



極限宇宙コロキウム, 2022. 4. 25

Graviton search with quantum information and quantum sensing

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A historical view

At the beginning of 20th century, there were two big discoveries.

General relativity



Gravitational waves
observed in 2015



Quantum gravity

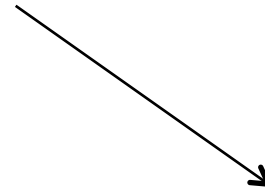
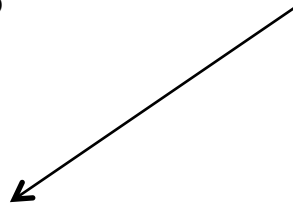


graviton

Quantum mechanics



Quantum field theory



Electromagnetic waves
observed in 1888



Quantum electrodynamics

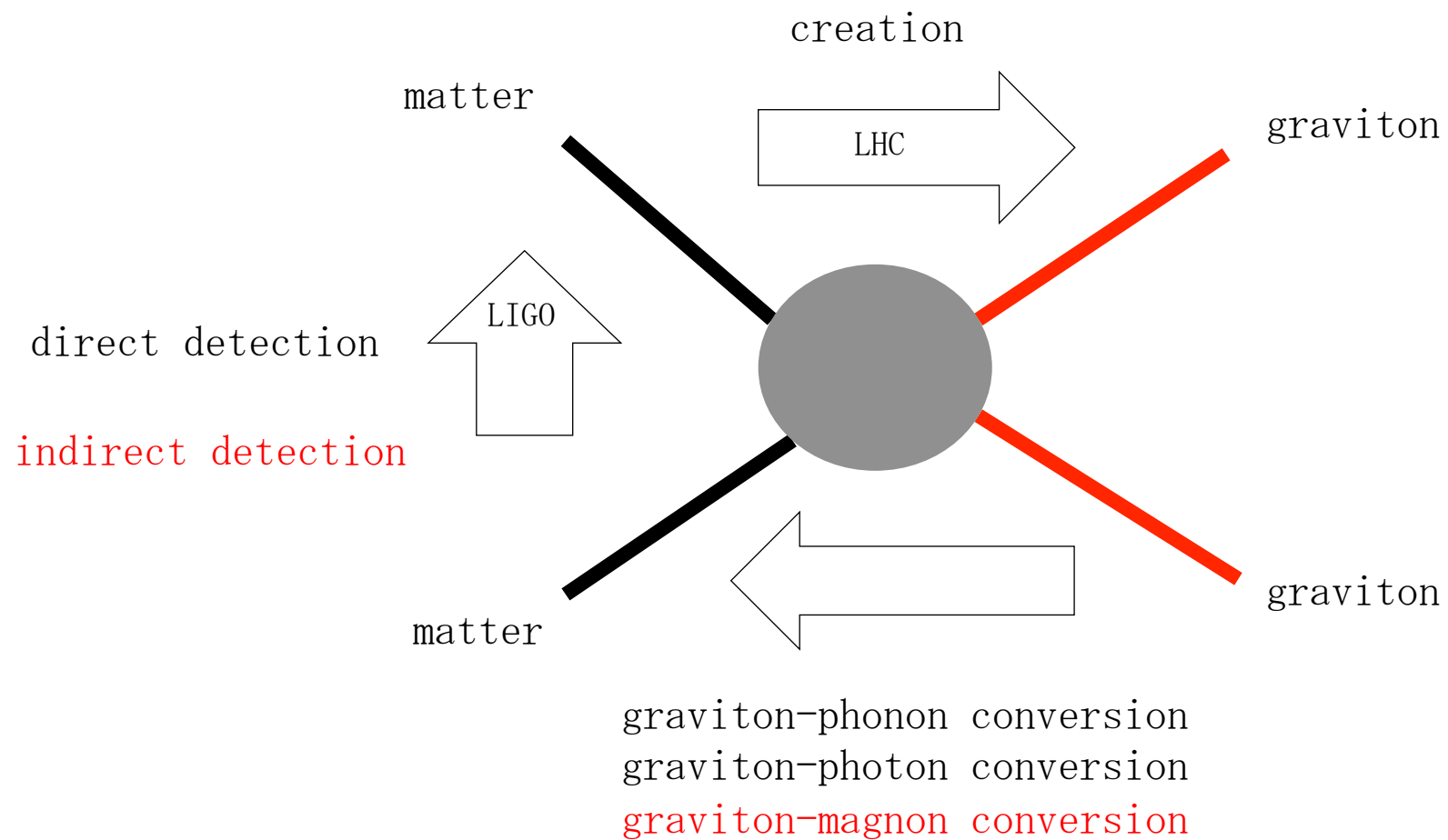


photon

Can we detect a graviton?

Graviton search

There are several different directions for detecting gravitons.

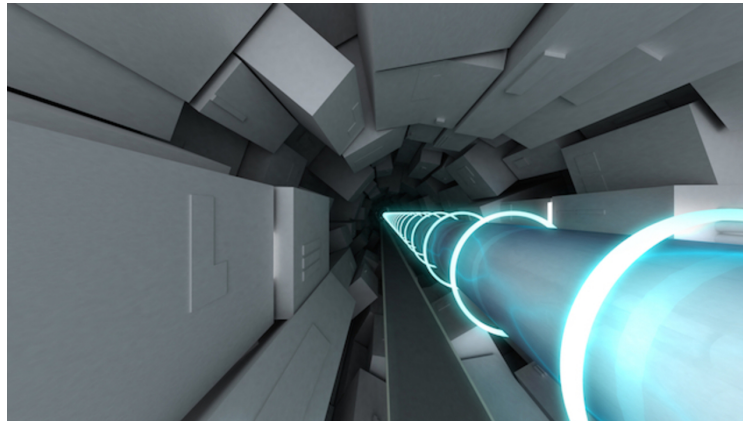


Can we create a graviton at the LHC?

Gravity, relativity, and quantum mechanics becomes important at the Planck energy scale

$$L_p = \sqrt{\frac{G\hbar}{c^3}} \approx 10^{-33} \text{cm} \Rightarrow 10^{19} \text{GeV}$$

Ultra-high energy accelerators?



< 100 TeV

It seems impossible to create a graviton!!

Can we detect a graviton with LIGO?

Astrophysical sources can create a bunch of gravitons!

However, it is difficult to identify a single graviton. Dyson 2013

The reason is simple.

GWs detected at LIGO have

a frequency 1kHz and an amplitude $h \approx 10^{-21}$.

energy density $\rho = \frac{c^2}{32\pi G} \omega^2 h^2$ $\omega = 1\text{kHz}, h=10^{-21} \Rightarrow 10^{-10} \text{erg/cm}^3$

energy density of a single graviton $\rho_s = \frac{\hbar \omega^4}{c^3} \Rightarrow 10^{-47} \text{erg/cm}^3$

number of gravitons detected $n_g = \frac{1}{32\pi} \frac{c^3}{G\hbar} \left(\frac{c}{\omega} \right)^2 h^2 = 10^{37}$

Hence, it is difficult to resolve a single graviton with LIGO.

There remain two possible directions

Indirect detection

It might be possible to detect gravitons indirectly through the noise of gravitons like as
a discovery of molecules through the Brownian motion.

Quantum information can be utilized.
We study the decoherence process of entanglement due to gravitons.

Direct detection

High frequency gravitational waves

Quantum sensing would be important.

A basic picture of the first part

The present universe originates from inflation,
which is supported by CMB and galaxy observations.

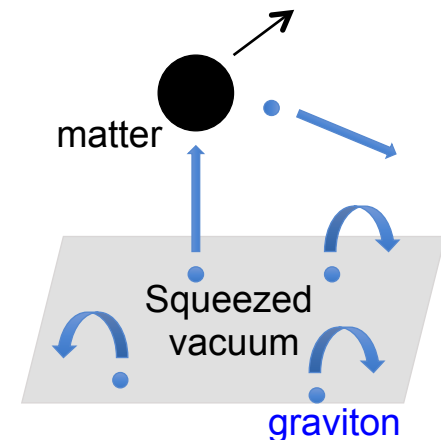
The inflation predicts **primordial gravitational waves**.
This can be regarded as the condensation of gravitons.
Indeed, the vacuum state of gravitons is **squeezed**.

We consider graviton fluctuations in this background.

Suppose a massive object is moving.

The object is interacting with gravitons.

This induces decoherence of the quantum entanglement.

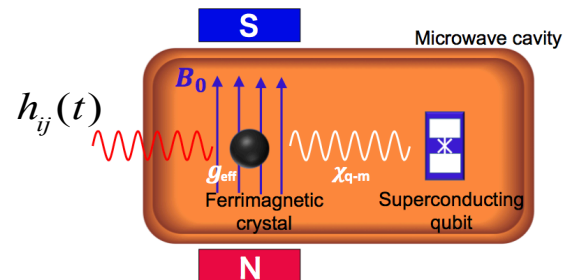


Thus, we need to know

primordial gravitational waves
and **how matter couples with gravity**.

A basic picture of the second part

The basic idea for detecting high frequency GWs is to use the interaction between quantum matter and high frequency GWs. We take magnons as the quantum matter in this talk.



As a working hypothesis, we use the duality between axion and gravity. More precisely, we use the existing data of axion experiments to give constraints on the amplitude of GWs at GHz. However, our aim is to detect high frequency GWs by utilizing recent development of quantum sensing with the hope detecting high frequency GWS leads to detecting a graviton.

Plan of this talk

- Basics of primordial GWs
 - How matter interact with gravity?
 - Quantum matter in graviton background
 - Indirect detection of gravitons
- } indirect detection
- Duality of axion and graviton experiments
 - Axion search with magnons
 - Graviton search with magnons
- } direct detection
- Summary

Basics of primordial GWs

Inflation

Flatness problem

$$|\Omega(t) - 1| = \frac{1}{a^2 H^2} \propto t \propto a^2$$

during radiation dominant stage

$$\frac{|\Omega - 1|_{t_0}}{|\Omega - 1|_{GUT}} = \frac{a_0^2}{a_{GUT}^2} = \frac{T_{GUT}^2}{T_0^2} = 10^{58}$$

$$T_0 = 2.7\text{K} = 10^{-13}\text{GeV}$$

$$T_{GUT} = 10^{16}\text{GeV}$$

We know $\Omega \approx 1$ observationally!

Inflation is necessary!

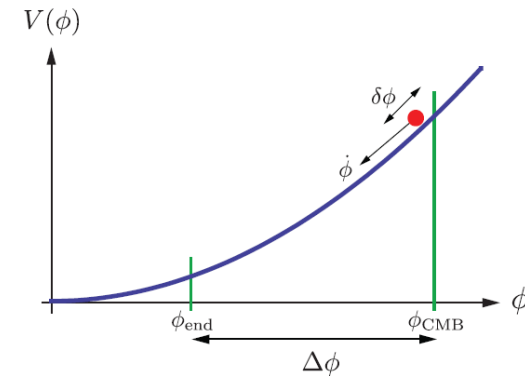
slow roll \longrightarrow V is almost constant

\longrightarrow deSitter $a(t) = e^{Ht}$

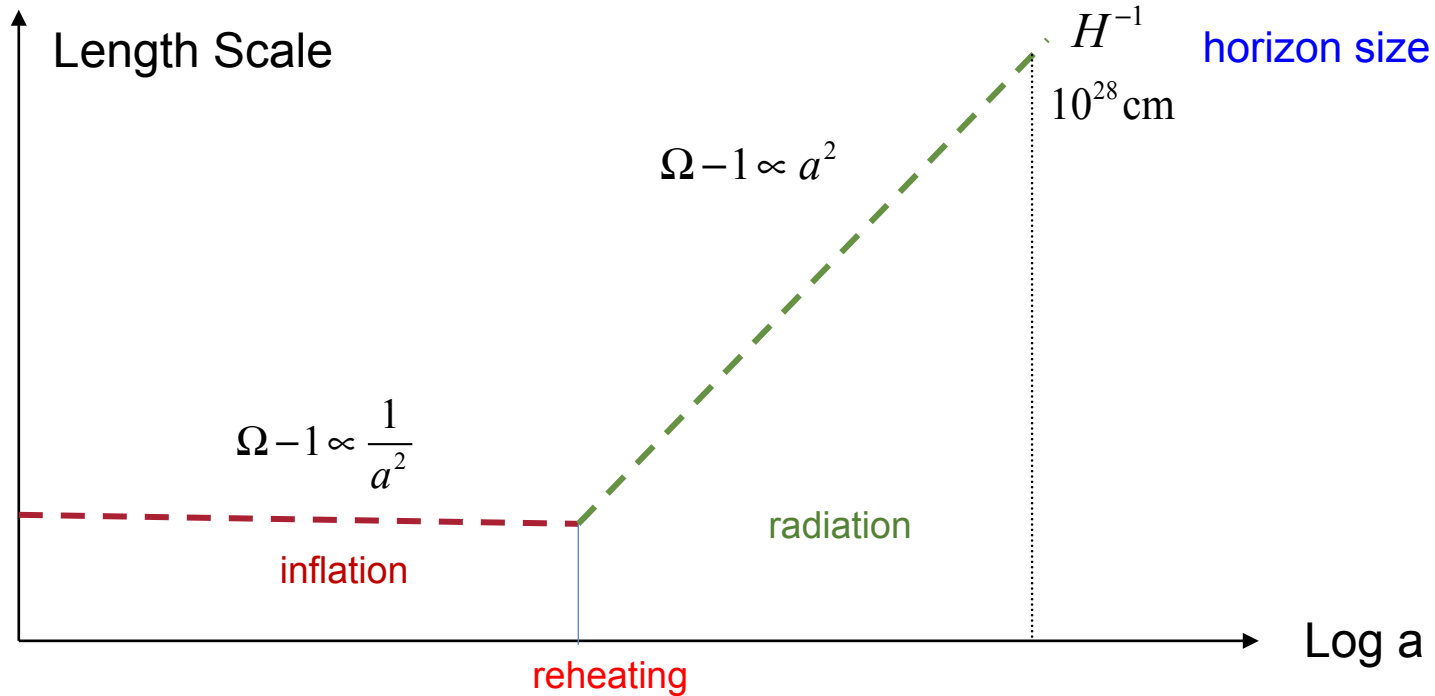
During inflation

$$|\Omega - 1| = \frac{1}{a^2 H^2} \propto \frac{1}{a^2}$$

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 \approx \frac{V}{3M_p^2}$$

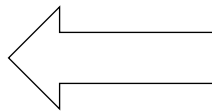


Flatness problem is solved



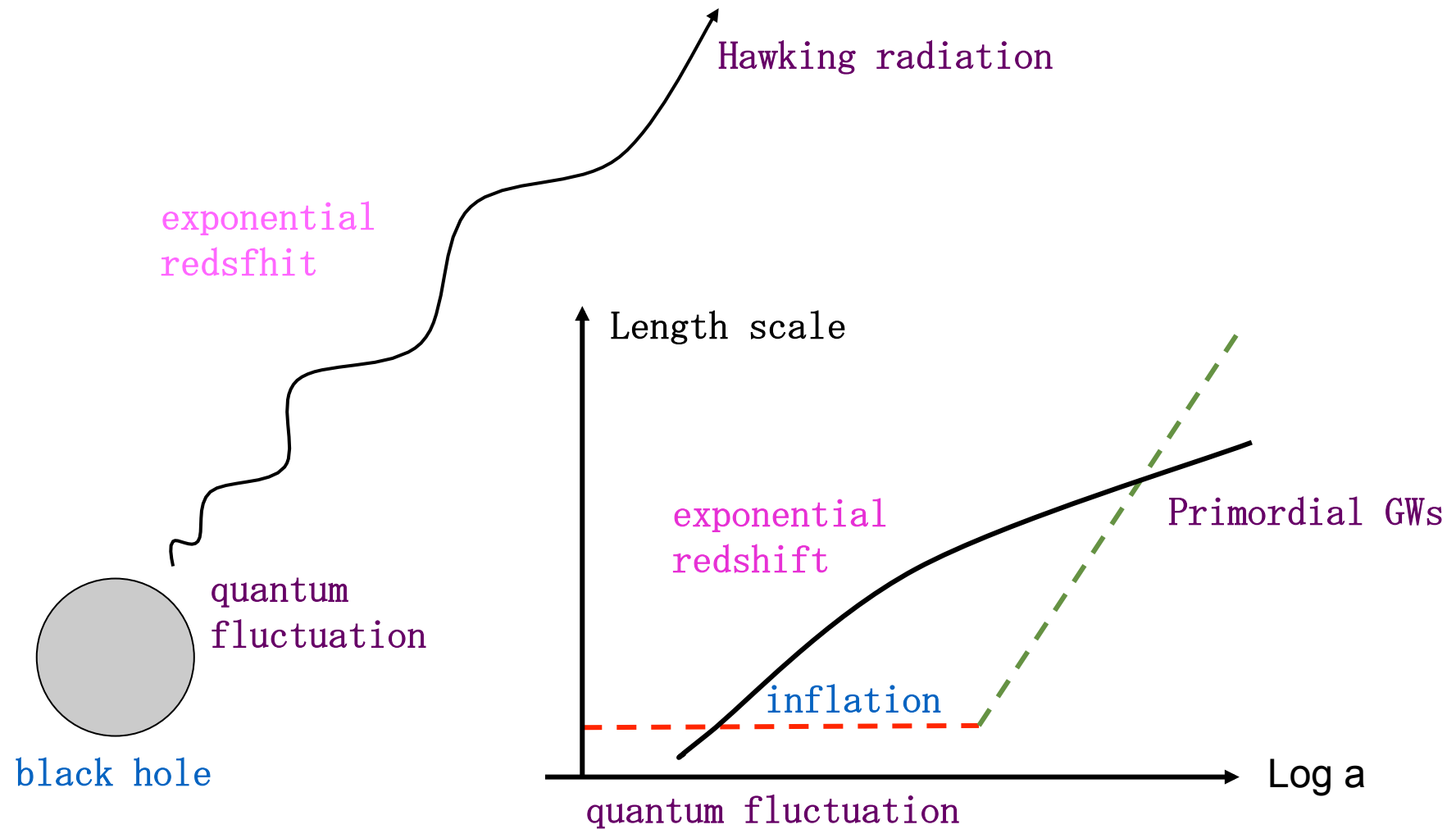
duration of inflation

$$\frac{a(t_e)}{a(t_i)} \approx 10^{29}$$



$$\frac{a_0}{a_{GUT}} = 10^{29}$$

PGWs as Quantum fluctuations of spacetime!

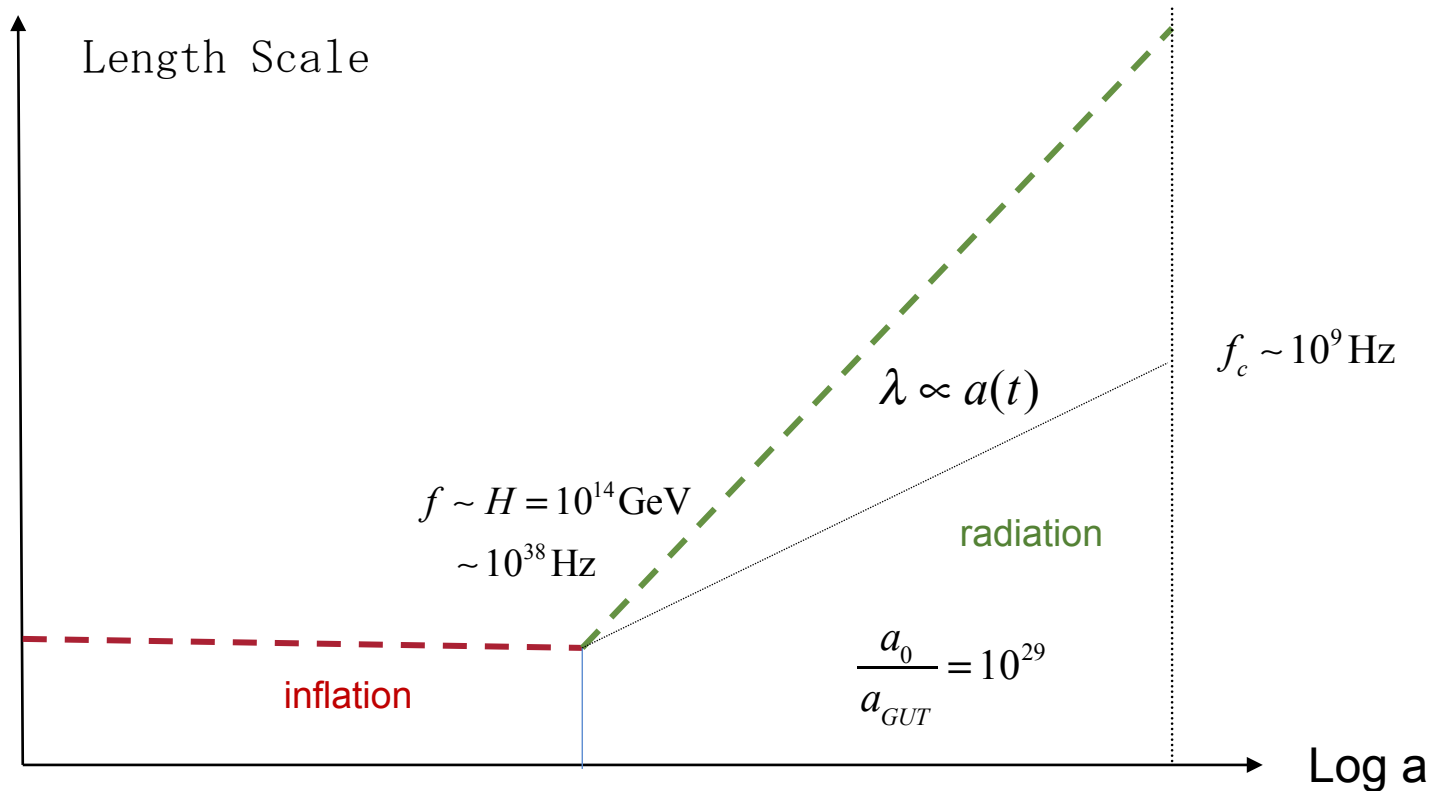


Maximal frequency of PGWs

Free fall time $t_{ff} \sim 1/\sqrt{G\rho}$ \rightarrow frequency $f \sim \sqrt{G\rho} \sim H$

We observe GWs with a red shifted frequency $f_{obs} \sim H \frac{a(t_e)}{a(t_0)} \propto a(t_e)$

Hence, GWs with the maximum frequency are created at the end of inflation.



Squeezed state

Grishchuk 1998

The initial condition is given by Bunch-Davies vacuum.

Because of the cosmic expansion, there occurs the particle production described by the Bogoliubov transformation.

Thus, the cosmic expansion creates the two mode **squeezed state**.

$$\begin{aligned} |BD\rangle &\propto \exp\left[\sum_k \tanh r_k b_k^\dagger b_{-k}^\dagger\right] |0_R\rangle \\ &\propto |0_k\rangle \otimes |0_{-k}\rangle + \tanh r_k |1_k\rangle \otimes |1_{-k}\rangle + \tanh^2 r_k |2_k\rangle \otimes |2_{-k}\rangle + \dots \end{aligned}$$

The squeezing parameter r_k can be calculated as

$$\sinh r_k = \frac{1}{2} \left(\frac{f_c}{f} \right)^2 \qquad f_c = 10^9 \sqrt{\frac{H}{10^{-4} M_p}} \text{ Hz}$$

We assume the present graviton state is kept to be squeezed.

How Matter interact with gravity?

Equivalence principle

Any metric can be set to that of Minkowski spacetime along a geodesic.

Thus, the geodesic motion of a single particle
is always decoupled with a geometry.

$$S_M = -M \int_{\gamma_\tau} d\tau = -M \int d\tau \sqrt{-\eta_{\mu\nu} \frac{dx^\mu}{d\tau} \frac{dx^\nu}{d\tau}}$$

In this local Lorentz coordinate system, we can expand the metric as

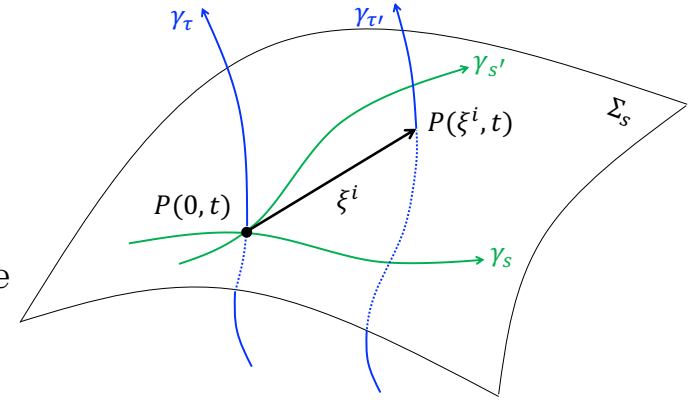
$$g_{\mu\nu}(x^\alpha) = \underbrace{\eta_{\mu\nu} + \frac{1}{2!} g_{\mu\nu,\alpha\beta} \Big|_{\gamma_\tau}}_{\text{described by the spacetime curvature}} (x^\alpha - x_0^\alpha)(x^\beta - x_0^\beta) + \dots$$

described by the spacetime curvature

Fermi normal coordinates

Because of the equivalence principle,
only the relative motion has physical meaning.

Along a geodesic, we can construct the local
Lorentz frame, so-called Fermi-normal coordinate



Action of a geodesics deviation reads

$$\begin{aligned}
 S_m &= -M \int_{\gamma_\tau} d\tau - m \int_{\gamma_{\tau'}} d\tau' = -m \int d\tau' \sqrt{-g_{\mu\nu}(x^\alpha(\tau')) \frac{dx^\mu(\tau')}{d\tau'} \frac{dx^\nu(\tau')}{d\tau'}} \\
 &= -m \int d\tau' \left[1 + \frac{1}{2} R_{0i0j}(t) \xi^i(t) \xi^j(t) - \frac{1}{2} \left(\frac{d\xi^i(t)}{dt} \right)^2 + \dots \right]
 \end{aligned}
 \quad R_{0i0j} = -\frac{1}{2} \frac{\partial^2 h_{ij}}{\partial t^2} \quad \text{in TT gauge}$$

Interaction between a particle and graviton

$$S_m = \int dt \left[\frac{m}{2} \left(\frac{d\xi^i}{dt} \right)^2 + \frac{m}{4} \ddot{h}_{ij}(x^i=0, t) \xi^i \xi^j \right]$$

Quantum matter in graviton background

S. Kanno, J. S. and J. Tokuda,
``Noise and decoherence induced by gravitons,’’
Phys. Rev. D 103, 044017 (2021)

Geodesic motion in graviton BG

Equations of motion

$$\ddot{h}^A(\mathbf{k}, t) + k^2 h^A(\mathbf{k}, t) = \frac{m}{2M_p \sqrt{V}} e_{ij}^{*A}(\mathbf{k}) \frac{d^2}{dt^2} \{ \xi^k(t) \xi^l(t) \}$$

$$\ddot{\xi}(t) = \frac{1}{M_p \sqrt{V}} \sum_{\mathbf{k}, A} e_{ij}^A(\mathbf{k}) \ddot{h}^A(k, t) \xi^j(t)$$

Quantum langevin equation

Parikh, Wilczek, Zahariade 2020, 2021
Kanno, Tokuda, Soda 2021

$$\ddot{\xi}^i(t) + \underbrace{\frac{m}{40\pi M_p^2} \left(\delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk} - \frac{2}{3} \delta_{ij} \delta_{kl} \right)}_{\text{reaction force}} \xi^j \frac{d^5}{dt^5} \{ \xi^k \xi^l \} = -N_{ij} \xi^j$$

Noise:

$$N_{ij} = \frac{2}{M_p \sqrt{V}} \sum_{\mathbf{k}, A} k^2 h_I^A(\mathbf{k}, t) e^{i\mathbf{k} \cdot \mathbf{x}} e_{ij}^A(\mathbf{k})$$

$$h_I^A(\mathbf{k}, t) = a_A(\mathbf{k}) u_k(t) + a_A^\dagger(-\mathbf{k}) u_k^*(t)$$

$$[a_A(\mathbf{k}), a_{A'}^\dagger(\mathbf{k}')] = \delta_{AA'} \delta_{\mathbf{k}, \mathbf{k}'}$$

Noise of gravitons in squeezed state

Noise correlation

$$\langle \psi | \{N_{ij}(t), N_{kl}(0)\} | \psi \rangle = \frac{1}{10\pi^2 M_p^2} \left(\delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk} - \frac{2}{3} \delta_{ij} \delta_{kl} \right) F(\Omega_m t) \quad \Omega_m : \text{cutoff}$$

$$F(\Omega_m t) = \int_0^{\Omega_m} dk k^6 \operatorname{Re} \left(u_k^{sq}(t) u_k^{sq*}(0) \right)$$

$$u_k^{sq}(t) = u_k^M(t) \cosh r_k - u_k^{M*}(t) \sinh r_k$$

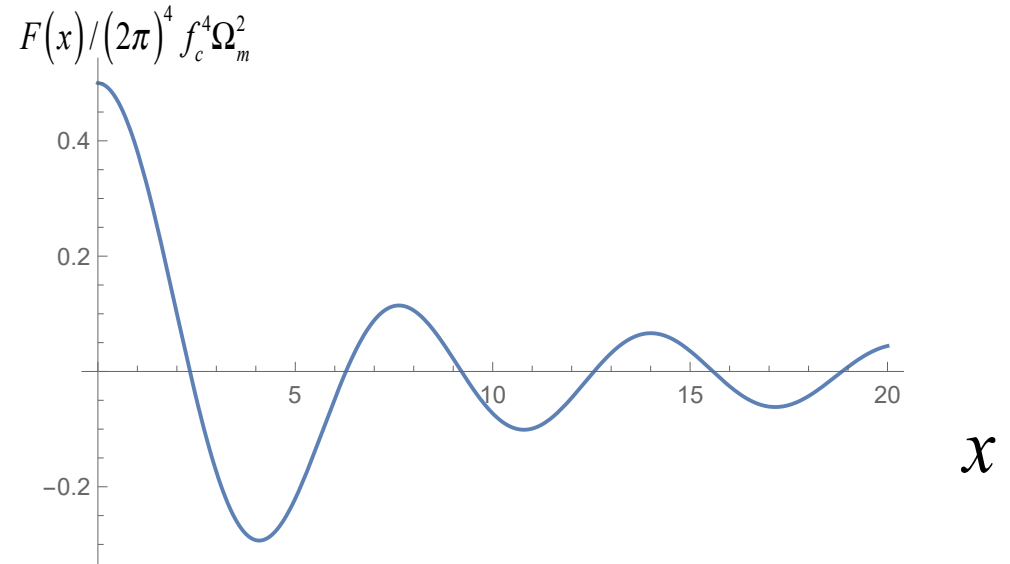
$$u_k^M(\eta) = \frac{1}{\sqrt{2k}} e^{-ik\eta}$$

Recall the formula

$$\sinh r_k = \frac{1}{2} \left(\frac{f_c}{f} \right)^2, \quad k = 2\pi f$$

For $r_k \gg 1$, we obtain

$$F(x) = (2\pi)^4 f_c^4 \Omega_m^2 \frac{x \sin x + \cos x - 1}{x^2}$$



Thus, squeezed state significantly enhances the noise of gravitons.

Indirect detection of gravitons

S.Kanno, J.S. and J.Tokuda,
``Indirect detection of gravitons through quantum entanglement,``
[arXiv:2103.17053 [gr-qc]].

Quantum mirrors and a single photon

By using laser cooling, we can make a ground state of mirrors.

$$|\psi(t_i)\rangle = \underbrace{|0\rangle \otimes |0\rangle}_{\text{mirror ground state}} \otimes |g\rangle$$

Yu et al. 2020

squeezed graviton state

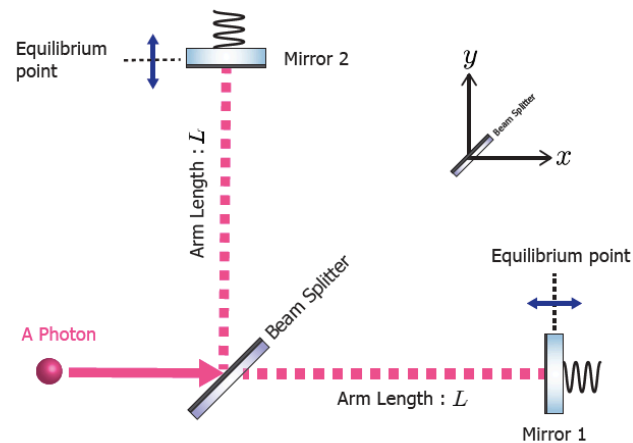


40kg quantum mirrors

A single photon goes through a beam splitter or reflected by it, which is described by a superposition state.

Marshall et al. 2003

$$|\Phi(t_i)\rangle = |\text{arm: 1}\rangle + |\text{arm: 2}\rangle$$



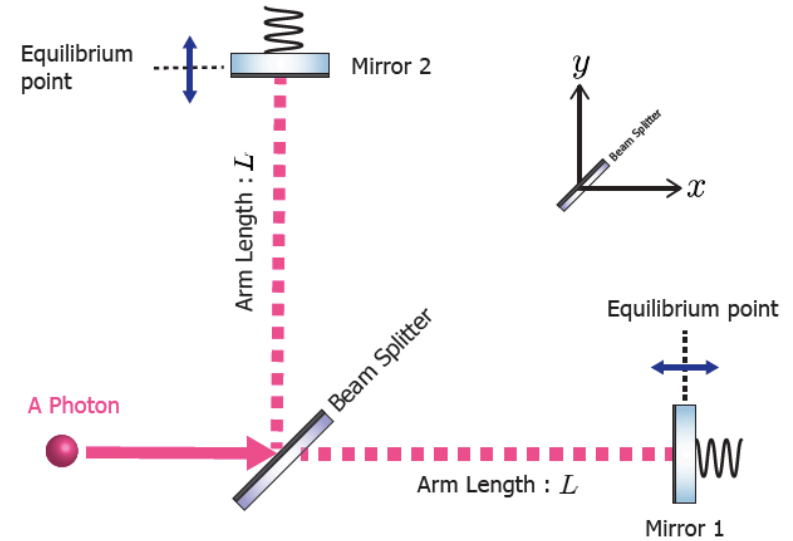
Entangled mirrors

When the photon hit a mirror, the mirror starts to oscillate.
Thus, there arises a superposition state of mirrors.

$$|\psi(t_i)\rangle = \left\{ \frac{1}{\sqrt{2}}|\xi_1\rangle \otimes |0\rangle + \frac{1}{\sqrt{2}}|0\rangle \otimes |\xi_2\rangle \right\} \otimes |g\rangle$$

Reduced density matrix

$$\begin{aligned} \rho(t_i) &= \text{Tr}_g |\psi(t_i)\rangle \langle \psi(t_i)| \\ &= \left\{ \frac{1}{\sqrt{2}}|\xi_1\rangle \otimes |0\rangle + \frac{1}{\sqrt{2}}|0\rangle \otimes |\xi_2\rangle \right\} \left\{ \frac{1}{\sqrt{2}}\langle \xi_1| \otimes \langle 0| + \frac{1}{\sqrt{2}}\langle 0| \otimes \langle \xi_2| \right\} \\ &= \frac{1}{2}|\xi_1\rangle \langle \xi_1| \otimes |0\rangle \langle 0| + \underbrace{\frac{1}{2}|0\rangle \langle \xi_1| \otimes |\xi_2\rangle \langle 0| + \frac{1}{2}|\xi_1\rangle \langle 0| \otimes |0\rangle \langle \xi_2|}_{\text{interference terms}} + \frac{1}{2}|0\rangle \langle 0| \otimes |\xi_2\rangle \langle \xi_2| \end{aligned}$$



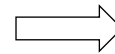
Can a single photon excite a mirror?

Condition for displacement by grand state size:

Momentum imparted by the photon has to be larger than the initial uncertainty of the mirror momentum.

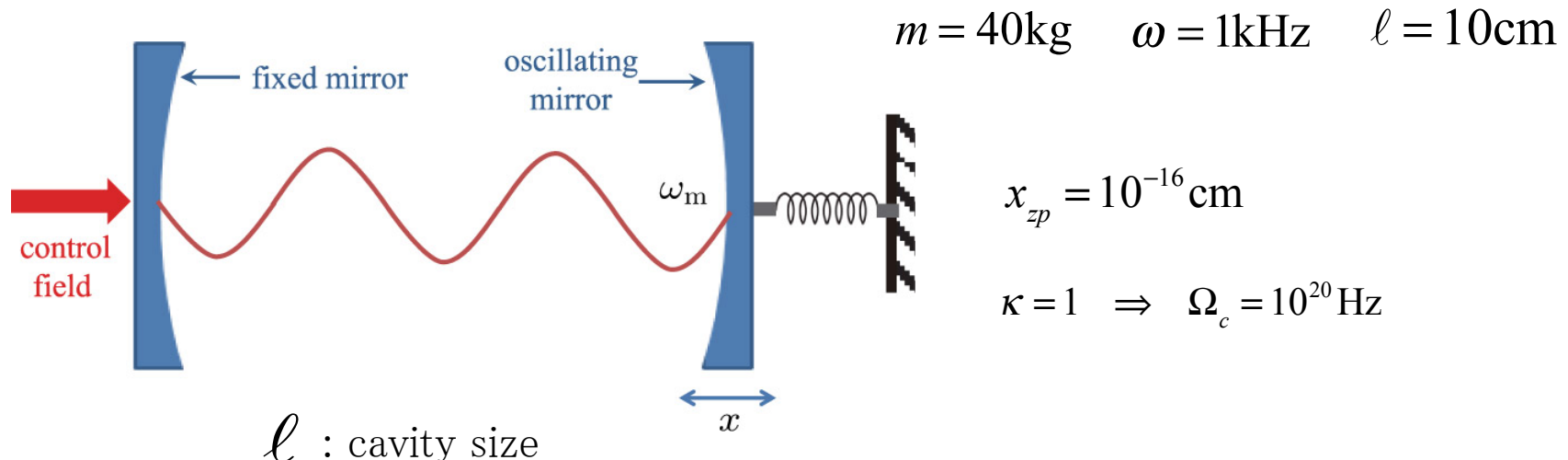
photon momentum period of mirror oscillation

$$\frac{\Omega_c}{c} \frac{2\pi}{\omega_m} \frac{1}{\ell} \geq \sqrt{m\omega_m} \quad \text{momentum uncertainty}$$



$$\kappa = \frac{\Omega_c}{\omega_m} \frac{x_{zp}}{\ell} \geq 1 \quad x_{zp} = \sqrt{\frac{\hbar}{2m\omega_m}}$$

time of one round trip



Decoherence of entangled mirrors

After a while, the mirrors are interacting with gravitons

$$S \simeq \sum_{A=1,2} \int dt \left[\frac{m}{4} \ddot{h}_{11}(0,t) \xi_A^1 \xi_A^1 + \frac{m}{4} \ddot{h}_{22}(0,t) \xi_A^2 \xi_A^2 \right]$$

Consequently, there appears the entanglement
between the mirrors and gravitons.

$$|\psi(t_i)\rangle = \frac{1}{\sqrt{2}} |\xi_1\rangle \otimes |0\rangle \otimes |g; \xi_1\rangle + \frac{1}{\sqrt{2}} |0\rangle \otimes |\xi_2\rangle \otimes |g; \xi_2\rangle$$

Thus, mirrors will be decohered due to noises of gravitons.

$$\rho(t) = \text{Tr}_g |\psi(t)\rangle \langle \psi(t)|$$

$$= \frac{1}{2} |\xi_1\rangle \langle \xi_1| \otimes |0\rangle \langle 0| + \frac{1}{2} \underbrace{\langle g; \xi_1 | g; \xi_2 \rangle |0\rangle \langle \xi_1| \otimes |\xi_2\rangle \langle 0| + \langle g; \xi_2 | g; \xi_1 \rangle |\xi_1\rangle \langle 0| \otimes |0\rangle \langle \xi_2|}_{\text{interference terms}} + \frac{1}{2} |0\rangle \langle 0| \otimes |\xi_2\rangle \langle \xi_2|$$

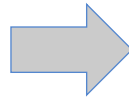
Entanglement Negativity

Initial density matrix of mirrors

$$\rho_m = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \rho_{11} & \rho_{12} & 0 \\ 0 & \rho_{21} & \rho_{22} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

After evolution

$$\rho_m = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \rho_{11} & \exp(i\Phi)\rho_{12} & 0 \\ 0 & \exp(-i\Phi^*)\rho_{21} & \rho_{22} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$



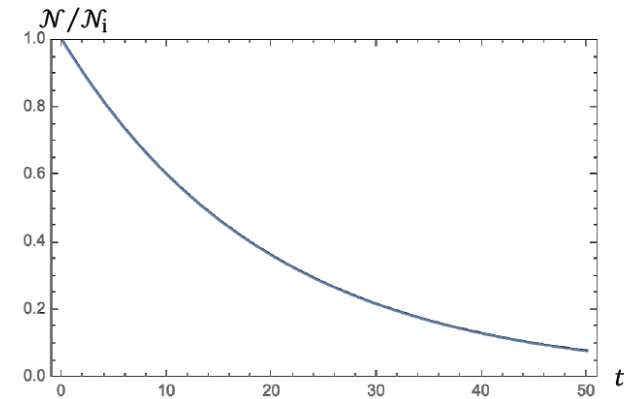
Taking a partial transpose,

$$\rho_m = \begin{pmatrix} 0 & 0 & 0 & \exp(i\Phi)\rho_{12} \\ 0 & \rho_{11} & 0 & 0 \\ 0 & 0 & \rho_{22} & 0 \\ \exp(-i\Phi^*)\rho_{21} & 0 & 0 & 0 \end{pmatrix}$$

We can calculate the negativity

$$\Gamma = \text{Im} \Phi$$

$$\mathcal{N} = |\rho_{12}(t_i)| \exp(-\Gamma)$$



Decoherence time

By solving non-Markovian master equation, we obtain the decoherence rate

$$\Gamma = \frac{4\pi^3}{5} \underbrace{\left(\frac{m}{M_p}\right)^2}_{\text{effective coupling}} \underbrace{(Lf_c)^4}_{\text{squeezing factor}} \left(\frac{A}{L}\right)^2 \omega \quad M_p \approx 10^{-5} g$$

Substituting

$$m = 40\text{kg}, \quad L = 40 \text{ km}, \quad A = 10 \frac{\hbar}{\sqrt{2m\omega}} = 10^{-15} \text{cm}, \quad \omega = 1\text{kHz}, \quad f_c = 1\text{GHz}$$

we see the decoherence time is **20s**.

Note that the decoherence due to air molecule is dominant among other decoherence sources.

In the present case, the time scale becomes

$$t_d = 1200 \left(\frac{a}{0.17\text{m}}\right)^{-2} \left(\frac{T}{10\text{K}}\right)^{-3/2} \text{ s} \quad P = 10^{-10} \text{ Pa}$$

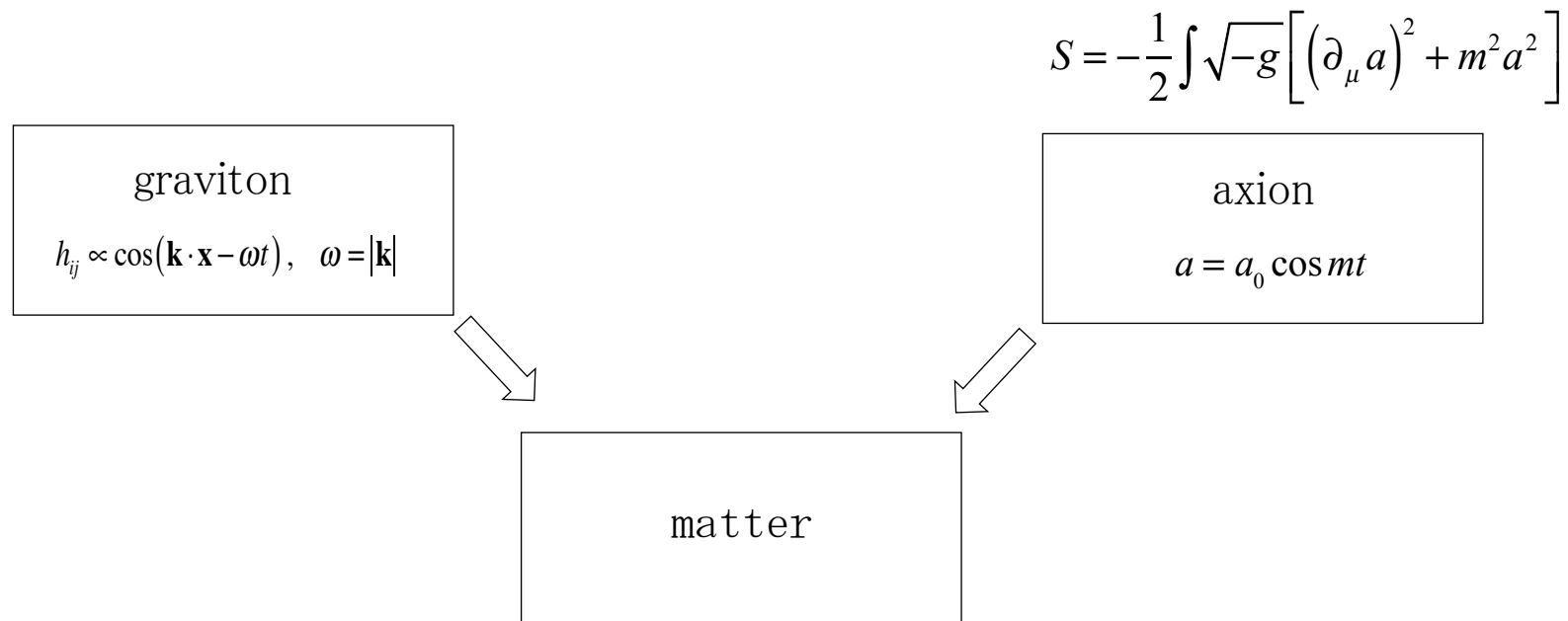
This time scale is much larger than the decoherence time due to noise of gravitons. Therefore, there is a chance to detect gravitons indirectly.

Duality of axion and graviton experiments

--- A working hypothesis ---

Duality of axion and graviton experiments

Both axions and graviton are coherently oscillating.



Remarkably, there exists a duality between axion and graviton experiments.

Detectors useful for axion search
is also useful for graviton search

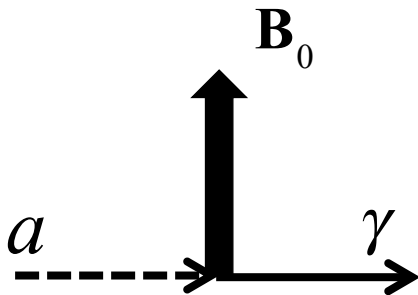
Detectors useful for axion search
is also useful for graviton search

Axion - photon - graviton conversion

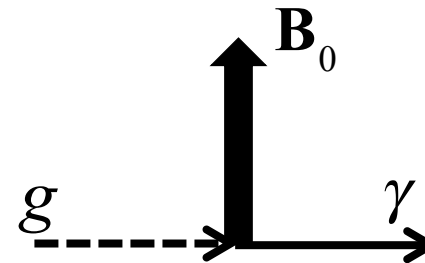
We often use photons to probe axions and gravitons.

$$S = \int \sqrt{-g} \left[-\frac{1}{4} g^{\mu\alpha} g^{\nu\beta} F_{\mu\nu} F_{\alpha\beta} + \frac{1}{4} a \epsilon^{\mu\nu\lambda\rho} F_{\mu\nu} F_{\lambda\rho} \right]$$

$$L \supset a \mathbf{E} \cdot \mathbf{B}_0 \quad \text{Sikivie 1983}$$



$$L \supset h_{ij} E^i B_0^j \quad \text{Gertsenshtein 1962}$$



The photons could be other excitations such as phonons, magnons, \dots .

An application of duality

A useful application of duality is
to use **existing data from axion experiments**
for giving constraints on gravitons.

Here, we take magnons and show how to use duality to probe gravitons.

Axion - **magnon** - graviton conversion

Remarkably, it is possible to detect a single magnon with the superconducting qubit.
In the future, we will be able to create the squeezed magnon system.
Thus, we can utilize the recent development of quantum sensing.

Axion search with magnons

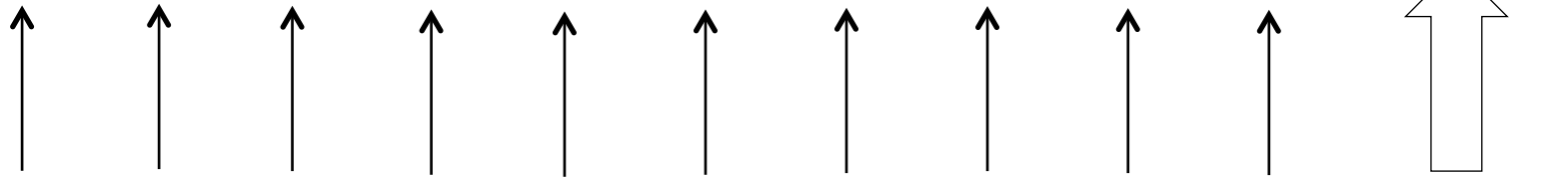
T. Ikeda, A. Ito, K. Miuchi, J. Soda, H. Kurashige and Y. Shikano,
``Axion search with quantum nondemolition detection of magnons,’’
[arXiv:2102.08764 [hep-ex]].

Spin waves

The homogeneous magnetic field is imposed.

Bohr magneton

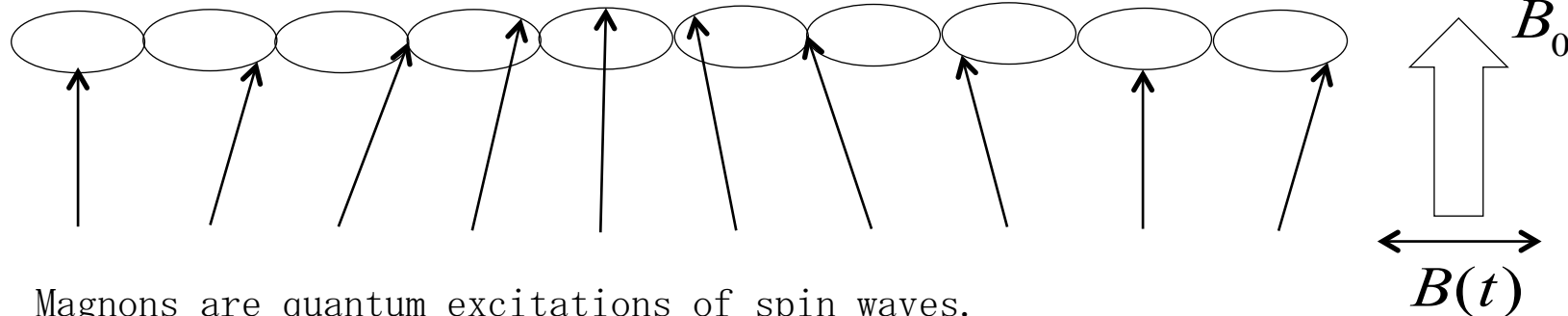
$$H = -2\mu_B \sum_i \hat{S}_i \cdot \vec{B}_0 - \sum_{i,j} J_{ij} \hat{S}_i \cdot \hat{S}_j \quad \mathbf{S} = \frac{1}{2} \boldsymbol{\sigma} \quad \mu_B = \frac{e\hbar}{2m_e}$$



The above is the ground state.

Microwaves are used for generating spin waves.

$$H = -2\mu_B \sum_i \hat{S}_i \cdot (\vec{B}_0 + B(t)) - \sum_{i,j} J_{ij} \hat{S}_i \cdot \hat{S}_j$$



Magnons are quantum excitations of spin waves.

Their creation and annihilation are described by c^\dagger and c .

$$H_{\text{magnon}} = \hbar\omega c^\dagger c \quad \hbar\omega = 2\mu_B B_0 \quad \text{Larmor frequency}$$

Axion - magnon interaction

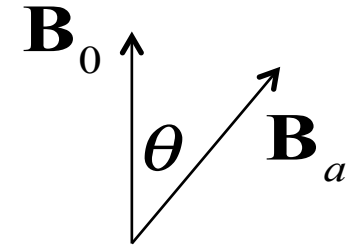
Interaction term
$$L_{\text{int}} = -ig_{aee} a \bar{\psi} \gamma_5 \psi = \frac{g_{aee}}{2m} \partial_\mu a \bar{\psi} \gamma^\mu \gamma_5 \psi$$

In a nonrelativistic approximation,

$$H \simeq \frac{(\mathbf{p} - e\mathbf{A})^2}{2m_e} - 2\mu_B \hat{S} \cdot \mathbf{B}_0 - 2\mu_B \hat{S} \cdot \mathbf{B}_a(t)$$

The coherently oscillating axion can plays a roll of microwaves.

$$\begin{aligned} \vec{B}_a(t) &= \frac{g_{aee}}{e} \vec{\nabla} a(t) \\ &= \left(\frac{1}{2} B_a \sin \theta \left(e^{-i\omega_a t} + e^{i\omega_a t} \right), 0, 0 \right) \end{aligned} \quad f_a = \frac{\omega_a}{2\pi} = \frac{m_a c^2}{h} = 0.24 \left(\frac{m_a}{1.0 \mu\text{eV}} \right) \text{GHz}$$



We consider only Kittel mode ($k=0$)

$$H_{m-a} = \hbar \omega c^\dagger c + g_{\text{eff}} \left(c^\dagger e^{-i\omega_a t} + c e^{i\omega_a t} \right)$$

Number of electron density

Case of YIG $N \approx 10^{22}$

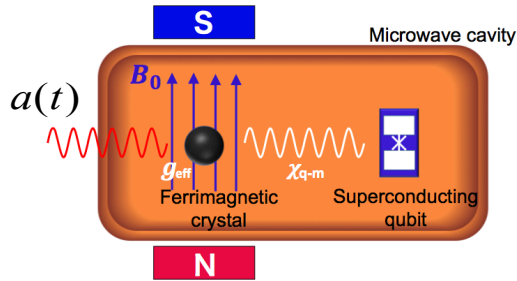
$$g_{\text{eff}} = \frac{1}{2} \mu_B B_a \sin \theta \sqrt{N}$$



Magnon limits on axions

Read out by Q-bit

Axion is coherently oscillating



$$a(t) \approx \frac{\sqrt{2\rho_{DM}}}{m_a} \cos m_a t$$

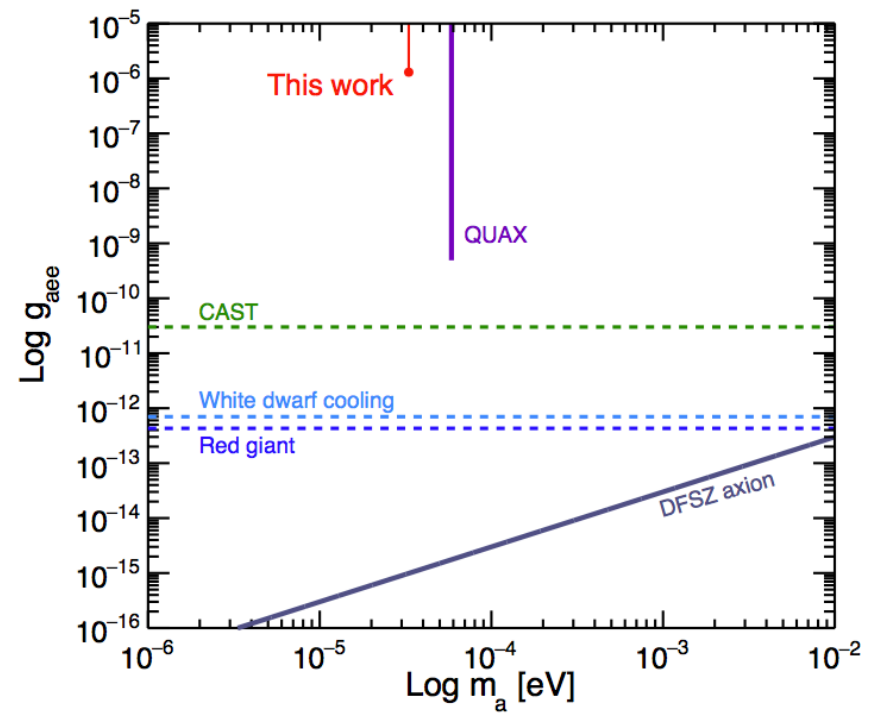
$$B_a = \frac{g_{aee}}{e} \nabla a$$

$$\simeq 4.4 \times 10^{-8} g_{aee} \left(\frac{\rho_{DM}}{0.45 \text{ GeV/cm}^3} \right)^{1/2} \left(\frac{v}{300 \text{ km/s}} \right) [\text{T}]$$

magnon limits on the axion electron coupling constant

$$B_a < 4.1 \times 10^{-14} [\text{T}]$$

$$\longrightarrow g_{aee} < 1.3 \times 10^{-6}$$



Ikeda et al. 2018

Graviton search with magnons

A. Ito, T. Ikeda, K. Miuchi and J. Soda,
``Probing GHz gravitational waves with graviton-magnon resonance,’’
Eur. Phys. J. C80, no.3, 179 (2020) [arXiv:1903.04843 [gr-qc]].

A. Ito and J. Soda,
``A formalism for magnon gravitational wave detectors,’’
Eur. Phys. J. C80, no.6, 545 (2020) [arXiv:2004.04646 [gr-qc]].

Graviton - magnon interaction

GWs

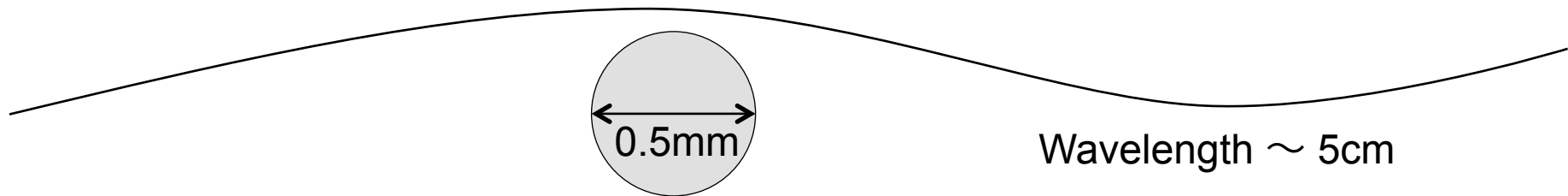
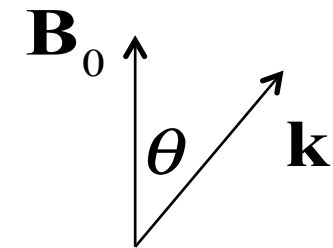
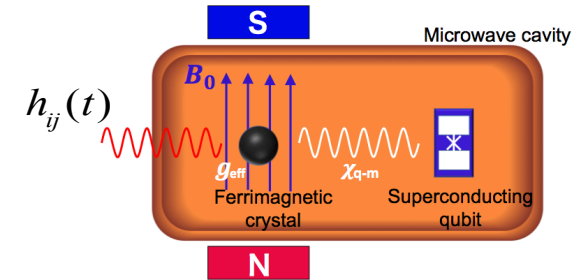
$$h_{ij}(t) = h^+(t)e_{ij}^+ + h^\times(t)e_{ij}^\times$$

$$h^{+, \times}(t) = \frac{h^{+, \times}}{2} \left(e^{-i\omega_h t} + e^{i\omega_h t} \right)$$

$$H = -2\mu_B \sum_i \hat{S}_i \cdot \vec{B}_0 - \mu_B \sum_i S_i^a h_{az}(t) B_0 - \sum_{i,j} J_{ij} \hat{S}_i \cdot \hat{S}_j$$

$$H_{m-g} = \hbar\omega c^\dagger c + g_{eff} \left(c^\dagger e^{-i\omega_h t} + c e^{i\omega_h t} \right)$$

$$g_{eff} = \frac{1}{4\sqrt{2}} \mu_B B_0 \sin\theta \sqrt{N} \left[\cos^2\theta \left(h^{(+)} \right)^2 + \left(h^{(\times)} \right)^2 \right]^{1/2}$$



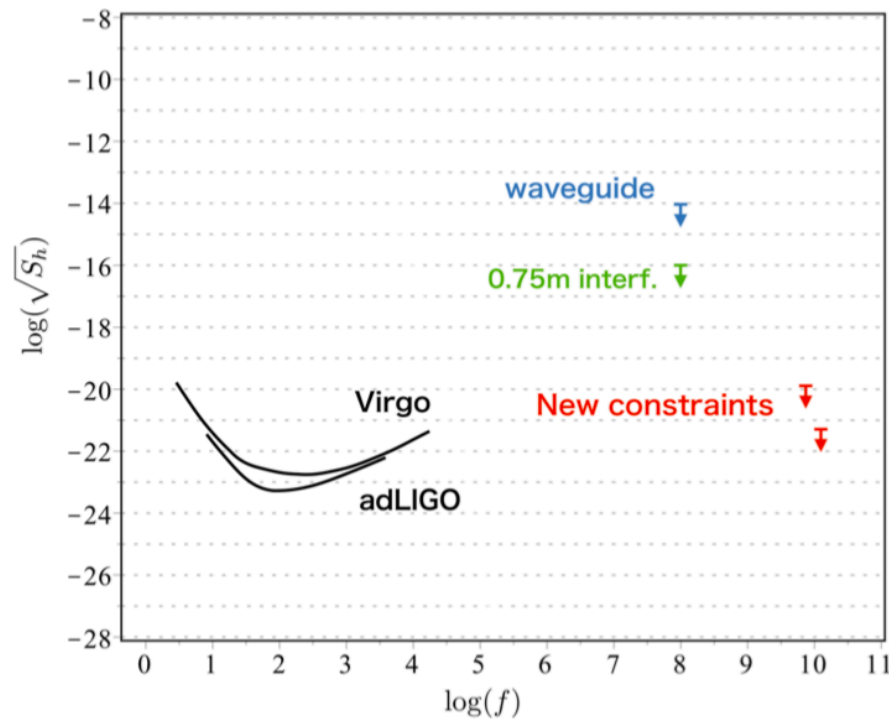
Magnon limits on GHz GWs

Ito et al. 2019
Ito & Soda 2020

Limits on axions

$$g_{eff} < \begin{cases} 3.5 \times 10^{-12} \text{ eV} & \text{QUAX, Crescini et al. 2018} \\ 3.1 \times 10^{-11} \text{ eV} & \text{Flower et al. 2018} \end{cases}$$

$$g_{eff} = \frac{1}{4\sqrt{2}} \mu_B B_z \sin \theta \sqrt{N} \left[\cos^2 \theta \left(h^{(+)} \right)^2 + \left(h^{(\times)} \right)^2 \right]^{1/2}$$



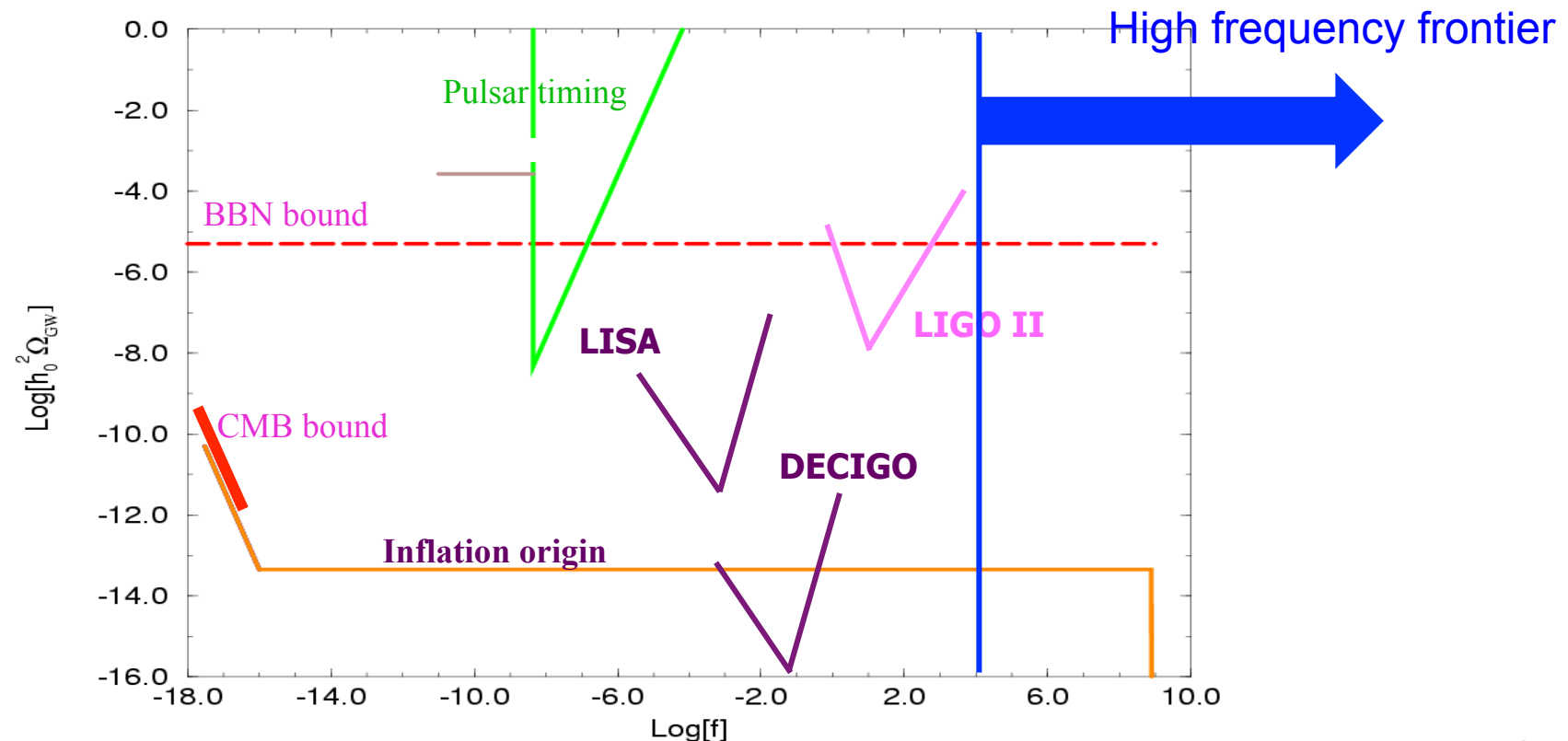
$$\sqrt{S_h} \approx h < \begin{cases} 7.6 \times 10^{-22} \text{ Hz}^{-1/2} & \text{at } 14 \text{ GHz} \\ 1.2 \times 10^{-20} \text{ Hz}^{-1/2} & \text{at } 8.2 \text{ GHz} \end{cases}$$

High frequency GW physics

It is interesting to probe PBHs and axion dark matter
with high frequency gravitational waves.

Necessary sensitivity is around $h \approx 10^{-26}$

It should be stressed that we borrowed the existing data from the axion experiment.
If we construct a detector for GWs, the sensitivity could be significantly improved.



Summary

- We obtained quantum Langevin equation for a massive particle with graviton noise.
- We have discussed **indirect** detection of gravitons.
The decoherence time is 20s much shorter than that of other decoherence sources. In principle, we can detect gravitons by observing the quantum **entanglement negativity**.
- Aiming at detecting a graviton, we developed a detection method for high frequency gravitational waves.
- By borrowing the existing data from axion search, we have succeeded in giving constraints on the amplitude of **GHz HFGWs**.