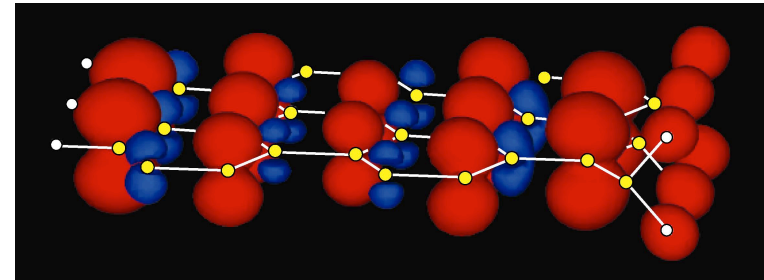




Osaka Univ.

# Possible nano-graphene device structures: A design and a simulation



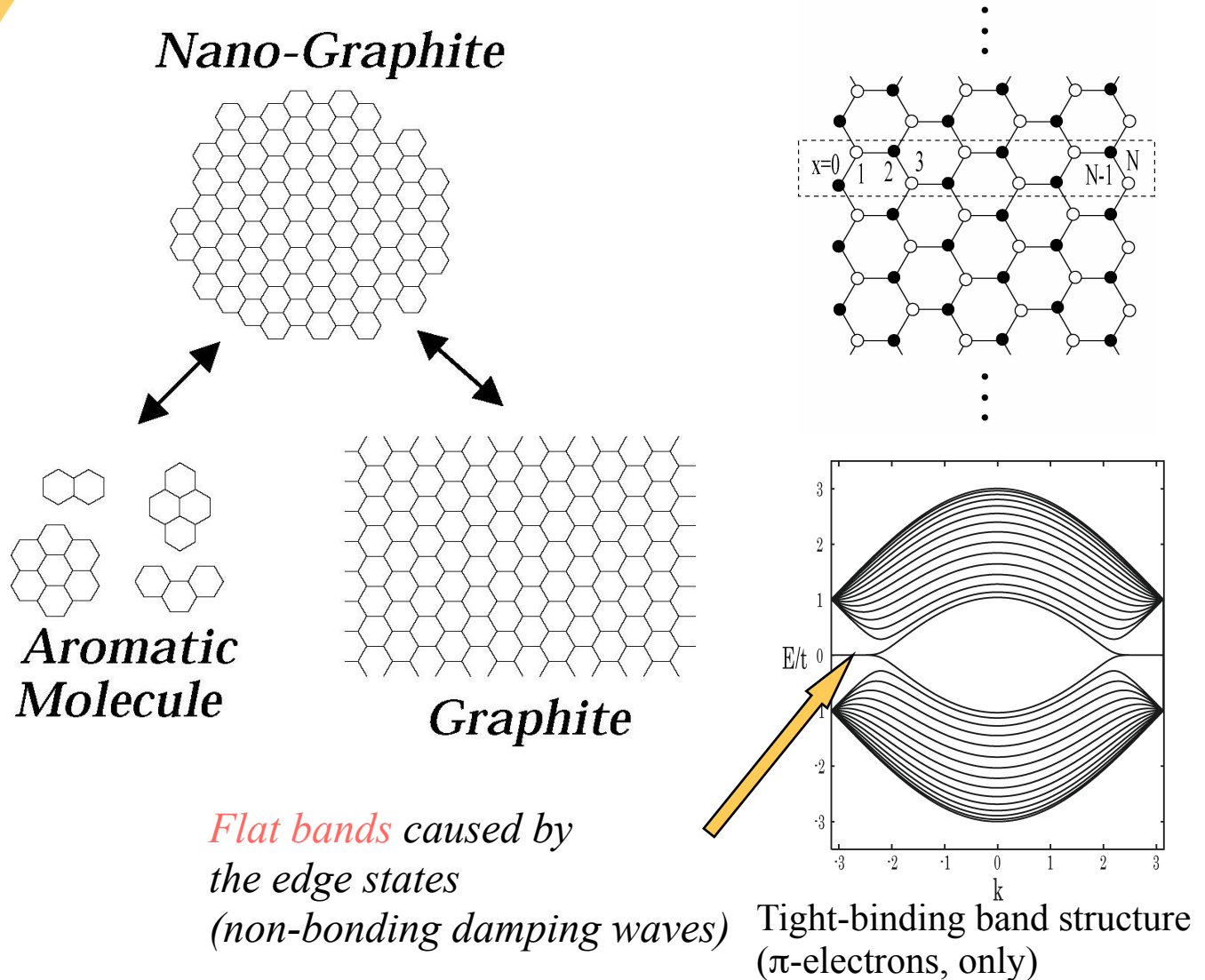
**Koichi Kusakabe**

The Graduate School of Engineering Science,

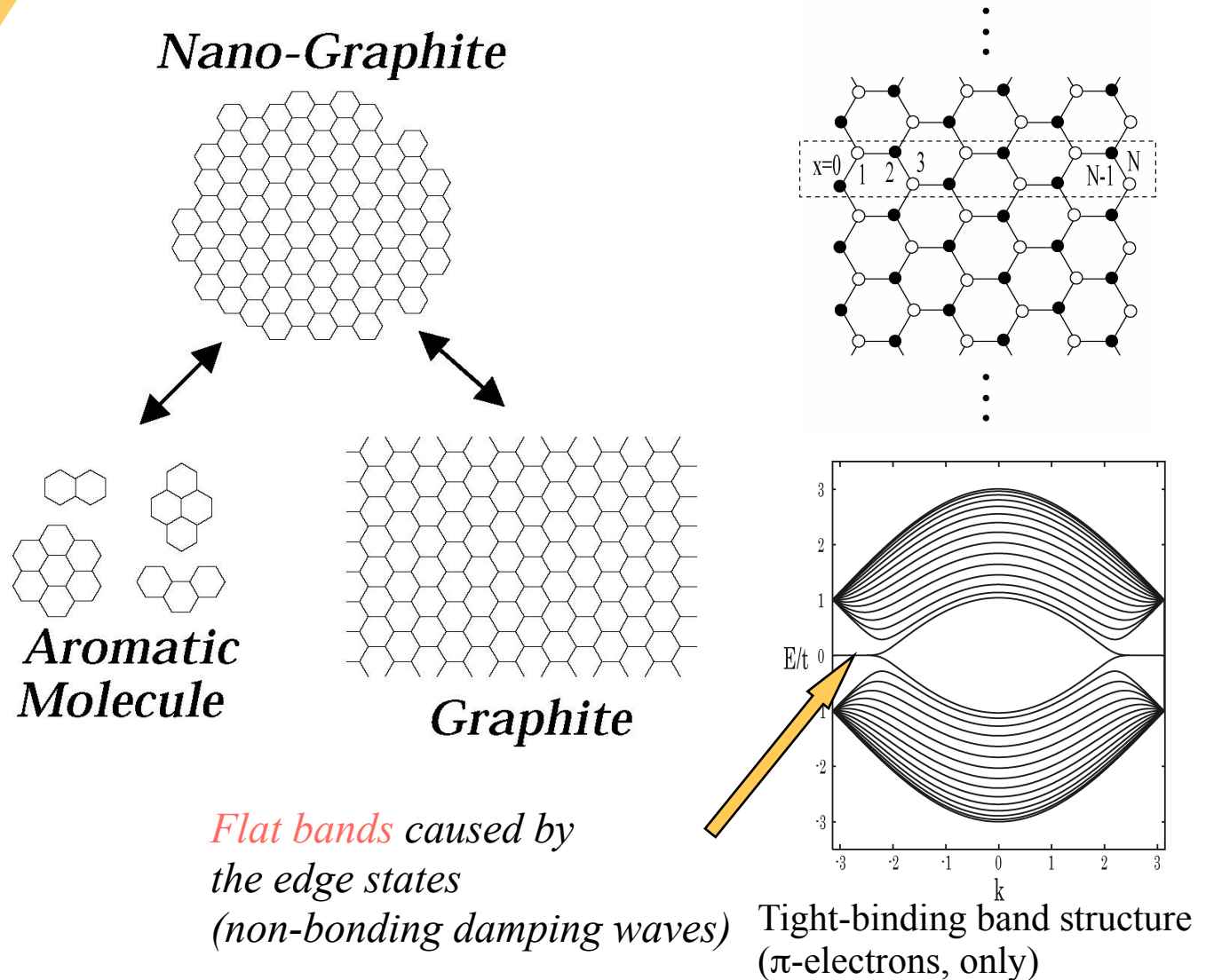
Osaka University,

1-3 Machikaneyama-cho, Toyonaka, Osaka 560-8531, Japan

# The nano-graphite: nanoscale graphene

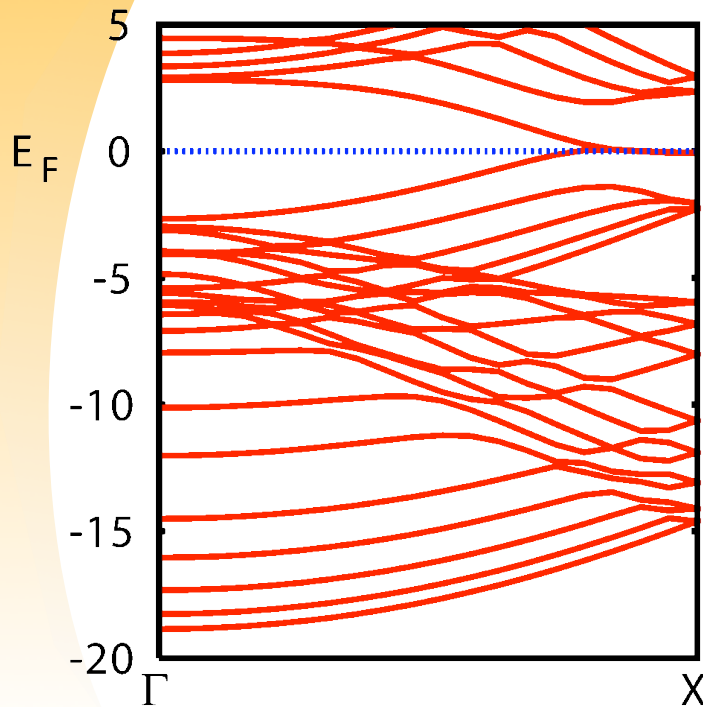


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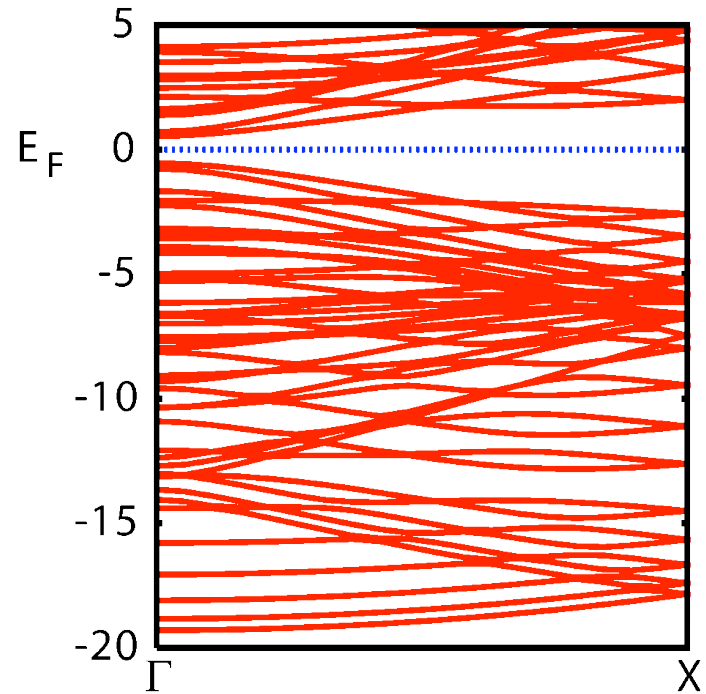


# Magnetic & non-magnetic edges

The DFT-LDA model tells that,



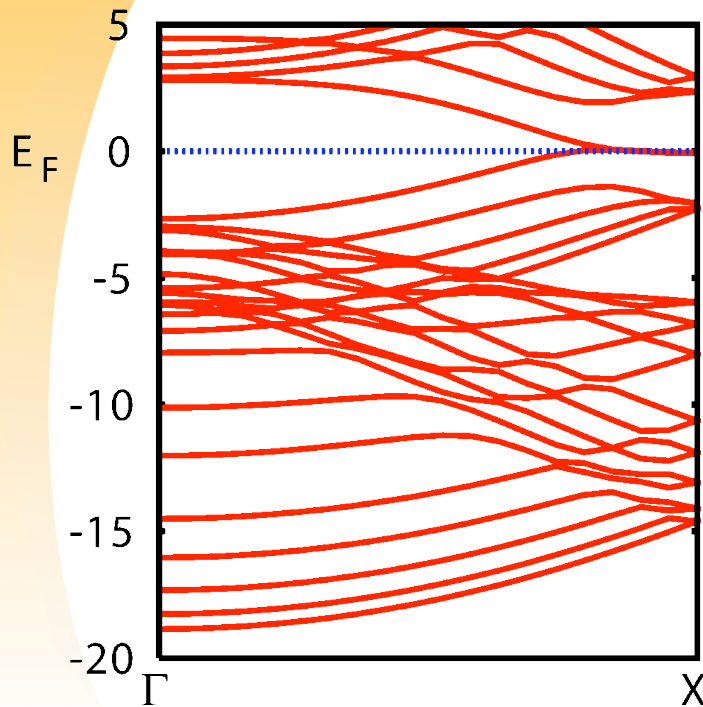
Hydrogen-terminated  
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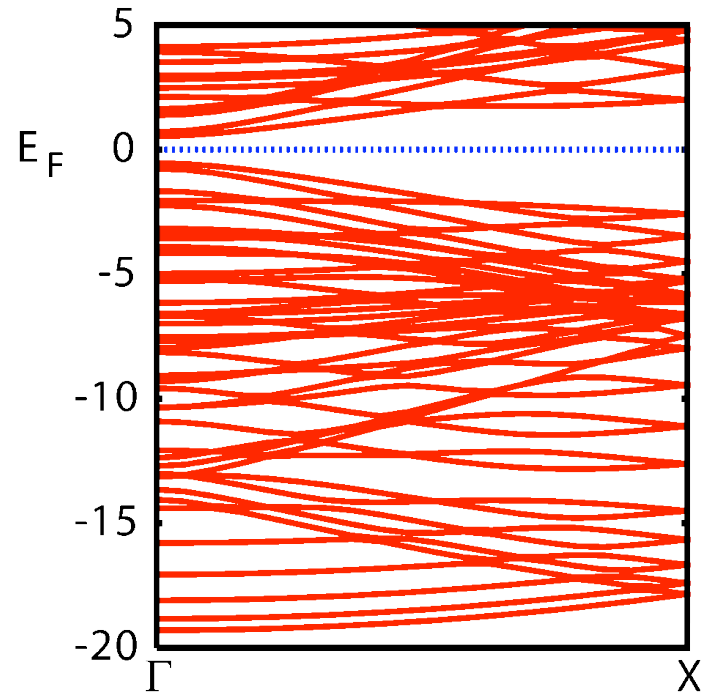
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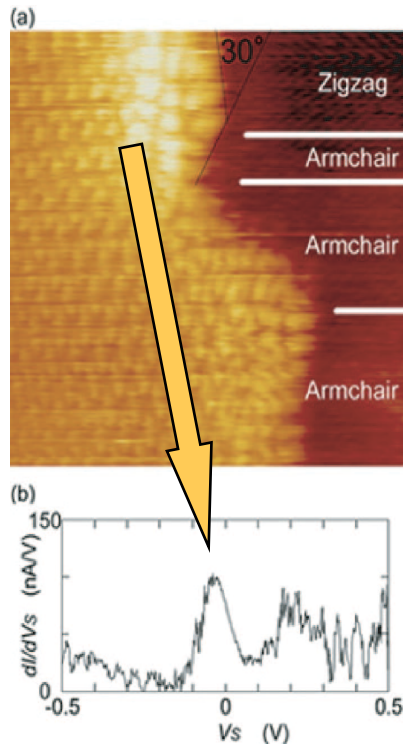
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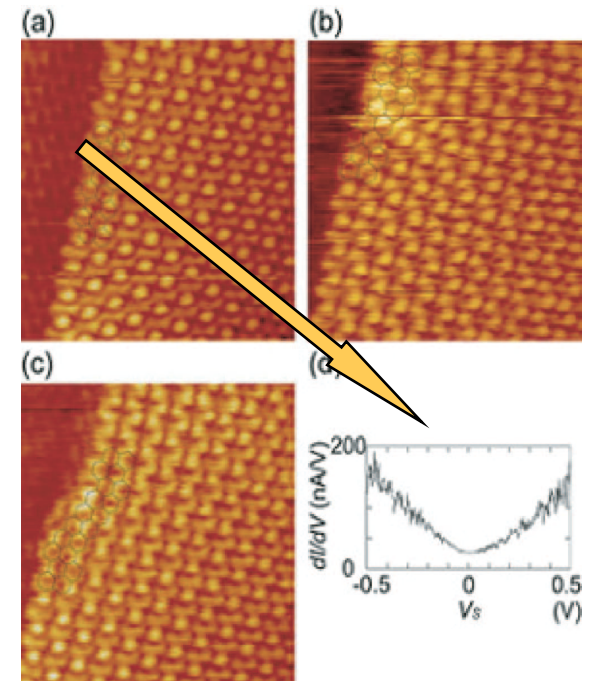
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STM & STS spectra of the zigzag edge



STM & STS spectra of the armchair edge

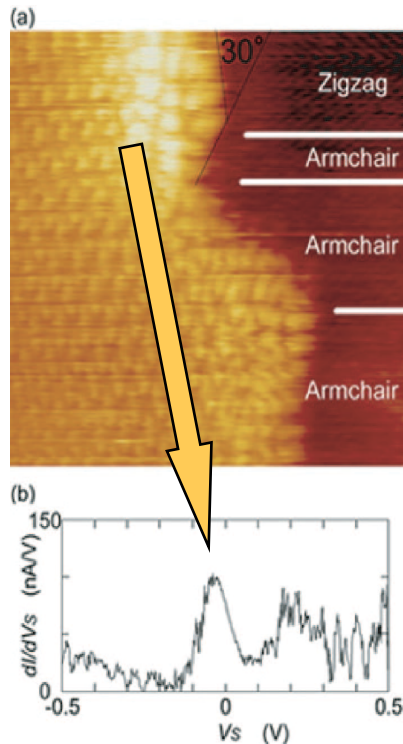


Existence of the edge state at the zigzag edge & non-existence of the state at the armchair edge are thus confirmed.

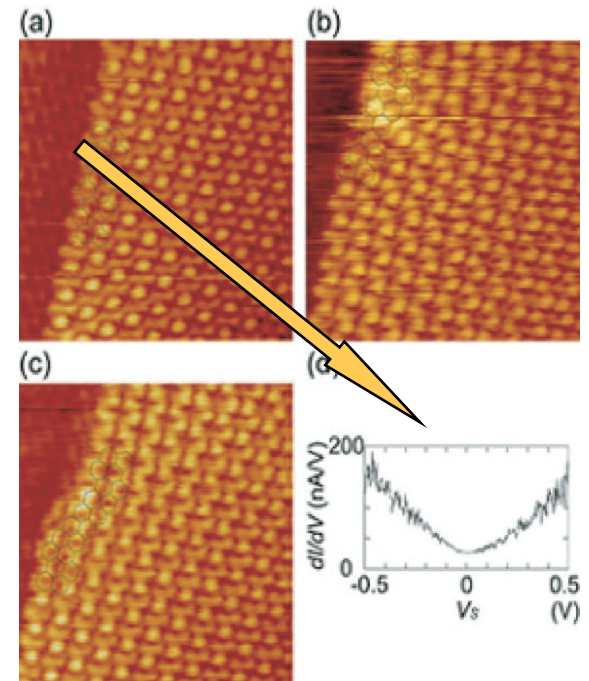
Y. Kobayashi et al., PRB 71 (2005) 193406.

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# Edge states & possible magnetism



Professor Mitsutaka Fujita  
(1959-1998)

Journal of the Physical Society of Japan  
Vol. 65, No. 7, July, 1996, pp. 1920-1923

LETTERS

## Peculiar Localized State at Zigzag Graphite Edge

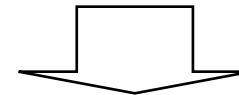
Mitsutaka FUJITA, Katsunori WAKABAYASHI, Kyoko NAKADA  
and Koichi KUSAKABE<sup>1</sup>

*Institute of Materials Science, University of Tsukuba, Tsukuba 305*  
<sup>1</sup>*Institute for Solid State Physics, University of Tokyo, Roppongi, Tokyo 106*

(Received April 30, 1996)

We study the electronic states of graphite ribbons with edges of two typical shapes, armchair and zigzag, by performing tight binding band calculations, and find that the graphite ribbons show striking contrast in the electronic states depending on the edge shape. In particular, a zigzag ribbon shows a remarkably sharp peak of density of states at the Fermi level, which does not originate from infinite graphite. We find that the singular electronic states arise from the partly flat bands at the Fermi level, whose wave functions are mainly localized on the zigzag edge. We reveal the puzzle for the emergence of the peculiar edge state by deriving the analytic form in the case of semi-infinite graphite with a zigzag edge. Applying the Hubbard model within the mean-field approximation, we discuss the possible magnetic structure in nanometer-scale micrographite.

KEYWORDS: edge state, micrographite, nanometer scale, flat band, localized state, graphite edge



The edge states, i.e. non-bonding surface states (zero modes) at the zigzag edges, may cause **localized magnetism** in graphitic structures, i.e. nano-graphite.

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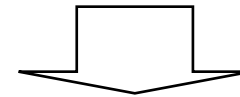
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**To reconfirm and to show the following issues by theoretical investigation of electron models.**

- **Nano-graphene : Electronic structure is affected by the shape of edges.**
  - Non-magnetic gapped, non-magnetic metallic.
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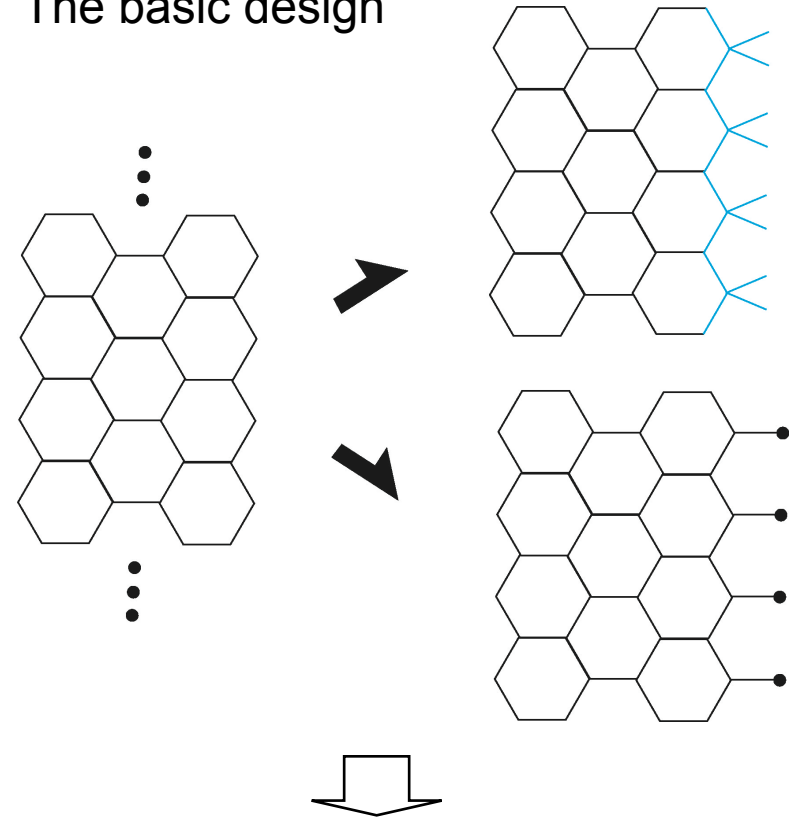
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- **Idea: Existence of flat-bands at  $E_F$  suggests magnetic instability.**
- **Strategy:  $\pi$ -topology**
- **Principle:**  
 $|N_A - N_B| > 0 \rightarrow S > 0$
- **Supporting facts:**
  - The Longuet-Higgins rule
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  - The Lieb theorem for the Hubbard model
  - The Shen, Qiu & Tian theorem for the ferrimagnetic RLO for the Hubbard model

The basic design



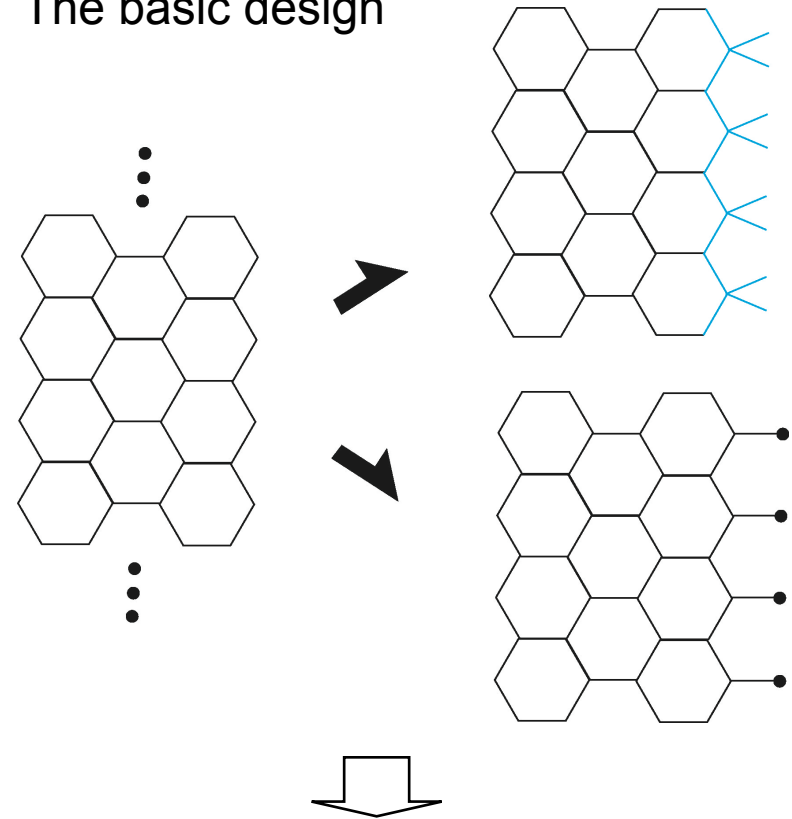
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- **All of available theoretical calculations are model calculations. We have a series of effective Hamiltonians approaching to the true Hamiltonian**
  - The tight-binding model without two-body terms
    - LCAO description
    - Non-interacting electron picture
  - The Hubbard model (the extended Hubbard model)
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  - The density-functional theory in the Kohn-Sham scheme
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Effective for  
Materials  
Design



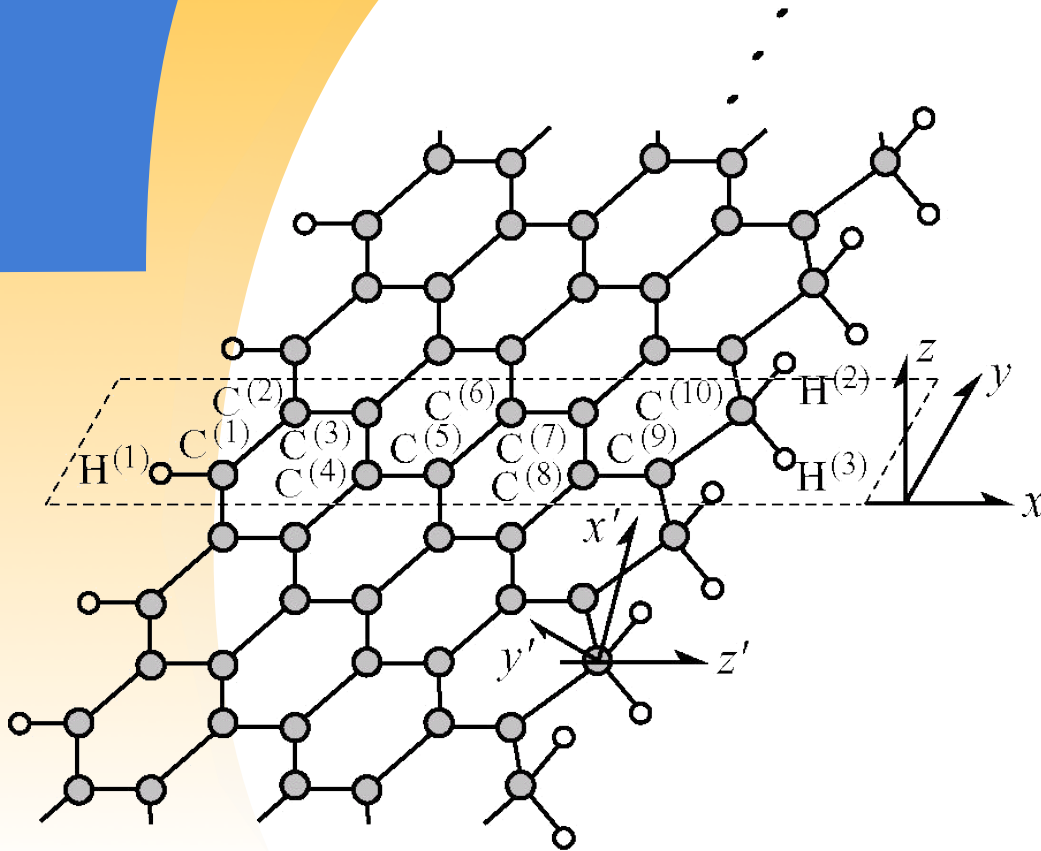
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# A graphene ribbon as a bipartite lattice

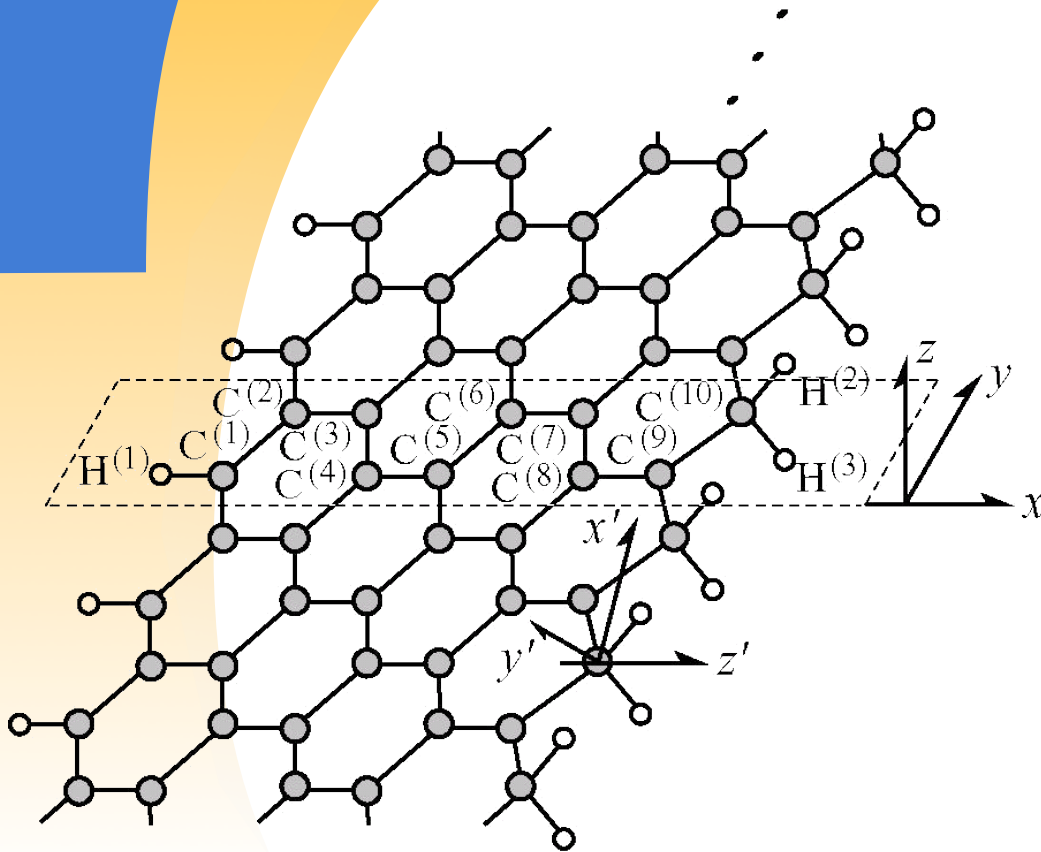


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# A flat-band Hubbard model

- Note that by making a linear combination of

$$\phi_1 = \phi_s + \phi_{x'} + \phi_{y'} + \phi_{z'}$$

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pointing to  $H^{(2)}$  and  $H^{(3)}$ , we have

$$\bar{\phi}_- = (\phi_1 - \phi_2)/\sqrt{2} = \phi_z.$$

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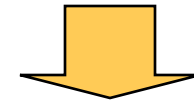
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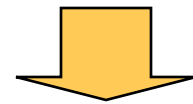
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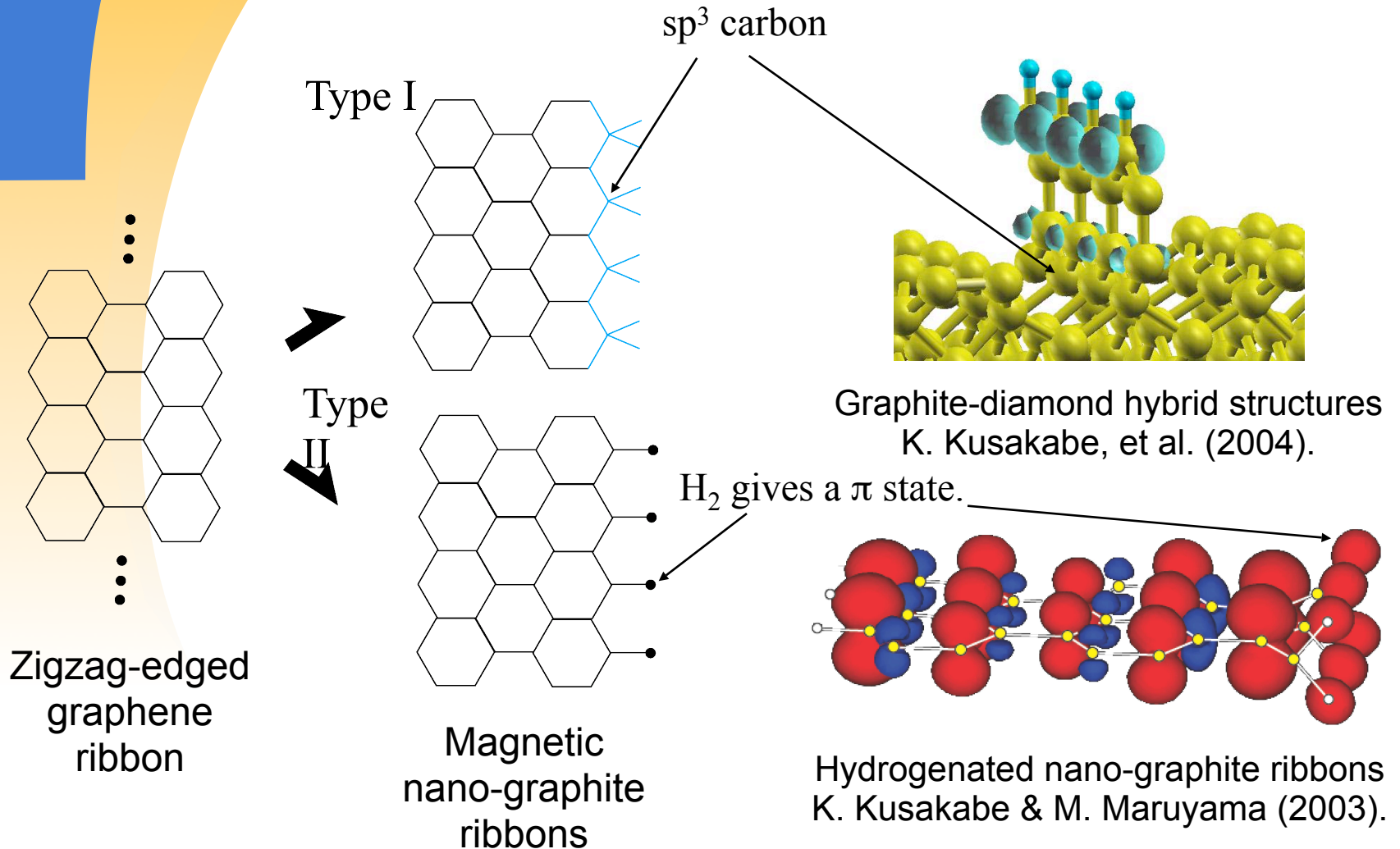
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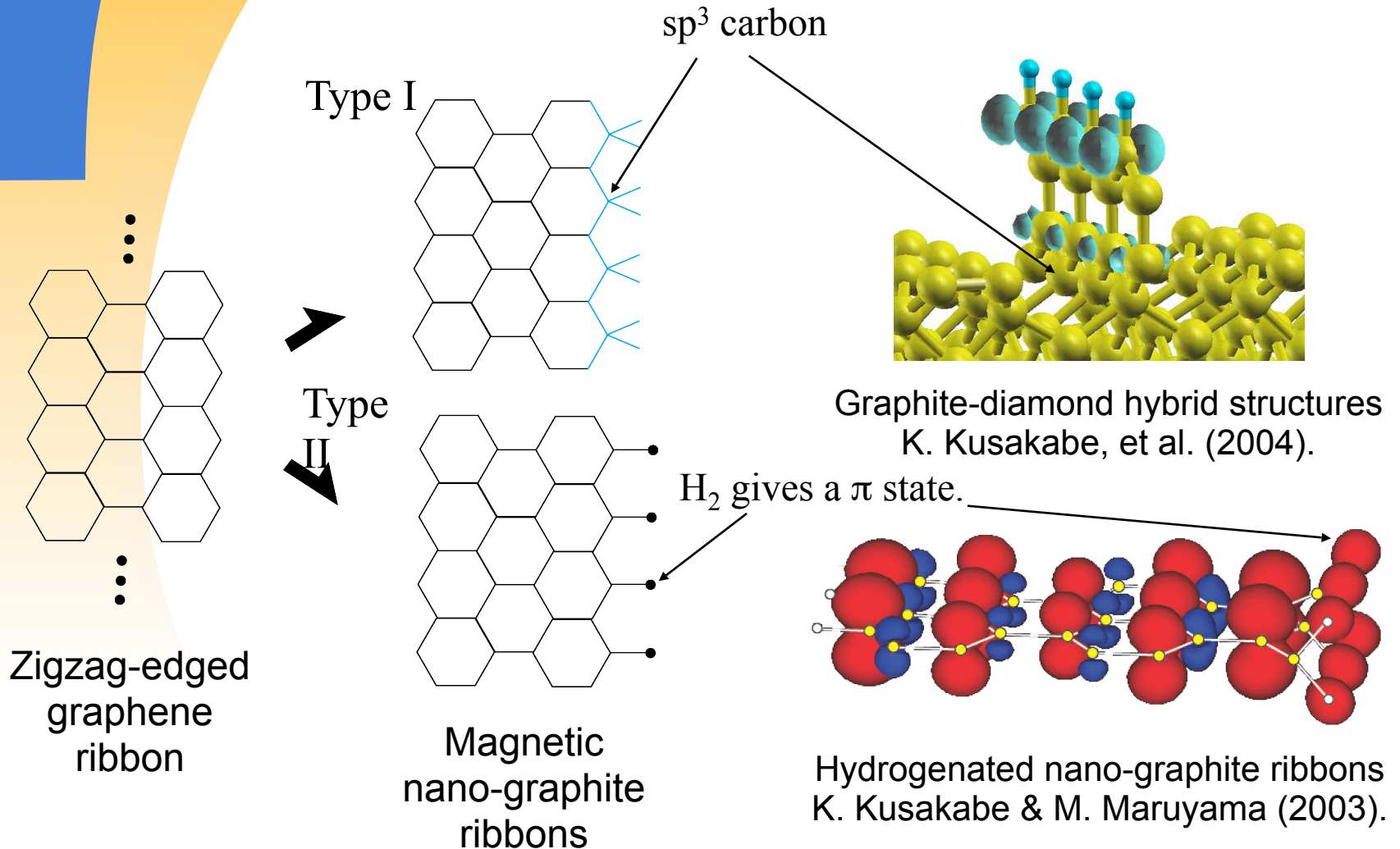
Magnets



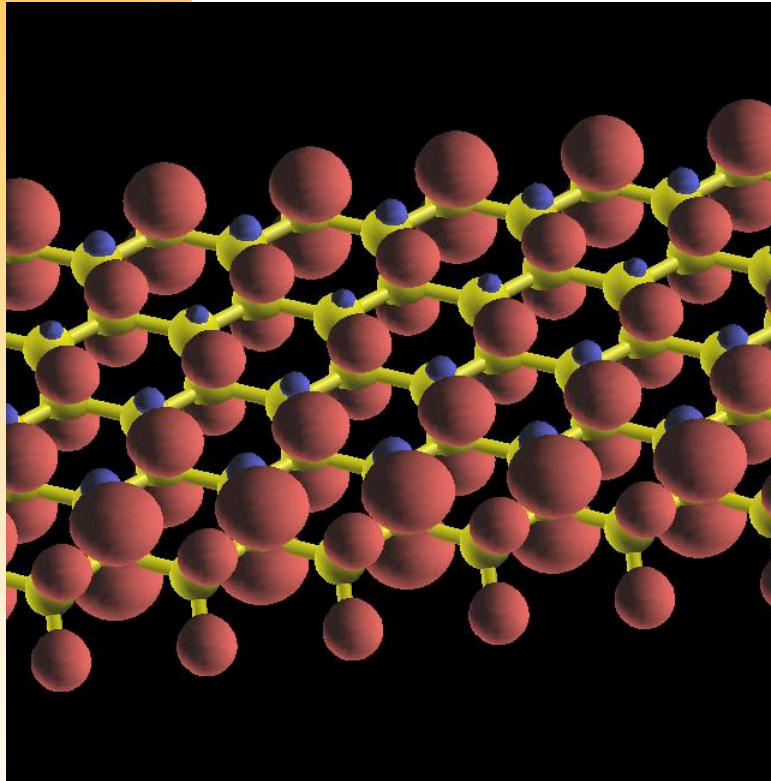
# Possible materials solutions



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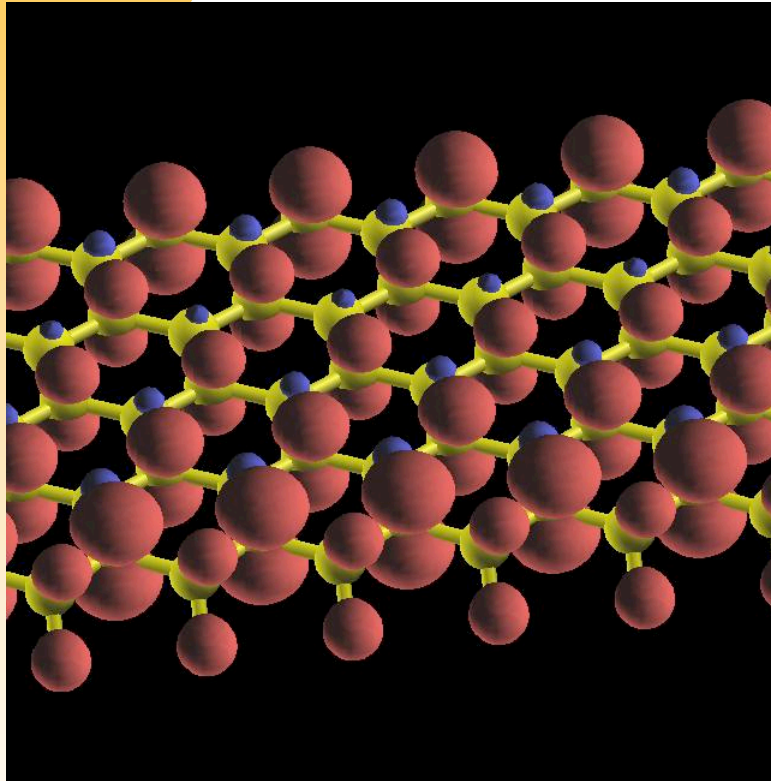
# A hydrogenated magnetic ribbon



LSDA calculation of the magnetic nanographite ribbon with mono- & di-hydrogenated zigzag edges (Isosurfaces represent spin density)

K. Kusakabe and M. Maruyama, PRB 67 (2003) 092406.

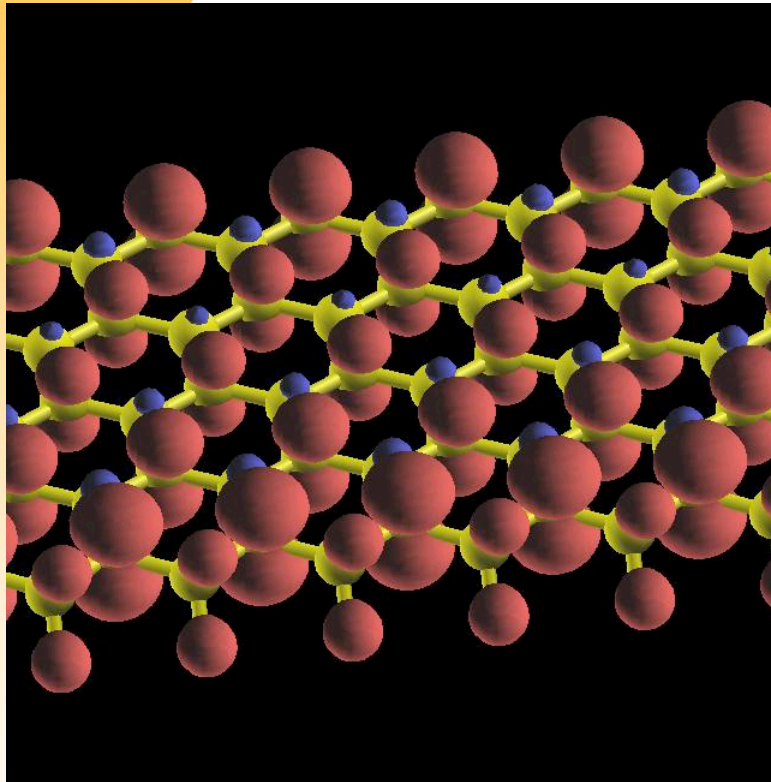
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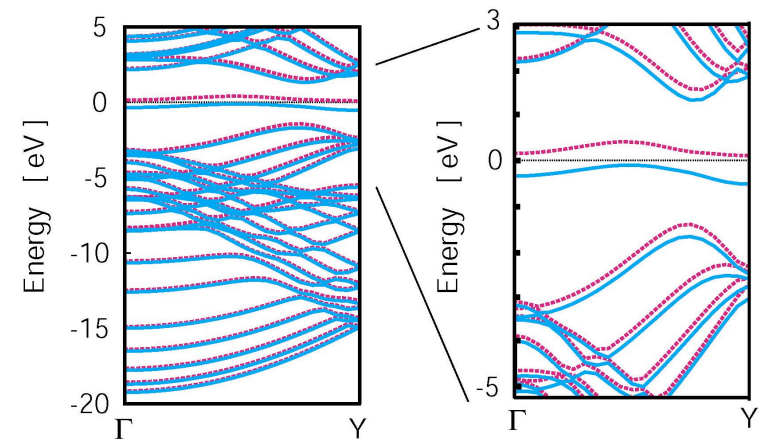
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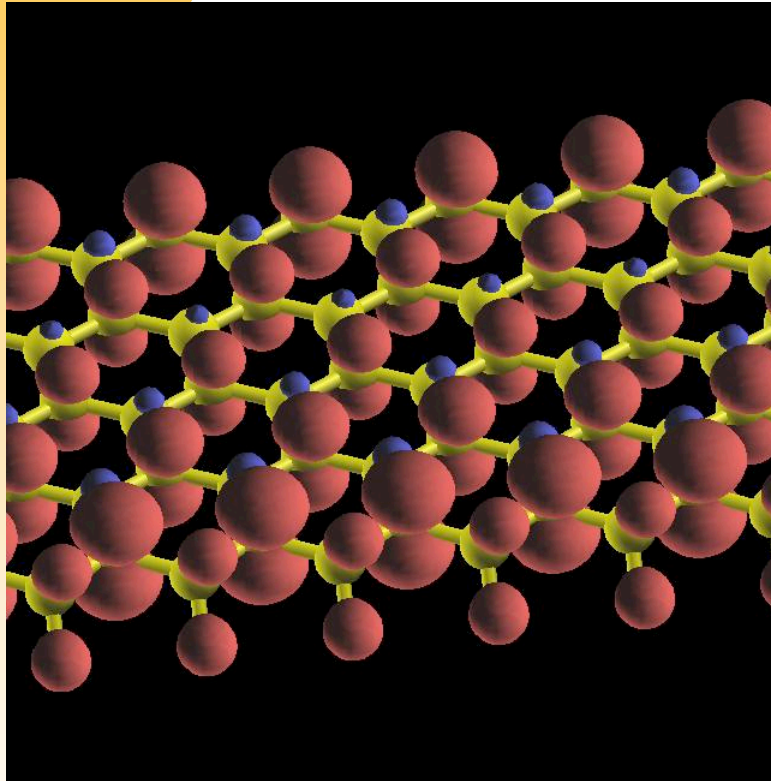


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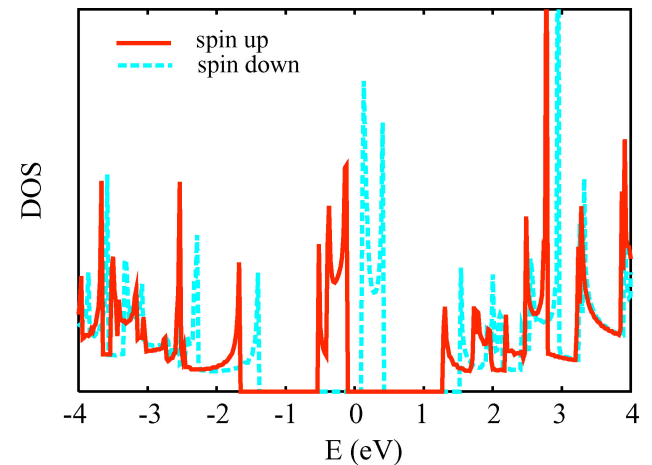
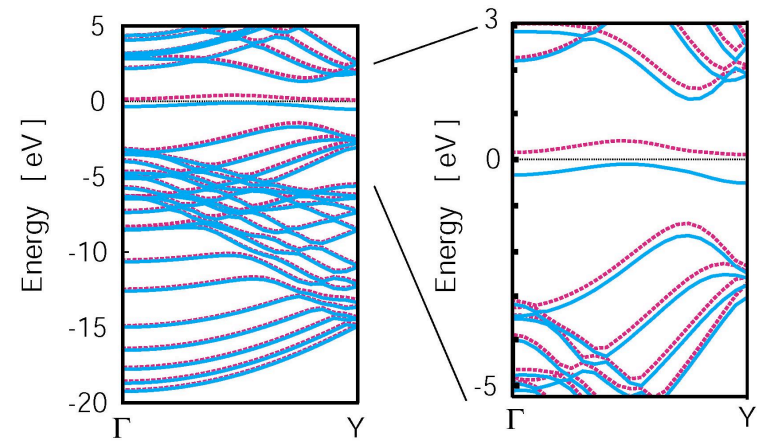


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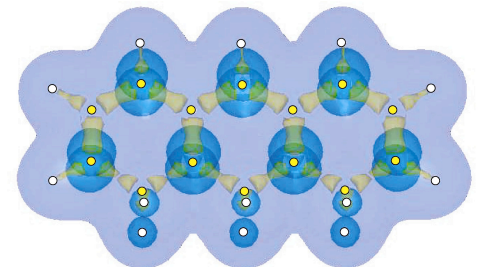


DOS of the magnetic graphene ribbon

K. Kusakabe and M. Maruyama, PRB 67 (2003) 092406.

# Confirmation within DFT & HF

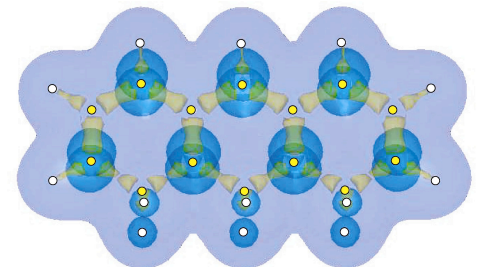
- **The magnetic nano-graphene ribbon with a mono-hydrogenated edge and a di-hydrogenated edge is confirmed to have ferrimagnetic spin alignment in 0 temperature by,**
  - LSDA calculation, GGA calculation
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  - TAPP, VASP
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By K. Akagi.

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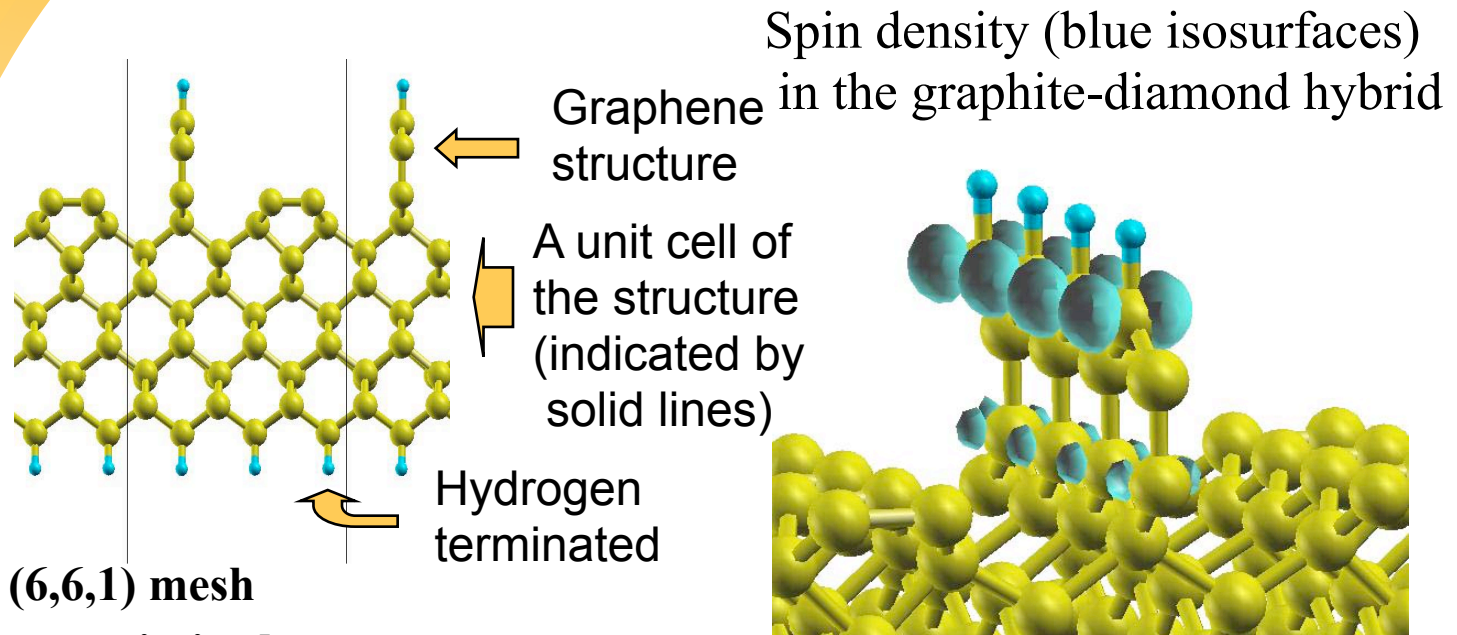
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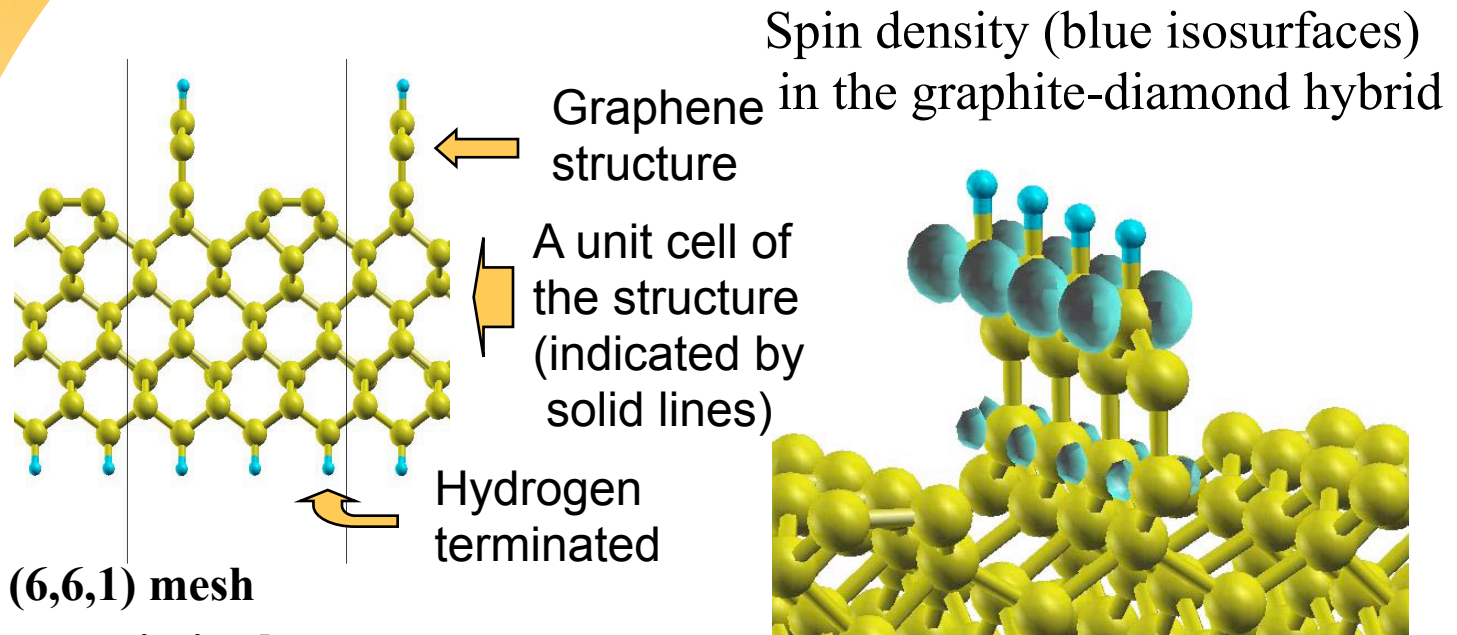
# A stable graphite-diamond hybrid structure



- **k-points on (6,6,1) mesh**
- **Structures are optimized.**
- **Graphene structures on 8-carbon layers in a (3×2) unit cell.**
- **S=1 (per unit cell). The moment of  $1\mu_B$  per each edge carbon atom.**
- **Spins exist only on graphitic structure.**
- **Symmetric dimers are created.**

K. Kusakabe and N. Suzuki, CP772, Physics of Semiconductors: 27th Int. Conf. Phys. Semicon. Part B 1359 (2004)

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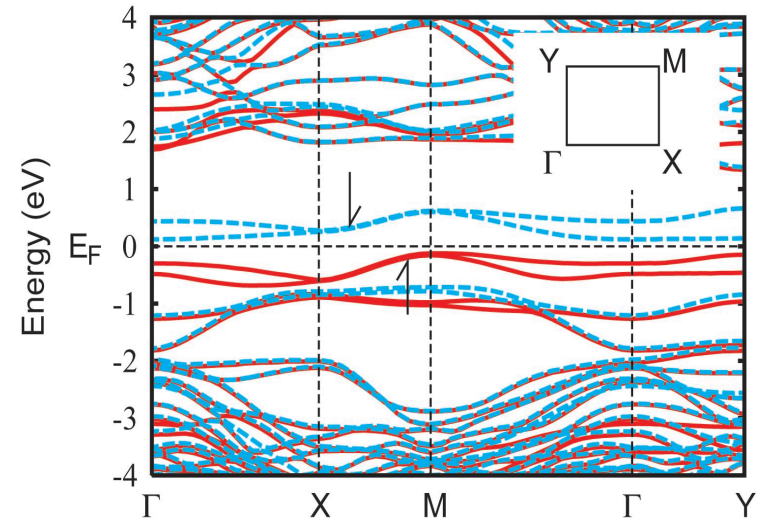
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# Band structure of the structure C

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- **The band (folded in the right figure due to a doubled unit cell) near  $E_F$  is strongly spin polarized. This nearly flat band consists of edge states.**
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- **$E_F$  may be shifted by applied gate voltage or by electron (or hole) doping.**

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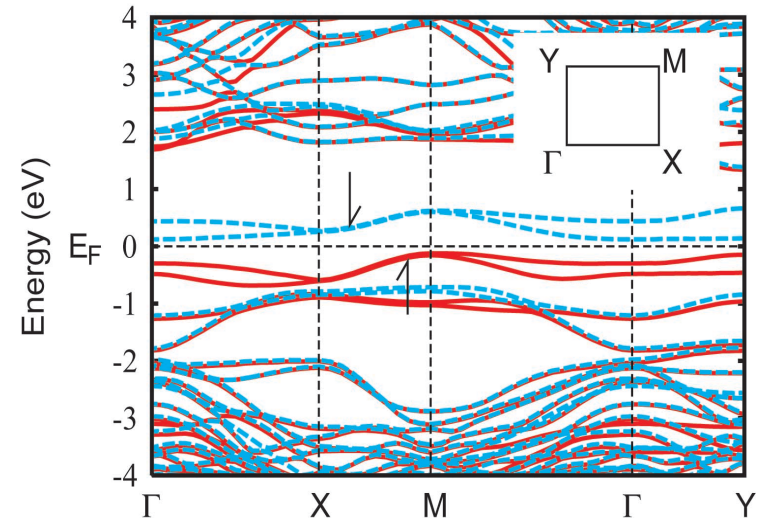
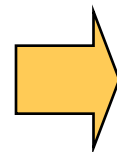
Electronic band structure of the graphite-diamond hybrid structure on a diamond (100) surface (the structure C).

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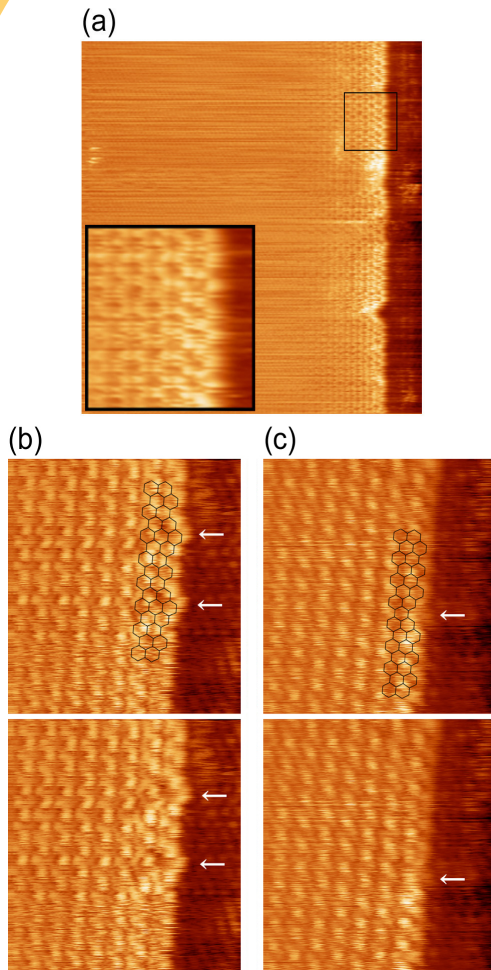
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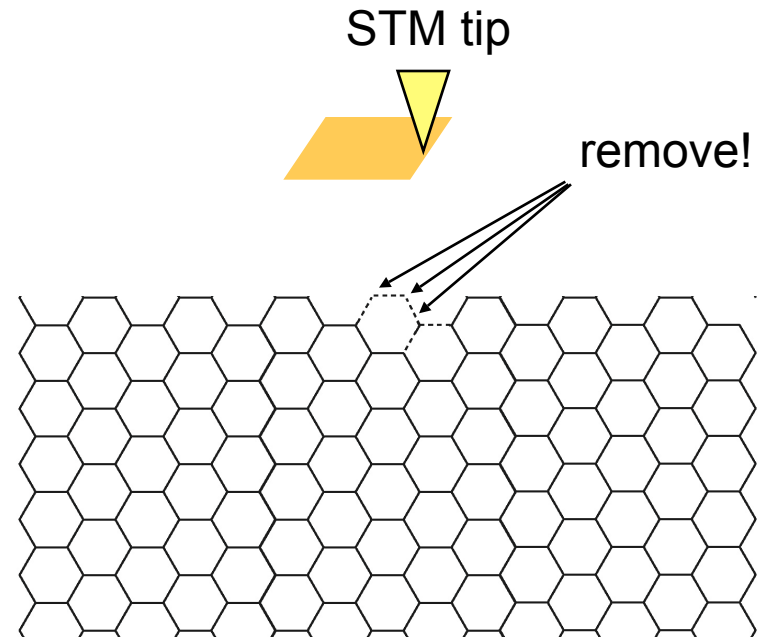
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# Manufacturing Magnetic Nanographite

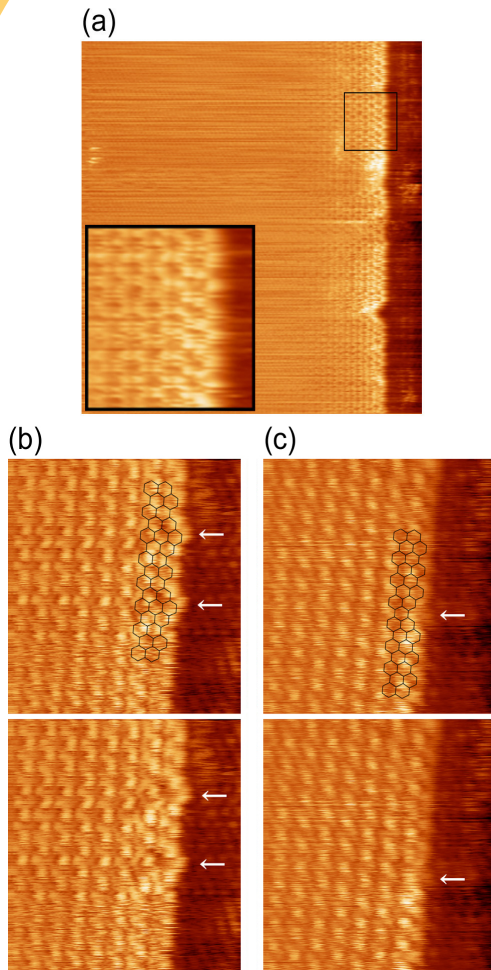


- The armchair edge is stable.
- Removal of odd-numbers carbon atoms would make magnetic moments.

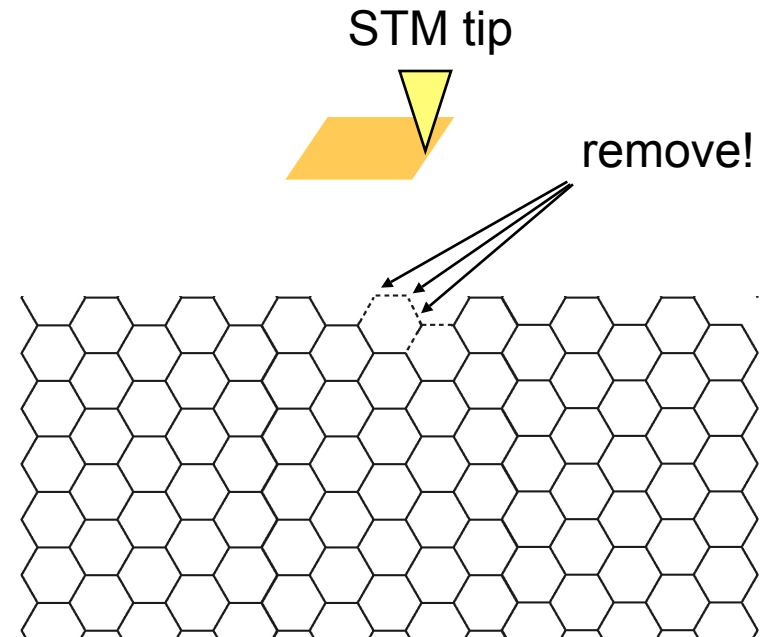


Y. Kobayashi et al. (2005).

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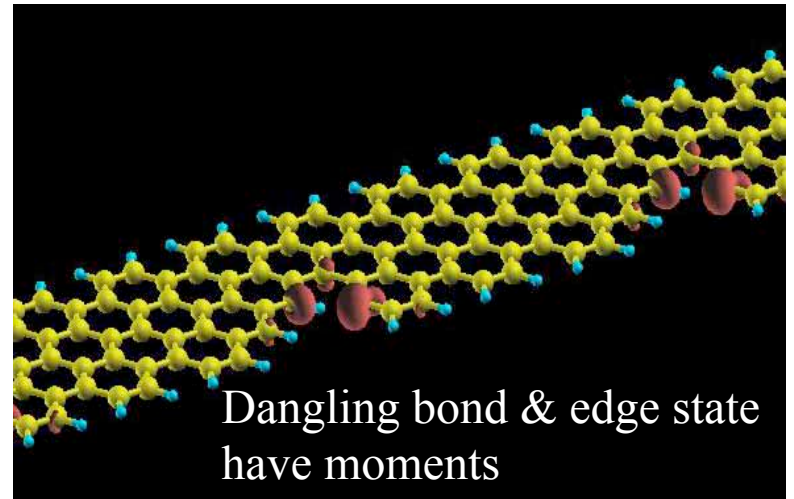
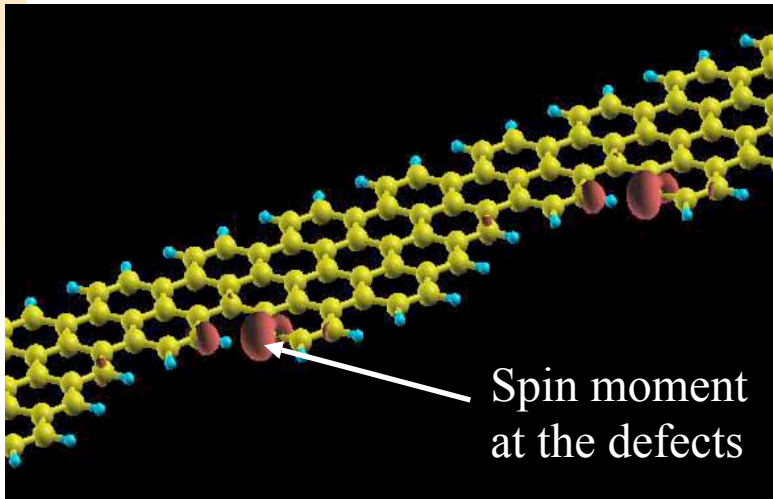
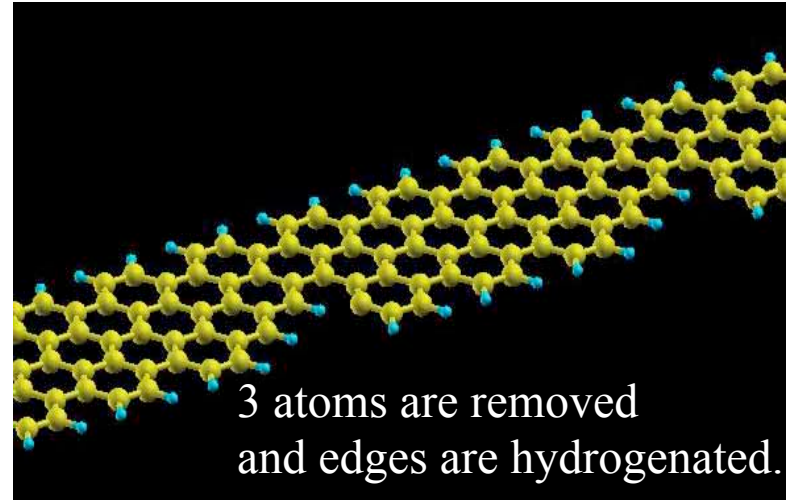
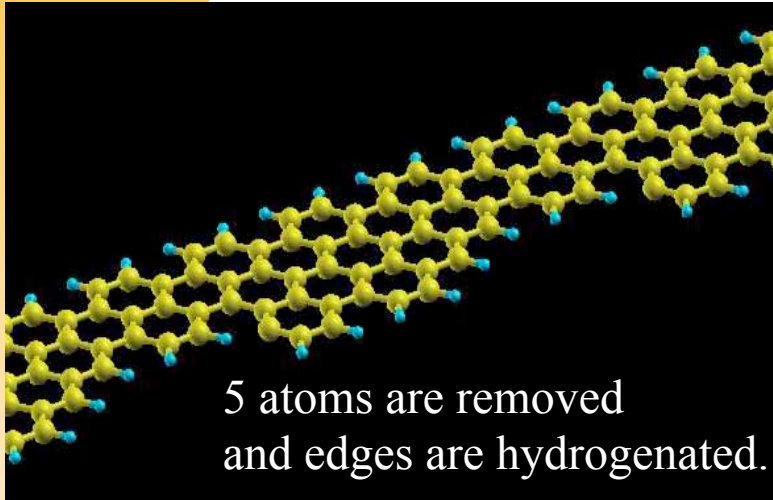


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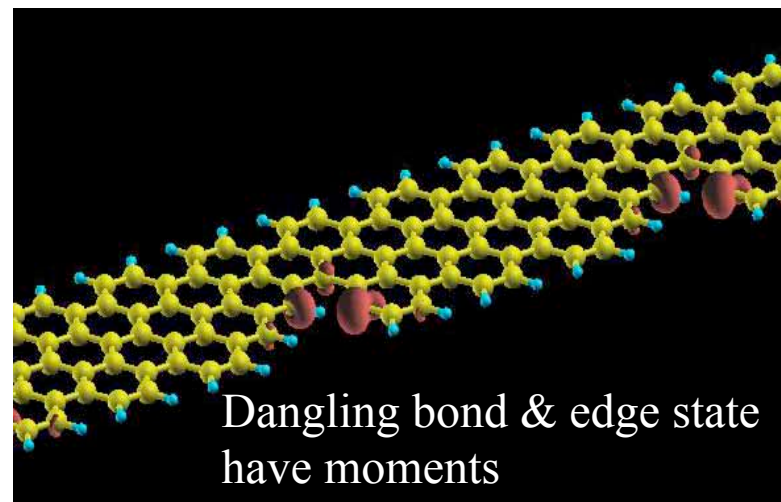
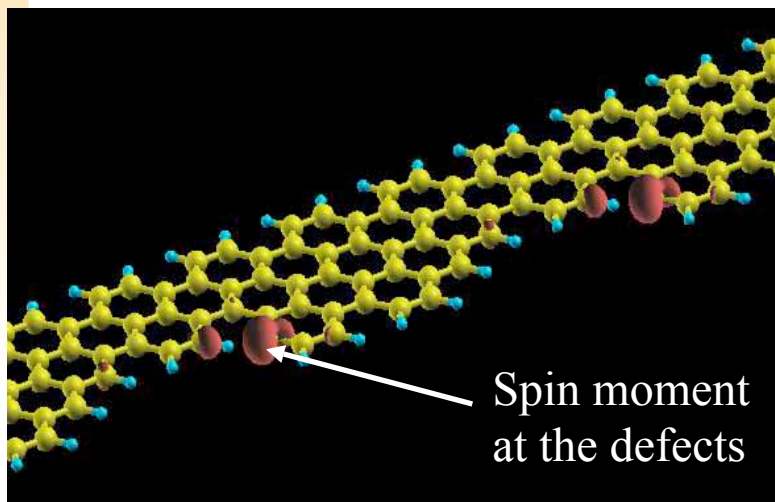
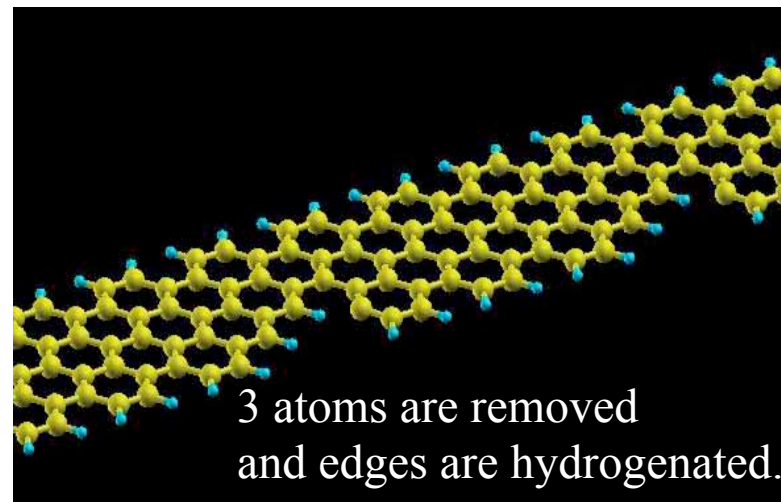
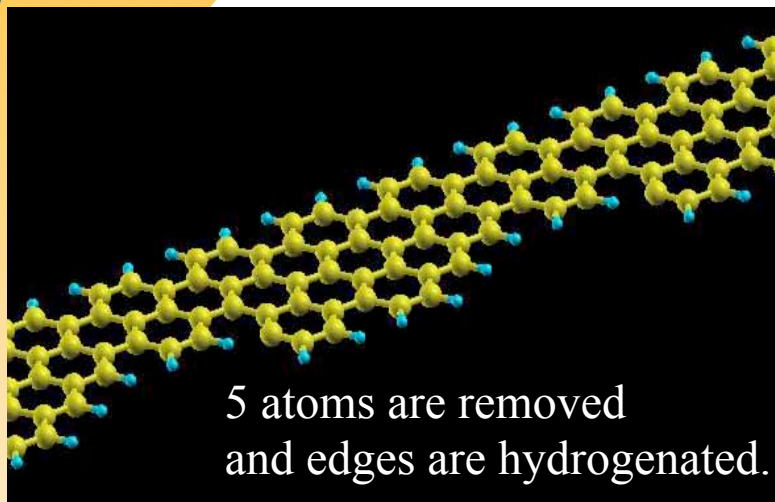


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# Defective armchair ribbons

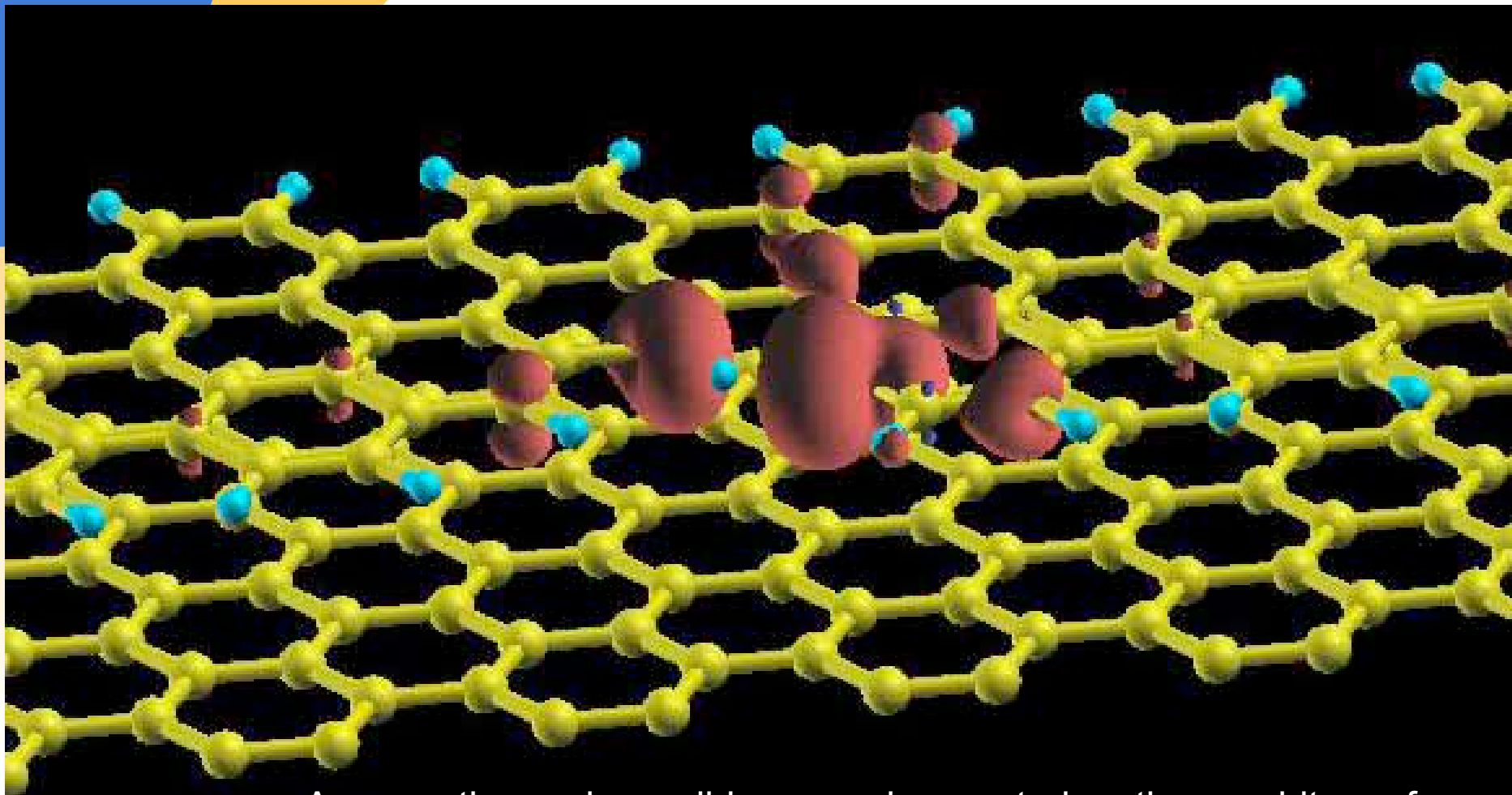


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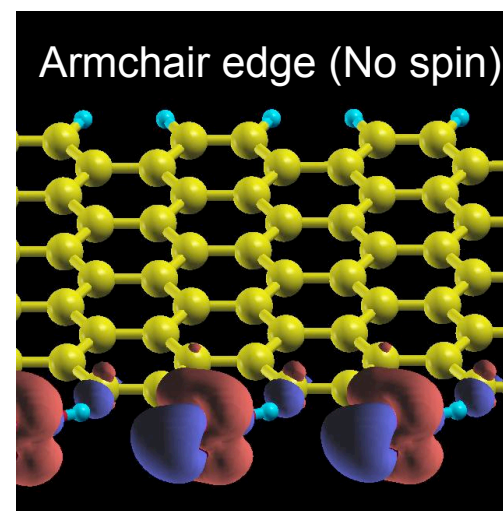
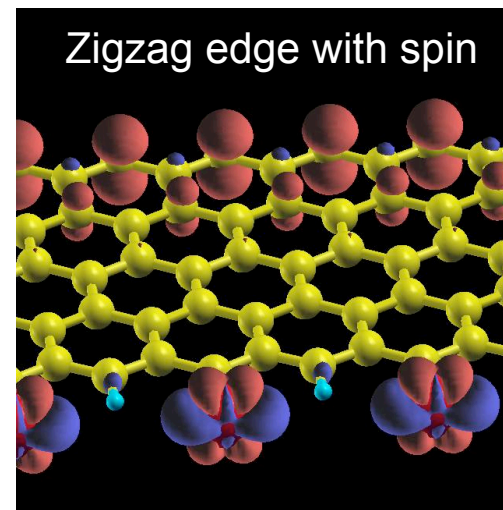
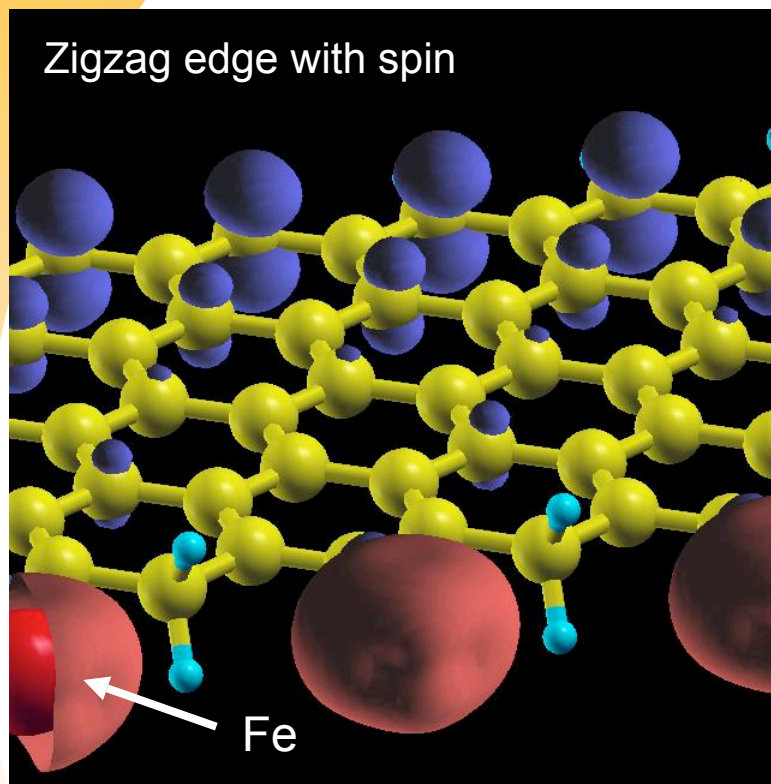


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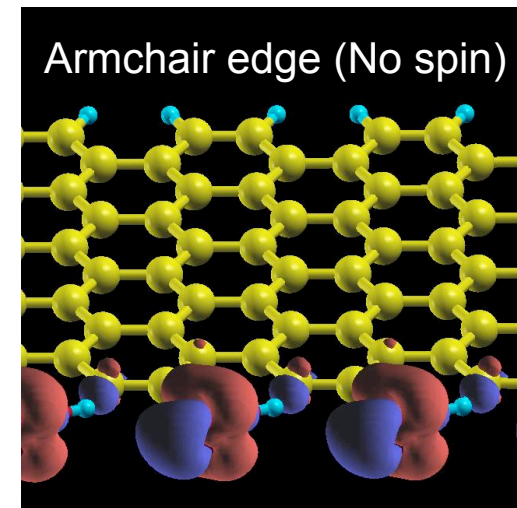
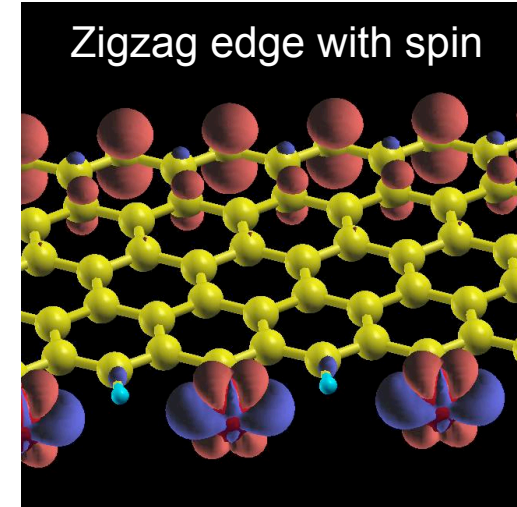
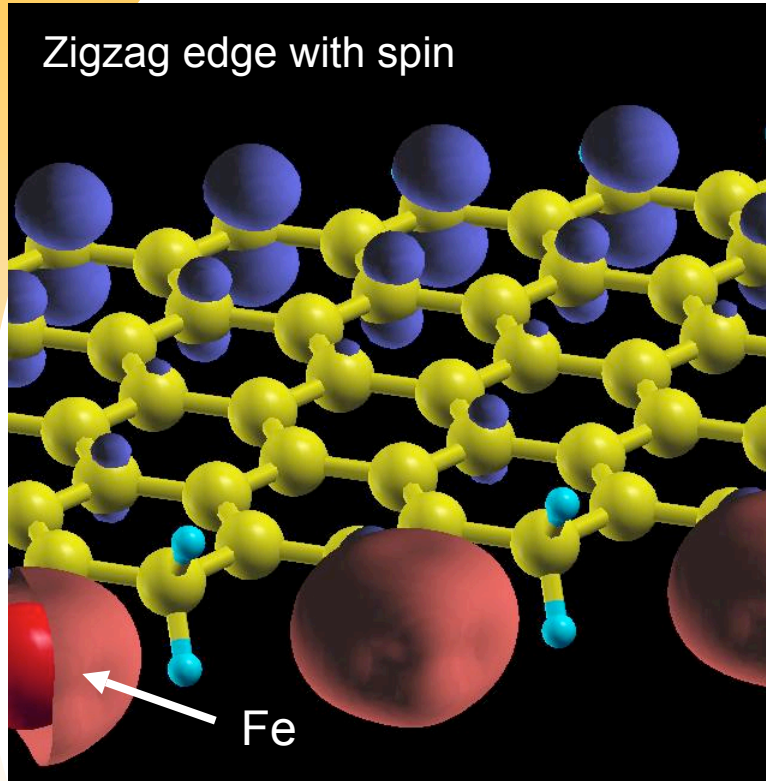
A magnetic graphene ribbon may be created on the graphite surface.

# Effects of Fe impurities



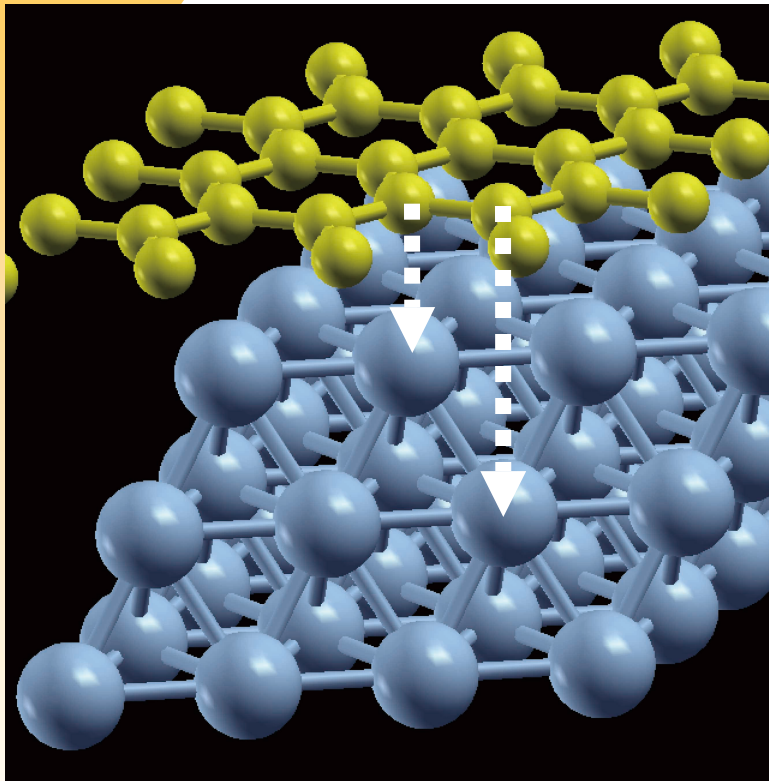
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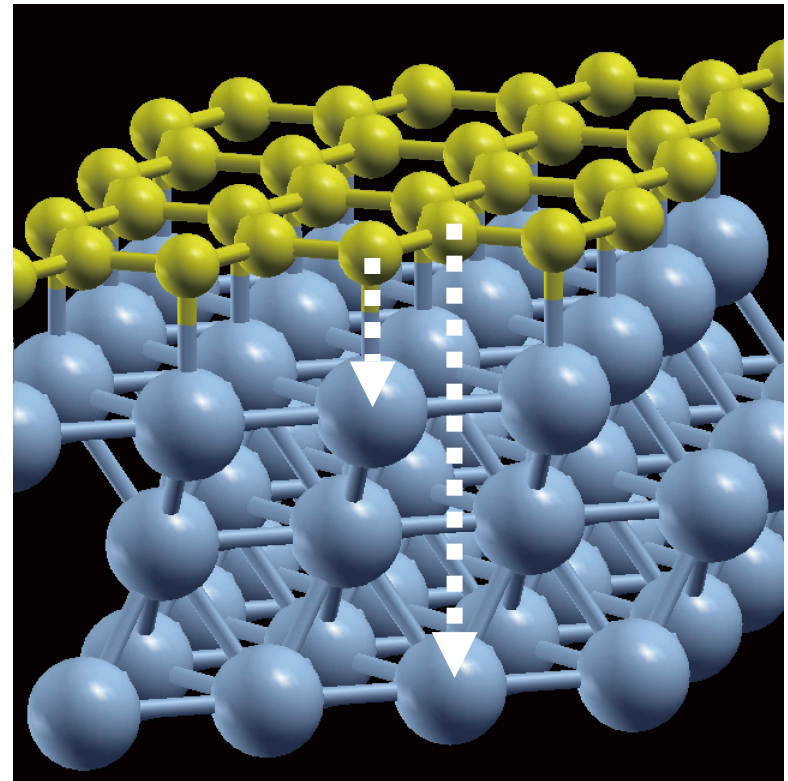


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# Graphene/Ni(111)



Model B

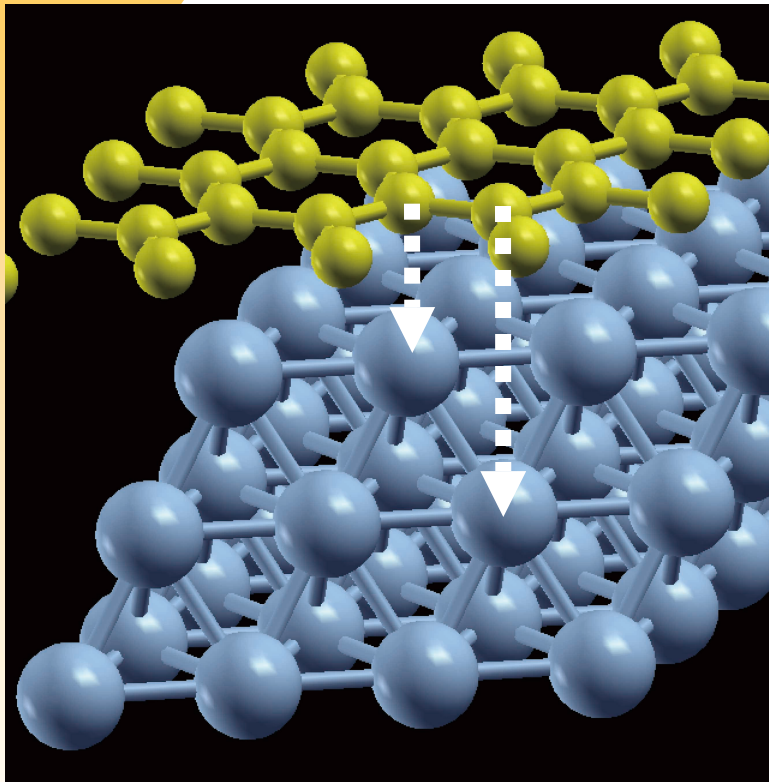


Model C

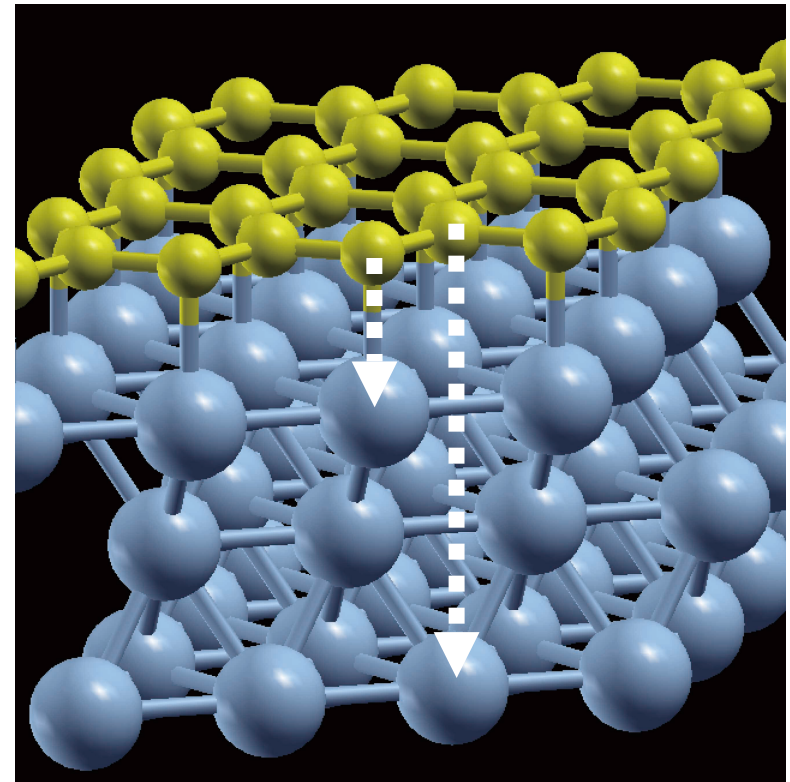
For both models, the majority band has a slightly filled upper  $\pi$  branch, and the minority band has a filled lower  $\pi$  branch at K.

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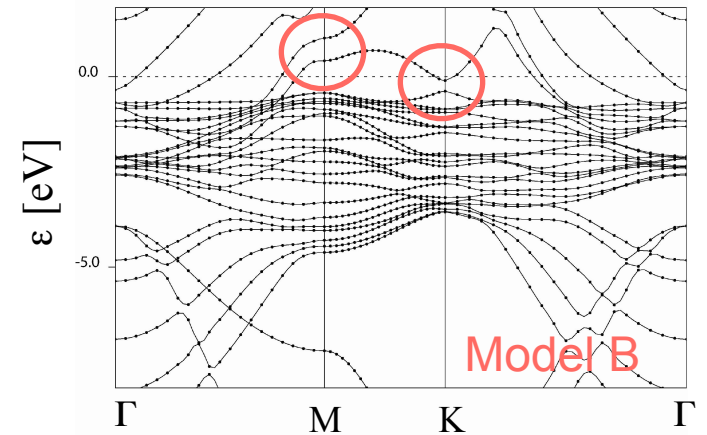
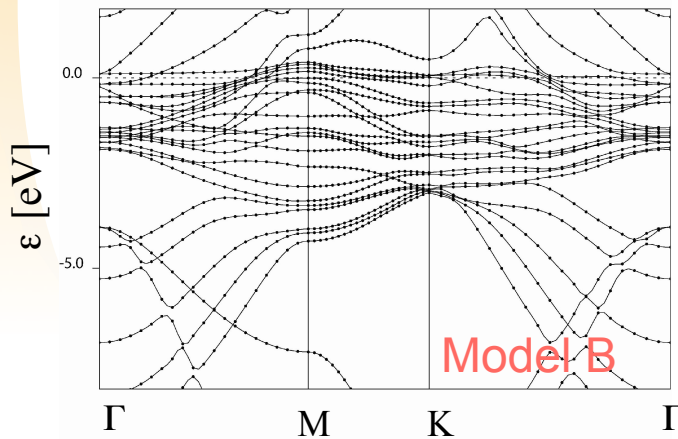
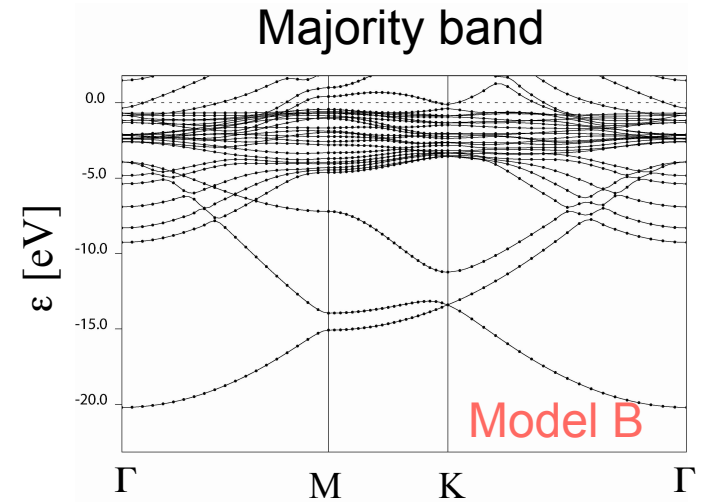
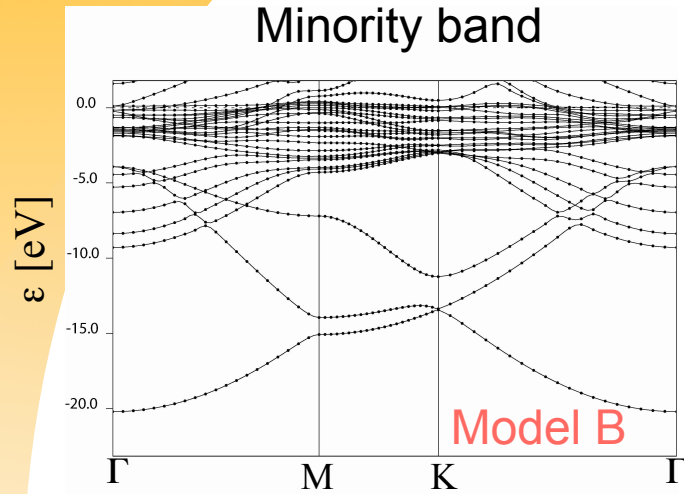
# Calculation conditions

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- **GGA by PBE96.**
- **Energy cut-off : 25Ry for wf, 150Ry for charge.**
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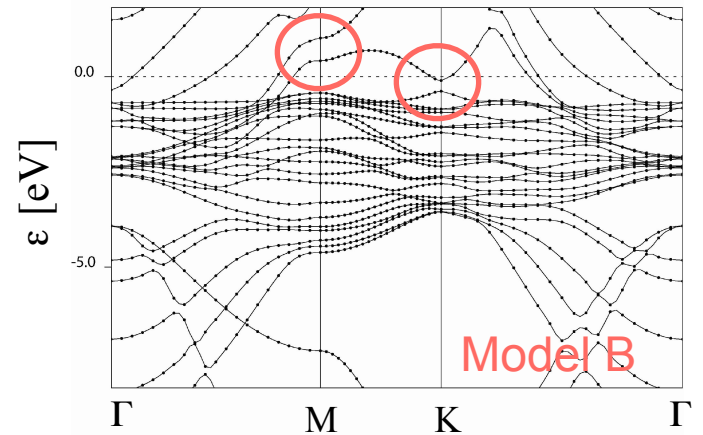
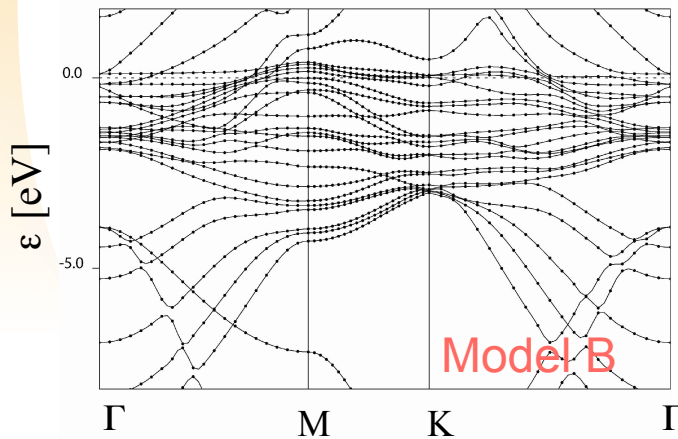
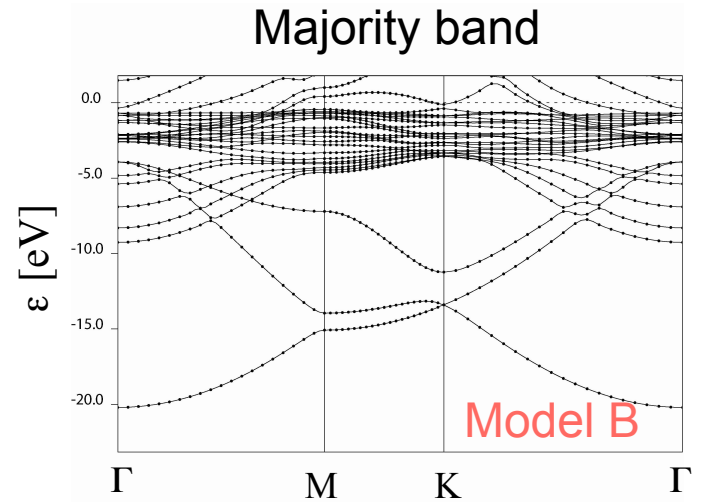
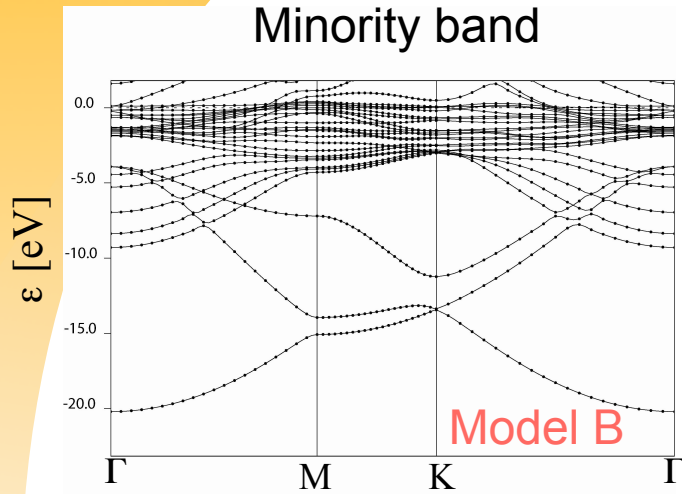
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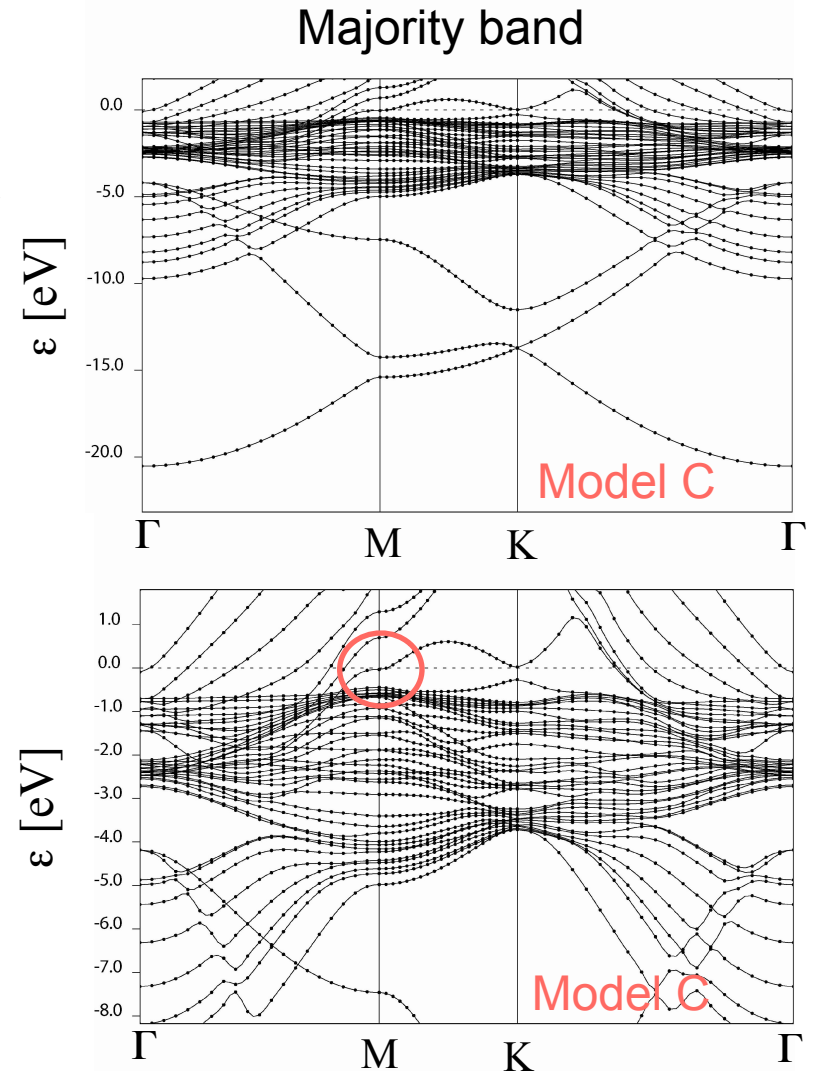


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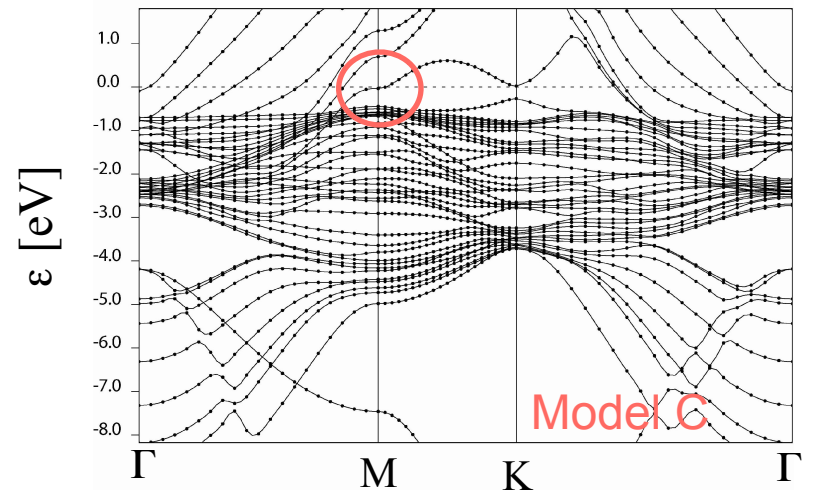
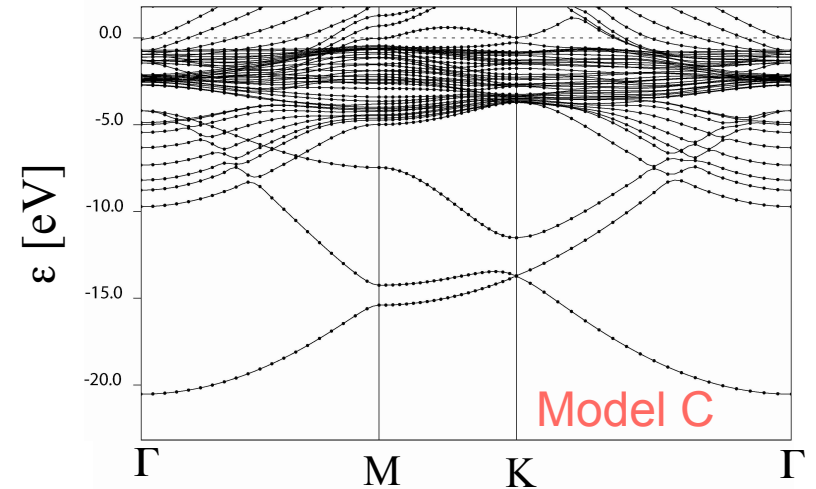
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- For the model B and C, the  $\pi$  band has a gap at the K point.
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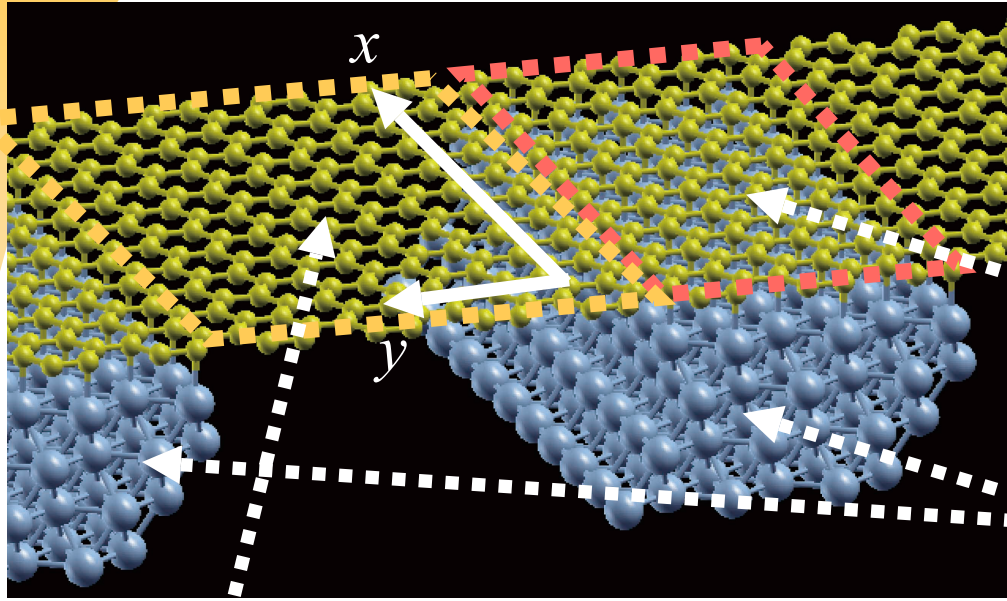
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Majority band



# A graphene/Ni junction structure



Gapped graphene  
(Gap at the K points)

Magnetic electrode

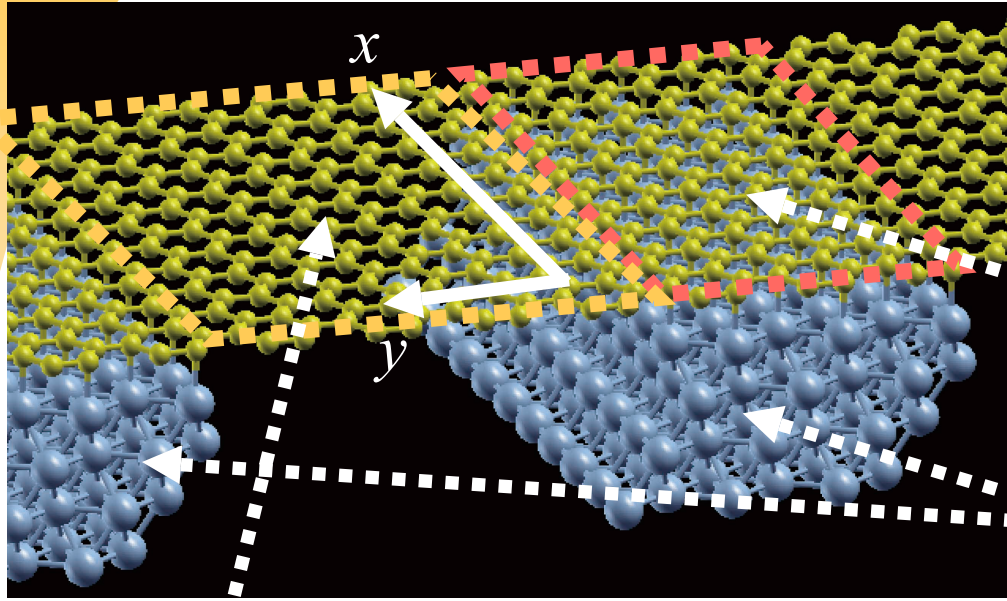
Metallic graphene

A MM/G/M/G/MM junction ( M: metal, G: Gapped, MM: magnetic metal)

Theoretical clues to understand its nature:

1. The LDA band structure loses dispersion in the  $y$  direction around  $E_F$ .
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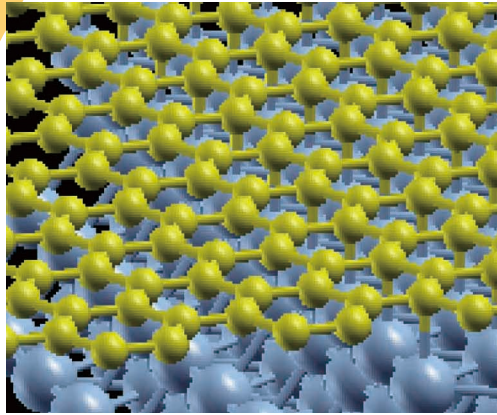
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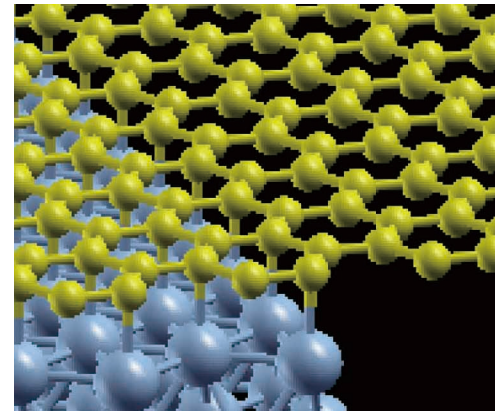
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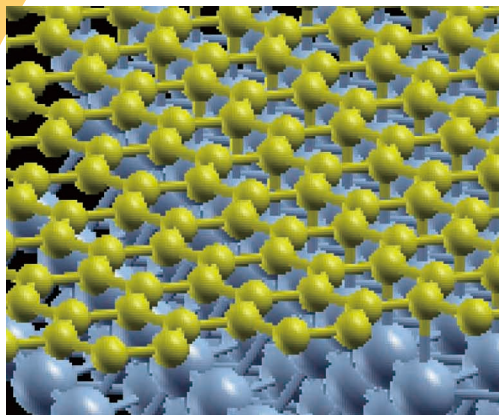
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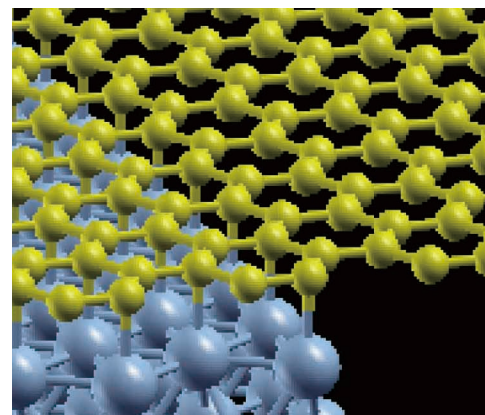
Klein's edge

- **In a tight binding description, Ni atoms produce site-selective potential, which appears as a diagonal (flavor dependent) potential to the two-dimensional Dirac fields.**
- **We would have two different edge structures of interfaces, a zigzag and Klein's edges, between graphene and Ni electrodes.**
- **Thus, we have a room to have a finite graphene ribbon in between two Ni electrodes.**

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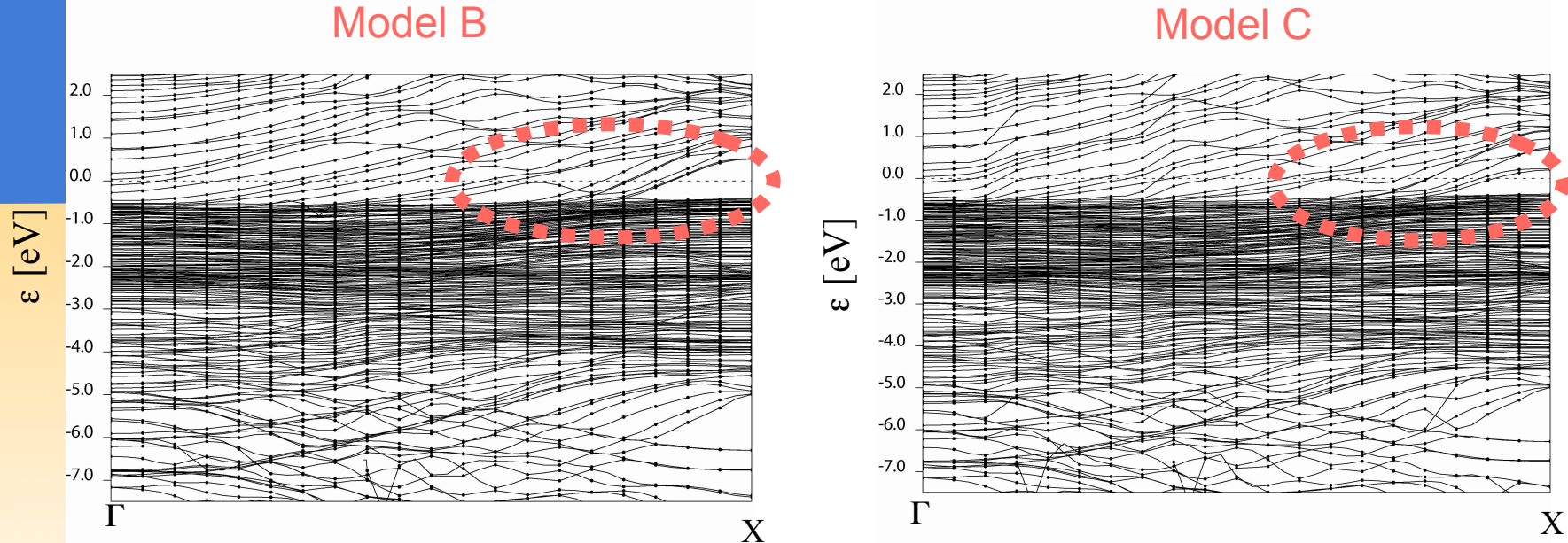
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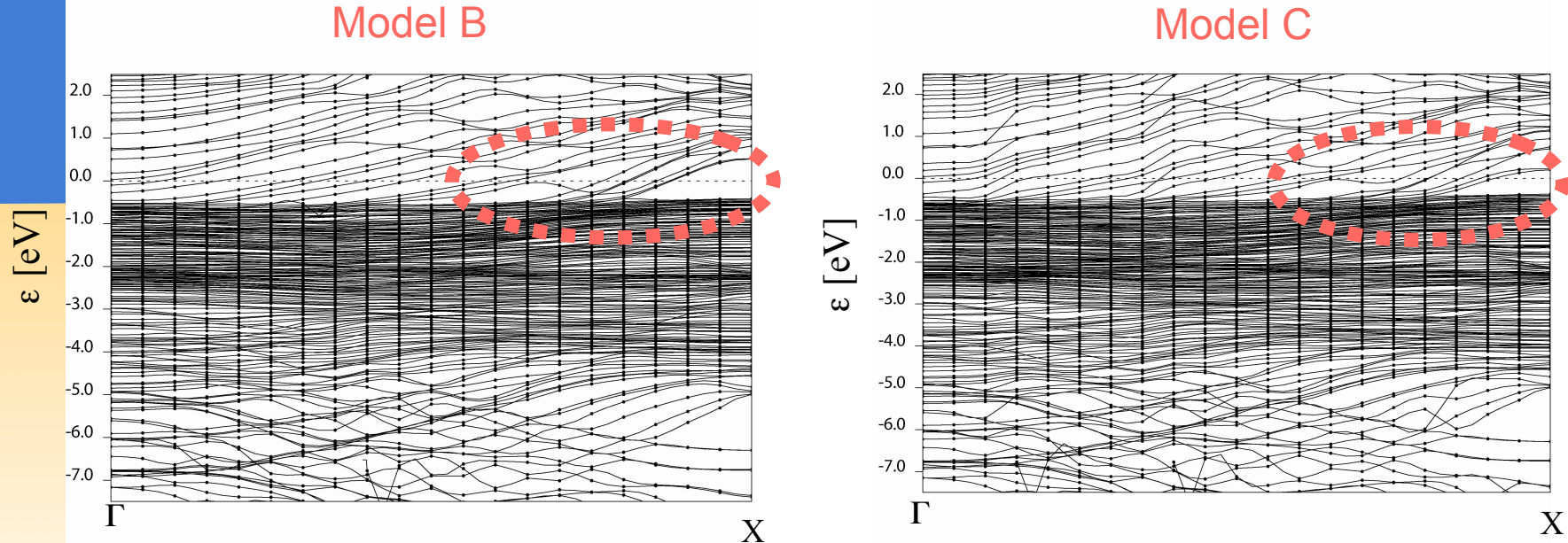
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- Dispersion relation around the X point suggests that  $\pi$  character remains in the electronic state.
- To construct an effective theory for this structure, modeling of d orbital as well as  $\pi$  orbital should be demanded.

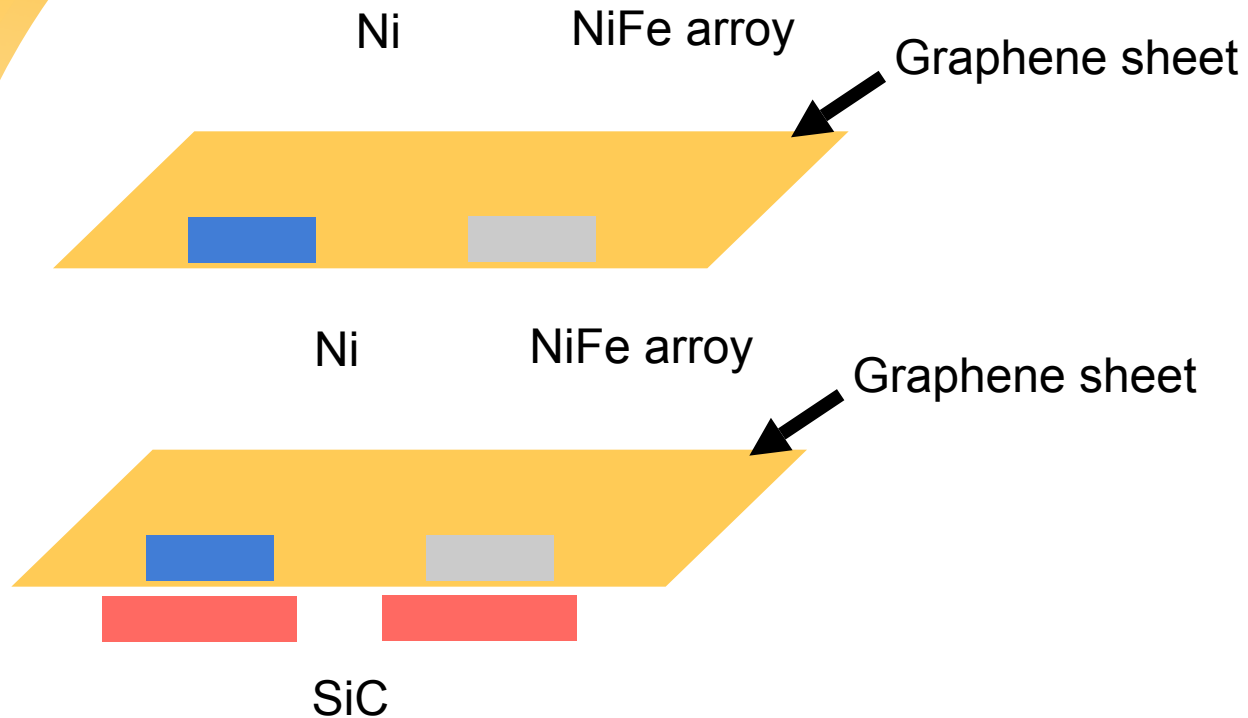


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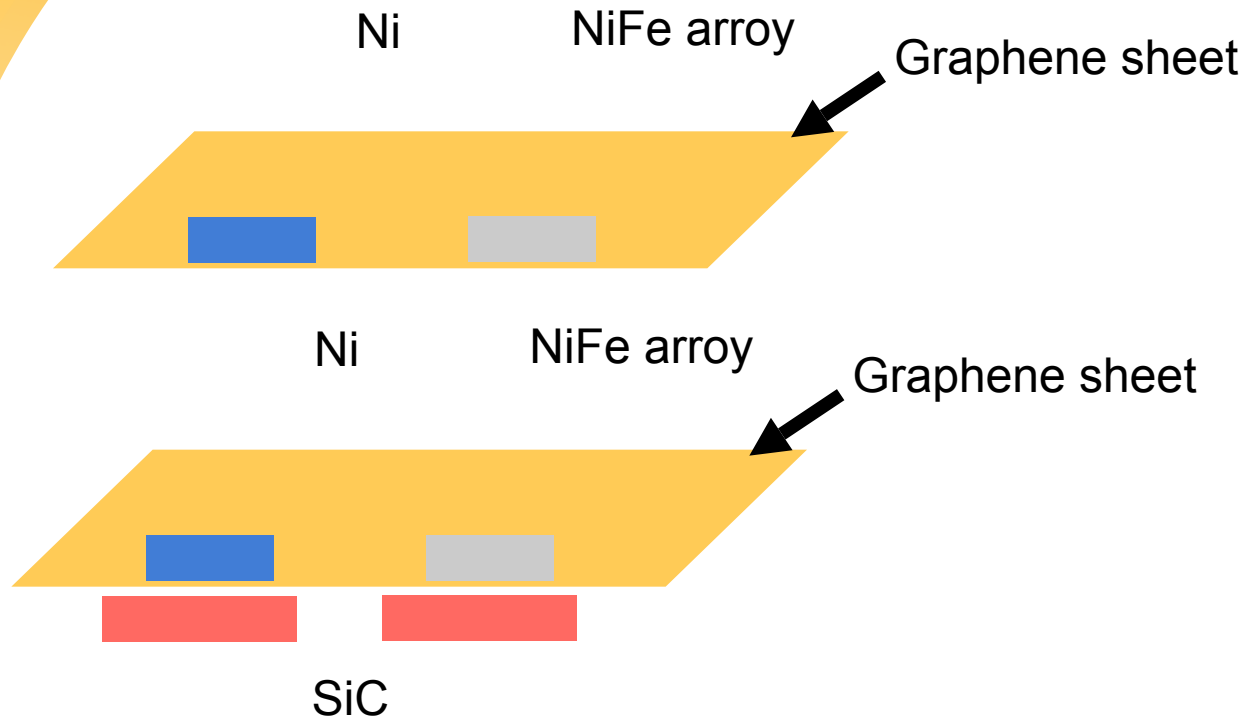
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1. To avoid undesired direct current flow from magnetic electrodes to graphene we may utilize SiC to induce alternating potential to make a gap in graphene.
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- **Possible device structures are proposed utilizing interfaces between graphene and the Ni (111) surface.**
- **All the available consideration using various electron models conclude existence of localized magnetism at the zigzag edges of finite graphene ribbon structures.**

# Design of Models of Magnetic Materials

- **Present DFT approach : Magnetism by LSDA**
    - Design of magnetic materials using the Heisenberg model, the Hubbard model, etc.
    - Confirm the magnetic solution using the first-principles calculation
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- **MR-DFT approach : Magnetism in many-body theory**
    - Design of magnetic materials directly using a correlated electron model from the first principles.
    - Direct simulation of functionality from the first principles: The quantum simulator.
    - **A self-consistent electronic structure calculation with interacting electron description enables** us to predict functional materials with **magnetism**.

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# A conclusion from MR-DFT

The Levy-Lieb energy functional is defined by,

$$F[n] = \min_{\Psi \rightarrow n} \langle \Psi | \hat{T} + \hat{V}_{ee} | \Psi \rangle.$$

Since  $F[n]$  is not a convex functional, it is impossible to have a functional derivative of  $F[n]$  w.r.t.  $n(\mathbf{r})$ . To have a well-defined derivative, we may consider the Lieb functional which is a Legendre transform of  $F[n]$ . There are several expressions as follows.

$$\begin{aligned} \bar{F}[n] &= \sup_{v \in L^{3/2} + L^\infty} \left[ \inf_{n' \in \mathcal{I}_N} \left\{ \min_{\Psi \rightarrow n'} \langle \Psi | \hat{T} + \hat{V}_{ee} | \Psi \rangle + \int d^3r v(\mathbf{r}) n'(\mathbf{r}) \right\} \right. \\ &\quad \left. - \int d^3r v(\mathbf{r}) n(\mathbf{r}) \right], \\ &= \inf_{\hat{D} \rightarrow n} \text{tr} \hat{D} (\hat{T} + \hat{V}_{ee}), \\ &= \sup_{v \in L^{3/2} + L^\infty} \left[ \min_{\Psi} \langle \Psi | \hat{T} + \hat{V}_{ee} + \int d^3r v(\mathbf{r}) (\hat{n}(\mathbf{r}) - n(\mathbf{r})) | \Psi \rangle \right]. \end{aligned}$$

**Quantum mechanics driven by  $n(\mathbf{r})$ .**

**Thus we can design future first-principles calculation methods starting from MR-DFT.**

# A conclusion from MR-DFT

The Levy-Lieb energy functional is defined by,

$$F[n] = \min_{\Psi \rightarrow n} \langle \Psi | \hat{T} + \hat{V}_{ee} | \Psi \rangle.$$

Since  $F[n]$  is not a convex functional, it is impossible to have a functional derivative of  $F[n]$  w.r.t.  $n(\mathbf{r})$ . To have a well-defined derivative, we may consider the Lieb functional which is a Legendre transform of  $F[n]$ . There are several expressions as follows.

$$\begin{aligned} \bar{F}[n] &= \sup_{v \in L^{3/2} + L^\infty} \left[ \inf_{n' \in \mathcal{I}_N} \left\{ \min_{\Psi \rightarrow n'} \langle \Psi | \hat{T} + \hat{V}_{ee} | \Psi \rangle + \int d^3r v(\mathbf{r}) n'(\mathbf{r}) \right\} \right. \\ &\quad \left. - \int d^3r v(\mathbf{r}) n(\mathbf{r}) \right], \\ &= \inf_{\hat{D} \rightarrow n} \text{tr} \hat{D} (\hat{T} + \hat{V}_{ee}), \\ &= \sup_{v \in L^{3/2} + L^\infty} \left[ \min_{\Psi} \langle \Psi | \hat{T} + \hat{V}_{ee} + \int d^3r v(\mathbf{r}) (\hat{n}(\mathbf{r}) - n(\mathbf{r})) | \Psi \rangle \right]. \end{aligned}$$

**Quantum mechanics driven by  $n(\mathbf{r})$ .**

**Thus we can design future first-principles calculation methods starting from MR-DFT.**