

Energy and width of a narrow $l=1/2$ DNN quasibound state



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Introduction



DN interaction and $\Lambda_c(2595)$



DNN quasi-bound state

- Variational calculation with DN potential
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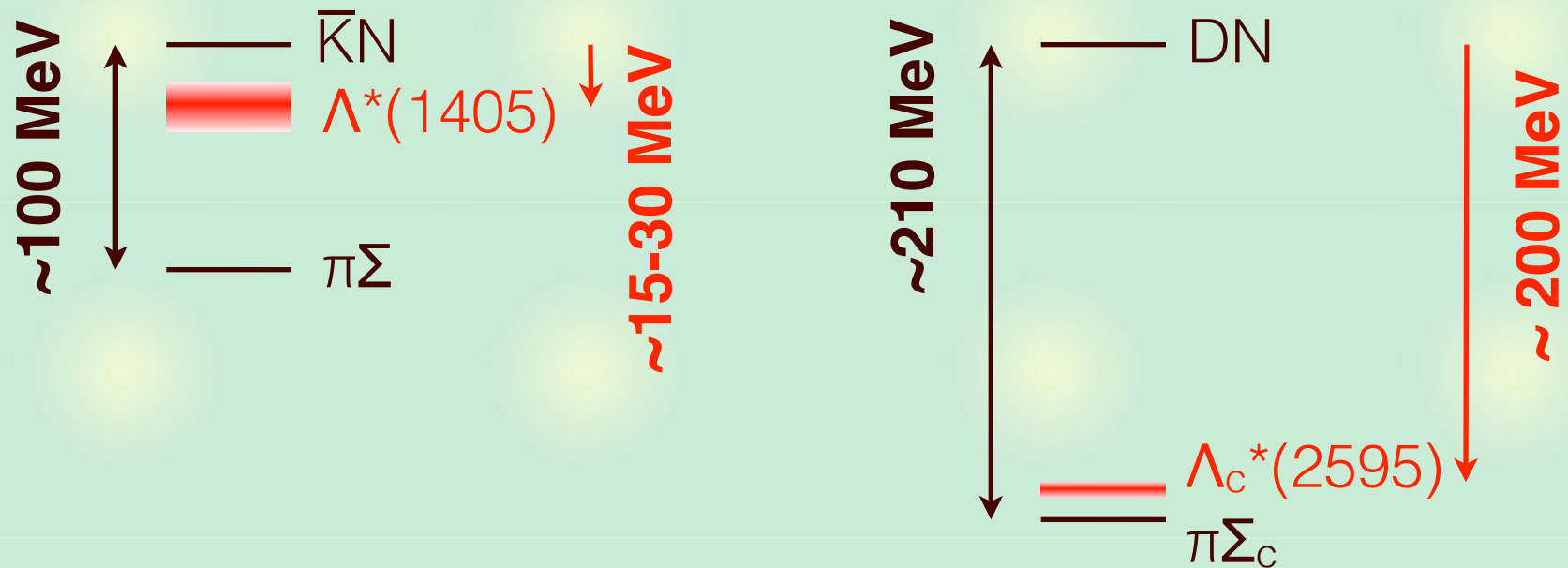
Summary

Why DN and DNN?

\bar{K} nuclei $\leftarrow \Lambda^*$: a $\bar{K}N$ bound state in the $\pi\Sigma$ continuum

D nuclei? $\leftarrow \Lambda_c^*$: a DN bound state in the $\pi\Sigma_c$ continuum

Comparison with $\bar{K}N$ system in $l=0$ channel



- narrow negative parity Λ_c^* , analogous to $\Lambda(1405)$?

(conventional view : $\Lambda_c^* \sim 3$ -quark state
200 MeV binding : too large?)

DN bound state picture ?

Can Λ_c^* (with large binding) be a DN quasi-bound state?

- Vector meson exchange picture leads to a **stronger** DN interaction than $\bar{K}N$ (at threshold)

$$\frac{V_D}{V_K} = \frac{m_D}{m_K} \sim 3.8 \quad (\text{next slide})$$

- D (1867 MeV) is heavier than \bar{K} (496 MeV).
Kinetic energy is suppressed.
 If the DN interaction were the same with $\bar{K}N$,
 system would develop a deeper quasi-bound state.

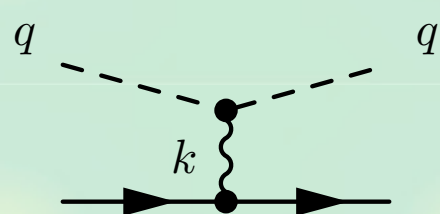
DN system can generate a **strongly bound state: Λ_c^* .**

$$B_{DN} > B_{\bar{K}N} = 15\text{-}30 \text{ MeV}$$

Vector meson exchange for DN

DN ($\bar{K}N$) interaction in vector meson exchange (low energy)

$$V \sim g \bar{u} \gamma^\mu u \times \frac{1}{k^2 - m_v^2} \left[g_{\mu\nu} - \frac{k_\mu k_\nu}{m_v^2} \right] \times g (q + q')^\nu$$

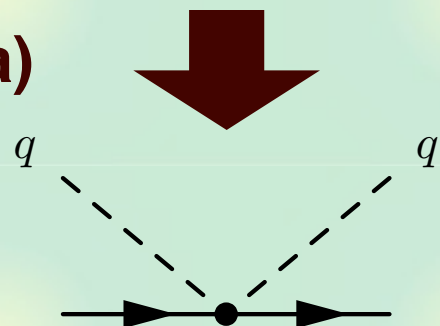


- $k \ll m_v$ + KSRF relation

$$\rightarrow -\frac{1}{2f^2} (q^0 + q'^0) \quad \text{(Weinberg-Tomozawa)}$$

- at threshold

$$\rightarrow -\frac{m}{f^2} \quad \text{(at threshold)}$$



Interaction in DN- $\pi\Sigma_c$ system (J/ Ψ exchange ignored)

$$V \sim \begin{pmatrix} \boxed{-3m_D} & \sqrt{\frac{3}{2}} \boxed{\kappa_c} \frac{m_D + m_\pi}{2} \\ \sqrt{\frac{3}{2}} \boxed{\kappa_c} \frac{m_D + m_\pi}{2} & -4m_\pi \end{pmatrix}$$

$$\boxed{\kappa_c \sim \frac{m_{K^*}^2}{m_{D^*}^2} \sim \frac{1}{4}}$$

- strong DN interaction --> large binding energy

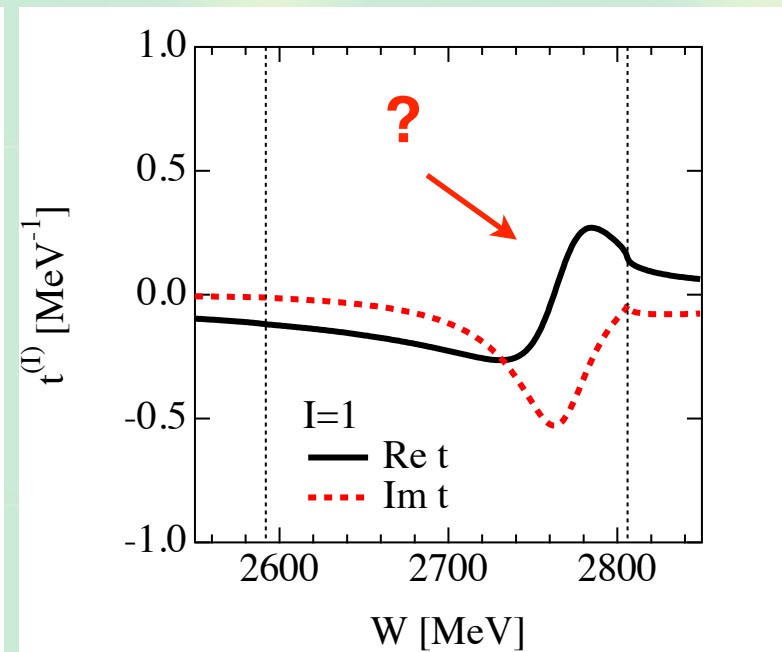
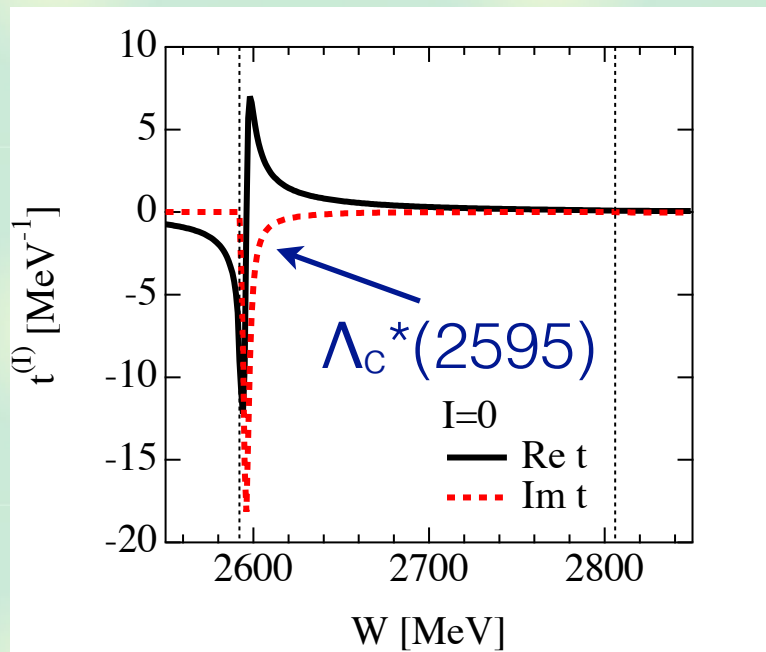
- suppressed off-diagonal coupling --> narrow width of Λ_c^*

DN scattering amplitude

Coupled-channel DN ($\pi\Sigma_c$, $\eta\Lambda_c$, $K\Xi_c$, $K\Xi_c'$, $D_s\Lambda$, $\eta'\Lambda_c$) scattering

see T. Mizutani, A. Ramos, *Phys. Rev. C* **74**, 065201 (2006)

Subtraction constants (cutoff parameters) are chosen to reproduce Λ_c^* in $l=0$. Apply the same constants to $l=1$.



A resonance at ~ 2760 MeV is generated in $l=1$ channel.
c.f. PDG 1*: $\Lambda_c(2765)$ or $\Sigma_c(2765)$??

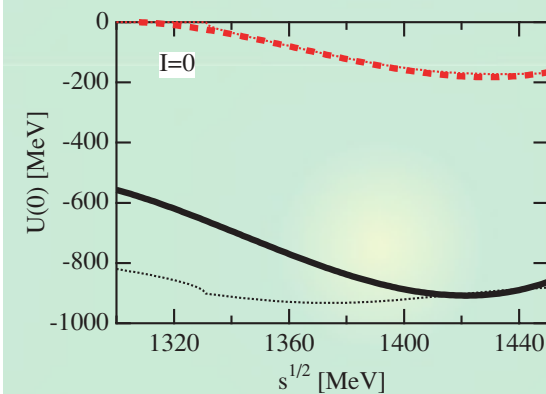
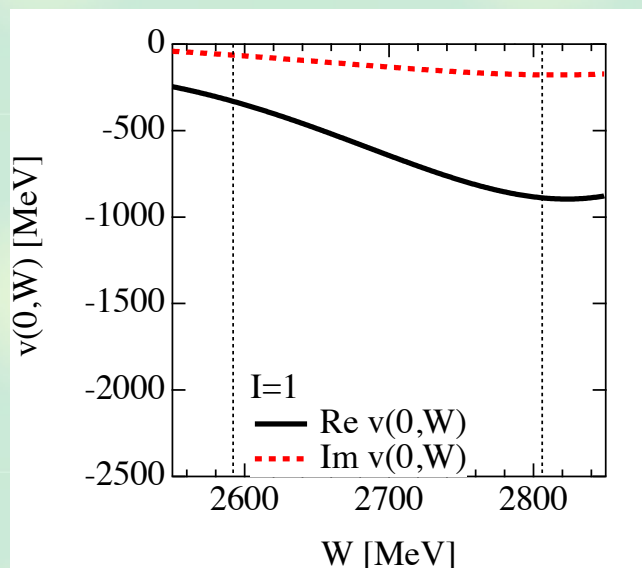
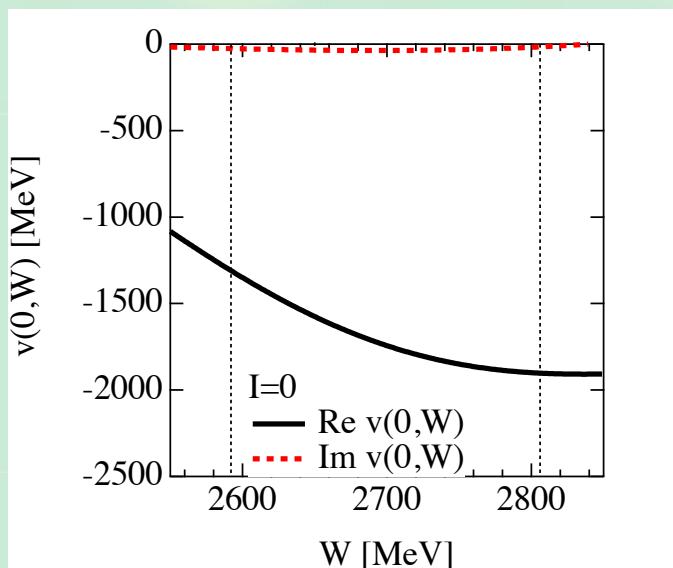
DN local potential

Equivalent single-channel local potential

T. Hyodo, W. Weise, Phys. Rev. C77, 035204 (2008)

$$v_{DN}(r; W) = \frac{M_N}{2\pi^{3/2} a_s^3 \tilde{\omega}(W)} [v^{\text{eff}}(W) + \Delta v(W)] \exp[-(r/a_s)^2]$$

- reproduces the coupled channel amplitude



c.f. $\bar{K}N$ case

- This potential reproduces the DN amplitude in CC model.
- Larger (smaller) real (imaginary) part than $\bar{K}N$

Strategy for DNN bound state

Coupled-channel model
DN amplitude, $\Lambda_c(2595)$

DN single-channel potential

↓ real part

Three-body variational calculation

- Structure from wave function
- NN dynamics is dynamically solved.

Coupled-channel ($\pi Y_c N$) effect is partly included.

Assume NN distribution

Fixed-center approximation to Faddeev equation

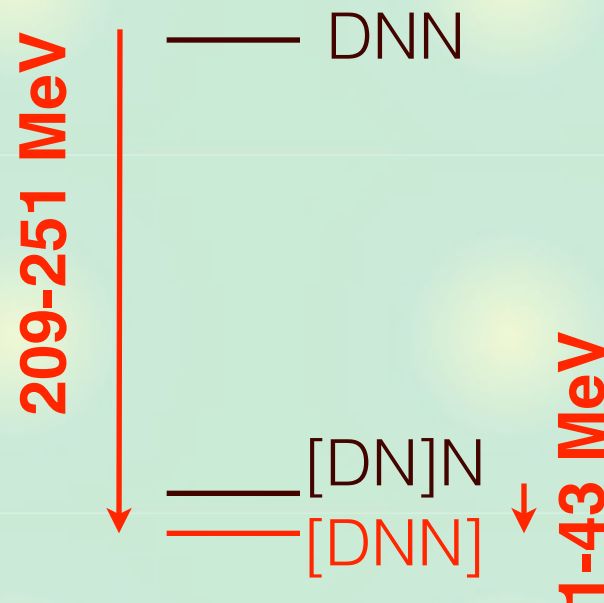
- Two-body absorption
- Imaginary part of the amplitude is treated.

Variational calculation: results

Results of the DNN system

- $J=0$ bound, $J=1$ unbound w.r.t. $[DN]N$
- mesonic decay width is small
- softer the core, larger the binding

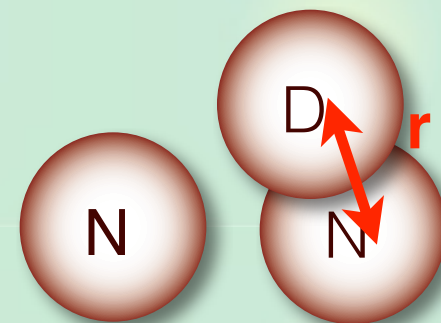
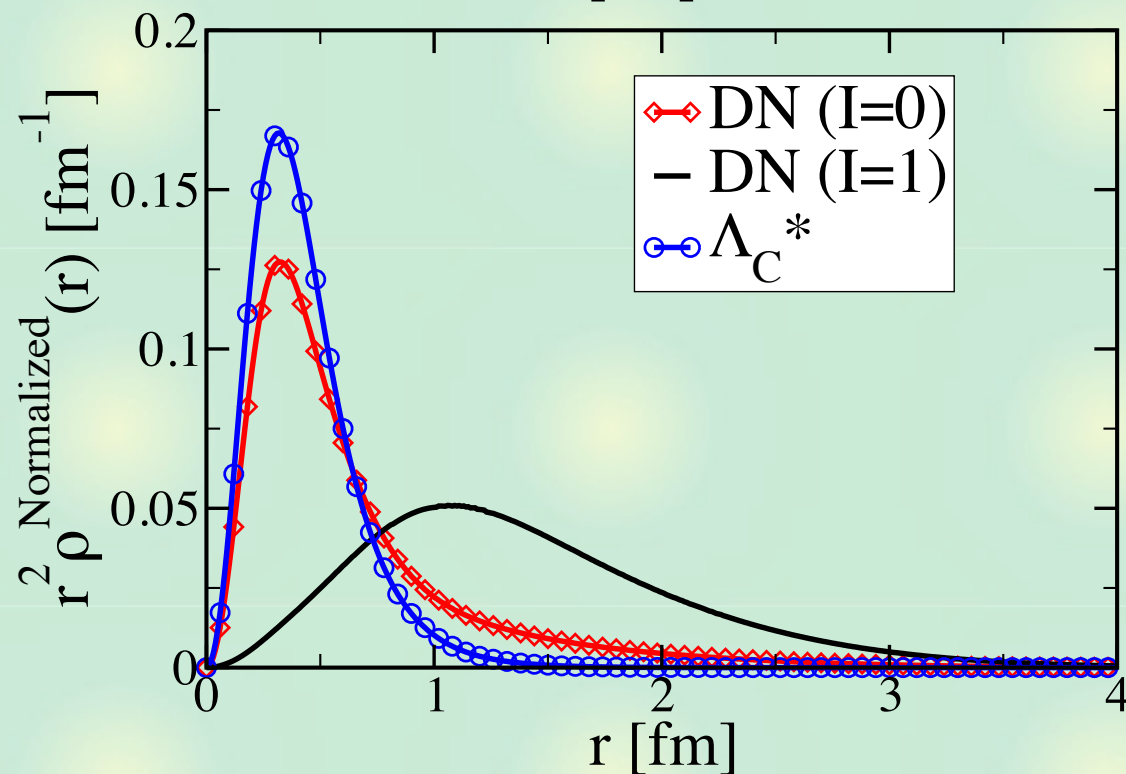
	HN1R	Minnesota	Av18
	$J = 1$	$J = 0$	$J = 0$
	unbound	bound	bound
B	208	225	209
M_B	3537	3520	3494
$\Gamma_{\pi Y_c N}$	-	26	38
E_{kin}	338	352	438
$V(NN)$	0	-2	19
$V(DN)$	-546	-575	-708
T_{nuc}	113	126	162
E_{NN}	113	124	181
$P(\text{Odd})$	75.0 %	14.4 %	7.4 %



Variational calculation: DN correlation

Isospin decomposition of DN two-body correlation

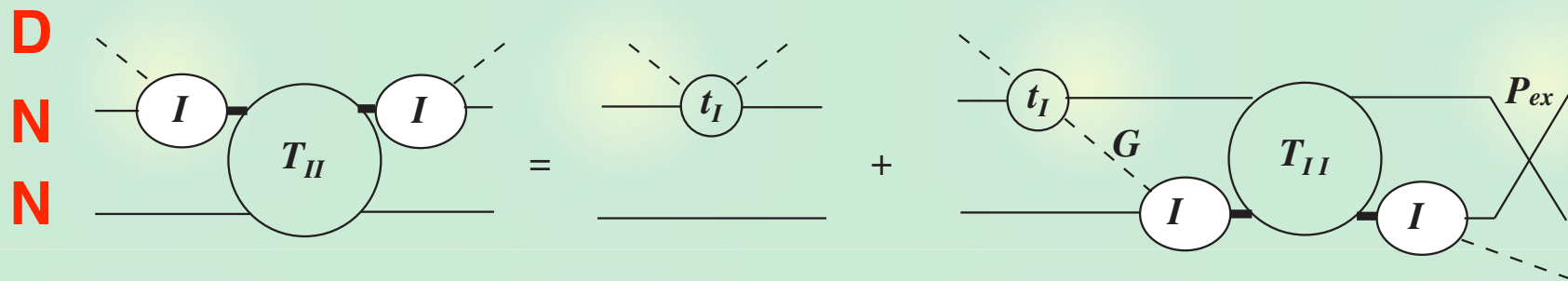
$$\rho_{DN}(r) = \langle \Psi | \sum_{i=1,2} \delta^3(|\mathbf{r}_D - \mathbf{r}_i| - r) | \Psi \rangle$$



DN ($I=0$) correlation is similar to Λ_C^*

FCA calculation

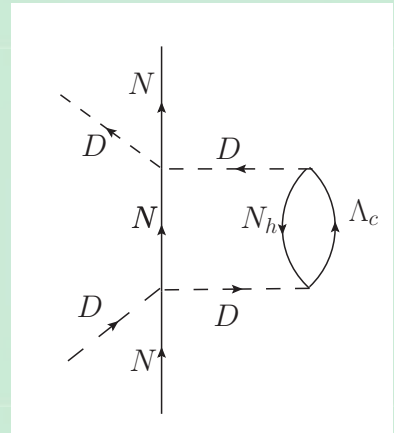
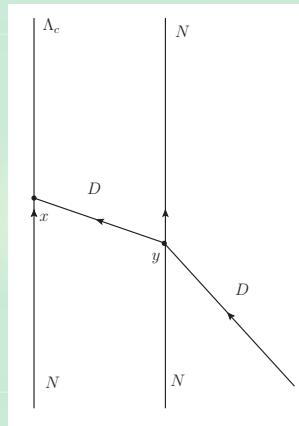
Fixed-center approximation to Faddeev equation



- **Complex DN amplitude**
- **all two-body pairs are in s-wave**
- **NN distribution is assumed**
(checked with the variational calculation result)

FCA calculation: two-body absorption

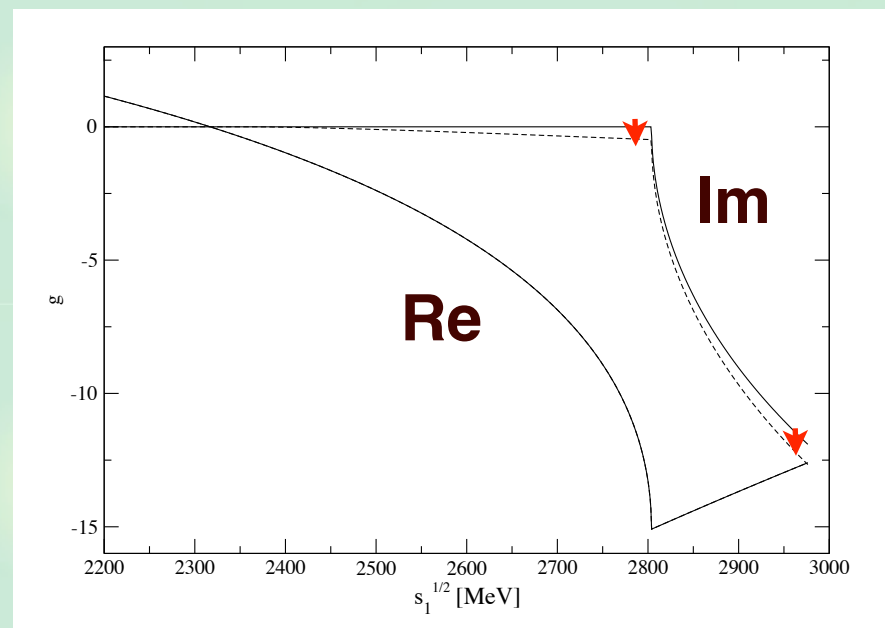
Two-body absorption --> imaginary part of DN amplitude



$$g_{DN} \rightarrow g_{DN} + i \text{Im } \delta \tilde{g}$$

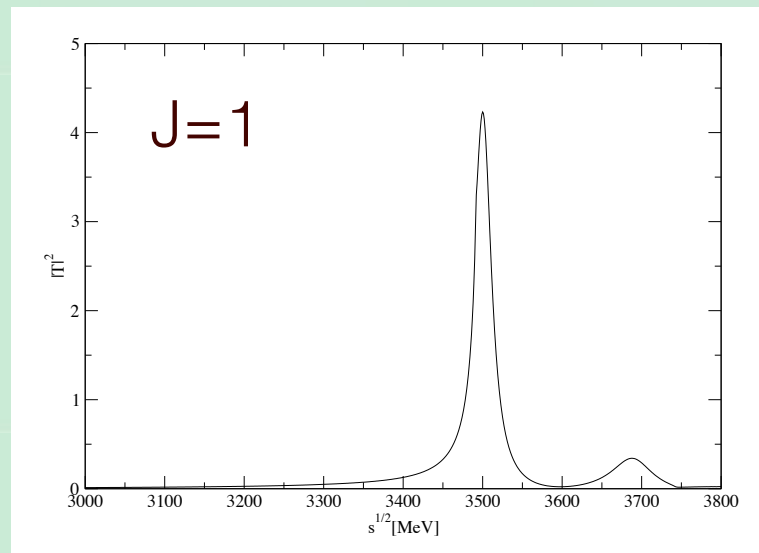
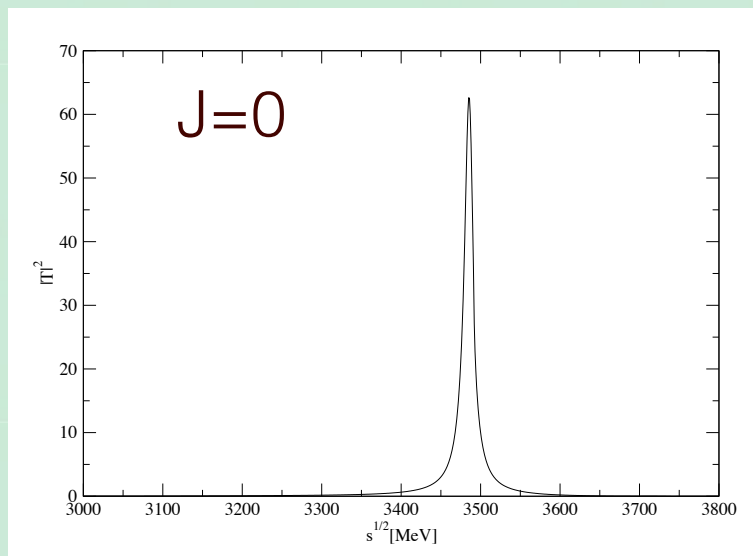
DN loop

two-body absorption contribution



FCA calculation: result

Magnitude of the three-body amplitude square



J=0 channel: $M \sim 3500$ MeV

- strong signal, consistent with the variational calculation

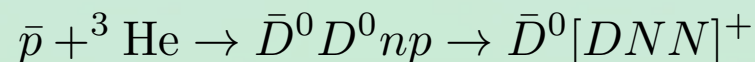
J=1 channel: $M \sim 3500$ MeV and $M \sim 3700$ MeV?

- weak signal, not found in the variational calculation??

- $l=1$ DN interaction is important for this channel.

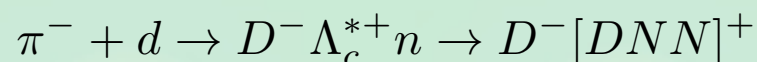
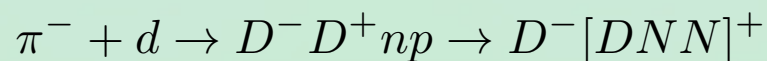
Possible experiments

Antiproton beam



- PANDA?

Pion beam



- J-PARC high momentum beamline?

Heavy Ion collision

Coalescence DNN (large binding), $\Lambda_c^* N$ (small binding)

- RHIC, LHC,...

Summary

We study DN interaction and DNN system

• DN interaction is constructed by regarding Λ_c^* as “DN quasi-bound state”.

• A narrow DNN quasi-bound state in spin $J=0$ and isospin $I=1/2$ channel.

$$B_{\text{DNN}} \sim 250 \text{ MeV}, \quad B_{\Lambda_c^* \text{N}} \sim 40 \text{ MeV}$$

$$\Gamma \sim 20\text{-}40 \text{ MeV}$$

• DN forms a compact cluster, but $\Lambda_c^* \text{N}$ bounds loosely.