



鉄系超伝導

Iron-based superconductor --- an overview

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My talk today

- ➡ A brief introduction for the iron-based SC
- ➡ Mechanism for $s \pm$ pairing
- ➡ Material-dependence ($s \pm \Leftrightarrow d$)
- ➡ Collective (phase) modes in multiband SC

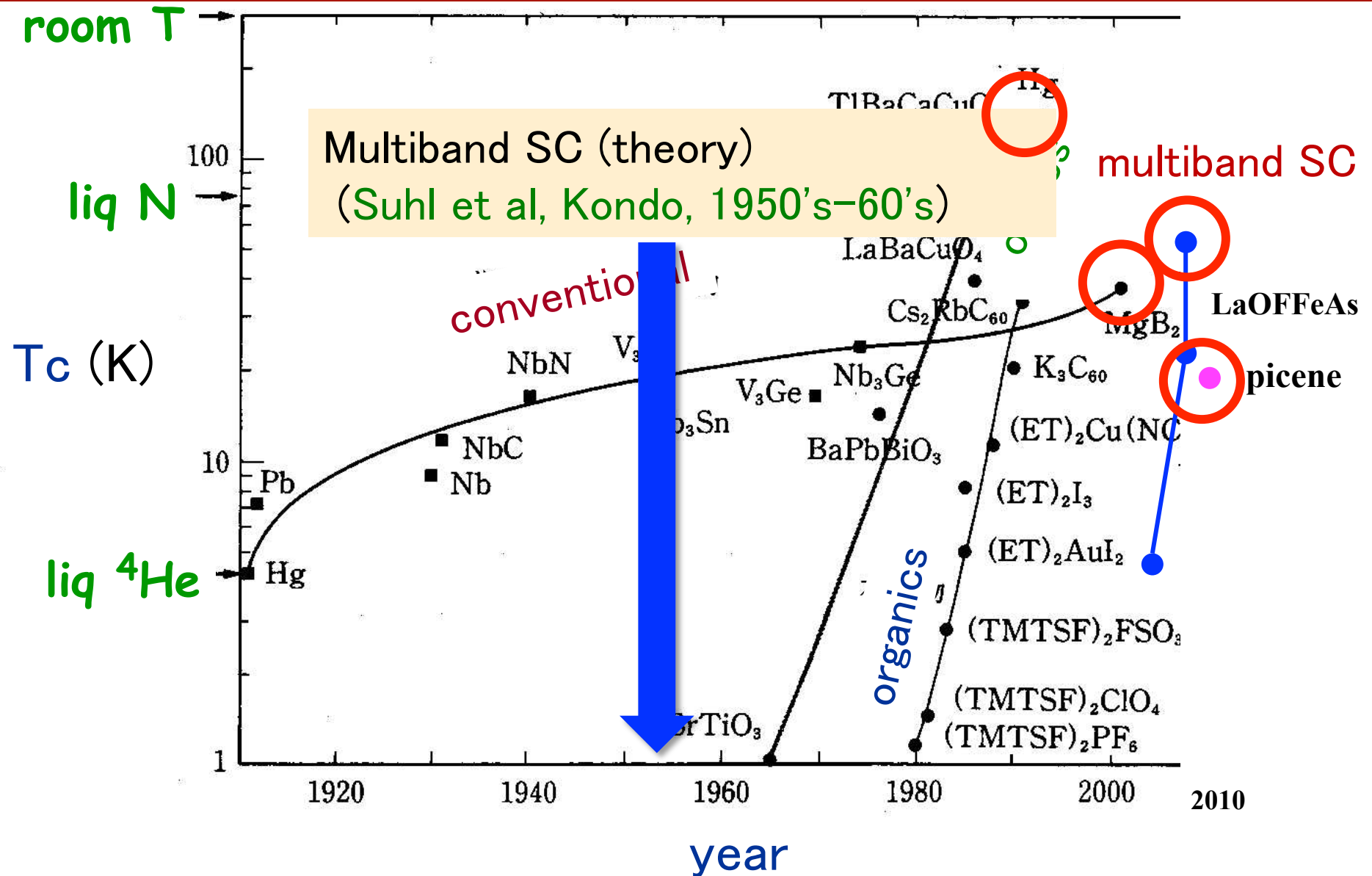
Keyword: Multiband SC

Kazuhiko Kuroki, Hidetomo Usui Univ Electro-Commun
Ryotaro Arita Univ Tokyo

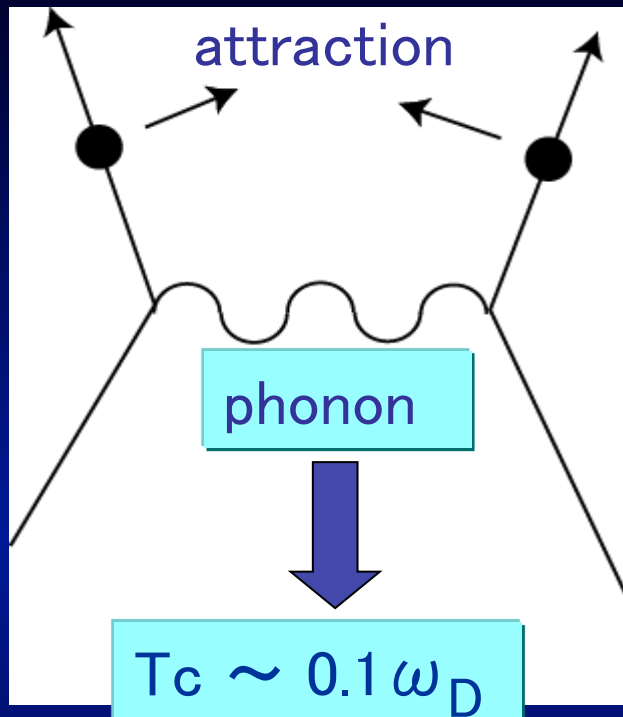
Yukihiro Ota, Masahiko Machida Japan Atomic Energy Agency
Tomio Koyama Tohoku Univ



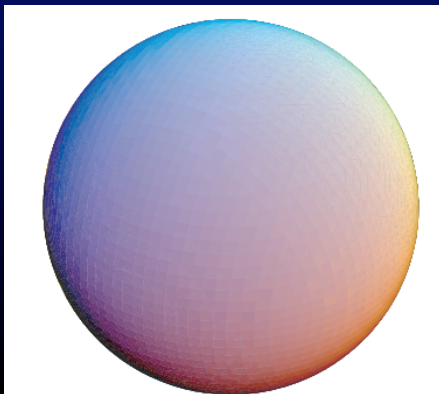
Why multiband SC ?



* phonon
mechanism

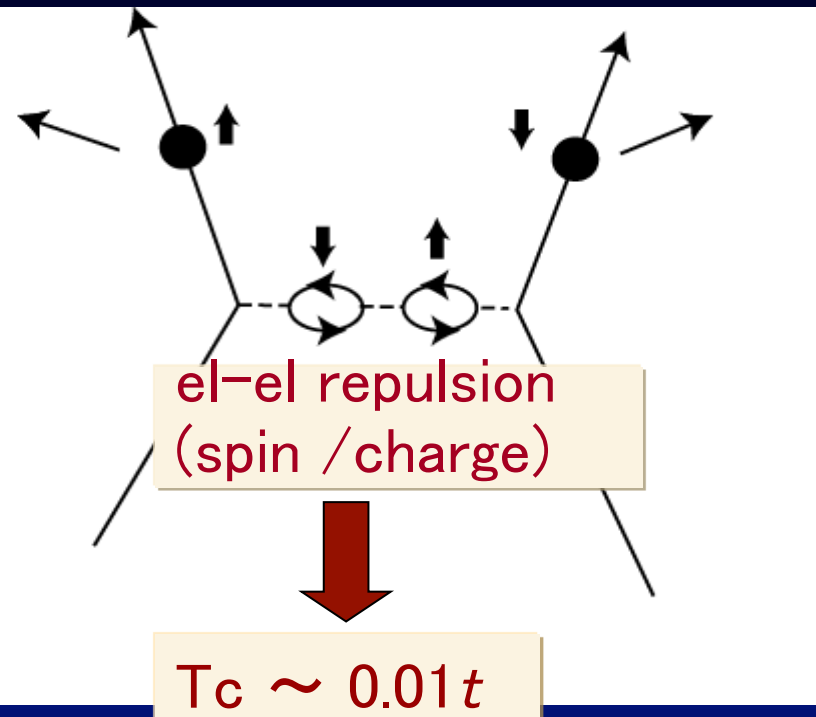


10K $\leftarrow$ 100K

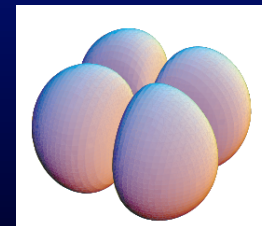


isotropic pairing

* electron
mechanism

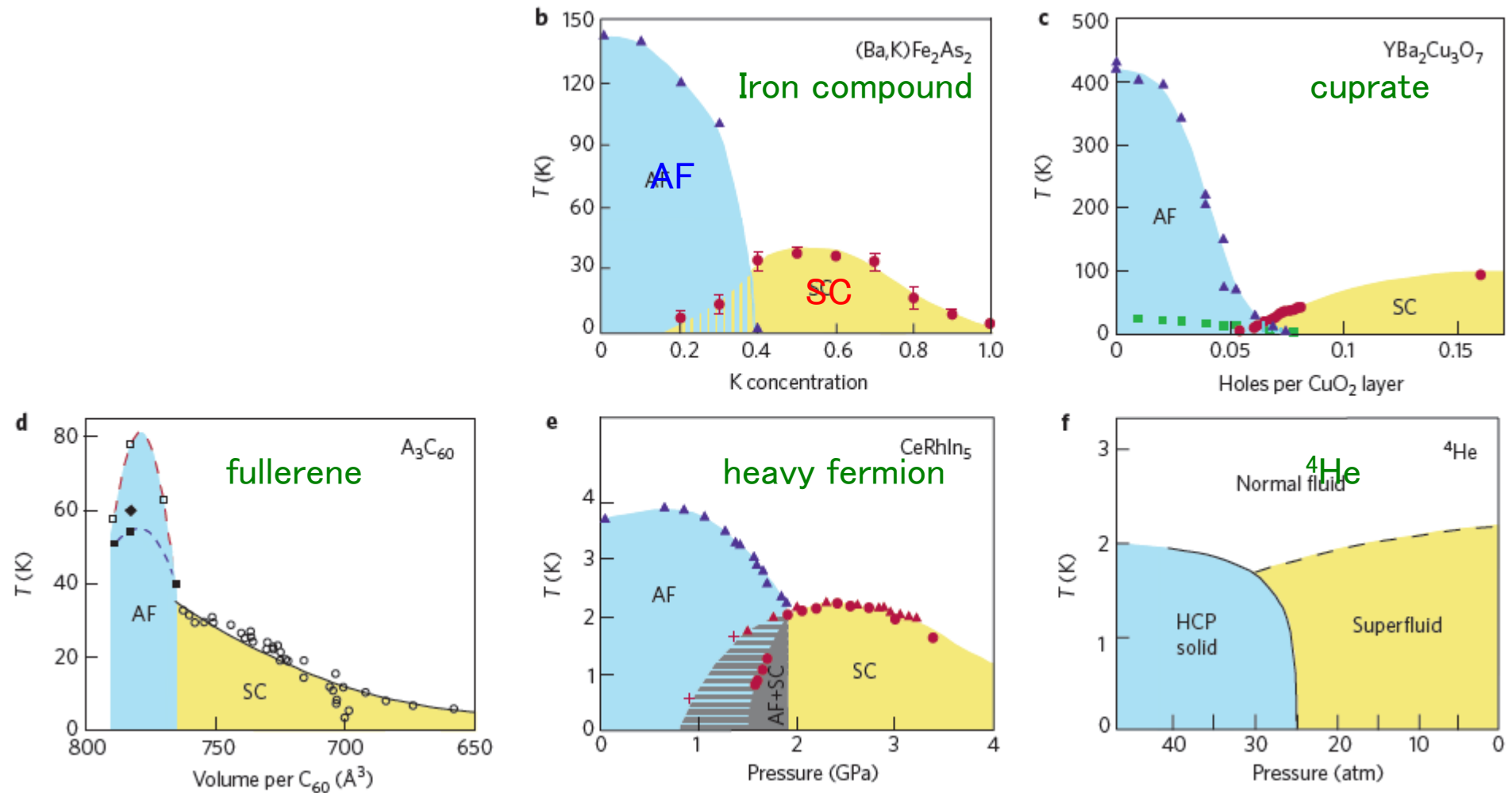


100K $\leftarrow$ 10000K

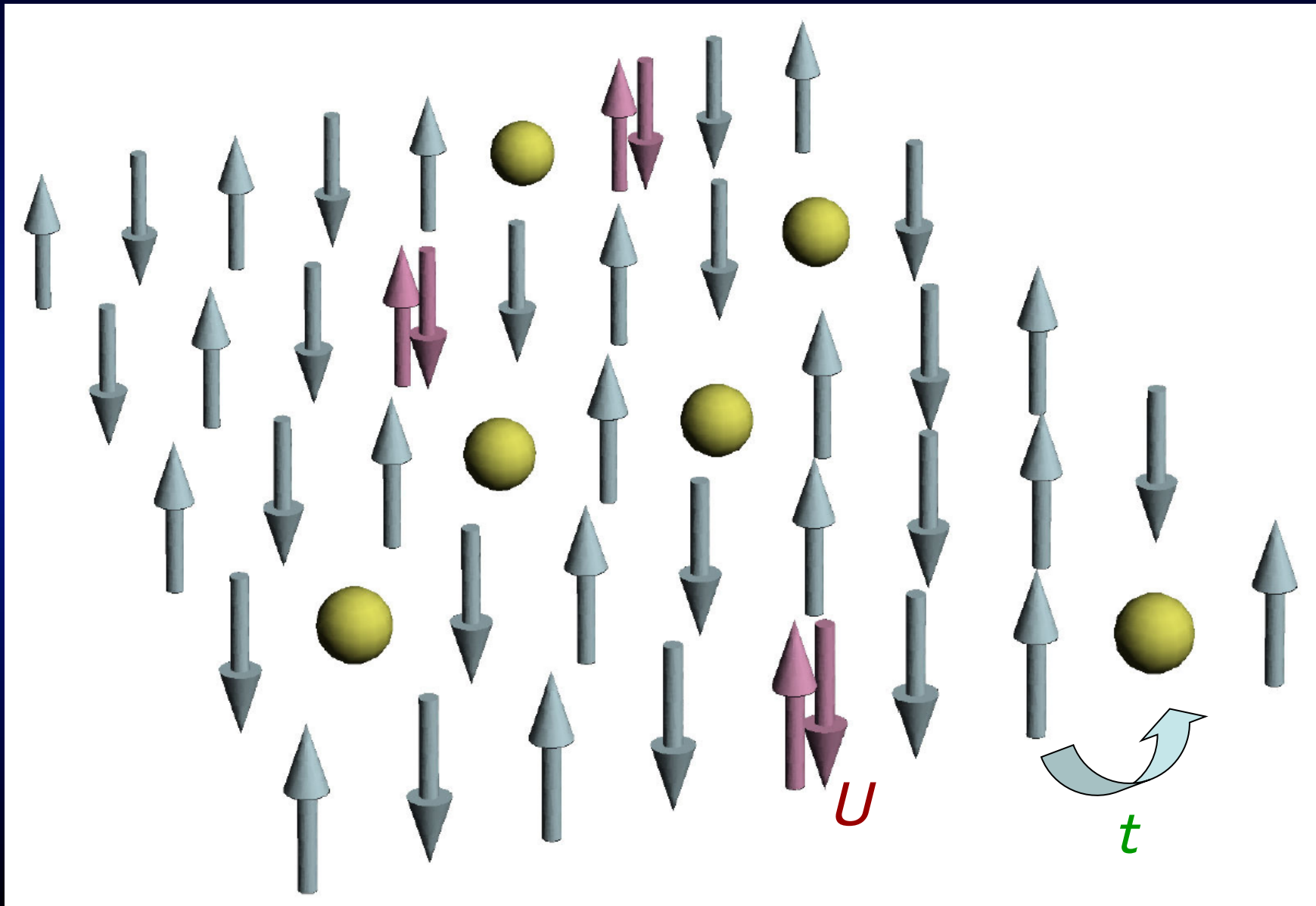


anisotropic pairing

Phase diagrams for various classes of materials



Hubbard model (a generic model)



$T_c \sim T_F/100$ is VERY low !

(1) Pairing int'action from el-el repulsion
= weak

Cf. Cold Fermi gas(2004)

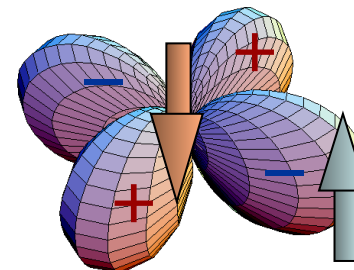
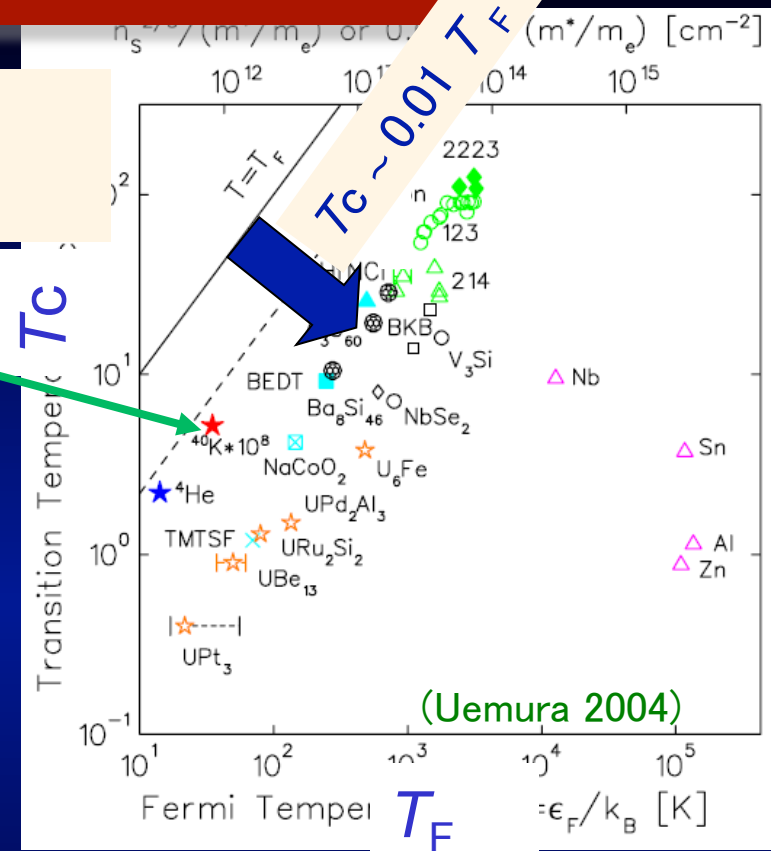
← superfluid $T_c \sim 0.1 T_F$

← attractive int'action

↑ Feshbach resonance

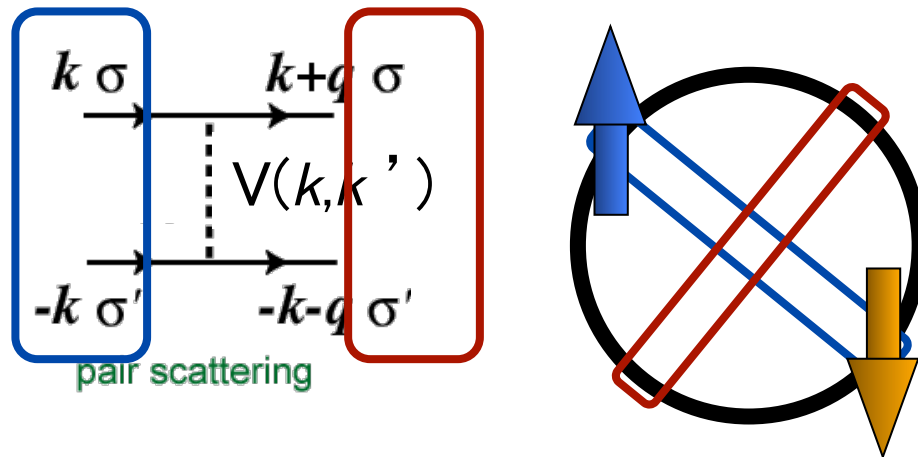
(2) Self-energy correction
→ quasi-particles short-lived

(3) Pairing from el-el repulsion
= anisotropic
(i.e., nodes in Δ_{BCS})



SC from repulsion: nothing strange

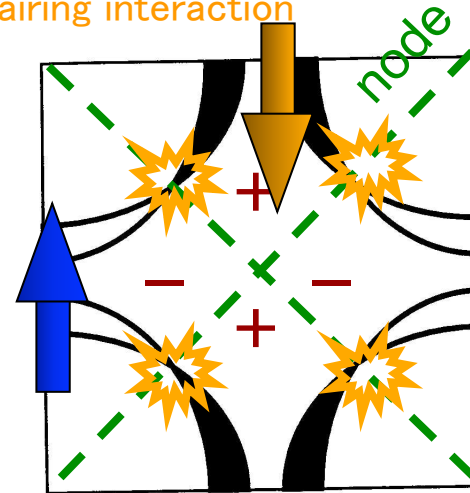
Attraction $\rightarrow$ isotropic SC



$$\Delta(k) = - \sum_{k'} V(k, k') \frac{\Delta(k')}{2E(k')} \tanh \left(\frac{1}{2} \beta E(k') \right)$$

Repulsion $\rightarrow$ anisotropic SC

spin-fluctuation mediated
pairing interaction

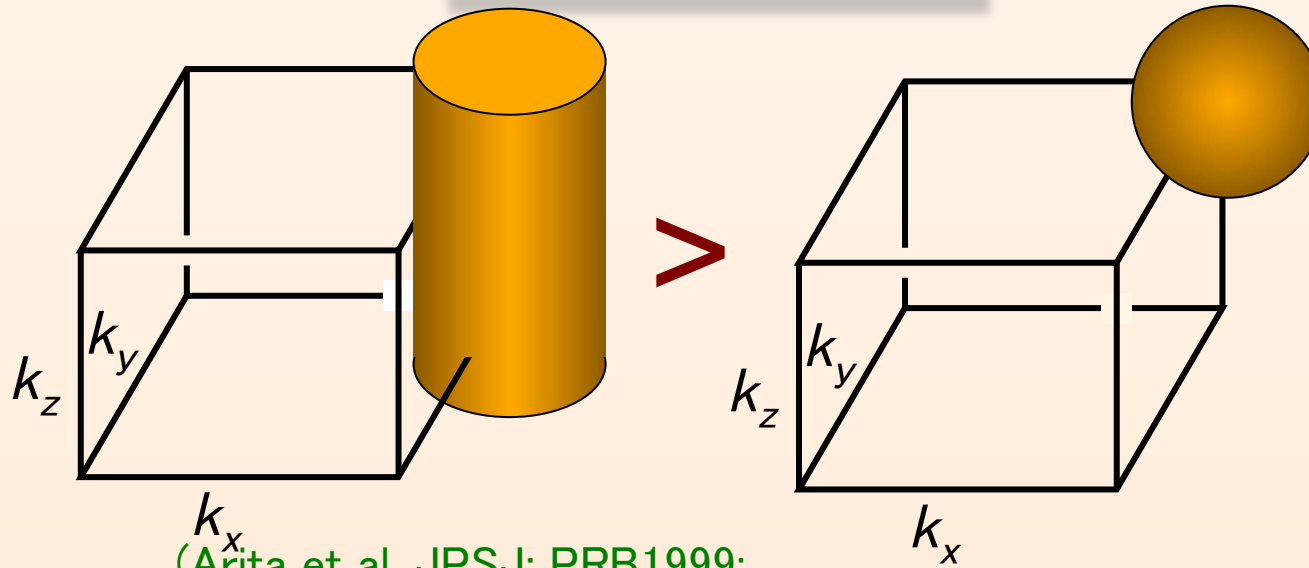


$\rightarrow$ attraction

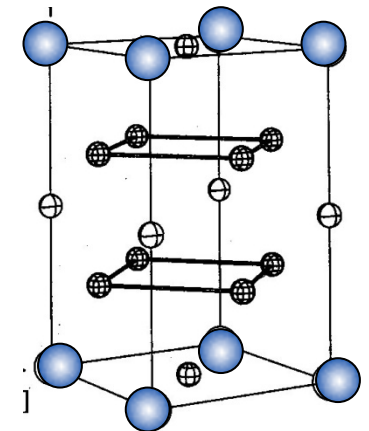
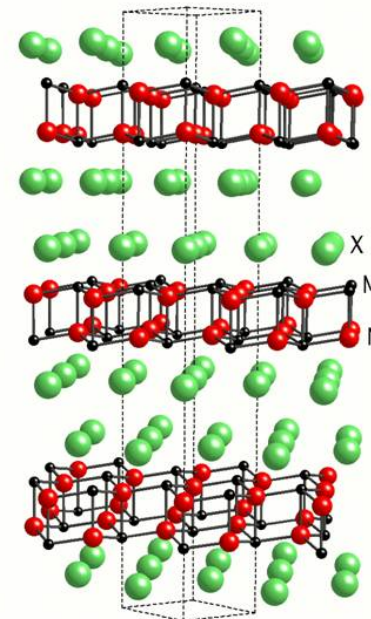
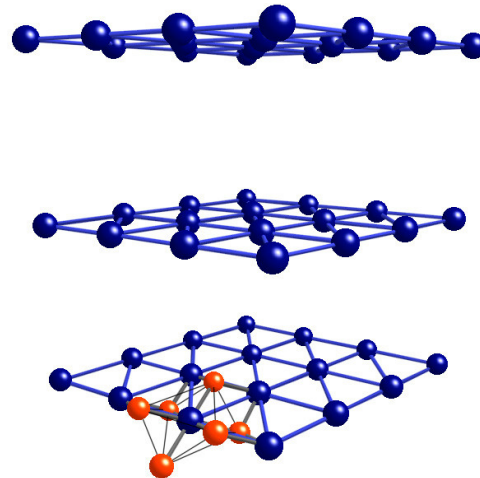
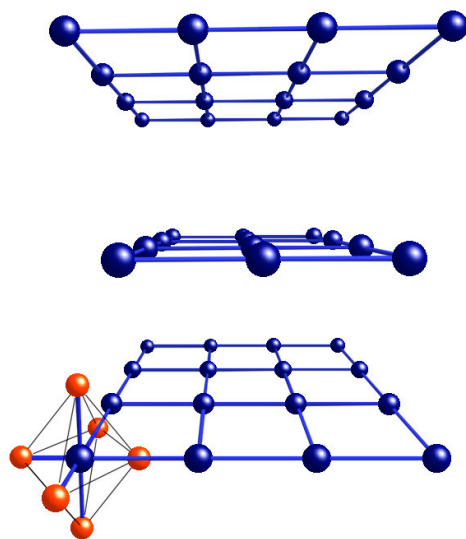
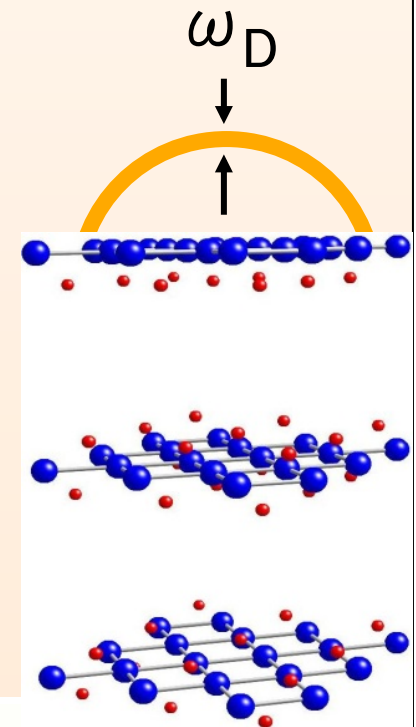
as in d wave pairing in cuprates

Scalapino et al,
Moriya & Ueda,
QMC: Kuroki & Aoki,
DCA: Jarrell,
VMC: Yokoyama et al, ...

2D or 3D ?



(Arita et al, JPSJ; PRB1999;
Monthoux & Lonzarich PRB 1999)

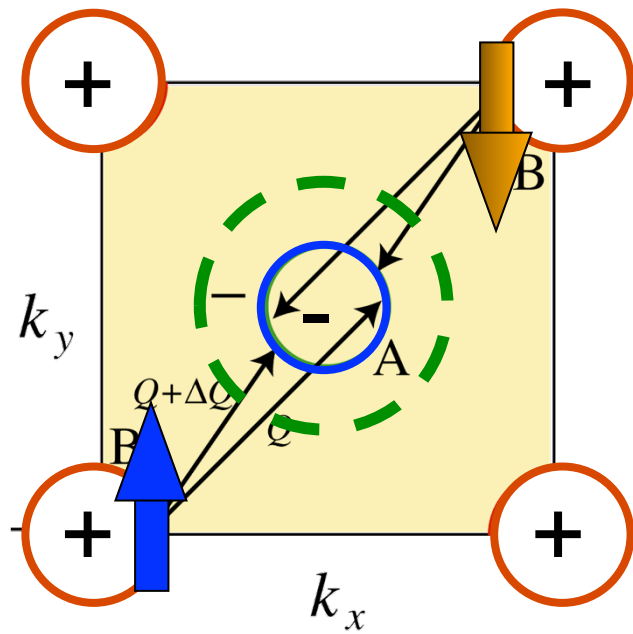


My talk today

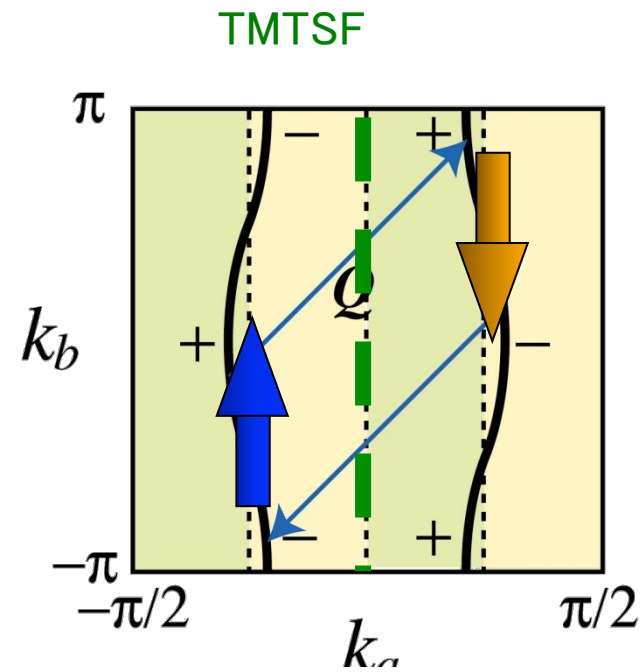
- ✓ A brief introduction for the iron-based SC
- ✓ Mechanism for $s_{\pm}$ pairing
[Kuroki et al, PRL 101, 087004 (2008)]
- ✓ Material-dependence ($s_{\pm} \Leftrightarrow d$)
- ✓ Collective (phase) modes in multiband SC

Keyword: Multiband SC

Disconnected Fermi surfaces

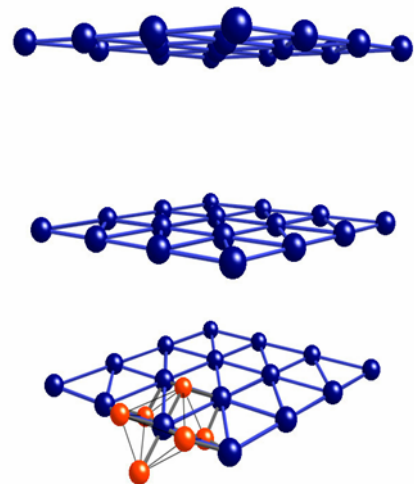


(Kuroki & Arita, 2001)

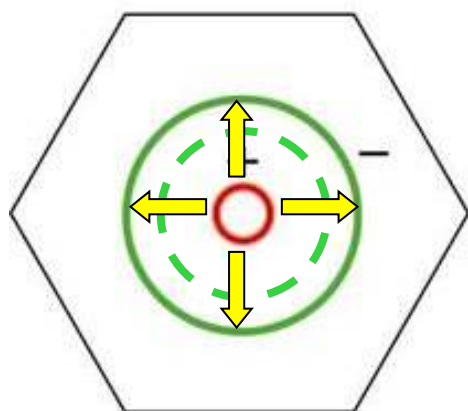


(Kuroki et al 2001; 2004)

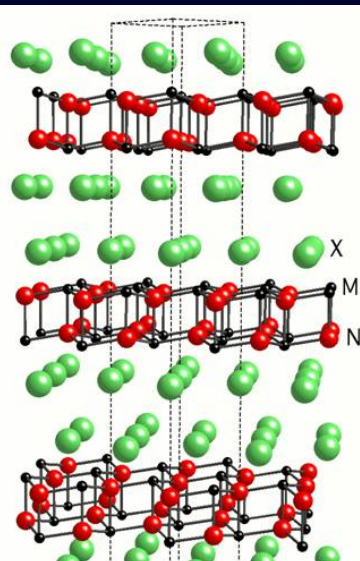
Disconnected Fermi surfaces in real materials



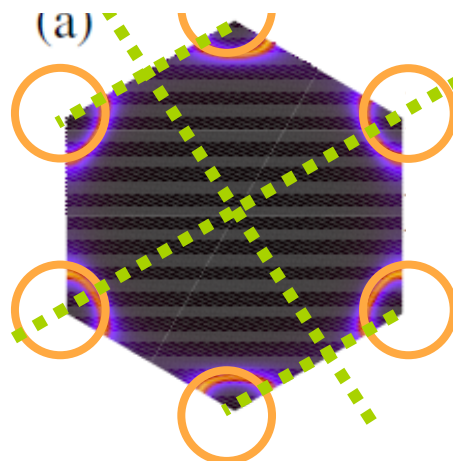
Co compound



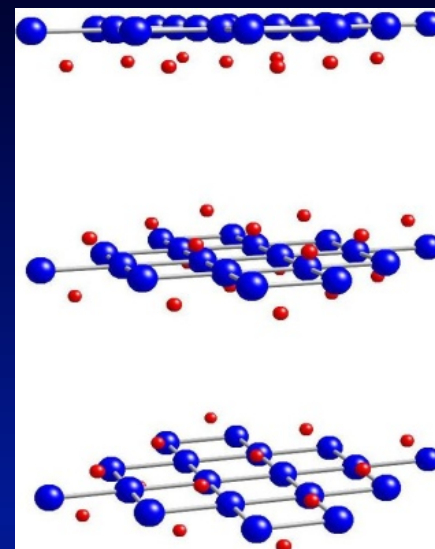
Kuroki et al, JPSJ(06);
PRL(07); JPSJ(07)



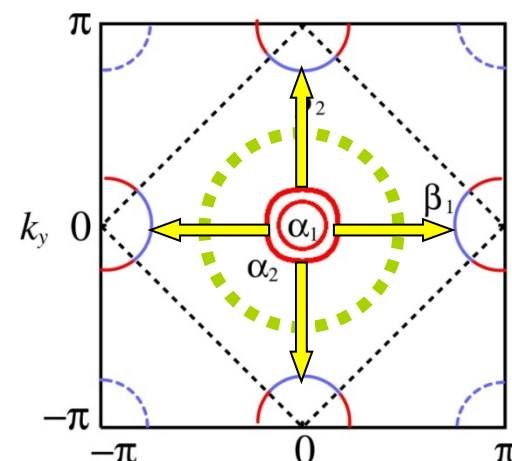
Hf nitrides



Kuroki, to appear in Proc LT 25;
arXiv0902.3695



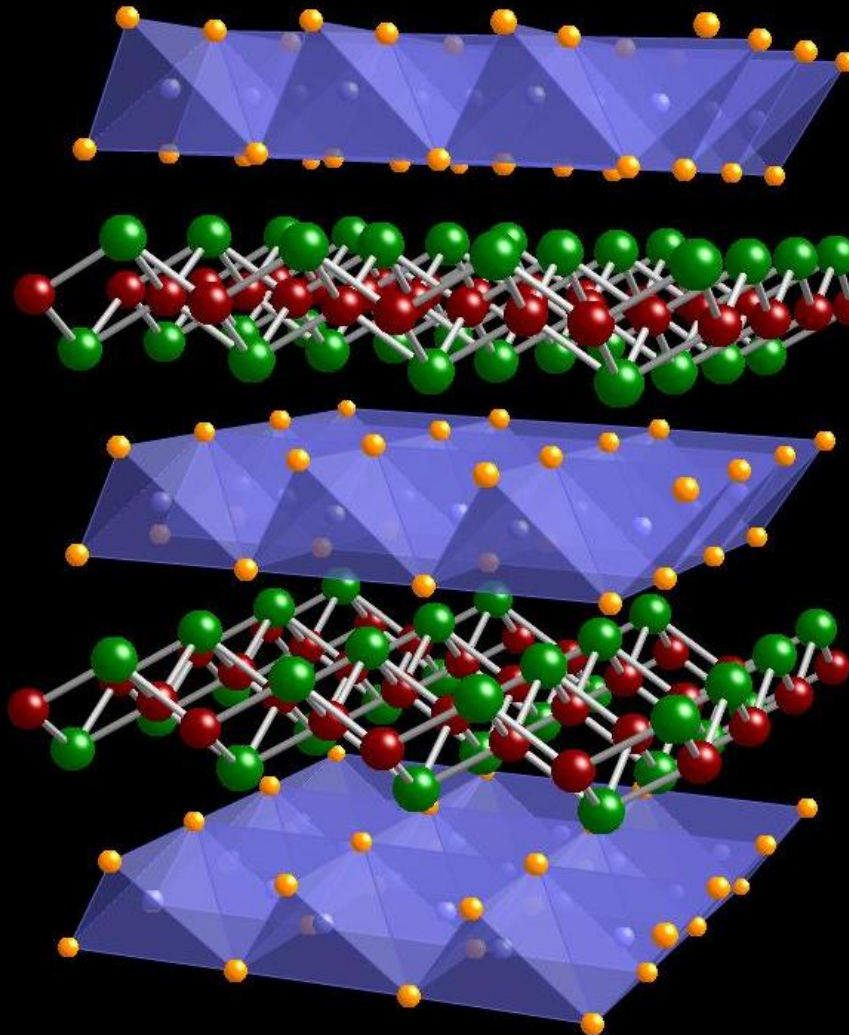
Fe compound



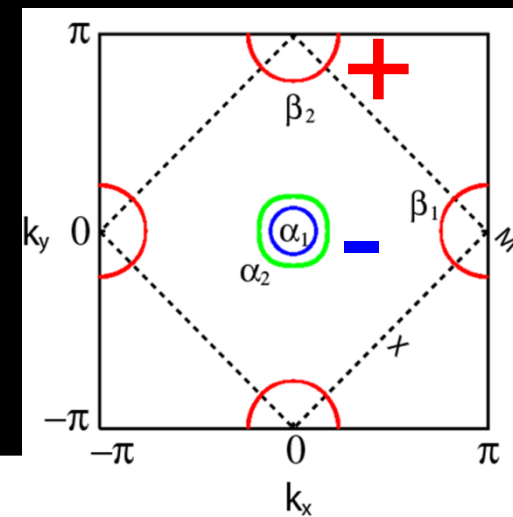
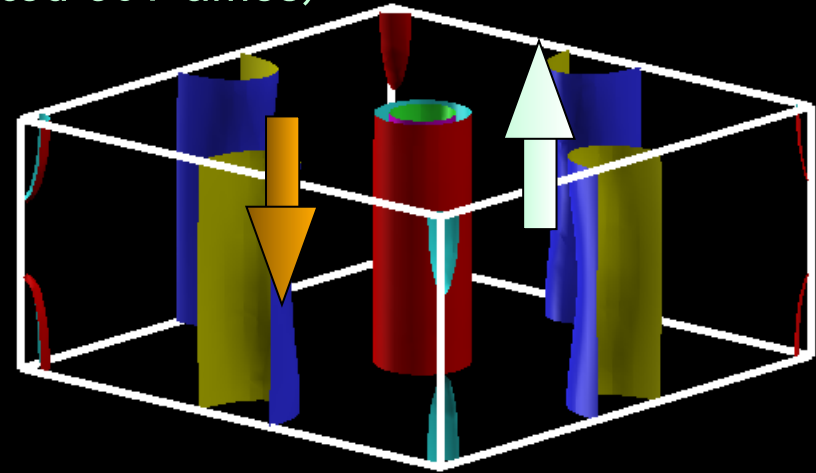
Kuroki et al, PRL(08)

Fe-compound

Kamihara et al, JACS 130, 3296 (2008)



Kuroki et al, PRL 101, 087004 (2008)
(cited 301 times)

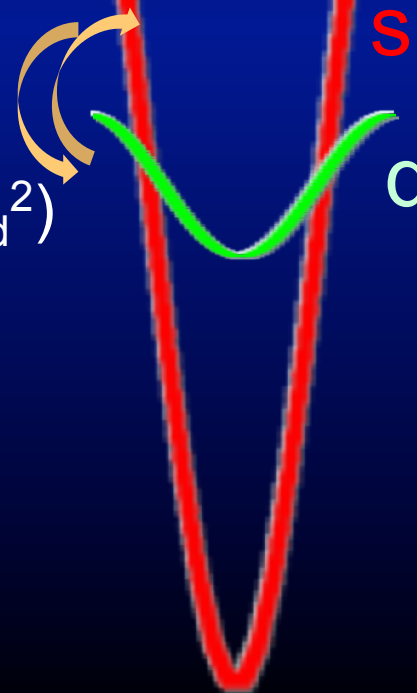


Suhl-Kondo mechanism

(Suhl et al 1959; Kondo 1963)

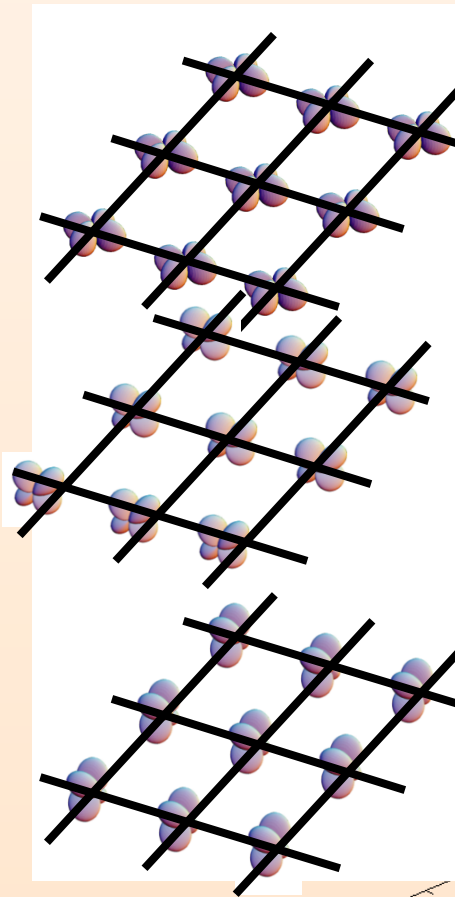
$$H = \sum_{\mathbf{k}\sigma} \epsilon_{\mathbf{k}s} c_{\mathbf{k}\sigma}^* c_{\mathbf{k}\sigma} + \sum_{\mathbf{k}\sigma} \epsilon_{\mathbf{k}d} d_{\mathbf{k}\sigma}^* d_{\mathbf{k}\sigma} - \sum_{\mathbf{k}\mathbf{k}'} V_{ss} c_{\mathbf{k}\uparrow}^* c_{-\mathbf{k}\downarrow} c_{-\mathbf{k}'\downarrow}^* c_{\mathbf{k}'\uparrow} - V_{dd} \sum_{\mathbf{k}\mathbf{k}'} d_{\mathbf{k}\uparrow}^* d_{-\mathbf{k}\downarrow} d_{-\mathbf{k}'\downarrow}^* d_{\mathbf{k}'\uparrow} \\ - V_{sd} \sum_{\mathbf{k}\mathbf{k}'} (c_{\mathbf{k}\uparrow}^* c_{-\mathbf{k}\downarrow} d_{-\mathbf{k}'\downarrow}^* d_{\mathbf{k}'\uparrow} + d_{\mathbf{k}\uparrow}^* d_{-\mathbf{k}\downarrow} c_{-\mathbf{k}'\downarrow}^* c_{\mathbf{k}'\uparrow})$$

Tc enhanced $\sim O(V_{sd}^2)$

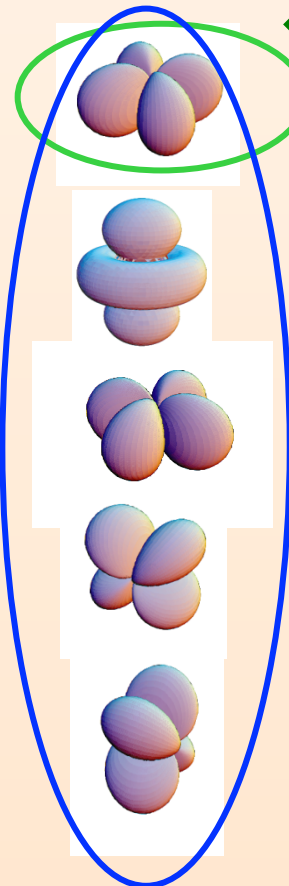
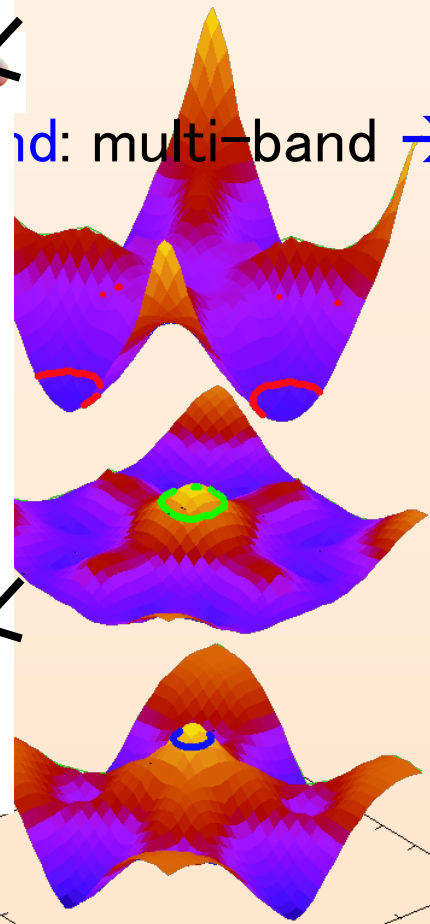


single-band vs multi-band

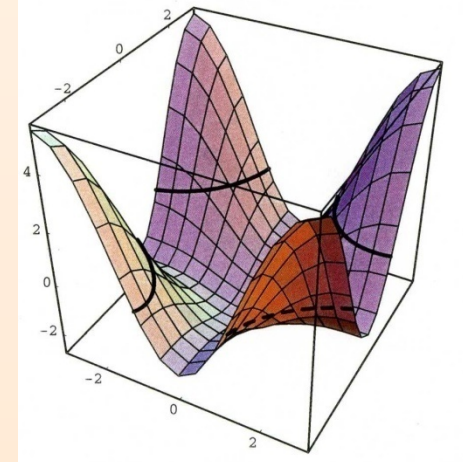
4	Ti $3d^2$	V $3d^3$			Fe $3d^6$	Co $3d^7$	Ni $3d^8$	Cu $3d^{10}$
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band: multi-band →

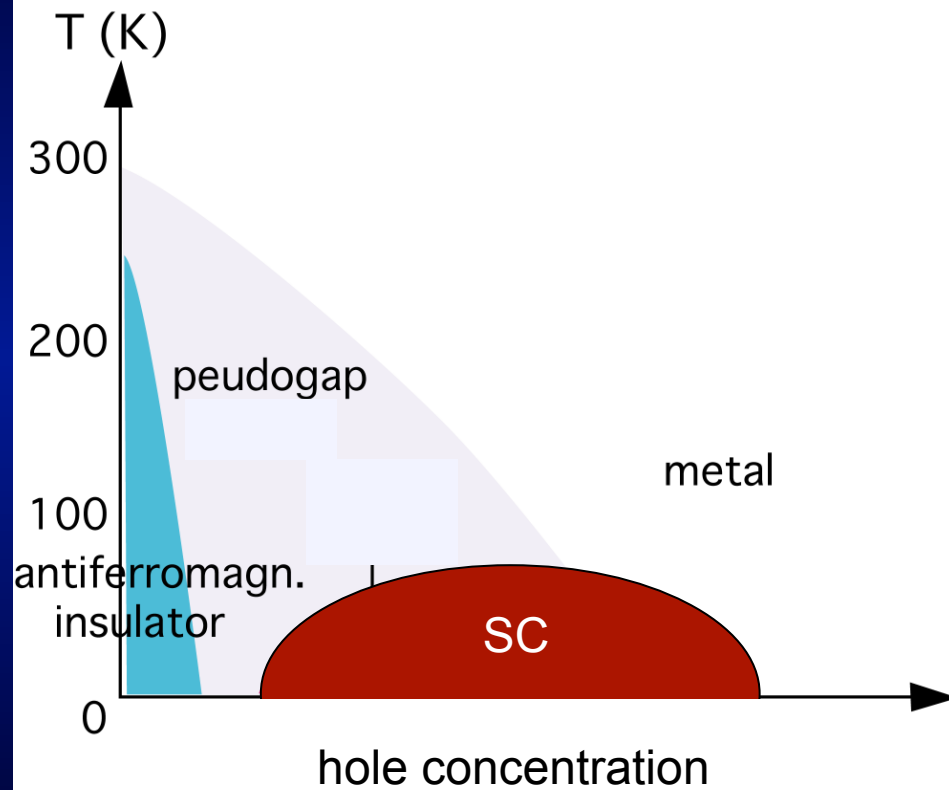


← Cuprate:
nearly half-filled one-band

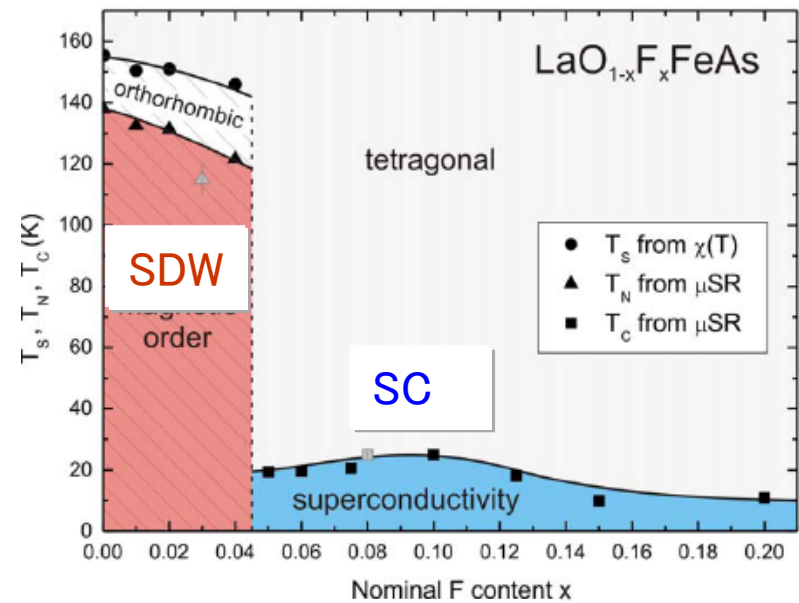


Phase diagram

High-Tc



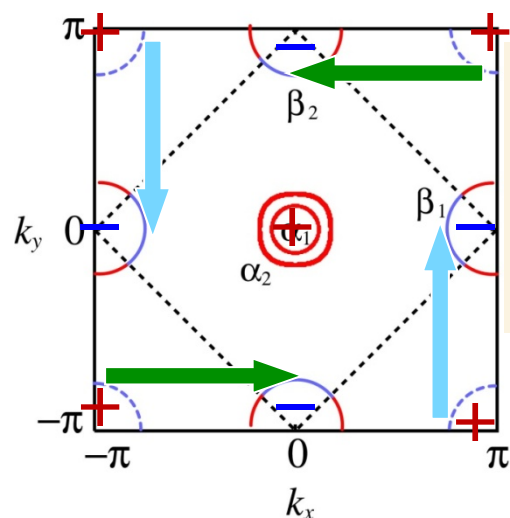
Iron-based



(Luetkens et al, 2008)

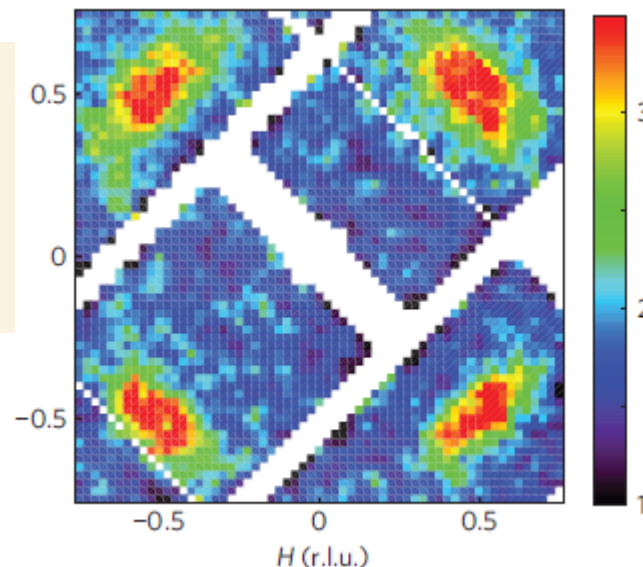
Susceptibilities: 5-band RPA result

5-band RPA
(Kuroki et al, PRL 2008)

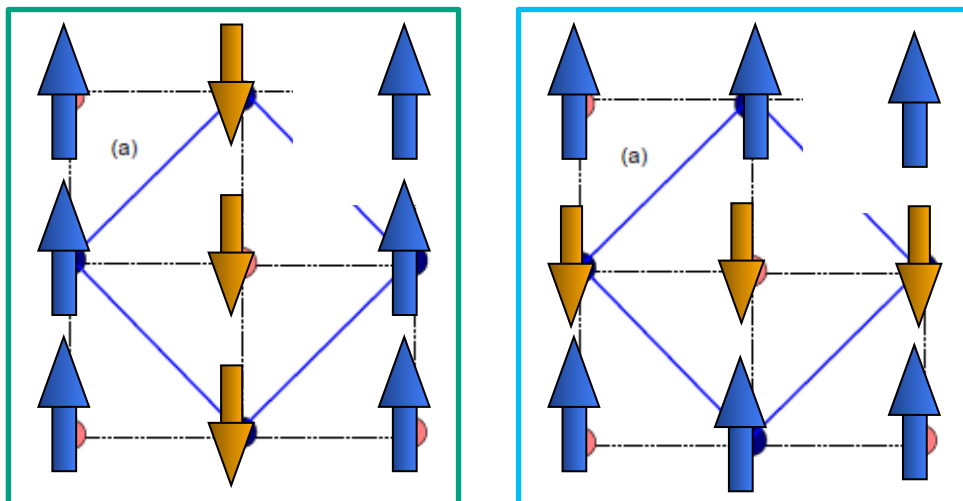


Spin-fluct
mediated
 $s \pm$ pairing

Inelastic neutron scattering
(Lumsden et al, nature phys 2010)



colinear SDW

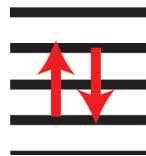


Hamiltonian

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_1$$

$$\mathcal{H}_0 = \sum_{ij} \sum_{\mu\nu} \sum_{\sigma} t_{ij}^{\mu\nu} c_{i\mu\sigma}^{\dagger} c_{j\nu\sigma} + \sum_{i\mu\sigma} \epsilon_{\mu} n_{i\mu\sigma} \quad i, j: \text{site}, m, n: \text{orbitals}$$

$$\mathcal{H}_1 = \sum_i \left[U \sum_{\mu} n_{i\mu\uparrow} n_{i\mu\downarrow} + U' \sum_{\mu > \nu} n_{i\mu} n_{i\nu} + J \sum_{\mu \neq \nu} \mathbf{S}_{i\mu} \cdot \mathbf{S}_{i\nu} + J' \sum_{\mu \neq \nu} c_{i\mu\uparrow}^{\dagger} c_{i\mu\downarrow}^{\dagger} c_{i\nu\downarrow} c_{i\nu\uparrow} \right]$$



intraorbital U



interorbital U'



Hund's J

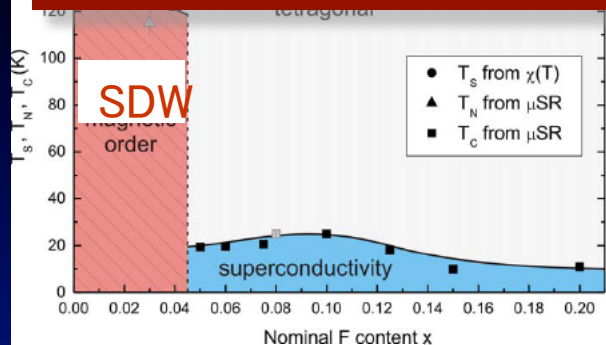


pair hopping J'

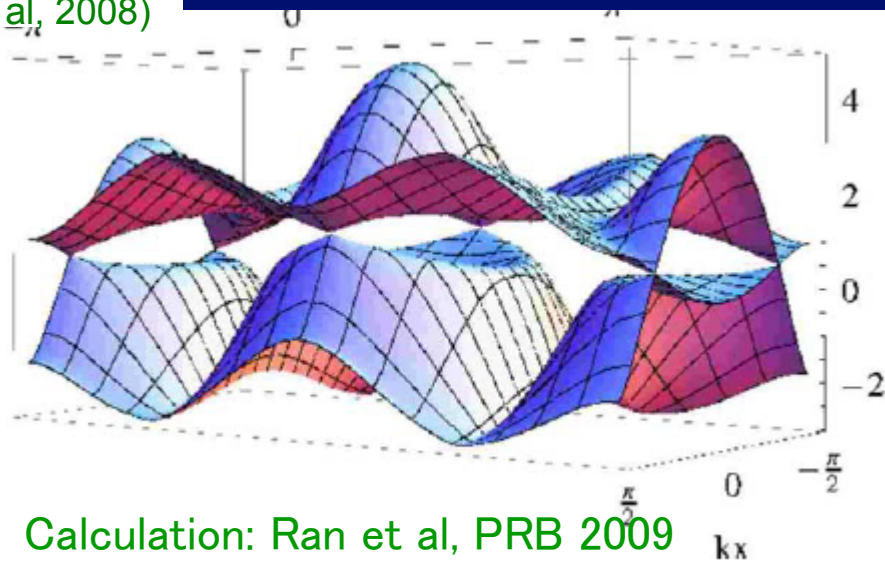
U, U', J, J' in general depends on orbital

Evaluation from first principles: Nakamura et al, JPSJ **77** (2008) 093711;
Anisimov et al, JPCM **21** 075602 (2009);
Miyake et al, JPSJ **77** Suppl.C 99 (2008)

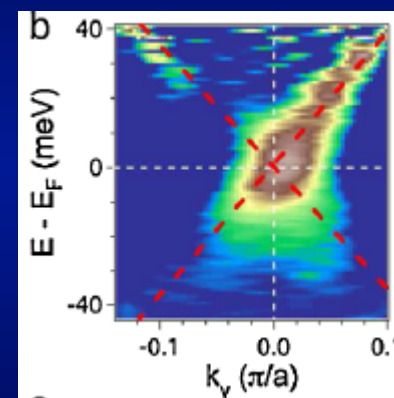
Dirac cones in the iron-based SC



(Luetkens et al, 2008)



Calculation: Ran et al, PRB 2009



ARPES: Richard et al, PRL 2010

Experimental evidence for multiband nature

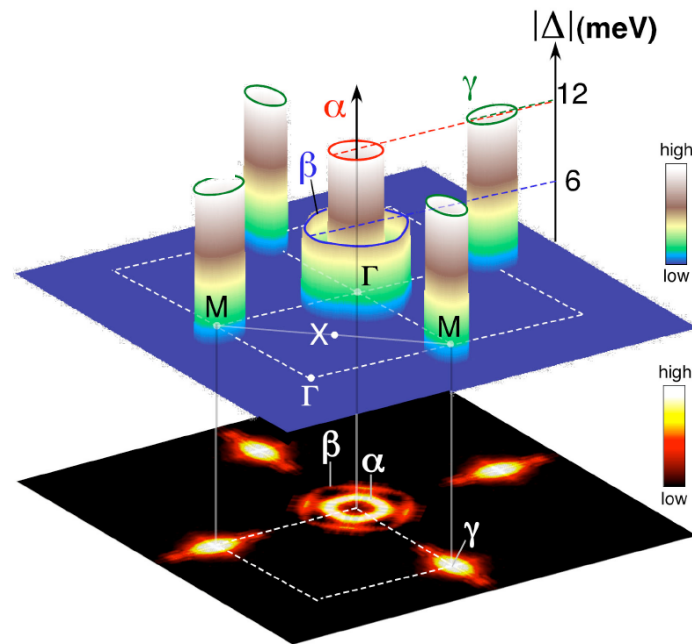
✓ Quasiparticle excitations (penetration depth, thermal conductivity)

✓ ARPES

✓ NMR

...

ARPES



(BaK)Fe₂As₂: Ding et al,
EPL 83, 47001 (2008)

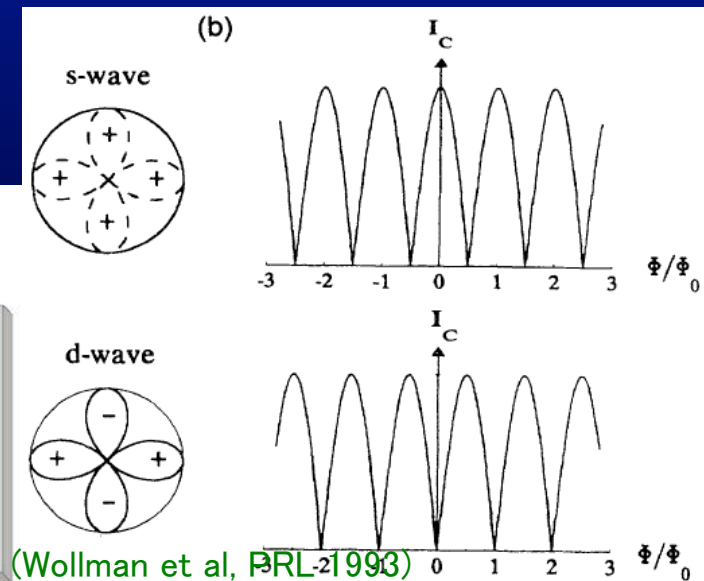
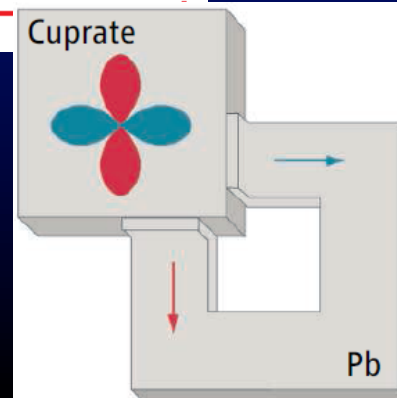
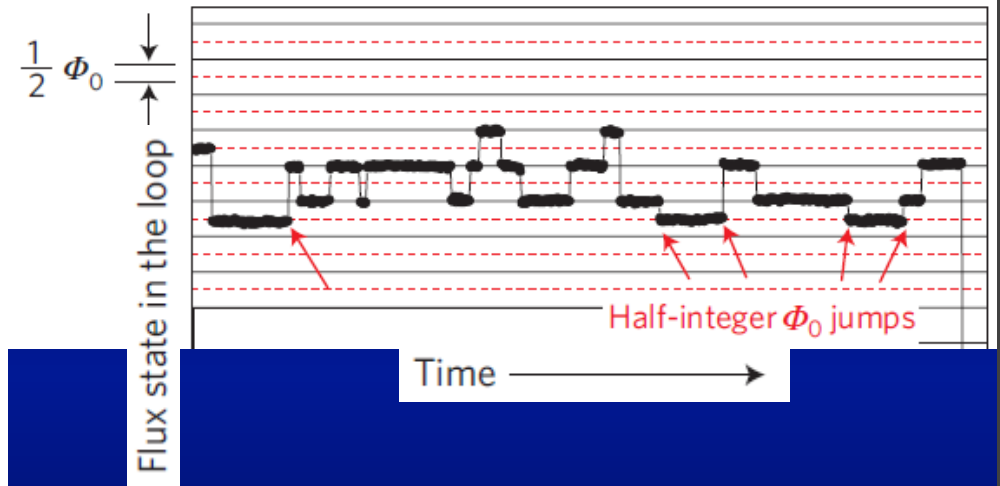
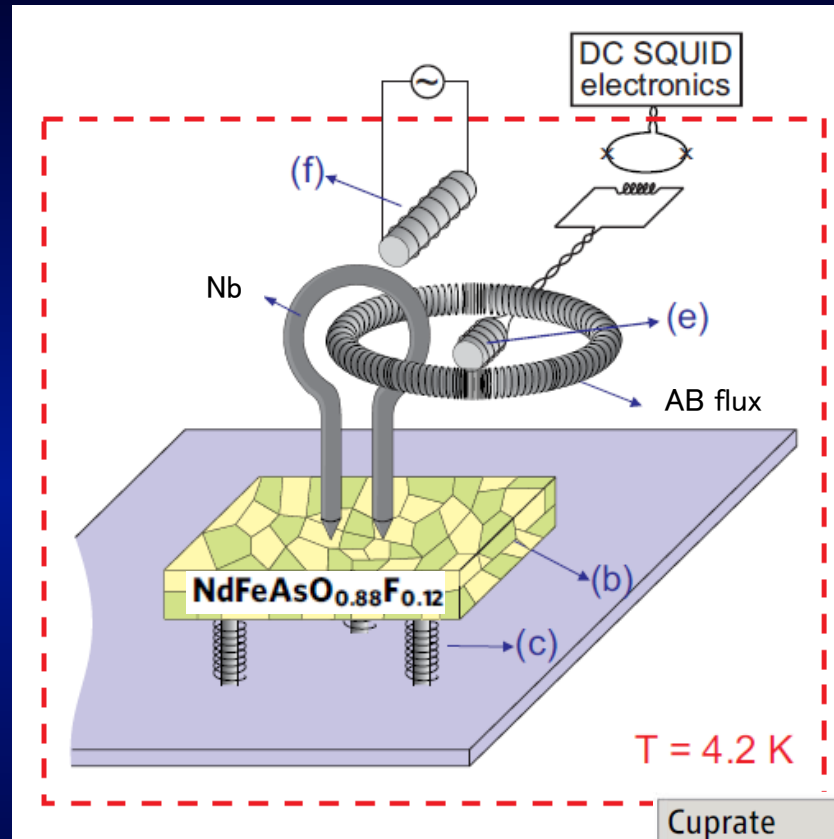
JPS 2010 March meeting

Symposium "Pairing symmetry in the iron-based SC"

- ✓ Shibauchi: Penetration depth, thermal cond
→ consistent with full gap, while P-compound has a node
- ✓ Shimojima: ARPES
→ 122 has full gap, but factors other than spin fluctuation may be relevant
- ✓ Hanaguri: Fourier transform STM
→ $s_{\pm}$
- ✓ Mukuda: NMR
→ various powers in T observed for T_1 below T_C
- ✓ Sato: neutron scattering
→ magnetic excitations, resonance peak
- ✓ Iketa: 1st principles calc for multiorbits, impurity potential
→ $s_{\pm}$
- ✓ Onari: : Theory for impurity effect, resonance peak
→ s_{++} , orbital fluctuation mechanism

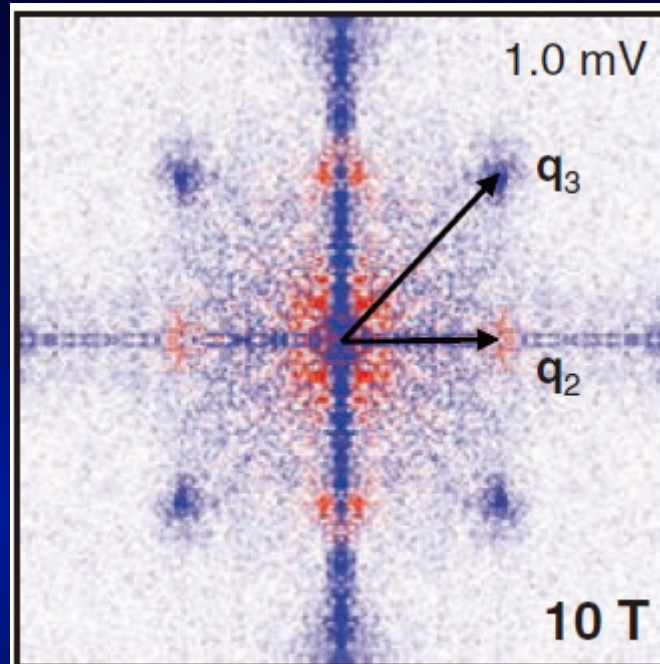
Phase-sensitive measurement (1)

(Chen et al, nature physics 2010)

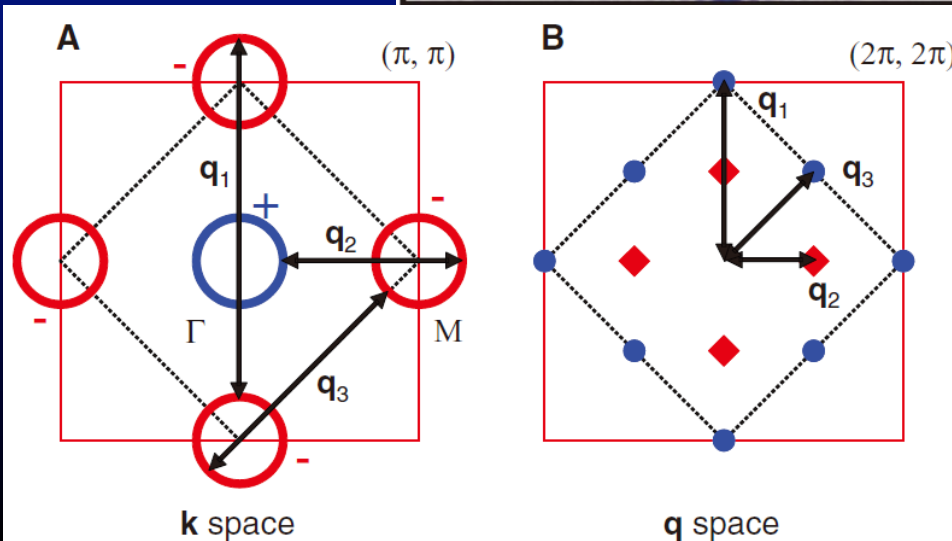


Phase-sensitive measurement (2)

— Fourier-transform STM spectroscopy



(Hanaguri et al,
Science 2010)

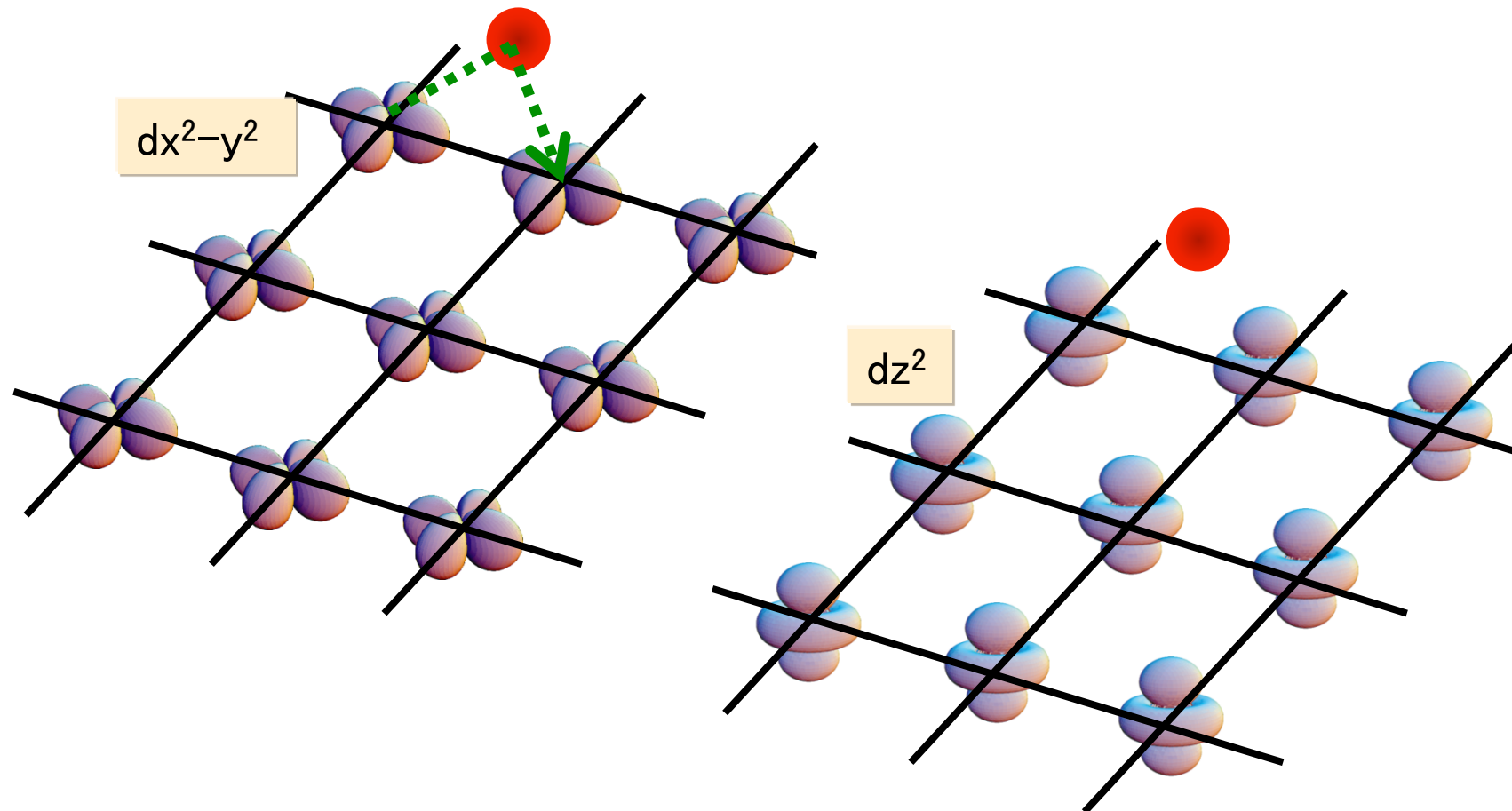
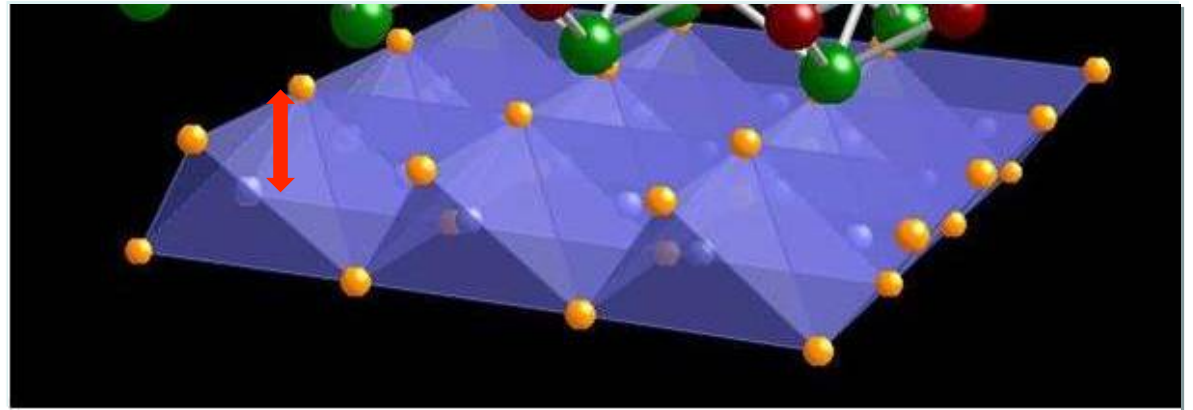


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[Kuroki et al, PRB **79**, 224511 (2009)]
- ✓ Collective (phase) modes in multiband SC

Keyword: Multiband SC

NdFeAsO	$h = 1.38 \text{ \AA}$
LaFeAsO	$h = 1.32 \text{ \AA}$
LaFePO	$h = 1.14 \text{ \AA}$



Multibands modified

(Kuroki et al, PRB 2009)

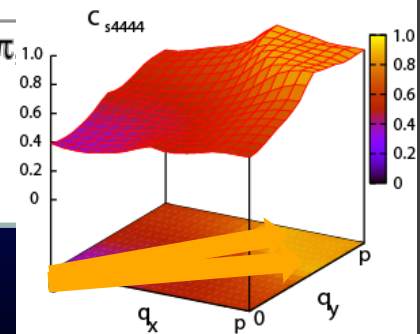
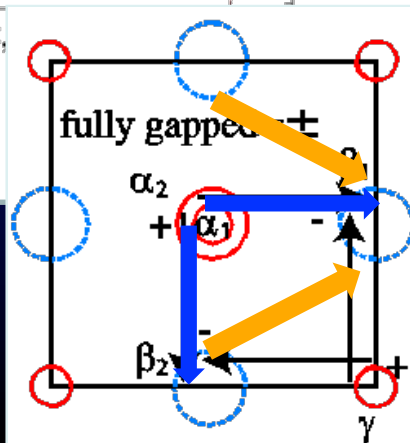
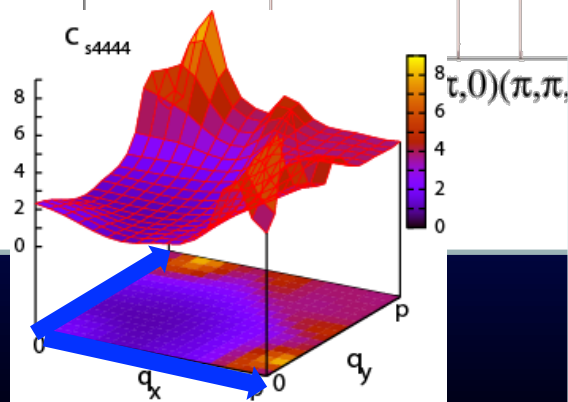
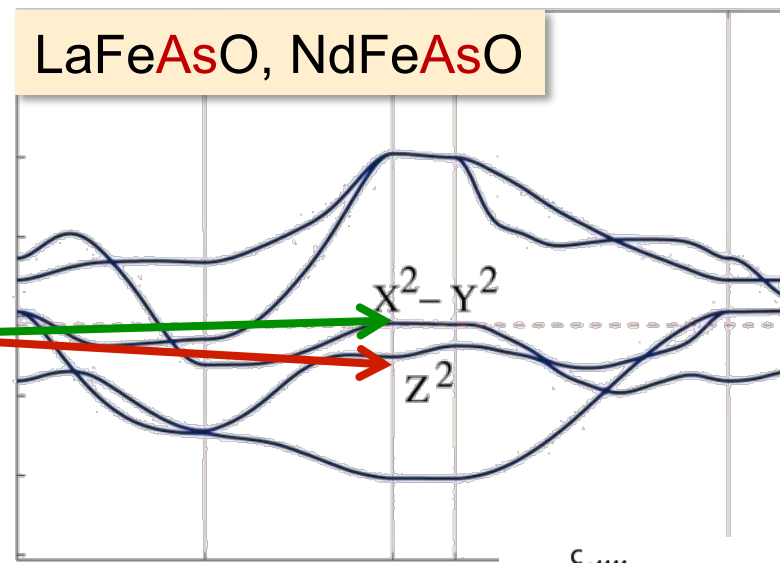
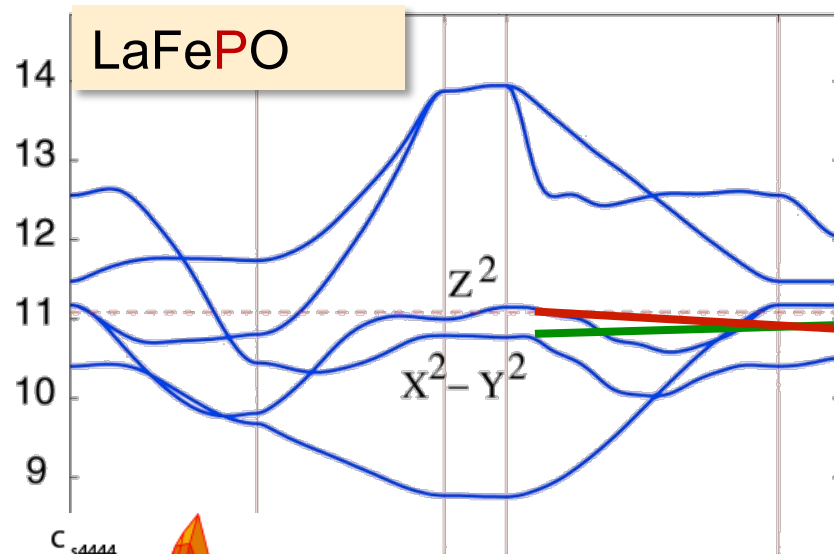
pnictogen height

$z_{\text{As}}=0.630$ ($h_{\text{As}}=1.14$)

$z_{\text{As}}=0.658$ ($h_{\text{As}}=1.38$)

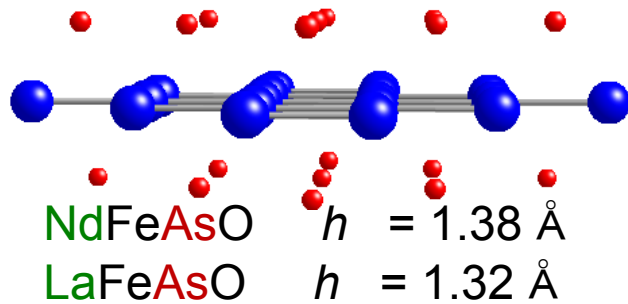
LaFePO

LaFeAsO, NdFeAsO



Multiple nesting vectors compete

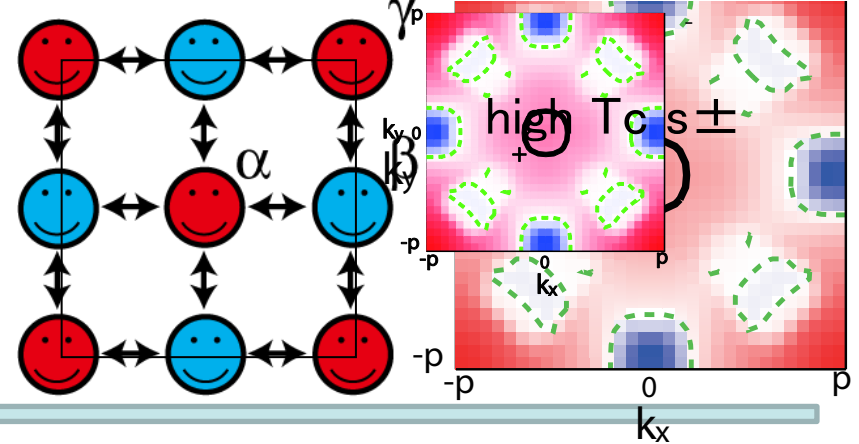
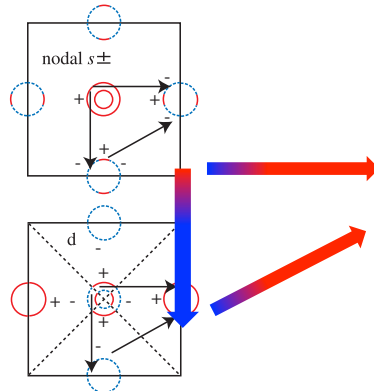
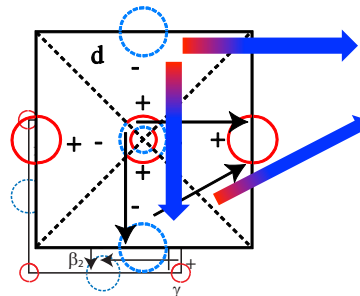
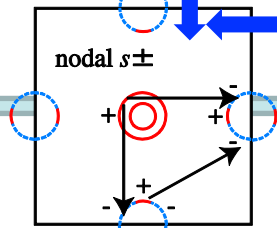
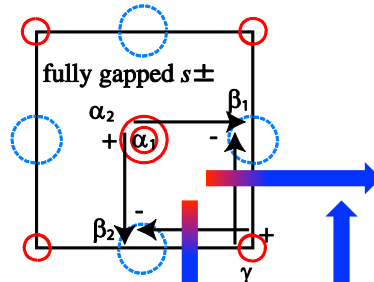
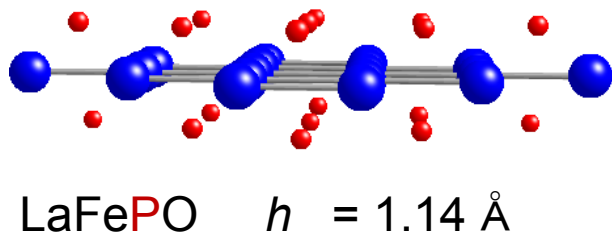
Kuroki et al, PRB 79, 224511 (2009)



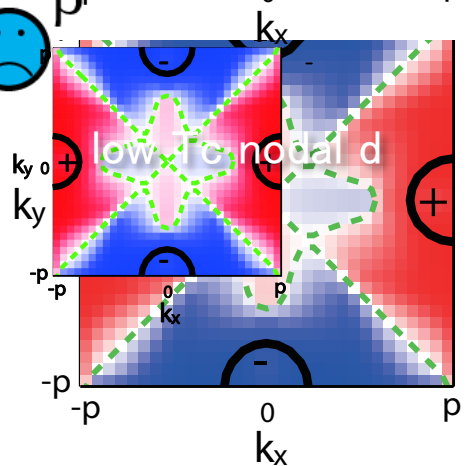
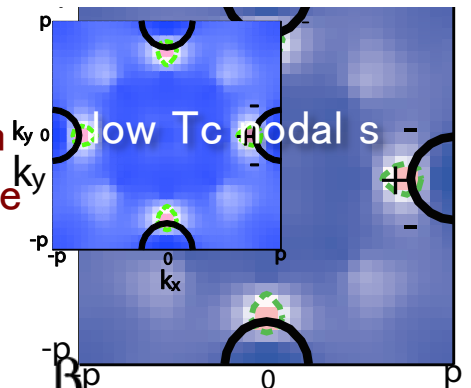
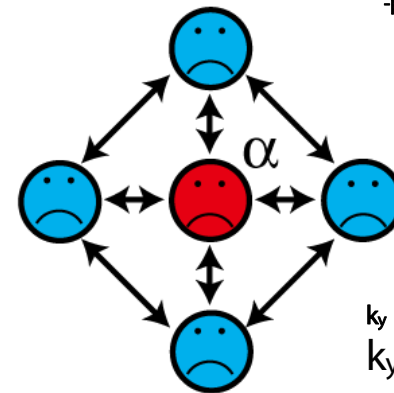
Pnictogen height as
 a “switch”



Height matters



“Frustration” in
 momentum space



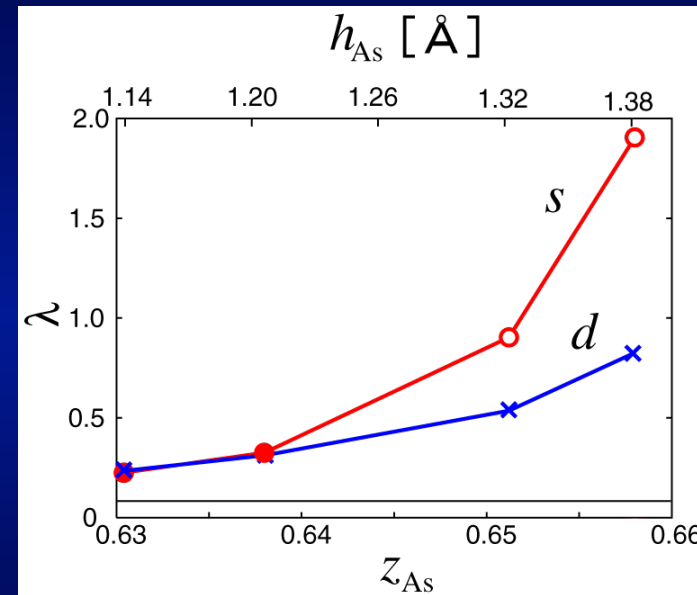
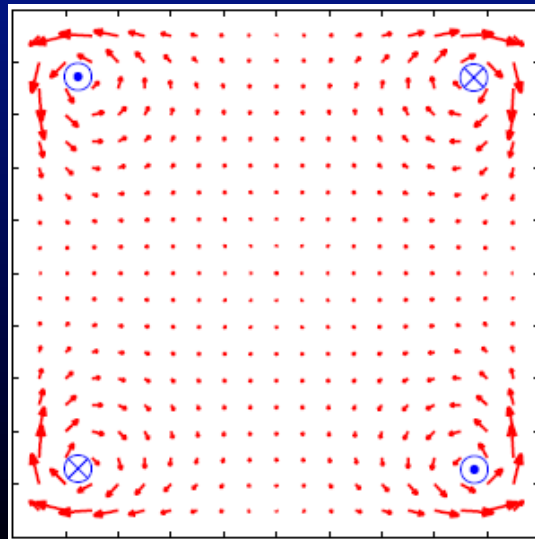
Multiband systems

→ various pairings when materials / p are tuned

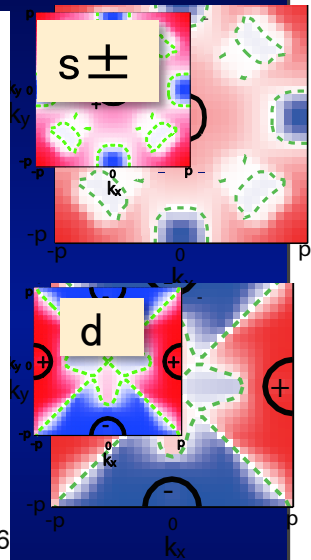
Degeneracy point

→ $s+id$?

(S.C. Zhang's group, PRL 2009)



(Kuroki et al, PRB 2009)



When T-broken pairing can occur?

When the space group has a **two-dimensional rep**:
as in

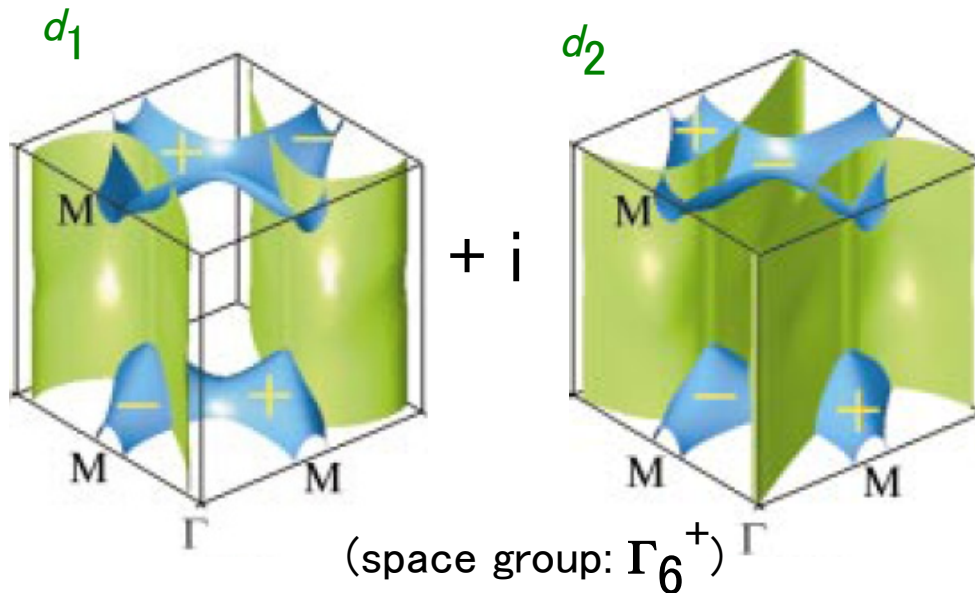
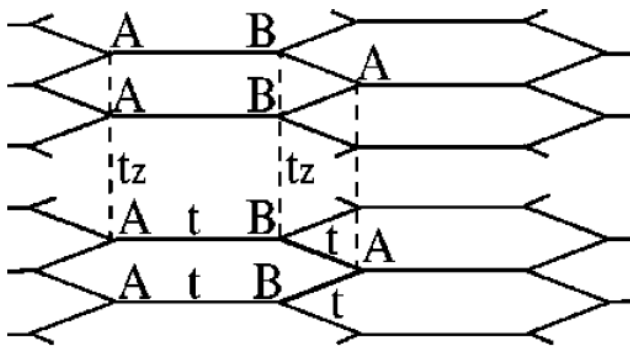
● $p + ip$ for triplet SC

● $p + ip$ for graphene

(Uchoa et al, PRL 2007)

● $d + id$ for singlet SC

(Onari et al, PRB 2002)



My talk today

- ✓ A brief introduction for the iron-based SC
- ✓ Mechanism for $s_{\pm}$ pairing
- ✓ Material-dependence ($s_{\pm} \Leftrightarrow d$)
- ✓ Collective (phase) modes in multiband SC
[Ota et al, arXiv:1008.3212]

Keyword: Multiband SC

Collective excitation modes in SC

Collective mode in one-band SC

Phase modes (Bogoliubov 1959, Anderson 1958, Nambu 1960)

= **massless** Nambu–Goldstone mode for neutral SC

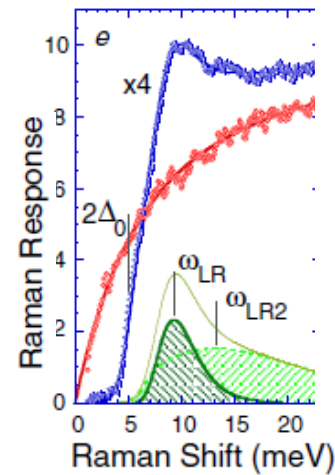
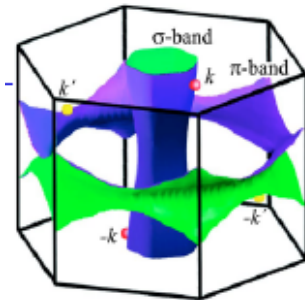
→ **massive** for real (charged) SC (Anderson–Higgs mechanism 1963)
as observed in NbSe₂ (Raman: Sooryakumar & Klein 1980,
Littlewood & Varma 1981)

Collective modes in **two**-band SC

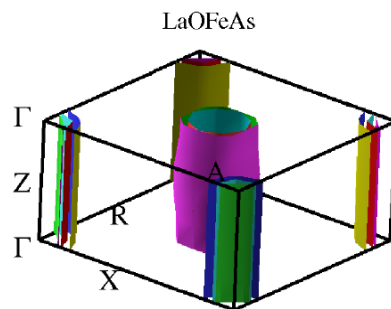
Out-of-phase (countersuperflow) mode (massive, Leggett 1966)

Two-band SC

Leggett mode observed in MgB_2 (Blumberg et al 2007)



Three-band SC



* Iron-compound

* Cold atoms on optical lattices
with multiple hyperfine states

Question: 3-band $\neq$ 2-band
in terms of the collective modes ?

Yes, **more than one collective Leggett modes** emerge
in 3-band SC

← large difference in mass when
multiple (internal) Josephson currents subtract

(Ota et al, arXiv:1008.3212)

Question here: 3-band = 2-band
in terms of the collective modes ?

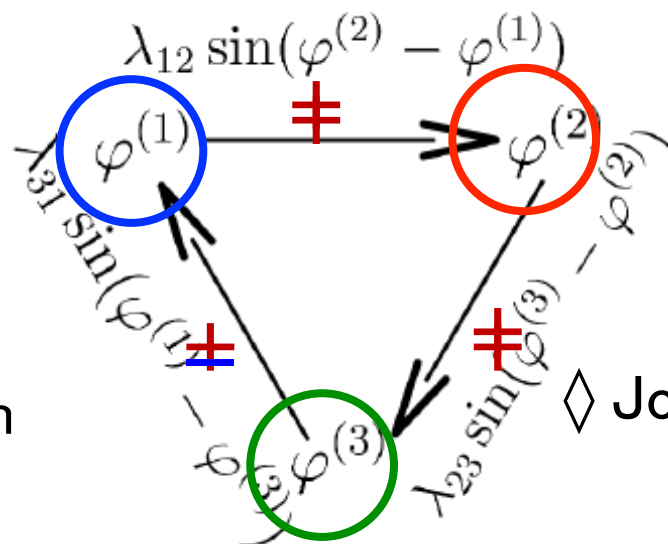
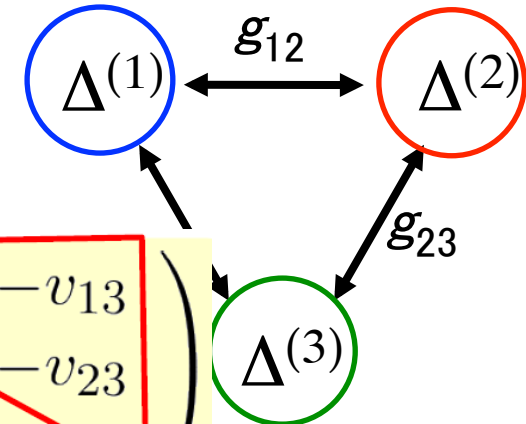
(Ota et al, 2010)

$$\hat{\mathcal{H}}_{\text{pair}} = - \sum_{i,j} g_{ij} \hat{\psi}_{\uparrow}^{(i)\dagger} \hat{\psi}_{\downarrow}^{(i)\dagger} \hat{\psi}_{\downarrow}^{(j)} \hat{\psi}_{\uparrow}^{(j)}$$

*i*th band *j*th band

$$\mathbf{g} = \begin{pmatrix} g_{11} & g_{12} & g_{13} \\ g_{12} & g_{22} & g_{23} \\ g_{13} & g_{23} & g_{33} \end{pmatrix}$$

$$\mathbf{g}^{-1} = \begin{pmatrix} v_{11} & -v_{12} & -v_{13} \\ -v_{12} & v_{22} & -v_{23} \\ -v_{13} & -v_{23} & v_{33} \end{pmatrix}$$



even / odd
← $(\mathbf{g}^{-1})_{ij}$

[class "even"]

→ internal Josephson
c's add

[class "odd"]

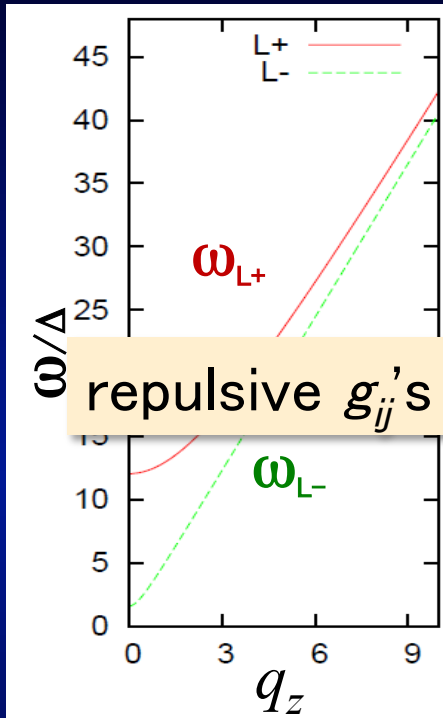
◇ Josephson c's subtract

When the pairing interactions g_{ij} are varied

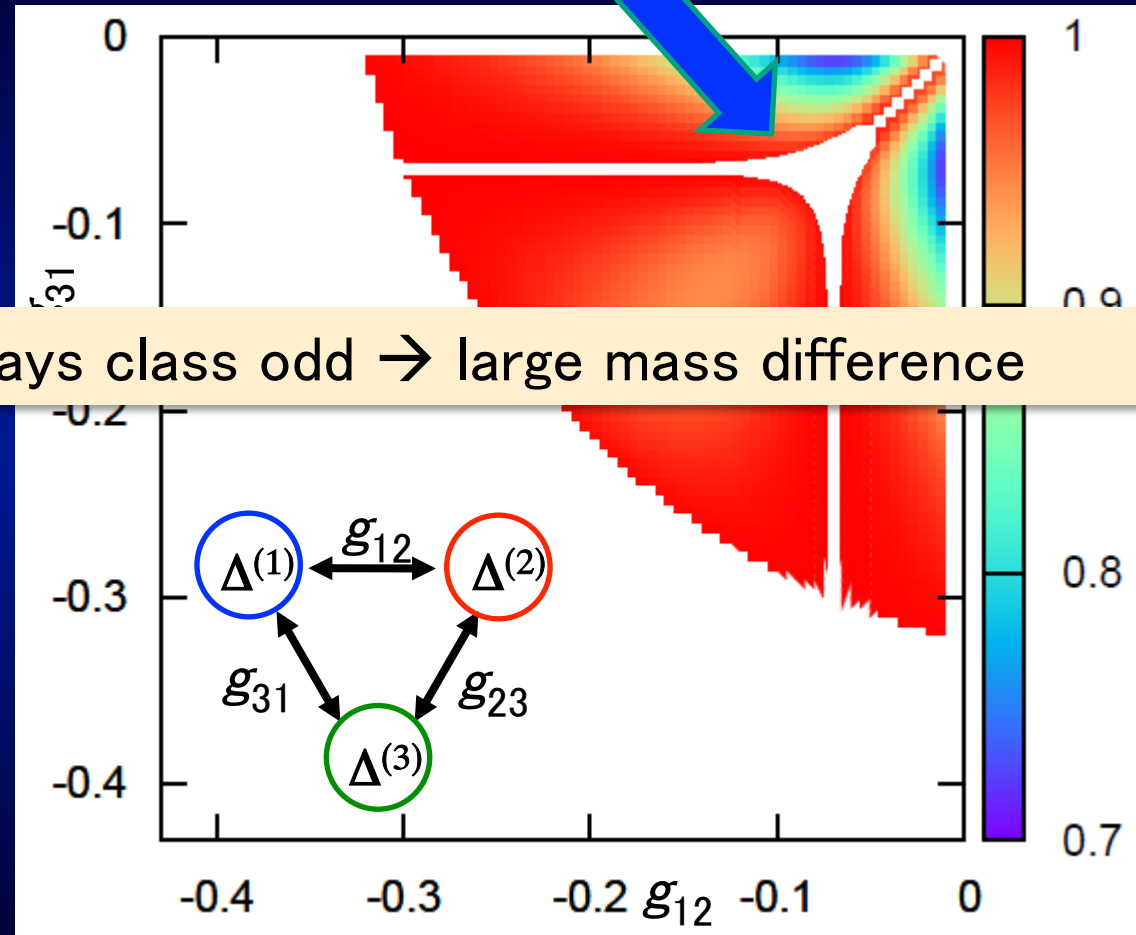
(Ota et al, arXiv1008.3212)

multiple Leggett modes

mass difference



repulsive g_{ij} 's $\rightarrow$ always class odd $\rightarrow$ large mass difference



$g_{23} = -0.07$

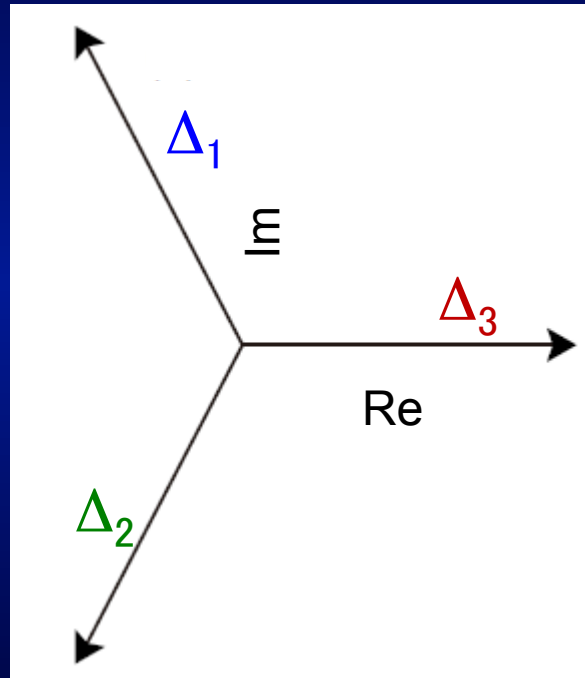
$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \begin{bmatrix} |d\rangle \\ |s\rangle \\ |b\rangle \end{bmatrix} = \begin{bmatrix} |d'\rangle \\ |s'\rangle \\ |b'\rangle \end{bmatrix}$$

“Frustration” in the three-band SC

→ complex (T-reversal broken) Δ

(Stanev & Tesanovic, PRB 2010)

when $|g_{12}| \sim |g_{23}| \sim |g_{31}|$



Summary and outlook

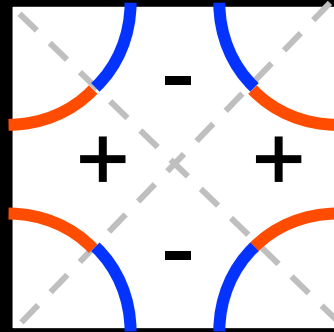
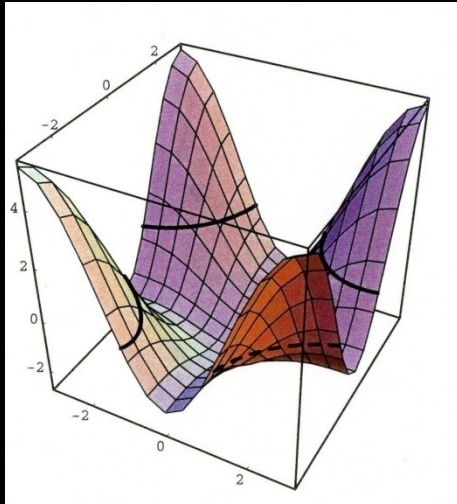
- ✓ Iron-based SC --- a prototype multiband SC
various possibilities incl. various pairings
- ✓ Collective phase mode in 3-band

Multiband SC → rich prospects

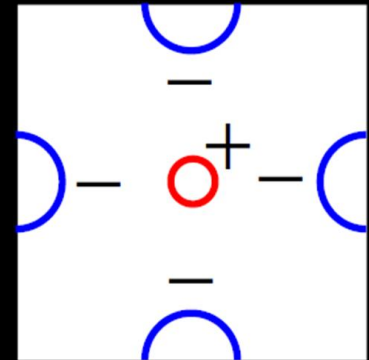
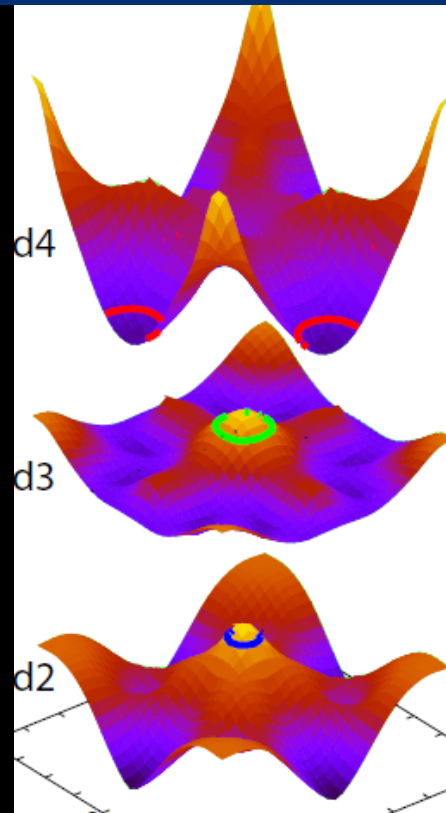
Other multiband SC's ?

- ✓ Even the cuprate has to be viewed as multiband

Cuprates: single-band



Iron-based: multi-band



Cuprates: still a lot of puzzles

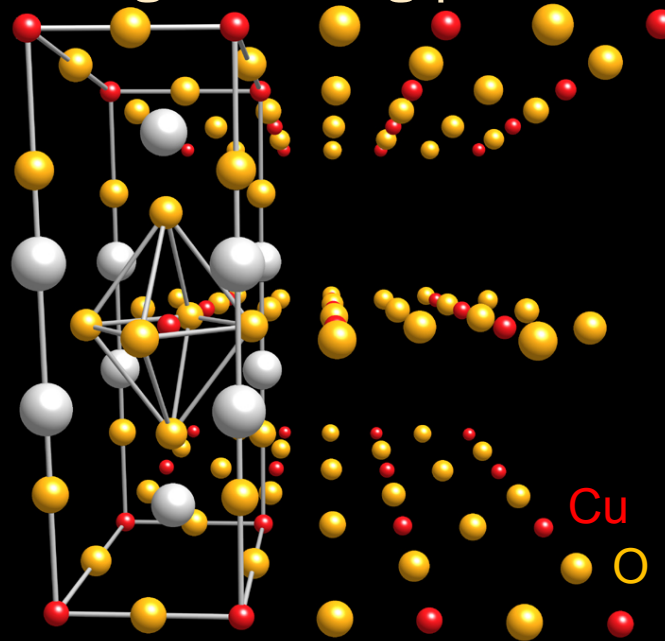
Various classes of cuprates

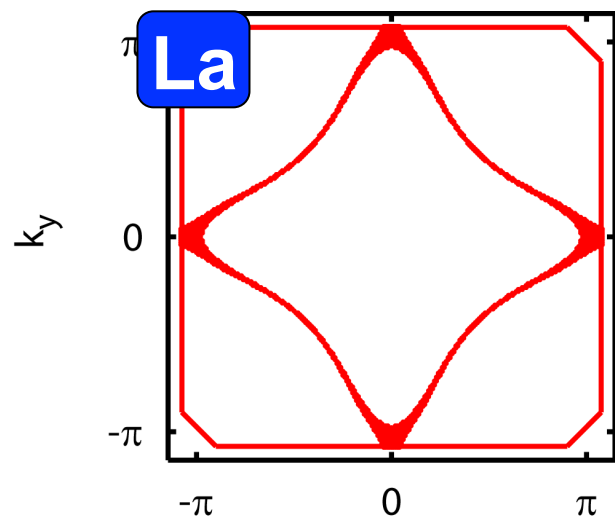
single-layered (simplest possible)

La_2CuO_4 : $T_c \sim 40\text{K}$

$\text{HgBa}_2\text{CuO}_4$: $T_c \sim 90\text{K}$

A long-standing puzzle

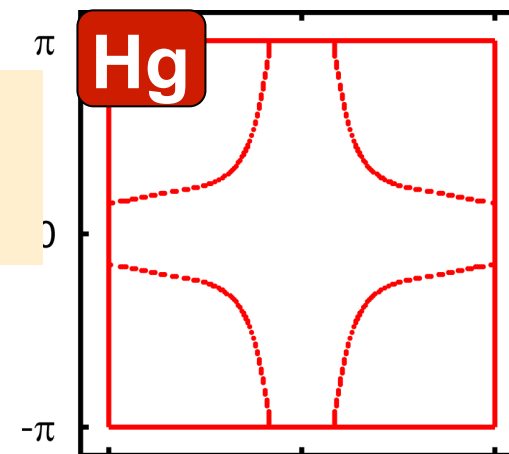




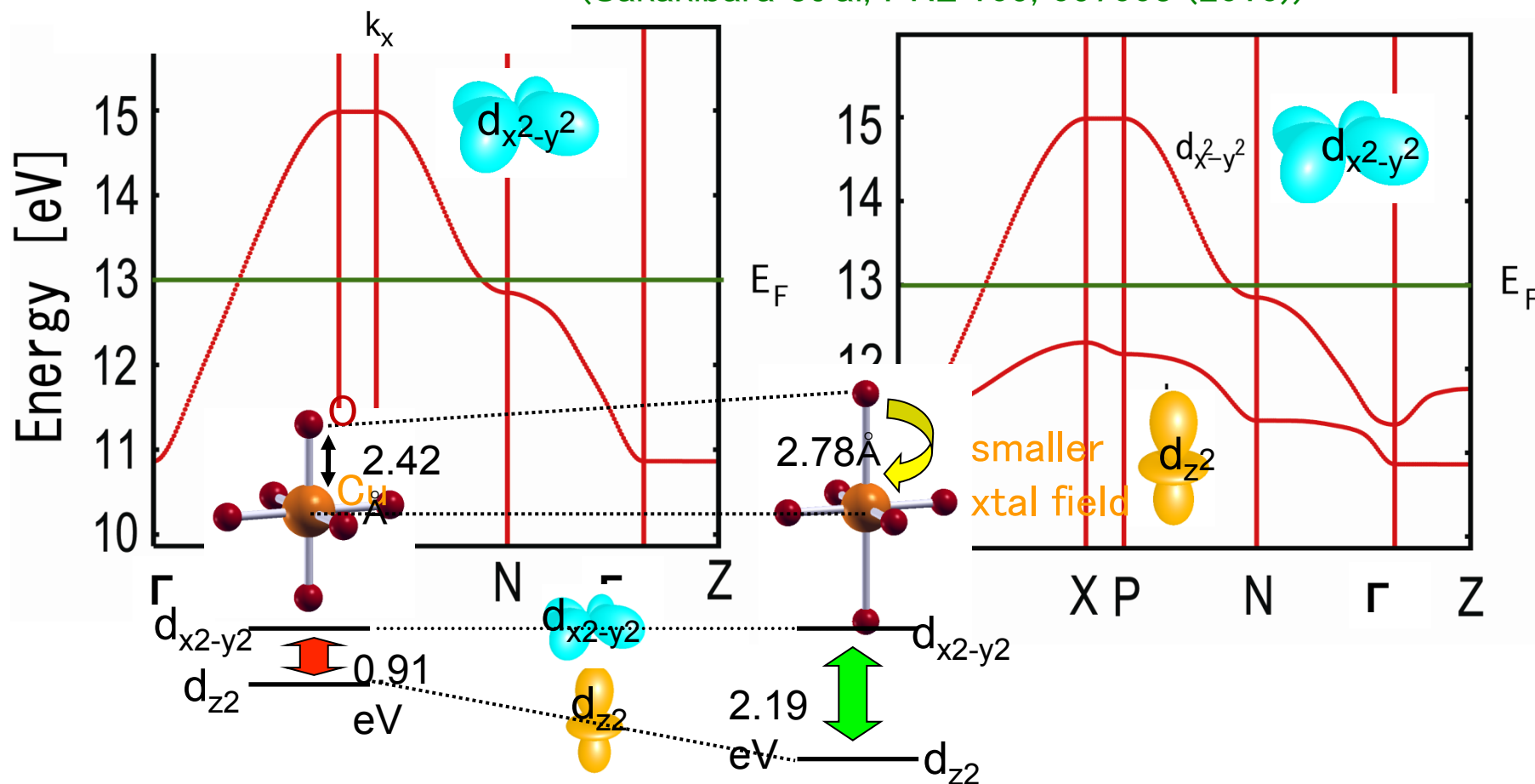
Th: $T_c(\text{La}) > T_c(\text{Hg})$

Ex: $40 \text{ K} < 90 \text{ K}$

contradiction!



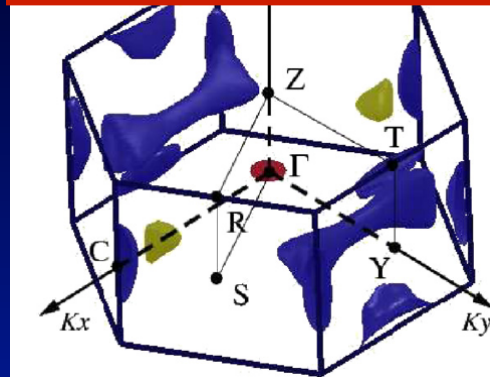
(Sakakibara et al, PRL 105, 057003 (2010))



Outlook (1): diverse multiband SC's

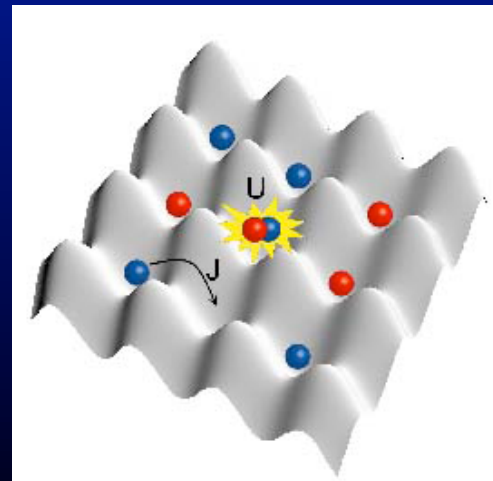
* Molecular solids tend to be multiband

Metallic H at 414 GPa



(Gross et al, 2009)

* Cold atoms
(different hyperfine states
on optical lattices)

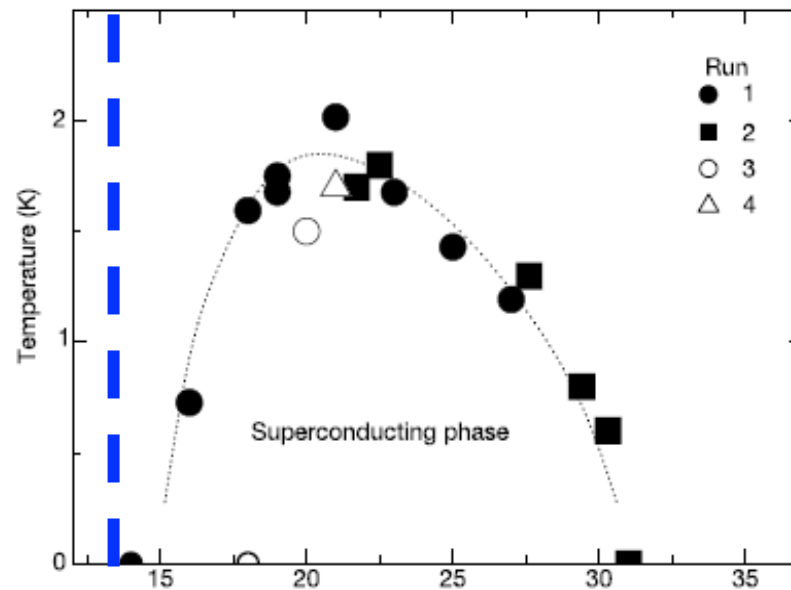


SC in elemental Fe under p

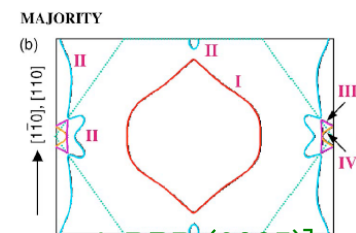
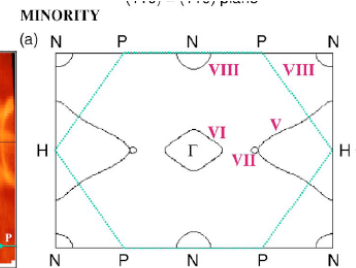
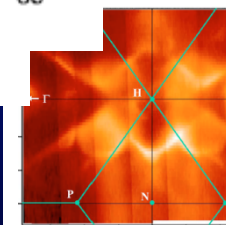
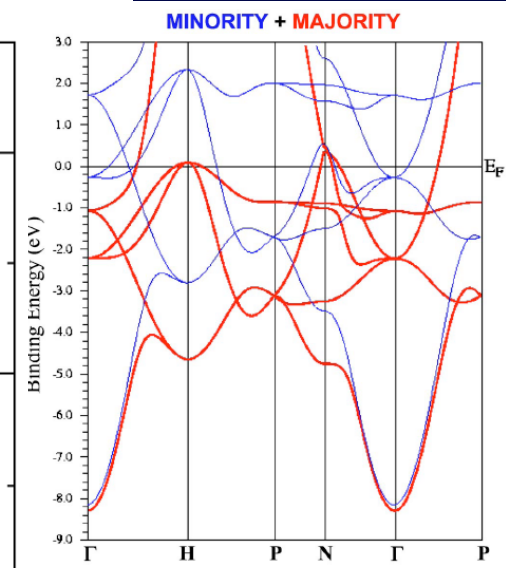


<http://www.physics.nmsu.edu>

[Shimizu et al, Nature 412, 316 (2001)]



bcc(magnetic) hcp(nonmagnetic, SC)



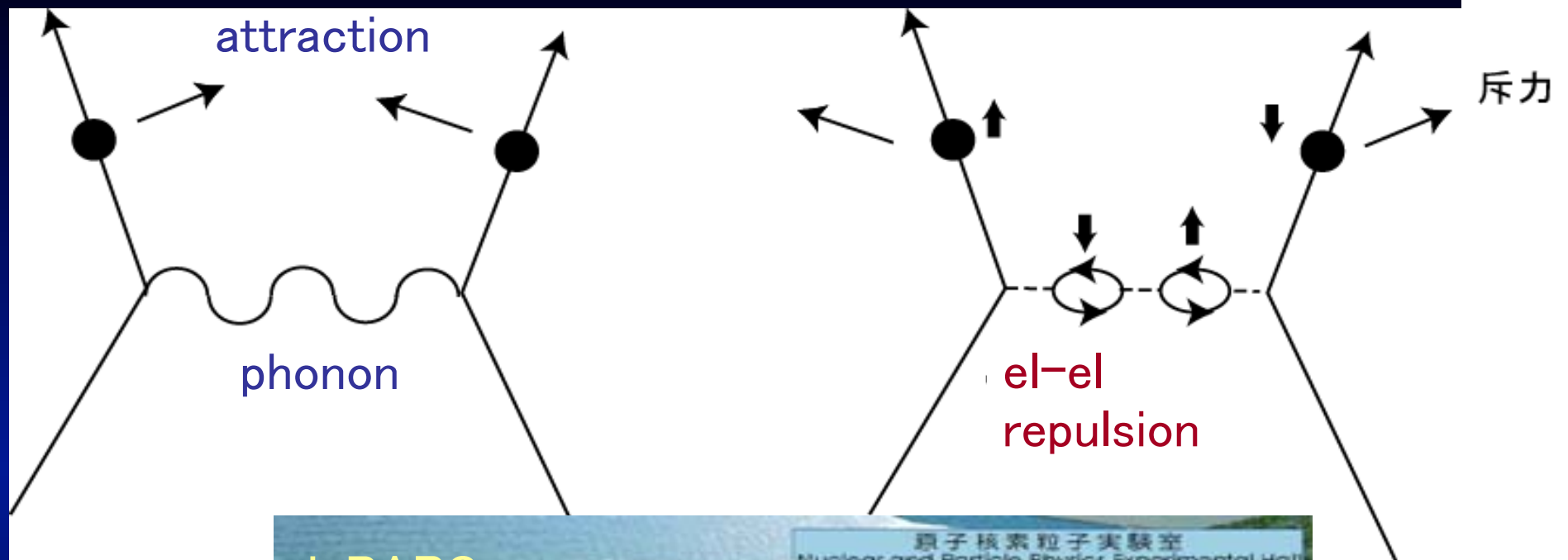
[Schafer et al, PRB (2005)]

Theories:

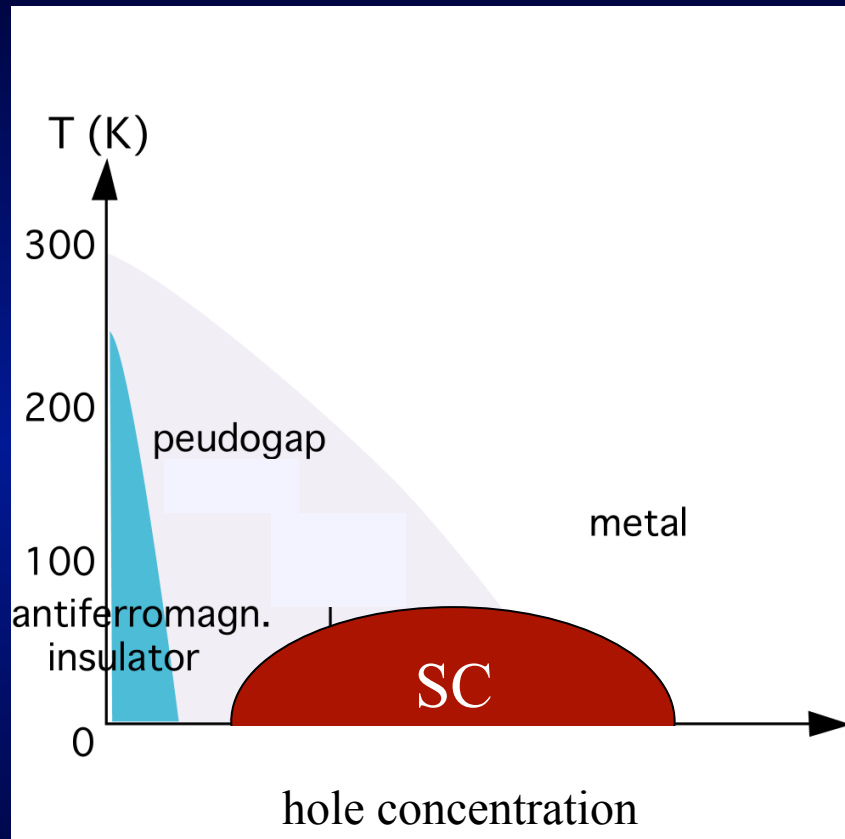
el-ph cannot explain T_c [Suzuki et al, 2002;
Mazin et al, PRB 2002],

→ spin fluctuations have to be considered

To actually look at the interactions

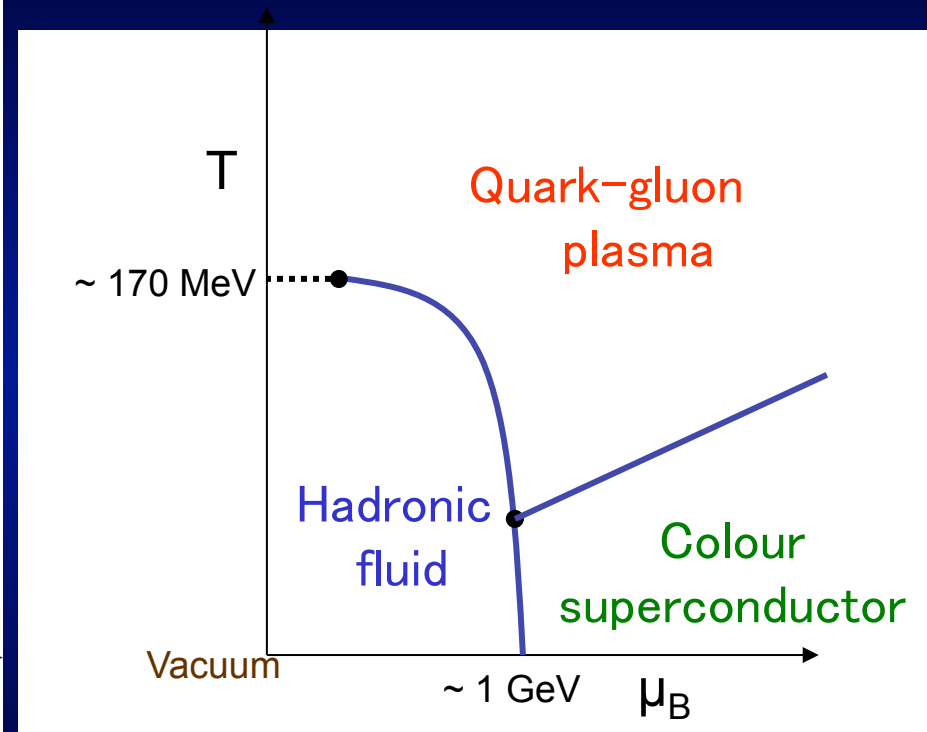


Outlook (2): Colour SC in hadron physics



Spin-fluct mediated,
Multi-band SC,

...



Gluon,
various SC phases,

...

Differences in SC in solid-state vs hadron phys

Energy scale	$\sim 10 \text{ meV}$	$\sim 100 \text{ MeV}$
Length scale	$1 \sim 10^3 \text{ nm}$	$1 \sim 10 \text{ fm}$
Particles involved	e's with anisotropic FS	relativistic quarks with isotr FS
Interaction	e-e, e-phonon	gluon-mediated long-range
T_c	$T_c \sim 0.01 \epsilon_F$	$T_c \sim 0.1 \epsilon_F$
<u>Internal deg</u>	<u>spin, orbit</u>	<u>colour, flavour, spin</u>
Order of phase tr	weakly 1st $\leftarrow$ fl of EM	1st $\leftarrow$ thermal fl of gluons