

PS-B-1

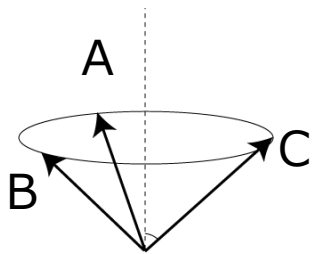
# Spin-chirality ordering and kinetic-driven effective interactions in geometrically-frustrated ferromagnetic Kondo-lattice systems

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# Unconventional anomalous Hall Effect

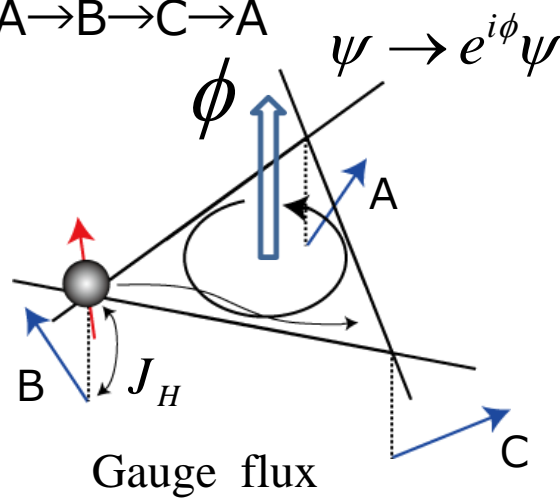
Spin configuration with a finite solid angle



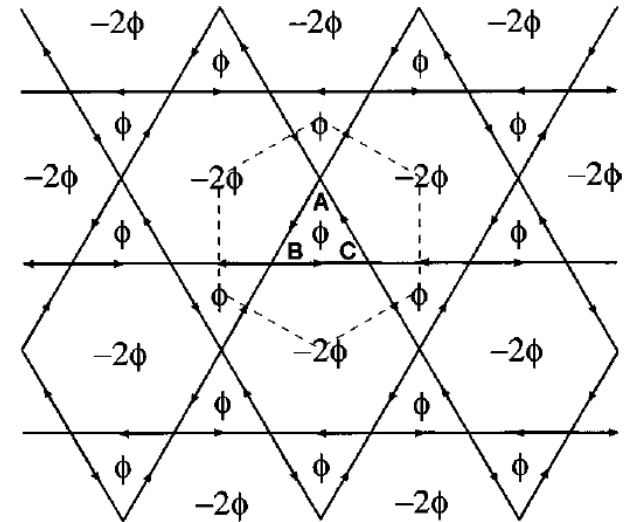
Scalar chirality

$$\vec{S}_A \cdot (\vec{S}_B \times \vec{S}_C)$$

Berry phase from electron hopping  
 $A \rightarrow B \rightarrow C \rightarrow A$



Distribution of flux on a kagome lattice



finite scalar chirality



Berry phase  
 (effective magnetic field that electron feels)



Unconventional Anomalous Hall Effect



K. Ohgushi, S. Murakami, and N. Nagaosa, Phys. Rev. B **62**, R6065 (2000).

R. Shindou and N. Nagaosa, Phys. Rev. Lett. **87**, 116801 (2001).

I. Martin and C. D. Batista, Phys. Rev. Lett. **101**, 156402 (2008).

# Motivation

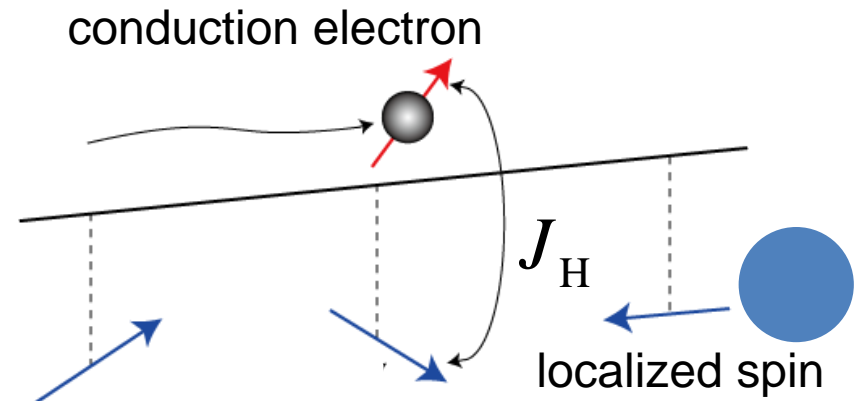
In the previous theories, the noncoplanar chiral order is given by hand.  
(Spin pattern is not affected by the electron motion.)

However, in the spin-charge coupled systems,  
electronic state and magnetic state are self-consistently  
determined to optimize the free energy.

- To clarify whether the chiral ordering is stabilized in the spin-charge coupled systems by examining the ground state phase diagram
- To clarify the stabilization mechanism of the chiral ordering

Ferromagnetic Kondo lattice model

$$H = -t \sum_{\langle i,j \rangle, \alpha} c_{i\alpha}^\dagger c_{j\alpha} - J_H \sum_{i, \alpha, \beta} \vec{S}_i \cdot c_{i\alpha}^\dagger \vec{\sigma}_{\alpha\beta} c_{i\beta}$$

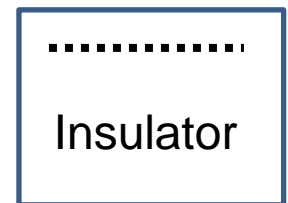
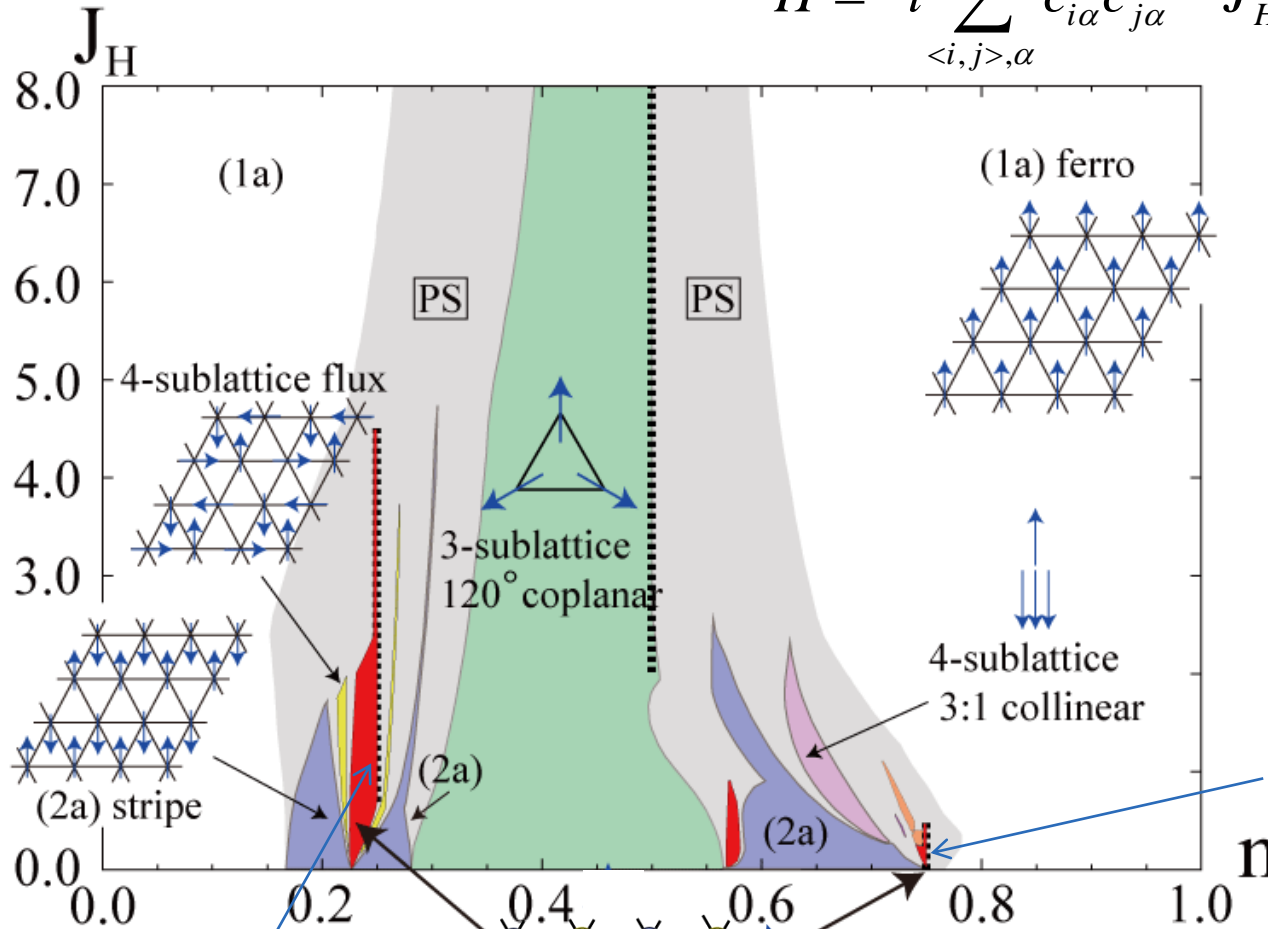


# Ground state phase diagram on triangular lattice

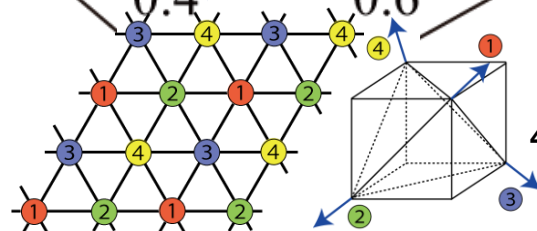
Ferromagnetic Kondo lattice model (=double-exchange model)

$$H = -t \sum_{\langle i,j \rangle, \alpha} c_{i\alpha}^\dagger c_{j\alpha} - J_H \sum_{i, \alpha, \beta} \vec{S}_i \cdot c_{i\alpha}^\dagger \vec{\sigma}_{\alpha\beta} c_{i\beta}$$

$\vec{S}_i$  : classical spin



new chiral phase!



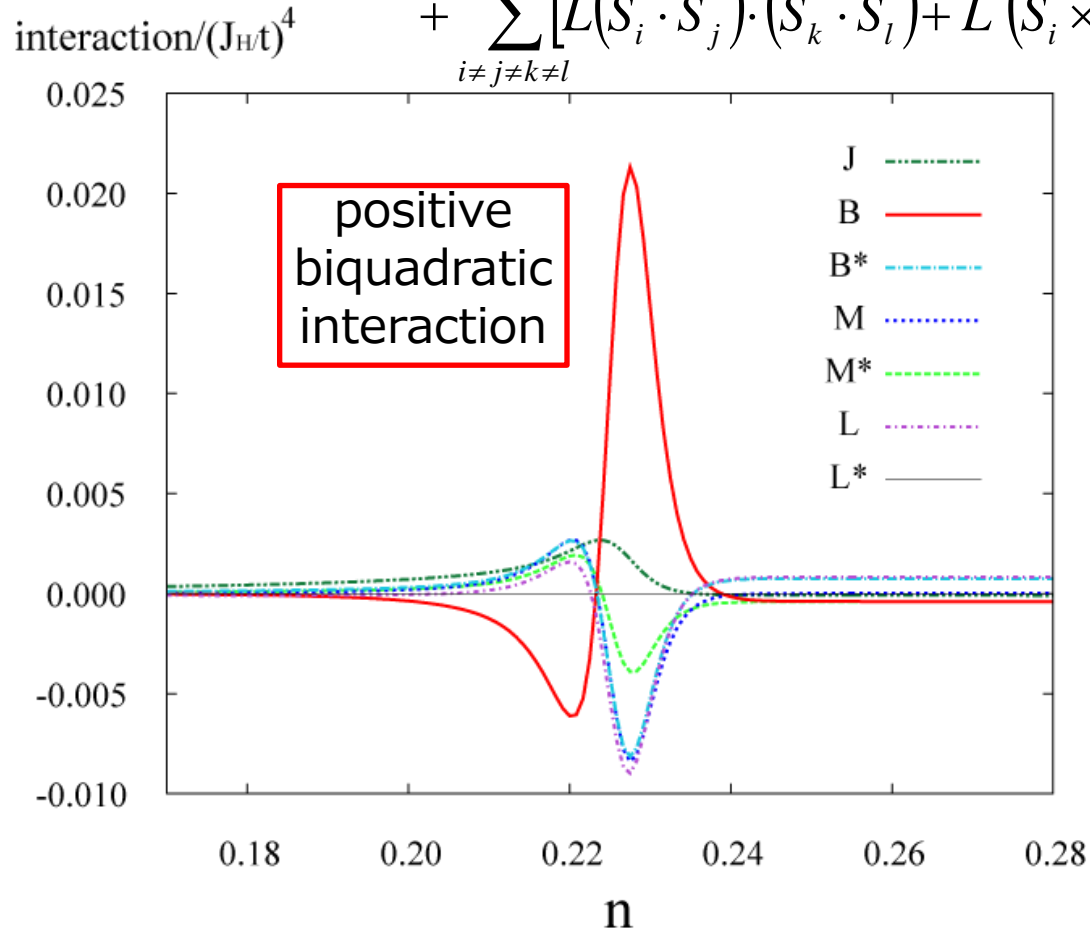
perfect nesting driven chiral phase

I. Martin and C. D. Batista, 2008

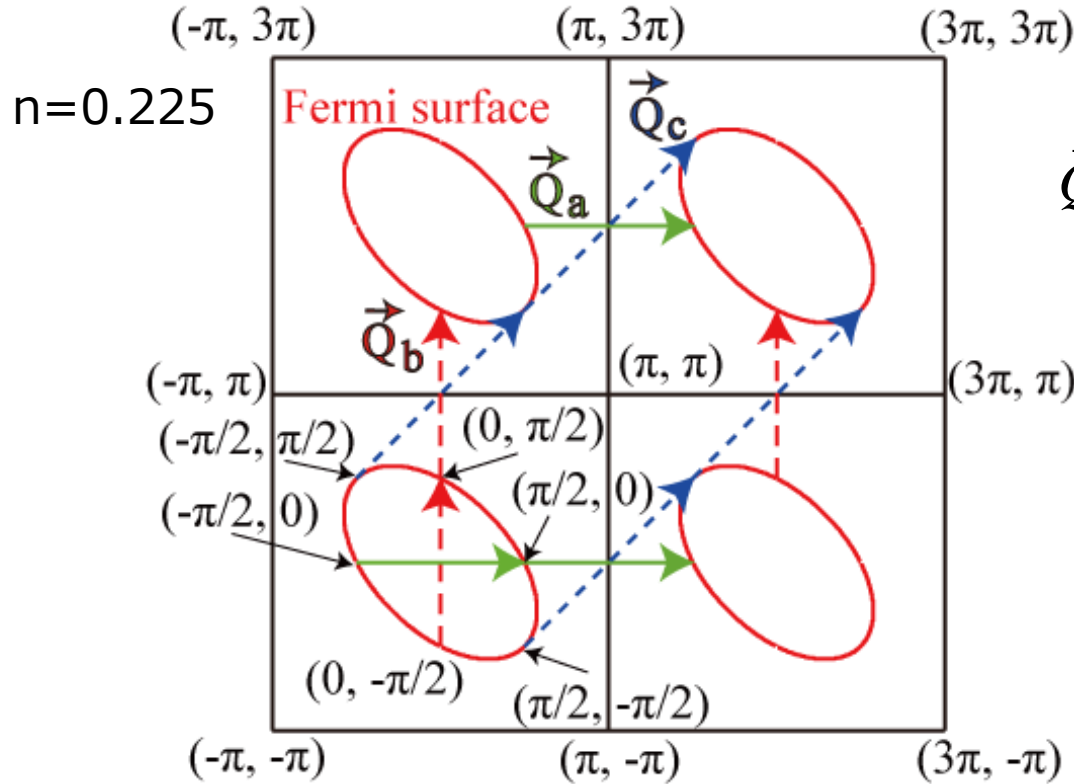


# Effective Hamiltonian (4th order perturbation in $J_H/t$ )

$$\begin{aligned}
 H_{eff}^{(4)} / (J_H / t)^4 = & \sum_{1 \leq i < j \leq 4} \left[ J \vec{S}_i \cdot \vec{S}_j + \underline{B (\vec{S}_i \cdot \vec{S}_j)^2} + B^* (\vec{S}_i \times \vec{S}_j)^2 \right] \\
 & + \sum_{i \neq j \neq k} \left[ M (\vec{S}_i \cdot \vec{S}_j) (\vec{S}_i \cdot \vec{S}_k) + M^* (\vec{S}_i \times \vec{S}_j) \cdot (\vec{S}_i \times \vec{S}_k) \right] \\
 & + \sum_{i \neq j \neq k \neq l} \left[ L (\vec{S}_i \cdot \vec{S}_j) \cdot (\vec{S}_k \cdot \vec{S}_l) + L^* (\vec{S}_i \times \vec{S}_j) \cdot (\vec{S}_k \times \vec{S}_l) \right]
 \end{aligned}$$

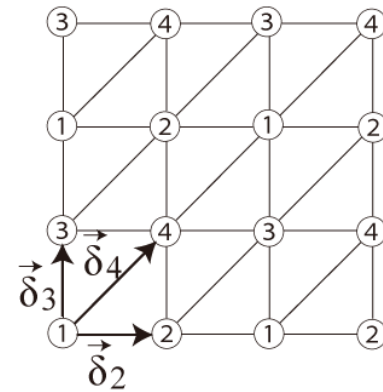


# Origin of positive biquadratic interaction



$\vec{Q}_a, \vec{Q}_b, \vec{Q}_c$  : 4-sublattice ordering wave vectors

triangular lattice



**Fermi surface connection**

cf. Kohn anomaly

Our topics

- ground-state phase diagram with scalar chiral ordering
- positive biquadratic interaction in the fourth-order perturbation
- higher-order Kohn anomaly by Fermi surface connection