

Particle-in-Cell simulation of propagation of Alfvén waves in magnetized pair plasmas

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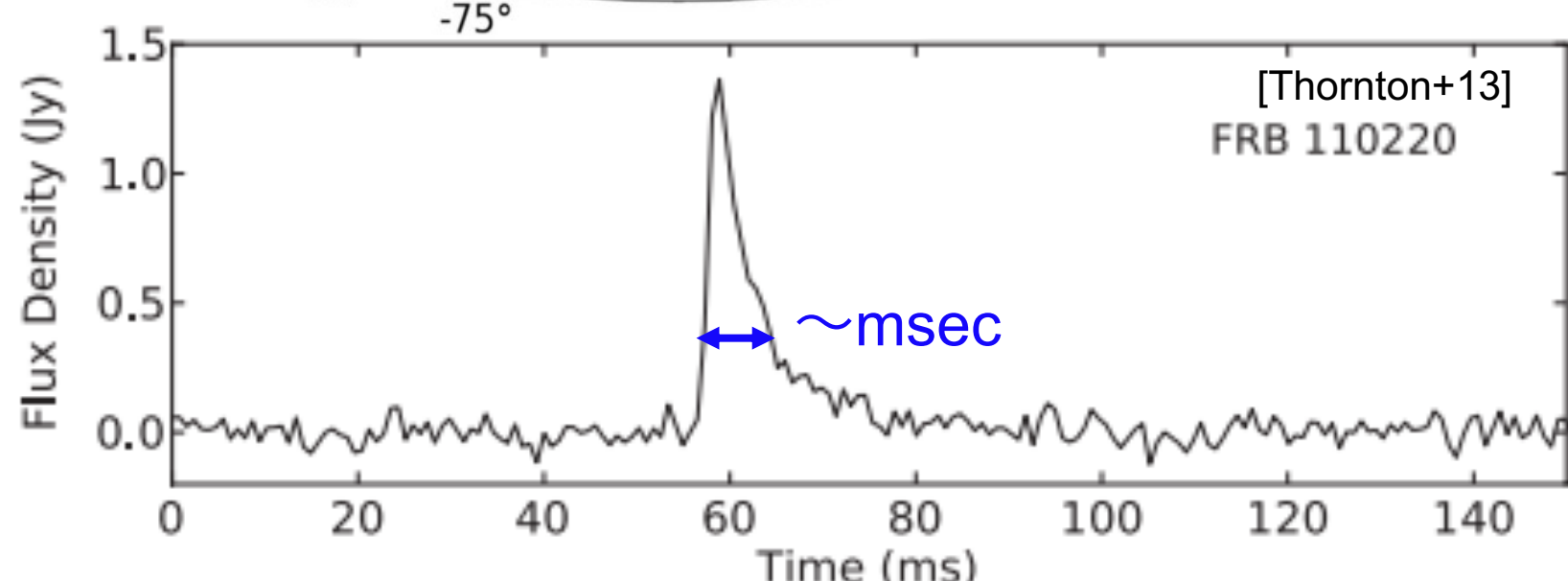
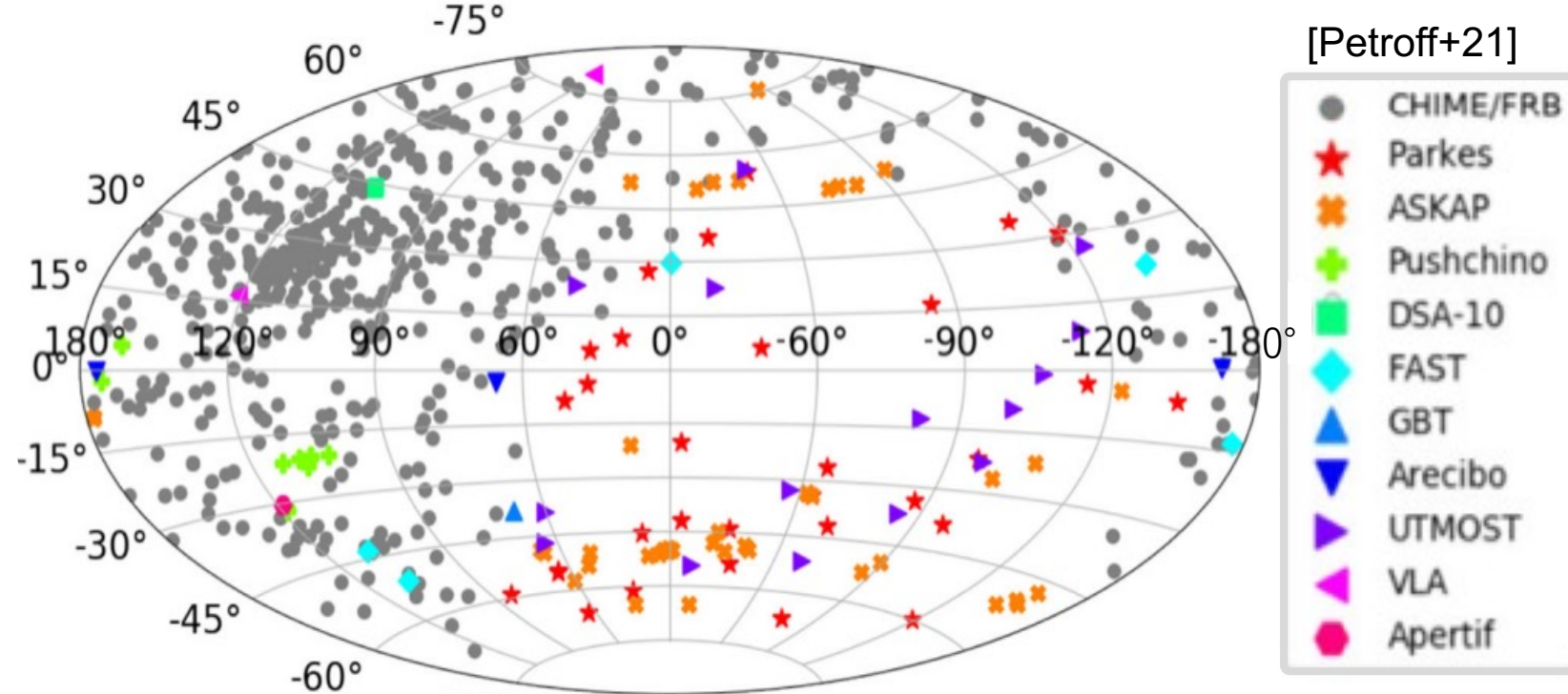
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Wataru Ishizaki (YITP)

Fast Radio Bursts (FRBs)

- Bright radio transient
- Cosmological
- Frequency: $\nu \sim \mathcal{O}(\text{GHz})$
- Duration: $\Delta t \sim \mathcal{O}(\text{msec})$
- Flux density:
 $S_\nu \sim \mathcal{O}(\text{Jy}) @ \text{GHz}$
- High brightness temp.
→ coherent emission

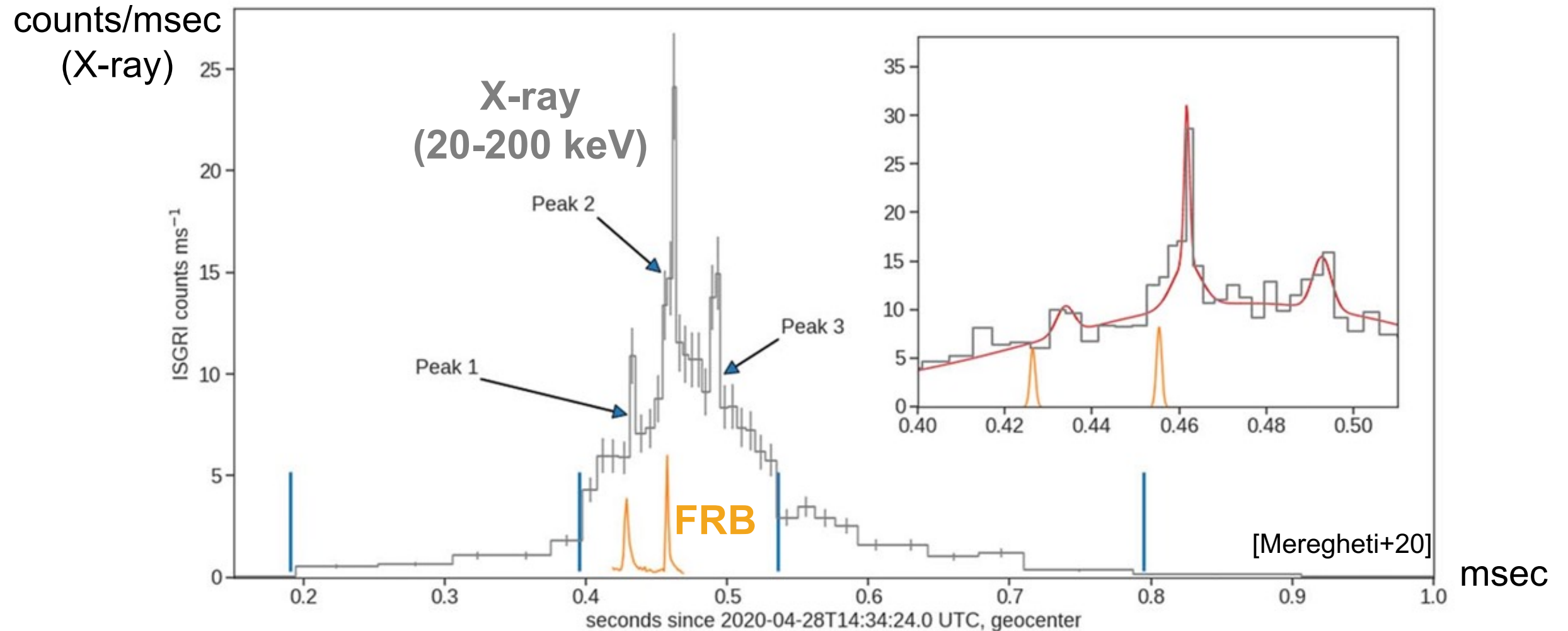
The origin and emission mechanism of FRBs are unclear.



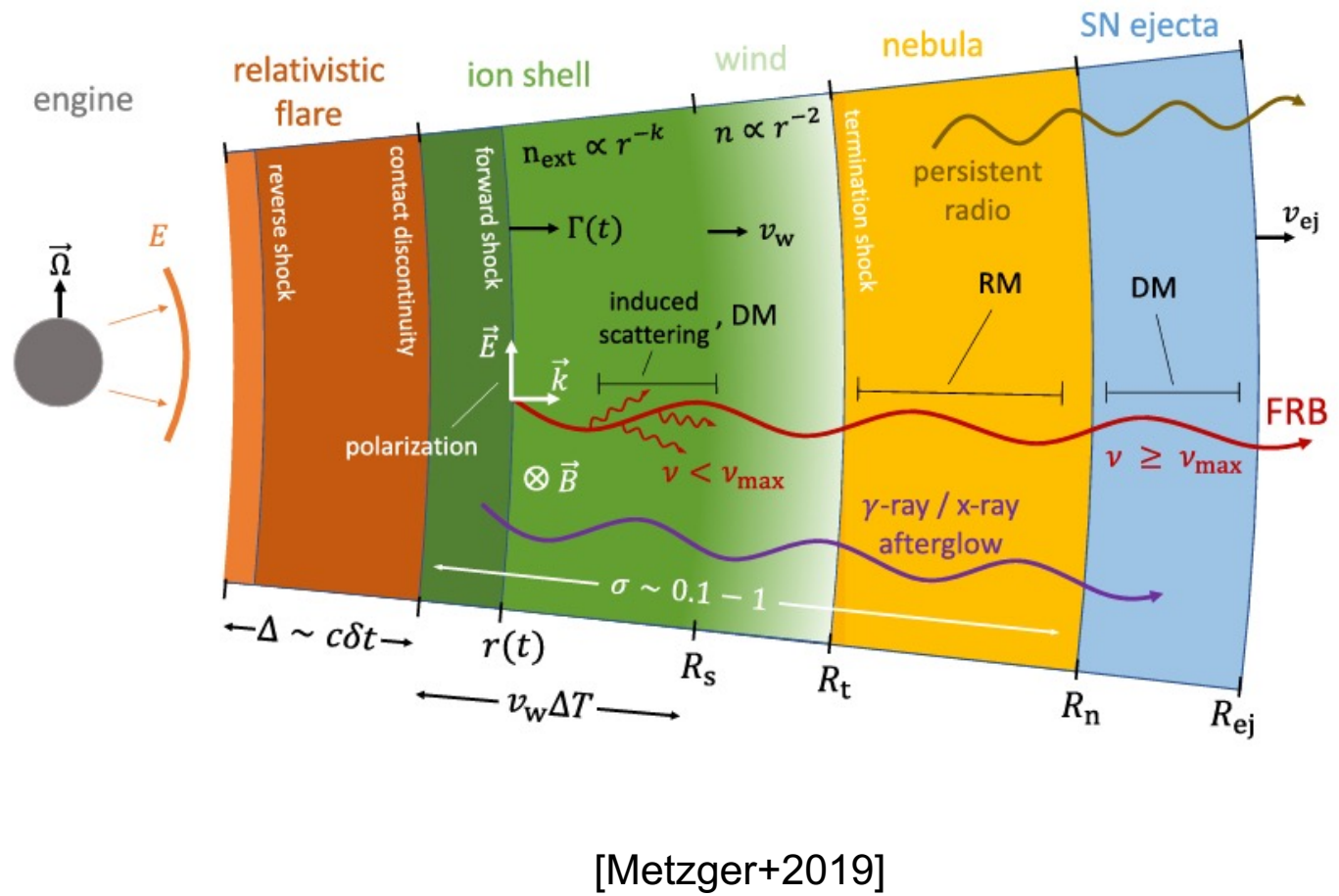
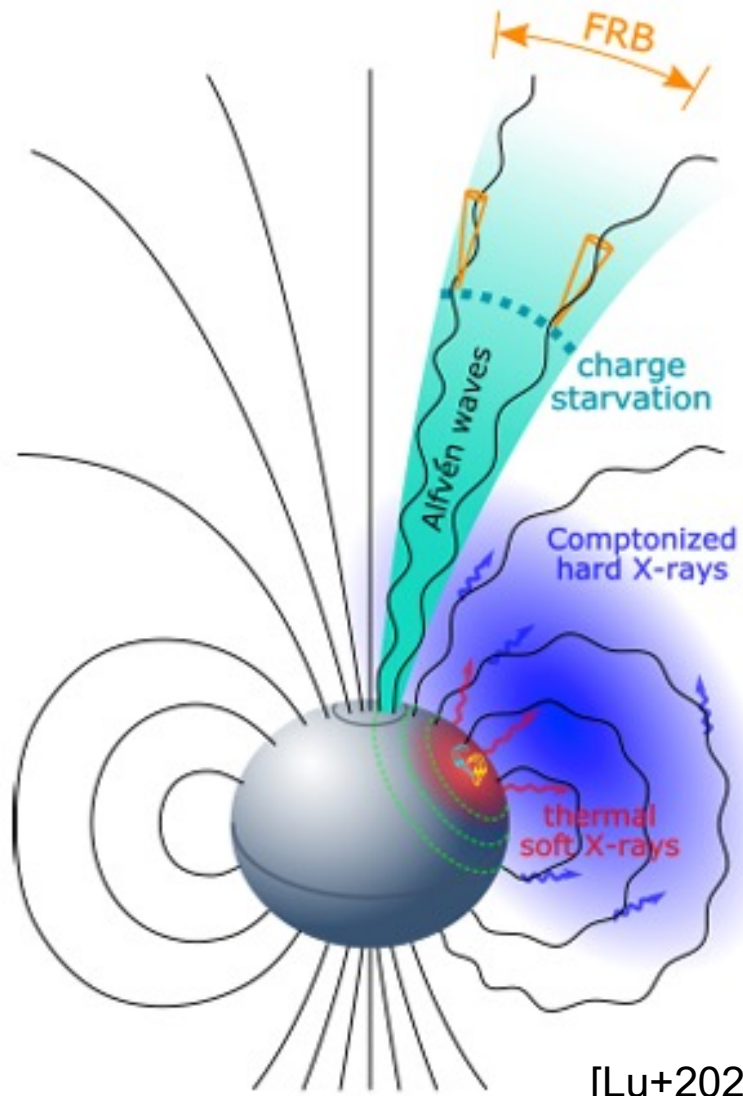
FRB 20200428A: FRB & short X-ray burst

FRB 20200428A associates with the short X-ray burst for the Galactic magnetar SGR 1935+2145.

→ **Magnetars are one of the plausible origin of FRBs.**



Magnetar models



The wave propagation in magnetized plasmas is common for both models.

Alfvén waves in magnetized plasmas

- Many instabilities [e.g. Matsukiyo & Hada 03]
 - e.g.) Parametric decay instability:
parent wave \rightarrow daughter electromagnetic wave + daughter electrostatic wave
- Particle acceleration by counter-propagating Alfvén waves [Matsukiyo & Hada 09, Isayama+23]
- Bunching of charged particles by charge-starved Alfvén wave [Kumar & Bosnjak 20, Kumar+22]
- Magnetic reconnection by the Alfvén wave-induced shear flow [Yuan+20]

We investigate the Alfvén wave propagation in the magnetized pair plasmas by using Particle-in-Cell simulations.

Realistic situation

e.g.) 3 dimension
Ambient B-field and plasma density change distant from the NS surface.
large-amplitude wave
etc.



Our simulation (as a first step)

1 dimension
uniform B-field & plasma density
small-amplitude wave

Simulation setup

□ Wuming (public code)

□ $e\pm$ pair plasma ($m_r = m_i/m_e = 1$)

$$\omega_{pe}\Delta t = \omega_{pi}\Delta t = 0.02 \quad \sigma_e = B_0^2/(4\pi n_e m_e c^2) = 25$$

$$\Omega_e\Delta t = (eB_0/(m_e c))\Delta t = \Omega_i\Delta t = \sqrt{\sigma_e}\omega_{pe}\Delta t = 0.1$$

□ circularly polarized Alfvén wave (parent wave)

$$\vec{B}_p = B_p[-\sin\phi_0 \hat{x} + \cos\phi_0 \hat{z}], \phi_0 = k_0 y - \omega_0 t \quad \omega_0\Delta t = 0.01$$

$$\vec{E}_p = -\frac{\omega_0}{ck_0} B_p[\cos\phi_0 \hat{x} + \sin\phi_0 \hat{z}]$$

$$1 - \left(\frac{ck_0}{\omega_0}\right)^2 - \frac{\omega_{pe}^2}{\omega_0(\gamma_e\omega_0 - \Omega_e)} - \frac{\omega_{pi}^2}{\omega_0(\gamma_i\omega_0 + \Omega_i)} = 0$$

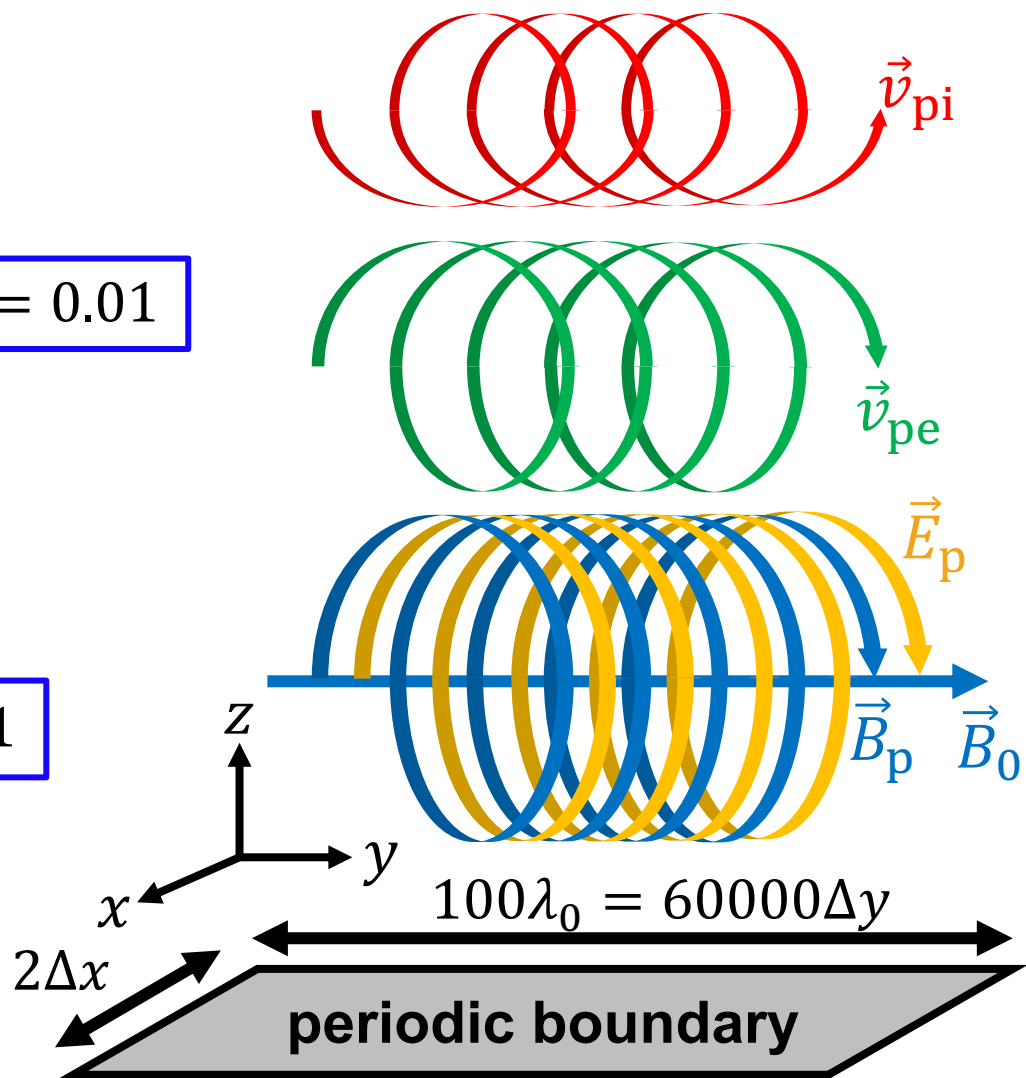
□ $e\pm$ velocity ($\vec{B} = \vec{B}_0 + \vec{B}_p, \vec{E} = \vec{E}_p$) $\eta = B_p/B_0 = 0.1$

$$\frac{\vec{v}_{pe}}{c} = \frac{\omega_0}{ck_0} \frac{\eta\Omega_e}{\gamma_e\omega_0 - \Omega_e} [-\sin\phi_0 \hat{x} + \cos\phi_0 \hat{z}]$$

$$\frac{\vec{v}_{pi}}{c} = -\frac{\omega_0}{ck_0} \frac{\eta\Omega_i}{\gamma_i\omega_0 + \Omega_i} [-\sin\phi_0 \hat{x} + \cos\phi_0 \hat{z}]$$

$$\Delta x = \Delta y = \Delta t = 1, m_e = 1, c = 1$$

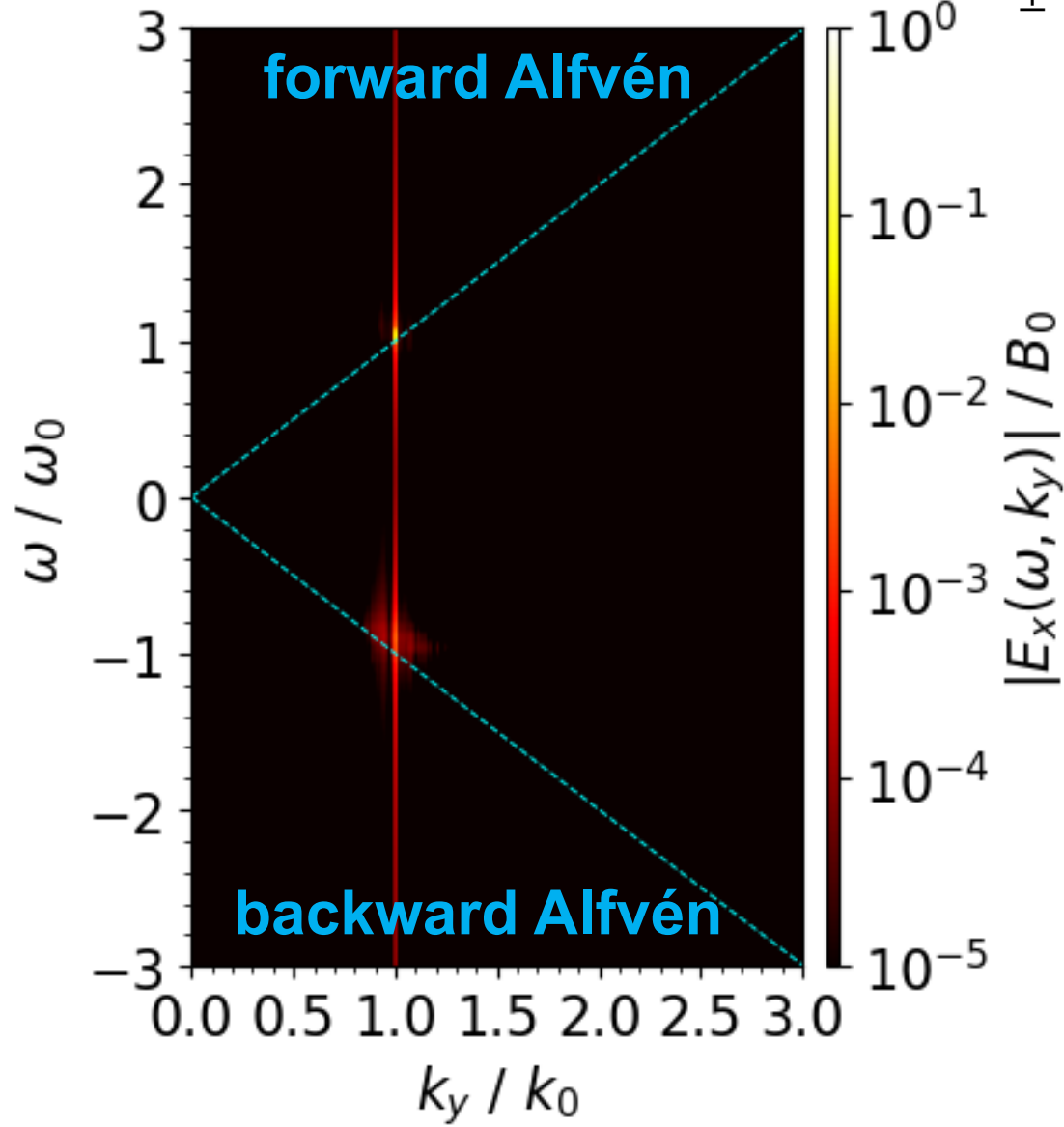
$$n_e = 20 / \text{cell}, v_{th,e}/c = v_{th,i}/c = 0.02$$



Fourier spectrum $(\omega_{pe}/\omega_0 = 2, \Omega_e/\omega_0 = 10)$

electromagnetic wave

$$|E_x(\omega, k_y)| / B_0$$

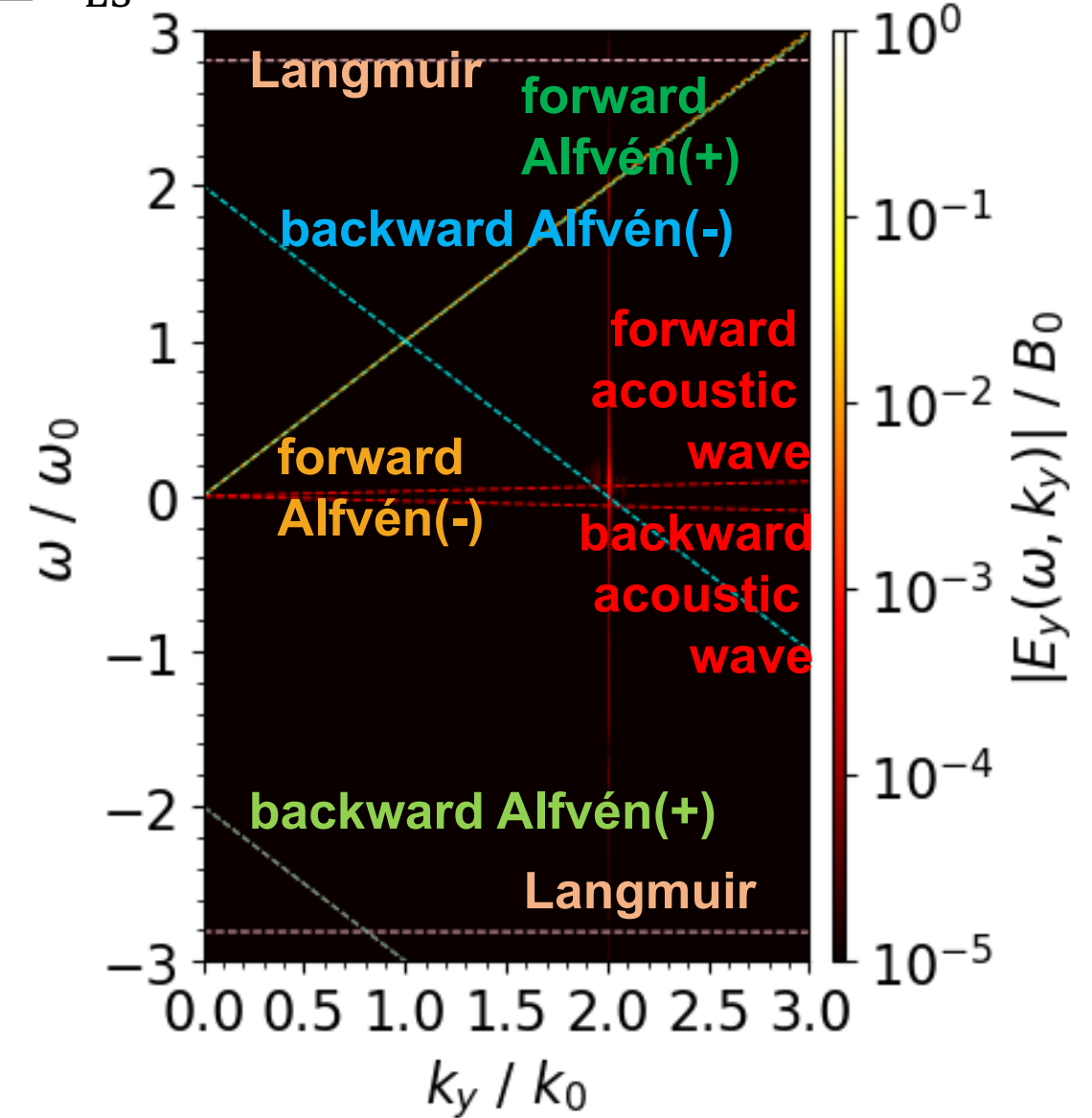


$$\omega_{\pm} = \omega_0 \pm \omega_{ES}$$

$$k_{\pm} = k_0 \pm k_{ES}$$

electrostatic wave

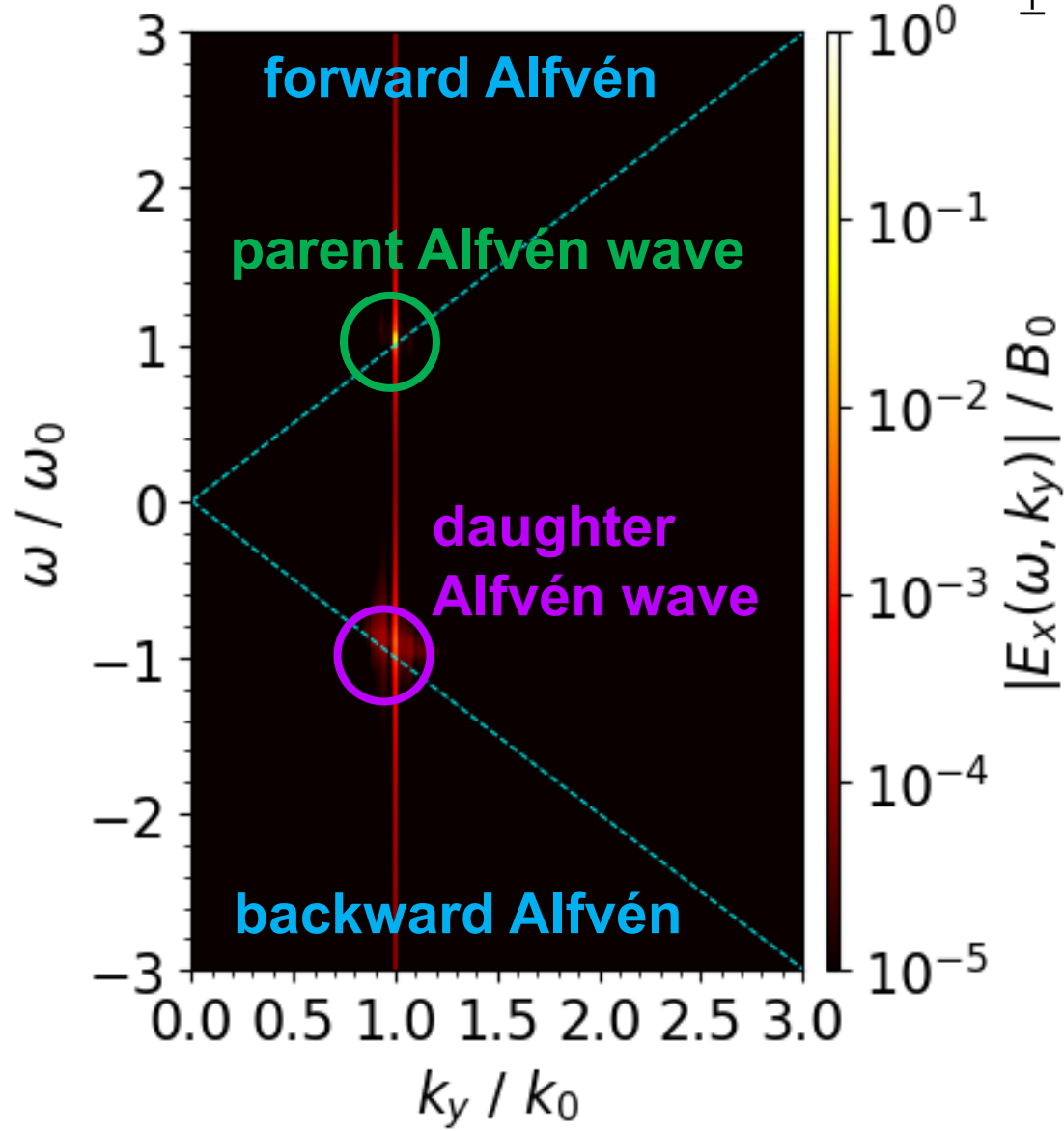
$$|E_y(\omega, k_y)| / B_0$$



Fourier spectrum $(\omega_{pe}/\omega_0 = 2, \Omega_e/\omega_0 = 10)$

electromagnetic wave

$$|E_x(\omega, k_y)| / B_0$$

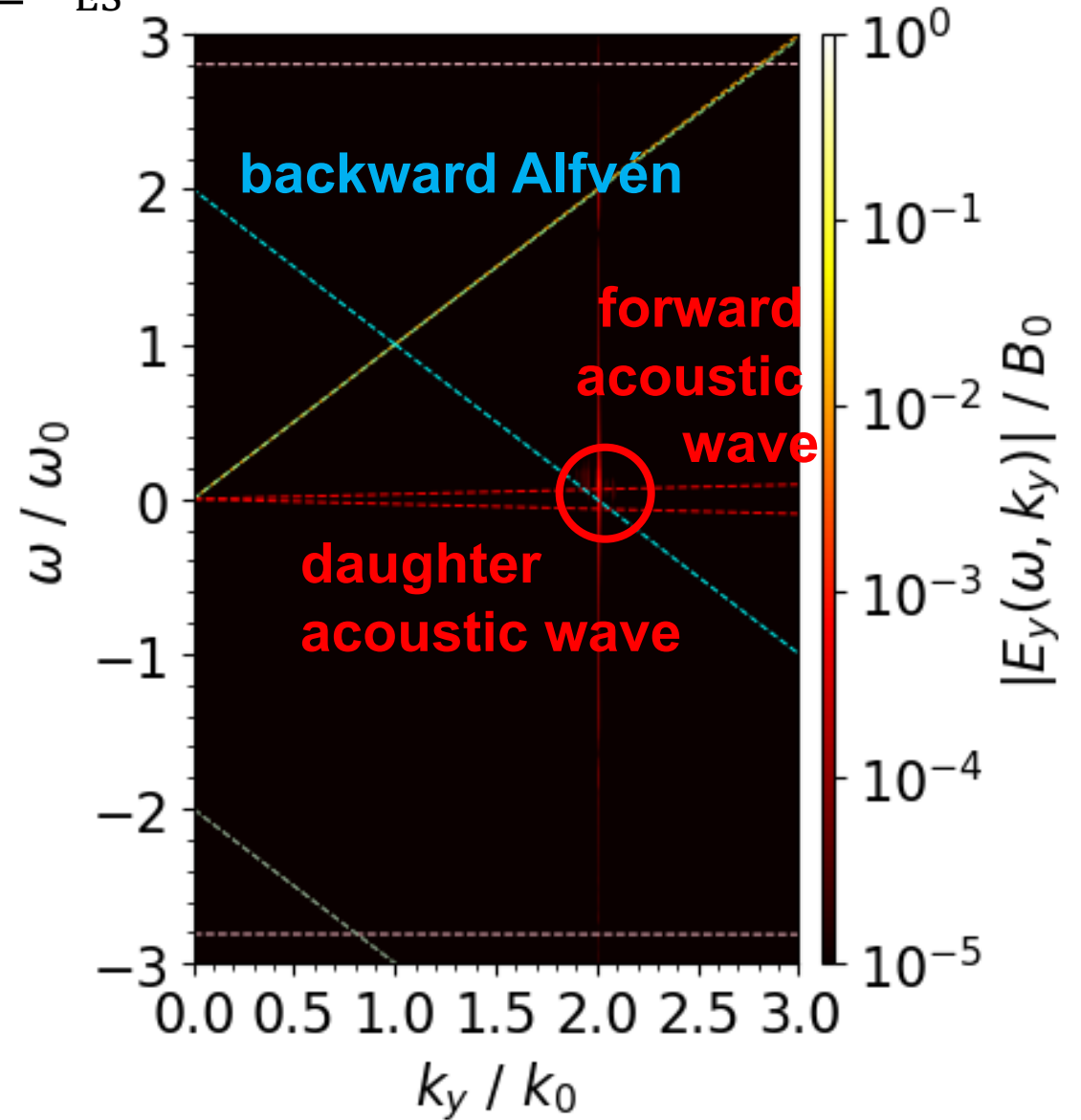


$$\omega_{\pm} = \omega_0 \pm \omega_{ES}$$

$$k_{\pm} = k_0 \pm k_{ES}$$

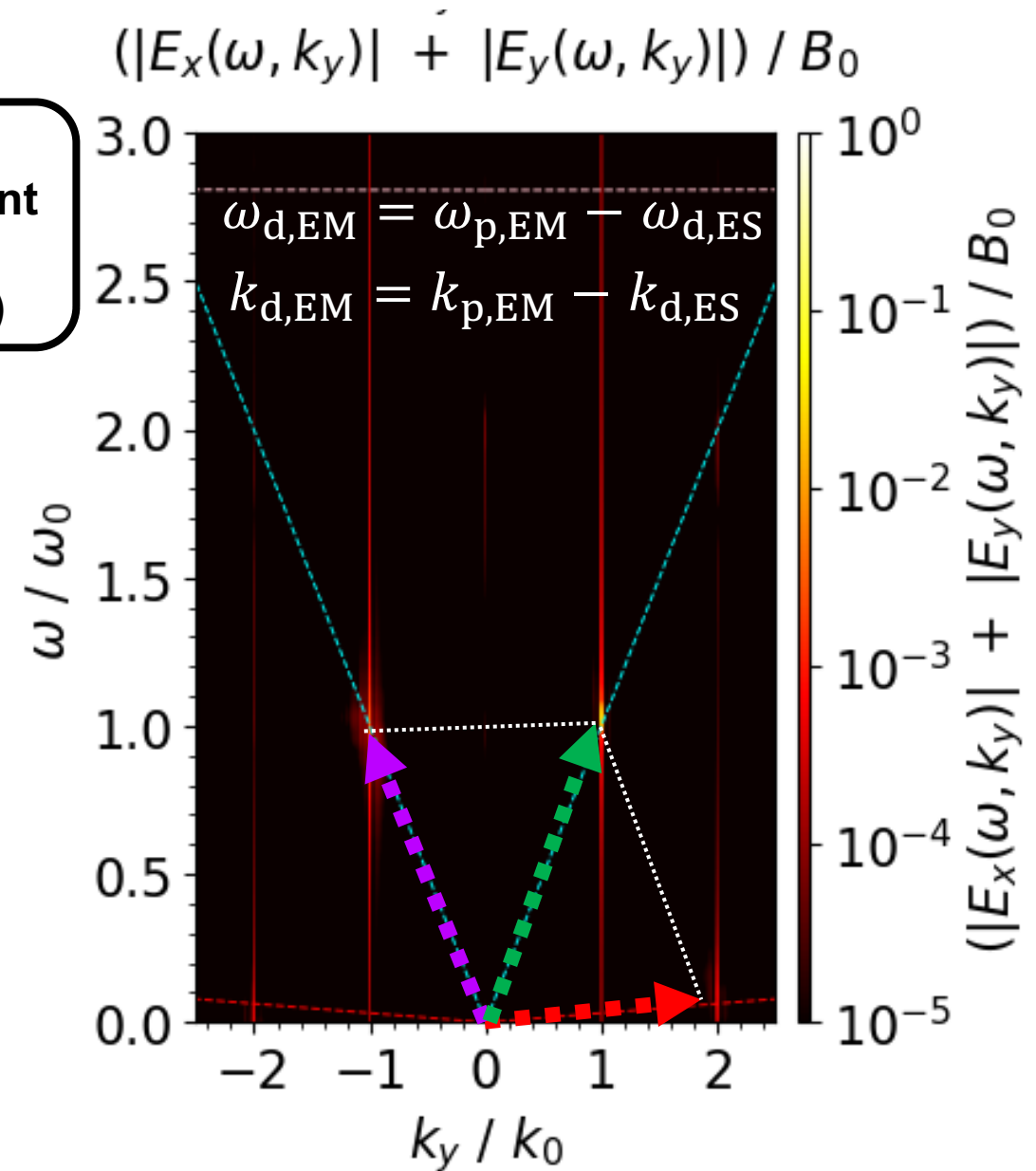
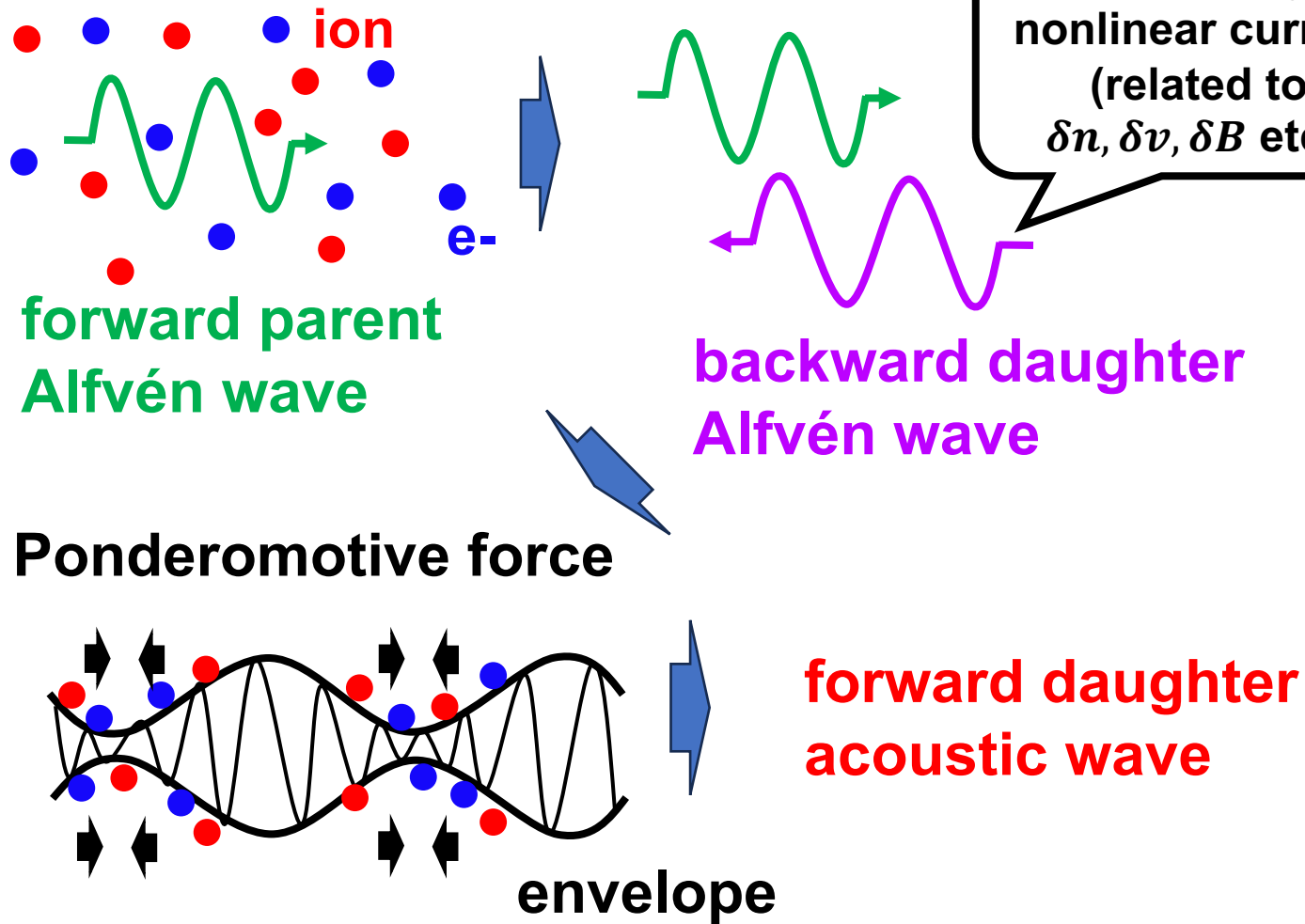
electrostatic wave

$$|E_y(\omega, k_y)| / B_0$$



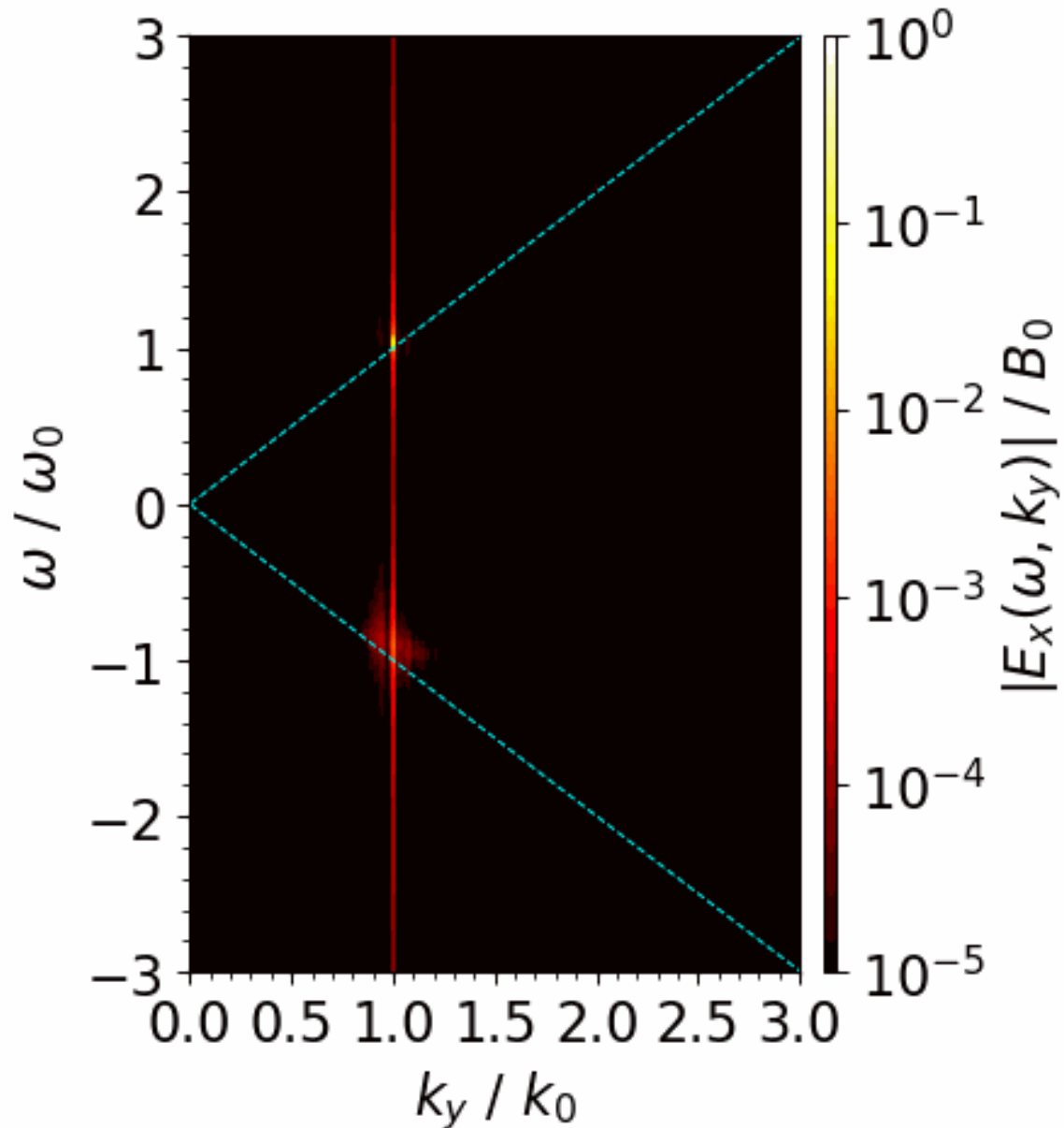
Decay instability

□ (Acoustic) decay instability

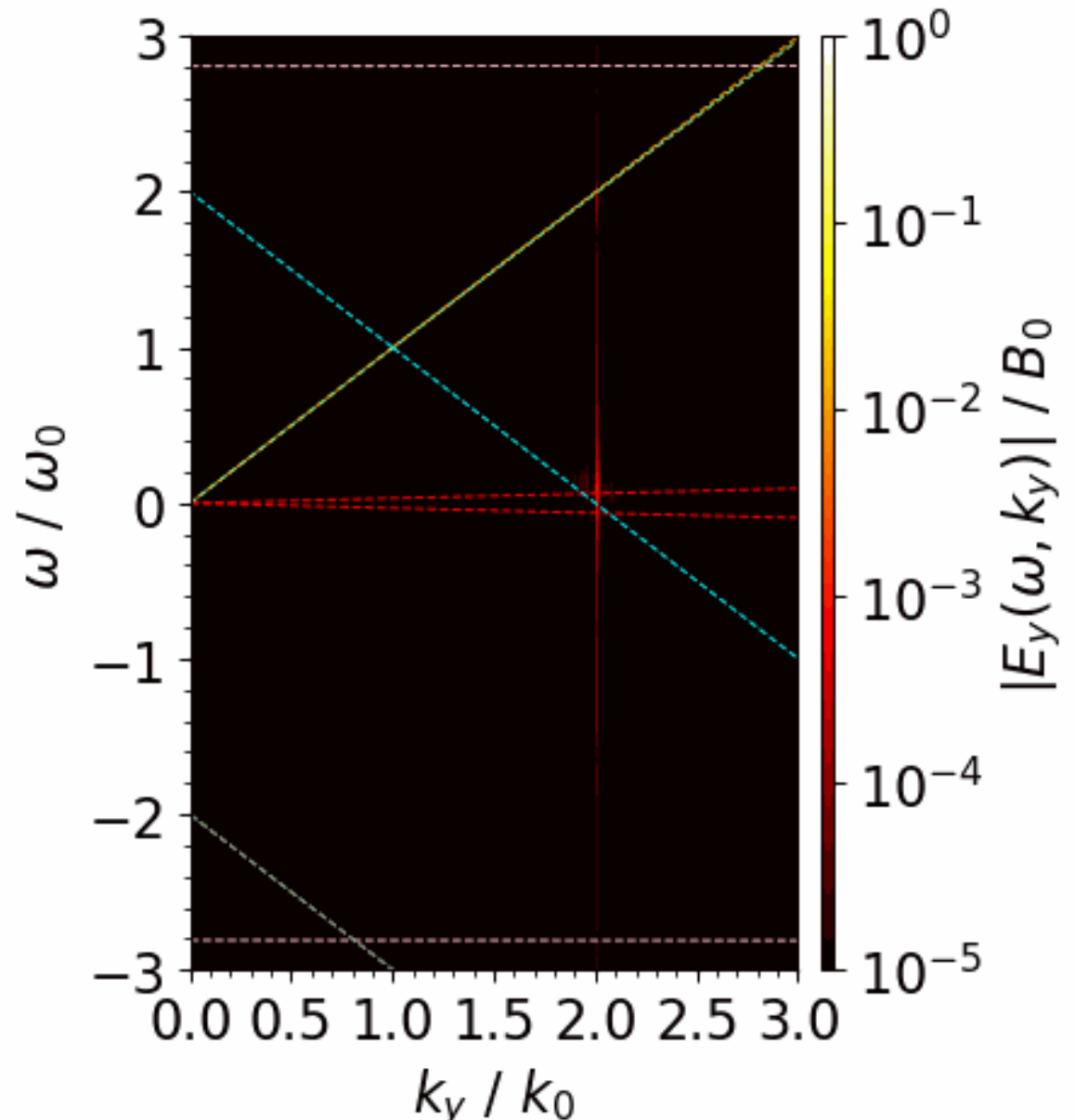


Time evolution of Fourier spectrum

$|E_x(\omega, k_y)| / B_0$

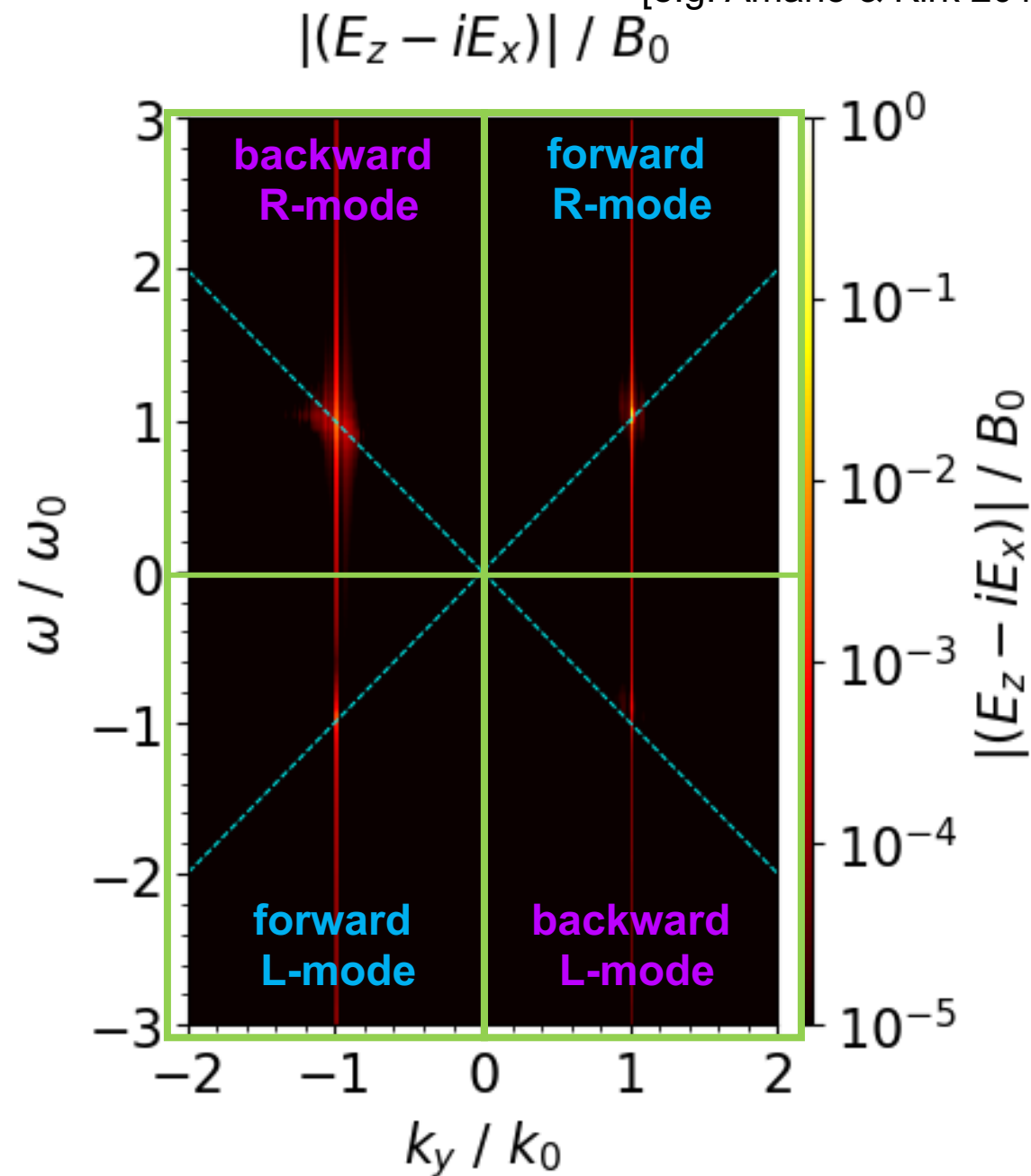
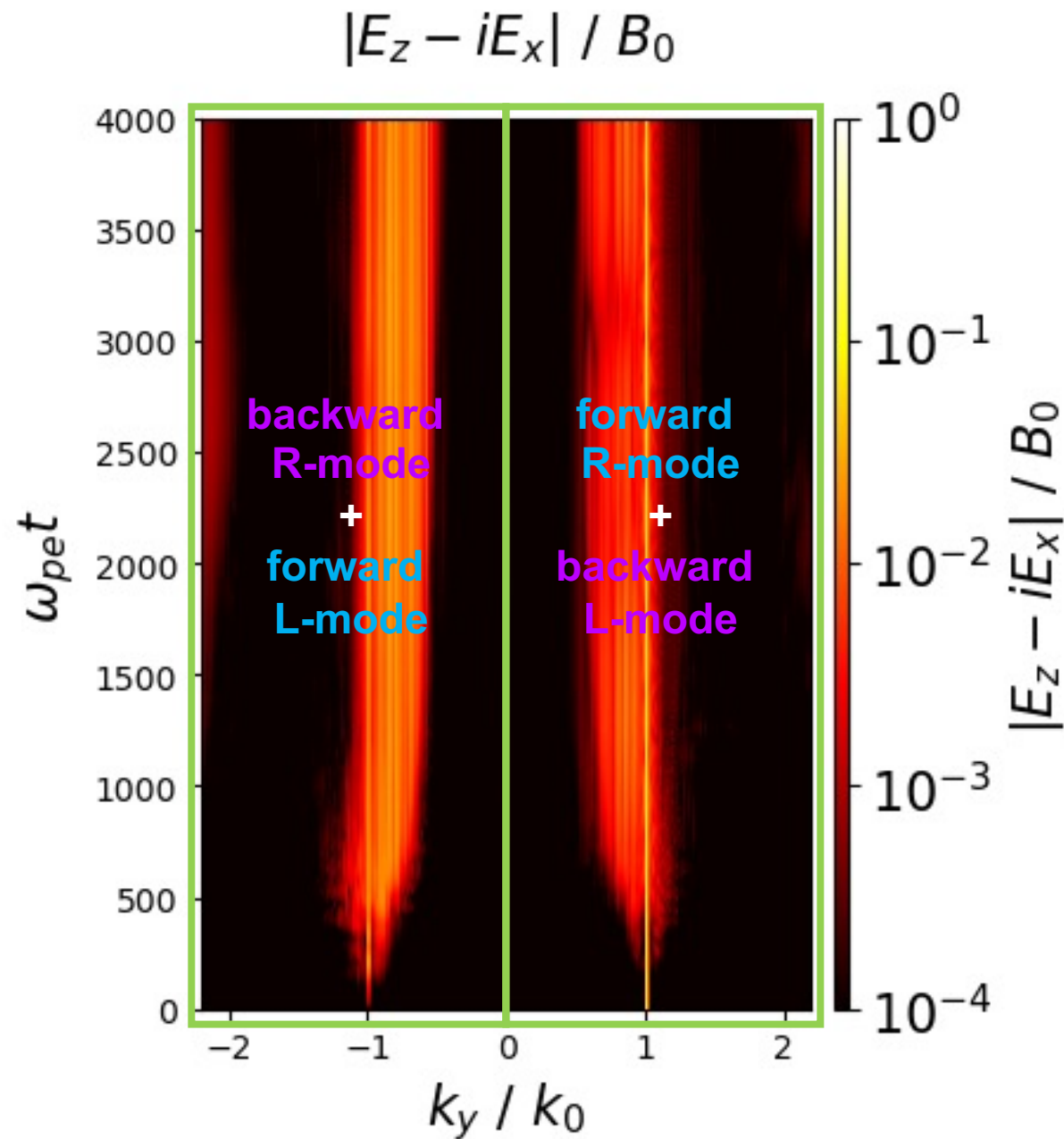


$|E_y(\omega, k_y)| / B_0$



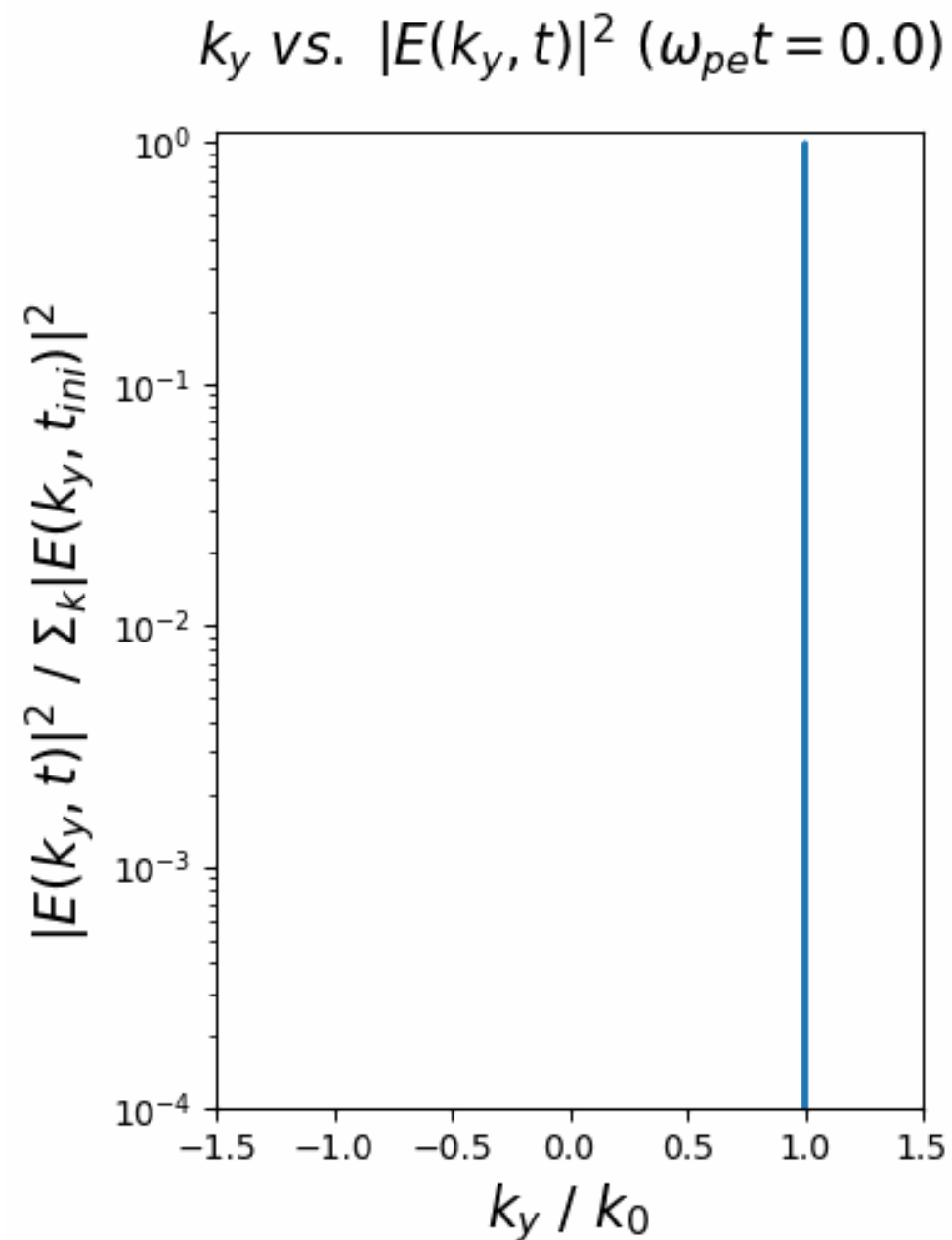
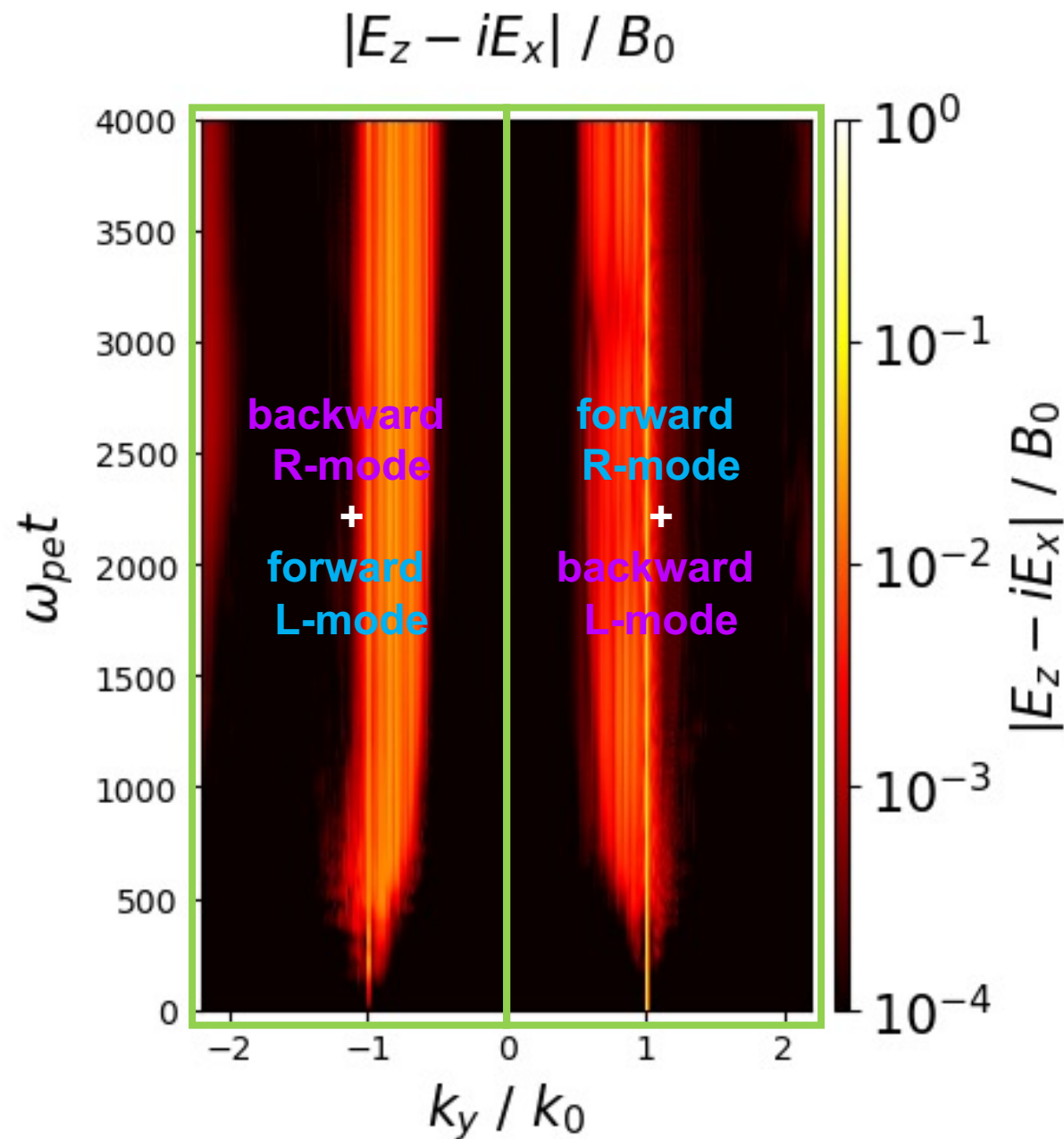
Mode decomposition

[e.g. Amano & Kirk 2013]



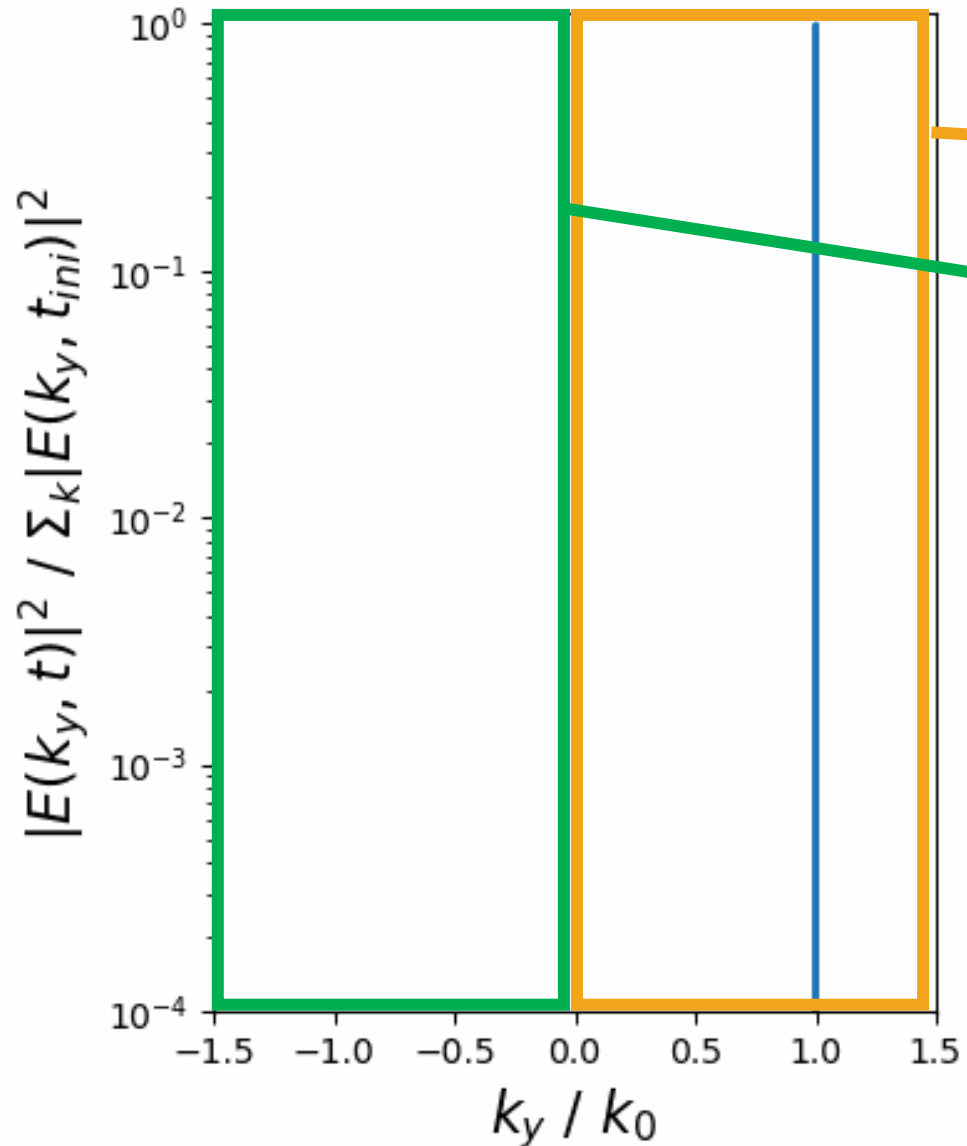
Mode decomposition

[e.g. Amano & Kirk 2013]



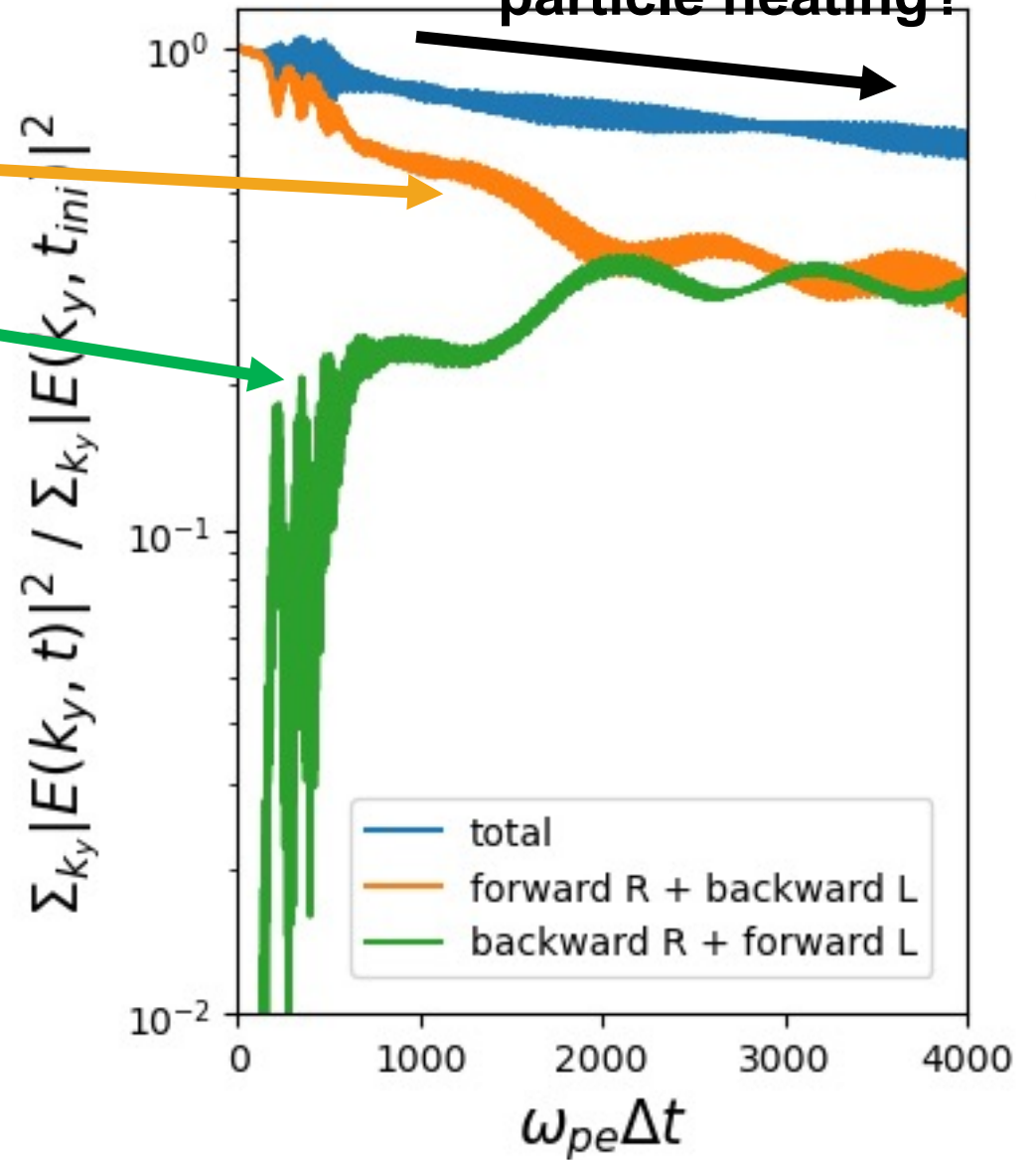
Time evolution of wave power

k_y vs. $|E(k_y, t)|^2$ ($\omega_{pe}t = 0.0$)



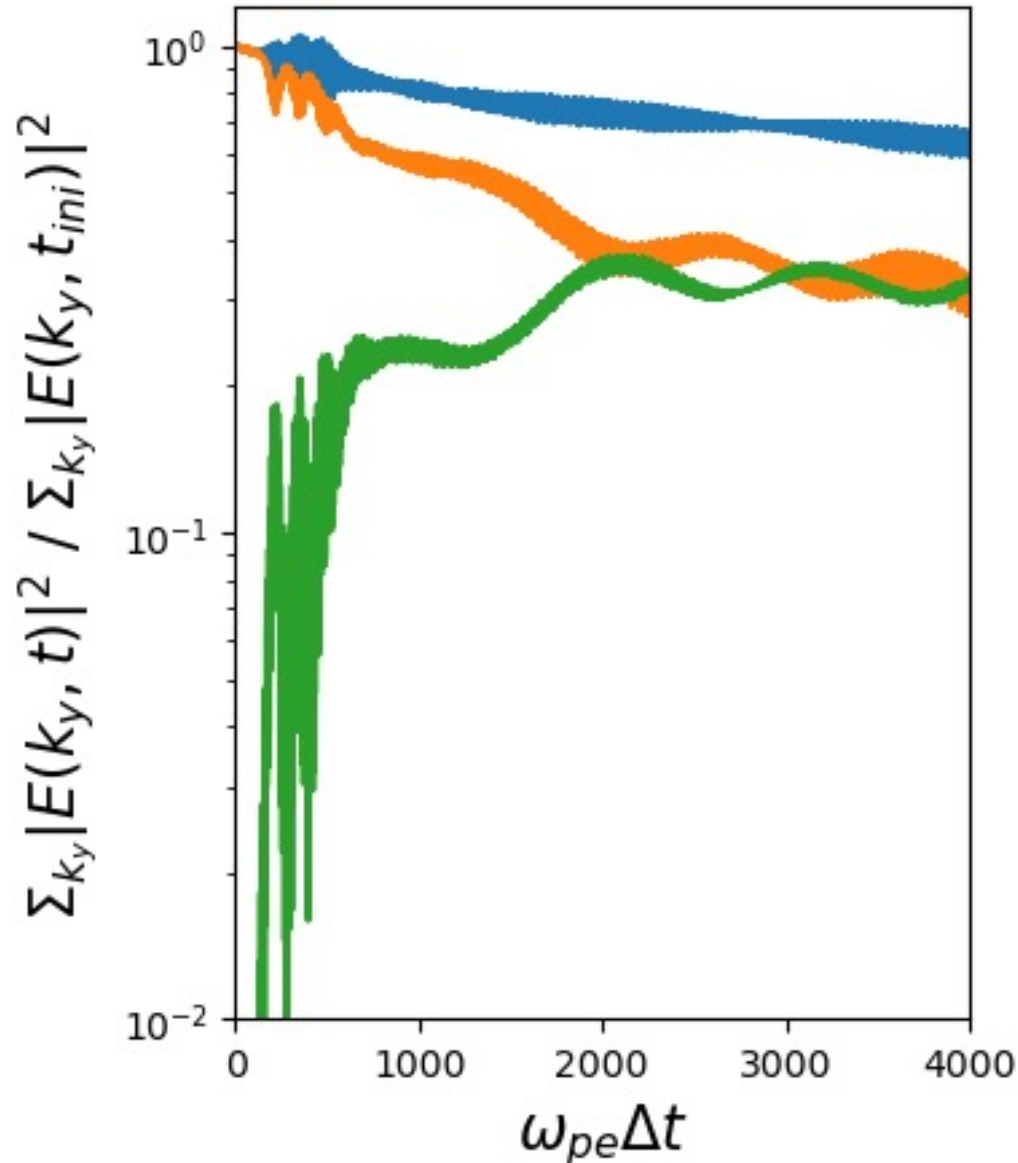
t vs. $\sum_{k_y} |E(k_y, t)|^2$

particle heating?



Time evolution of wave power

t vs. $\Sigma_{k_y} |E(k_y, t)|^2$



— total
— forward R + backward L
— backward R + forward L

**30 - 40% of the parent wave power remains.
at the end of this simulation.**

→ **We will perform long & multidimensional
simulations.**

In 2D simulations, waves could decay rapidly
compared to 1D simulations.

[Umeda, Saito, & Nariyuki 2018]

Summary & Future Work

- ❑ We investigate the Alfvén wave propagation in magnetized pair plasmas by using Particle-in-Cell simulations.
- ❑ The acoustic decay instability is confirmed in the early stage.
- ❑ Some wave-wave interactions occur, and many waves are generated as time elapses.
- ❑ The wave power of forward propagating waves remains 30 – 40 % of the wave power of the incident parent wave.
- ❑ We will analyze what wave-wave interactions occur.
- ❑ We will perform multi-dimensional PIC simulations.