

A new control parameter for the glass transition of glycerol.

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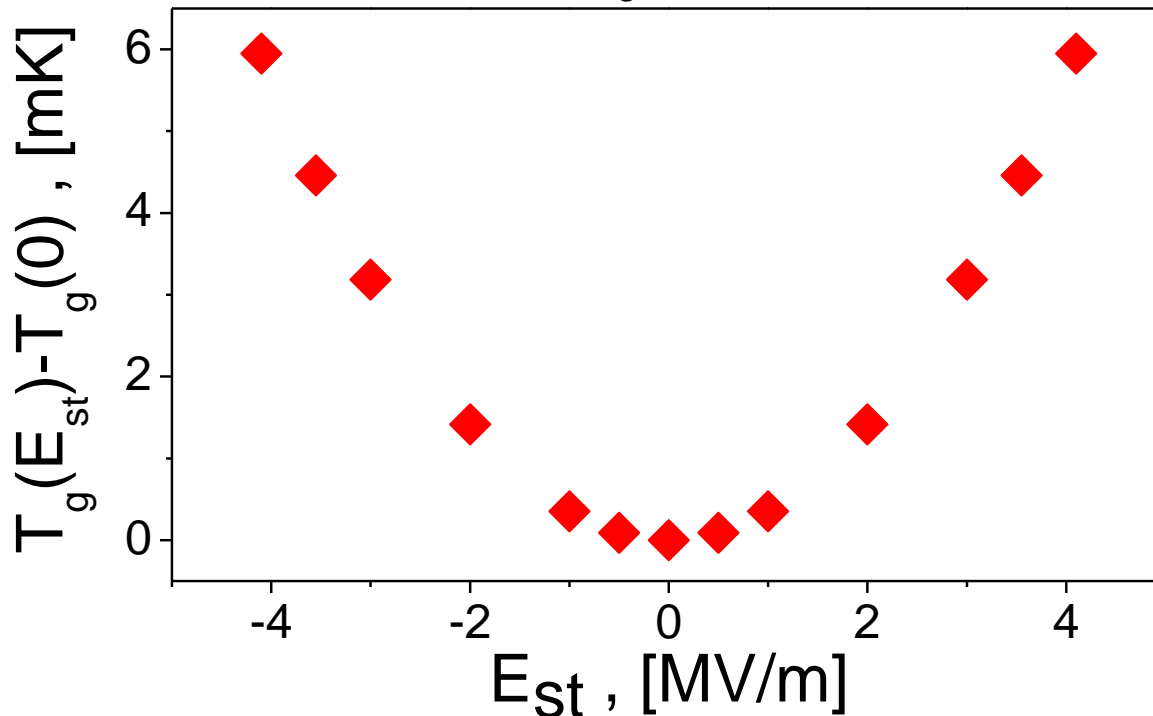


Additional Funding:



The most emblematic claim of this work :

Glycerol ($T_g = 187\text{K}$ at $E_{st} = 0$)



- E_{st} is a new control parameter in Glycerol.
- Previously, the unique way to change T_g was the Pressure Π

- Small effect: discovered through a nonlinear technique (see L'Hôte, Tourbot, Ladieu, Gadige PRB 90, 104202 (2014))

- As for Π exp^{ts}, the most interesting is not $T_g(\Pi)$ in itself but what we learn about the glass transition when varying the control parameter.

Outline:

I) Motivations for nonlinear experiments

- What happens around T_g ?
- Dynamical Heterogeneities
- Special interest of nonlinear responses !

II) Our specially designed experiment

→ it works !

III) Results on Glycerol

- Order of magnitude and comparison to the Box model
- Relation to N_{corr}
- T_g shift

Summary and Perspectives.

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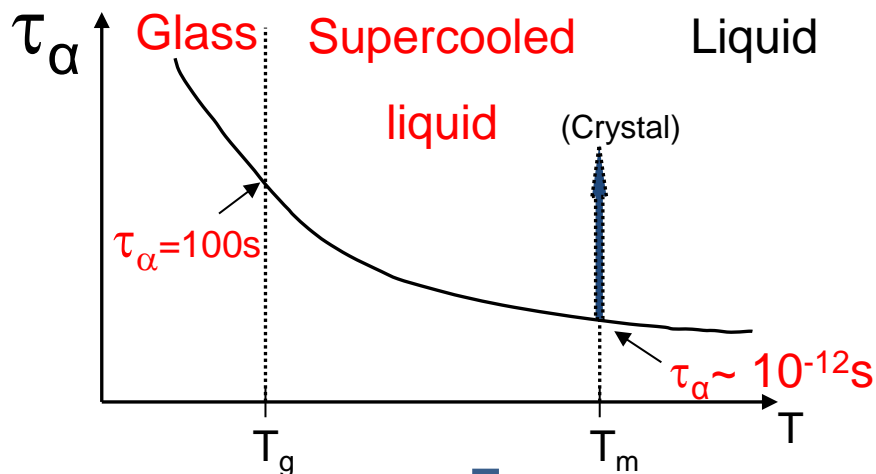
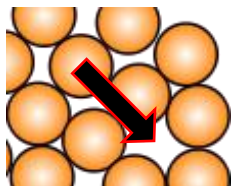
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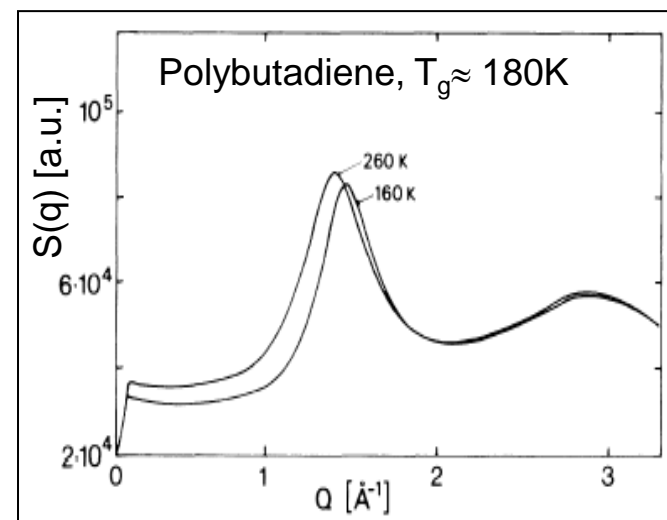
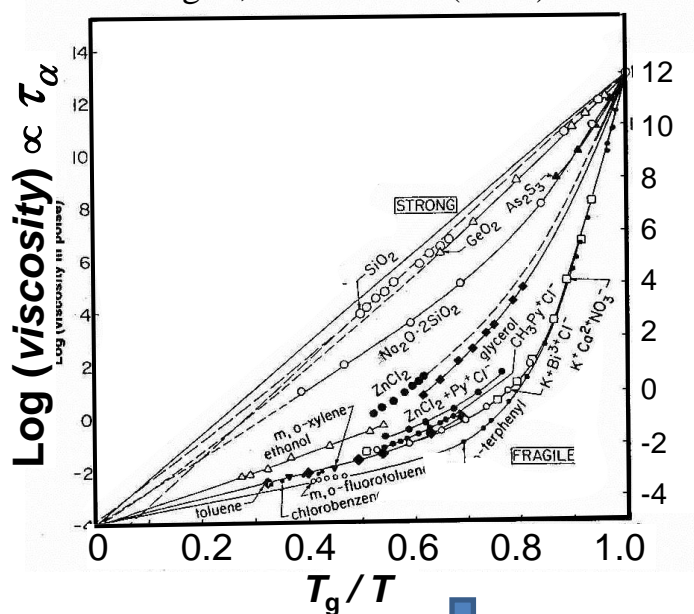
What happens around T_g ?

Relaxation time τ_α



$\eta \sim \tau_\alpha \sim e^{\frac{E_a}{T}}$
 $E_a \nearrow$ when $T \searrow$
 \Rightarrow Correlations \nearrow when $T \searrow$

Angell, Science **267** (1995)



No (static) order

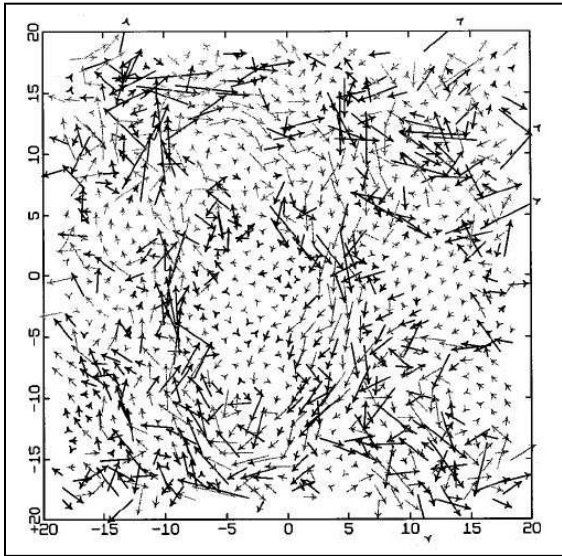
How to combine the existence of correlations with the absence of order ?

Dynamical Heterogeneities in supercooled liquids

- N_{corr} = average number of dynamically correlated molecules : $N_{corr} \propto \xi^3$

... directly observed in granular matter or in numerical simulations.

Example : numerical simulations on soft spheres :

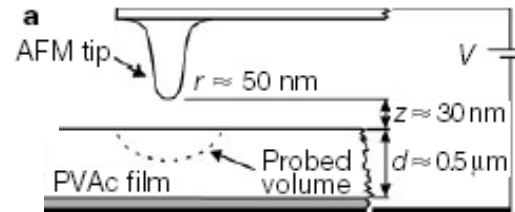


Hurley,
Harowell,
PRE, 52,
1694, (1995)

... Experimentally, the heterogeneous nature of the dynamics has been established through various breakthroughs:

- NMR experiments Tracht *et al.* PRL81, 2727 (98), J. Magn. Res. 140 460 (99),...

- Local measurements E. Vidal Russell and N.E. Israeloff, Nature 408, 695 (2000).



« clusters »
of 30-90
monomers

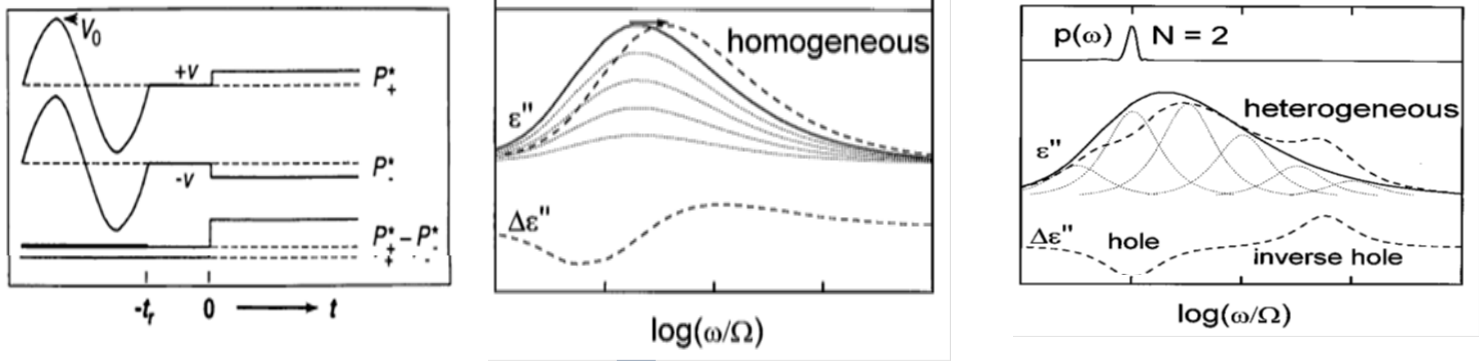
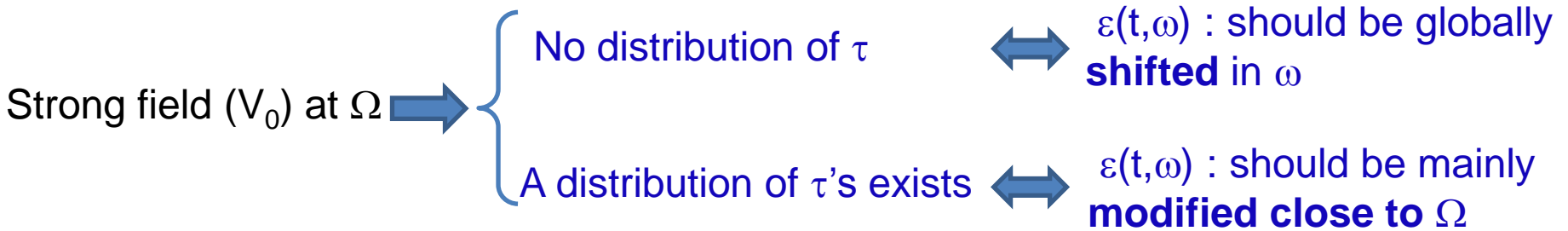
- Hole burning experiments

When $T \downarrow$: N_{corr} **would** \uparrow , which **would** explain why τ_α increases so much

Dynamical Heterogeneities and NHB.

- Many **improvements** since Schiener, Böhmer, Loidl, Chamberlin Science, **274**, 752, (1996)
 e.g. R.Richert's group: PRL, **97**, 095703 (2006); PRB **75**, 064302 (2007); EPJB, **66**, 217, (2008); PRL, **104**, 085702, (2010)...

- The central idea in Schiener et al 's seminal paper in 1996:



Non Res Hole Burning: \Rightarrow supercooled dynamics IS heterogeneous (at least in time)

•... Can nonlinear experiments give MORE than originally expected ??.... \rightarrow

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Summary and Perspectives.

The prediction of Bouchaud-Biroli (\Leftrightarrow B&B): PRB 72, 064204 (2005)

DH characterisation \Leftrightarrow

$$g_4(\vec{r}, t) = \langle \bar{p}(\vec{0}, 0) \bar{p}(\vec{0}, t) \bar{p}(\vec{r}, 0) \bar{p}(\vec{r}, t) \rangle_c$$

AND

$N_{\text{corr}} \ll \text{large enough} \gg$

$$E(t) = E e^{i\omega t} \quad \frac{P}{\epsilon_0} = \chi_{\text{Lin}} E + \chi_3 E^3 + \dots$$

$$\chi_3(\omega, T) = \frac{\epsilon_0 \chi_s^2 a^3}{k_B T} N_{\text{corr}}(T) H(\omega \tau_\alpha(T))$$

Natural scale of χ_3

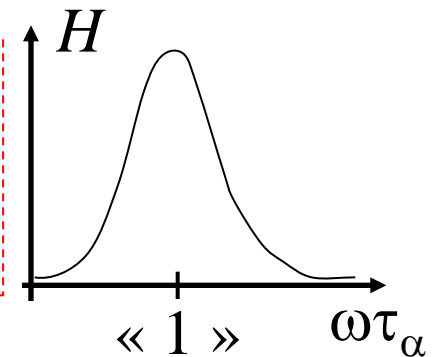
χ_s = static value of χ_{Lin}

a^3 = molecular volume

N_{corr} = number of dynamic. correlated molec.

$\tau_\alpha(T)$: typical relaxation time

H : scaling function



Systematic $\chi_3(\omega, T)$ measurements to test the prediction and possibly get $N_{\text{corr}}(T)$

The issue of interpretations : Box Model versus B&B

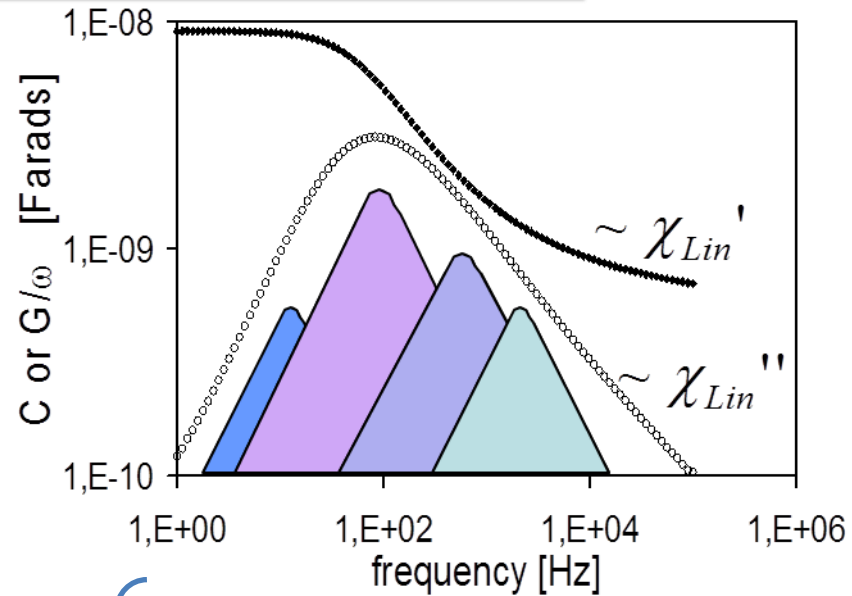
Box model assumptions (designed for NHB):

→ Each DH « k » has a Debye dynamics.
 $\{\tau_k\}$ chosen to recover $\chi_{lin}(\omega)$ at each given T.

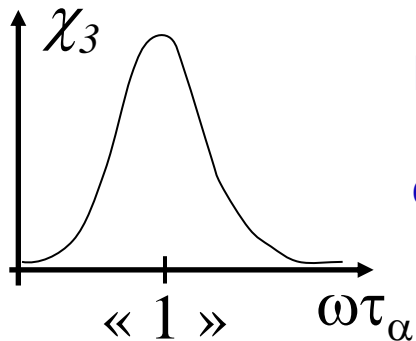
→ Applying E: each DH « k » is heated by δT_k (τ_{therm})

with $\tau_{therm} \sim \tau_k$.

↔ as $\{\tau_k\} \sim \tau_\alpha$ heat diffusion **over one DH** takes a **macroscopic time** close to T_g .



$$\left\{ \begin{array}{l} \tau_k \frac{\partial(\delta T_k)}{\partial t} + \delta T_k = \frac{\text{heat power density}}{c} \\ \text{(heat power density} \sim \chi_k'' \omega E^2) \end{array} \right\} \xrightarrow{\delta T_k \sim E^2} \left\{ \begin{array}{l} P_k - P_{k, Lin} = \frac{\partial P_{k, Lin}}{\partial T} \delta T_k \sim E^3 \\ (P_{k, Lin} \sim \chi_k E) \end{array} \right.$$



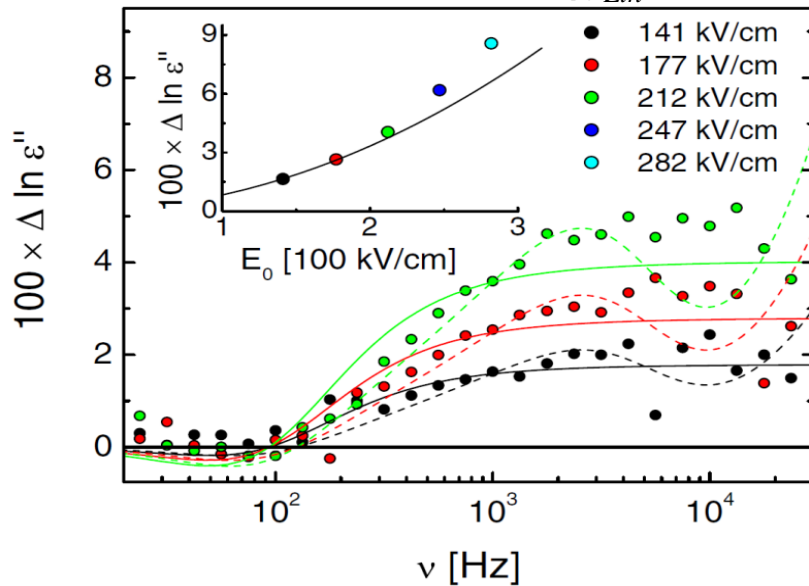
For a pure ac field $E_{ac} \cos(\omega t)$:
 ω and T dependences are **qualitatively similar** in the Box model and in B&B

χ_3 does NOT contain N_{corr} (Box model is space free)

$\chi_3(\omega, T) : N_{corr}(T)$ or not ?

Some experiments done since B&B's prediction (2005)

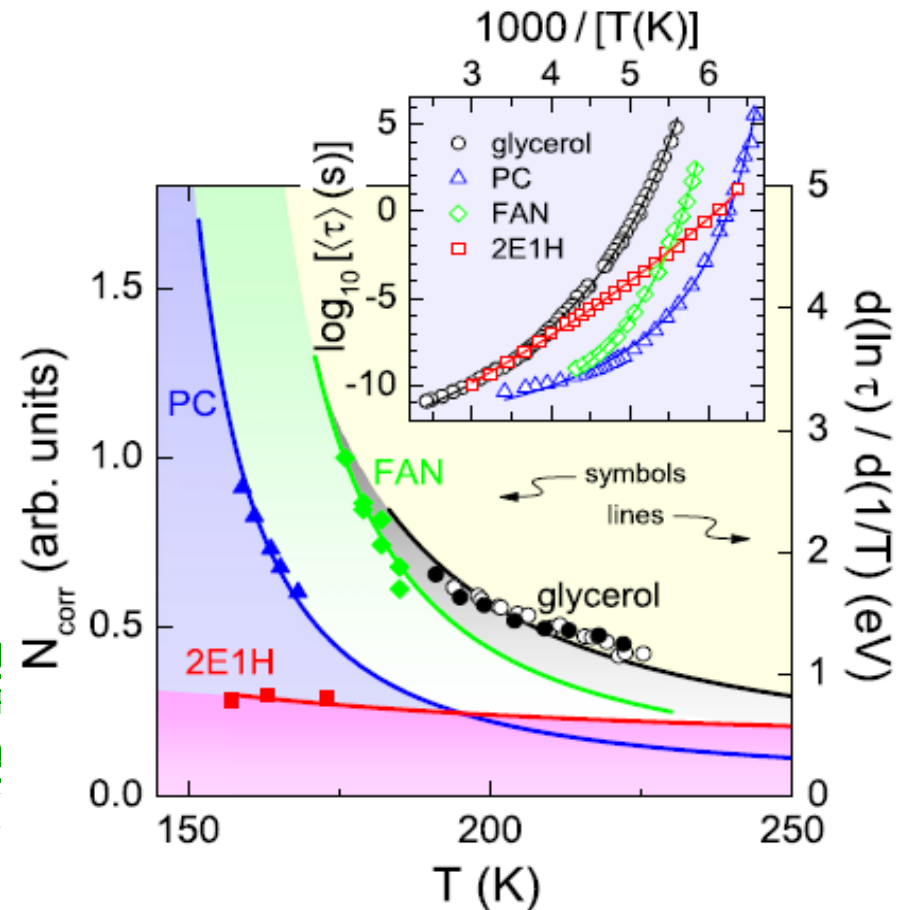
Box model :
$$\delta \ln \varepsilon'' = \frac{-\text{Im}(\chi_3^{(1)})E^2}{\text{Im}(\chi_{Lin})}$$



e.g. R.Richert's group: PRL, **97**, 095703 (2006); PRB **75**, 064302 (2007); EPJB, **66**, 217, (2008); PRL, **104**, 085702, (2010)...

- Very good fits at 1ω (better than at 3ω)
- Accounts for the transient regime at 1ω
- Several liquids tested (Richert PRL (2007))

B&B: $\chi_3^{(1)}$ as well as $\chi_3^{(3)}$



- Evolution of $N_{\text{corr}}(T)$ or of $N_{\text{corr}}(t_a)$
- Several liquids tested (Bauer, Lunkenheimer, Loidl, PRL **111**, 225702 (2013))



Using E_{st} will shed a new light on this interpretation issue

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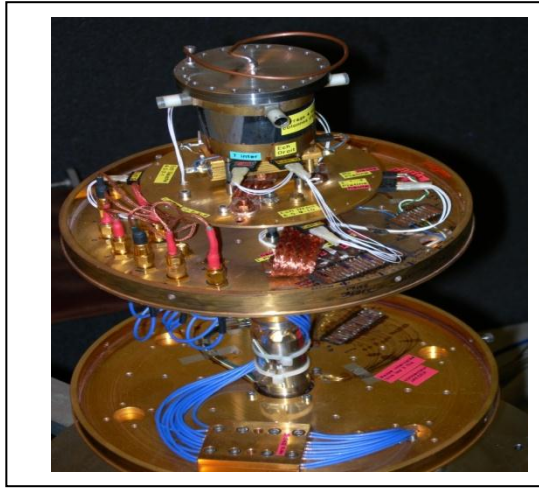
II) Our specially designed experiment

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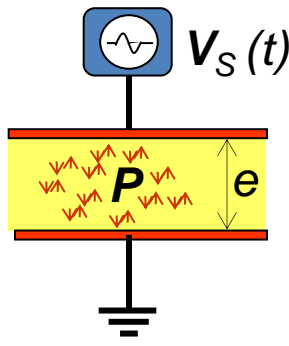
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Summary and Perspectives.

Dielectric setup and orders of magnitude



Supercooled liquid, controlled T



For "low enough" E

$$\frac{P(t)}{\epsilon_0} = \underbrace{\int_{-\infty}^{+\infty} \chi_{lin}(t-t')E(t')dt'}_{\text{Linear term}} + \underbrace{\int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \chi_3(t-t'_1, t-t'_2, t-t'_3)E(t'_1)E(t'_2)E(t'_3)dt'_1 dt'_2 dt'_3}_{\text{First non-linear term}} + \dots$$

First non-linear term

$$E(t) = E_{ac} \cos(\omega t) + E_{st}$$

$$\frac{P(t) - P_{Lin}}{\epsilon_0} = \frac{1}{4} E_{ac}^3 \text{Re} \left[3\chi_3^{(1)}(\omega) e^{-j\omega t} + \chi_3^{(3)}(\omega) e^{-j3\omega t} \right] + 3E_{st}^2 E_{ac} \text{Re} \left[\chi_{2;1}^{(1)}(\omega) e^{-j\omega t} \right] + \text{even harmonics}$$

$$\chi_3^{(1)}(\omega) = F.T. \{ \chi_3 \}_{(-\omega, \omega, \omega)} \quad \chi_{2;1}^{(1)}(\omega) = F.T. \{ \chi_3 \}_{(0, 0, \omega)}$$

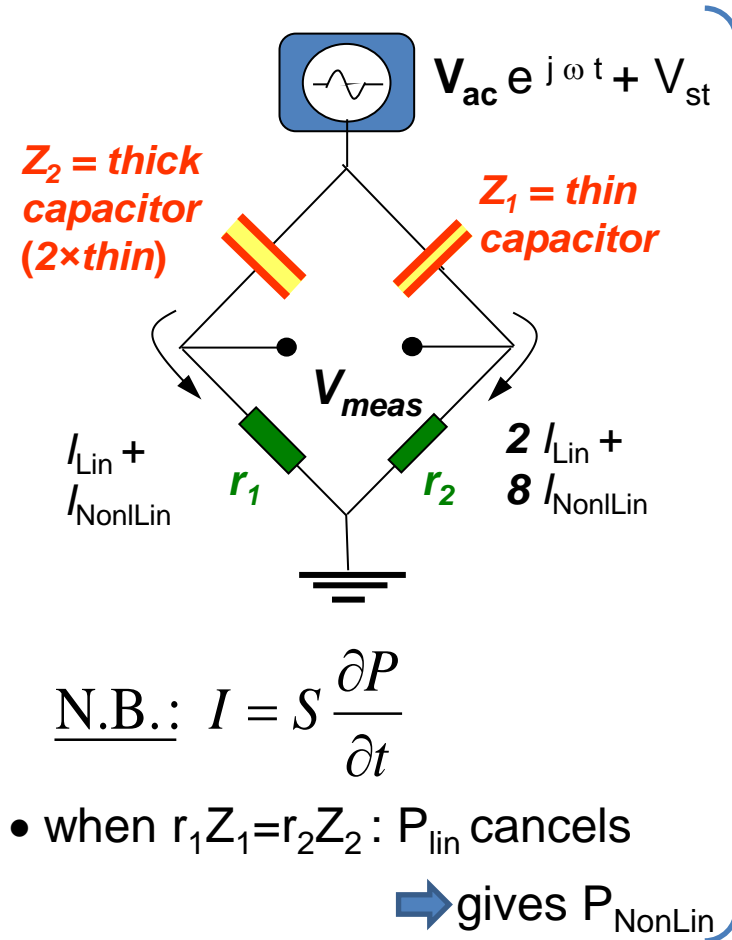
$$\chi_3^{(3)}(\omega) = F.T. \{ \chi_3 \}_{(\omega, \omega, \omega)}$$

For $E \approx 1 \text{ MV/m}$, $\frac{\text{cubic terms}}{\text{linear term}} \approx 10^{-6} - 10^{-4} \Rightarrow$ Specially designed setup

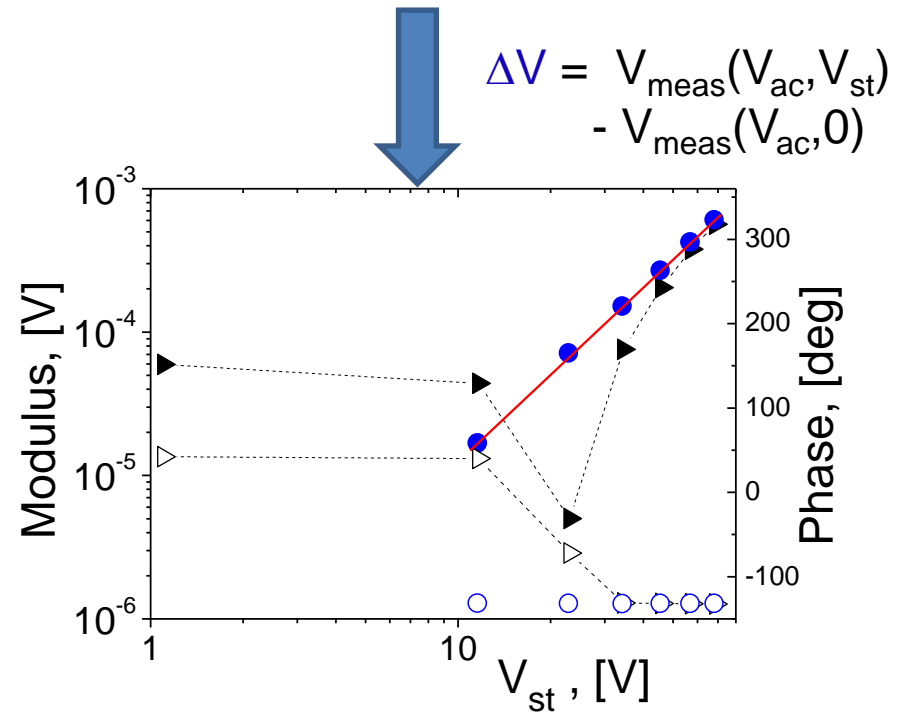
Our setup to measure cubic susceptibilities

Bridge with two glycerol-filled capacitors of different thicknesses

C. Thibierge et al, RSI
79, 103905 (2008))



$$\left(\frac{P - P_{Lin}}{\epsilon_0} \right)_{1\omega} = \frac{3}{4} E_{ac}^3 \text{Re} \left[\chi_3^{(1)}(\omega) e^{-j\omega t} \right] + 3 E_{st}^2 E_{ac} \text{Re} \left[\chi_{2;1}^{(1)}(\omega) e^{-j\omega t} \right]$$



$\Delta V \sim V_{st}^2 V_{ac}$

Phase (ΔV) = cte

→ $\chi_{2;1}^{(1)} \propto \frac{\Delta V}{V_{st}^2 V_{ac}}$

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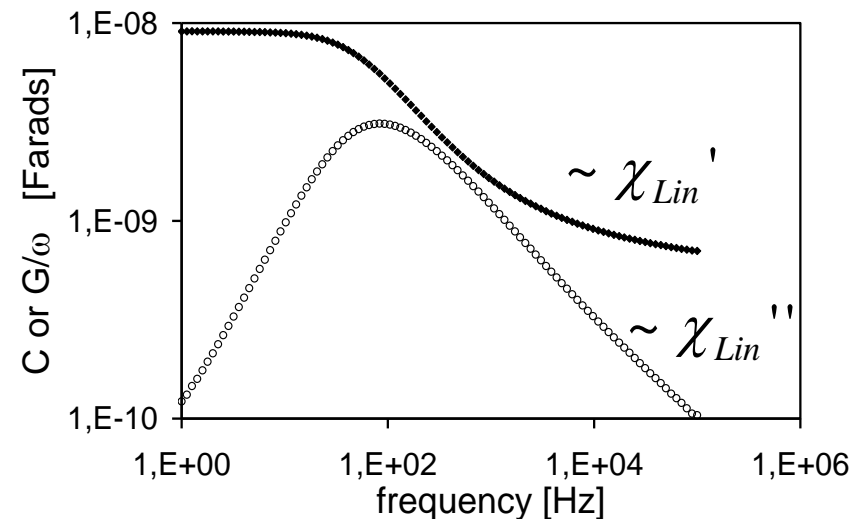
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Summary and Perspectives.

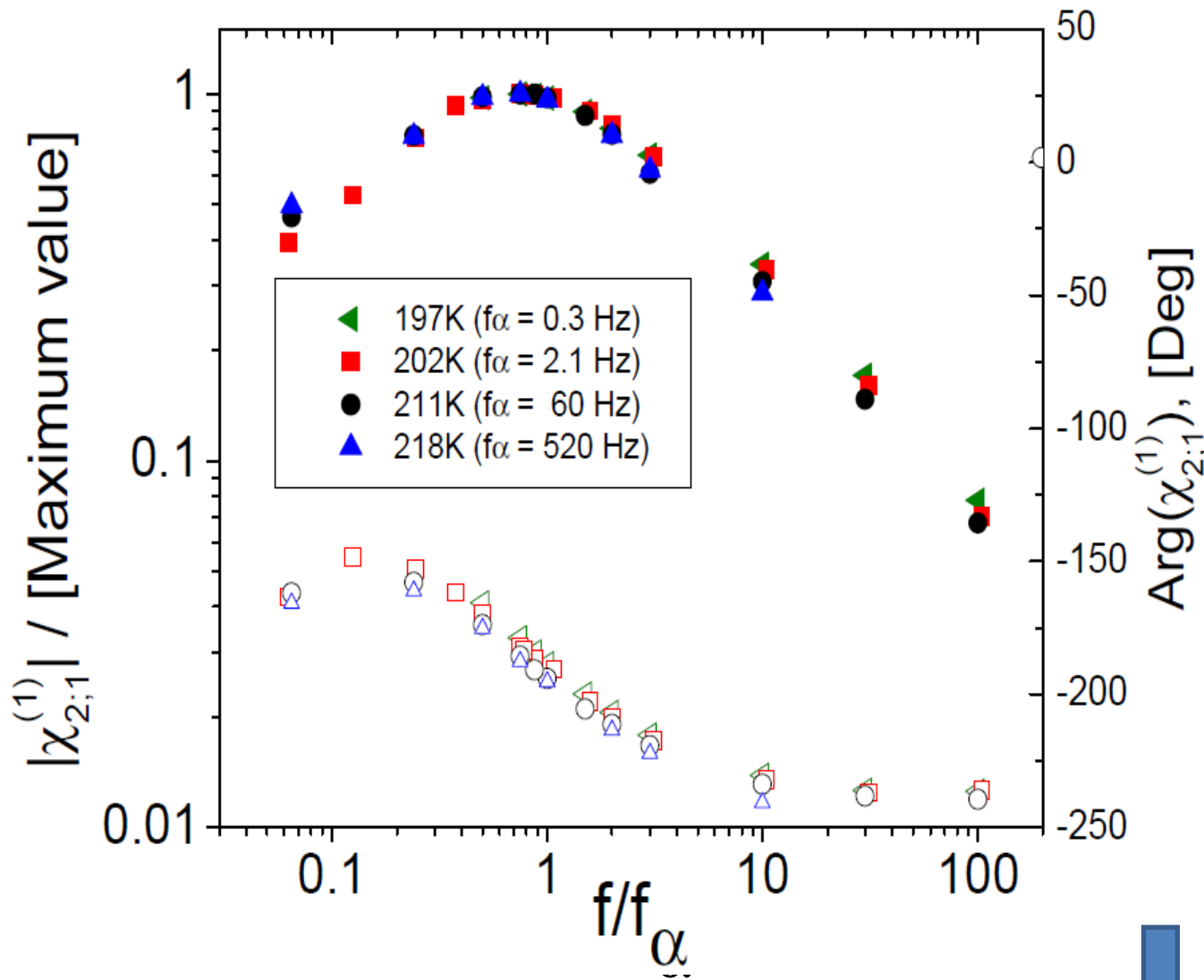
• NB: $\omega\tau_{\alpha} \equiv f/f_{\alpha}$

$f_{\alpha} \Leftrightarrow$ peak of $\chi_{\text{lin}}''(\omega)$

$|\chi_{\text{lin}}(\omega)|$ has no peak



Main features of $\chi_{2;1}^{(1)}(\omega, T)$



At constant T:

- humped shape for $|\chi_{2;1}^{(1)}|$
- maximum happens in the range of f_α

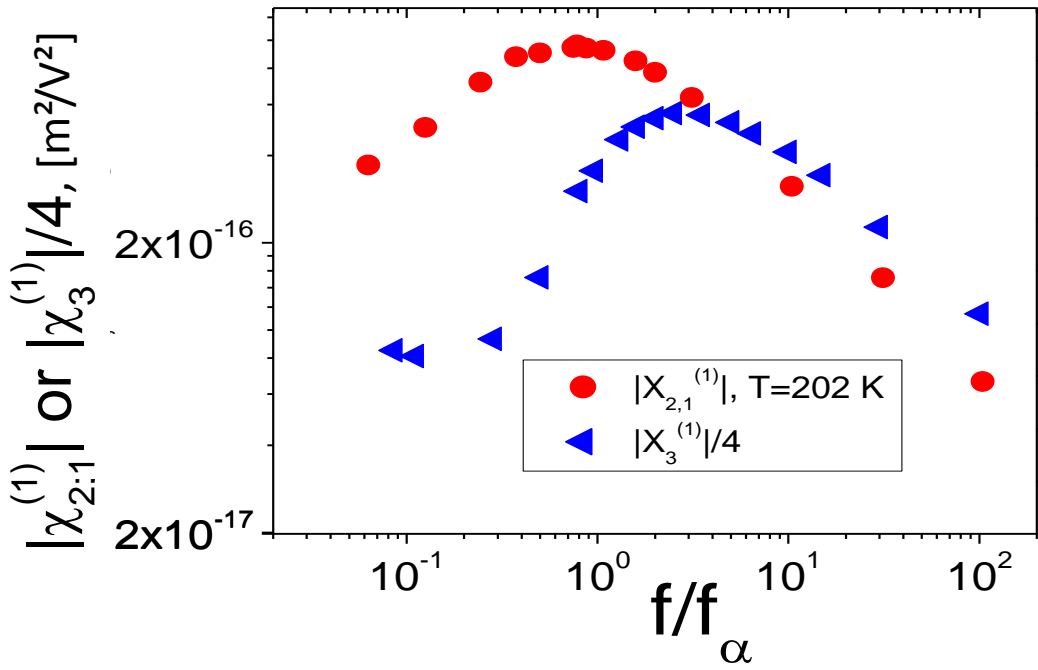
Scaling of the hump in T



Same qualitative trends as for $\chi_3^{(1)}$ and $\chi_3^{(3)}$

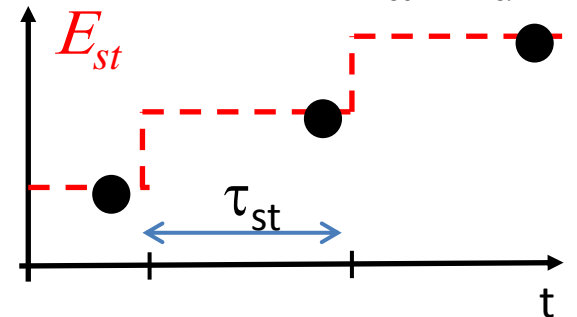
Comparing $\chi_{2;1}^{(1)}(\omega, T)$ and $\chi_3^{(1)}(\omega, T)$

$$\left(\frac{P - P_{Lin}}{\epsilon_0}\right)_{1\omega} = \frac{3}{4} E_{ac}^3 \text{Re}[\chi_3^{(1)}(\omega)e^{-j\omega t}] + 3E_{st}^2 E_{ac} \text{Re}[\chi_{2;1}^{(1)}(\omega)e^{-j\omega t}] \Rightarrow \text{Compare } |\chi_3^{(1)}|/4 \text{ and } |\chi_{2;1}^{(1)}|$$



→ Same order of magnitude

→ Measurements (●) are in the stationary regime ($\tau_{st} \gg \tau_\alpha$)



Varying $E_{st} \Leftrightarrow$ ZERO dissipated power

In the Box Model:
 $\delta T_k \sim$ dissipated power

Box model's prediction : $|\chi_{2;1}^{(1)}| \ll |\chi_3^{(1)}|$

↓ (ions)

Box model's prediction is too small by a factor 300 for $|\chi_{2;1}^{(1)}|$

For the first time, Box Model is unable to account for a cubic response:

→ **Decisive point for the interpretation issue ...**

The latest paper: Samanta, Richert, J.Chem.Phys. 142, (2015).

$$\Delta S \sim \varepsilon_0 (E_{static})^2 \frac{\partial(\Delta\chi_1)}{\partial T} \text{ plugged in } Ln(\tau_\alpha) = \frac{A}{T S_c(T)} \Rightarrow \delta T_g \sim (E_{static})^2$$



$\chi_{2;1}^{(1)}$: E_{static} entropy variation

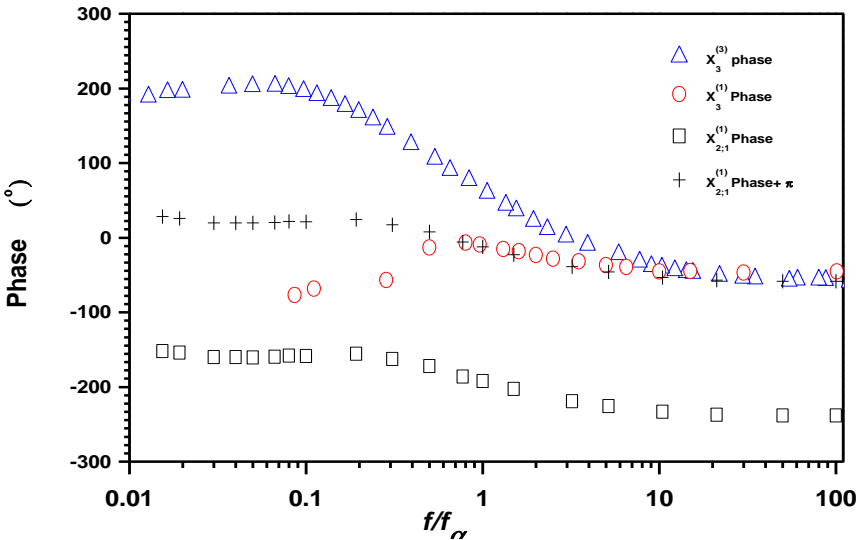
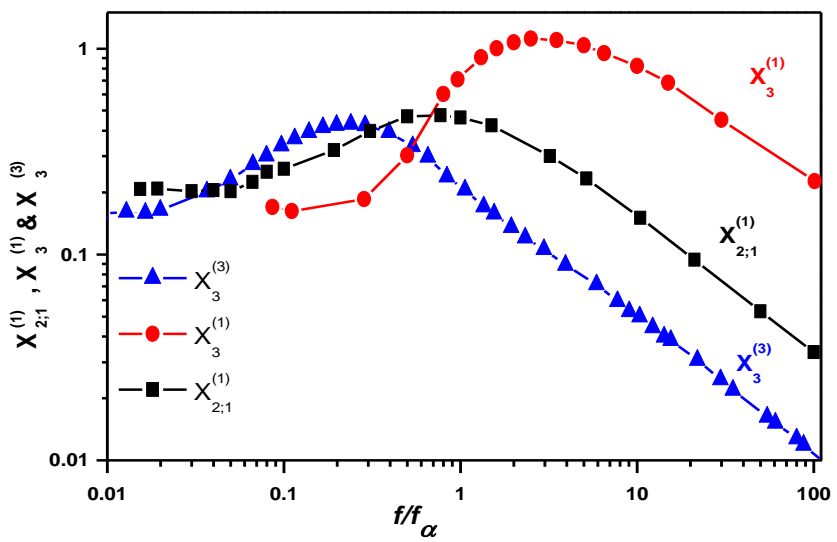
$\chi_3^{(1)}$ and $\chi_3^{(3)}$: E_{ac} heating (box model)



Two different mechanisms at play ?



Very unlikely due to the similarities of $\chi_{2;1}^{(1)}$, $\chi_3^{(1)}$, and $\chi_3^{(3)}$.



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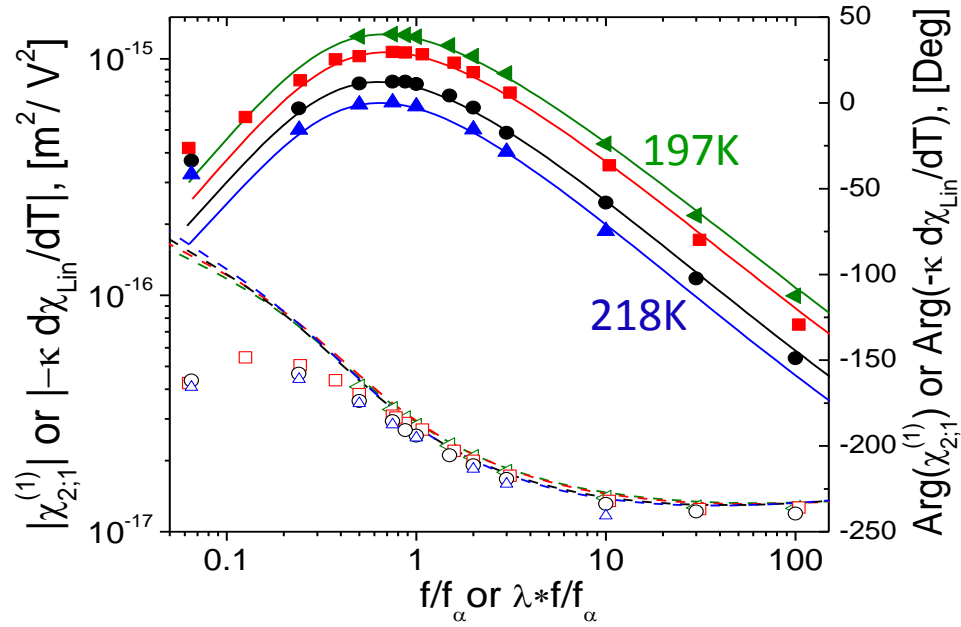
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Summary and Perspectives.

Comparing the ω dependences of $\chi_{2;1}^{(1)}(\omega, T)$ and of $\left(\frac{\partial \chi_{Lin}}{\partial T}\right)_{E_{st}=0}$



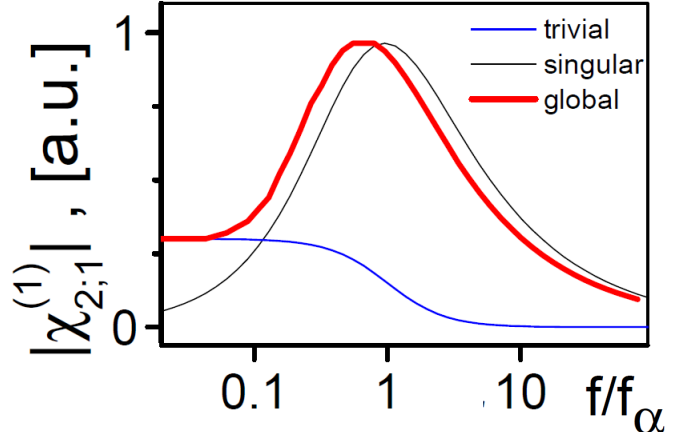
• For $f/f_\alpha > 0.2$:

$$\chi_{2;1}^{(1)}(T, \omega) = -\kappa \left(\frac{\partial \chi_{Lin}}{\partial T} \right)_{0, T, \frac{\omega}{\lambda}}$$

with $\kappa \cong 1.2 \times 10^{-16} \frac{Km^2}{V^2}$, $\lambda \cong 0.80$

∇T
 for both Re and Im parts

Direct link with $n_{corr}^{estim} \sim T \frac{d\chi_{Lin}}{dT}$ expected from Berthier et al., Science (2005); JCP, (2007); PRE (2007).



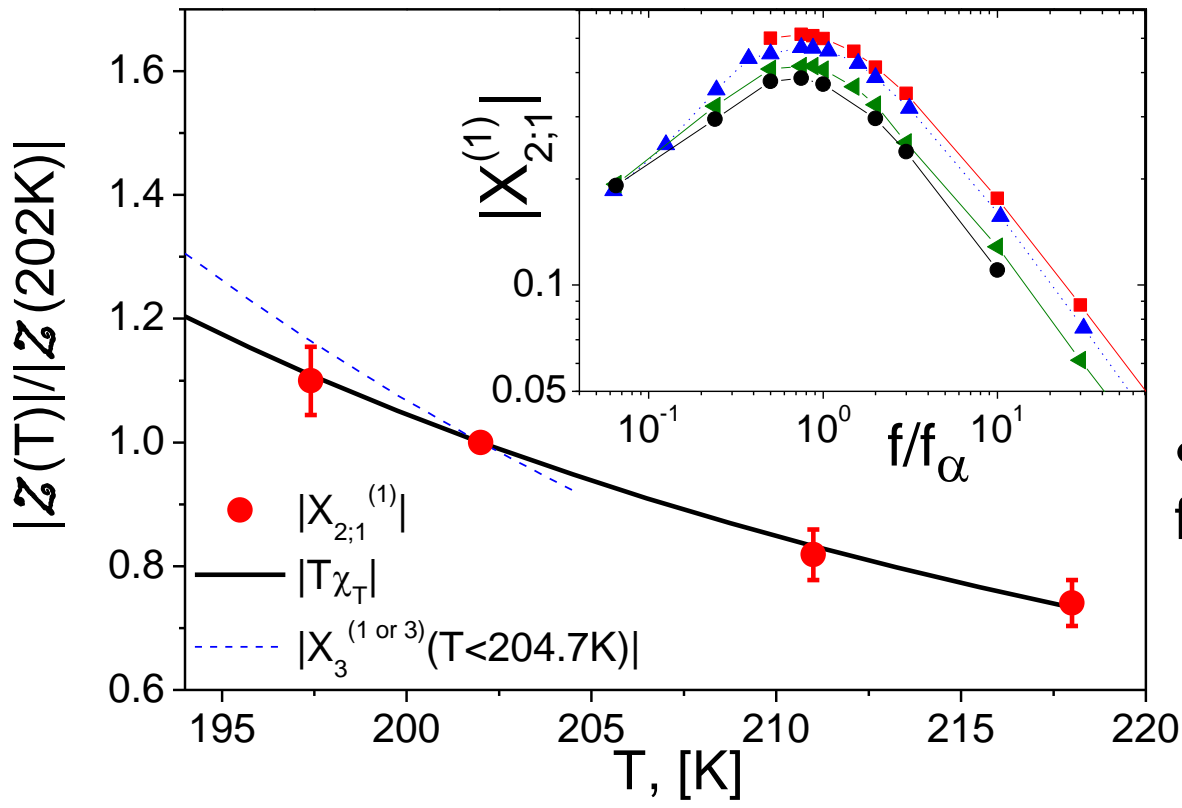
• For $f/f_\alpha < 0.2$: “Trivial” dominates
 Reshuffling \Rightarrow Ideal gas at $t \gg \tau_\alpha$

\Rightarrow ~~$\chi_{2;1}^{(1)}(\omega, T) = -\kappa \left(\frac{\partial \chi_{Lin}}{\partial T} \right)$~~

T-dependences of the dimensionless cubic susceptibility $X_n^{(k)}$

$$X_n^{(k)}(\omega, T) = \frac{\chi_n^{(k)}(\omega, T)}{\left(\frac{\epsilon_0 \chi_s^2 a^3}{k_B T} \right)}$$

is T-independent in the trivial limit (ideal gas)
 = $N_{corr}(T) H_n^k(\omega \tau_\alpha(T))$ if B&B's prediction holds



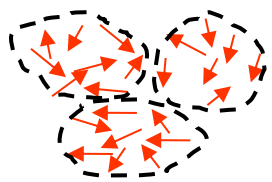
• “Trivial” $X_{2;1}^{(1)}$ looks OK

• Similar T dependences for $X_n^{(k)}$ and for $T \partial \chi_{Lin} / \partial T$

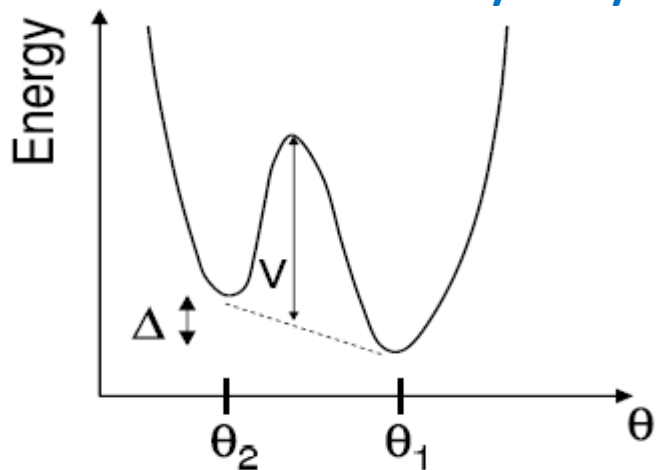


ω and T dependences consistent with $X_{2;1}^{(1)} \sim N_{corr}$ (OK within MCT)

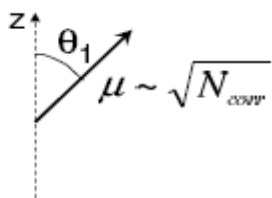
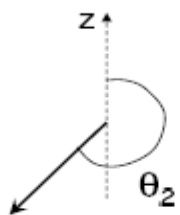
Can we fit nonlinear resp. ? The "toy model" as an attempt :



Each Dyn.Het. \Leftrightarrow
 $\mu = \mu_m \sqrt{N_{corr}}$
 in a double well
 (to get long τ),
 of assymetry Δ



$\vec{E} // z$



Simplest example: $\Delta=0=\theta_1$

$$\frac{\tau}{\text{ch } e} \frac{\partial P}{\partial t} + P = M \text{th } e$$

where

$$\left\{ \begin{aligned} e &= \frac{\mu_m \sqrt{N_{corr}} E(t)}{k_B T} \sim \sqrt{N_{corr}} \\ M &= \frac{\mu_m \sqrt{N_{corr}}}{N_{corr} a^3} \sim \frac{1}{\sqrt{N_{corr}}} \end{aligned} \right.$$

$$P_{Lin} \sim M e \sim \frac{\sqrt{N_{corr}}}{\sqrt{N_{corr}}} E$$

$$P_3 \sim M e^3 \sim \frac{(\sqrt{N_{corr}} E)^3}{\sqrt{N_{corr}}}$$

$$\chi_{Lin} \sim 1$$

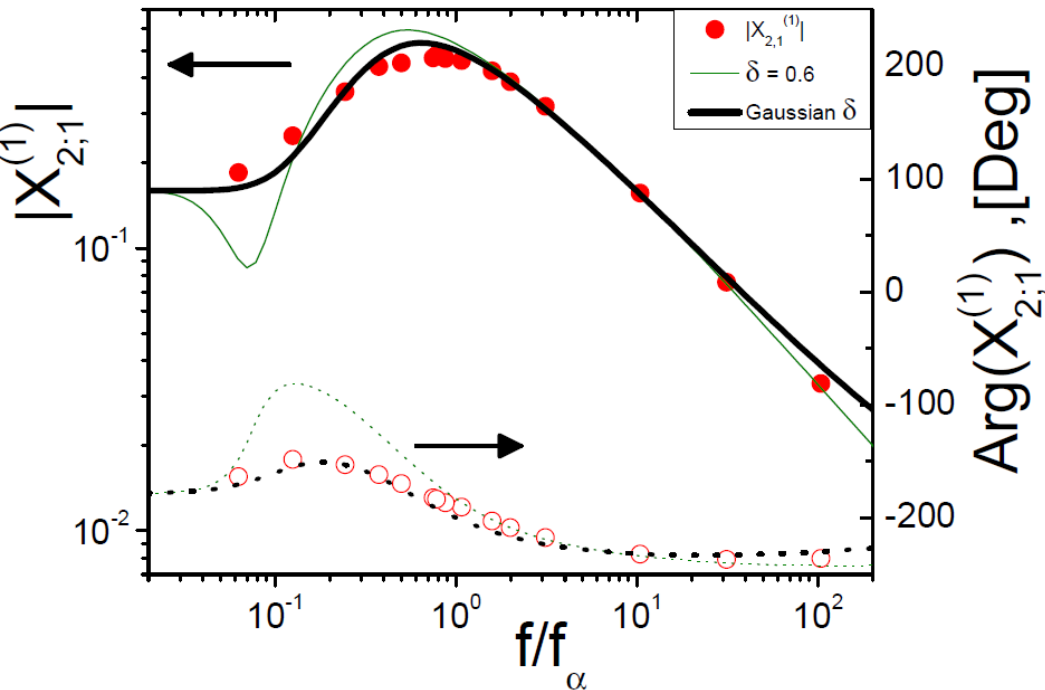
$$\chi_3 \sim N_{corr}$$

Two key points $\left\{ \begin{aligned} \mu \sim \sqrt{N_{corr}} &\Leftrightarrow \text{Amorphous Order («as» in S.G.)} \\ \text{Crossover to trivial is enforced at } f \ll f_\alpha \end{aligned} \right.$

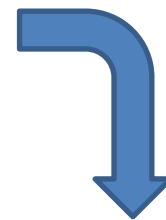
can it fit the data ? ...

Fits at Tg+17K:

$N_{\text{corr}}=10$
 $\delta=0.60$

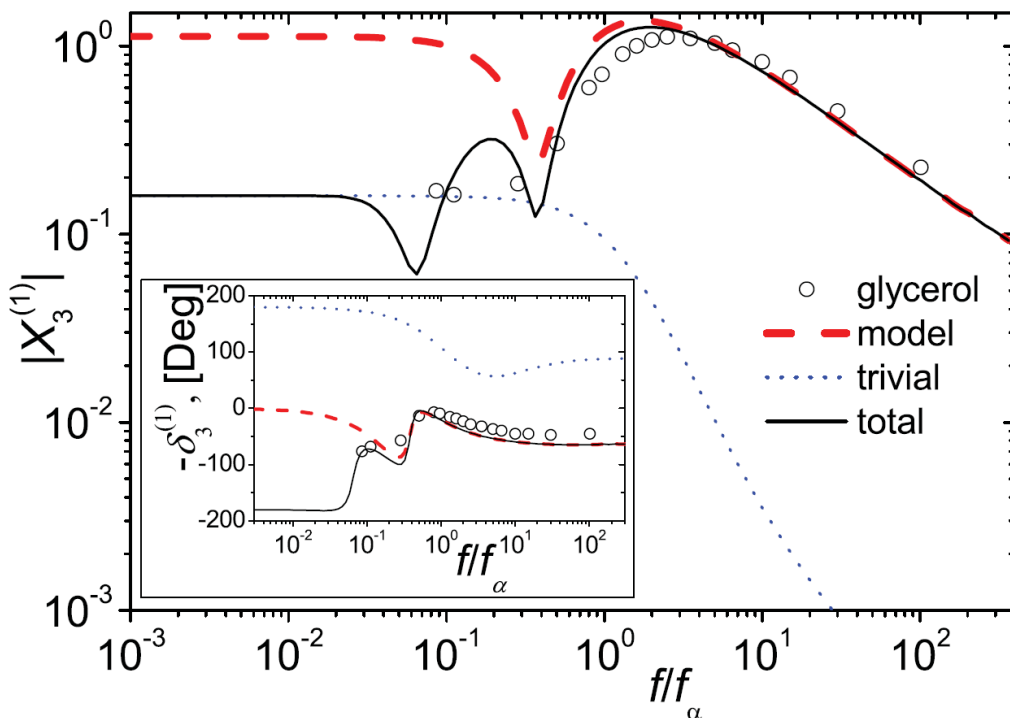


L'Hôte, Tourbot, Ladieu,
Gadige PRB 90, 104202
(2014)



- N_{corr} has the right order of magnitude
- good fits for ALL the $X_n^{(k)}$
- ... but with different values of N_{corr} (**toy model**)

$N_{\text{corr}}=15$
 $\delta=0.60$



Ladieu, Brun, L'Hôte, PRB
85, 184207, (2012)



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Summary and Perspectives.

Translating $\chi_{2,1}^{(1)}$ as a δT_g shift

Pressure experiments:

$\delta T_g(\Pi)$ is drawn from :

$$P(\omega; \Pi; T) \equiv P(\omega; 0; T - \delta T_g(\Pi))$$

Same method for E_{st} :

$$P(\omega; E_{st}; T) \equiv P(\omega; 0; T - \delta T_g(E_{st}))$$

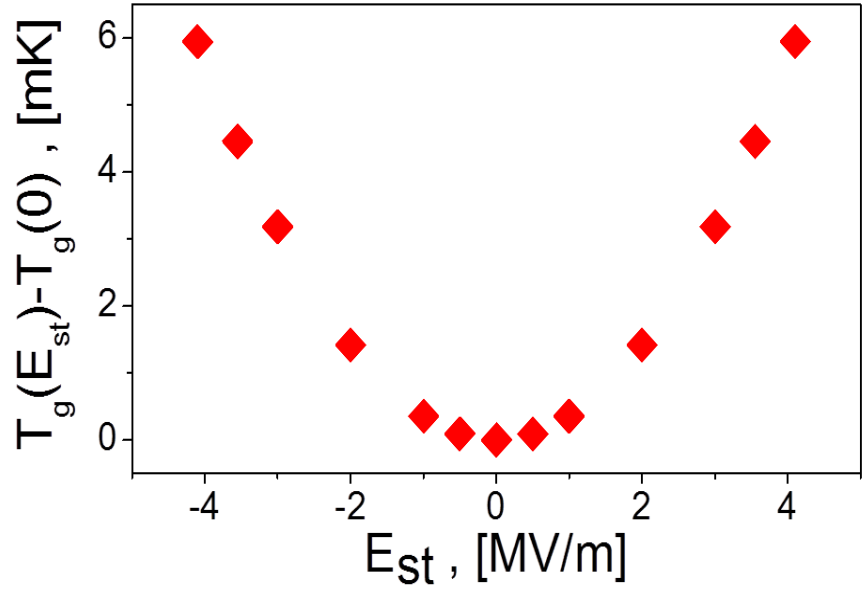
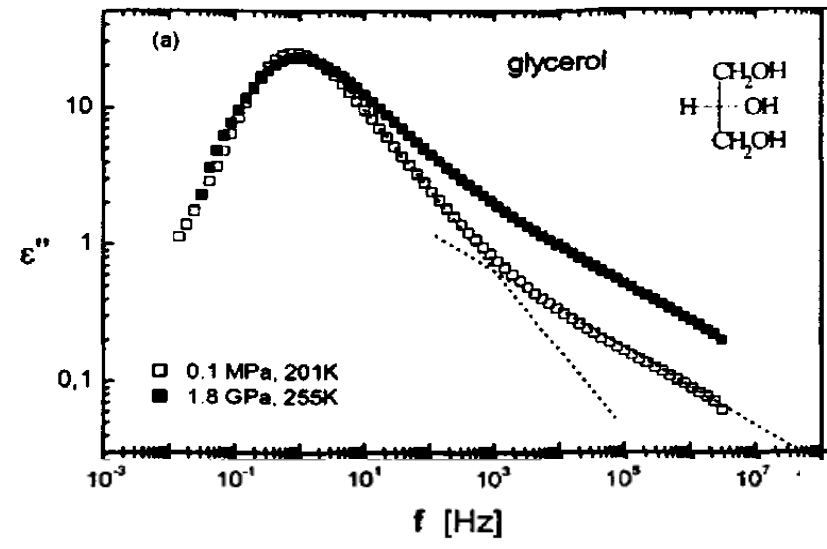
$\delta T_g(E_{st}) = 3\kappa E_{st}^2$

$$\chi_{2;1}^{(1)}(T, \omega) = -\kappa \left(\frac{\partial \chi_{Lin}}{\partial T} \right)_{0, T, \frac{\omega}{\lambda}} \text{ with } \lambda = 1$$

Slight trivial distortion
 of $\chi_{2,1}^{(1)} \Rightarrow \lambda \neq 1$

$\delta T_g = 3\kappa E_{st}^2 \Leftrightarrow E_{st}$ is a new control parameter in glycerol

Hensel-Bielowka et al. , PRE (2004)



A picture: D.H.
 \approx overcrowded
subway



N_{corr}

Increasing Pressure ...



Increasing E_{st} ...



Density \uparrow ... $\Rightarrow \Sigma \downarrow$ and $\tau_\alpha \uparrow$

$E_{st} \uparrow$... $\Rightarrow \Sigma \downarrow$ and $\tau_\alpha \uparrow$

Summary and Perspectives.

- Our very sensitive setup has successfully measured $\chi_{2;1}^{(1)}(\omega, T)$
- The interpretation issue is now clarified since :
 - the Box Model cannot account for the order of magnitude of $\chi_{2;1}^{(1)}$
 - Global consistency with $\chi_n^{(k)} \sim N_{\text{corr}}$:
 - ω and T dependences,
 - fits with the toy model



- Perspectives = systematic studies of $N_{\text{corr}} \Leftrightarrow$ the scale on which the systems is **solid, during τ_α** :
 - study $\chi_3(\omega_1; \omega_2; \omega_3)$ in other directions than $(0, 0, \omega)$ or $(\pm\omega, \omega, \omega)$
 - study $\chi_{2;1}^{(1)}$ at high temperatures (no heating)
 - Study $\chi_{2;1}^{(1)}$ at higher fields or in other liquids
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