

Thermal modifications of meson states in lattice QCD and relations to heavy ion collisions

Yu Maezawa (YITP, Kyoto University)

with Frithjof Karsch^{1,2}, Swagato Mukherjee², Peter Petreczky²

¹Universität Bielefeld, ²Brookhaven National Lab.

- ✧ Full-QCD lattice simulations on physical point
- ✧ All mesons modified even below T_C except for charmonium
- ✧ Universal mass shifts depending on parity channels

Contents

Introduction

- Mesons in medium
- Lattice QCD simulations
 - Full-QCD approach
 - Spatial correlation functions

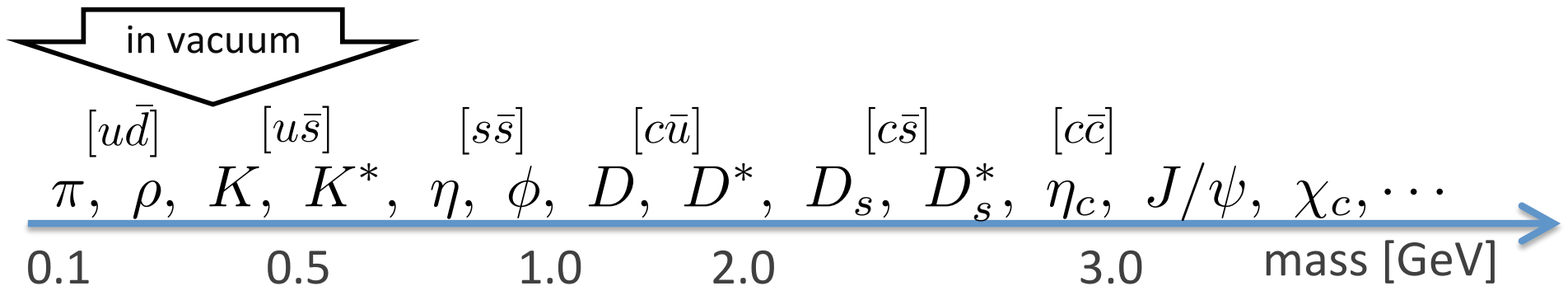
Lattice simulations

- Modification of spectral function
 - appears all mesons below T_C ,
 - but charmonium stable beyond T_C
- Universal mass shift of screening masses

Summary & Discussions

Variety of mesons

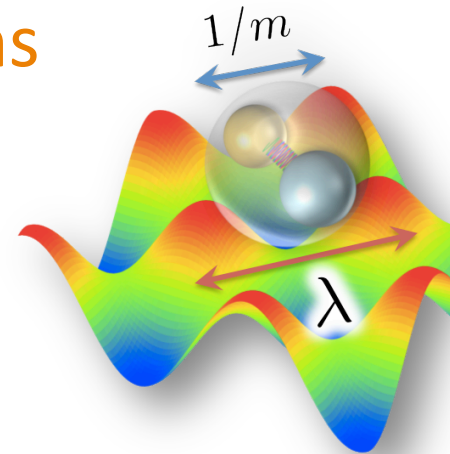
up/down: $m_{ud} \sim 3\text{--}5$ MeV, strange: $m_s \sim 95$ MeV, charm: $m_c \sim 1.2$ GeV...



In medium: modified due to thermal fluctuations

significant when: (thermal wavelength λ) $>$ (size $1/m$)

Modification pattern: Good probes of QCD matter



- Light mesons: sensitive to chiral properties

scaling law Brown and Rho (1991)

$$\sqrt[3]{\frac{\langle \bar{q}q \rangle^*}{\langle \bar{q}q \rangle}} \approx \frac{f_\pi^*}{f_\pi} \approx \frac{m_\rho^*}{m_\rho} \quad \rightarrow \quad \text{mass shift? and restoration?}$$

- Quarkonium: Sequential dissolution pattern

J/ψ suppression Matsui and Satz (1986)

\rightarrow charmonium stable in quark-gluon plasma?

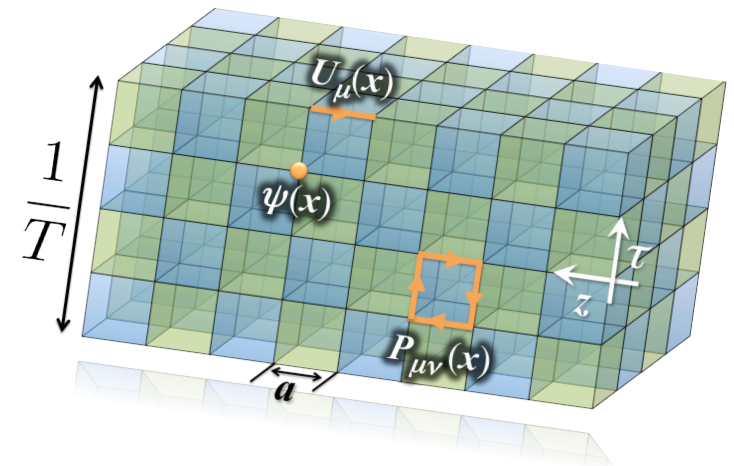
Lattice QCD simulations

QCD: Strong non-linearity and infinite-dimensional integral

→ Field theory on lattice
in Euclidean space

→ Monte-Carlo simulations
based on importance sampling

$$\begin{aligned}\langle \mathcal{O} \rangle &= \frac{1}{Z} \int D\bar{q} Dq DA \mathcal{O}(\bar{q}, q, A) e^{-S_{QCD}} \\ &= \frac{1}{N_{\text{conf}}} \sum_{\{U_i\}}^{N_{\text{conf}}} \mathcal{O}(U_i) \pm O\left(\frac{1}{\sqrt{N_{\text{conf}}}}\right)\end{aligned}$$



Fundamental parameters:

$\Lambda_{\text{QCD}}, m_{u/d}, m_s, m_c$
determined at $T = 0$



Finite temperature:

**Theoretical prediction
in 1st principle calculations**

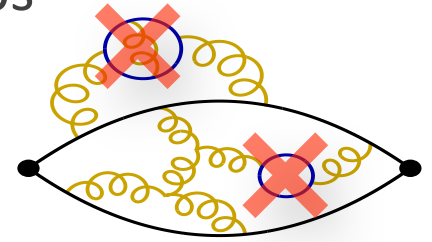
Applicable: Static & homogeneous system

(difficult: non-equilibrium, time dependent, high density...)

Key: Full(2+1)-QCD simulations on physical point

↔ e.g.) Quenched simulations: neglect quark-loops

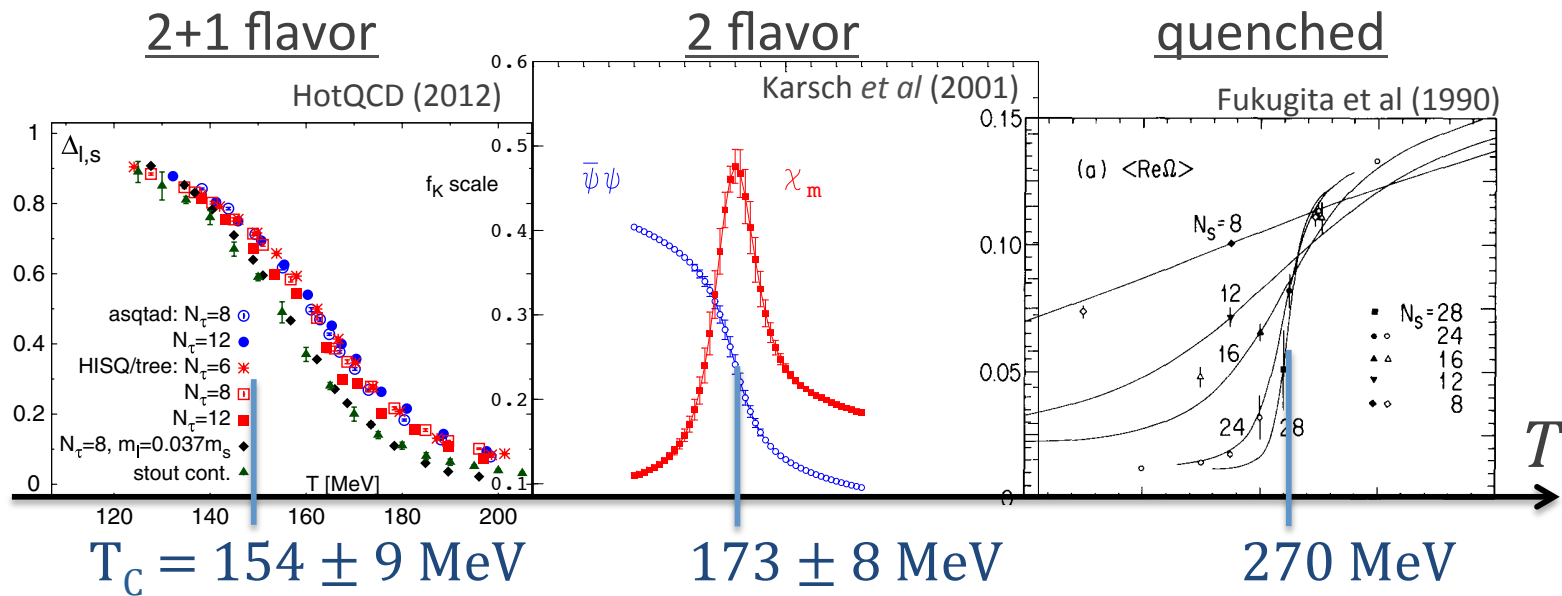
$$Z_{\text{QCD}} = \int dU \det D(U) e^{-S_{\text{gluon}}}$$



$T = 0$: Reproduce physical hadron spectra within 10-20% deviations
CP-PACS Coll. (2000)

$T > 0$: Significant discrepancy, e.g. phase transition

Quenched: 1st order PT → Full(2+1 and 2): Crossover PT



Full-QCD simulations: indispensable for thermal properties

Mesons on lattice

difficult at finite temperature...

Temporal correlation function

e.g.) $J_H = \bar{q}\Gamma_H q$

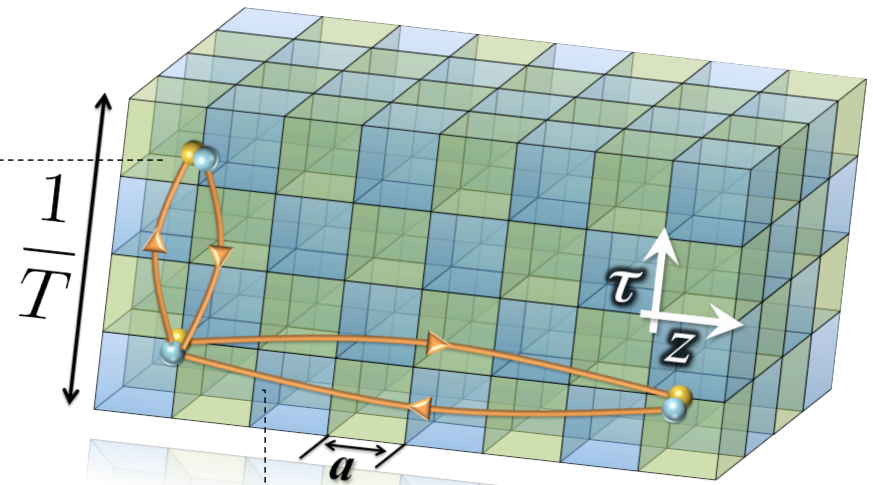
$$G(\tau) = \int d^3x \langle J_H^\dagger(\tau, \mathbf{x}) J_H(0, \mathbf{0}) \rangle = \underbrace{A_0 e^{-m_0 \tau}}_{\text{Ground state: dominant at large } \tau} + \underbrace{A_1 e^{-m_1 \tau}}_{\text{1st excited state } (m_1 > m_0)} + \dots$$

Physical limitation $\tau < 1/T$:
difficult to access thermal modification

Spatial correlation function

$$G^S(z, T) = \int_0^{1/T} d\tau \int dx dy \langle J_H(\tau, \vec{x}) J_H(0, \vec{0}) \rangle \xrightarrow{z \rightarrow \infty} A e^{-M(T)z}$$

$M(T)$: screening mass



No limitation: more sensitive to in-medium modification

Mesons on lattice

Spectral function $\sigma(\omega, T) \in$ pole mass, width and thermal modification...

Temporal correlation function

$$G^T(\tau, T) = \int_0^\infty d\omega \frac{\cosh(\omega(\tau - 1/2T))}{\sinh(\omega/2T)} \sigma(\omega, T)$$

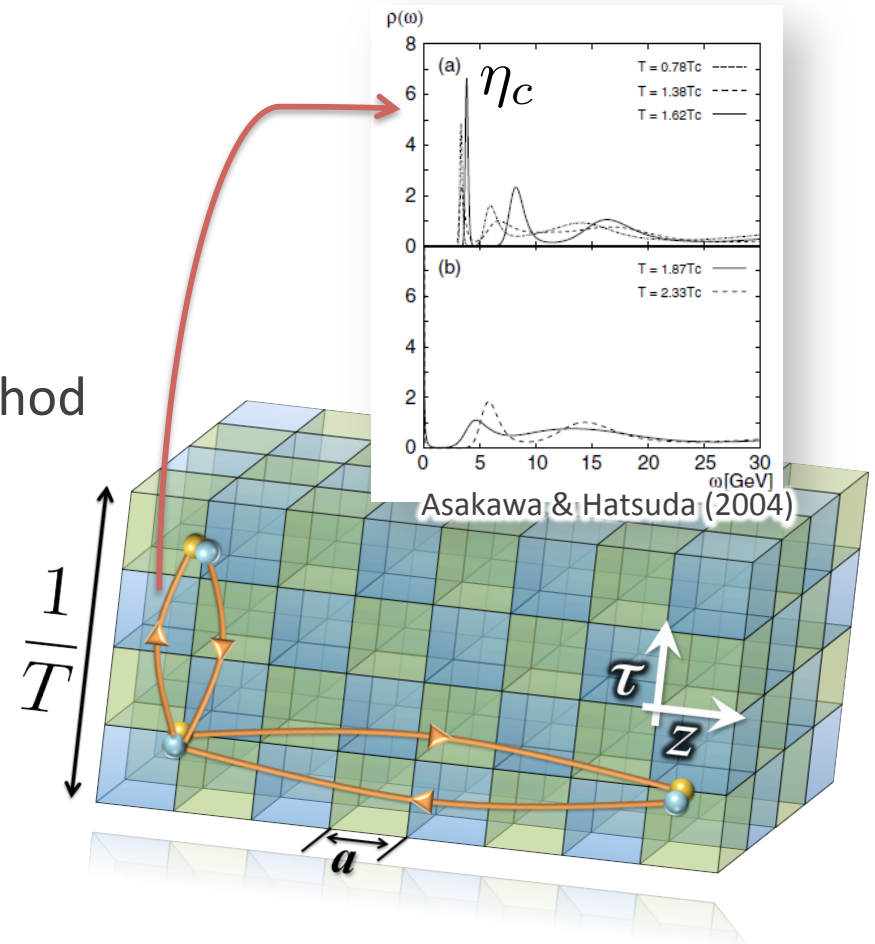
Reconstruction of σ : Maximum Entropy Method
large # of time separation: necessary
almost done in Quenched approx.

Spatial correlation function

$$G^S(z, T) = \int_0^\infty \frac{2d\omega}{\omega} \int_{-\infty}^\infty dp_z e^{ip_z z} \sigma(\omega, p_z, T)$$

No T dependence in Kernel

$G^S(z, T)/G^S(z, T=0)$: direct probe of thermal modification of σ
accessible in Full-QCD simulations



Mesons on lattice

Spatial correlation function

$$G^S(z, T) = \int_0^{1/T} d\tau \int dx dy \langle J_H(\tau, \vec{x}) J_H(0, \vec{0}) \rangle \xrightarrow{z \rightarrow \infty} A e^{-M(T)z} \quad M(T): \text{screening mass}$$

Behavior in limiting cases:

At low T , bound state w/o thermal effect:

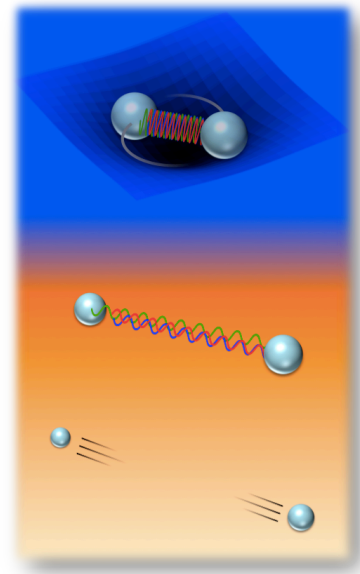
$$\begin{aligned} \rightarrow & G^S(z, T)/G^S(z, T=0) = 1 \\ & M(T) \sim m_0 \text{ pole mass at } T=0 \\ & \sigma(\omega, 0, 0, p_z, T) \sim \delta(\omega^2 - p_z^2 - m_0^2) \end{aligned}$$

At $T \sim T_c$, in-medium modification and/or dissolution:

$$\begin{aligned} \rightarrow & G^S(z, T)/G^S(z, T=0) \neq 1 \\ & M(T): \text{Leading response of mass shift} \\ & M(T) > m_0 \text{ or } < m_0 ? \end{aligned}$$

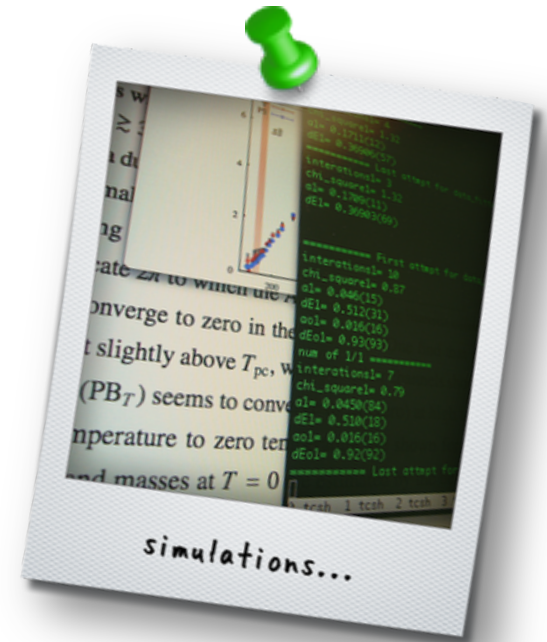
At $T \rightarrow \infty$, free quark-antiquark pair: $M \rightarrow 2\sqrt{m_q^2 + (\pi T)^2}$

with the lowest Matsubara frequency



Lattice QCD simulations

- 2+1 flavor QCD in HISQ action HotQCD '11, '14 (charm quenched)
- m_s : physical, $m_l/m_s = 1/20$
($m_\pi \sim 160$ MeV, $m_K \sim 504$ MeV)
- $N_\tau = 8, 10, 12$: keeping $N_s/N_\tau = 4$ → continuum limit
- $32^4 \text{--} 48^3 \times 64$ at $T = 0$
- scale: f_k input
- calculating quark-line connected part



Mesons

Γ	J^P	$u\bar{d}$	$u\bar{s}$	$u\bar{c}$	$s\bar{s}$	$s\bar{c}$	$c\bar{c}$
γ_5	0^-	π	K	D	$(\eta_{s\bar{s}})$	D_s	η_c
1	0^+	–	K_0^*	D_0^*	–	D_{s0}^*	χ_{c0}
γ_i	1^-	ρ	K^*	D^*	ϕ	D_s^*	J/ψ
$\gamma_i\gamma_5$	1^+	a_1	K_1	D_1	$f_1(1420)$	D_{s1}	χ_{c1}

Thermal modifications

$$G^S(z, T)/G^S(z, T = 0)$$

Screening masses

$$G^S(z, T) \rightarrow Ae^{-M(T)z}$$

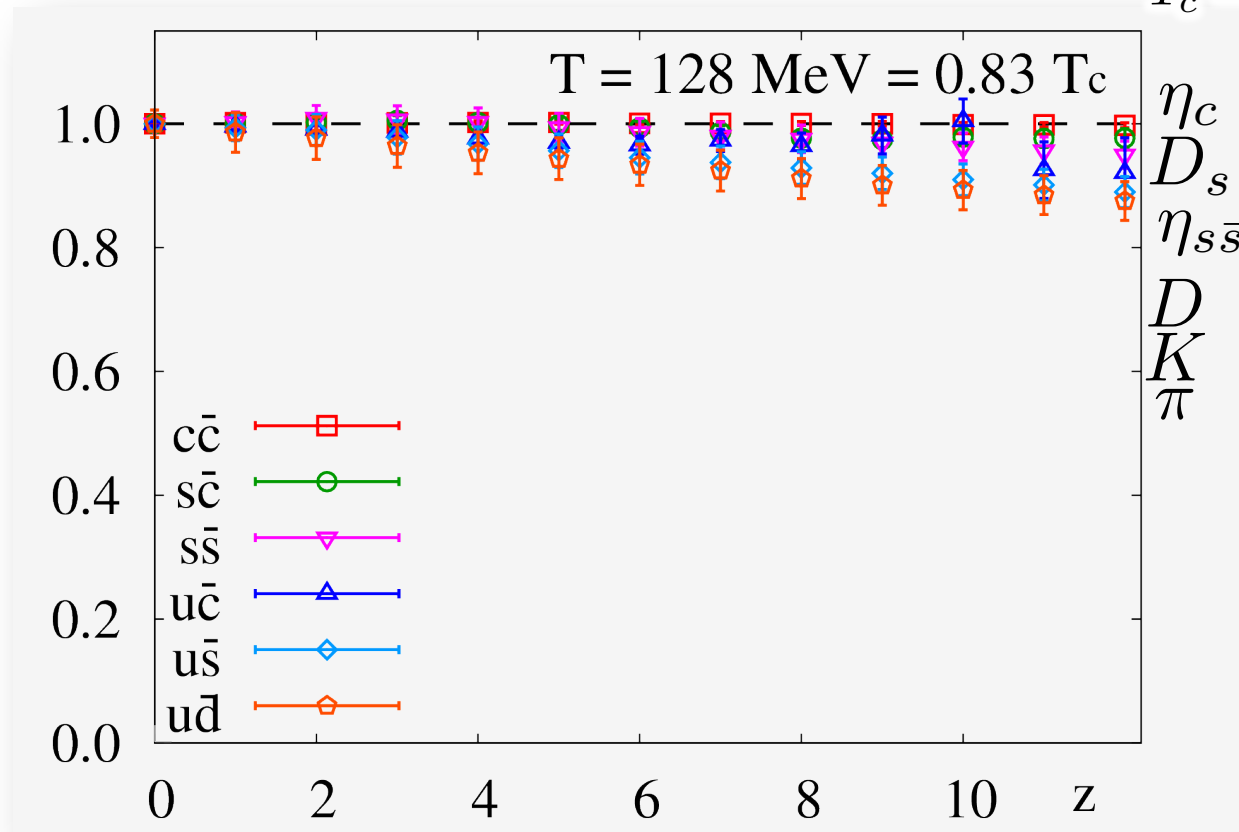
Ratio of spatial correlation functions

Probe of thermal modifications of spectral function

$G^S(z, T)/G^S(z, T = 0) \simeq 1$ the same σ at $T = 0$, or $\neq 1$ modified

$T_c = (154 \pm 9) \text{ MeV}$

Pseudo-scalar
 $J^P = 0^-$



- modification even at $T < T_c$, except for charmonium

- significant flavor dependence at $T > T_c$,

but no change on η_c : modified at $T \gtrsim 1.3 T_c$

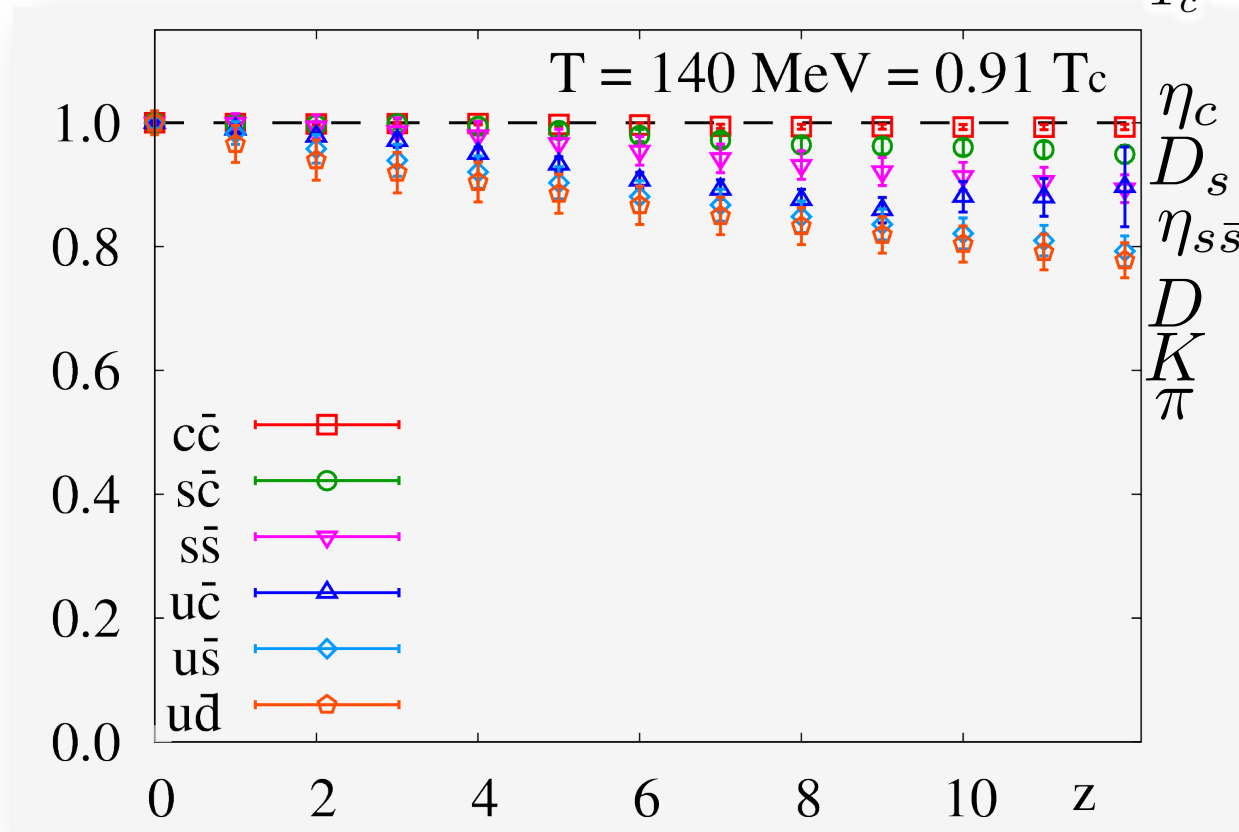
Ratio of spatial correlation functions

Probe of thermal modifications of spectral function

$G^S(z, T)/G^S(z, T = 0) \simeq 1$ the same σ at $T = 0$, or $\neq 1$ modified

$T_c = (154 \pm 9) \text{ MeV}$

Pseudo-scalar
 $J^P = 0^-$



- modification even at $T < T_c$, except for charmonium

- significant flavor dependence at $T > T_c$,

but no change on η_c : modified at $T \gtrsim 1.3 T_c$

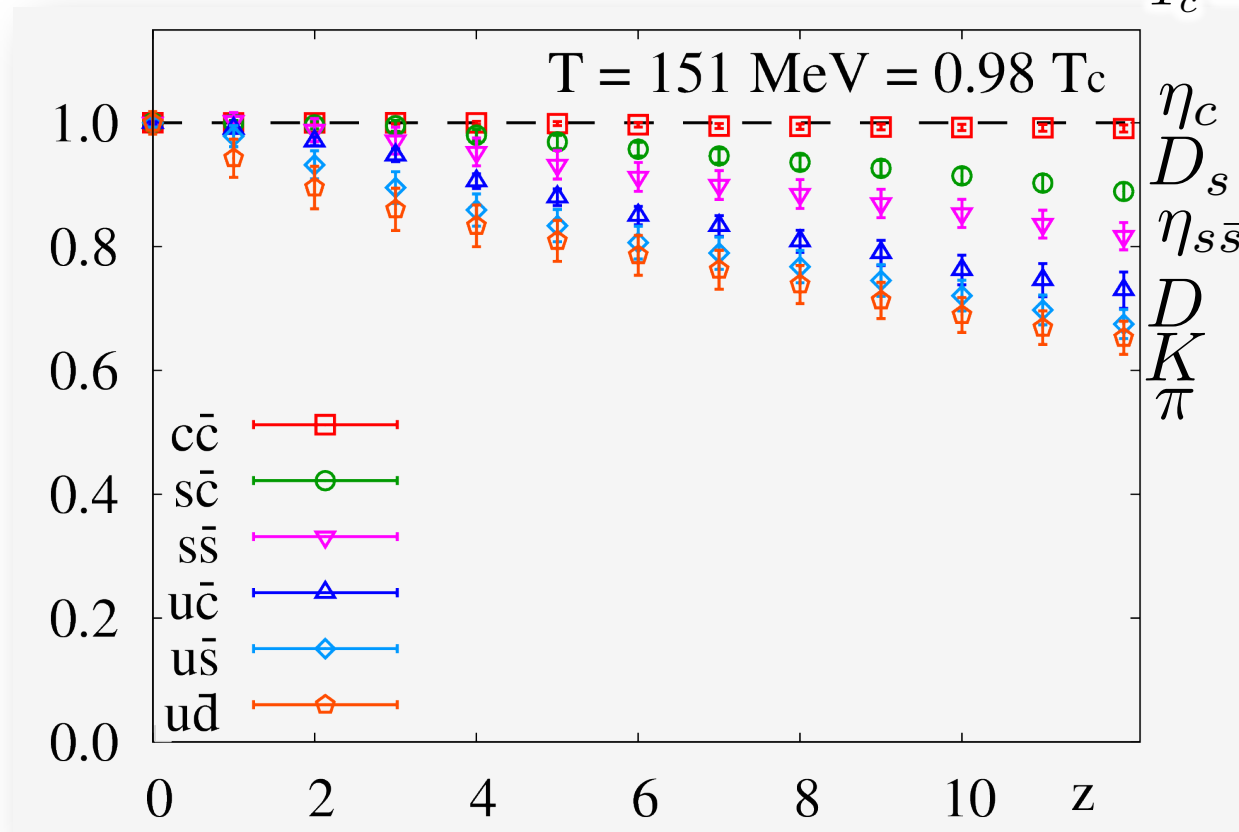
Ratio of spatial correlation functions

Probe of thermal modifications of spectral function

$G^S(z, T)/G^S(z, T = 0) \simeq 1$ the same σ at $T = 0$, or $\neq 1$ modified

$T_c = (154 \pm 9) \text{ MeV}$

Pseudo-scalar
 $J^P = 0^-$



- modification even at $T < T_c$, except for charmonium

- significant flavor dependence at $T > T_c$,

but no change on η_c : modified at $T \gtrsim 1.3 T_c$

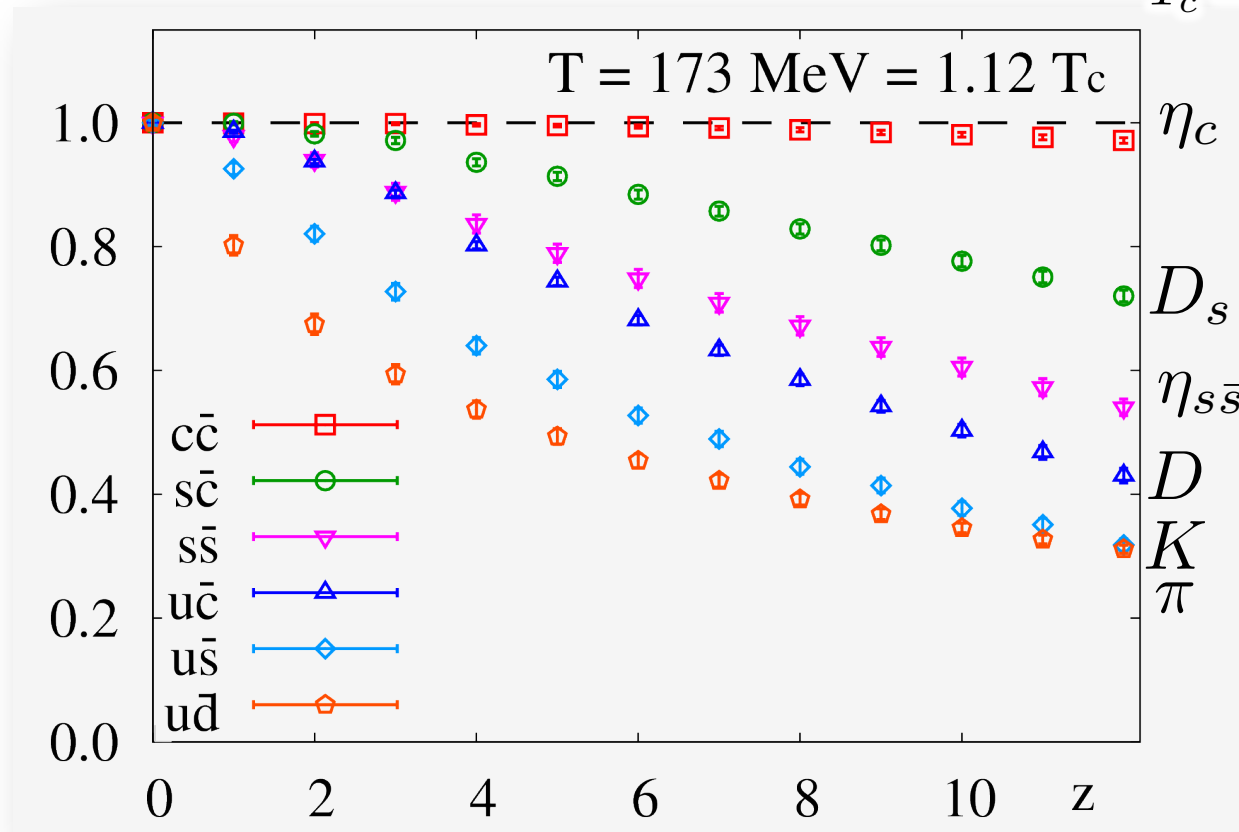
Ratio of spatial correlation functions

Probe of thermal modifications of spectral function

$G^S(z, T)/G^S(z, T=0) \simeq 1$ the same σ at $T=0$, or $\neq 1$ modified

$T_c = (154 \pm 9) \text{ MeV}$

Pseudo-scalar
 $J^P = 0^-$



- modification even at $T < T_c$, except for charmonium
- significant flavor dependence at $T > T_c$

but no change on η_c : modified at $T \gtrsim 1.2\text{--}1.3 T_c$

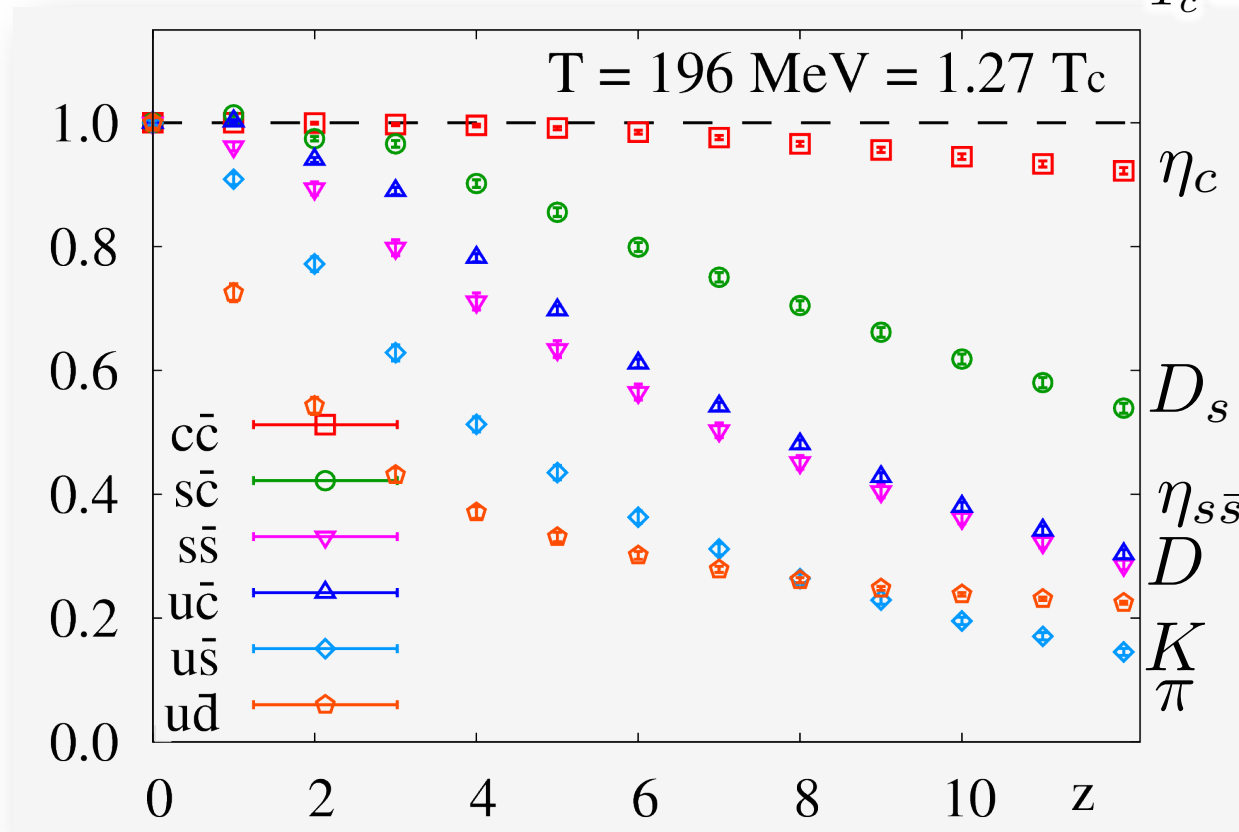
Ratio of spatial correlation functions

Probe of thermal modifications of spectral function

$G^S(z, T)/G^S(z, T=0) \simeq 1$ the same σ at $T=0$, or $\neq 1$ modified

$T_c = (154 \pm 9) \text{ MeV}$

Pseudo-scalar
 $J^P = 0^-$



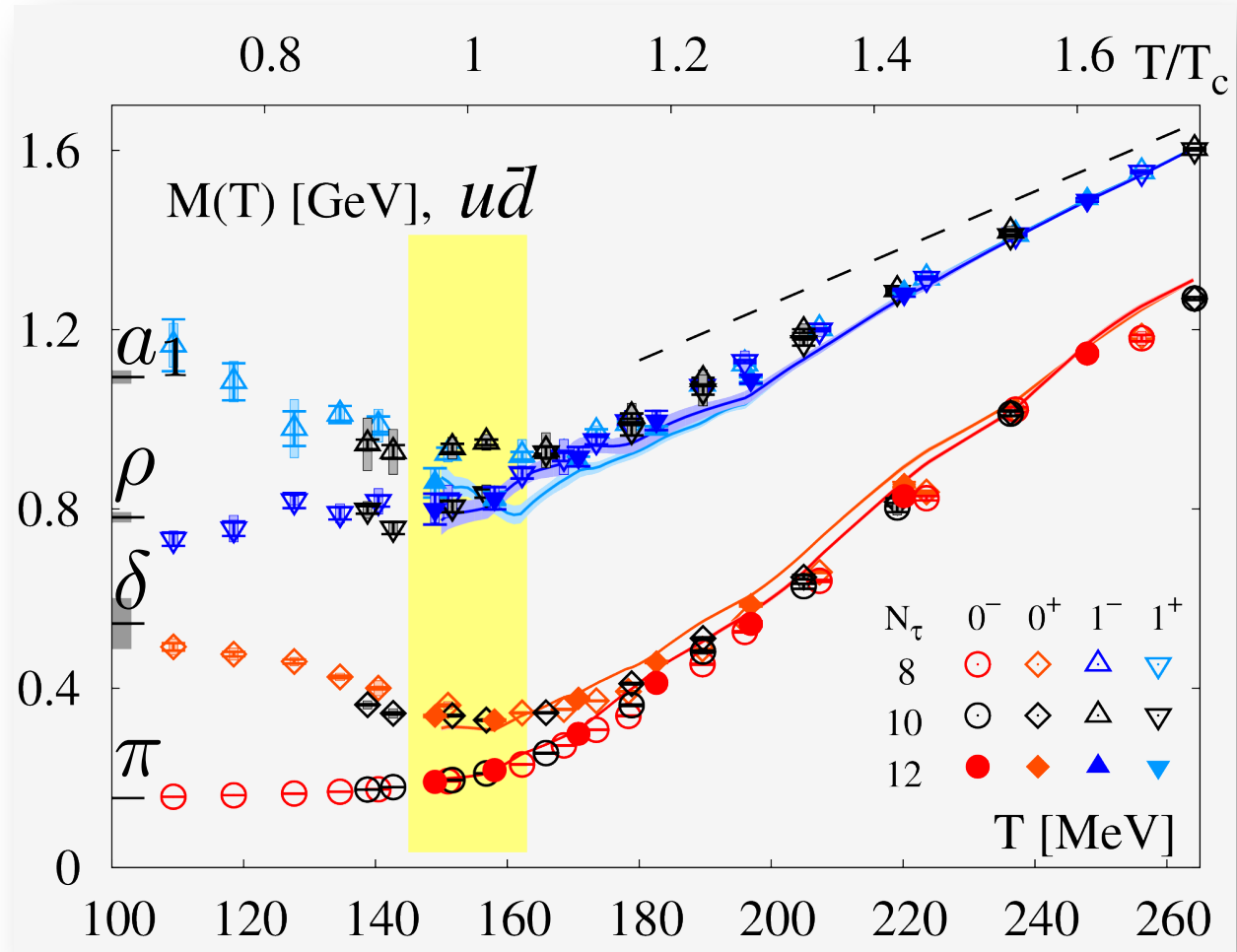
- modification even at $T < T_c$, except for charmonium
- significant flavor dependence at $T > T_c$

but no change on η_c : modified at $T \gtrsim 1.2\text{--}1.3 T_c$

Screening mass in light mesons

$$G^S(z, T)$$

$$\xrightarrow{z \rightarrow \infty} A e^{-M(T)z}$$

 J^P
 1^+
 1^-
 0^+
 0^-
 0^-


mass shift

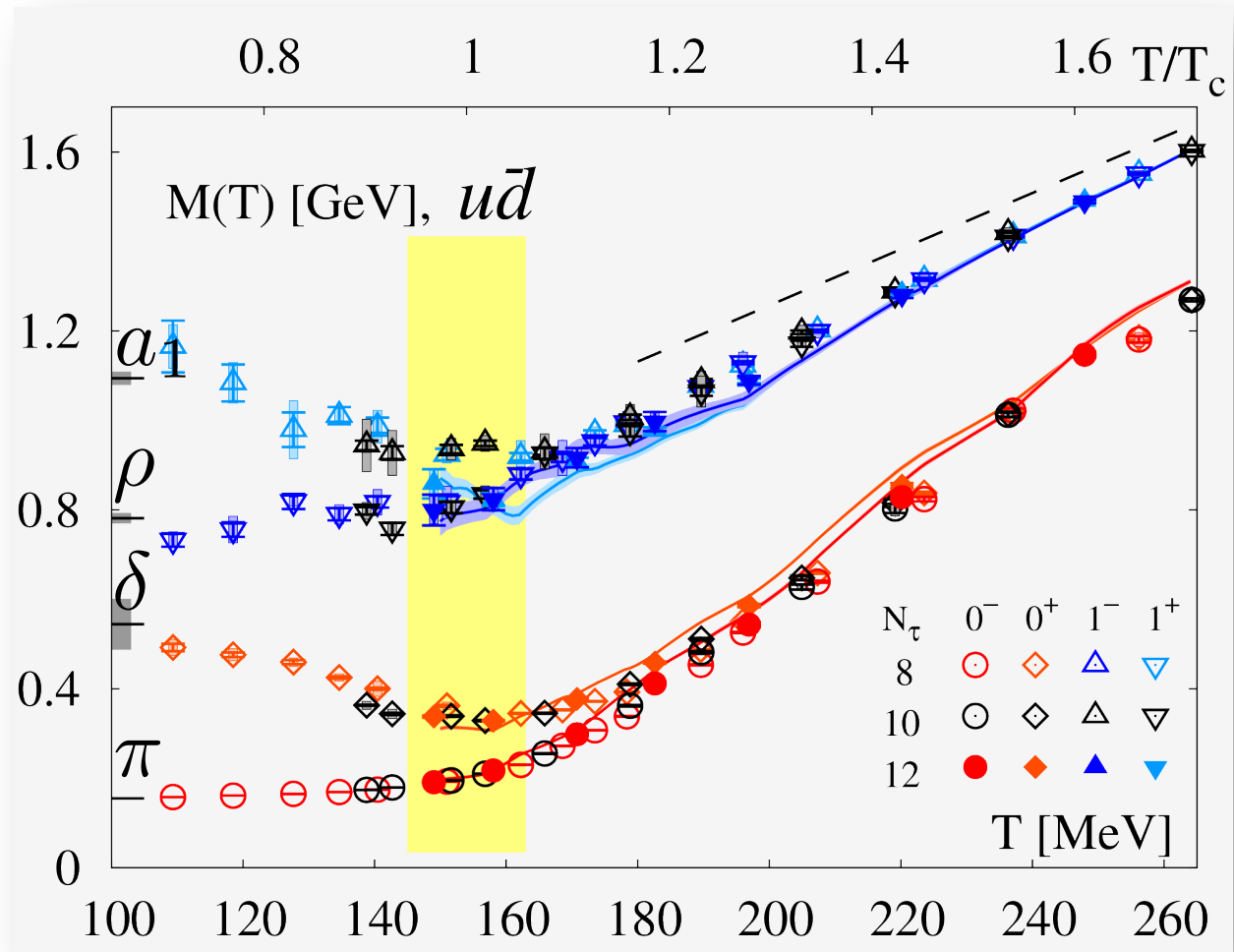
- P^- : not significant at $T < T_c$, monotonically increasing at $T > T_c$
- P^+ : decreasing at $T < T_c$, increasing at $T > T_c$
- Almost linear at $T > 1.2T_c$ ➡ no mesonic bound states

cf.) dashed line: free limit $M \rightarrow 2\sqrt{m_q^2 + (\pi T)^2}$

Screening mass in light mesons

$$G^S(z, T)$$

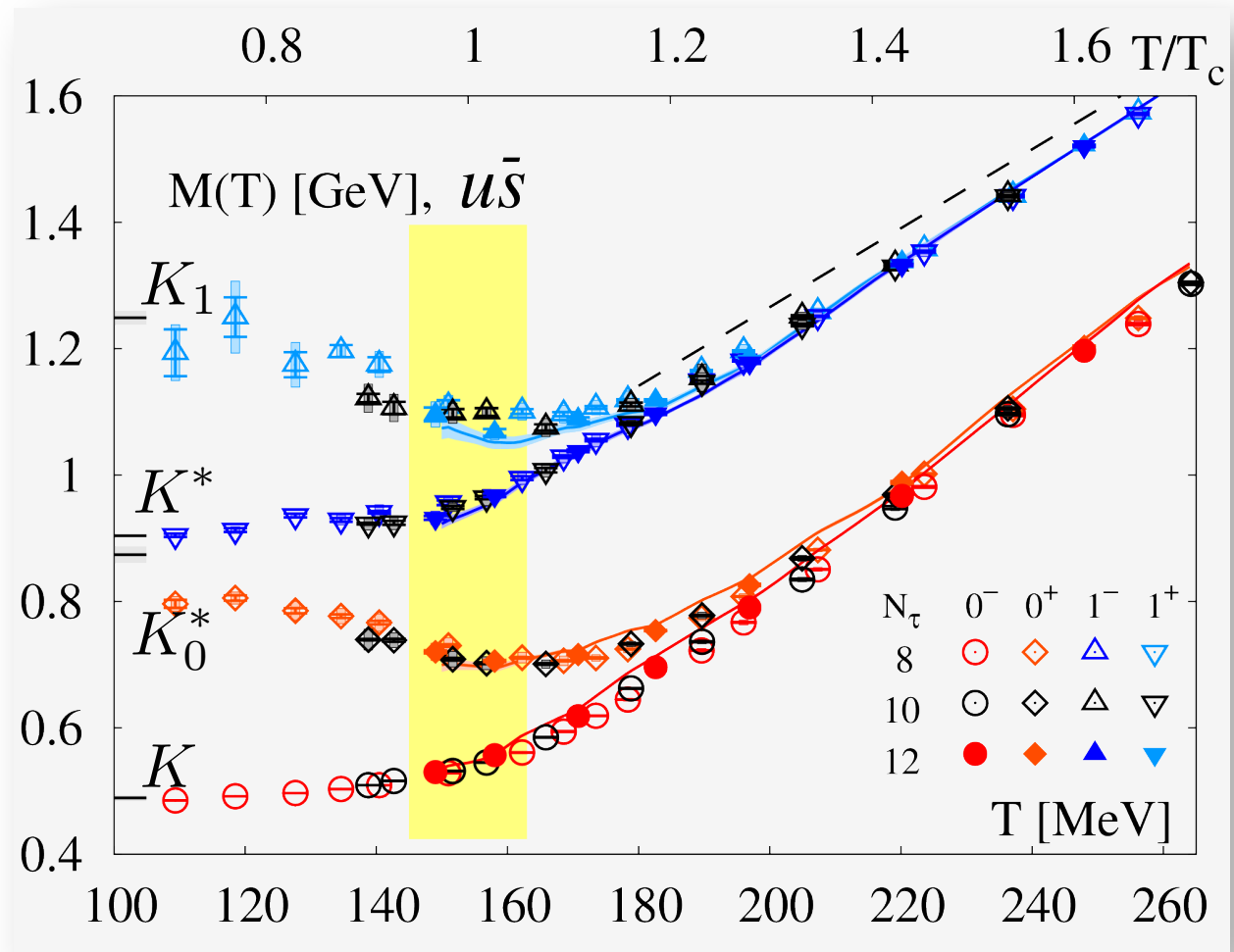
$$\xrightarrow{z \rightarrow \infty} A e^{-M(T)z}$$

 J^P
 1^+
 1^-
 0^+
 0^-


Restoration of broken symmetries

- Vector partner degenerates at $T \sim 1.0T_c$ -- $1.1T_c$ → chiral
- Scalar partner degenerates at $T \sim 1.4T_c$ -- $1.6T_c$ → chiral + $U_A(1)$

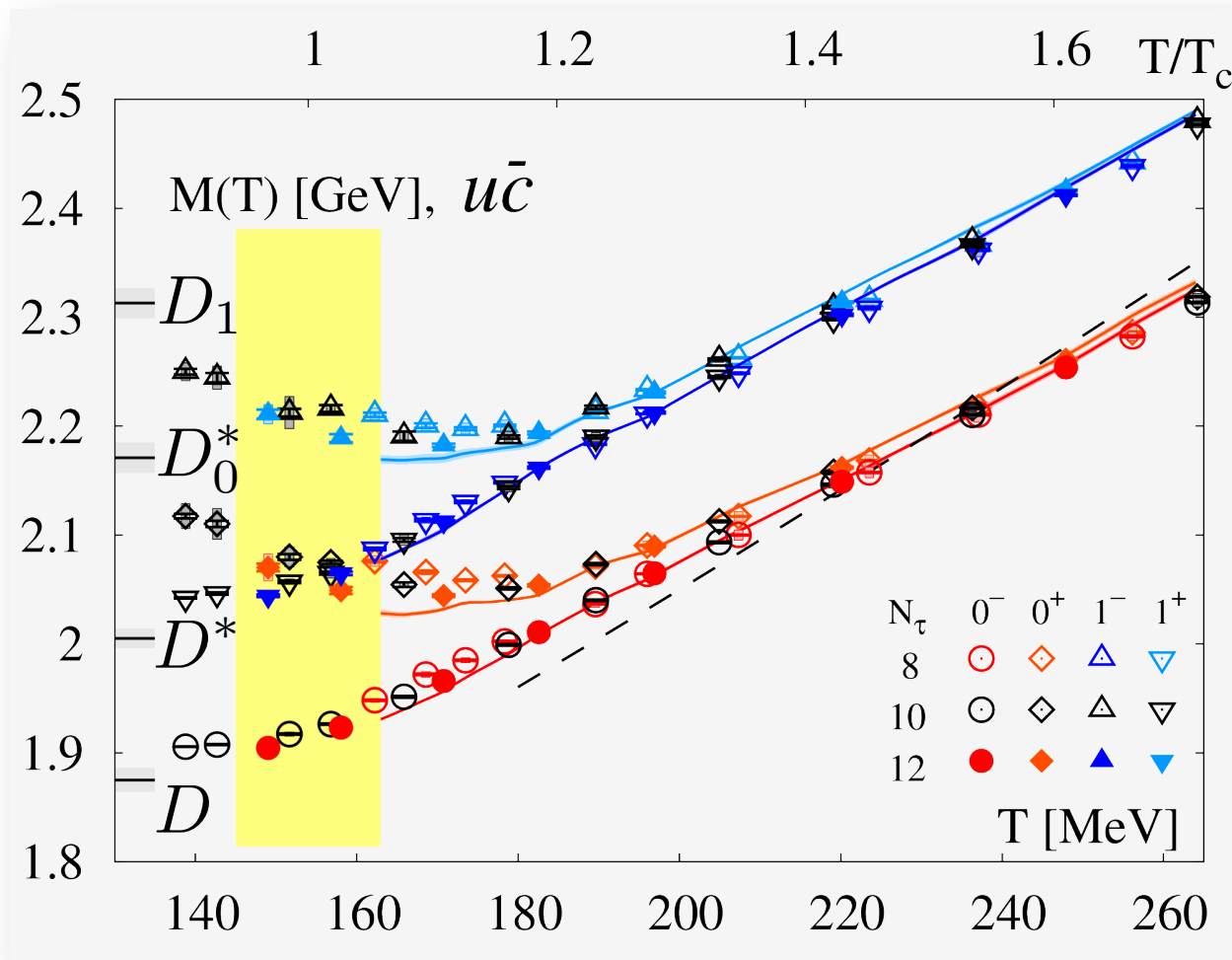
Flavor dependence



Restoration pattern

- Similar to $u\bar{d}$
- Degeneracies appear at $T \sim 1.3T_C$ for vector and $T \sim 1.6T_C$ for scalar

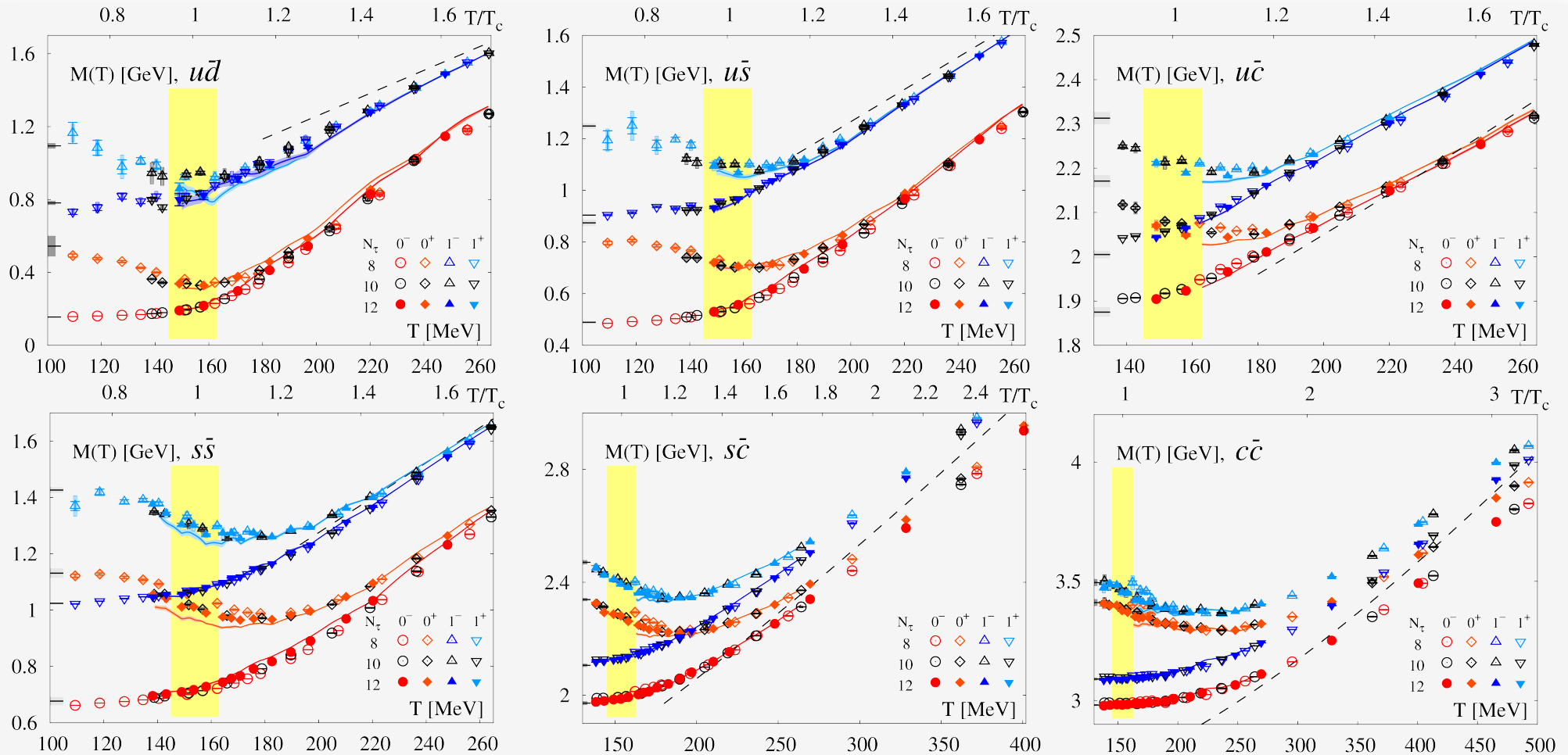
Flavor dependence



Restoration pattern

- Similar to $u\bar{d}$
 - Degeneracies appear at $T \sim 1.6T_C$ for both vector and scalar
- ➔ restoration of chiral: depend on flavors
 $U_A(1)$: independent

Flavor dependence



Universal mass shift: P– increasing monotonically

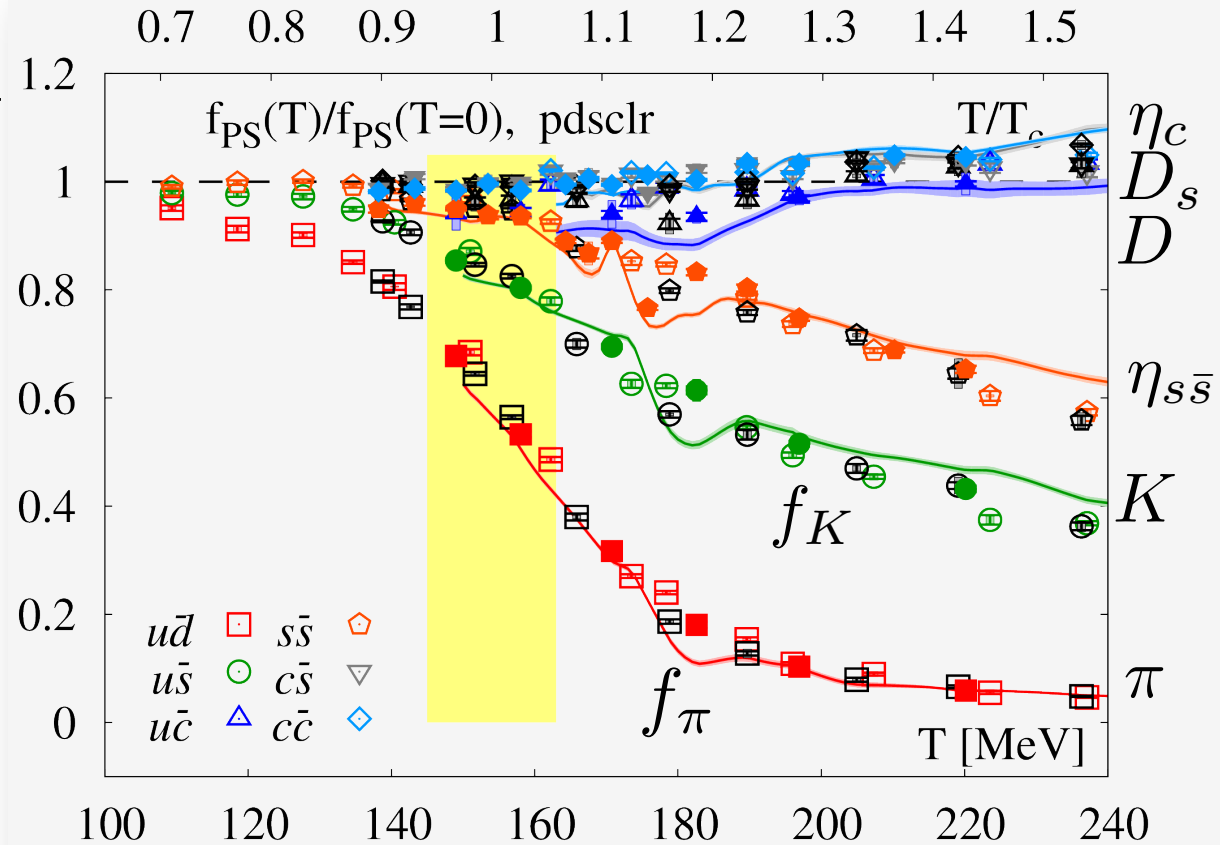
P+ decreasing first and increasing above some T

Scale (chiral restored T): depend on flavors

trivial? or...? effective scale: further different from chiral to heavy quarks
 $m_{ud} \simeq 3\text{--}5$ MeV, $m_s \simeq 95$ MeV, $m_c \simeq 1.2$ GeV

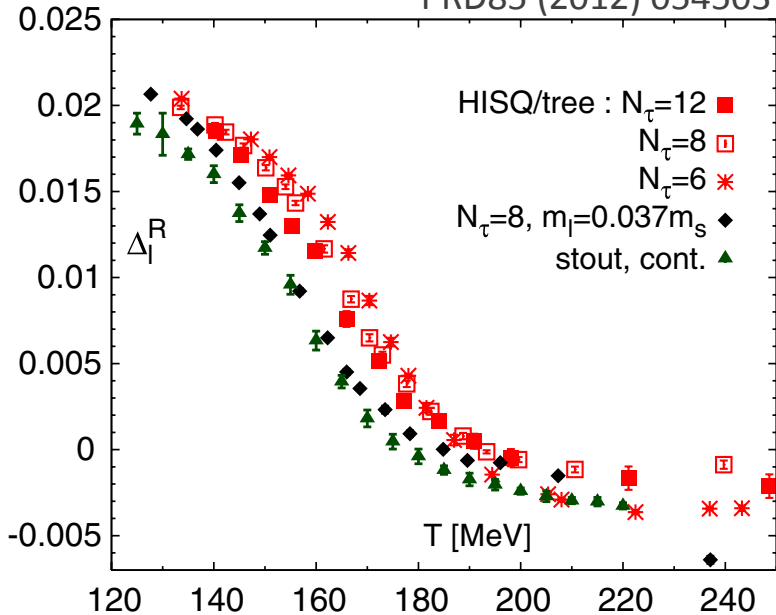
Leptonic decay constant

$$\frac{f_{PS}(T)}{f_{PS}(0)}$$



Renormalized chiral condensate

PRD85 (2012) 054503



decreasing with T increasing for $u\bar{d}$, $u\bar{s}$ and $s\bar{s}$
 no significant T dependence for $u\bar{c}$, $s\bar{c}$ and $c\bar{c}$

Lattice indicates: $\sqrt[3]{\frac{\langle \bar{q}q \rangle^*}{\langle \bar{q}q \rangle}} \approx \frac{f_\pi^*}{f_\pi} \neq \frac{m_\rho^*}{m_\rho}$

Summary

Full-QCD lattice simulations on physical point

In-medium mesons from spatial correlation functions:

- sensitive to thermal modifications
- probe of modification of spectral function $G^S(z, T)/G^S(z, T = 0)$

All meson modified even below T_c except for charmonium

In heavy-ion collision,

- Signal of creating quark-gluon plasma
 ➔ modification of charmonium (η_c and J/ψ)
- Thermal effect: appears on other meson states
- Restorations of broken symmetries: parity partners

Universal mass shift depending on parity channels

T dependence of screening mass: $G^S(z, T) \xrightarrow{z \rightarrow \infty} A e^{-M(T)z}$

- Leading response of mass shift
- P- increasing monotonically
- P+ decreasing first and then increasing
- Different from chiral effective approach

$$\sqrt[3]{\frac{\langle \bar{q}q \rangle^*}{\langle \bar{q}q \rangle}} \approx \frac{f_\pi^*}{f_\pi} \times \frac{m_\rho^*}{m_\rho}$$