

$$\alpha_{EM} = \frac{e^2}{4\pi} \longrightarrow \alpha = G_N M_{\text{BH}} \mu_a = R_g \mu_a$$