

YKIS 07
Kyoto
November 14,
2007

Finite-Temperature Mott Transition in 2D Frustrated Hubbard Models

Norio Kawakami
(Kyoto)

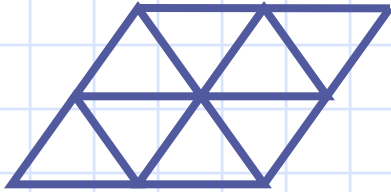
Collaborator
s

T. Ohashi (Osaka)

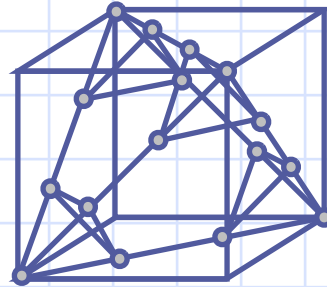
H. Tsunetsugu (Tokyo)

T. Momoi (Riken)

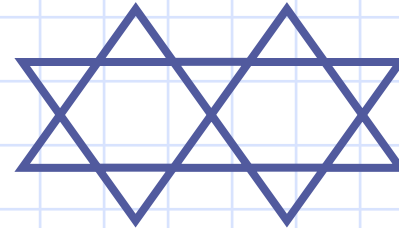
Electron Systems with Frustration



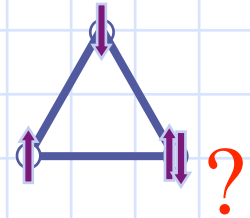
Triangular



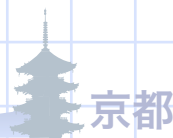
Pyrochlore



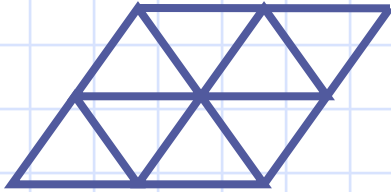
Kagomé



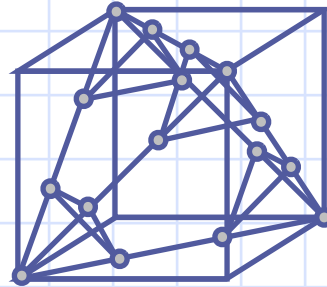
- ◆ Heavy Fermion: LiV_2O_4 , etc
- ◆ Superconductivity: $\text{Na}_x\text{CoO}_2 \cdot y\text{H}_2\text{O}$, AOs_2O_6 , etc
- ◆ Quantum spin liquid: $\kappa\text{-(BEDT-TTF)}_2\text{-X}$, etc



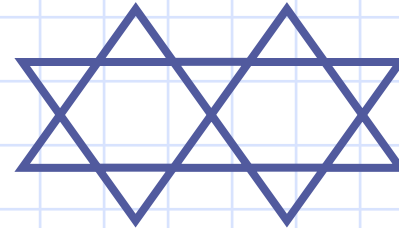
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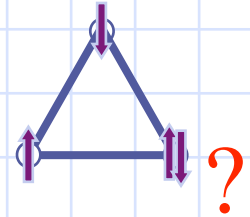
Triangular



Pyrochlore



Kagomé

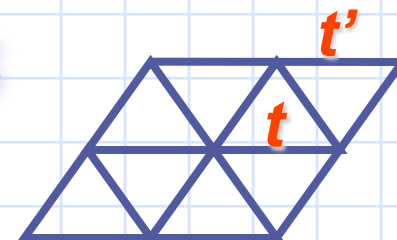


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Mott Transitions
with Strong Frustration

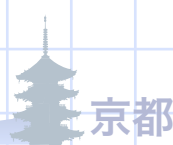
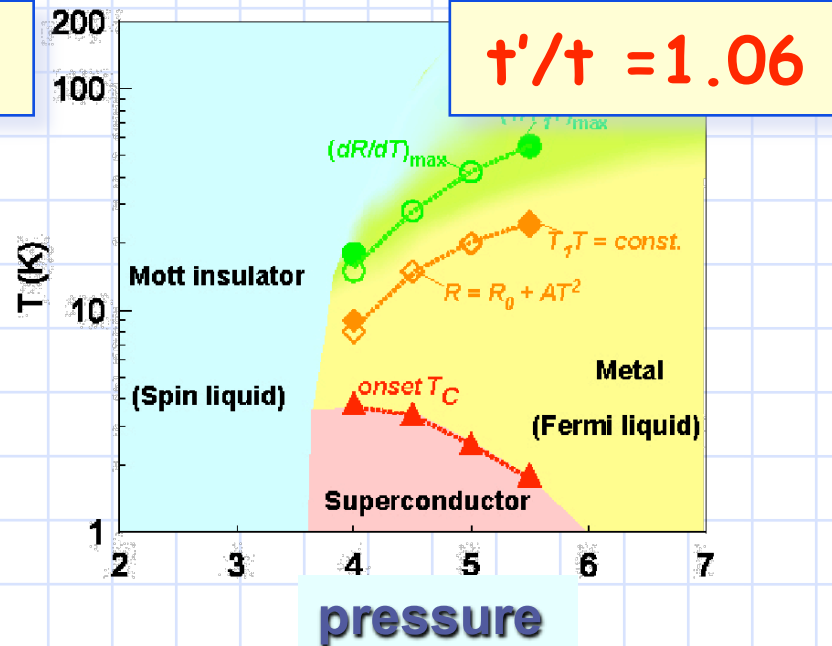
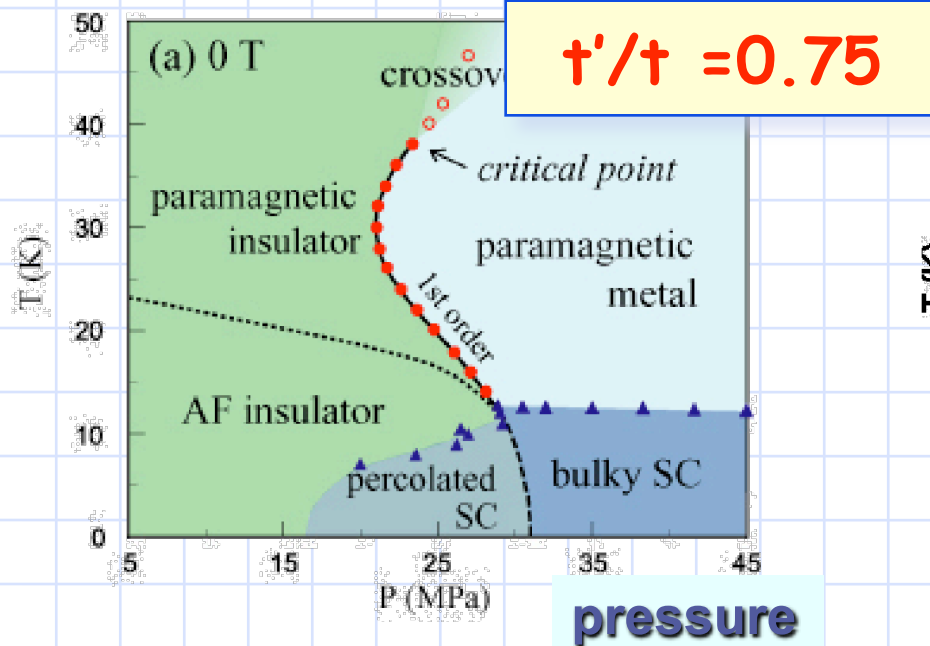
MIT in organic materials

Anisotropic triangular lattice



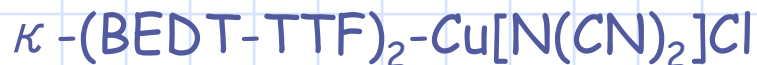
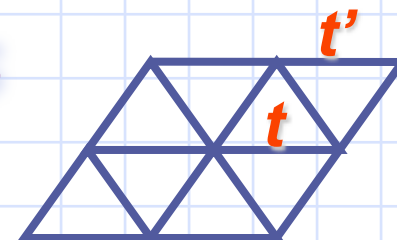
κ -(BEDT-TTF)₂-Cu[N(CN)₂]Cl
F. Kagawa et al. (2004)

κ -(BEDT-TTF)₂-Cu₂(CN)₃
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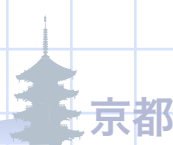
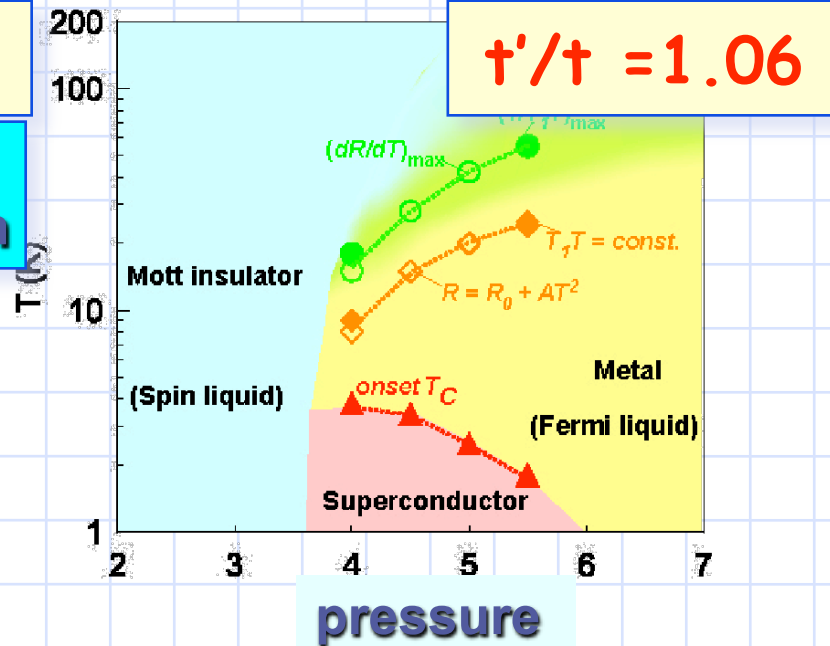
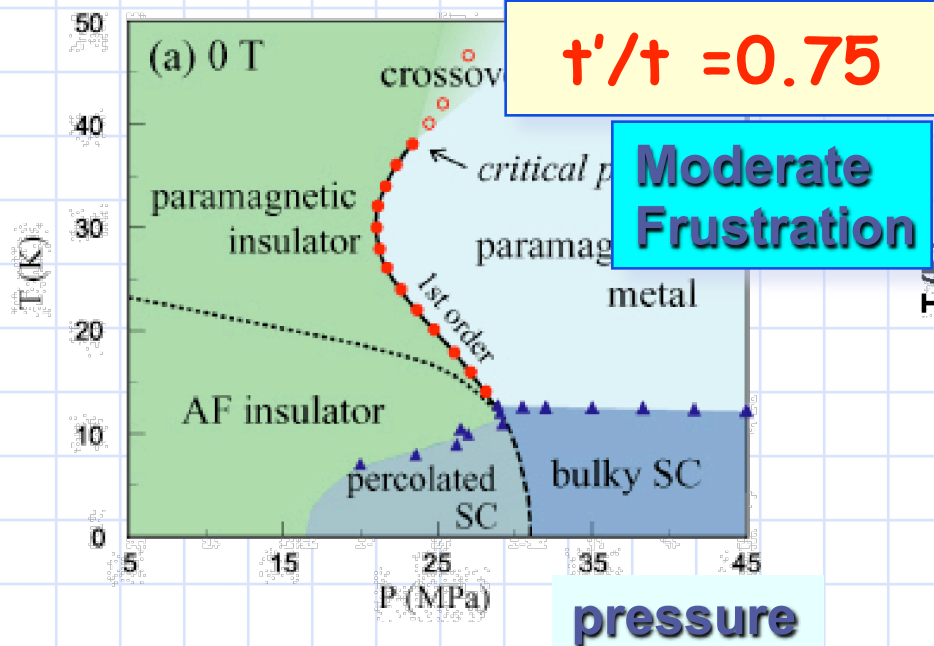
Anisotropic triangular lattice



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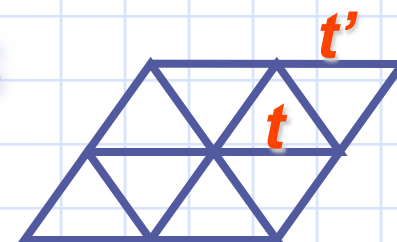


Y. Kurosaki et al. (2005)



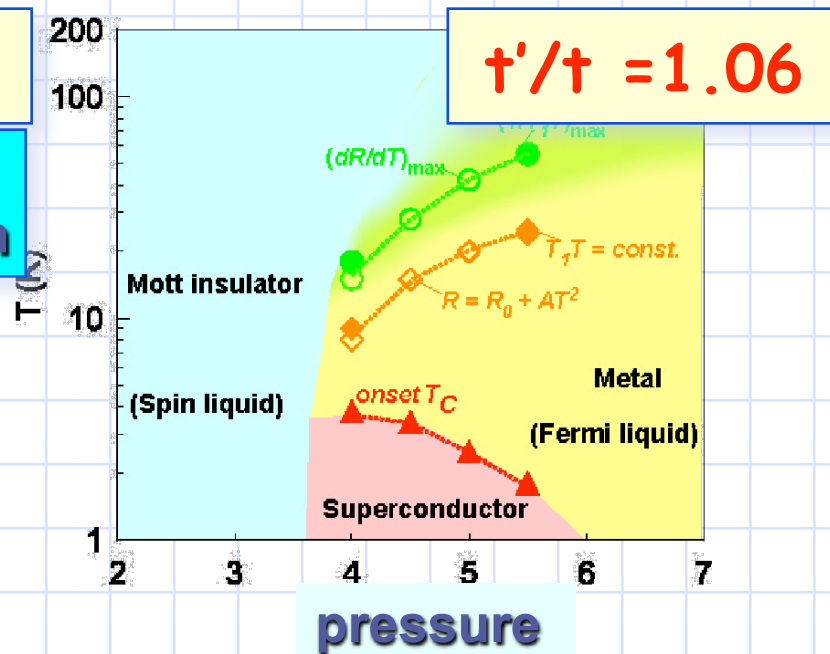
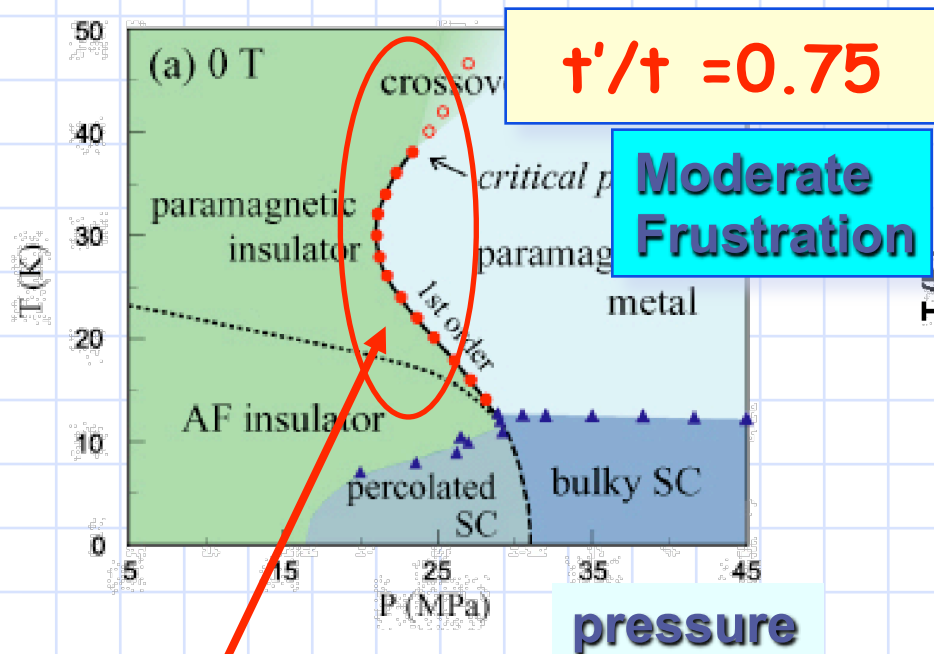
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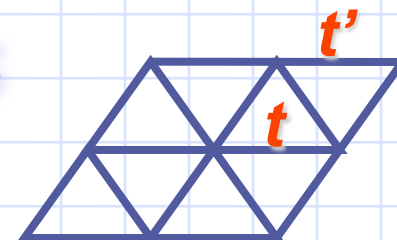
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Finite-T Mott transition
Reentrant behavior

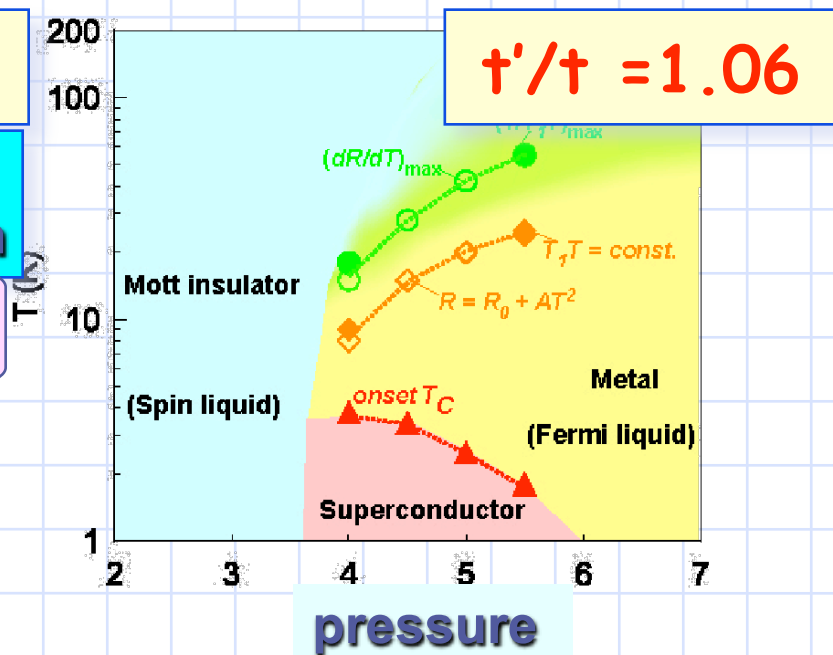
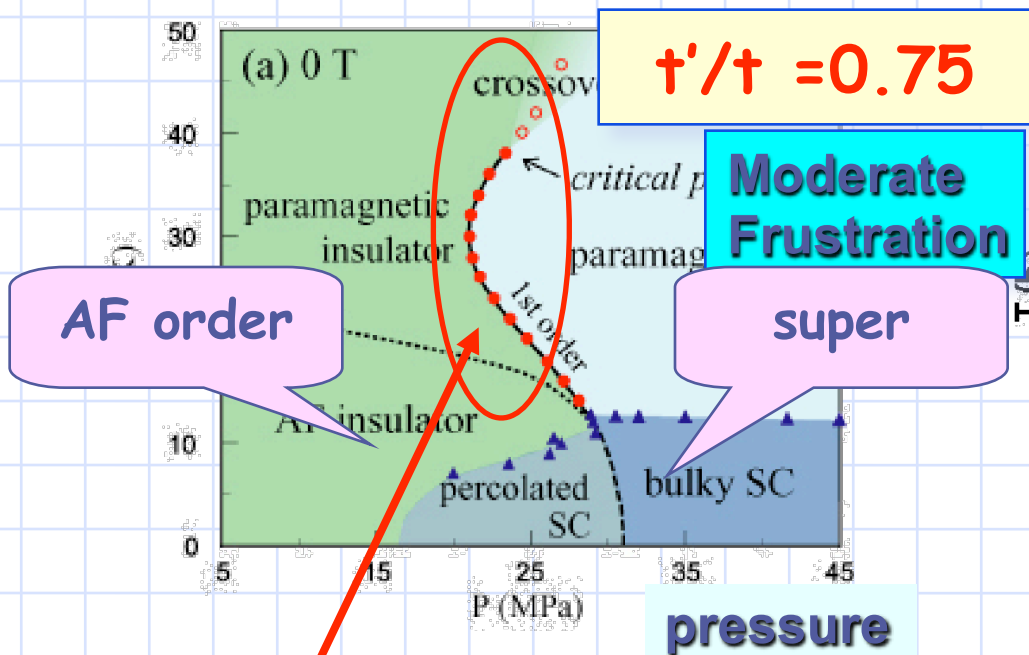
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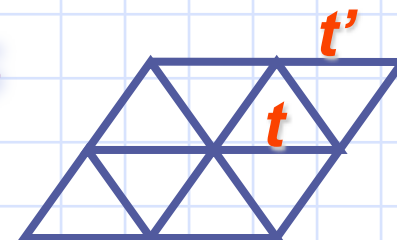
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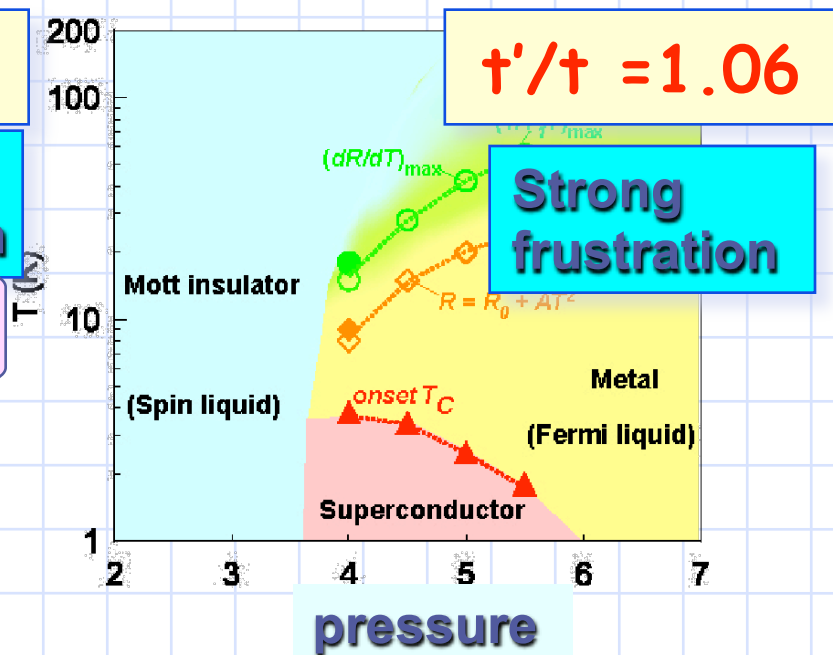
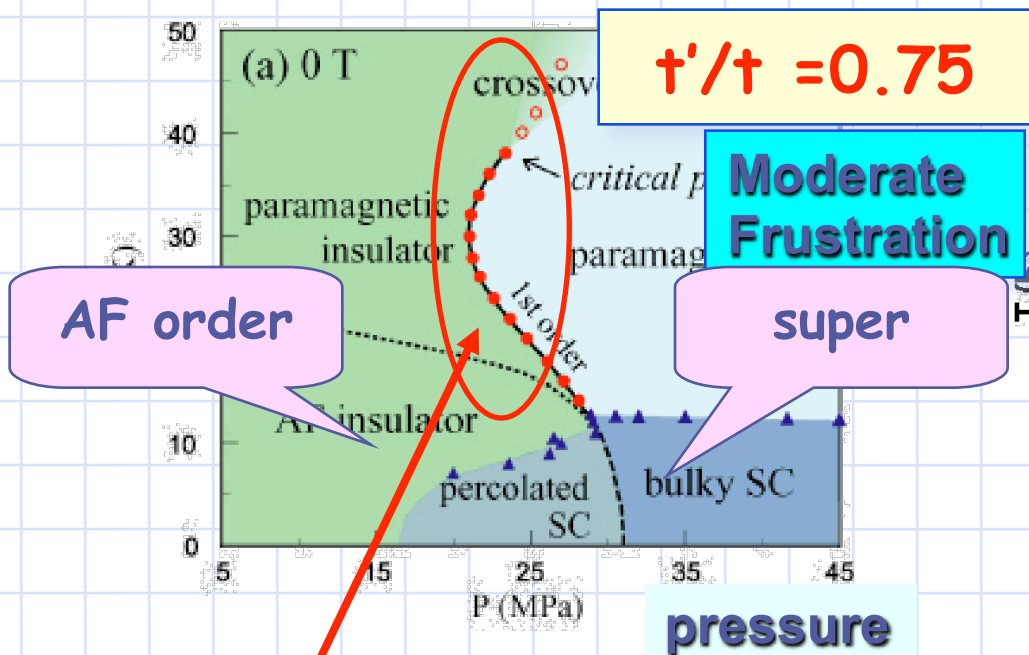
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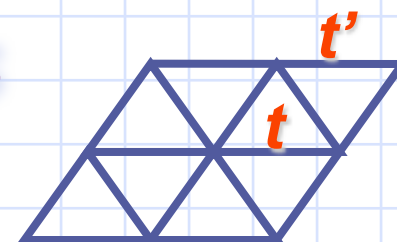
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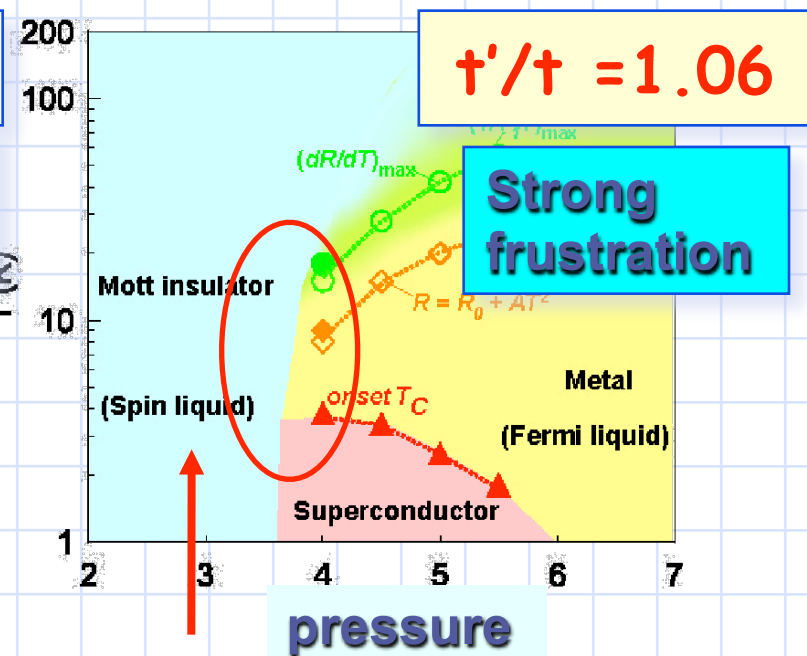
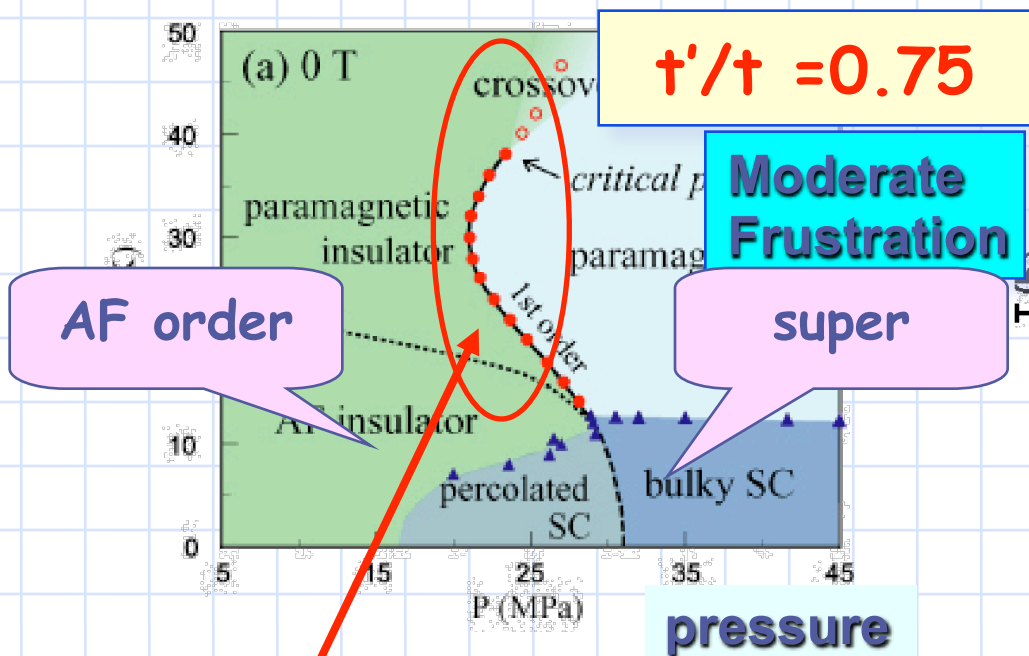
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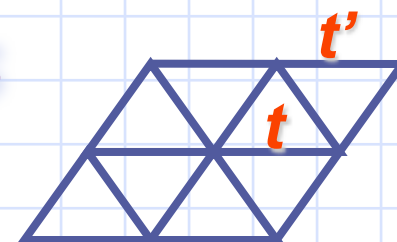


Finite-T Mott transition
Reentrant behavior

Spin liquid state
No Reentrant behavior

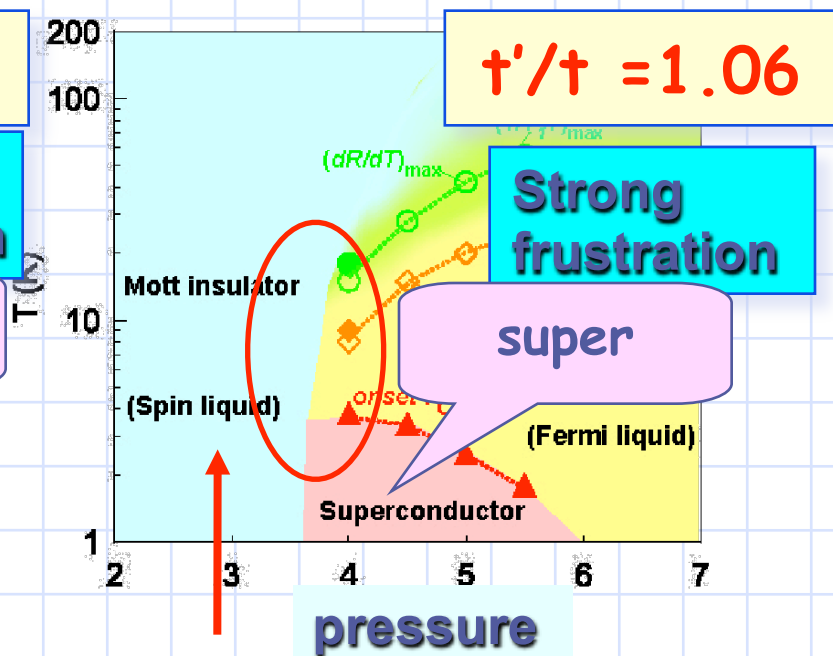
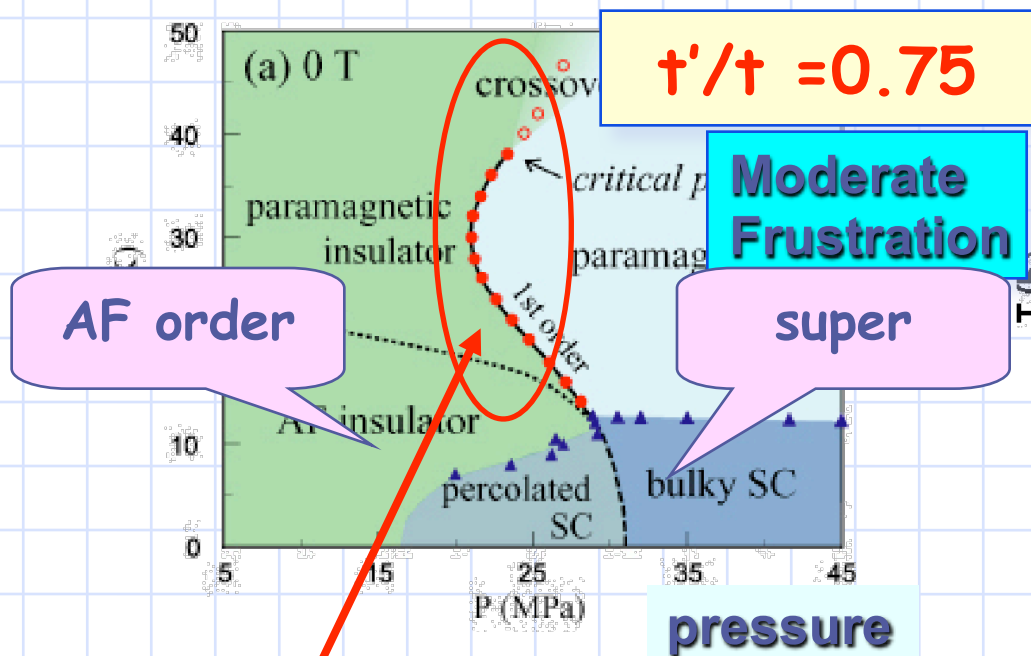
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Finite-T Mott transition
Reentrant behavior

Spin liquid state
No Reentrant behavior

Outline

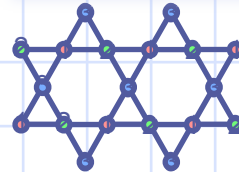
Frustrated Electron Systems in 2D

Mott transition with Frustration

Hubbard Model

On-site repulsion

Kagome



Triangular



Common to Mott transition with frustration

Example

Reentrant behavior



Outline

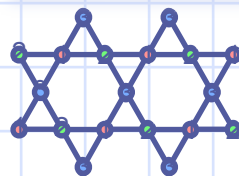
Frustrated Electron Systems in 2D

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Triangular



Itineracy vs Frustration

Anomalous properties near MIT

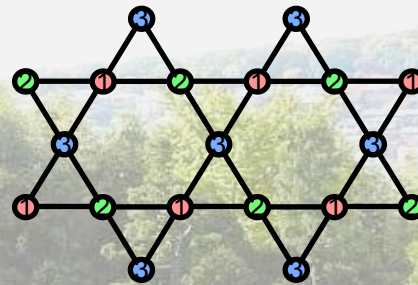
Common to Mott transition with frustration

Example

Reentrant behavior



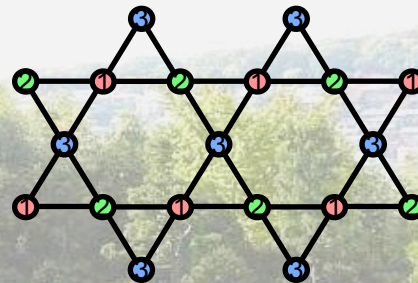
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Ohashi et al. PRL (2006)

Kagome-lattice systems

Mott transition with Frustration



Ohashi et al. PRL (2006)

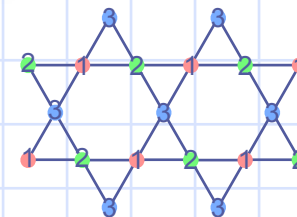
2D correlated systems Frustration

Kagome lattice Hubbard model

Imai, NK, Tsunetsugu(2003) FLEX

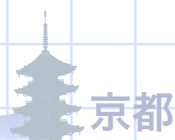
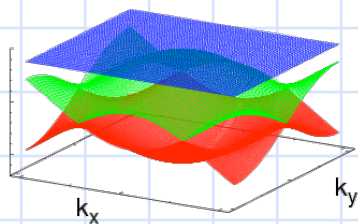
Koshibae - Maekawa (2003) Co superconductor

Bulut, Koshibae, Maekawa (2005) QMC



3-band system

Co oxide
Superconductor



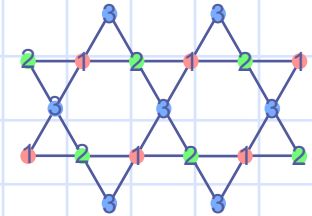
2D correlated systems Frustration

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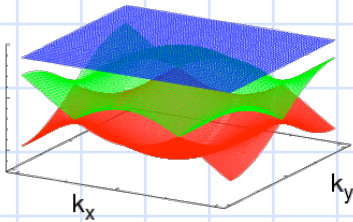
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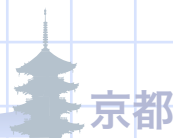
Co oxide
Superconductor



Metallic state near MIT?

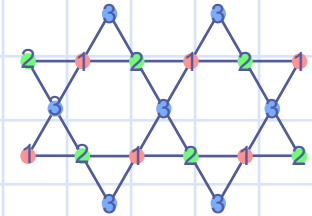
Ohashi et al. (2006) Cluster DMFT

Kuratani et al.(2006) Variational MC



2D correlated systems Frustration

Kagome lattice Hubbard model



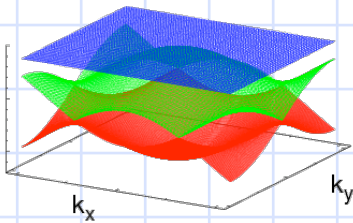
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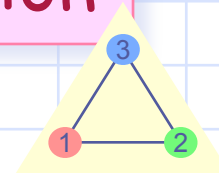


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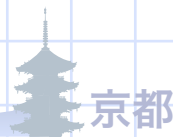
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Frustration



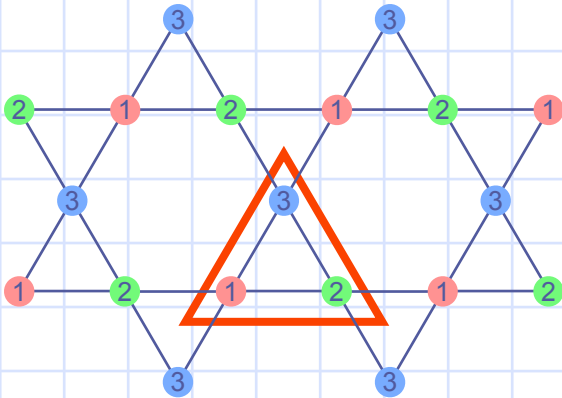
Cluster DMFT



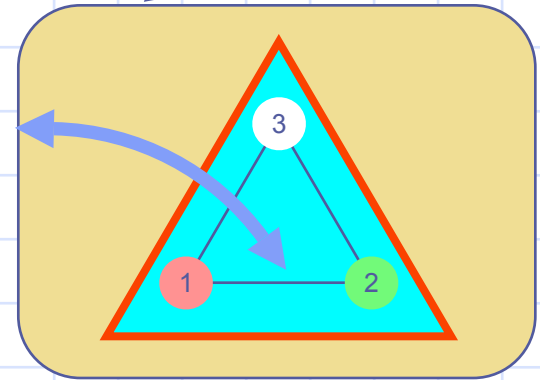
Cellular DMFT

Hubbard Model on Kagome lattice

Original Kagome lattice Hubbard model



Three sites cluster



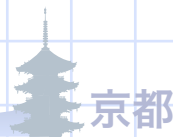
Effective cluster model



QMC method

(Hirsch-Fye algorithm)

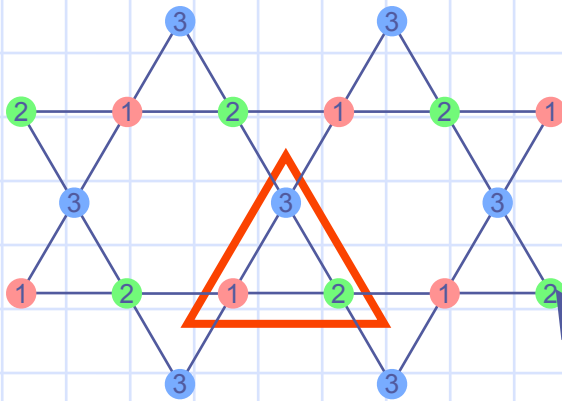
- Strong correlation
- Frustration



Cellular DMFT

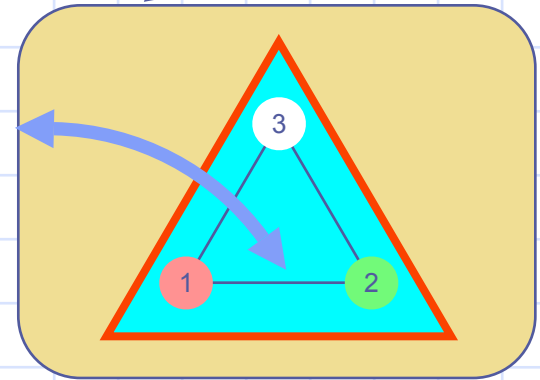
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Self-consistent
†

Three sites cluster

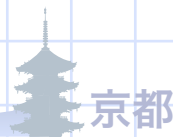


Effective cluster model

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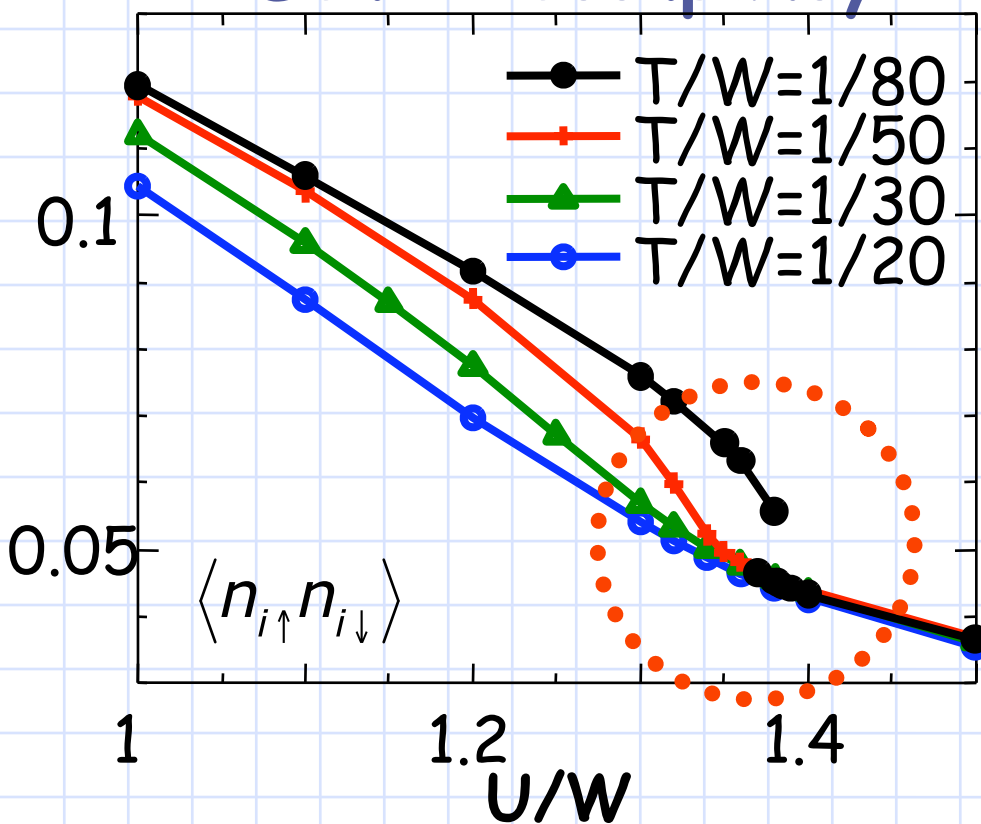
(Hirsh-Fye algorism)



Hubbard
half-filling

Mott transition

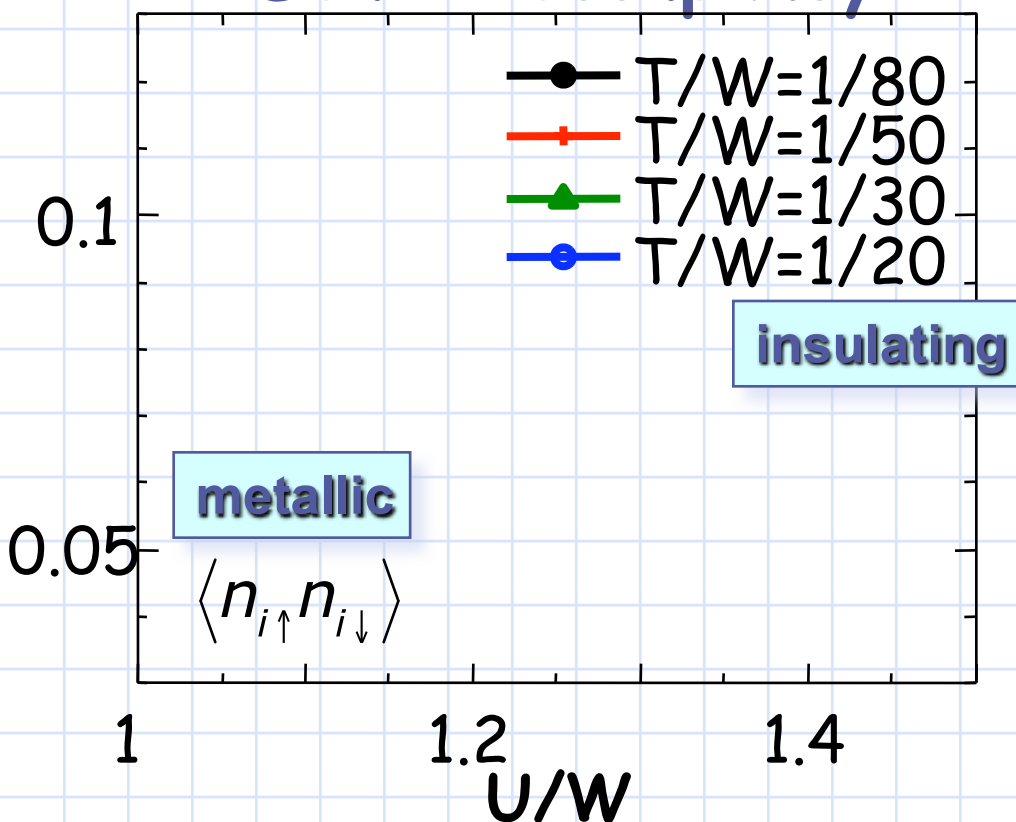
Double occupancy

(bandwidth $W=6t$)

Mott transition

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Double occupancy



(bandwidth $W=6t$)

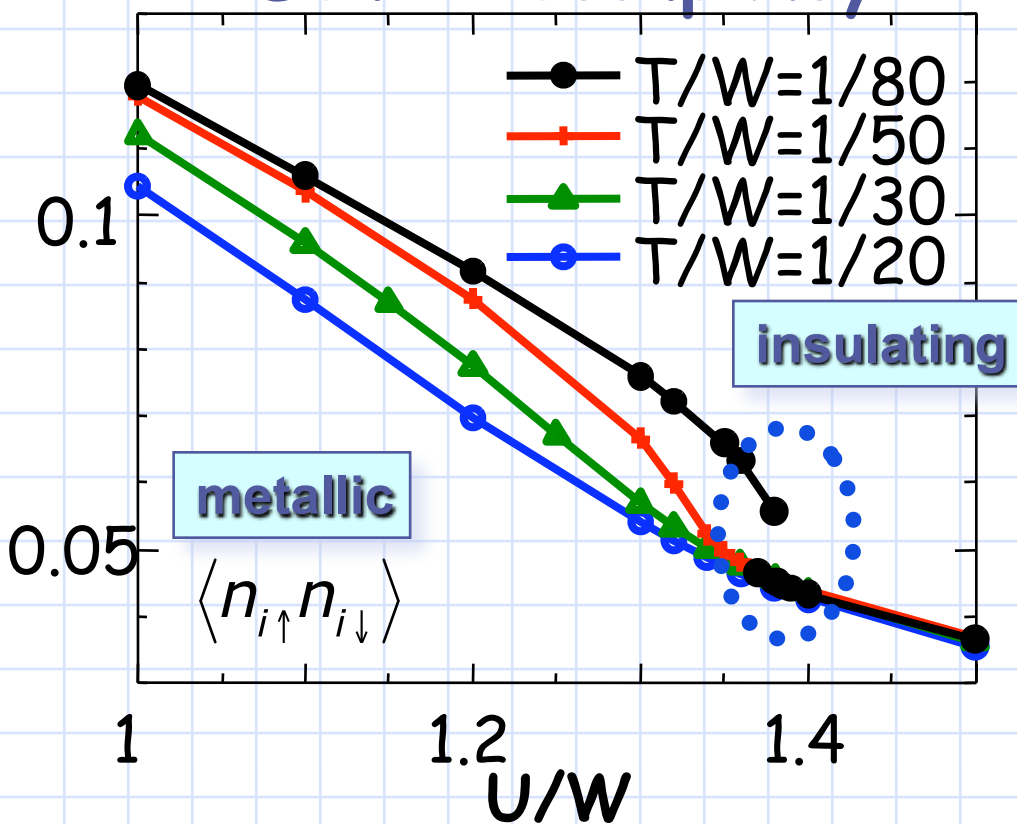
High temperature
 $T/W > 1/80$

Crossover: $U_c/W \sim 1.35$

Mott transition

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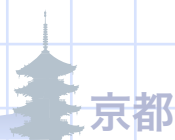
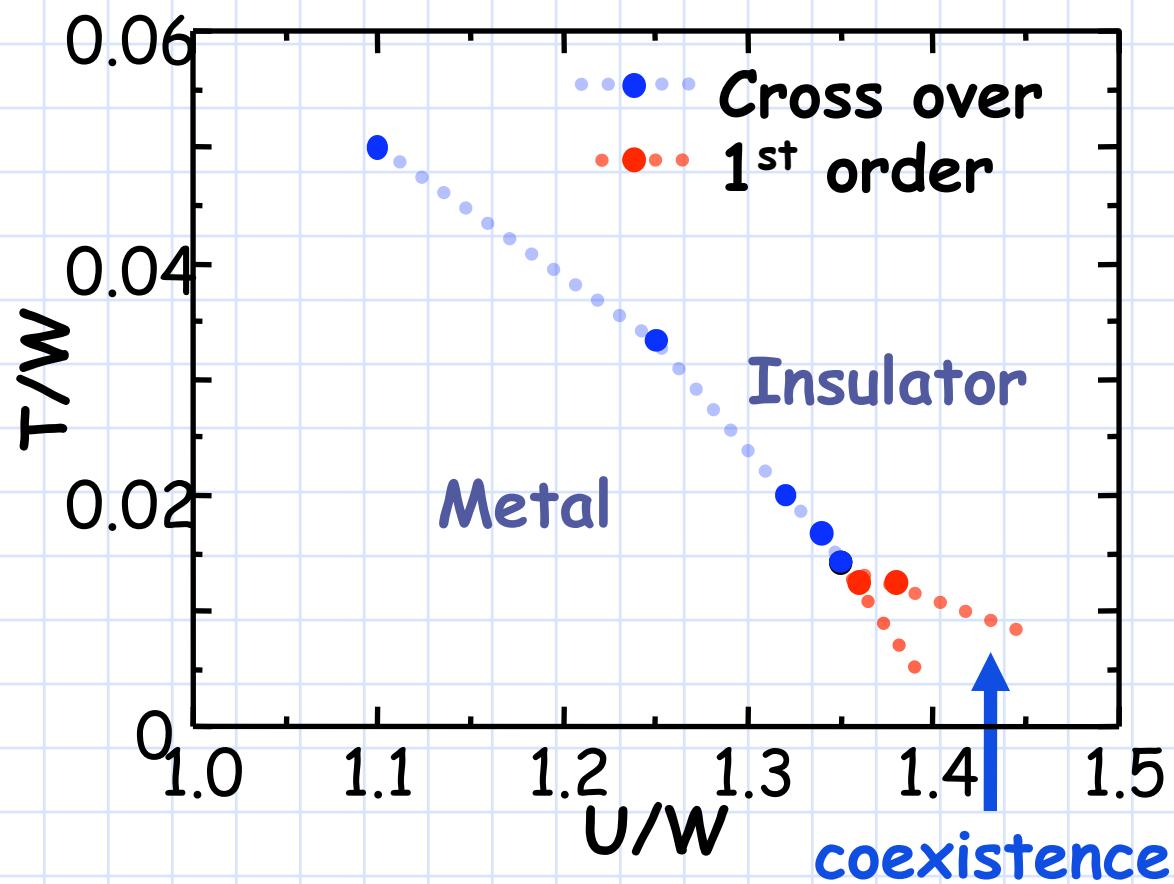
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Low temperature
 $T/W = 1/80$

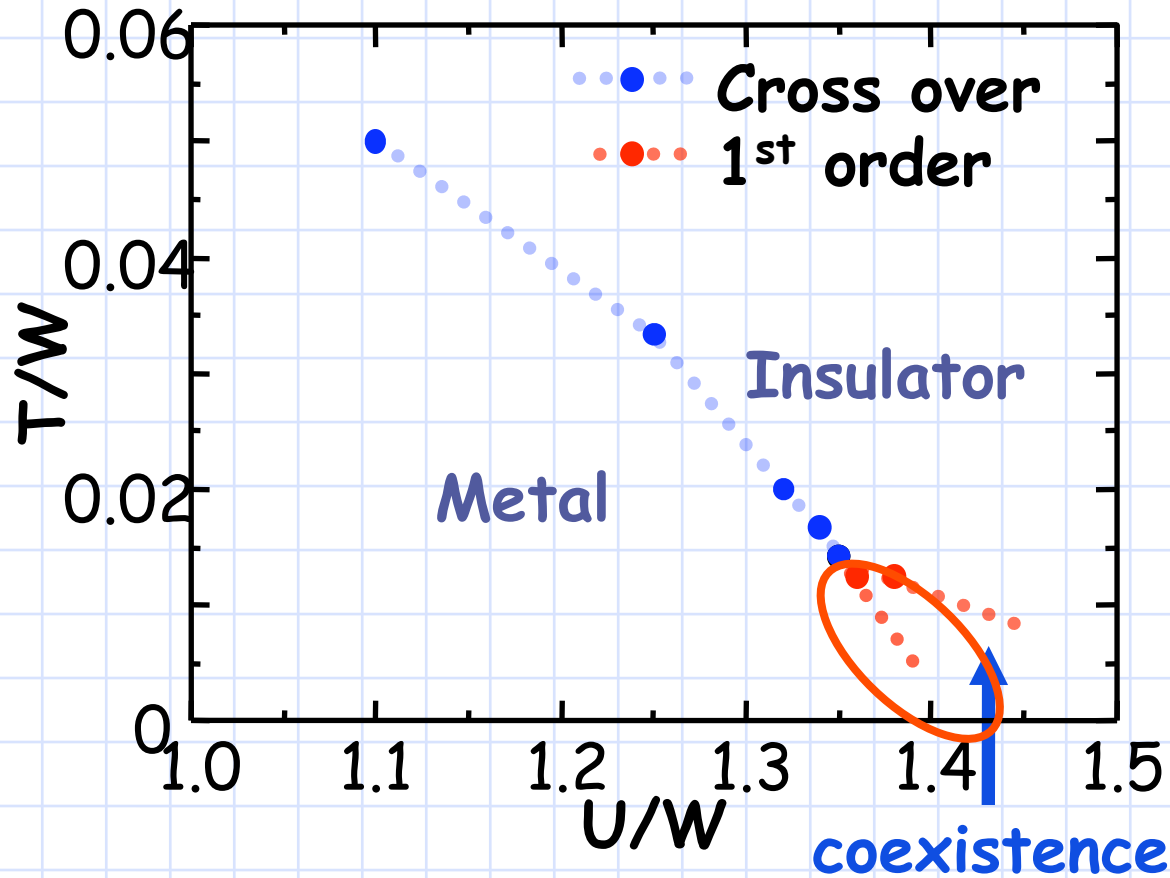
1st order transition with
hysteresis

$U_c/W \sim 1.37$

Phase diagram of MIT



Phase diagram of MIT



- Mott transition:
 $U_c/W \sim 1.4$

Large U_c

- Square lattice
(Cross over)

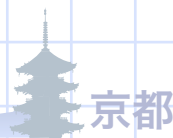
$U_c/W < 0.5$

Moukouri & Jarrell (2001).

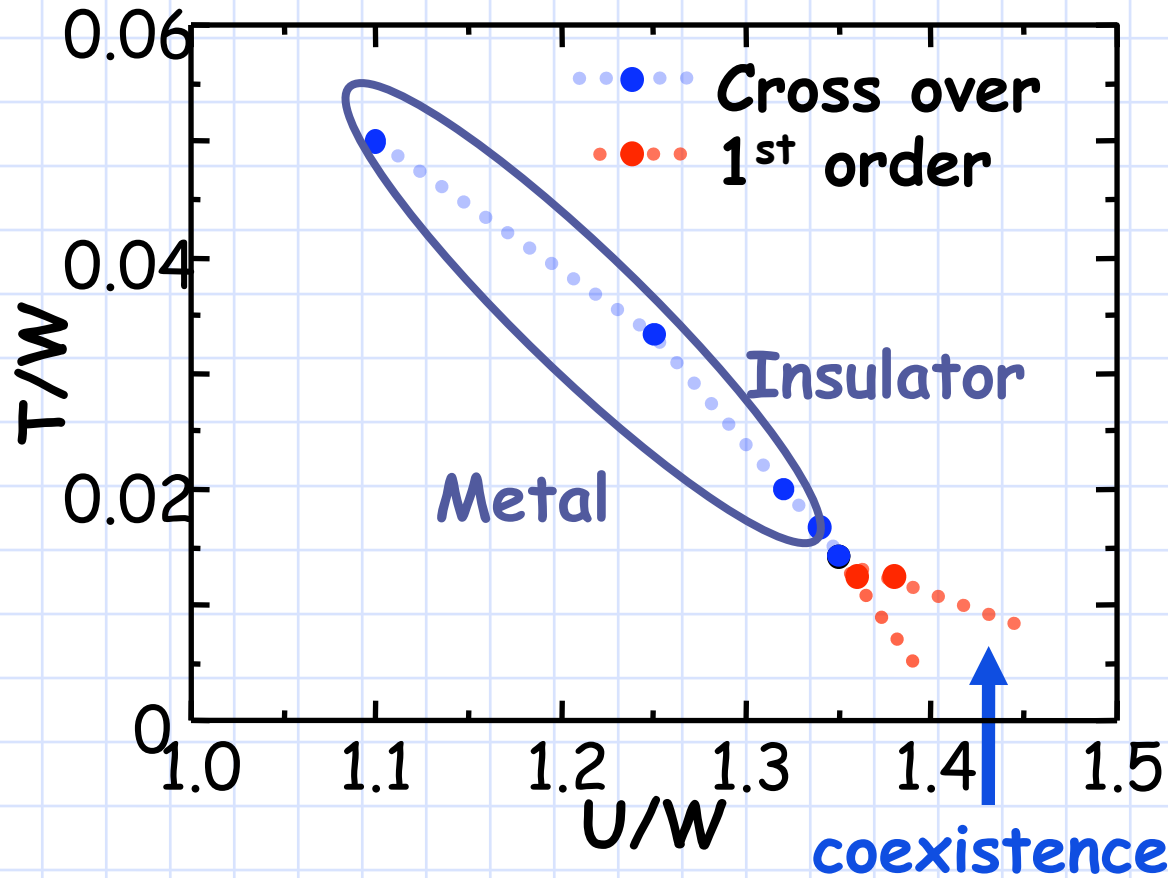
- triangular lattice

$U_c/W \sim 1.04$

Parcollet & Kotliar (2003).



Phase diagram of MIT



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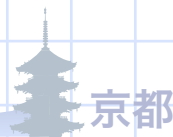
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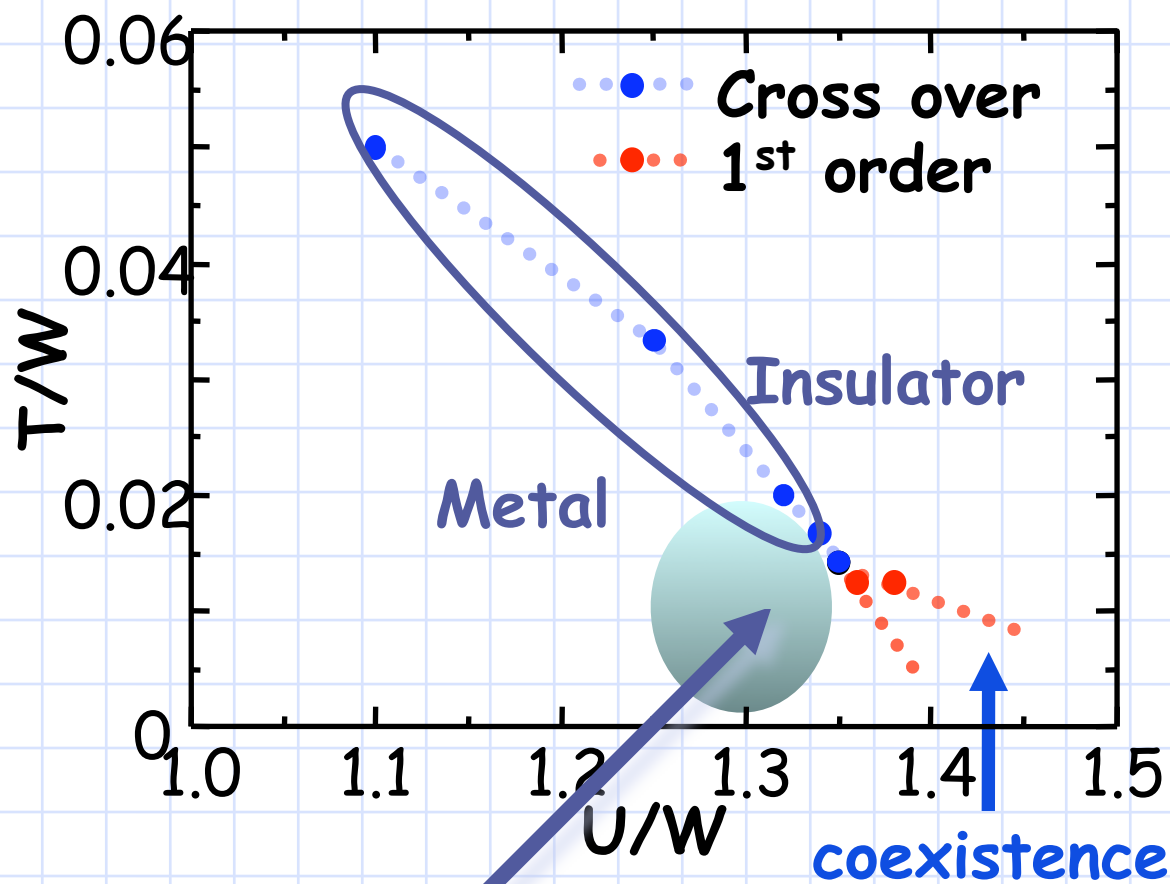
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Phase diagram of MIT



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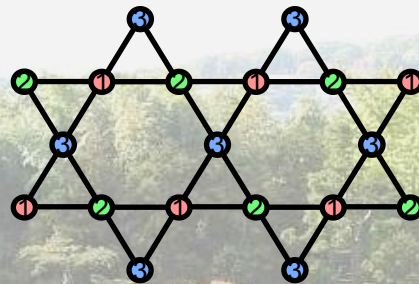
- triangular lattice

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Close to MIT:
anomalous metallic properties

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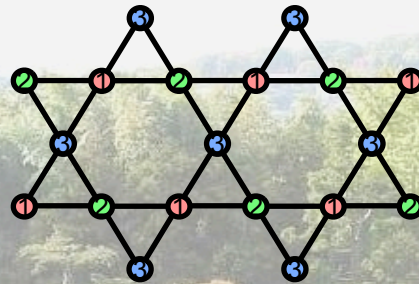


Ohashi et al. PRL (2006)

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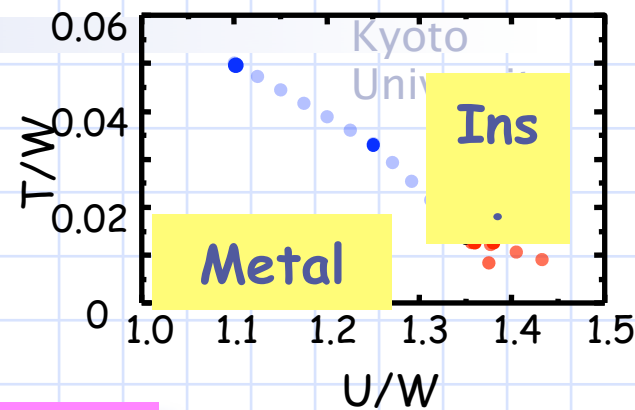
Anomalous metallic properties

Near Mott phase

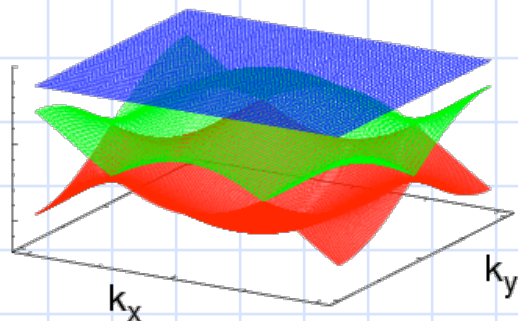


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Hubbard (half-filling)

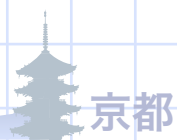
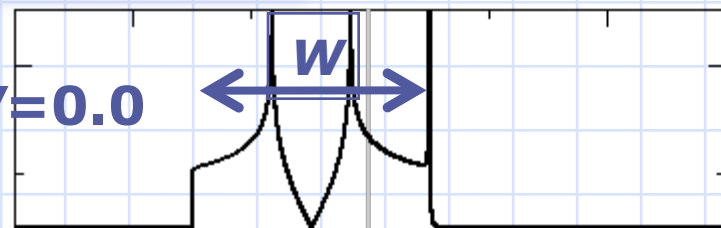


dispersion: $U=0$



DOS ($T/W = 1/80$)

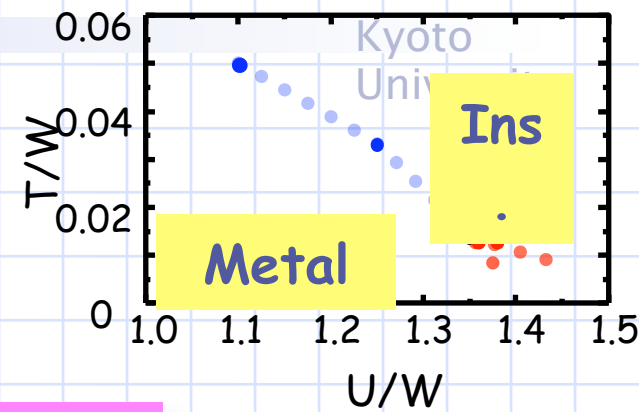
$U/W = 0.0$



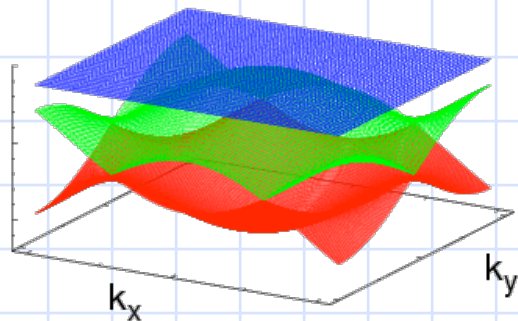
Bandwidth
: $W=6t$

Density of states

Hubbard (half-filling)

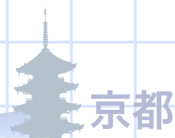
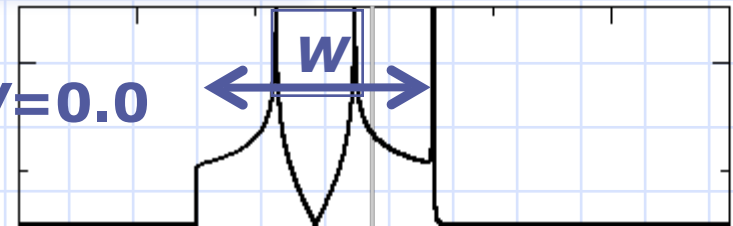


dispersion: $U=0$



DOS ($T/W = 1/80$)

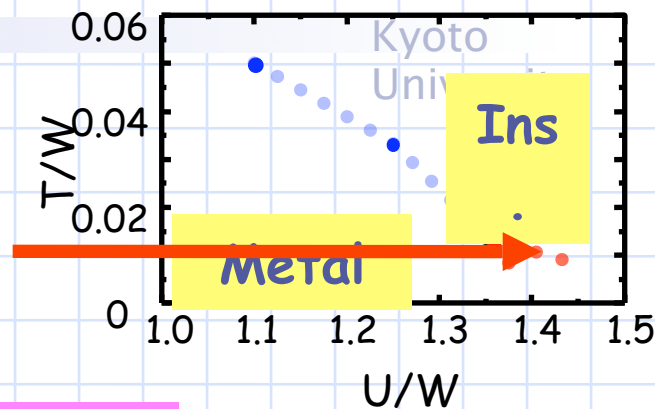
$U/W = 0.0$



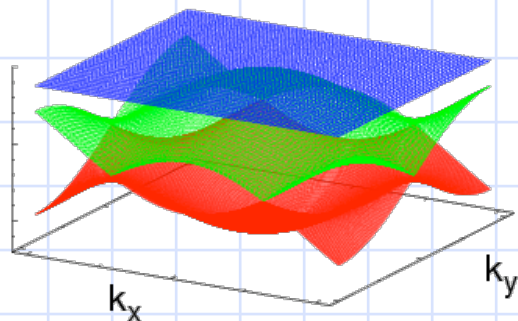
Bandwidth
: $W=6t$

Density of states

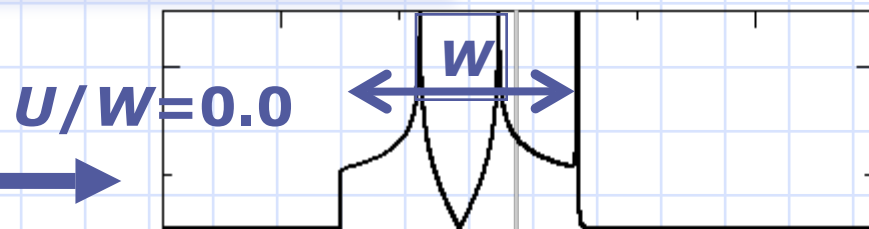
Hubbard (half-filling)



dispersion: $U=0$



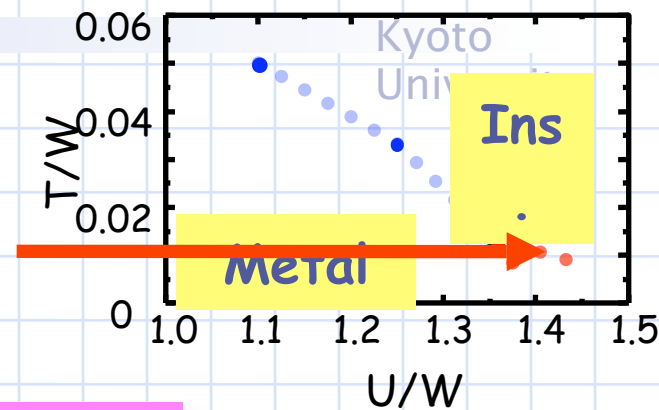
DOS ($T/W = 1/80$)



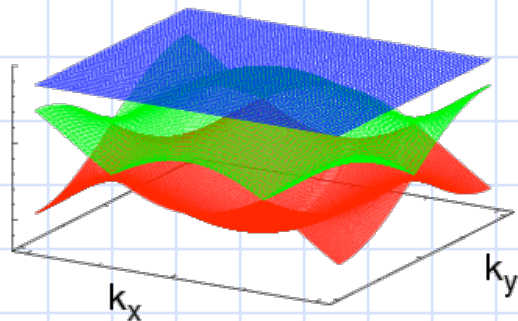
Bandwidth
: $W=6t$

Density of states

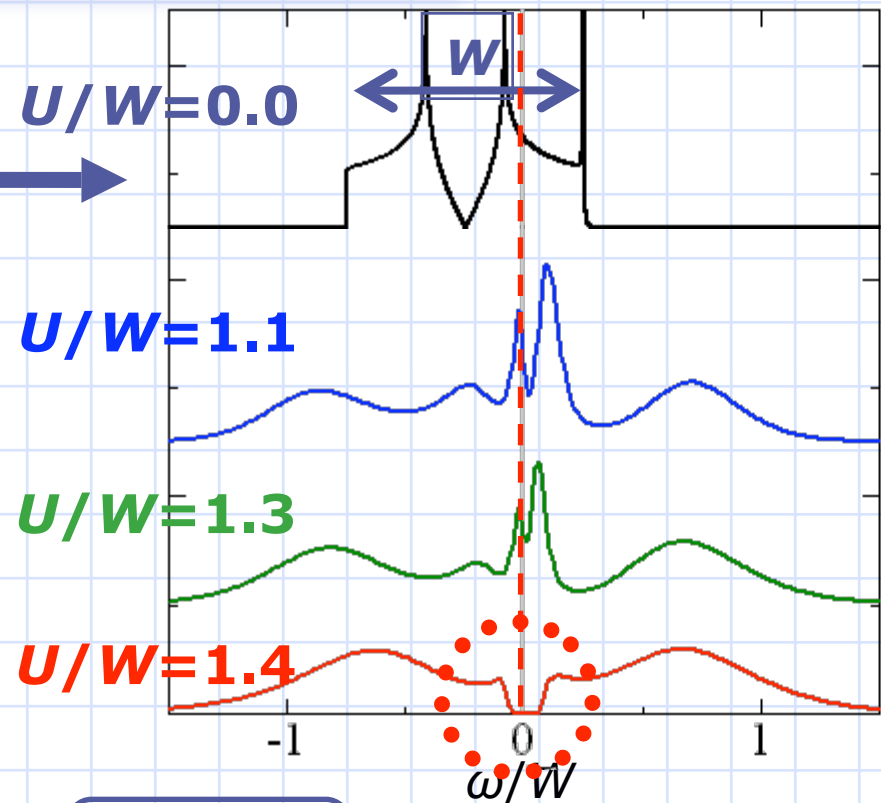
Hubbard (half-filling)



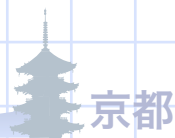
dispersion: $U=0$



DOS ($T/W = 1/80$)

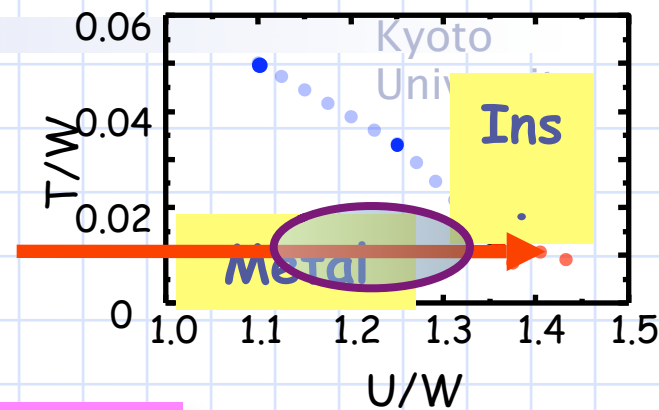


Bandwidth
: $W=6t$

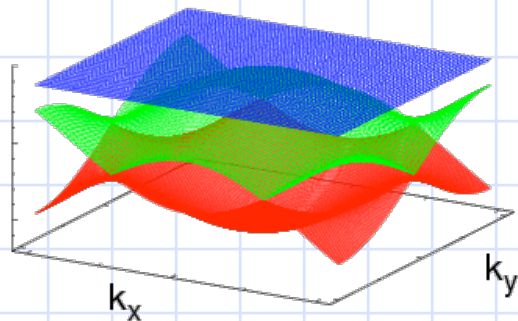


Density of states

Hubbard (half-filling)



dispersion: $U=0$



DOS ($T/W = 1/80$)

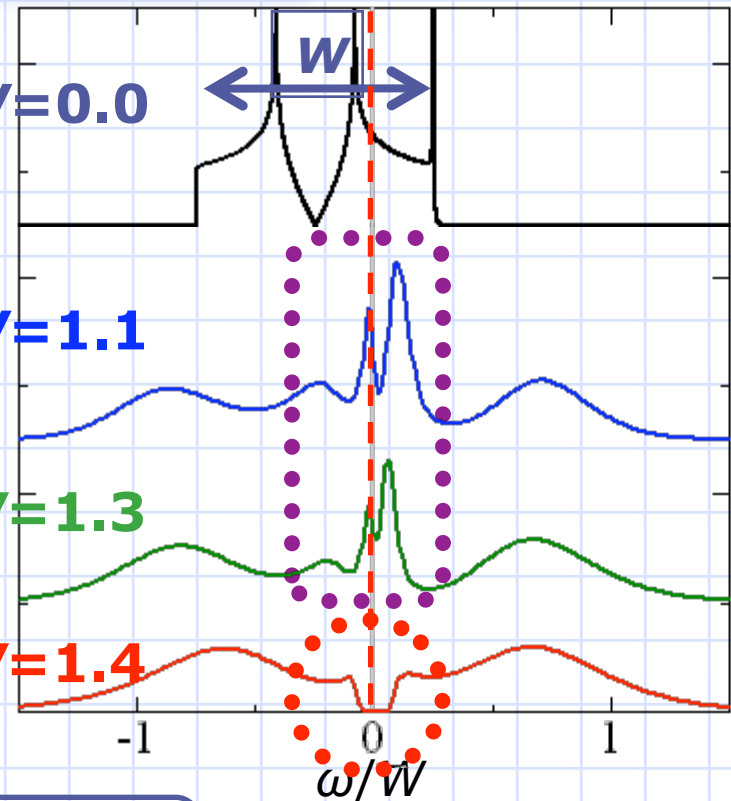
metal

$U/W = 0.0$

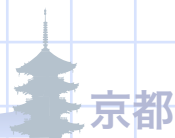
$U/W = 1.1$

$U/W = 1.3$

$U/W = 1.4$

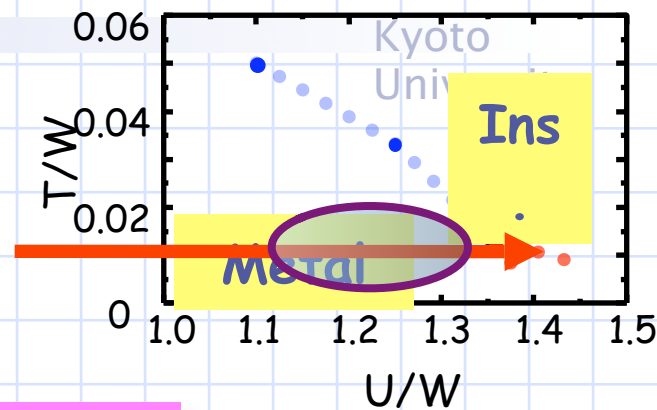


Bandwidth
: $W = 6t$

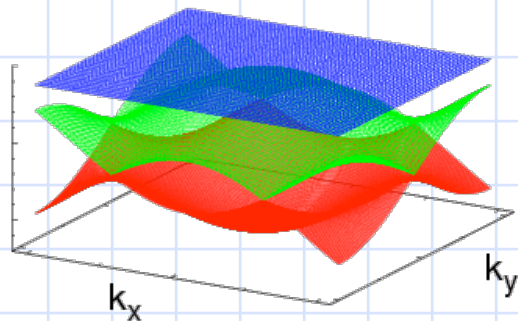


Density of states

Hubbard (half-filling)



dispersion: $U=0$



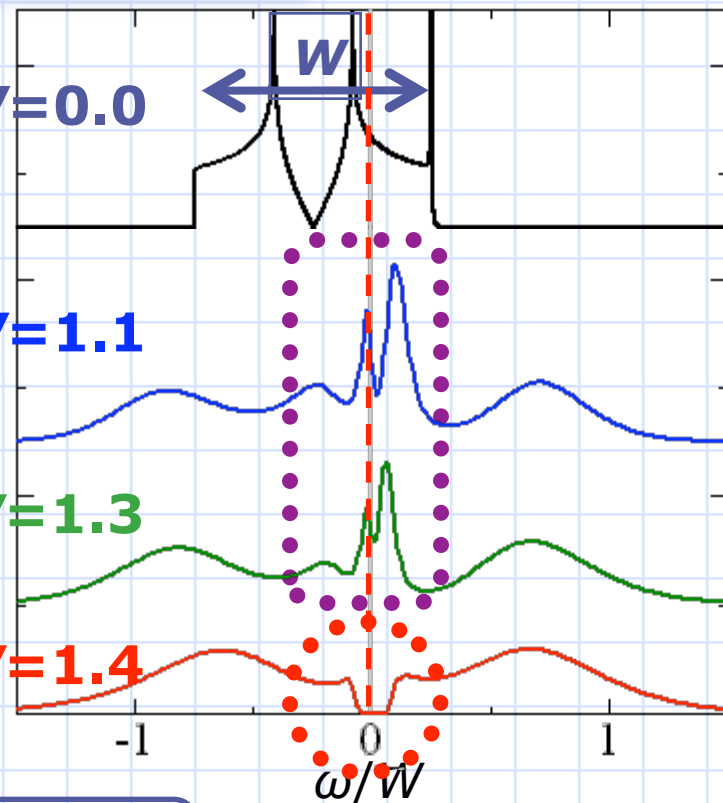
DOS ($T/W = 1/80$)

$U/W = 0.0$

$U/W = 1.1$

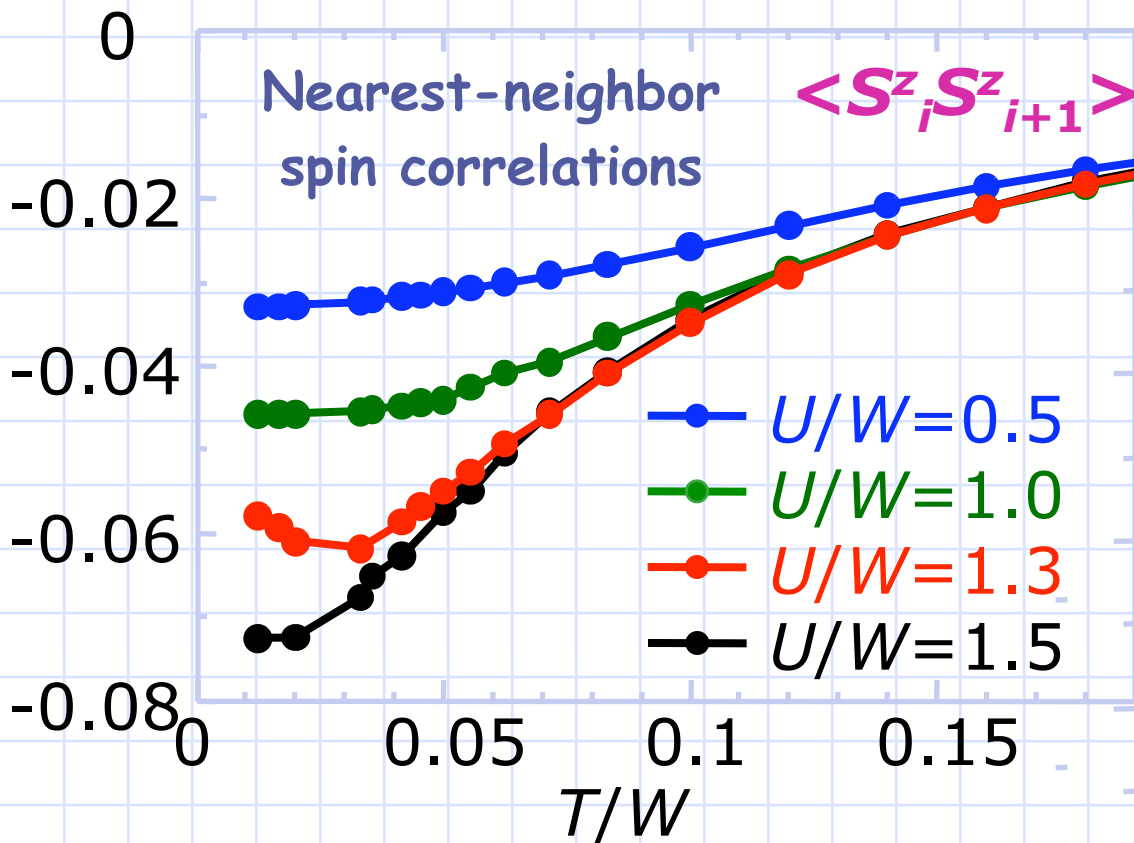
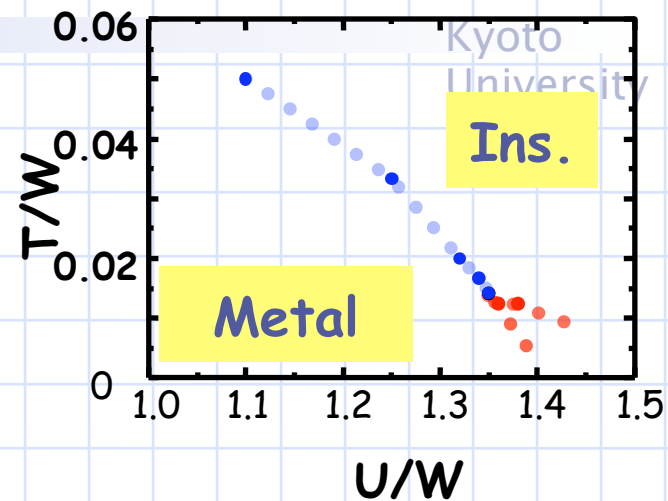
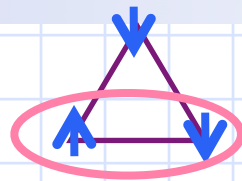
$U/W = 1.3$

$U/W = 1.4$

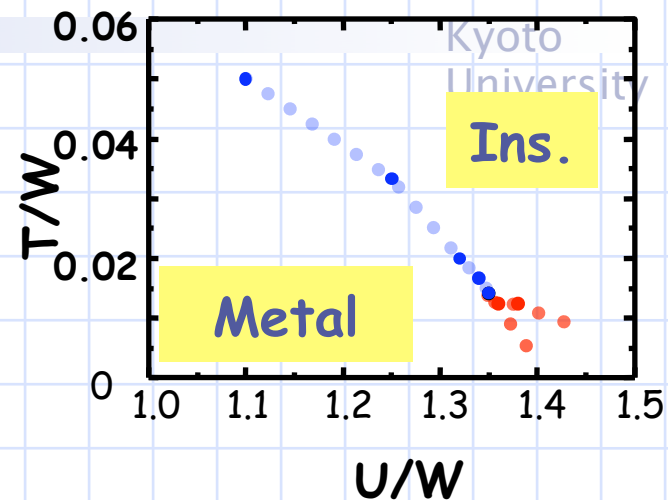
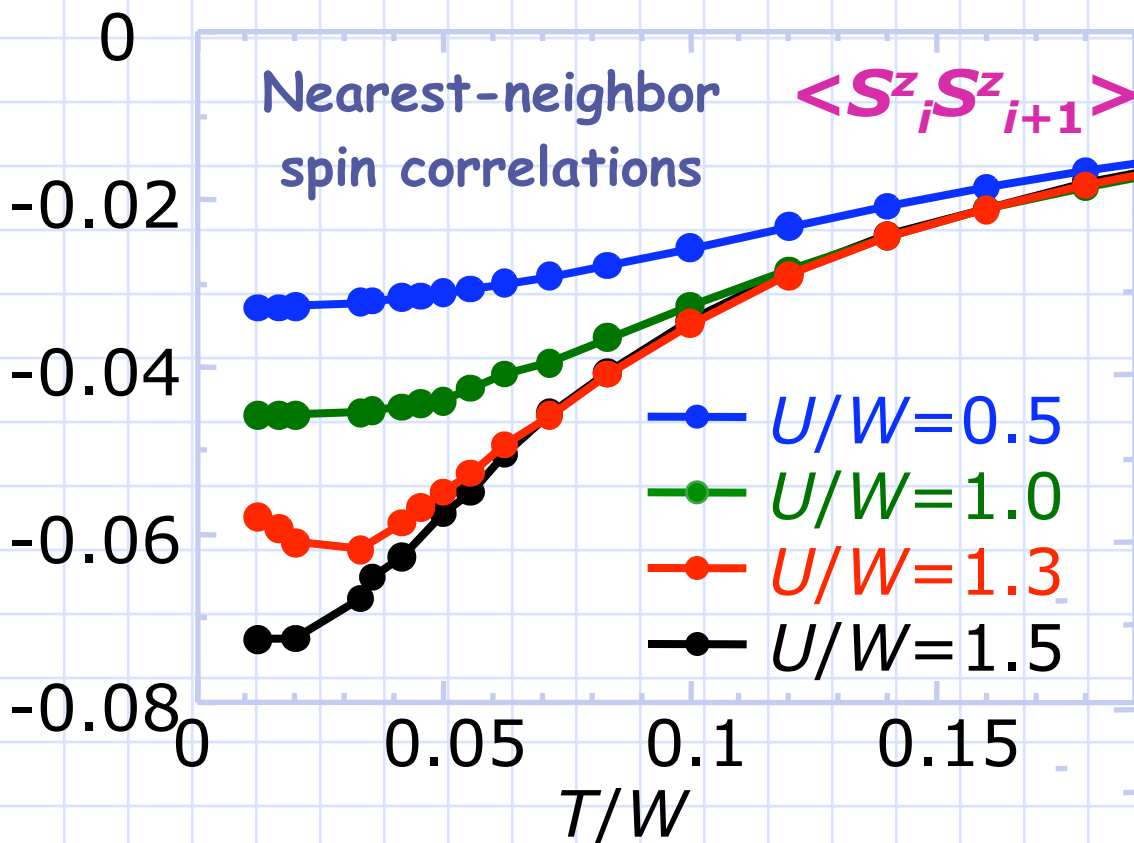
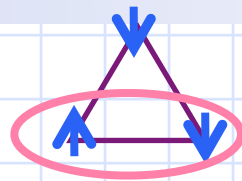


- all bands renormalized
- multi-band heavy fermions

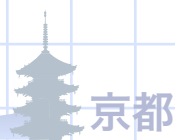
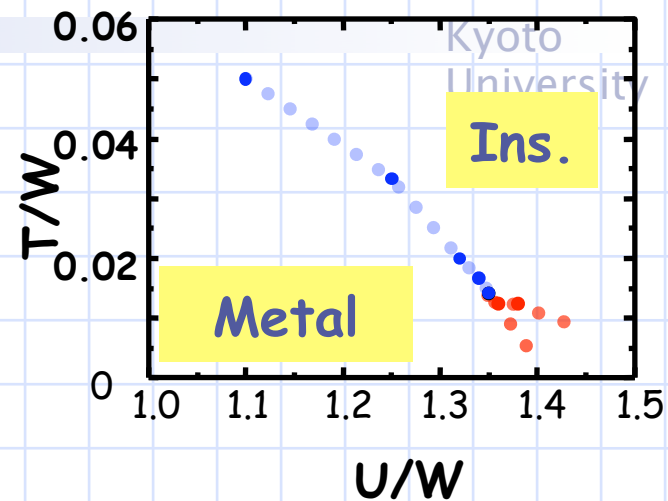
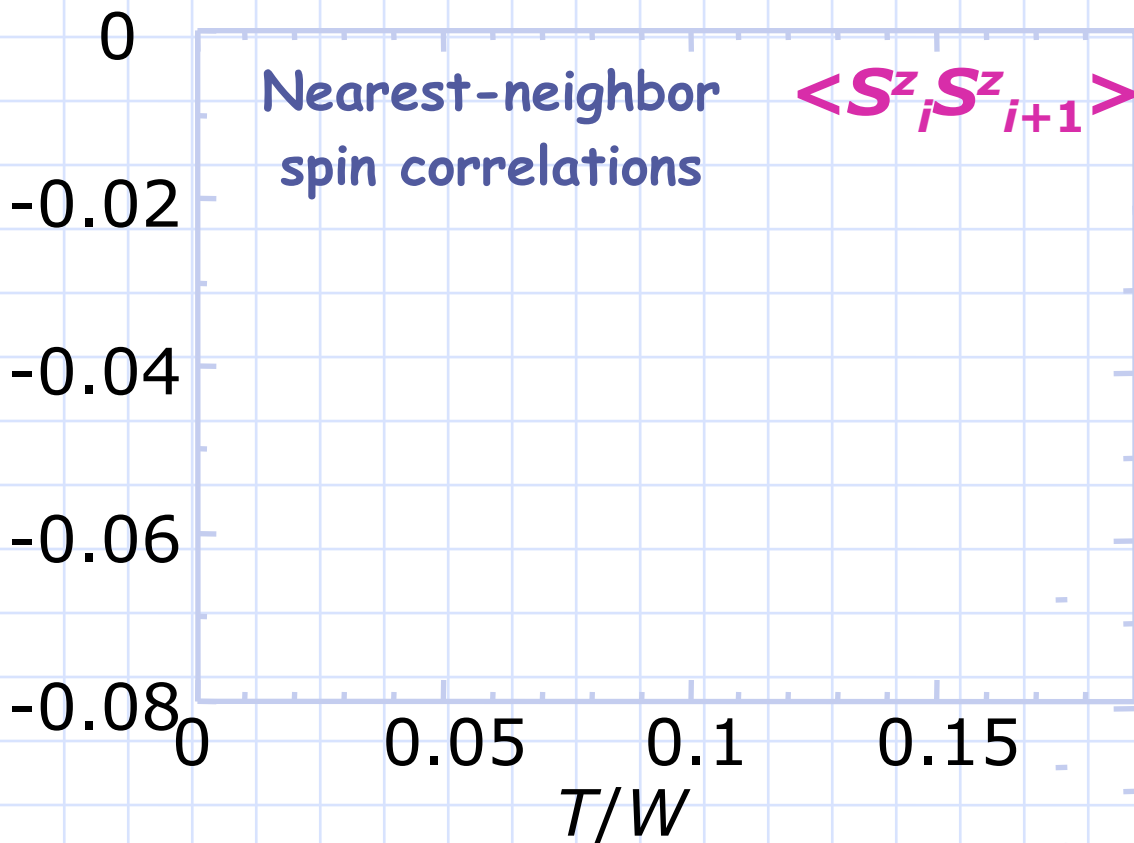
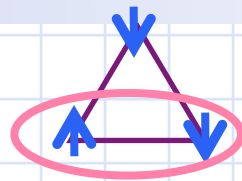
Bandwidth
: $W = 6t$



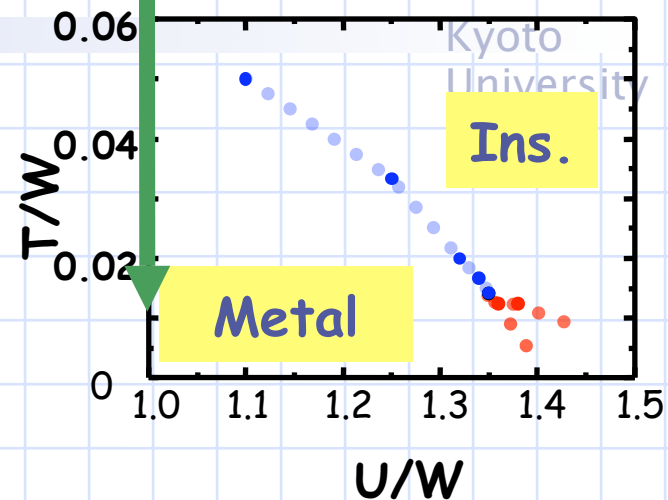
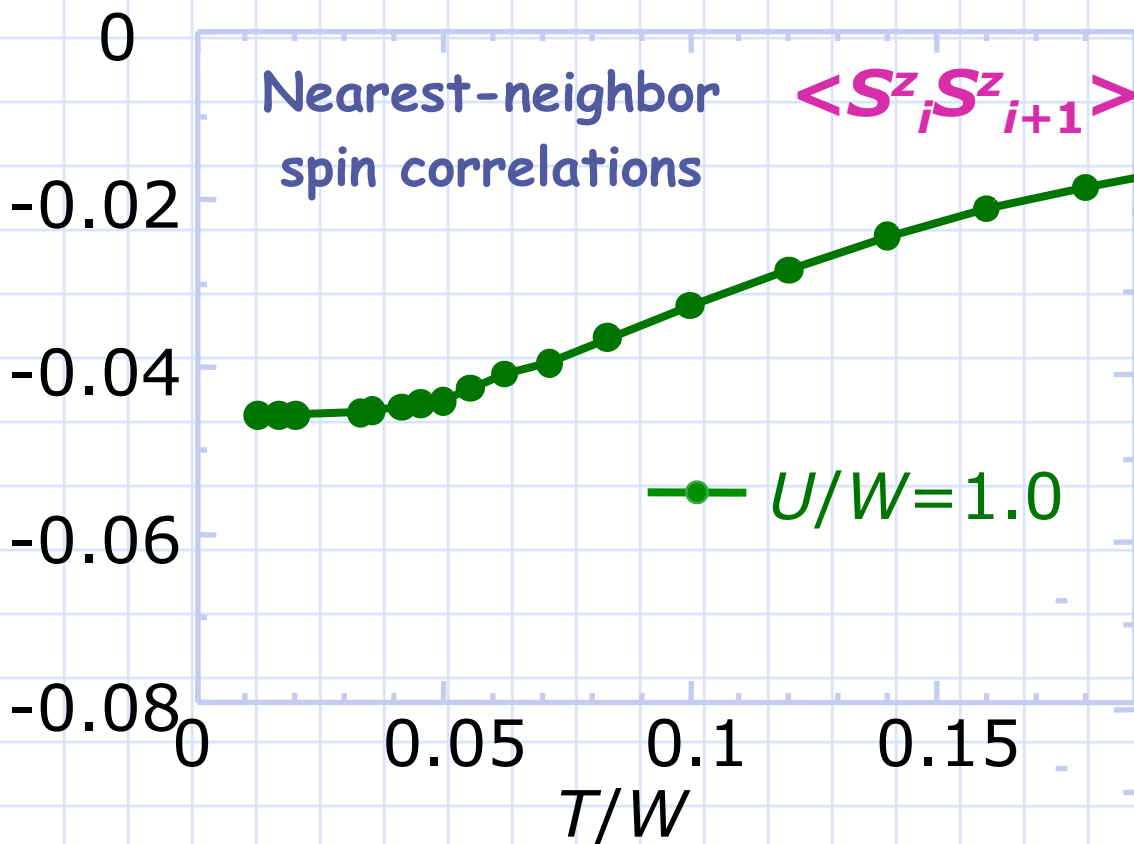
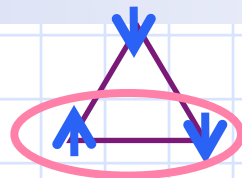
Unusual behavior in spin correlations



Unusual behavior in spin correlations



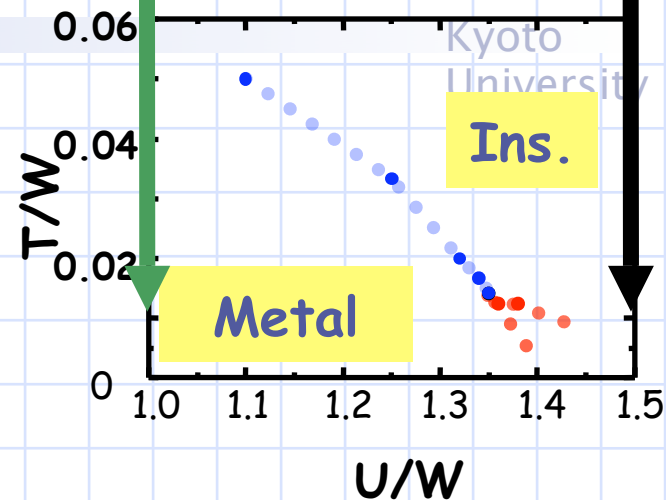
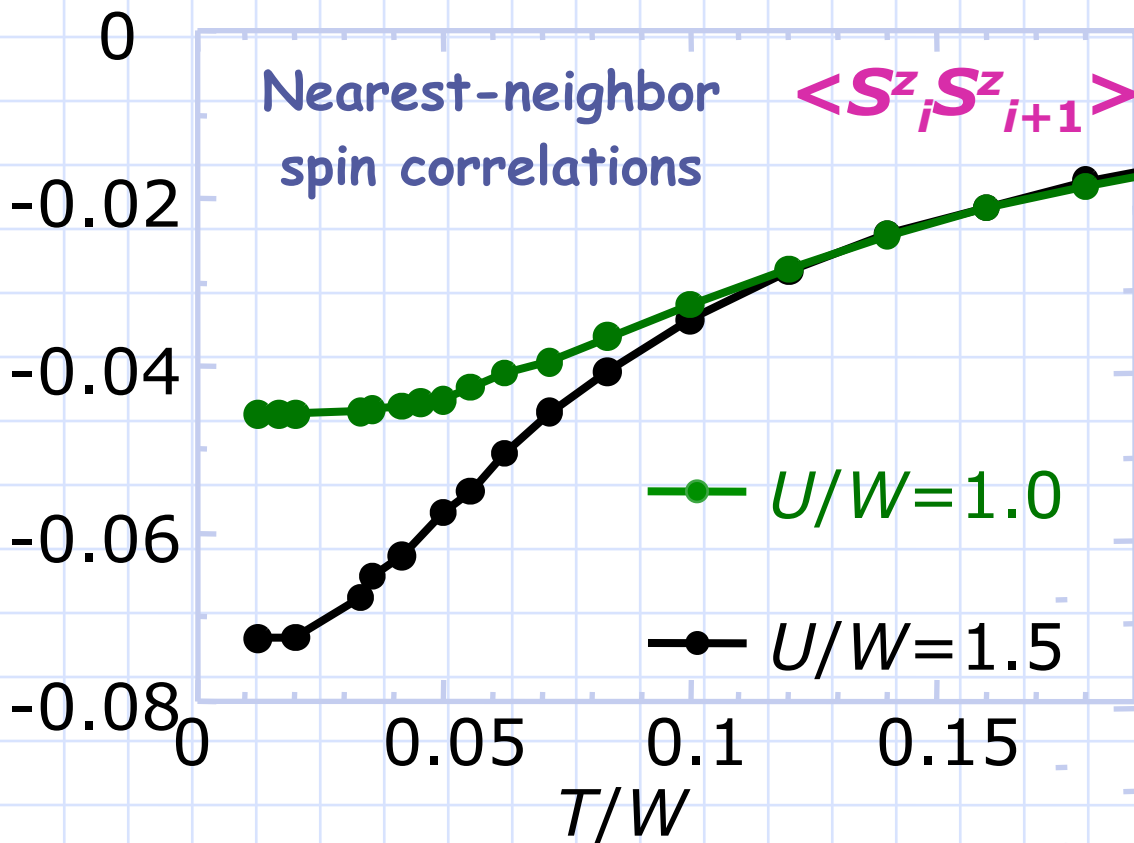
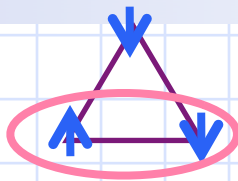
Unusual behavior in spin correlations



Metallic phase
 \Rightarrow weak AF correlations



Unusual behavior in spin correlations

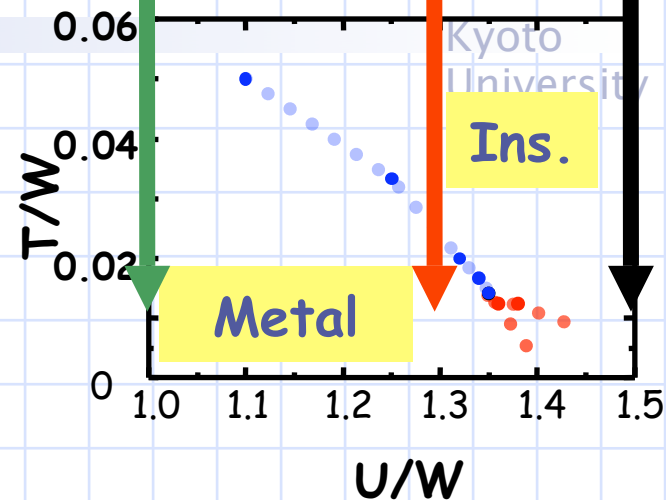
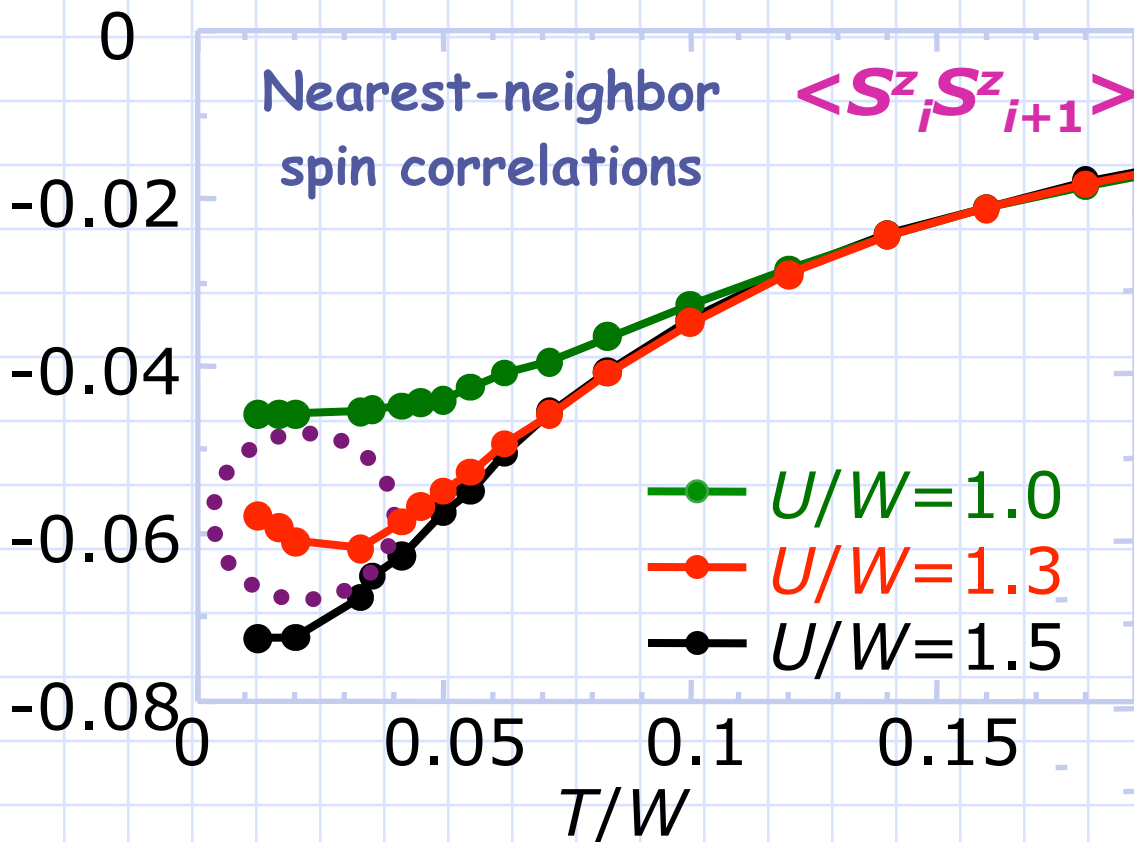
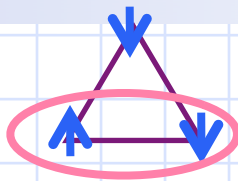


Metallic phase
⇒ weak AF correlations

Insulating phase
⇒ Strong frustration
RVB-like insulator



Unusual behavior in spin correlations



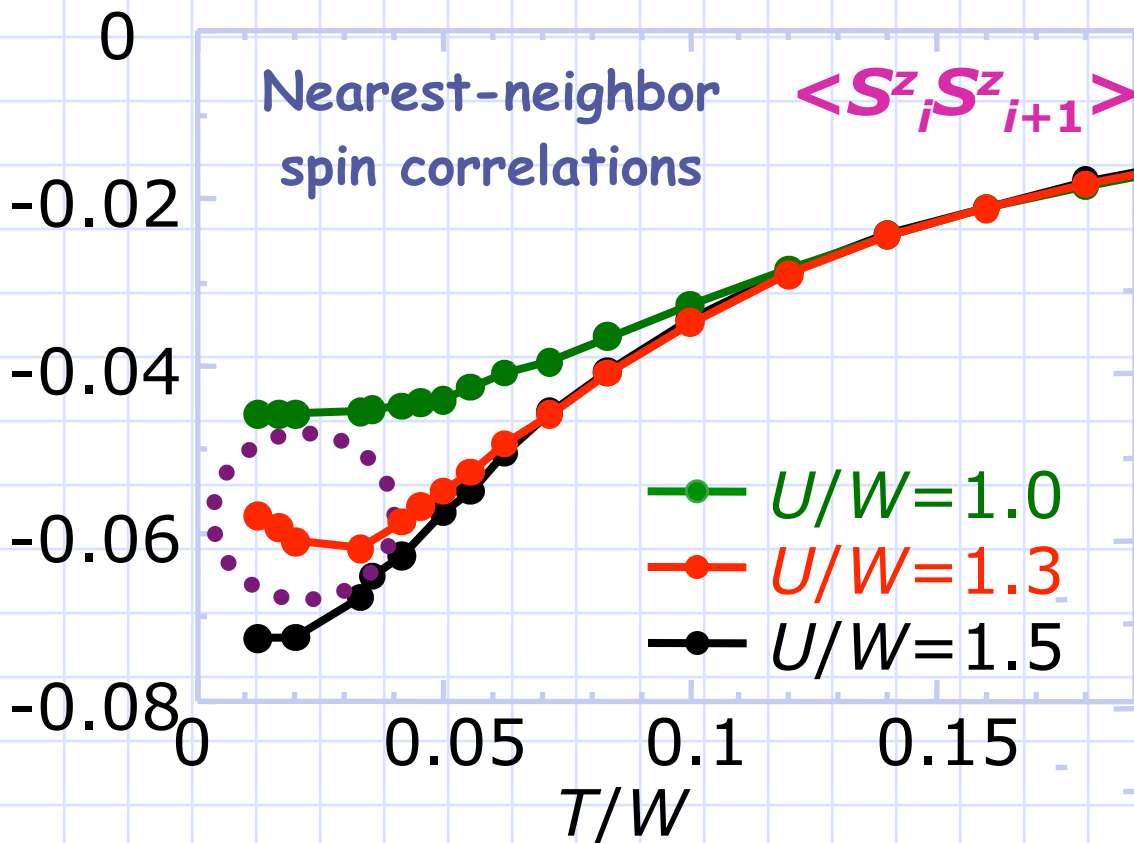
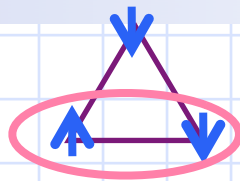
Metallic phase
⇒ weak AF correlations

Insulating phase
⇒ Strong frustration
RVB-like insulator

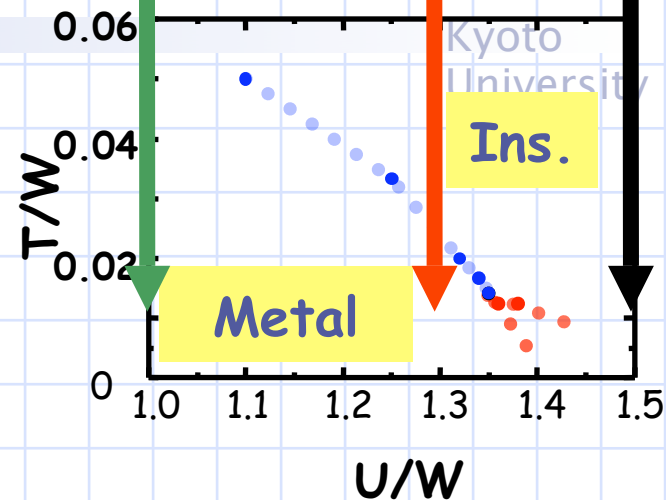
Metallic phase near MIT
Non-monotonic behavior
⇒ AF correlations
suppressed at low T!



Unusual behavior in spin correlations



Recovery of coherence
Relaxation of frustration



Metallic phase
⇒ weak AF correlations

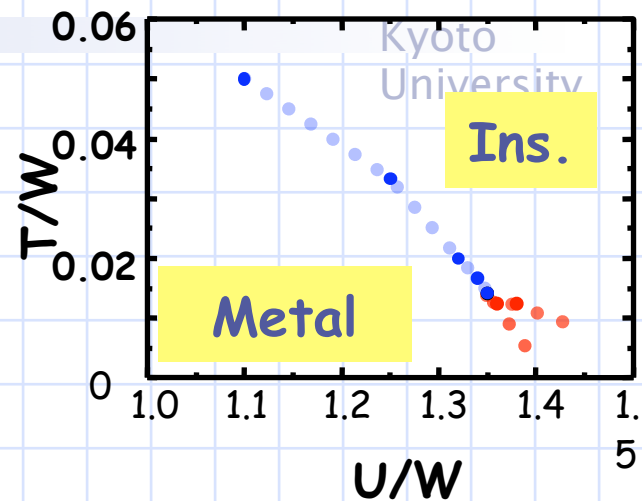
Insulating phase
⇒ Strong frustration
RVB-like insulator

Metallic phase near MIT
Non-monotonic behavior
⇒ AF correlations
suppressed at low T!

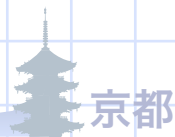
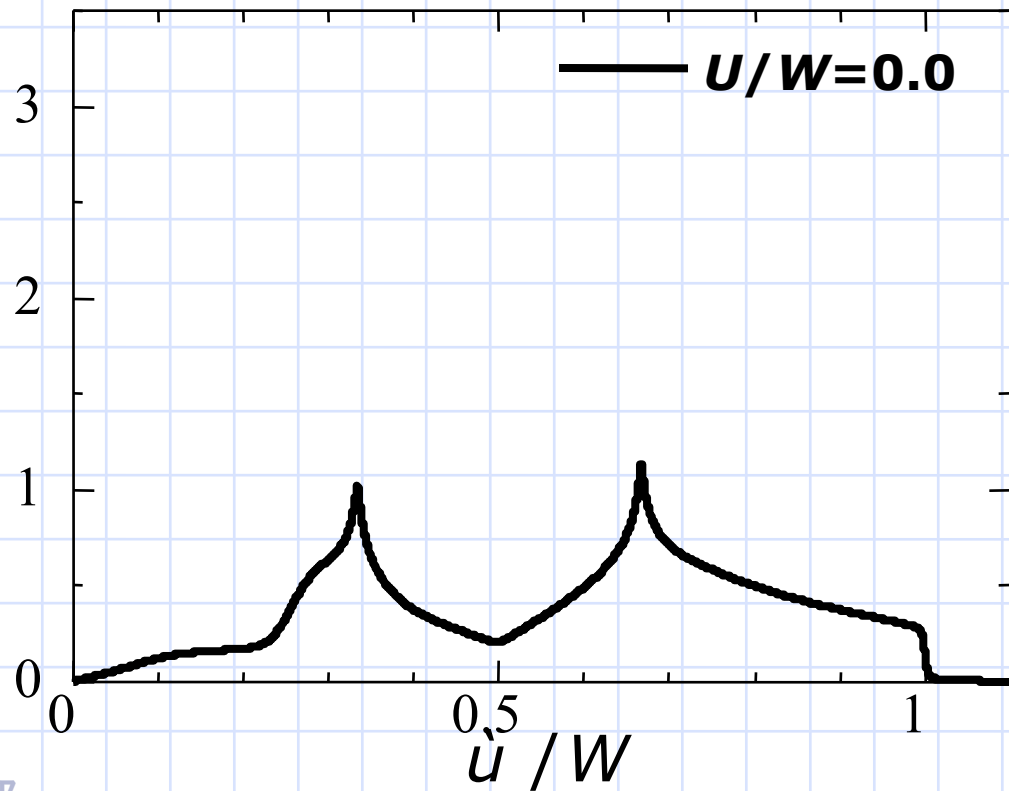
Dynamical spin susceptibility

Loca $\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$

Metallic phase



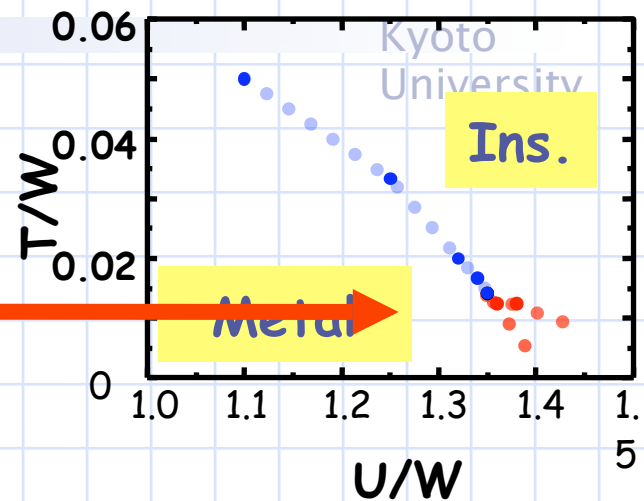
Temp: $T/W = 1/80$



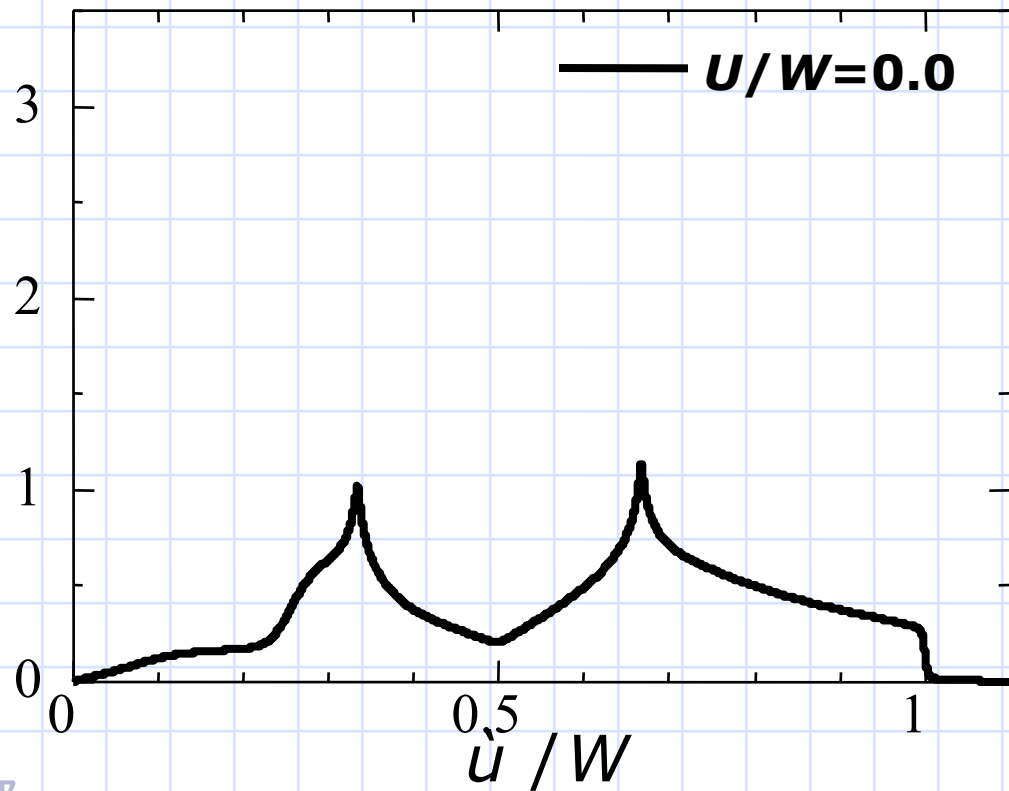
Dynamical spin susceptibility

Local $\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$

Metallic phase



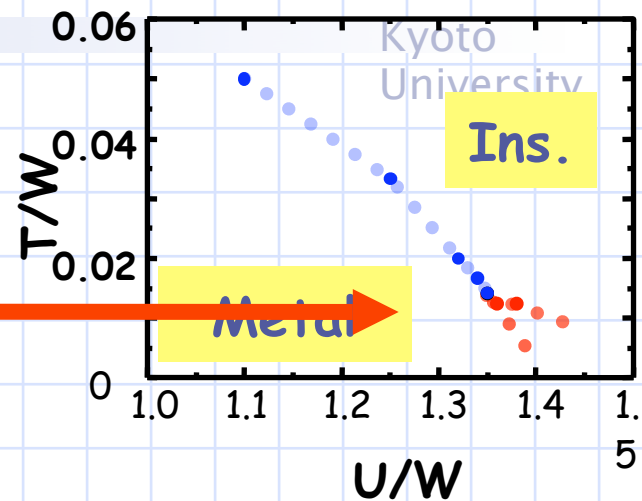
Temp: $T/W = 1/80$



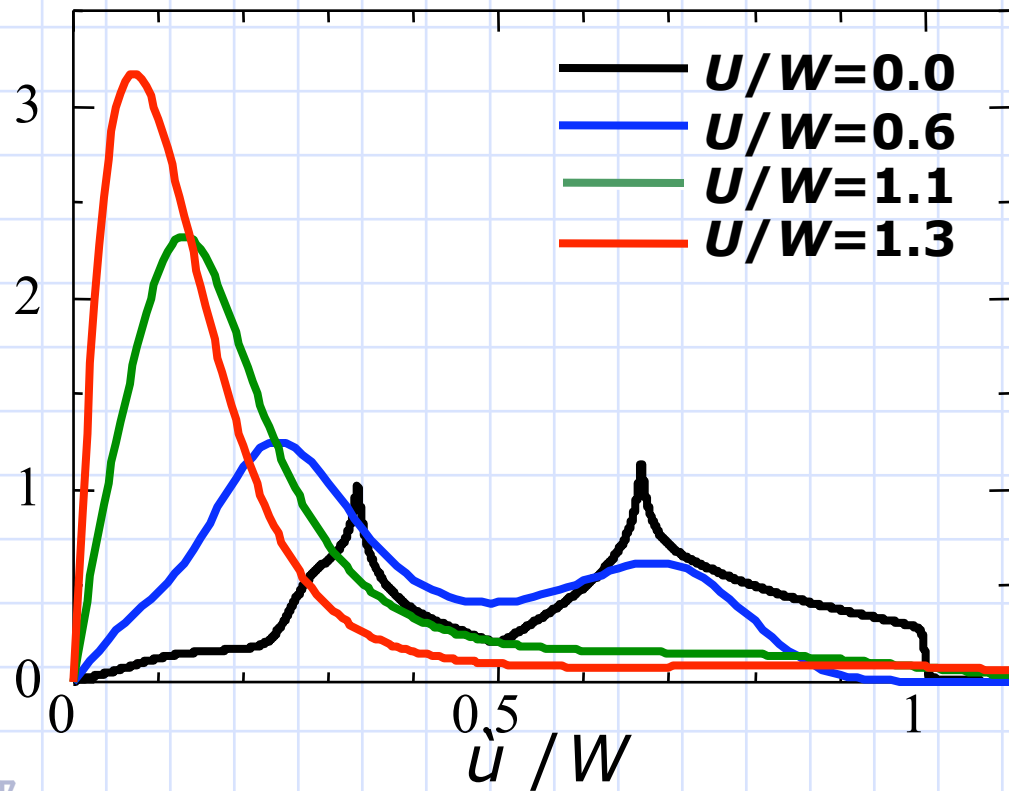
Dynamical spin susceptibility

Loca $\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$

Metallic phase



Temp: $T/W = 1/80$



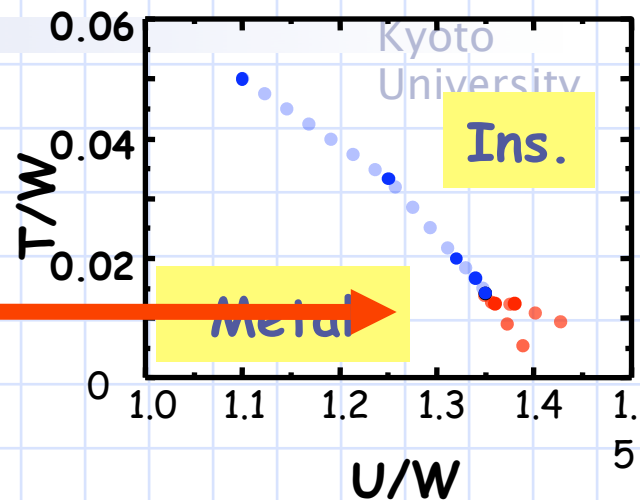
Dynamical spin susceptibility

Local $\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$

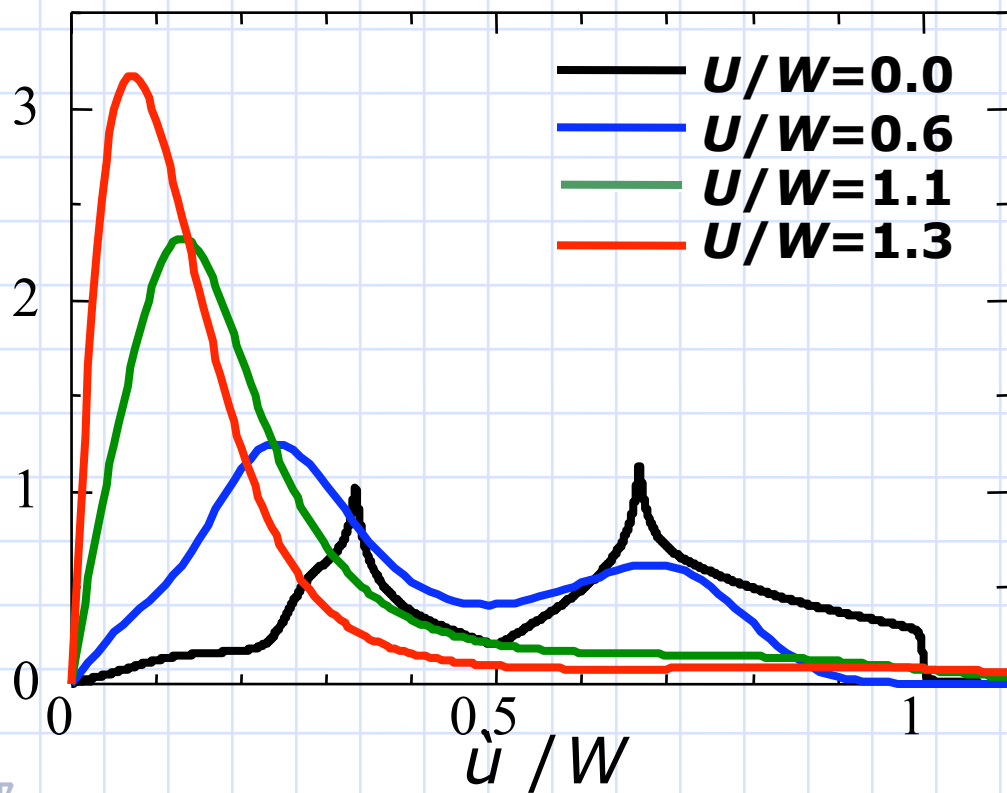
Metallic phase

$U \Rightarrow$ large

- shift
- peak enhanced



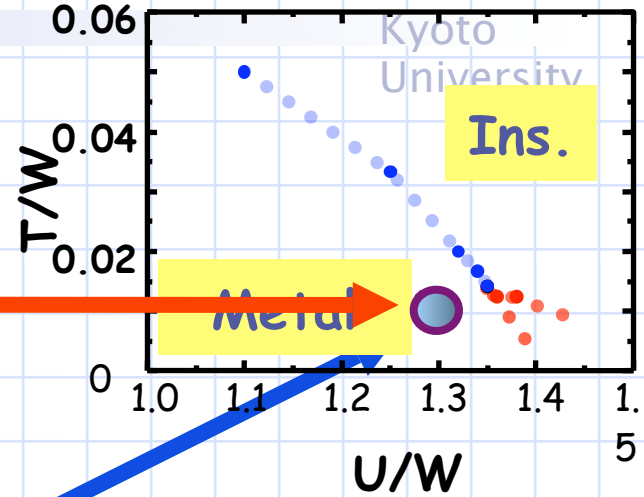
Temp: $T/W = 1/80$



Dynamical spin susceptibility

Local $\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$

Metallic phase

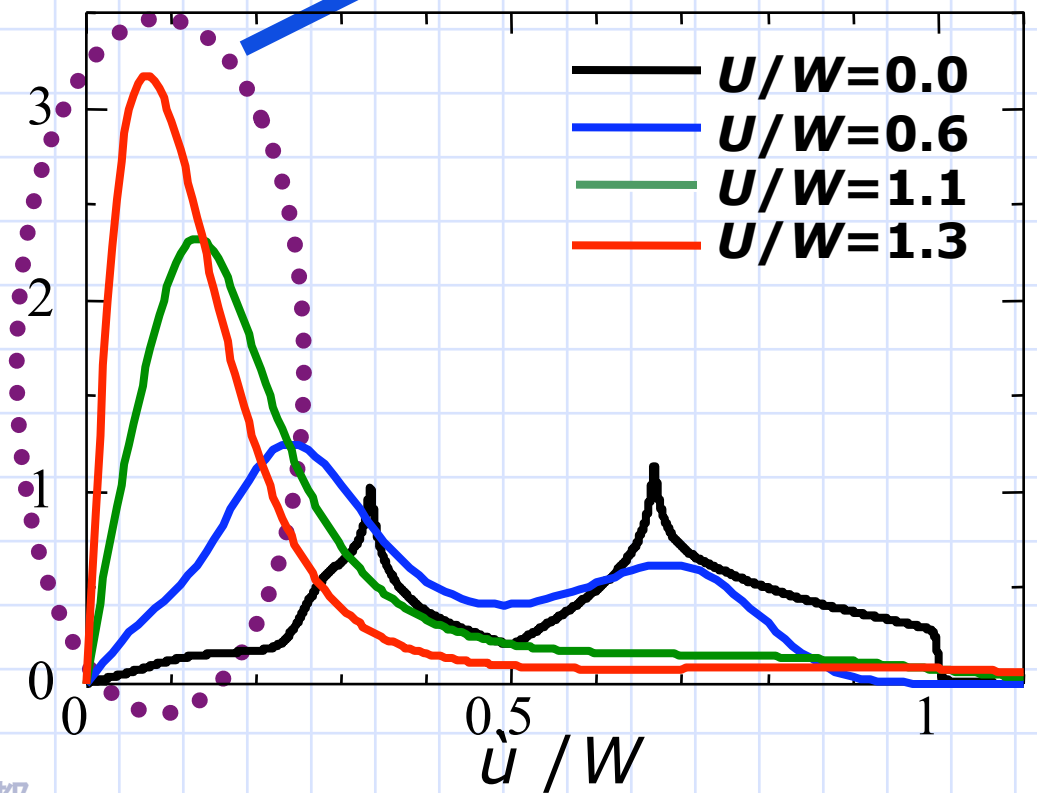


$U \Rightarrow$ large

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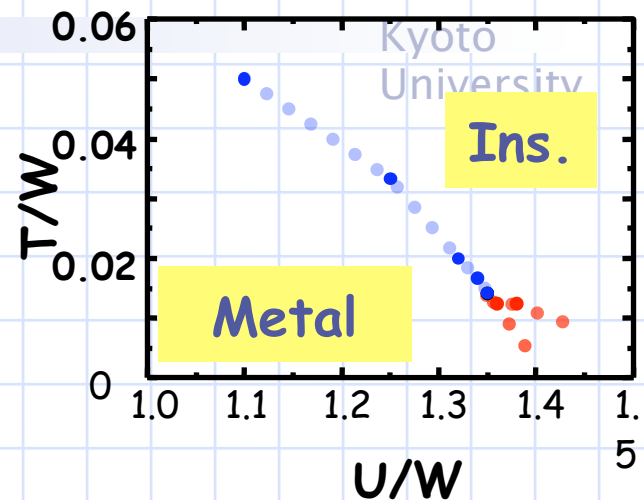
Heavy fermions

Temp: $T/W = 1/80$

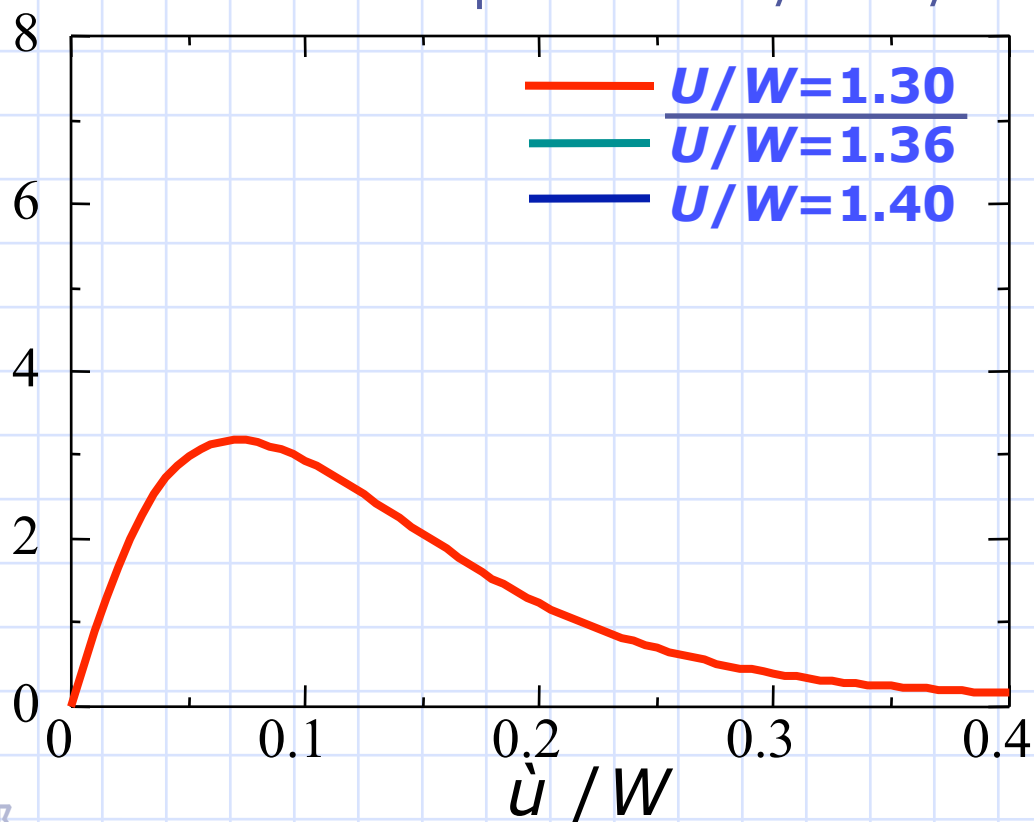


Dynamical spin susceptibility

$$\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$$

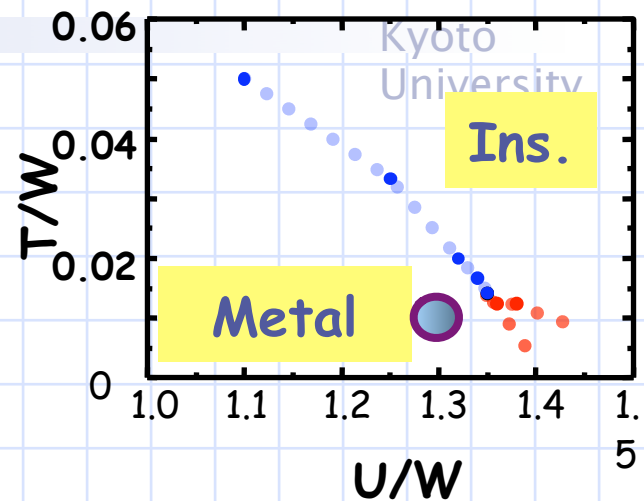


temperature: $T/W = 1/80$

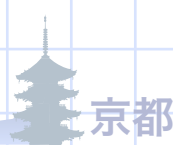
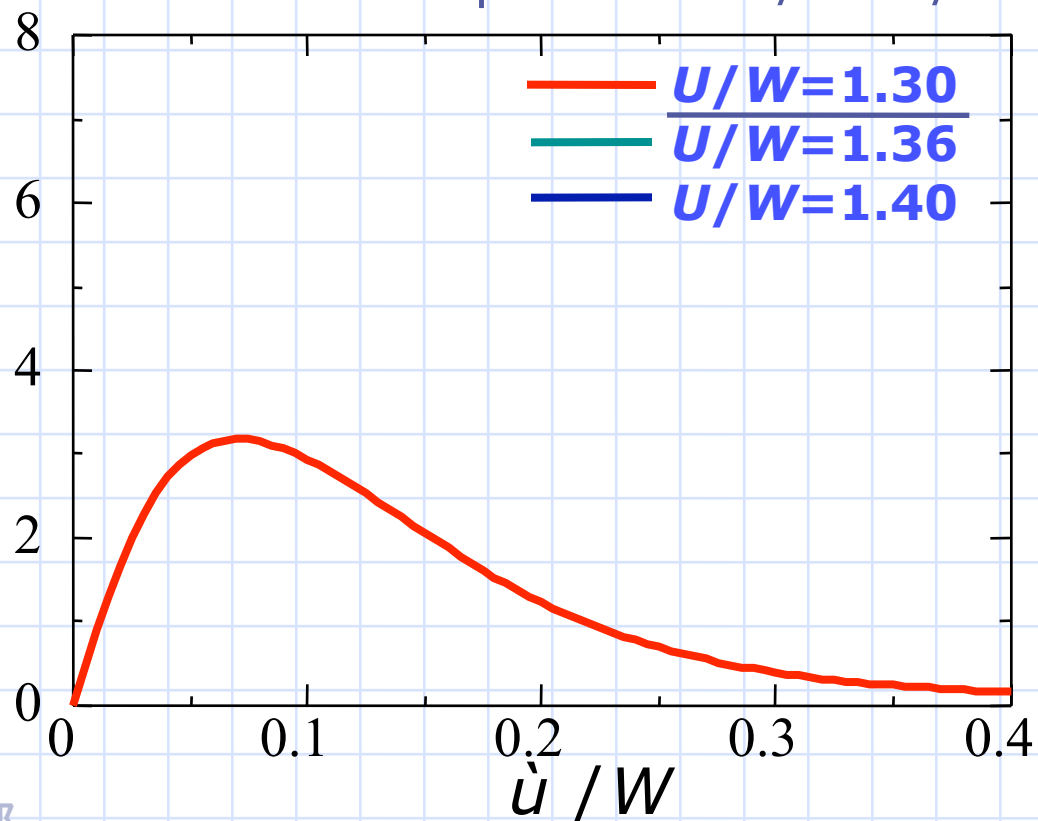


Dynamical spin susceptibility

$$\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$$



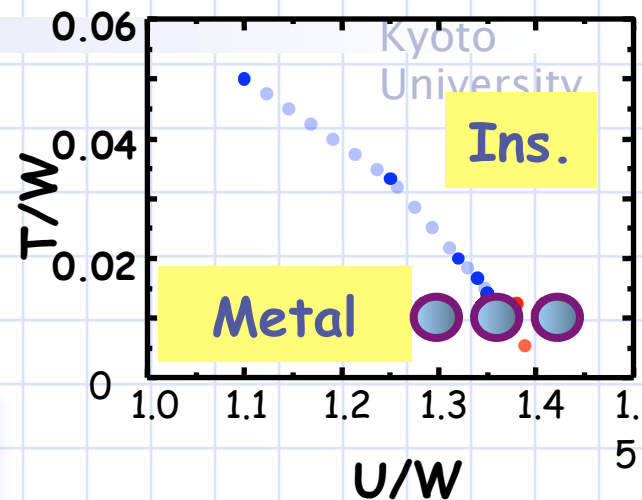
temperature: $T/W = 1/80$



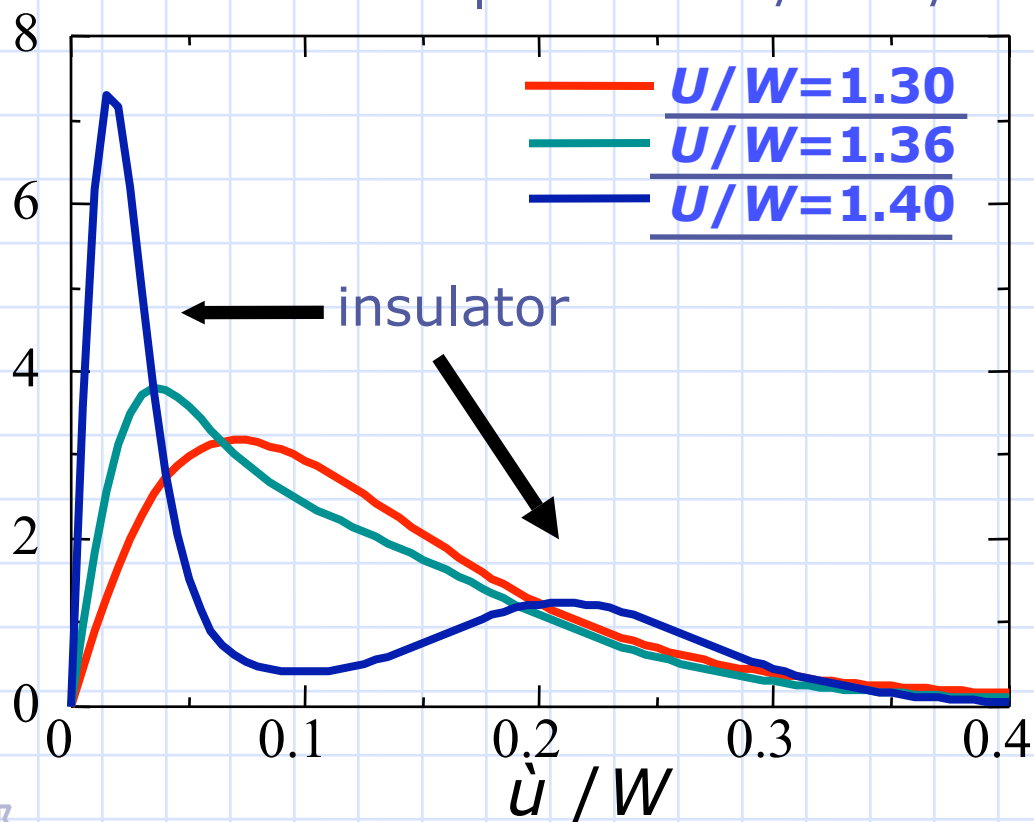
Dynamical spin susceptibility

$$\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$$

Mott transition ($U_c/W \sim 1.37$)



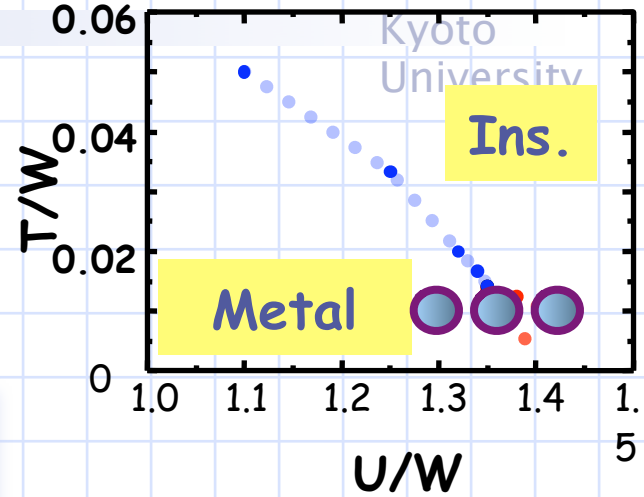
temperature: $T/W = 1/80$



Dynamical spin susceptibility

$$\chi_{loc}(\dot{u}) = -i \int \langle [S_i^z(t), S_i^z(0)] \rangle e^{-it\dot{u}} dt$$

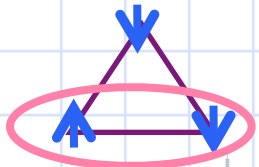
Mott transition ($U_c/W \sim 1.37$)



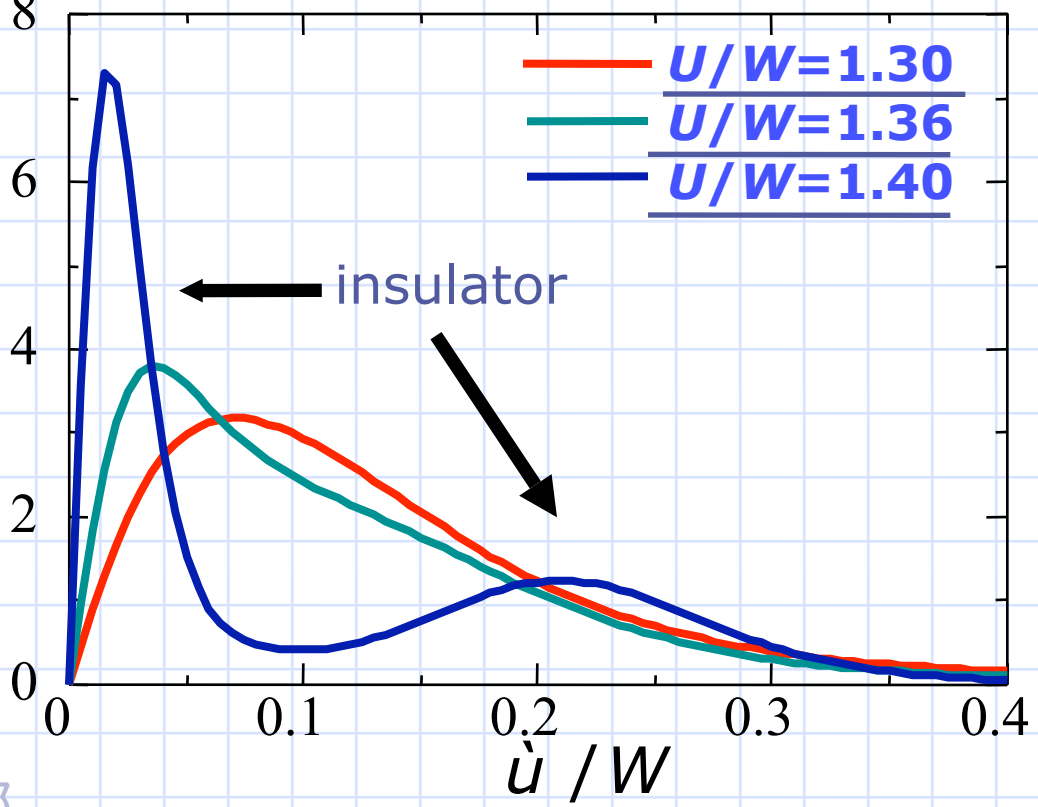
metal \Rightarrow insulator

Peak: splitting

Pair correlations revived

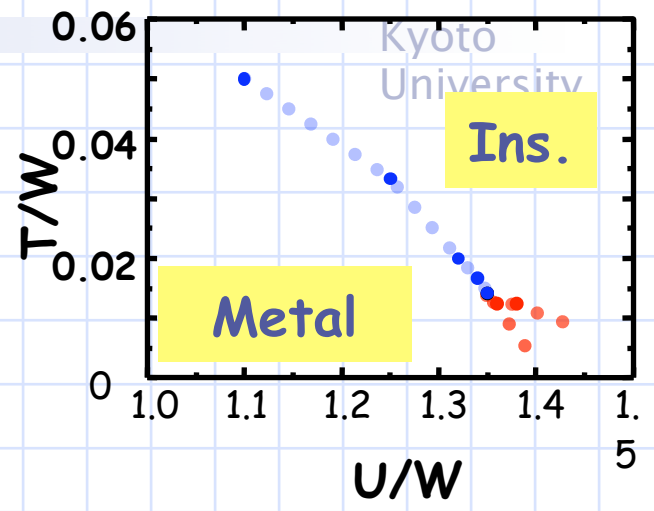


temperature: $T/W = 1/80$



Low T

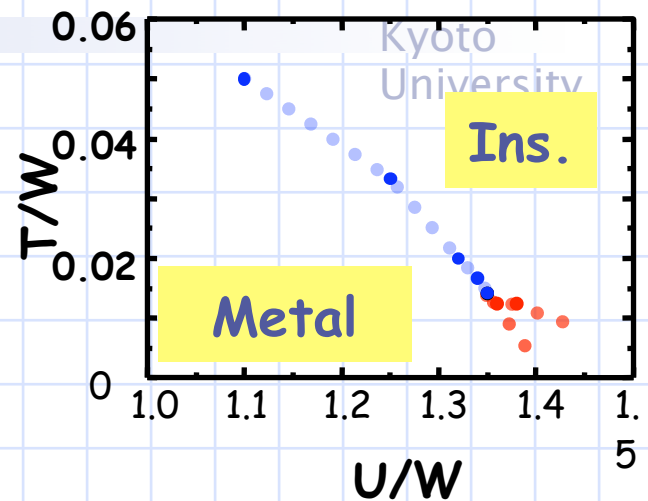
Very low T



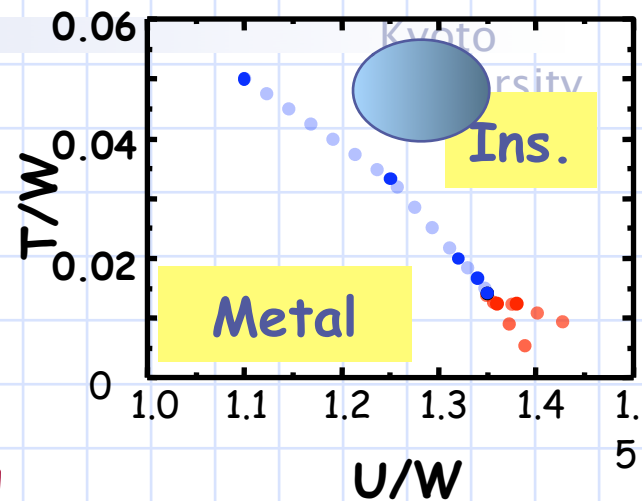
Near Mott transitions

Low T

Very low T



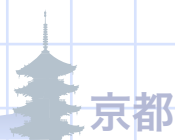
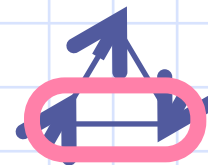
Near Mott transitions



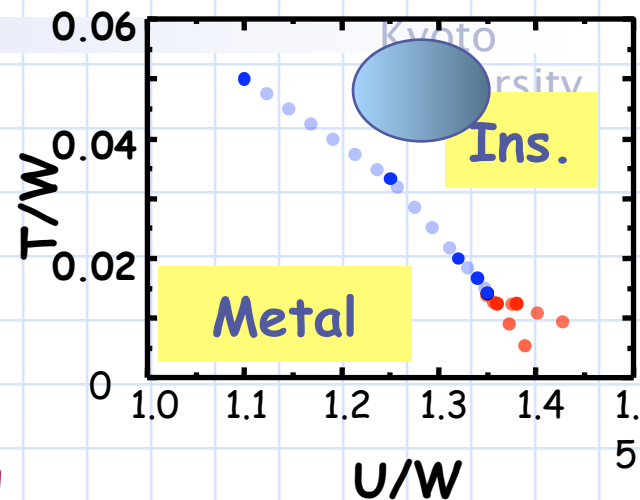
Low T

Pair correlations developed

Very low T



Near Mott transitions

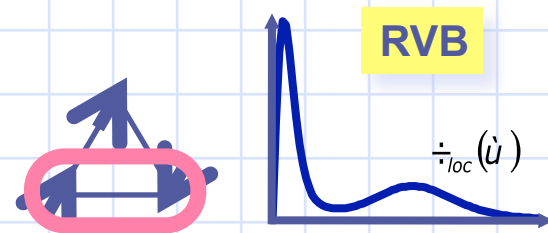


Low T

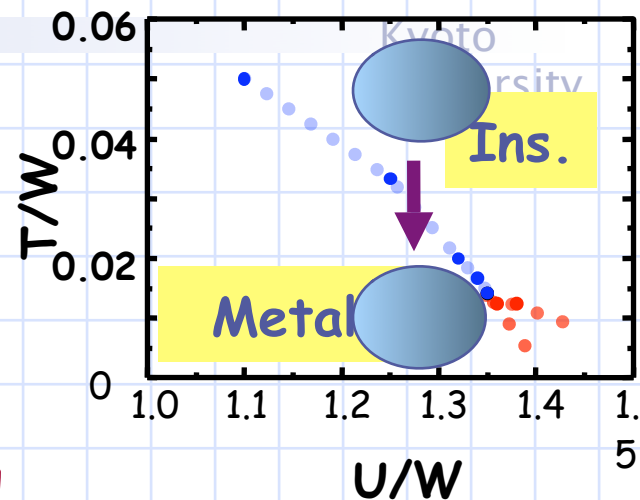
Pair correlations developed

Causes frustration

Very low T



Near Mott transitions

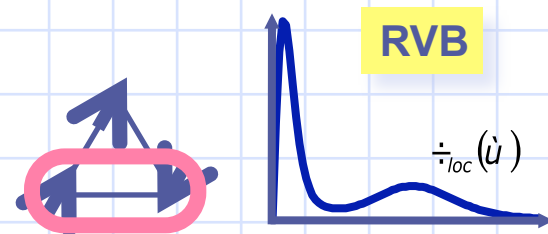


Low T

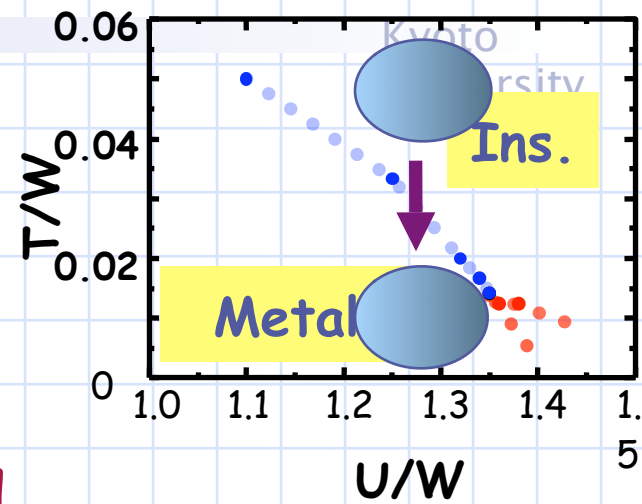
Pair correlations developed

Causes frustration

Very low T



Near Mott transitions



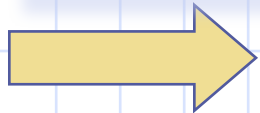
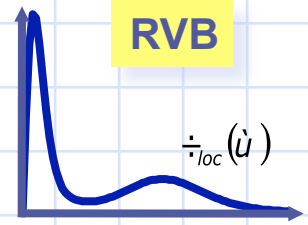
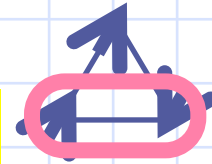
Low T

Pair correlations developed

Causes frustration

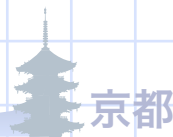
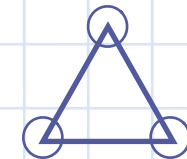
Very low T

reduce frustration

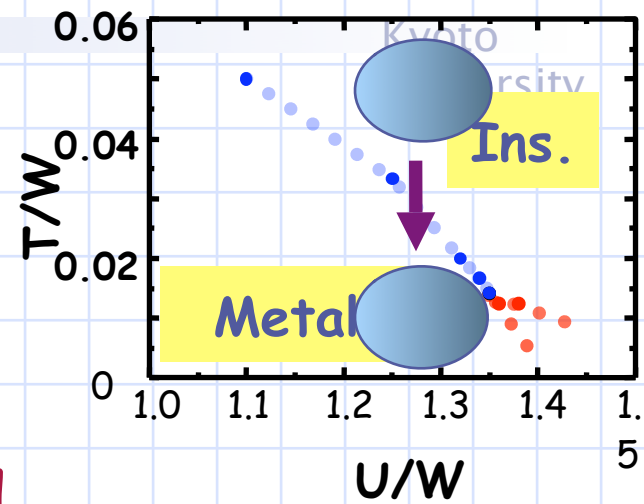


Itineracy induced

Suppresses pair correlations



Near Mott transitions



Low T

Pair correlations developed

Causes frustration

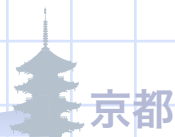
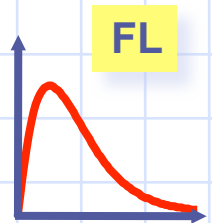
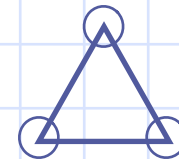
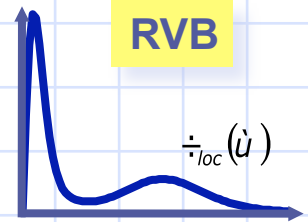
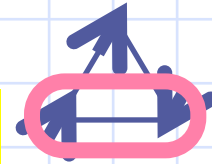
Very low T

reduce frustration

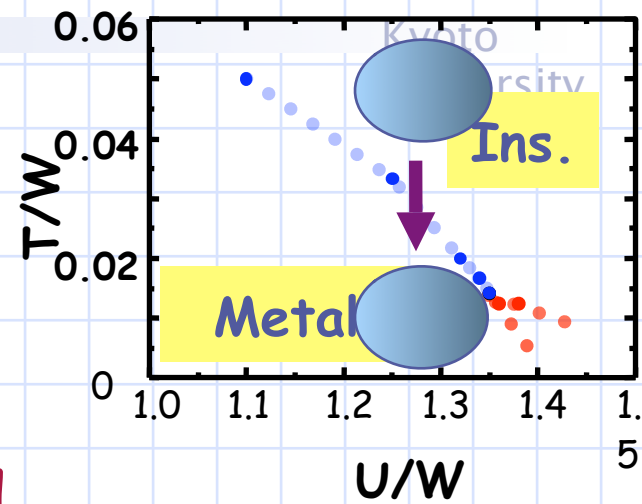
Itineracy induced

Suppresses pair correlations

Heavy fermions



Near Mott transitions



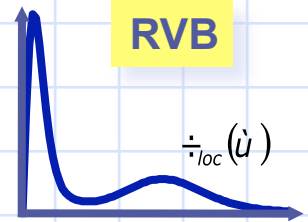
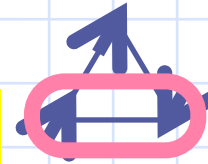
Low T

Pair correlations developed

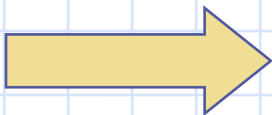
Causes frustration

Very low T

reduce frustration

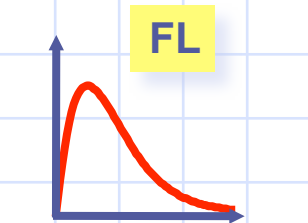
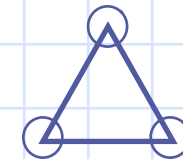


Itineracy induced



Suppresses pair correlations

Heavy fermions



Anomalous metallic behavior

Frustration induced

Crossover: RVB-Fermi liquid

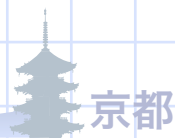
Enhanced pair correlations

Masked by itineracy

Very low energy scale

To avoid strong frustration

hidden



What is expected ?

Enhanced pair correlations

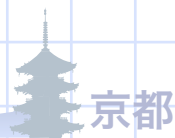
Masked by itineracy

Very low energy scale

To avoid strong frustration



hidden



What is expected ?

Enhanced pair correlations

Masked by itineracy

Very low energy scale

To avoid strong frustration



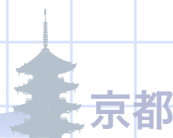
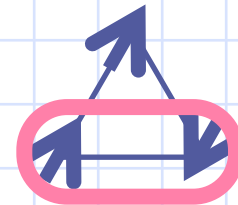
Slight deviations



Filling control

Temperature, etc

Revive pair correlations



What is expected ?

Enhanced pair correlations

Masked by itineracy

Very low energy scale

To avoid strong frustration



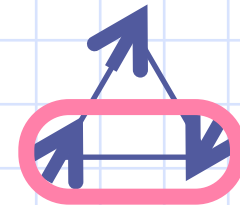
Slight deviations



Filling control

Temperature, etc

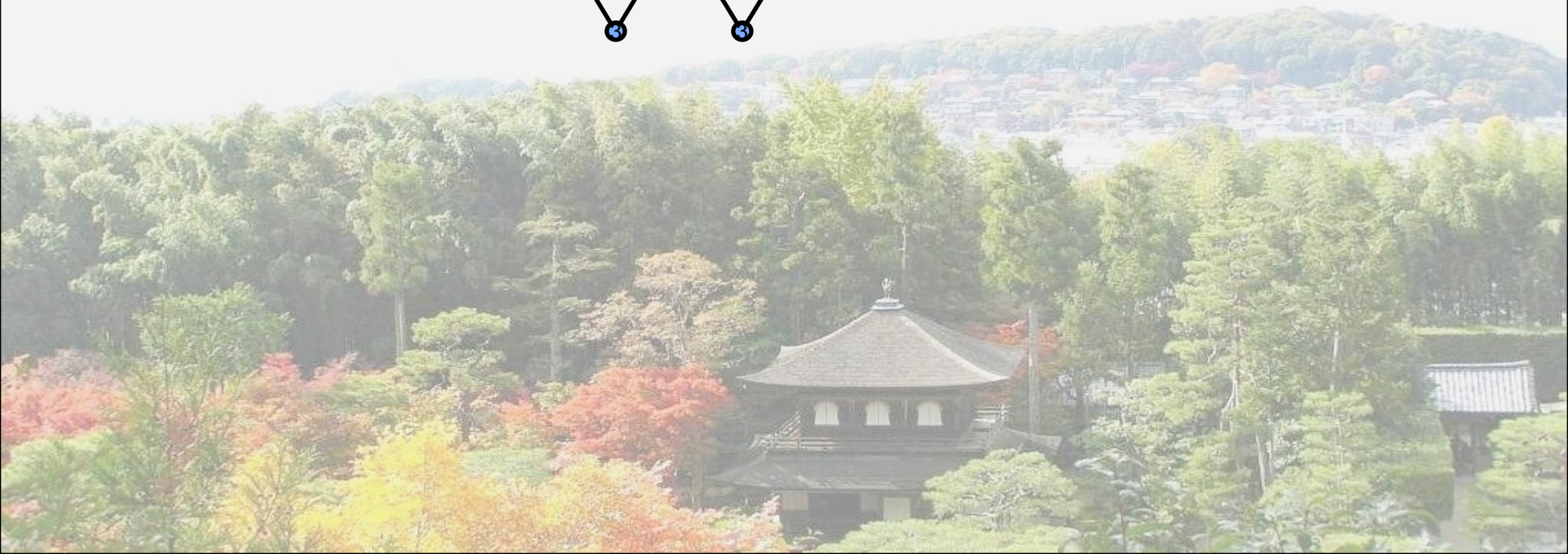
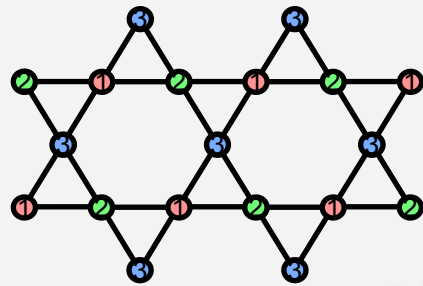
Revive pair correlations



Unusual phenomena ?

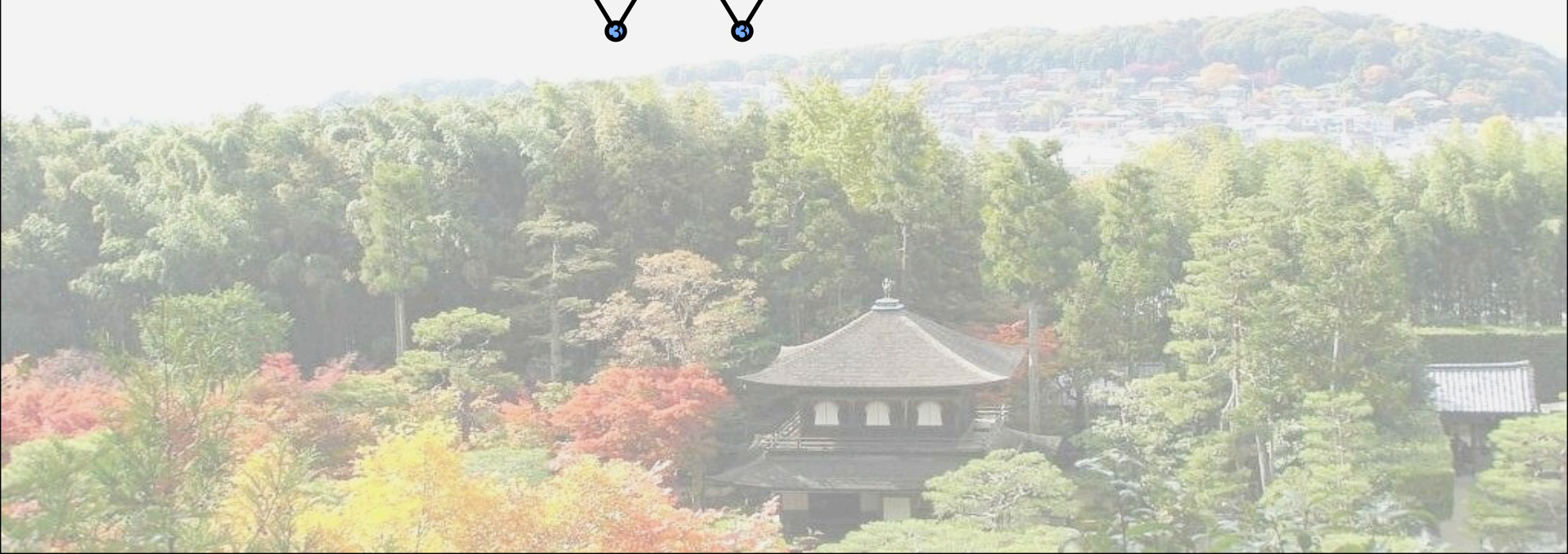
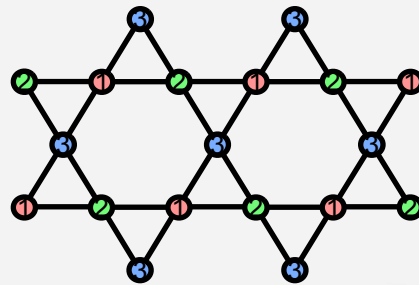


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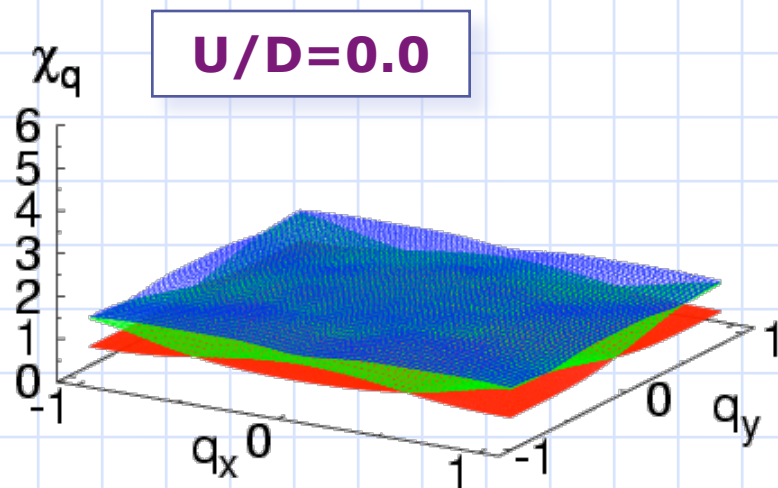
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Kyoto
November 14,
2007

Magnetic Instability ?



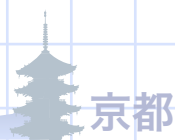
Magnetic susceptibility χ_q

$$T/D=1/30$$

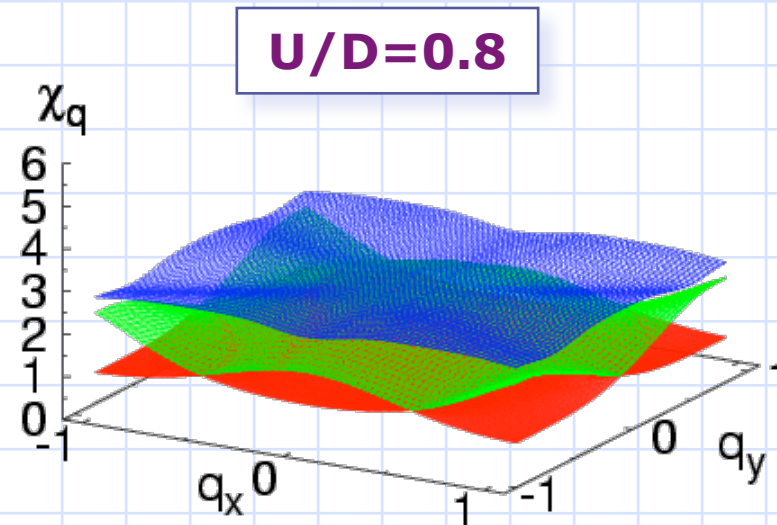
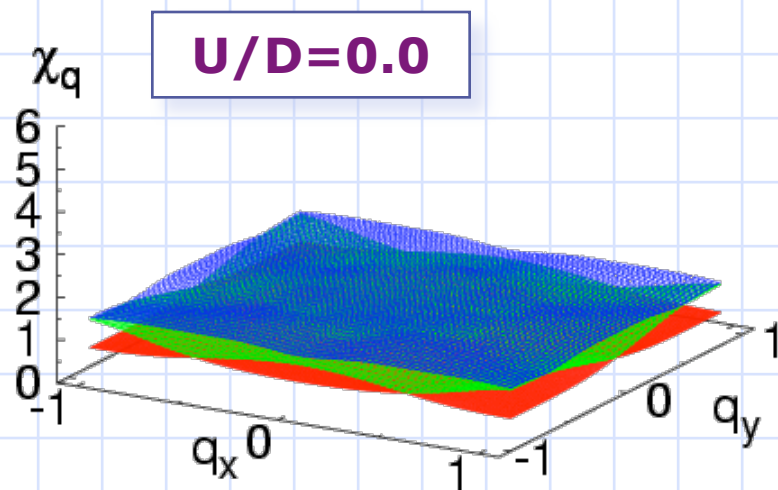


$$U/D=0.8$$

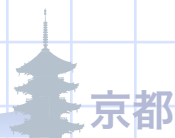
$$U/D=1.1$$



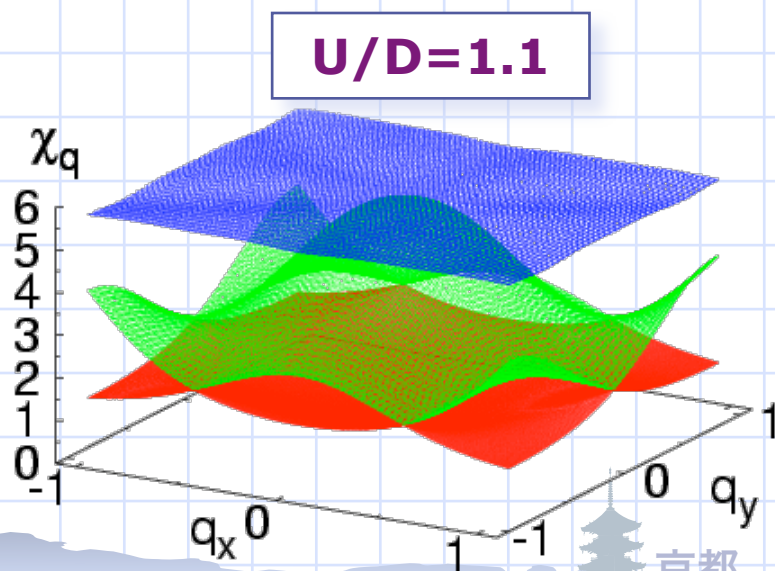
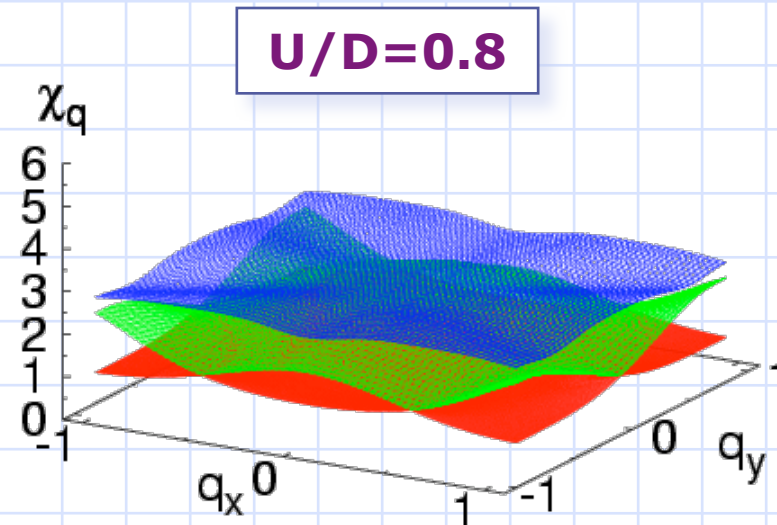
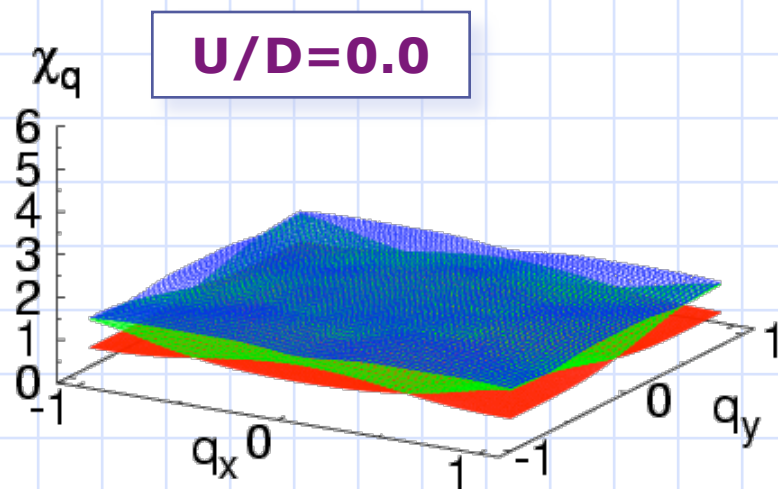
Magnetic susceptibility χ_q

 $T/D=1/30$ 

$U/D=1.1$

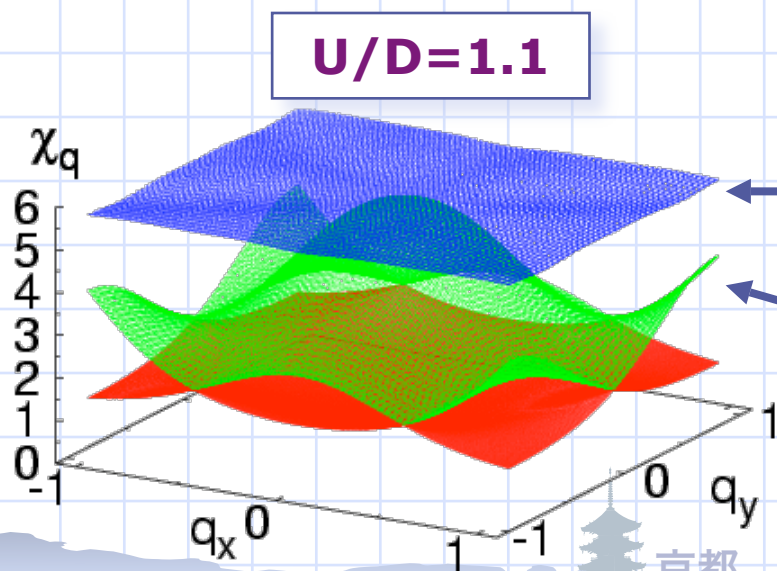
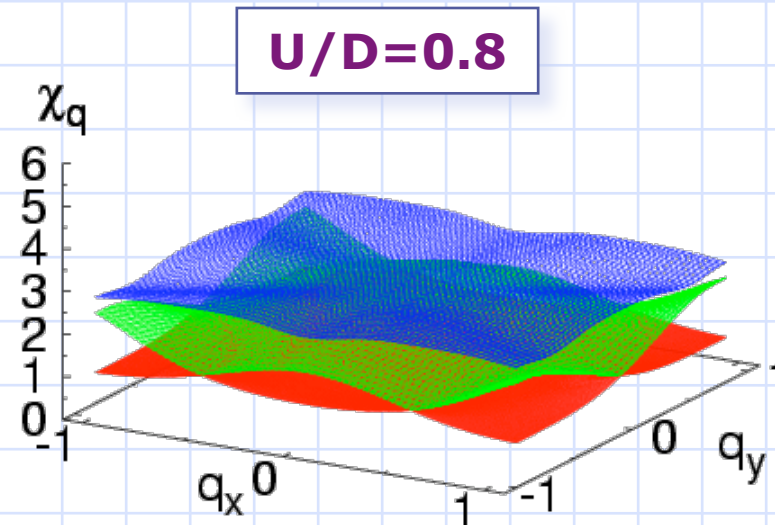
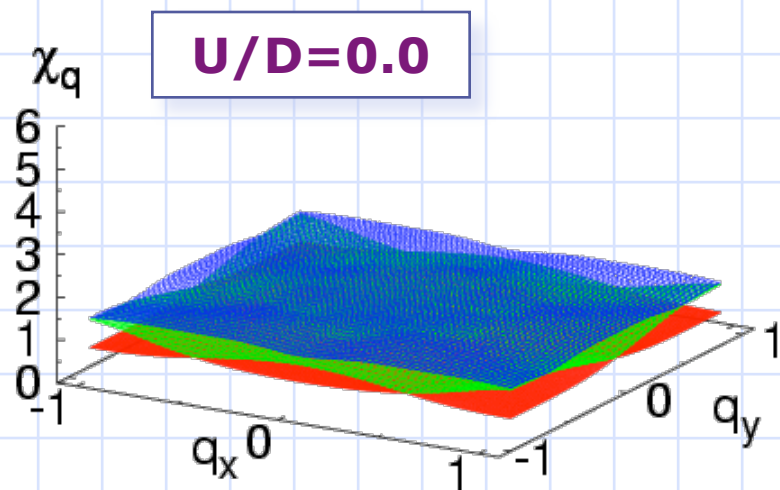


Magnetic susceptibility χ_q

 $T/D=1/30$ 

Magnetic susceptibility χ_q

$T/D=1/30$

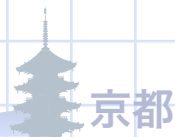
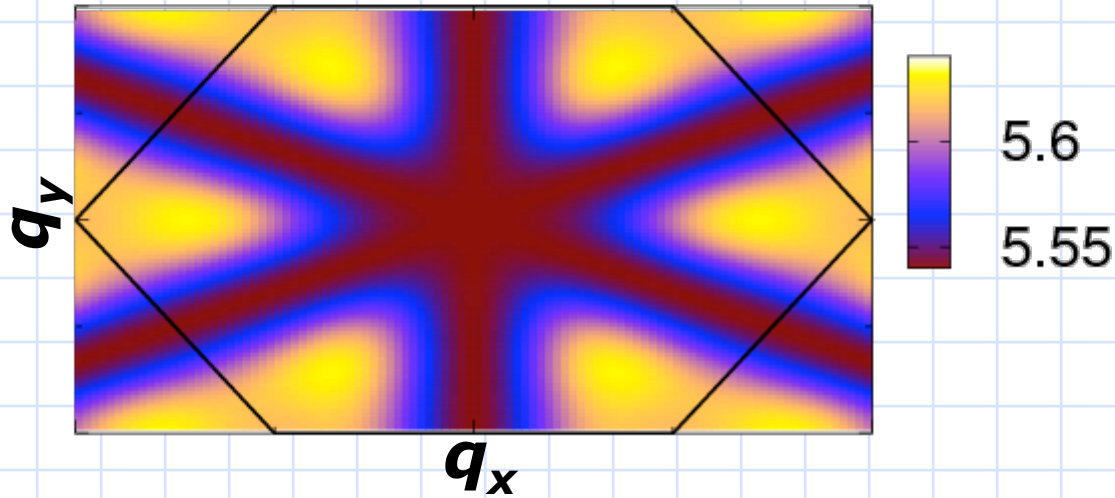


- maximum:
q-dependence \rightarrow small
- middle:
q=[0,0] \rightarrow large

c.f. Imai et al, Bulut et al

Maximum eigenvalues

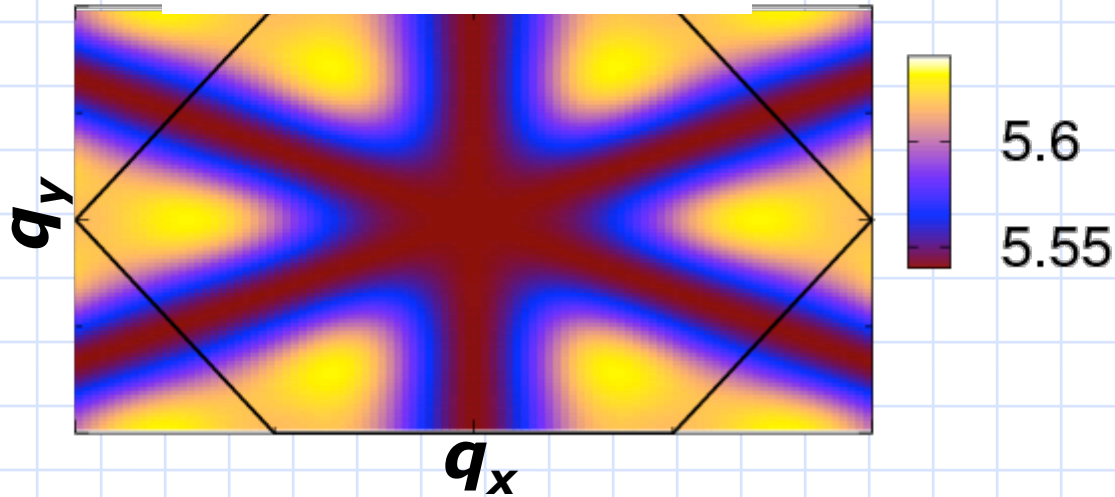
(temperature: $T/W=1/30$)



Maximum eigenvalues

(temperature: $T/W=1/30$)

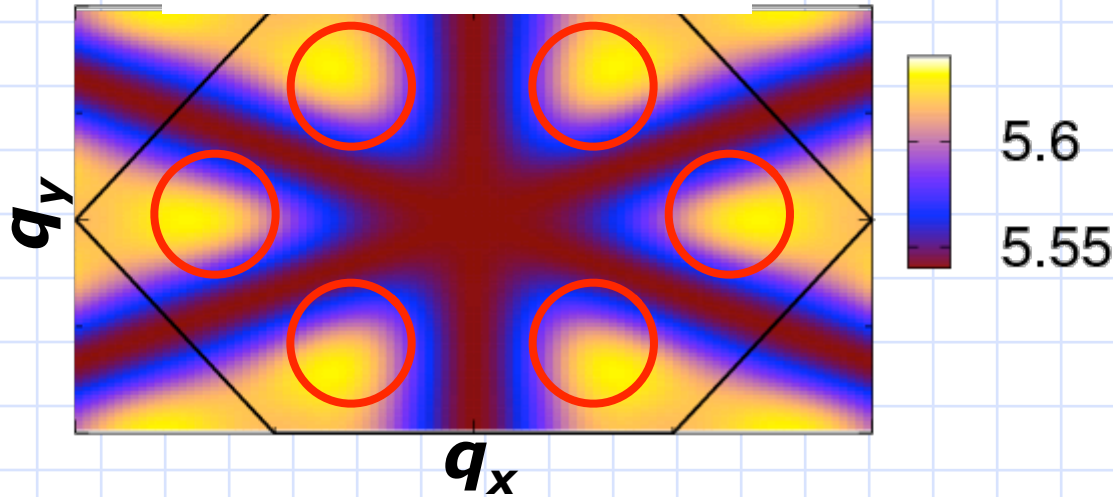
Metal: $U/W=1.1$



Maximum eigenvalues

(temperature: $T/W=1/30$)

Metal: $U/W=1.1$

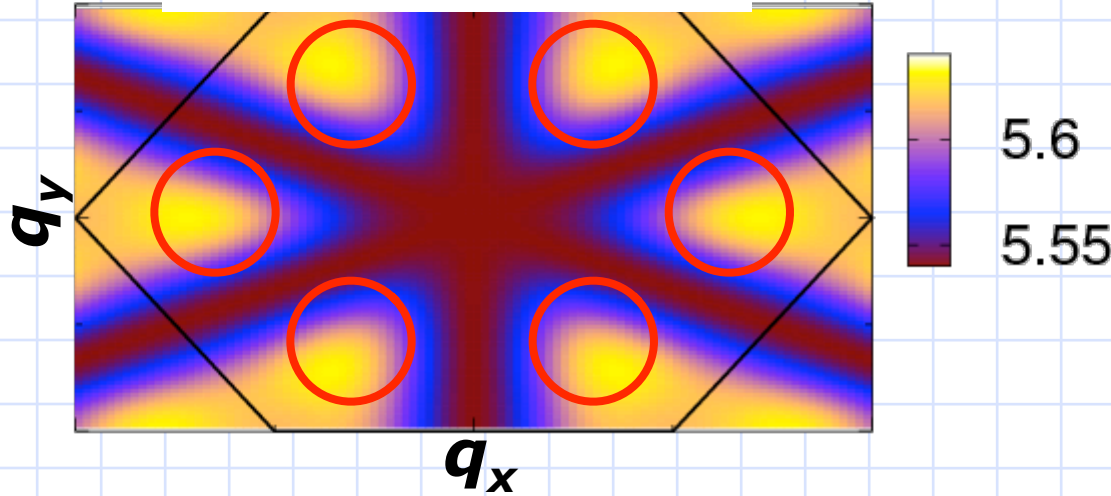


- Nesting of Fermi surface
- Maximum at six points

Maximum eigenvalues

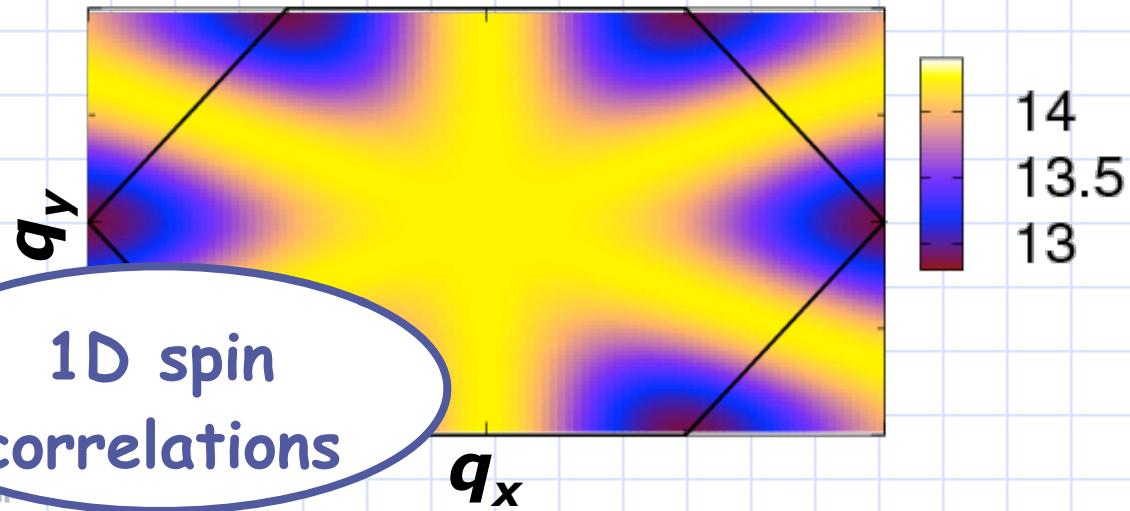
(temperature: $T/W=1/30$)

Metal: $U/W=1.1$



- Nesting of Fermi surface
- Maximum at six points

Insulating phase: $U/W=1.4$

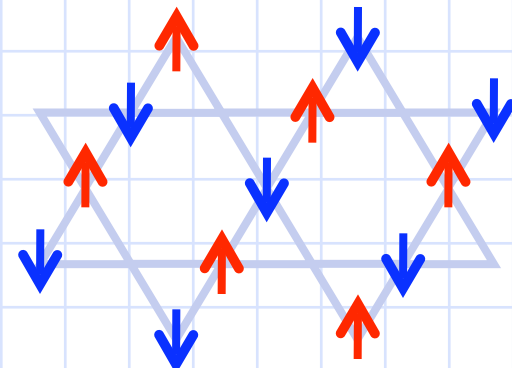
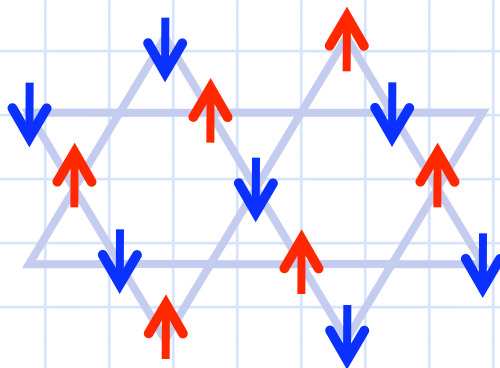
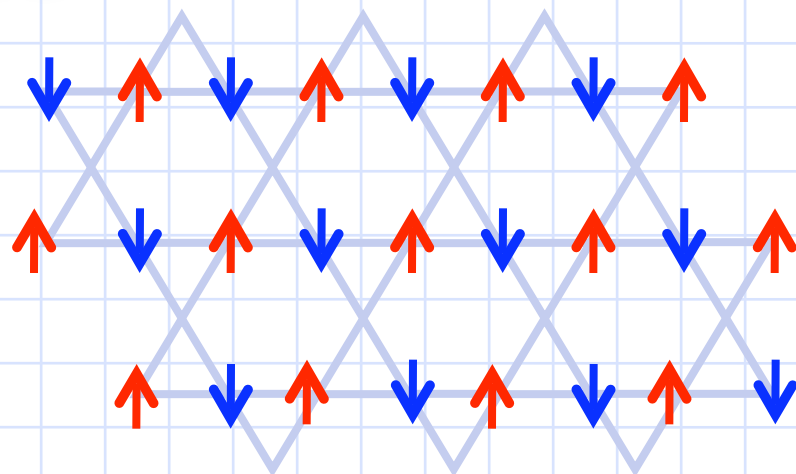
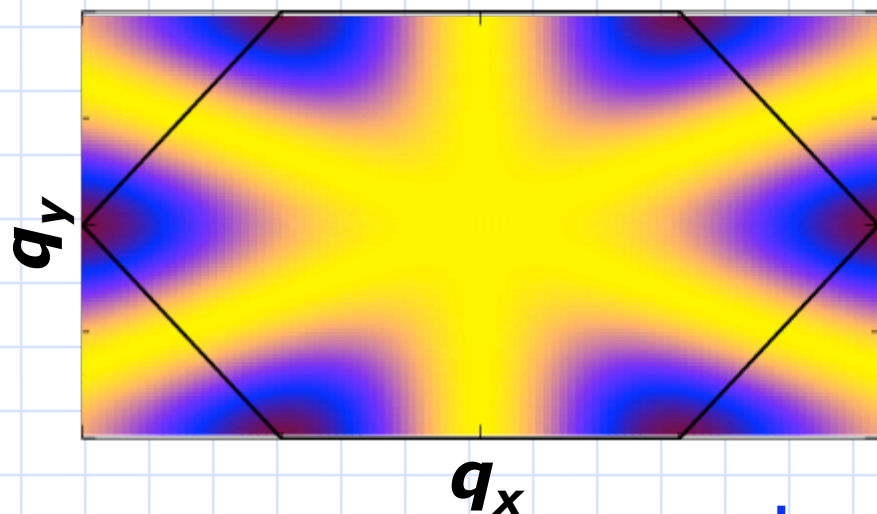


- n.n. spin correlation
- change in q -dependence !

1D spin correlations

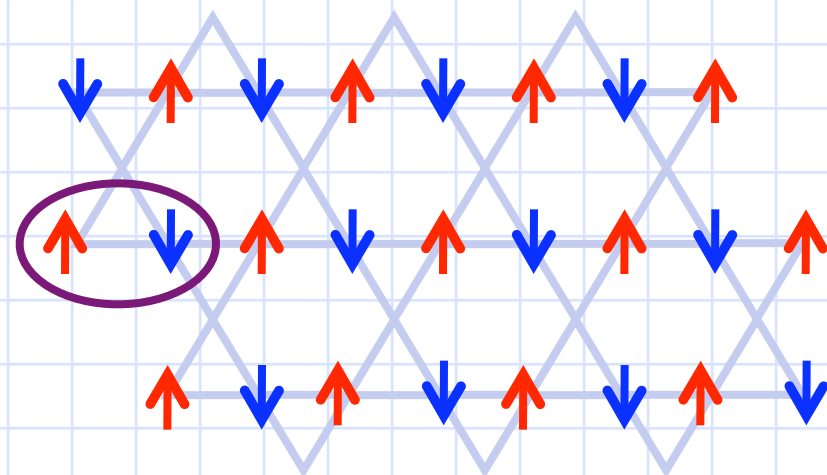
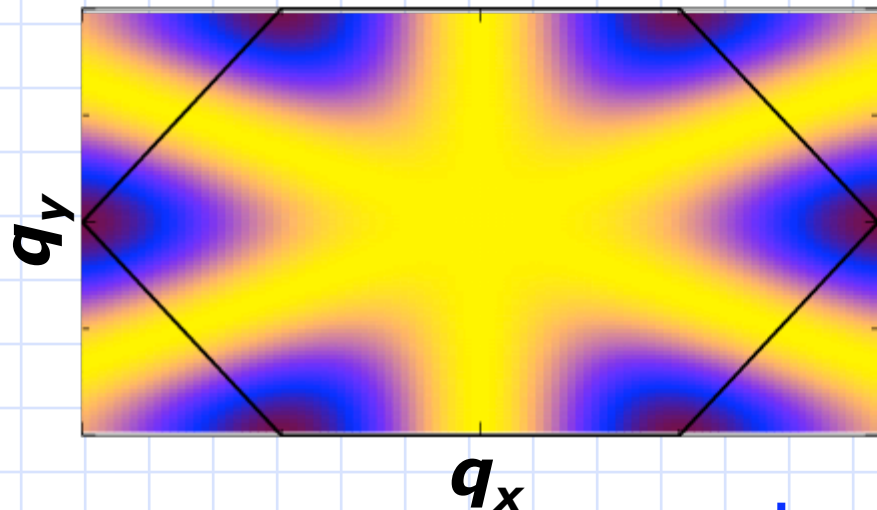
Dominant Spin Configurations

Mott phase

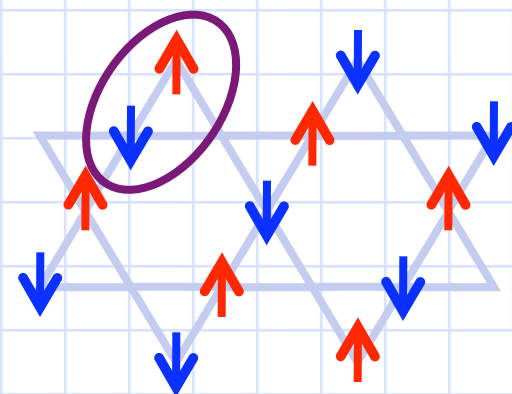
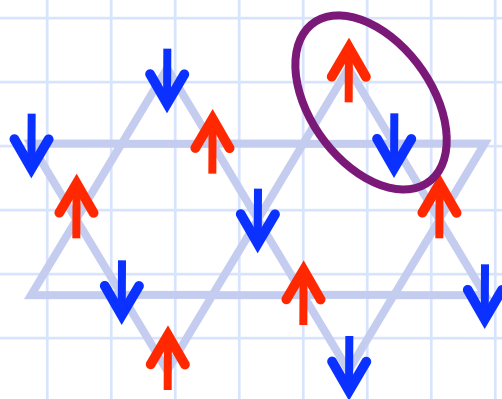


Dominant Spin Configurations

Mott phase

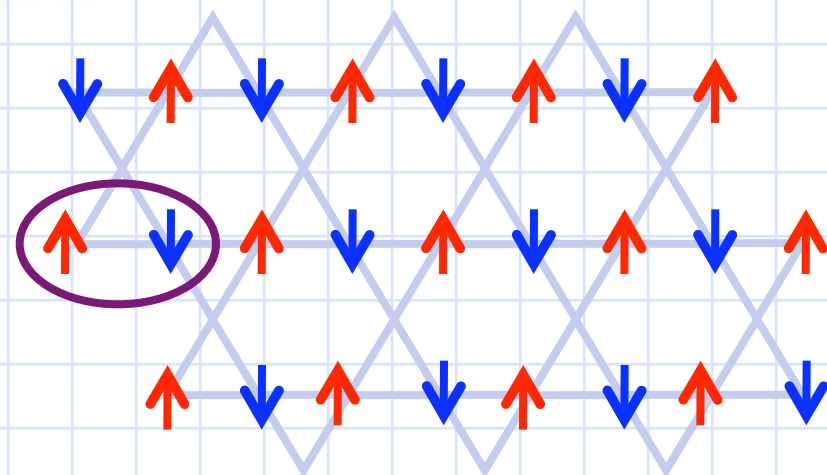
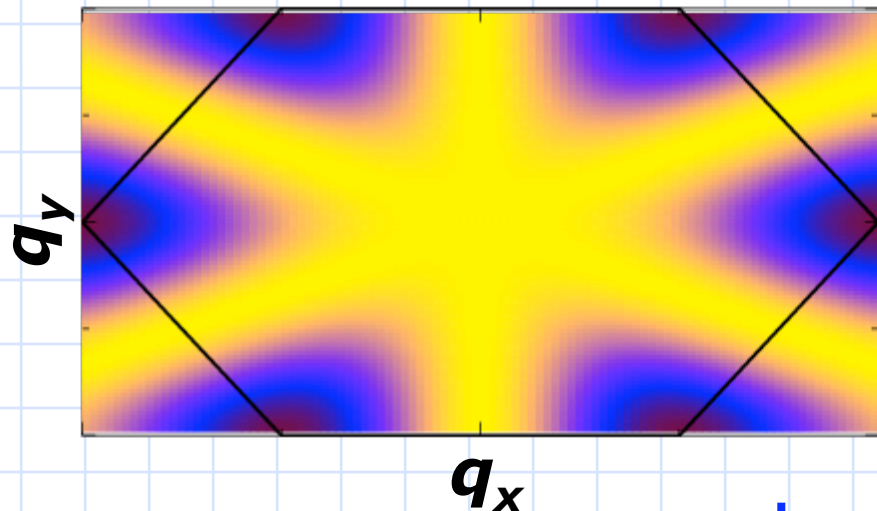


Short range
Pair correlations

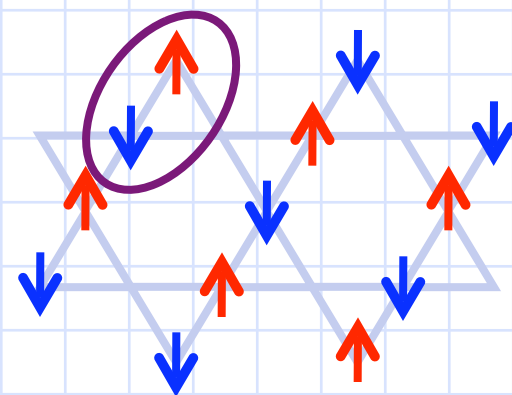
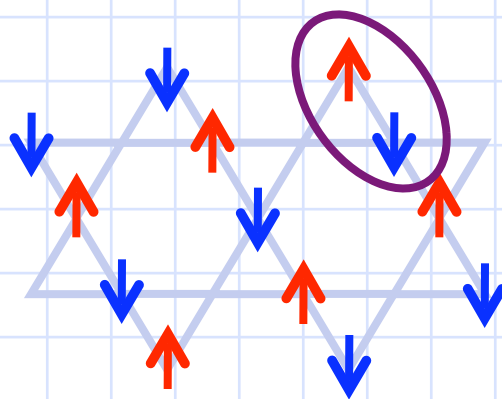


Dominant Spin Configurations

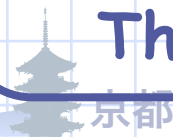
Mott phase



Short range
Pair correlations

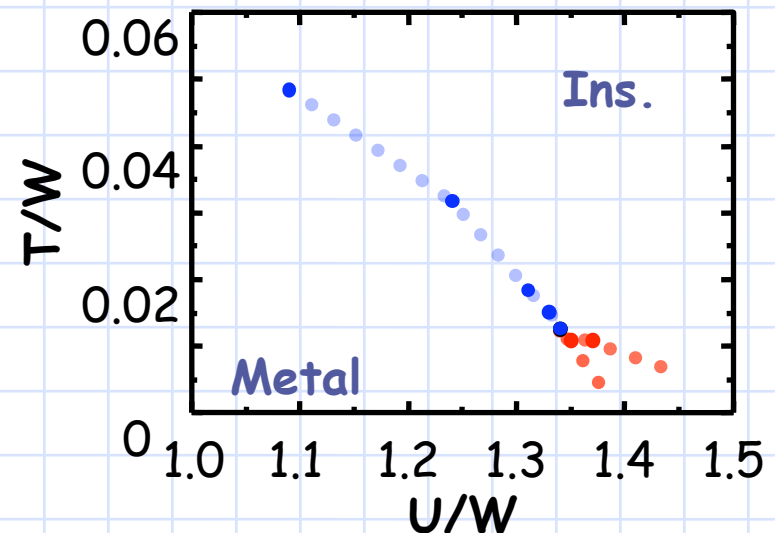


Three AF-correlated 1D chains



Kagome lattice Hubbard model

- ◆ 1st order Mott transition
 - $U_c/W \sim 1.37$ ($T/W = 1/80$)
- ◆ Metallic phase close to MIT

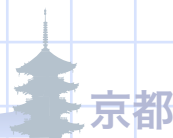
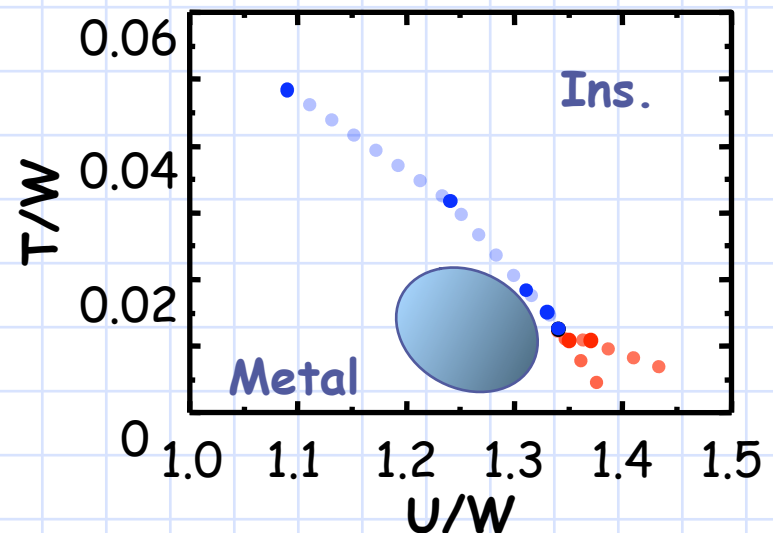


Kagome lattice Hubbard model

- ◆ 1st order Mott transition
 - $U_c/W \sim 1.37$ ($T/W = 1/80$)
- ◆ Metallic phase close to MIT

frustration-induced heavy fermions

Enhanced spin correlations are masked by itineracy



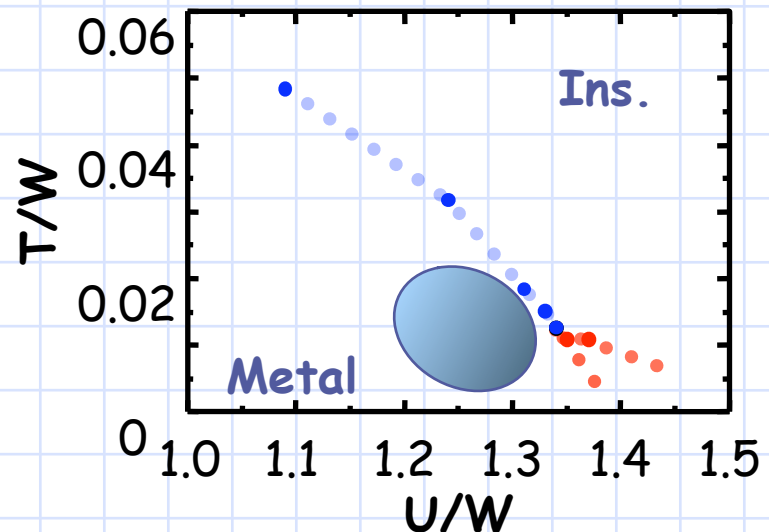
Kagome lattice Hubbard model

- ◆ 1st order Mott transition
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frustration-induced heavy fermions

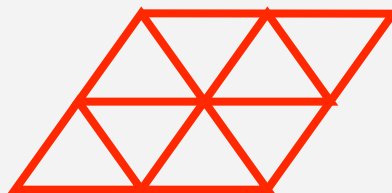
Enhanced spin correlations are masked by itineracy

Common to MT
with frustration



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Triangular Lattice



Organics

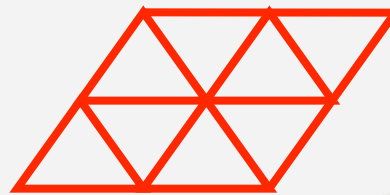
Ohashi et al. (2007)



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Triangular Lattice

Reentrant transition



Organics

Ohashi et al. (2007)



Organic conductors

- ◇ Correlated Electron Systems
 - ◇ Simple electronic structure in k space
- highly compressible**

Pressure-induced !

Mott transitions
Superconductivity
Magnetism

Pressure-induced Mott transition

Band-width control

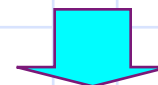
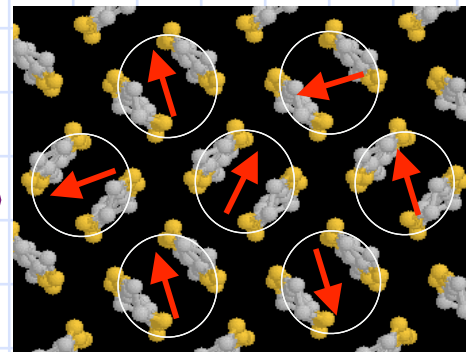
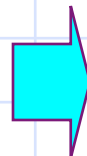
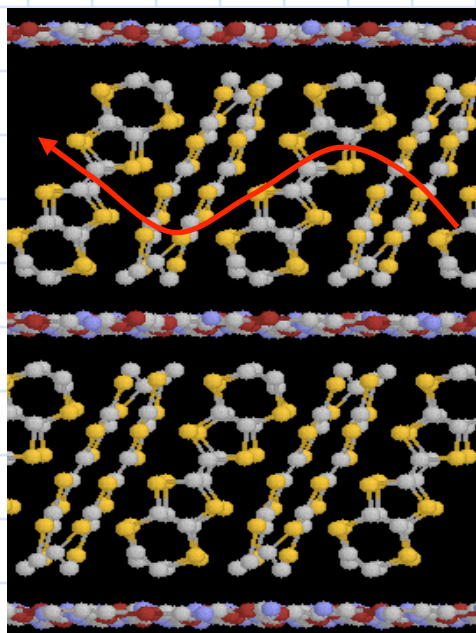
Kanoda group

Quasi-2D organics $\kappa\text{-(ET)}_2\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$

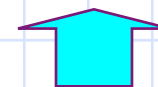
ET molecules

$\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$

ET molecules



pressure

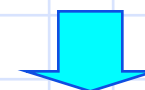
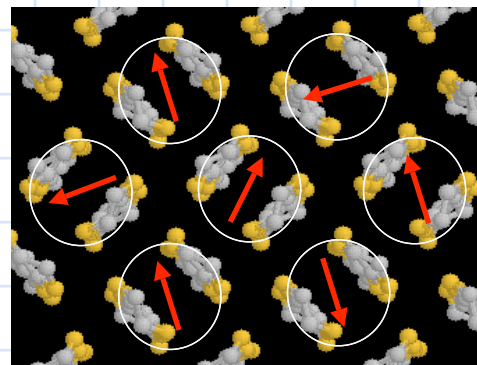
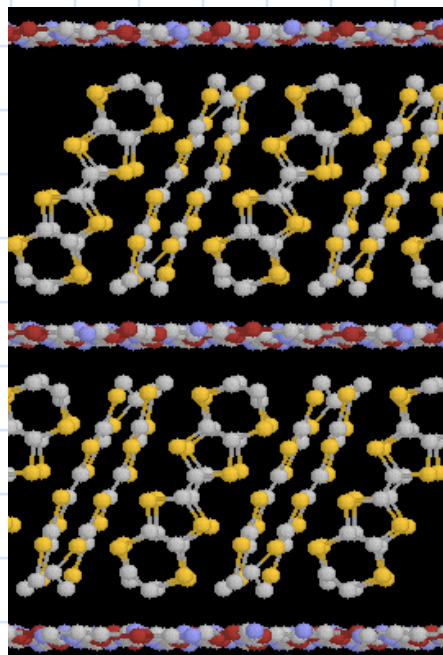


κ -(ET)₂X organics **Triangular lattice**

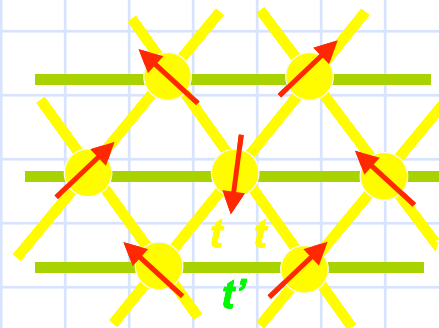
Layer structure

ET layer

X layer

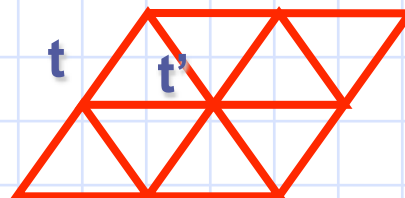


dimer model

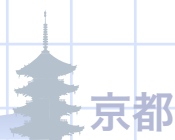


Half-filling

κ	t'/t
$\text{Cu}_2(\text{CN})_3$	1.06
$\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$	0.75

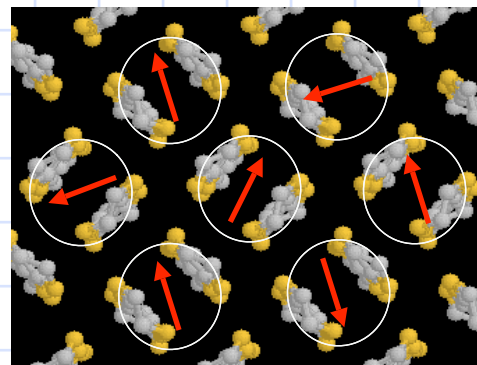
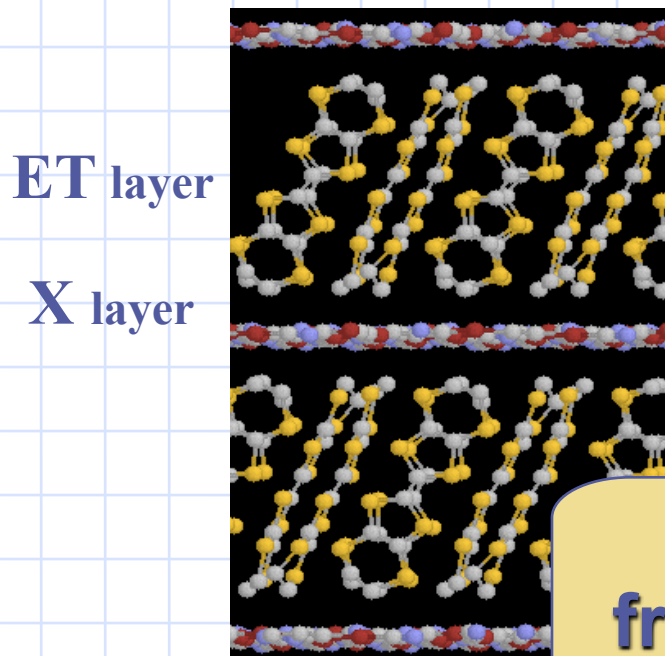


Anisotropic Triangular



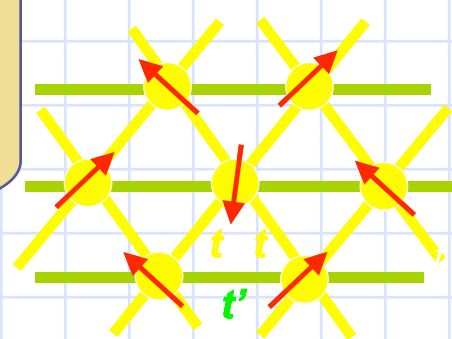
κ -(ET)₂X organics **Triangular lattice**

Layer structure



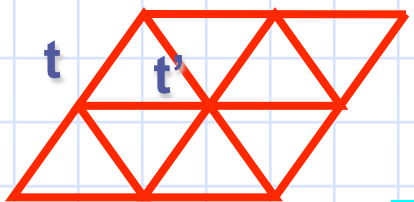
Fully frustrated

dimer model



Half-filling

κ	t'/t
$\text{Cu}_2(\text{CN})_3$	1.06
$\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$	0.75

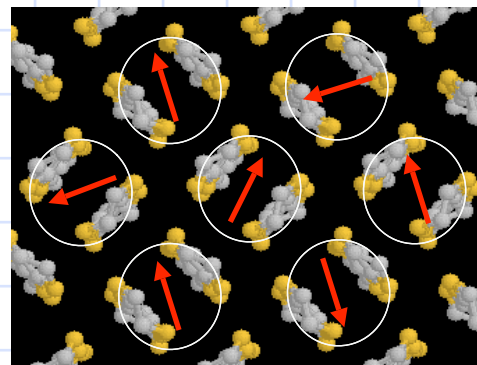
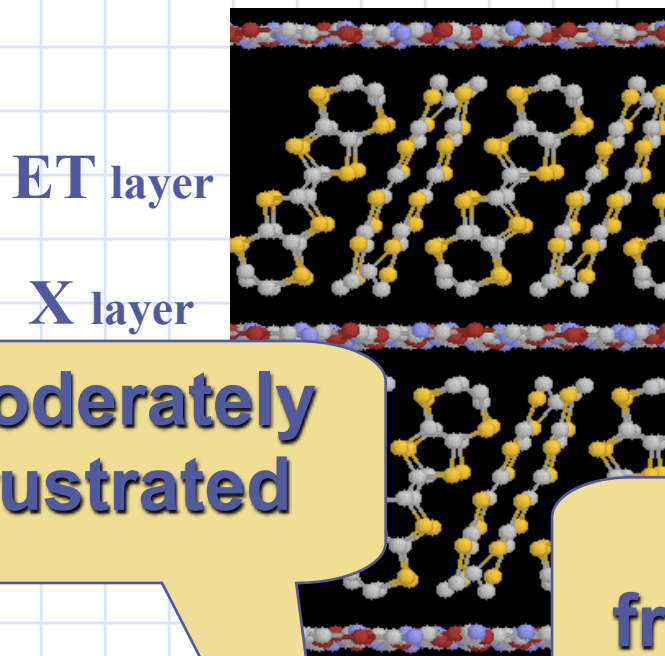


Anisotropic Triangular



κ -(ET)₂X organics **Triangular lattice**

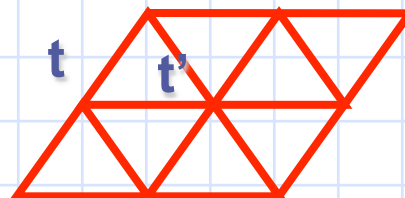
Layer structure



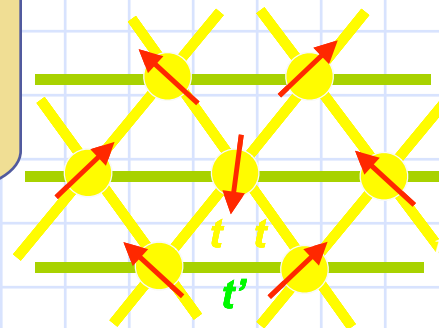
moderately frustrated

Fully frustrated

κ	t'/t
$\text{Cu}_2(\text{CN})_3$	1.06
$\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$	0.75

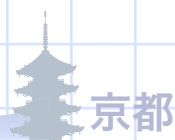


dimer model



Half-filling

Anisotropic Triangular



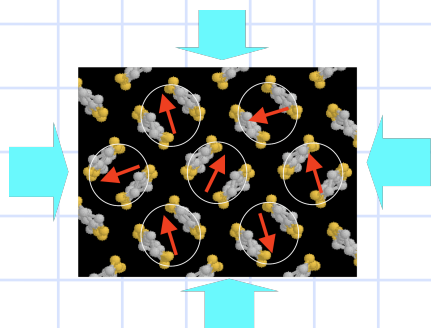
Mott transition by pressure

$\kappa\text{-(ET)}_2\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$

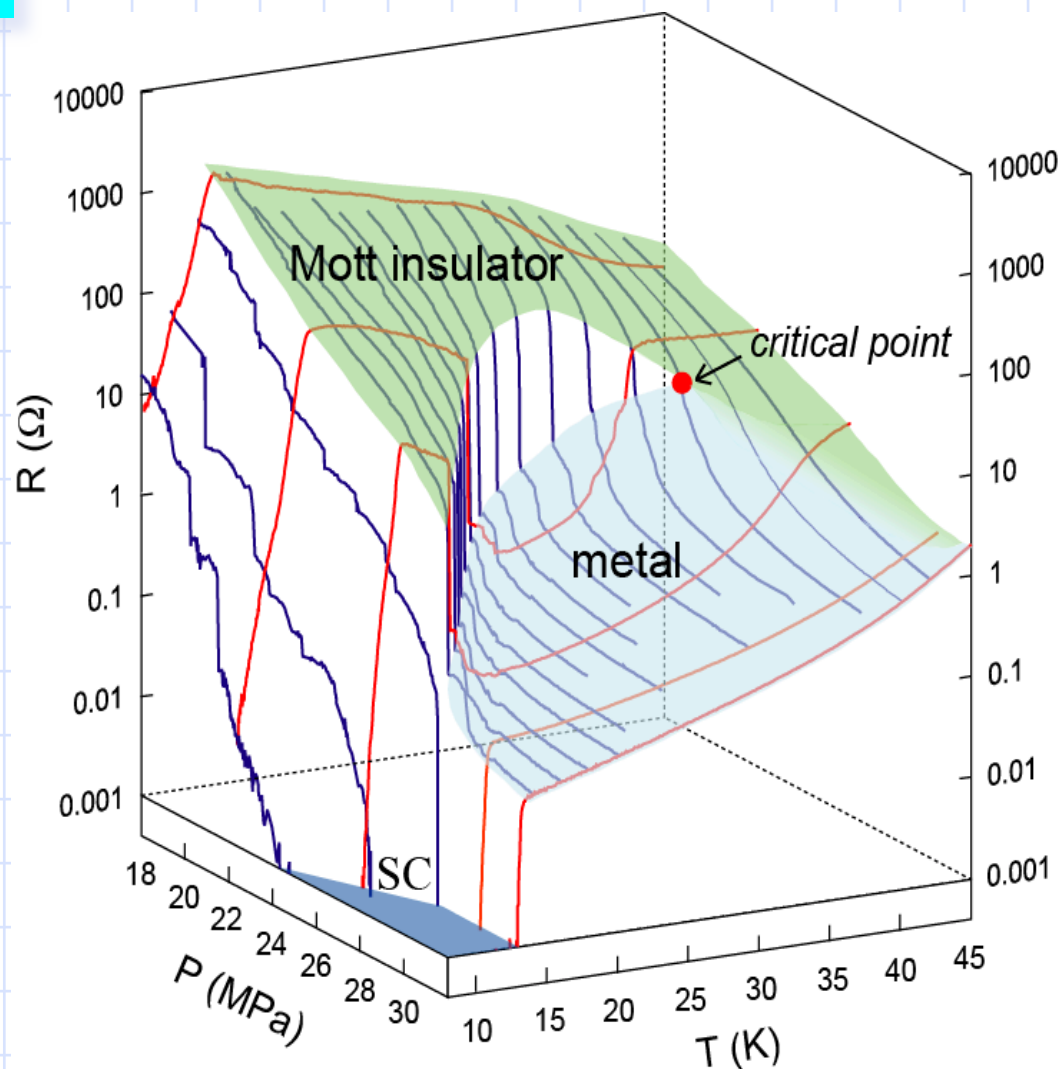
$t'/t=0.75$

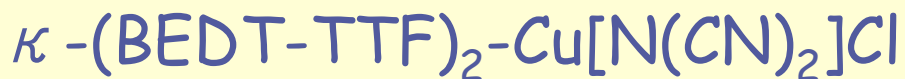
Kanoda group

Kagawa *et al.*, PRB 69 (2004)
064511

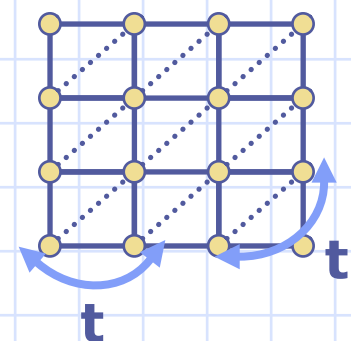
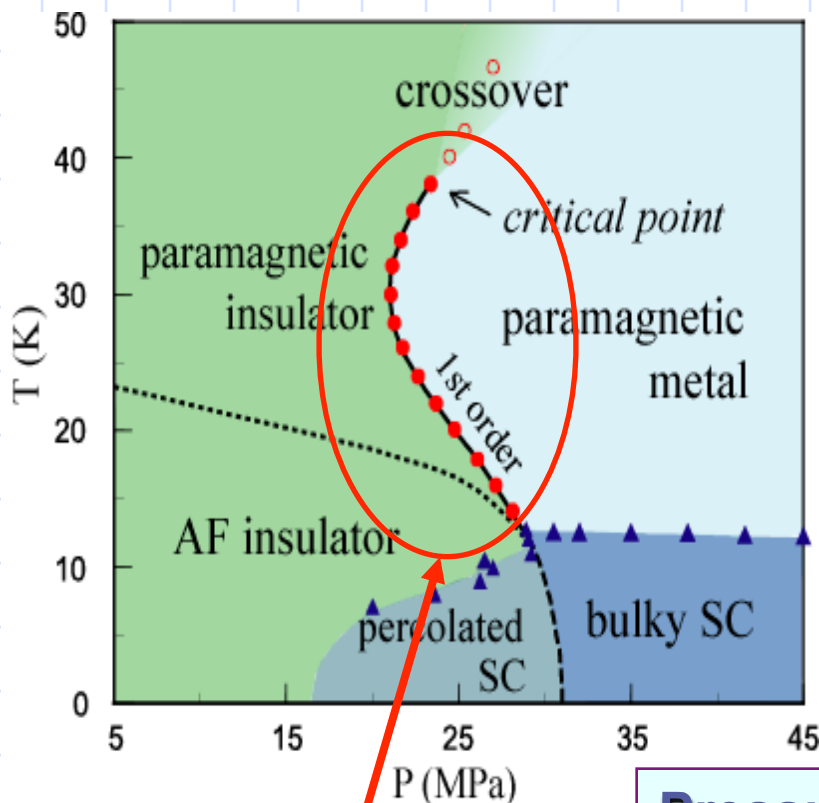


Resistance





F. Kagawa et al., PRB 69, 064511 (2004)

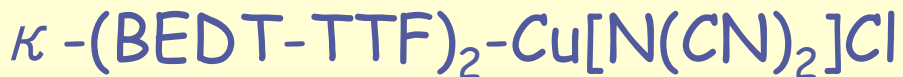


$t'/t = 0.8$

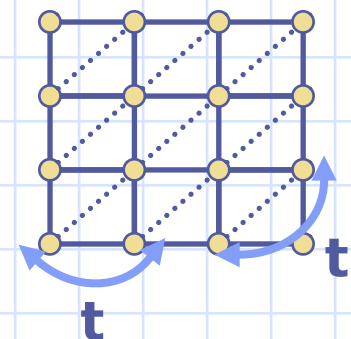
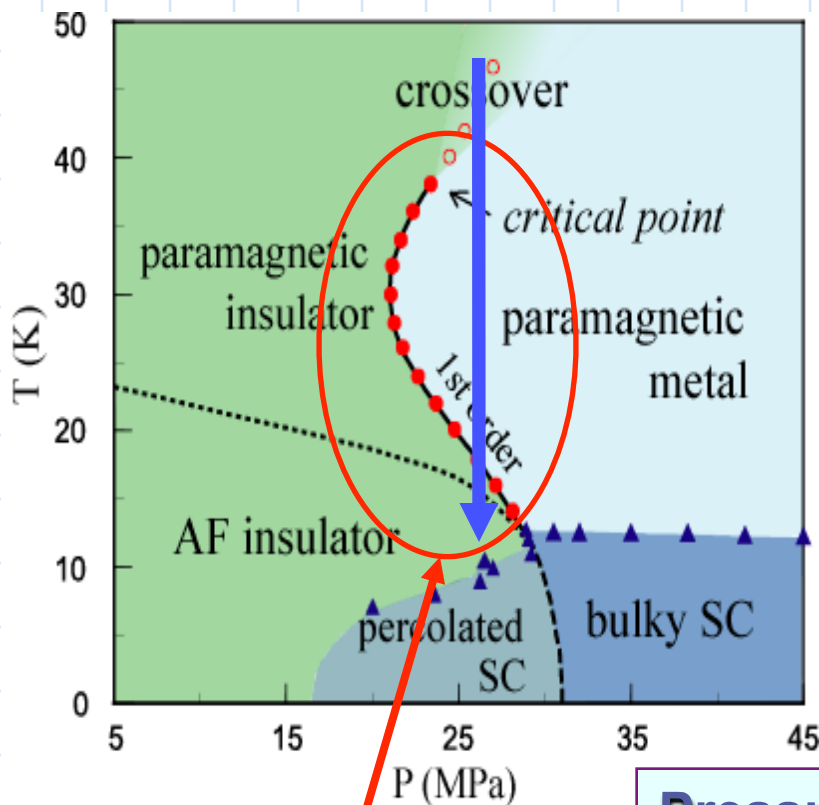
moderately frustrated

Finite-T Mott transition
Reentrant behavior





F. Kagawa et al., PRB 69, 064511 (2004)



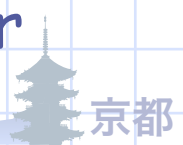
$t'/t = 0.8$

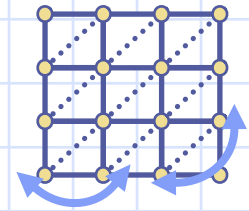
moderately frustrated

Pressure

Finite-T Mott transition
Reentrant behavior

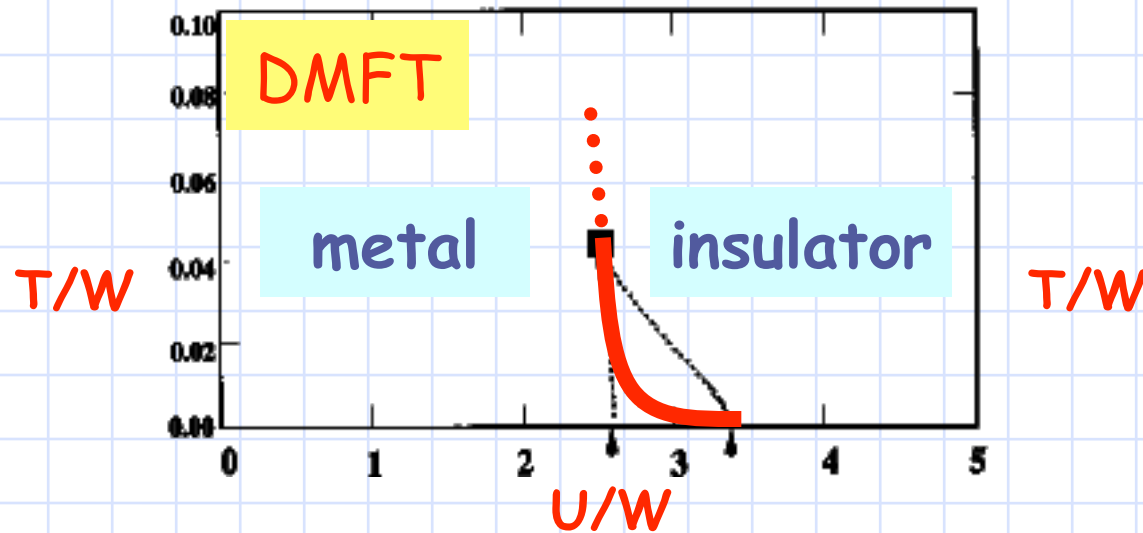
Itineracy vs Frustration



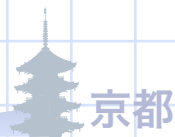


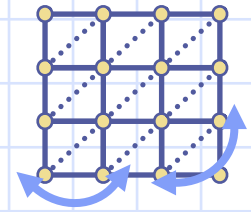
Basic & Naive question

$D = \infty$ Hubbard model



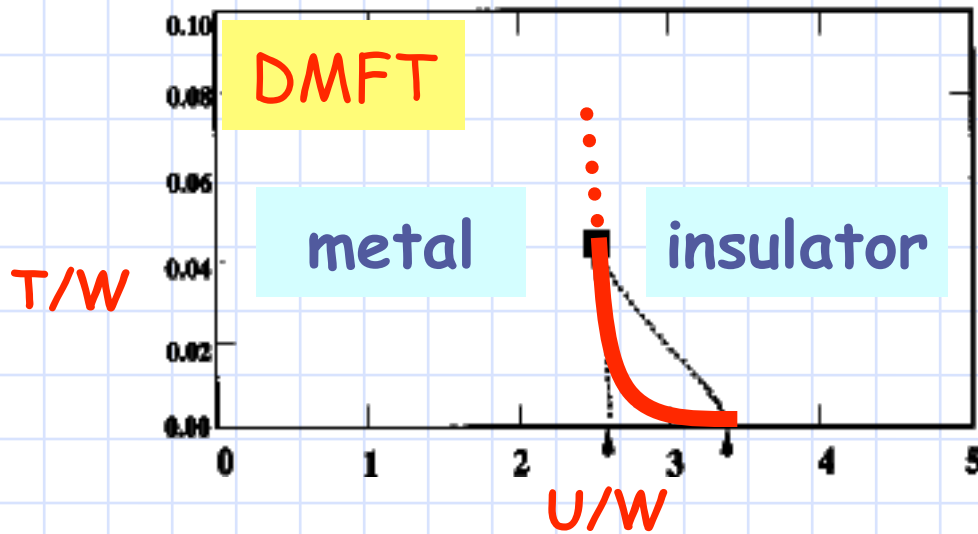
Georges et al., RMP, 68, 13 (1996)





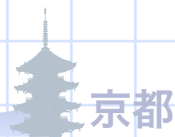
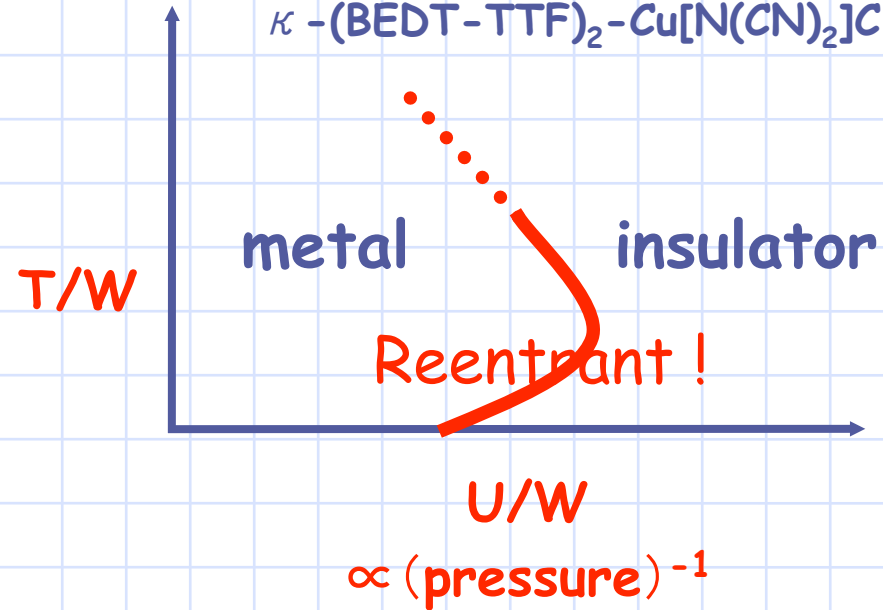
Basic & Naive question

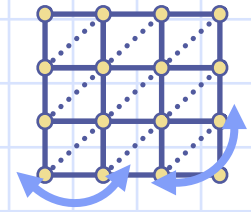
$D = \infty$ Hubbard model



Georges et al., RMP, 68, 13 (1996)

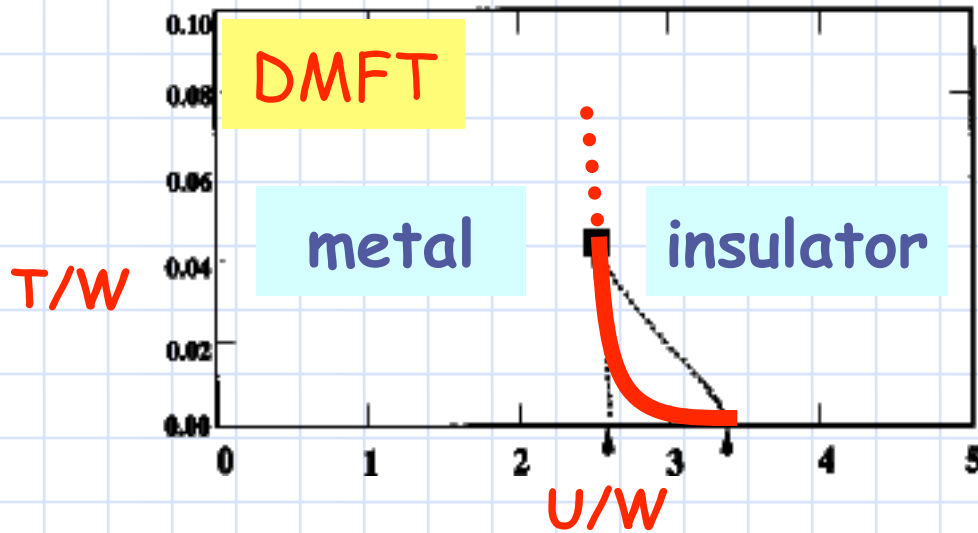
organics





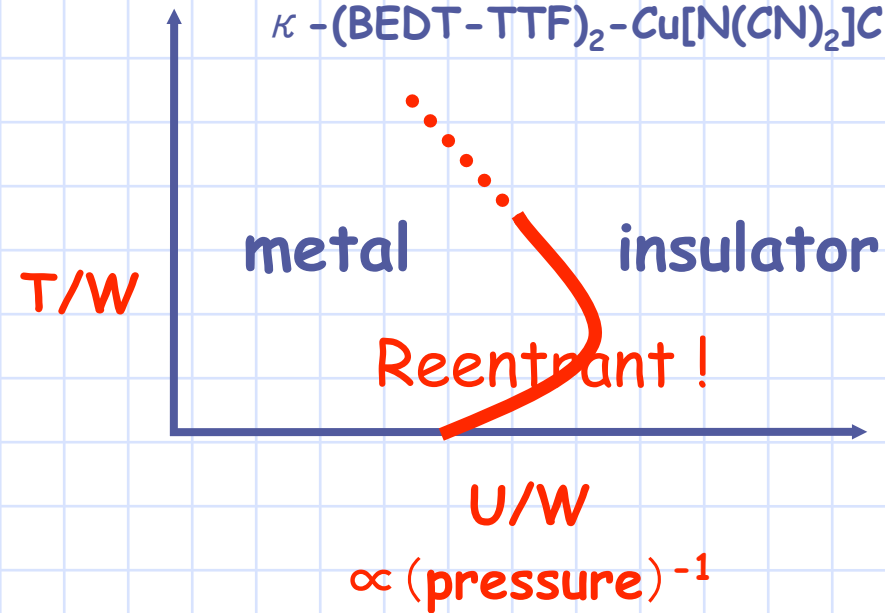
Basic & Naive question

$D = \infty$ Hubbard model



Georges et al., RMP, 68, 13 (1996)

organics



Effects of frustration



Cluster
(Cellular-DMFT)

YKIS 07
Kyoto
November 14,
2007

Cellular DMFT treatment



YKIS 07
Kyoto
November 14,
2007

Cellular DMFT treatment

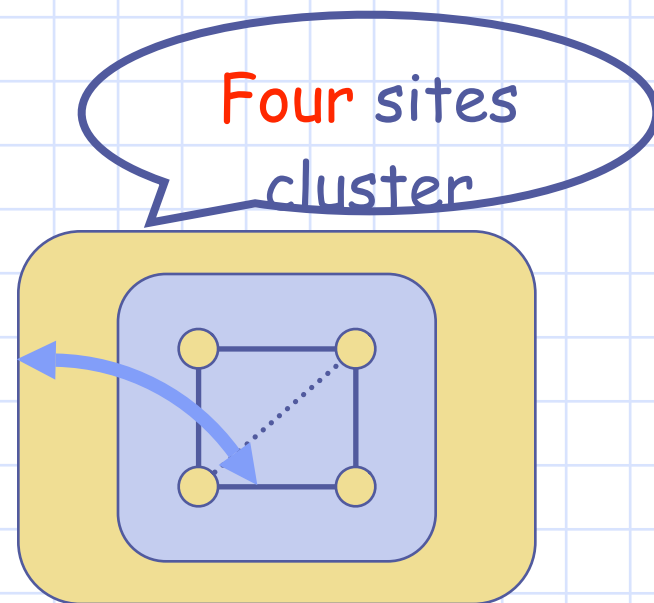
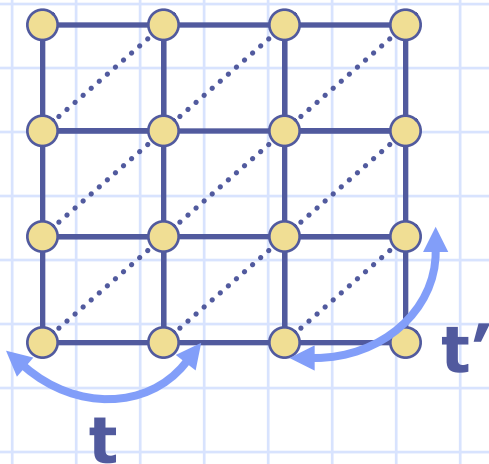
Reentrant Mott transition

Magnetic transition



Cellular-DMFT

Original Hubbard model

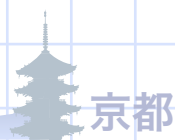


Effective cluster model



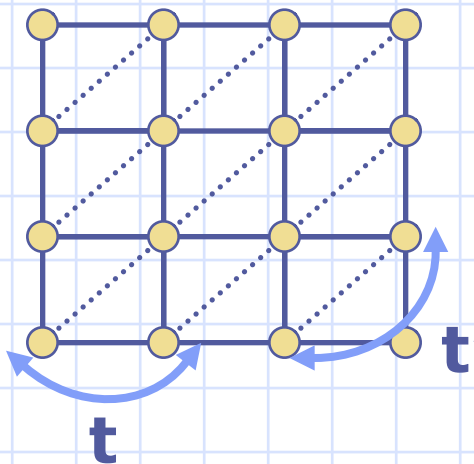
QMC method

(Hirsh-Fye algorithm)



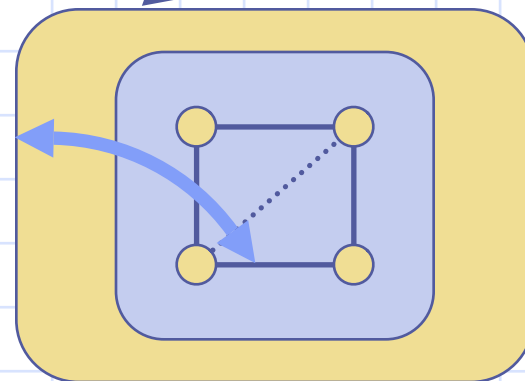
Cellular-DMFT

Original Hubbard model



Self-consistent
†

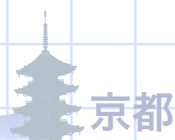
Four sites cluster



Effective cluster model

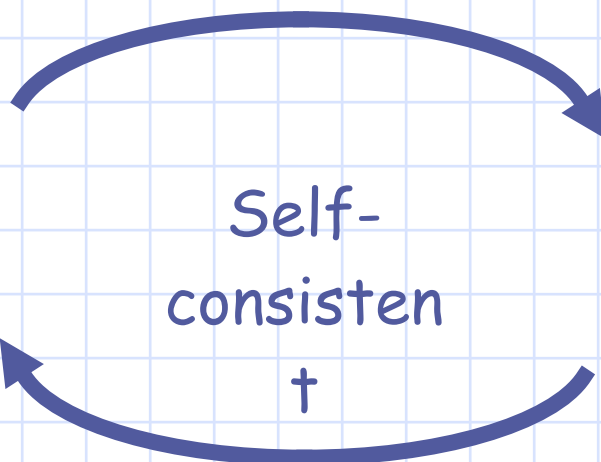
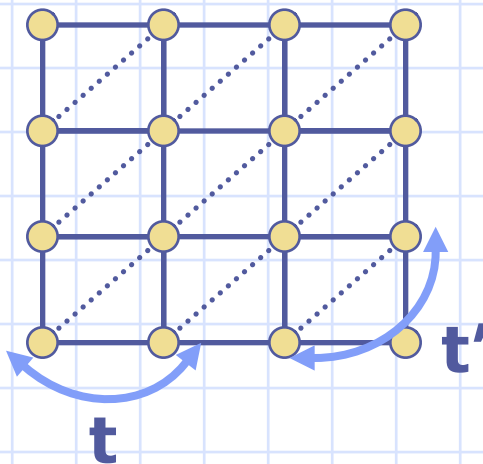
QMC method

(Hirsh-Fye algorithm)

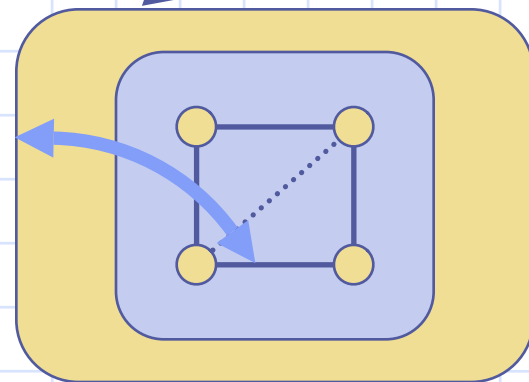


Cellular-DMFT

Original Hubbard model



Four sites cluster



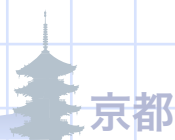
Effective cluster model



QMC method

(Hirsh-Fye algorithm)

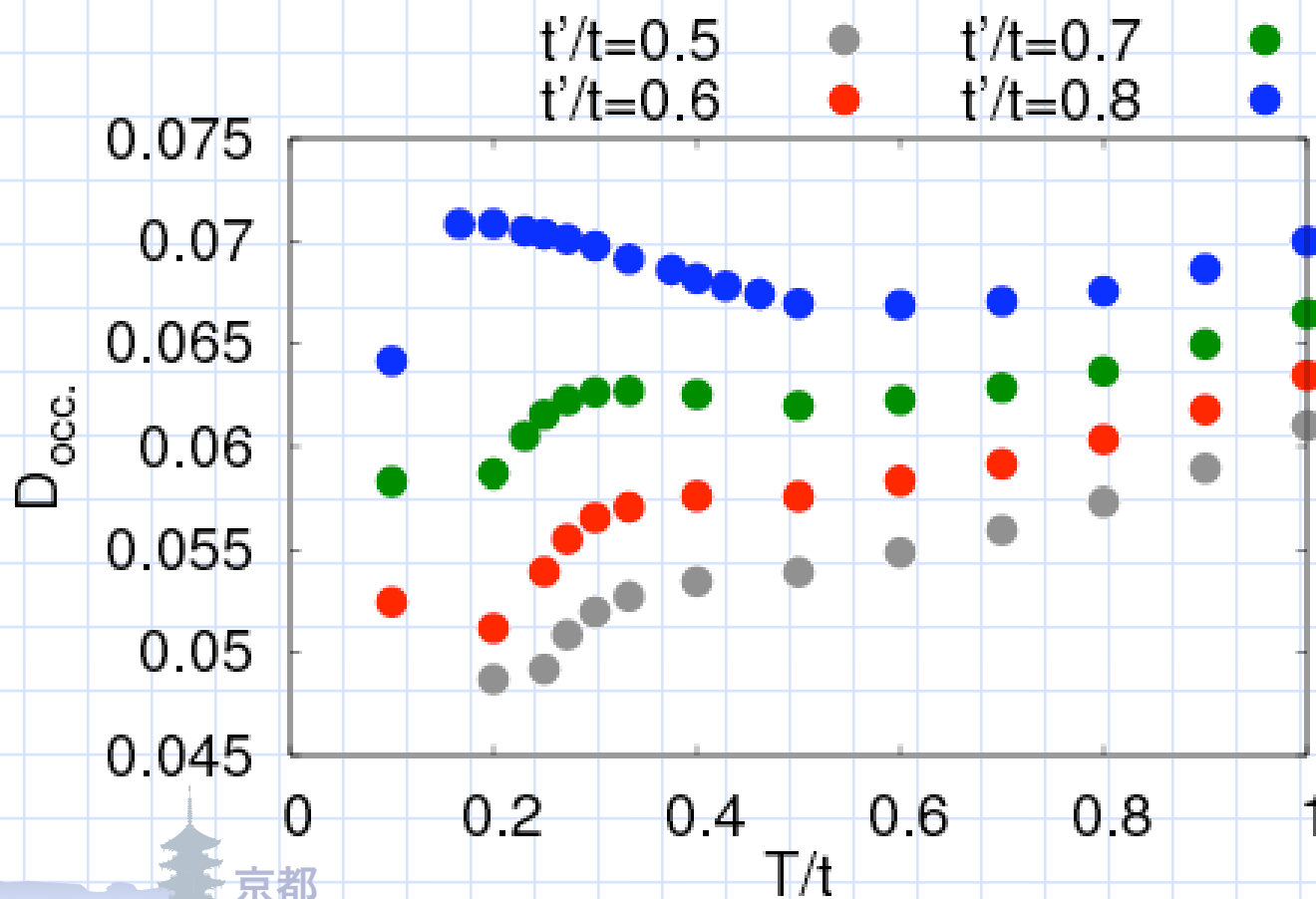
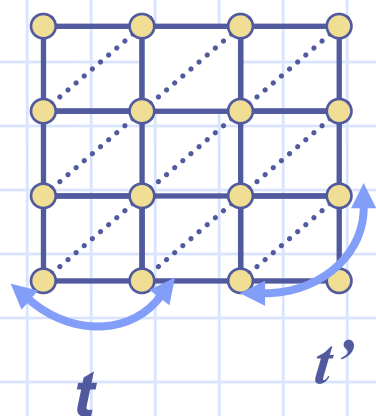
$t'/t=0$: square lattice
 $t'/t=1$: triangular lattice



Nonmonotonic T-dependence

Cellular DMFT

$$U/t = 8$$

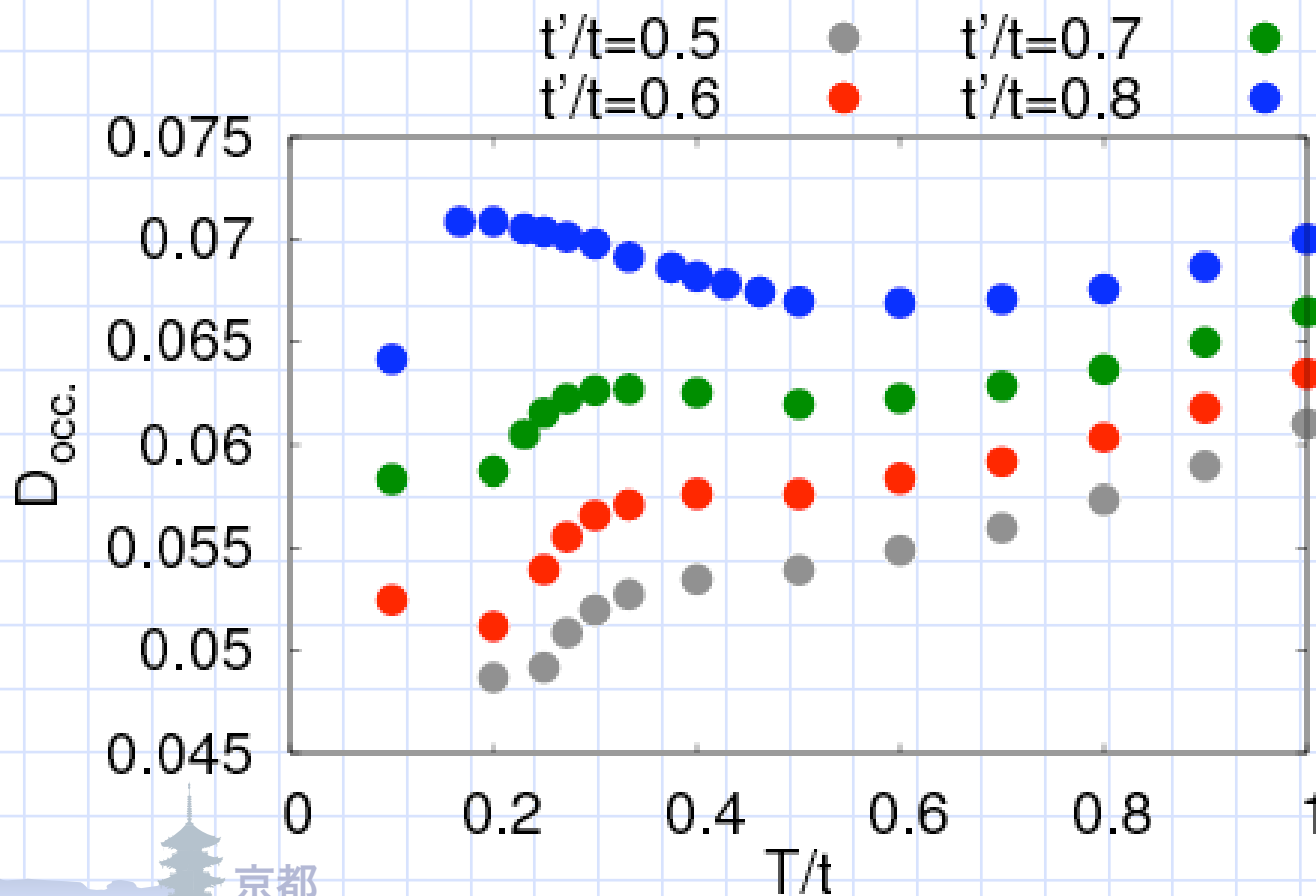
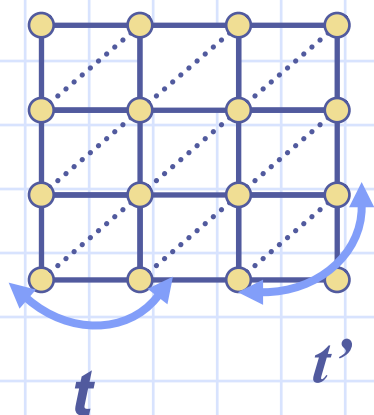


Nonmonotonic T-dependence

Cellular DMFT

Double occupancy

$$U/t = 8$$

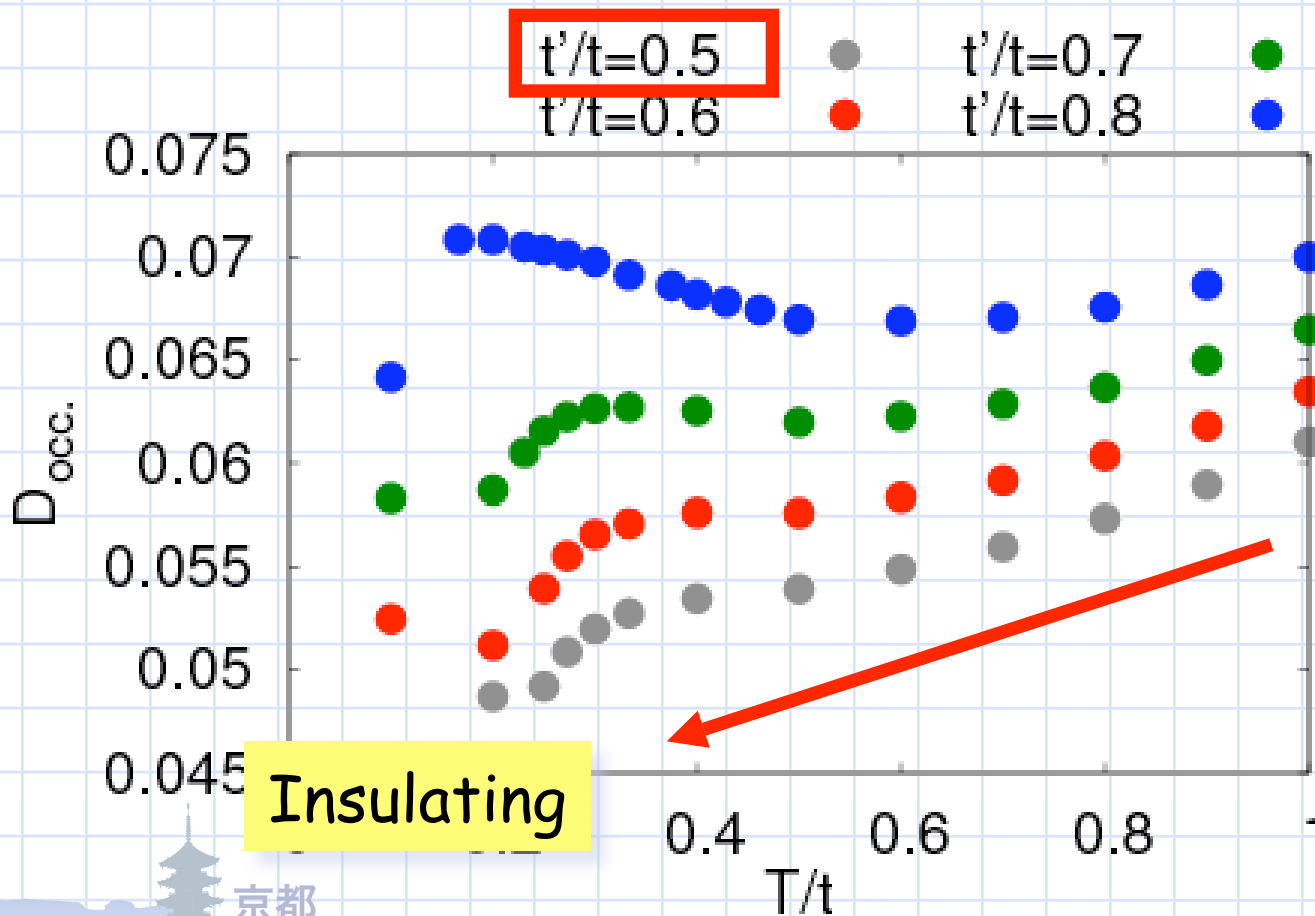
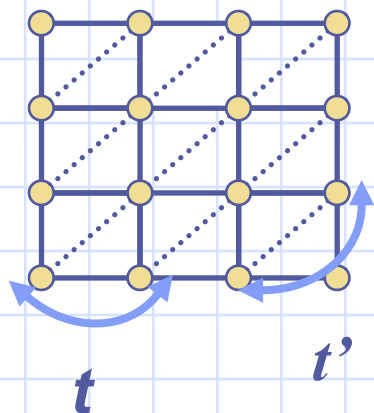


Nonmonotonic T-dependence

Cellular DMFT

Double occupancy

$$U/t = 8$$

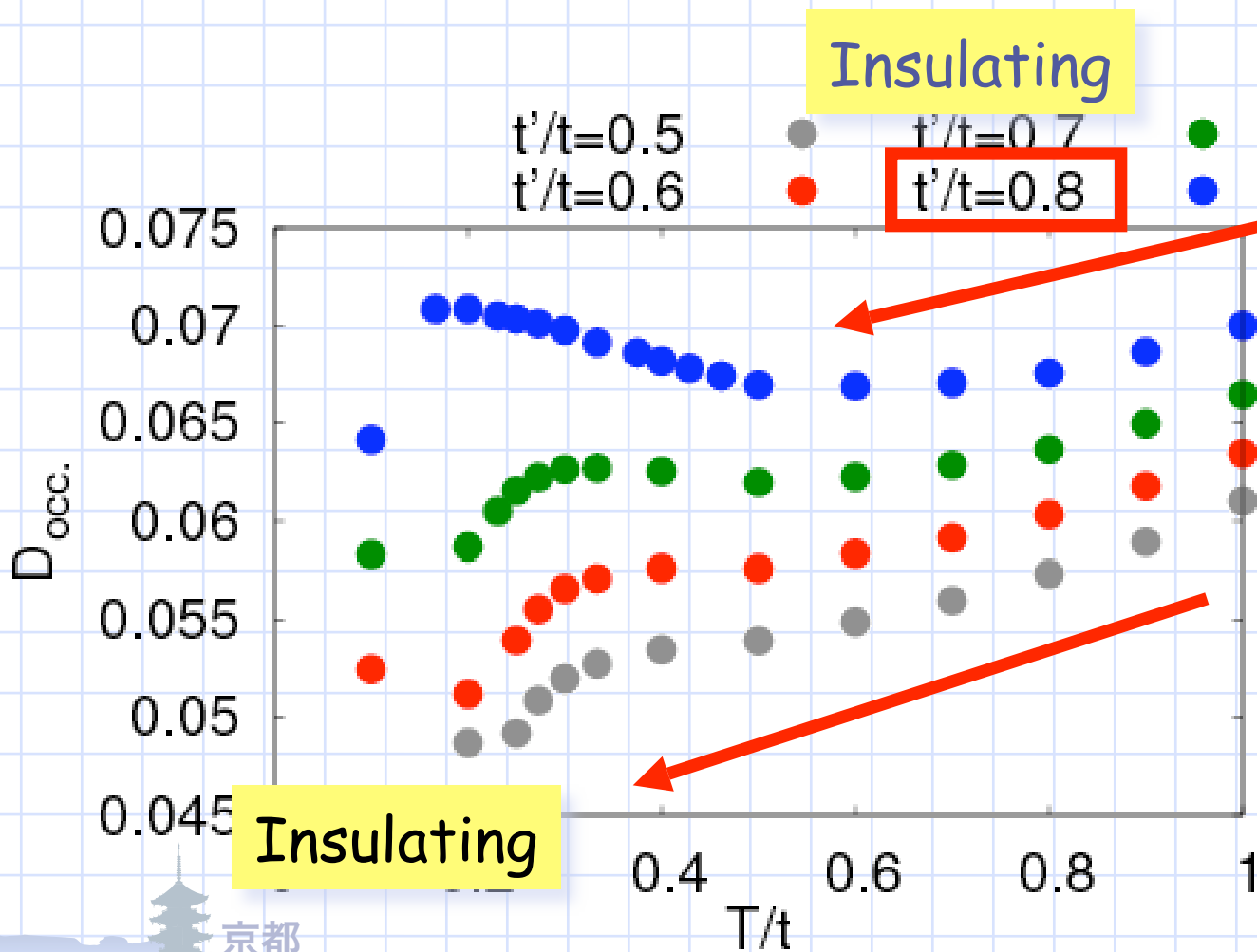
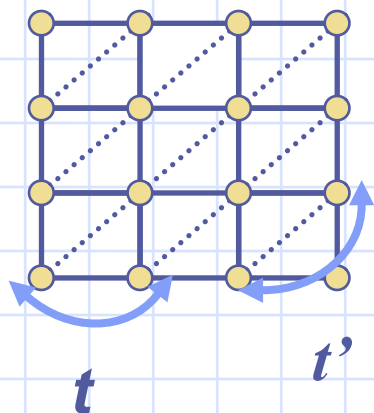


Nonmonotonic T-dependence

Cellular DMFT

Double occupancy

$$U/t = 8$$



Nonmonotonic T-dependence

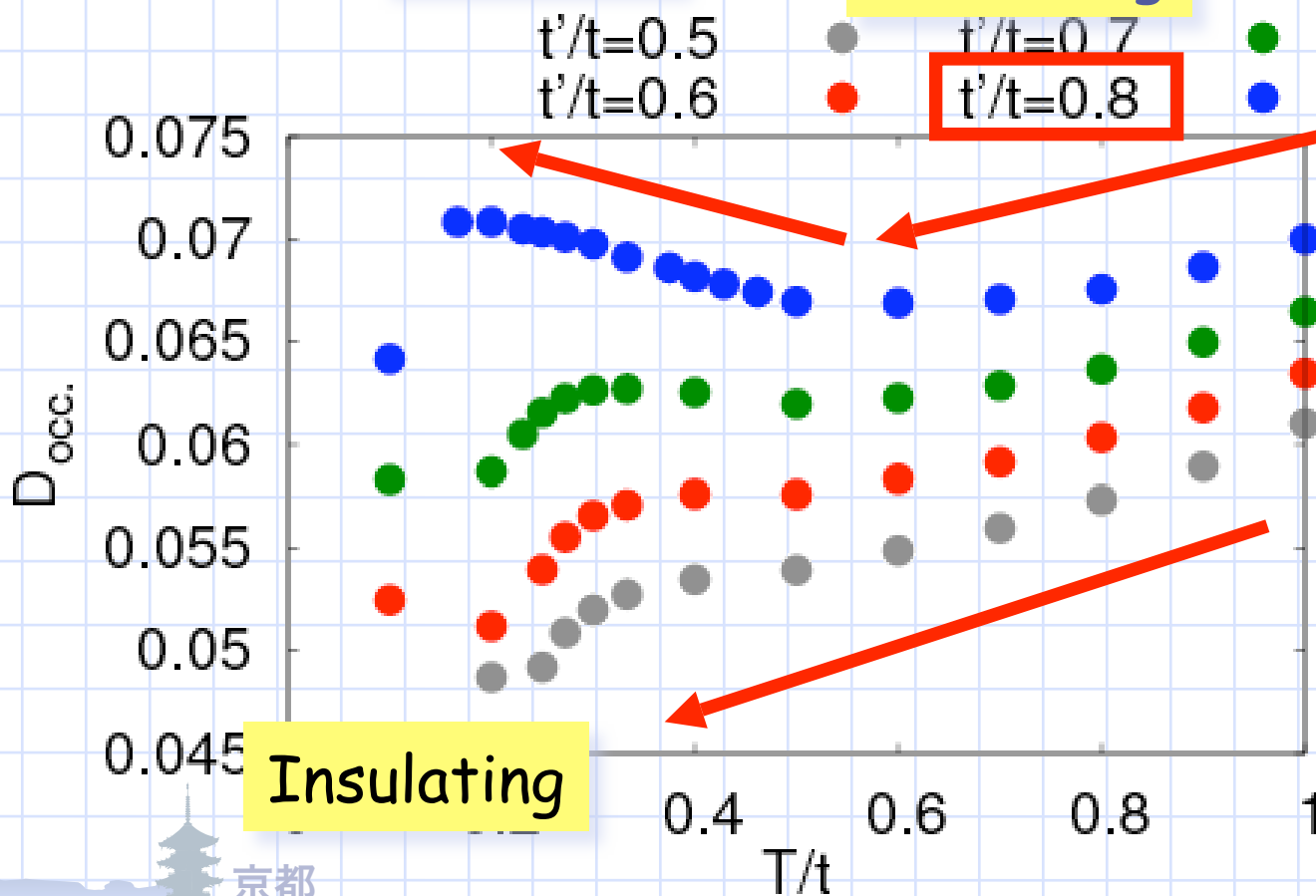
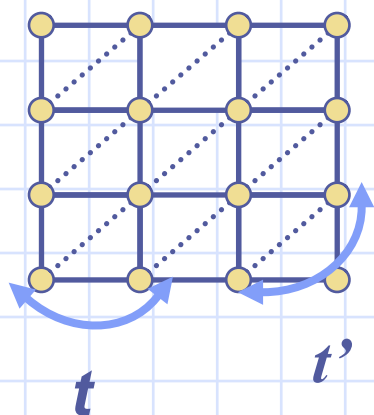
Cellular DMFT

Double occupancy

$$U/t = 8$$

Metallic

Insulating



Insulating

Nonmonotonic T-dependence

Cellular DMFT

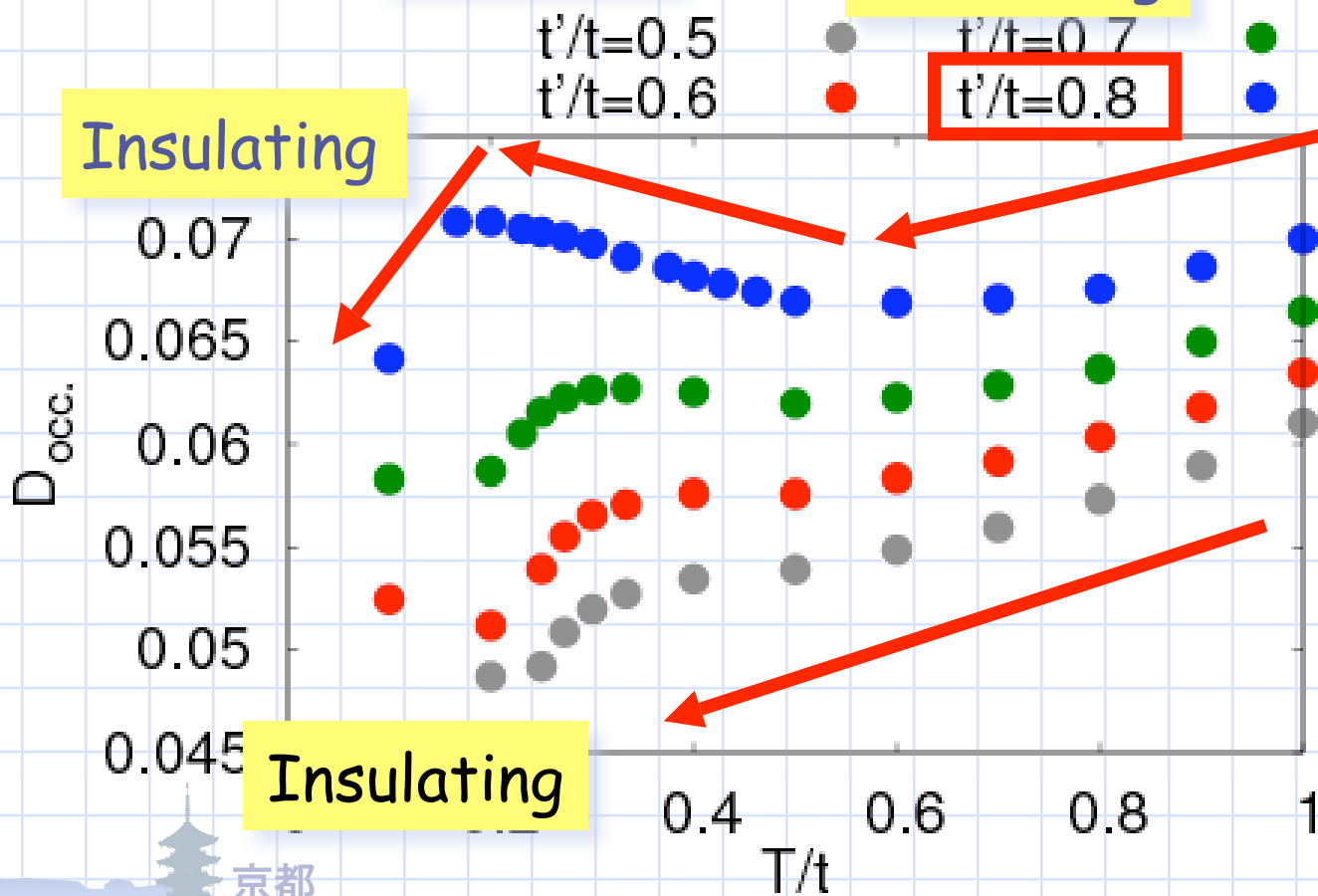
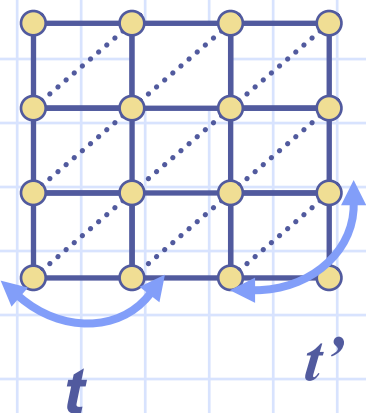
Double occupancy

$$U/t = 8$$

Metallic

Insulating

Insulating



Insulating

Nonmonotonic T-dependence

Cellular DMFT

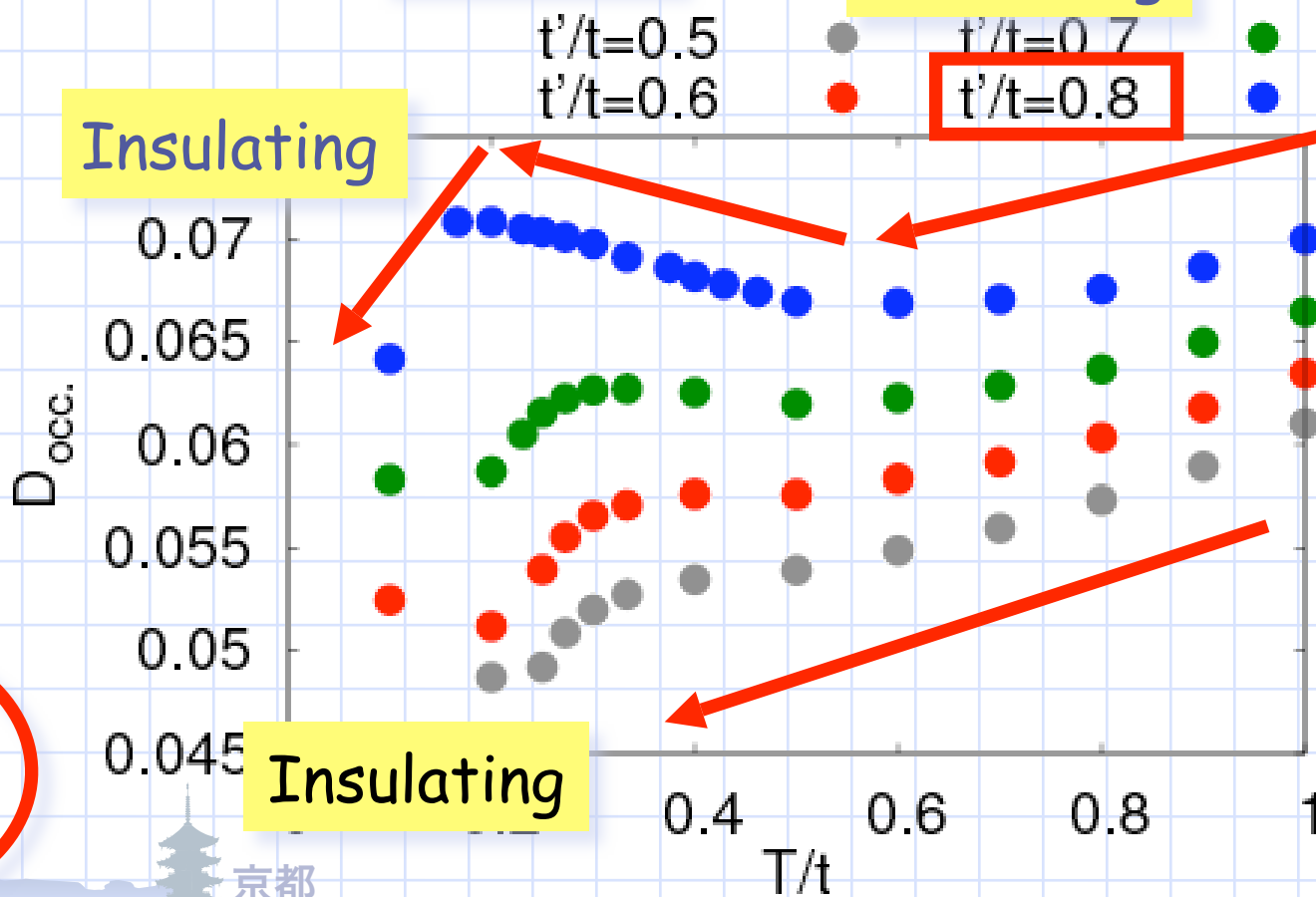
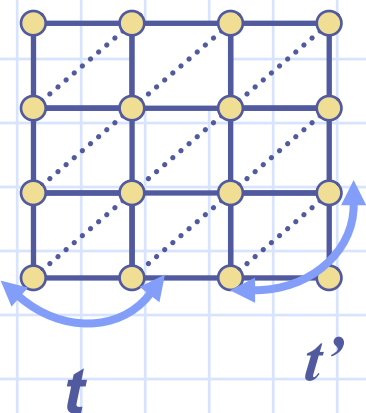
Double occupancy

$$U/t = 8$$

Metallic

Insulating

Insulating

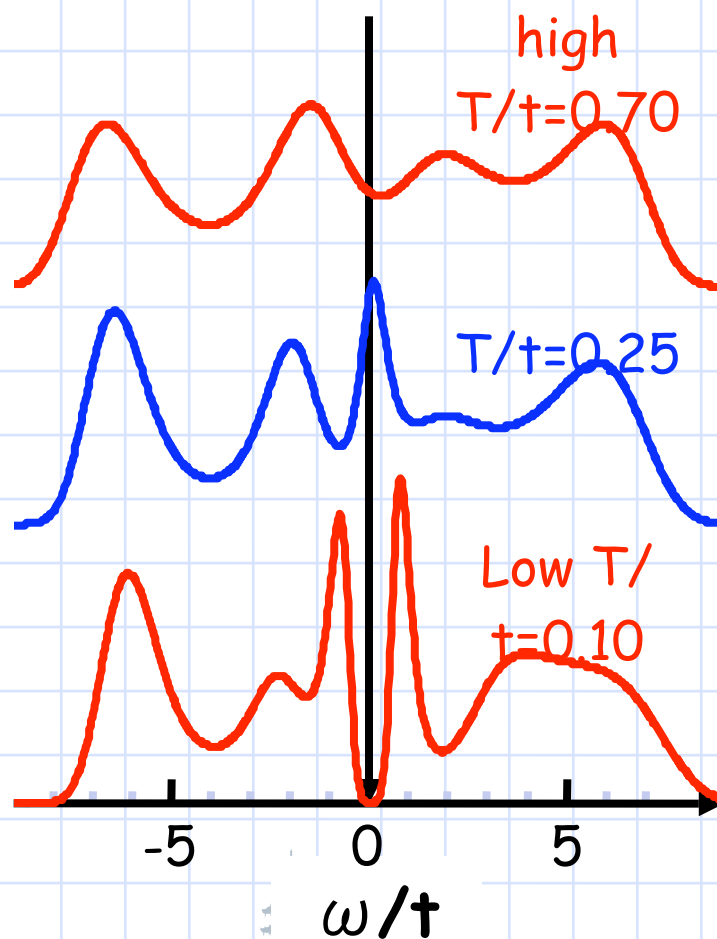


focus

$t'/t=0.8$

Density of states

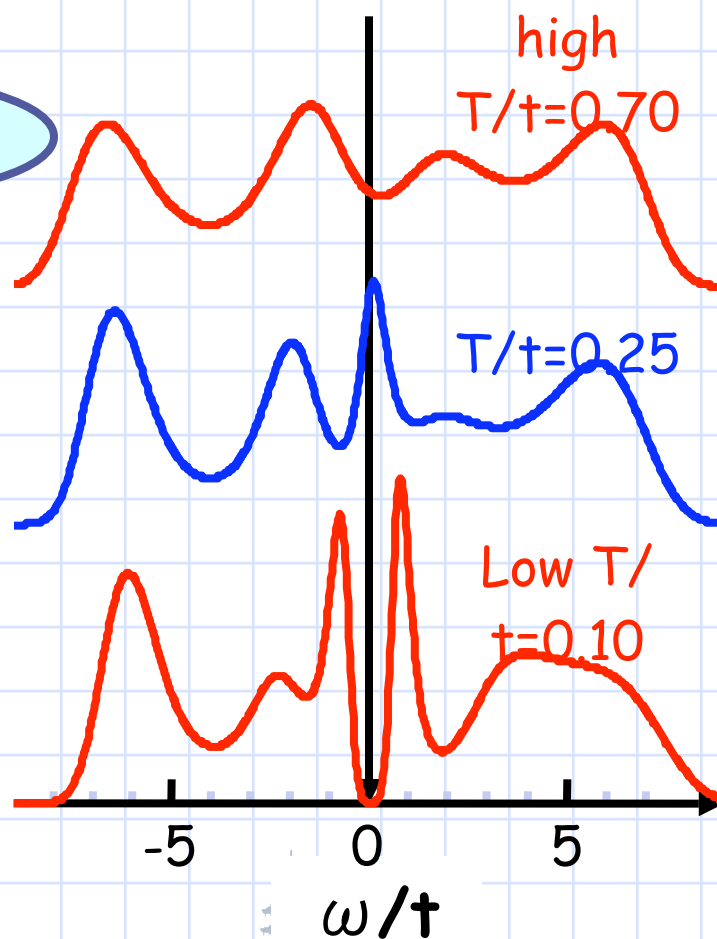
$$U/t = 8 \quad t'/t = 0.8$$



Density of states

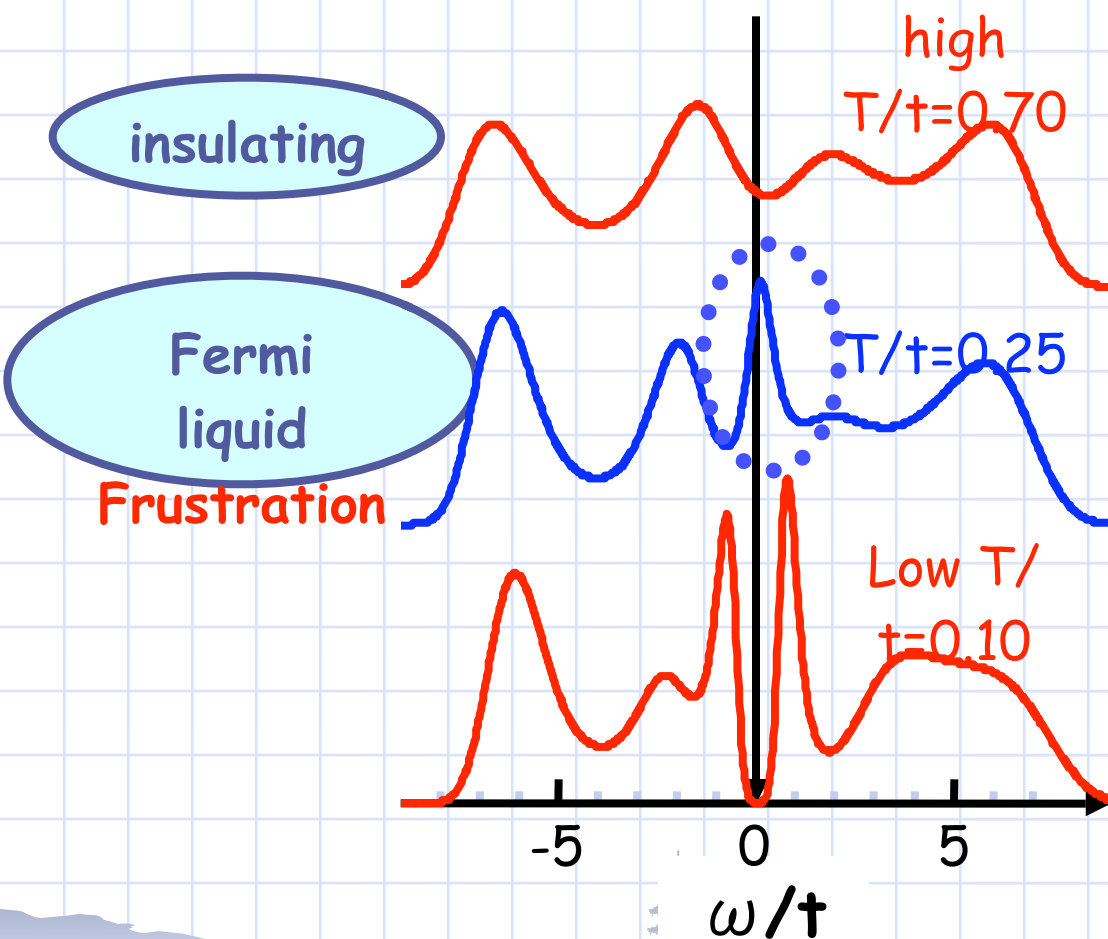
$$U/t = 8 \quad t'/t = 0.8$$

insulating



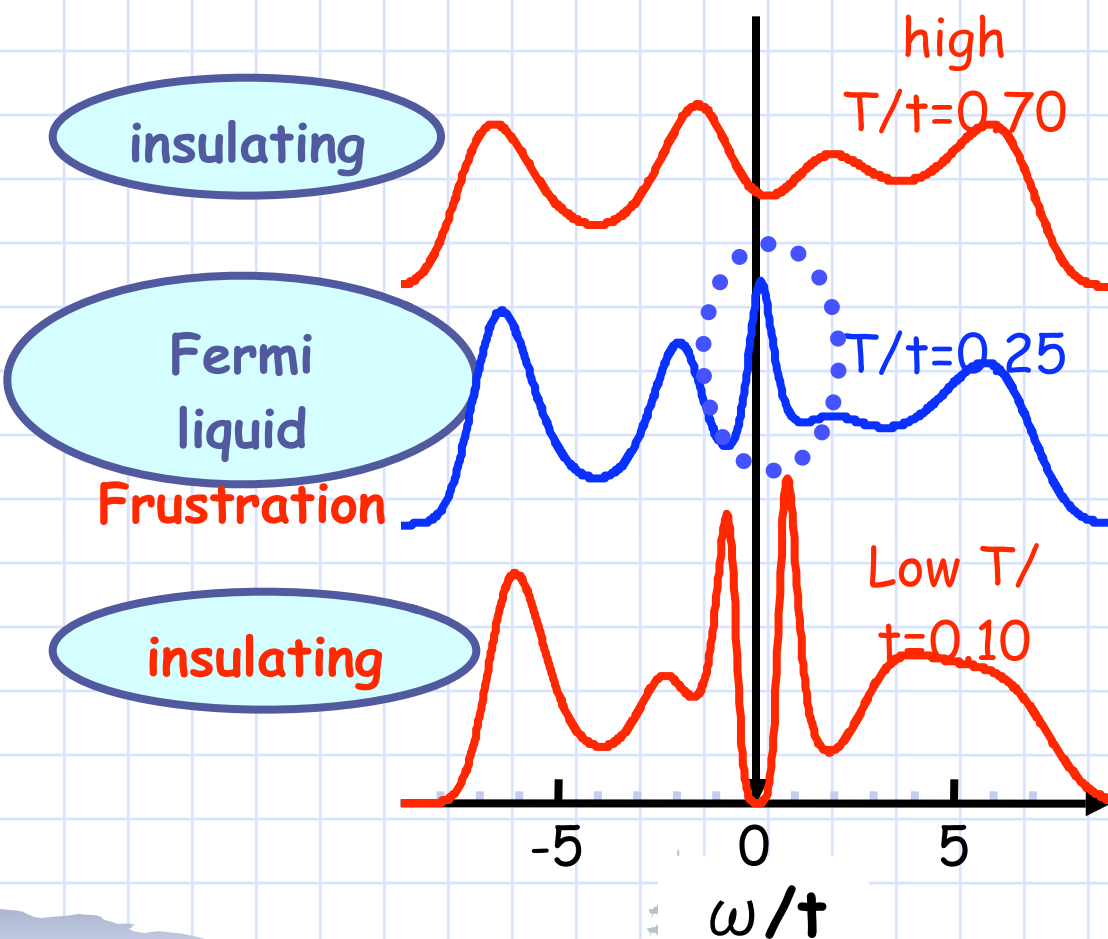
Density of states

$$U/t = 8 \quad t'/t = 0.8$$



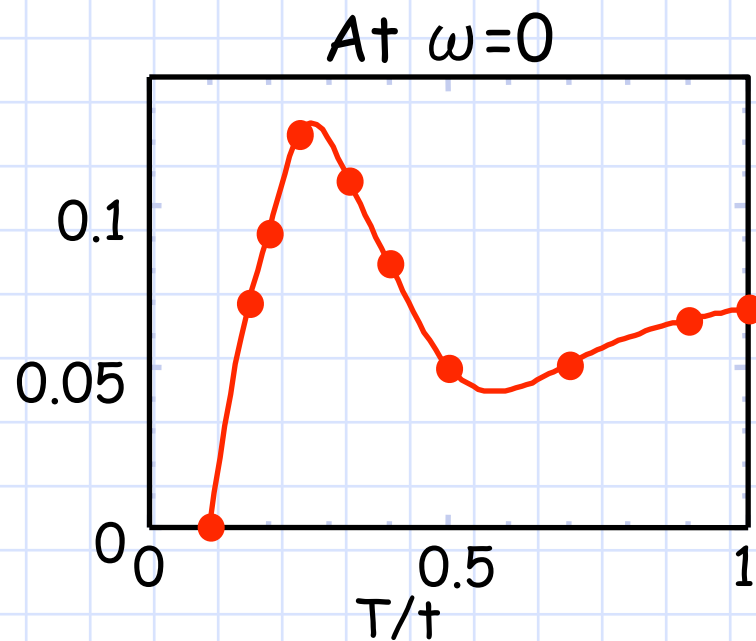
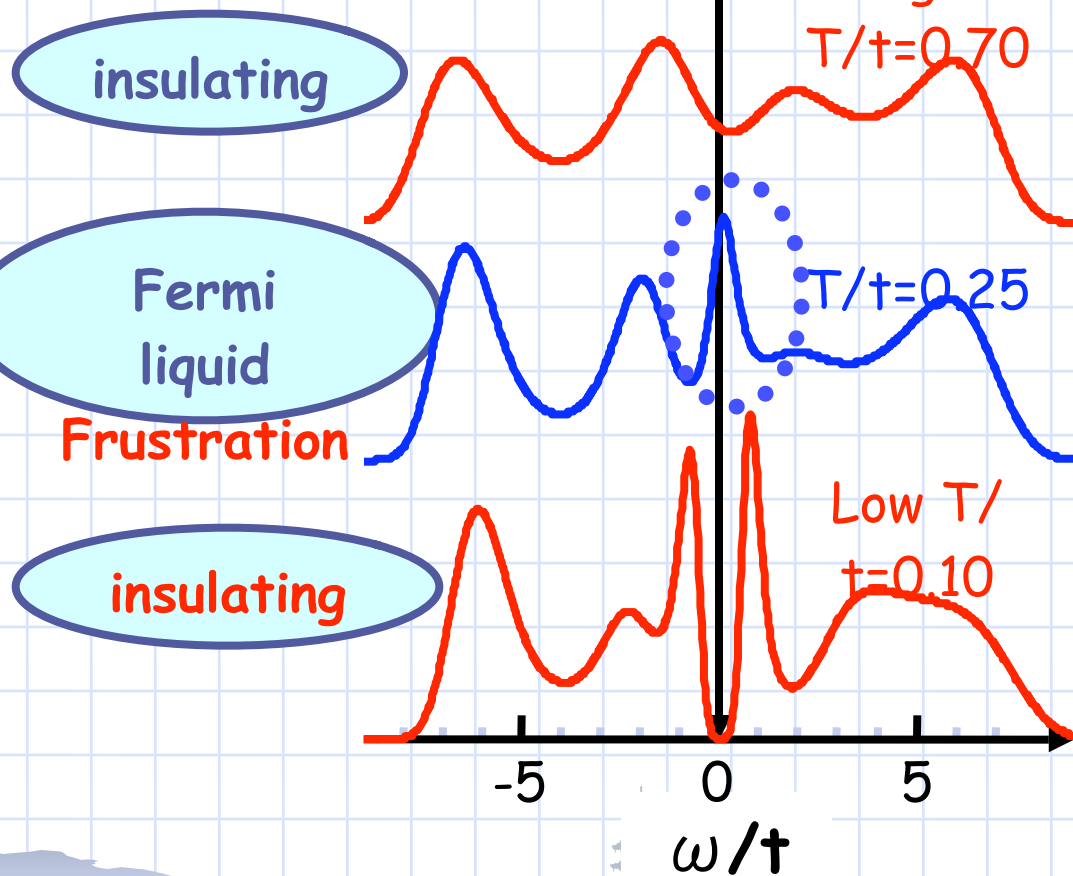
Density of states

$$U/t = 8 \quad t'/t = 0.8$$



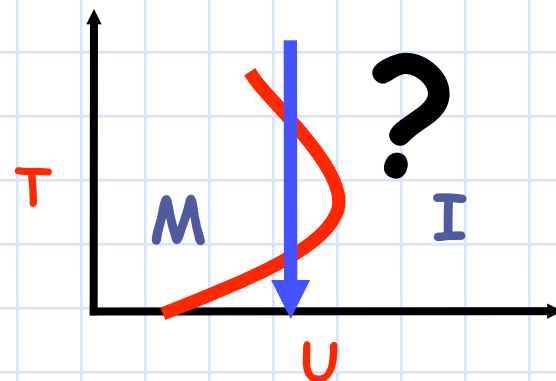
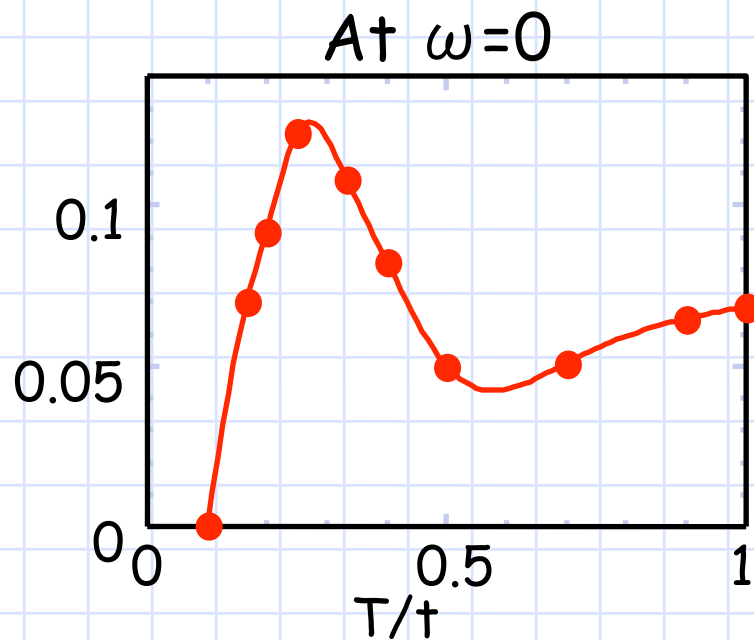
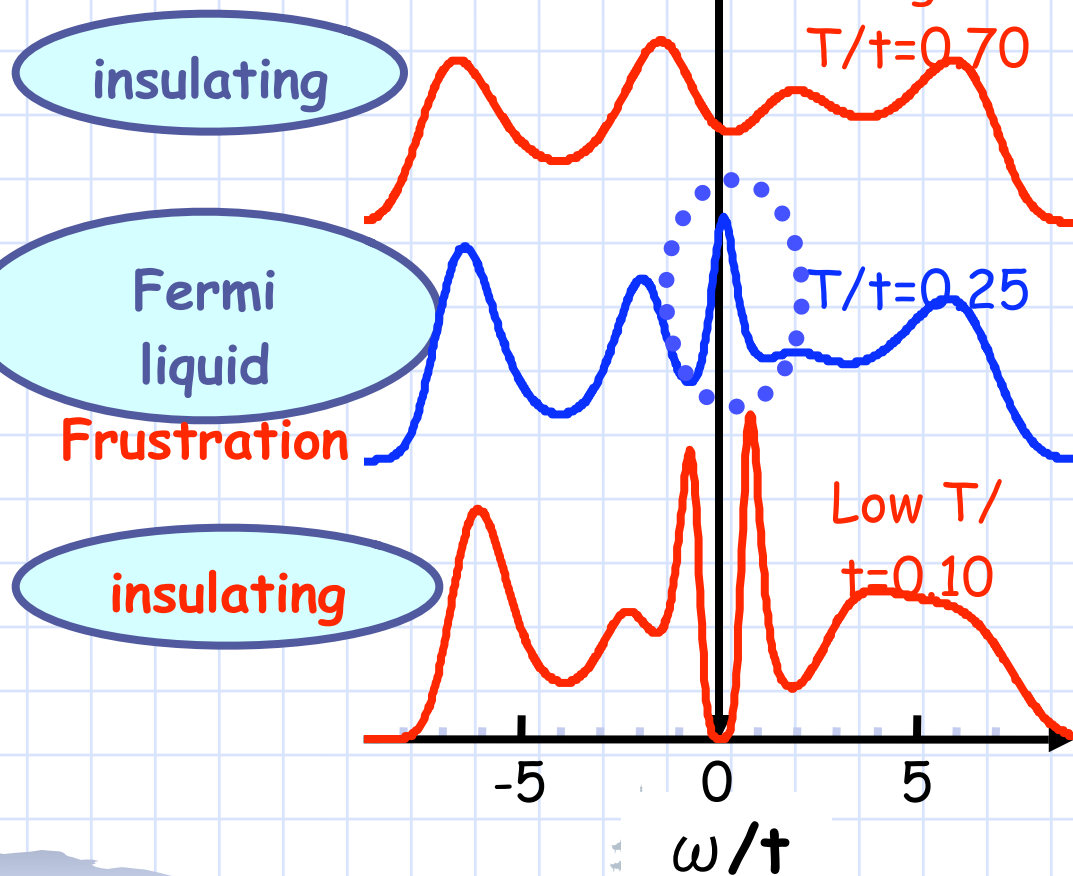
Density of states

$$U/t = 8 \quad t'/t = 0.8$$



Density of states

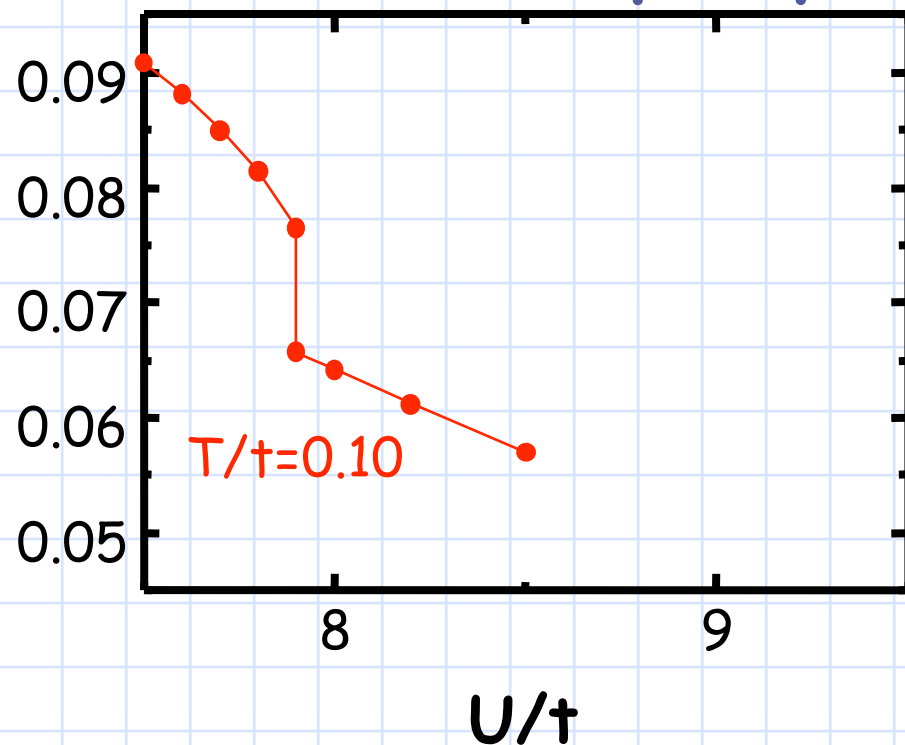
$$U/t = 8 \quad t'/t = 0.8$$



Mott transition

$$t'/t=0.8$$

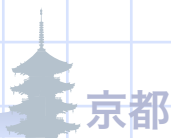
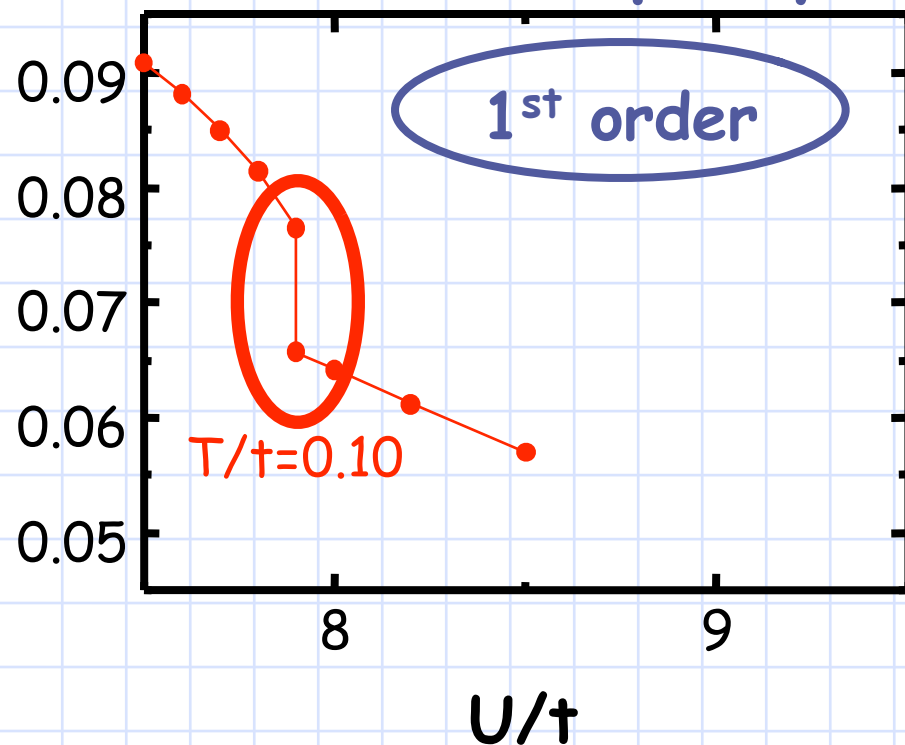
Double occupancy



Mott transition

$$t'/t=0.8$$

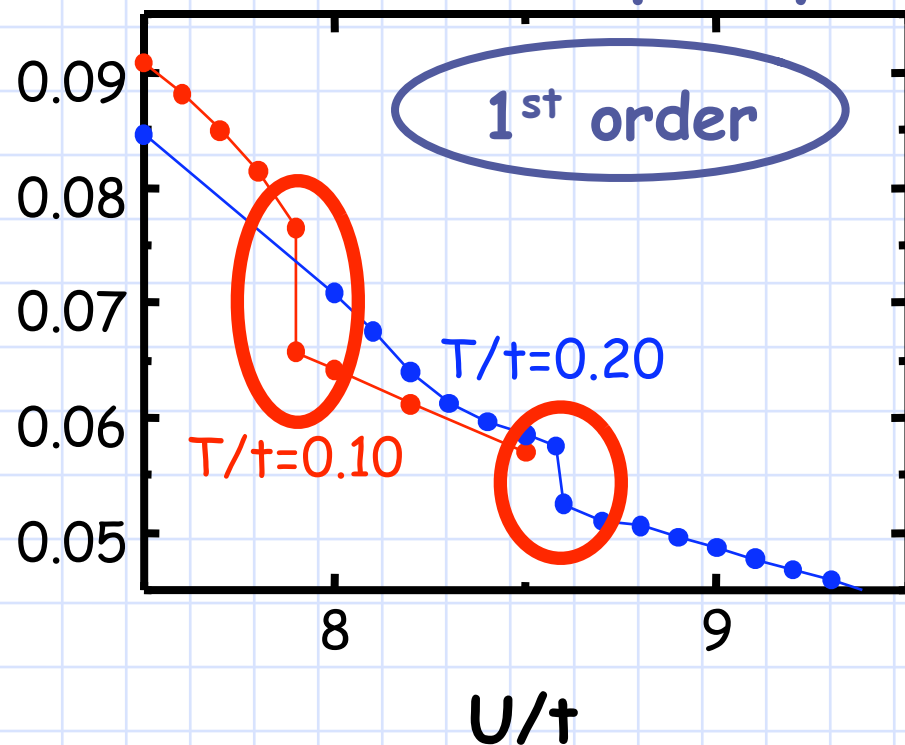
Double occupancy



Mott transition

$$t'/t=0.8$$

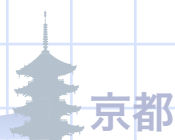
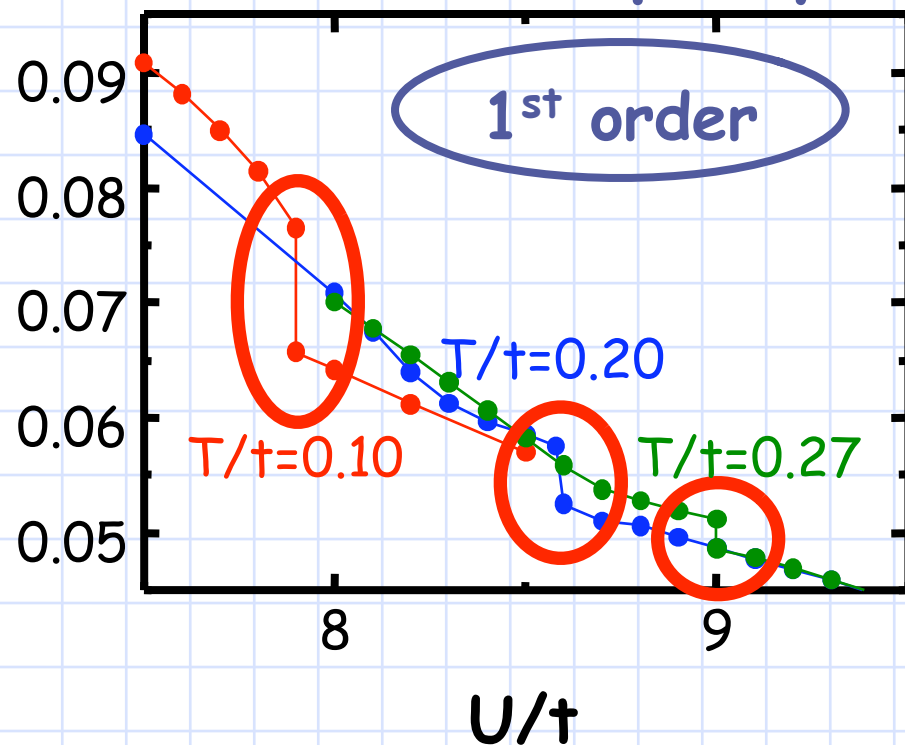
Double occupancy



Mott transition

$$t'/t=0.8$$

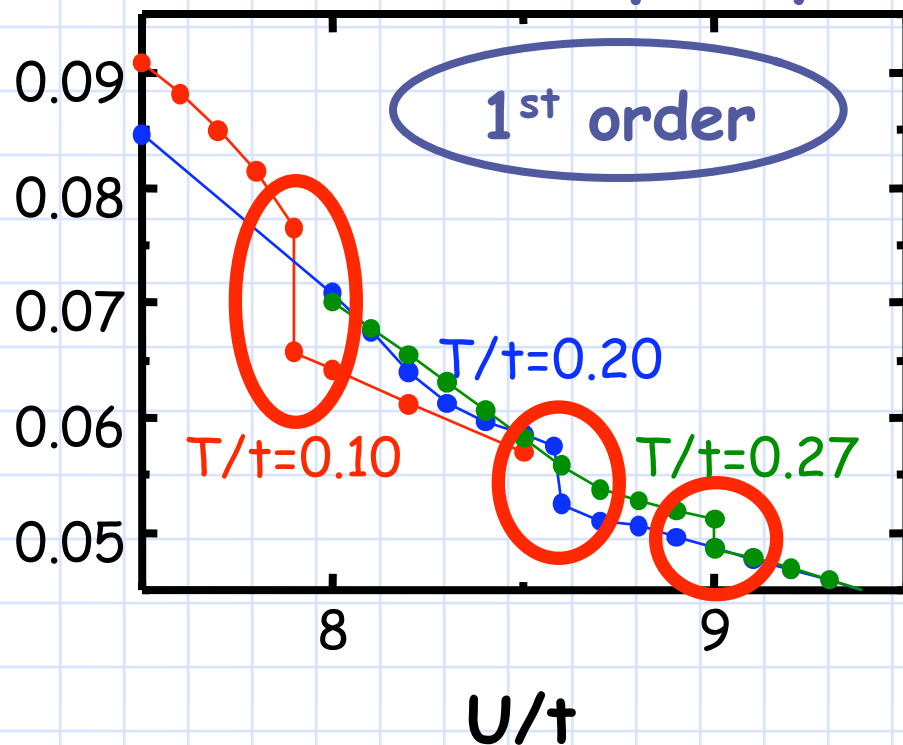
Double occupancy



Mott transition

$$t'/t=0.8$$

Double occupancy

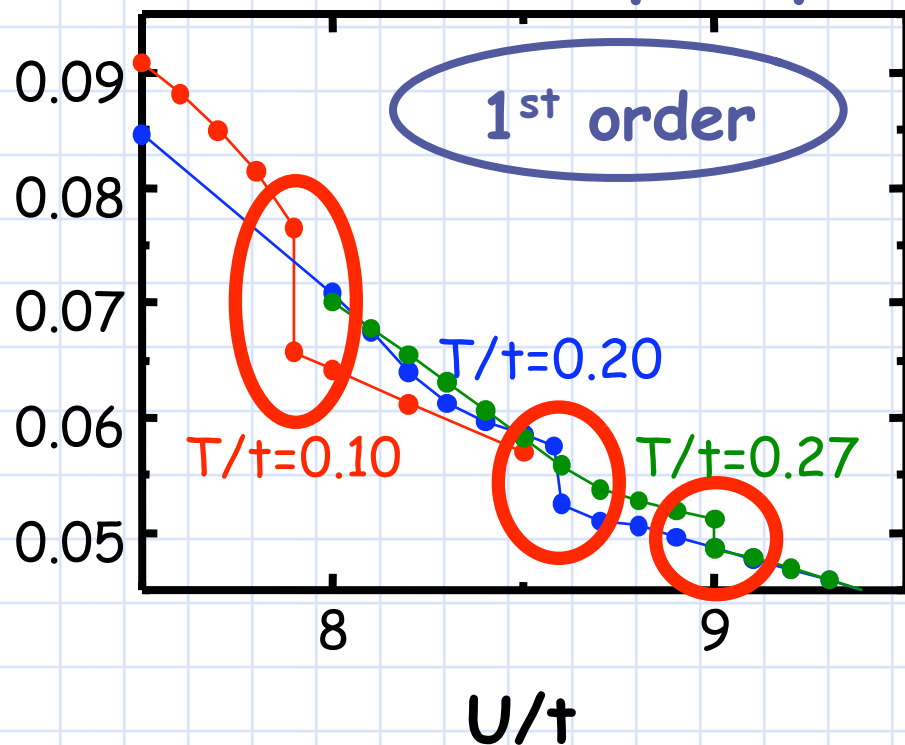


U_c increases with T

Mott transition

$t'/t=0.8$

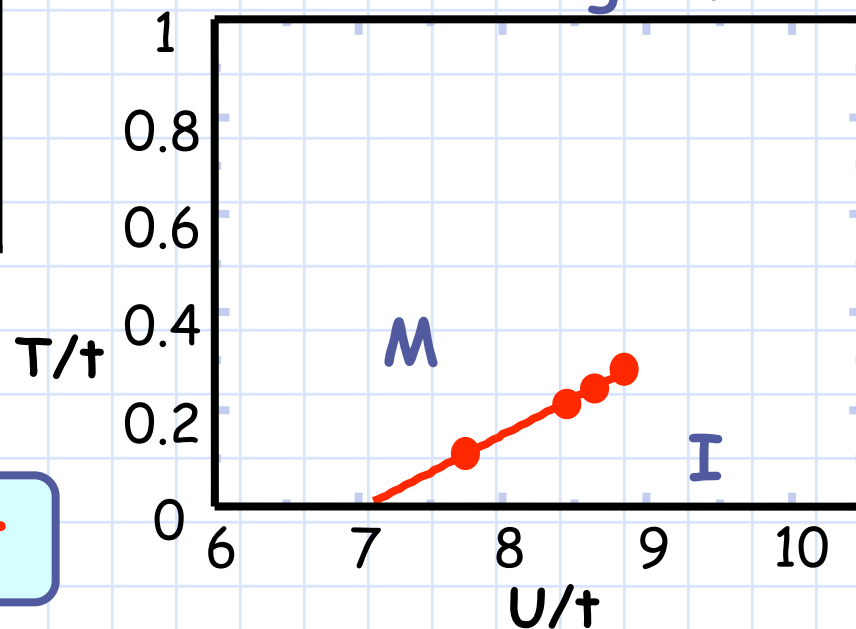
Double occupancy



U_c increases with T

Contrasted to
DMFT

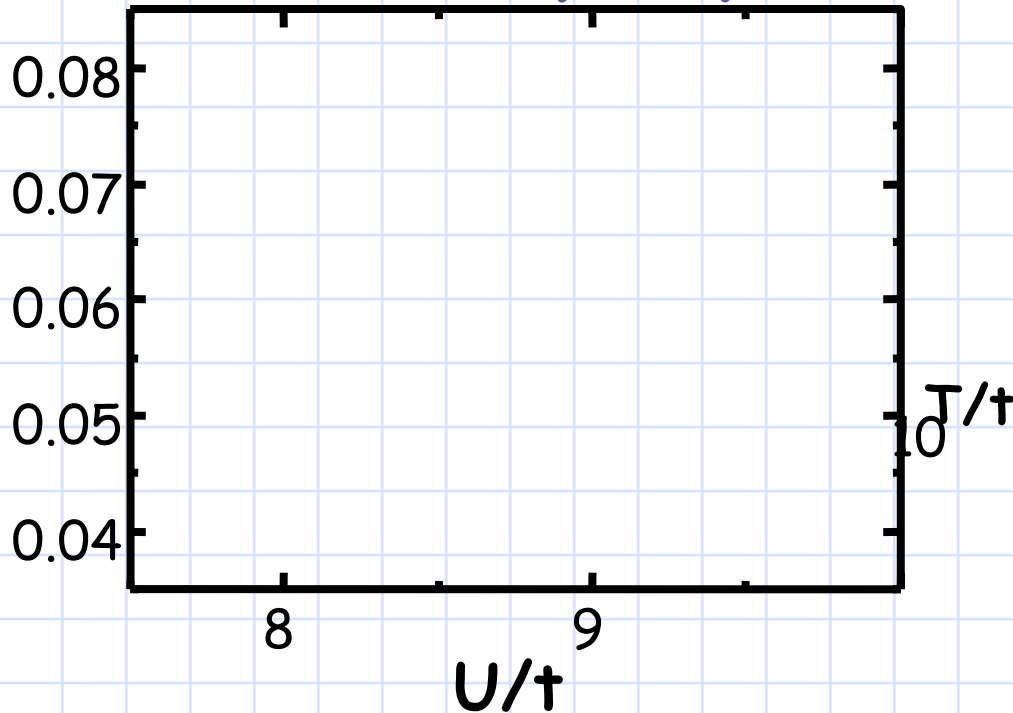
Phase diagram



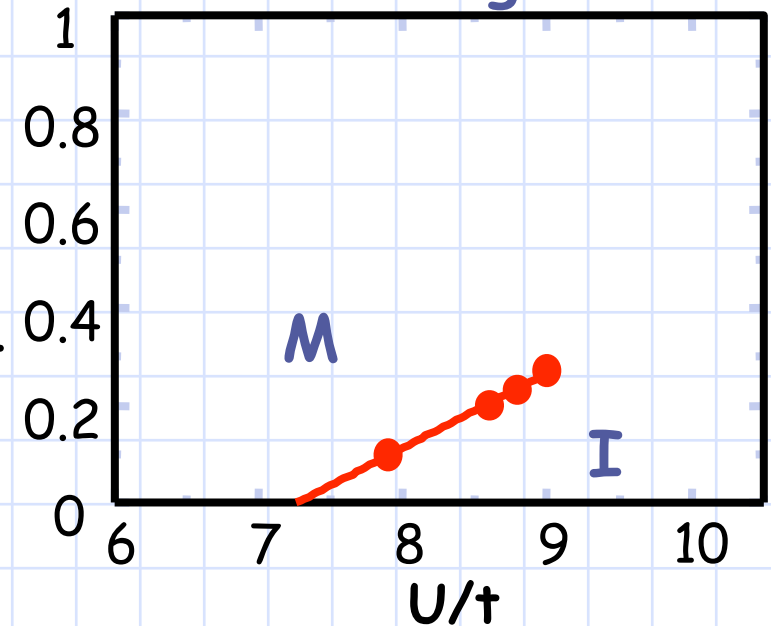
High-temperature behavior

$$t'/t=0.8$$

Double occupancy



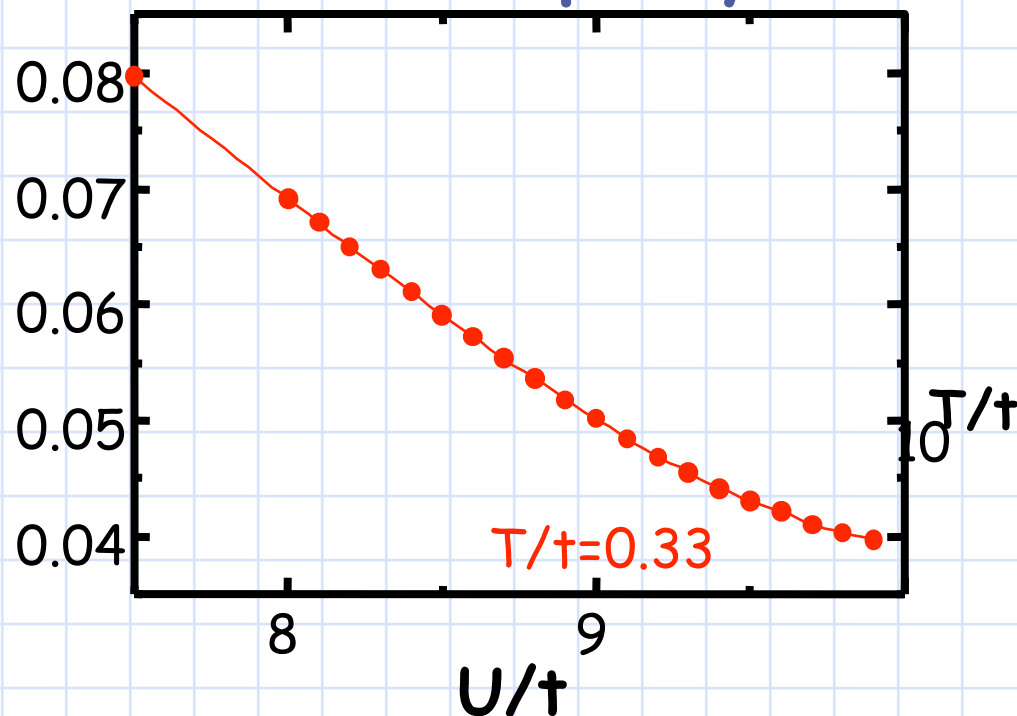
Phase diagram



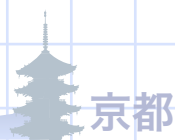
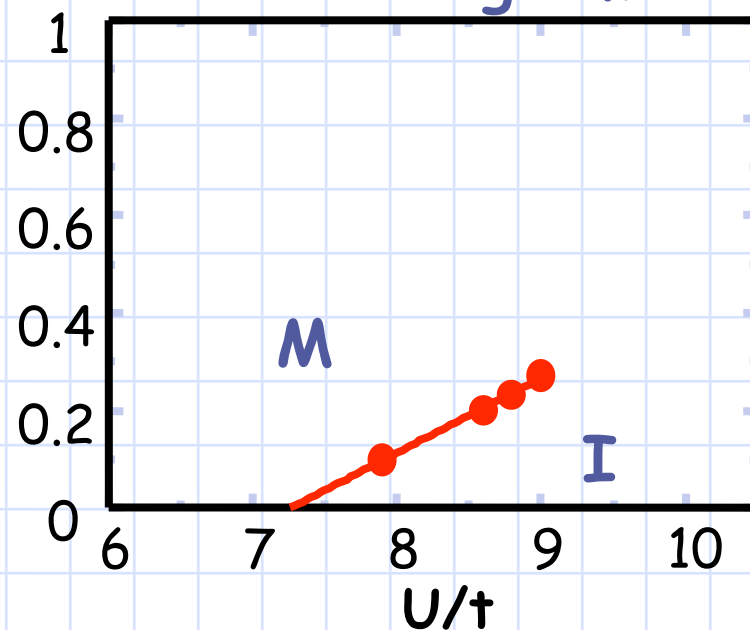
High-temperature behavior

$$t'/t=0.8$$

Double occupancy



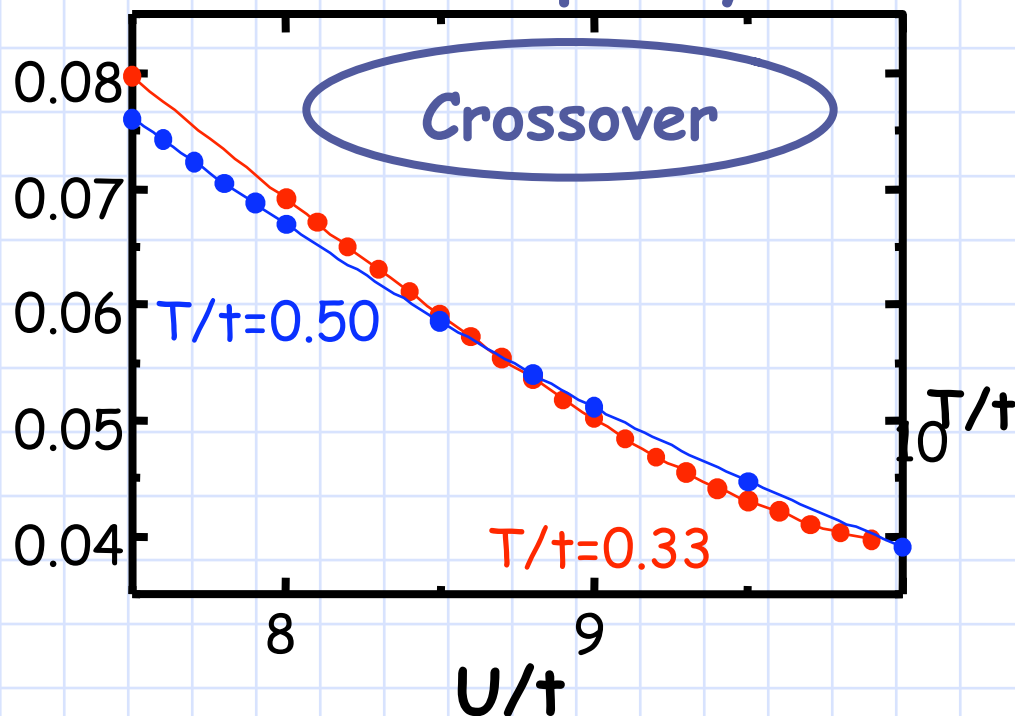
Phase diagram



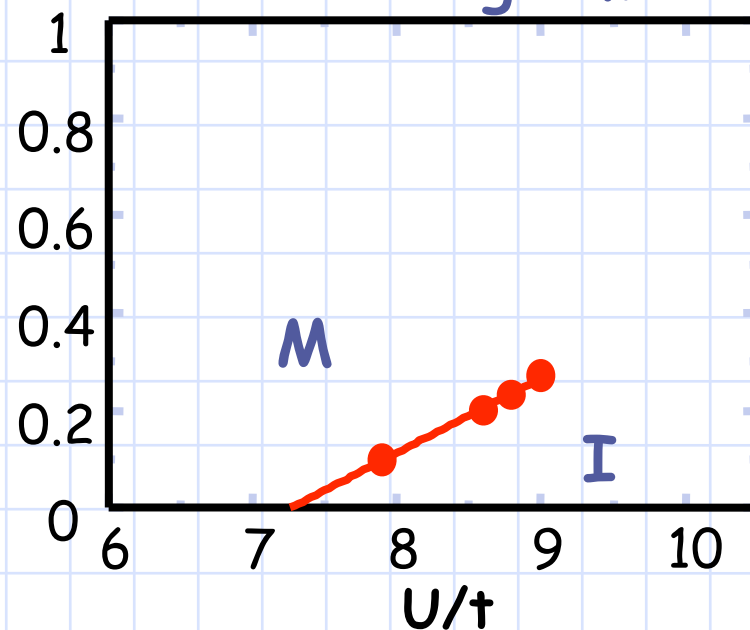
High-temperature behavior

$$t'/t=0.8$$

Double occupancy



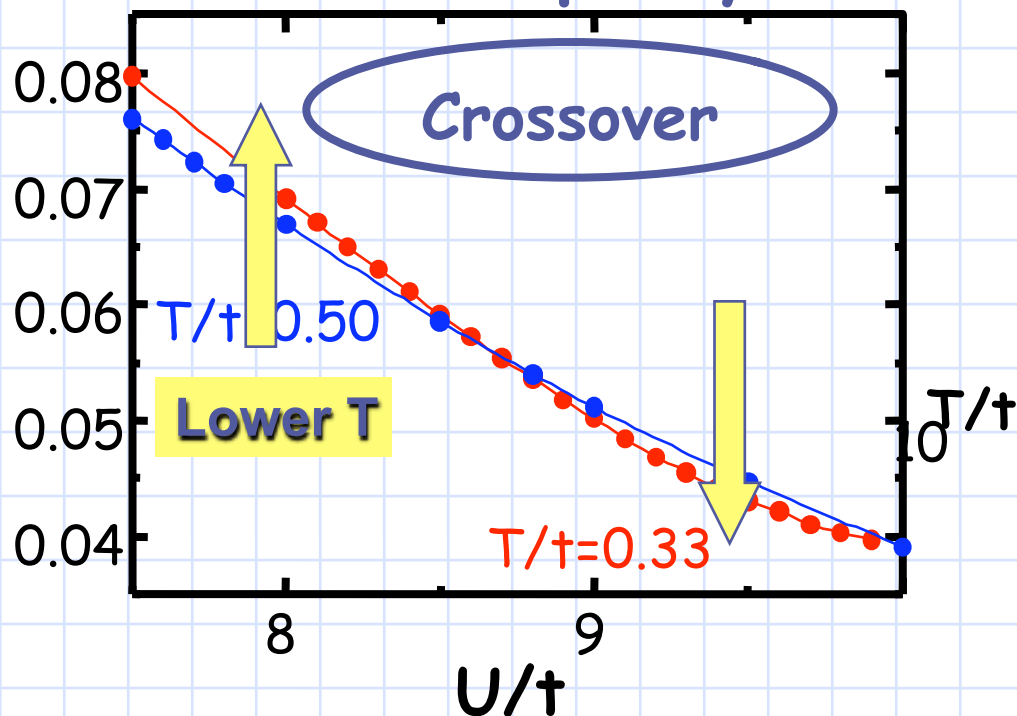
Phase diagram



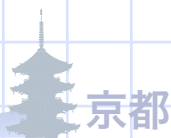
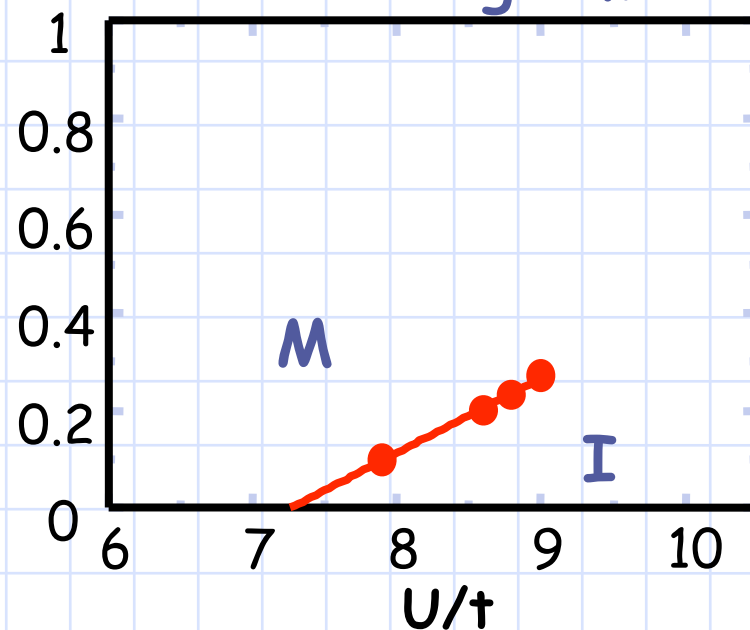
High-temperature behavior

$$t'/t=0.8$$

Double occupancy



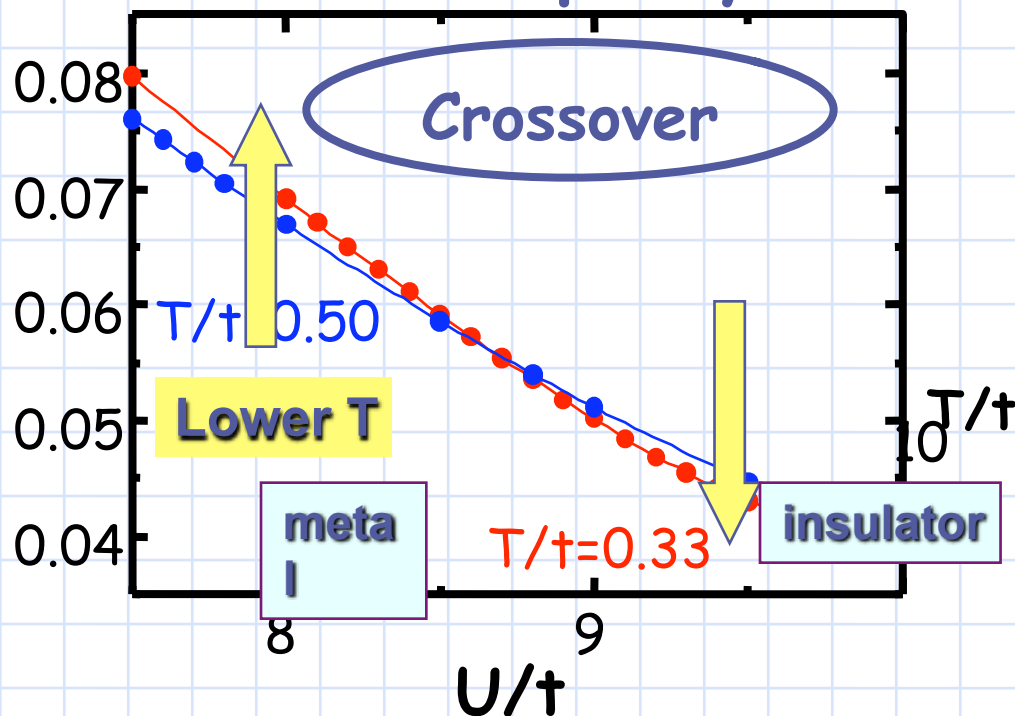
Phase diagram



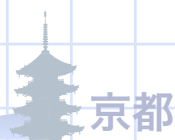
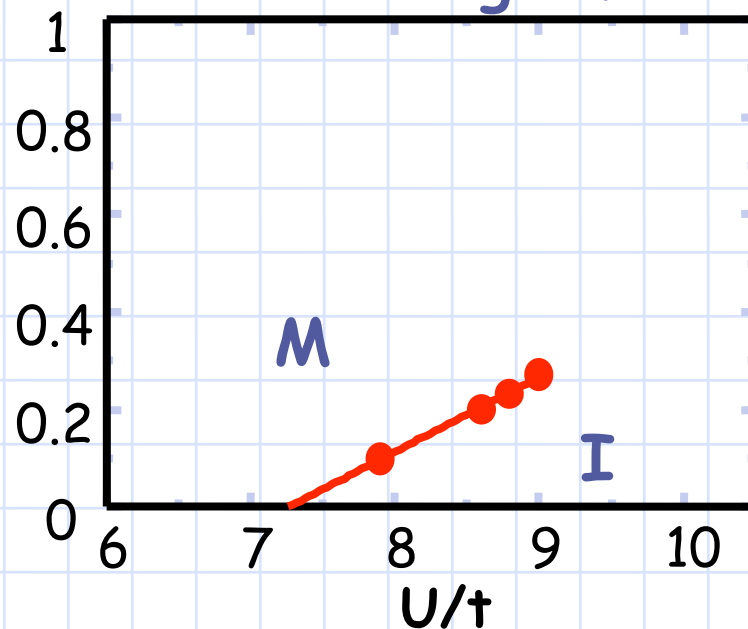
High-temperature behavior

$t'/t=0.8$

Double occupancy



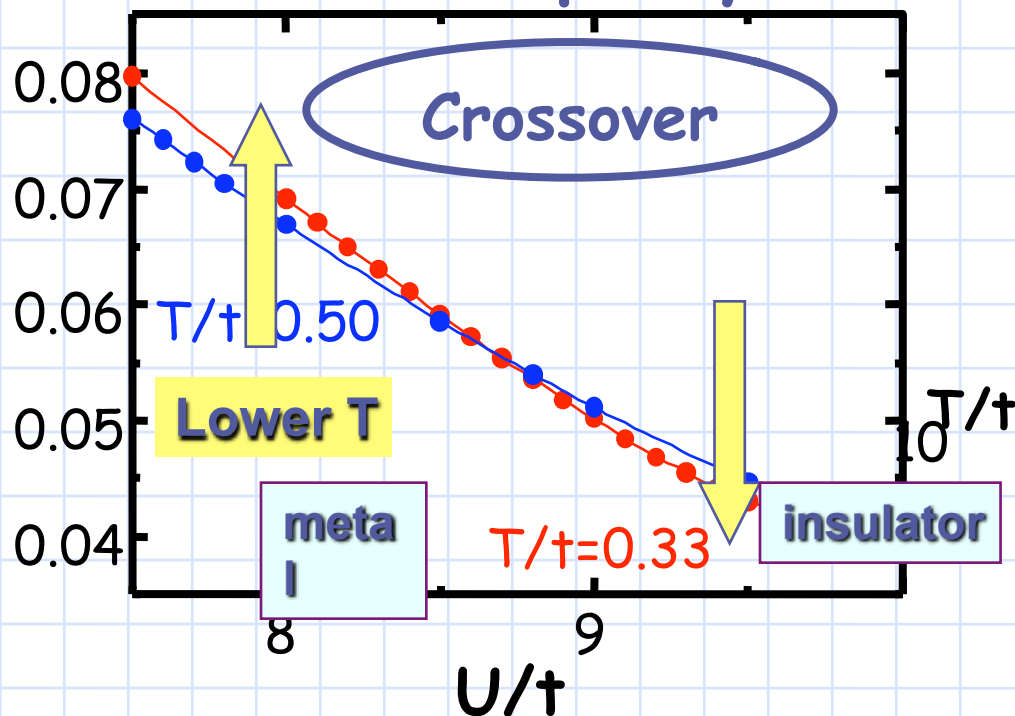
Phase diagram



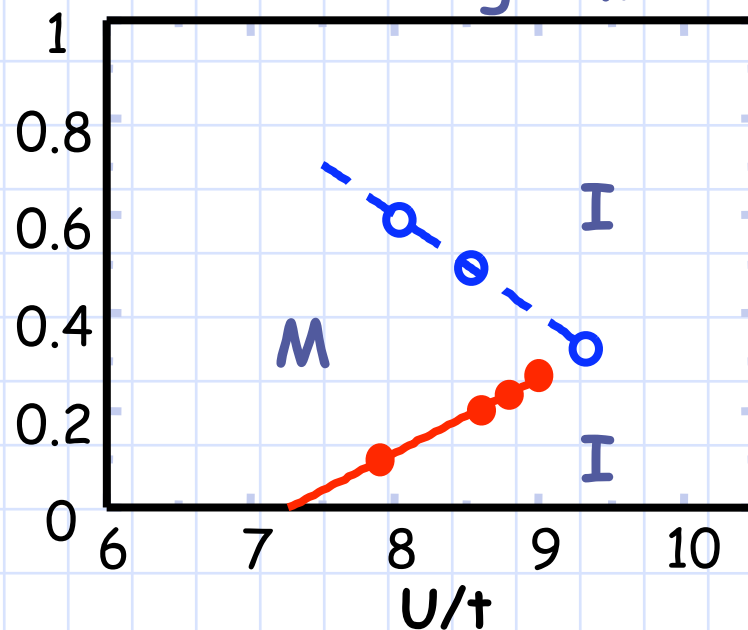
High-temperature behavior

$t'/t=0.8$

Double occupancy



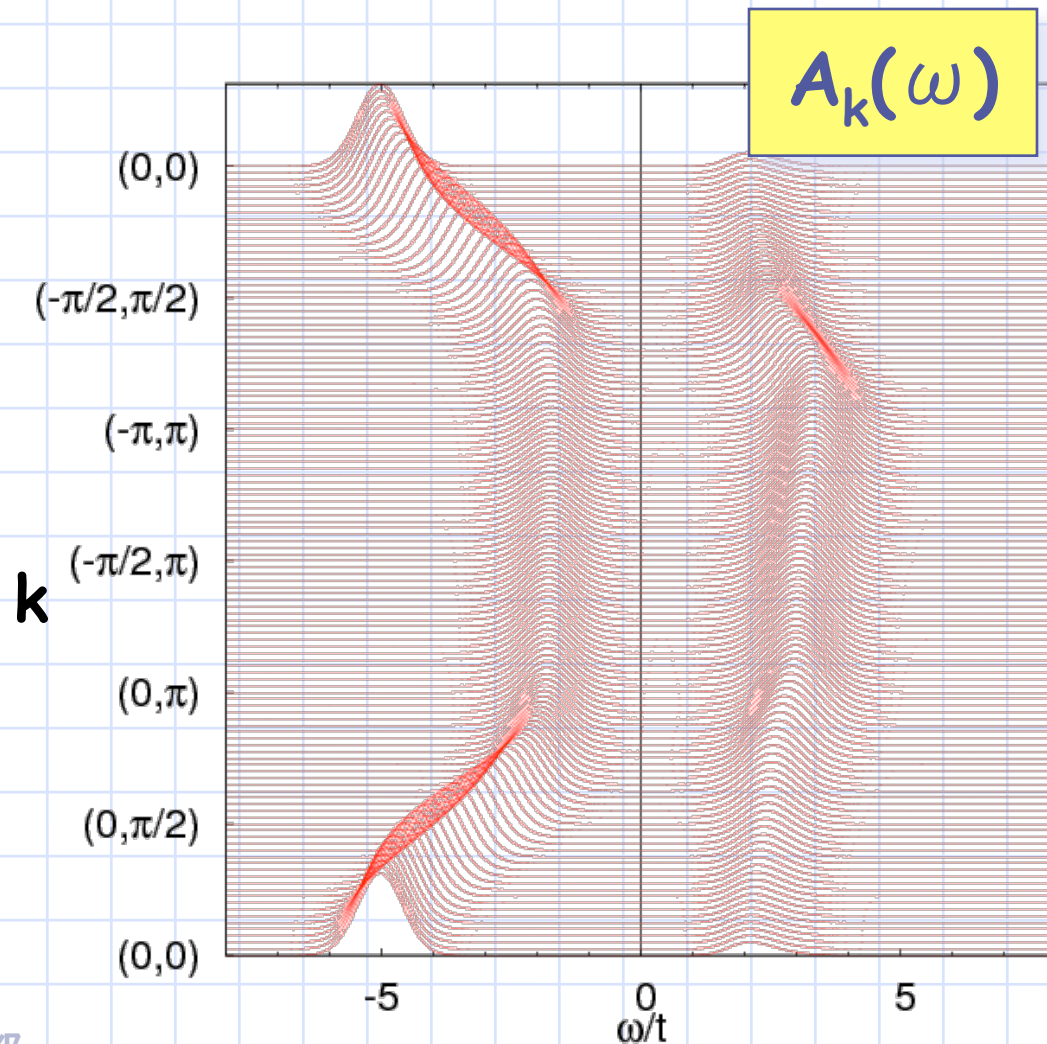
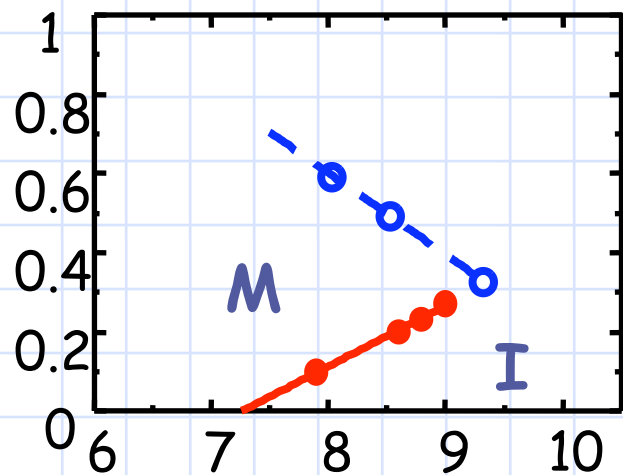
Phase diagram



Reentrant !



k-dependent spectral function

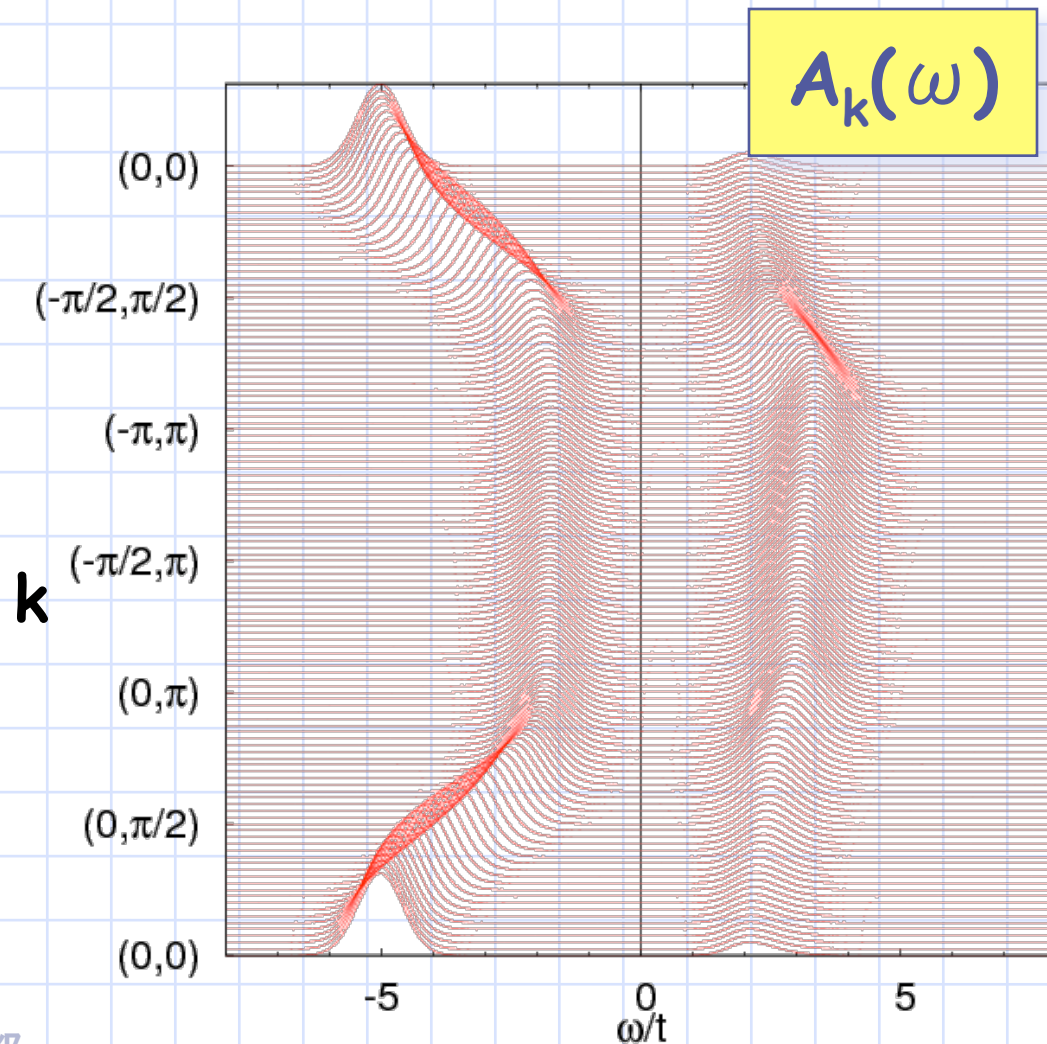
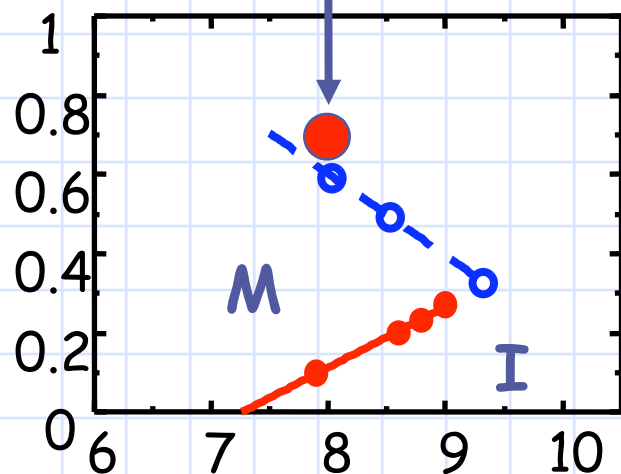


k-dependent spectral function

High T

$U/t=0.8$, $t'/t=0.8$,

$T/t=0.7$

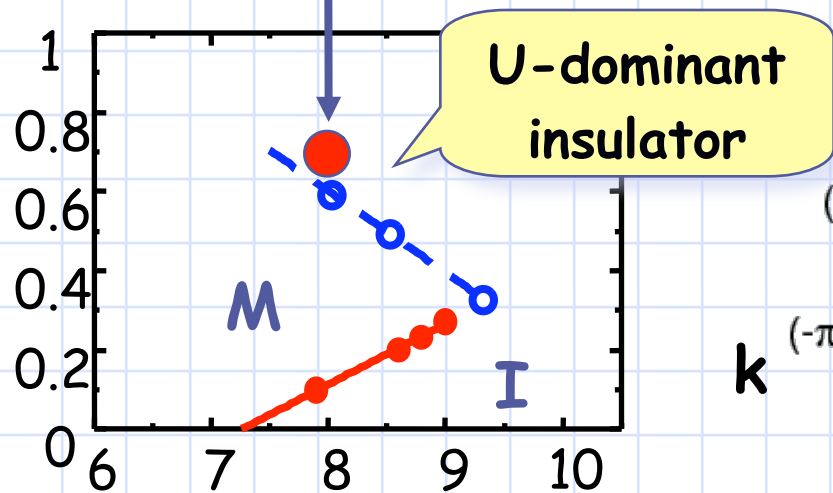


k-dependent spectral function

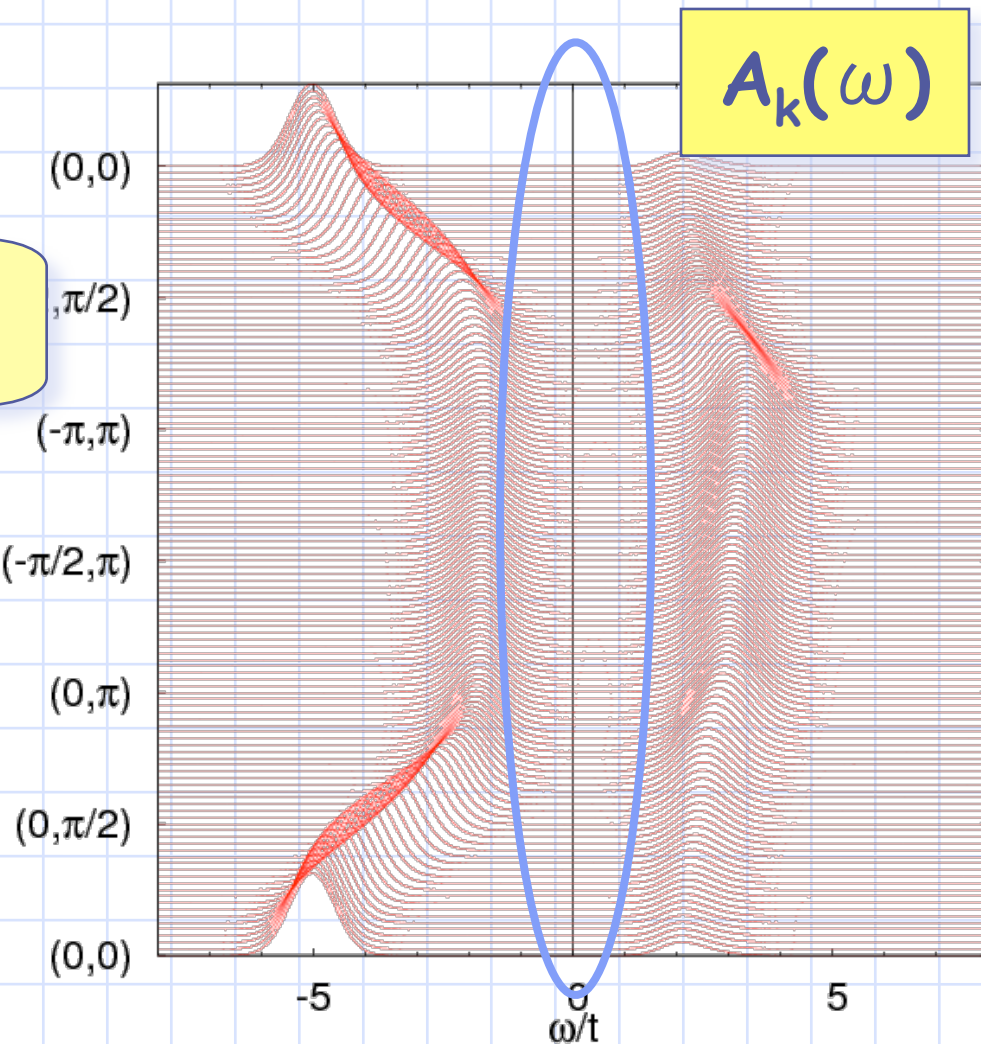
High T

$U/t=0.8, t'/t=0.8,$

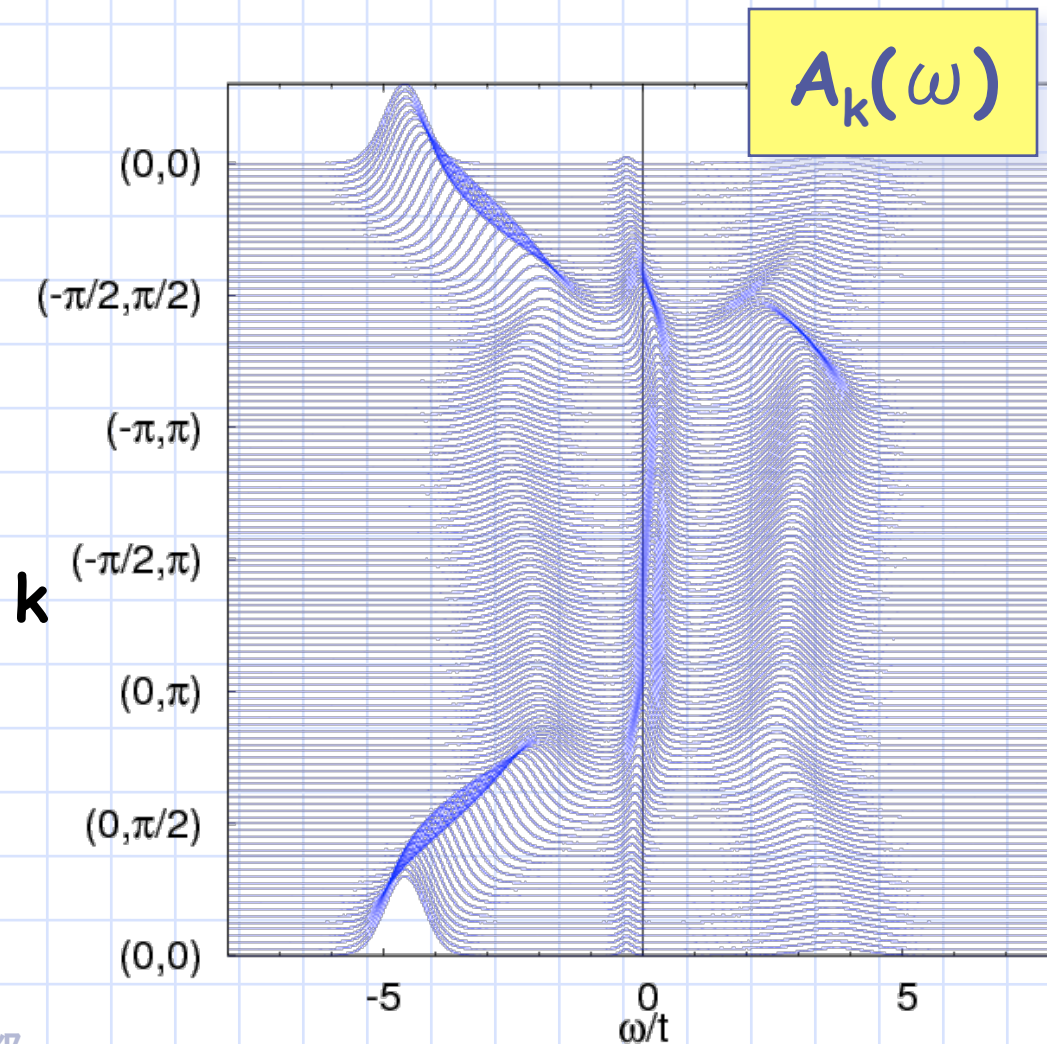
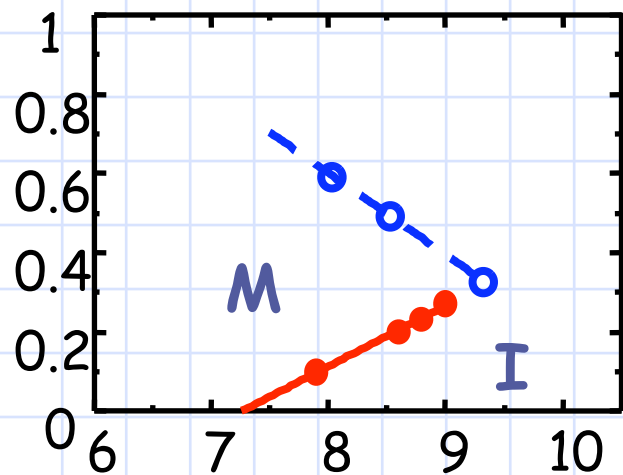
$T/t=0.7$



No quasi-particles



k-dependent spectral function

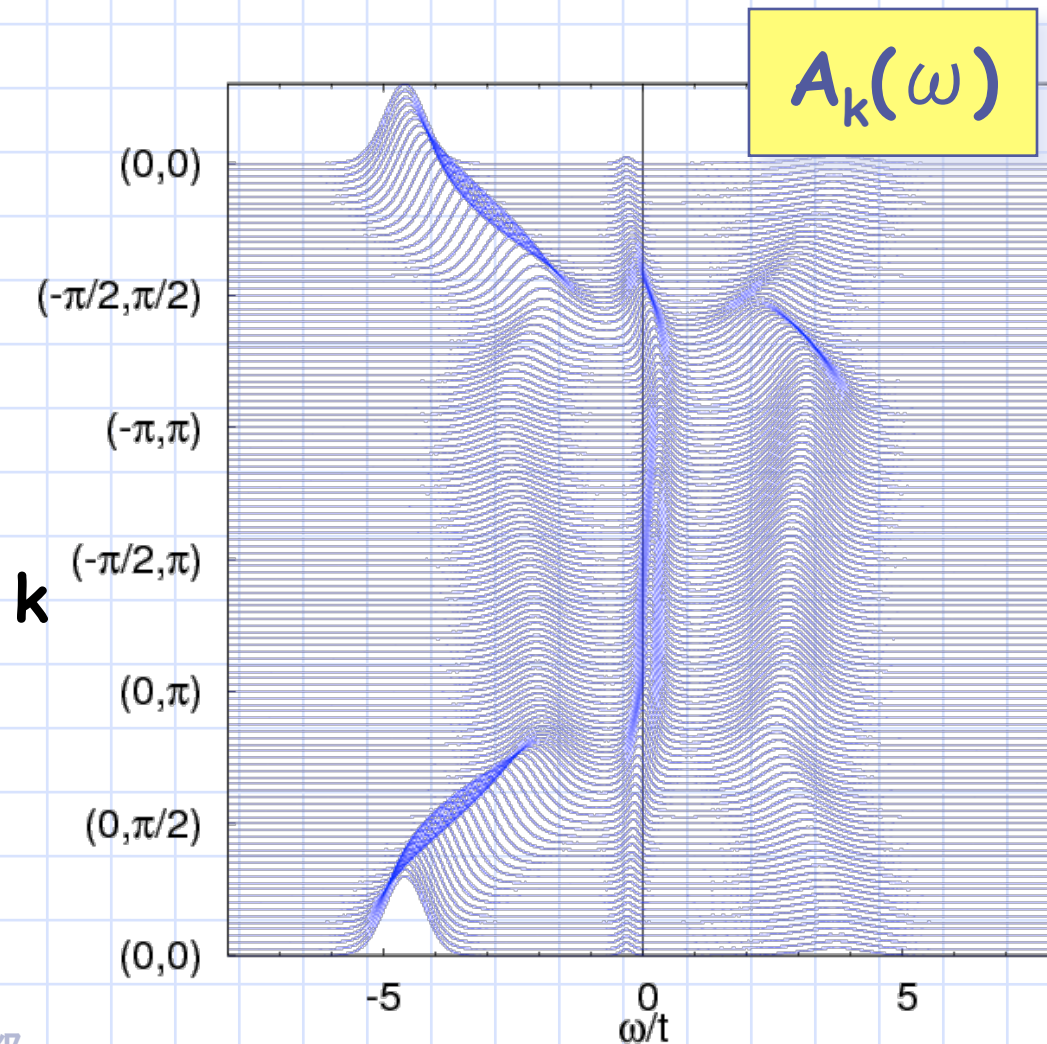
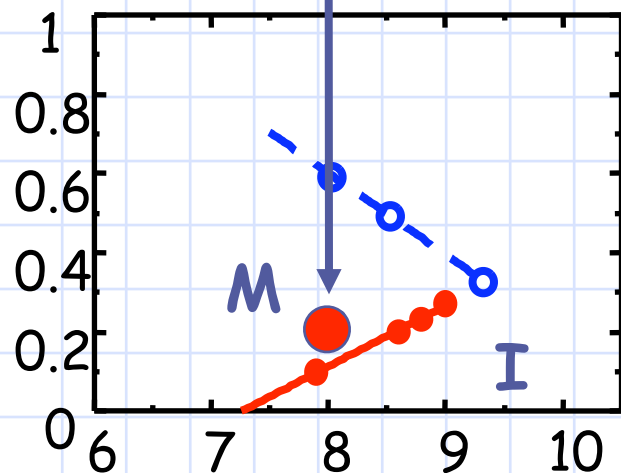


k-dependent spectral function

Intermediate T

$U/t=0.8$, $t'/t=0.8$,

$T/t=0.2$



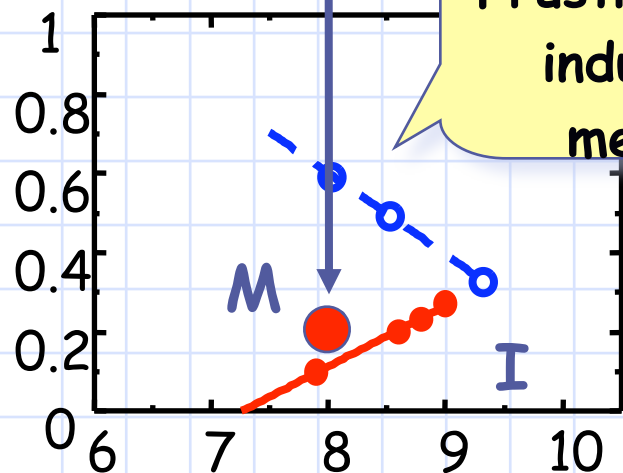
k-dependent spectral function

Intermediate T

$U/t=0.8, t'/t=0.8,$

$T/t=0.2$

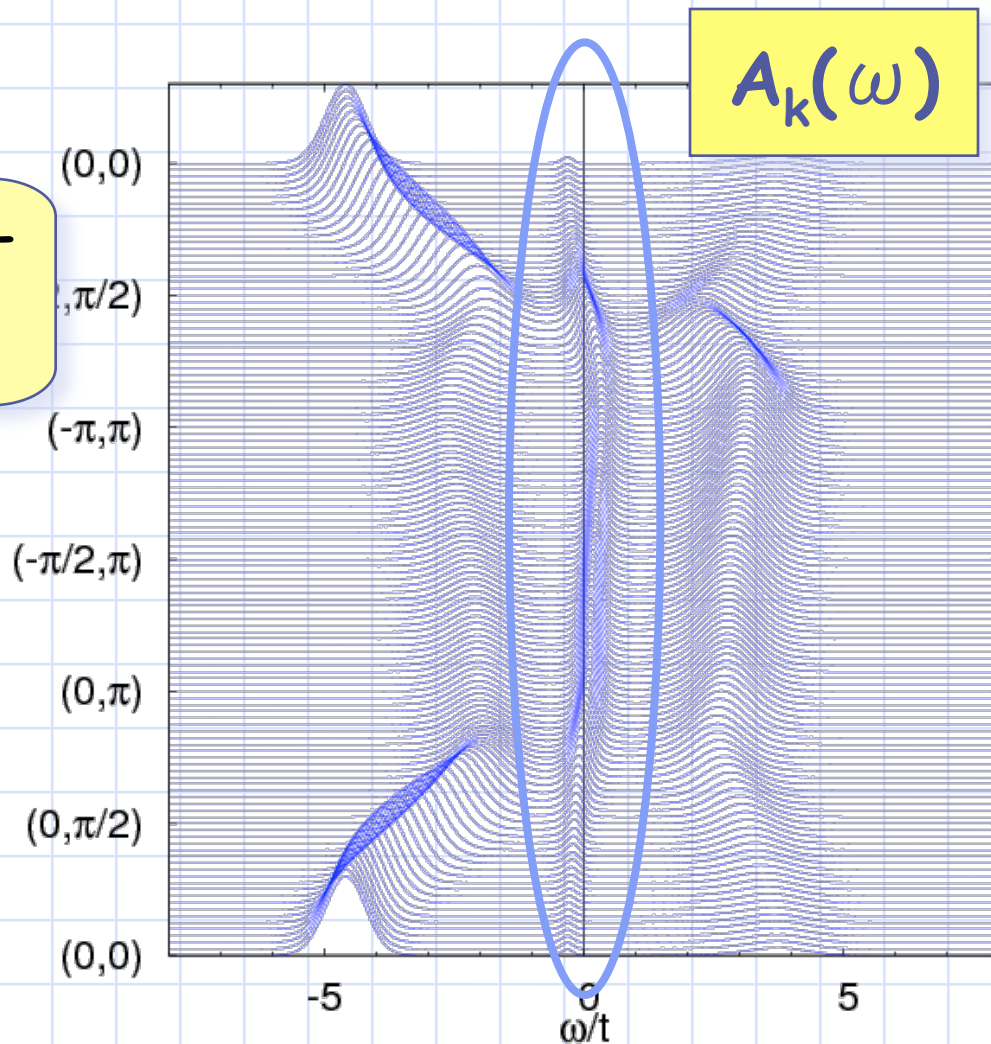
Frustration-induced metal



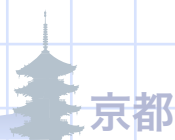
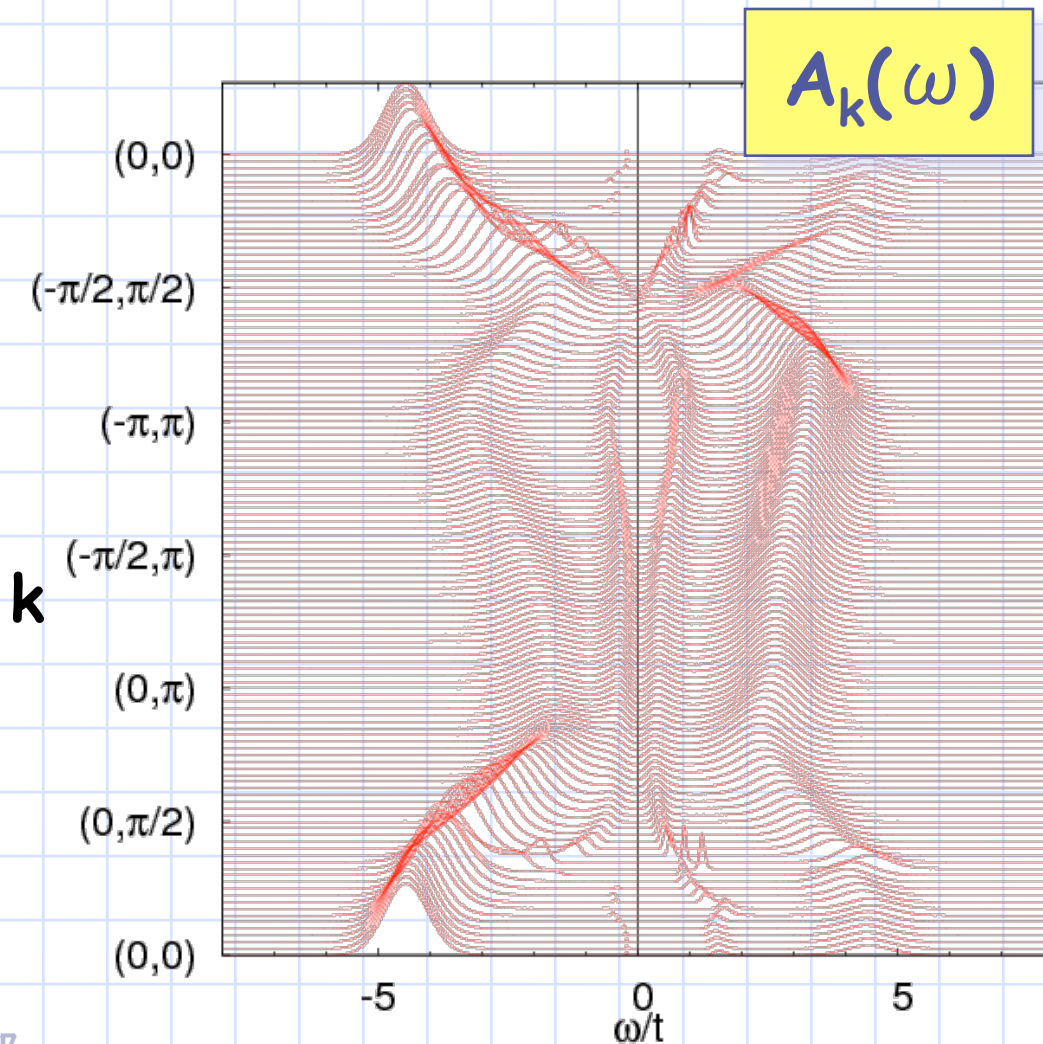
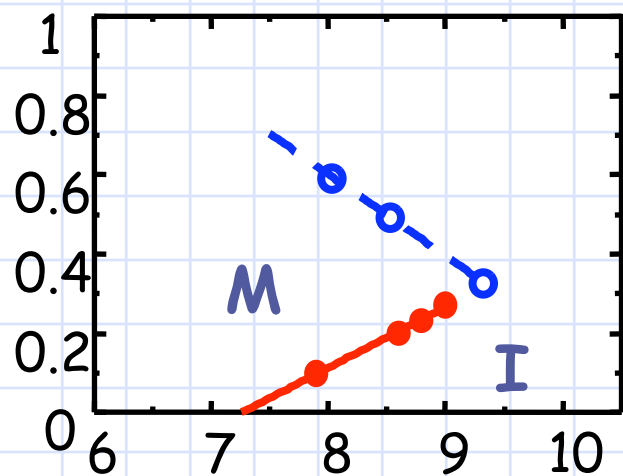
Quasi-particles

frustration

k



k-dependent spectral function

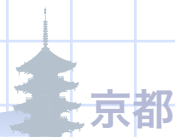
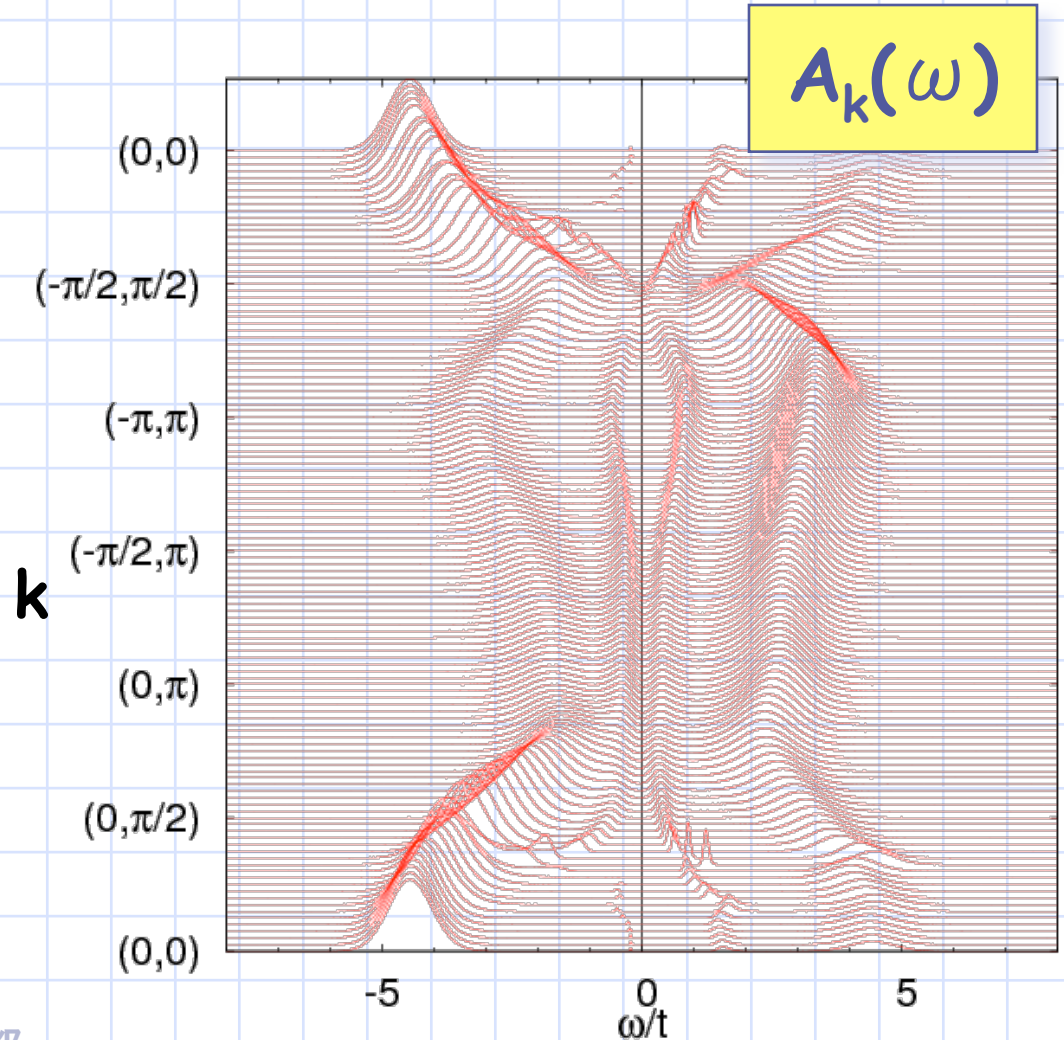
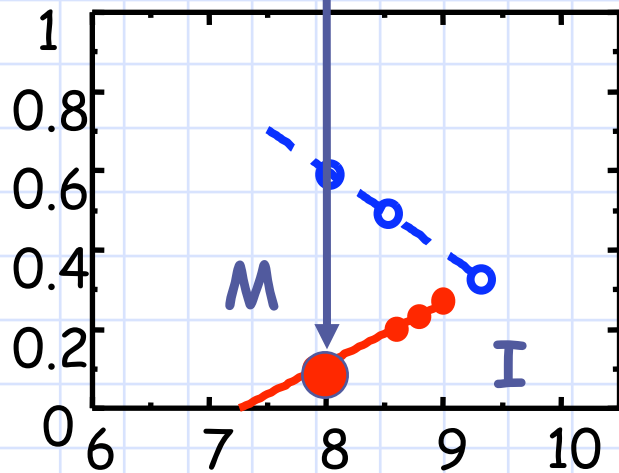


k-dependent spectral function

Low T

$U/t=0.8, t'/t=0.8,$

$T/t=0.1$

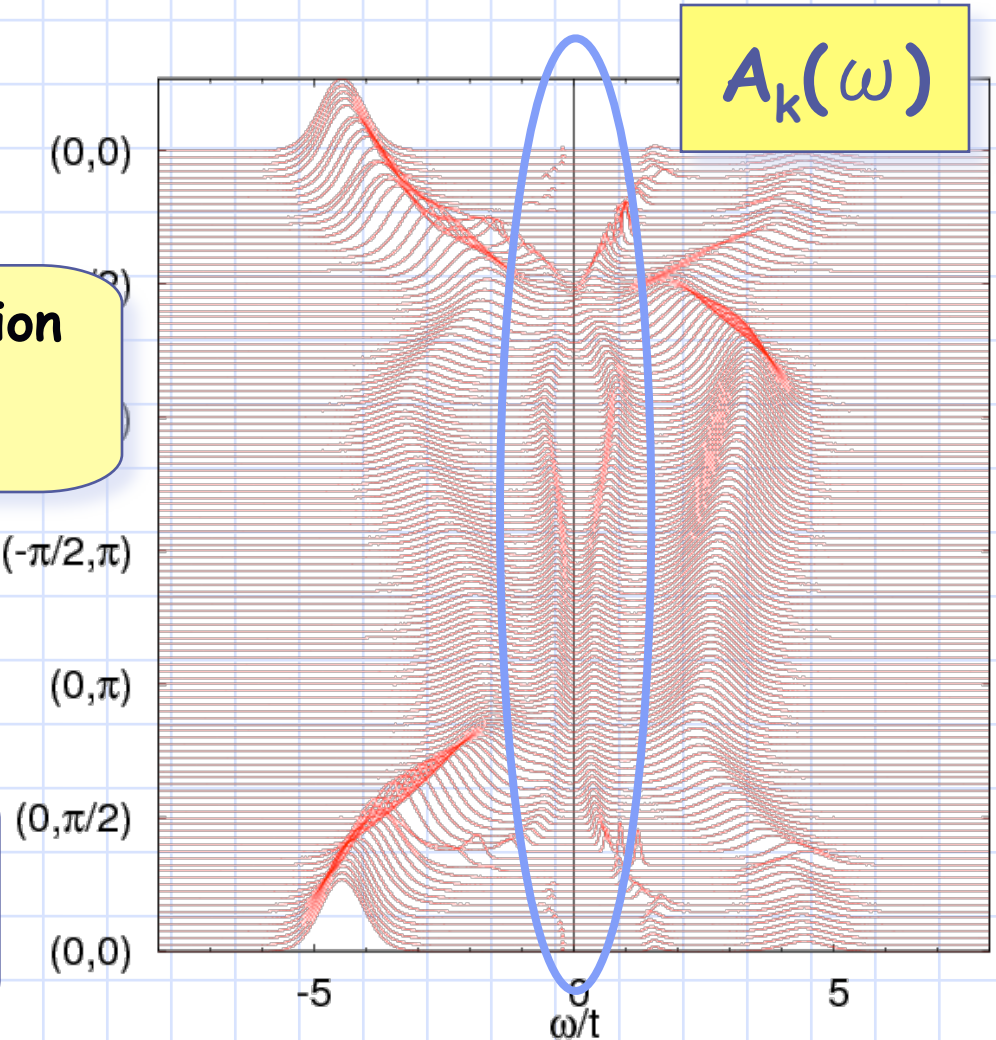
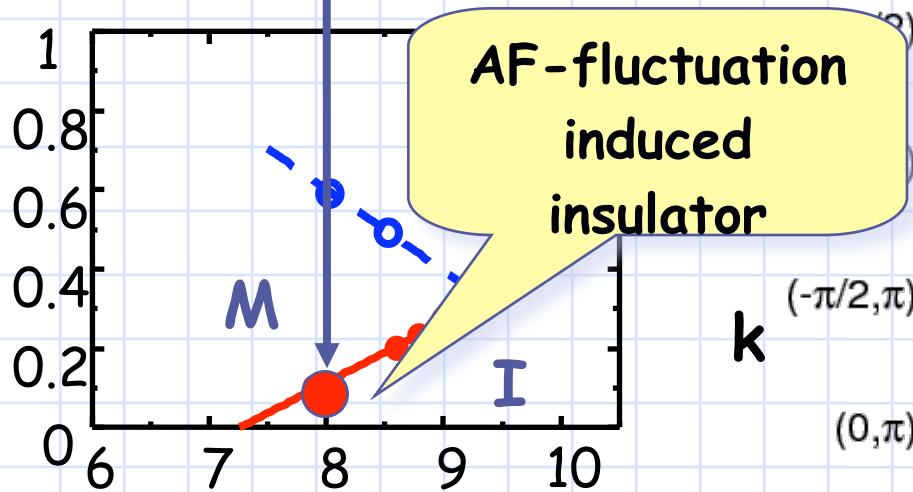


k-dependent spectral function

Low T

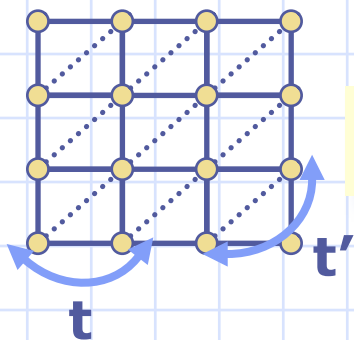
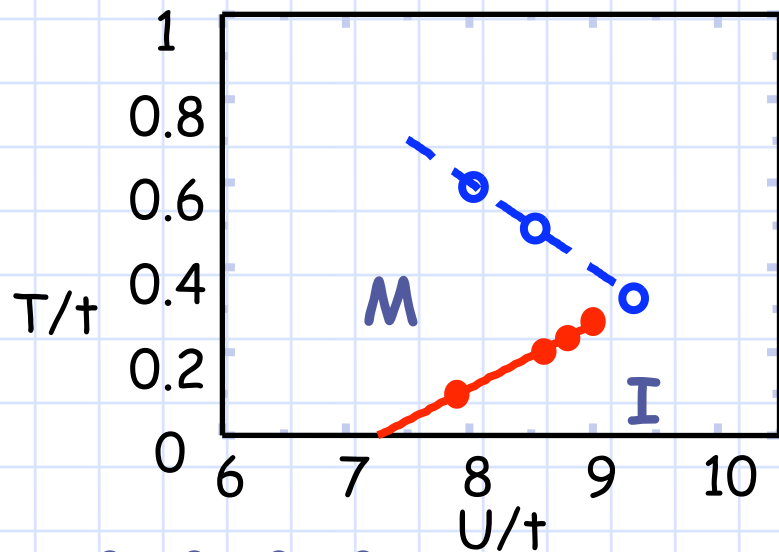
$U/t=0.8, t'/t=0.8,$

$T/t=0.1$



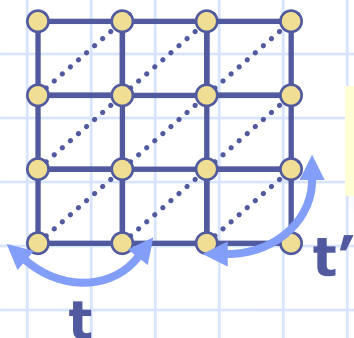
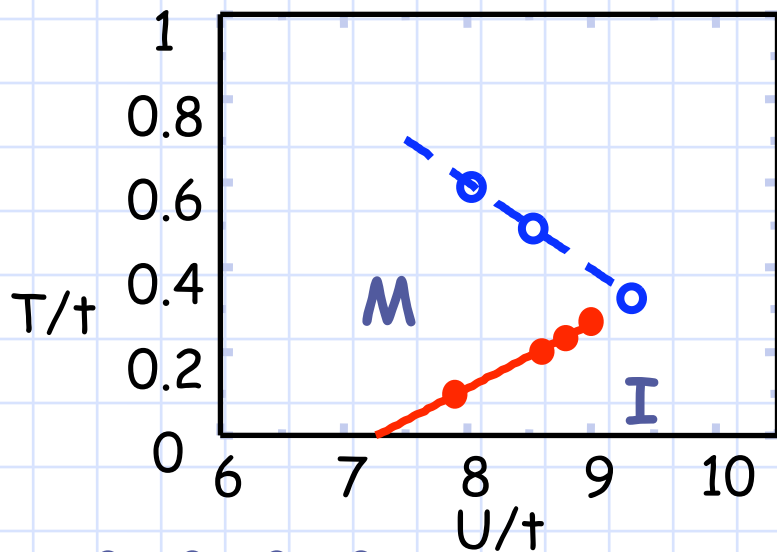
- splitting of QP peak
- different from high T

Phase diagram



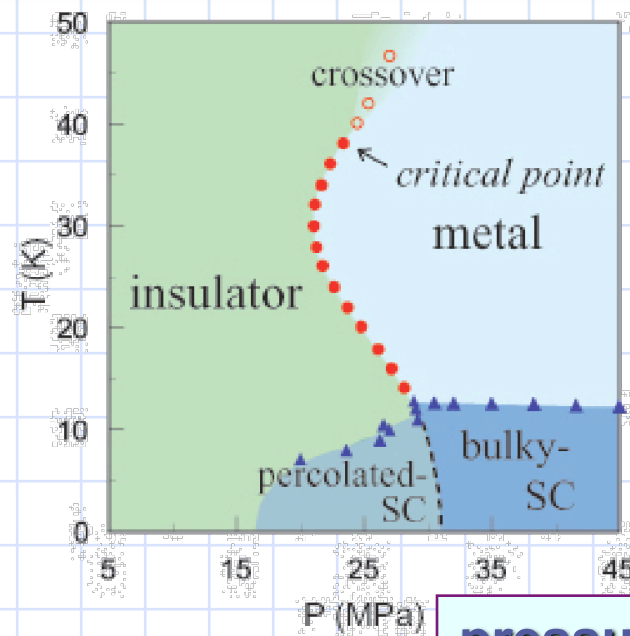
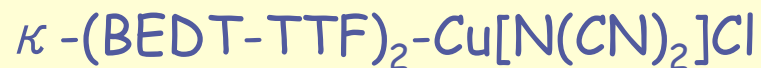
$t'/t = 0.8$

Phase diagram



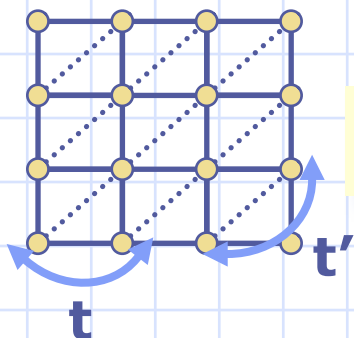
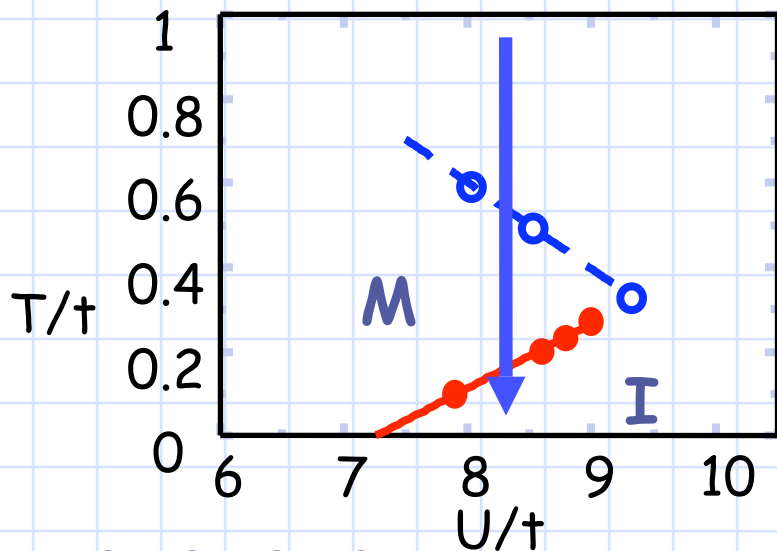
$t'/t = 0.8$

Kanoda group



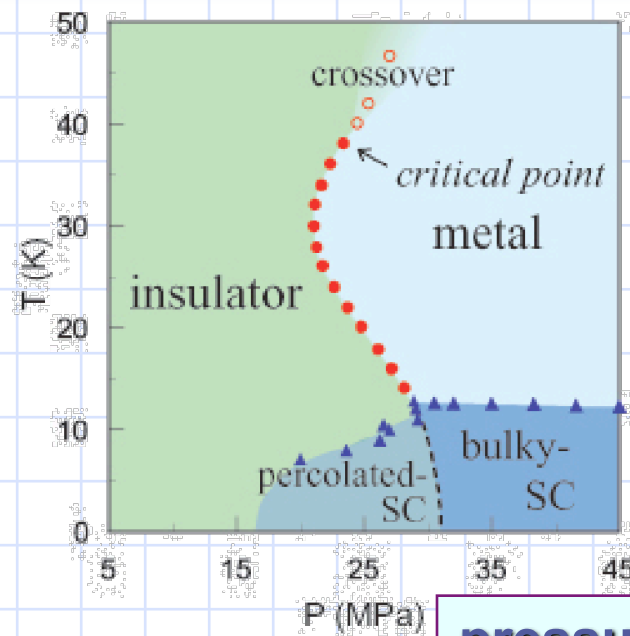
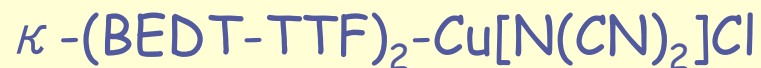
pressure

Phase diagram



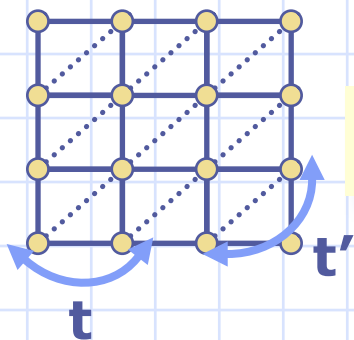
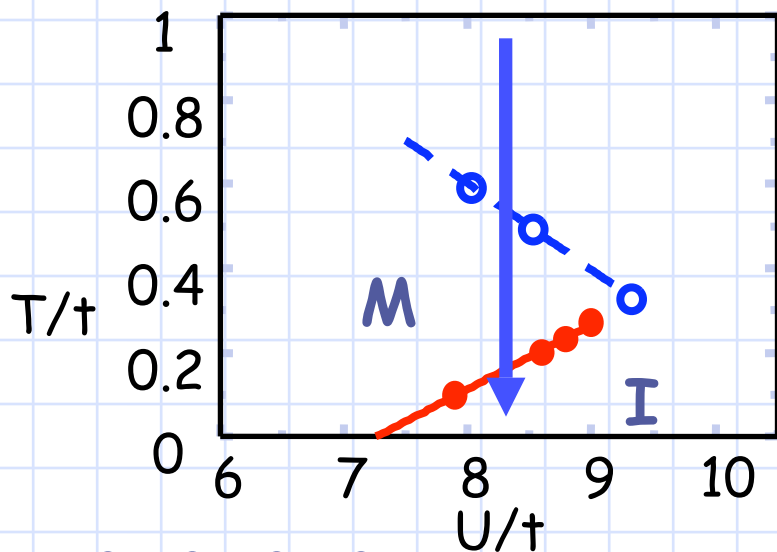
$$t'/t = 0.8$$

Kanoda group



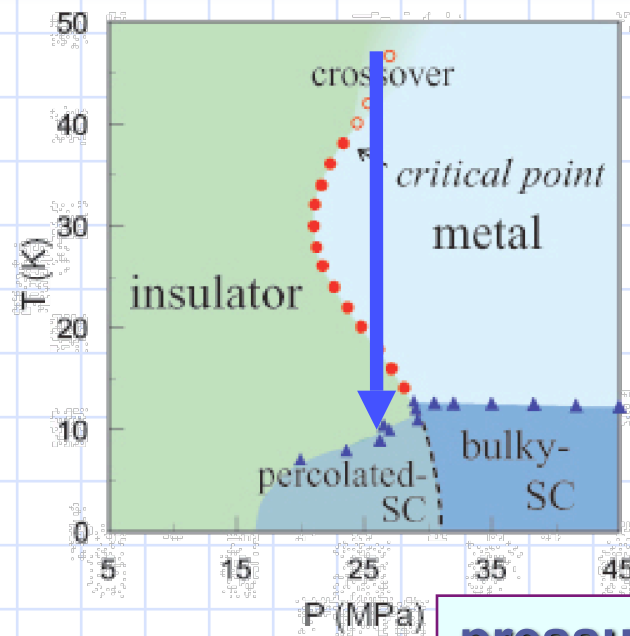
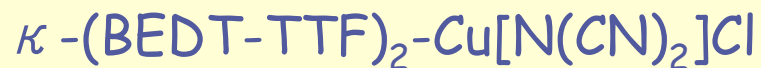
pressure

Phase diagram



$t'/t = 0.8$

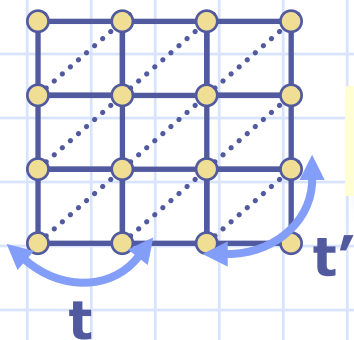
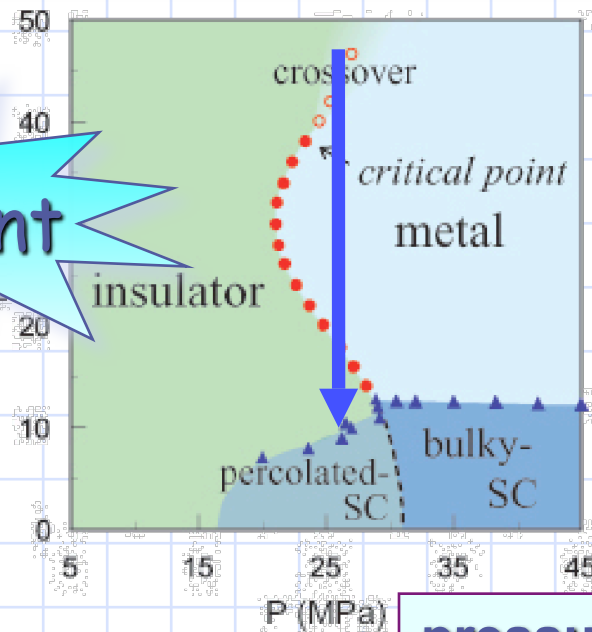
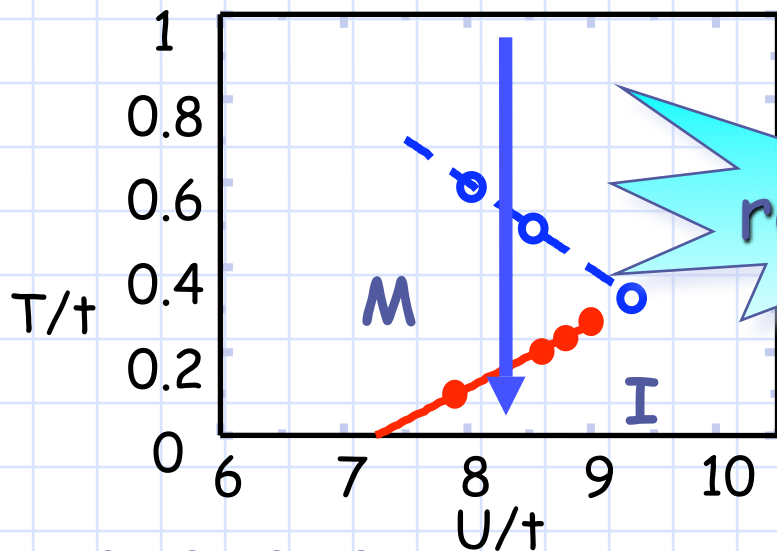
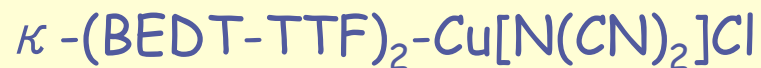
Kanoda group



pressure

Phase diagram

Kanoda group

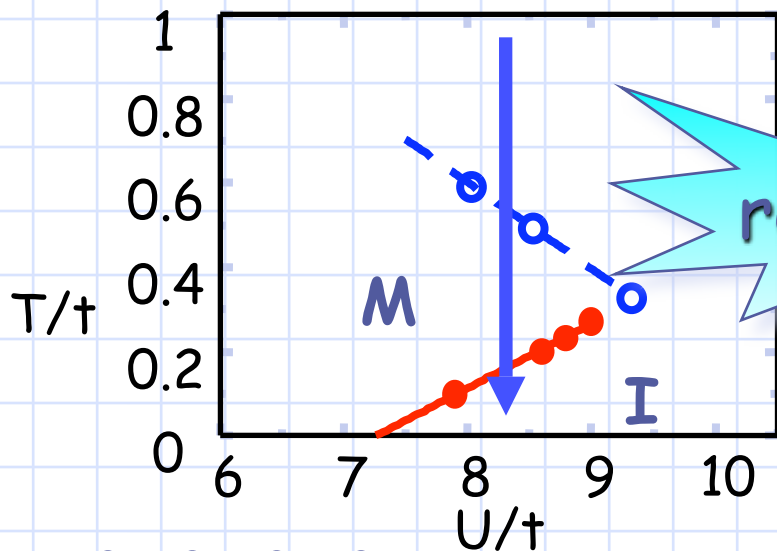
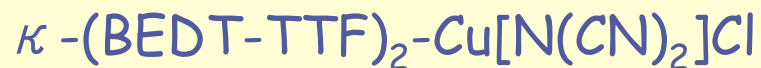


$t'/t = 0.8$

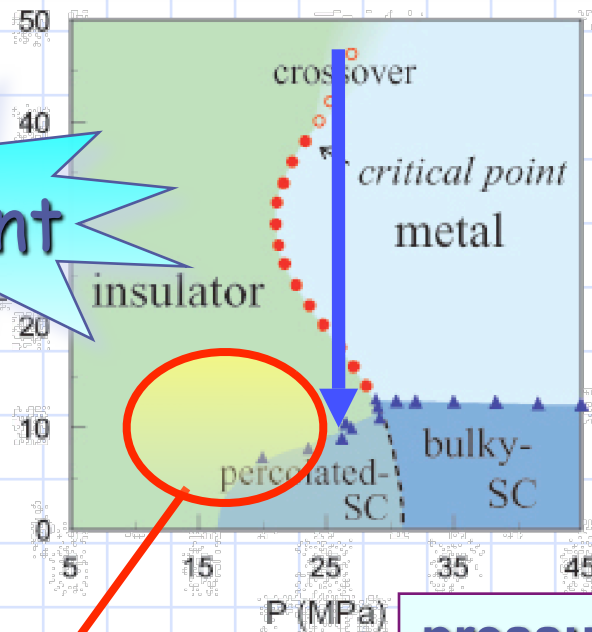
pressure

Phase diagram

Kanoda group

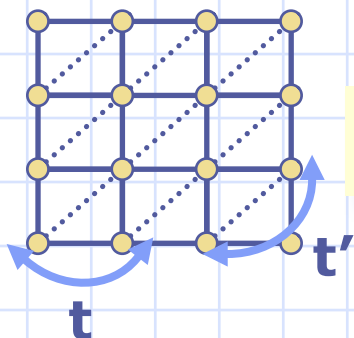


reentrant



pressure

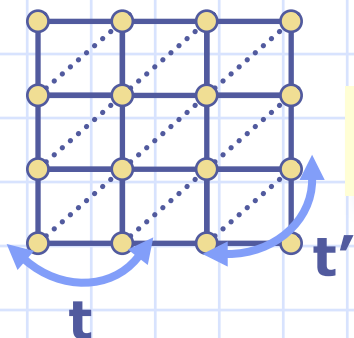
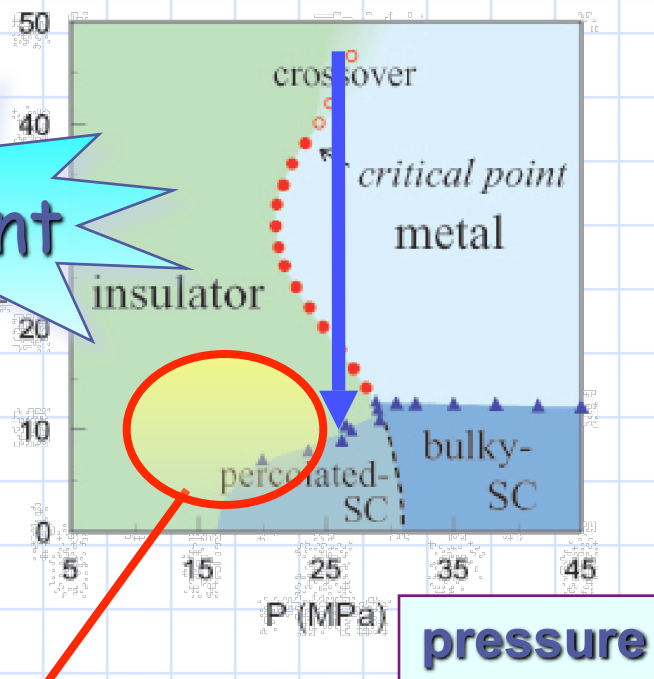
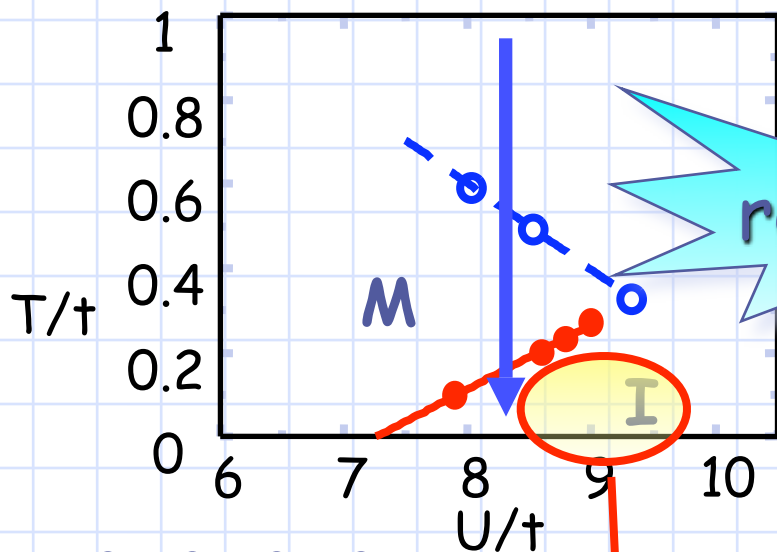
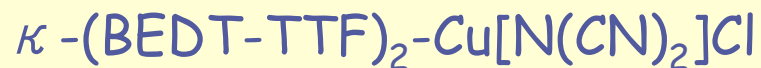
Magnetic order



$t'/t = 0.8$

Phase diagram

Kanoda group



$t'/t = 0.8$

?

Magnetic order



YKIS 07
Kyoto
November 14,
2007

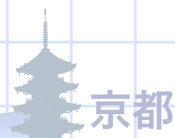
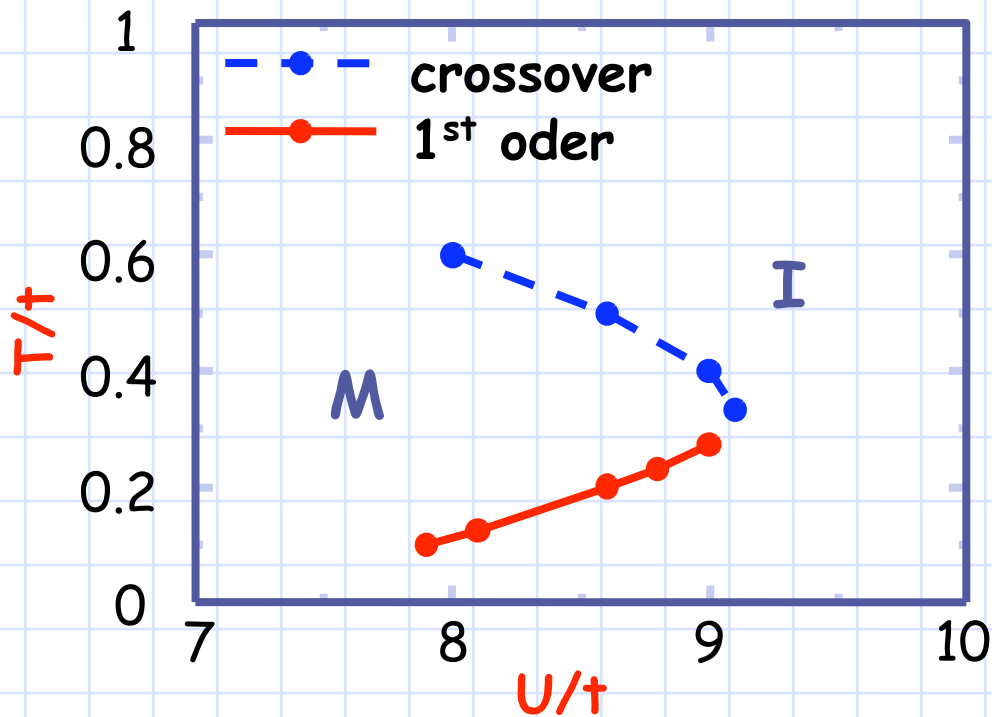
Magnetic instability



Magnetic instability

Cellular-DMFT \longrightarrow • ordering at finite T

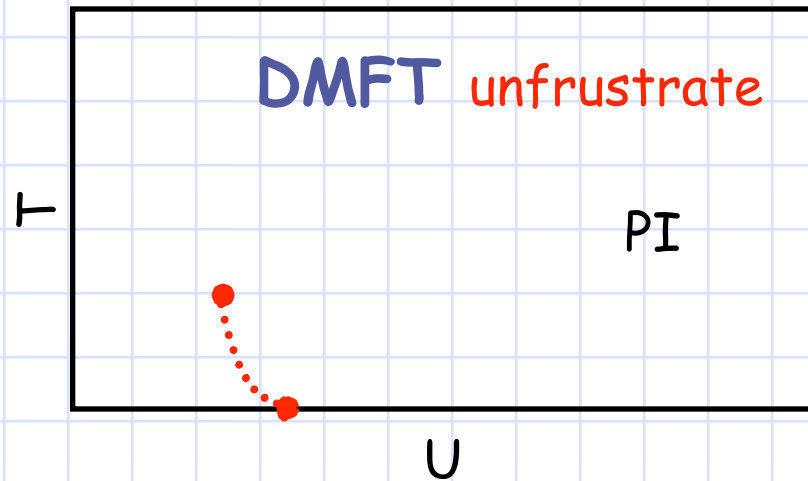
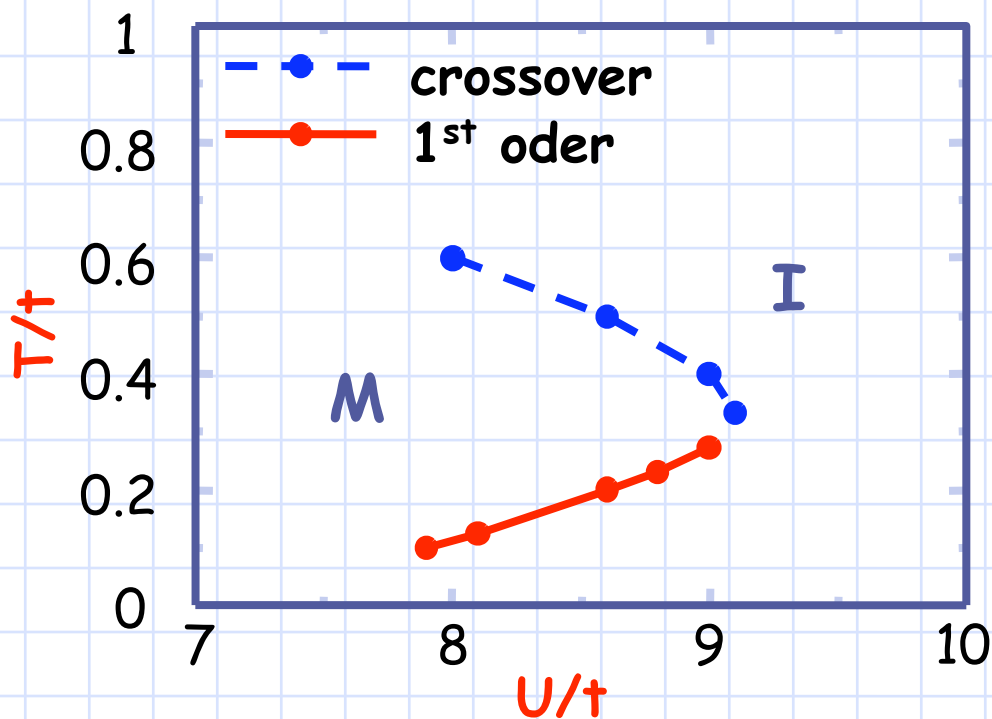
$t'/t=0.8$



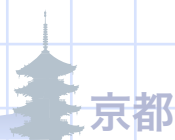
Magnetic instability

Cellular-DMFT \longrightarrow ordering at finite T

$t'/t=0.8$



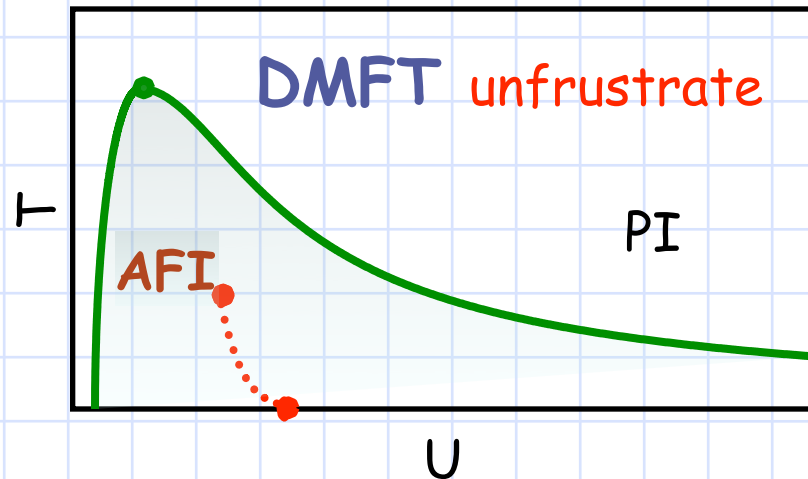
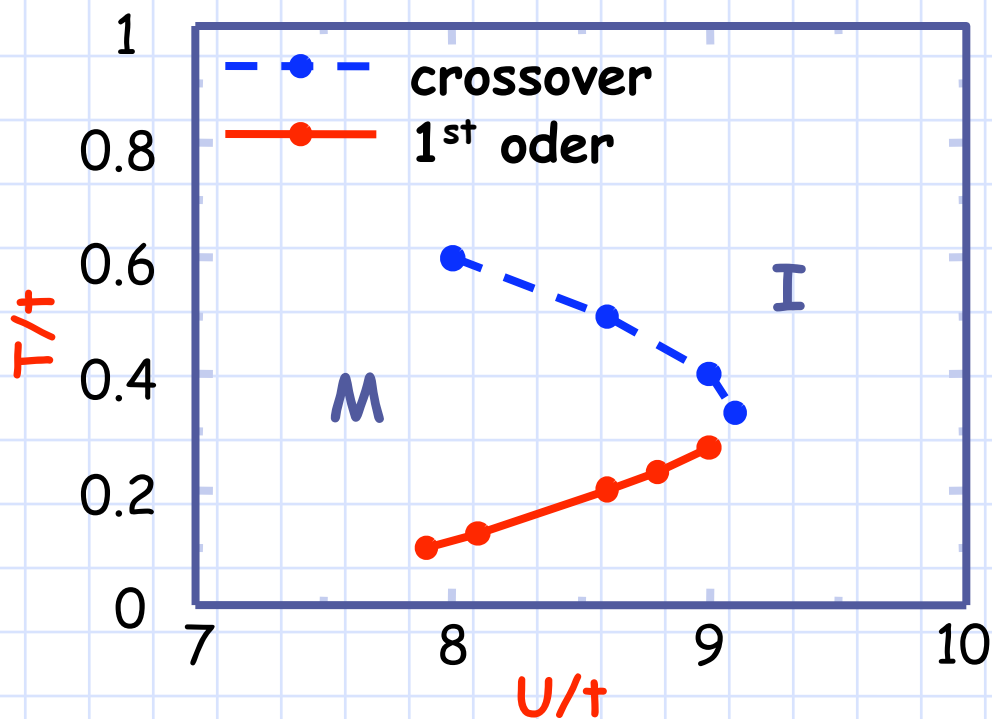
Georges et al. RMP 68, 13 (1996)
 Zitzler et al. PRL 93 016406 (2004)



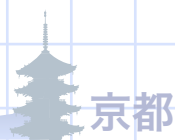
Magnetic instability

Cellular-DMFT \longrightarrow ordering at finite T

$t'/t=0.8$



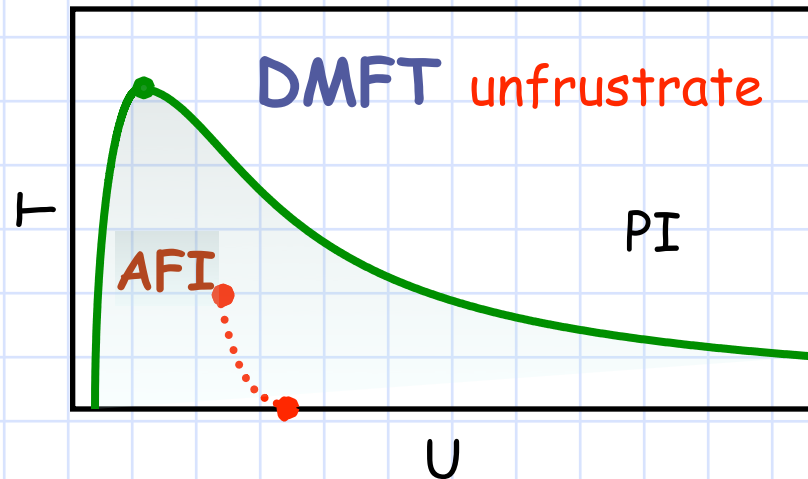
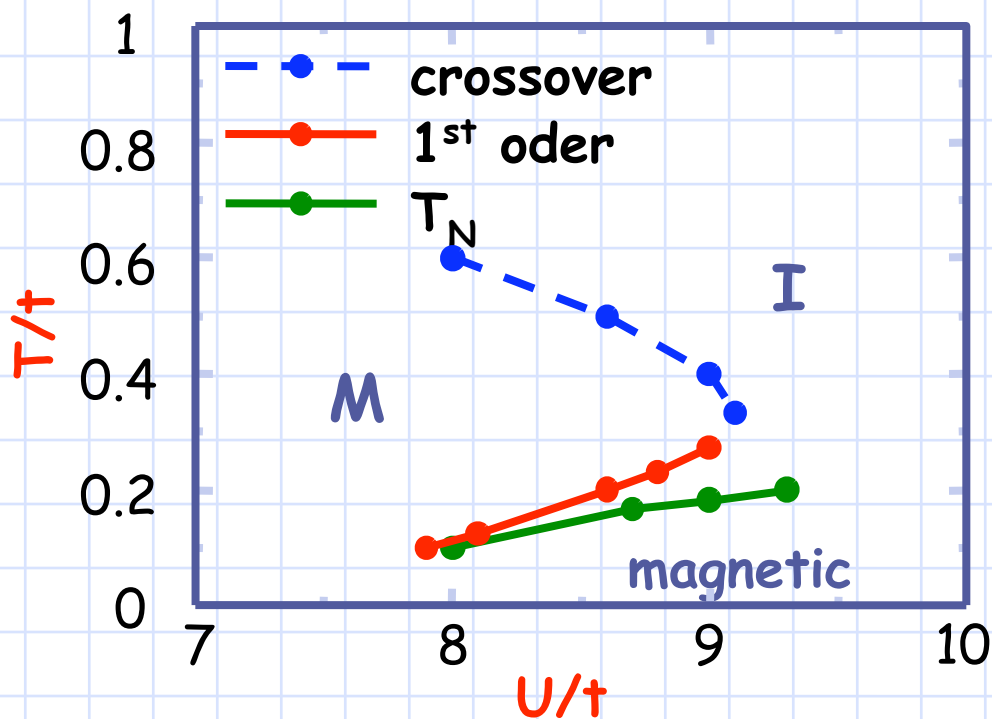
Georges et al. RMP 68, 13 (1996)
 Zitzler et al. PRL 93 016406 (2004)
 Mott transition disappears



Magnetic instability

Cellular-DMFT \longrightarrow ordering at finite T

$t'/t=0.8$



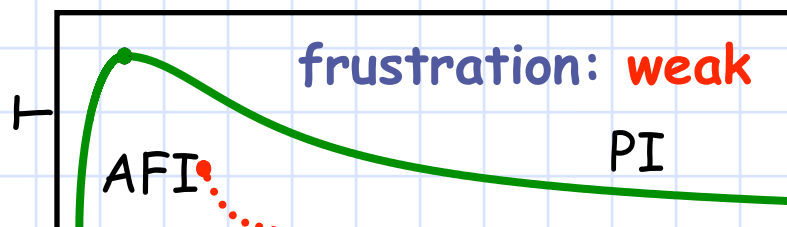
Georges et al. RMP 68, 13 (1996)
 Zitzler et al. PRL 93 016406 (2004)
 Mott transition disappears

Frustration: Mott transition survives !

Frustration ∞ dimensions

DMFT: frustrated Bethe lattice

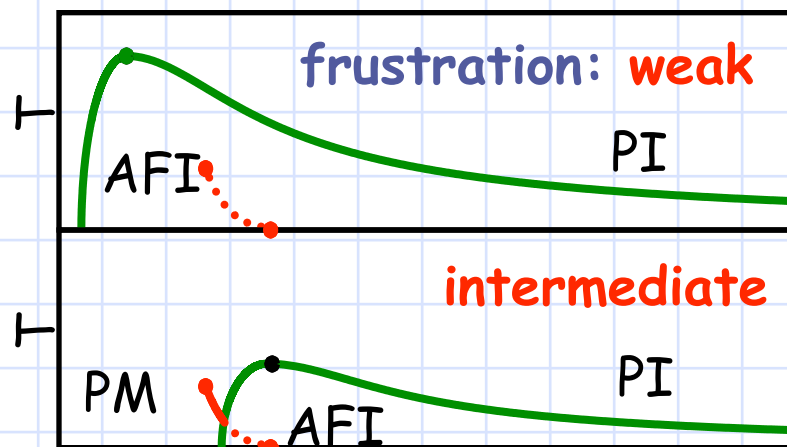
Zitzler et al. Phys. Rev. Lett. 93 016406



Frustration ∞ dimensions

DMFT: frustrated Bethe lattice

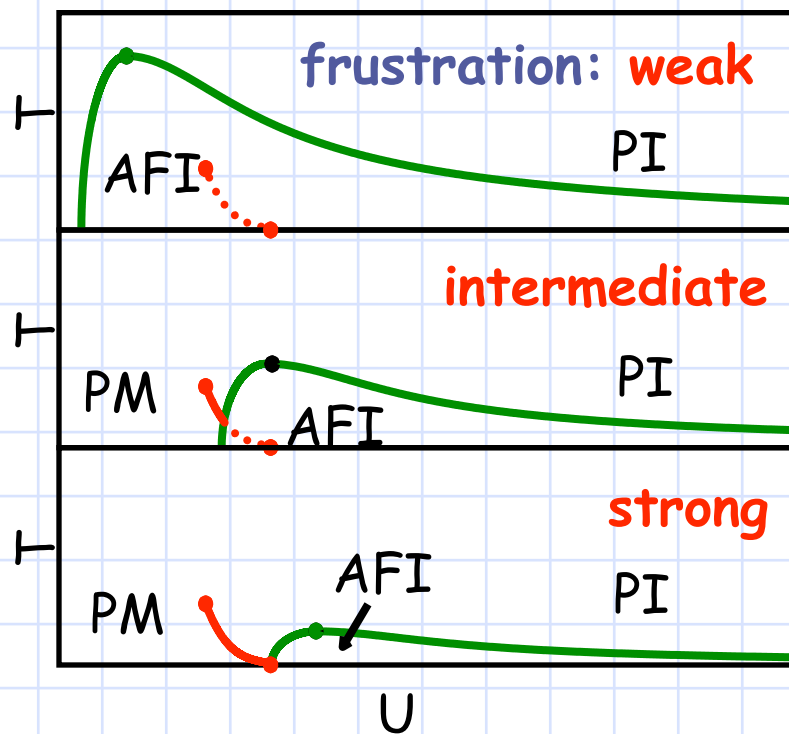
Zitzler et al. Phys. Rev. Lett. 93 016406



Frustration ∞ dimensions

DMFT: frustrated Bethe lattice

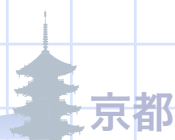
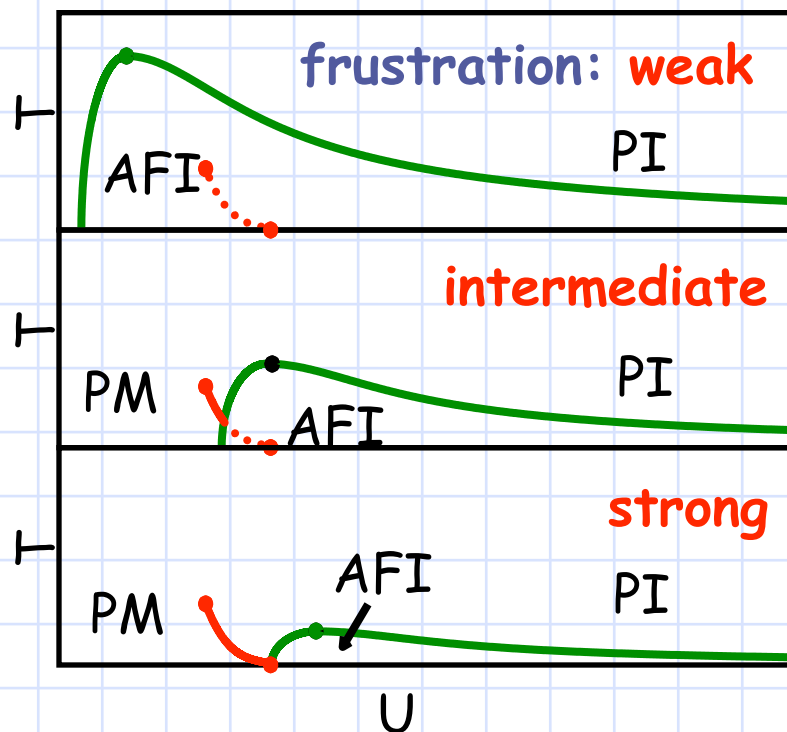
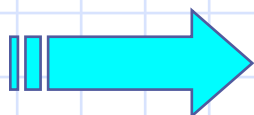
Zitzler et al. Phys. Rev. Lett. 93 016406



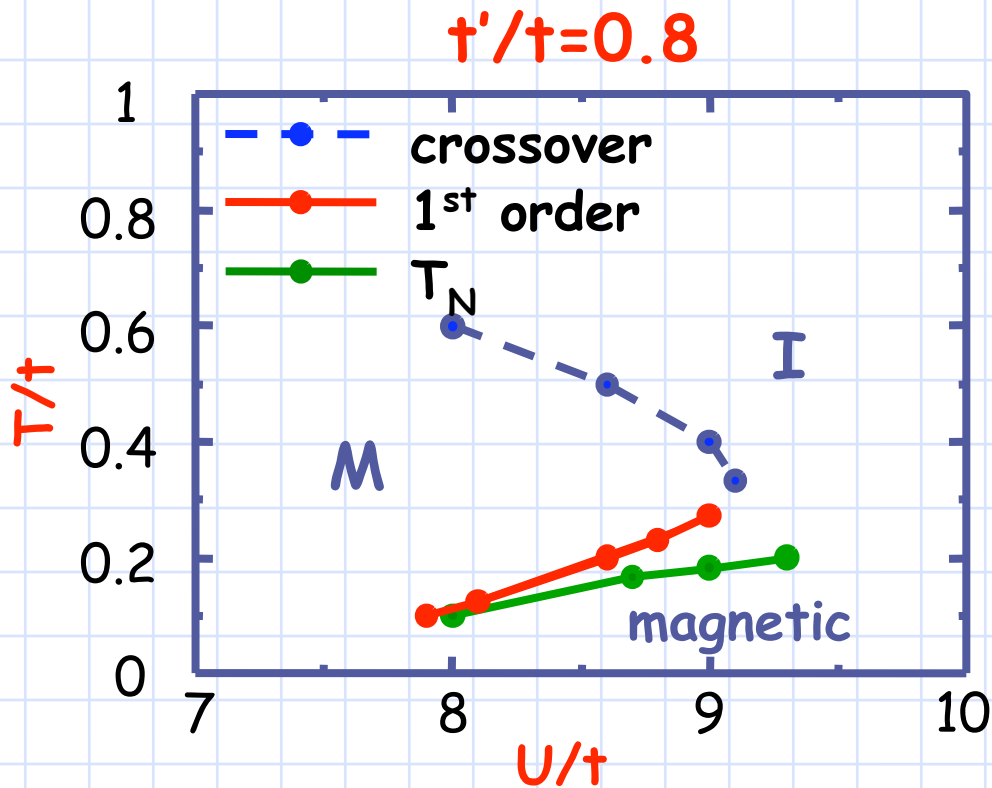
Frustration ∞ dimensions

DMFT: frustrated Bethe lattice

Zitzler et al. Phys. Rev. Lett. 93 016406



Comparison: frustrated systems in infinite dimensions



Cellular-DMFT

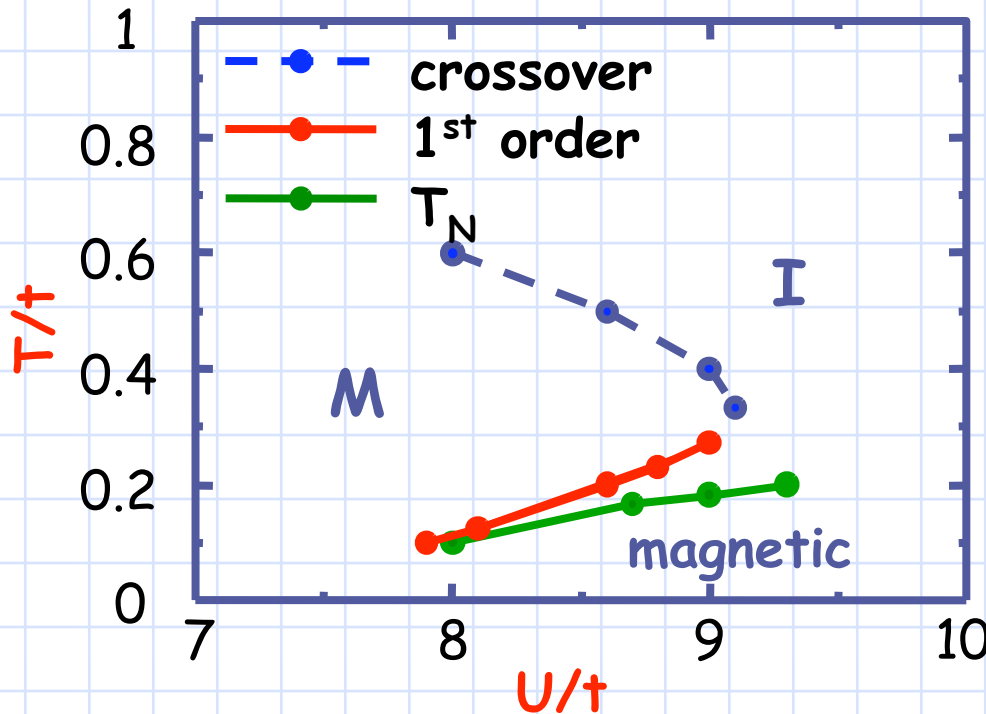


Comparison: frustrated systems in infinite dimensions

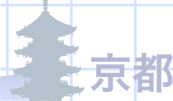
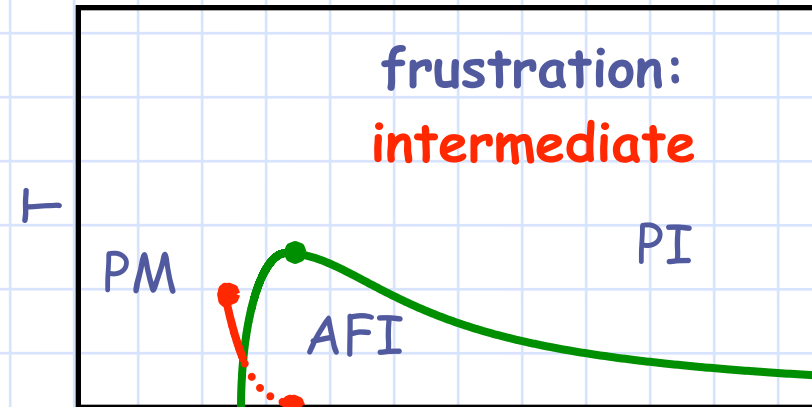
DMFT: frustrated Bethe lattice

Zitzler et al. PRL 93 016406 (2004)

$t'/t=0.8$



Cellular-DMFT

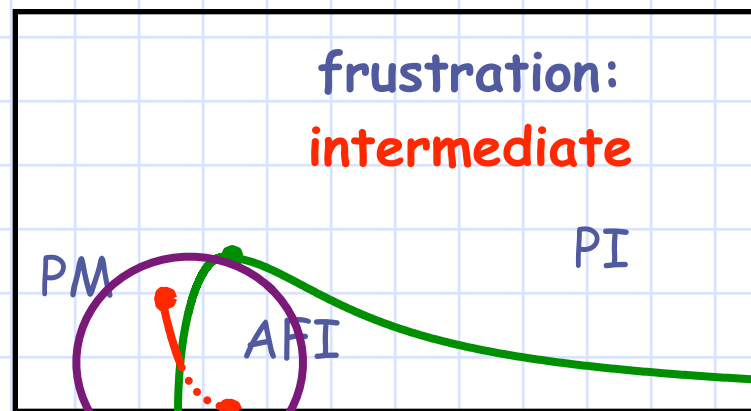
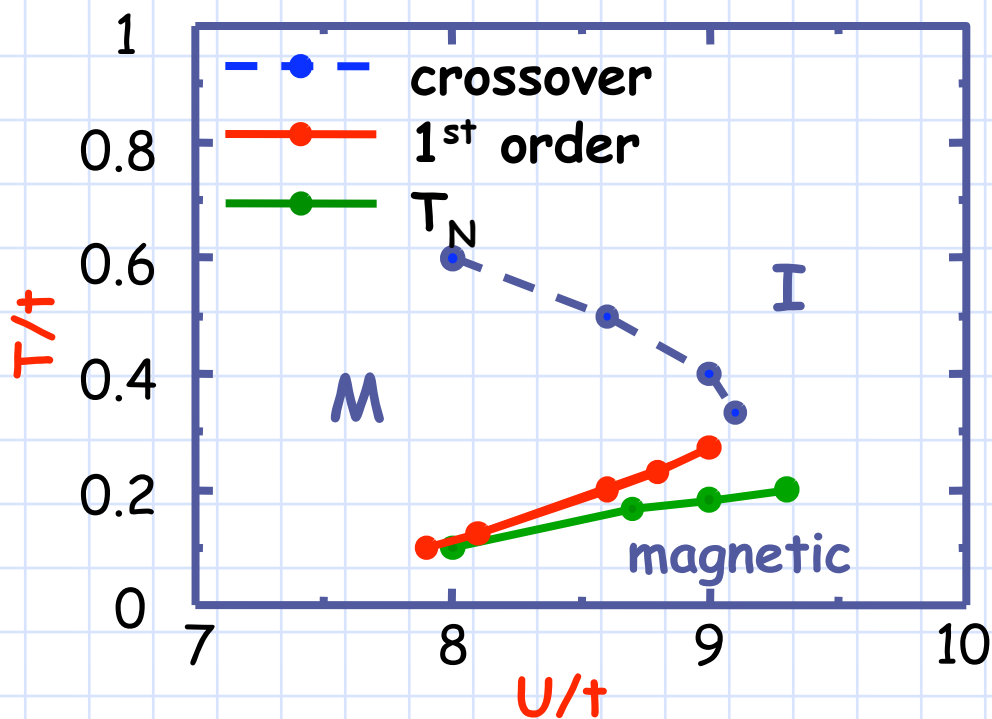


Comparison: frustrated systems in infinite dimensions

DMFT: frustrated Bethe lattice

Zitzler et al. PRL 93 016406 (2004)

$t'/t=0.8$

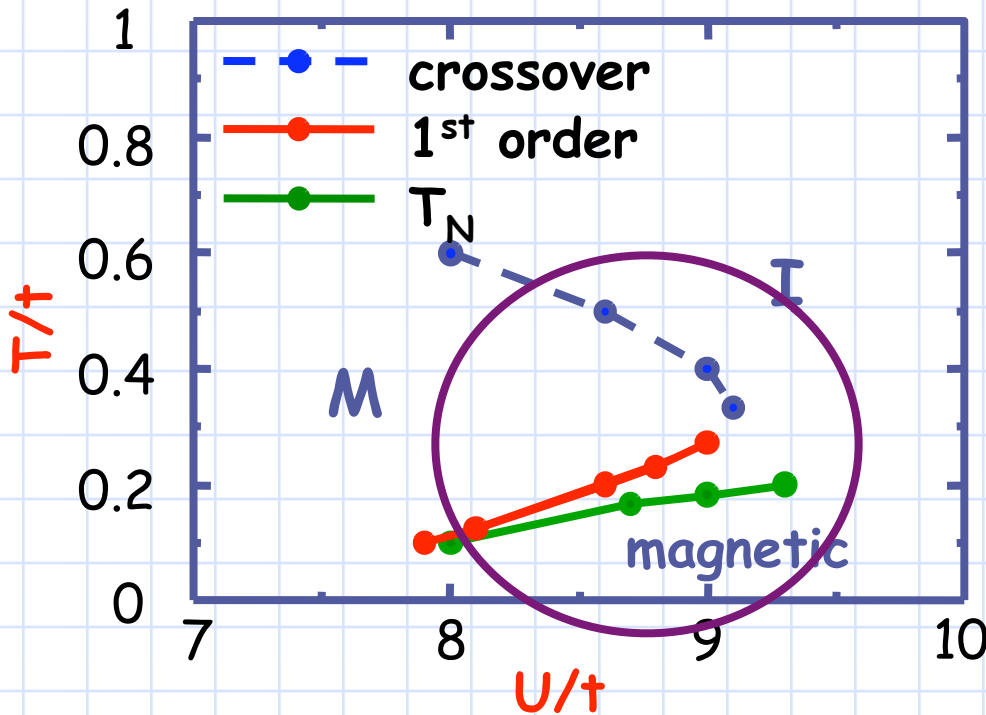


Cellular-DMFT



Comparison: frustrated systems in infinite dimensions

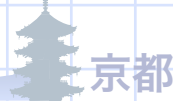
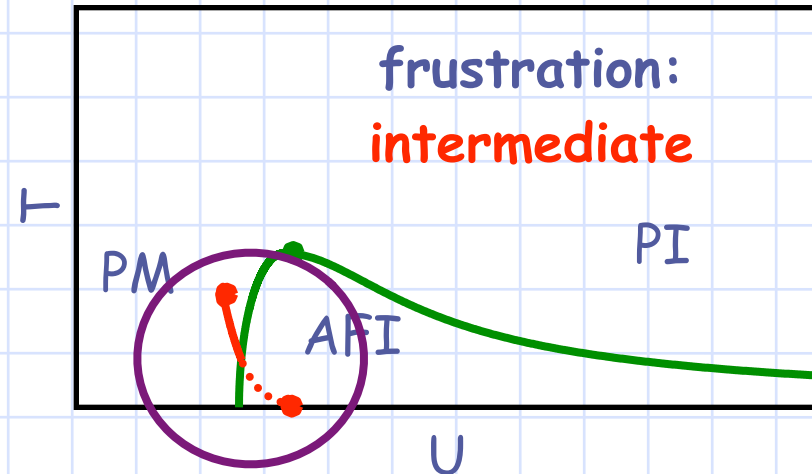
$t'/t=0.8$



Cellular-DMFT

DMFT: frustrated Bethe lattice

Zitzler et al. PRL 93 016406 (2004)

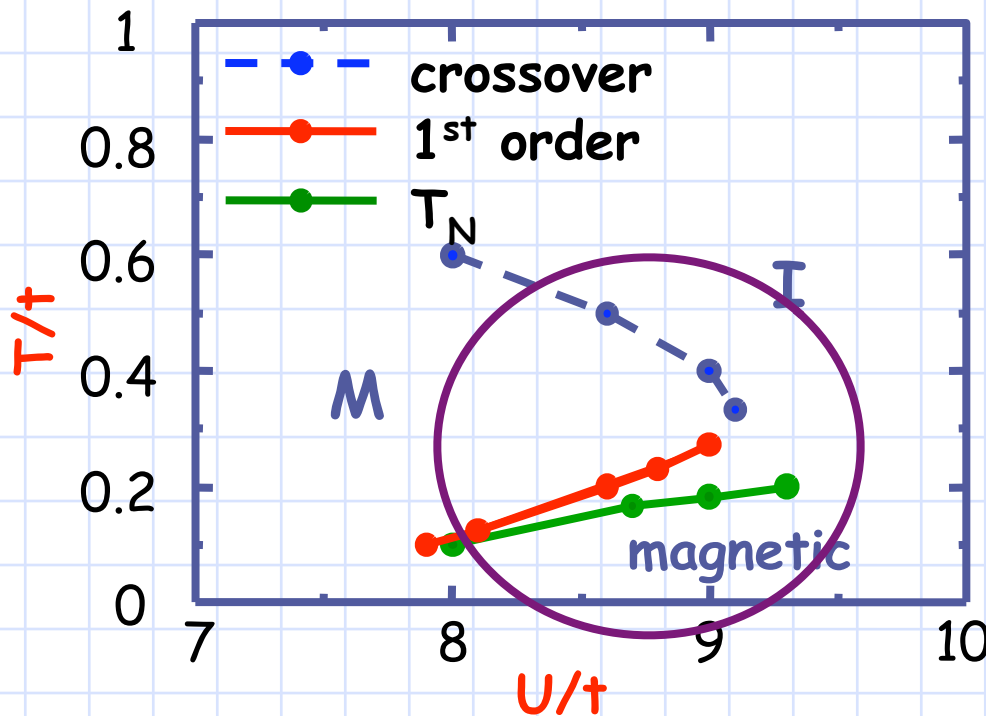


Comparison: frustrated systems in infinite dimensions

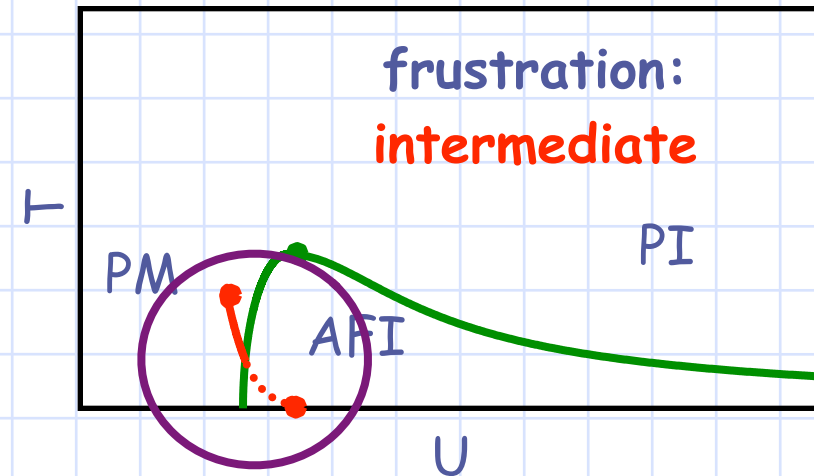
DMFT: frustrated Bethe lattice

Zitzler et al. PRL 93 016406 (2004)

$t'/t=0.8$



Cellular-DMFT



Spatial fluctuations

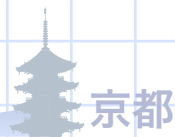
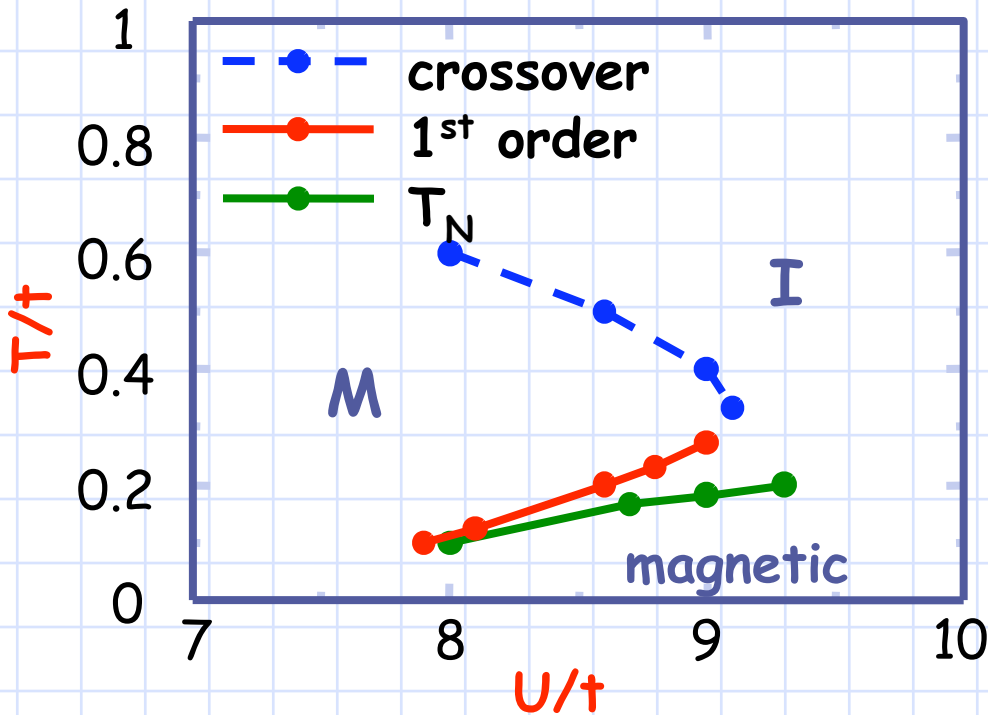
change in U_c critical line

nonmag. insulator

Comparison with organics

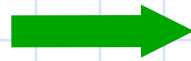
Cellular-DMFT \longrightarrow • order at finite T

$t'/t=0.8$



Comparison with organics

Cellular-DMFT

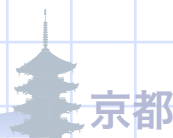
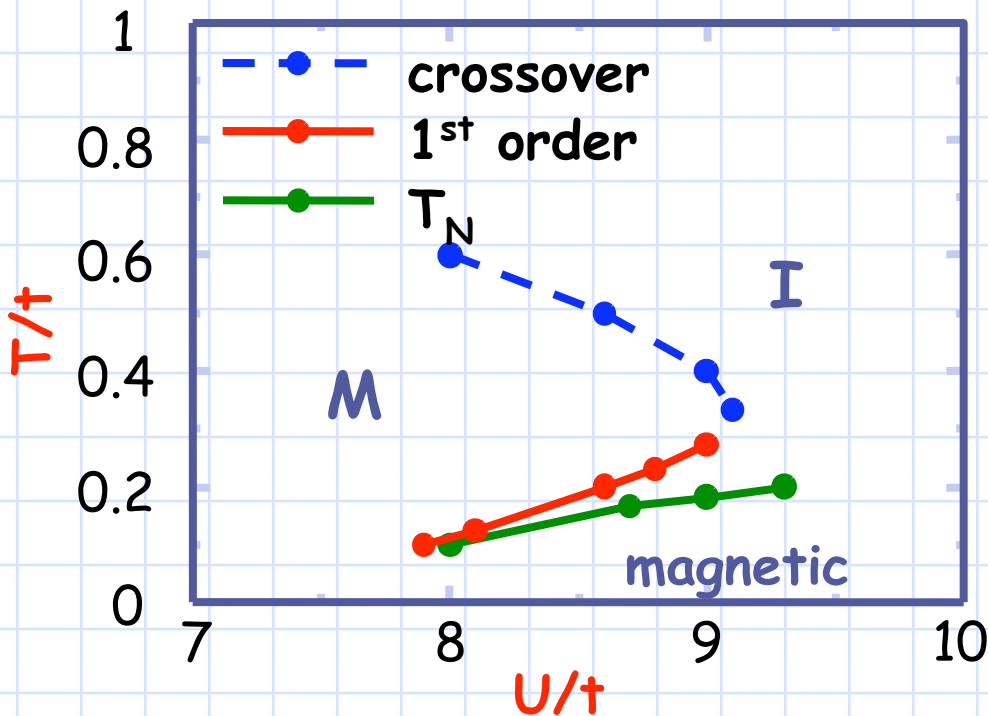


- order at finite T

$t'/t=0.8$

- stabilized by 3D

Maier et al., PRL 85, 1524 (2000)



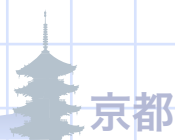
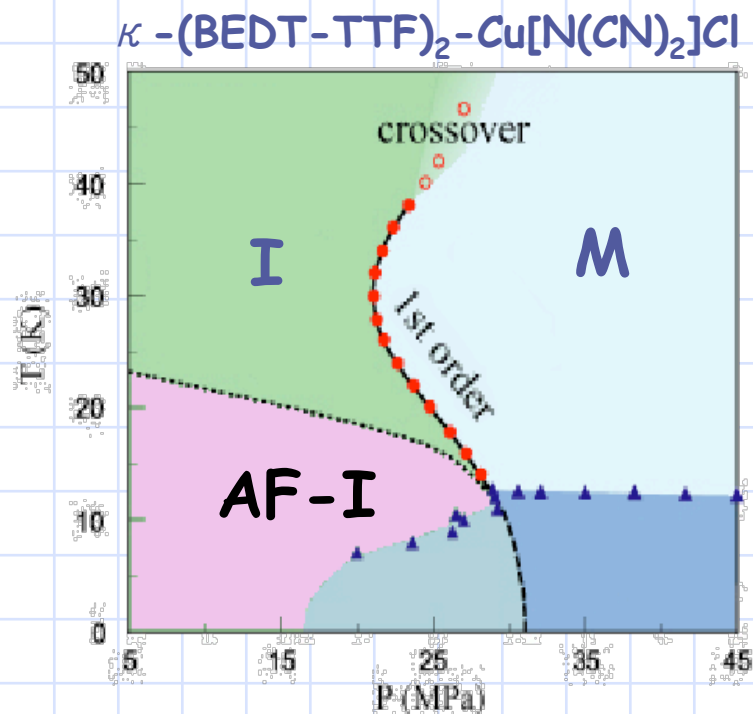
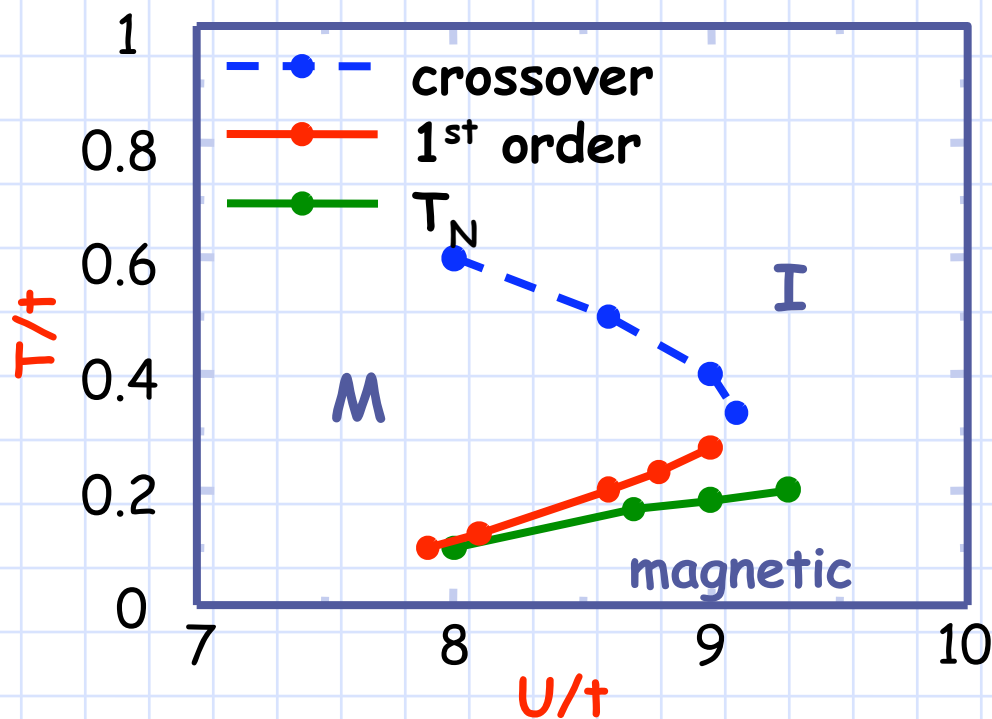
Comparison with organics

Cellular-DMFT ➔

$t'/t=0.8$

- order at finite T
- stabilized by 3D

Maier et al., PRL 85, 1524 (2000)



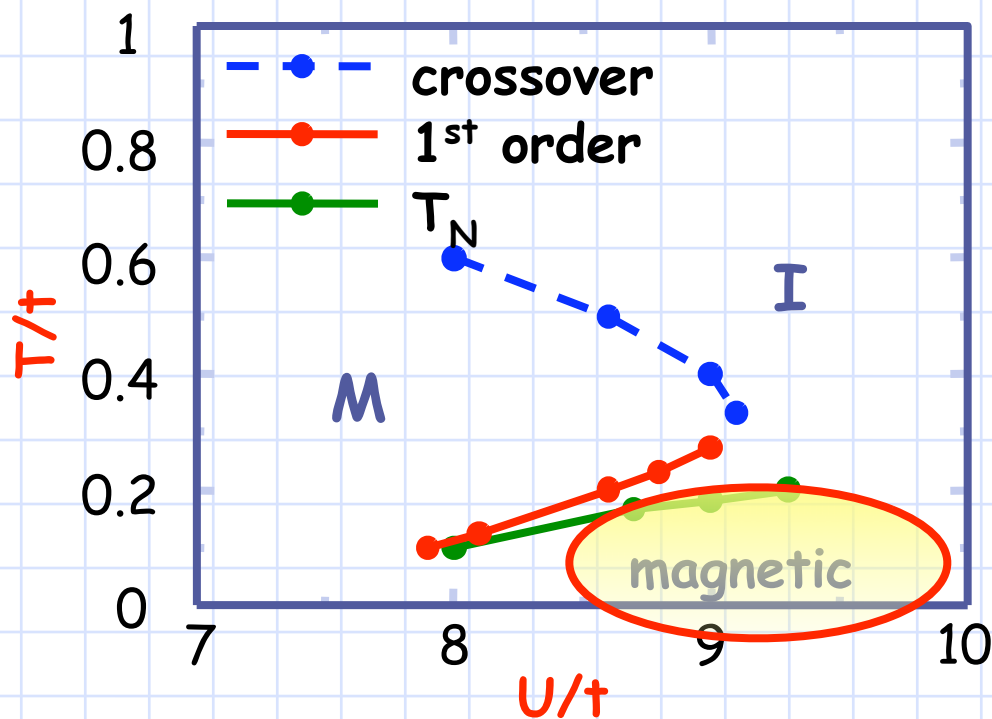
Comparison with organics

Cellular-DMFT \longrightarrow

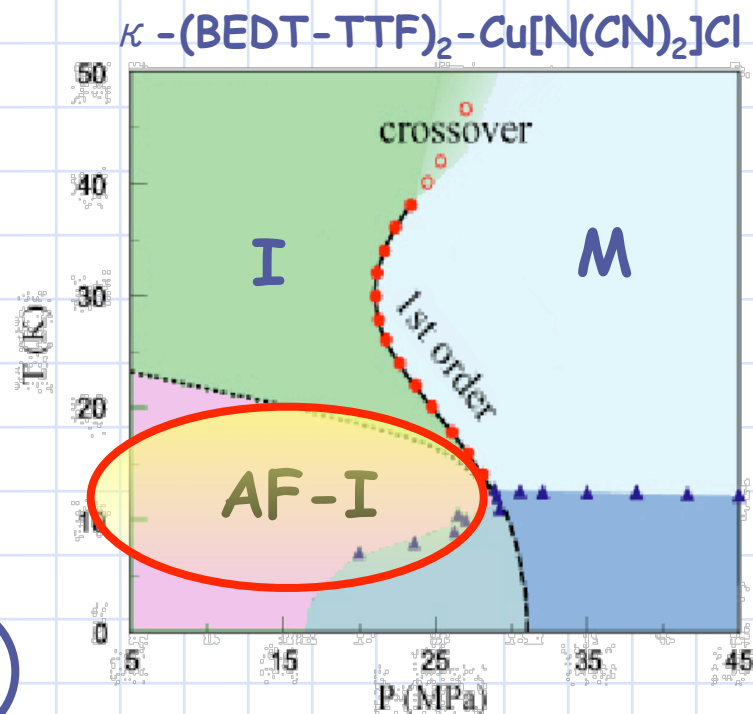
$t'/t=0.8$

- order at finite T
- stabilized by 3D

Maier et al., PRL 85, 1524 (2000)



Consistent with EXP.



Comparison with organics

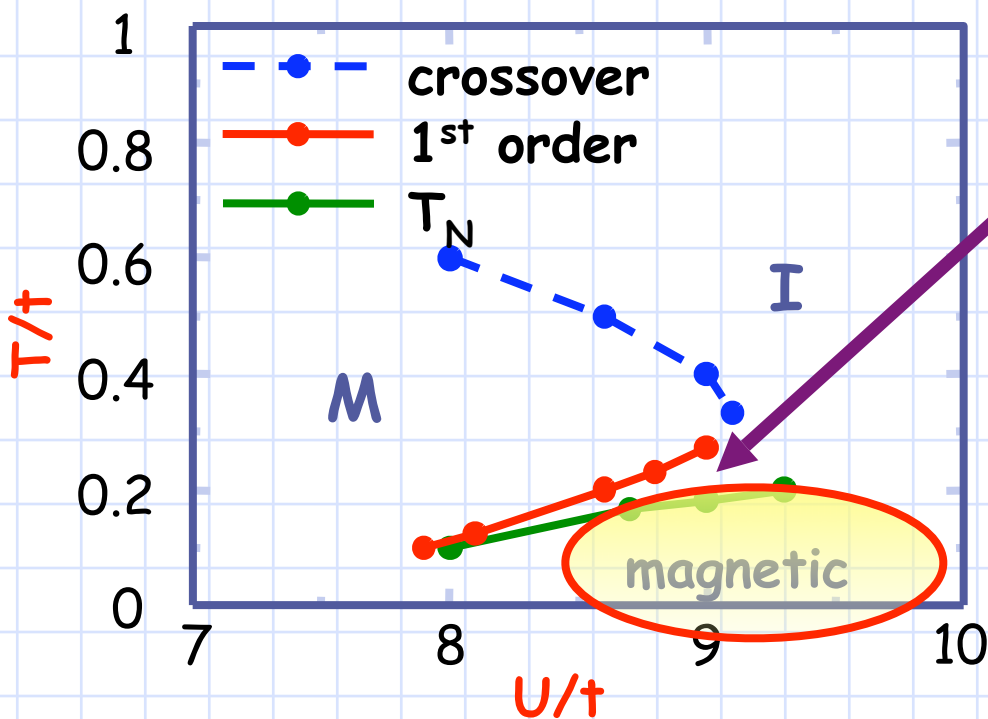
Nonmag insulator

Cellular-DMFT \rightarrow

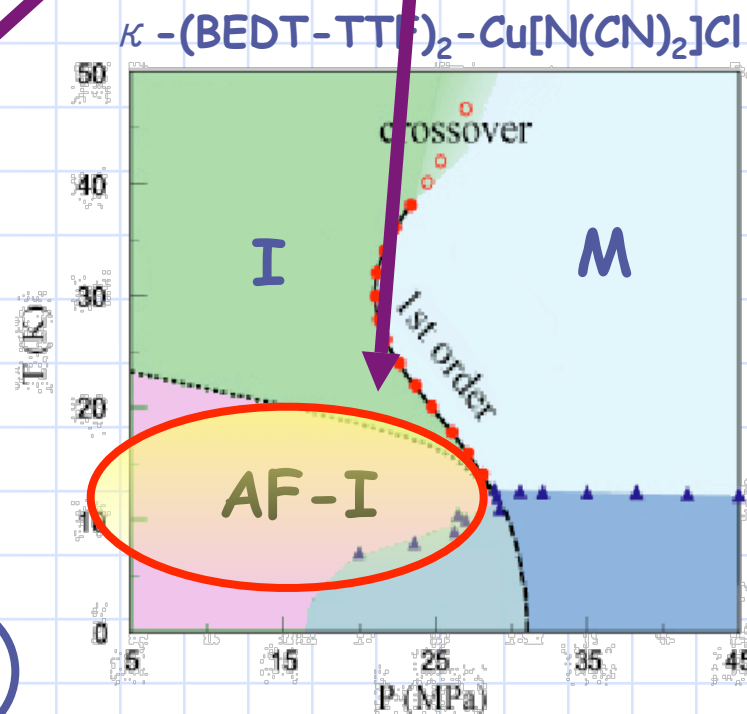
$t'/t=0.8$

- order at finite T
- stabilized by 3D

Maier et al., PRL 85, 1524 (2000)

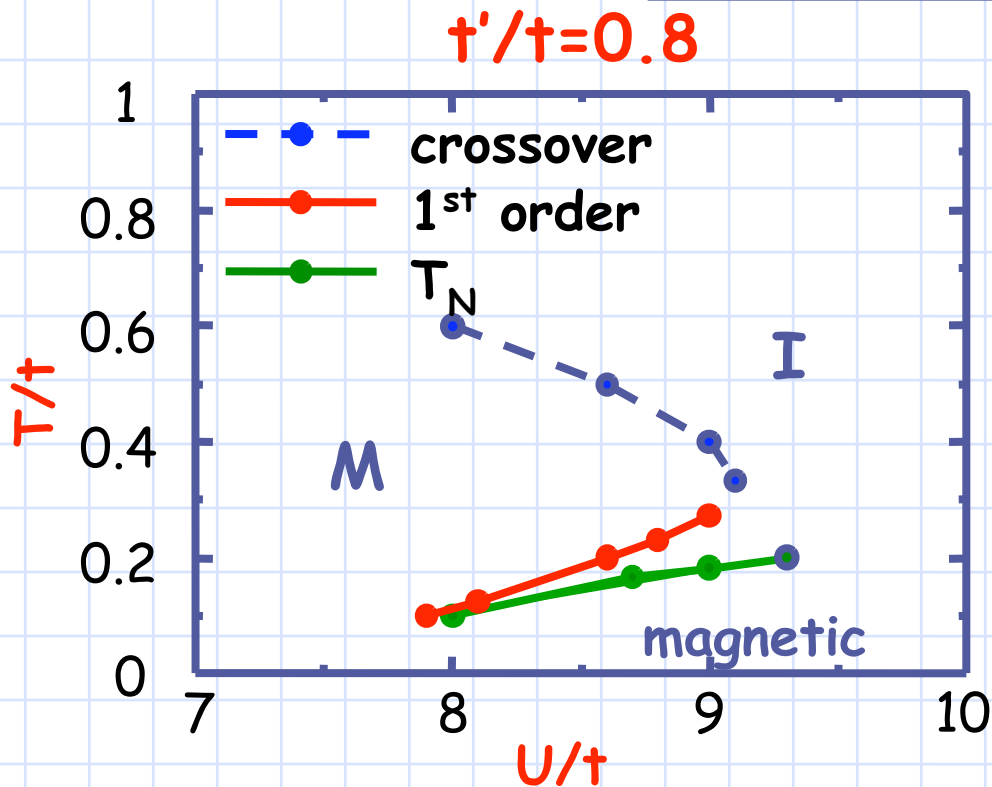


Consistent with EXP.



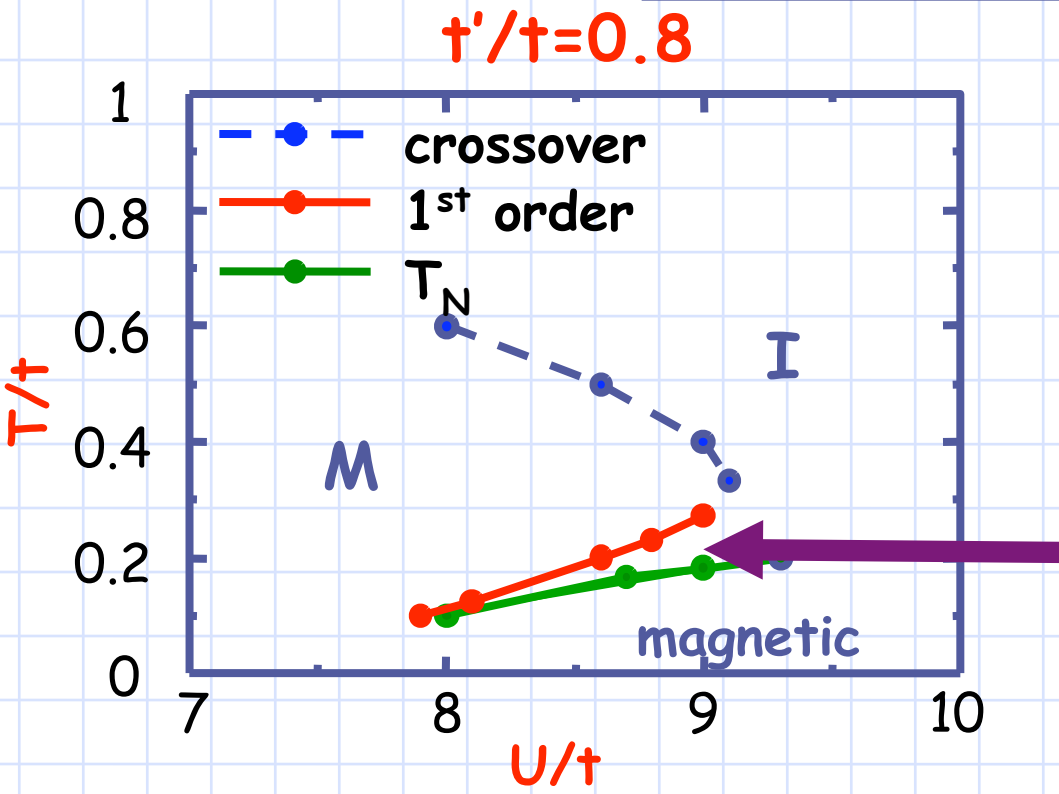
q-dependent susceptibility

Inherent in nonmagnetic insulator !

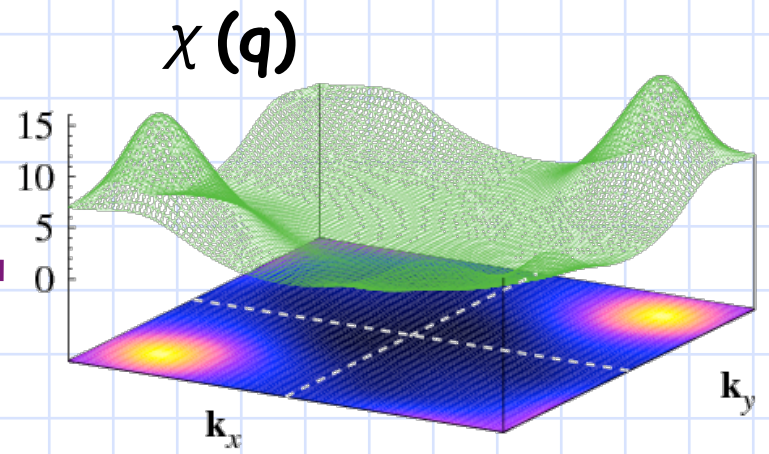


q-dependent susceptibility

Inherent in nonmagnetic insulator !

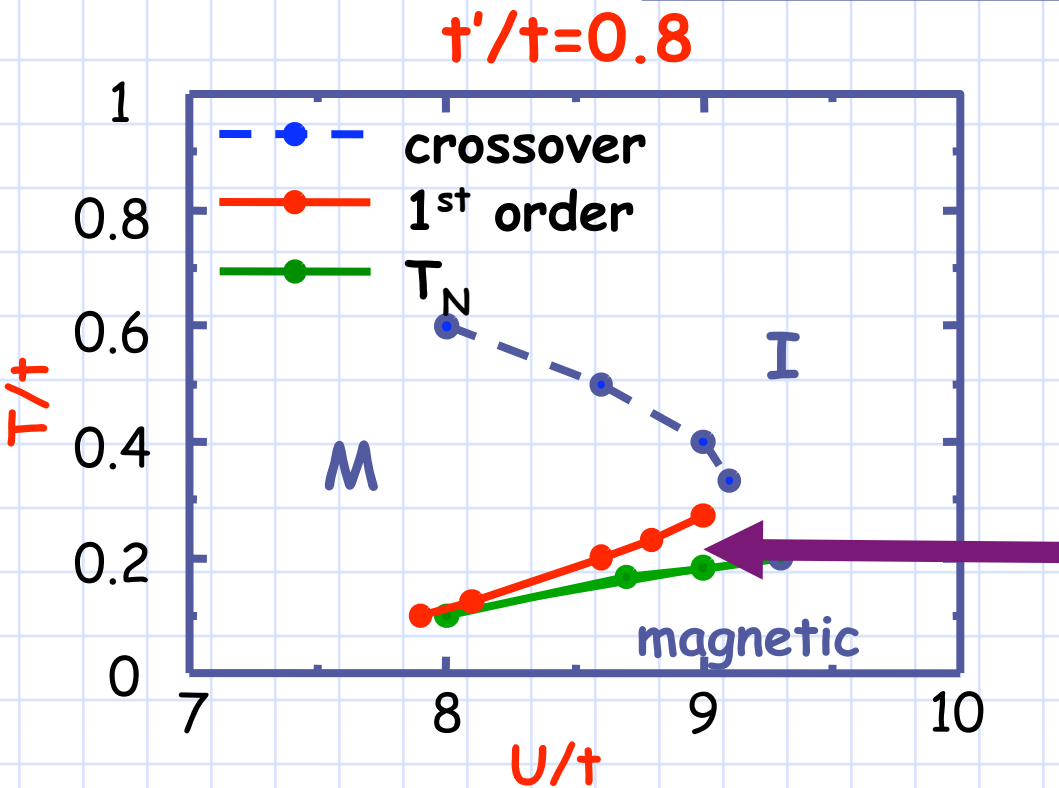


$U/t=9, T/t=0.2$

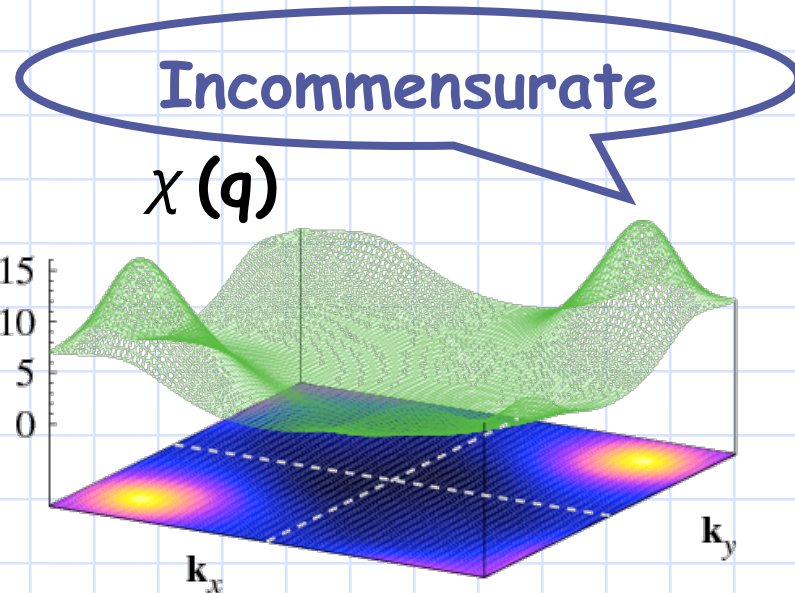


q-dependent susceptibility

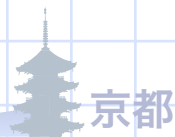
Inherent in nonmagnetic insulator !



$U/t=9, T/t=0.2$



- peak at $q \sim (0.75 \pi, 0.75 \pi)$
- not diverge



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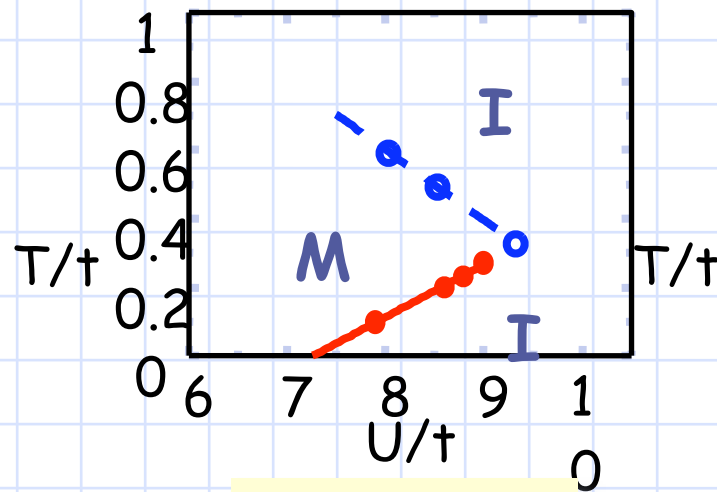
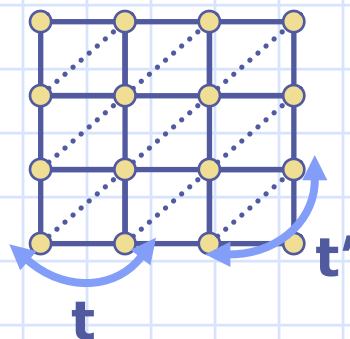


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What happens ?
control frustration
by changing *t'/t*

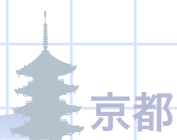


Phase diagram

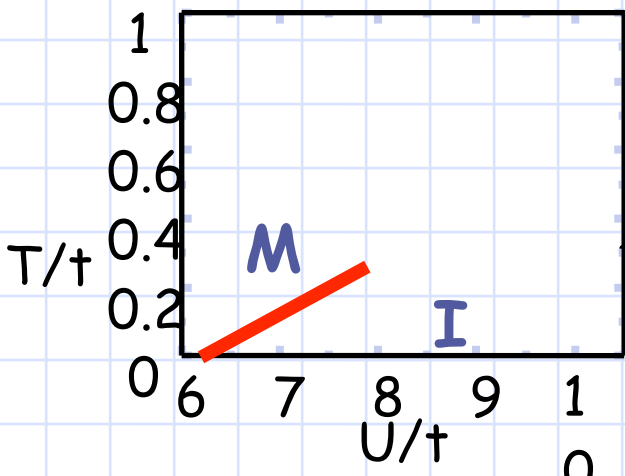
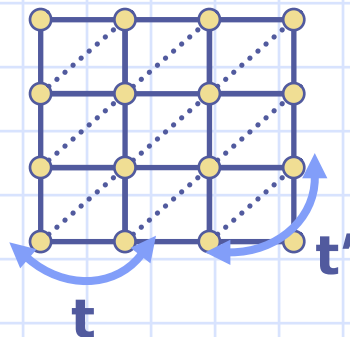


$t'/t = 0.8$

Intermediate

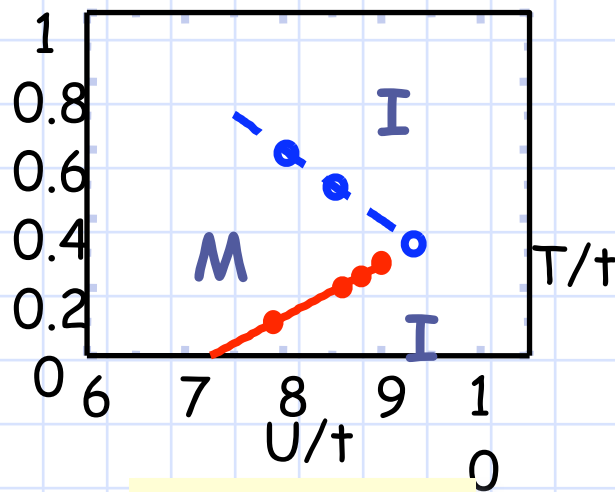


Phase diagram



smaller t'/t

Weak frustration

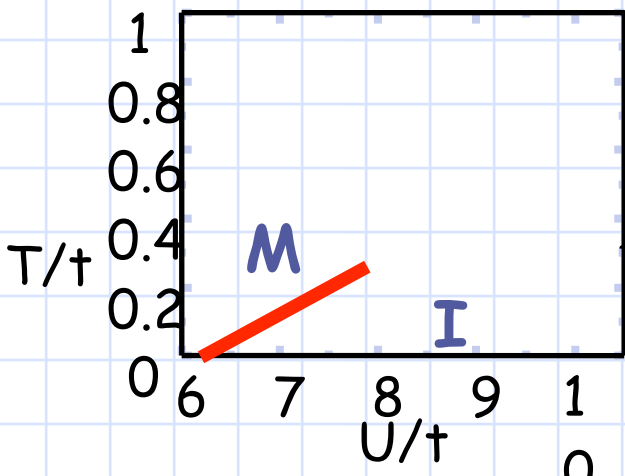
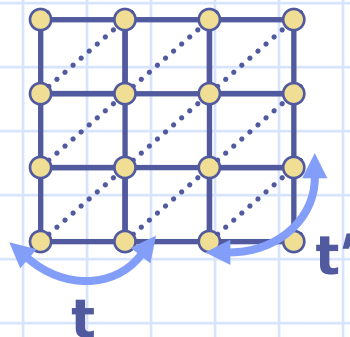


$t'/t = 0.8$

Intermediate

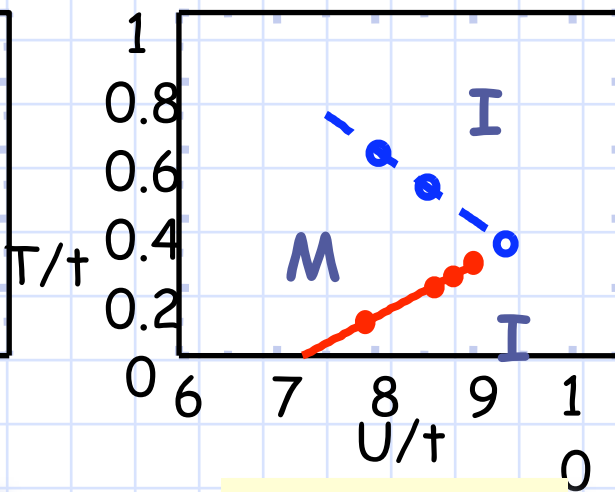


Phase diagram



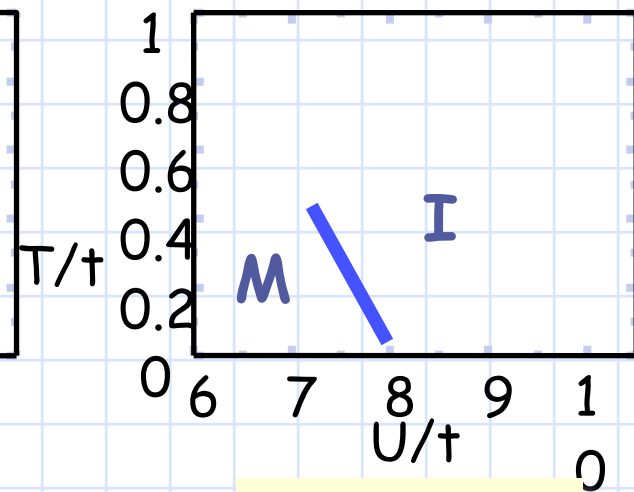
smaller t'/t

Weak frustration



$t'/t = 0.8$

Intermediate

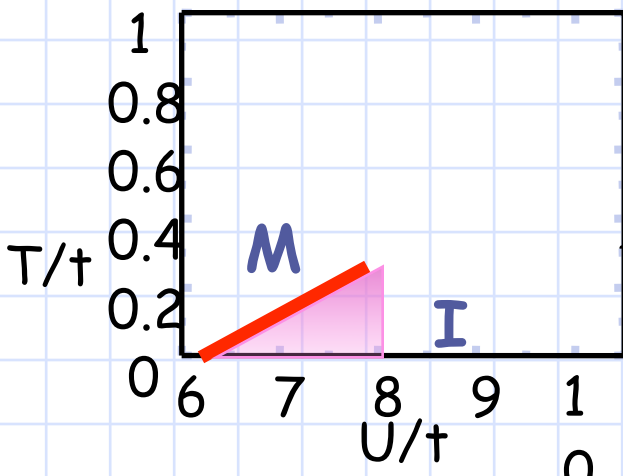
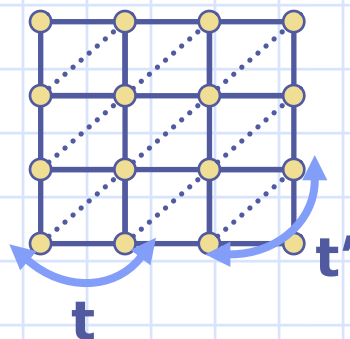


$t'/t = 1$

Strong frustration



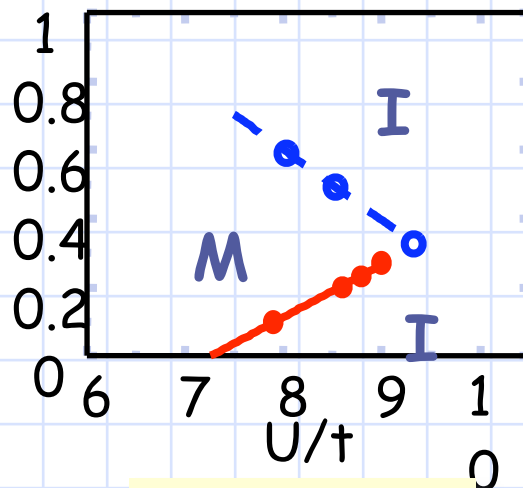
Phase diagram



smaller t'/t

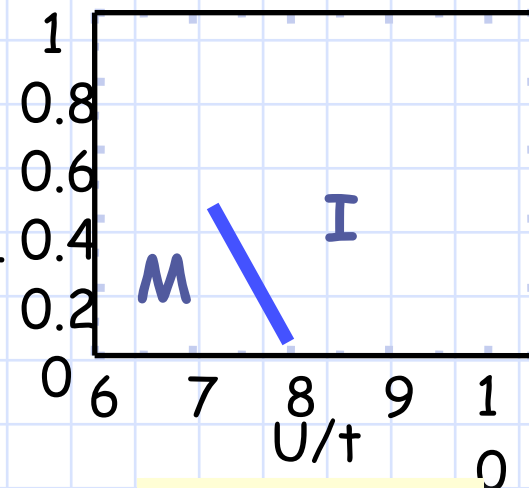
Weak frustration

Magnetic order ?



$t'/t = 0.8$

Intermediate

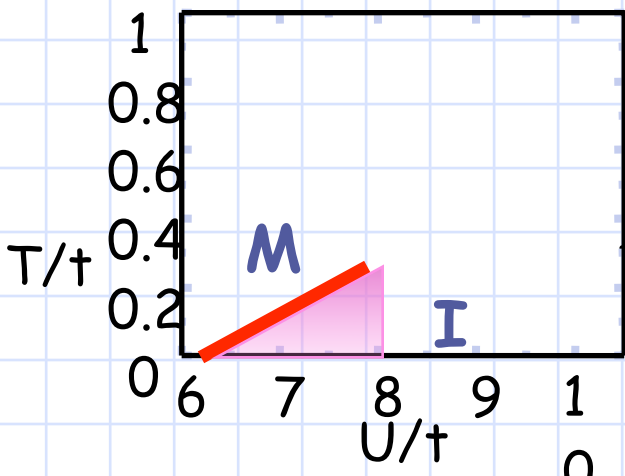
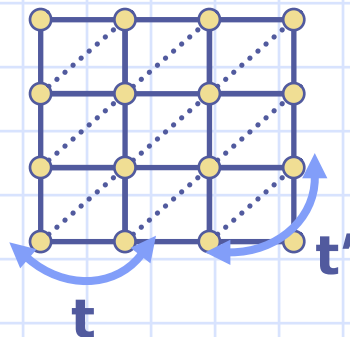


$t'/t = 1$

Strong frustration



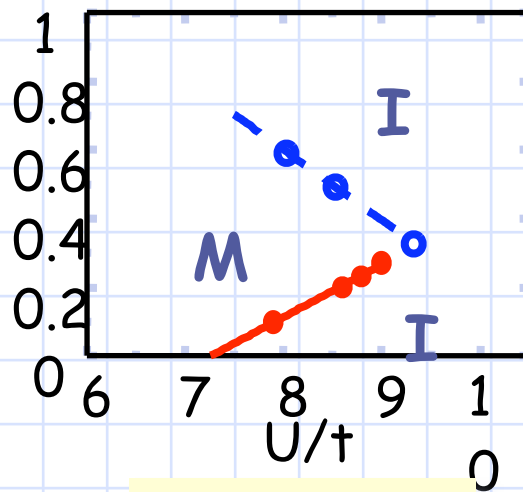
Phase diagram



smaller t'/t

Weak frustration

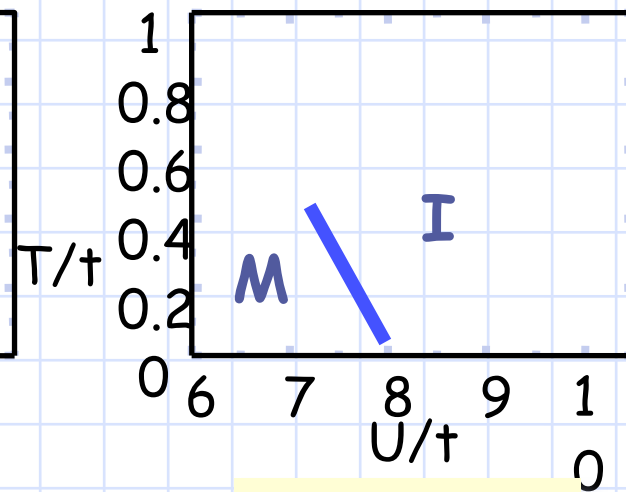
Magnetic order ?



$t'/t = 0.8$

Intermediate

Reentrant

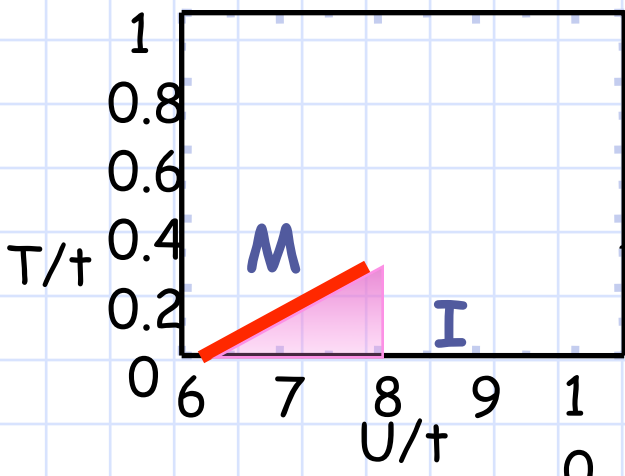
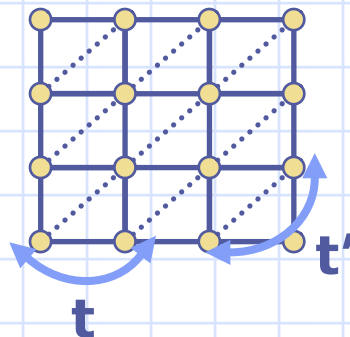


$t'/t = 1$

Strong frustration



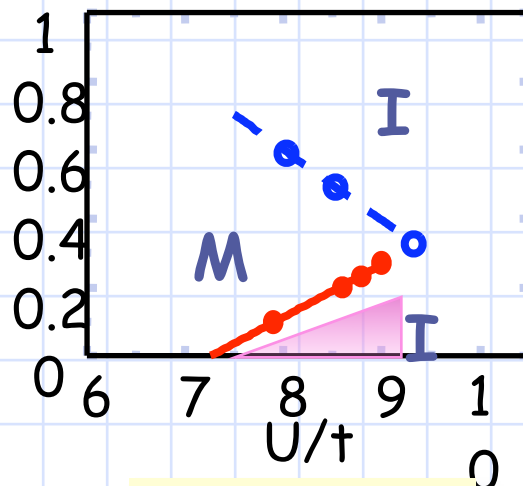
Phase diagram



smaller t'/t

Weak frustration

Magnetic order ?

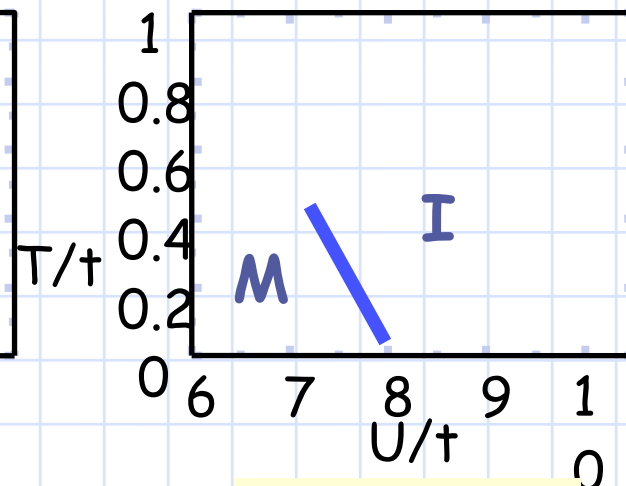


$t'/t = 0.8$

Intermediate

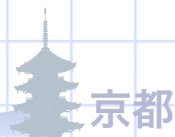
Reentrant

AF correlations at low T

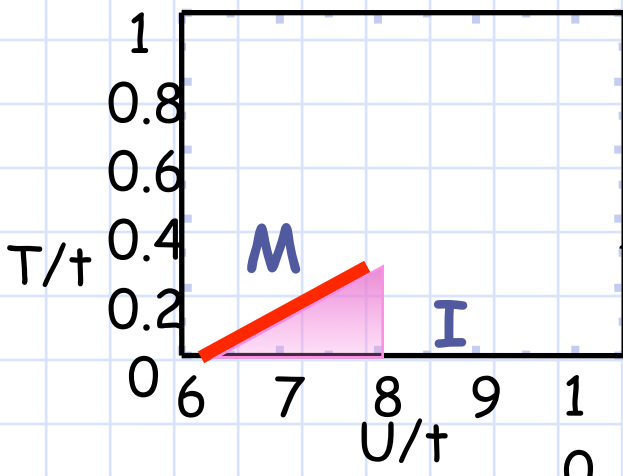
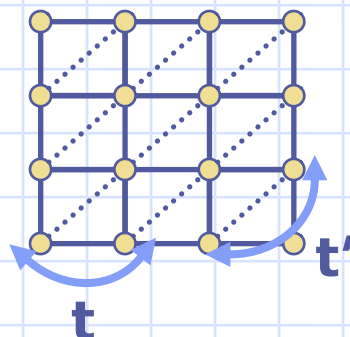


$t'/t = 1$

Strong frustration



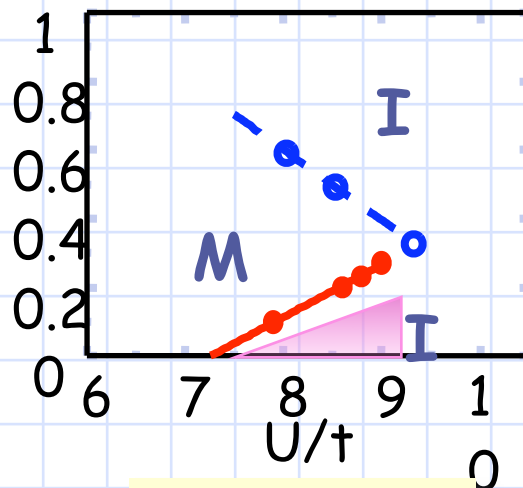
Phase diagram



smaller t'/t

Weak frustration

Magnetic order ?

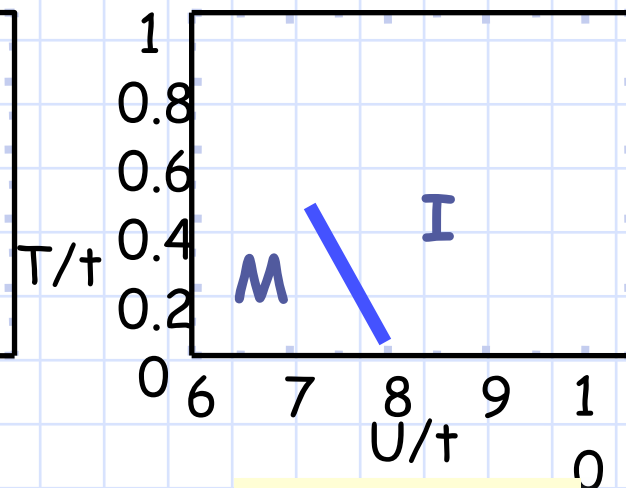


$t'/t = 0.8$

Intermediate

Reentrant

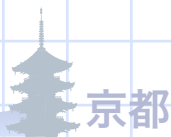
AF correlations at low T



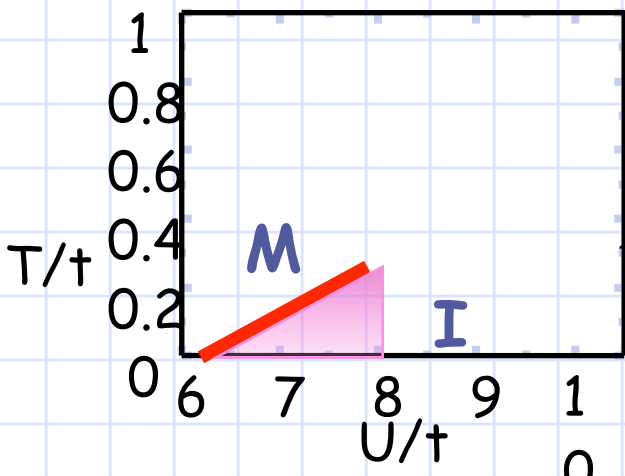
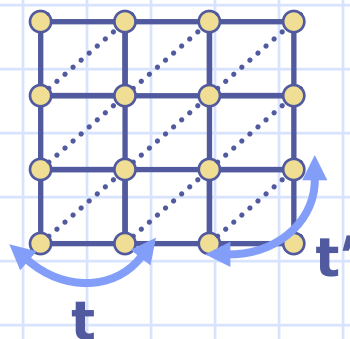
$t'/t = 1$

Strong frustration

Non-monotonic T-dependence



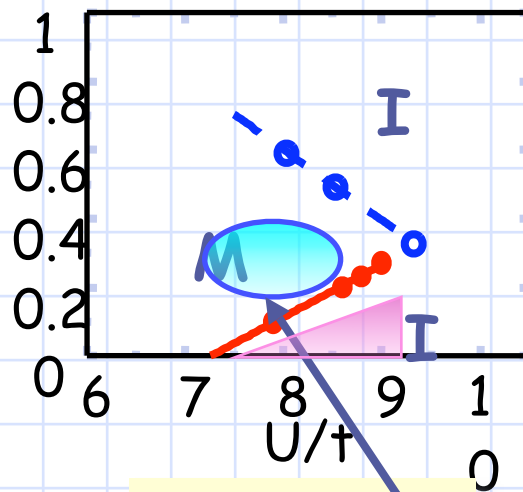
Phase diagram



smaller t'/t

Weak frustration

Magnetic order ?

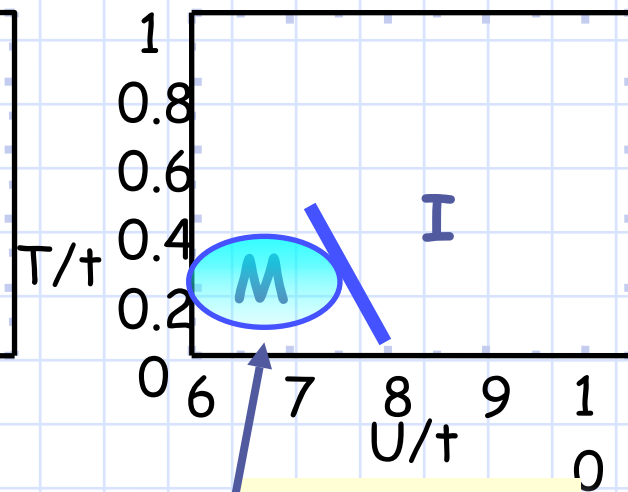


$t'/t = 0.8$

Intermediate

Reentrant

AF correlations at low T



$t'/t = 1$

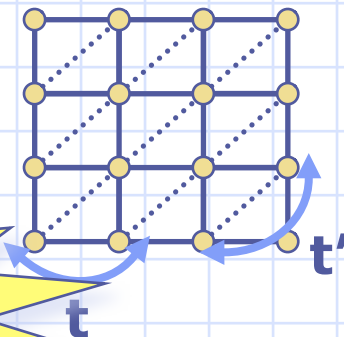
Strong frustration

Non-monotonic T-dependence

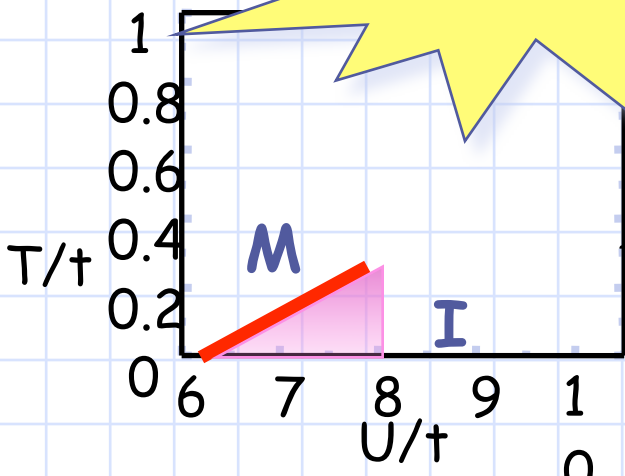
Frustration-induced heavy electrons



Phase diagram



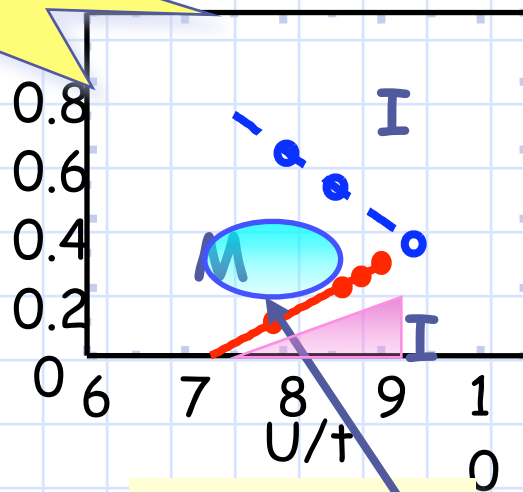
Universal feature



smaller t'/t

Weak frustration

Magnetic order ?

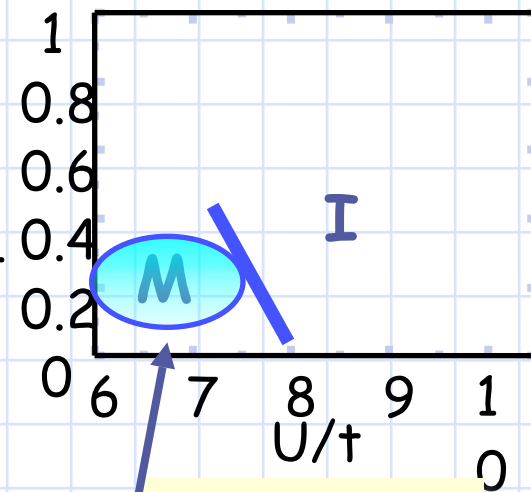


$t'/t = 0.8$

Intermediate

Reentrant

AF correlations at low T



$t'/t = 1$

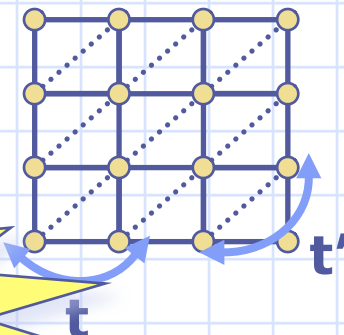
Strong frustration

Non-monotonic T-dependence

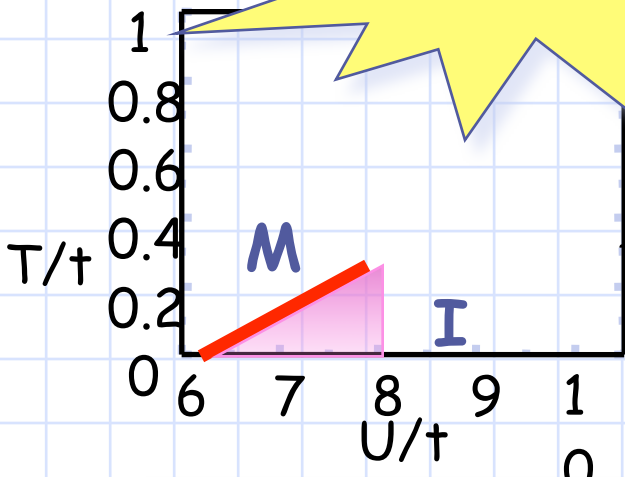
Frustration-induced heavy electrons



Phase diagram



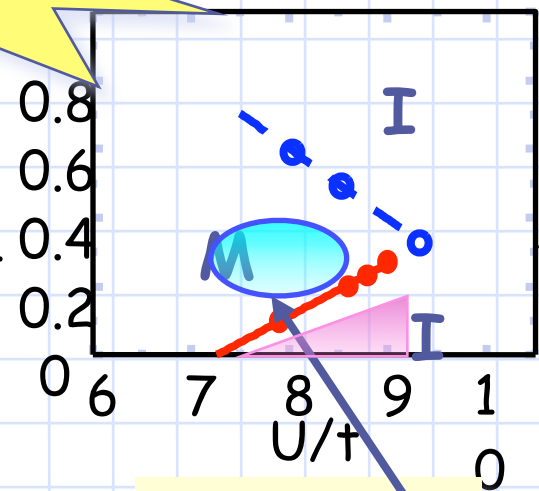
Similar to Kagome



smaller t'/t

Weak frustration

Magnetic order ?

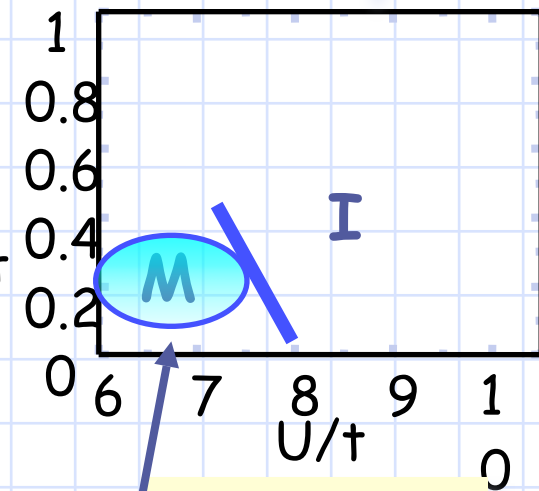


$t'/t = 0.8$

Intermediate

Reentrant

AF correlations at low T



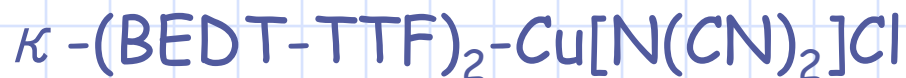
$t'/t = 1$

Strong frustration

Non-monotonic T-dependence

Frustration-induced heavy electrons

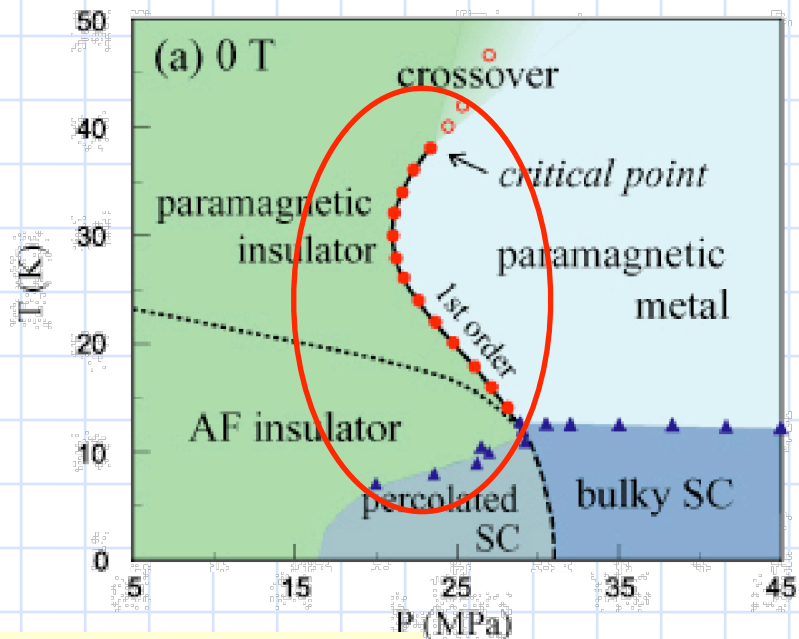




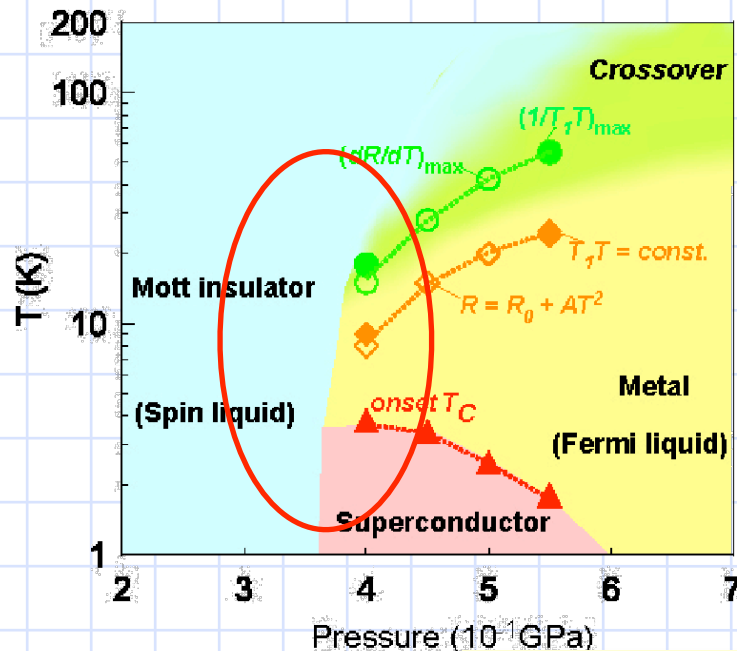
F. Kagawa et al., PRB 69, 064511 (2004)



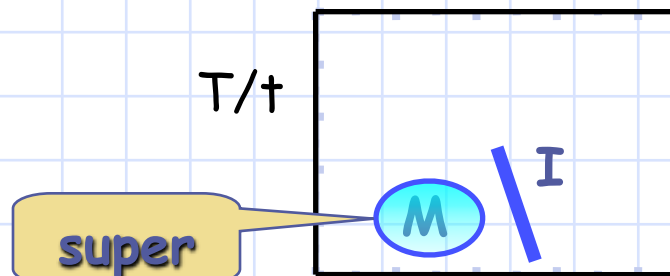
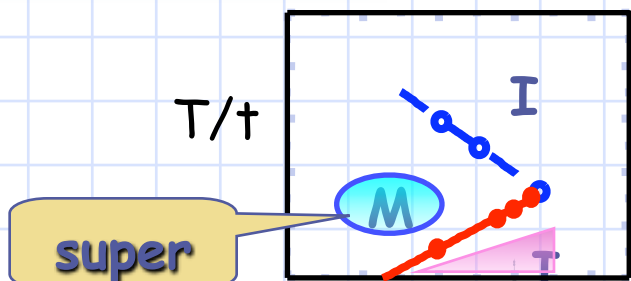
Y. Kurosaki et al., PRL 95, 177001 (2005)

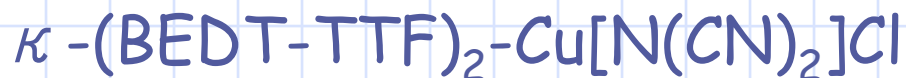


$t'/t = 0.75$



$t'/t = 1.06$

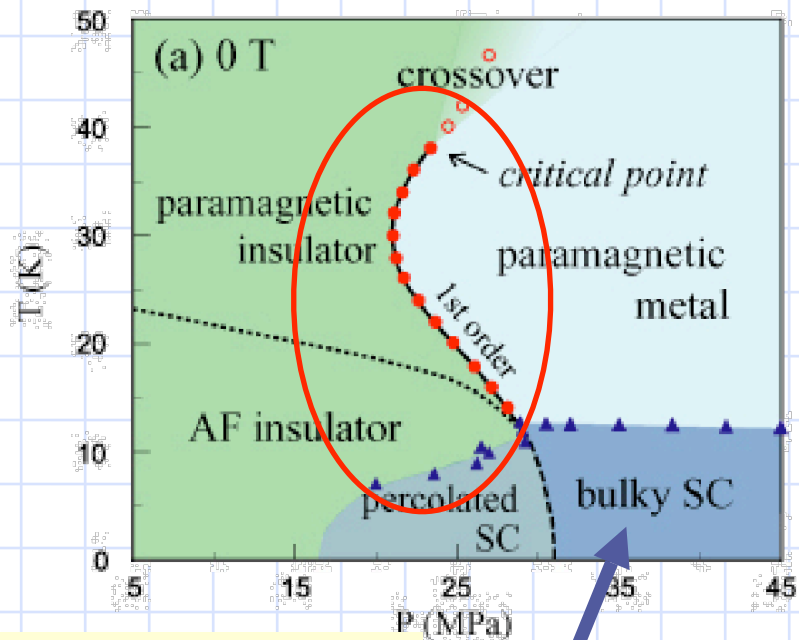




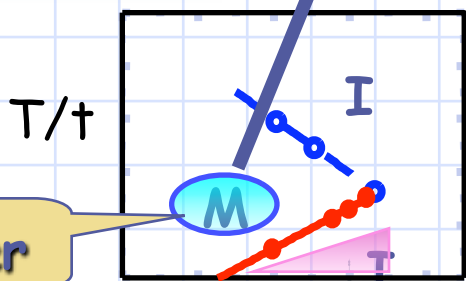
F. Kagawa et al., PRB 69, 064511 (2004)



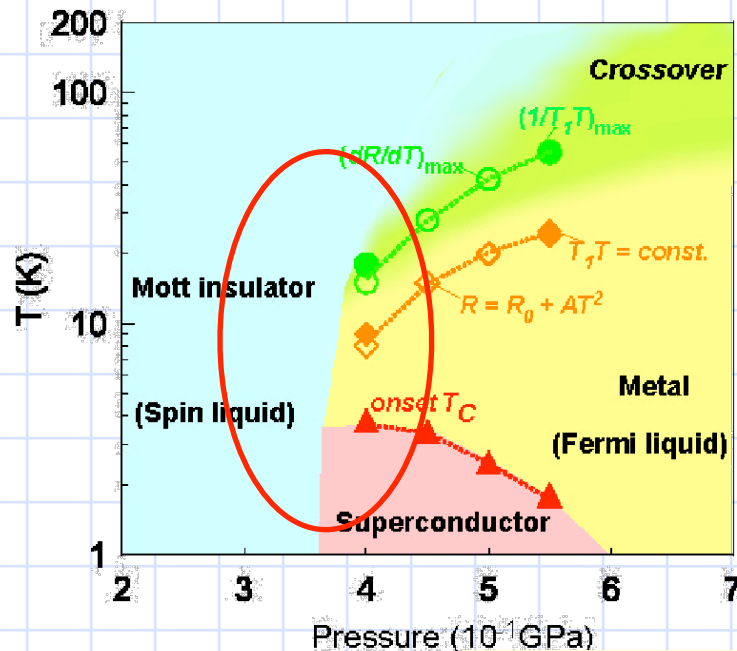
Y. Kurosaki et al., PRL 95, 177001 (2005)



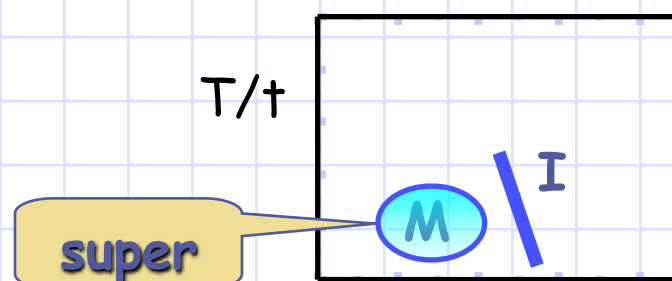
$t'/t = 0.75$



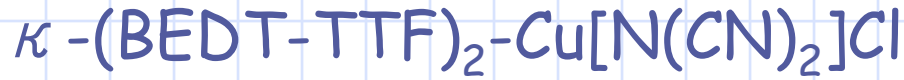
U/t 京都



$t'/t = 1.06$



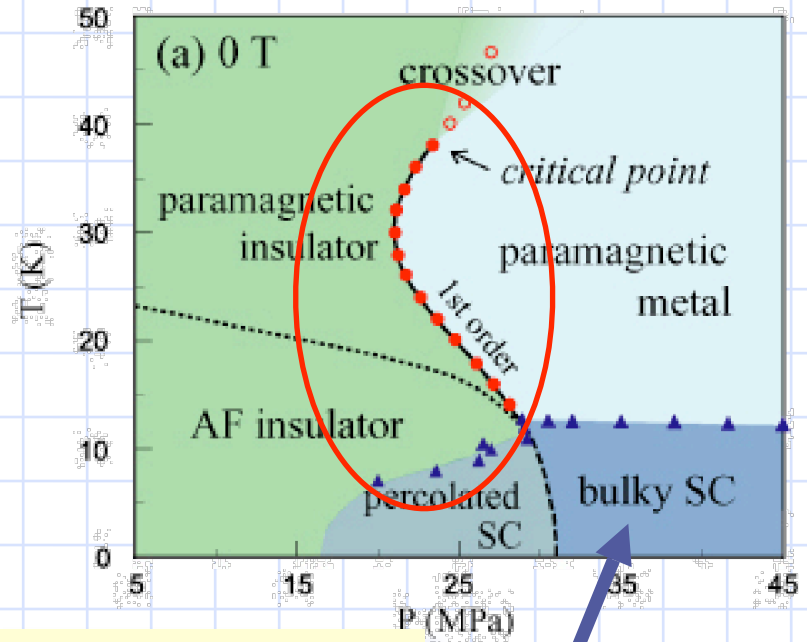
U/t



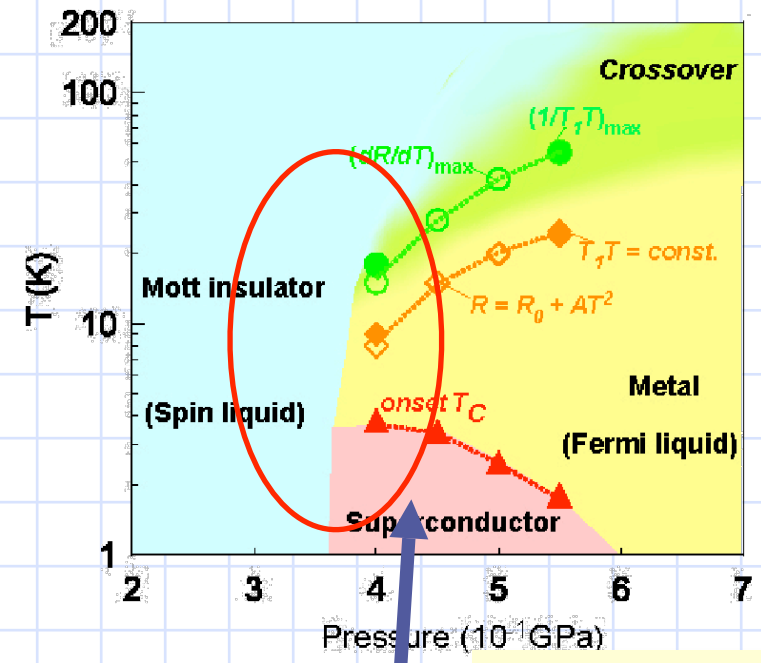
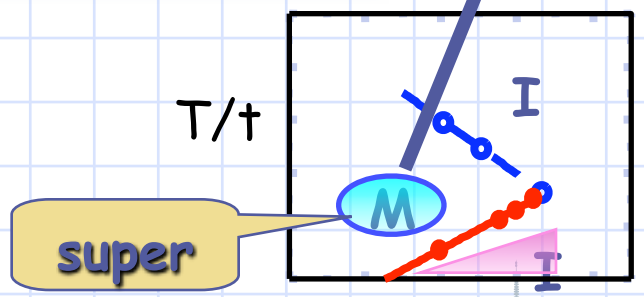
F. Kagawa et al., PRB 69, 064511 (2004)



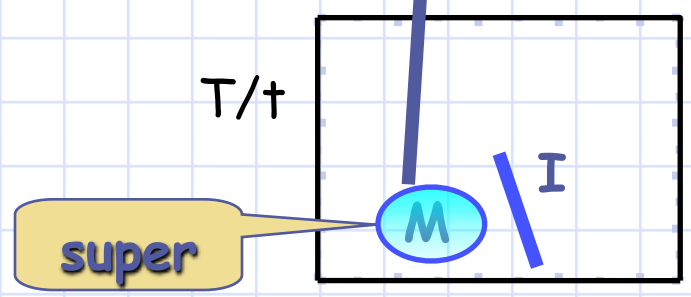
Y. Kurosaki et al., PRL 95, 177001 (2005)



$t'/t = 0.75$



$t'/t = 1.06$

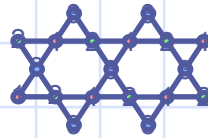


Summary

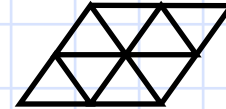
Mott transitions: frustrated systems

Hubbard model

Kagome



Triangular



Anomalous behavior near MIT (finite T)

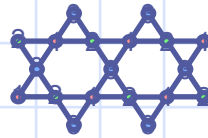


Summary

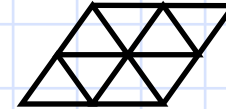
Mott transitions: frustrated systems

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Triangular



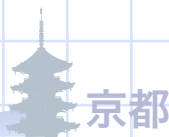
Anomalous behavior near MIT (finite T)

1. Strong frustration

Frustration-induced heavy electrons

2. Intermediate frustration

Reentrant behavior

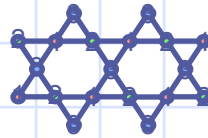


Summary

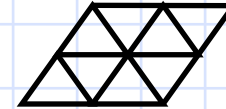
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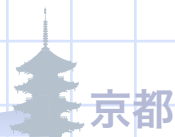
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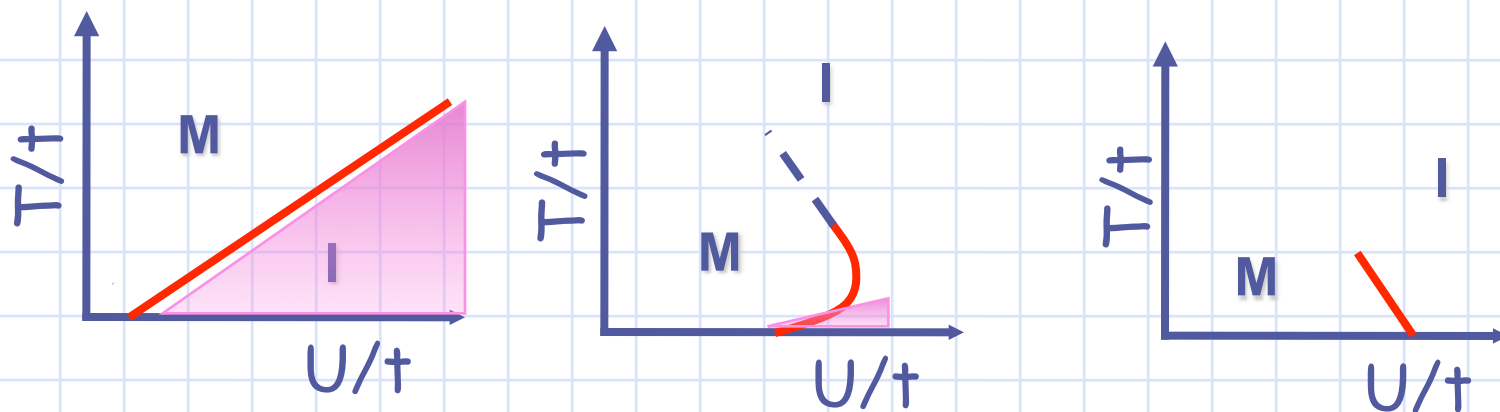
Reentrant behavior

Common



Generic features !?

correlations
frustration
Quantum fluctuations

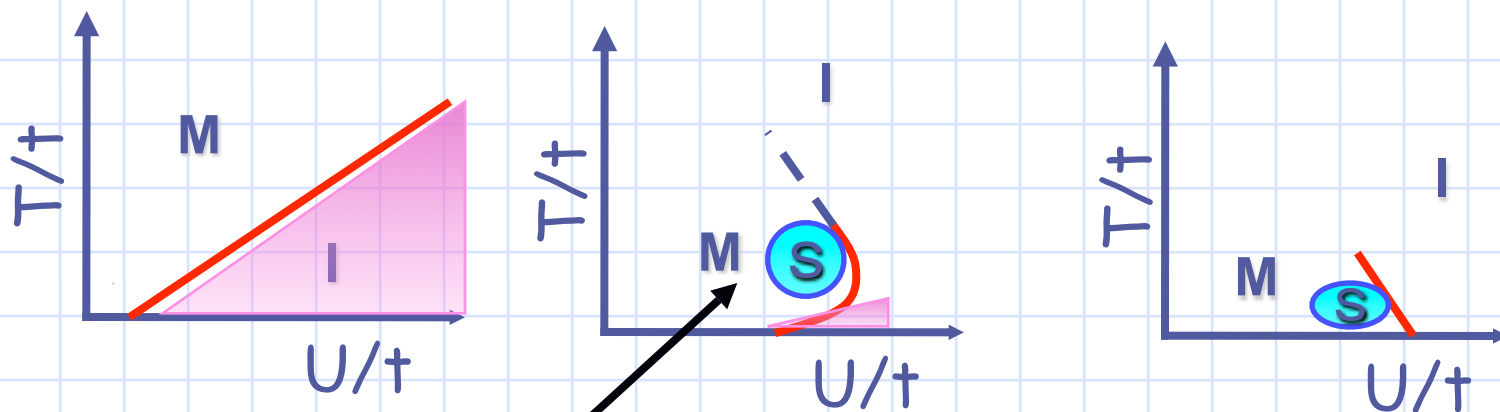


Frustration



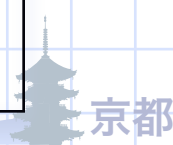
Generic features !?

correlations
frustration
Quantum fluctuations



Frustration

Moderately high T_c



YKIS 07
Kyoto
November 14,
2007

**Thank you
for your attention !**

