

Yukawa International Seminar (YKIS) 2007
"Interaction and Nanostructural Effects in Low-
Dimensional Systems"
Workshop-2 (Nov. 15: 2D systems and Nano)

Electrical Control of Electron Spin and Nuclear Spin in Quantum Dots

S. Tarucha

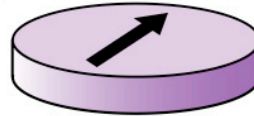
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ICORP-JST INQIE-MEXT

Tokyo-U	A. Oiwa	ICORP-JST	Y. Tokura	NTT
	M. Yamamoto		M. Pioro-Ladriere	
	K. Hitachi		T. Obata	
	J. Baugh (Waterloo-U)		Y-S Shin	
			S. Yoshida	
Riken/ICORP	K. Ono	INQIE	T. Koder	

Spin-based QC with QDs: Loss-DiVincenzo '98

QD holding just an electron spin

$$\text{Qubit} = a|\uparrow\rangle + b|\downarrow\rangle$$



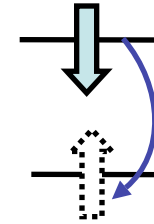
ST et al. *PRL* 96
Ciorga et al. *PRL*02

Robust spin degree of freedom

$$T_1 = \text{msec to sec}$$

Triplet to Singlet: Fujisawa, ST et al. *Nature* 02

Zeeman states: Amasha et al. *PR* 06

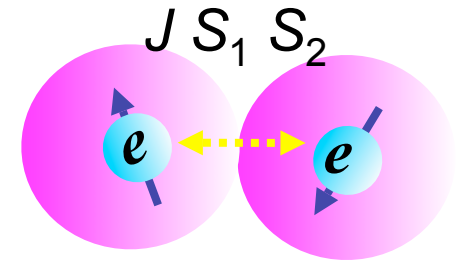


Entanglement linked to Fermionic nature

$$H_{\text{int}} = J_{\text{exch}} S_1 S_2$$

SWAP: Petta et al. *Science* 05

Heitler-London: Hatano, ST et al. *Science* 05

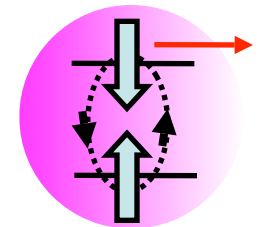


Single spin readout

Pauli spin blockade: Ono, ST et al. *Science* 02

Spin rotation using P-SB: Koppens et al. *Nature* 06

Zeeman splitting: Elzerman et al. *Nature* 05

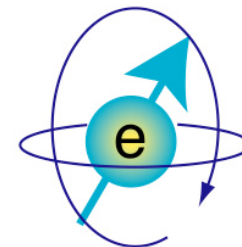


Coherent spin manipulation

SWAP-qubit: Petta et al. *Science*05

On-chip coil qubit: Koppens et al. *Nature* 06

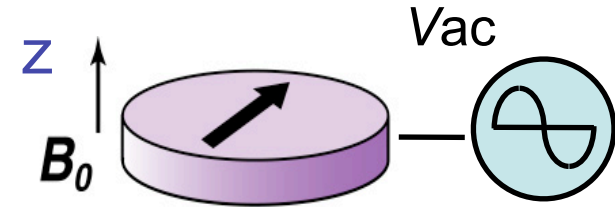
SO-EDSR qubit: Nowack *et al.*, arXiv0707.3080



Progress Necessary for Spin Qubits with QDs

Robust, scalable qubit
Beyond standard ESR

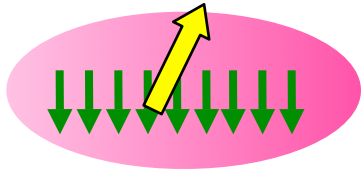
....Voltage-driven ESR



Decoherence problem

Spin-orbit..... $T_2 \sim T_1 = \text{msec to sec}$ Fujisawa, ST et al 02, Amasha et al. 07,
Golovach, Khaetskii, Loss 04

Nuclei Short $T_2^* \sim \text{a few 10 ns}$ influenced by fluctuating nuclear fields



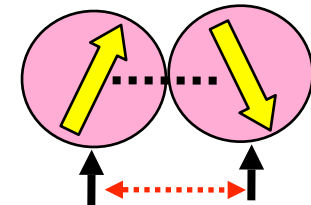
← Full polarization Simon, Loss 07 (Thermodynamic pol.)

Projection measurement Klauser, Coish, Loss 06

Other materials such as nanotubes, Si, Si/Ge
with no substantial SO and nuclear spin effect

Fast, reliable readout

Single spin...10 kHz to MHz (charge) using QPC
Entanglement....Cross-correlation of shot noise



CNOT, Error correction,

Outline

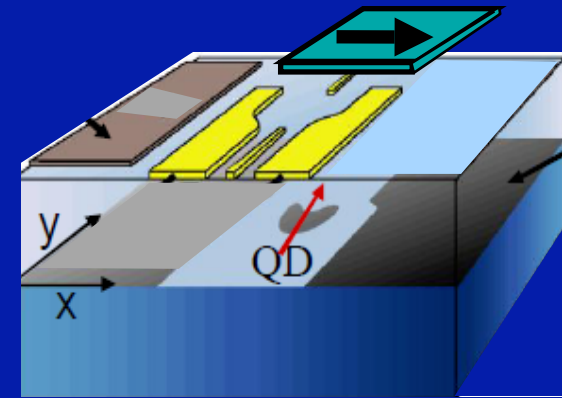
Spin control with GaAs quantum dots

Voltage driven electron spin resonance and spin qubits with quantum dots

Spin rotation using a slanting Zeeman field
formed by a micro-magnet

Two-spin addressing

Micro-magnet design for scalability

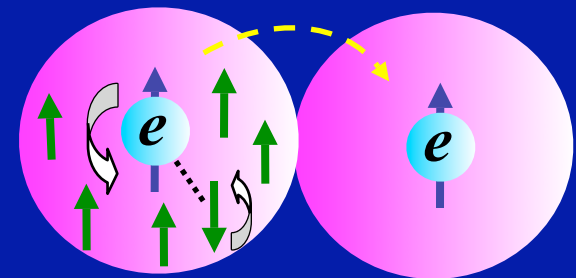


Electrical control of nuclear spin polarization

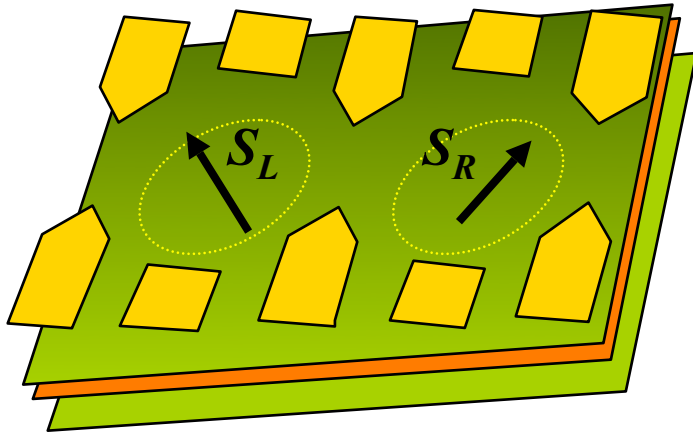
Voltage-controlled hyperfine coupling
in the Pauli spin blockade

Tunable polarization up to ~50 %

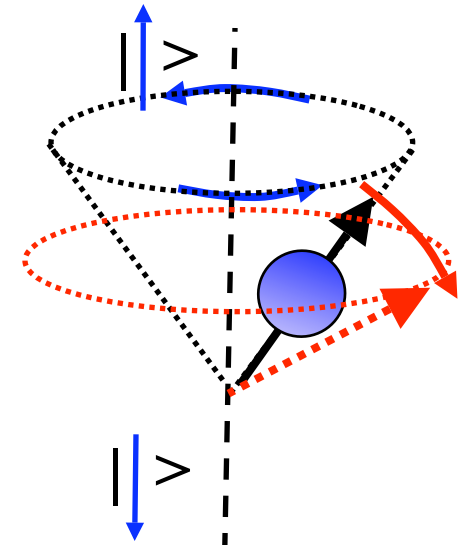
Possible approach to full polarization



Concept of Spin Qubit = ESR



Qubit: $a|\uparrow\rangle + b|\downarrow\rangle$

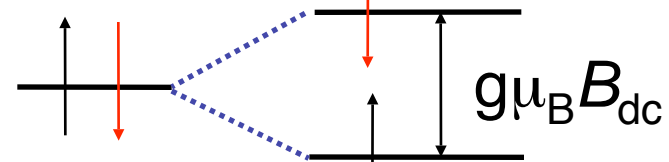
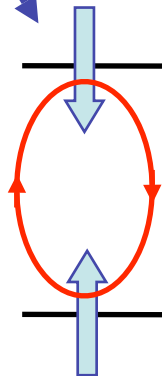


$$H_{2\text{level}} = \frac{\epsilon_z}{2} \sigma_z + \frac{\epsilon_x(t)}{2} \sigma_x$$

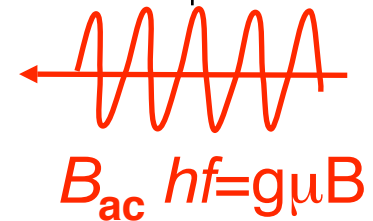
Static B_z

AC B_x

ESR Hamiltonian



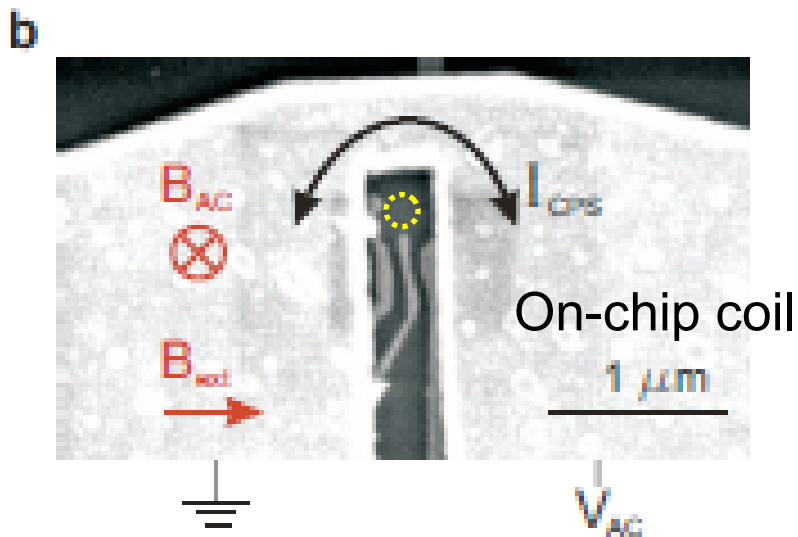
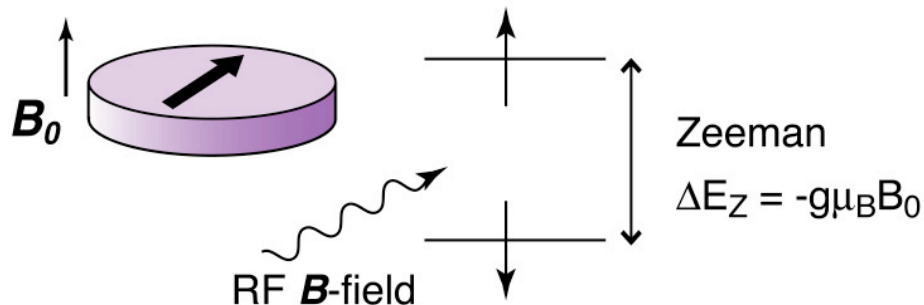
B_{dc}



B_{ac} with $f = g\mu_B/h = 15$ GHz
at $B_0 = 5$ T for GaAs QD

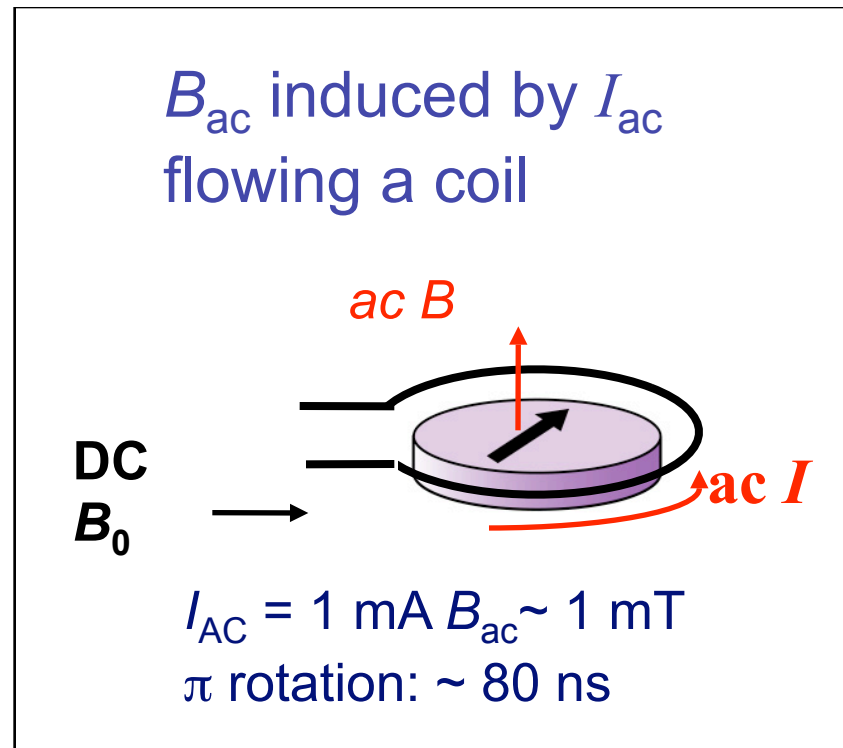
ESR to Address Individual Spins

“Global dc B_z and local ac B_x for single spin resonance”



Current driven ESR

F. Koppens et al. *Science* 06

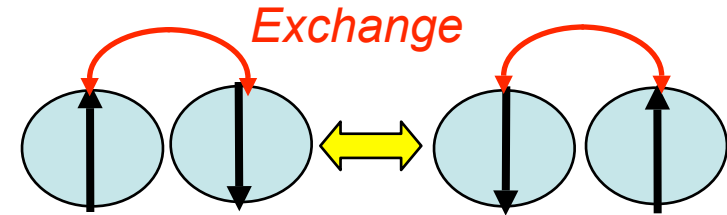


→ *Heating problem*
Difficult for local access
↑ *Voltage-driven ESR*

Voltage-driven Single Spin Resonance

Exchange control in a double quantum dot (inter-dot coupling gate modulation)
: Spin qubit with a basis of two-spin states

J. Petta et al. *Nature* 05



Electric dipole spin resonance (EDSR) via local interaction
between electron spin and electric field

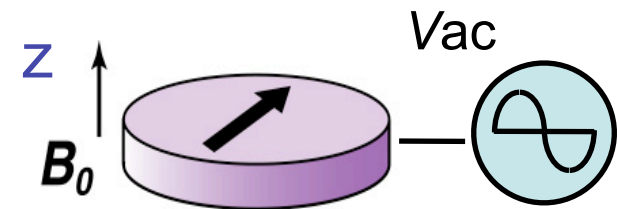
Spin-orbit interaction

V.N. Golovach et al. *PRB* 06 (Theory)

K.C. Nowack *et al.*, arXiv0707.3080

Inhomogeneous hyperfine interaction

Laird *et al.*, arXiv 0707.0557

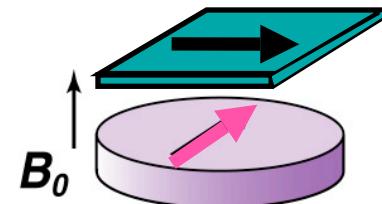


We proposed....

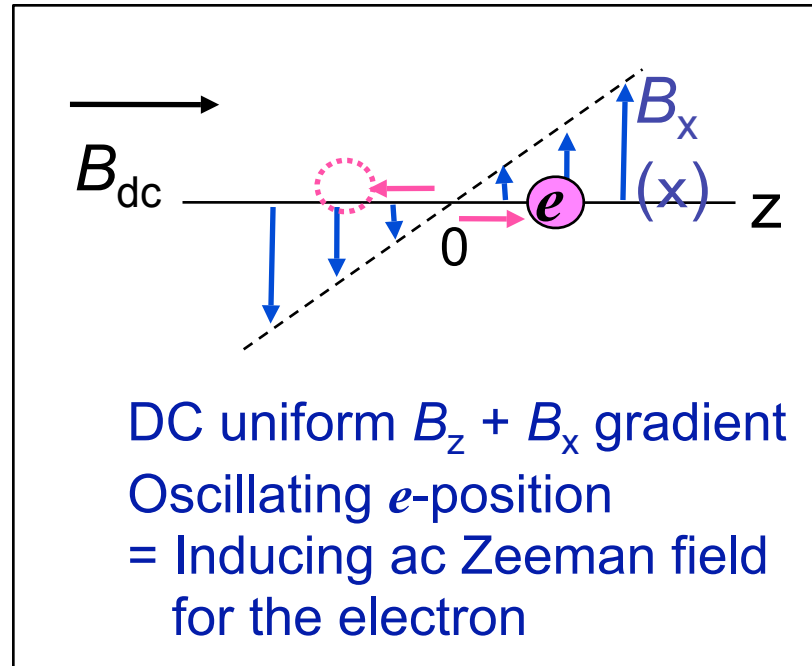
Electron oscillation in a slanting Zeeman field formed by a micro-magnet

Y. Tokura, ST, et al. *PRL* 06 M. Ladriere, ST et al. *APL* 07 (Theory)

Experiment....This talk



ESR in a Slanting Magnetic Field



Proposal:

Y. Tokura, ST PRL 06

M. Pioro-Ladriere, ST APL 07

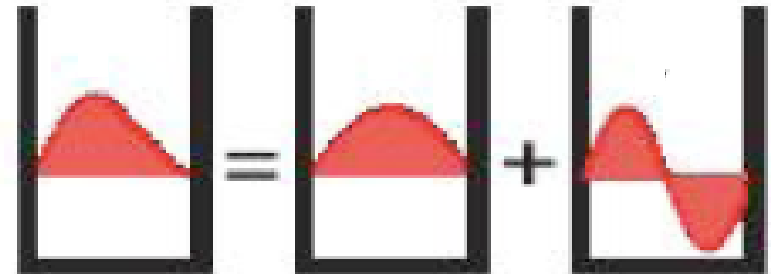
Quantum picture

Up and down quasi-spins

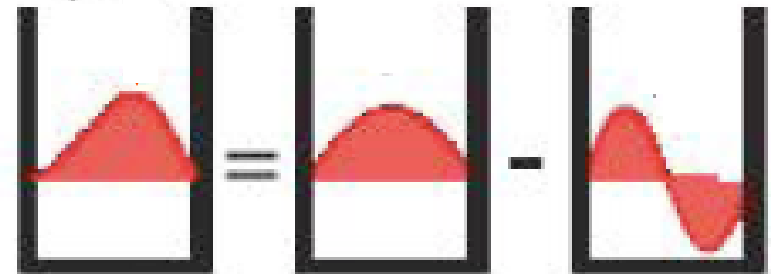
$$|G_{-}\rangle = |1 \uparrow\rangle + C_{1\uparrow}|2 \downarrow\rangle$$

$$|G_{+}\rangle = |1 \downarrow\rangle + C_{1\downarrow}|2 \uparrow\rangle$$

$$|C_1| \ll 1$$



$|+\rangle$

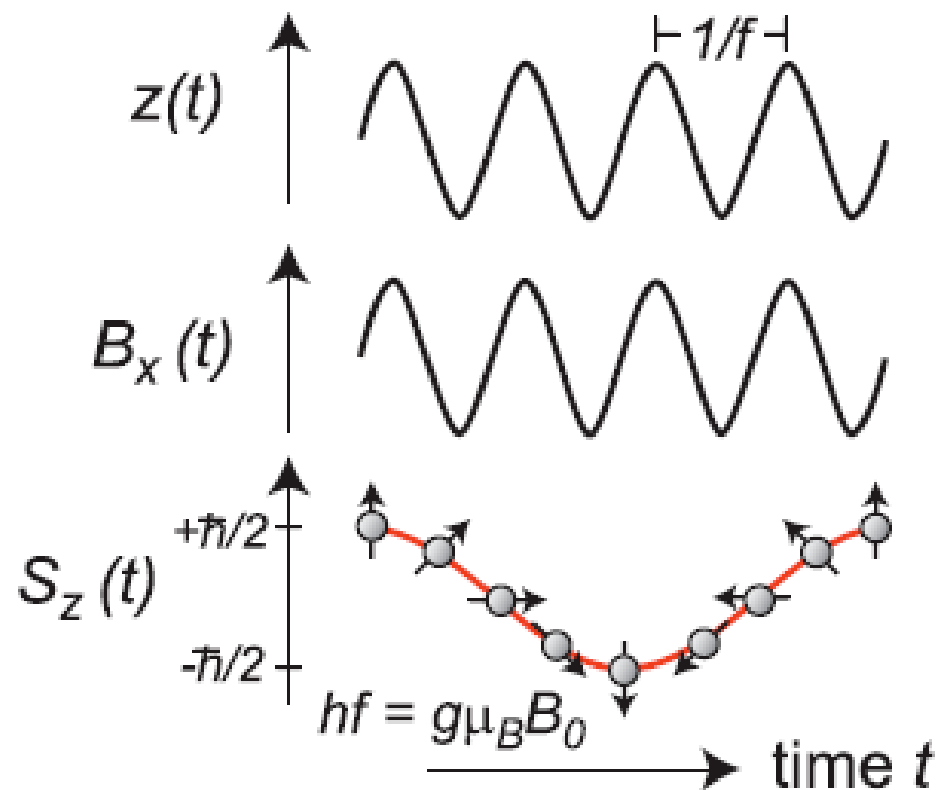
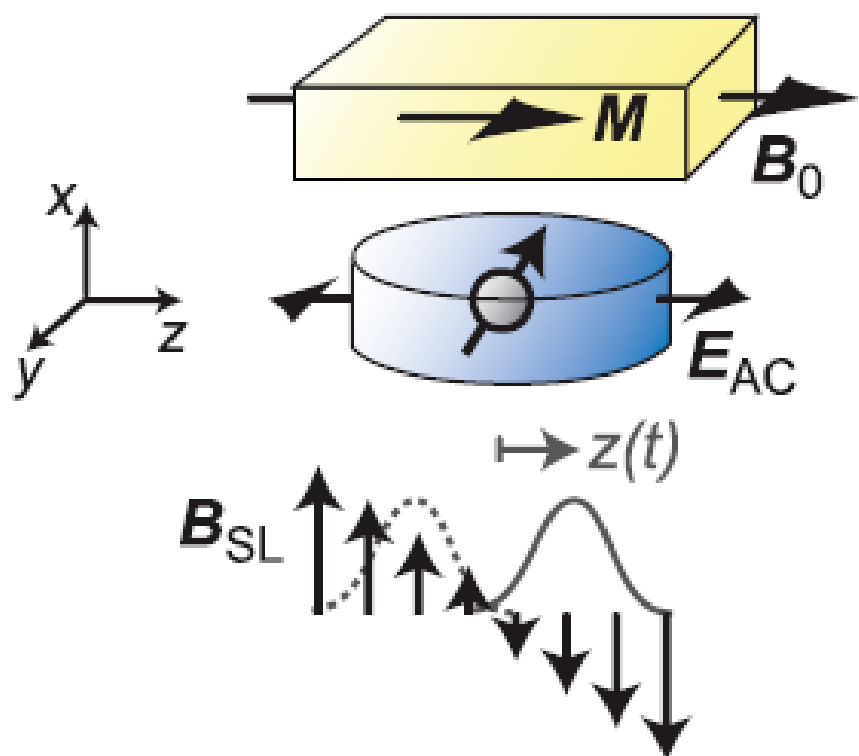


$|-\rangle$

$n=1$

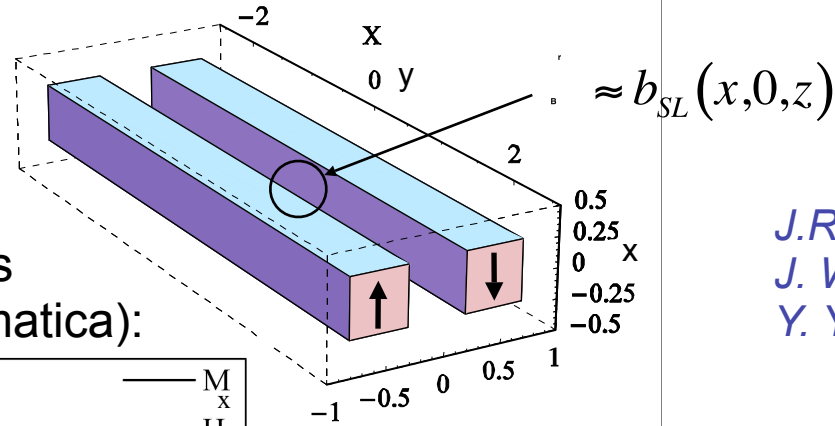
$n=2$

Electron Motion in a Slanting Magnetic Field



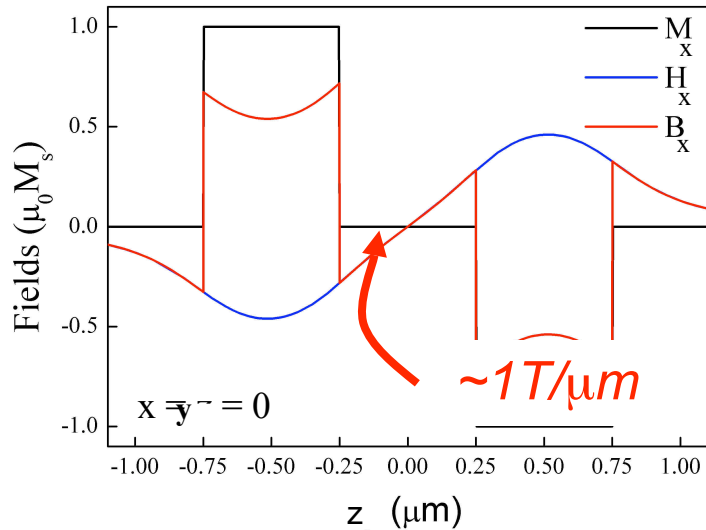
Slanting Field between Ferromagnets

2 permanent magnets (5 mm x 0.5 μm x 0.5 μm)
separated by 0.5 μm gap



J.R. Goldman et al., 2000
J. Wrobel et al., 2004
Y. Yamamoto et al.

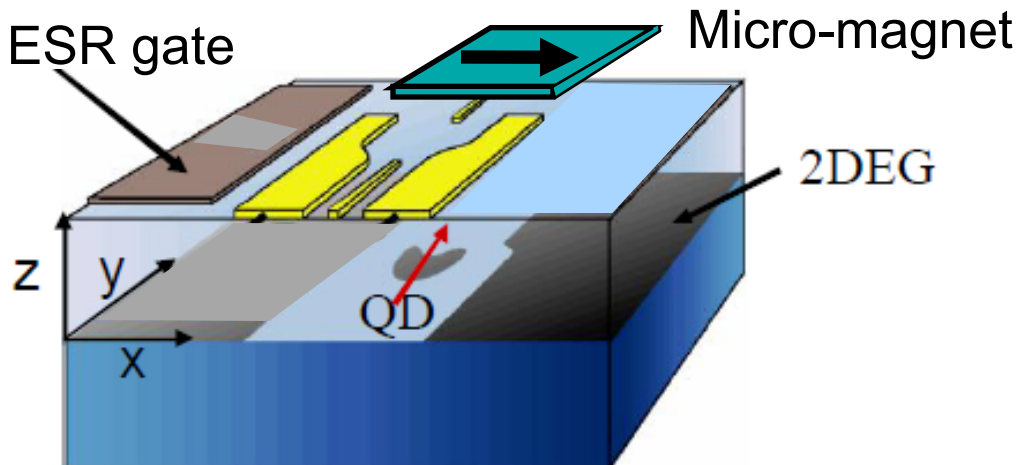
Simulation results
(Radia©+Mathematica):



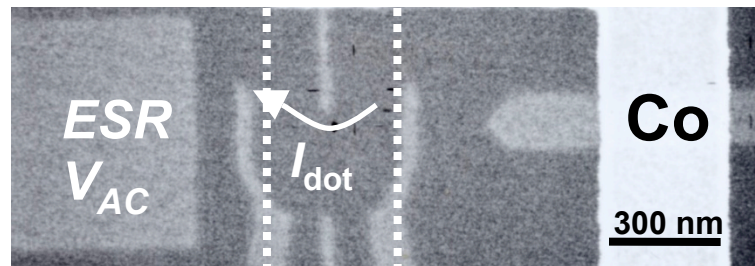
Material	T_C ($^{\circ}C$)	$\mu_0 M_S$ (T)	b_{SL} (T/ μm)
Fe	770	2.19	2.23
Co	1115	1.82	1.86
Py	596	1.70	1.73
Ni	354	0.64	0.65

Dy, Gd,....

Device



$$V_{AC} = V_0 \sin(2\pi ft)$$



❑ Few-electron lateral QD

Isolation of single electrons

M. Ciorga *et al.*, PRL **88** 256804 (2002)

❑ Pauli spin blockade

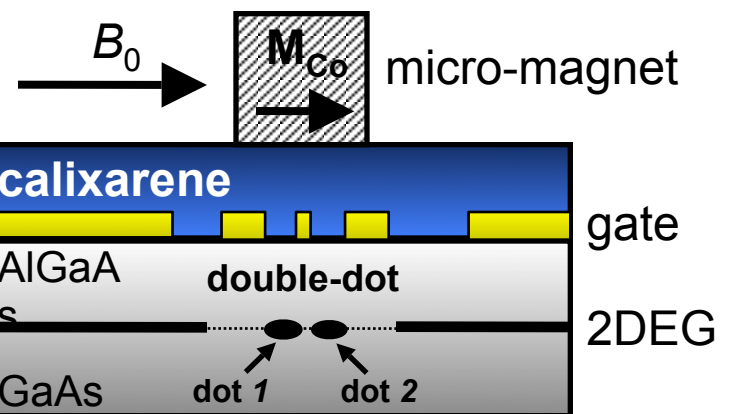
ESR detection

Koppens *et al.* Nature **442** 766 (2006)

❑ ESR gate

AC electric field E_{AC}

MPL *et al.* APL **90** 024105 (2007)



Stray Magnetic Field Profile: Simulation

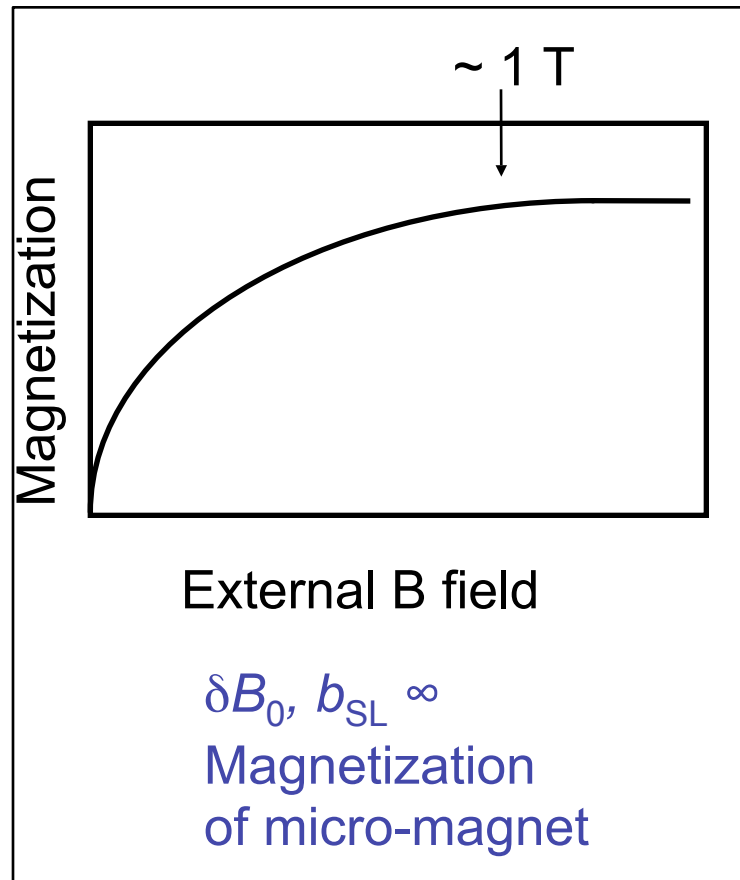
Static Zeeman field: $B_0 + \delta B_0$

→ Shift of f_{ESR} In the low B_0 range

Slanting Zeeman field: b_{SL}

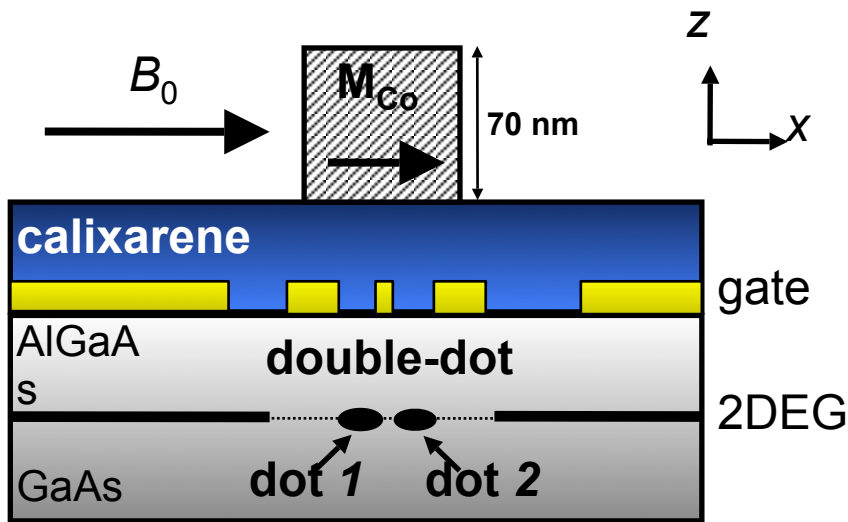
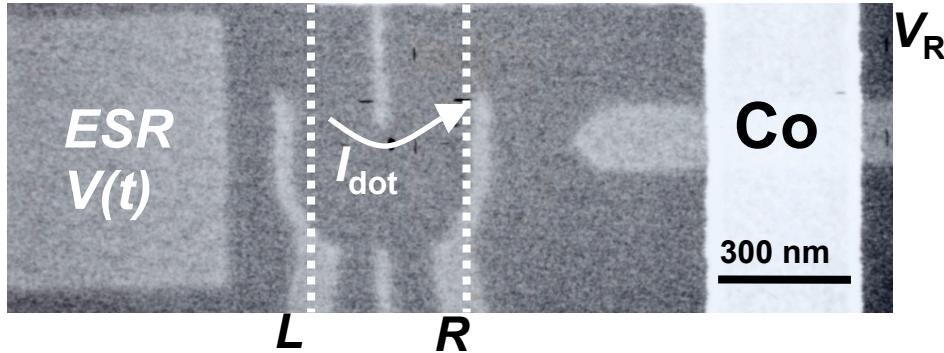
→ Change of I_{ESR}

Stray field of micro-magnet



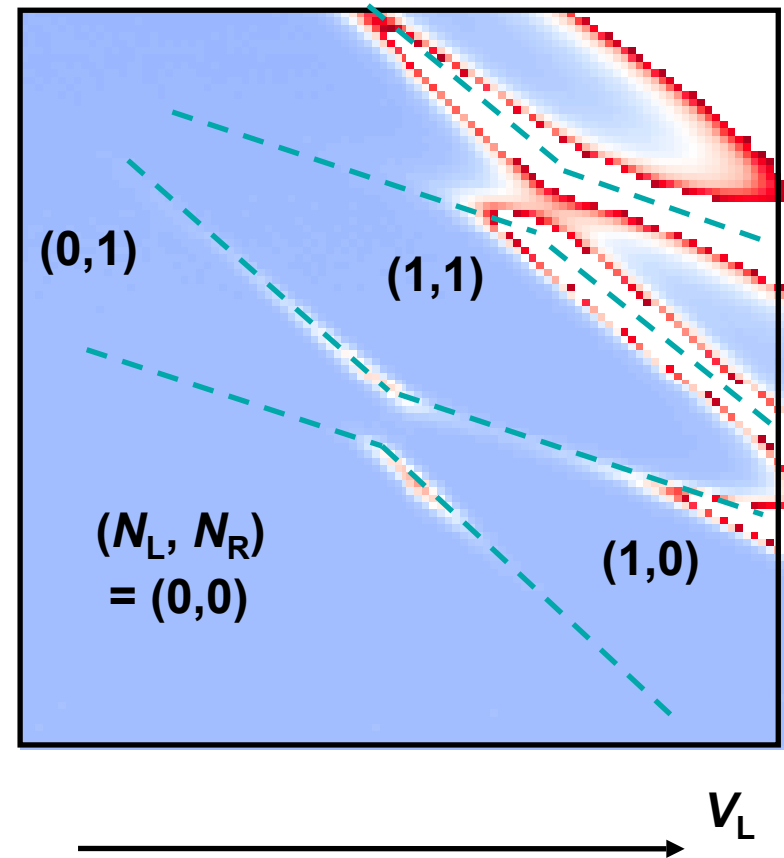
Formation of Double Quantum Dot

$$V(t) = V_0 \sin(2\pi f t)$$



Dot 1: Target Dot 2: Detector

By adjusting two side gate voltage, A double quantum dot is formed.



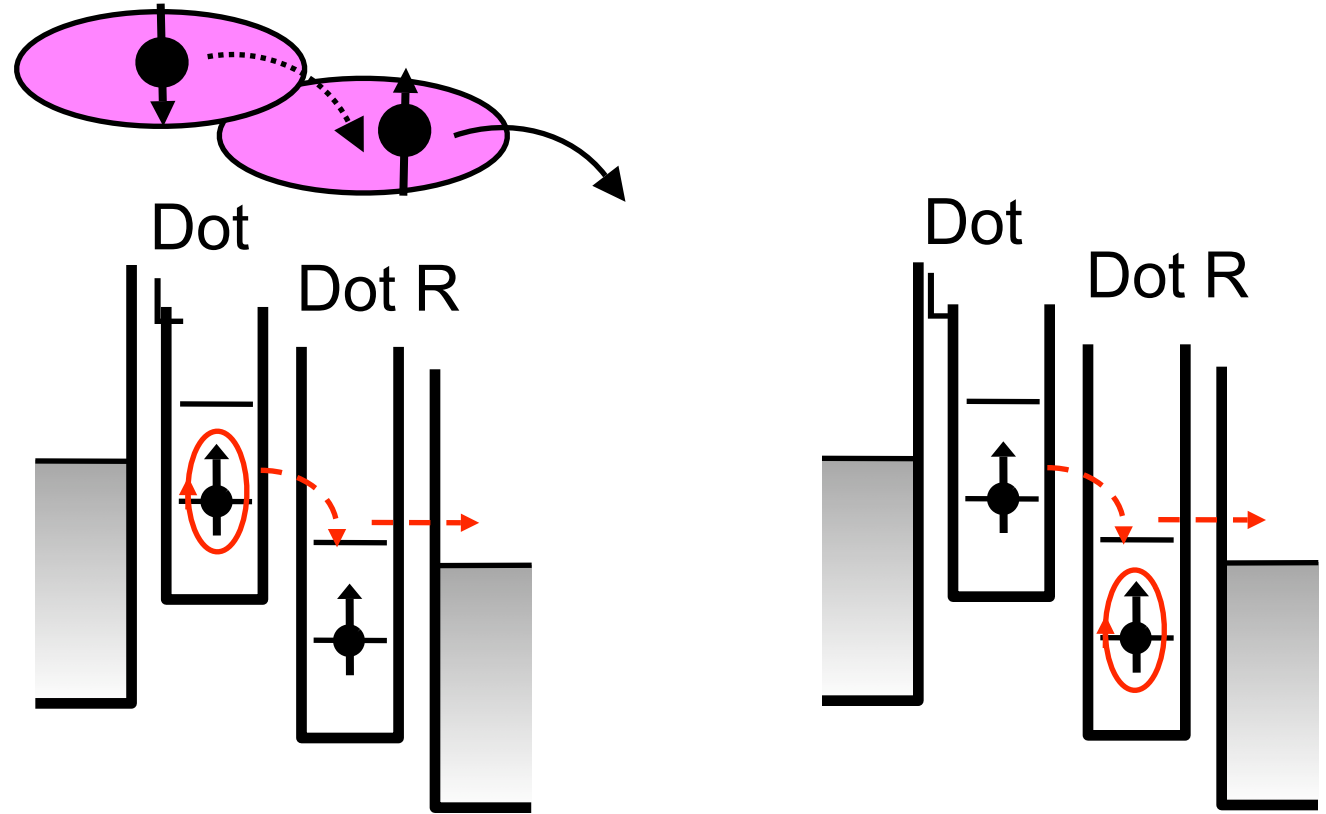
Three contributions coexist...

$$B_{\text{ESR}} = B_{\text{Slant}} + B_{\text{Hyper}} \pm B_{\text{SO}}$$

\pm : depending on crystal orientation)

They have different dependencies on B_{ext} and E_{ext} .
....can be distinguished

Two Spins in a Displaced Ferro-magnet



If stray field from micro-magnet

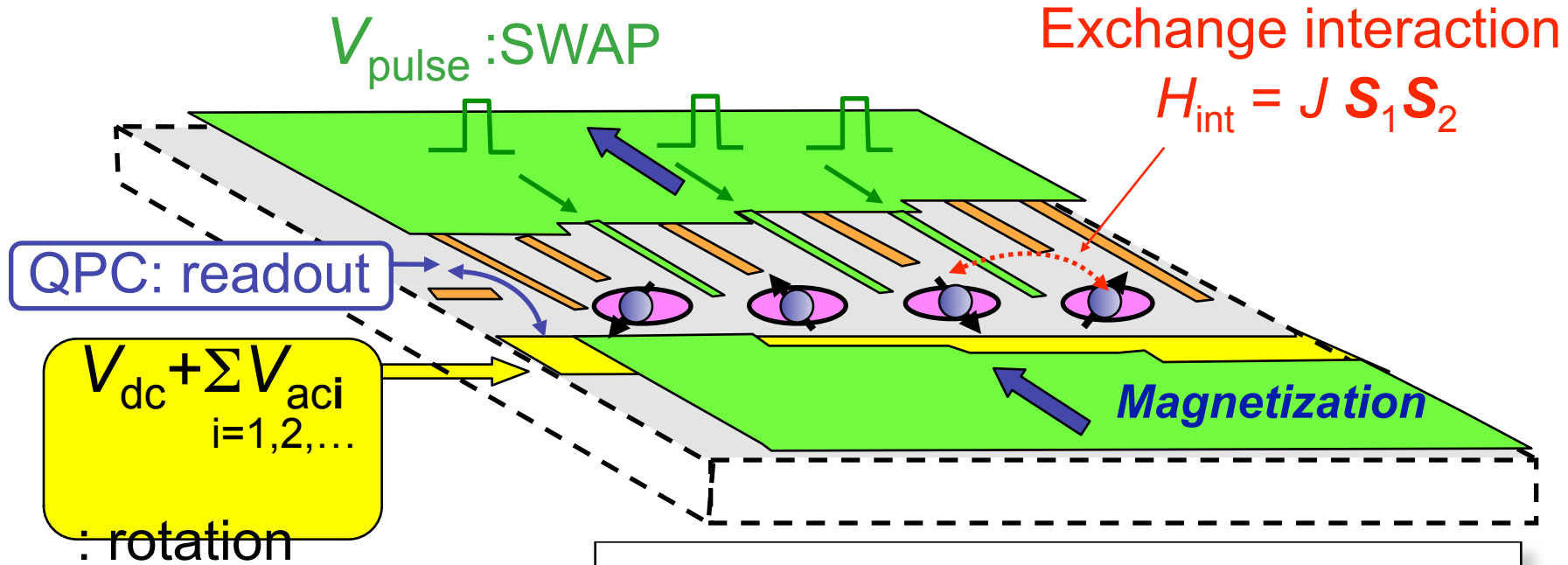
$$|\delta B_0(\text{Dot L})| > |\delta B_0(\text{Dot R})|$$

The
n $f_{\text{ESR}}(\text{Dot L}) < f_{\text{ESR}}(\text{Dot R})$

$$\Delta f > 1/T_2^*$$

Address two spins
at two different f_{ESR} s

Micro-magnet Design for Scalability



$hf_i = E_{\text{Zeeman}}^i$ for V_{aci}
 Local Zeeman energy
 $E_{\text{Zeeman}}^i = g\mu_B B_0^i$

.... V_{ac} frequency mixing

$\Delta f_{\text{ESR}} = 10 \text{ MHz} > 1/T_2^*$ \Rightarrow 100 qubits with $\Delta d \sim 3 \text{ nm}$

δB_0 in the range of 200 mT = 1.2 GHz for $d = 0.1$ to $0.4 \mu\text{m}$

Micro-magnet

Nuclear Spin Effect

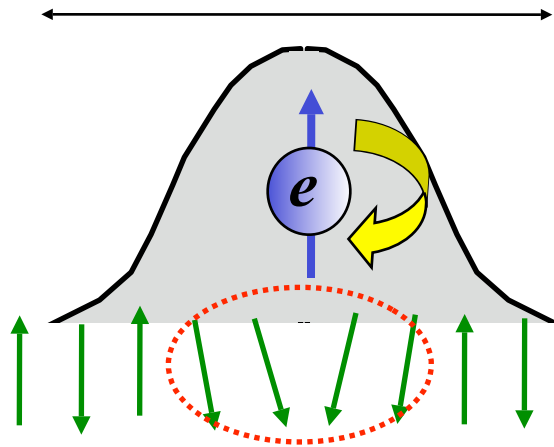
Hyperfine coupling

$$H_{\text{HF}} = A|\psi(x)|^2 \left(\frac{I_+ S_- + I_- S_+}{2} + I_z S_z \right)$$

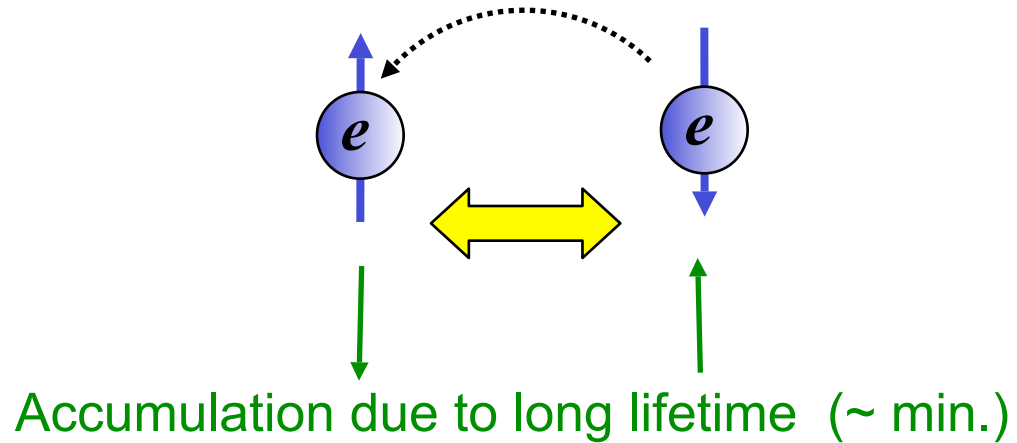
Flip-flop Recovery due to short lifetime

GaAs quantum dot

50 nm



$10^5 \sim 10^6$ nuclei in QD



→ Dynamical nuclear spin polarization, which imposes an extra magnetic field on the electronic spin
.....Overhauser effect

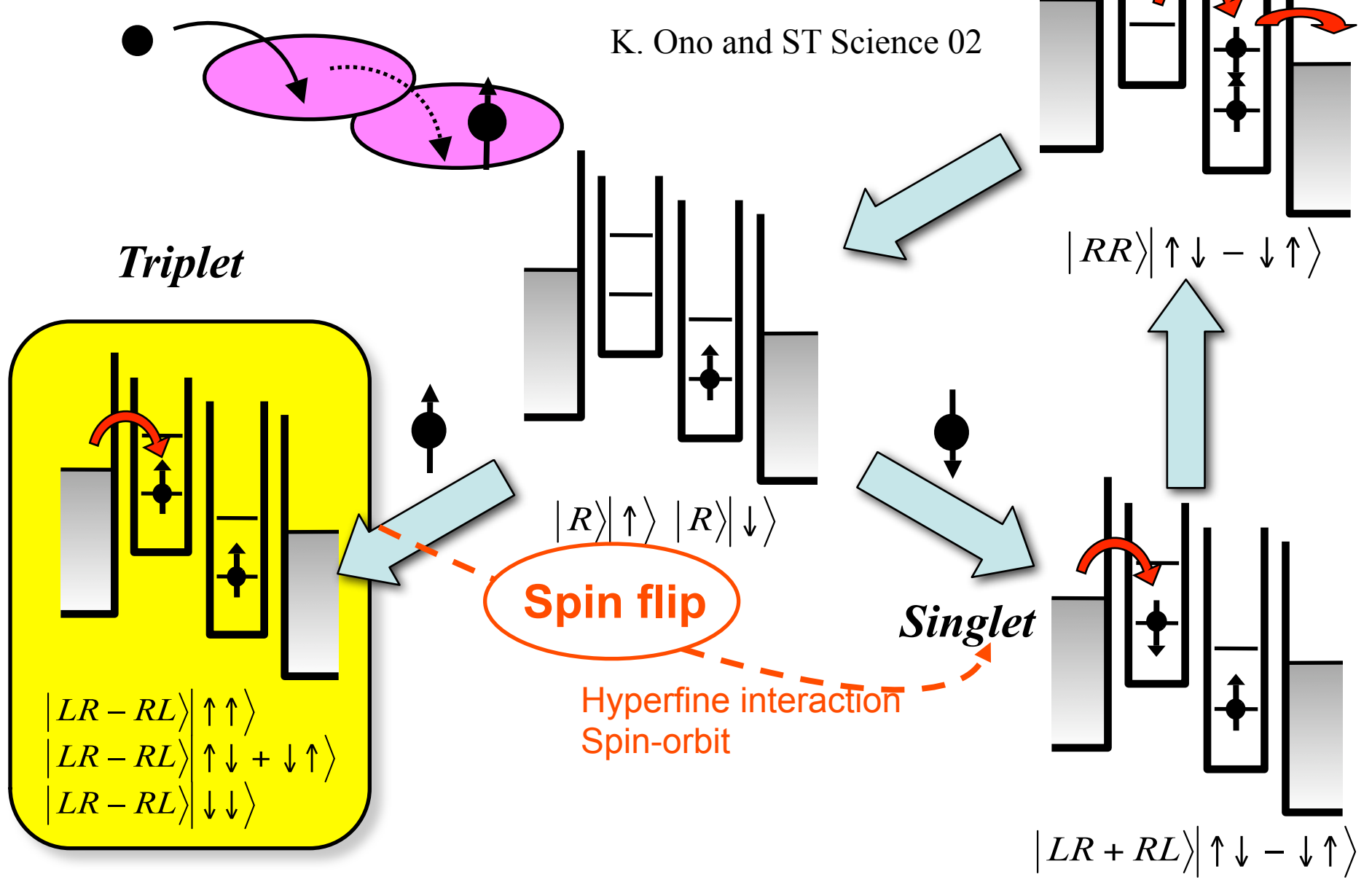
Nuclear spin polarization up to ~60 %

J. Baugh, ST... PRL 07

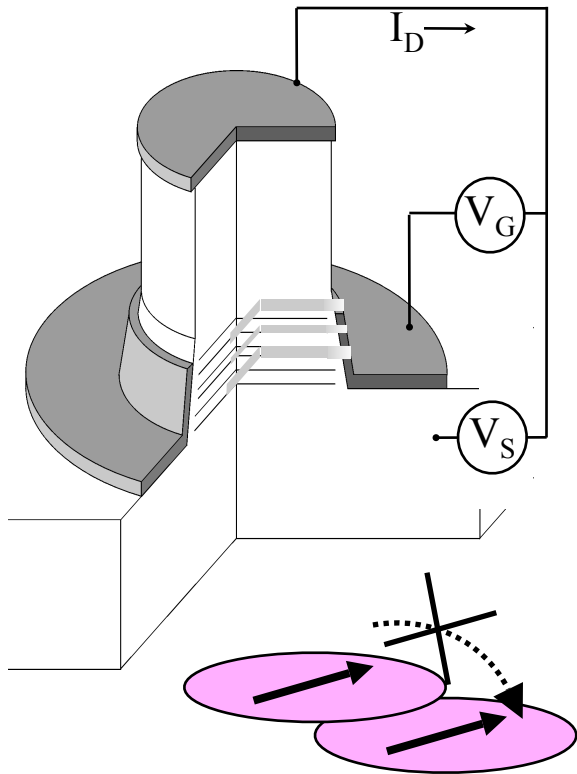
→ Can be observed as lifting of Pauli spin blockade

Formation of Spin Triplet and P-SB

K. Ono and ST Science 02



Pauli Spin Blockade in Double QD



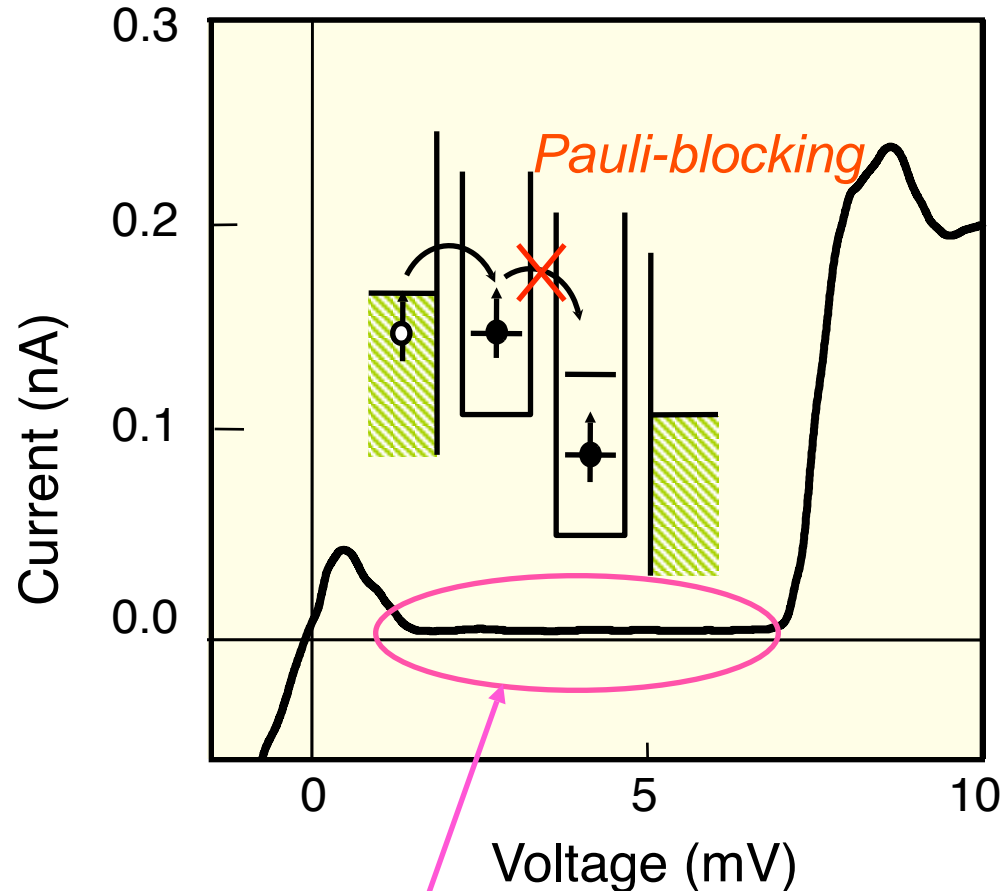
$D \sim 30 \text{ nm}$

$N \approx 10^5$

Laterally coupled dots

Johnson et al. *Nature* 05

Koppens et al. *Science* 05



Voltage (mV)

Ono and ST, *Science* 02

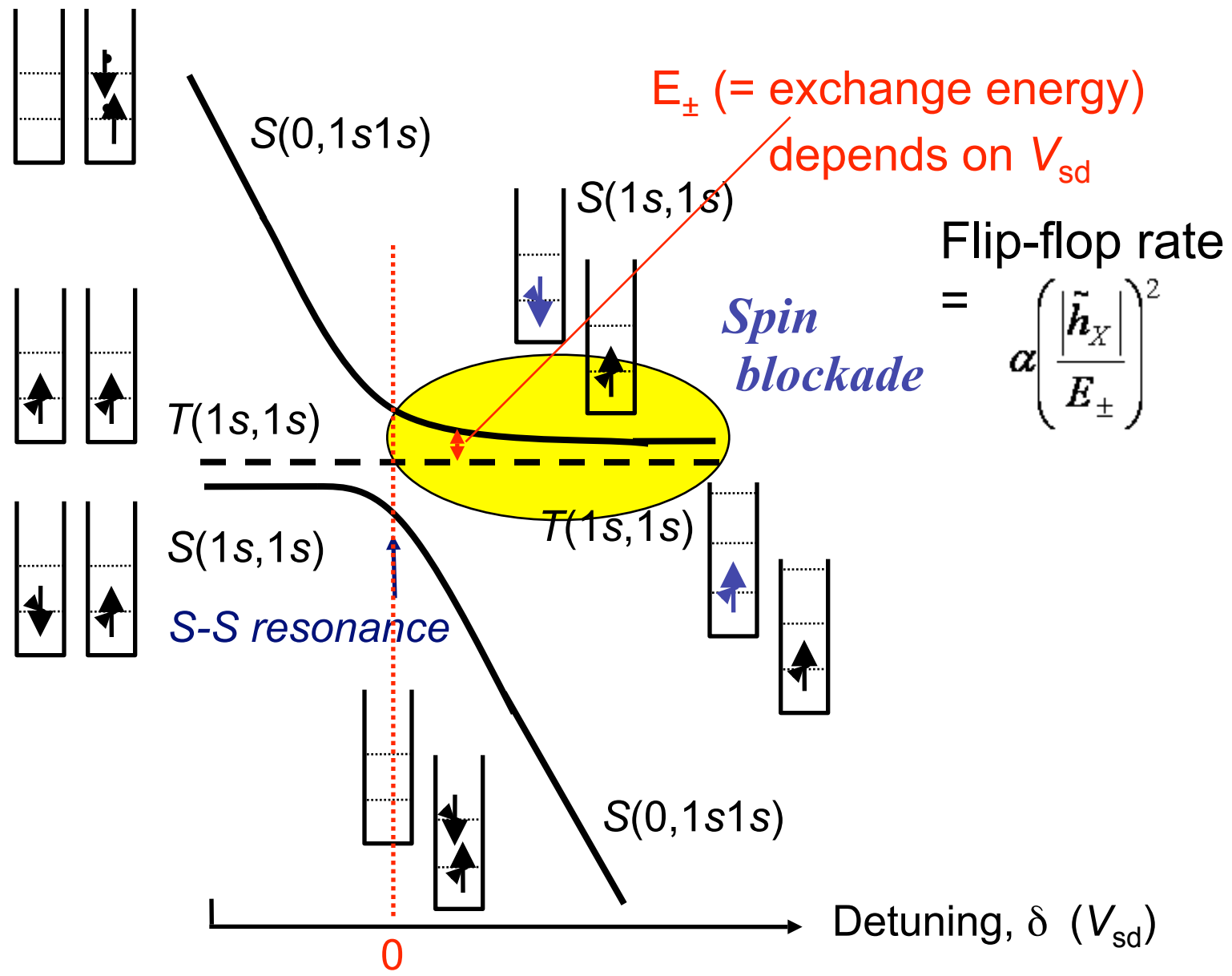
PRL 04

Can be lifted by coupling to nuclear spin

GaAs QD:

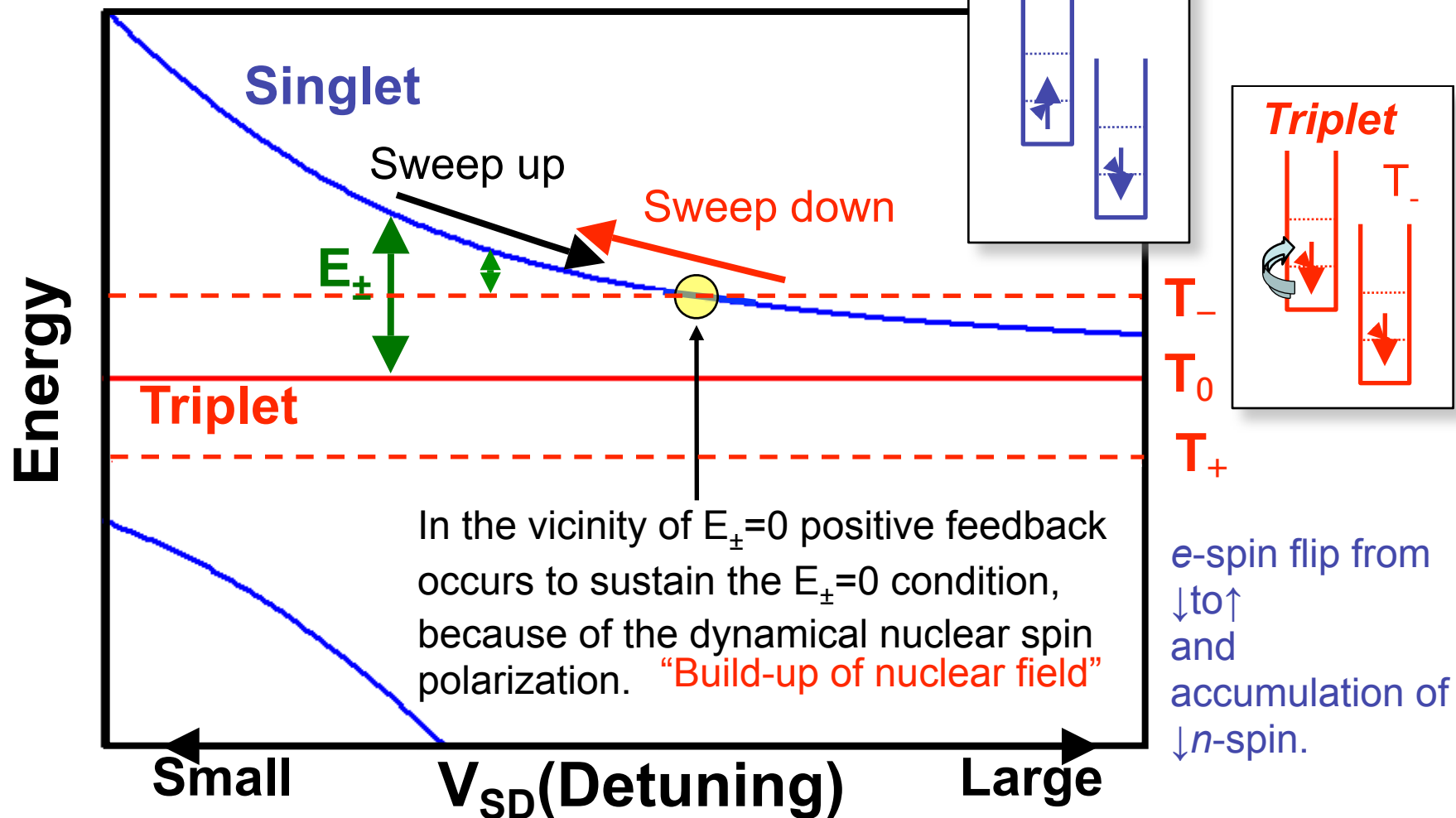
^{71}Ga , ^{69}Ga , ^{75}As : $I=3/2$

How to electrically control hyperfine coupling



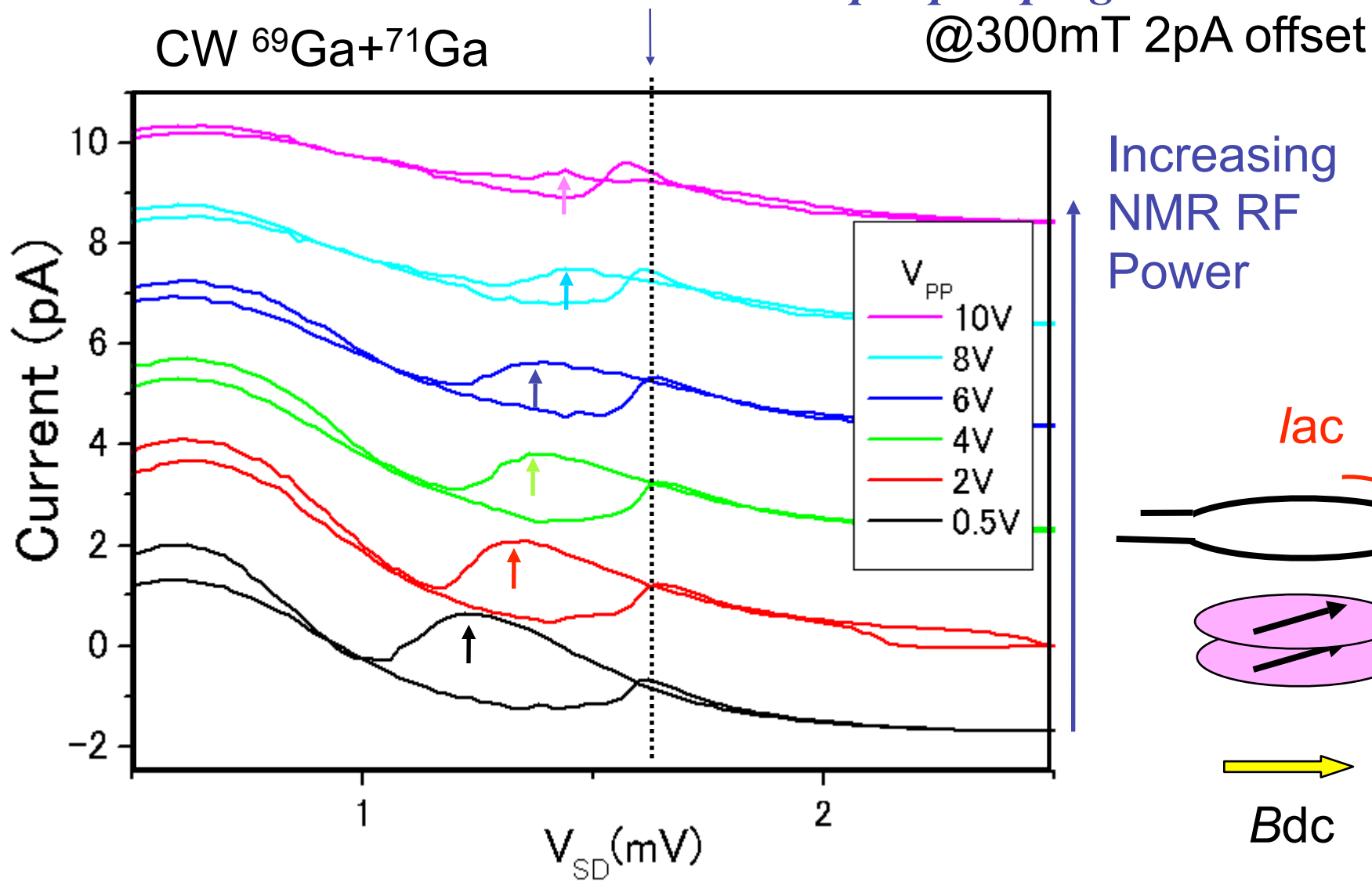
How to control nuclear spin coupling

Apply a fixed B_{ext} field and sweep V_{sd}



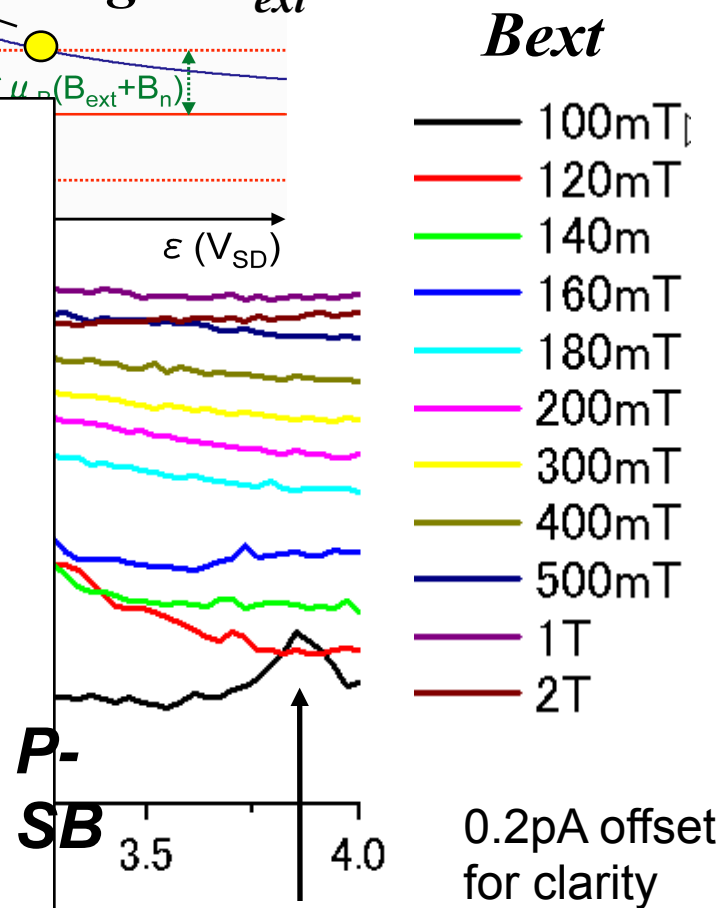
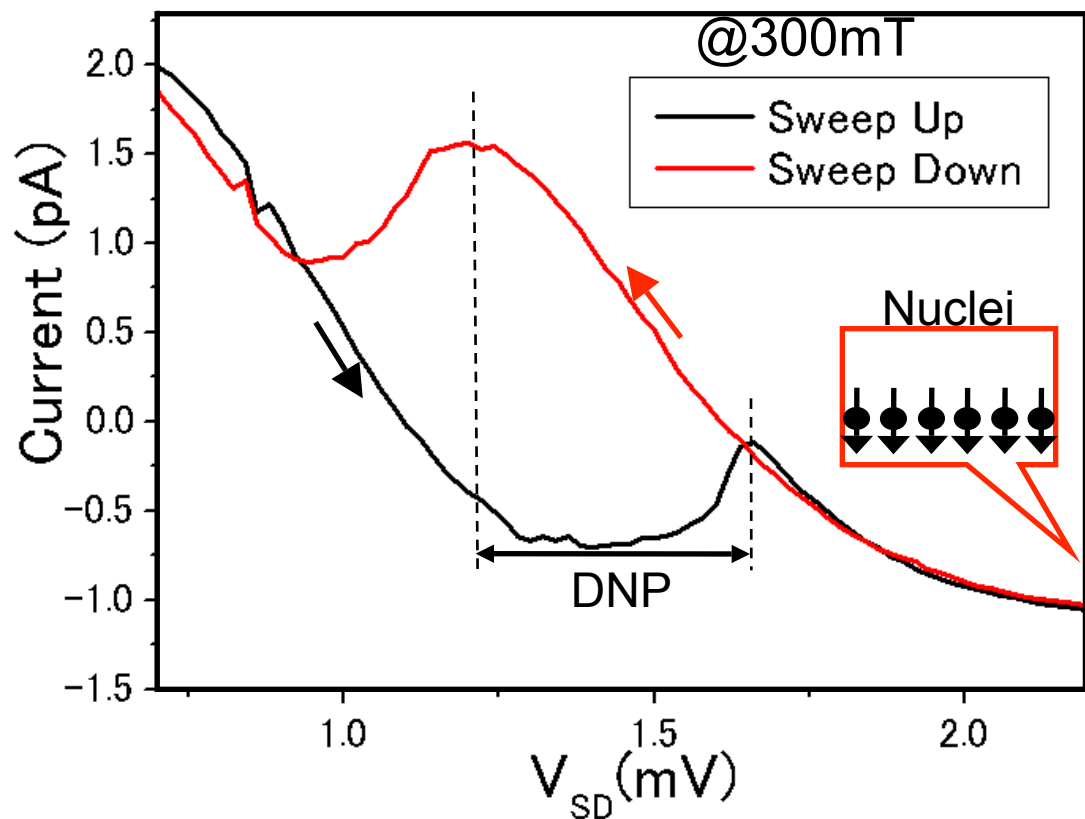
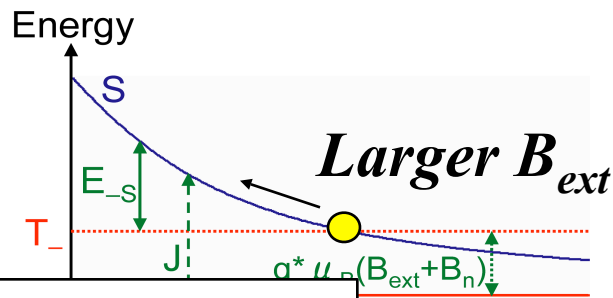
Nuclear Spin Depolarization by CW NMR RF

Hysteresis=DNP? ← Test using NMR to depolarize the nuclei
Weak nuclear spin pumping



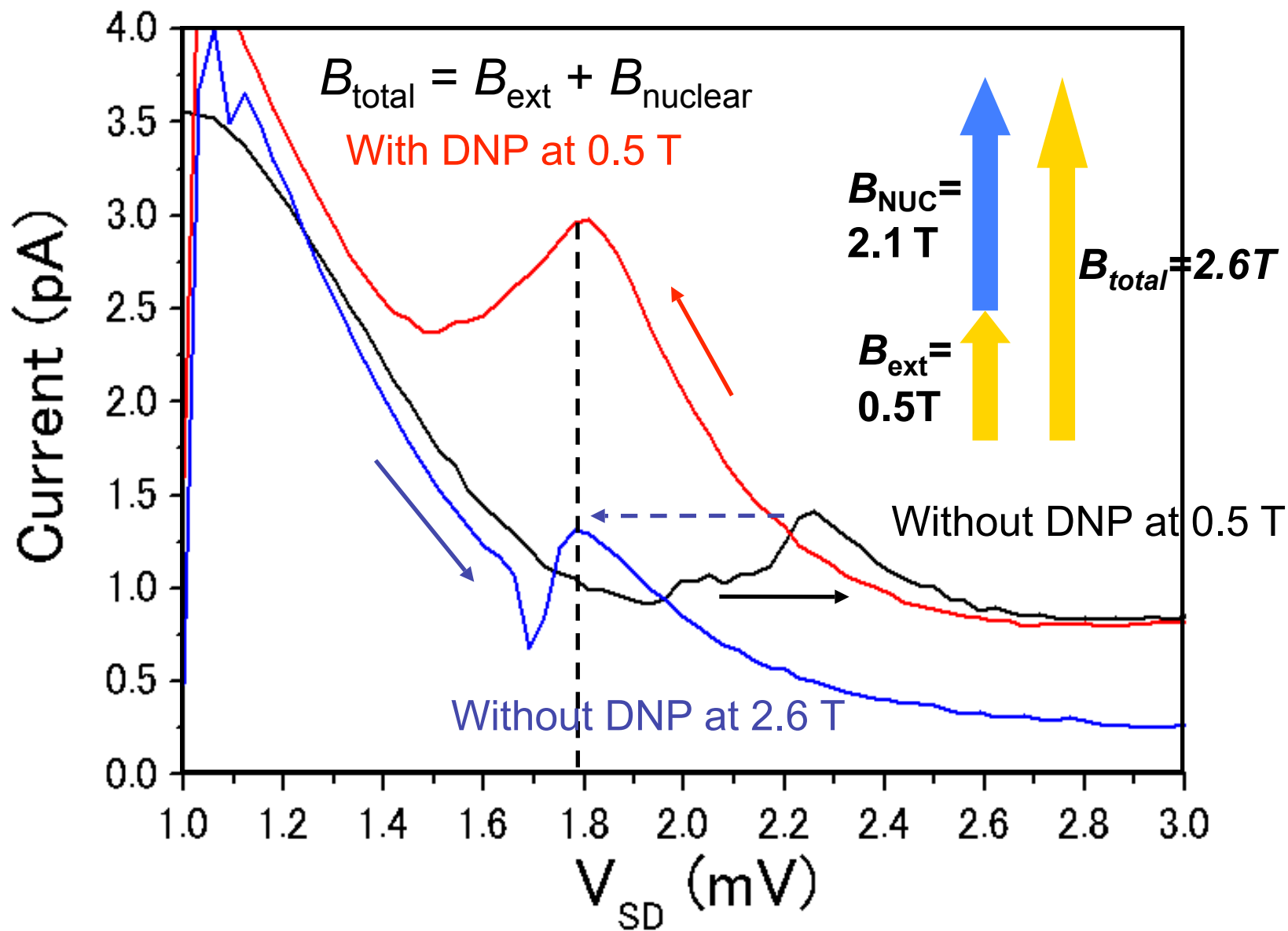
$|T_-\rangle$ - $|S\rangle$ Degeneracy Depending on B_{ext}

Current in the P-SB

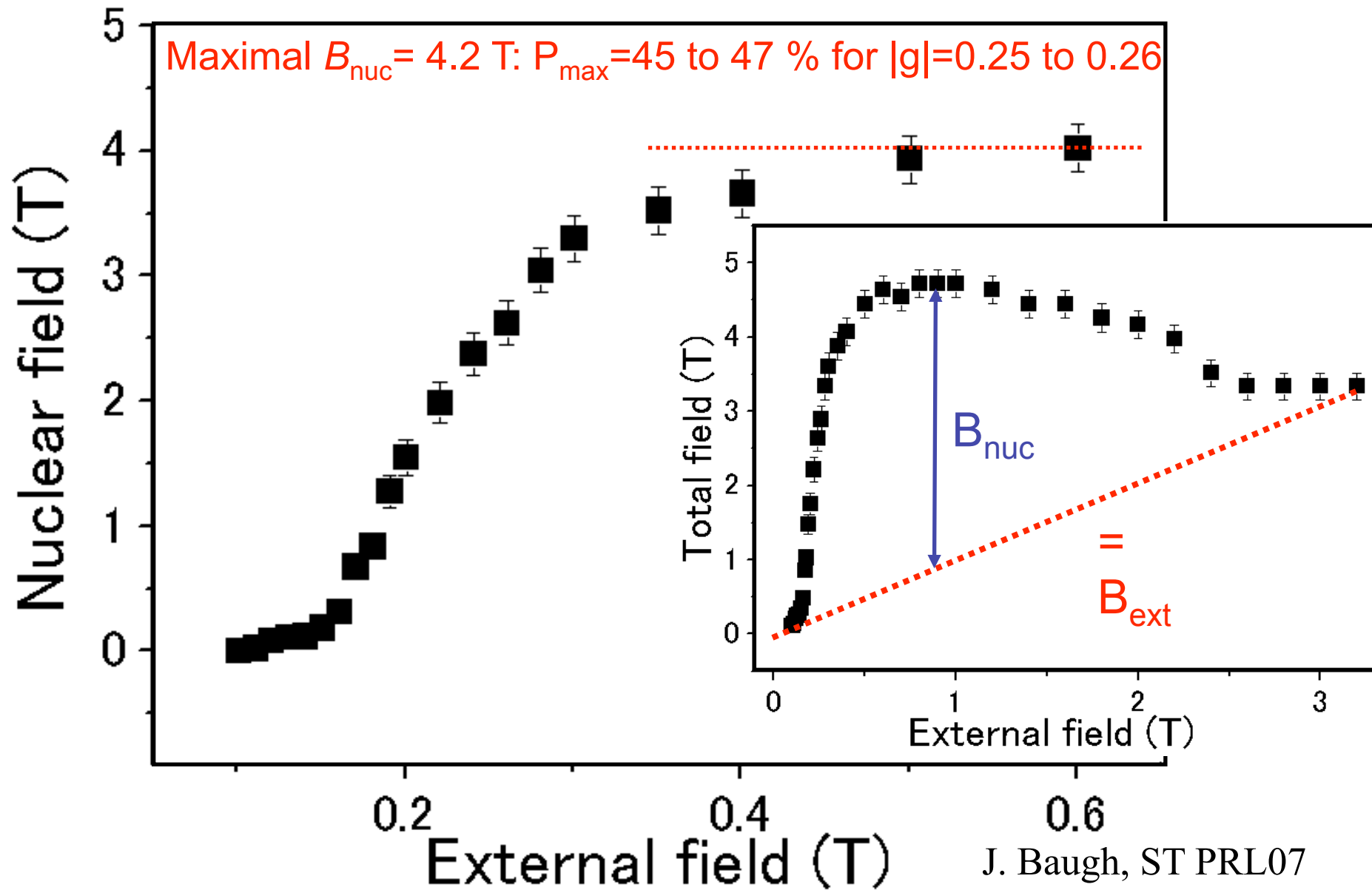


Lifting of P-SB by V_{sd} induced $|T_-\rangle = |S\rangle$

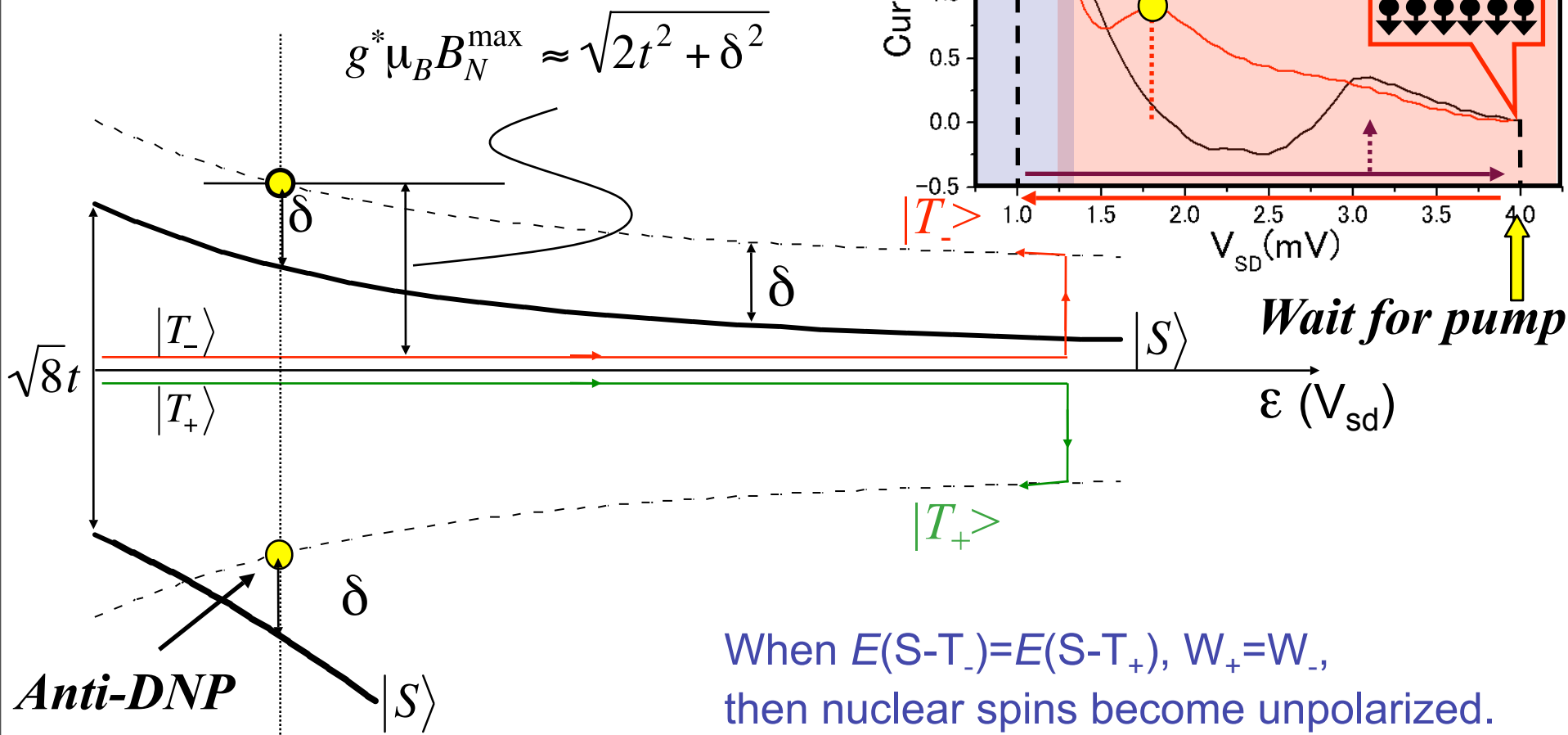
Nuclear Field due to DNP



Control of Nuclear Spin Polarization



Approach to full polarization (simple picture)



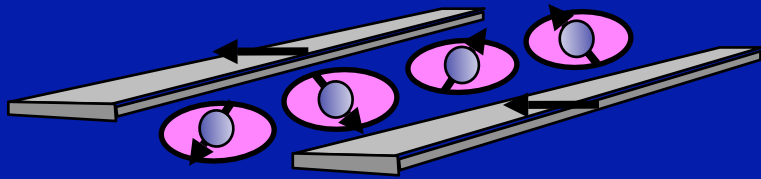
$B_N^{\max} \sim 10T$ (full polarization) for $t \sim 70\mu eV$

$t \gg \delta$

Conclusion

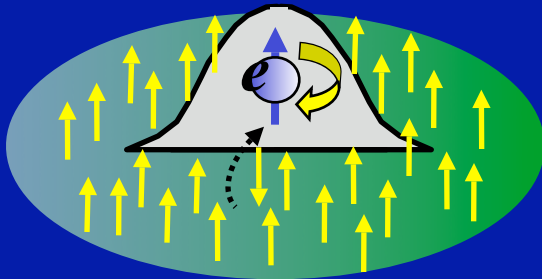
Voltage-driven single spin resonance

using a slanting Zeeman field



- Developed a spin resonance technique with QDs using a micro-magnet
- Demonstrated two-spin addressing, which can provide a technique for multiple qubit operation ... good for scalability

Electrical control of dynamical nuclear polarization



- Demonstrated tunable polarization from 0 to ~50 %, using a voltage-controlled exchange coupling and Pauli spin-blockade
- Discussed a possible approach for full polarization