

THE ASTROPHYSICS OF EMRIS

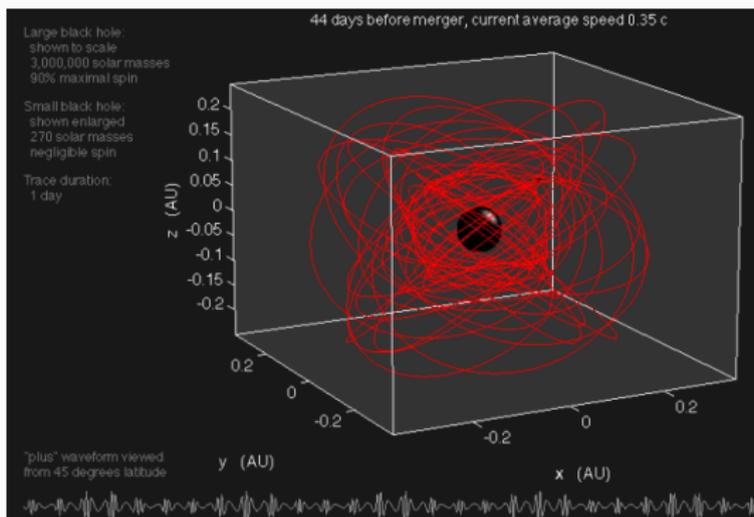
Capture of compact objects by SMBHs

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Max-Planck Institute for Gravitational Physics (Albert Einstein Institute)

CAPTURE OF COMPACT OBJECTS



[Figure Steve Drasco]

- Stellar mass object spiraling into $10^4 - 10^6 M_{\odot}$
- This range of masses corresponds to relaxed nuclei (!)
- Only compact objects (extended stars disrupted early)
- With eLISA stellar BH $z \gtrsim 0.7$

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- ▷ Bridge between **astrophysics and GR**

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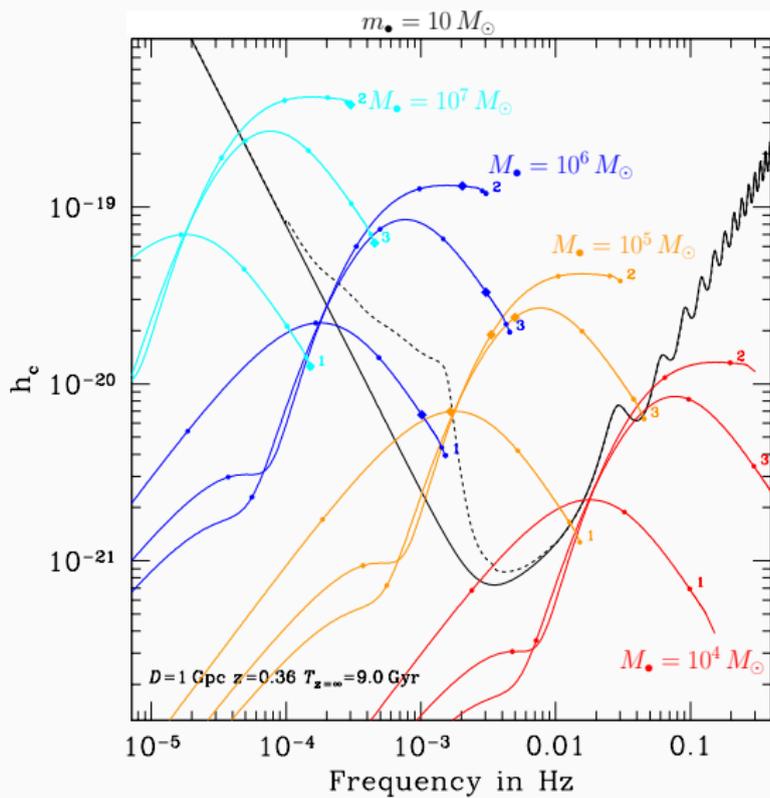
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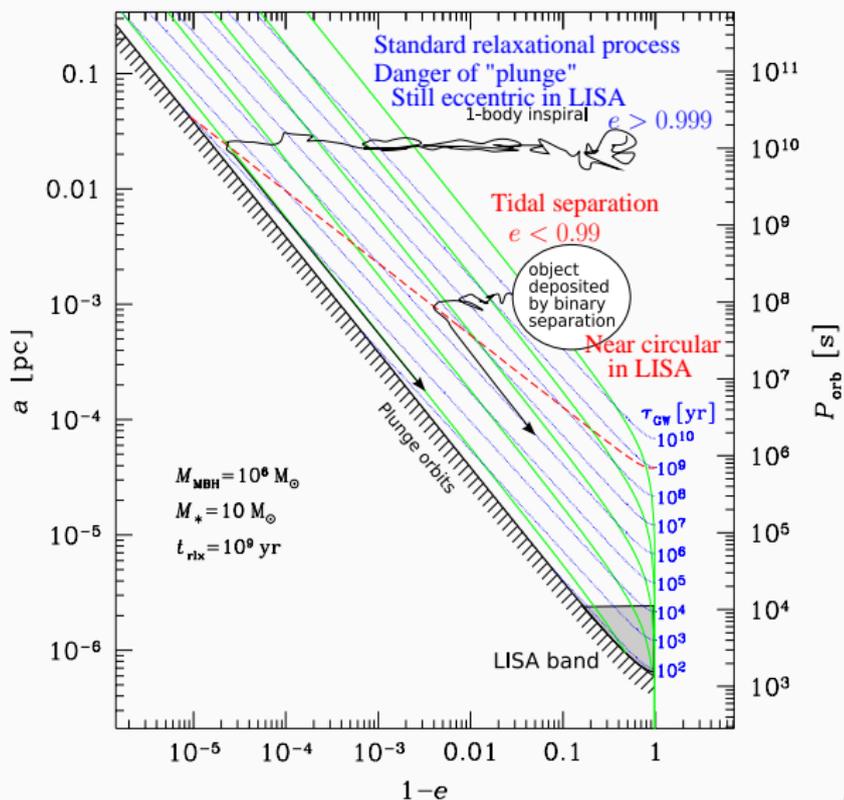
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- ▷ Many years before launch we’re making new discoveries
- ▷ In this talk we’ll see some of these difficulties, and how we’ve made progress: **Microphysics around SMBHs**

RANGE OF MASSES



DICHOTOMIZING AN EMRI

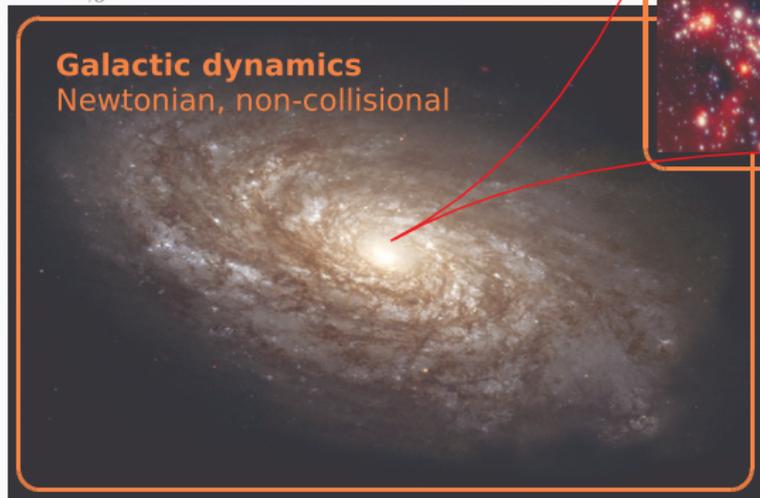


DISTRIBUTION OF STARS AROUND SMBHS

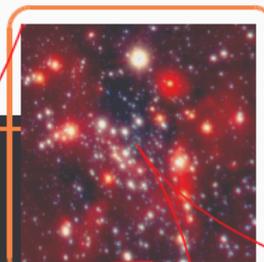
THE THREE REALMS OF STELLAR DYNAMICS

$$\begin{aligned}\rho_{\star, \text{gal}} &\sim 0.05 M_{\odot} \text{pc}^{-3} \\ \sigma_{\star, \text{gal}} &\sim 40 \text{ km s}^{-1} \\ t_{\text{rlx, gal}} &\sim 10^{15} \text{ yrs}\end{aligned}$$

Galactic dynamics
Newtonian, non-collisional



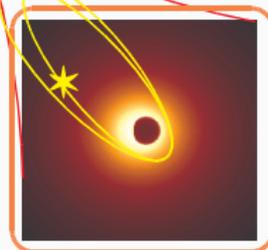
Cluster dynamics
Newtonian, collisional



$$\begin{aligned}\rho_{\star, \text{cl}} &\sim 10^6 - 10^8 M_{\odot} \text{pc}^{-3} \\ \sigma_{\star, \text{cl}} &\sim 100 - 1000 \text{ km s}^{-1} \\ t_{\text{rlx, cl}} &\sim 10^8 - 10^{10} \text{ yrs}\end{aligned}$$

$\times 1000$

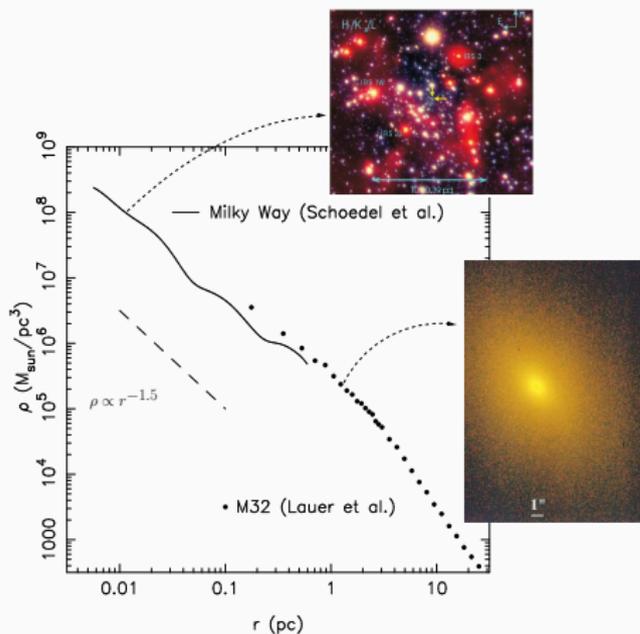
$\times 10^7$



Relativistic dynamics
collisional or not (low N)

$$\begin{aligned}\mathcal{M}_{\bullet} &\sim 10^6 - 10^9 M_{\odot} \\ R_{\text{Schw}} &= 10^{-7} - 10^{-4} \text{ pc}\end{aligned}$$

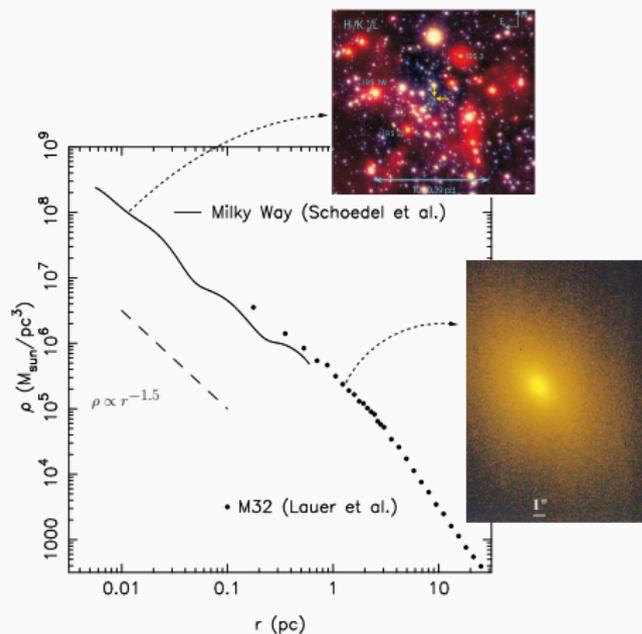
HOW MANY A YEAR?



[Adapted from Merritt 2006]

- ▷ 0th question: How many stars?
How do they distribute?

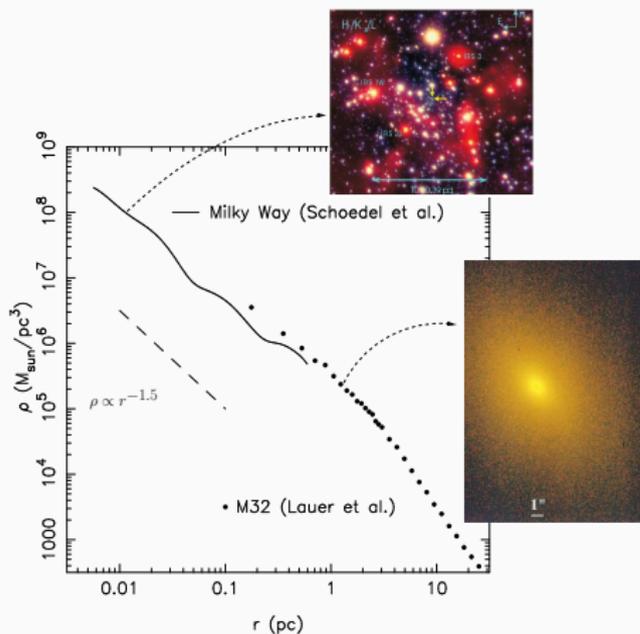
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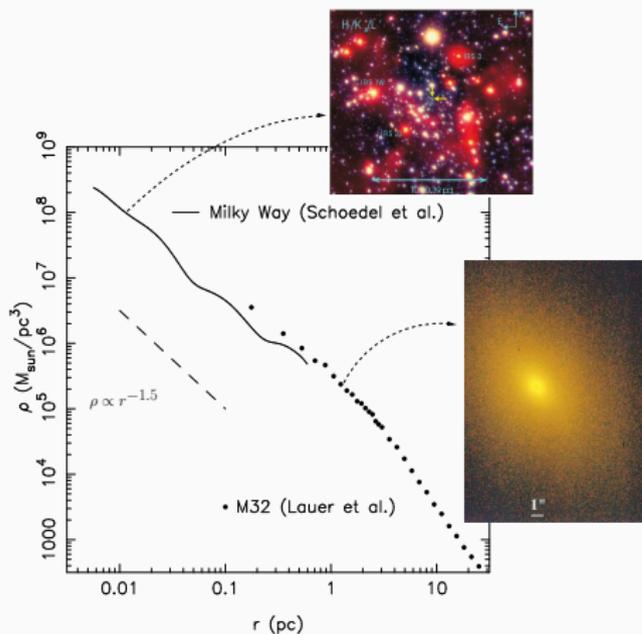
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- Considerable amount of
modelling: Are these profiles a
coincidence?

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- ▷ Confirmed later with a detailed kinematic treatment for single-mass *[Bahcall & Wolf 1976]*: $\gamma = 7/4$ and $p = \gamma - 3/2 = 1/4$

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- ▷ Initial Mass Functions $\in [0.1, \sim 120]M_{\odot}$ to first order by two (well-separated) mass scales: $\mathcal{O}(1M_{\odot})$ (Main Sequence, White Dwarfs, Neutron Stars) and $\mathcal{O}(10M_{\odot})$ (Stellar Black Holes)

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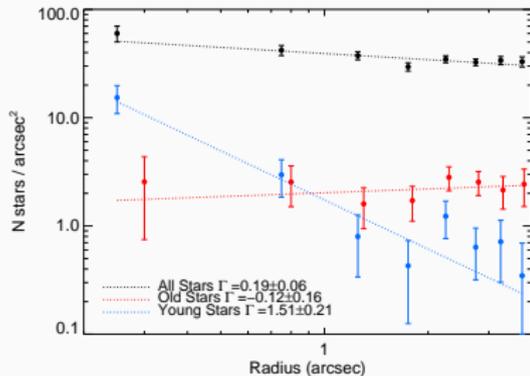
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- ▷ Two branches for the solution: A “weak” (unrealistic) branch and a “strong” branch

[Hopman & Alexander 2009, Preto & Amaro-Seoane 2010, Amaro-Seoane & Preto 2011]

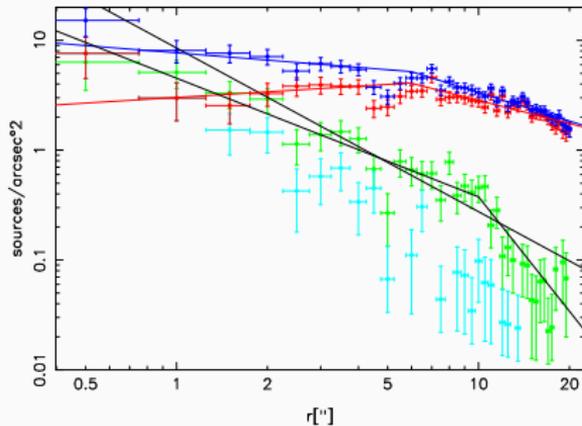
CUSPS IN DISTRESS

REGROWTH OF CUSPS

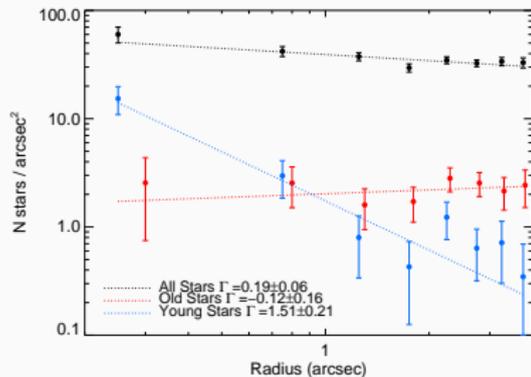


- ▷ Deficit of old stars based on number counts of spectroscopically identified, old stars in sub-parsec SgrA* (down to magnitude $K = 15.5$)

[Do et al. 2009, Buchholz et al 2009]



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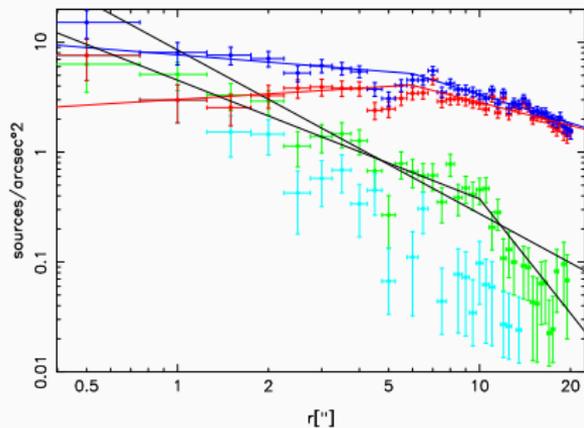


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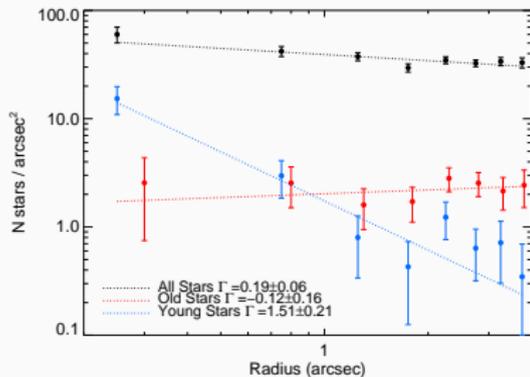
[Do et al. 2009, Buchholz et al 2009]

- ▷ Best fits seem to favor **negative slopes $\gamma < 1$**

[Schödel et al 2009, Chatzopoulos et al 2014]



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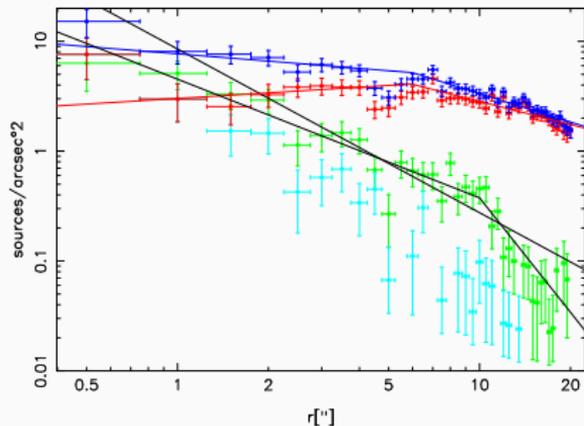
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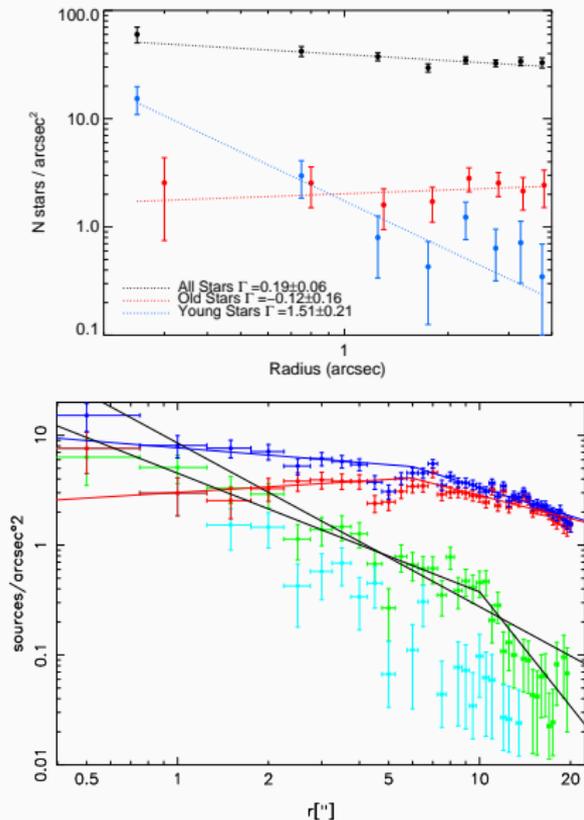
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- ▷ Possibility of a core with ρ_{\star} decreasing, $\gamma < 0$
- ▷ Observers only see essentially late-type giants: **Detectable stars are still a small fraction**

HOW DO YOU CARVE A HOLE AT THE GALACTIC CENTER?

1. **Infalling clusters carve a hole** – But need a steady inflow of one at roughly every 10^7 years

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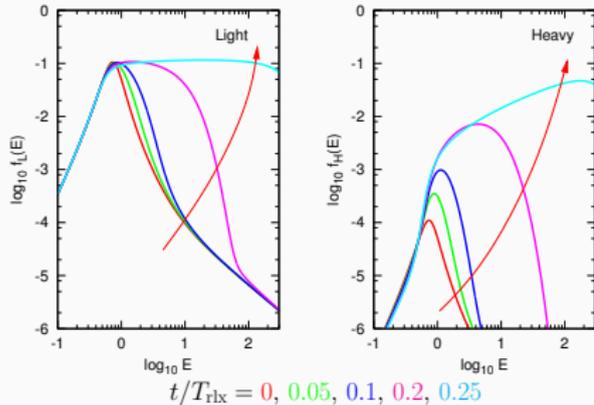
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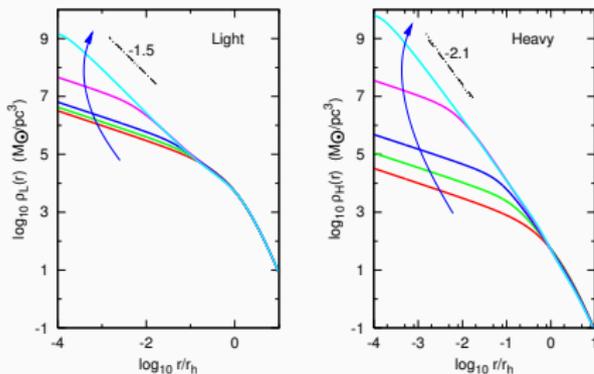
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 - ▷ Must invoke unlikely events to get rid of it
 - ▷ Let's play the game What is the time necessary for cusp growth if at some point a central core is carved?
 - ▷ We have now the correct, more efficient, solution of mass segregation

ISOCORE ... REGROWTH

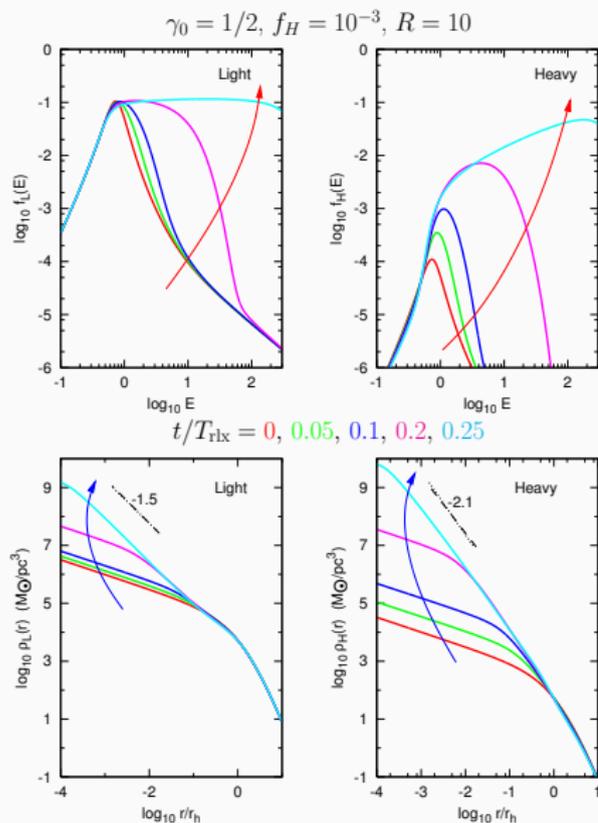
$$\gamma_0 = 1/2, f_H = 10^{-3}, R = 10$$



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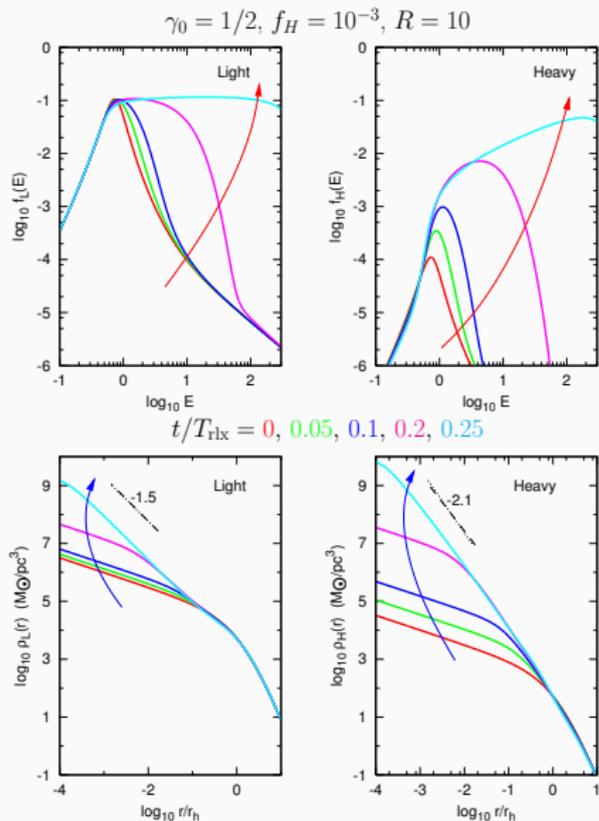


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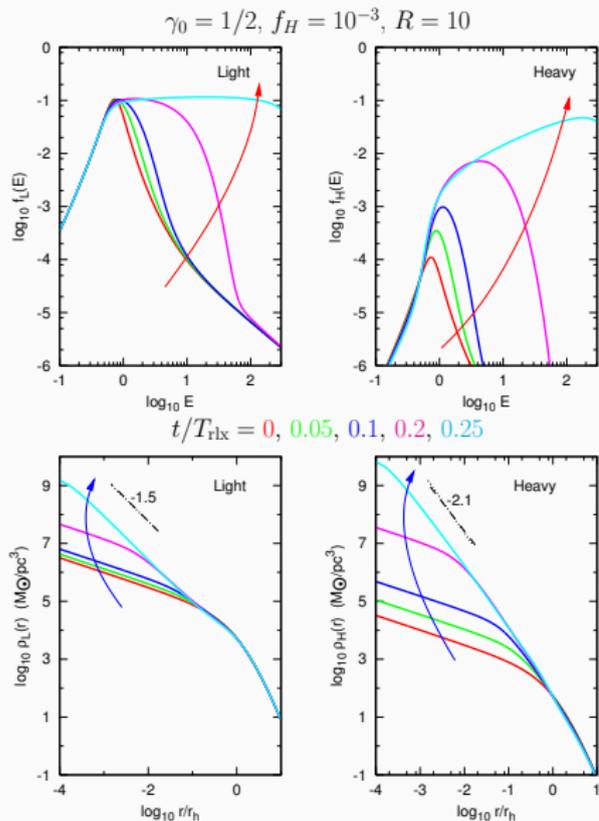
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- ▷ Our results confirmed later [Gualandris & Merritt 2011]

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- Stellar cusps may re-grow in less than a T_H but the existence of cored nuclei still remains a possibility

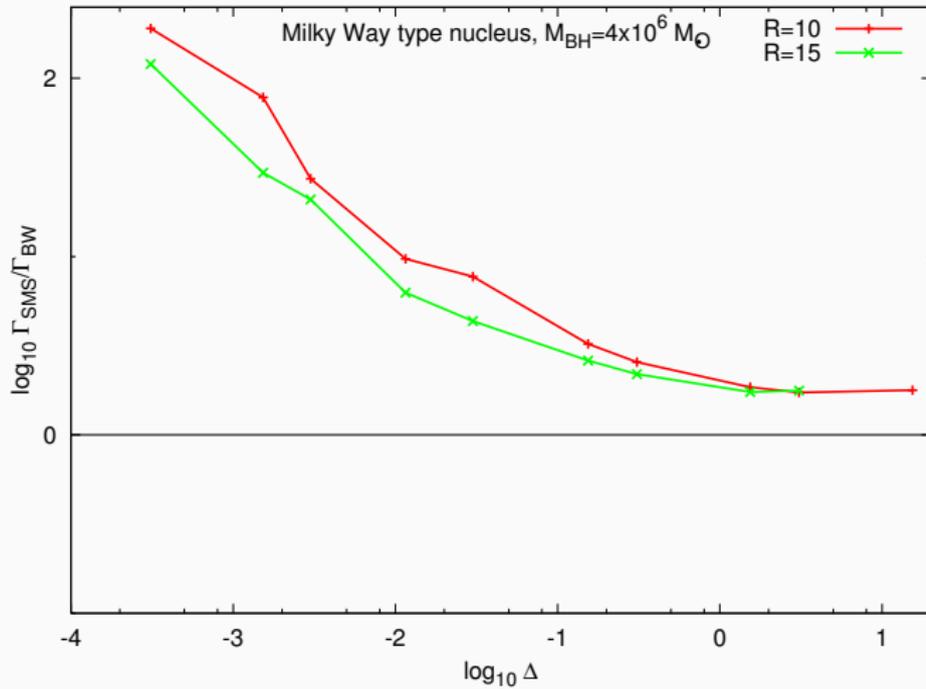
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- Stellar cusps may re-grow in less than a T_H but the existence of cored nuclei still remains a possibility
- The Milky Way nucleus is *not* necessarily the prototype of the nucleus from which e-LISA detections will be more frequent
- We still expect that a substantial fraction of EMRI events will originate from segregated stellar cusps, in particular with our new solution of mass segregation

EVENT RATES



DISGUISED CAPTURES

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- ▷ Plunges are more frequent than “adiabatic” EMRIs A common result to all event rate estimates
- ▷ What if these stars did not plunge? We’d have extremely eccentric sources, and event rates orders of magnitude larger

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- ▷ (p, e, i) , calculate constants of motion (E, L_z, C) , then the average flux of these “constants”, i.e. the average time evolution $(\dot{E}, \dot{L}_z, \dot{C})$

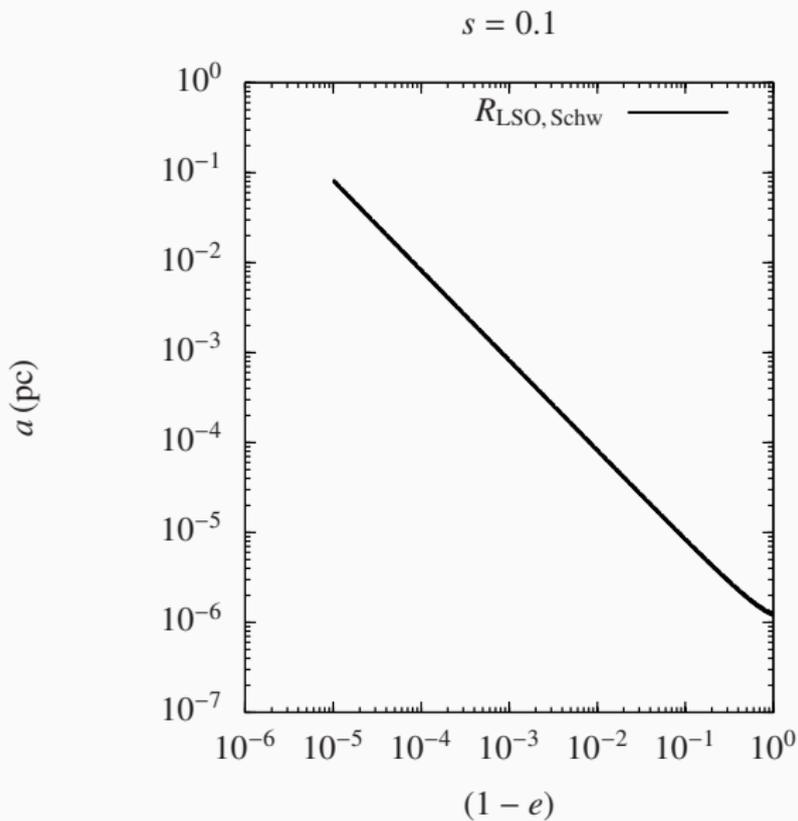
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- ▷ Calculate time to go from apo to periapsis and back (radial periode) and thus the change in (E, L_z, C) and so the new constants of motion, therefore: $(p_{\text{new}}, e_{\text{new}}, i_{\text{new}})$

SOME RESULTS DEPENDING ON THE SPIN

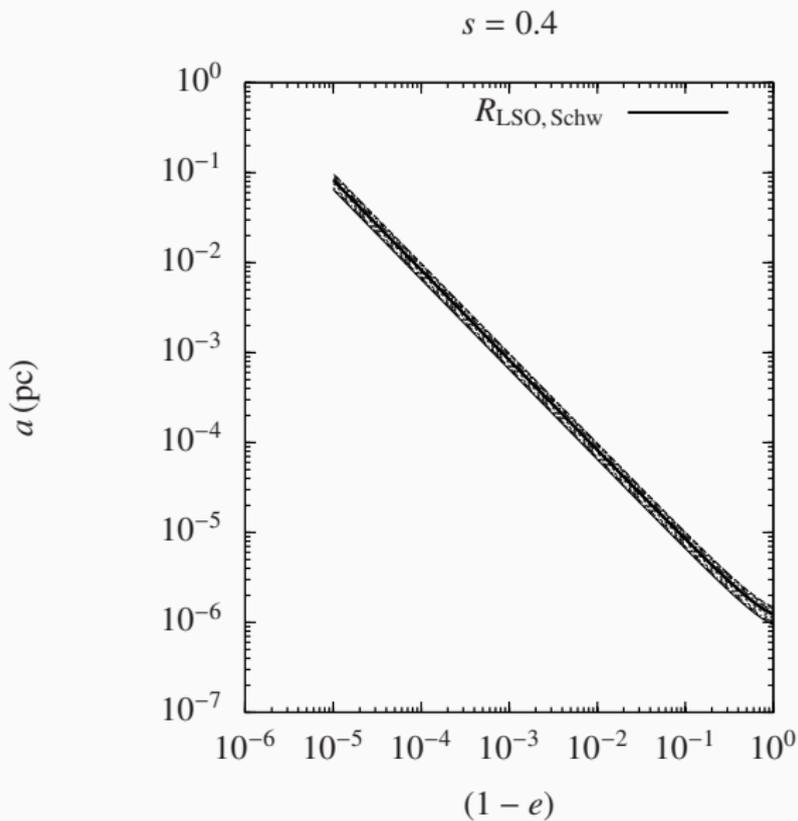
\mathcal{M}_\bullet	Spin (a/M)	a_0 (pc)	e_i	i (rad)	τ_{mrg} (yrs)	$\tau_{\text{e-LISA}}$	Peri (e-LISA)
3E6	0.990	8.6182E-4	0.9990	0.6	2.6755E3	6.8409E2	432503
1E6	0.990	2.8727E-4	0.9990	0.6	2.9743E2	1.1915E2	146074
1E6	0.500	2.8727E-4	0.9990	0.6	2.4714E2	9.8328E1	97715
3E6	0.500	8.6182E-4	0.9990	0.6	2.2229E3	5.6105E2	288372
1E6	0.900	2.3939E-4	0.9990	0.2	1.5328E2	6.8038E1	90555
3E6	0.900	7.1818E-4	0.9990	0.2	1.3785E3	3.9237E2	268423
3E6	0.900	7.1786E-3	0.9999	0.2	4.6101E3	3.9131E2	267802
3E6	0.900	5.7429E-3	0.9999	0.2	2.0757E3	1.9956E2	149747
3E6	0.900	5.0250E-3	0.9999	0.2	1.3164E3	1.3607E2	106563
1E6	0.900	1.6750E-3	0.9999	0.2	1.4843E2	2.3449E1	35889
1E6	0.900	1.4357E-3	0.9999	0.2	9.1260E1	1.5533E1	24593
1E6	0.900	1.4357E-3	0.9999	0.1	9.2711E1	1.5769E1	25038
3E6	0.900	4.3071E-3	0.9999	0.1	8.1857E2	9.1641E1	74371
5E6	0.900	7.1786E-3	0.9999	0.1	2.2652E3	2.0548E2	122993
1E6	0.900	1.4357E-3	0.9999	0.1	1.8272E2	3.1556E1	50075
4E6	0.700	6.7000E-3	0.9999	0	1.8937E3	1.7207E2	96284
4E6	0.998	6.7000E-3	0.9999	0	2.6993E3	2.4753E2	170494
4E6	0.998	9.5714E-3	0.9999	0	8.7952E3	6.6162E2	395248
4E6	0.998	7.6571E-3	0.9999	0	4.1097E3	3.5062E2	230973
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4E6	0.998	5.7429E-3	0.9999	0	1.7598E3	1.7468E2	123868
4E6	0.998	5.7429E-3	0.9999	0.3	1.6574E3	1.6506E2	117974

Note: Prograde orbits, $m_\bullet = 10 M_\odot$

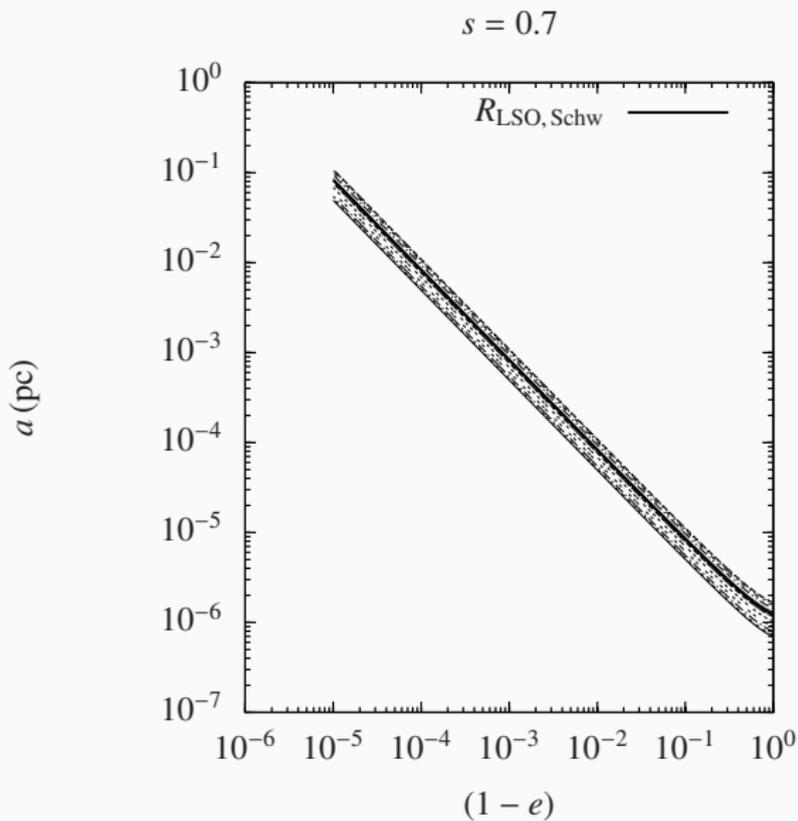
A FAMILY OF SEPARATRICES: $s = 0.1$



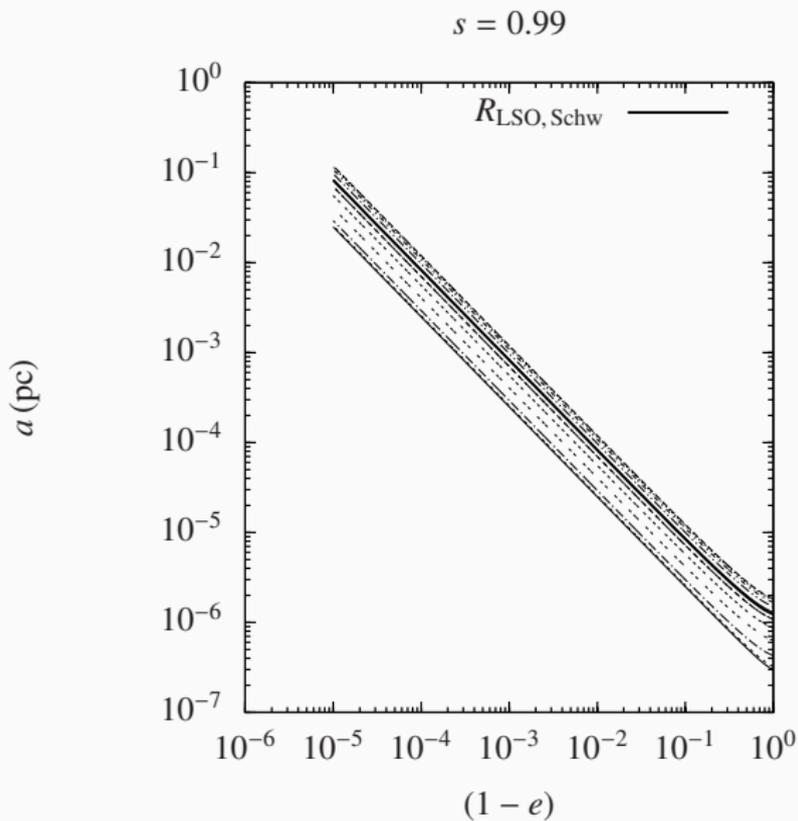
A FAMILY OF SEPARATRICES: $s = 0.4$



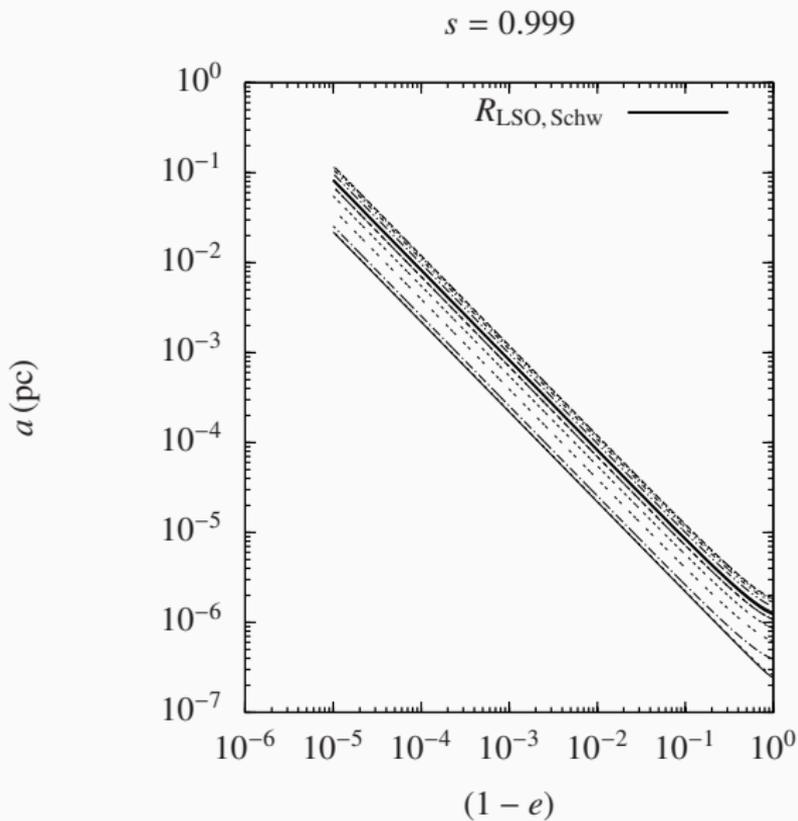
A FAMILY OF SEPARATRICES: $s = 0.7$



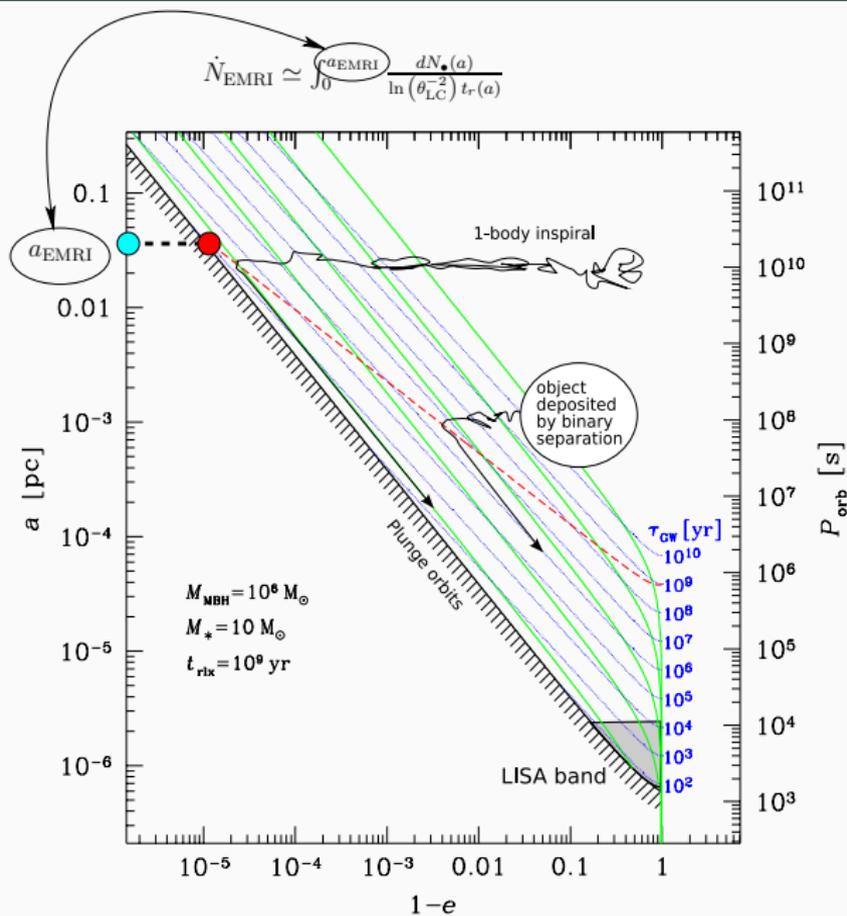
A FAMILY OF SEPARATRICES: $s = 0.99$



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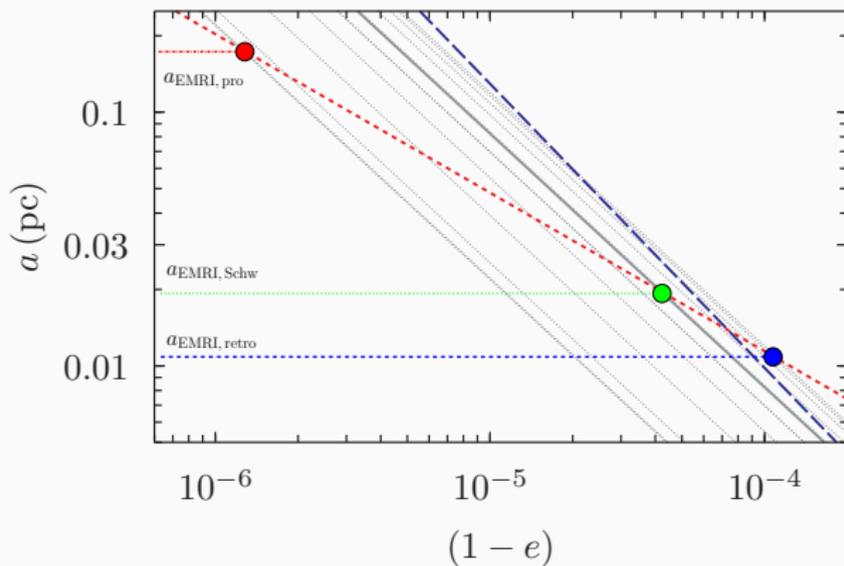
IMPACT OF THE SPIN ON THE RATES?



IT'S ALL ABOUT AN UPPER LIMIT

$$\dot{N}_{\text{EMRI}} \simeq \int_0^{a_{\text{EMRI}}} \frac{dN_{\bullet}(a)}{\ln(\theta_{\text{LC}}^{-2}) t_r(a)}$$

$$s = 0.999$$



$$a_{\text{EMRI}}^{\text{Kerr}} = a_{\text{EMRI}}^{\text{Schw}} \times \mathcal{W}^{\frac{-5}{6-2\gamma}}(\iota, s)$$

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- ▷ Take a typical value of a prograde orbit with high spin: $\mathcal{W} = 0.15$;
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- ▷ When taking into account spinning MBHs EMRI rates are boosted

THE BUTTERFLY EFFECT

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- ▷ Then

$$M(R) = \int_0^R 4\pi r^2 \rho(r) dr \propto \int_0^R r^{-\gamma+2} dr \propto R^{3-\gamma}$$

$$N(R) \simeq 8.6 \times 10^4 \left(\frac{R}{6 \times 10^{-4} \text{ pc}} \right)^{3-\gamma}$$

$$R_1 \simeq 6 \times 10^{-4} \text{ pc} \times \left(\frac{1}{8.6 \times 10^4} \right)^{\frac{1}{3-\gamma}}$$

▷ $R_1 \simeq 3 \times 10^{-7}$ pc for $\gamma = 1.5$

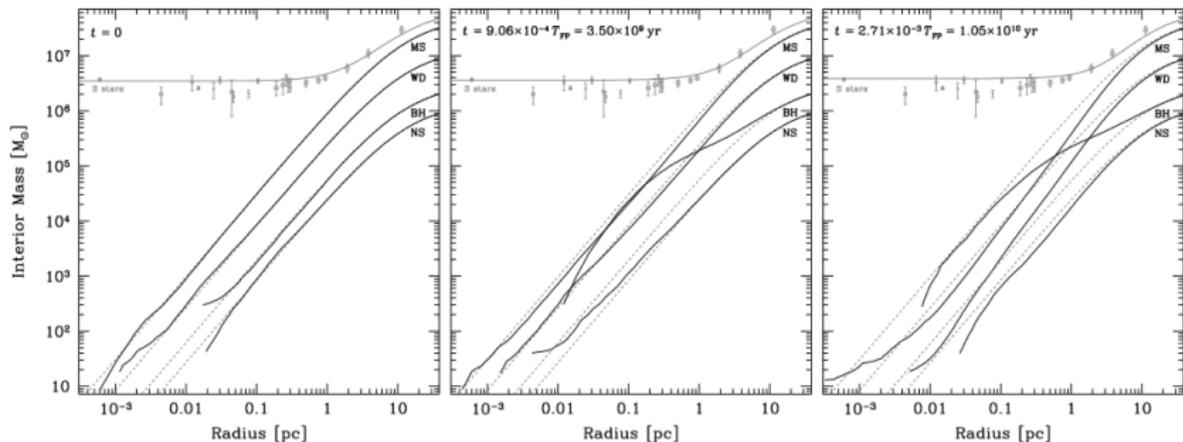


FIG. 11.— Evolution of the profiles of enclosed mass for GN25. The solid lines are the results of the MC simulation. For reference, the dashed lines show $\eta = 1.5$ profiles adjusted on the total mass and half-mass radius of each component. The top thin line is the total mass, including the central MBH; it is compared to the observational constrains for the MW center (see Fig. 3). [See the electronic edition of the *Journal* for a color version of this figure.]

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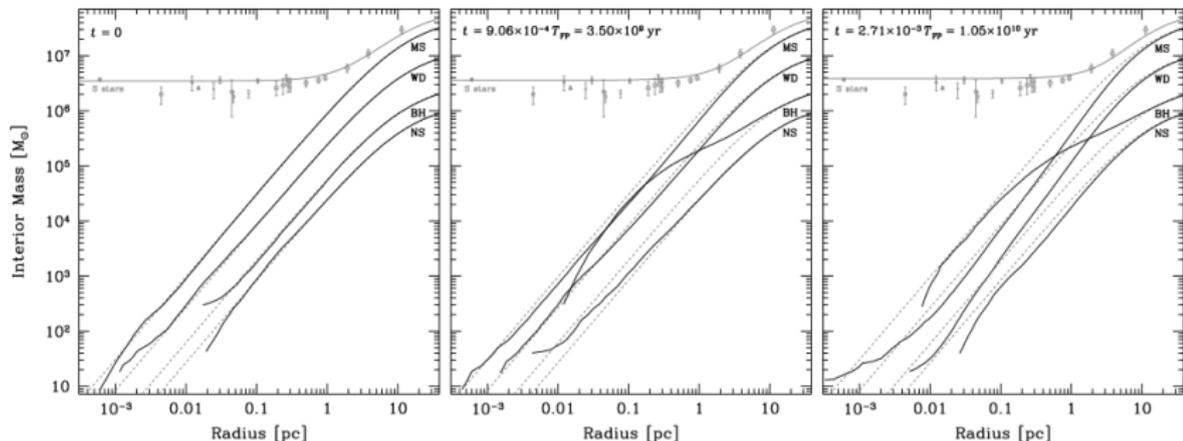


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[Freitag, Amaro-Seoane & Kalogera 2006]

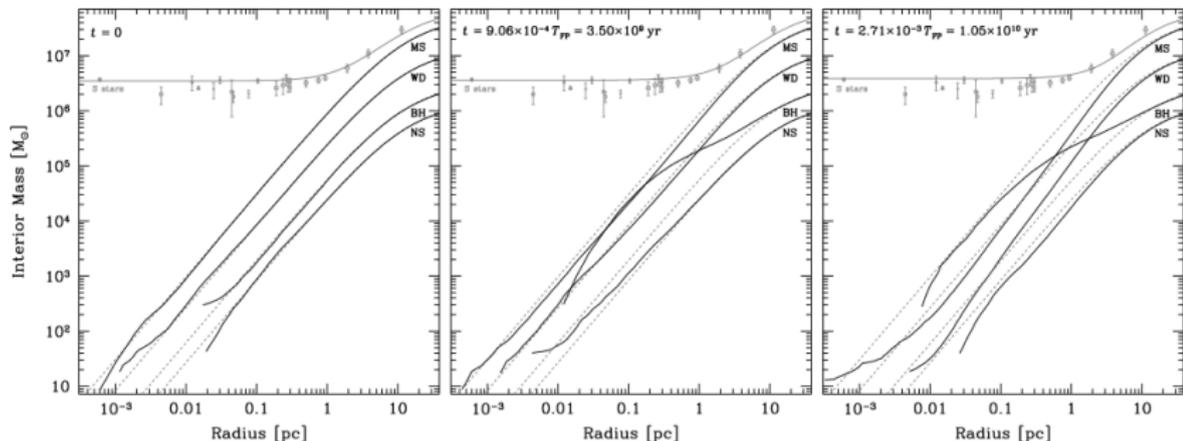


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- ▷ Watch out: I am cheating

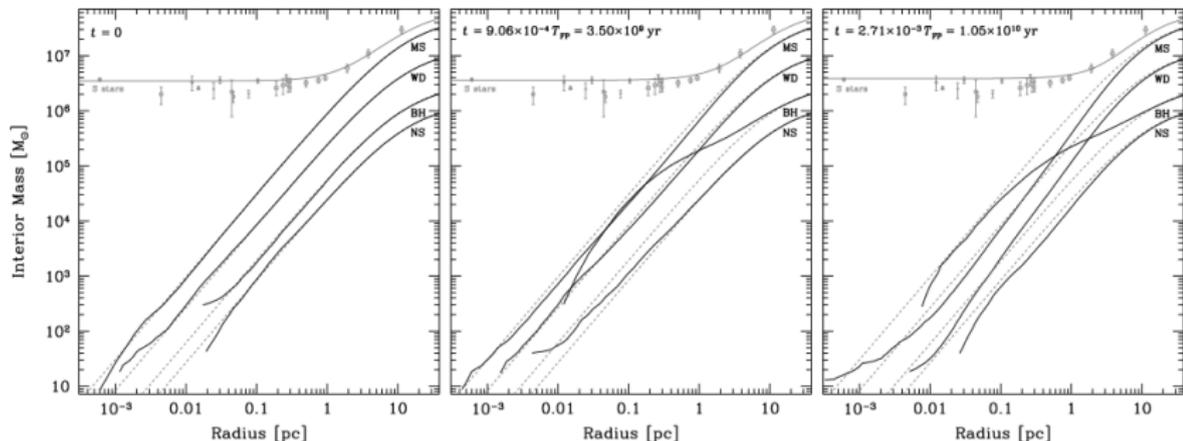
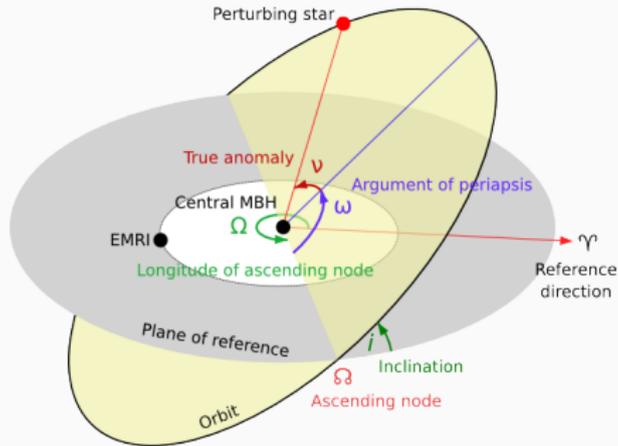


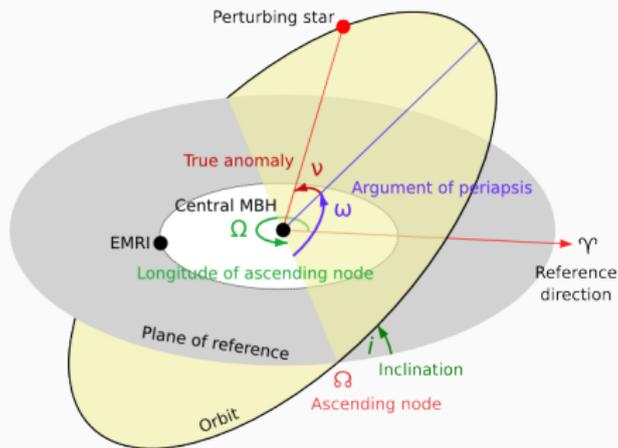
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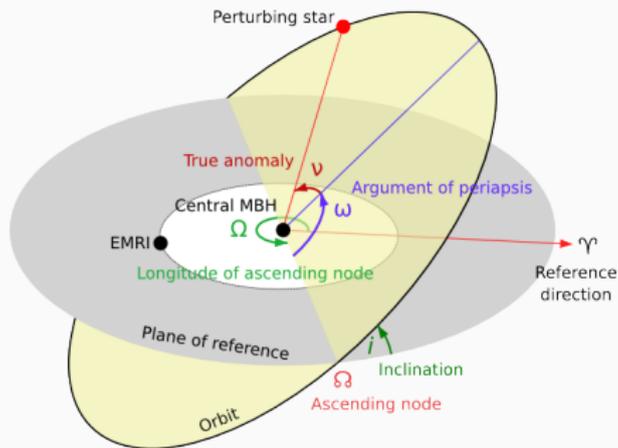


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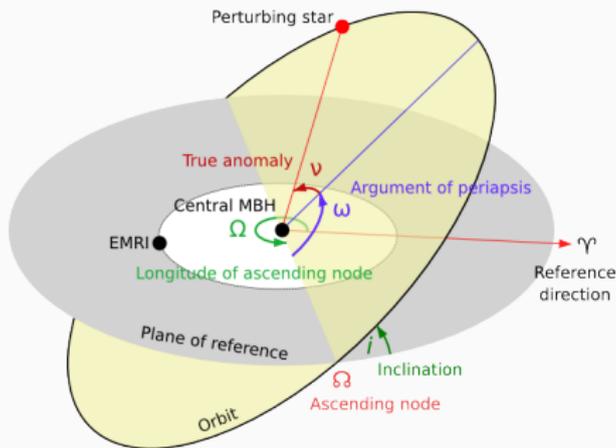
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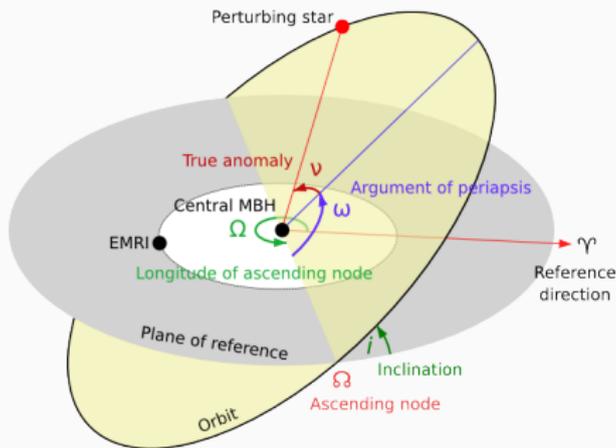
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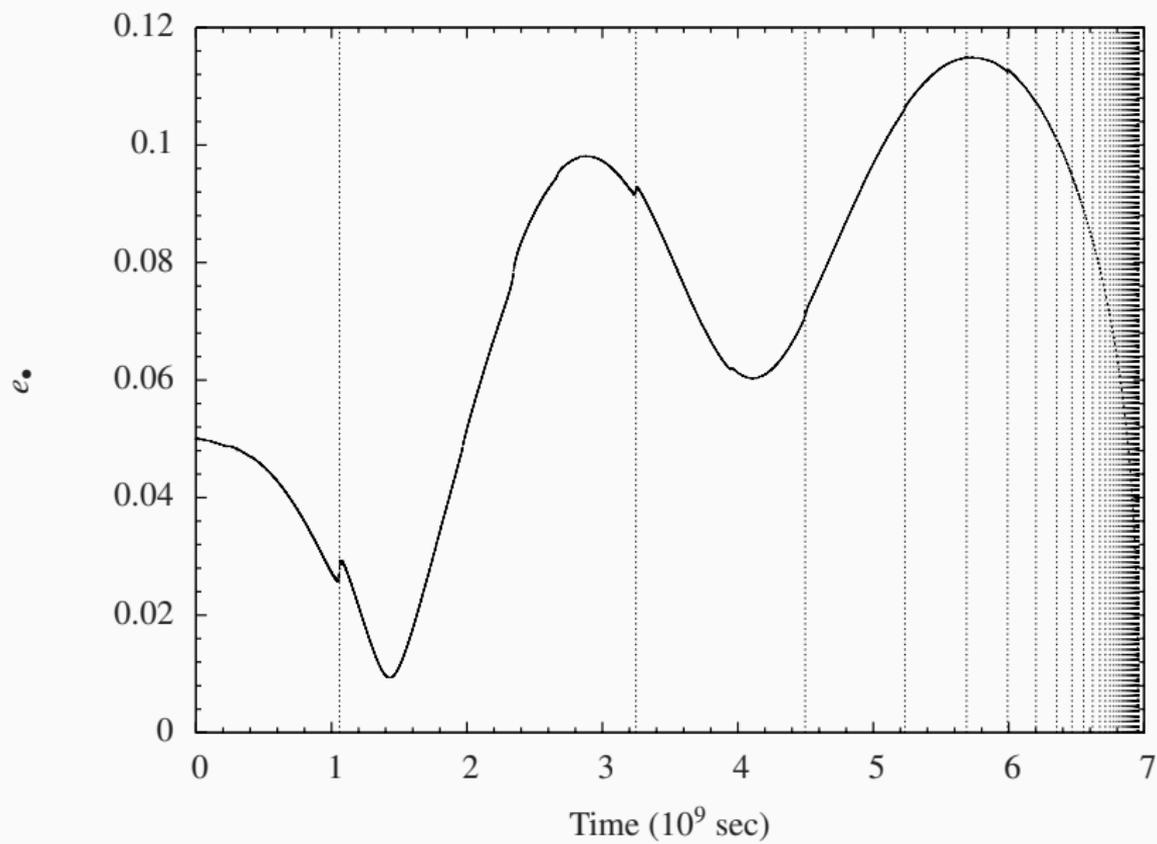


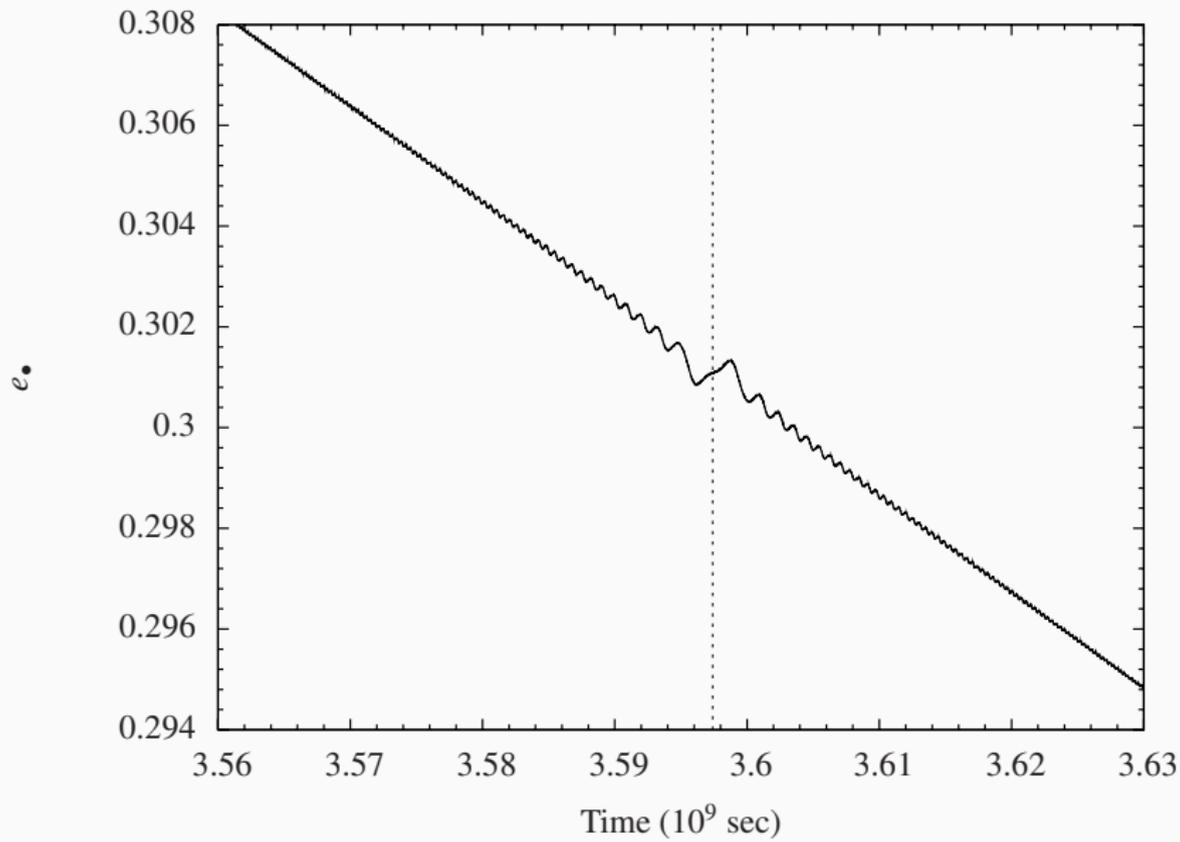
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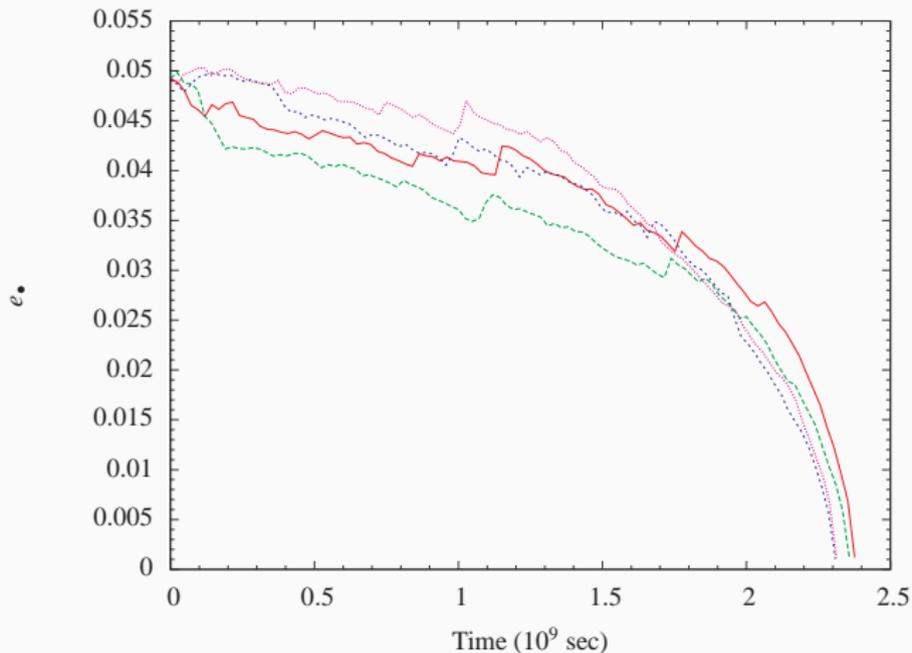


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- ▷ Evolution of the eccentricity when taking **energy loss**, i.e. 2.5 PN into account?



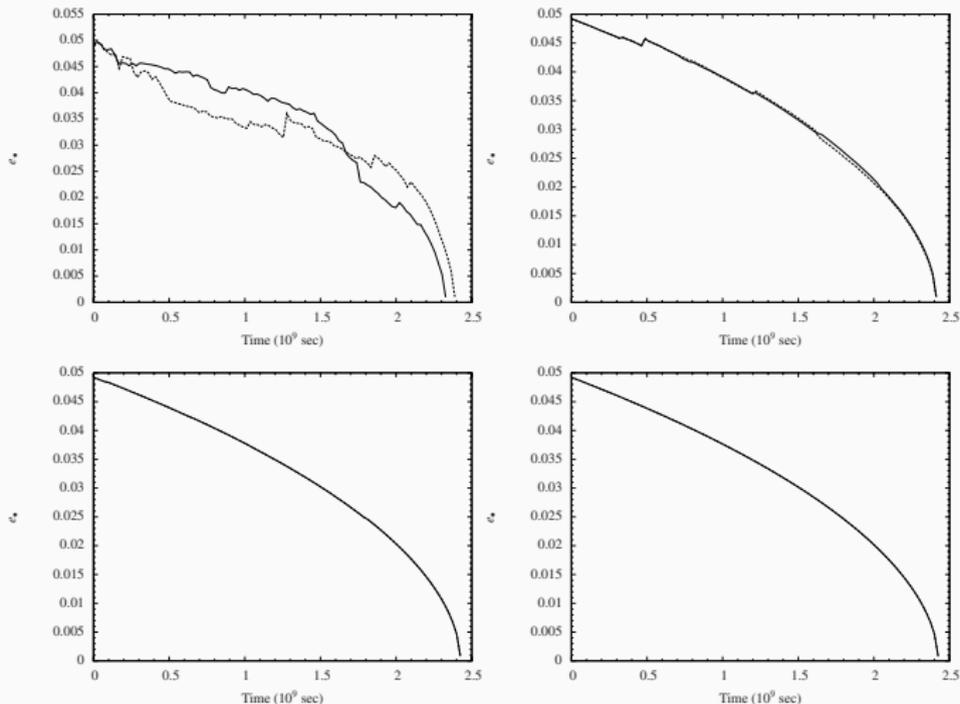






Red $i_* = 30^\circ$, green $i_* = 30.001^\circ$, blue fiducial plus a *ten billionth* of a degree, $i_* = 30.0000000001^\circ$ and magenta plus a *ten trillionth* of a degree, $i_* = 30.00000000000001^\circ$

NO, IT'S NOT A BUG



$a_{\star} = 4 \times 10^{-6}$ pc, 6×10^{-6} pc, 9×10^{-6} pc and 4.07243×10^{-5} pc

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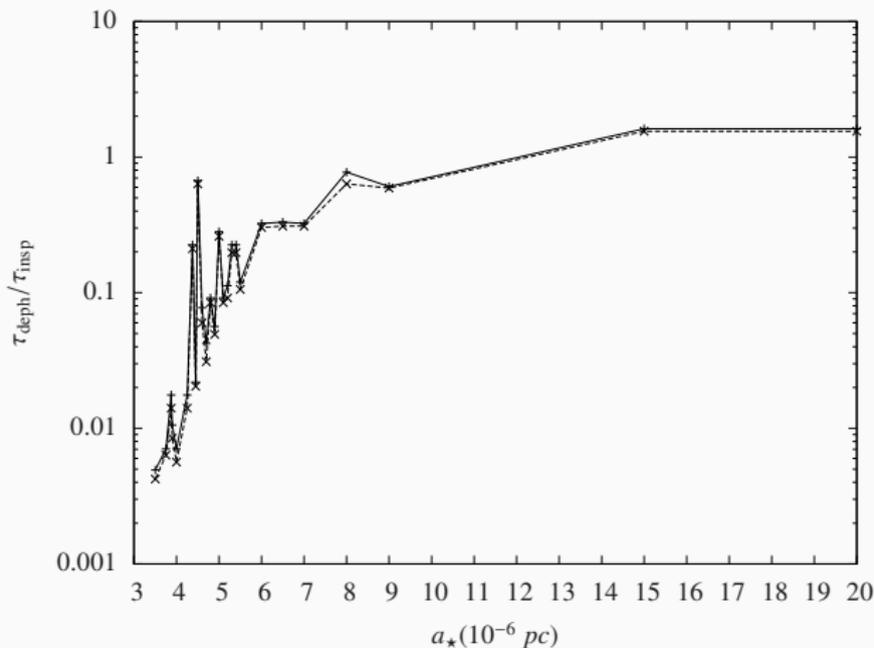
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- ▷ This is not a classical system
- ▷ How to characterise the chaos?



Start with a fiducial case and another one a *bit* different in phase space. Let them evolve. Calculate time for the “distance” to be $2 \times a_{\bullet}$ and divide it by the isolated inspiral time : Characteristic time

CONCLUSIONS

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- GR must not always be wrong: *It could be an innocent star nearby*

QUESTIONS?