

# $\Theta^+$ production and two-meson coupling of antidecuplet



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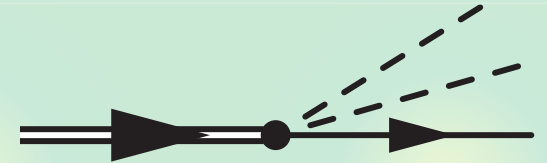
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★ Introduction and motivations

★ Effective Lagrangian



★ Self-energy of antidecuplet

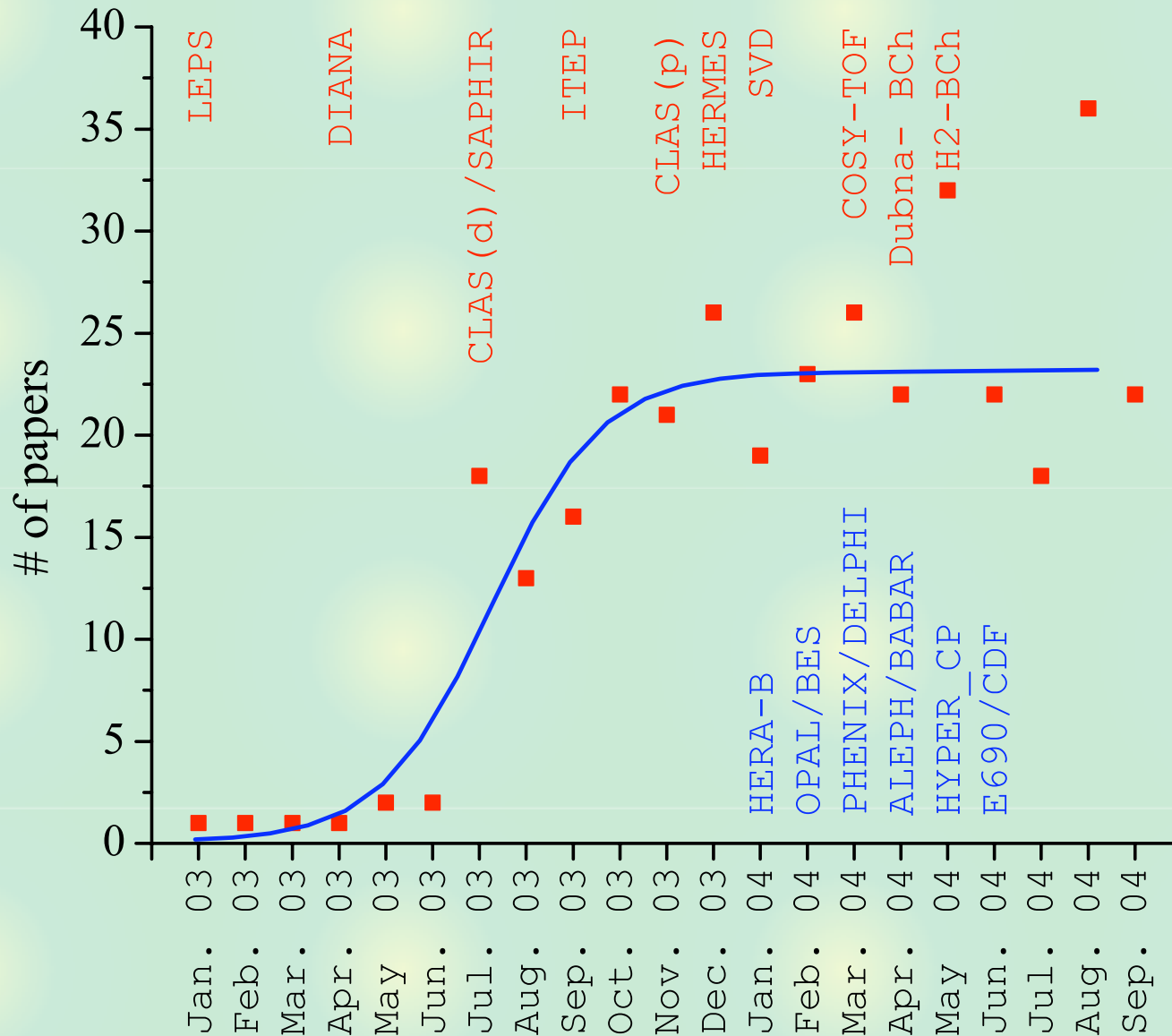
★ Mass shifts

★ Decay widths

★ Reaction cross section

★ Summary and conclusions

# Introduction : Exotic activities



## Introduction : Flavor SU(3) symmetry

Flavor SU(3) symmetry and its breaking by the strange quark mass

-> Phenomenologically well realized

Gell-Man – Okubo mass formulae ~ 3%

N(938),  $\Lambda(1116)$ ,  $\Sigma(1192)$ ,  $\Xi(1320)$ ,  
 $\Delta(1232)$ ,  $\Sigma(1385)$ ,  $\Xi(1530)$ ,  $\Omega(1670)$

Coleman-Glashow relation ~ 20%

Magnetic moments of baryon octet

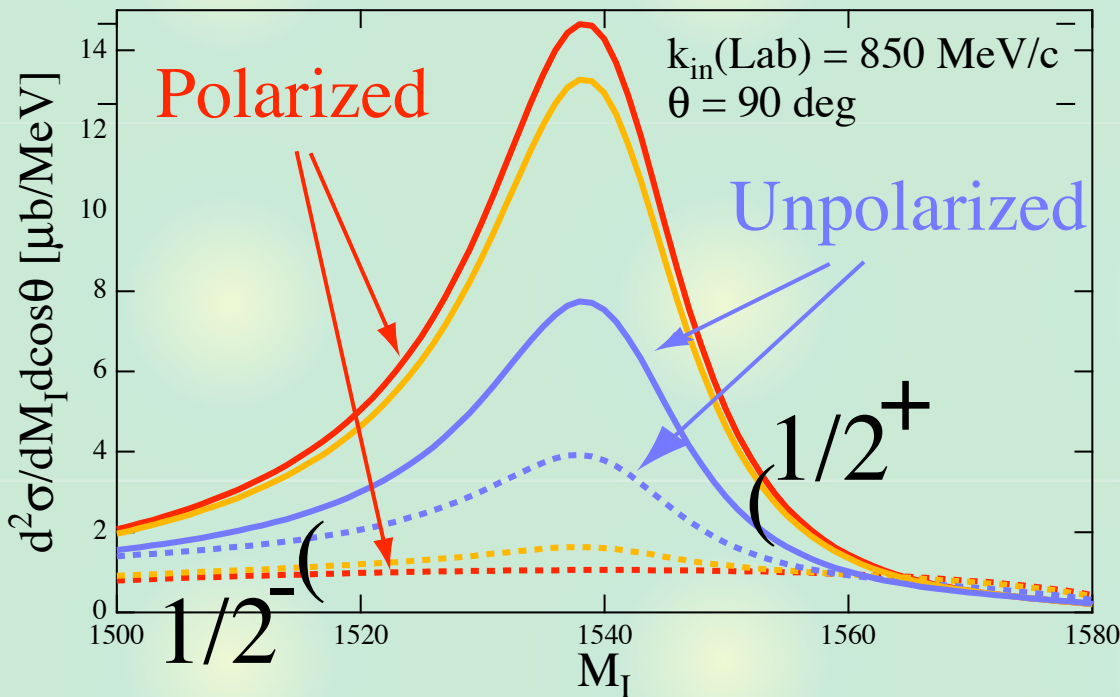
Existence of  $\Theta^+$  + Flavor SU(3) symmetry

➔ Existence of **flavor partners** of  $\Theta^+$

# Introduction : determining the quantum numbers

We have proposed  $K^+ p \rightarrow \pi^+ \Theta^+ \rightarrow \pi^+ K^+ n (K^0 p)$

Polarization observable  
can be used to determine  
the quantum numbers



T. H., A. Hosaka, E. Oset,  
Phys. Lett. B579, 290 (2004).

➔ Understanding of reaction mechanism

# Motivations

Results of  $\pi^- p \rightarrow K^- \Theta^+$  reaction at KEK

Total cross section  $\sim 2 \mu\text{b}$

K. Miwa, talk given at PENTAQUARK04

Why so small? What about  $K^+ p \rightarrow \pi^+ \Theta^+$  ?

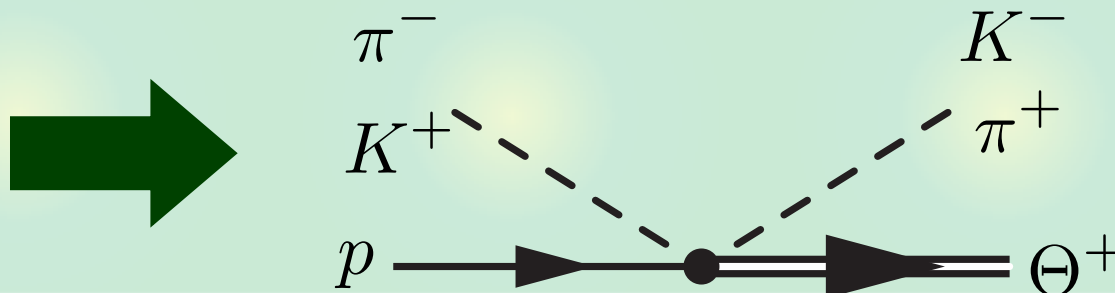
Two-meson coupling effects for  $\Theta^+$

Possibility of  $K\pi N$  bound state

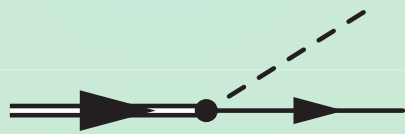
P. Bicudo, *et al.*, Phys. Rev. C69, 011503 (2004)

T. Kishimoto, *et al.*, hep-ex/0312003

F. J. Llanes-Estrada, *et al.*, Phys. Rev. C69, 055203 (2004)



# Two-meson coupling

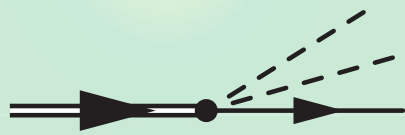


$$\Theta^+ \rightarrow KN$$

**Very narrow**

$$N(1710) \rightarrow \pi N$$

**10–20 %**

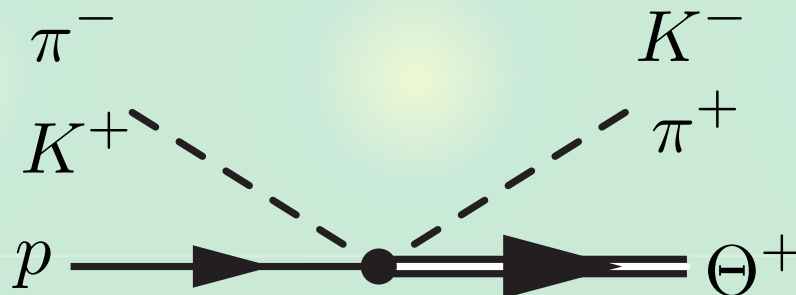


$$\Theta^+ \rightarrow K\pi N$$

**Forbidden**

$$N(1710) \rightarrow \pi\pi N$$

**40–90 %**



**Large??**

**Effective interactions which account for the  $N(1710) \rightarrow \pi\pi N$  decay**

# Criteria to construct the Lagrangian

**Interaction is SU(3) symmetric**

**Chiral symmetric? -> later**

**Small number of derivatives**

**low energy : OK**

**Assumptions for  $\Theta^+$**

**N(1710) is the S=0 partner of antidecuplet**

**->  $J^P = 1/2^+$**

**No mixing with 8, 27,...**

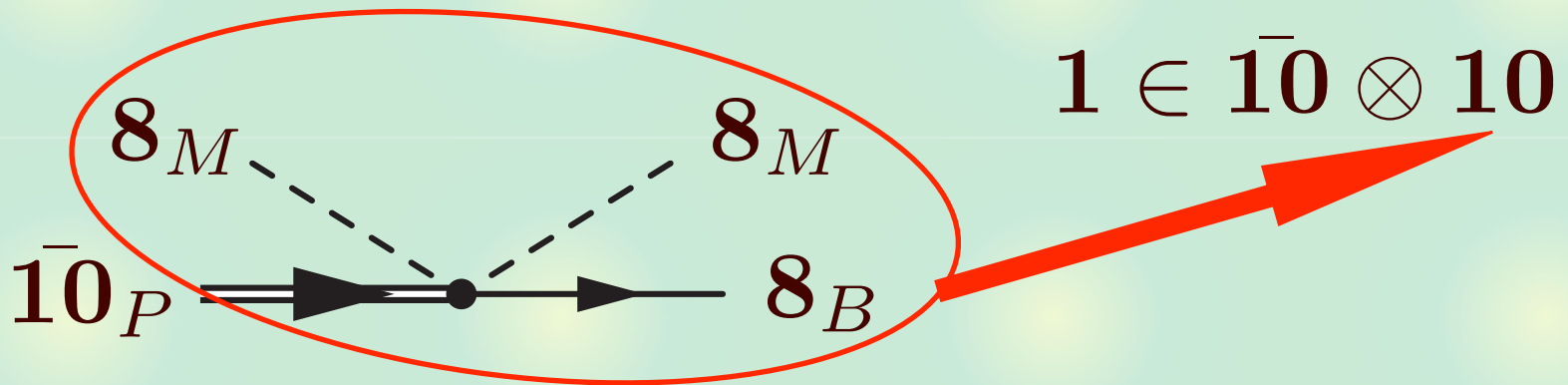
T.D. Cohen, Phys. Rev. D70, 074023 (2004)

S. Pakvasa and M. Suzuki, Phys. Rev. D70, 036002 (2004)

S. Ceci, *et al.*, nucl-th/0406055



# SU(3) structure of effective Lagrangian



$$8_M \otimes 8_M \otimes 8_B = (1 \oplus 8^s \oplus 8^a \oplus 10 \oplus \bar{10} \oplus 27)_{MM} \otimes 8_B$$

$$= 8 \quad \leftarrow \text{from } 1_{MM} \otimes 8_B$$

$$\oplus (1 \oplus 8 \oplus 8 \oplus \mathbf{10} \oplus \bar{10} \oplus 27) \quad \leftarrow \text{from } \underline{8^s_{MM}} \otimes 8_B$$

$$\oplus (1 \oplus 8 \oplus 8 \oplus \mathbf{10} \oplus \bar{10} \oplus 27) \quad \leftarrow \text{from } \underline{8^a_{MM}} \otimes 8_B$$

$$\oplus (8 \oplus \mathbf{10} \oplus 27 \oplus 35) \quad \leftarrow \text{from } \underline{10_{MM}} \otimes 8_B$$

$$\oplus (8 \oplus \bar{10} \oplus 27 \oplus 35') \quad \leftarrow \text{from } \bar{10}_{MM} \otimes 8_B$$

$$\oplus (8 \oplus \mathbf{10} \oplus \bar{10} \oplus 27 \oplus 27 \oplus 35 \oplus 35'' \oplus 64) \quad \leftarrow \text{from } \underline{27_{MM}} \otimes 8_B$$

# Interaction Lagrangians 1

## Antidecuplet field

$$P^{333} = \sqrt{6}\Theta_{10}^+$$

$$P^{133} = \sqrt{2}N_{10}^0 \quad P^{233} = -\sqrt{2}N_{10}^+$$

$$P^{113} = \sqrt{2}\Sigma_{10}^- \quad P^{123} = -\Sigma_{10}^0 \quad P^{223} = -\sqrt{2}\Sigma_{10}^+$$

$$P^{111} = \sqrt{6}\Xi_{10}^{--} \quad P^{112} = -\sqrt{2}\Xi_{10}^- \quad P^{122} = \sqrt{2}\Xi_{10}^0 \quad P^{222} = -\sqrt{6}\Xi_{10}^+$$

## Meson and baryon fields


$$\Phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}$$
$$B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda \end{pmatrix}$$

# Interaction Lagrangians 2

## Construction of 8s Lagrangian

$$\begin{aligned} D_i^j[\mathbf{8}_{MM}^s] &= \phi_i^a \phi_a^j + \phi_i^a \phi_a^j - \frac{2}{3} \delta_i^j \phi_a^b \phi_b^a \\ &= 2\phi_i^a \phi_a^j - \frac{2}{3} \delta_i^j \phi_a^b \phi_b^a \end{aligned}$$

$$T^{ijk}[\bar{\mathbf{10}}_{BMM(8s)}] = 2\phi_l^a \phi_a^i B_m^j \epsilon^{lmk} + (i, j, k \text{ symmetrized})$$


$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + h.c.$$

# Interaction Lagrangians 3

## Terms without derivative

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + h.c. \quad \mathbf{8s}$$

$$\mathcal{L}^{8a} = 0$$

$$\mathcal{L}^{10} = 0$$

**← symmetry under exchange of mesons**

$$\mathcal{L}^{27} = \frac{g^{27}}{2f} \left[ 4\bar{P}_{ijk} \epsilon^{lbk} \phi_l^i \phi_a^j B_b^a - \frac{4}{5} \bar{P}_{ijk} \epsilon^{lbk} \phi_l^a \phi_a^j B_b^i \right] + h.c.$$

## Experimental information

$$N(1710) \rightarrow \pi\pi (s\text{-wave}, I = 0) N$$

$$N(1710) \rightarrow \pi\pi (p\text{-wave}, I = 1) N$$

## With one derivative

**8a**

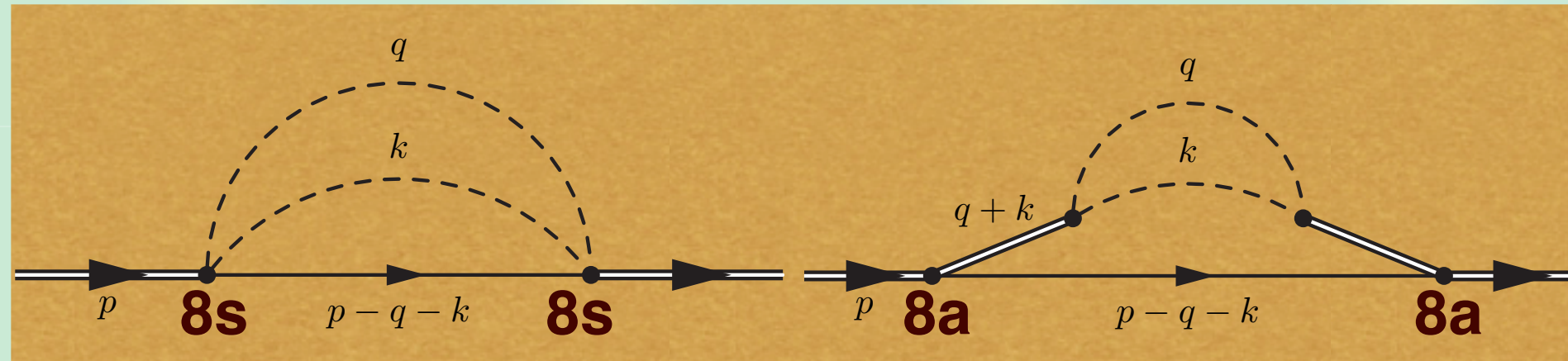
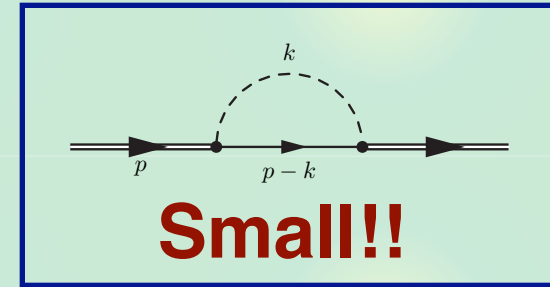
$$\mathcal{L}^{8a} = i \frac{g^{8a}}{4f^2} \bar{P}_{ijk} \epsilon^{lmk} \gamma^\mu (\partial_\mu \phi_l^a \phi_a^i - \phi_l^a \partial_\mu \phi_a^i) B_m^j + h.c.$$

# Diagrams for self-energy

Real part : mass shift

Imaginary part : decay width

SU(3) breaking : masses of particles

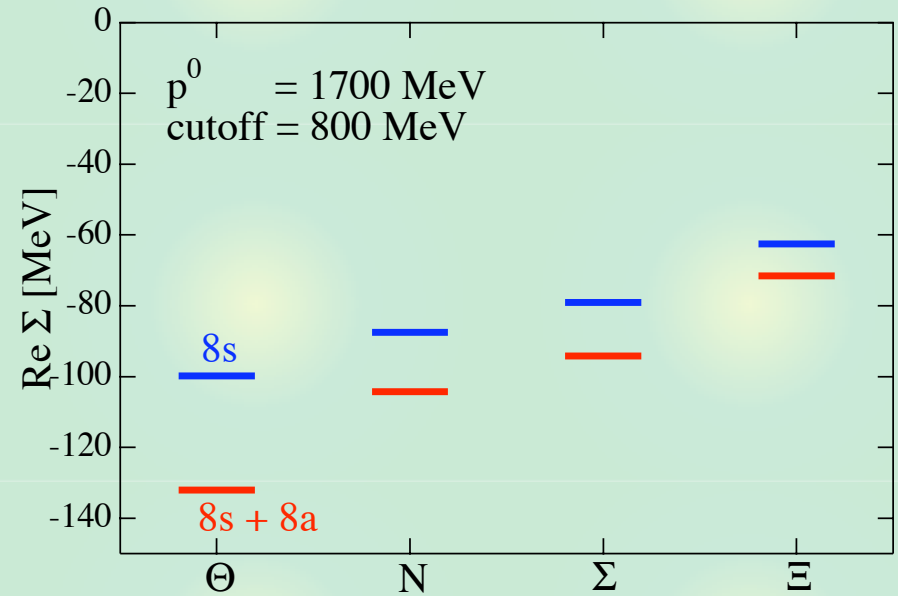
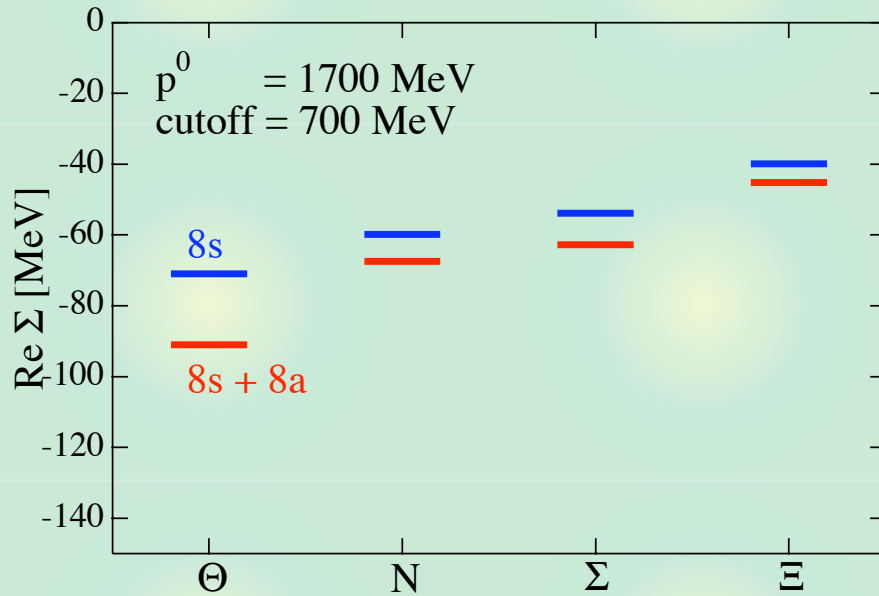


$$N(1710) \rightarrow \pi\pi (s\text{-wave}, I = 0) N \quad \mathbf{25 \text{ MeV}}$$

$$N(1710) \rightarrow \pi\pi (p\text{-wave}, I = 1) N \quad \mathbf{15 \text{ MeV}}$$

➔  $g^{8s} = 1.88$  ,  $g^{8a} = 0.315$

# Results of self-energy : Real part (mass shift)



**All mass shifts are attractive.**

**More bound for larger strangeness.**

**Mass difference between  $\Theta$  and  $\Xi$**

**-> 60 MeV : ~20 % of 320 = 1860–1540**

# Results of self-energy : Imaginary part (decay width)

Decay [MeV]	$\Gamma^{(8s)}$	$\Gamma^{(8a)}$	$\Gamma_{BMM}^{(tot)}$
$N(1710) \rightarrow N\pi\pi$ (inputs)	25	15	40
$N(1710) \rightarrow N\eta\pi$	0.58	-	
$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	6.0	24
$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10	0.62	
$\Sigma(1770) \rightarrow \Lambda\pi\pi$	-	2.9	
$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.46	2.1
$\Xi(1860) \rightarrow \Xi\pi\pi$	-	1.1	

## Other possible Lagrangians

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + h.c.$$

### Two-meson 27 interaction

$$\mathcal{L}^{27} = \frac{g^{27}}{2f} \left[ 4\bar{P}_{ijk} \epsilon^{lbk} \phi_l^i \phi_a^j B_b^a - \frac{4}{5} \bar{P}_{ijk} \epsilon^{lbk} \phi_l^a \phi_a^j B_b^i \right] + h.c.$$

### Chiral symmetric interaction

$$\mathcal{L}^\chi = \frac{g^\chi}{2f} \bar{P}_{ijk} \epsilon^{lmk} (A_\mu)_l^a (A^\mu)_a^i B_m^j + h.c.$$

$$A_\mu = \frac{i}{2} (\xi^\dagger \partial_\mu \xi - \xi \partial_\mu \xi^\dagger) = -\frac{\partial_\mu \phi}{\sqrt{2}f} + \mathcal{O}(p^3) \quad \xi = e^{i\phi/\sqrt{2}f}$$

$$(A_\mu)_l^a (A^\mu)_a^i \rightarrow \frac{1}{2f^2} \partial_\mu \phi_l^a \partial^\mu \phi_a^i$$

### SU(3) breaking interaction $M = \text{diag}(\hat{m}, \hat{m}, m_s)$

$$\mathcal{L}^M = \frac{g^M}{2f} \bar{P}_{ijk} \epsilon^{lmk} S_l^i B_m^j$$

$$S = \xi M \xi + \xi^\dagger M \xi^\dagger = \mathcal{O}(\phi^0) - \frac{1}{2f^2} (2\phi M \phi + \phi \phi M + M \phi \phi) + \mathcal{O}(\phi^4)$$



# Chiral symmetric Lagrangian

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + h.c.$$

$$\mathcal{L}^{\chi(2)} = \frac{g^\chi}{2f} \bar{P}_{ijk} \epsilon^{lmk} \frac{1}{2f^2} \partial_\mu \phi_l^a \partial^\mu \phi_a^i B_m^j + h.c.$$

**SU(3) structure : Identical !**

**Only loop integral is changed**

**<- adjusting the cutoff, we would have the same results**

**N(1710) decay ->  $g^\chi = 0.218$**

# Results of chiral Lagrangian

[MeV]

Re{ $\Sigma$ }	8s	$\chi(2)$	Decay	8s	$\chi(2)$
$\Theta$	-100	-99	$N(1710) \rightarrow N\pi\pi$	25	25
N	-87	-83	$N(1710) \rightarrow N\eta\pi$	0.58	0.32
$\Sigma$	-79	-70	$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	4.5
$\Xi$	-63	-57	$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10	3.6
cutoff	800	525	$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.40

Almost the same results

**Difference** comes from the SU(3) breaking of momenta at the vertex

## 27 and mass Lagrangians

$$\mathcal{L}^{27} = \frac{g^{27}}{2f} \left[ 4\bar{P}_{ijk}\epsilon^{lbk}\phi_l^i\phi_a^j B_b^a - \frac{4}{5}\bar{P}_{ijk}\epsilon^{lbk}\phi_l^a\phi_a^j B_b^i \right] + h.c.$$

$$\mathcal{L}^M = \frac{g^M}{2f}\bar{P}_{ijk}\epsilon^{lmk}\left(-\frac{1}{2f^2}\right)(2\phi M\phi + \phi\phi M + M\phi\phi)_l^i B_m^j + h.c.$$

**Fitting couplings to the N(1710) decay**

**-> large binding energy of 1 GeV : unrealistic**

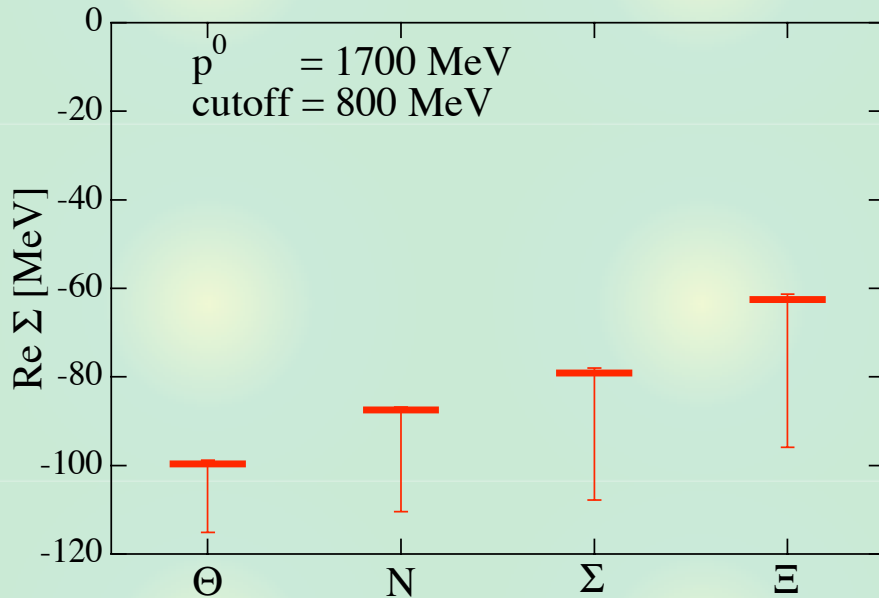
**Treat them as a small perturbation to the 8s.**

$$g^{27} = g^M = g^{8s} = 1.88, \quad b_{27} = -\frac{5}{4}(1-a), \quad b_M = \frac{f^2}{m_\pi^2}(1-a)$$

$$\mathcal{L}^{int} = a\mathcal{L}^{8s} + b_{27,M}\mathcal{L}^{27,M}$$

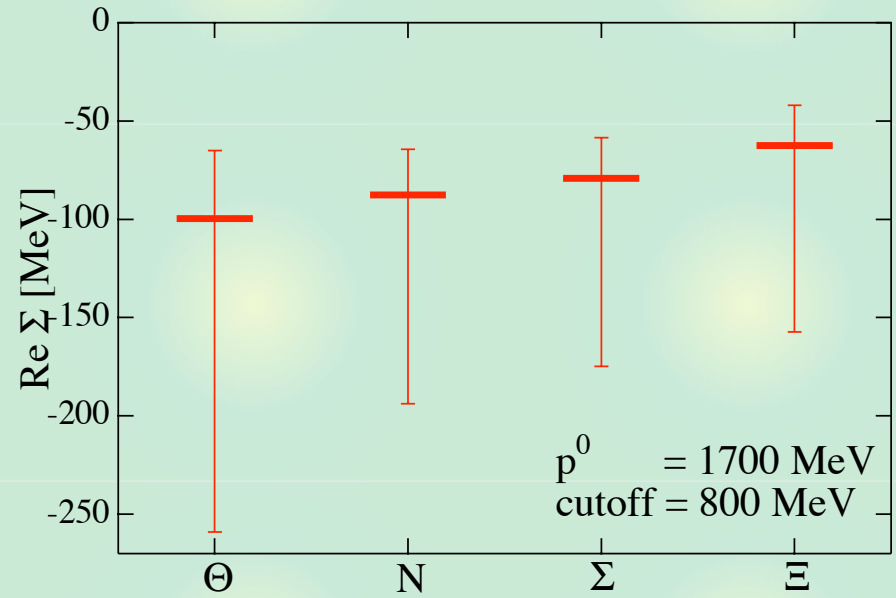
**Deviation from a = 1 : weight of new terms**

# Results of 27 and mass Lagrangians



**27**

$$0.90 < a < 1.06$$



**M**

$$0.76 < a < 1.06$$

**Contributions of these terms are considered as a theoretical uncertainty in the analysis.**

## Conclusion 1 : self-energy

We study the two-meson virtual cloud effect to the self-energy of baryon antidecuplet.




Two types of Lagrangians (8s, 8a) are important among several possible interaction Lagrangians.

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + h.c.$$

$$\mathcal{L}^{8a} = i \frac{g^{8a}}{4f^2} \bar{P}_{ijk} \epsilon^{lmk} \gamma^\mu (\partial_\mu \phi_l^a \phi_a^i - \phi_l^a \partial_\mu \phi_a^i) B_m^j + h.c.$$

## Conclusion 1 : self-energy

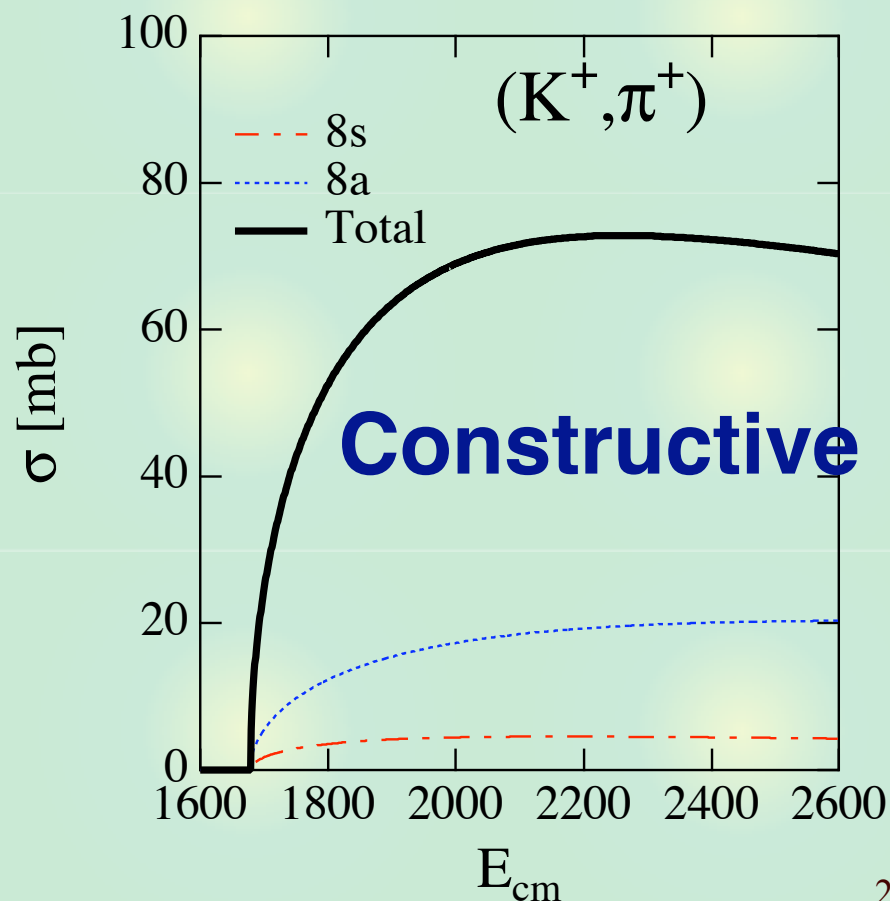
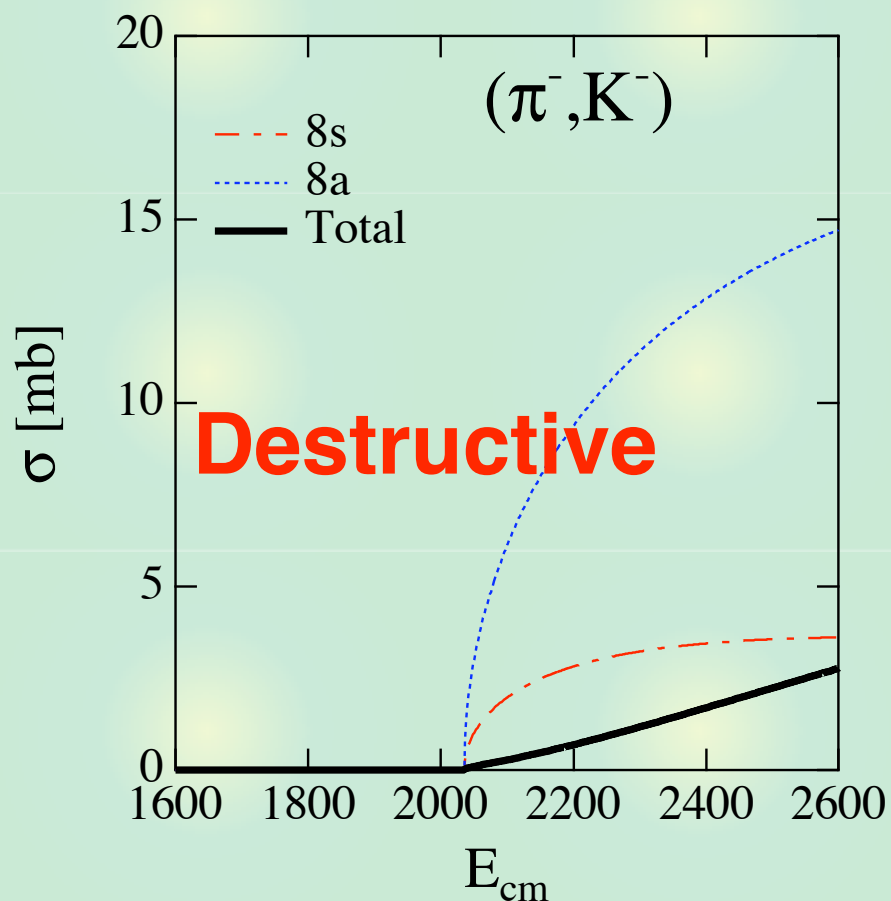
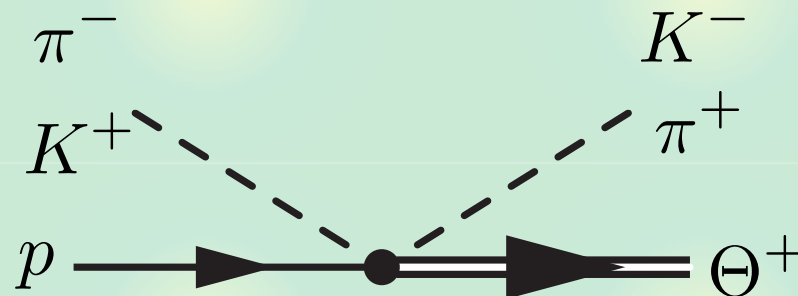
 Two-meson cloud effects are always **attractive**, and contribute to the antidecuplet **mass splitting**, of the order of **20%**.

 Antidecuplet members have relatively **small decay widths to MMB channel**.

T. H., A. Hosaka, F. J. Llanes-Estrada, E. Oset, J. R. Pelaez, M. J. Vicente Vacas, *in preparation*

# Results of reaction : cross sections

## Total cross section of



## Conclusion 2 : reactions

We investigate the  $\Theta$  production in  $(\pi^-, K^-)$  and  $(K^+, \pi^+)$  reactions, with the vertices obtained from the self-energy study.



The small cross section of the order of a few micro barn in  $(\pi^-, K^-)$  reaction may require some special mechanisms, such as **interference of two amplitudes.**

T. H., A. Hosaka, E. Oset, M. J. Vicente Vacas, *in preparation*



## Future works



### Self-energy

Chiral symmetric Lagrangian,  
Possible mixing with the other flavor  
multiplets (8, 27, ...),



### Reaction

Quantitative analysis (Form factor),  
background cross section