

$$\frac{M_{\text{cloud}}}{M_{\text{BH}}} \sim \frac{f_a^2}{M_{\text{Planck}}^2} \frac{l^2}{a^2} \sim 10^{-4}$$