

$$\omega_{\text{axion}} < m_{\Omega_+}$$