ii) Energy spectrum of axions radiated from axion strings

(We would like to know the number of axions to evaluate the final abundance.)

 Davis, Battye, and Shellard
 Spectrum has a sharp peak around the horizon.

Strings oscillate many times before emission.

Sikivie et al

Spectrum decreases in proportional to wavenumber. Average energy is enhanced by the factor  $log(t_0/d) \sim 70$ , which leads to less number of axions.

Strings oscillate almost once before emission.



Raffelt

 $\mu \sim \int d^2 r |\nabla \Phi|^2 = 2\pi \int dr r \left| \frac{1}{r} \frac{\partial \Phi}{\partial \theta} \right|^2 = 2\pi f_a^2 \ln \frac{r_{\text{cut}}}{\delta}$  $\longrightarrow \quad \mu \propto \ln(1/d) \propto \ln k \quad \Longrightarrow \quad \frac{d\mu}{dk} \propto \frac{1}{k}$ 

# Which is correct ?



A sharp peak around the horizon scale

# **Estimation for the spectrum of emitted axions**



FIG. 2 (color online). Schematic overview of our pipeline.

### **Contamination removal**



FIG. 3 (color online). Validity check of our estimation method using PPSE. Three different spectra are plotted (see text for details). Only statistical errors are shown; bars corresponds to the square root of the diagonal components of covariance matrices.

# update



Figure 5: Evolution of the mean momentum of radiated axions in units of the Hubble expansion rate (see Eq. (11)). Color and symbol are the same as in Figure 1.

#### Average momentum is still around the horizon scale.

# **Present abundance of axions**

**Energy density of radiated axions** (axions are relativistic at emission) Spectrum, average energy **Peak around the horizon scale Current number density** (Axions are now non-relativistic.) Multiplying its mass leads to the current energy density.

Strings evolve according to scaling law



If the log dependence keeps until

the QCD phase transition,  $\xi$  is

# Conclusions

We have tried to estimate axion abundance emitted from axion string.

- Scaling property is slightly broken through the logarithmic dependence.
- Average energy of axion radiated from axion strings is still around the horizon scale.

We need to explain this logarithmic dependence analytically.

Unfortunately, we have yet known neither whether this logarithmic dependence continues or stops at some later time nor the final value of  $\xi$ .