Dark matter models, properties and particle physics candidates

Takashi Toma



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Outline

- **I** Introduction
 - · WIMP
 - \cdot Status of direct detection experiments
- 2 EWIMP, SIMP, cannibal DM, FIMP
- **3** A pseudo-Nambu-Goldstone dark matter (pNG DM)
- 4 Summary



WIMP is thermalized with SM particles in early universe

- To get $\Omega_{\chi}h^2 = 0.12$, roughly $\sigma \sim 1 \mathrm{pb} \sim 10^{-26} \mathrm{cm}^3/\mathrm{s} \sim 10^{-36} \mathrm{cm}^2$
- Almost independent on DM mass

WIMP

Status of direct detection experiments



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WIMP

Future sensitivity of direct detection experiments



DM models

Classification of DM models from experimental results

- **1** WIMP with suppressed cross section for direct detection
 - · EWIMP \Rightarrow loop-induced $\sigma_{\rm SI}$

 - pNGB DM : $\mathcal{L} \supset \frac{s}{v} \left[\left(\partial_{\mu} \chi \right)^2 m_{\chi}^2 \chi^2 \right]$ DM with a pseudo-scalar mediator : $\mathcal{L} \supset a \overline{\chi} \gamma_5 \chi \Rightarrow \sigma_{\mathrm{SI}} \propto v_{\chi}^2$
- 2 Sub-GeV DM (unexplored mass region)
 - SIMP (Strongly Interacting Massive Particle)
 - · DM with a new light particle
- 3 Very small interactions with SM
 - · FIMP (Feebly Interacting Massive Particle) $\Rightarrow \lambda \sim 10^{-11}$
 - · Cannibal DM $\Rightarrow \lambda \leq 10^{-8}$, but large couplings in dark sector

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DM models

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EWIMP (ElectroWeak-Intereacting Massive Particle)

Farina et al., JHEP (2013) [arxiv:1303.7244]

Quantum numbers			DM could	DM mass	$m_{\rm DM^{\pm}} - m_{\rm DM}$	Finite naturalness	$\sigma_{ m SI}$ in
$SU(2)_L$	$\mathrm{U}(1)_Y$	Spin	decay into	in TeV	in MeV	bound in TeV	$10^{-46}{\rm cm}^2$
2	1/2	0	EL	0.54	350	$0.4 imes \sqrt{\Delta}$	$(0.4 \pm 0.6) 10^{-3}$
2	1/2	1/2	EH	1.1	341	$1.9 imes \sqrt{\Delta}$	$(0.3 \pm 0.6) 10^{-3}$
3	0	0	HH^*	$2.0 \rightarrow 2.5$	166	$0.22 imes \sqrt{\Delta}$	0.12 ± 0.03
3	0	1/2	LH	$2.4 \rightarrow 2.7$	166	$1.0 imes \sqrt{\Delta}$	0.12 ± 0.03
5	0	1/2	stable	$4.4 \rightarrow 10$	166	$0.4 imes \sqrt{\Delta}$	1.0 ± 0.2
7	0	0	stable	$8 \rightarrow 25$	166	$0.06 imes \sqrt{\Delta}$	4 ± 1

• Quintuplet is automatically stabilized by accidental \mathbb{Z}_2 symmetry.



EWIMP

Gamma-ray line search

Lefranc et al., arXiv:1608.00786

- CTA prospect (expected to start in 2026) Energy range: 20 GeV - 300 TeV
- Both of DM and baryon number is large in Galactic center



Broad gamma-ray search



EWIMP

Disappearing tracks at colliders



SIMP (Strongly Interacting Massive Particle)

Y. Hochberg et al. PRL (2014) [arxiv:1402.5143]

- DM abundance is determined by $3 \rightarrow 2$ or $4 \rightarrow 2$ processes in dark sector, but not $2 \rightarrow 2$ processes (WIMP).
- \blacksquare Kinetic eq. with the SM at least until $2 \rightarrow 2$ freeze-out.

Condition for thermal SIMP: $\Gamma_{ann} < \Gamma_{3\rightarrow 2} < \Gamma_{kin}$



 $\begin{array}{l} \mathbf{m}_{\chi} \sim \mathcal{O}(10) \text{ MeV for } 3 \rightarrow 2 \text{ process} \\ \frac{dn}{dt} + 3Hn = -\langle \sigma_{3 \rightarrow 2} v^2 \rangle \left(n^3 - n^2 n_{\text{eq}} \right) \end{array} \begin{array}{l} \text{Ex: } \mathbb{Z}_3 \text{ symmetry} \\ V \supset \kappa \chi^3 + \text{h.c.} + \frac{\lambda}{4} |\chi|^4 \end{array}$

 $m_{\chi} \sim \mathcal{O}(100)$ keV for $4 \rightarrow 2$ process \Rightarrow naively conflict with BBN

SIMP properties

Y. Hochberg et al. PRL (2014) [arxiv:1402.5143]

Large self-interactions are required for observed abundance Ωh² = 0.12.
 Improve small scale problems σ_{self}/m_χ ~ 1 cm²/g.

Ex. core vs cusp problem



Tulin and Yu, Phys.Rept. (2018) [arxiv:1705.02358]

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Cannibal DM



Cannibal DM

Cannibal DM

Pappadopulo et al. PRD (2016) [arxiv:1602.04219], JHEP (2016) [arxiv:1607.03108]



- $\langle \sigma v \rangle$ larger than WIMP is needed for observed relic.
- Indirect detection signals are enhanced.

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FIMP

FIMP (Feebly Interacting Massive Particle)



- FIMP is never thermalized with SM sector, and is slowly produced by decays or scatterings.
- $\Omega_{\text{FIMP}} \propto (\text{coupling})^n$ cf: $\Omega_{\text{WIMP}} \propto (\text{coupling})^{-n}$
- coupling $\sim 10^{-11}$ to reproduce the PLANCK value.
- Candidates: sterile neutrino, Higgs portal DM etc

FIMP signals

Hall et al., JHEP 03 (2010) 080 [arXiv:0911.1120] Hambye et al., PRD (2018) [arXiv:1807.05022]

- Detection of FIMP is challenging.
- Enhanced direct detection rate Ex. DM coupled with a light dark photon $\mathcal{L} \supset -\frac{\epsilon}{2}F_{\mu\nu}F'^{\mu\nu}$



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13th September 2022

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FIMP

Summary of DM models



• χ : DM, f: SM particles, ϕ : light dark sector particles

Other candidates

Other possibilities

ELDER (ELastically DEcoupling Relic) Kuflik et al., PRL 116, 221302 (2016)



2 Zombie DM Kramer et al., PRL 126, 081802 (2021)

· Reduce DM numbers by $\chi \zeta^{\dagger} \rightarrow \zeta \zeta$

· thermal production is possible even if DM mass is heavy as 10^8 GeV without violating the unitarity bound.



A pseudo-Nambu-Goldstone DM

The simplest pNGB DM model

C. Gross, O. Lebedev, TT, PRL (2017)

- Introduce complex scalar field $S = (s + i\chi)/\sqrt{2}$
- Global U(1) symmetry is assumed (invariant under $S \rightarrow e^{i\alpha}S$)

$$\begin{split} \mathcal{V} = & -\frac{\mu_H^2}{2} |H|^2 - \frac{\mu_S^2}{2} |S|^2 + \frac{\lambda_H}{2} |H|^4 + \lambda_{HS} |H|^2 |S|^2 + \frac{\lambda_S}{2} |S|^4 \\ & - \left(\frac{\mu_S'^2}{4} S^2 + \text{H.c.}\right) \quad \leftarrow \text{ soft breaking mass term} \end{split}$$

 \blacksquare After H and S get VEVs, ϕ and s mix

$$H = \begin{pmatrix} 0 \\ (v + \phi)/\sqrt{2} \end{pmatrix}, \qquad S = \frac{v_s + s + i\chi}{\sqrt{2}}$$
$$\begin{pmatrix} \phi \\ s \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$$

• $\sin \theta \lesssim 0.3 \quad \leftarrow \text{Constrained by EWPT}$, h_2 direct search at LHC

Model

Bound on $\sin \theta$ A. Falkowski et al., JHEP 1505 (2015) [arxiv:1502.01361]



- **Red**: h_2 direct search at LHC
- Yellow: h_1 coupling measurements
- Green: Favored region from stability of scalar potential
- Gray: Electroweak precision tests

$$|\sin\theta| \lesssim 0.3 \text{ if } m_{h_2} \gtrsim m_{h_1}$$

• $m_{\chi} \leq m_{h_2}$ (above EW scale)

Direct detection (tree level) C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]



Scattering amplitude cancels between h_1, h_2 mediated diagrams

$$i\mathcal{M} \sim i\left(\frac{m_{h_1}^2}{q^2 - m_{h_1}^2} - \frac{m_{h_2}^2}{q^2 - m_{h_2}^2}\right) \sim i\frac{q^2(m_{h_1}^2 - m_{h_2}^2)}{m_{h_1}^2 m_{h_2}^2} \to 0$$

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Direct detection (tree level) C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

Rewrite with
$$S = \frac{(v_s + s)}{\sqrt{2}} e^{i\chi/v_s} \Rightarrow \mathcal{L} \supset \frac{1}{v_s} s \left[(\partial_\mu \chi)^2 - m_\chi^2 \chi^2 \right]$$



The cancellation is due to nature of Goldstone boson

All interactions are written with derivative couplings $\mathcal{L}_{int} = \mathcal{L}_{int}(\partial_{\mu}\chi)$

• Only 4 independent parameters $(m_{\chi}, m_{h_2}, \sin \theta, v_s (\lambda_S))$

D. Azevedo et al., JHEP [arXiv:1810.06105] K. Ishiwata, TT, JHEP [arXiv:1810.08139] S. Glaus et al., JHEP [arXiv:2008.12985] Direct detection (1-loop level)

Compute Feynman diagrams at 1-loop level



q

(i) self-energy correction

q

q

- (ii) vertex correction
- (iii) box and triangle \rightarrow two Yukawa couplings
 - \rightarrow sub-dominant in most cases

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Numerical analysis (1-loop level) K. Ishiwata, TT, JHEP [arXiv:1810.08139]



 $\sin \theta = 0.1$

- Invisible Higgs decay $Br(h_1 \rightarrow inv) \leq 20\%$ at LHC
- $\sigma_{\rm SI}^p = \mathcal{O}(10^{-48}) \ {\rm cm}^2$ at most
- Unitarity bound: $\lambda_S \leq 8\pi/3$
- More recent calculation: Glaus et al., JHEP 12 (2020) 034 [arXiv:2008.12985]

Numerical analysis (1-loop level) K. Ishiwata, TT, JHEP [arXiv:1810.08139]



 $\sin \theta = 0.2$

- Invisible Higgs decay $Br(h_1 \rightarrow inv) \leq 20\%$ at LHC
- $\sigma_{\rm SI}^p = \mathcal{O}(10^{-48}) \ {\rm cm}^2$ at most
- Unitarity bound: $\lambda_S \leq 8\pi/3$
- More recent calculation: Glaus et al., JHEP 12 (2020) 034 [arXiv:2008.12985]

Domain wall problem

- Domain walls due to spontaneous breaking of \mathbb{Z}_2 symmetry \Rightarrow distort CMB
- Solutions: UV compettion
 - · low energy inflation after the \mathbb{Z}_2 breaking
 - · decay before BBN (making the domain wall unstable)



Press, Ryden, Spergel ApJ (1989)

UV completion Y. Abe, TT, K. Tsumura, JHEP (2020) [arXiv:2001.03954]

• Origin of the soft breaking term? $\frac{m_{\chi}^2}{4}S^2 + H.c.$

	Q_L	u_R^c	d_R^c	L	e_R^c	Н	ν_R^c	S	Φ
$SU(3)_c$	3	$\overline{3}$	$\overline{3}$	1	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	2	1	1	1
$U(1)_Y$	+1/6	-2/3	+1/3	-1/2	+1	+1/2	0	0	0
$U(1)_{B-L}$	+1/3	-1/3	-1/3	-1	+1	0	+1	+1	+2

- Gauged $U(1)_{B-L}$ extension (New fields: ν_R , Φ)
- Potential $\mathcal{V} \supset \mu_c \Phi^* S^2 + h.c. \rightarrow m_{\chi}^2 S^2$ at low energy The soft breaking term is induced.
- **3** ν_R for anomaly cancellation
 - Seesaw for ν mass $\mathcal{L} \supset \Phi \nu_R \nu_R$

GUT embedding Y. Abe, TT, K. Tsumura, N. Yamatsu, PRD (2021) [arXiv:2104.13523]

		fermions	H	S	Φ	<u>SO(10)</u>
	A_{μ}	Ψ_{16}	Φ ₁₀	Φ ₁₆	$\Phi_{\overline{126}}$	Φ ₂₁₀
SO(10)	45	16	10	16	$\overline{126}$	210

- We embed the UV complete model in SO(10) GUT.
- The pNGB model is reproduced at low energy.
- Breaking pattern: SO(10) → G_{PS} → G_{SM} at µ = M_U at µ = M_I
 Pati-Salam symmetry: G_{PS} = SU(4)_C × SU(2)_L × SU(2)_R
 GUT scale (M_U) Intermediate scale (M_I) = breaking scale of U(1)_{B-L},
- Proton decay SK limit: $\tau_{p \to e^+\pi^0} > 2.4 \times 10^{34}$ years Rough estimate: $\tau \sim (\alpha_U^2 m_p^5 / M_U^4)^{-1} = 1.1 \times 10^{37}$ years

Gauge coupling unification



1-loop RGEs are solved.

Intermediate scale, GUT scale: determined by matching conditions of gauge couplings

$$v_{\phi} = M_I = 1.26 \times 10^{11} \text{ GeV}, \ M_U = 2.06 \times 10^{16} \text{ GeV}$$

 $g_{B-L} = 0.38 \text{ at } \mu = M_I$

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DM decay

 χ

DM decay

 χ

DM lifetime: $\tau_{\rm DM} \gtrsim 10^{17}$ sec at least (the age of the universe).

 h_i

Cosmic ray observations give stronger limits: $\tau_{\rm DM} \gtrsim 10^{27}$ sec. 3-body decays $\chi \to ffh_i, ffZ$ if $m_{\chi} \gtrsim m_{h_i}, m_Z \rightarrow \text{excluded}$



Parameter space



•
$$v/v_s \sim \sqrt{\lambda_S}$$

Fermi-LAT: $\chi\chi \to b\bar{b}, WW \to \gamma$ production

• close to the h_2 resonance

Other variations of pNGB DM

- **THDM** + S with global U(1) Zhang, Cai, Jiang, Tang, Yu, Zhang, JHEP 05 (2021) 160
 - \Rightarrow Gravitational waves from strong 1st order phase transition



■ pNGB from global SU(2) Abe and Hamada, arXiv: 2205.11919 ⇒ No domain wall problem, two-component DM

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Summary

- Dark matter direct detection experiments impose the strong bounds on the scattering cross section.
 Wayout: suppression of scattering, sub-GeV mass, very small couplings
- 2 A pNGB dark matter is a candidate naturally avoiding the bounds.
- **3** UV completion and GUT embedding have been done.

The simplest pNGB DM model

C. Gross, O. Lebedev, TT, PRL (2017)

\$\chi_{\chi}\$ is mass eigenstate itself \$m_{\chi_{\chi}}^2 = \mu_S'^2\$ Invariant under \$S \rightarrow S^{\dagger}\$, \$\Rightarrow \chi_{\chi}\$ can be a DM candidate
 Higgs portal DM

Scalar potential $\mathcal{V} = \mu_{h_1\chi\chi}h_1\chi^2 + \mu_{h_2\chi\chi}h_2\chi^2 + \cdots$ $\mu_{h_1\chi\chi} = -\frac{m_{h_1}^2 \sin \theta}{v_c}, \quad \mu_{h_2\chi\chi} = \frac{m_{h_2}^2 \cos \theta}{v_c},$ SM Yukawa int. $\mathcal{L} \supset y_q \Big(\cos \theta h_1 + \sin \theta h_2\Big) \overline{q} q$ $\lambda_{H} = \frac{\cos^{2}\theta m_{h_{1}}^{2} + \sin^{2}\theta m_{h_{2}}^{2}}{n^{2}}, \quad \lambda_{S} = \frac{\sin^{2}\theta m_{h_{1}}^{2} + \cos^{2}\theta m_{h_{2}}^{2}}{n^{2}},$ $\lambda_{HS} = \frac{\sin\theta\cos\theta(m_{h_2}^2 - m_{h_1}^2)}{2}$ $\mathcal{V}\mathcal{V}_{c}$

Direct detection (1-loop level) K. Ishiwata, TT, JHEP [arXiv:1810.08139]

Compute Feynman diagrams at 1-loop level

$$\sigma_{\rm SI}^N = \frac{1}{\pi} \frac{m_N^2}{(m_\chi + m_N)^2} |f_{\rm scalar}^N|^2$$

where $\frac{f_{\text{scalar}}^N}{m_N} = \sum_{q=u,d,s} C_S^q f_{Tq}^N - \frac{8}{9} C_S^G f_{Tg}^N \quad (f_{Tq}^N, f_{TG}^N: \text{ nucleon matrix elements})$

$$\langle N|m_q \overline{q}q|N\rangle = f_{Tq}^N m_N, \quad \langle N|\frac{\alpha_s}{\pi} G^a_{\mu\nu} G^{a\mu\nu}|N\rangle = -\frac{8}{9} f_{Tg}^N m_N$$

 f_{Tq}^N, f_{Tg}^N are calculated by QCD lattice simulation

 $\mathcal{L}_{\text{eff}} = C_S^q m_q \chi^2 \overline{q} q + C_S^G \frac{\alpha_s}{\pi} \chi^2 G_{\mu\nu}^a G^{a\mu\nu} \quad \leftarrow C_S^q \text{ and } C_S^G \text{ (calculated)}$

Calculate up to 2-loop level in terms of QCD α_s (NLO) \rightarrow scattering amplitude is $\mathcal{O}(\alpha_s)$ J. Hisano, K. Ishiwata, N. Nagata, arXiv:1504.00915

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Direct detection (1-loop level) K. Ishiwata, TT, JHEP [arXiv:1810.08139]



(i)+(ii) is dominant for large DM mass
NLO is O(10%) correction

Origin of the soft term C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

U(1) is extended to gauge symmetry, and a new field \$\Delta\$ is introduced
Odd charge for \$S\$, even charge for \$\Delta\$

Ex.
$$q_S = 3$$
, $q_{\Phi} = 2$
 $\mathcal{V} \supset \frac{1}{\Lambda} \Phi^{\dagger^3} S^2 + \frac{1}{\Lambda^3} \Phi^{\dagger^3} |H|^2 S^2 + \frac{1}{\Lambda^3} \Phi^{\dagger^3} |S|^2 S^2 + \cdots$

- After Φ gets a VEV, μ'_S is generated ($\mu'^2_S = \langle \Phi \rangle^3 / \Lambda$)
- Other terms are suppressed by higher dimensional operators \rightarrow the previous model is reproduced in low energy
- CP violation induces DM decay

$$\mathcal{V} \supset \left(\frac{\langle \Phi \rangle}{\Lambda}\right)^3 |H|^2 s \chi \longrightarrow \text{lifetime } \tau_{\chi} \sim \frac{8\pi}{100 \text{ GeV}} \left(\frac{\Lambda}{\langle \Phi \rangle}\right)^6$$

Ex. when $\Lambda = 10^{16} \text{ GeV}$, $\langle \Phi \rangle = 10^7 \text{ GeV} \Rightarrow \tau_{\chi} \sim 10^{29} \text{ s}$

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Majorana DM model

G. Arcadi et al., JCAP 1803 (2018), T. Abe et al. arxiv:1810.01039, ···

Majorana DM interacting with pseudo-scalar

$$\mathcal{L} \supset \frac{g_{\chi}}{2} a \overline{\chi} \gamma_5 \chi - c_2 a^2 |H_2|^2 + \cdots \rightarrow i \mathcal{M} \sim \overline{u} \gamma_5 u \sim \boldsymbol{q} \cdot \boldsymbol{J}_{1/2}$$

- Two Higgs Doublet + fermion DM (χ) + pseudo-scalar (a).
- Tree level amplitude vanishes in non-relativistic limit



Indirect detection

DM annihilations

 $\chi\chi \to h_i h_j, WW, ZZ, f\overline{f}$

- Gamma-rays are produced at the end
- Constraints from dSphs

(less visible matter and more DM)





- $\mathcal{O}(50)$ dSphs have been found so far.
- DM models are constrained.

Indirect detection



L. Roszkowski et al., Rept.Prog.Phys. 81 (2018), [arXiv:1707.06277]

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Indirect detection

Huitu, Koivunen, Lebedev, Mondal, TT, arXiv:1812.05952



- Small parameter space is excluded by Fermi-LAT gamma-ray observation
- Thermal WIMP scenarios can be tested only when m_{\chi} = O(100) GeV
 CTA is sensitive in heavy DM mass region (DM profile dependent) (\(\chi \chi \chi \chi h_2 h_2 may dominate in this mass range)\)

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Collider search

Huitu, Koivunen, Lebedev, Mondal, TT, PRD (2019) [arXiv:1812.05952]

Constraint on h_2 production cross section at LHC

 $\sigma_{\text{prod}} = \sigma(pp \to h_2) \operatorname{Br}(h_2 \to \operatorname{SM}) \propto \sin^2 \theta \operatorname{Br}(h_2 \to \operatorname{SM})$

■ $pp \rightarrow h_2 \rightarrow ZZ$ mode When $\sin \theta \gtrsim 0.2$ and $m_{h_2} \lesssim 2m_{h_1}$, parameters are constrained.

Back Up



Collider search

Huitu, Koivunen, Lebedev, Mondal, TT, PRD (2019) [arXiv:1812.05952]

- Signal channel (VBF)
 h₁ and h₂, both contributions are important
- We focus on $m_{h_2} \geq 2m_{\chi}$
- Simulate the events and put appropriate cuts *E*_T > 250 GeV, p_j > 80 GeV etc



- Signal significance $S = \frac{S}{\sqrt{S + B + \sigma_B^2}}$
- Background $B \pm \sigma_B = 1779 \pm 96$ at 35.9 fb⁻¹ (CMS)
- Analyzed with 3000 fb^{-1} .



Signal significance can be S ≈ 4 − 6 at most.
 m_χ ≤ 100 GeV can be visible.

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Direct detection for light DM (electron scattering)



- SENSEI: ongoing, Oscura: next generation
- **7**–8 orders of magnitude improvement is expected.

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