

Exotic hadrons in s-wave chiral dynamics



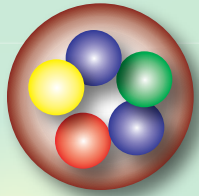
Tetsuo Hyodo^a

YITP, Kyoto^a

2007, Feb. 9th

Pentaquark Θ^+

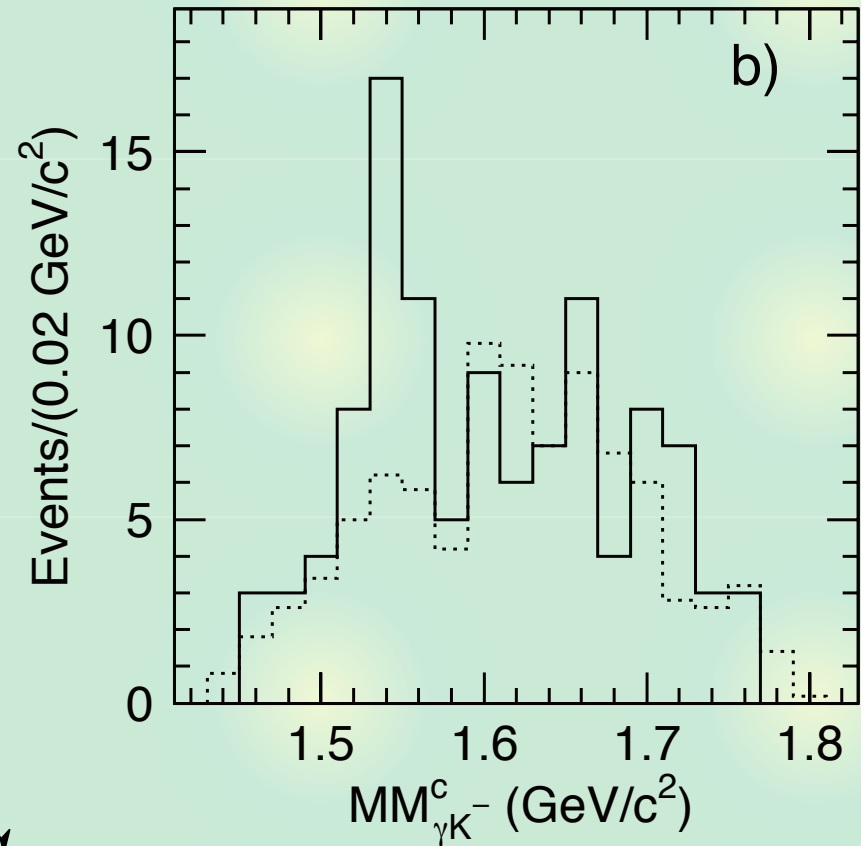
Θ^+ : $uudd\bar{s}$ state



$S = +1$

Candidate for a manifestly exotic hadron

$$\gamma n \rightarrow K^- K^+ n \quad \text{in } C$$

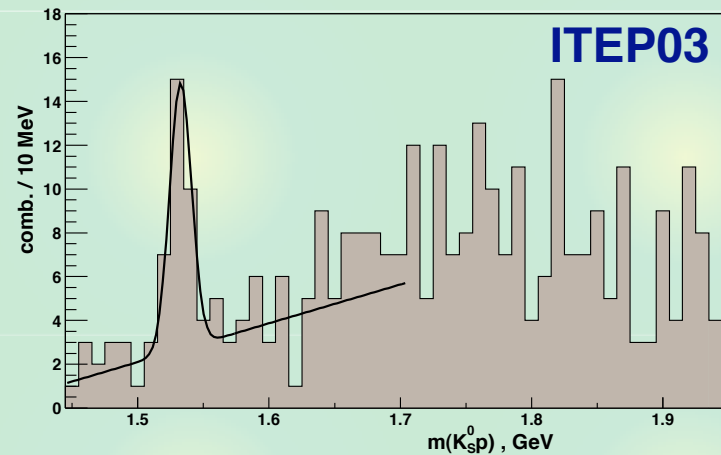
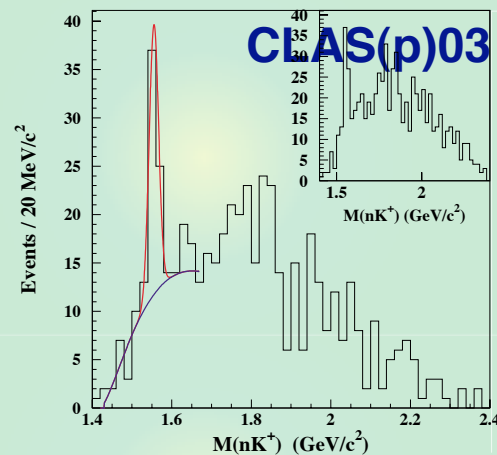
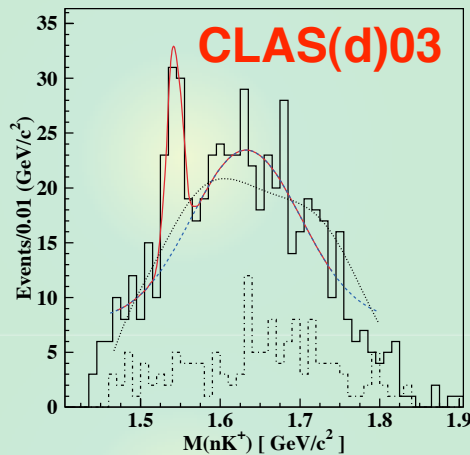
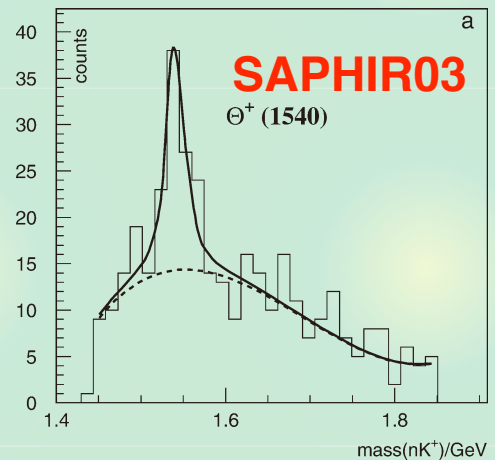
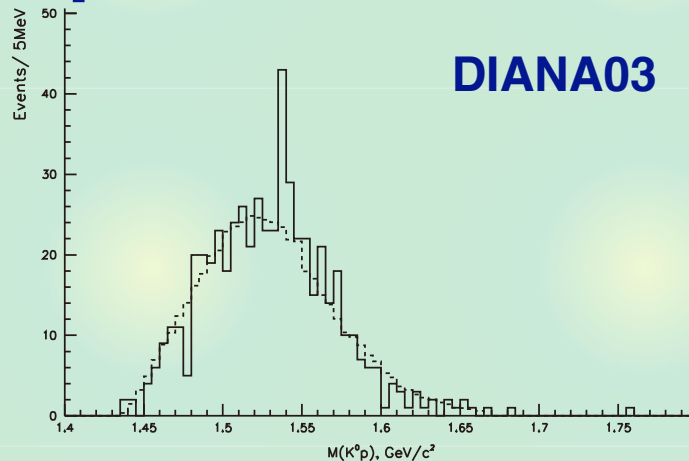
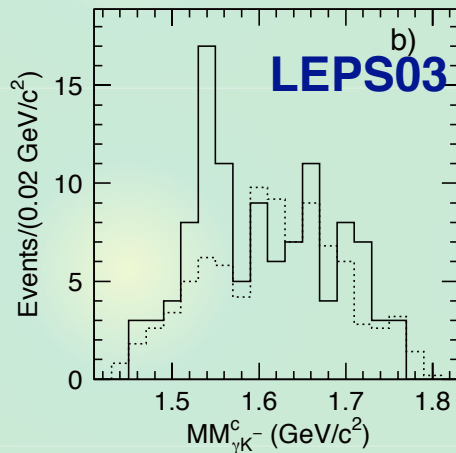


LEPS2003

Let us take a look at experiments

Status of pentaquark Θ^+

2003 ~ 2004 : 6 positive results



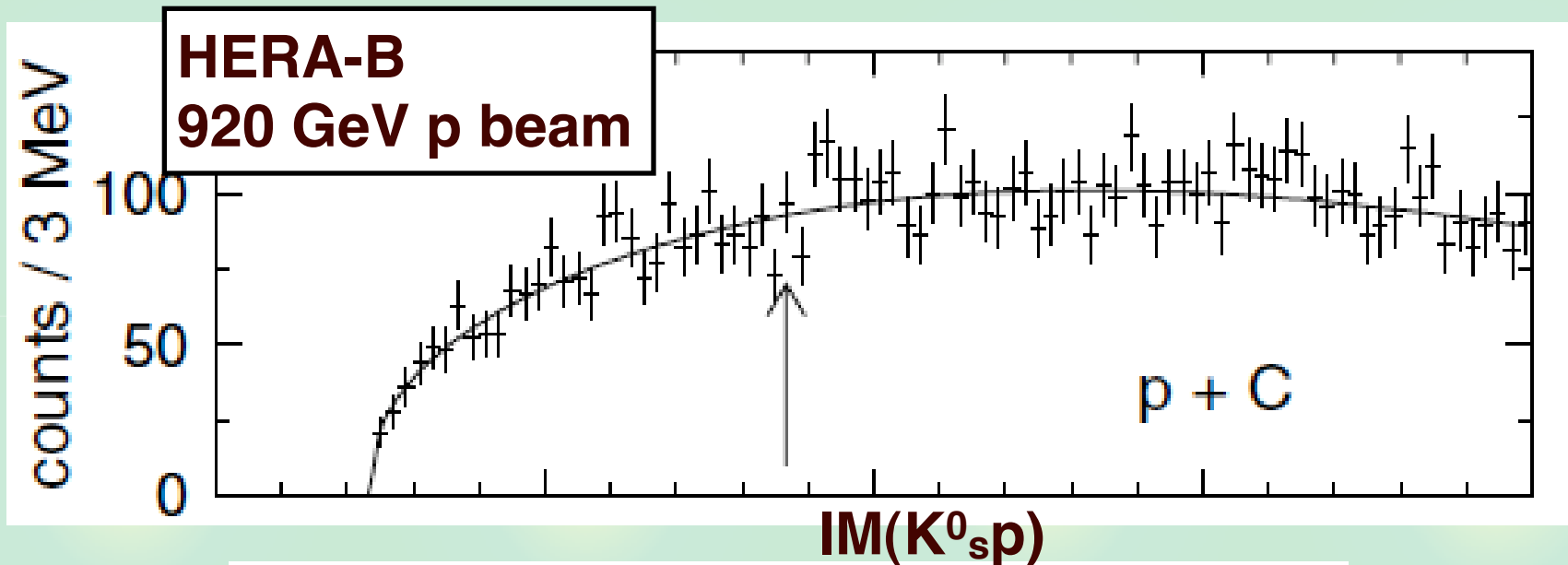
Citation: S. Eidelman *et al.* (Particle Data Group), Phys. Lett. B 592, 1 (2004) (URL: <http://pdg.lbl.gov>)

$\Theta(1540)^+$

$I(J^P) = 0(?)^?$ Status: ***

Status of pentaquark Θ^+

~ 2005 : **12 positive** results,
7 negative (high-energy inclusive).



elman *et al.* (Particle Data Group), Phys. Lett. B 592, 1 (2004) and 2005 partial update for edition 2006 (UR)

$\Theta(1540)^+$

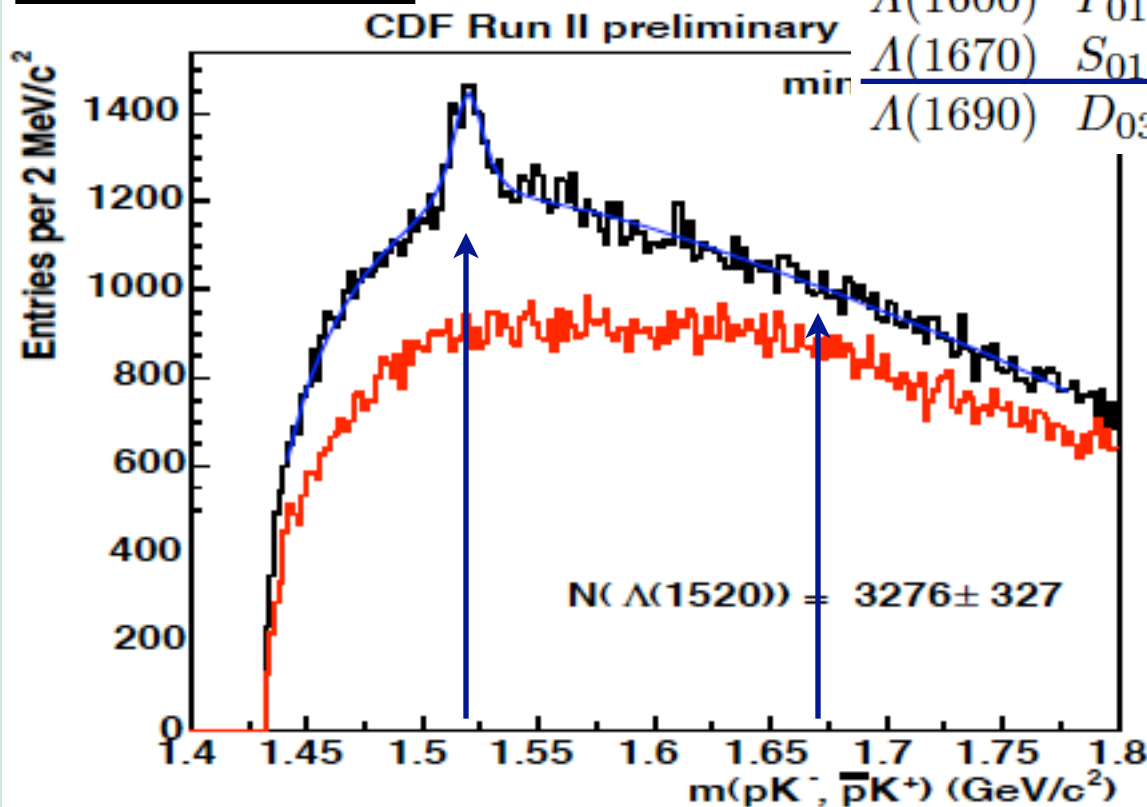
$I(J^P) = 0(?^?)$ Status: **

* limited number of resonances are observed in high energy exp.

Status of pentaquark Θ^+

What about $\Lambda(1670)$?

CDF
1.96 TeV $p\bar{p}$



Particle	$L_{I,2J}$	Overall status	$N\bar{K}$
$\Lambda(1116)$	P_{01}	****	
$\Lambda(1405)$	S_{01}	****	****
$\Lambda(1520)$	D_{03}	****	****
$\Lambda(1600)$	P_{01}	***	***
$\Lambda(1670)$	S_{01}	****	****
$\Lambda(1690)$	D_{03}	****	****

$\Gamma = 15 \text{ MeV}$

$\Gamma = 35 \text{ MeV}$

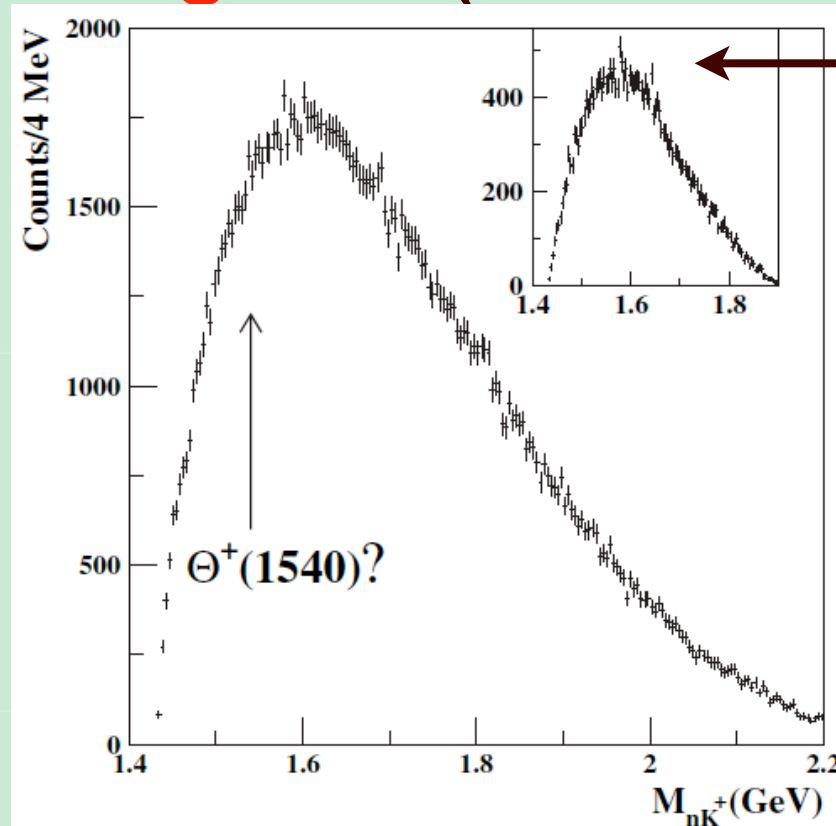
Same argument:
 $\Sigma(1670)$ in K^0p ?
 $\Gamma = 60 \text{ MeV}$

Status of pentaquark Θ^+

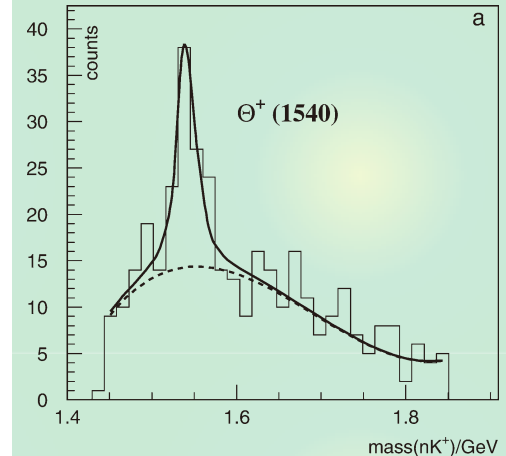
~ present : **14 positive** results,
13 negative (also in low energy)

CLAS06

$$\gamma p \rightarrow \bar{K}^0 K^+ n$$



Same
kinematical
cuts with
SAPHIRO3



Citation: W.-M. Yao *et al.* (Particle Data Group), J. Phys. G **33**, 1 (2006) (URL: <http://pdg.lbl.gov>)

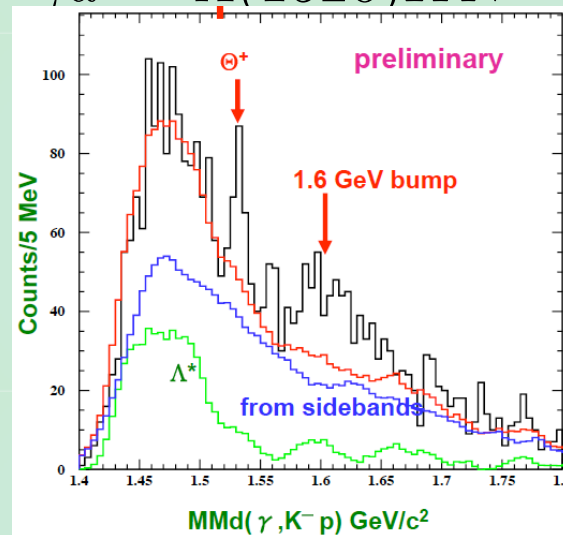
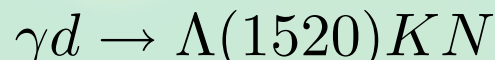
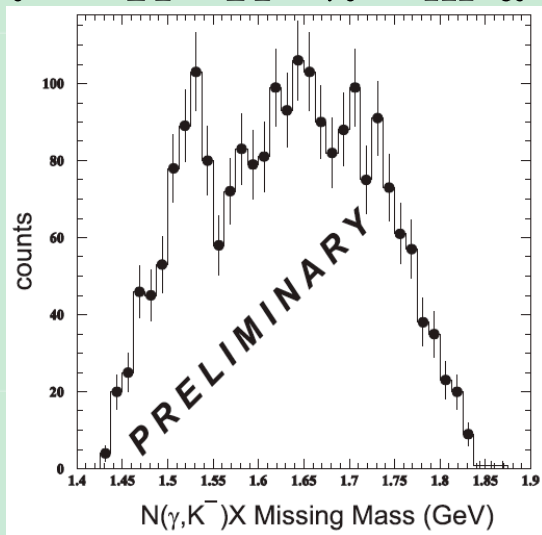
$\Theta(1540)^+$

$I(J^P) = 0(??)$ Status: *

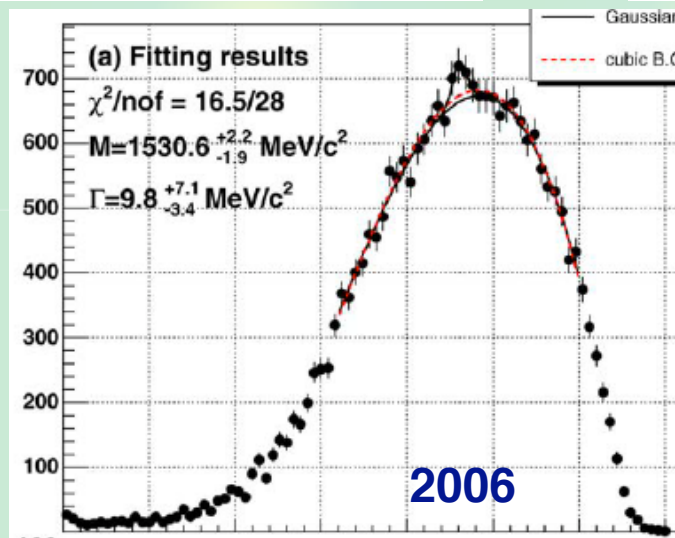
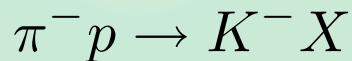
Status of pentaquark Θ^+

New positive(?) results:

LEPS



KEK



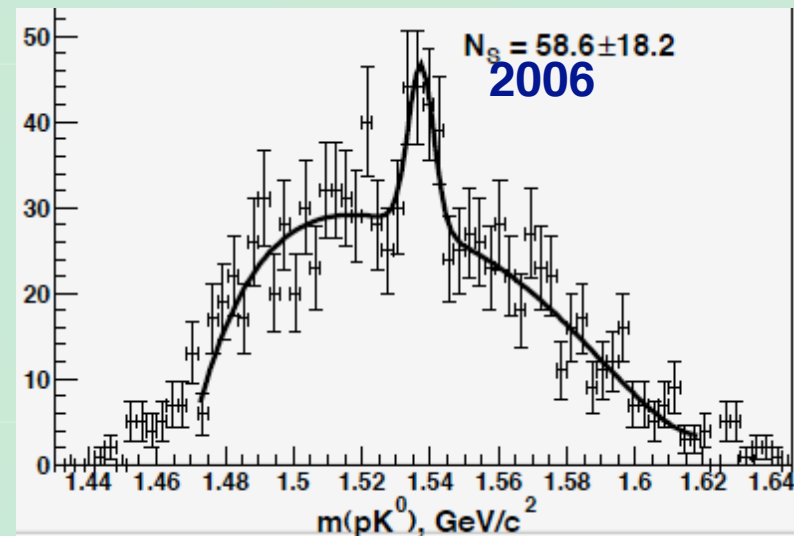
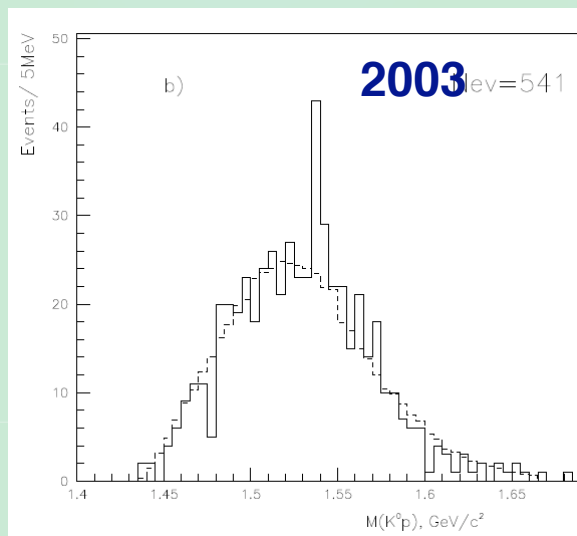
See Titov et al, PRC2006

Status of pentaquark Θ^+

Updated positive results:

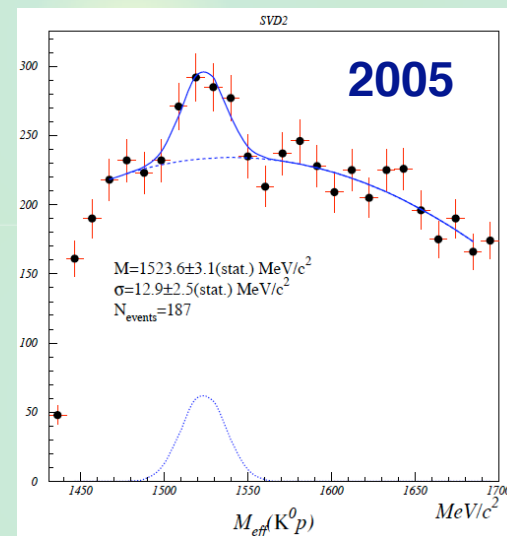
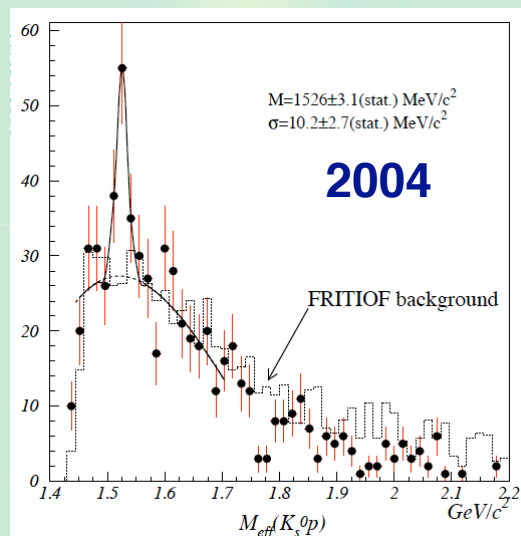
DIANA

$$K^+ n \rightarrow K^0 p \text{ in } Xe$$



SVD

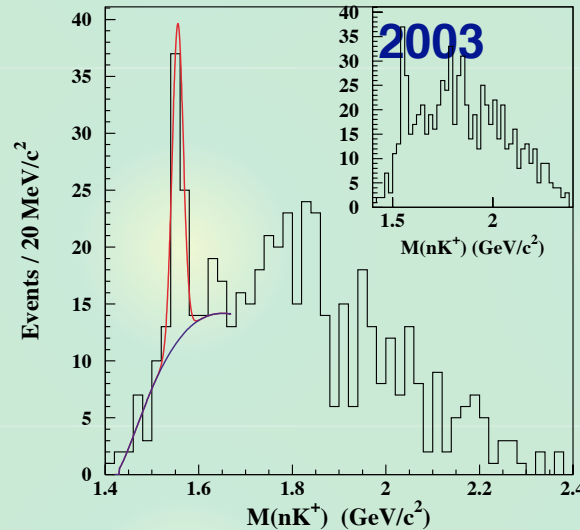
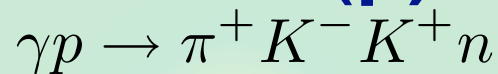
$$pA \rightarrow pK_s^0 + X$$



Status of pentaquark Θ^+

Remaining (not yet denied) positive results:

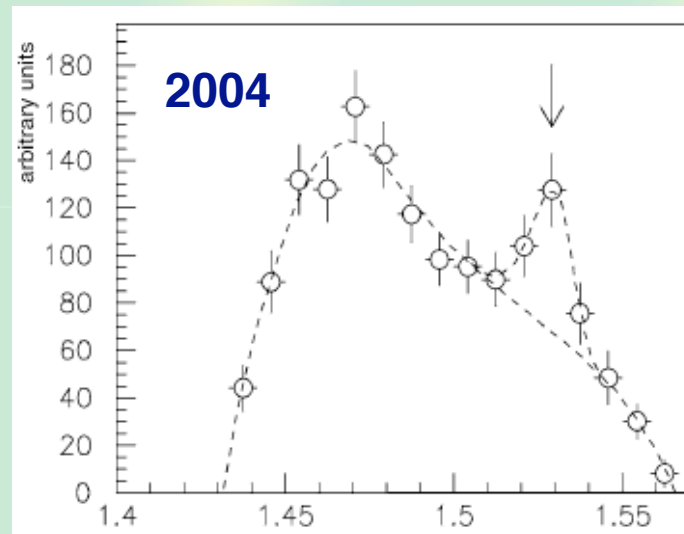
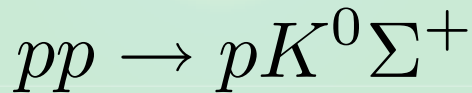
CLAS(p)



7 sigma!!

The experiment will be run in 2007

COSY-TOF



4-6 sigma

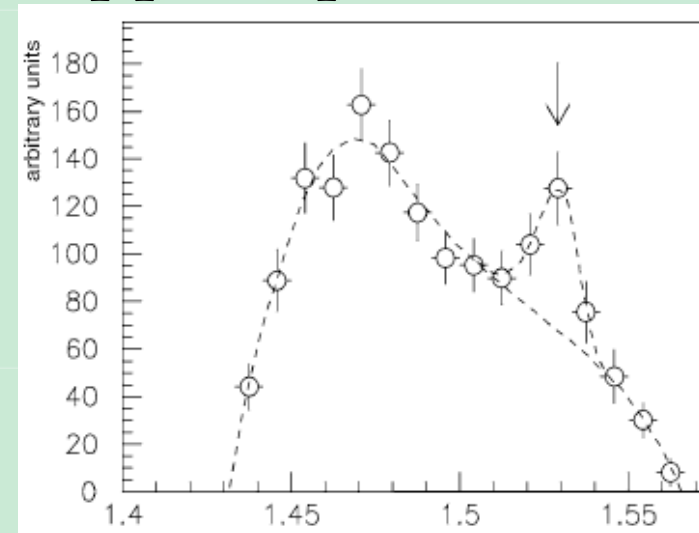
Large no. of events!!

last year new data came up...

Status of pentaquark Θ^+

COSY new (hep-ex/0612048)

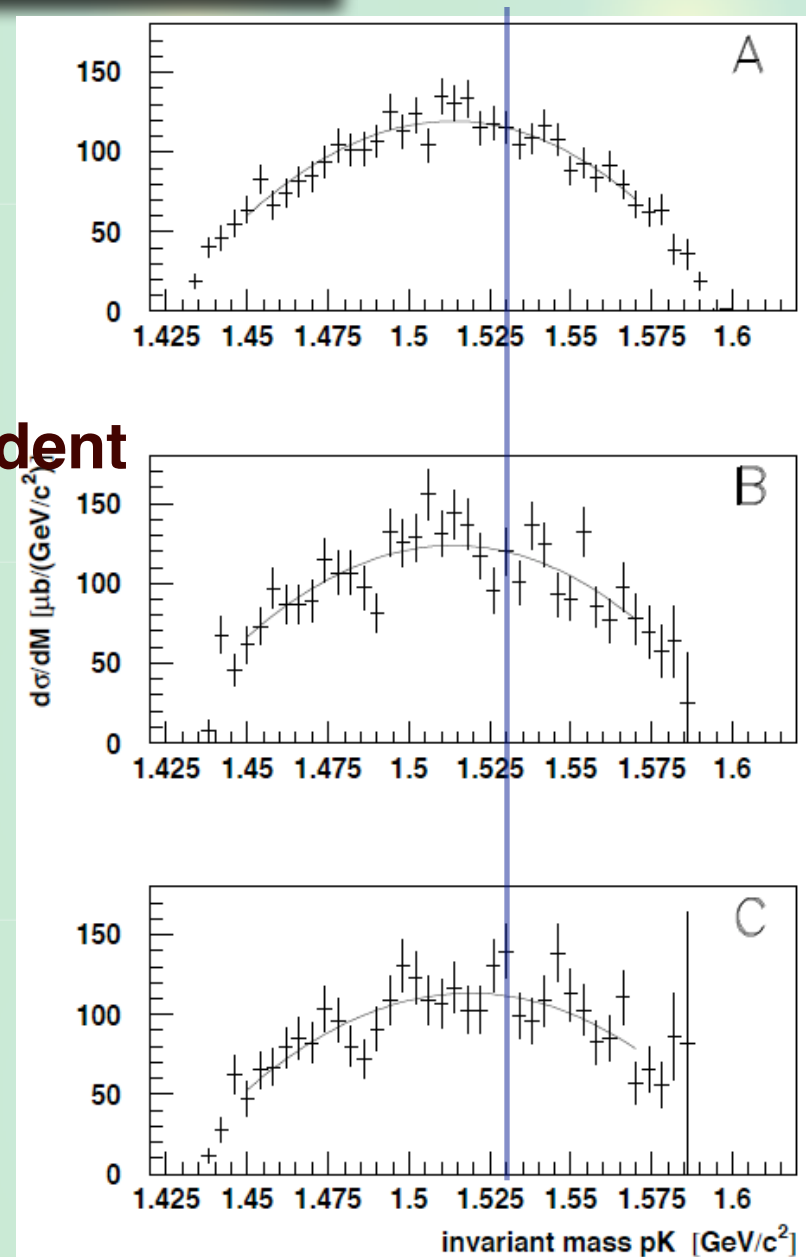
$$pp \rightarrow pK^0\Sigma^+$$



new data
3 independent
analysis

“Analysis does not confirm Θ^+ .”
cross section $\sigma < 0.3 \mu\text{b}$

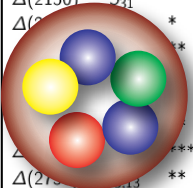
Beam energy slightly different
“A” does not tag Σ^+ decay
previous $\sigma = 0.4 \pm 0.1 \pm 0.1 \mu\text{b}$



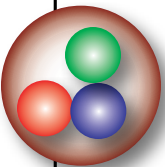
Exotic hadrons

Observed hadrons in experiments (PDG06) :

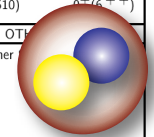
p	P_{11}	****	$\Delta(1232)$	P_{33}	****	Λ	P_{01}	****	Σ^+	P_{11}	****	Ξ^0	P_{11}	****
n	P_{11}	****	$\Delta(1600)$	P_{33}	***	$\Lambda(1405)$	S_{01}	****	Σ^0	P_{11}	****	Ξ^-	P_{11}	****
$N(1440)$	P_{11}	****	$\Delta(1620)$	S_{31}	****	$\Lambda(1520)$	D_{03}	****	Σ^-	P_{11}	****	$\Xi(1530)$	P_{13}	****
$N(1520)$	D_{13}	****	$\Delta(1700)$	D_{33}	****	$\Lambda(1600)$	P_{01}	***	$\Sigma(1385)$	P_{13}	****	$\Xi(1620)$	*	
$N(1535)$	S_{11}	****	$\Delta(1750)$	P_{31}	*	$\Lambda(1670)$	S_{01}	****	$\Sigma(1480)$	*		$\Xi(1690)$	***	
$N(1650)$	S_{11}	****	$\Delta(1900)$	S_{31}	**	$\Lambda(1690)$	D_{03}	****	$\Sigma(1560)$	**		$\Xi(1820)$	D_{13}	***
$N(1675)$	D_{15}	****	$\Delta(1905)$	F_{35}	****	$\Lambda(1800)$	S_{01}	***	$\Sigma(1580)$	D_{13}	*	$\Xi(1950)$	***	
$N(1680)$	F_{15}	****	$\Delta(1910)$	P_{31}	****	$\Lambda(1810)$	P_{01}	***	$\Sigma(1620)$	S_{11}	**	$\Xi(2030)$	***	
$N(1700)$	D_{13}	***	$\Delta(1920)$	P_{33}	***	$\Lambda(1820)$	F_{05}	****	$\Sigma(1660)$	P_{11}	***	$\Xi(2120)$	*	
$N(1710)$	P_{11}	***	$\Delta(1930)$	D_{35}	***	$\Lambda(1830)$	D_{05}	****	$\Sigma(1670)$	D_{13}	****	$\Xi(2250)$	**	
$N(1720)$	P_{13}	****	$\Delta(1940)$	D_{33}	*	$\Lambda(1890)$	P_{03}	****	$\Sigma(1690)$	**		$\Xi(2370)$	**	
$N(1900)$	P_{13}	****	$\Delta(1950)$	F_{37}	****	$\Lambda(2000)$	*		$\Sigma(1750)$	S_{11}	**	$\Xi(2500)$	*	
$N(1990)$	F_{17}	**	$\Delta(2000)$	F_{35}	**	$\Lambda(2020)$	F_{07}	*	$\Sigma(1770)$	P_{11}	*			
$N(2000)$	F_{15}	**	$\Delta(2150)$	S_{31}	*	$\Lambda(2100)$	G_{07}	****	$\Sigma(1775)$	D_{15}	****	Ω^-	****	
$N(2080)$	D_{13}	**	$\Delta(2150)$	*	*	$\Lambda(2110)$	F_{05}	***	$\Sigma(1840)$	P_{13}	*	$\Omega(2250)^-$	***	
$N(2090)$	S_{11}	*	$\Delta(2150)$	*	*	$\Lambda(2110)$	F_{05}	***	$\Sigma(1840)$	P_{13}	*	$\Omega(2380)^-$	**	
$N(2100)$	P_{11}	*	$\Delta(2150)$	*	*	$\Lambda(2325)$	D_{03}	*	$\Sigma(1880)$	P_{11}	**	$\Omega(2470)^-$	**	
$N(2100)$	P_{11}	*	$\Delta(2150)$	*	*	$\Lambda(2350)$	H_{09}	***	$\Sigma(1915)$	F_{15}	****			
$N(2190)$	G_{17}	****	$\Delta(2150)$	*	*	$\Lambda(2585)$	**	**	$\Sigma(1940)$	D_{13}	***	Λ_c^+	****	
$N(2200)$	D_{15}	**	$\Delta(2150)$	*	*				$\Sigma(2000)$	S_{11}	*	$\Lambda_c(2593)^+$	***	
$N(2220)$	H_{19}	****	$\Delta(2150)$	*	*				$\Sigma(2030)$	F_{17}	****	$\Lambda_c(2625)^+$	***	
$N(2250)$	G_{19}	****	$\Delta(2150)$	*	*				$\Sigma(2070)$	F_{15}	*	$\Lambda_c(2765)^+$	*	
$N(2600)$	$h_{1,11}$	***	$\Delta(2950)$	$K_{3,15}$	**				$\Sigma(2080)$	P_{13}	**	$\Lambda_c(2880)^+$	**	
$N(2700)$	$K_{1,13}$	**	$\Theta(1540)^+$	*	*				$\Sigma(2100)$	G_{17}	**	$\Sigma_c(2455)$	****	



1
286



LIGHT UNFLAVORED (S = C = B = 0)		STRANGE (S = ±1, C = B = 0)		BOTTOM (B = ±1)	
$\rho^i (J^PC)$	$\rho^i (J^PC)$	$\rho^i (J^PC)$	$\rho^i (J^PC)$	$\rho^i (J^PC)$	$\rho^i (J^PC)$
π^+	$1^-(0^-)$	$\pi_2(1670)$	$1^-(2^-)$	K^+	$1/2(0^-)$
π^0	$1^-(0^-)$	$\phi(1680)$	$0^-(1^-)$	K^0	$1/2(0^-)$
η	$0^+(0^-)$	$\rho_3(1690)$	$1^+(3^-)$	K_S^0	$1/2(0^-)$
$\eta(578)$	$0^+(0^-)$	$\rho_3(1700)$	$1^+(1^-)$	K_L^0	$1/2(0^-)$
$\eta(958)$	$0^+(0^-)$	$a_2(1700)$	$1^-(2^{++})$	$K_2^*(800)$	$1/2(0^+)$
$\eta(980)$	$0^+(0^-)$	$\omega(1710)$	$0^+(0^{++})$	$K^*(892)$	$1/2(1^-)$
$\phi(1020)$	$0^-(1^-)$	$\eta(1760)$	$0^+(0^-)$	$K_1(1270)$	$1/2(1^+)$
$h_1(1170)$	$0^-(1^-)$	$\pi(1800)$	$1^-(0^-)$	$K_1(1400)$	$1/2(1^+)$
$h_1(1235)$	$1^+(1^-)$	$\pi(1810)$	$0^+(2^{++})$	$K^*(1410)$	$1/2(1^-)$
$a_1(1260)$	$1^-(1^{++})$	$X(1835)$	$?^?(?^-)$	$K_S^*(1430)$	$1/2(0^+)$
$f_2(1270)$	$0^+(2^{++})$	$\phi_3(1850)$	$0^-(3^-)$	$K_2^*(1430)$	$1/2(2^+)$
$f_1(1285)$	$0^+(1^{++})$	$\eta_2(1870)$	$0^+(2^-)$	$K(1460)$	$1/2(0^-)$
$\eta(1295)$	$0^-(0^-)$	$\pi_2(1900)$	$1^+(1^-)$	$K_2(1580)$	$1/2(2^-)$
$\eta(1300)$	$0^-(0^-)$	$f_3(1910)$	$0^+(2^{++})$	$K(1630)$	$1/2(2^?)$
$a_2(1320)$	$1^-(2^{++})$	$f_1(1950)$	$0^+(2^{++})$	$K_1(1650)$	$1/2(1^?)$
$f_0(1370)$	$0^+(0^{++})$	$\rho_3(1990)$	$1^-(3^-)$	$K^*(1680)$	$1/2(1^-)$
$h_1(1380)$	$?^-(1^-)$	$f_2(2010)$	$0^+(2^{++})$	$K_2(1770)$	$1/2(2^-)$
$\pi_1(1400)$	$1^-(1^-)$	$\phi_4(2020)$	$0^+(0^{++})$	$K_3^*(1780)$	$1/2(3^-)$
$\eta(1405)$	$0^-(0^-)$	$a_4(2040)$	$1^-(4^{++})$	$K_2(1820)$	$1/2(2^-)$
$f_1(1420)$	$0^+(1^{++})$	$f_4(2050)$	$0^+(4^{++})$	$K(1830)$	$1/2(0^-)$
$\omega(1420)$	$0^-(1^-)$	$\pi_2(2100)$	$1^-(2^-)$	$K_2^*(1950)$	$1/2(0^+)$
$f_2(1430)$	$0^+(2^{++})$	$f_0(2100)$	$0^+(0^{++})$	$K_2^*(1980)$	$1/2(2^+)$
$a_0(1450)$	$1^-(0^-)$	$f_2(2150)$	$0^+(2^{++})$	$K_1^*(2045)$	$1/2(4^+)$
$\rho(1450)$	$1^-(1^-)$	$\rho(2150)$	$1^-(1^-)$	$K_2(2250)$	$1/2(2^-)$
$\eta(1475)$	$0^-(0^-)$	$\rho(2200)$	$0^+(0^{++})$	$K_3(2320)$	$1/2(3^+)$
$f_0(1500)$	$0^+(0^{++})$	$a_0(1450)$	$1^-(0^-)$	$K_1^*(2380)$	$1/2(5^-)$
$f_1(1510)$	$0^+(1^{++})$	$\rho(1450)$	$1^-(1^-)$	$K_4(2500)$	$1/2(4^-)$
$f_2'(1525)$	$0^+(2^{++})$	$\eta(1475)$	$0^-(0^-)$	$K(3100)$	$?^?(?^?)$
$h_1(1595)$	$0^-(1^-)$	$f_0(1500)$	$0^+(0^{++})$		
$\pi_1(1600)$	$1^-(1^-)$	$f_1(1510)$	$0^+(1^{++})$		
$a_1(1640)$	$1^-(1^{++})$	$f_2(1565)$	$0^+(2^{++})$		
$f_2(1640)$	$0^+(2^{++})$	$h_1(1595)$	$0^-(1^-)$		
$\omega(1650)$	$0^-(1^-)$	$\pi_1(1600)$	$1^-(1^-)$		
$\omega_3(1670)$	$0^-(3^-)$	$a_1(1640)$	$1^-(1^{++})$		



127 baryons

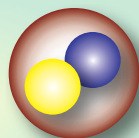
159 mesons

Exotic hadrons are indeed exotic !!

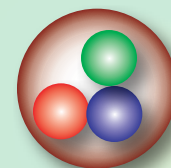
Motivation 1 : Exotic hadrons

Exotic hadrons : states other than $q\bar{q}$, qqq .
Experimentally, they are **exotic**.

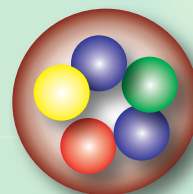
159 mesons



127 baryons



1 pentaquark with *



Theoretically, are they exotic?

--> QCD does not forbid exotic states,
effective models neither.

How exotic are they??

Motivation 2 : Chiral unitary approaches

Hadron excited states \sim 

- Interaction \leftarrow chiral symmetry
- Amplitude \leftarrow unitarity

R.H. Dalitz, and S.F. Tuan, *Ann. Phys. (N.Y.)* 10, 307 (1960)

J.H.W. Wyld, *Phys. Rev.* 155, 1649 (1967)

N. Kaiser, P. B. Siegel and W. Weise, *Nucl. Phys.* A594, 325 (1995)

E. Oset and A. Ramos, *Nucl. Phys.* A635, 99 (1998)

J. A. Oller and U. G. Meissner, *Phys. Lett.* B500, 263 (2001)

M.F.M. Lutz and E. E. Kolomeitsev, *Nucl. Phys.* A700, 193 (2002)

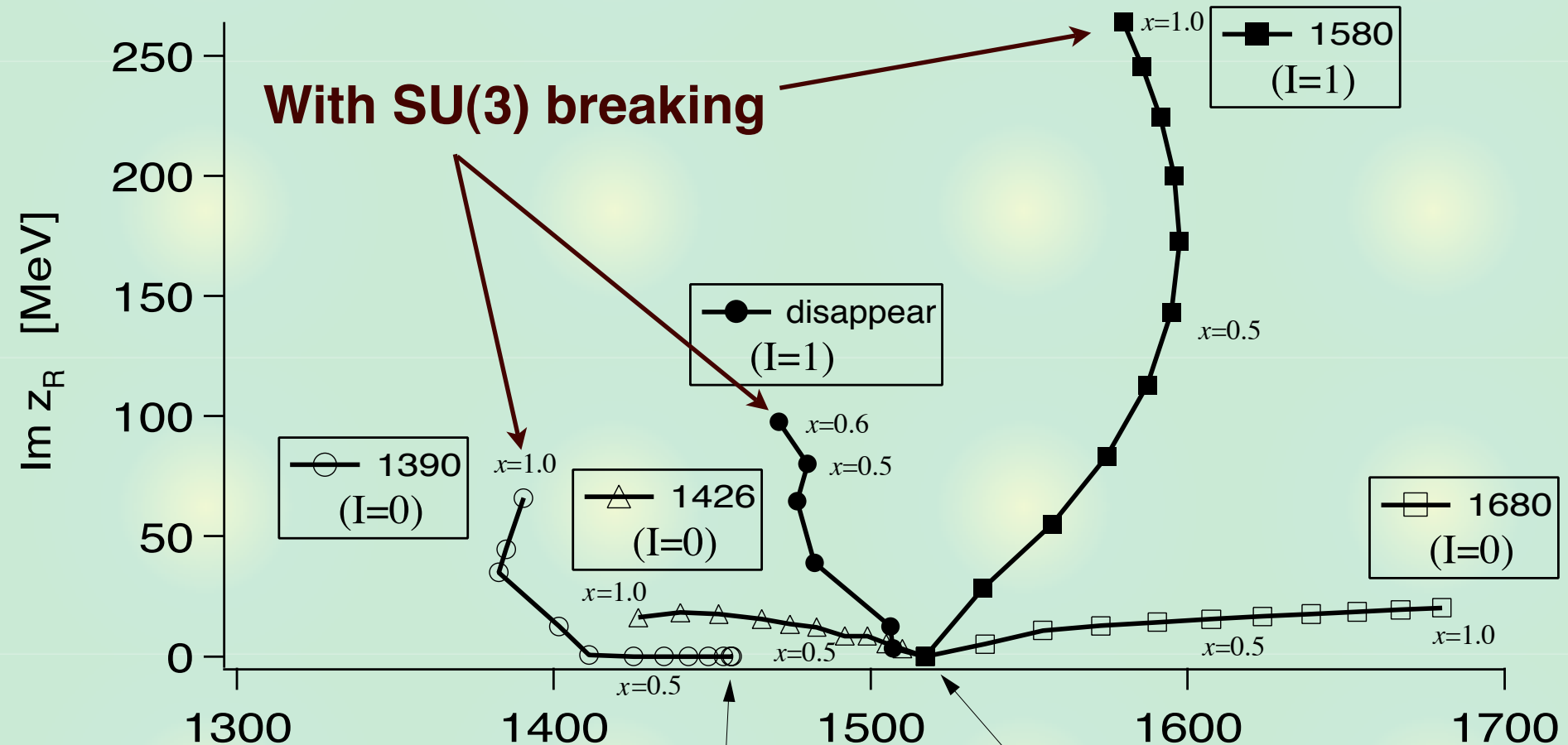
Many hadron resonances ($\Lambda(1405)$, $N(1535)$, $\Lambda(1520)$, $D_s(2317)$,...) are well described.

What about exotic hadrons?

Origin of the resonances

Pole positions :

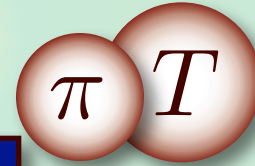
D. Jido, et al., Nucl. Phys. A 723, 205 (2003)



--> Search for **bound states in SU(3) symmetric limit.**

Outline

Hadron-NG boson bound state



Chiral Symmetry

s-wave low energy interaction

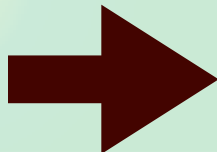
$$V_{\alpha} = -\frac{\omega}{2f^2} C_{\alpha,T} \quad C_{\text{exotic}} = 1$$

Scattering theory

Critical strength for a bound state

$$C_{\text{crit}} = \frac{2f^2}{m(-G(M_T + m))}$$

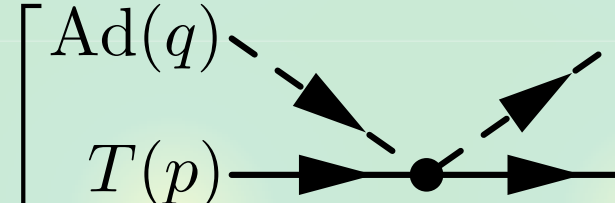
physical values : $C_{\text{exotic}} < C_{\text{crit}}$



No exotic state exists.

Low energy s-wave interaction

Scattering of a target (T) with the pion (Ad)

$$\alpha \left[\begin{array}{c} \text{Ad}(q) \\ T(p) \end{array} \right] = \frac{1}{f^2} \frac{p \cdot q}{2M_T} \langle \mathbf{F}_T \cdot \mathbf{F}_{\text{Ad}} \rangle_\alpha + \mathcal{O} \left((m/M_T)^2 \right)$$


s-wave : Weinberg-Tomozawa term

$$V_\alpha = -\frac{\omega}{2f^2} C_{\alpha,T}$$

proportional to pion energy

Coupling : pion decay constant

Y. Tomozawa, *Nuovo Cim.* **46A**, 707 (1966)

S. Weinberg, *Phys. Rev. Lett.* **17**, 616 (1966)

$$C_{\alpha,T} \equiv -\langle 2\mathbf{F}_T \cdot \mathbf{F}_{\text{Ad}} \rangle_\alpha = C_2(T) - C_2(\alpha) + 3 \quad (\text{for } N_f = 3)$$

Coupling strengths : Examples

Examples of C_α : (positive is attractive)

$$C_{\alpha,T} = C_2(T) - C_2(\alpha) + 3$$

α	1	8	10	$\bar{10}$	27	35
T=8 (N,Λ,Σ,Ξ)	6	3	0	0	-2	
T=10(Δ,Σ^*,Ξ^*,Ω)		6	3		1	-3

α	$\bar{3}$	6	$\bar{15}$	24
T=$\bar{3}$ (Λ_c,Ξ_c)	3	1	-1	-2
T=6 (Σ_c,Ξ_c^*,Ω_c)	5	3	1	

- **Exotic channels** : mostly repulsive
- **Attractive interaction** : **C = 1**

Coupling strengths : General expression

$$T = [p, q] \quad \alpha \in [p, q] \otimes [1, 1]$$

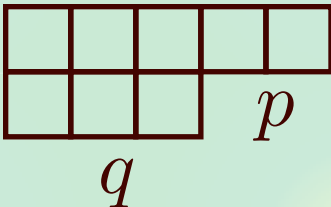
α	$C_{\alpha, T}$	sign
$[p + 1, q + 1]$	$-p - q$	repulsive
$[p + 2, q - 1]$	$1 - p$	
$[p - 1, q + 2]$	$1 - q$	
$[p, q]$	3	attractive
$[p, q]$	3	attractive
$[p + 1, q - 2]$	$3 + q$	attractive
$[p - 2, q + 1]$	$3 + p$	attractive
$[p - 1, q - 1]$	$4 + p + q$	attractive

- **C should be integer.**
- **Sign is determined for most cases.**

Exoticness

Exoticness : minimal number of extra $\bar{q}q$.


For $[p, q]$ and baryon number B ,

$$E = \epsilon\theta(\epsilon) + \nu\theta(\nu)$$



$$\epsilon \equiv \frac{p + 2q}{3} - B, \quad \nu \equiv \frac{p - q}{3} - B$$

V. Kopeliovich, Phys. Lett. B259, 234 (1991)

D. Diakonov and V. Petrov, Phys. Rev. D 69, 056002 (2004)

but... $[p, q] = [6, 0] = 28, \quad B = 1$  **uuu $u\bar{d}$ $u\bar{d}$**
 $E = 2, \quad \epsilon = 1$

E. Jenkins and A.V. Manohar, Phys. Rev. Lett. 93, 022001 (2004)

but... $[p, q] = [0, 0] = 1, \quad B = 1$  **uds**
 $E = 0, \quad \epsilon = -1, \quad \nu = -1$

Exotic channels

Consider α is more “exotic” than T

For $[p, q]$ and baryon number B ,

$$E = \epsilon\theta(\epsilon) + \nu\theta(\nu) \quad \epsilon \equiv \frac{p+2q}{3} - B, \quad \nu \equiv \frac{p-q}{3} - B$$

$\Delta E = E_\alpha - E_T = +1$ is realized when

○ $\Delta\epsilon = 1, \Delta\nu = 0, \epsilon_T \geq 0,$

$\alpha = [p+1, q+1] : C_{\alpha,T} = -p - q$ **repulsive**

○ $\Delta\epsilon = 0, \Delta\nu = 1, \nu_T \geq 0,$

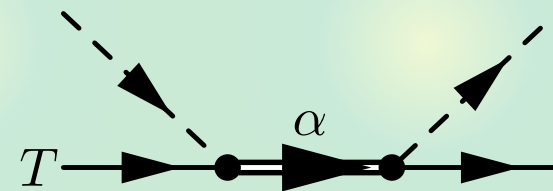
$\alpha = [p+2, q-1] : C_{\alpha,T} = 1 - p$

attraction : $p = 0$ then $\nu_T \geq 0 \rightarrow B \leq -q/3$ **not considered here**

○ $\Delta\epsilon = 1, \Delta\nu = -1, \nu_T \leq 0,$

$\alpha = [p-1, q+2] : C_{\alpha,T} = 1 - q$

attraction : $q = 0$ then $\nu_T \leq 0 \rightarrow B \geq p/3$ **OK!**



Universal attraction for more “exotic” channel

$$C_{\text{exotic}} = 1 \quad \text{for} \quad T = [p, 0], \quad \alpha = [p-1, 2]_{20}$$

Renormalization and bound states

Solve the scattering problem with $V_\alpha = -\frac{\omega}{2f^2} C_{\alpha,T}$

$$T = \frac{1}{1 - VG} V$$

Unitarity : OK

Renormalization parameter : condition

$$G(\mu) = 0, \quad \Leftrightarrow \quad T(\mu) = V(\mu) \quad \text{at} \quad \mu = M_T$$

K. Igi, and K. Hikasa, *Phys. Rev. D* **59**, 034005 (1999)

M.F.M. Lutz, and E. Kolomeitsev, *Nucl. Phys. A* **700**, 193-308 (2002)

Matching with the u-channel amplitude : OK

Bound state:

$$1 - V(M_b)G(M_b) = 0 \quad M_T < M_b < M_T + m_{21}$$

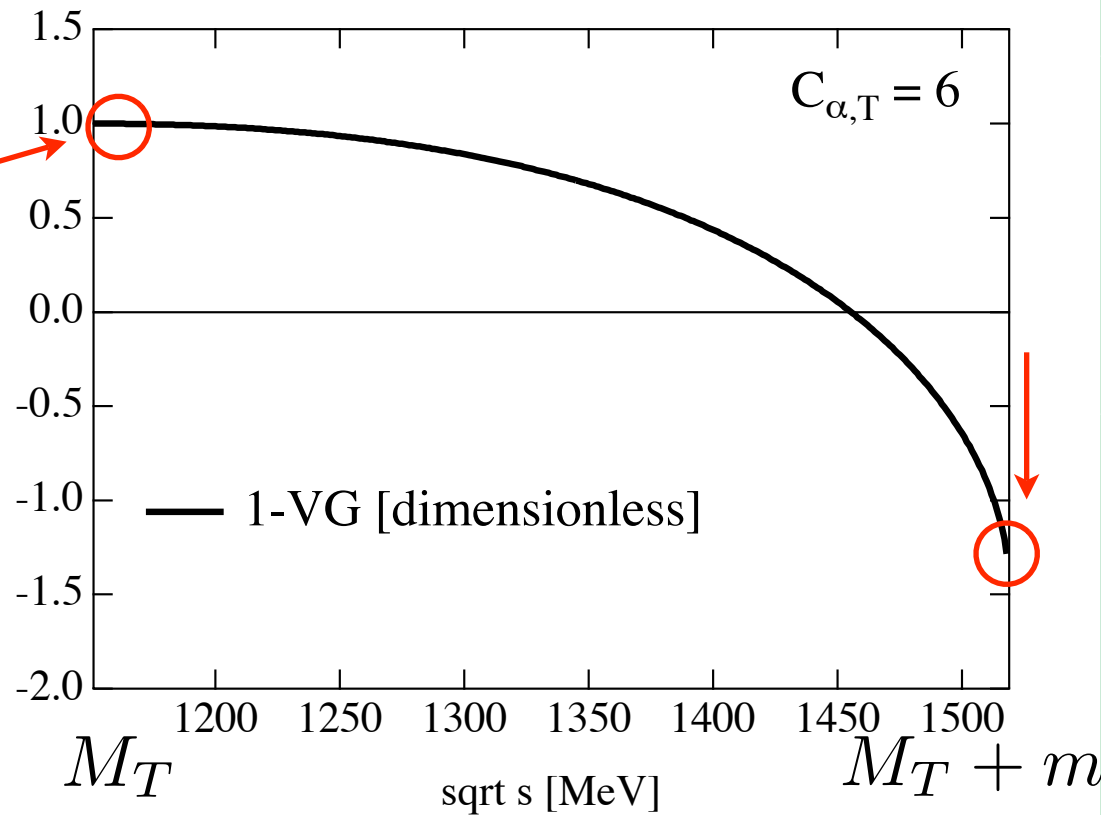
Critical attraction

$1 - V(\sqrt{s})G(\sqrt{s})$: monotonically decreasing.

Fixed

$$G(M_T) = 0$$

$$1 - VG = 1$$

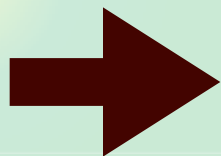
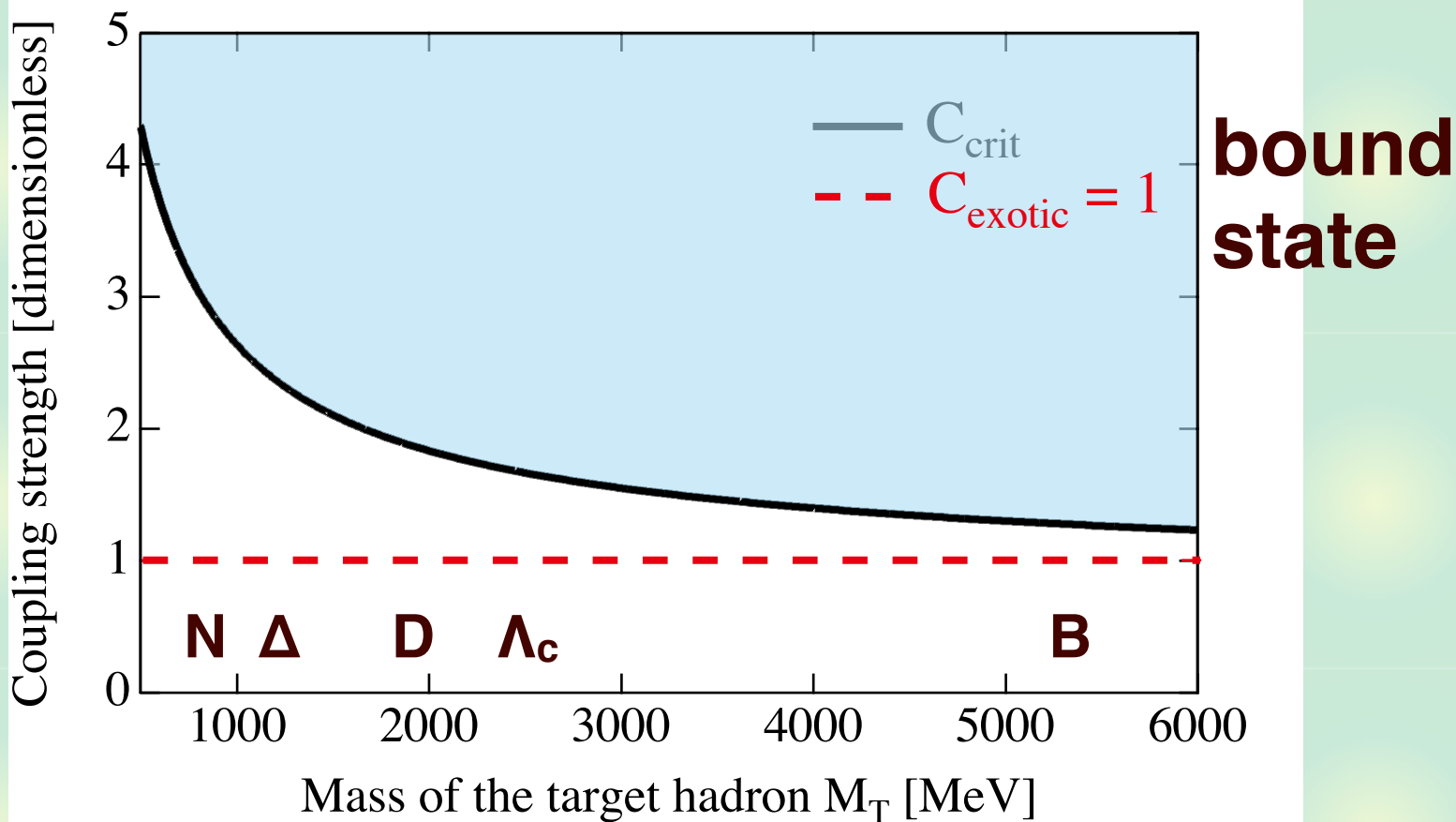


Critical attraction : $1 - VG = 0$ at $\sqrt{s} = M_T + m$

$$C_{\text{crit}} = \frac{2f^2}{m(-G(M_T + m))}$$

Critical attraction and exotic channel

$$m = 368 \text{ MeV} \text{ and } f = 93 \text{ MeV}$$



Strength is not enough.

Large N_c limit : introduction

$1/N_c$: a possible expansion parameter

G. 't Hooft, Nucl. Phys. B72, 461 (1974)

E. Witten, Nucl. Phys. B160, 57 (1979)

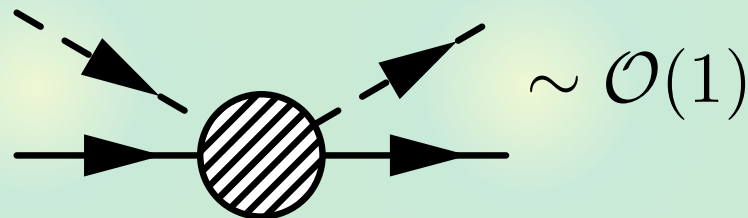
Scaling of the physical quantities
 ← N_c^2 gluons and N_c quarks.

Meson mass : $m \sim \mathcal{O}(1)$

Baryon mass : $M \sim \mathcal{O}(N_c)$

Decay constant : $f \sim \mathcal{O}(\sqrt{N_c})$

MB scattering :



Coupling strengths in large N_c limit

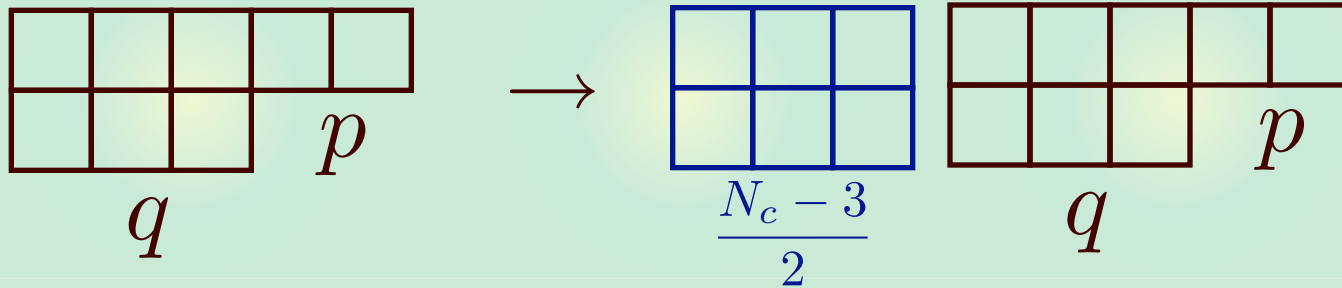
WT interaction in large N_c limit

$$V_\alpha = -\frac{\omega}{2f^2} C_{\alpha,T} \sim \frac{1}{N_c} \times C_{\alpha,T}$$

Flavor representation

$$[p, q] \rightarrow \left[p, q + \frac{N_c - 3}{2} \right]$$

$$C_2(T) - C_2(\alpha) + 3$$



$$C \left(\left[p, q + \frac{N_c - 3}{2} \right] \right) = \frac{1}{3} \left(-\frac{9}{4} + p^2 + \frac{3p}{2} + pq + q^2 \right) + \frac{1}{3} \left(\frac{p}{2} + q \right) N_c + \frac{N_c^2}{12}$$

Non-trivial N_c dependence

Coupling strengths for the general target

For arbitrary N_c ,

$$V \propto -\frac{1}{f^2} C \sim \frac{1}{N_c} C(N_c)$$

α	$C^{\text{"}\alpha\text{"}, \text{"}T\text{"}}(N_c)$	$V(N_c \rightarrow \infty)$	ΔE
$[p + 1, q + 1]$	$(3 - N_c)/2 - p - q$	repulsive	1 or 0
$[p + 2, q - 1]$	$1 - p$	0	1 or 0
$[p - 1, q + 2]$	$(5 - N_c)/2 - q$	repulsive	1 or 0
$[p, q]$	3	0	0
$[p, q]$	3	0	0
$[p + 1, q - 2]$	$(3 + N_c)/2 + q$	attractive	0 or -1
$[p - 2, q + 1]$	$3 + p$	0	0 or -1
$[p - 1, q - 1]$	$(5 + N_c)/2 + p + q$	attractive	0 or -1

- **Exotic attraction --> repulsion**
- **No attraction in exotic channels.**

Different large N_c extensions

There are different ways for N_c extension :

Dulinski, Acta Phys. Polon. B19, 891 (1988)

Praszalowicz, Talk at YKIS2006

$$[p, q] \rightarrow \left[p, q + \frac{N_c - 3}{2} \right]$$

$$[p, q] \rightarrow \left[p + \frac{N_c - 3}{3}, q + \frac{N_c - 3}{3} \right]$$

$$[p, q] \rightarrow [p + N_c - 3, q]$$

- **No attraction exists in exotic channels for all extensions.**

Coupling strengths in large N_c limit

C_α with arbitrary N_c : (positive is attractive)

α	“1”	“8”	“10”	“ $\bar{10}$ ”	“27”	“35”
$T=$ “8”	$\frac{9}{2} + \frac{N_c}{2}$	3	0	$\frac{3}{2} - \frac{N_c}{2}$	$-\frac{1}{2} - \frac{N_c}{2}$	
$T=$ “10”	<div style="border: 1px solid black; padding: 5px; color: blue; font-weight: bold;"> $\Lambda(1405)$ two-pole? </div>		3		$\frac{5}{2} - \frac{N_c}{2}$	$-\frac{1}{2} - \frac{N_c}{2}$

α	“ $\bar{3}$ ”	“6”	“ $\bar{15}$ ”	“24”
$T=$ “ $\bar{3}$ ”	3	1	$-\frac{N_c}{3}$	
$T=$ “6”	5	3	$\frac{5}{2} - \frac{N_c}{2}$	$\frac{1}{2} - \frac{5N_c}{6}$

Attraction
-> repulsion

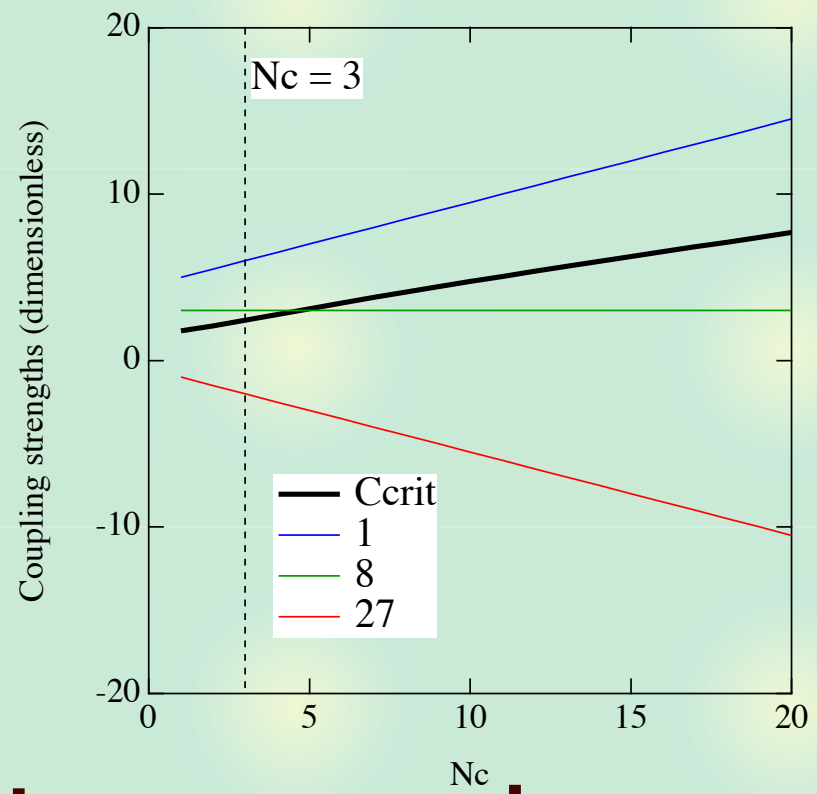
$S = -1$ $I = 0$ channel in $SU(3)$ basis

α	“1”	“8”	“8”	“27”
T=“8”	$\frac{9}{2} + \frac{N_c}{2}$	3	3	$-\frac{1}{2} - \frac{N_c}{2}$

$$C_{\text{crit}}(N_c) = \frac{2[f(N_c)]^2}{m[-G(M_T(N_c) + m)]}$$

$$M_T(N_c) = M_0 \times \frac{N_c}{3}$$

$$f(N_c) = f_0 \times \sqrt{\frac{N_c}{3}}$$



○ **Attraction in “1” is strong enough.**

S = -1 I = 0 channel in Isospin basis

Basis transformation via CG Coef. with Nc

T.D. Cohen, and R.F. Lebed, Phys. Rev. D 70, 096015 (2004)

$$C_{ij}(N_c) = \begin{pmatrix} \bar{K}N & \pi\Sigma & \eta\Lambda & K\Xi \\ \frac{1}{2}(3 + N_c) & -\frac{\sqrt{3}}{2}\sqrt{-1 + N_c} & \frac{\sqrt{3}}{2}\sqrt{3 + N_c} & 0 \\ -\frac{\sqrt{3}}{2}\sqrt{-1 + N_c} & 4 & 0 & \frac{\sqrt{3 + N_c}}{2} \\ \frac{\sqrt{3}}{2}\sqrt{3 + N_c} & 0 & 0 & -\frac{\sqrt{3}}{2}\sqrt{-1 + N_c} \\ 0 & \frac{\sqrt{3 + N_c}}{2} & -\frac{\sqrt{3}}{2}\sqrt{-1 + N_c} & \frac{1}{2}(9 - N_c) \end{pmatrix}$$

Combining with the 1/Nc factor of 1/f²,

- $\bar{K}N \rightarrow \bar{K}N$: attractive at large Nc
- $\bar{K}N \rightarrow \pi\Sigma$: $\mathcal{O}(1/\sqrt{N_c})$
- $\pi\Sigma \rightarrow \pi\Sigma$: $\mathcal{O}(1/N_c)$




Summary 1 : SU(3) limit

We study the **exotic bound states** in **s-wave** chiral dynamics in flavor SU(3) limit.

- The interaction in exotic channels are in most cases **repulsive**.
- There are **attractive interactions** in exotic channels, with **universal** and the smallest strength : $C_{\text{exotic}} = 1$
- The strength is **not enough** to generate a bound state : $C_{\text{exotic}} < C_{\text{crit}}$
- **No attractive interaction exists** in exotic channels in the large N_c limit.

Summary 2 : Physical world

Caution!

-  The exotic hadrons here are the **s-wave** meson-hadron molecule states ($1/2^-$ for Θ^+).
-  We do not exclude the exotics which have **other origins** (genuine quark state, soliton rotation,...)
-  In practice, **SU(3) breaking** effect, **higher order** terms,...

It is **difficult** to generate exotic hadrons as in the same way with $\Lambda(1405)$, $\Lambda(1520)$,... based on chiral dynamics.

[T. Hyodo, D. Jido, A. Hosaka, Phys. Rev. Lett. 97, 192002 \(2006\)](#)

[T. Hyodo, D. Jido, A. Hosaka, Phys. Rev. D 75, 034002 \(2007\)](#)