

Pseudo-Nambu-Goldstone boson as thermal dark matter

Takashi Toma



Kashiwa dark matter symposium 2021 at virtual

Based on PRL 119 191801, JHEP 1812 (2018) 089,
PLB 822 (2021) 136639,
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Collaborators:

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Yoshihiko Abe (Kyoto), Koji Tsumura (Kyushu) and more

Outline

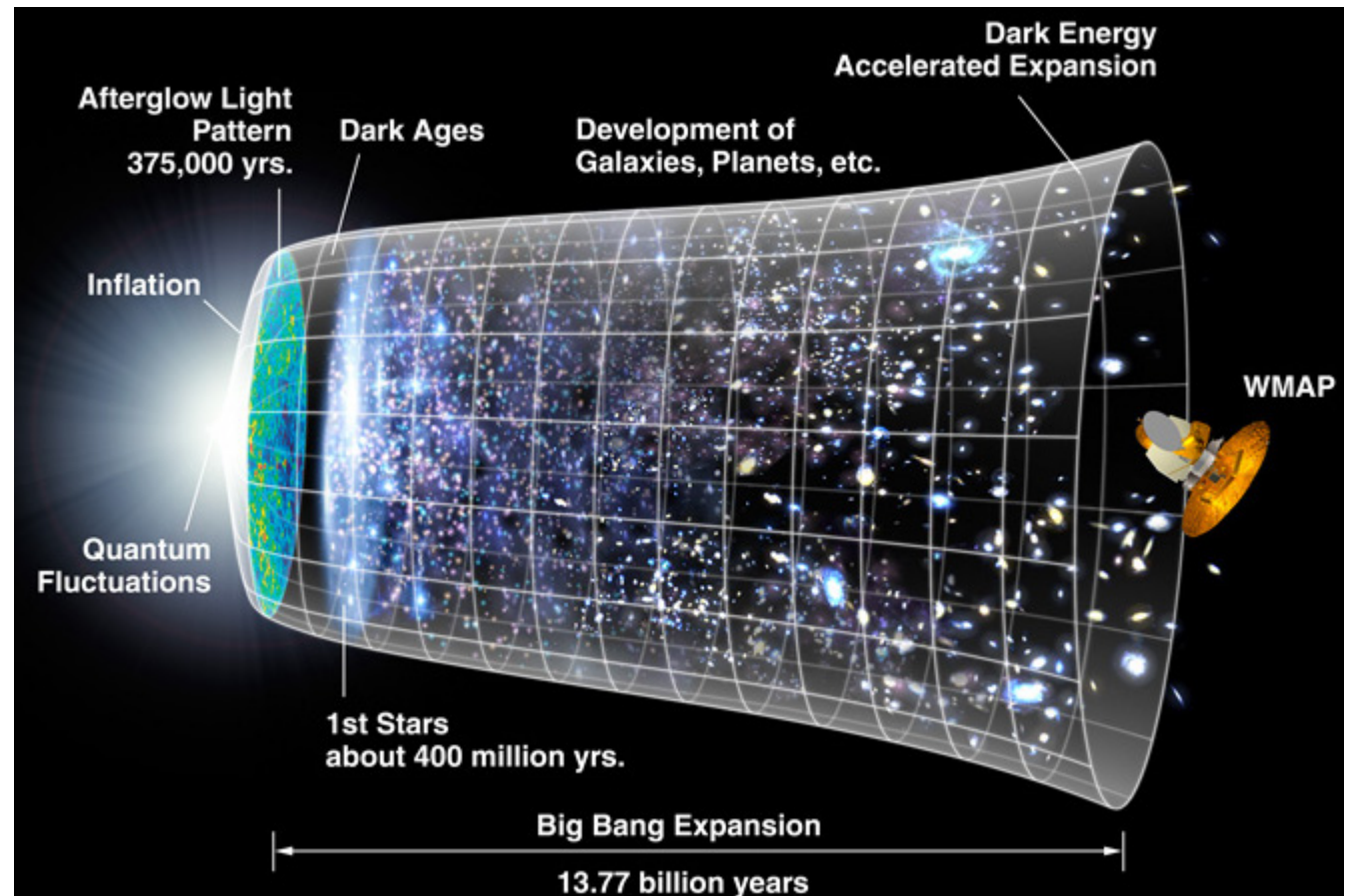
- 1 Introduction
 - WIMP
- 2 Pseudo-Nambu-Goldstone dark matter (pNGB DM)
 - Model
 - Direct detection (tree, 1-loop)
 - Direct detection with light mediator
- 3 Summary

Nature of DM

- Stable (at least longer than age of universe)
- Electrically neutral (may have very small charge)
- Occupy 27% of energy density of the universe
- Gravitational interaction
- Non-relativistic (cold)

Strong candidates:
 WIMP, FIMP, SIMP,
 axion, sterile neutrino,
 primordial black holes
 etc

↑
 Revived by recent obser-
 vations of gravitational
 waves

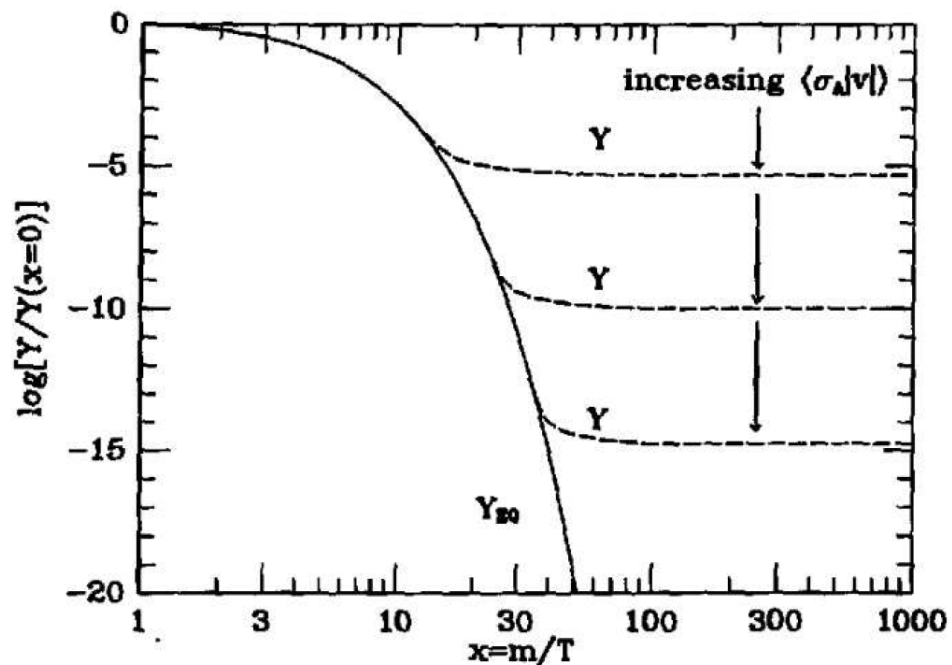


WIMP thermal production

Evolution of DM number density follows the Boltzmann eq.

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle (n_\chi^2 - n_\chi^{\text{eq}2})$$

change variables $t \leftrightarrow x \equiv \frac{m}{T}$, $n_\chi \leftrightarrow Y \equiv \frac{n_\chi}{s}$, $\Gamma \equiv \langle\sigma v\rangle n_\chi^{\text{eq}}$,



- DM relic is determined by $\langle\sigma v\rangle$.

- σv can be expanded by v .

$$\rightarrow \sigma v = a + bv^2 + \mathcal{O}(v^4)$$

a : s-wave, b : p-wave

- $\Omega h^2 \sim \frac{10^{-10} [\text{GeV}^{-2}]}{\langle\sigma v\rangle} \sim 0.1$

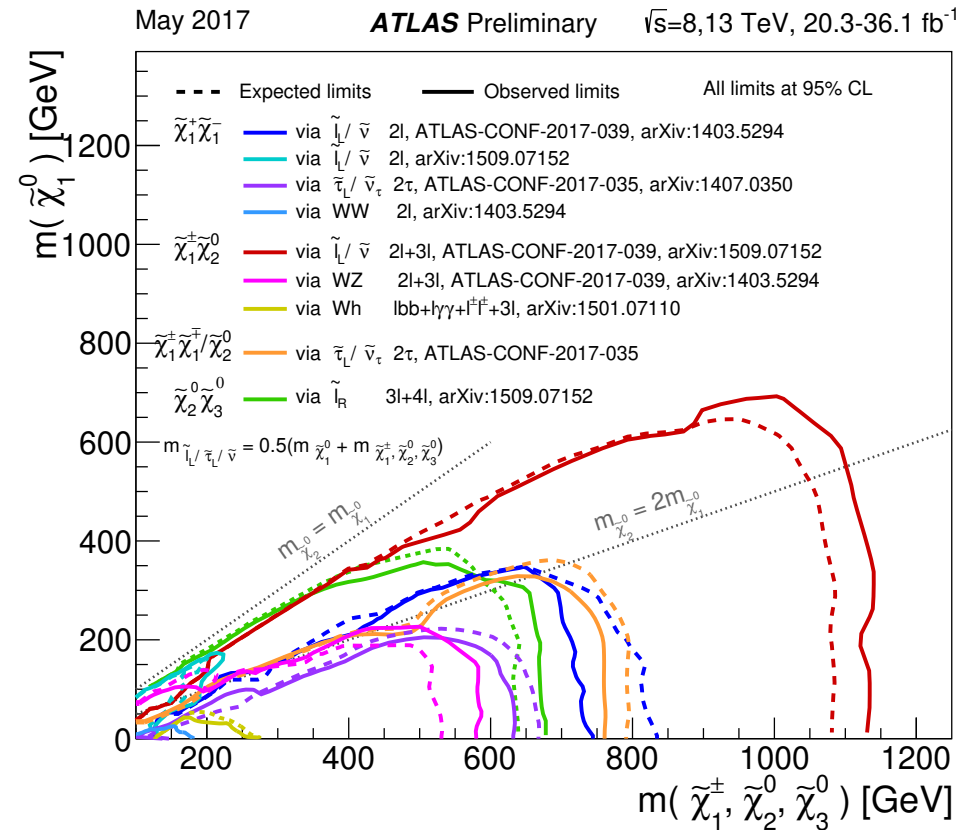
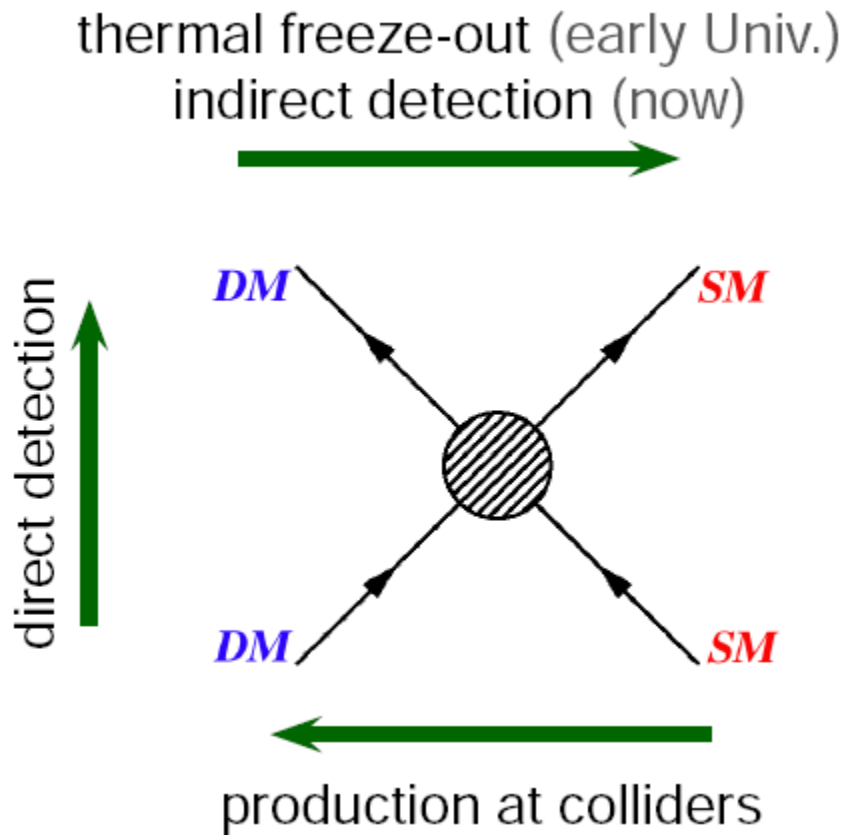
(Planck Coll.)

$$\rightarrow \langle\sigma v\rangle \sim 10^{-9} [\text{GeV}^{-2}]$$

$$\approx 10^{-26} [\text{cm}^3/\text{s}]$$

WIMP search status

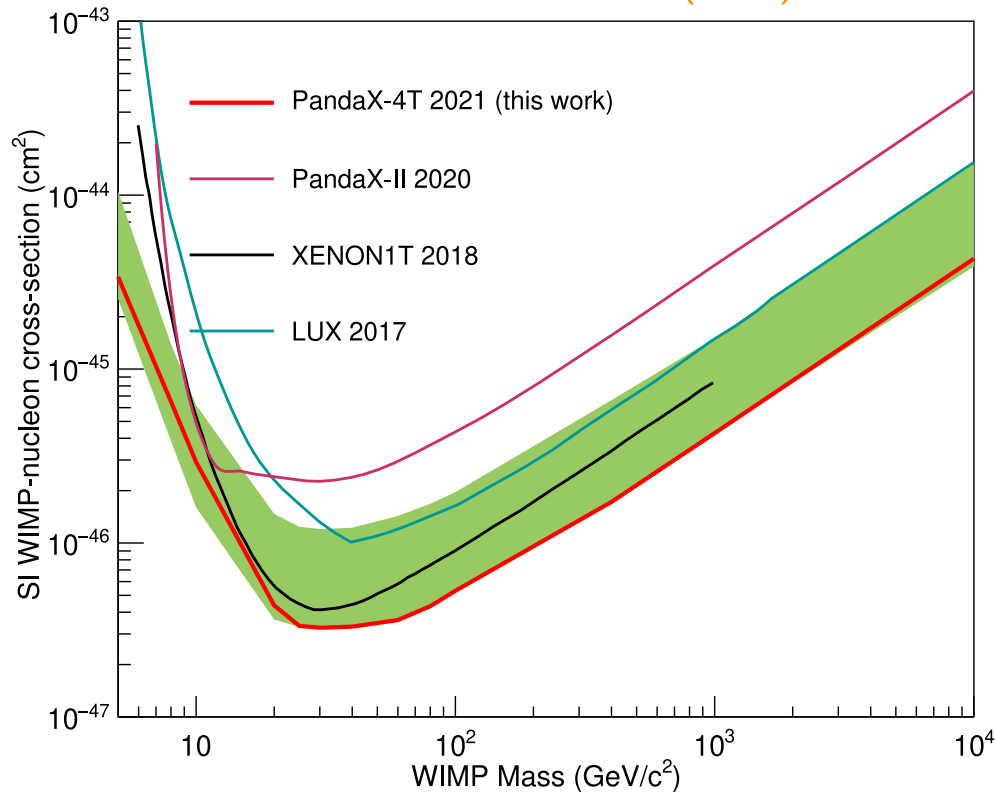
Collider search Summary plot from ATLAS



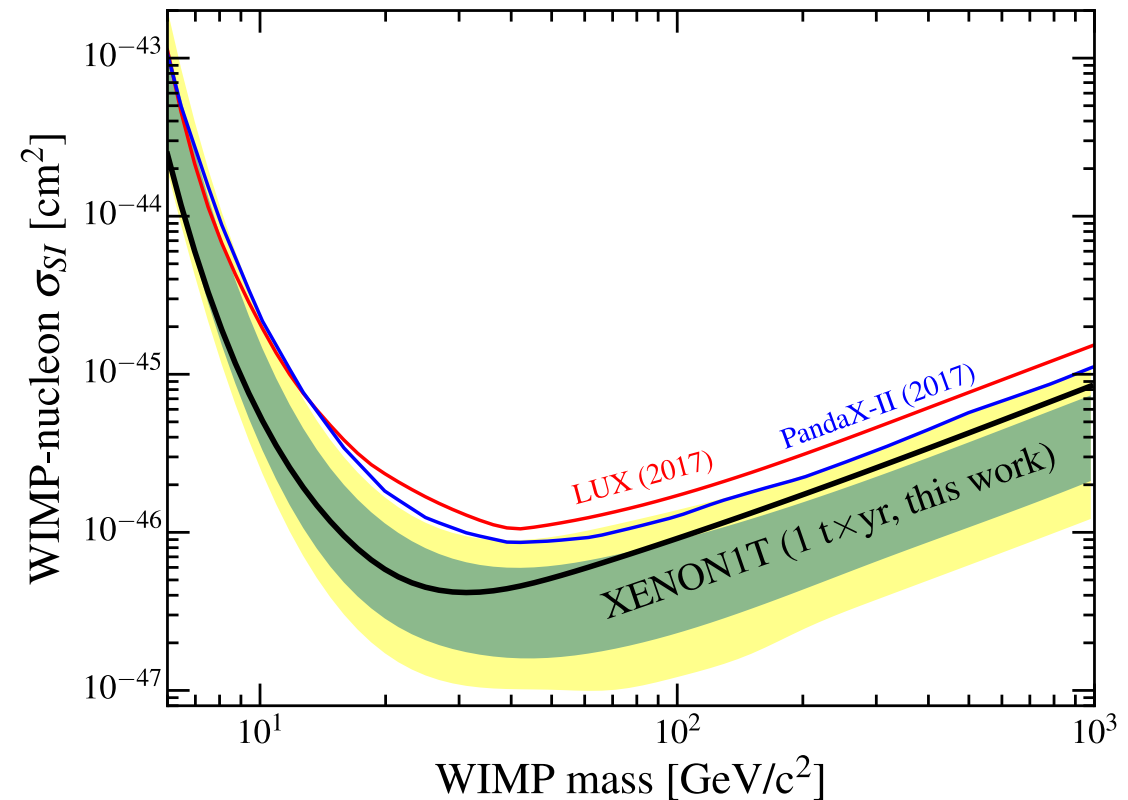
- WIMP DM can experimentally be detectable.
- Collider search: mass degenerate is required.

WIMP search status

Direct detection PandaX-4T (2021) 2107.13438



XENON1T (2020)



- Experimental bounds are stronger and stronger.
- Interactions between DM and SM are very weak? \rightarrow non-WIMP DM?

In this talk, I will consider a simple DM model naturally evading the strong DD constraint. \Rightarrow pseudo-Nambu-Goldstone boson

Pseudo-Nambu-Goldstone DM

PNGB DM model

C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

- Introduce complex scalar field $S = (s + i\chi)/\sqrt{2}$
- Global $U(1)$ symmetry is assumed (invariant under $S \rightarrow e^{i\alpha} S$)

$$\mathcal{V} = -\frac{\mu_H^2}{2}|H|^2 - \frac{\mu_S^2}{2}|S|^2 + \frac{\lambda_H}{2}|H|^4 + \lambda_{HS}|H|^2|S|^2 + \frac{\lambda_S}{2}|S|^4 - \left(\frac{\mu_S'^2}{4} S^2 + \text{H.c.} \right) \leftarrow \text{soft breaking mass term}$$

- After H and S get VEVs, ϕ and s mix

$$H = \begin{pmatrix} 0 \\ (v + \phi)/\sqrt{2} \end{pmatrix}, \quad S = \frac{v_s + s + i\chi}{\sqrt{2}}$$

$$\begin{pmatrix} \phi \\ s \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$$

- $\sin \theta \lesssim 0.3$ \leftarrow Constrained by EWPT, h_2 direct search at LHC

PNGB DM model

C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

- χ is mass eigenstate itself $m_\chi^2 = \mu_S'^2$
Invariant under $S \rightarrow S^\dagger$, $\Rightarrow \chi$ can be a DM candidate

- Higgs portal DM

- Scalar potential $\mathcal{V} = \mu_{h_1\chi\chi} h_1 \chi^2 + \mu_{h_2\chi\chi} h_2 \chi^2 + \dots$

$$\mu_{h_1\chi\chi} = -\frac{m_{h_1}^2 \sin \theta}{v_s}, \quad \mu_{h_2\chi\chi} = \frac{m_{h_2}^2 \cos \theta}{v_s},$$

SM Yukawa int. $\mathcal{L} \supset y_q (\cos \theta h_1 + \sin \theta h_2) \bar{q} q$

$$\lambda_H = \frac{\cos^2 \theta m_{h_1}^2 + \sin^2 \theta m_{h_2}^2}{v^2}, \quad \lambda_S = \frac{\sin^2 \theta m_{h_1}^2 + \cos^2 \theta m_{h_2}^2}{v_s^2},$$

$$\lambda_{HS} = \frac{\sin \theta \cos \theta (m_{h_2}^2 - m_{h_1}^2)}{v v_s}$$

UV completion Y. Abe, TT, K. Tsumura, JHEP (2020) [arXiv:2001.03954]

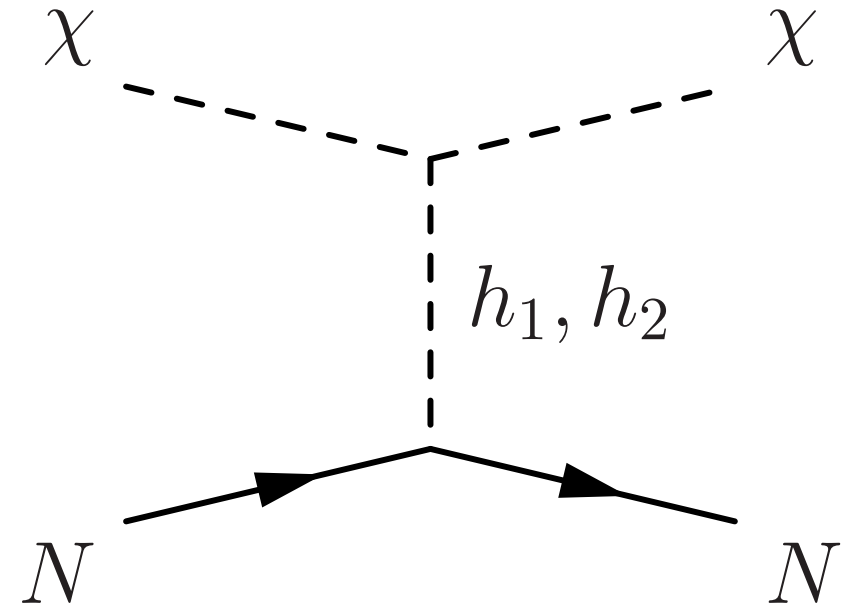
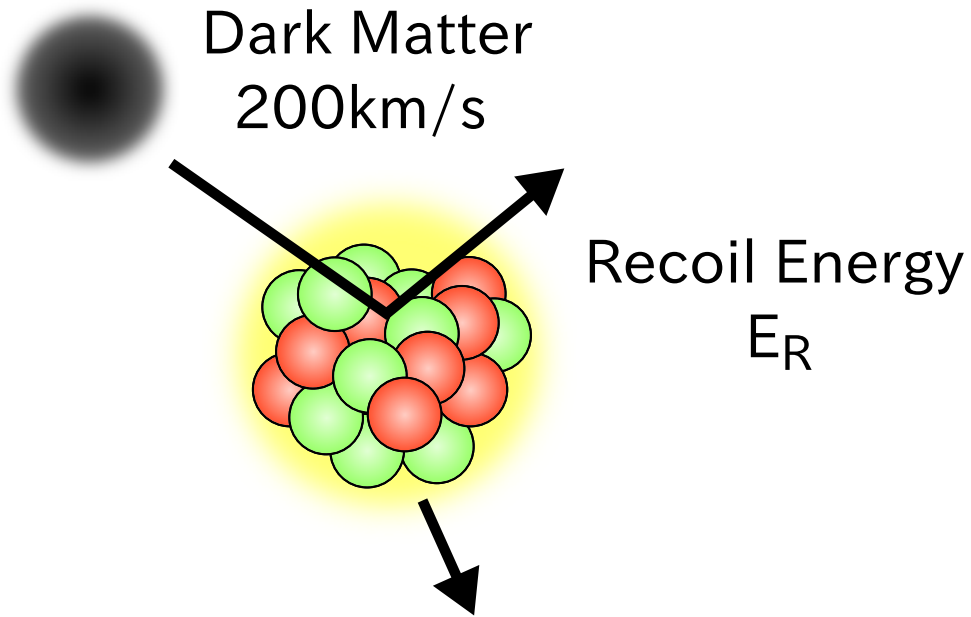
- Origin of the soft breaking term? $\frac{m_\chi^2}{4} S^2 + \text{H.c.}$

| | Q_L | u_R^c | d_R^c | L | e_R^c | H | ν_R^c | S | Φ |
|--------------|----------|--------------------|--------------------|----------|----------|----------|-----------|----------|----------|
| $SU(3)_c$ | 3 | $\bar{\mathbf{3}}$ | $\bar{\mathbf{3}}$ | 1 | 1 | 1 | 1 | 1 | 1 |
| $SU(2)_L$ | 2 | 1 | 1 | 2 | 1 | 2 | 1 | 1 | 1 |
| $U(1)_Y$ | +1/6 | -2/3 | +1/3 | -1/2 | +1 | +1/2 | 0 | 0 | 0 |
| $U(1)_{B-L}$ | +1/3 | -1/3 | -1/3 | -1 | +1 | 0 | +1 | +1 | +2 |

- Gauged $U(1)_{B-L}$ extension (New fields: ν_R, Φ)
- Potential $\mathcal{V} \supset \mu_c \Phi^* S^2 + \text{h.c.} \rightarrow m_\chi^2 S^2$ at low energy
The soft breaking term is induced.
- 3 ν_R for anomaly cancellation
- Seesaw for ν mass $\mathcal{L} \supset \Phi \nu_R \nu_R$

Direct detection (tree level)

C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]



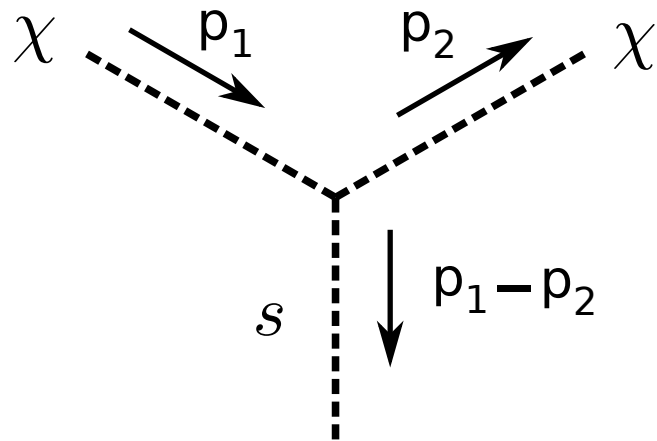
- Scattering amplitude cancels between h_1, h_2 mediated diagrams

$$i\mathcal{M} \sim i \left(\frac{m_{h_1}^2}{q^2 - m_{h_1}^2} - \frac{m_{h_2}^2}{q^2 - m_{h_2}^2} \right) \sim i \frac{q^2(m_{h_1}^2 - m_{h_2}^2)}{m_{h_1}^2 m_{h_2}^2} \rightarrow 0$$

Direct detection (tree level)

C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

$$\text{Rewrite with } S = \frac{(v_s + s)}{\sqrt{2}} e^{i\chi/v_s} \quad \Rightarrow \quad \mathcal{L} \supset \frac{1}{v_s} s \left[(\partial_\mu \chi)^2 - m_\chi^2 \chi^2 \right]$$



$$\rightarrow i\mathcal{M} \sim -\frac{i}{v_s} (p_1 - p_2)^2 \sim -\frac{i}{v_s} m_\chi^2 v_\chi^2 \rightarrow 0$$

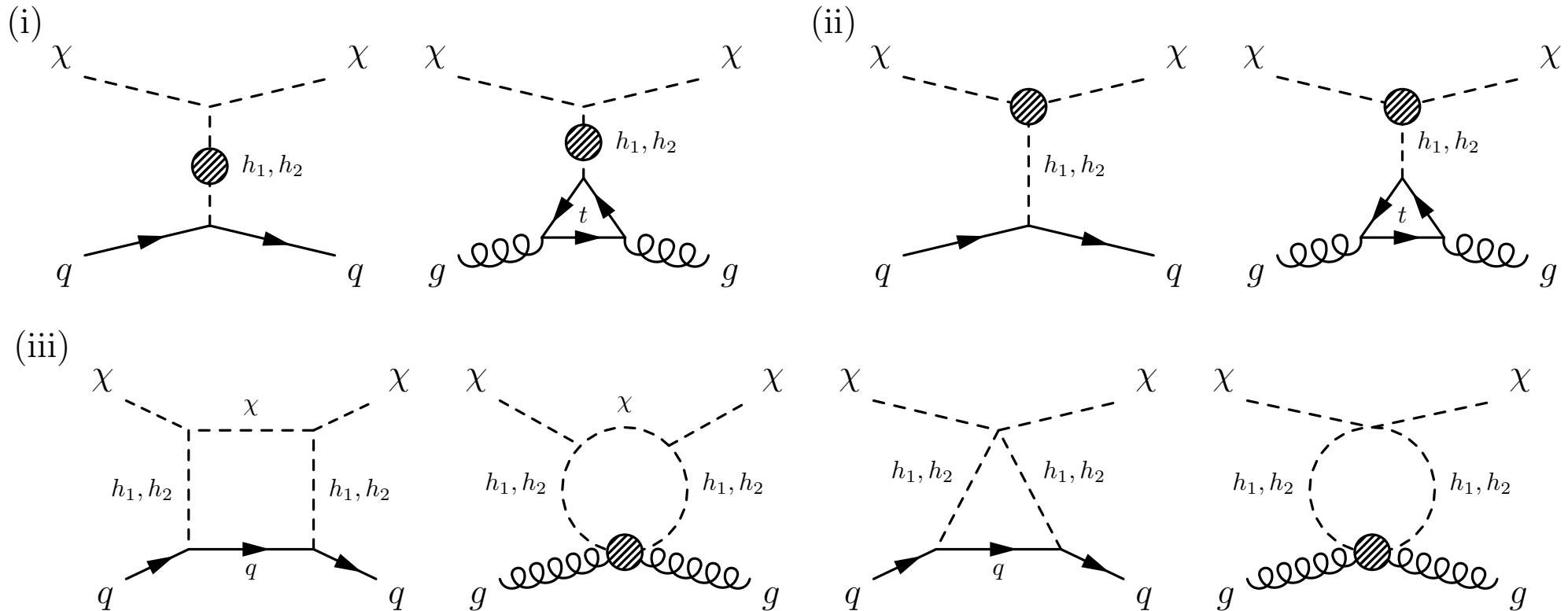
$$v_\chi \sim \mathcal{O}(10^{-3})$$

- Cancellation is due to nature of Goldstone boson
- All interactions are written with derivative couplings $\mathcal{L}_{\text{int}} = \mathcal{L}_{\text{int}}(\partial_\mu \chi)$

Direct detection (1-loop level)

D. Azevedo et al., JHEP [arXiv:1810.06105]
 K. Ishiwata, TT, JHEP [arXiv:1810.08139]
 S. Glaus et al., JHEP [arXiv:2008.12985]

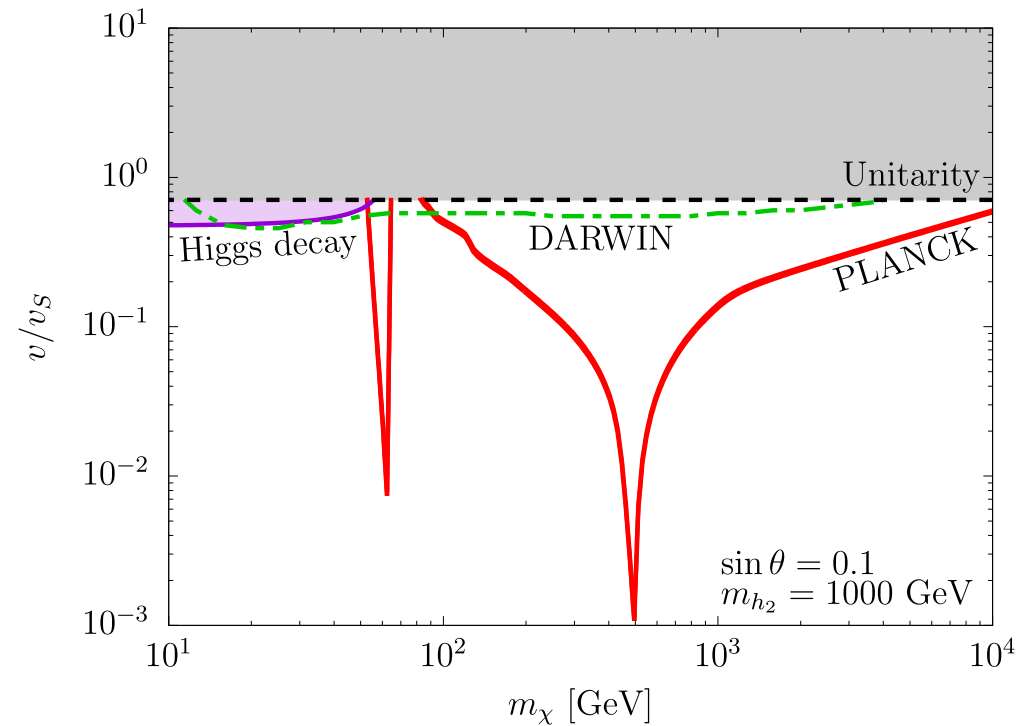
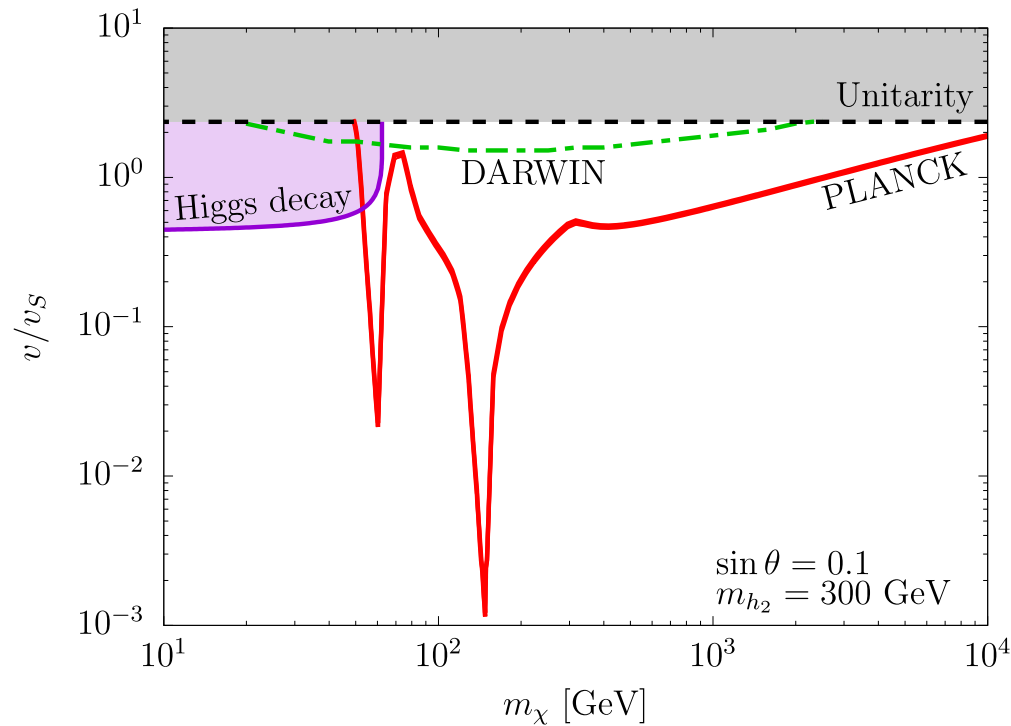
- Compute Feynman diagrams at 1-loop level



- (i) self-energy correction
- (ii) vertex correction
- (iii) box and triangle → two Yukawa couplings
→ sub-dominant in most cases

Numerical analysis (1-loop level)

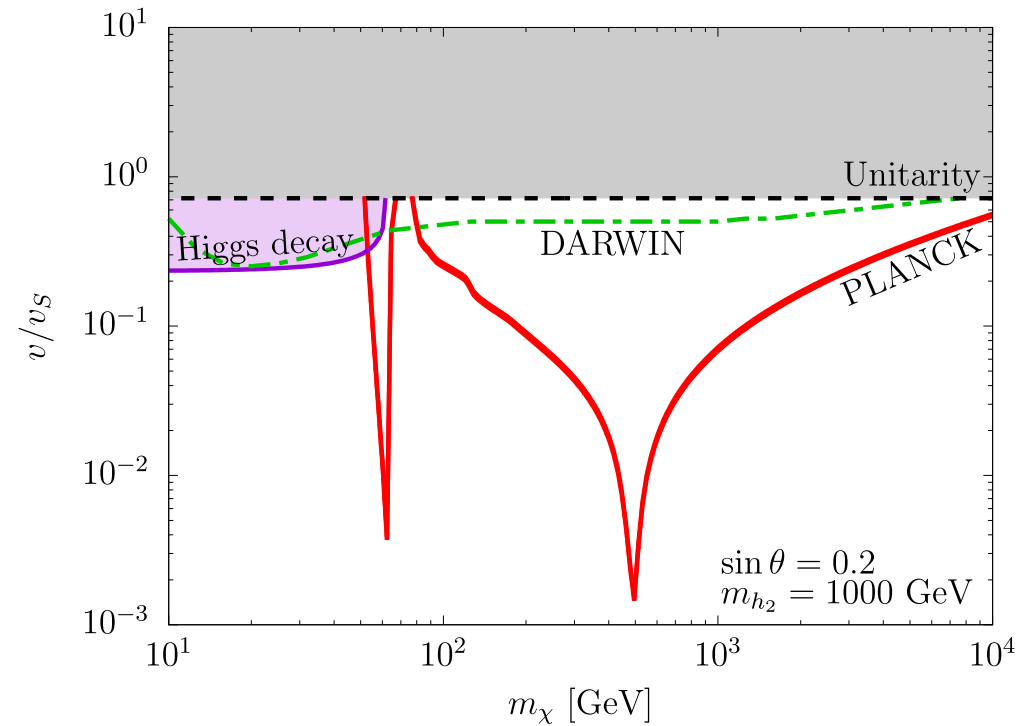
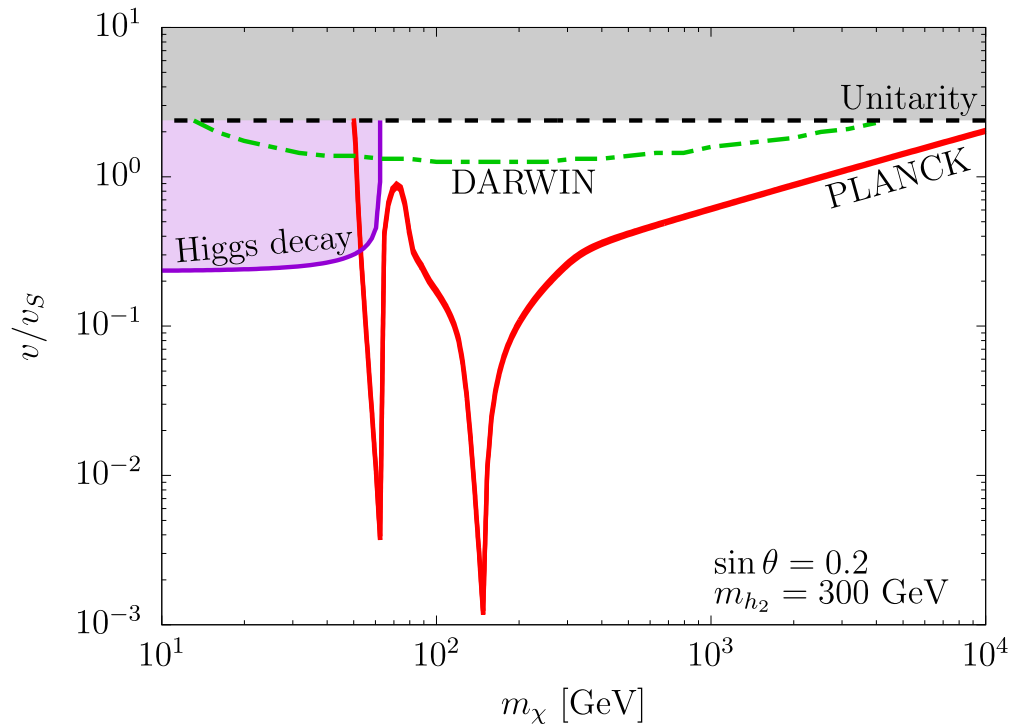
K. Ishiwata, TT, JHEP [arXiv:1810.08139]



- Only 4 independent parameters (m_χ , m_{h_2} , $\sin \theta$, v_s (λ_S))
- $\sin \theta = 0.1$
- Invisible Higgs decay $\text{Br}(h_1 \rightarrow \text{inv}) \lesssim 20\%$ at LHC
- $\sigma_{\text{SI}}^p = \mathcal{O}(10^{-48}) \text{ cm}^2$ at most
- Unitarity bound: $\lambda_S \leq 8\pi/3$

Numerical analysis (1-loop level)

K. Ishiwata, TT, JHEP [arXiv:1810.08139]



- $\sin \theta = 0.2$
- Invisible Higgs decay $\text{Br}(h_1 \rightarrow \text{inv}) \lesssim 20\%$ at LHC
- $\sigma_{\text{SI}}^p = \mathcal{O}(10^{-48}) \text{ cm}^2$ at most
- Unitarity bound: $\lambda_S \leq 8\pi/3$

Pseudo-Nambu-Goldstone DM with light mediator h_2

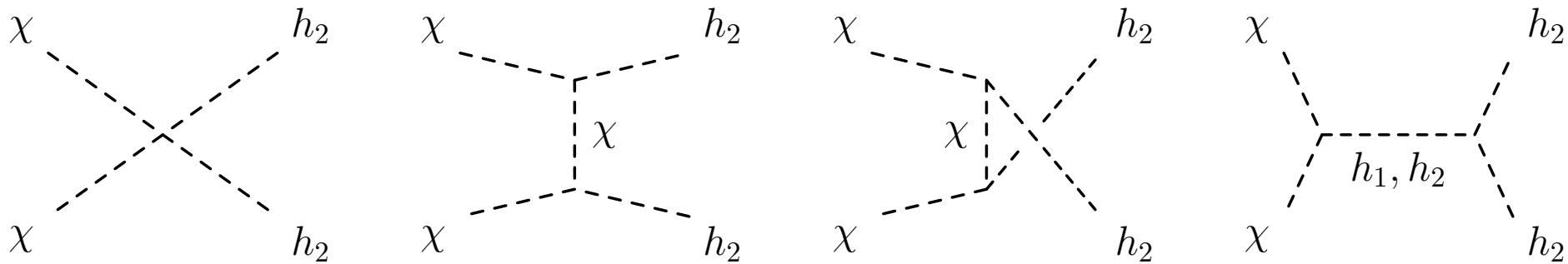
Light mediator h_2

Abe, TT, PLB (2021) [arXiv:2108.10647]

- $m_{h_2} \ll m_\chi$ ($m_{h_2} \gg m_\chi$ since $\mathbb{Z}_2 \rightarrow U(1)$?)

UV completion $\mathcal{V} \supset \mu\Phi^*S^2 \rightarrow \mu\langle\Phi\rangle S^2 \Rightarrow m_{h_2} \ll m_\chi$ if $\langle S \rangle \ll \langle \Phi \rangle$

- Main annihilation channel: $\chi\chi \rightarrow h_2h_2$



$$\sigma_{h_2h_2} v_{\text{rel}} = \frac{\lambda_S^2}{16\pi s} \left| 1 + \frac{m_{h_1}^2}{m_{h_2}^2} \frac{\sin^2 \theta_S}{s - m_{h_1}^2 + im_{h_1}\Gamma_{h_1}} \right|^2$$

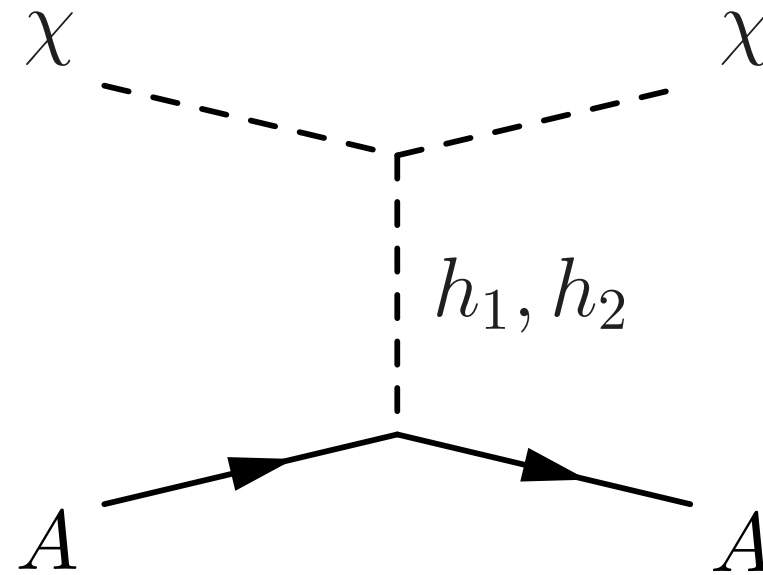
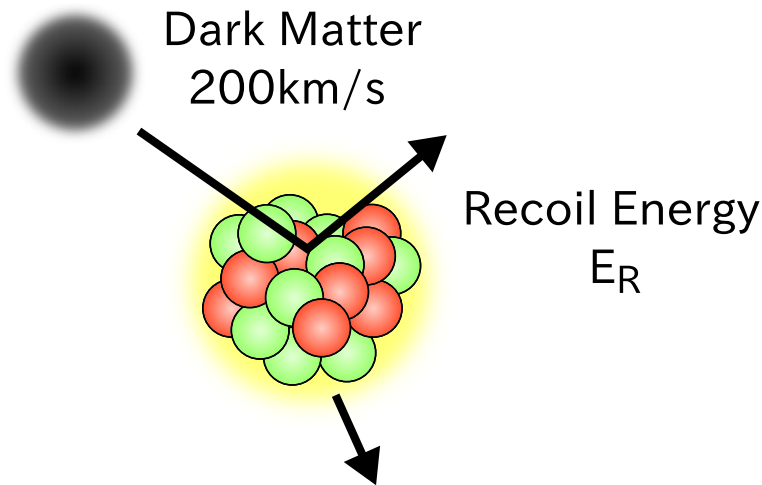
- The other channels: $\chi\chi \rightarrow WW, ZZ, f\bar{f}, h_1h_1, h_1h_2$

$$\sigma v_{\text{rel}} \propto \sin^2 \theta$$

- We focus on the mass range $20 \text{ MeV} \lesssim m_{h_2} \lesssim 200 \text{ MeV}$

Event rate

Abe, TT, PLB (2021) [arXiv:2108.10647]



■ Differential cross section

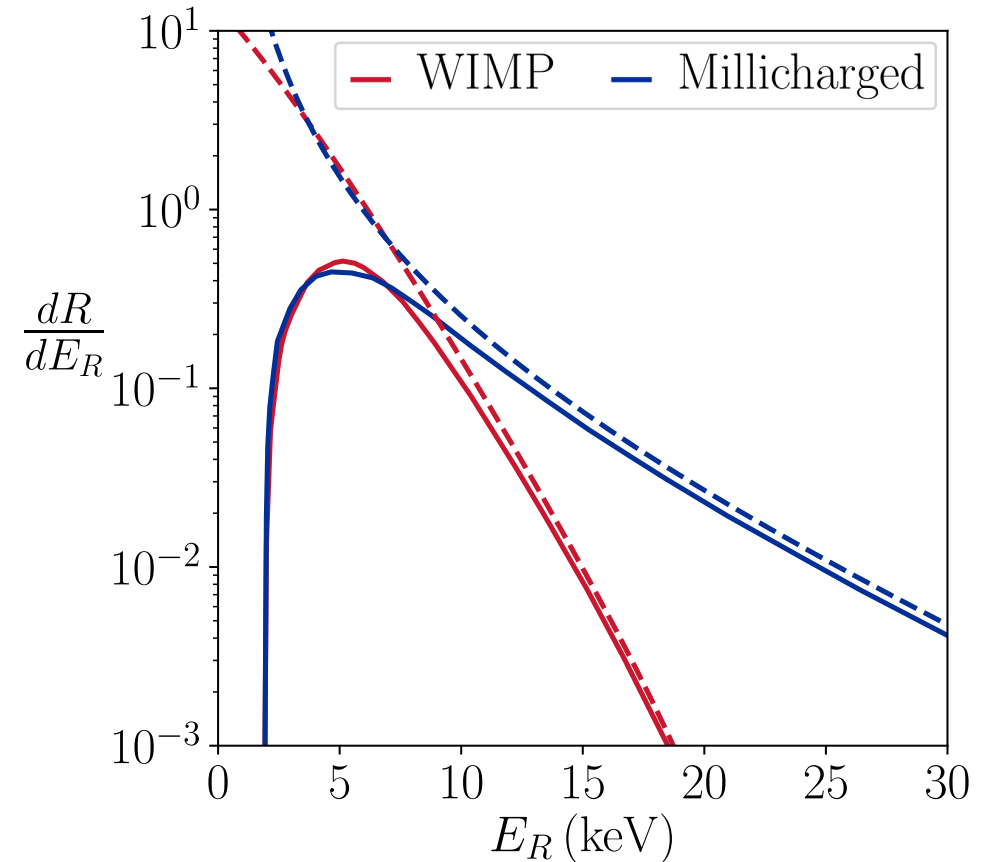
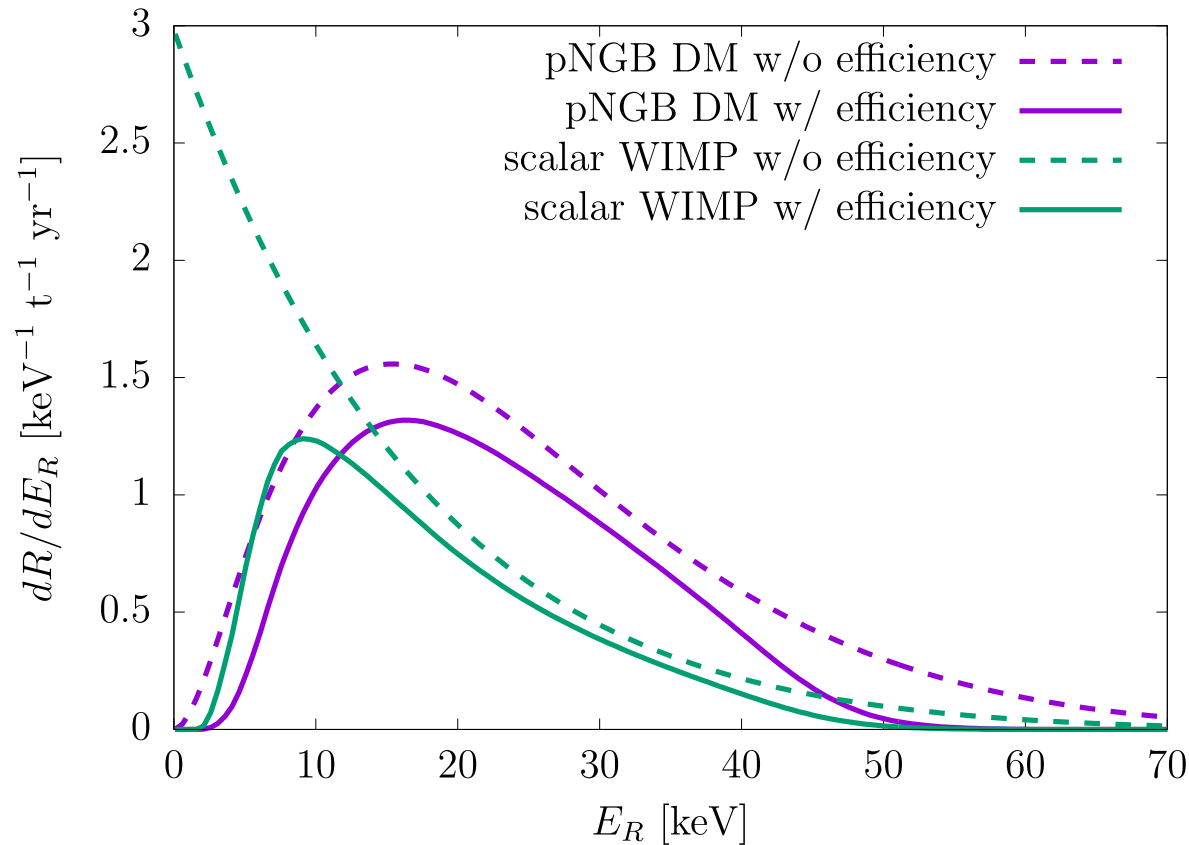
$$\begin{aligned} \frac{d\sigma_A}{dE_R} &\approx \frac{m_A \kappa_A^2 \sin^2 \theta}{8\pi m_\chi^2 v_\chi^2} \frac{q^4}{v^2 v_s^2 (q^2 - m_{h_2}^2)^2} F^2(E_R) \xrightarrow{v_\chi \rightarrow 0} 0 \\ &= \frac{m_A \kappa_A^2 \sin^2 \theta}{8\pi m_\chi^2 v_\chi^2} \frac{q^4}{v^2 v_s^2} F^2(E_R) \begin{cases} 1 & \text{for } q^2 \gg m_{h_2}^2 \\ \frac{q^4}{m_{h_2}^4} & \text{for } q^2 \ll m_{h_2}^2 \end{cases} \end{aligned}$$

■ PNGB DM can be tested by DD if the mediator is light enough.

Energy spectrum

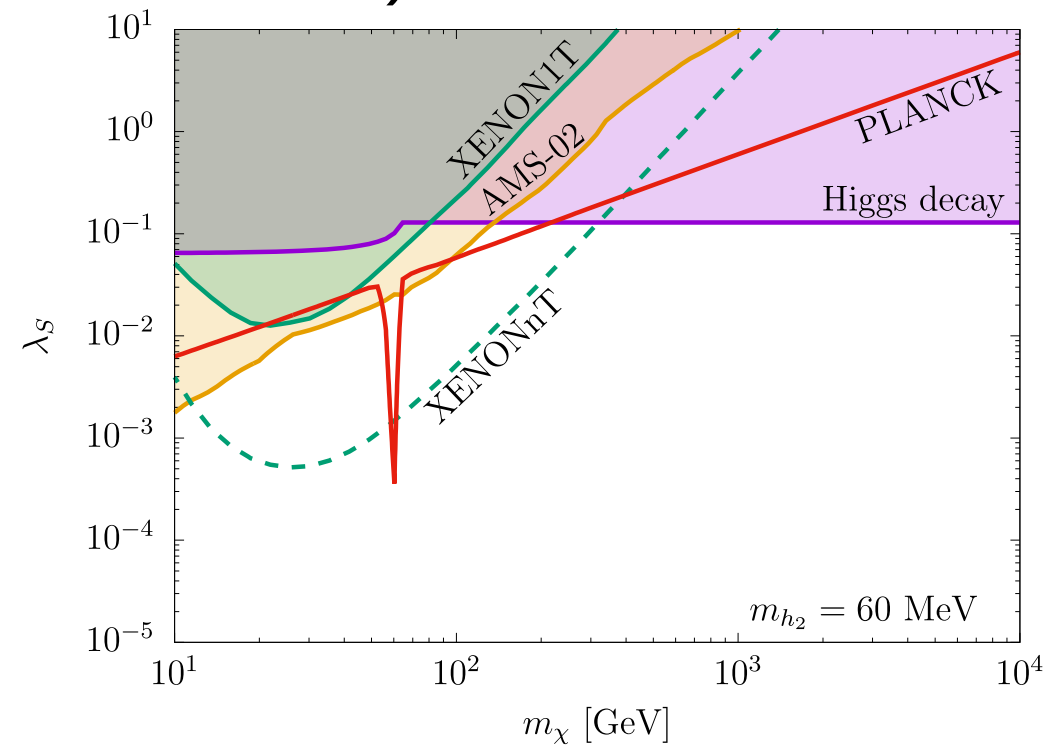
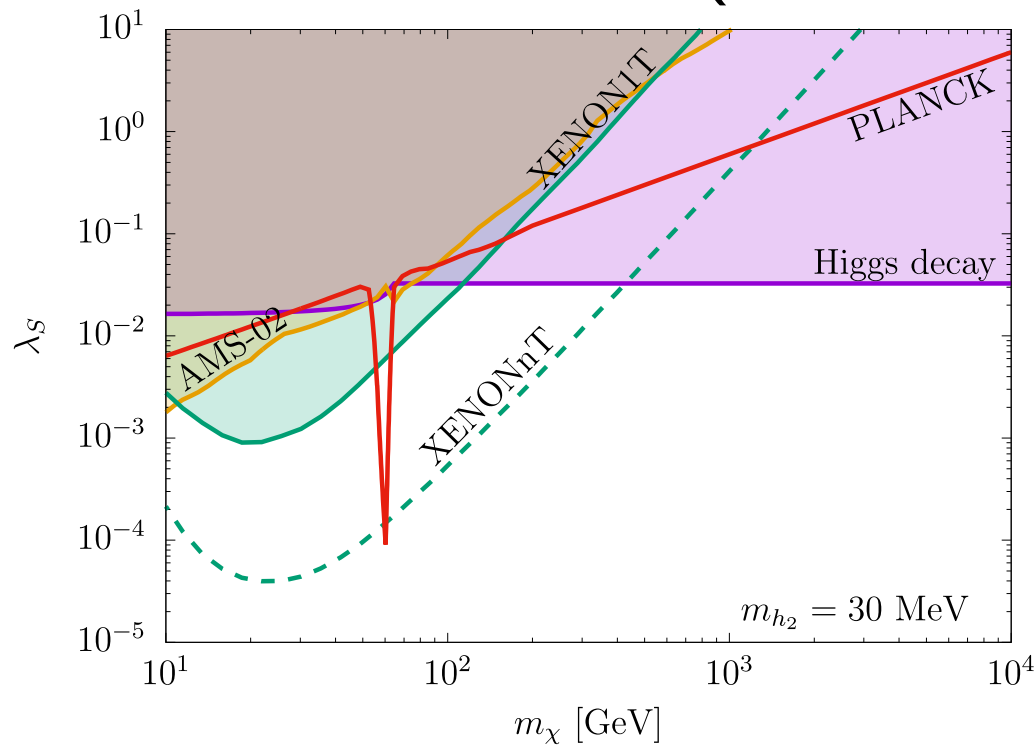
Abe, TT, PLB (2021) [arXiv:2108.10647]

Hambye et al., PRD (2018) [arXiv:1807.05022]



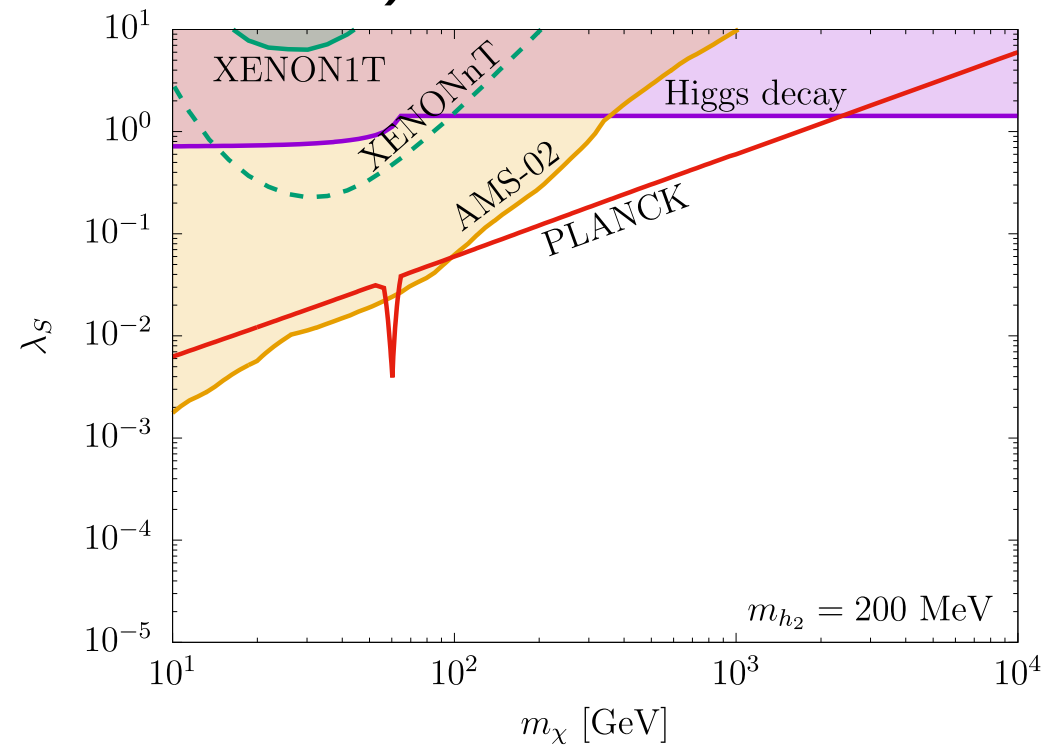
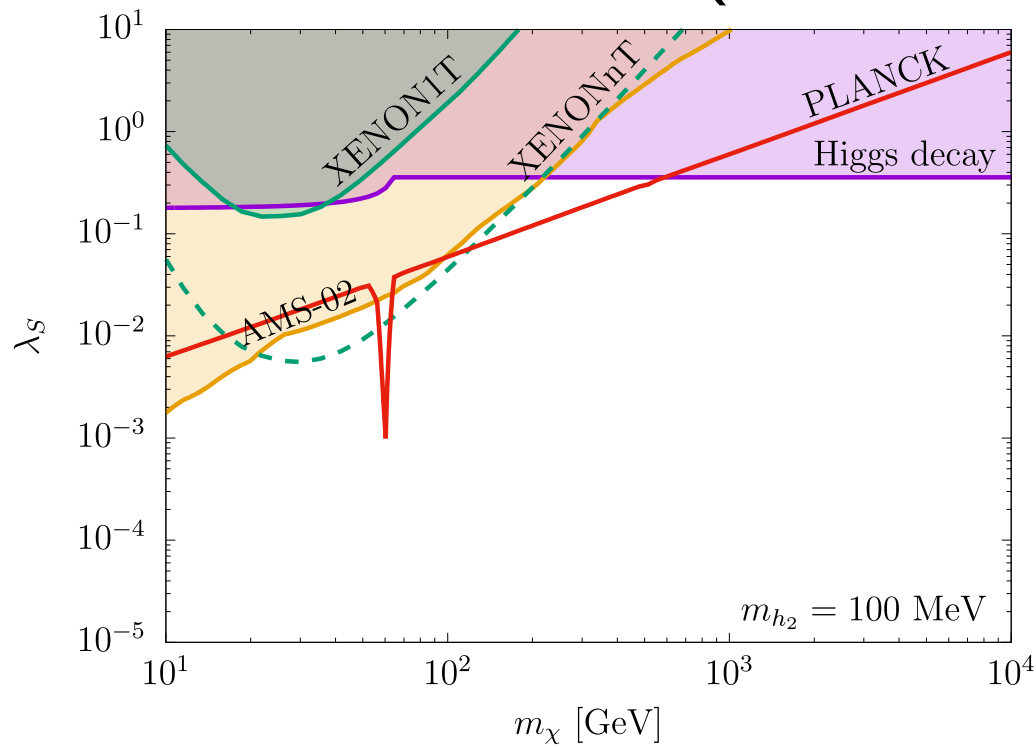
- Energy spectrum for pNGB DM is different from normal WIMP.
- But similar energy spectra can be induced from inelastic scattering and the other momentum dependent scatterings.

Numerical results ($\sin \theta = 3 \times 10^{-5}$) Abe, TT, PLB (2021) [arXiv:2108.10647]



- Higgs resonance at $m_\chi \approx m_{h_1}/2$
- Right plot: $100 \text{ GeV} \lesssim m_\chi \lesssim 200 \text{ GeV}$ can be tested by XENONnT.

Numerical results ($\sin \theta = 3 \times 10^{-5}$) Abe, TT, PLB (2021) [arXiv:2108.10647]



- Larger m_{h_2} case
- More parameter space is allowed.
- No sensitivity for direct detection.

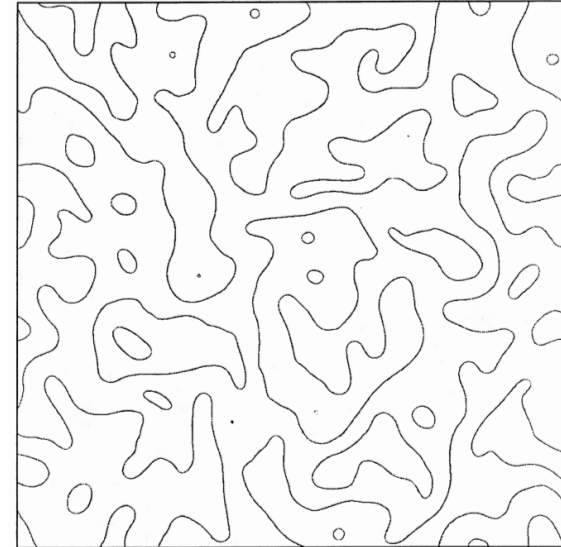
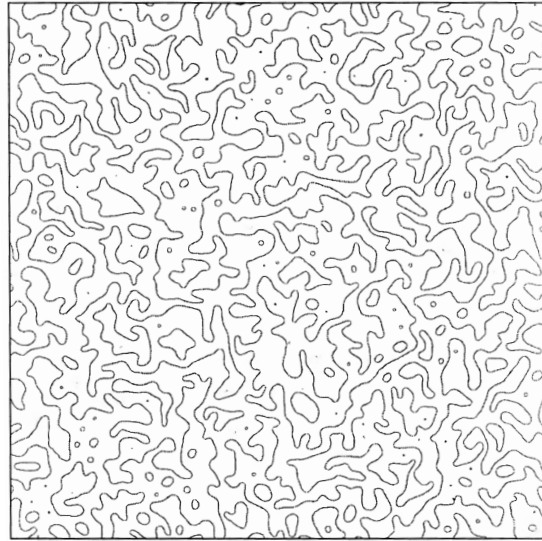
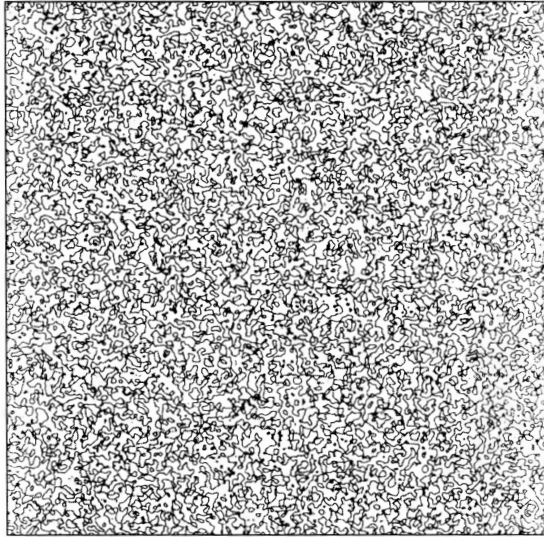
Summary

- 1 Thermal WIMP DM is strongly constrained by recent direct detection experiments.
⇒ PNGB DM can naturally avoid it.
- 2 For $m_{h_2} \gtrsim m_\chi$, elastic cross section with nucleon (1-loop) is $\sigma_{\text{SI}}^N = \mathcal{O}(10^{-48}) \text{ cm}^2$ at most.
- 3 For light mediator h_2 ($m_{h_2} \lesssim 200 \text{ MeV}$), non-zero direct detection rate emerges.
 - Some region can be tested by XENONnT.
 - Energy spectrum can differ from normal WIMP.

Back Up

Domain wall problem

- Domain walls due to spontaneous breaking of \mathbb{Z}_2 symmetry
⇒ distort CMB
- Solutions:
 - UV completion
 - low energy inflation after the \mathbb{Z}_2 breaking
 - decay before BBN (making the domain wall unstable)

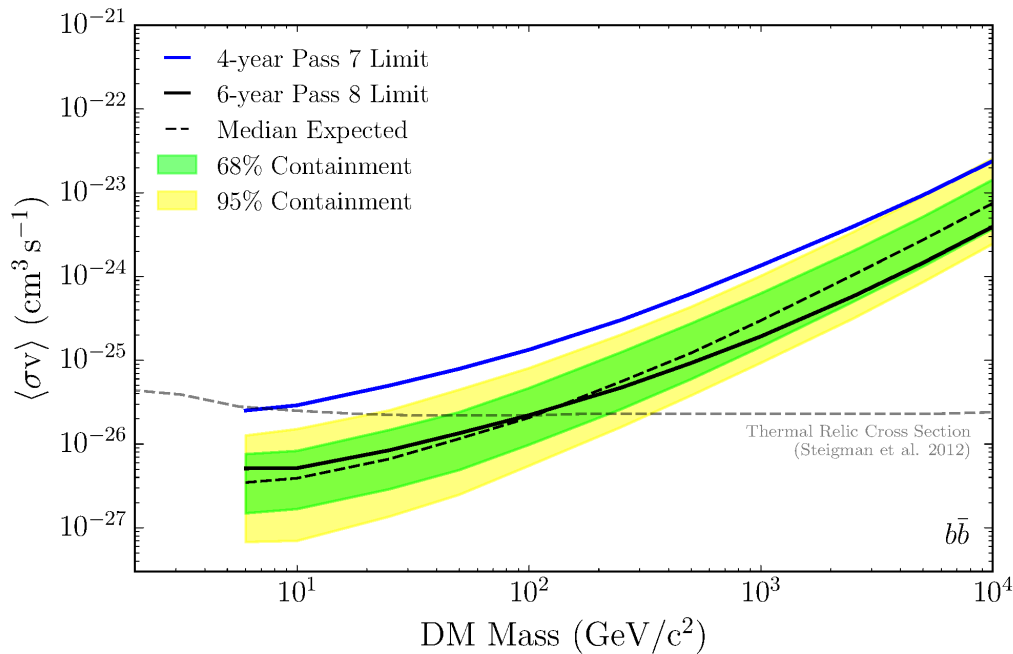


Press, Ryden, Spergel ApJ (1989)

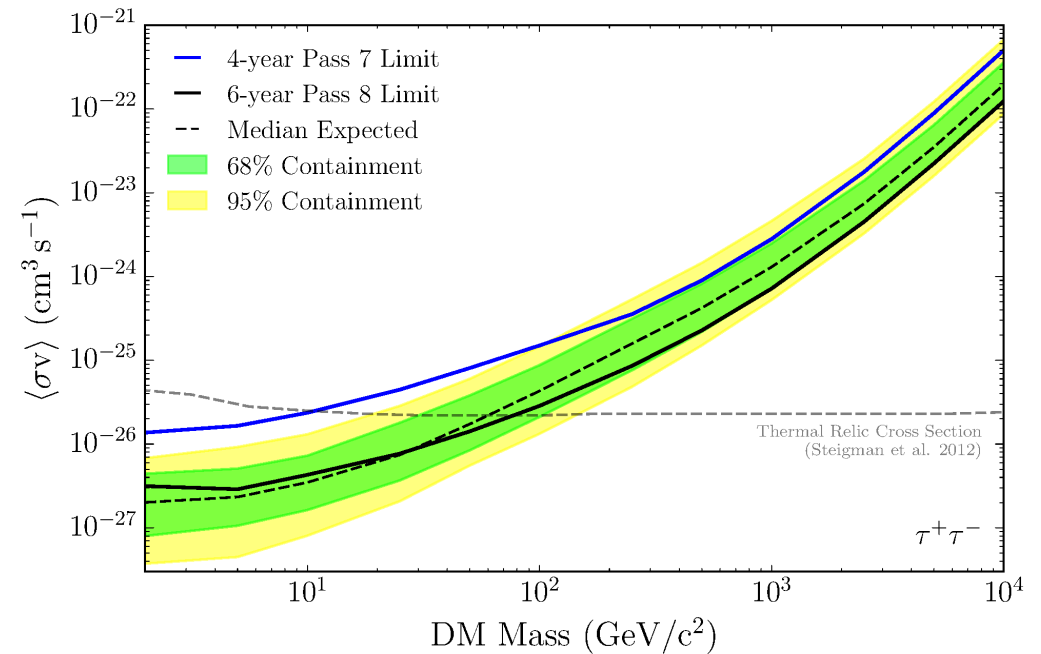
WIMP search status

Indirect detection (Gamma-rays from dSphs)

$$\chi\chi \rightarrow b\bar{b}$$



$$\chi\chi \rightarrow \tau^+\tau^-$$

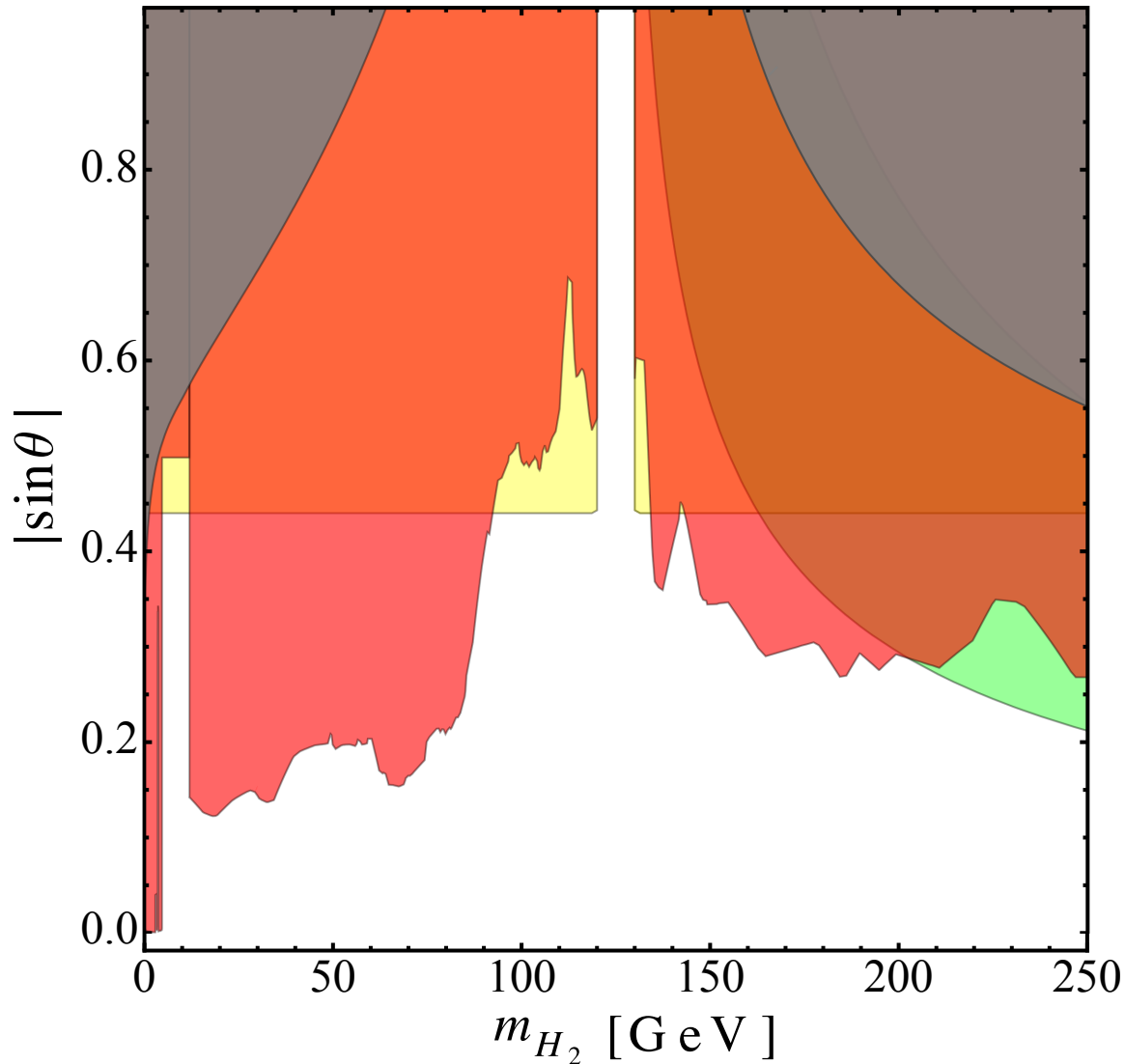


Fermi-LAT, PRL (2015) [arxiv:1503.02641](https://arxiv.org/abs/1503.02641)

- A lot of gamma-rays are generated if final state particles are charged.
- $m_{\text{DM}} \lesssim 100$ GeV is excluded if thermal WIMP scenarios are assumed.
- $\langle\sigma v\rangle \sim 10^{-26}$ cm³/s for thermal DM

Bound on $\sin \theta$

A. Falkowski et al., JHEP 1505 (2015) [arxiv:1502.01361]



- Red: h_2 direct search at LHC
- Yellow: h_1 coupling measurements
- Green: Favored region from stability of scalar potential
- Gray: Electroweak precision tests
- $|\sin \theta| \lesssim 0.3$ if $m_{h_2} \gtrsim m_{h_1}$
- $m_\chi \lesssim m_{h_2}$ (above EW scale)

The pNGB DM model

C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

■ Cubic couplings

$$\mathcal{V} \supset \frac{\kappa_{111}}{3!} h_1^3 + \frac{\kappa_{112}}{2!} h_1^2 h_2 + \frac{\kappa_{122}}{2!} h_1 h_2^2 + \frac{\kappa_{222}}{3!} h_2^3$$

$$\kappa_{111} = 3m_{h_1}^2 \left(-\frac{\sin^3 \theta}{v_s} + \frac{\cos^3 \theta}{v} \right),$$

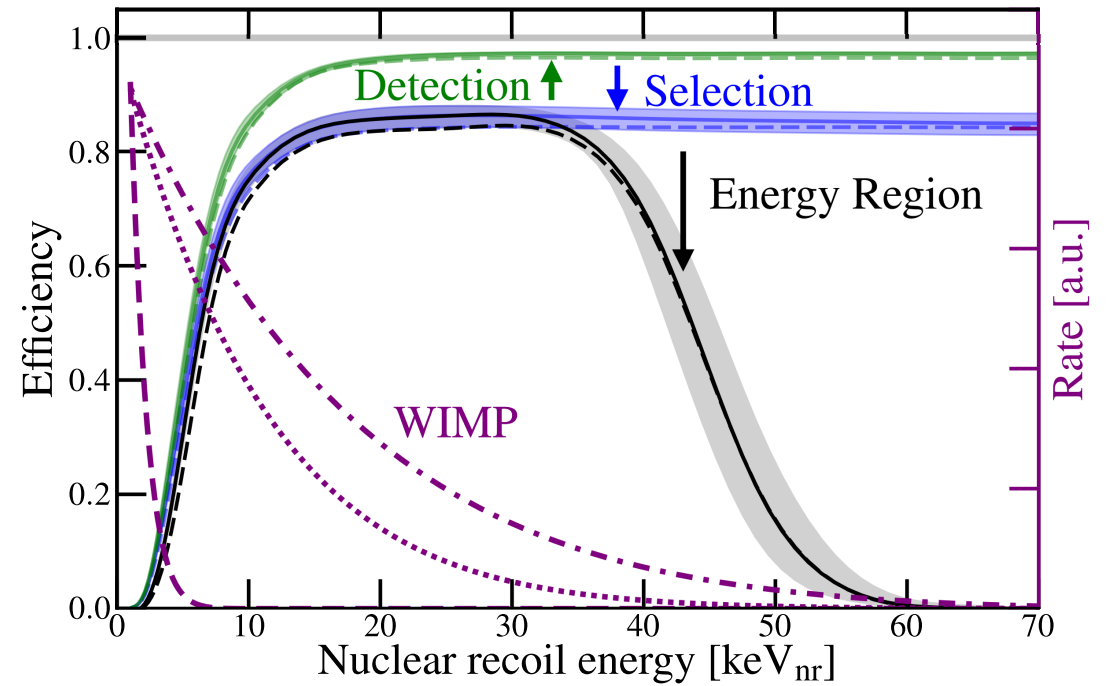
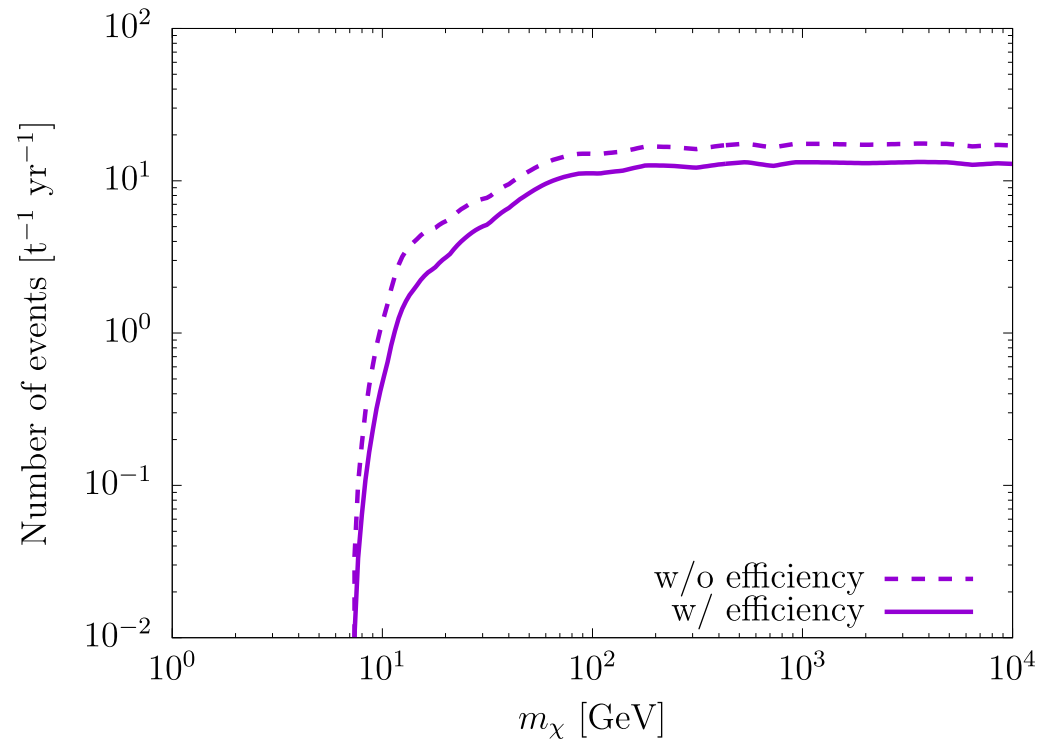
$$\kappa_{112} = (2m_{h_1}^2 + m_{h_2}^2) \sin \theta \cos \theta \left(\frac{\sin \theta}{v_s} + \frac{\cos \theta}{v} \right),$$

$$\kappa_{122} = (m_{h_1}^2 + 2m_{h_2}^2) \sin \theta \cos \theta \left(-\frac{\cos \theta}{v_s} + \frac{\sin \theta}{v} \right),$$

$$\kappa_{222} = 3m_{h_2}^2 \left(\frac{\cos^3 \theta}{v_s} + \frac{\sin^3 \theta}{v} \right),$$

Event rate

Abe, TT, PLB (2021) [arXiv:2108.10647]



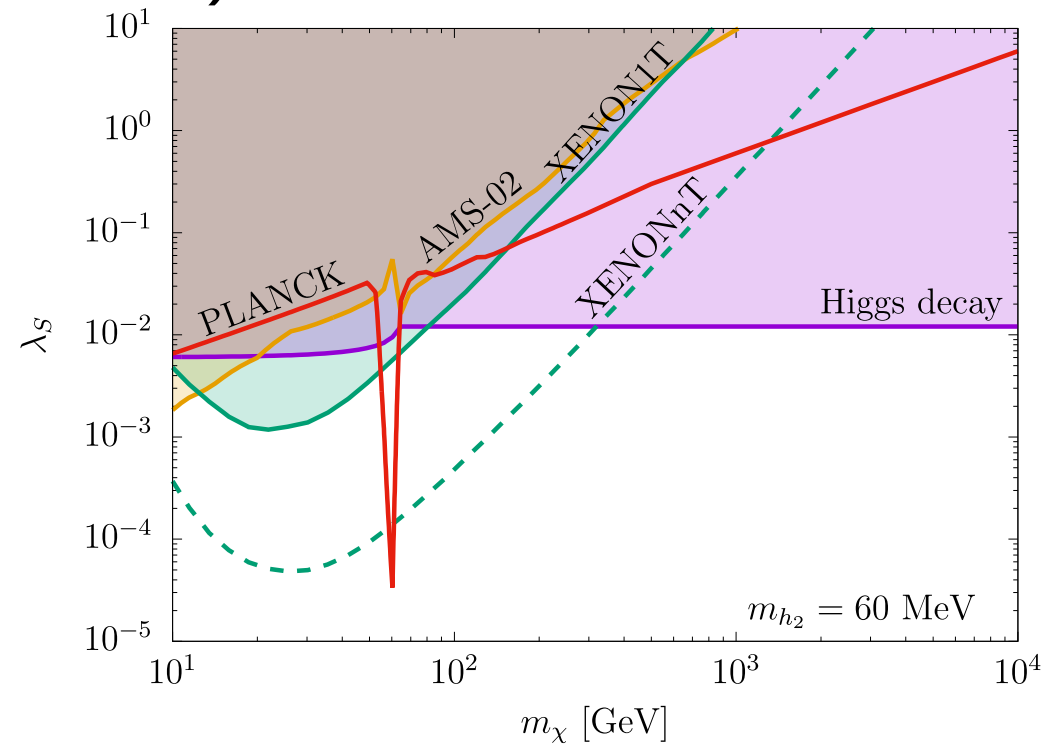
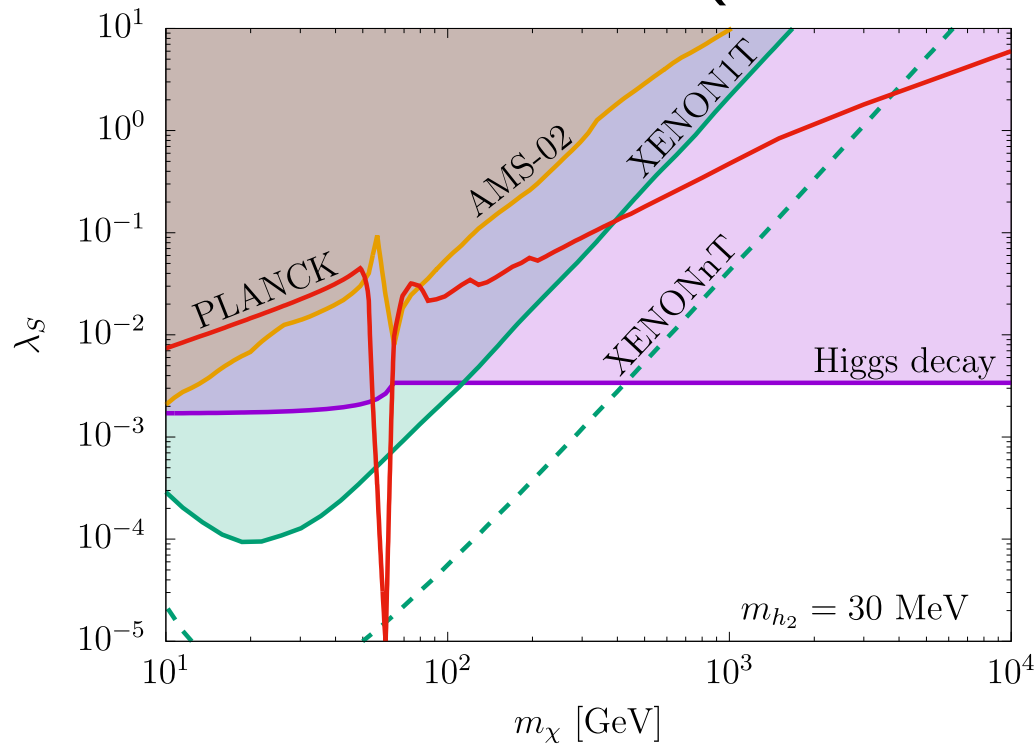
XENON1T, PRL (2018) [arXiv:1805.12562]

■ Event rate

$$\frac{dR}{dE_R} = \frac{\rho_\odot}{m_\chi} N_T \int_{v > v_{\min}} \frac{d\sigma_A}{dE_R} v_\chi f_\odot(\mathbf{v}_\chi) d^3v_\chi$$

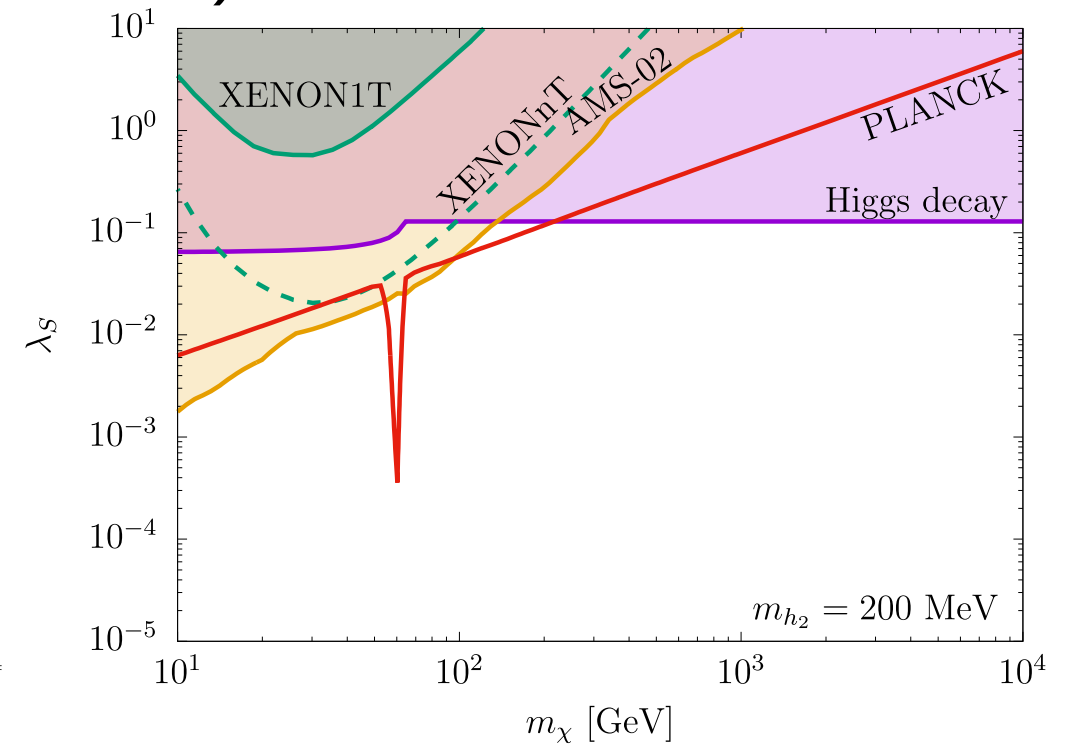
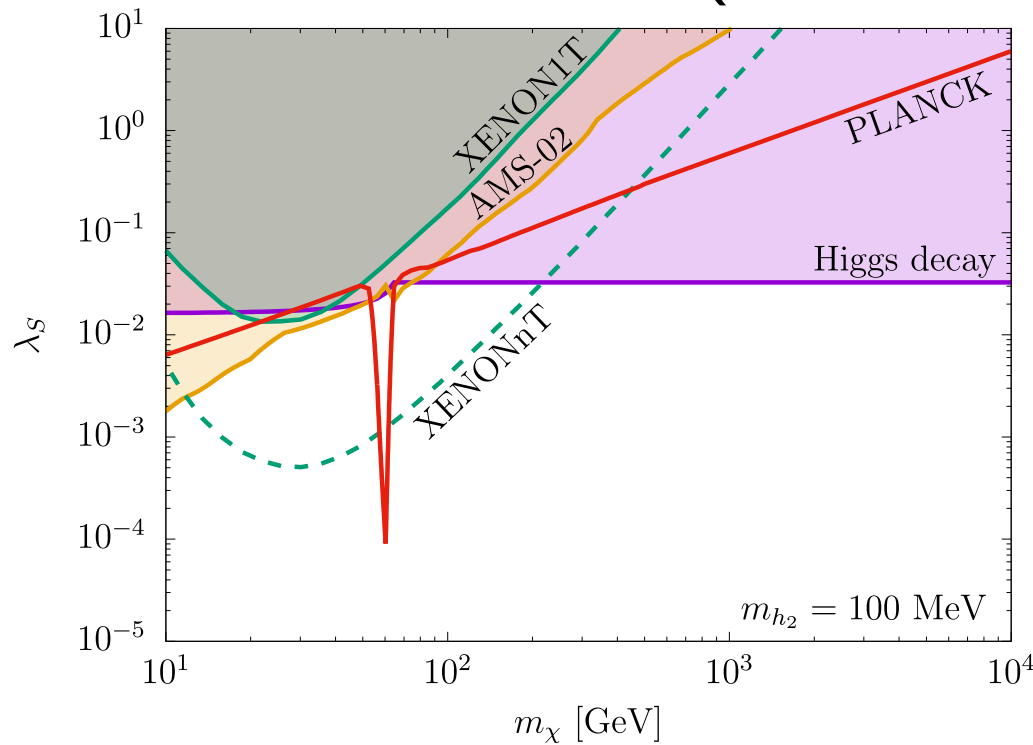
■ Total event rate R can be compared with experiments.

Numerical results ($\sin \theta = 10^{-4}$) Abe, TT, PLB (2021) [arXiv:2108.10647]



- Resonance at $2m_\chi \sim m_{h_1}$
- Only resonance region can be allowed.

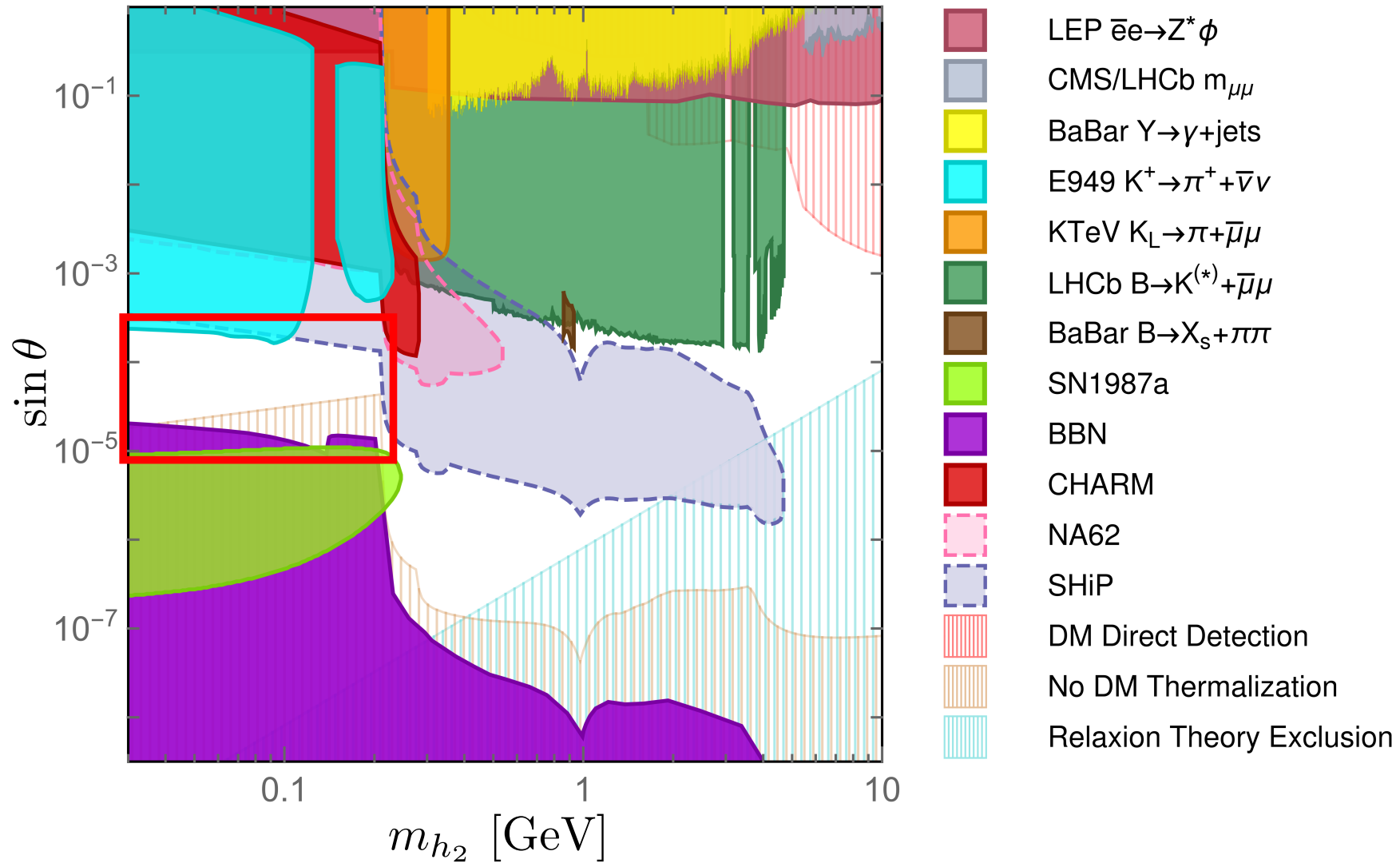
Numerical results ($\sin \theta = 10^{-4}$) Abe, TT, PLB (2021) [arXiv:2108.10647]



- The other parameter region is allowed for heavier m_{h_2} .
- But direct detection rate becomes small as expected.

Mixing angle

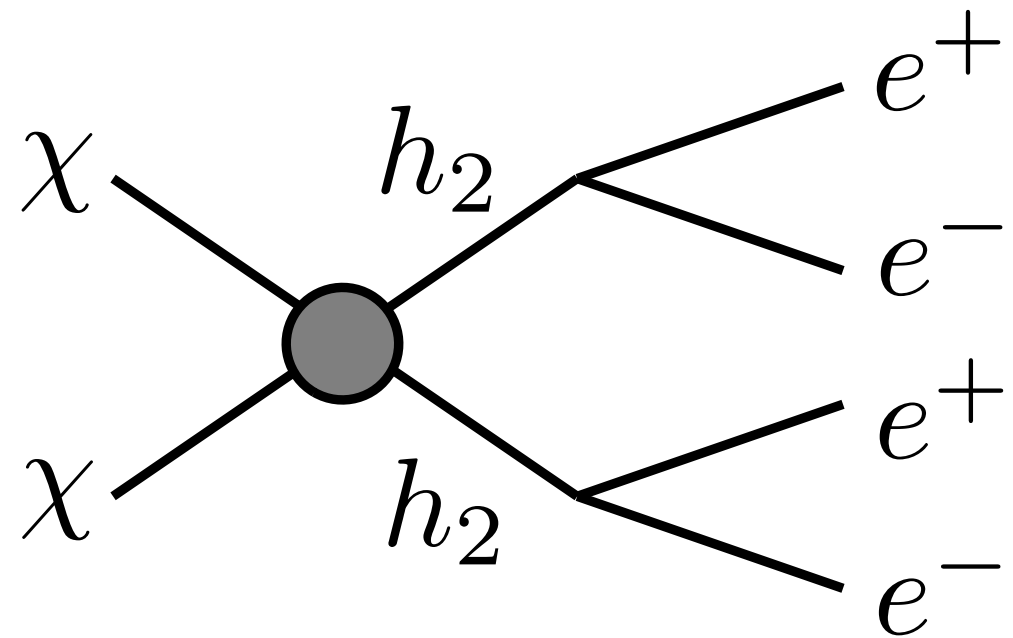
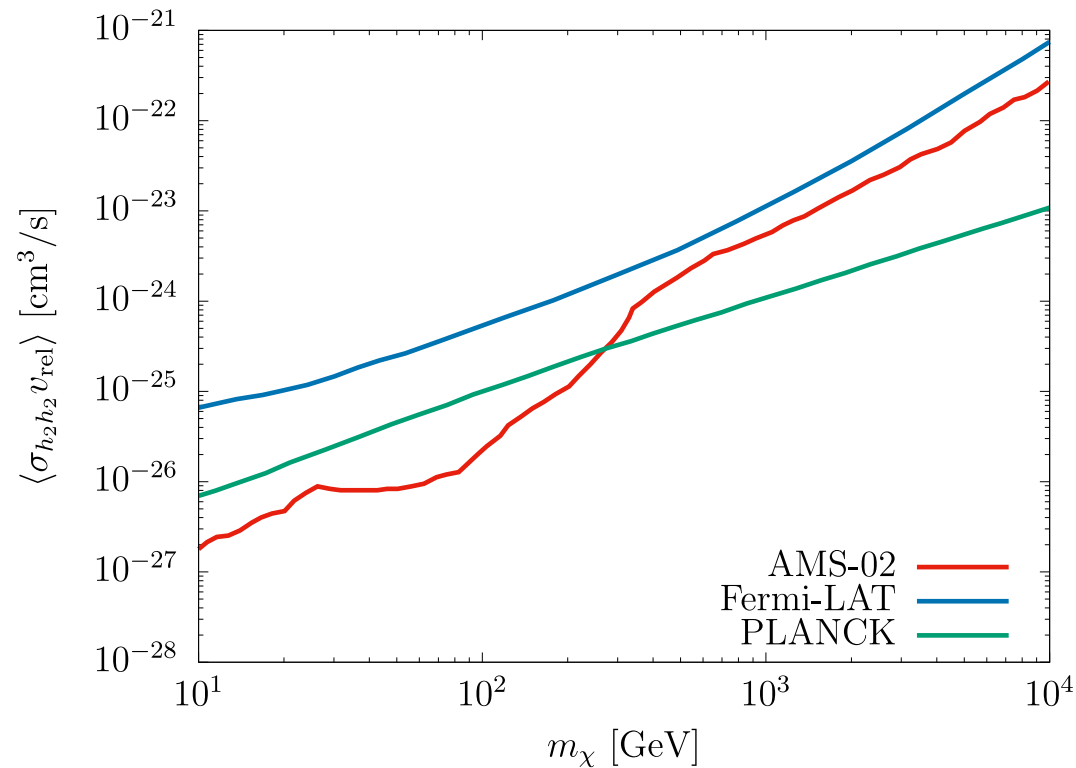
Winkler, PRD (2019) [arXiv:1809.01876]



■ $2 \times 10^{-5} \lesssim \sin \theta \lesssim 10^{-4}$

Limit on $\sigma_{h_2 h_2} v_{\text{rel}}$

Abe, TT, PLB (2021) [arXiv:2108.10647]



Elor et al., JCAP (2016) [arXiv:1511.08787]

- $\chi\chi \rightarrow e^+e^-e^+e^-$ (AMS-02), gamma-rays (Fermi-LAT) and CMB (PLANCK)
- Model-independent indirect detection constraints from cascade decays

Higgs decays

Abe, TT, PLB (2021) [arXiv:2108.10647]

- $h_1 \rightarrow h_2 h_2, \chi\chi$ contributes to Higgs invisible decay.

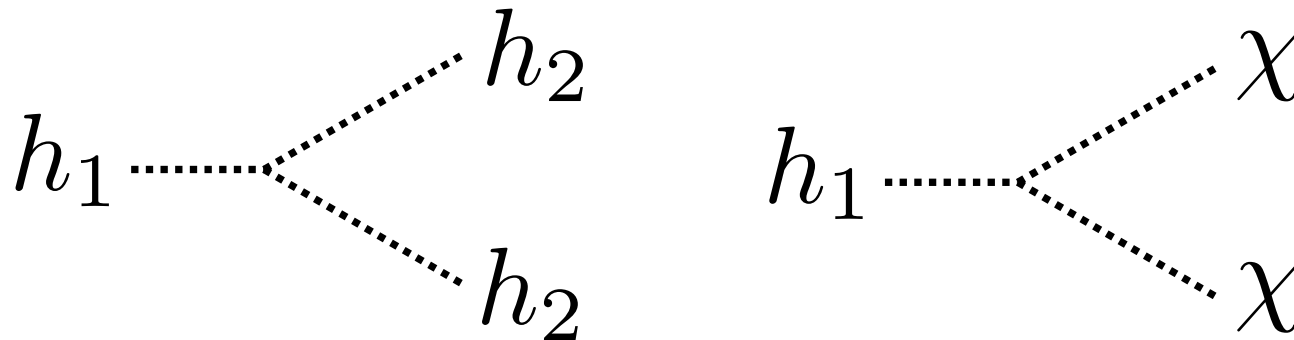
$$\Gamma_{h_2 h_2} = \frac{\kappa_{122}^2}{32\pi m_{h_1}} \sqrt{1 - 4\frac{m_{h_2}^2}{m_{h_1}^2}} \approx \frac{\lambda_S m_{h_1}^3 \sin^2 \theta}{32\pi m_{h_2}^2},$$

$$\Gamma_{\chi\chi} \approx \frac{\lambda_S m_{h_1}^3 \sin^2 \theta}{32\pi m_{h_2}^2} \sqrt{1 - 4\frac{m_\chi^2}{m_{h_1}^2}}$$

- Experimental limit: $\text{Br}_{\text{inv}} \leq 0.11$

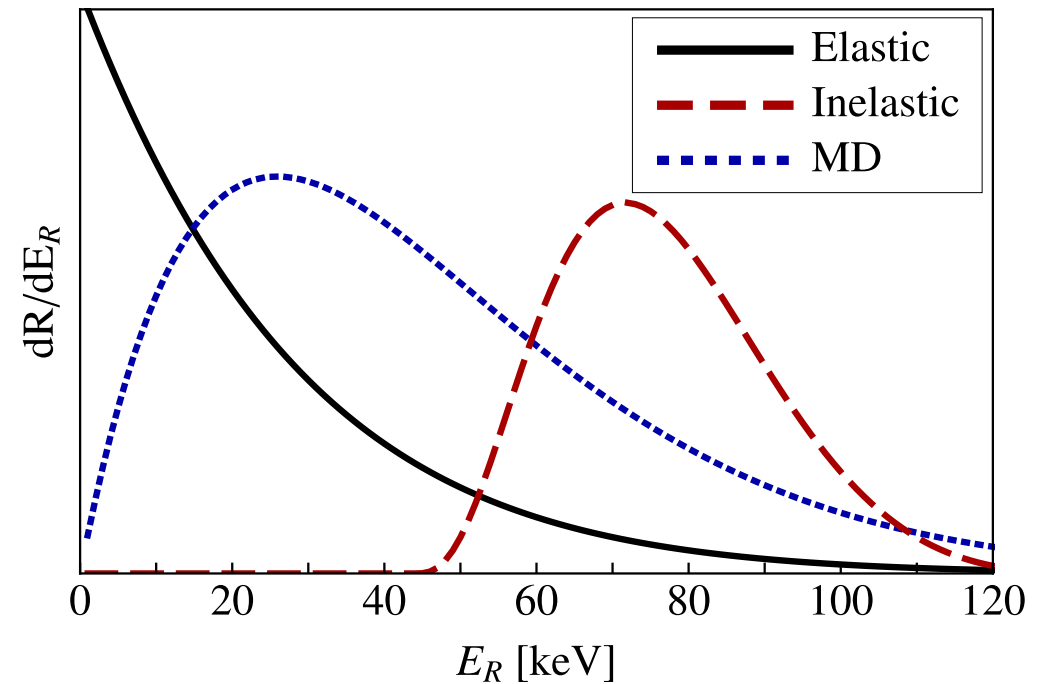
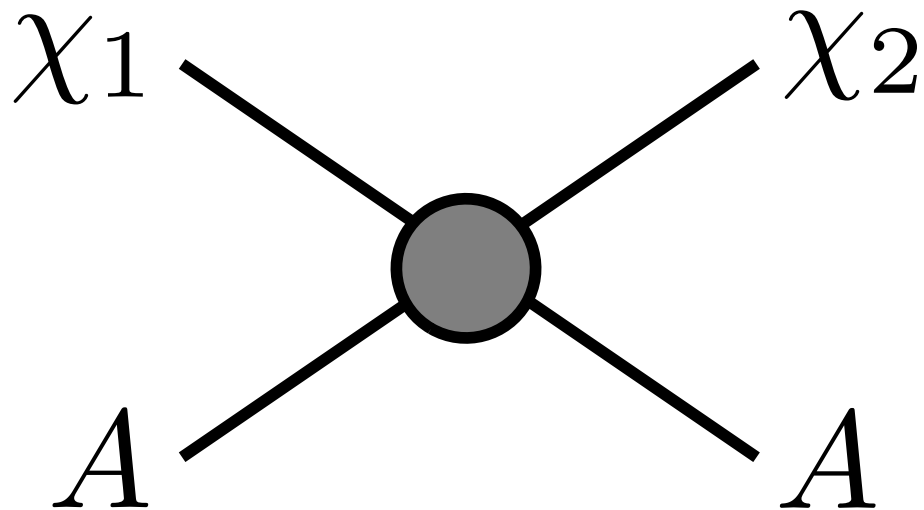
Higgs signal strength is translated into the constraint of branching ratio

$\Rightarrow \lambda_S \gtrsim \mathcal{O}(1)$ region is excluded.



Energy spectrum 2

McCabe, PRD (2010) [arXiv:1005.0579]



- Inelastic scattering $\chi_1 A \rightarrow \chi_2 A$ where $m_{\chi_1} < m_{\chi_2}$ and $\delta = m_{\chi_2} - m_{\chi_1}$

- $$v_{\min} = \sqrt{\frac{1}{2m_A E_R} \left(\frac{m_A E_R}{\mu_A} + \delta \right)}$$

- Similar energy spectrum from inelastic scatterings.

GUT embedding

Y. Abe, TT, K. Tsumura, N. Yamatsu, PRD (2021) [arXiv:2104.13523]

| | fermions | H | S | Φ | $SO(10)$ | |
|----------|-----------|-------------|-------------|-------------|------------------------------------|--------------|
| | A_μ | Ψ_{16} | Φ_{10} | Φ_{16} | $\Phi_{\overline{126}}$ | Φ_{210} |
| $SO(10)$ | 45 | 16 | 10 | 16 | $\overline{126}$ | 210 |

- We embed the UV complete model in $SO(10)$ GUT.

- The pNGB model is reproduced at low energy.

- Breaking pattern: $SO(10) \rightarrow G_{\text{PS}} \rightarrow G_{\text{SM}}$
at $\mu = M_U$ at $\mu = M_I$

Pati-Salam symmetry: $G_{\text{PS}} = SU(4)_C \times SU(2)_L \times SU(2)_R$

- GUT scale (M_U)

Intermediate scale (M_I) = breaking scale of $U(1)_{B-L}$,

Determined by matching conditions of gauge couplings

GUT embedding

Y. Abe, TT, K. Tsumura, N. Yamatsu, PRD (2021) [arXiv:2104.13523]

| | fermions | H | S | Φ | $SO(10)$ | |
|----------|-----------|-------------|-------------|-------------|------------------------------------|--------------|
| | A_μ | Ψ_{16} | Φ_{10} | Φ_{16} | $\Phi_{\overline{126}}$ | Φ_{210} |
| $SO(10)$ | 45 | 16 | 10 | 16 | $\overline{126}$ | 210 |

- Two $U(1)$: $U(1)_{B-L} \subset SU(4)_C/SU(3)_C$, $U(1)_R \subset SU(2)_R$
- $U(1)_{B-L}$ and $U(1)_R$ are orthogonal, but $U(1)_{B-L}$ and $U(1)_Y$ are not.

$$\begin{matrix} U(1)_Y \\ U(1)_{B-L} \end{matrix} : \begin{pmatrix} B_\mu \\ C_\mu \end{pmatrix} = \begin{pmatrix} 1 & -\tan \epsilon \\ 0 & \frac{1}{\cos \epsilon} \end{pmatrix} \begin{pmatrix} B'_\mu \\ C'_\mu \end{pmatrix} =: U_{GK} \begin{pmatrix} B'_\mu \\ C'_\mu \end{pmatrix} : \begin{matrix} U(1)_R \\ U(1)_{B-L} \end{matrix}$$

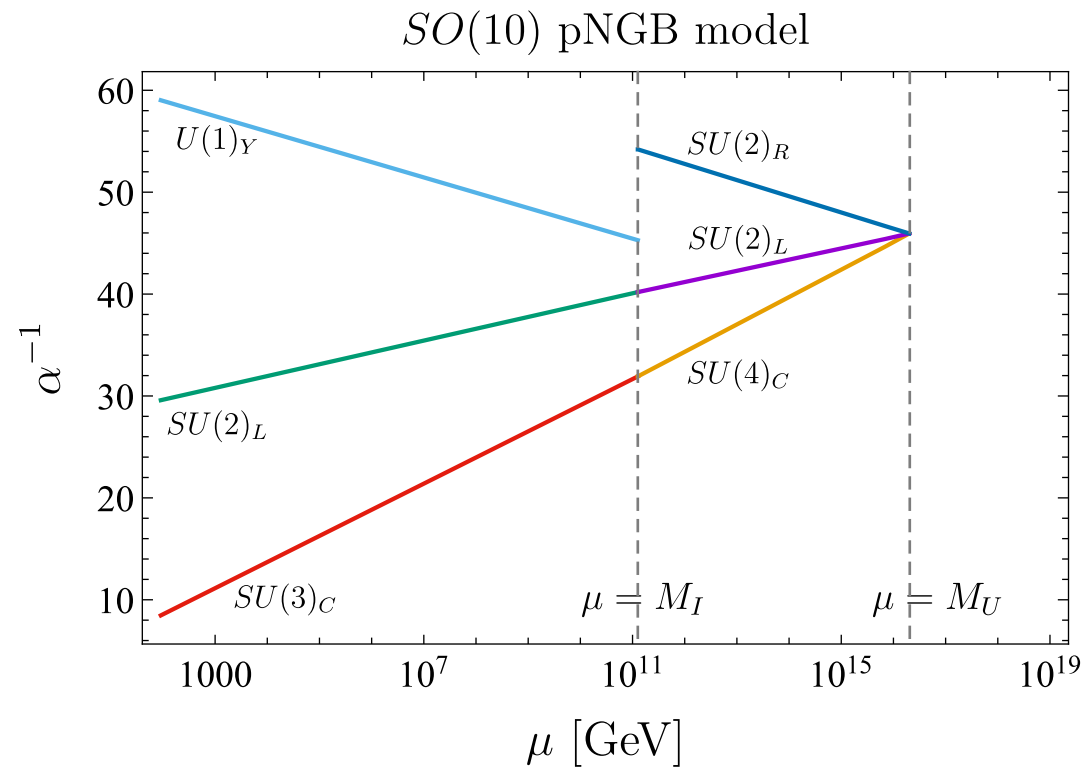
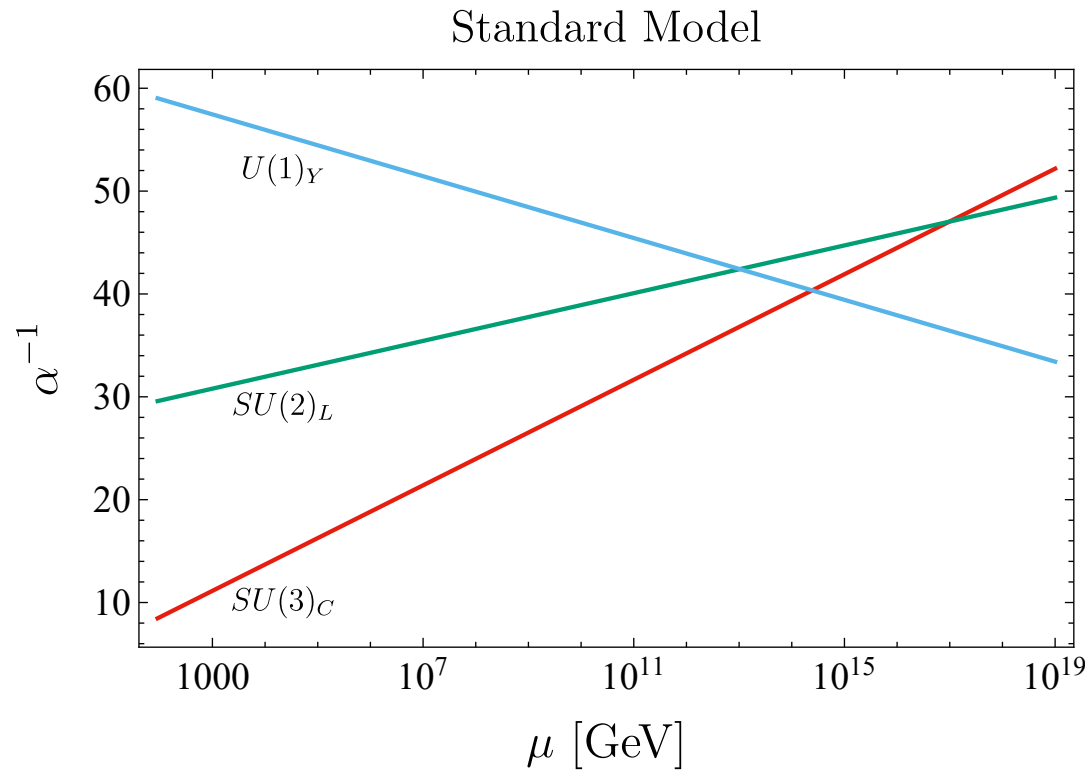
→ Kinetic mixing between $U(1)_{B-L}$ and $U(1)_Y$: $\tan \epsilon = -\sqrt{2/3}$

- Proton decay

SK limit: $\tau_{p \rightarrow e^+ \pi^0} > 2.4 \times 10^{34}$ years

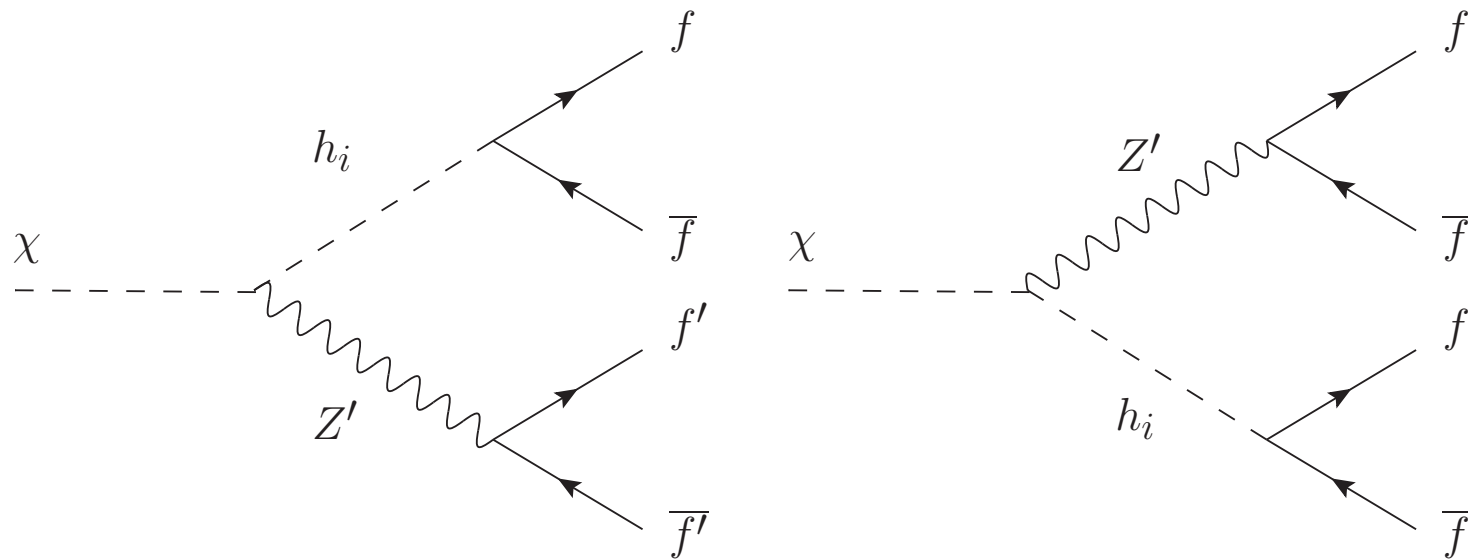
Rough estimate: $\tau \sim (\alpha_U^2 m_p^5 / M_U^4)^{-1} = 1.1 \times 10^{37}$ years

RGE



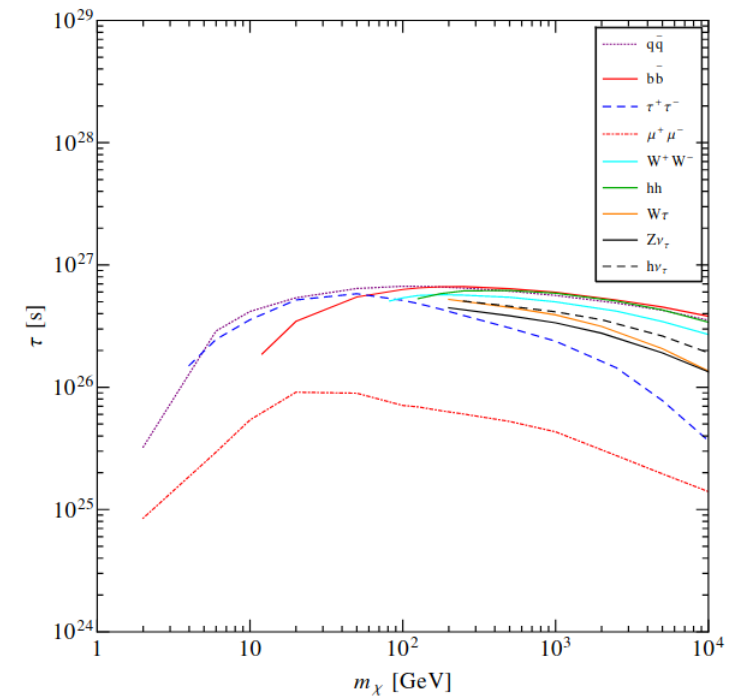
- 1-loop RGEs are solved.
- Intermediate scale, GUT scale: determined by matching conditions of gauge couplings
- $v_\phi = M_I = 1.26 \times 10^{11}$ GeV, $M_U = 2.06 \times 10^{16}$ GeV
 $g_{B-L} = 0.38$ at $\mu = M_I$

DM decay

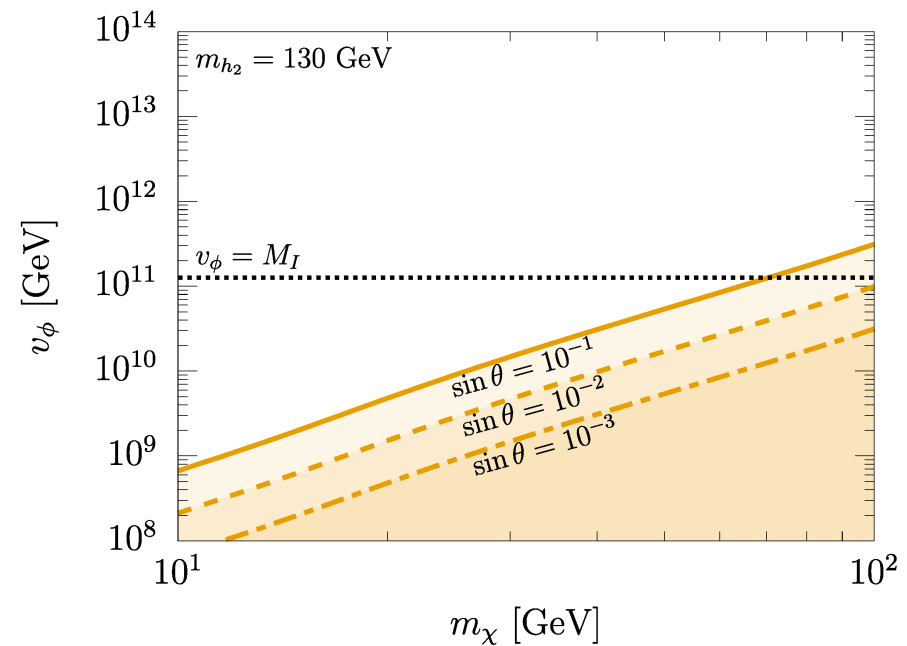
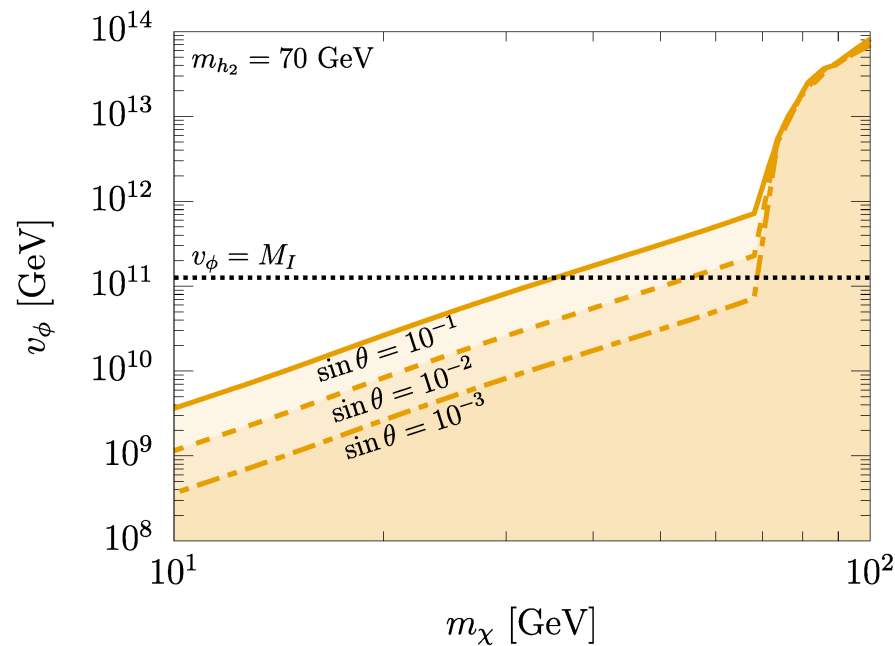


- DM lifetime: $\tau_{\text{DM}} \gtrsim 10^{17}$ sec at least (the age of the universe).
- Cosmic ray observations give stronger limits: $\tau_{\text{DM}} \gtrsim 10^{27}$ sec.
3-body decays $\chi \rightarrow f\bar{f}h_i, f\bar{f}Z$ if $m_\chi \gtrsim m_{h_i}, m_Z \rightarrow$ excluded

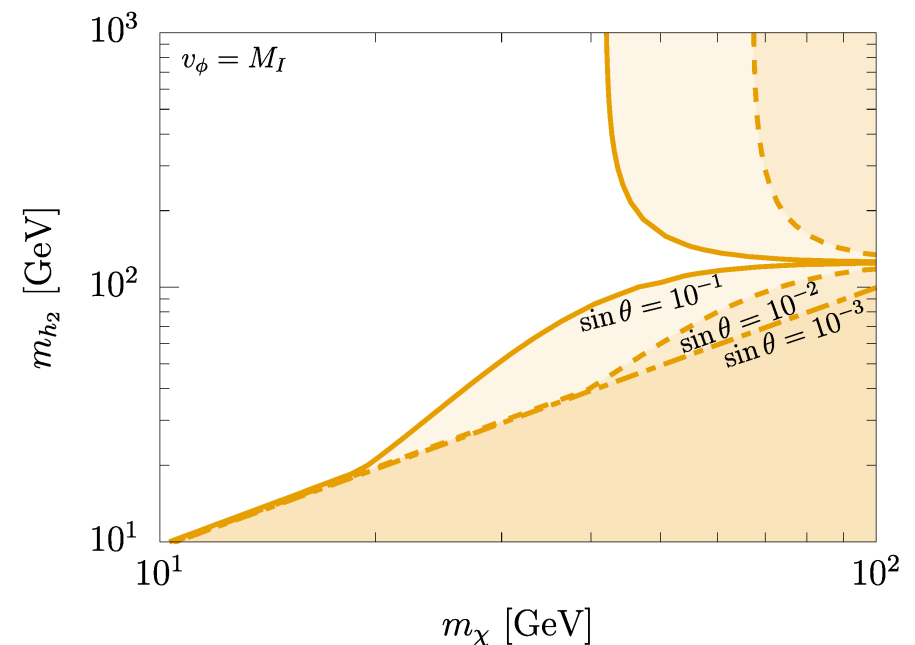
Baring et al. (2015)



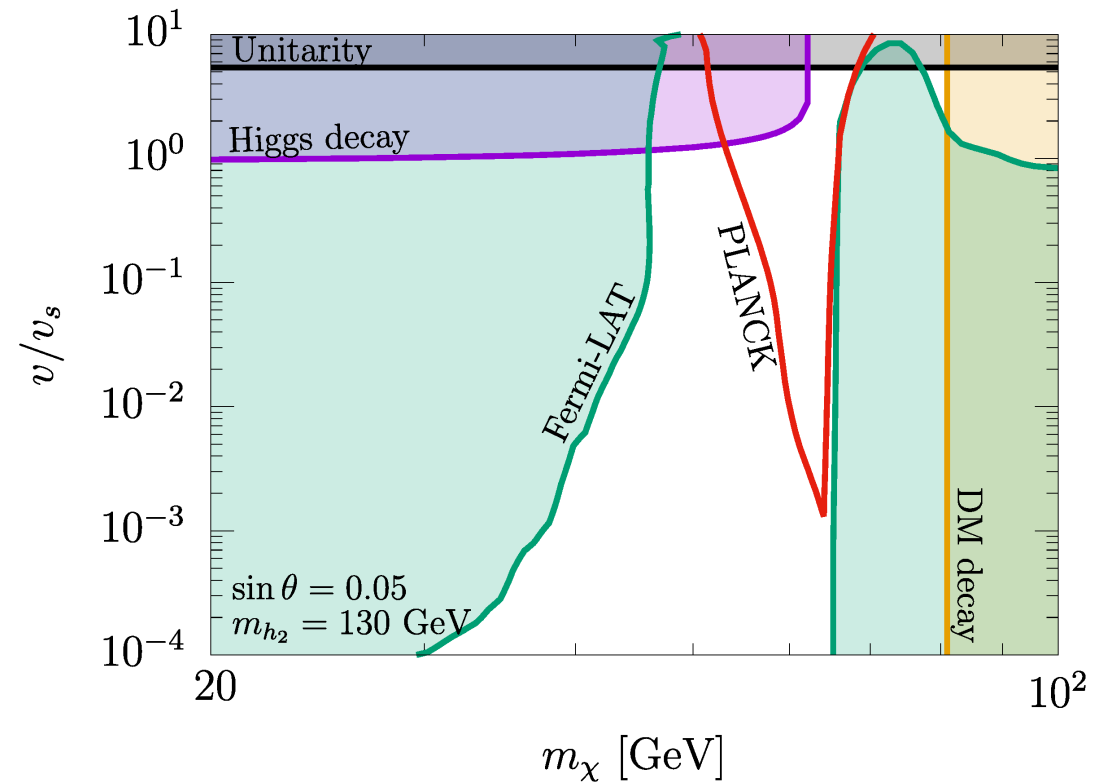
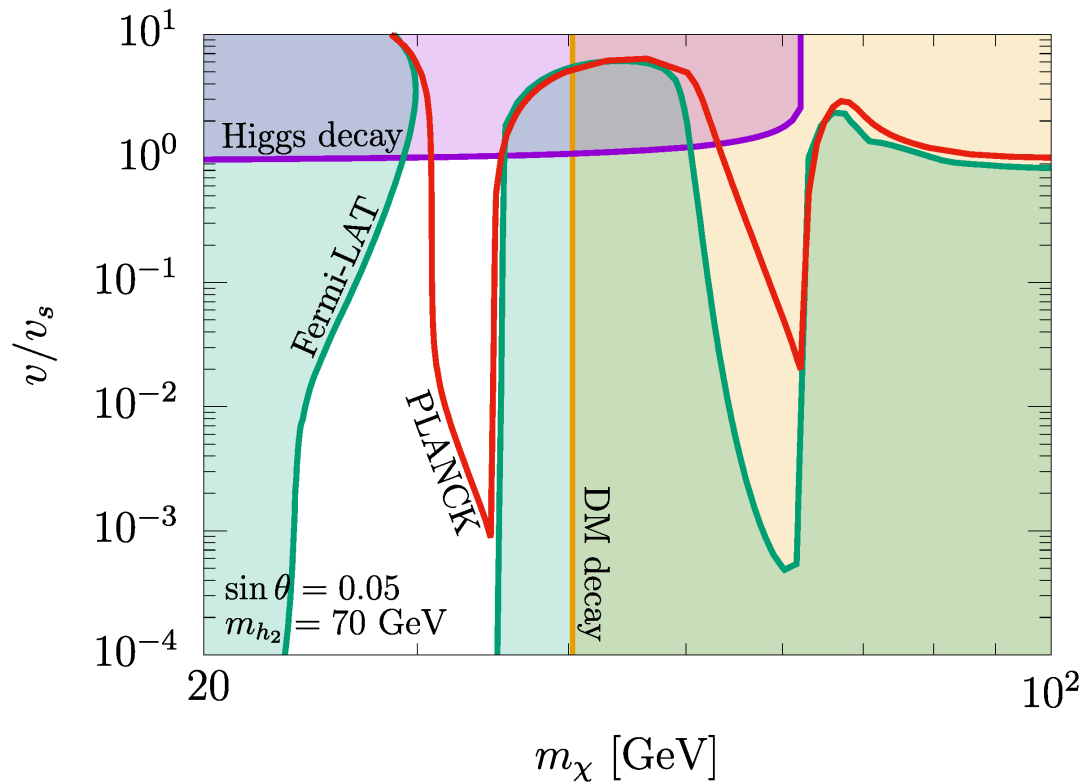
DM decay2



- Orange region is excluded.
($\tau_{\text{DM}} \lesssim 10^{27} \text{ sec}$)
- DM should be $\lesssim 100 \text{ GeV}$
- $v_\phi = M_I \sim 10^{11} \text{ GeV}$



Parameter space



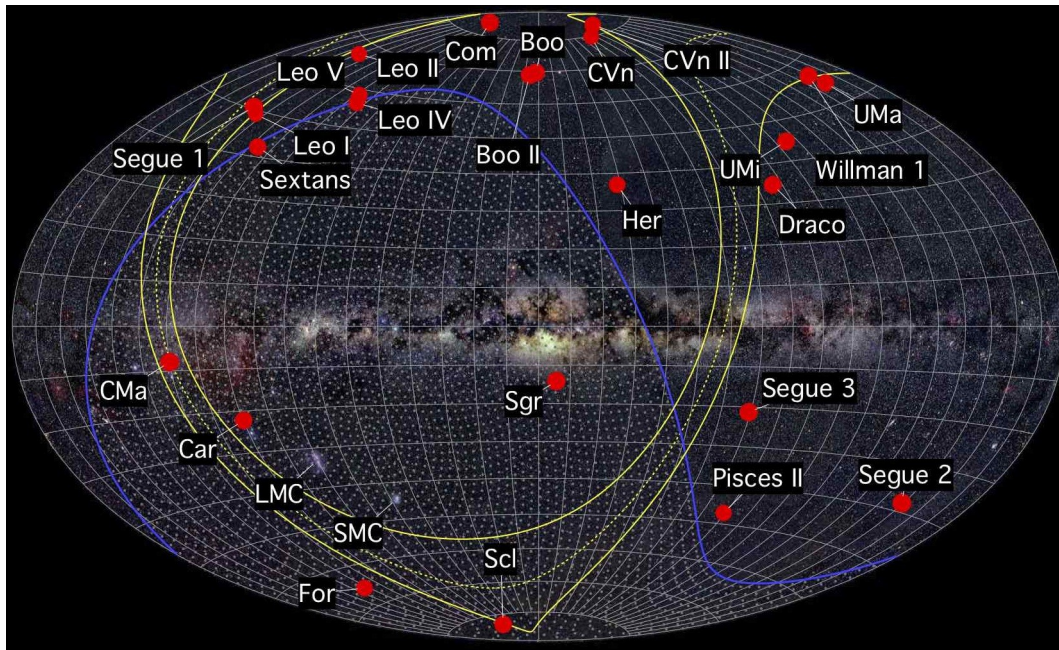
- $v/v_s \sim \sqrt{\lambda_S}$
- Fermi-LAT: $\chi\chi \rightarrow b\bar{b}, WW \rightarrow \gamma$ production
- close to the h_2 resonance

Indirect detection

DM annihilations

$$\chi\chi \rightarrow h_i h_j, WW, ZZ, f\bar{f}$$

- Gamma-rays are produced at the end
- Constraints from dSphs
(less visible matter and more DM)



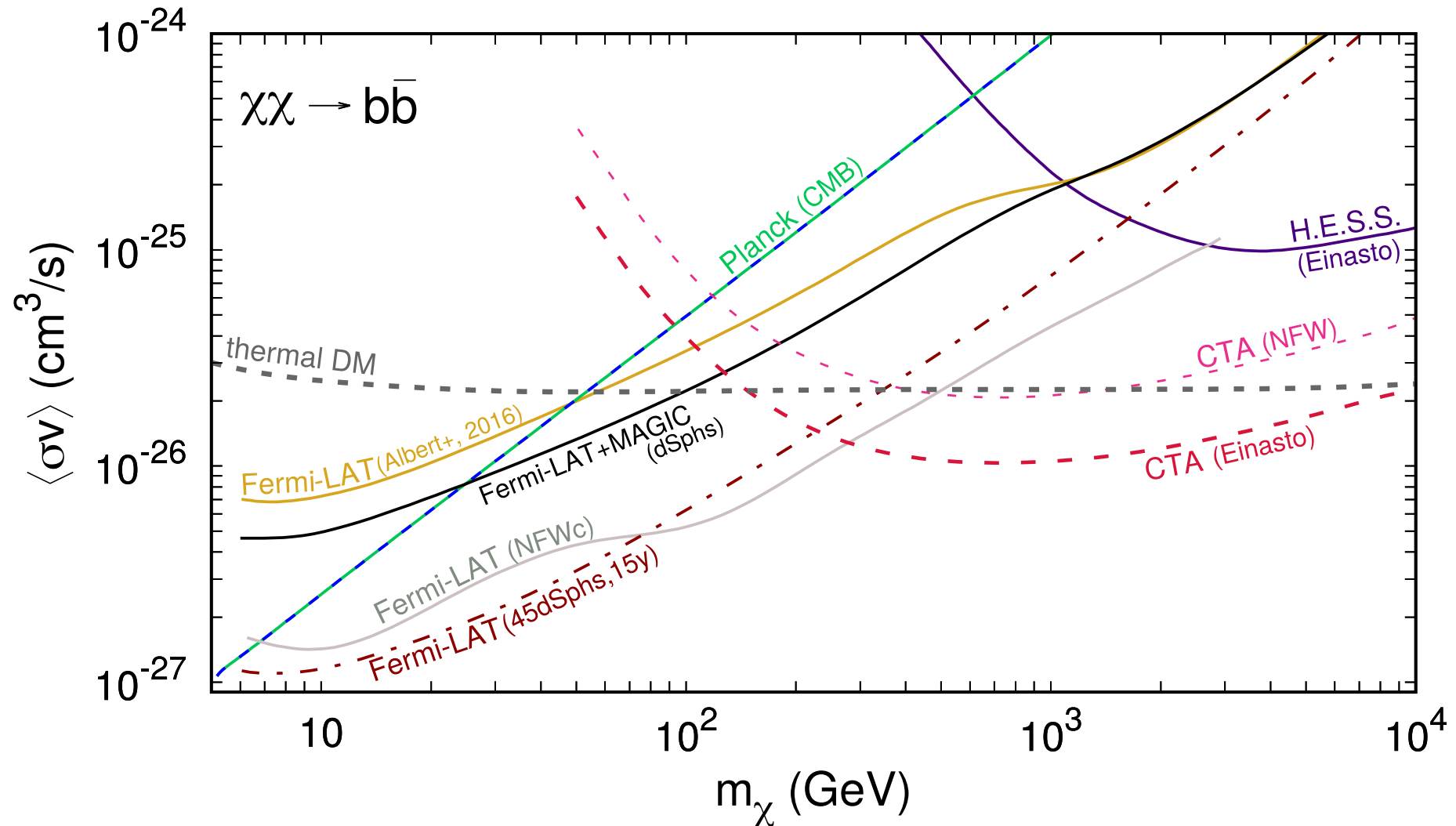
©A. Frebel (MIT)



- $\mathcal{O}(50)$ dSphs have been found so far.
- DM models are constrained.

Indirect detection

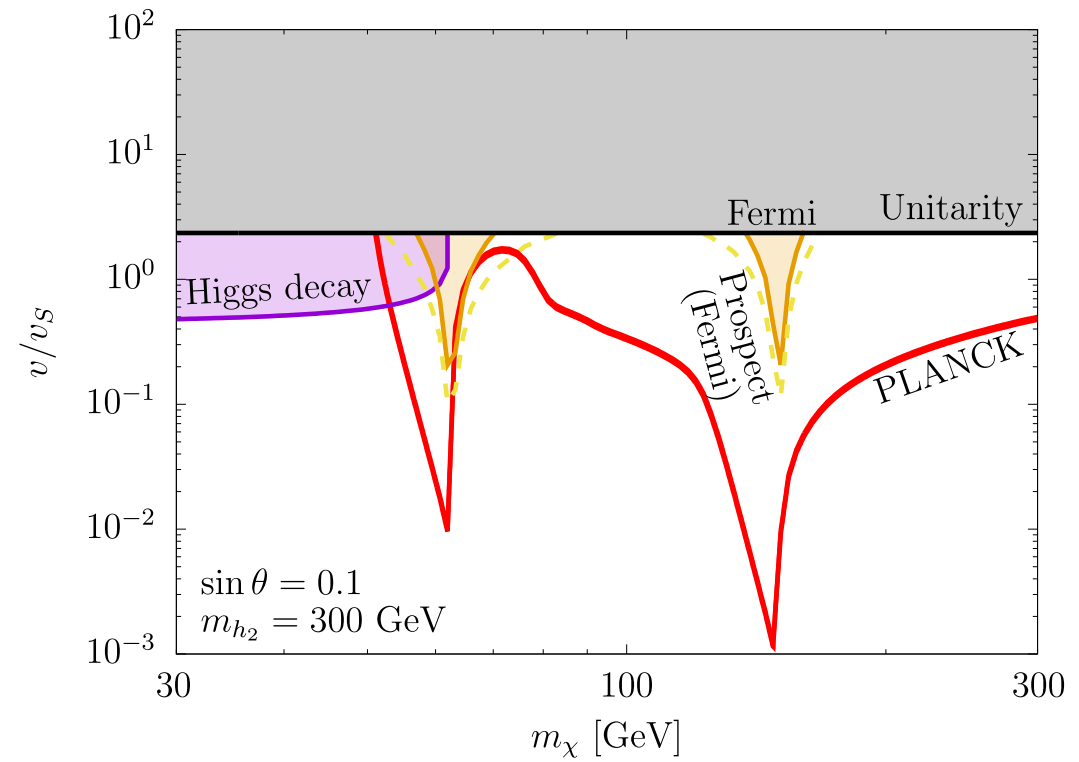
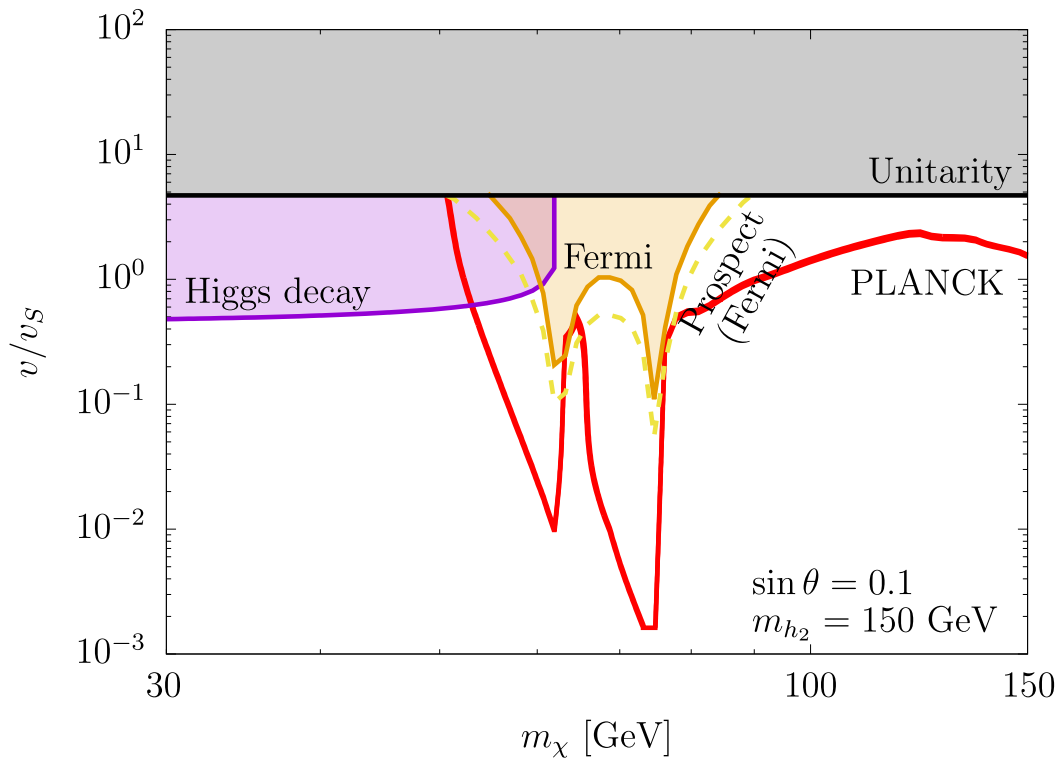
- Present bounds and future prospects ($\chi\chi \rightarrow b\bar{b}$)



L. Roszkowski et al., Rept.Prog.Phys. 81 (2018), [arXiv:1707.06277]

Indirect detection

Huitu, Koivunen, Lebedev, Mondal, TT, arXiv:1812.05952



- Small parameter space is excluded by Fermi-LAT gamma-ray observation
- Thermal WIMP scenarios can be tested only when $m_\chi = \mathcal{O}(100)$ GeV
- CTA is sensitive in heavy DM mass region (DM profile dependent)
 $(\chi\chi \rightarrow h_2 h_2)$ may dominate in this mass range)

Collider search

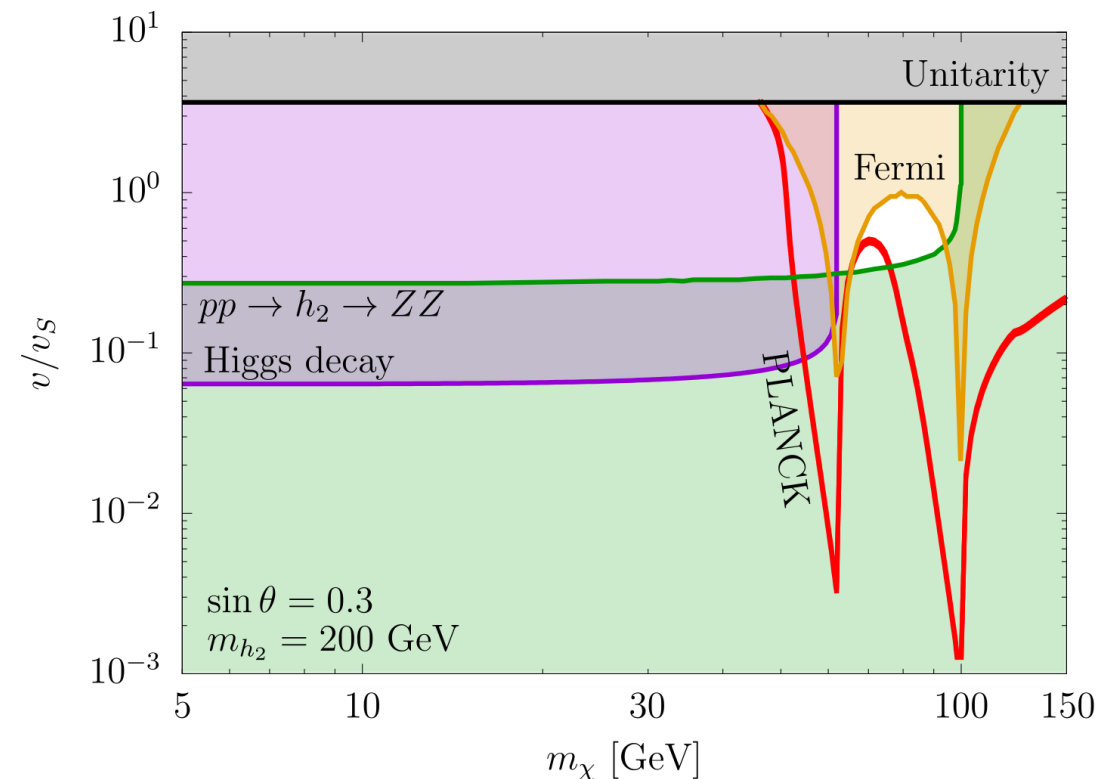
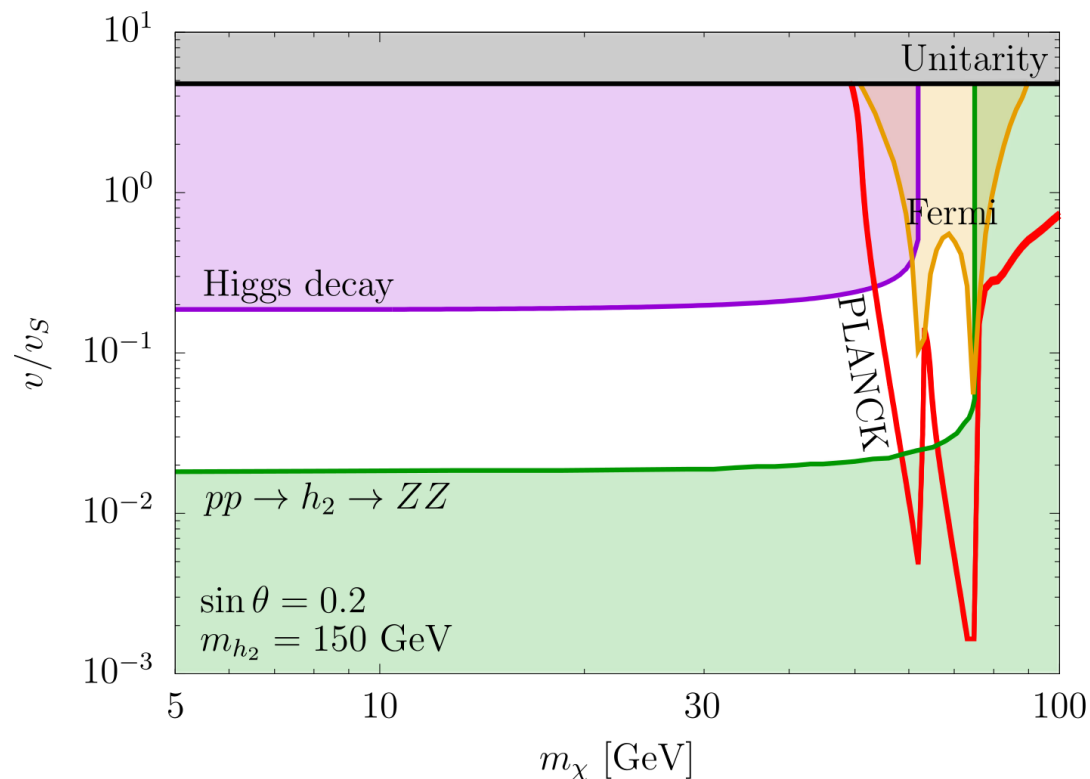
Huitu, Koivunen, Lebedev, Mondal, TT, PRD (2019) [arXiv:1812.05952]

- Constraint on h_2 production cross section at LHC

$$\sigma_{\text{prod}} = \sigma(pp \rightarrow h_2) \text{Br}(h_2 \rightarrow \text{SM}) \propto \sin^2 \theta \text{Br}(h_2 \rightarrow \text{SM})$$

- $pp \rightarrow h_2 \rightarrow ZZ$ mode

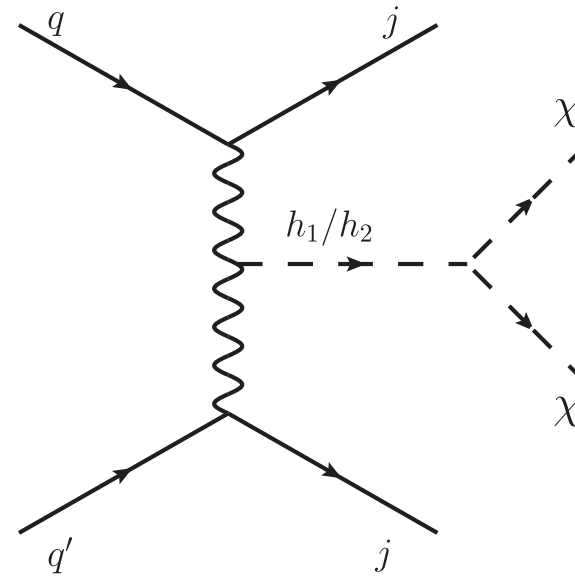
When $\sin \theta \gtrsim 0.2$ and $m_{h_2} \lesssim 2m_{h_1}$, parameters are constrained.



Collider search

Huitu, Koivunen, Lebedev, Mondal, TT, PRD (2019) [arXiv:1812.05952]

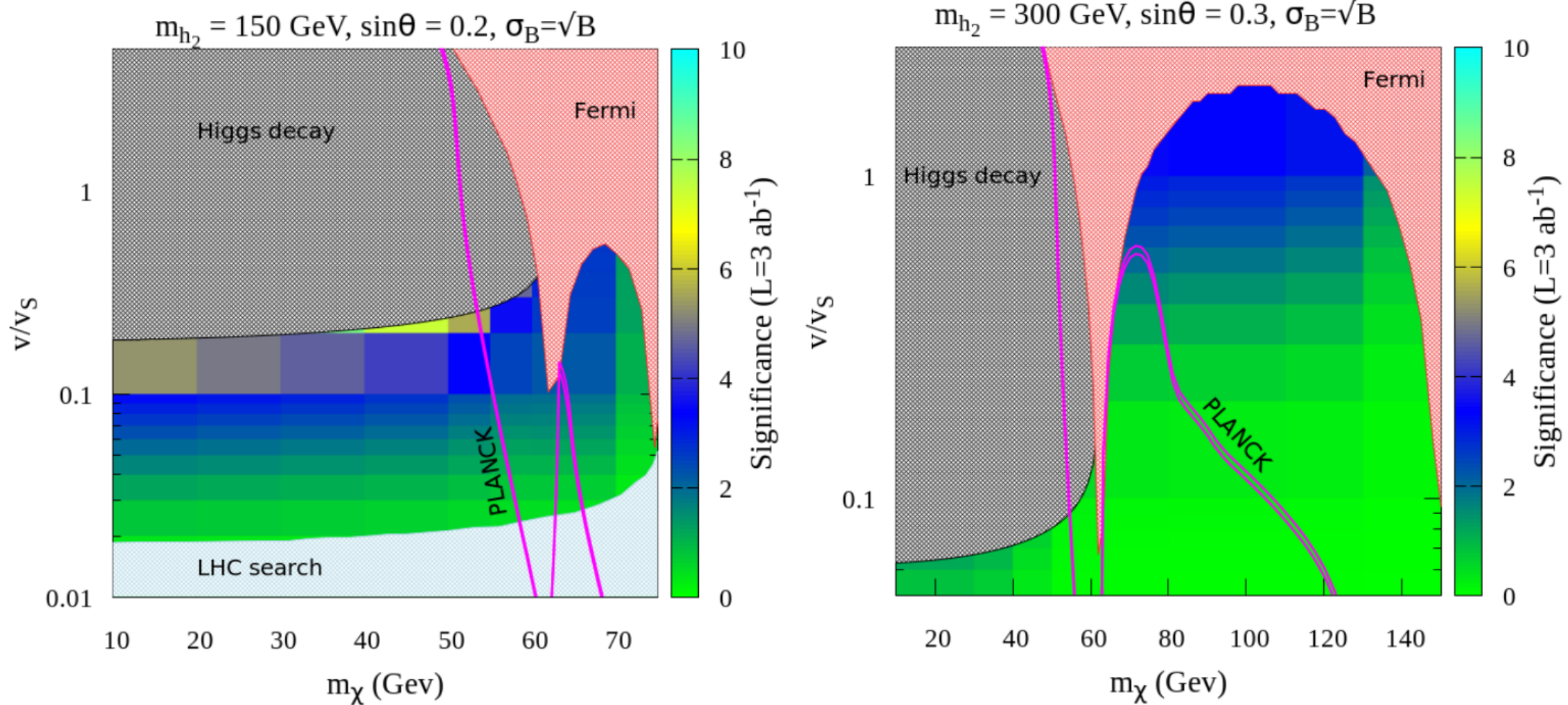
- Signal channel (VBF)
 h_1 and h_2 , both contributions are important
- We focus on $m_{h_2} \geq 2m_\chi$
- Simulate the events and put appropriate cuts
 $\cancel{E}_T > 250 \text{ GeV}$, $p_j > 80 \text{ GeV}$ etc



- Signal significance
$$\mathcal{S} = \frac{S}{\sqrt{S + B + \sigma_B^2}}$$
- Background $B \pm \sigma_B = 1779 \pm 96$ at 35.9 fb^{-1} (CMS)
- Analyzed with 3000 fb^{-1} .

Collider search

Huitu, Koivunen, Lebedev, Mondal, TT, PRD (2019) [arXiv:1812.05952]



- Signal significance can be $\mathcal{S} \approx 4 - 6$ at most.
- $m_\chi \lesssim 100 \text{ GeV}$ can be visible.

Direct detection (1-loop level) K. Ishiwata, TT, JHEP [arXiv:1810.08139]

- Compute Feynman diagrams at 1-loop level

$$\sigma_{\text{SI}}^N = \frac{1}{\pi} \frac{m_N^2}{(m_\chi + m_N)^2} |f_{\text{scalar}}^N|^2$$

where $\frac{f_{\text{scalar}}^N}{m_N} = \sum_{q=u,d,s} C_S^q f_{Tq}^N - \frac{8}{9} C_S^G f_{Tg}^N$ (f_{Tq}^N, f_{Tg}^N : nucleon matrix elements)

$$\langle N | m_q \bar{q}q | N \rangle = f_{Tq}^N m_N, \quad \langle N | \frac{\alpha_s}{\pi} G_{\mu\nu}^a G^{a\mu\nu} | N \rangle = -\frac{8}{9} f_{Tg}^N m_N$$

f_{Tq}^N, f_{Tg}^N are calculated by QCD lattice simulation

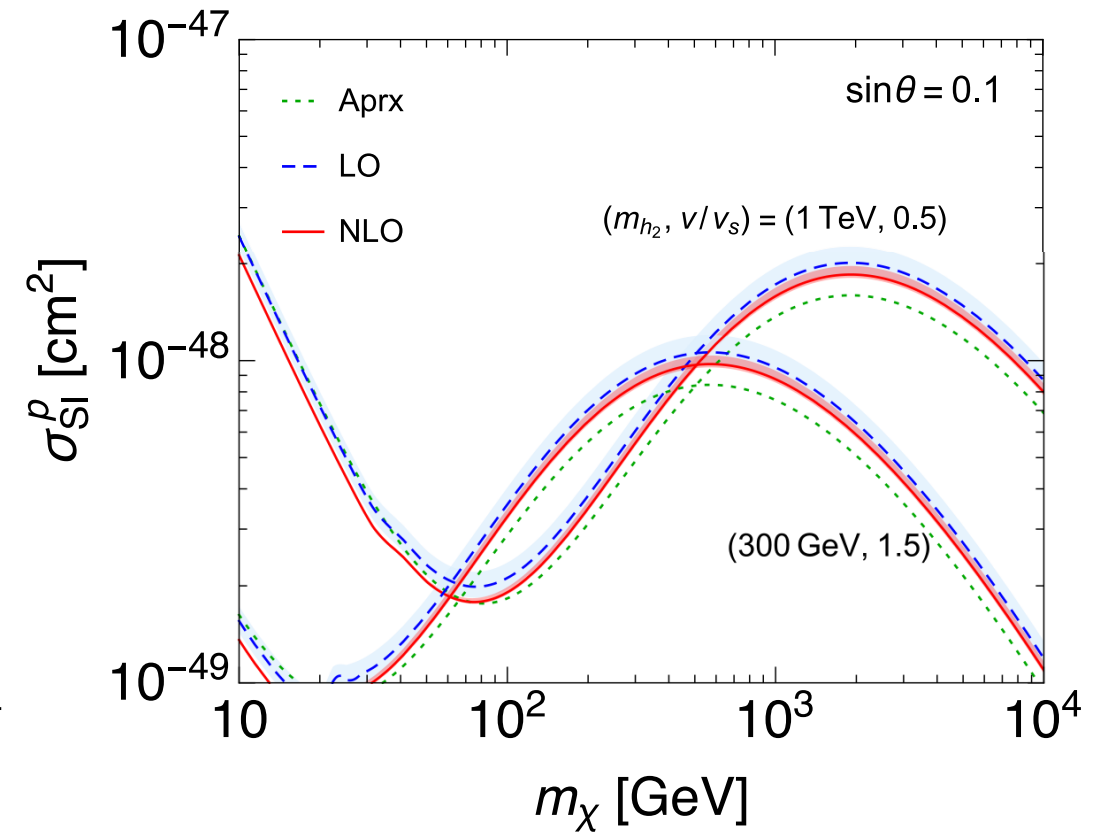
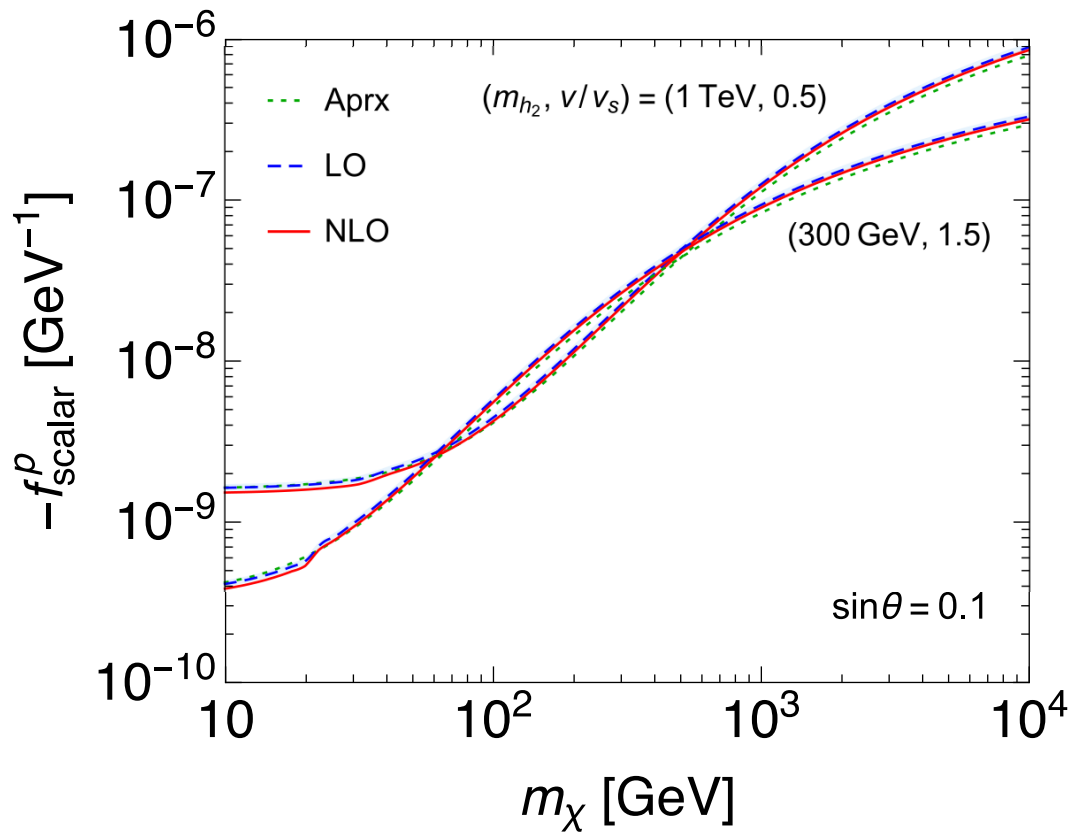
$$\mathcal{L}_{\text{eff}} = C_S^q m_q \chi^2 \bar{q}q + C_S^G \frac{\alpha_s}{\pi} \chi^2 G_{\mu\nu}^a G^{a\mu\nu} \quad \leftarrow C_S^q \text{ and } C_S^G \text{ (calculated)}$$

- Calculate up to 2-loop level in terms of QCD α_s (NLO)

→ scattering amplitude is $\mathcal{O}(\alpha_s)$ J. Hisano, K. Ishiwata, N. Nagata, arXiv:1504.00915

Direct detection (1-loop level)

K. Ishiwata, TT, JHEP [arXiv:1810.08139]



- (i)+(ii) is dominant for large DM mass
- NLO is $\mathcal{O}(10\%)$ correction

Origin of the soft term

C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

- $U(1)$ is extended to gauge symmetry, and a new field Φ is introduced
- Odd charge for S , even charge for Φ

Ex. $q_S = 3, q_\Phi = 2$

$$\mathcal{V} \supset \frac{1}{\Lambda} \Phi^{\dagger 3} S^2 + \frac{1}{\Lambda^3} \Phi^{\dagger 3} |H|^2 S^2 + \frac{1}{\Lambda^3} \Phi^{\dagger 3} |S|^2 S^2 + \dots$$

- After Φ gets a VEV, μ'_S is generated ($\mu'^2_S = \langle \Phi \rangle^3 / \Lambda$)
- Other terms are suppressed by higher dimensional operators
→ the previous model is reproduced in low energy

- CP violation induces DM decay

$$\mathcal{V} \supset \left(\frac{\langle \Phi \rangle}{\Lambda} \right)^3 |H|^2 s \chi \quad \rightarrow \text{lifetime } \tau_\chi \sim \frac{8\pi}{100 \text{ GeV}} \left(\frac{\Lambda}{\langle \Phi \rangle} \right)^6$$

Ex. when $\Lambda = 10^{16} \text{ GeV}$, $\langle \Phi \rangle = 10^7 \text{ GeV} \Rightarrow \tau_\chi \sim 10^{29} \text{ s}$

Collider anomalies

Heinemeyer, Stefaniak, arXiv:1812.05864
 CMS-PAS-HIG-14-037, CMS-PAS-HIG-17-013

- Collider anomalies around 96 GeV. 2.3σ (LEP) and 2.9σ (CMS)

$$b\bar{b} \text{ excess at LEP : } \mu_{\text{LEP}} \equiv \frac{\sigma_{\text{exp}}(e^+e^- \rightarrow h_2 \rightarrow Zb\bar{b})}{\sigma_{\text{SM}}(e^+e^- \rightarrow h_{\text{SM}}(96) \rightarrow Zb\bar{b})} = 0.117 \pm 0.057$$

$$\gamma\gamma \text{ excess at CMS : } \mu_{\text{CMS}} \equiv \frac{\sigma_{\text{exp}}(gg \rightarrow h_2 \rightarrow \gamma\gamma)}{\sigma_{\text{SM}}(gg \rightarrow h_{\text{SM}}(96) \rightarrow \gamma\gamma)} = 0.6 \pm 0.2$$

- Both anomalies cannot be explained at the same time in the model.
- But can be explained if a new scalar quark Φ is added.
 → change $h\gamma\gamma$ and hgg effective couplings (and other couplings)
- Φ is triplet or sextet

$$\mathcal{L} = -\lambda_{S\Phi}|S|^2|\Phi|^2 - \lambda_{H\Phi}|H|^2|\Phi|^2 + \left(y_{\Phi}\Phi^*\overline{q_R}q_R^c \quad \text{or} \quad \frac{\Phi}{\Lambda^3}(\overline{q_R}q_R^c)^2 \right)$$

$$m_{\Phi}^2 = \mu_{\Phi}^2 + \frac{\lambda_{S\Phi}}{2}v_s^2 + \frac{\lambda_{H\Phi}}{2}v^2 \equiv \mu_{\Phi}^2 + \bar{\mu}_{\Phi}^2$$

Collider anomalies

Cline, TT, PRD (2019) [arXiv:1906.07659]

■ Model list:

| model | q_Φ | N_c | $\frac{m_\Phi}{ \lambda_{S\Phi} ^{1/2}}$ [GeV] | $\frac{\bar{\mu}_\Phi}{ \lambda_{S\Phi} ^{1/2}}$ [GeV] | s_θ | $\lambda_{S\Phi}$ | $\lambda_{H\Phi}$ | $\chi^2/\text{d.o.f.}$ |
|-------|----------|-------|--|--|------------|-------------------|-------------------|------------------------|
| 1 | 8/3 | 6 | 943 | 836 | 0.39 | 1.9 | 3.3 | 3.6 |
| 2 | 8/3 | 3 | 601 | 778 | 0.36 | 1.4 | 1.6 | 2.2 |
| 3 | 5/3 | 6 | 700 | 741 | 0.34 | 3.4 | 3.5 | 2.1 |
| 4 | 5/3 | 3 | 417 | 838 | 0.39 | 3.0 | 5.2 | 3.7 |
| 5 | 2/3 | 6 | 588 | 795 | 0.37 | 4.8 | 5.9 | 1.4 |
| 6(*) | 2/3 | 3 | 284 | 765 | 0.35 | 3.4 | 3.6 | 1.5 |
| 7 | -1/3 | 6 | 554 | 830 | 0.39 | 5.4 | 8.0 | 1.5 |
| 8(*) | -1/3 | 3 | 256 | 810 | 0.38 | 4.1 | 5.6 | 1.4 |
| 9 | -4/3 | 6 | 666 | 752 | 0.35 | 3.8 | 3.9 | 1.8 |
| 10(*) | -4/3 | 3 | 333 | 737 | 0.34 | 2.4 | 3.0 | 2.5 |

■ We need large couplings $\lambda_{S\Phi}$, $\lambda_{H\Phi}$, and large mixing s_θ

■ Mass bounds: $m_\Phi \gtrsim 720$ GeV (triplet 4jet)

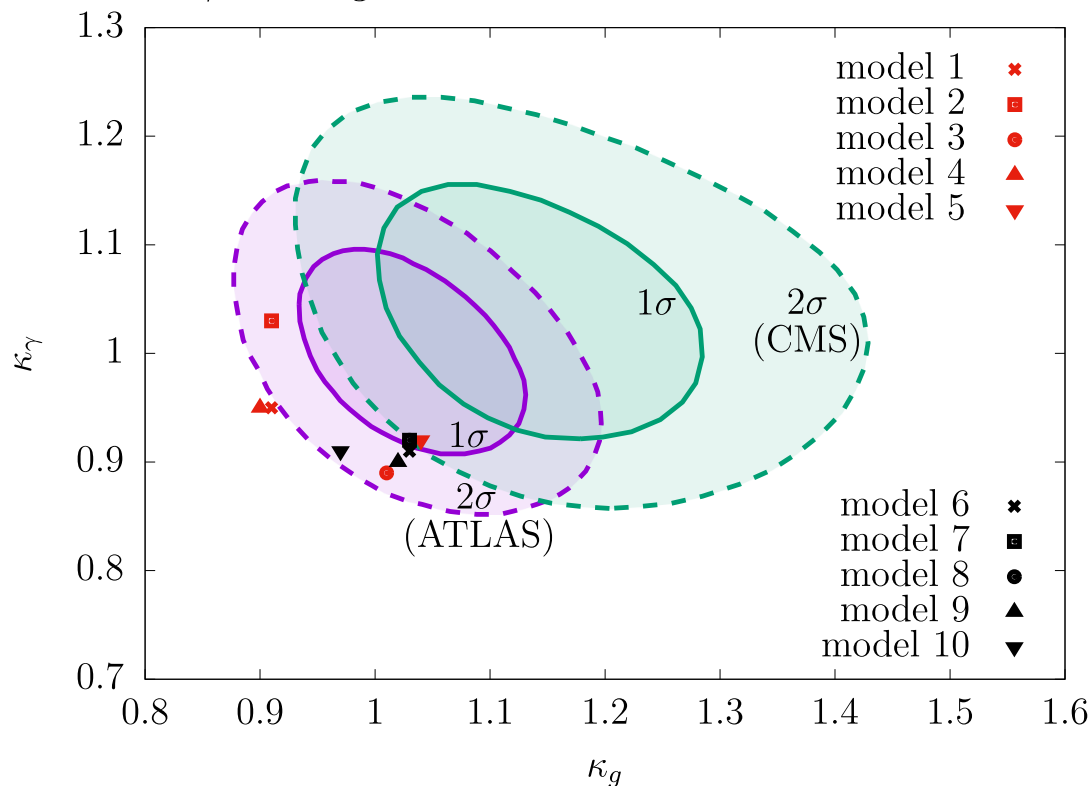
$m_\Phi \gtrsim 1.3$ TeV (sextet 4jet)

$m_\Phi \gtrsim 520$ GeV (triplet 2jet)

Collider anomalies

Cline, TT, PRD (2019) [arXiv:1906.07659]

■ $\kappa_\gamma - \kappa_g$ plane



- Higgs coupling strengths are also affected

$$\kappa_i = \frac{\text{coupling in our model}}{\text{coupling in SM}}$$

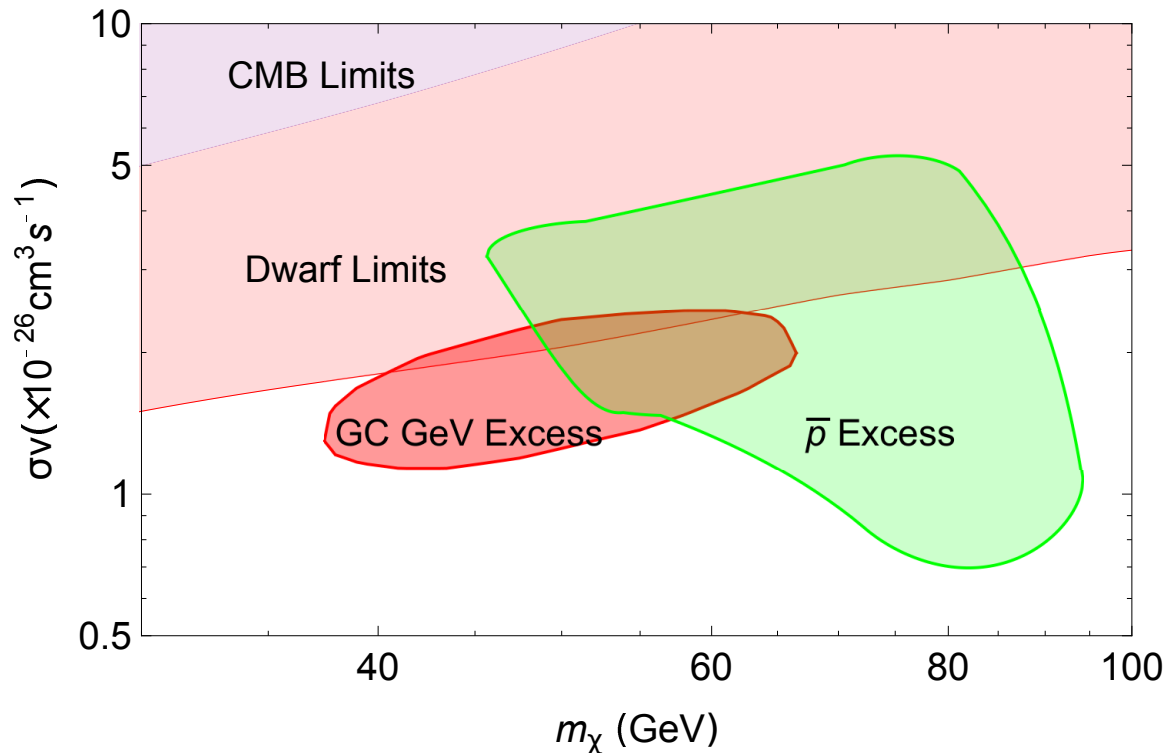
ex. $\mathcal{L} = g_{hZZ} h Z^2 \rightarrow \kappa_Z = c_\theta$

- Model 5,6,7,8 within 2σ range (all observables).

- $\chi\chi \rightarrow \gamma\gamma$ is also enhanced by Φ . $\rightarrow \sigma_{\gamma\gamma\nu} \sim 10^{-28} \text{ cm}^3/\text{s}$ slightly below the Fermi bound $(0.5 - 4) \times 10^{-28} \text{ cm}^3/\text{s}$

Cosmic ray anomalies

Cholis, Linden, Hooper, PRD (2019) [arXiv:1903.02549]



- Excesses in gamma ray and anti-proton cosmic ray. $\gtrsim 4\sigma$
- could be (thermal) DM signal. (other explanations: pulsar etc)

$$\chi\chi \rightarrow f\bar{f}, WW, ZZ \rightarrow \gamma, \bar{p}$$

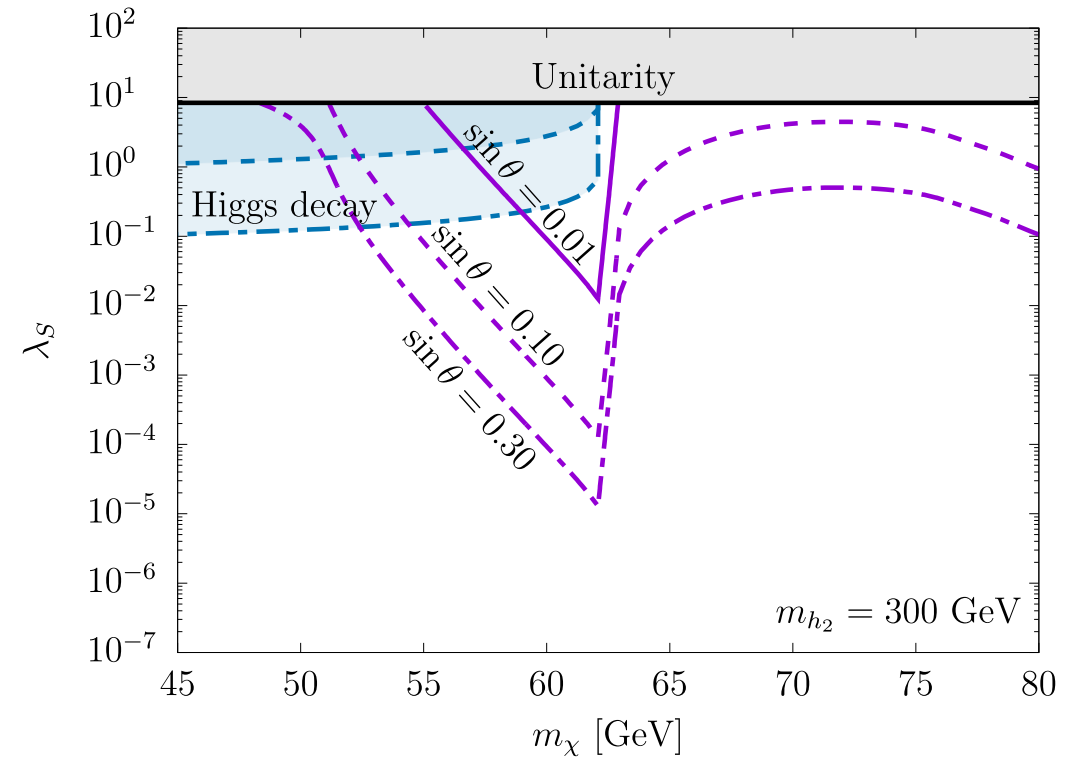
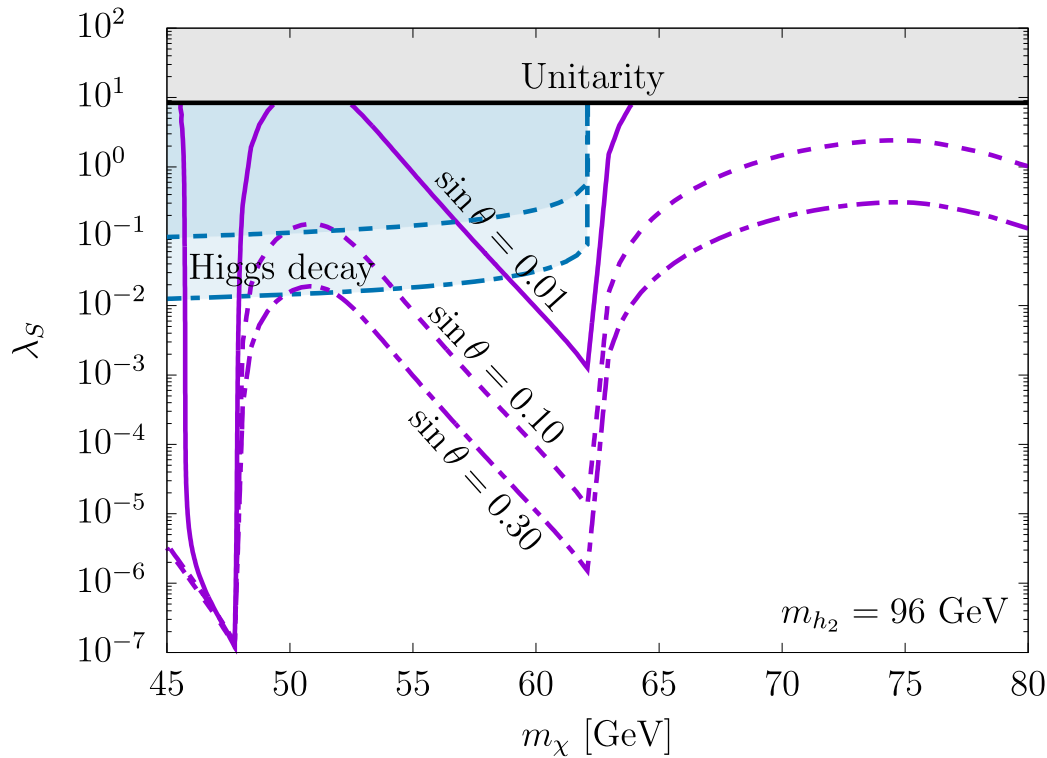
- Cross section: $\langle \sigma_{b\bar{b}v} \rangle \approx (0.8 - 5.2) \times 10^{-26} \text{ cm}^3/\text{s}$
DM mass: 64 – 88 GeV

→ coincide with $\langle \sigma v \rangle$ for thermal WIMP scenarios.

- Typical thermal WIMP conflicts with direct detection bound. But pseudo Goldstone DM can naturally avoid the constraint.

Cosmic ray anomalies

Cline, TT, PRD (2019) [arXiv:1906.07659]



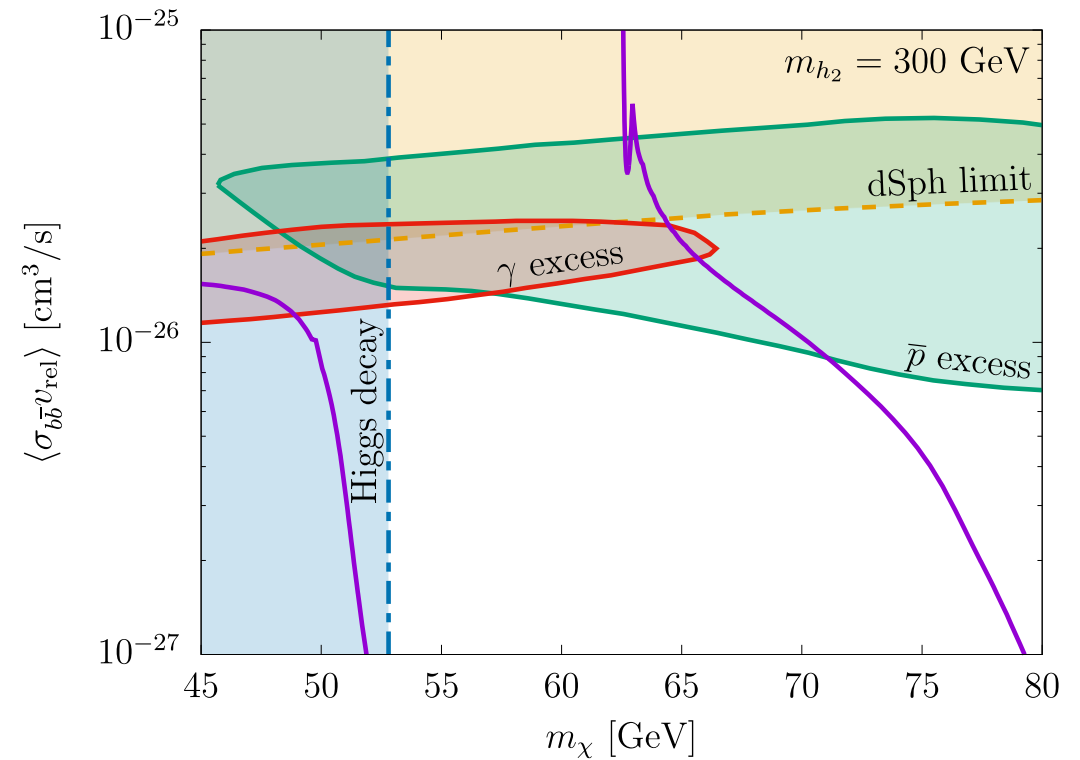
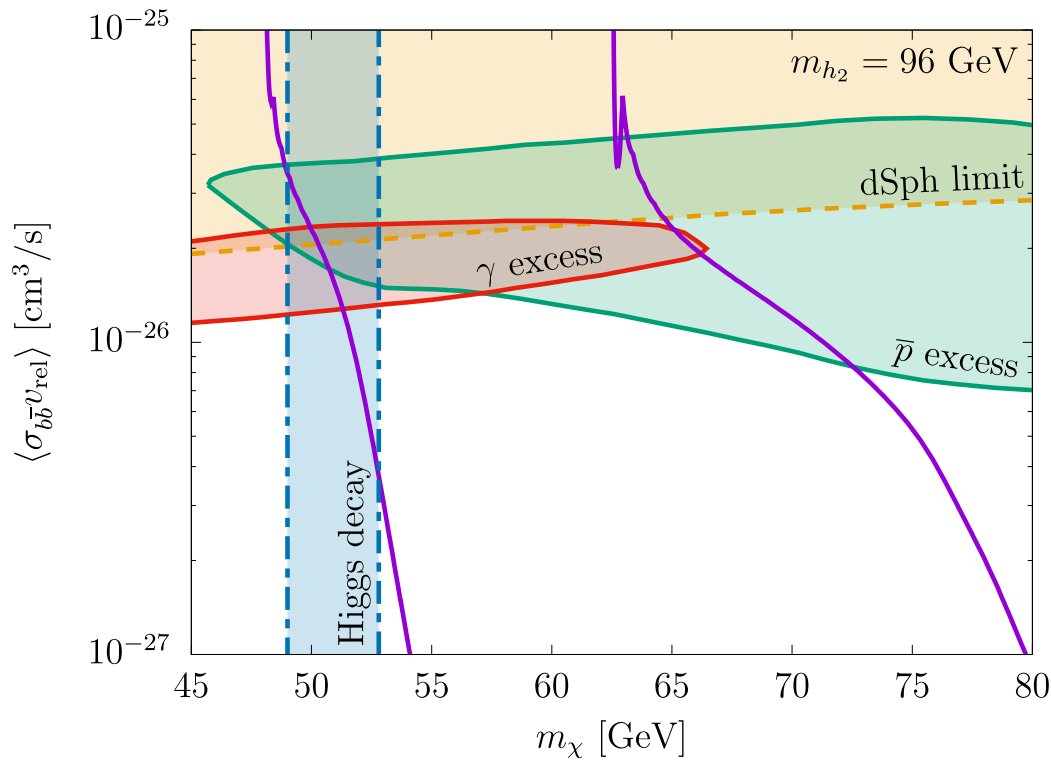
- $m_{h_2} = 96, 300 \text{ GeV}$.

- Higgs invisible decay $\text{Br}(h_1 \rightarrow \text{inv}) \lesssim 0.2$. $\Gamma_{\text{inv}} = \frac{\sin^2 \theta m_{h_1}^3}{32\pi v_s^2} \sqrt{1 - 4 \frac{m_\chi^2}{m_{h_1}^2}}$

- Purple lines: thermal relic abundance at PLANCK

Cosmic ray anomalies

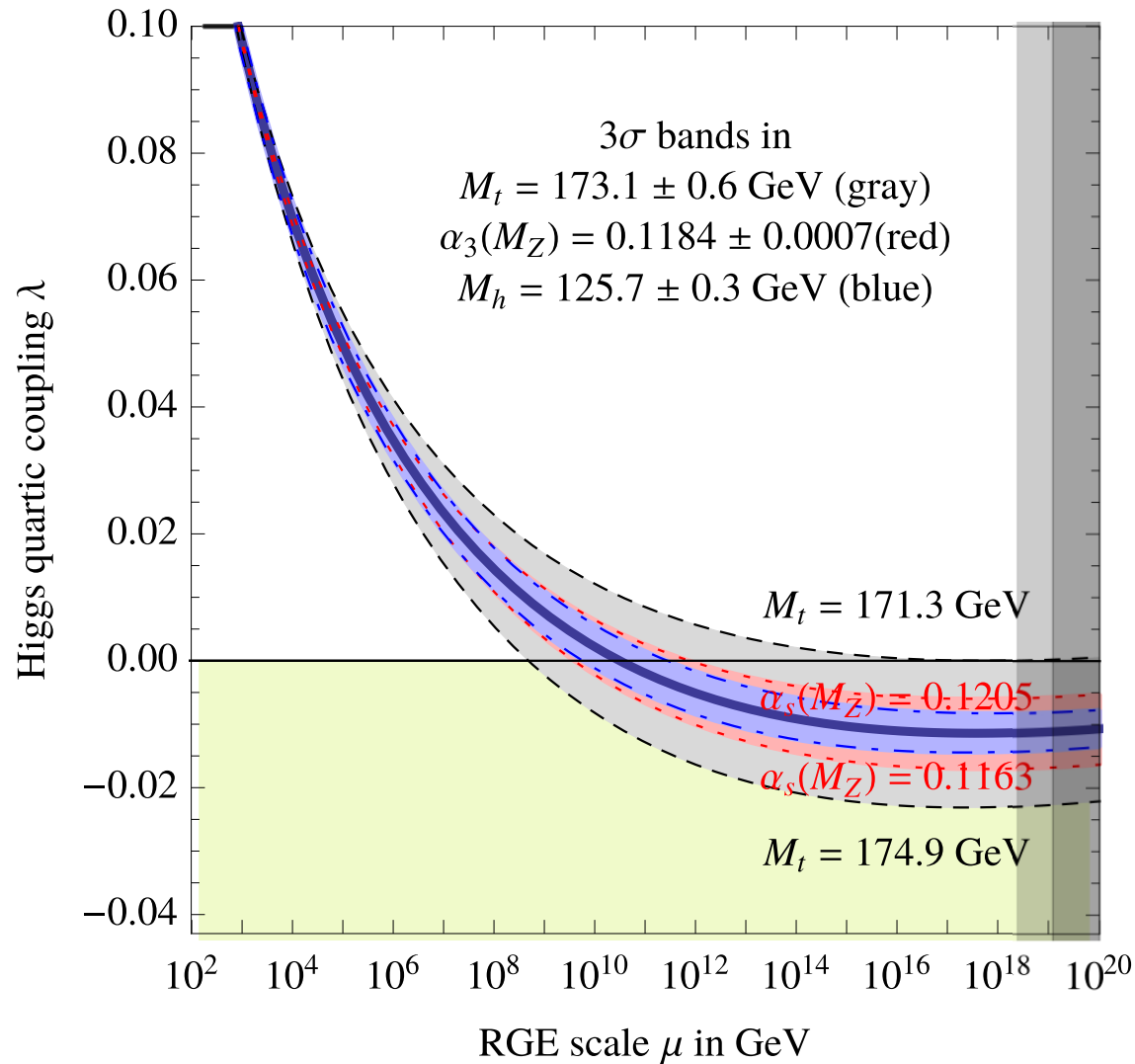
Cline, TT, PRD (2019) [arXiv:1906.07659]



- $\chi\chi \rightarrow b\bar{b}$ cross section
- $m_{h_2} = 96, 300$ GeV.
- Additional channel $\chi\chi \rightarrow h_2 h_2$ if $m_\chi > m_{h_2}$. \rightarrow mixing dependence
- Cosmic-ray anomalies can be explained by pseudo Goldstone DM in 2σ CL if $m_\chi = 64 - 67$ GeV.

Potential stability in SM

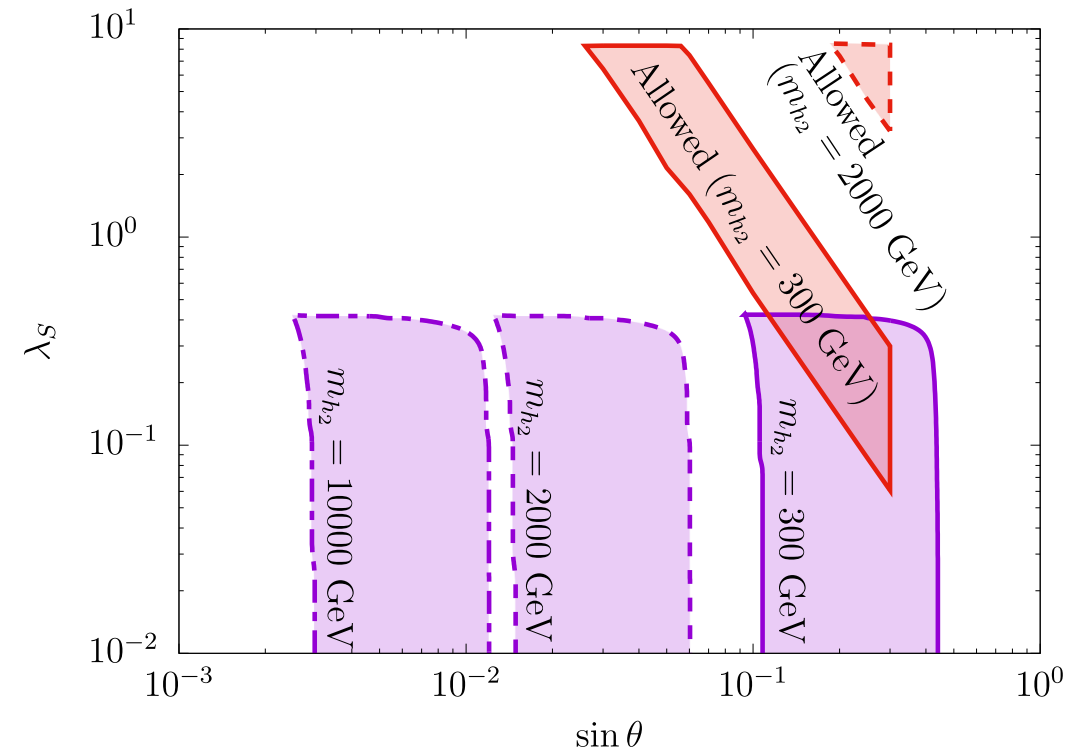
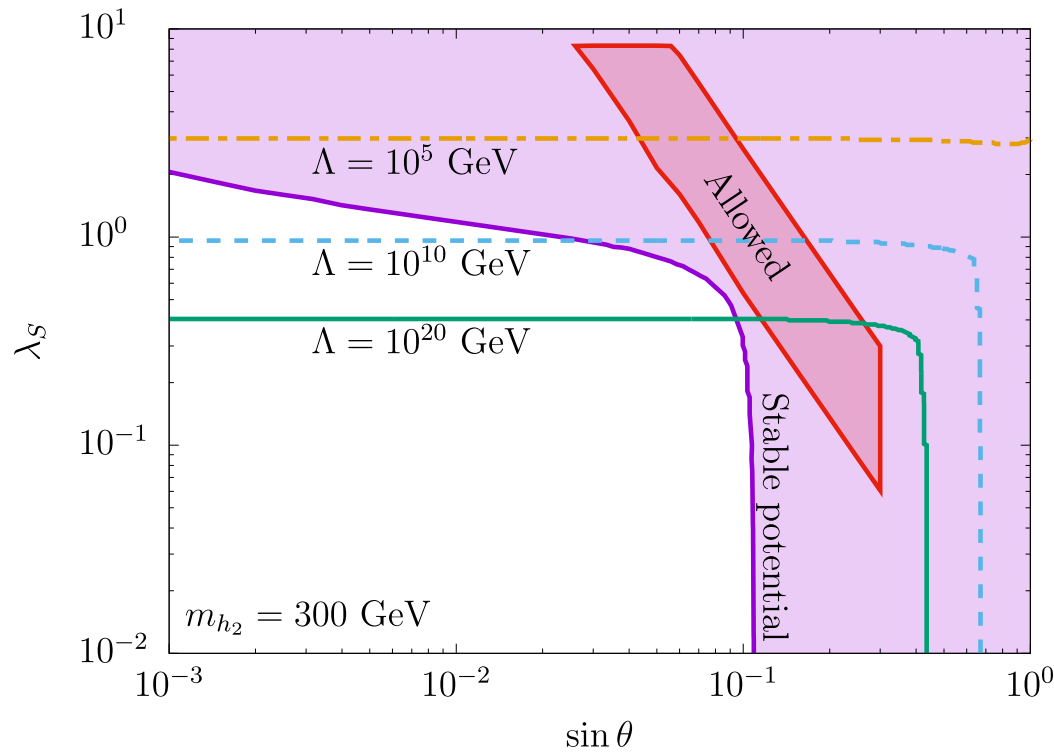
Degrassi et al., JHEP (2012) [arXiv:1205.6497]



- Running of λ_H via β function
- Potential is destabilized around $\mu \sim 10^{11}$ GeV. $\rightarrow \lambda_H < 0$
- Strongly depends on m_t

Potential stability with h_2

Cline, TT, PRD (2019) [arXiv:1906.07659]



- Stability and perturbativity ($\leq 4\pi$) up to Planck scale
- Red region: explain cosmic ray anomalies
- Cosmic ray anomalies, potential stability and perturbative couplings up to Planck scale
 $\rightarrow 140 \lesssim m_{h_2} \lesssim 500 \text{ GeV}$