

*ExHIC in YITP, 2016, Mar.*

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# $\Xi$ resonances in the weak decay of $\Xi_c$

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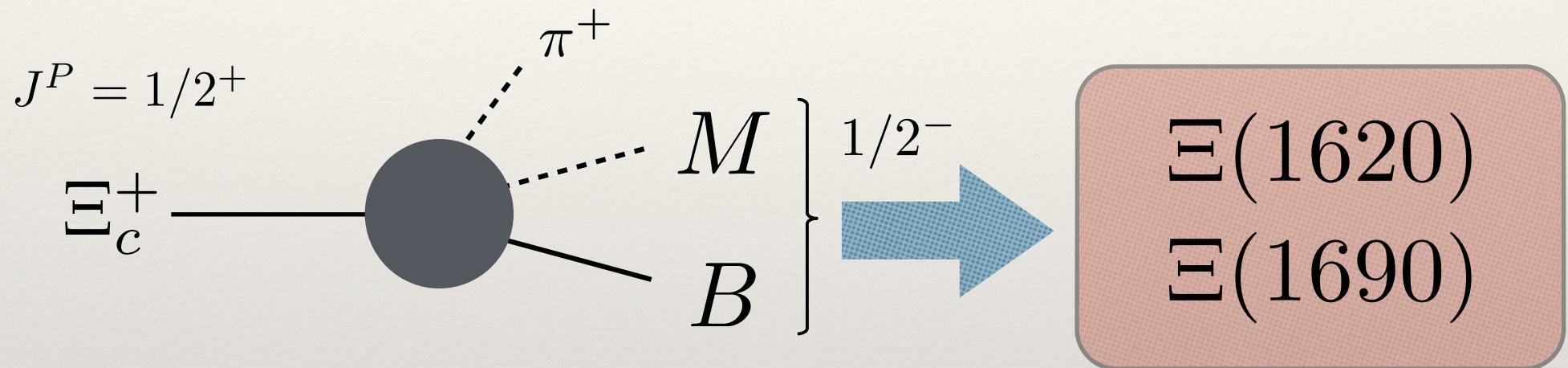
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# Introduction

## $\Xi_c$ -decay



- Weak decay
- $\bar{q}q$  creation
- Final State Interaction

exp.) Belle, BESIII, ...

- existence...?
- $J^P$ ...?
- theoretically controversial

## ❖ $\Xi$ resonances

- a small number of measured  $\Xi^*$
- poor information about  $J^P$

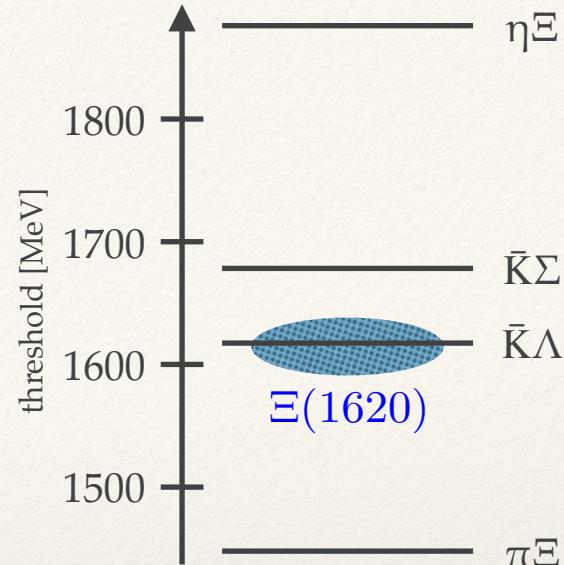
### ❖ $\Xi(1620)$

- one-star in PDG
- $J^P = ??$

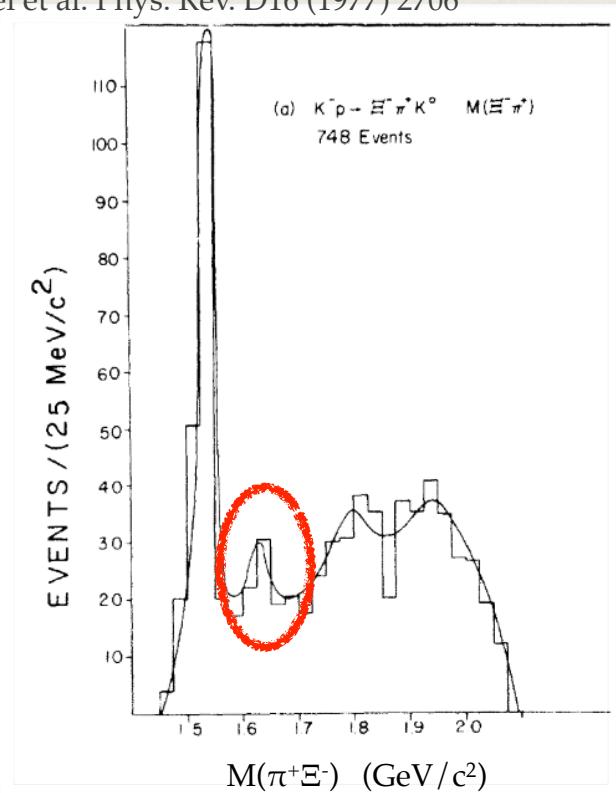
exp.)  $K^- p \rightarrow K^0 (\pi^+ \Xi^-)$

theory) mainly coupled to  
 $\pi\Xi$  and  $\bar{K}\Lambda$  channels

Ramos, Oset, Benhold, Phys. Rev. Lett. 89 (2002) 252001



Briefel et al. Phys. Rev. D16 (1977) 2706



## ❖ $\Xi(1690)$ resonance

- three-star in PDG
- $(M, \Gamma) = (1690 \pm 10, < 30) \text{ MeV}$
- $J^P = ??$

theory)

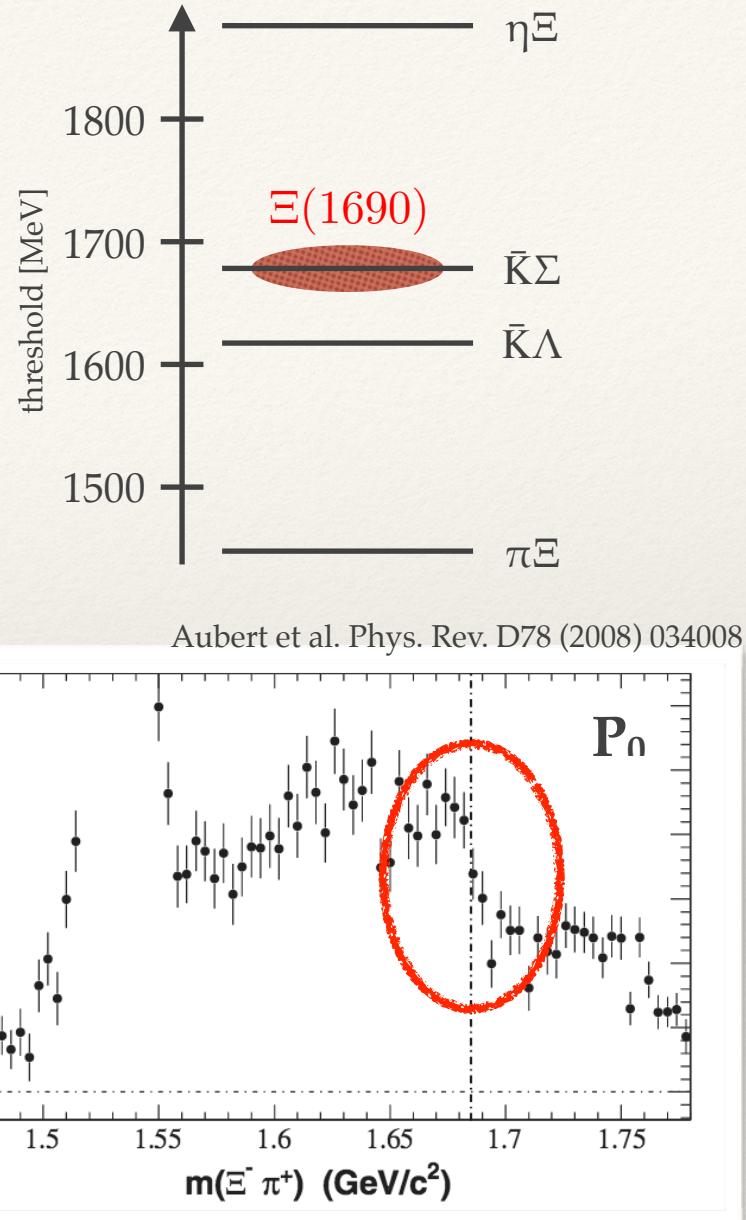
- $J^P$  assignment is controversial
- mainly coupled to  
 $\bar{K}\Sigma$  and  $\eta\Xi$  channels

Garcia-Recio, Lutz, Nieves,  
Phys. Lett. B 582 (2004) 49

exp.)

- $K^-$ , hyperon + nucleon  
 $\rightarrow (\bar{K}\Sigma), (\bar{K}\Lambda), (\pi\Xi)$  distribution
- $\Lambda_c \rightarrow K^+ (\bar{K}\Lambda), (\bar{K}\Sigma), \underline{(\pi\Xi)}$

some evidence  
of  $J^P=1/2^-$

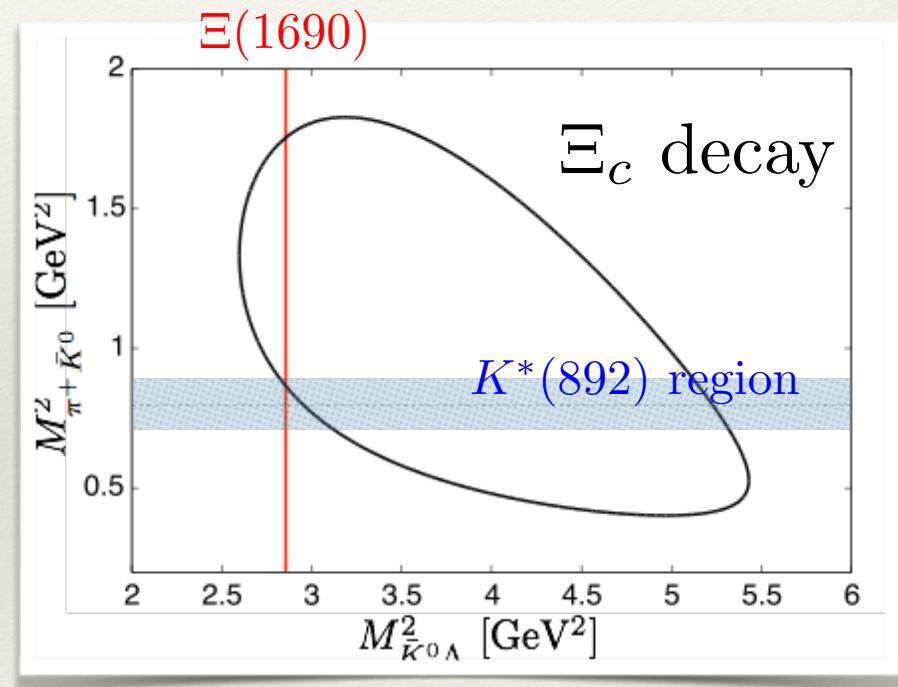
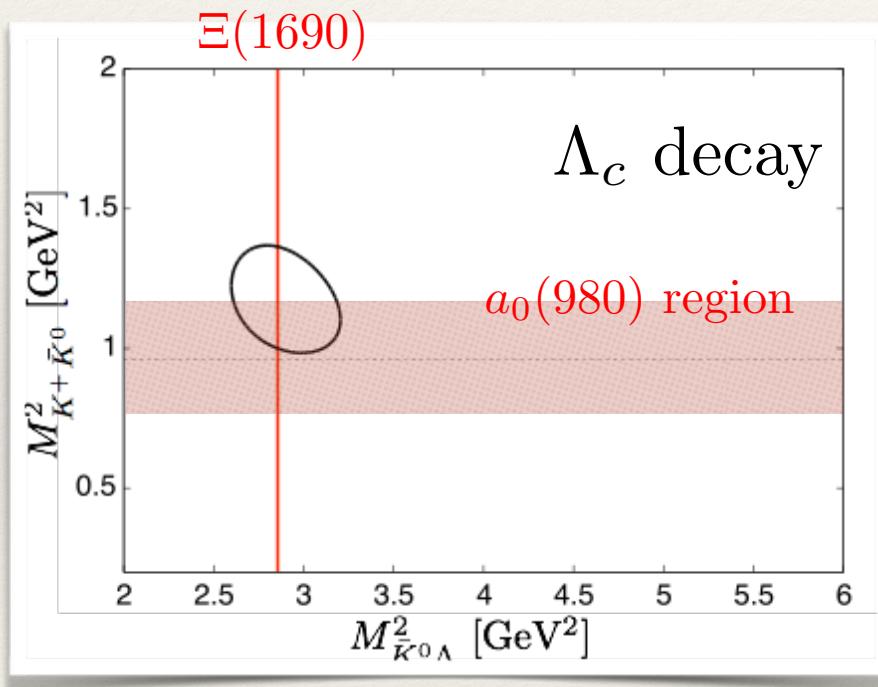


Legendre polynomial moment :

$$\begin{aligned}
P_0 &= \frac{1}{N} \int_{-1}^1 \frac{dN}{d \cos \theta_{\Xi^-}} P_0(\cos \theta_{\Xi^-}) d \cos \theta_{\Xi^-} \\
&= \frac{1}{\sqrt{2}} \left[ |S^{1/2}|^2 + |P^{1/2}|^2 + |P^{3/2}|^2 + |D^{3/2}|^2 + |D^{5/2}|^2 \right]
\end{aligned}$$

## ❖ $\Xi(1690)$ exp.

- $\Xi(1690)$  coupling to  $\pi\Xi$  channel is too weak.  
 $\rightarrow \bar{K}\Lambda, \bar{K}\Sigma$  are the ideal channels
- In  $\Lambda_c \rightarrow \underline{K^+} (\bar{K}\Lambda)$  reaction,  $a_0(980)$  contribution is obstructive.



In  $\Xi_c \rightarrow \pi^+ (\bar{K}\Lambda)$  process,  
other interaction effect is relatively small.

❖  $\Xi(1690)$  exp.

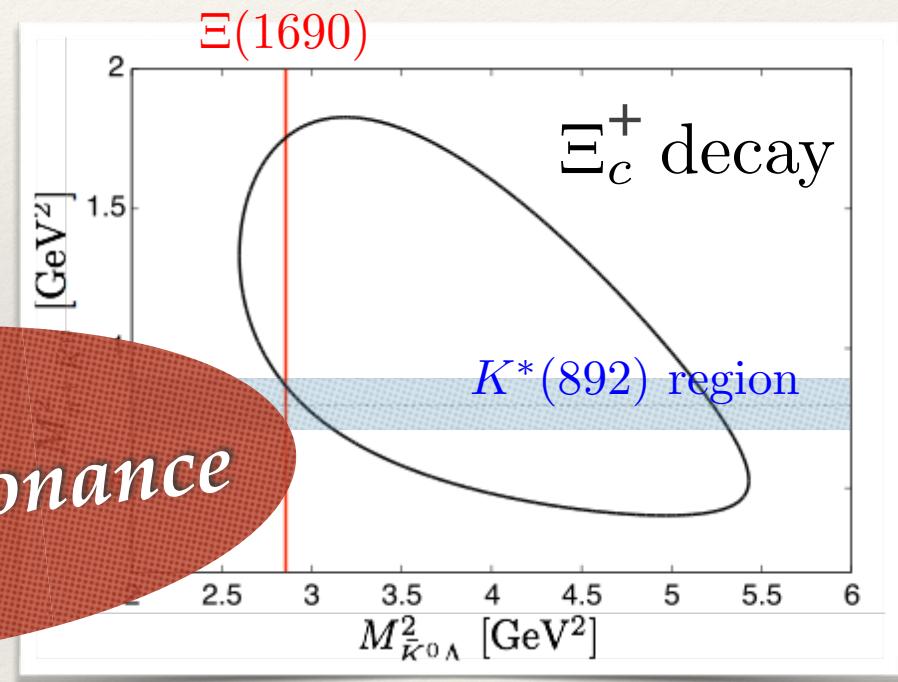
- $\Xi(1690)$  coupling to  $\pi\Xi$  channel is too weak.  
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$$\begin{aligned} \Xi_c^+ &\rightarrow \underline{\pi^+} (\bar{K}^0 \Lambda) \\ I_3 : +1 &+1/2 \\ &\rightarrow I = 3/2 \text{ only} \end{aligned}$$

cf)

$$\begin{aligned} \Xi_c^0 &\rightarrow \underline{\pi^+} (K^-\Lambda) \\ I = 1/2, 3/2 & \end{aligned}$$

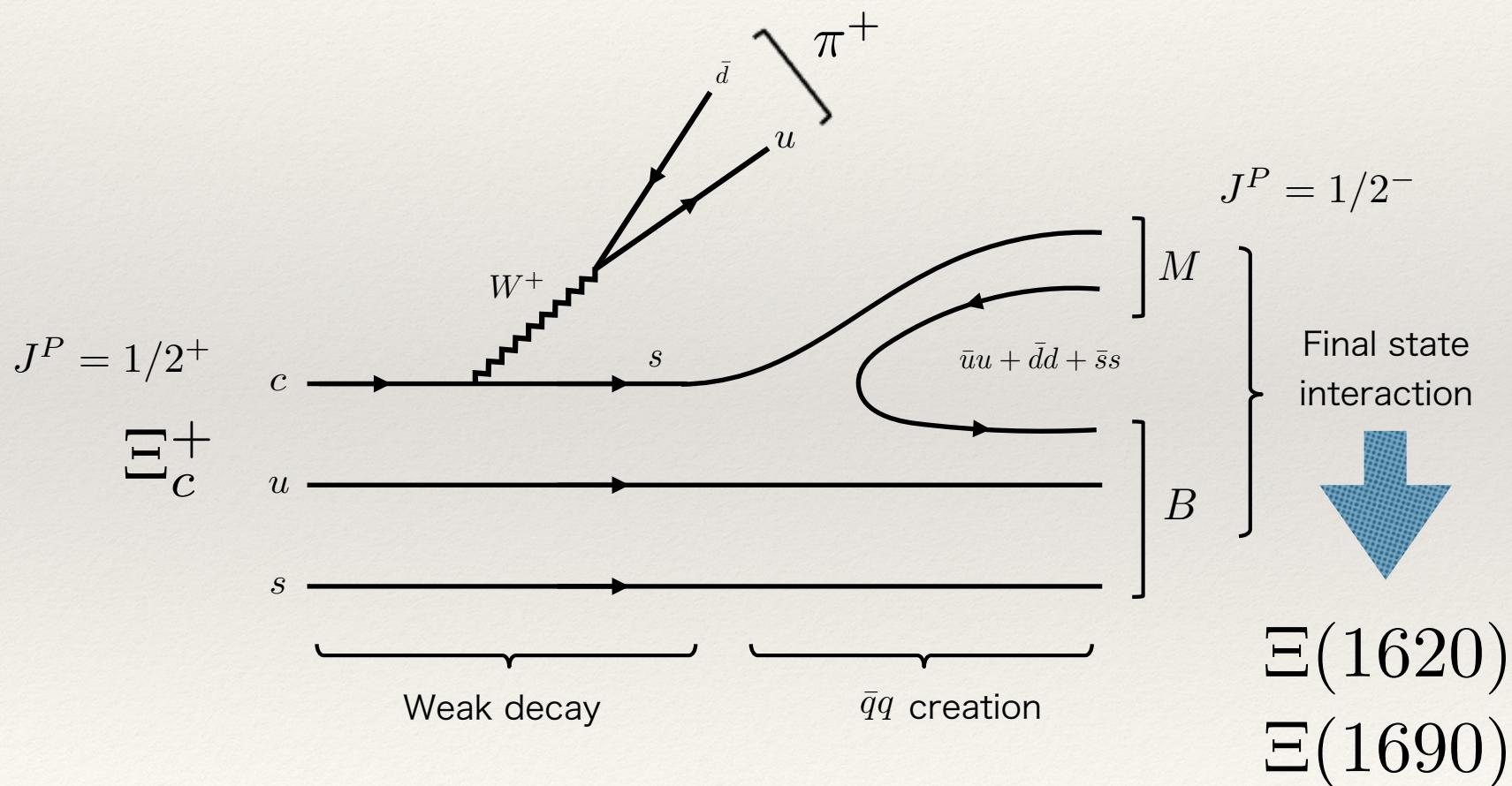
*no meson resonance*



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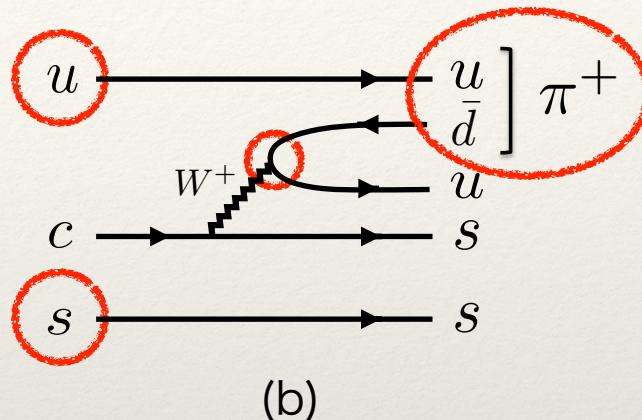
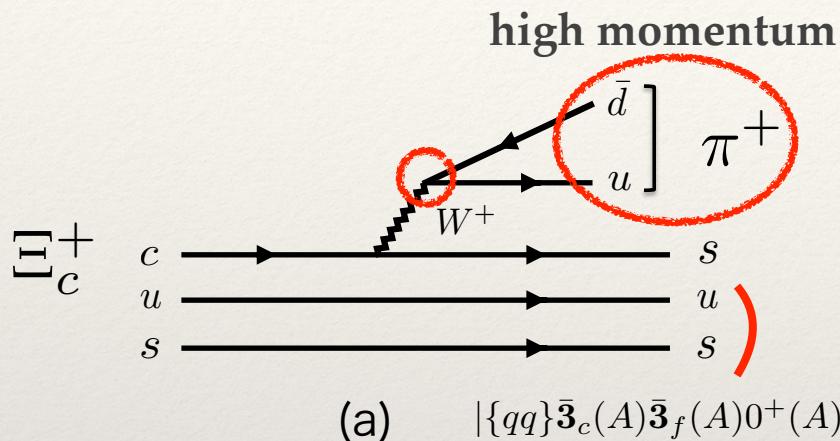
# Formalism

Considering Cabibbo-Kobayashi-Maskawa matrix and diquark correlation, the following diagram is favored.



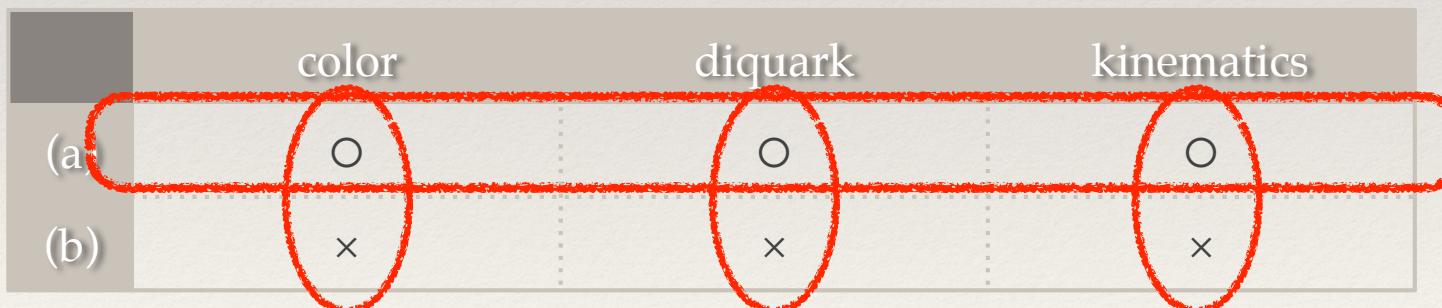
## ❖ Weak decay

### Cabibbo favored diagrams



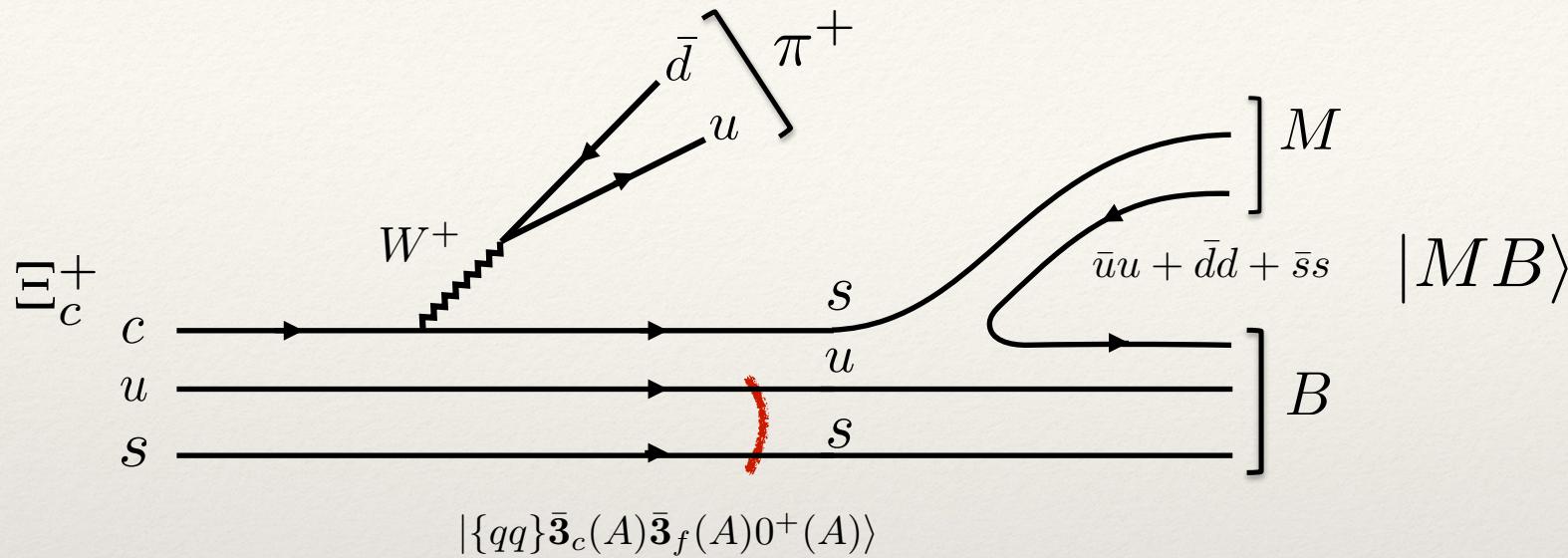
“ good diquark ”

Jaffe, Phys. Rept. 409, 1 (2005)



Diagram(a) is the most favored

## ❖ $\bar{q}q$ creation

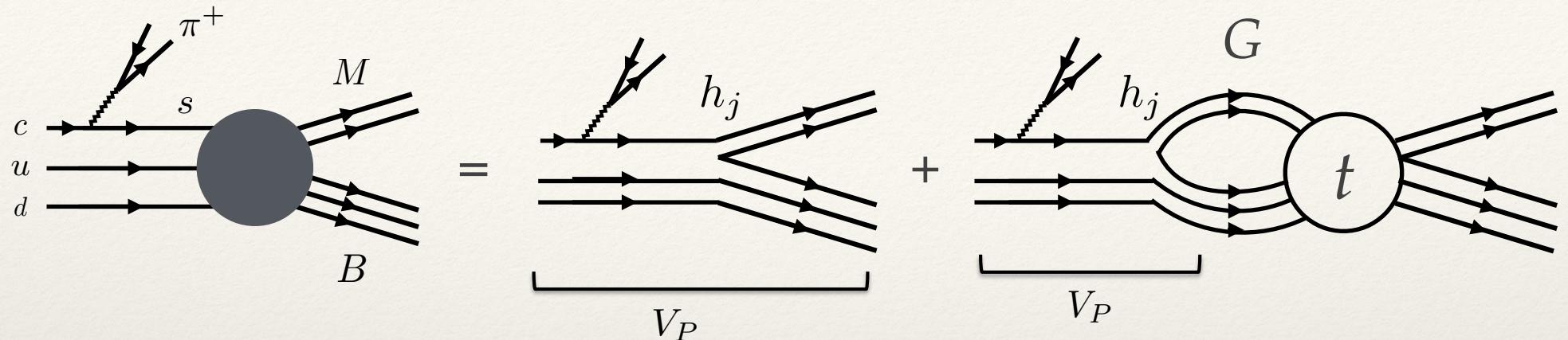


Jaffe, Phys. Rept. 409, 1 (2005)

With the hadron degrees of freedom,

$$|MB\rangle = -\frac{1}{\sqrt{6}}|\bar{K}\Lambda\rangle - \sqrt{\frac{3}{2}}|\bar{K}\Sigma\rangle + \frac{1}{\sqrt{3}}|\eta\Lambda\rangle$$

## ❖ Final State Interaction



$$\mathcal{M}_j = V_P \left( h_j + \sum_i h_i G_i(M_{\text{inv}}) t_{ij}(M_{\text{inv}}) \right)$$

$$\frac{d\Gamma_j}{dM_{\text{inv}}} = \frac{1}{(2\pi)^3} \frac{p_{\pi^+} p_j M_{\Lambda_c^+} M_j}{M_{\Lambda_c^+}^2} |\mathcal{M}_j|^2$$

coefficients can be  
determined from  $|MB\rangle$

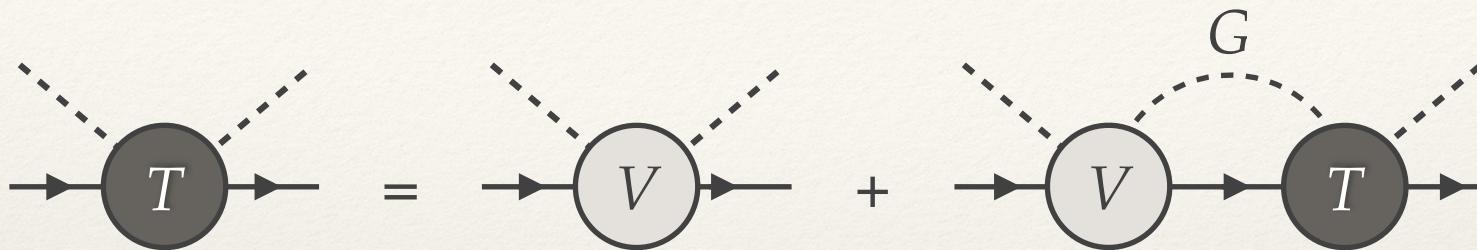
$$\begin{cases} h_{\pi\Xi} = 0, & h_{\bar{K}\Lambda} = -\frac{1}{\sqrt{6}}, \\ h_{\bar{K}\Sigma} = -\sqrt{\frac{3}{2}}, & h_{\eta\Xi} = \frac{1}{\sqrt{3}}. \end{cases}$$

$G_i$  : meson-baryon loop function

$t_{ij}$  : meson-baryon scattering matrix

chiral unitary  
approach

- chiral unitary approach
  - non-perturbative treatment  
(bound state, resonance state)



$$\begin{aligned}
 T &= V + VGT = V + VGV + VGVGV + \dots \\
 &= (V^{-1} - G)^{-1} : \text{pole} \quad \longleftrightarrow \quad \text{resonance state}
 \end{aligned}$$

$$G(W) = i \int \frac{d^4 q}{(2\pi)^4} \frac{2M}{(P-q)^2 - M^2 + i\epsilon} \frac{1}{q^2 - m^2 + i\epsilon}$$

dimensional regularization



subtraction constant  
**free parameter**

fit scattering data → well describe

resonance state

# Results

**ROB**

$\Xi(1620) : (M, \Gamma) = (1606, 132) \text{ MeV}$

$\Xi(1690) :$  no pole

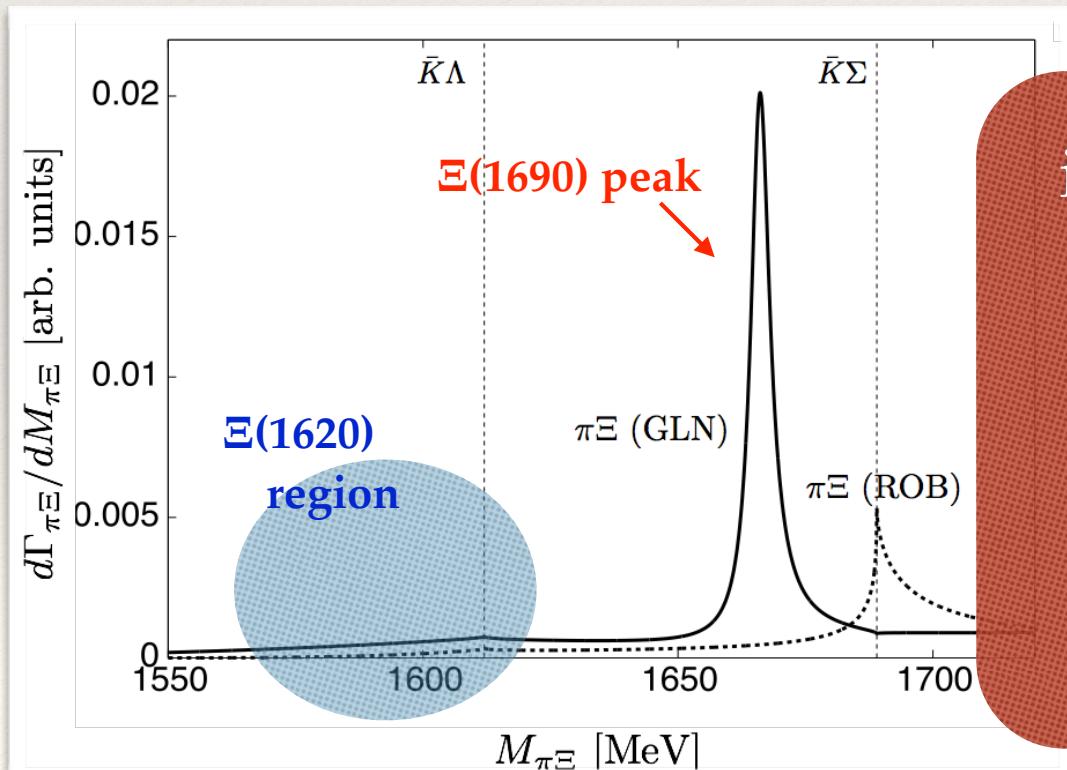
Ramos, Oset, Benhold, Phys. Rev. Lett. 89 (2002) 252001

**GLN**

$\Xi(1620) : (M, \Gamma) = (1568, 252) \text{ MeV}$

$\Xi(1690) : (M, \Gamma) = (1667, 4) \text{ MeV}$

Garcia-Recio, Lutz, Nieves, Phys. Lett. B 582 (2004) 49



in  $\pi\Xi$  channel

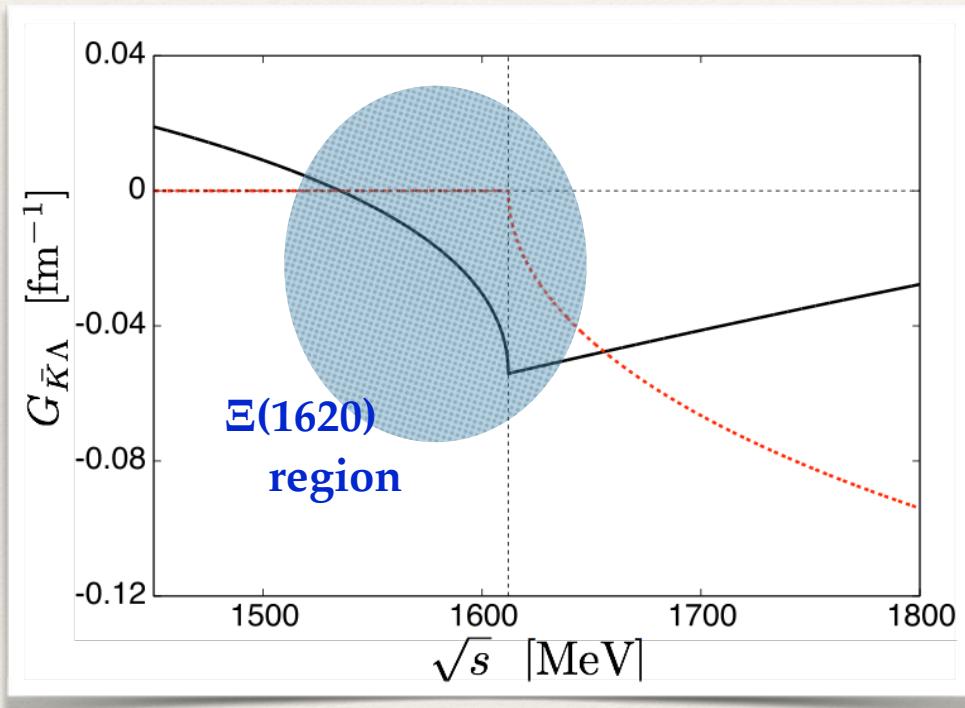
- $\Xi(1620)$  peak cannot be seen.
- $\Xi(1690)$  peak can be seen clearly.
- $\bar{K}\Sigma$  threshold also gives the peak-like structure

## ❖ Discussion

$\Xi(1620)$  mainly couples to  $\pi\Xi$  and  $\bar{K}\Lambda$  channel



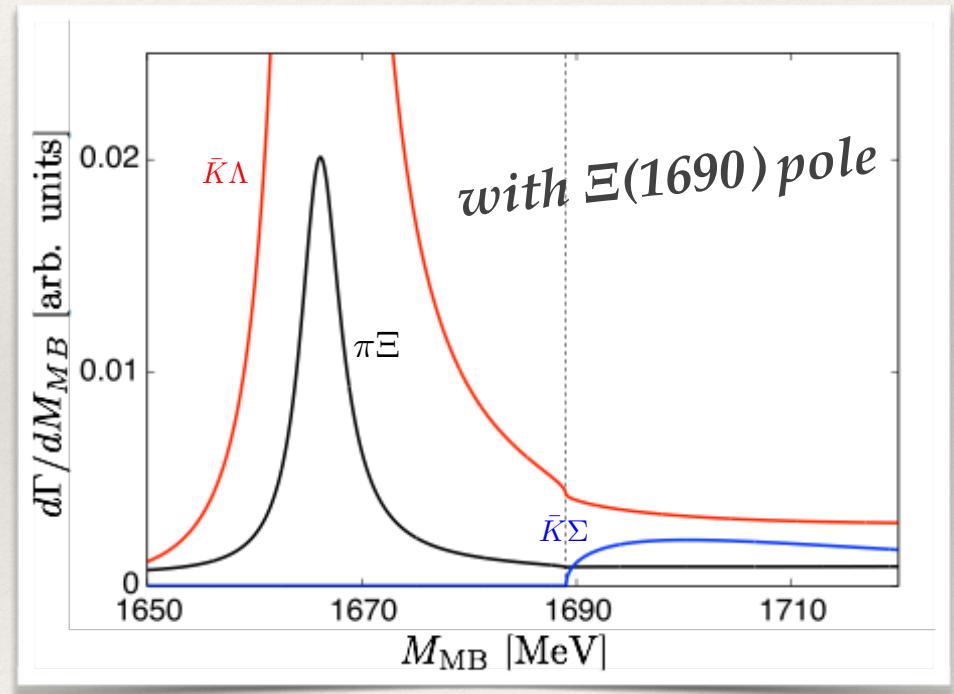
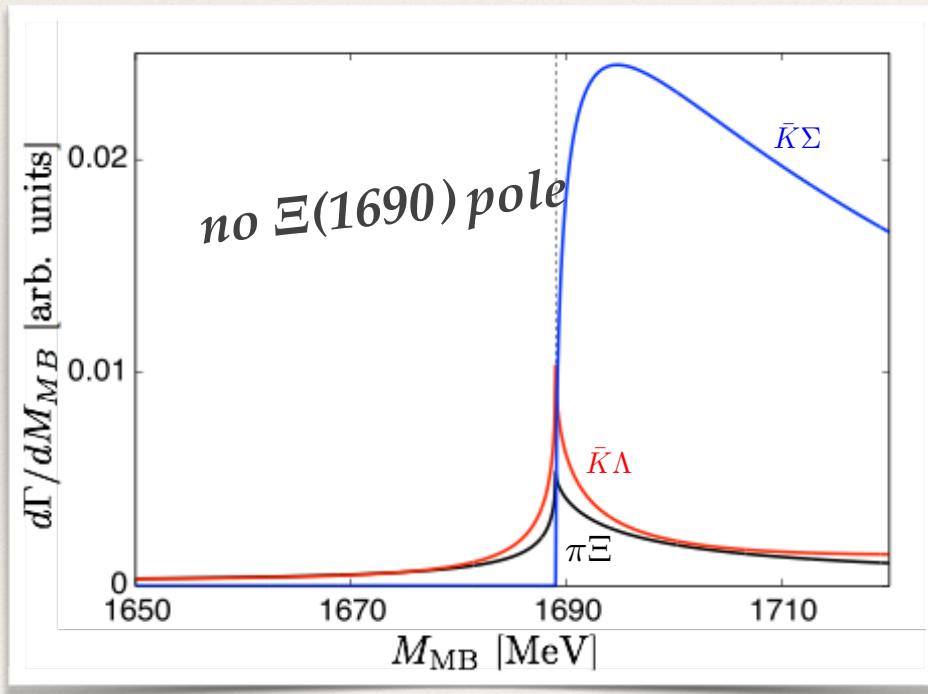
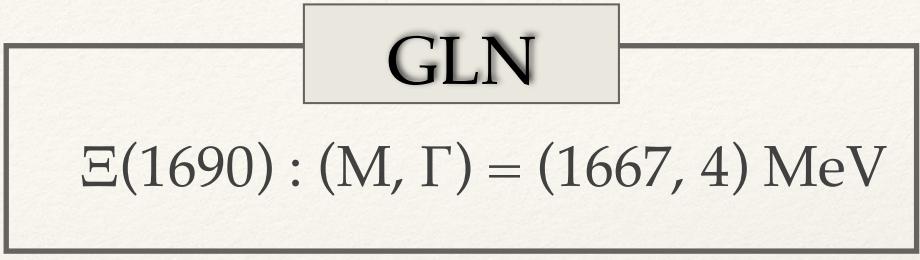
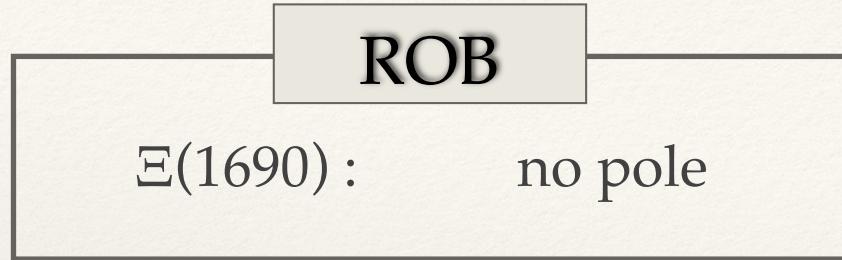
$$\mathcal{M}_{\pi\Xi} \sim -V_P \frac{1}{\sqrt{6}} G_{\bar{K}\Lambda}(M_{\text{inv}}) t_{\bar{K}\Lambda, \pi\Xi}(\text{inv})$$



- | MB> does not include the  $\pi\Xi$  channel.
- $\bar{K}\Lambda$  loop function is small around the  $\Xi(1620)$  region below the  $\bar{K}\Lambda$  threshold.

In  $\Xi_c^+ \rightarrow \pi^+$  (MB) reaction,  $\Xi(1620)$  is difficult to see.

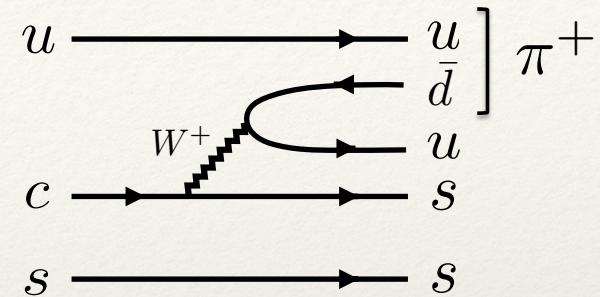
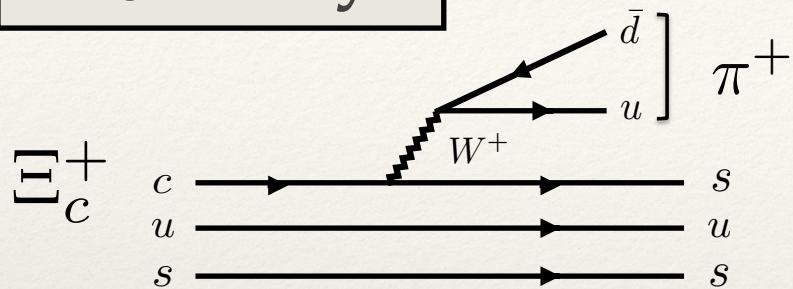
## ❖ Discussion



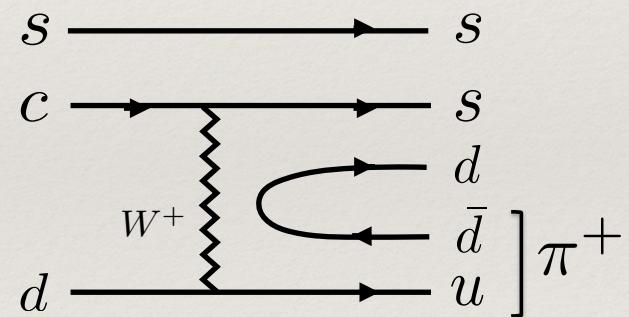
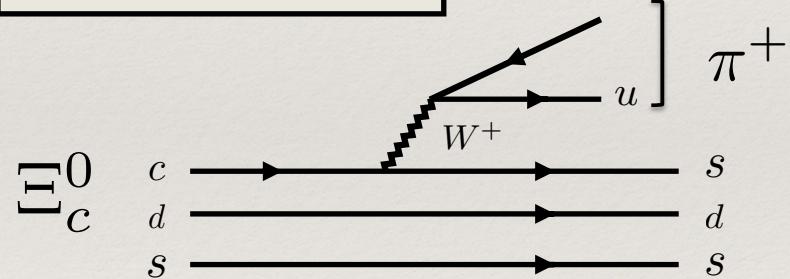
The ratios of the decay fractions may be useful.

## ❖ Discussion

### $\Xi_c^+$ decay



### $\Xi_c^0$ decay



Comparison between  $\Xi_c^+$  and  $\Xi_c^0$  decays  
may clarify the effect of other diagrams.

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# Summary

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- ❖ We have studied  $\Xi(1620)$  and  $\Xi(1690)$  resonances from  $\Xi_c$ -decay.
- ❖ Considering CKM matrix, color factor, diquark correlation, and kinematics, we have chosen the most favored diagram.
- ❖ It has been found that the  $\Xi(1620)$  peak is difficult to see in  $\Xi_c$  decay.
- ❖  $\Xi(1690)$  peak has been seen clearly. The decay fraction may be useful to distinguish the resonance peak from the threshold effect.