

# Probing strong gravity when gravity waves

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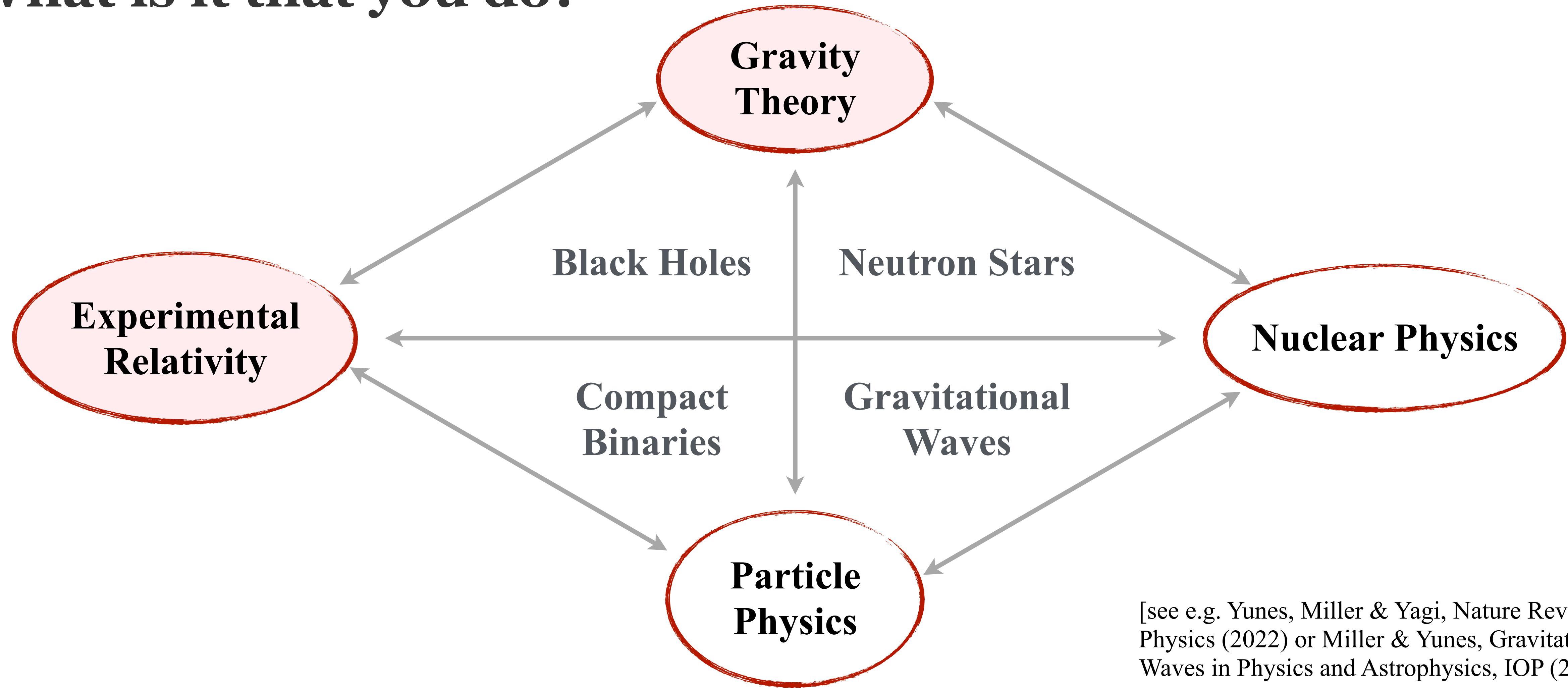
## Nico's Graviteers



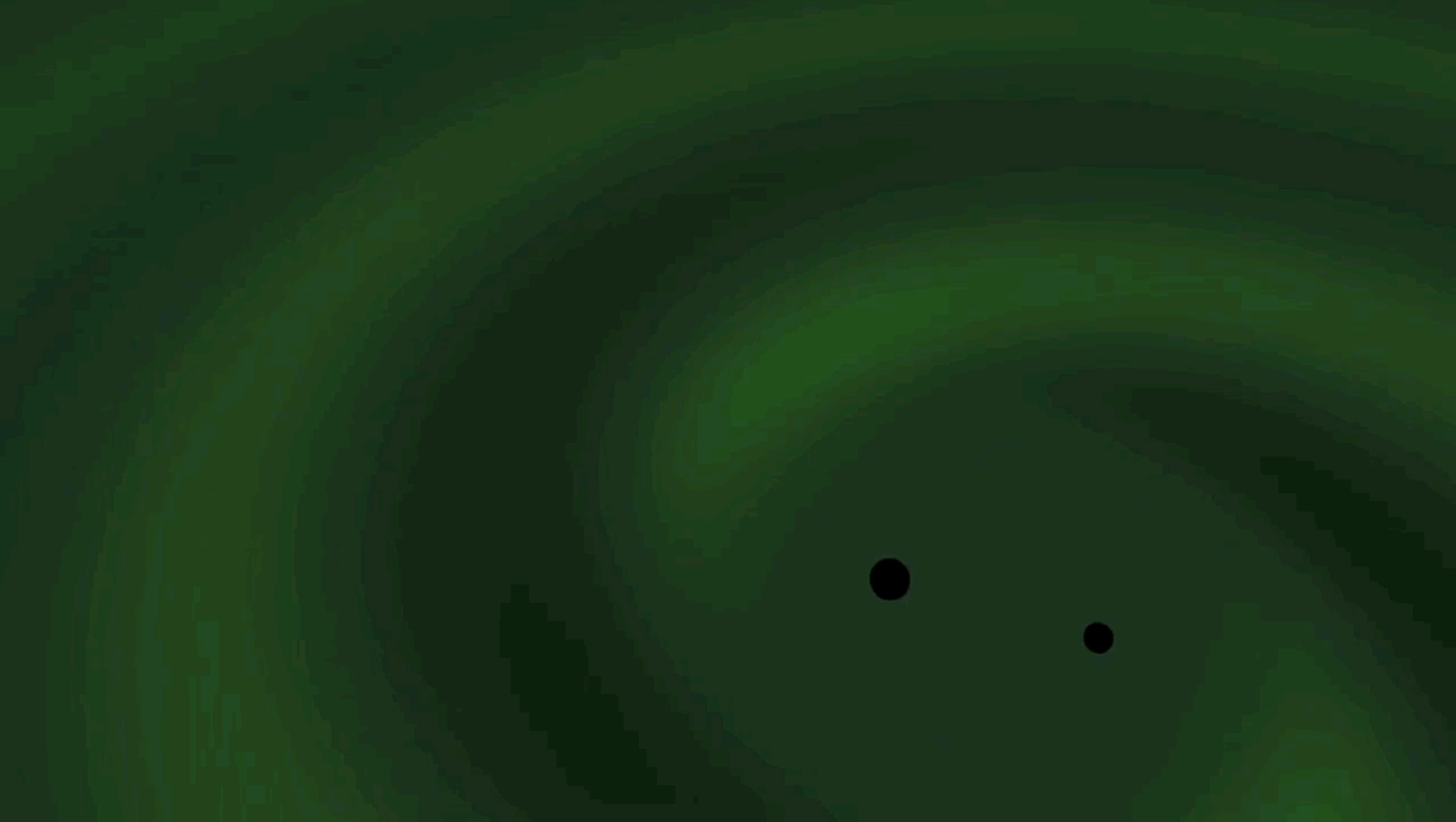
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# What is it that you do?



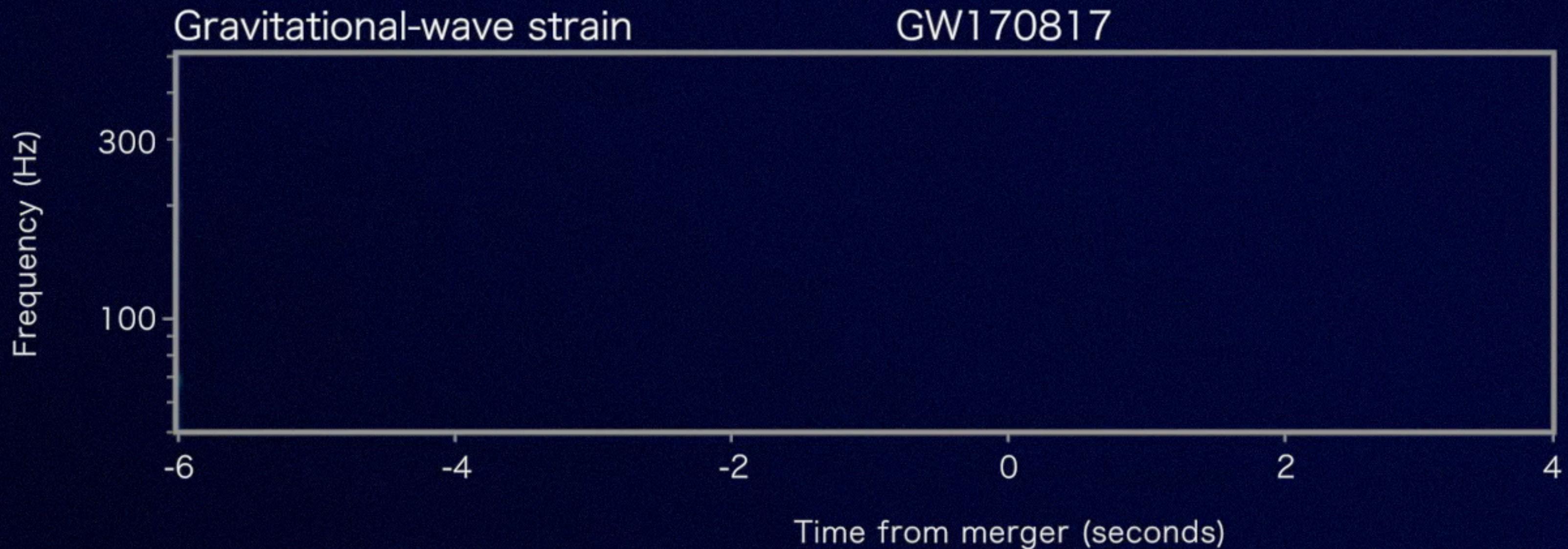
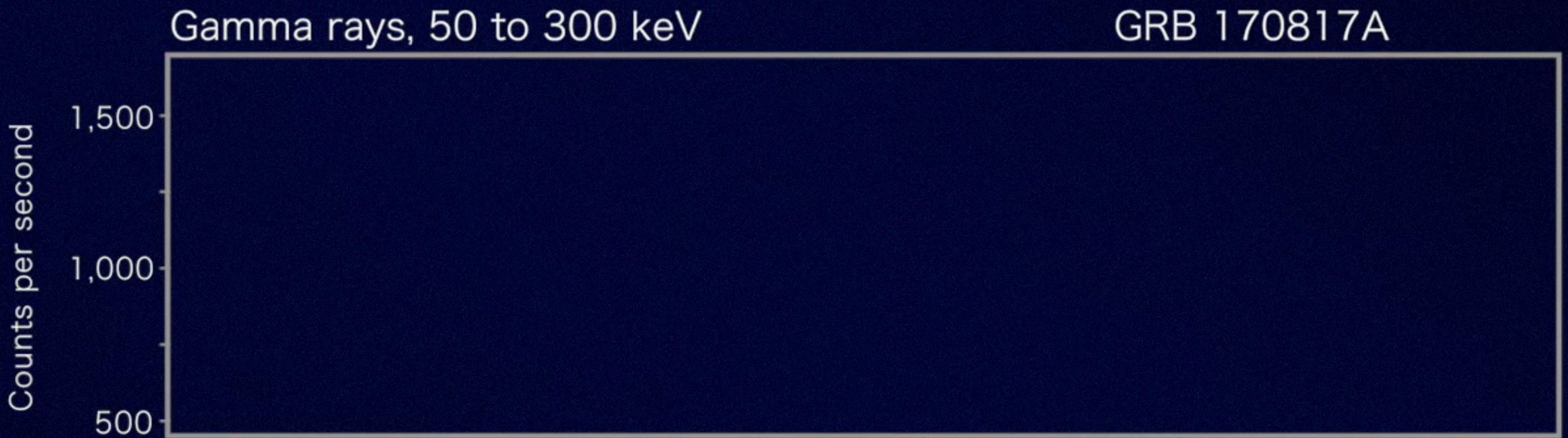
What “fundamental” physics have we/will we learn from gravitational wave observations?



Fermi

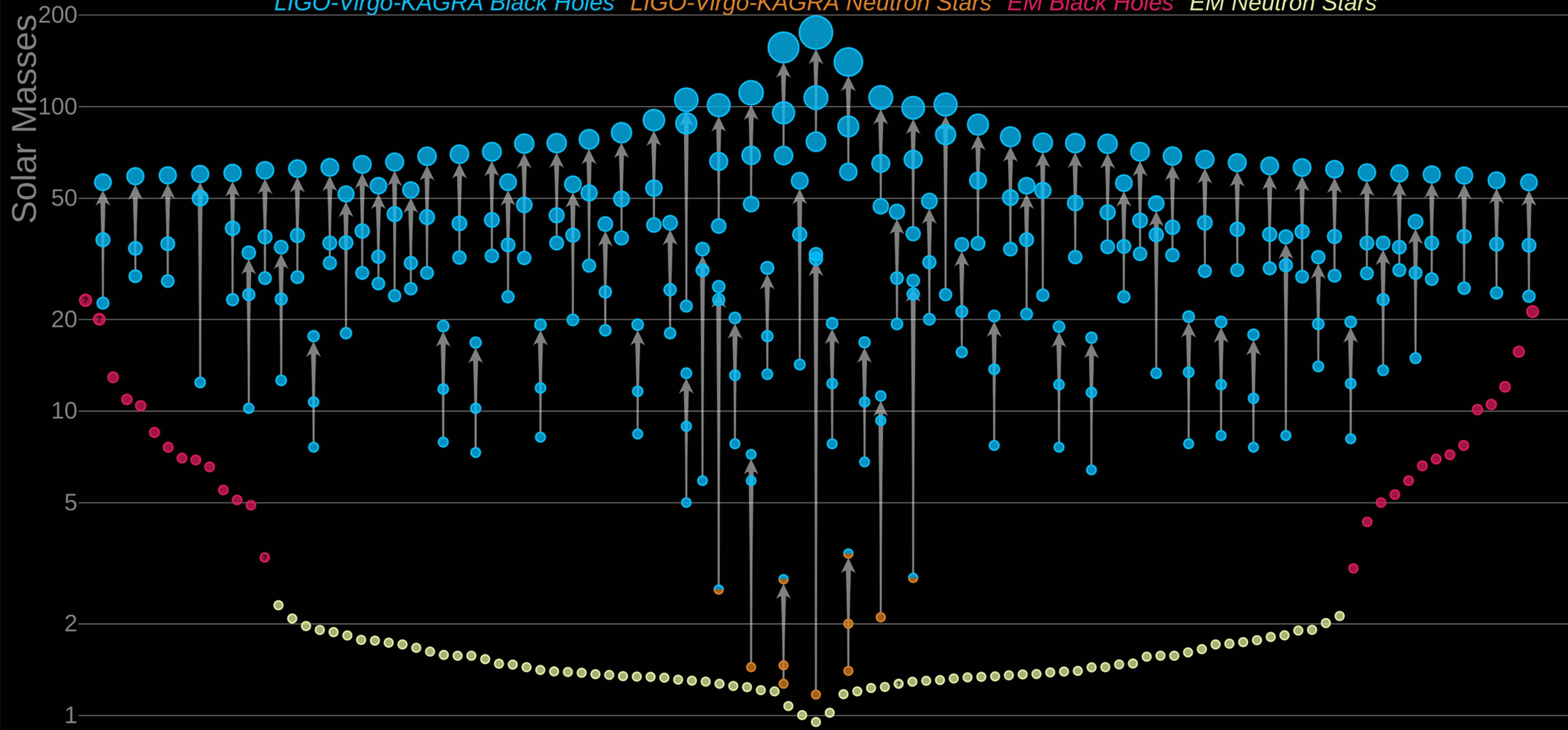


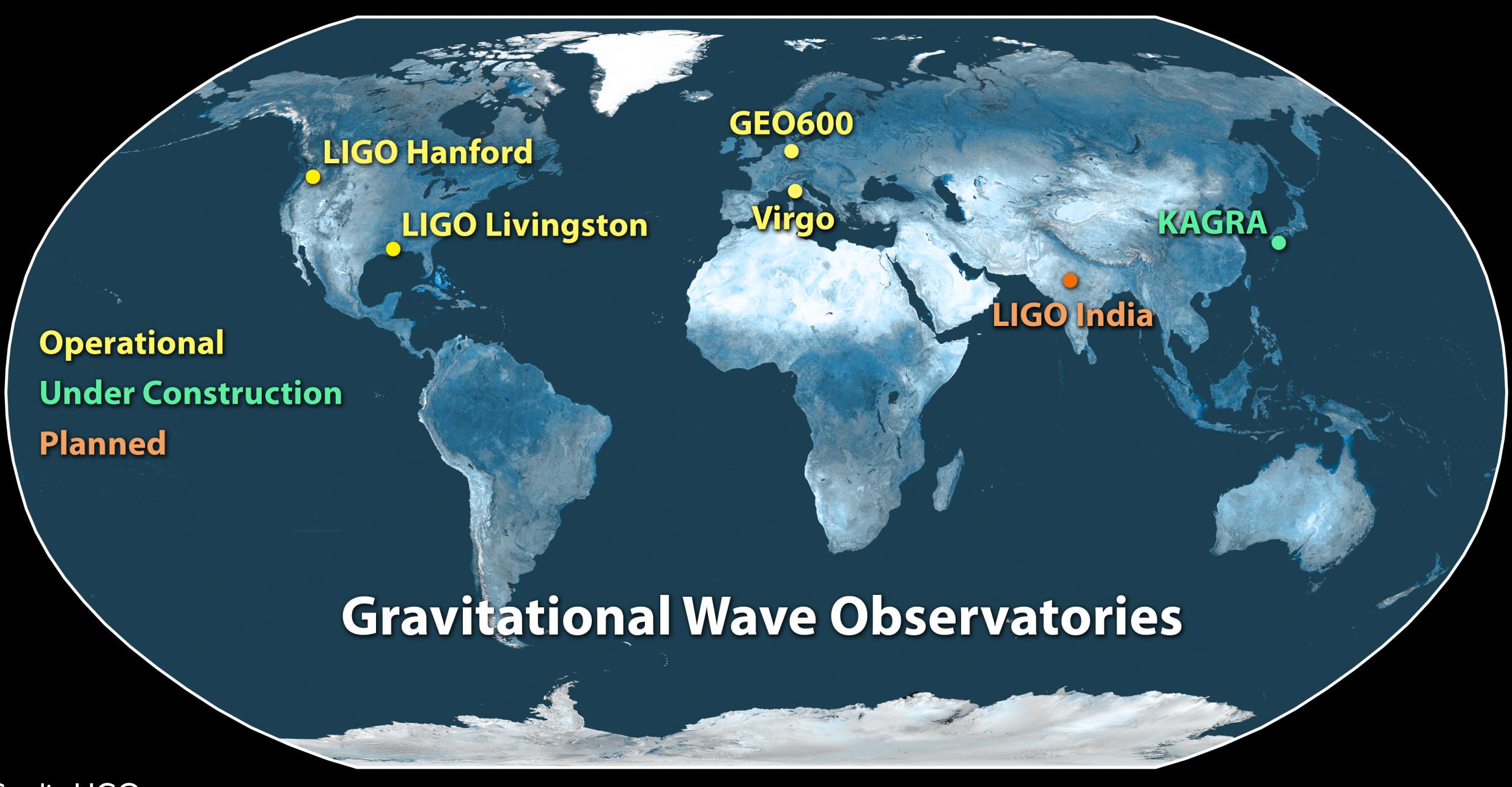
LIGO



# Masses in the Stellar Graveyard

LIGO-Virgo-KAGRA Black Holes LIGO-Virgo-KAGRA Neutron Stars EM Black Holes EM Neutron Stars



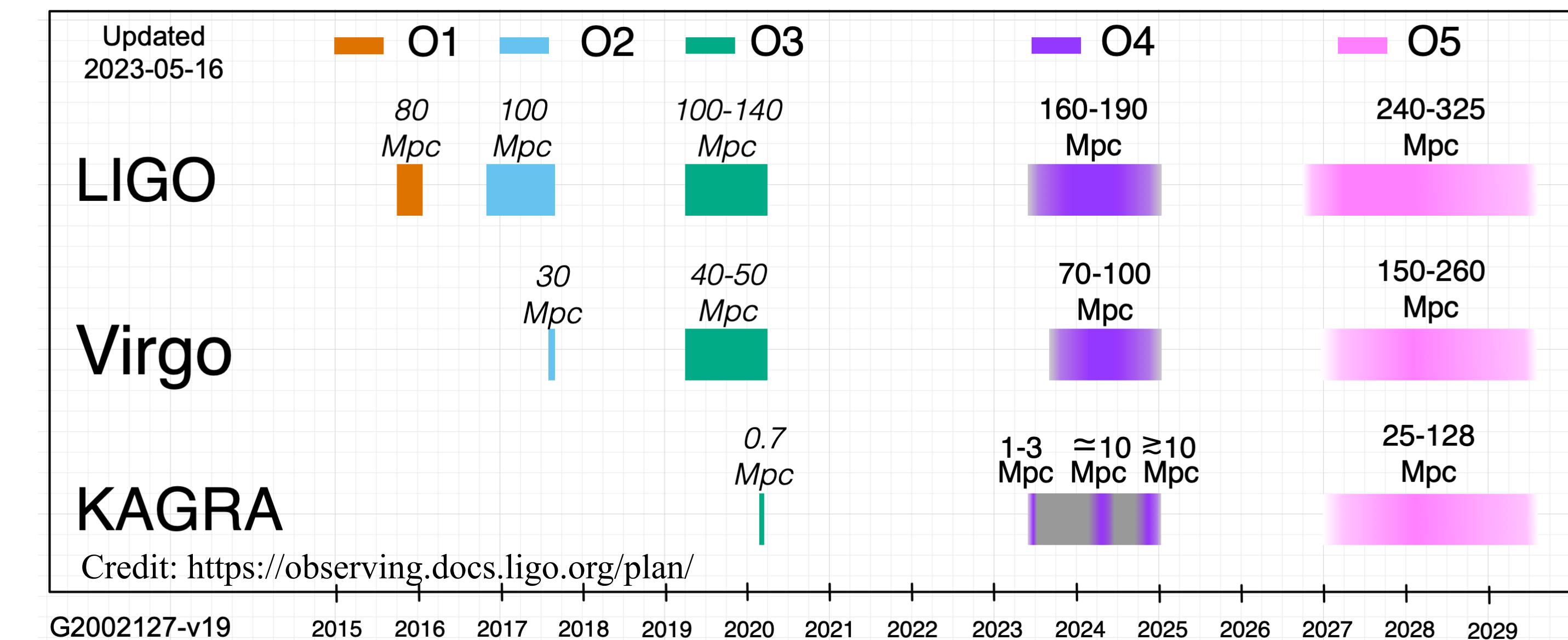


**Fact**

The future is loud

**Challenge**

So what are you going to do with all this data?



**ABC of GWs**

Frodo and Sam

**Probing  
Fundamental  
Physics**

**Into the  
Unknown**

# What are gravitational waves and how are they generated?

## eXtreme Gravity:

where gravity is  
(a) non-linear *and*  
(b) dynamical

## Gravitational Waves (GWs):

Wave-like perturbation  
of the gravitational field.

## Generation of GWs:

Accelerating masses  
(t-variation in multipoles)

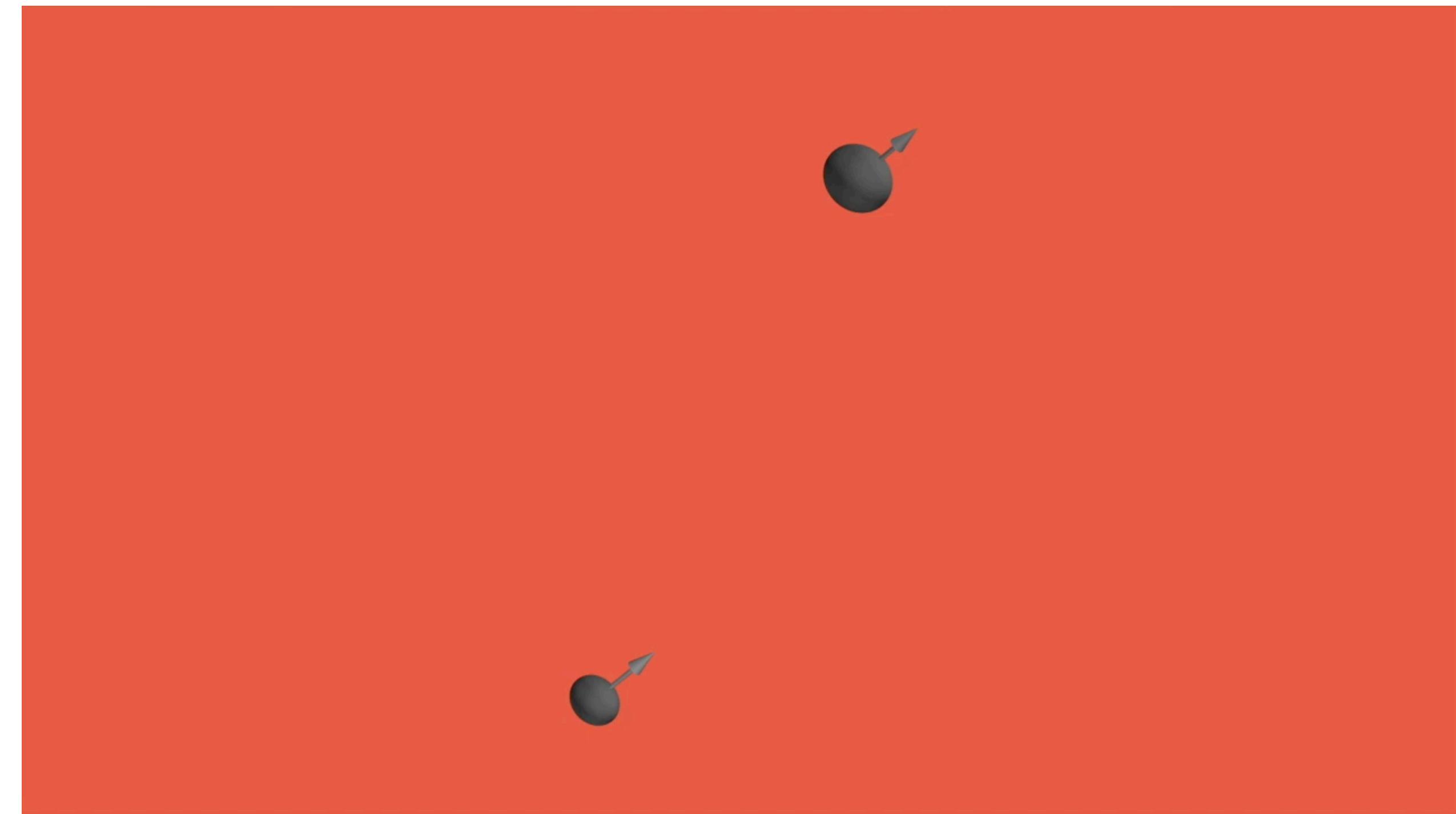
## Propagation of GWs:

Light speed, weakly  
interacting,  $1/R$  decay.

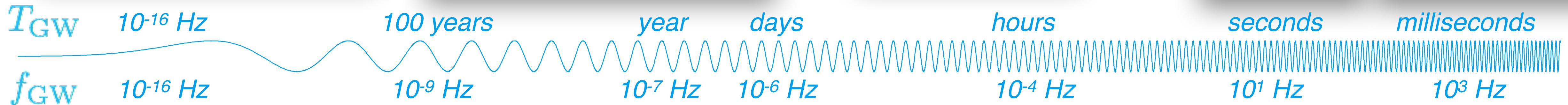
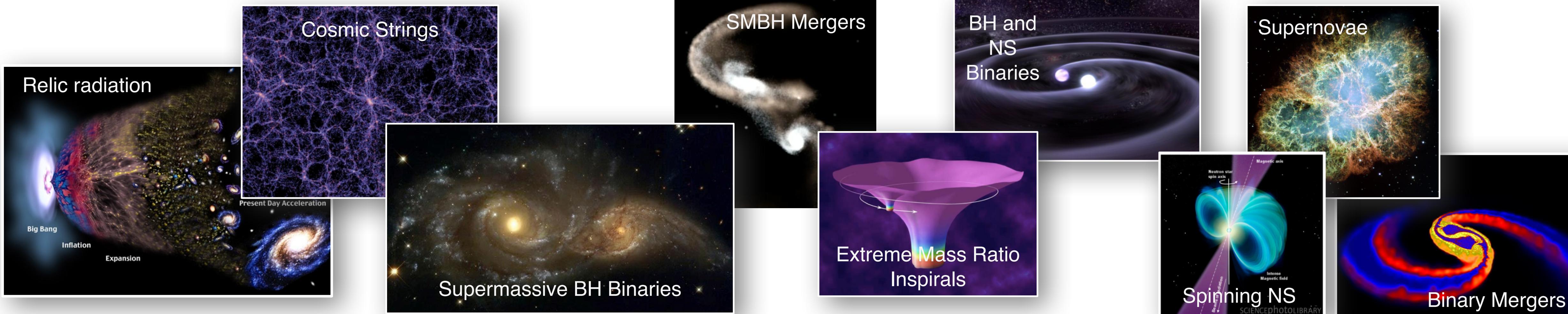
## GW Spectrum:

Kepler 3rd Law!

$$\frac{f}{2\pi} = \sqrt{\frac{G m_{\text{tot}}}{r_{12}^3}} = \sqrt{\frac{c^6}{8G^2 m_{\text{tot}}^2}} \sim \frac{1}{m_{\text{tot}}}$$



# What are the sources of gravitational waves?



# How do you extract information from gravitational waves?

Modelling

Data Analysis

1. C

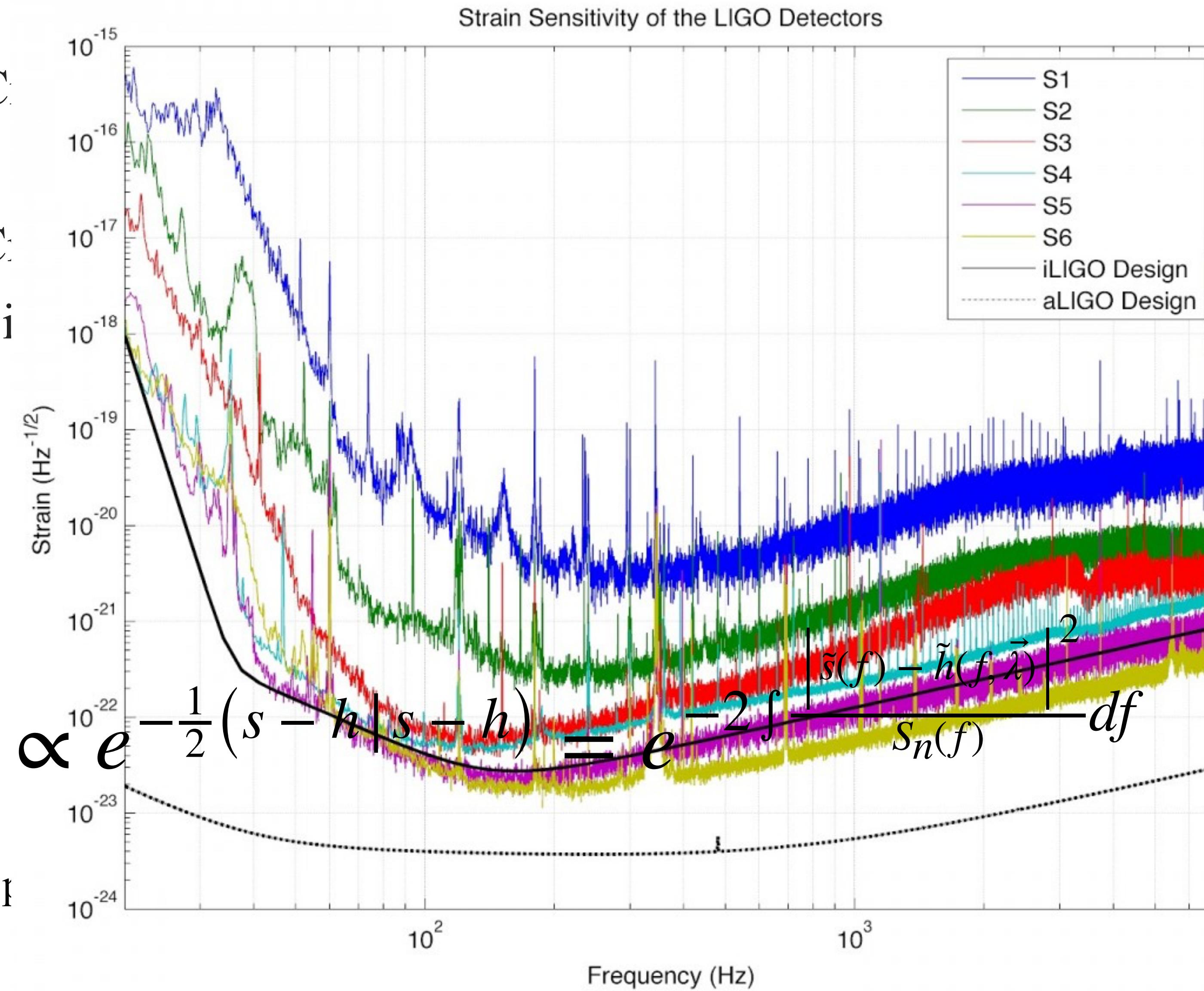
2. C

3. Fi

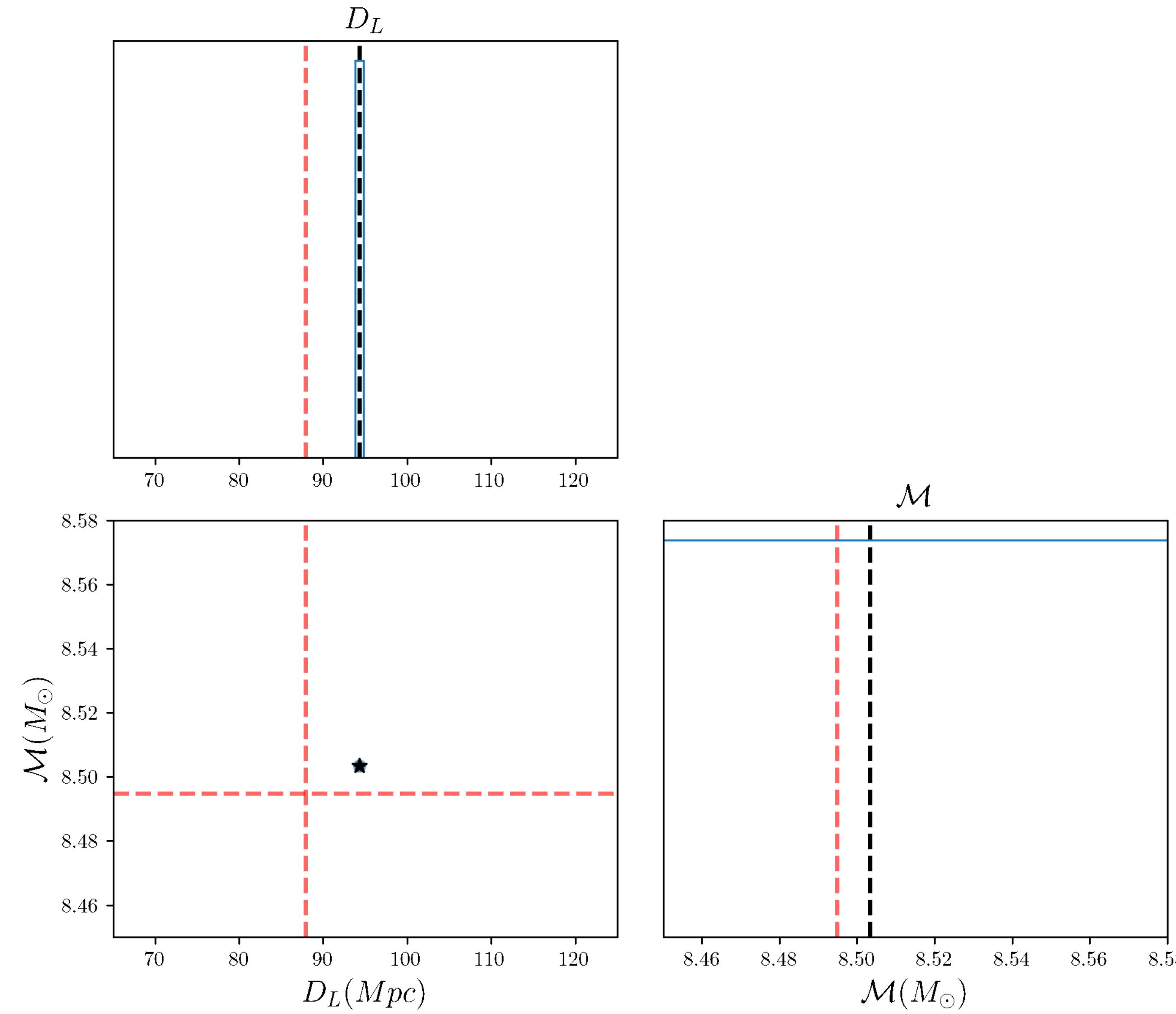
Likelihood function

$$\mathcal{L} \propto e^{-\frac{1}{2}(s - h | s - h)} = e^{-\frac{1}{2} \int \frac{|\tilde{s}(f) - \tilde{h}(f, \vec{\lambda})|^2}{S_n(f)} df}$$

inner  $\vec{\lambda}$

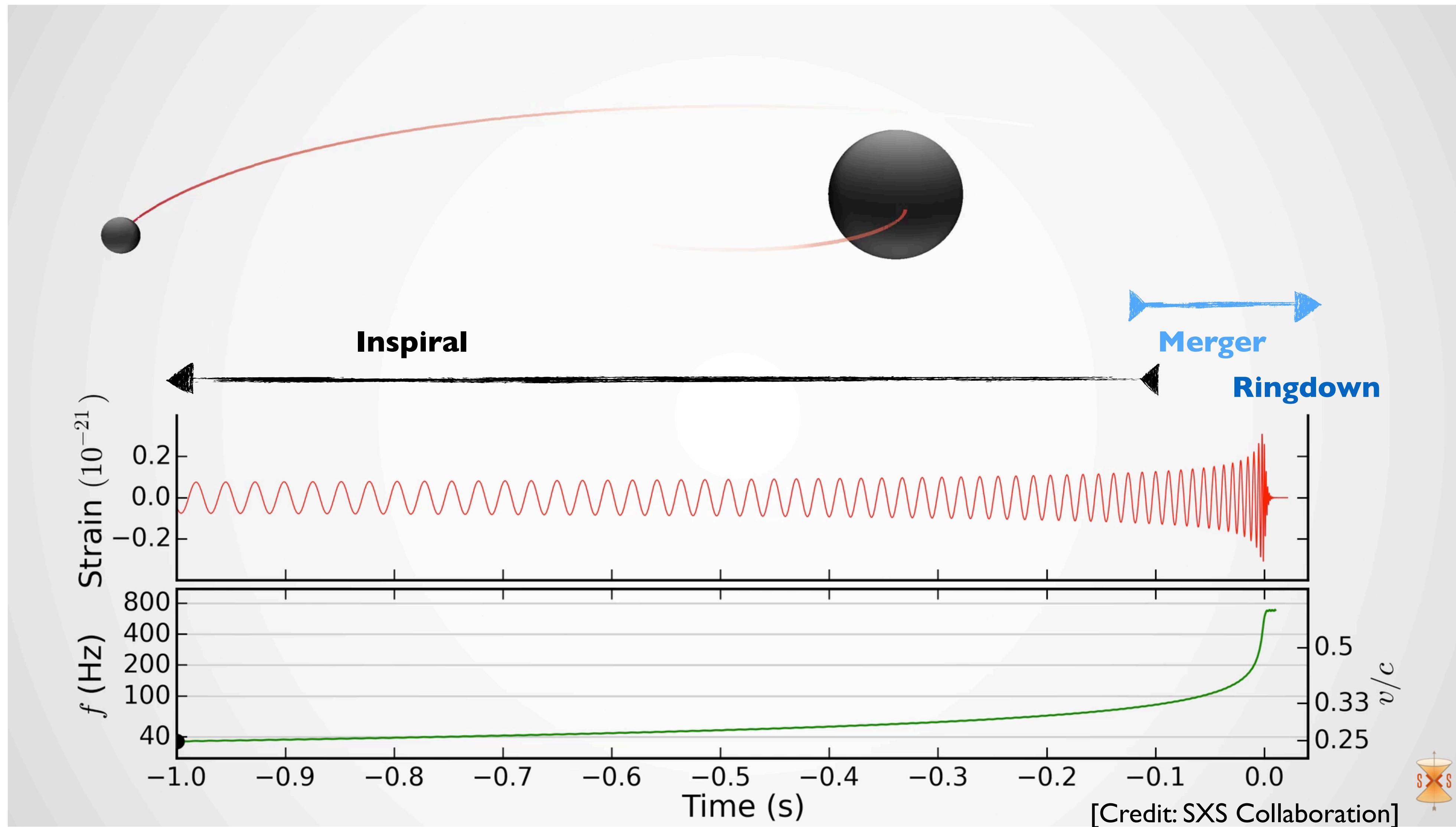


# Searching for needles in a haystack...



[Credit: Rohit Chandramouli]

# The model used in matched filtering is crucial



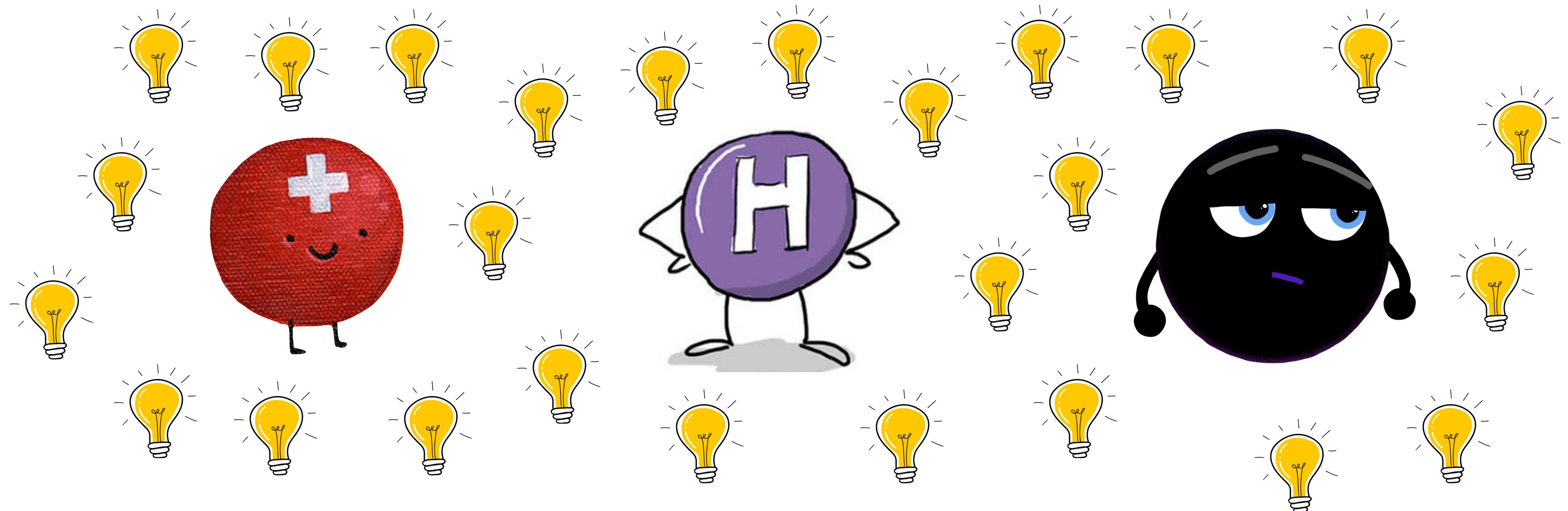
**ABC of GWs**

Frodo and Sam

**Probing  
Fundamental  
Physics**

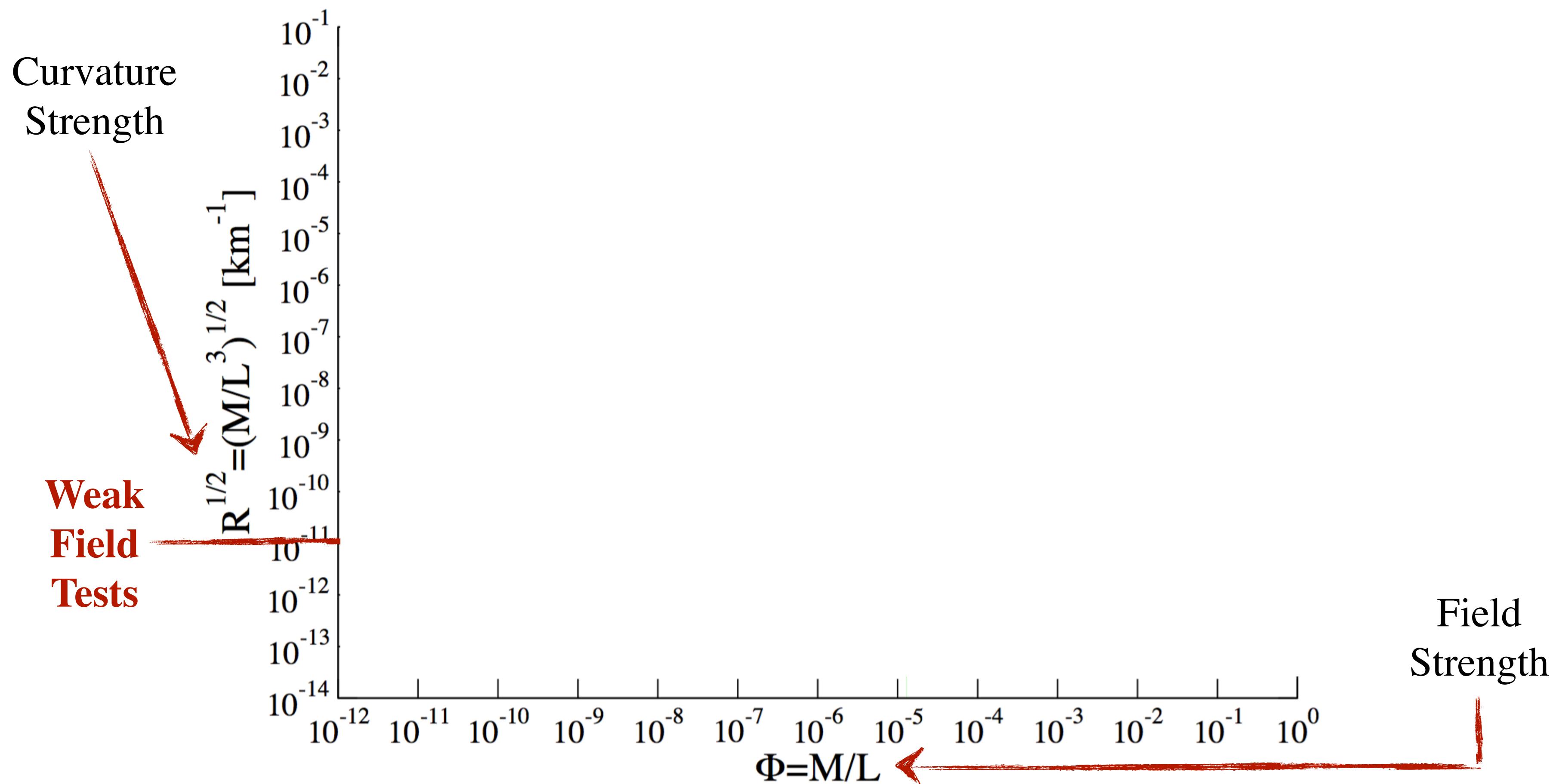
**Into the  
Unknown**

# What is fundamental physics?



For this talk: “fundamental physics” are deviations from general relativity  
that can be probed with gravitational waves

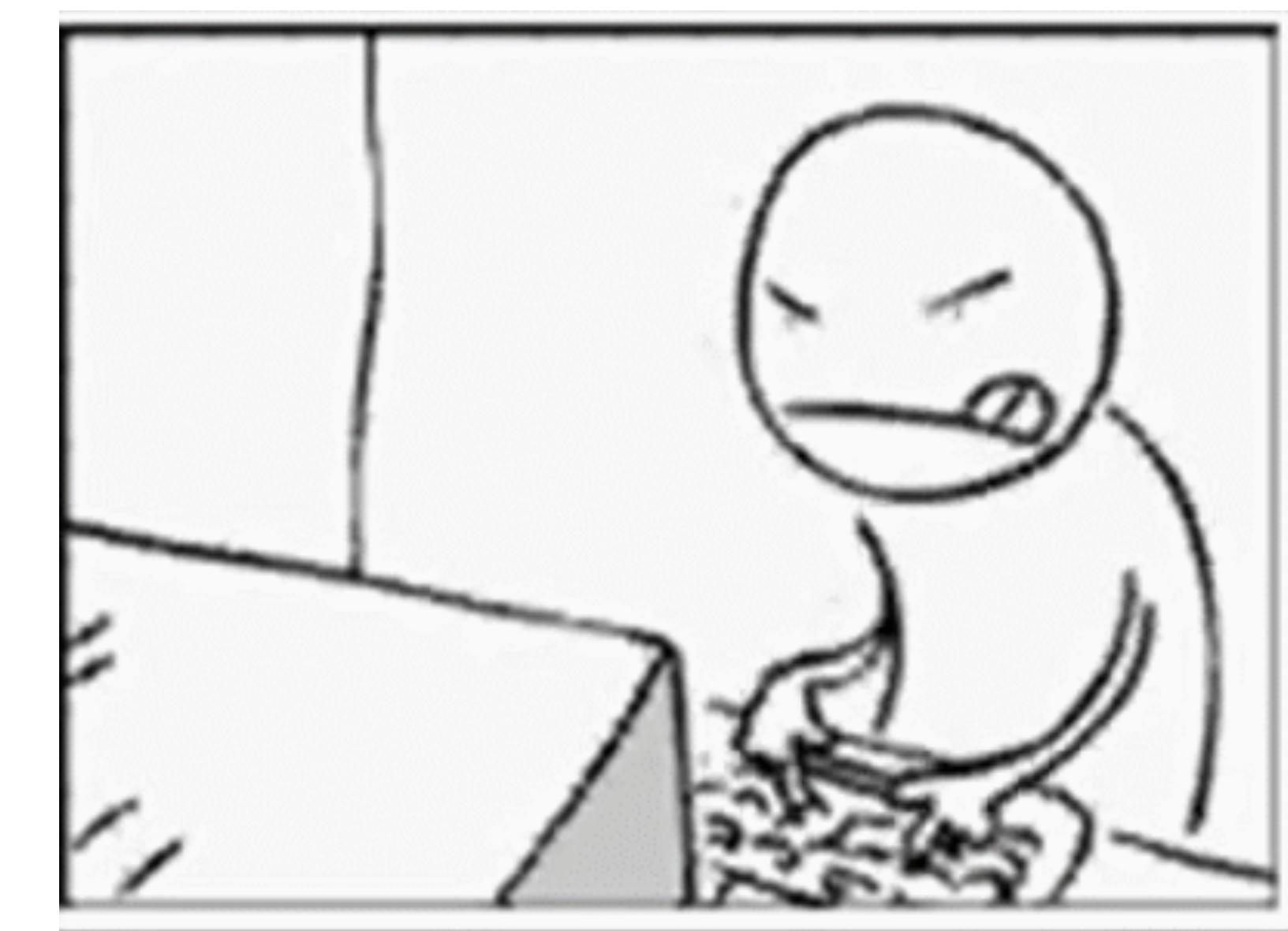
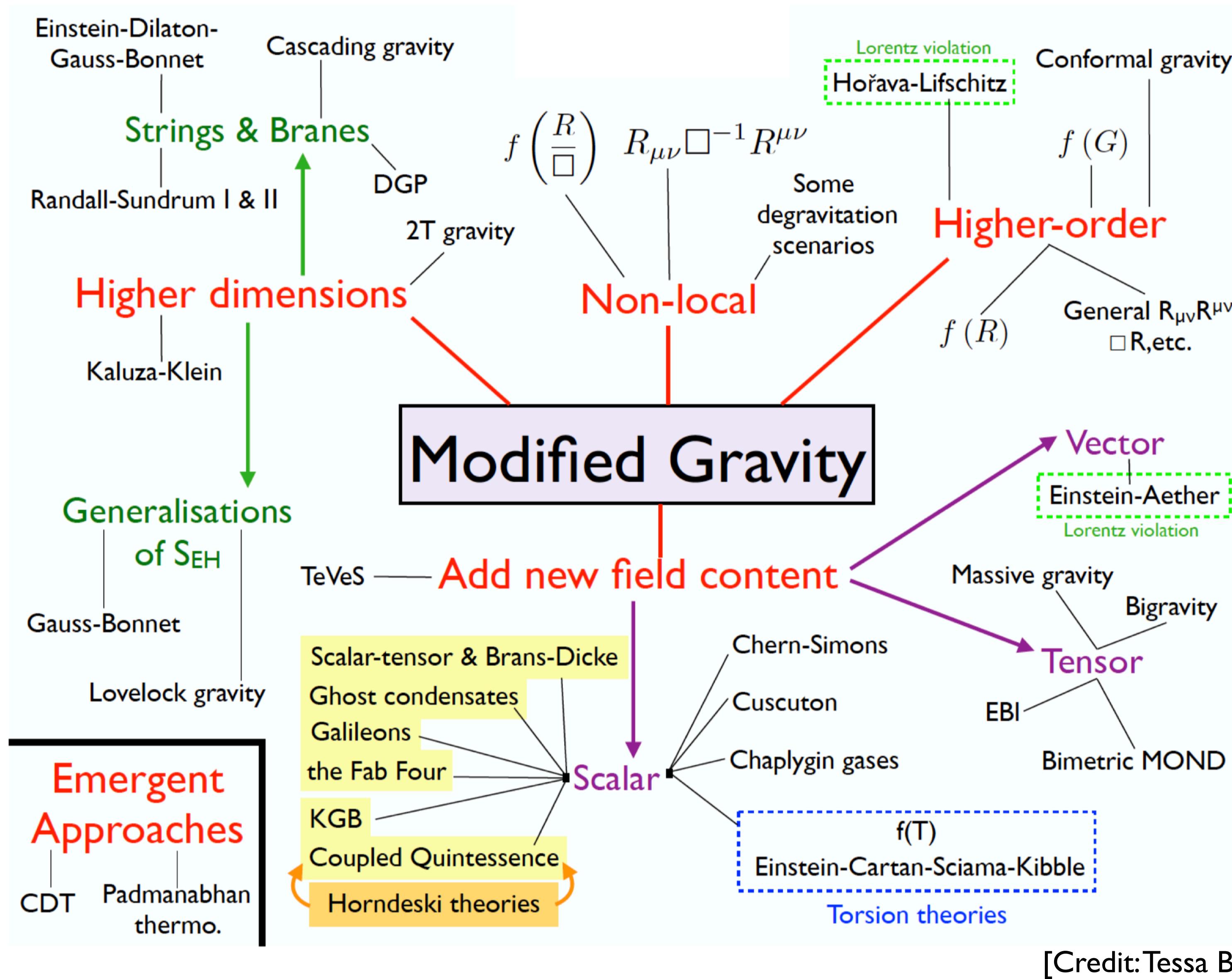
# Why probe “fundamental physics” when gravity waves?



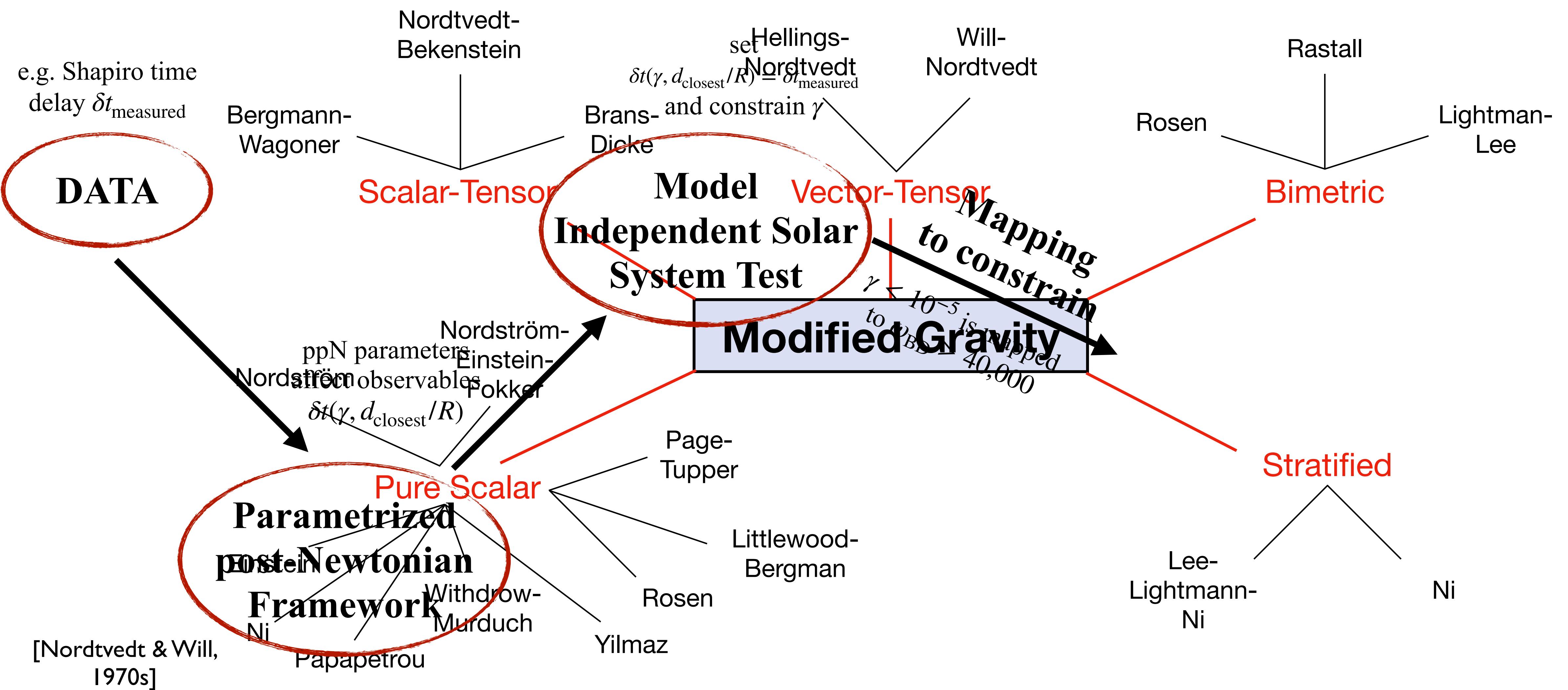
GWs probe eXtreme Gravity

[Will, Liv. Rev., 2005, Psaltis, Liv. Rev., 2008, Baker, et al, Siemens & Yunes, Liv. Rev. 2013, Yunes, et al PRD 2016]

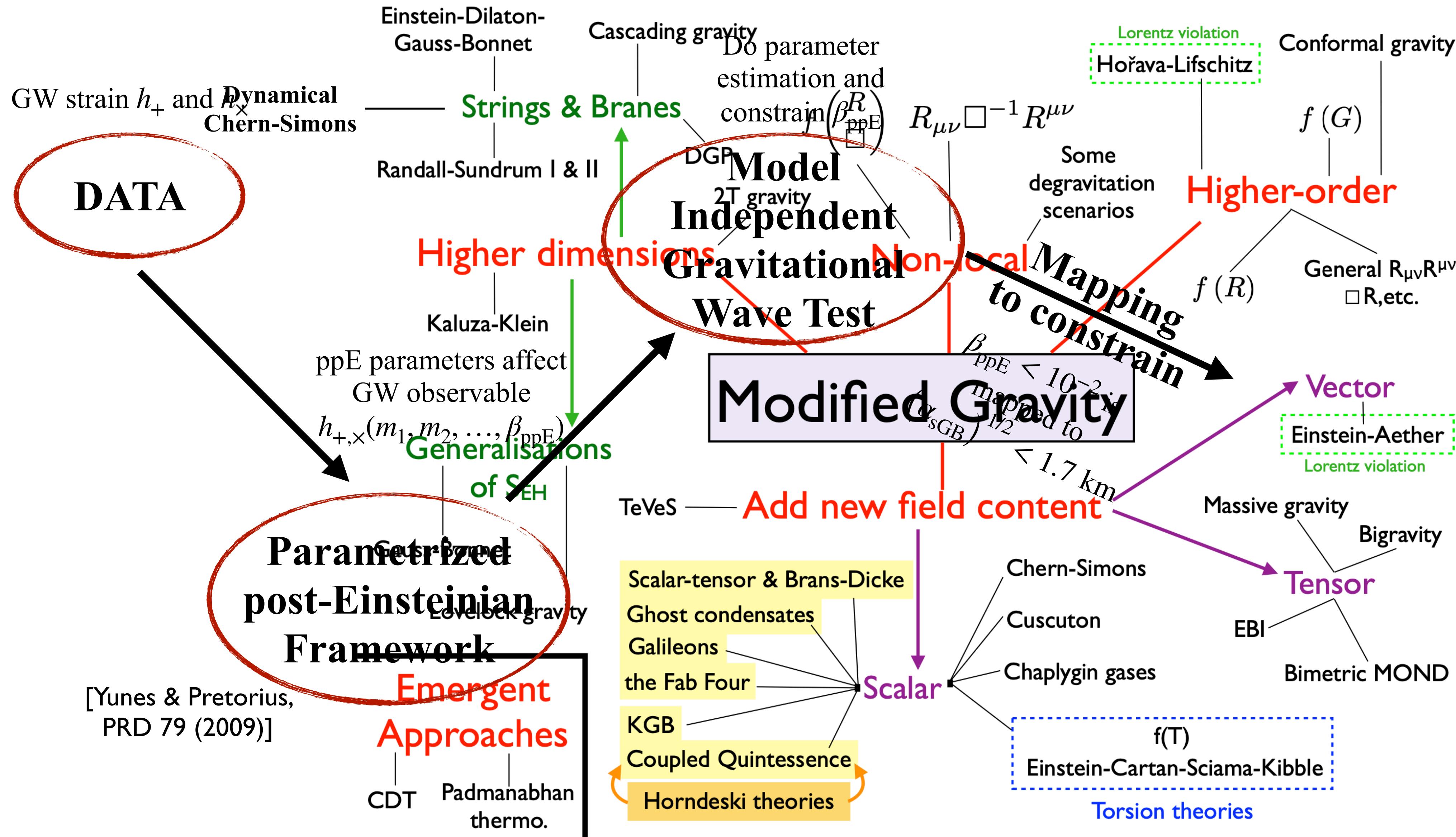
# How do we probe the modified gravity bestiary?



# A page from the past



# Taming the bestiary



# Effectively deforming away from general relativity

Principle of Equivalence	massless spin-2 field	Lorentz Invariance	Parity Invariance	Diffeomorphism Invariance	Dispersionless Propagation	...
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**One example:**  $S = \int \sqrt{-g} \kappa R$

Test properties of General Relativity by constructing theories that violate its pillars

Dynamical Chern-Simons

Scalar-tensor theories

Horava gravity

Einstein-dilaton-Gauss-Bonnet

Einstein-AEther theory

Massive gravity

[Yunes & Pretorius, PRD 80 ('09)]

[Endlich, Gorbenko, Huang, Senatore, JHEP 09 ('17)]

[Yunes & Siemens, Liv. Rev. in Rel ('13)]

...

# Calculate ppE observable through deformations of GR

I. Parametrically deform the Hamiltonian.

$$H = H_{\text{GR}} + \delta H \quad \delta H = \alpha_H v^{a_H}$$

II. Parametrically deform the RR force.

$$\vec{F}_{\text{RR}} = \vec{F}_{\text{RR,GR}} + \delta \vec{F}_{\text{RR}} \quad \delta \vec{F}_{\text{RR}} = \vec{\alpha}_{RR} v^{a_{RR}}$$

III. Deform waveform generation.

$$h = F_+ h_+ + F_\times h_\times + F_s h_s + \dots$$

IV. Parametrically deform g propagation.

$$E_g^2 = p_g^2 c^4 + \tilde{\alpha} p_g^{\tilde{a}}$$

Result: To leading PN order and leading GR deformation

$$\tilde{h}(f) = \tilde{h}_{GR}(f) (1 + \alpha f^a) e^{i\beta f^b}$$

[Yunes & Pretorius, PRD 80 ('09)  
Mirshekari, Yunes & Will, PRD 85 ('12)  
Chatzilioannou, Yunes & Cornish, PRD 86 ('12)]

## Parameterized post-Einsteinian Framework

# Parameterized post-Einsteinian theory

$$\tilde{h}(f) = \tilde{h}_{GR}(f) (1 + \alpha f^a) e^{i\beta f^b}$$

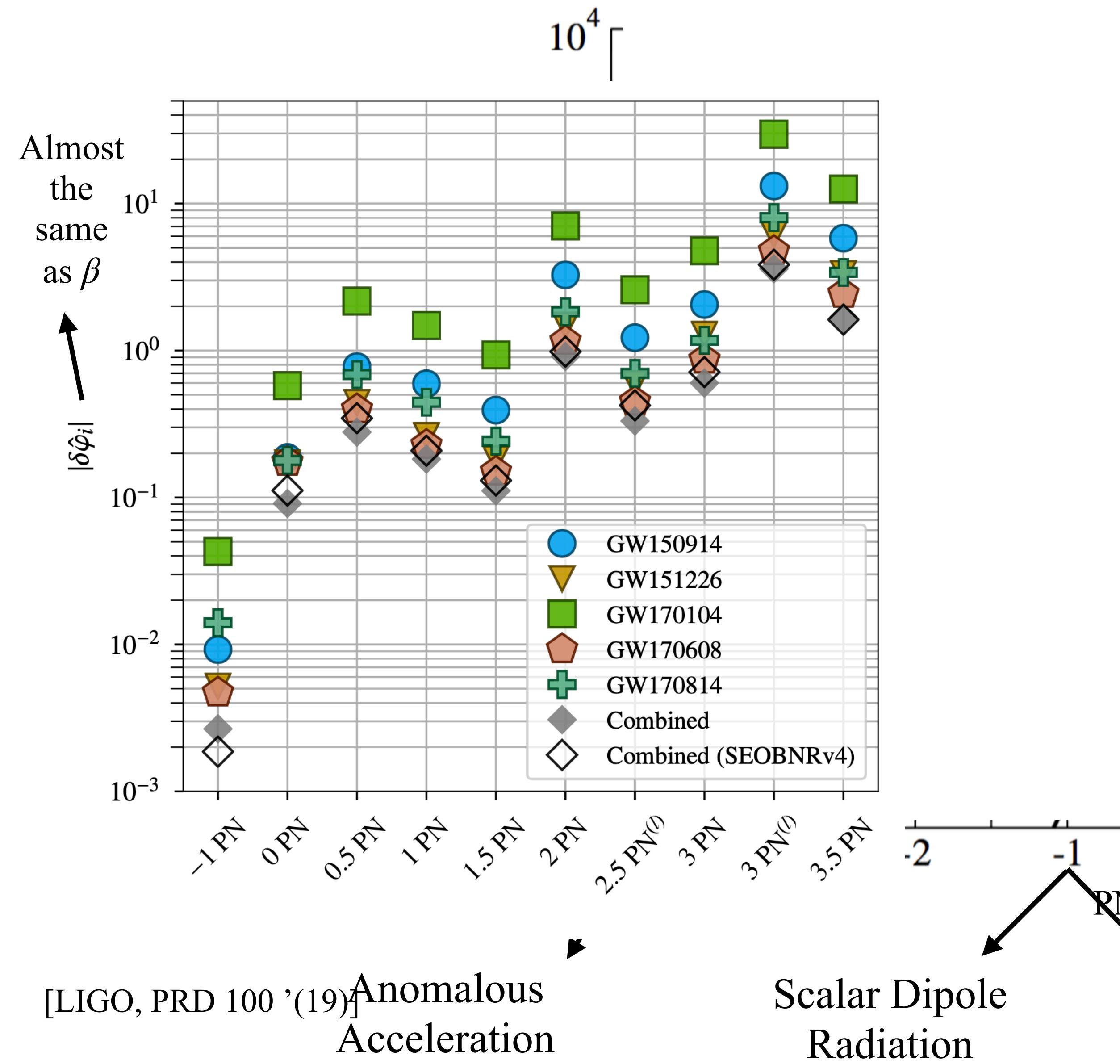
[Yunes & Pretorius, PRD 80 ('09)]

Theoretical Effect	Theoretical Mechanism	Theories	ppE $b$	Order	Mapping
Scalar Dipolar Radiation	Scalar Monopole Field Activation BH Hair Growth	EdGB [140, 142, 149, 150] Scalar-Tensor Theories [59, 151]	-7 -7	-1PN -1PN	$\beta_{\text{EdGB}}$ [140] $\beta_{\text{ST}}$ [59, 151]
Anomalous Acceleration	Extra Dimension Mass Leakage Time-Variation of $G$	RS-II Braneworld [152, 153] Phenomenological [137, 154]	-13 -13	-4PN -4PN	$\beta_{\text{ED}}$ [141] $\beta_{\dot{G}}$ [137]
Scalar Quadrupolar Radiation Scalar Dipole Force Quadrupole Moment Deformation	Scalar Dipole Field Activation due to Gravitational Parity Violation	dCS [140, 155]	-1	+2PN	$\beta_{\text{dCS}}$ [146]
Scalar/Vector Dipolar Radiation Modified Quadrupolar Radiation	Vector Field Activation due to Lorentz Violation	EA [109, 110], Khronometric [111, 112]	-7 -5	-1PN 0PN	$\beta_{\mathcal{A}}^{(-1)}$ [113] $\beta_{\mathcal{A}}^{(0)}$ [113]
Modified Dispersion Relation	GW Propagation/Kinematics	Massive Gravity [156–159] Double Special Relativity [160–163] Extra Dim. [164], Horava-Lifshitz [165–167], gravitational SME ( $d = 4$ ) [179] gravitational SME ( $d = 5$ ) [179] gravitational SME ( $d = 6$ ) [179] Multifractional Spacetime [168–170]	-3 +6 +9 +3 +6 +9 3–6	+1PN +5.5PN +7PN +4PN +5.5PN +7PN 4–5.5PN	$\beta_{\text{MDR}}$ [145, 156]

Mapping between  
ppE parameters  
( $\beta, b$ ) to specific  
modified theories

[Cornish et al PRD 84 ('11), Gair & Yunes PRD 84 ('11), Chatzioannou et al PRD 86 ('12), Sampson et al PRD 87 ('13), Sampson, et al PRD 88 ('13), Sampson et al PRD 89 ('14), Huwyler et al PRD 91 ('14), Yunes, Yagi & Pretorius PRD 94 ('16), Tahura & Yagi PRD 98 ('16), Quiao et al PRD 100 ('19), Zhang et al PRD 100 ('19), Moore & Yunes CQG 37 ('20), Bonilla, Kumar & Teukolsky ('22), Mezzasoma & Yunes PRD ('22), ...]

# ppE constraints with gravitational waves



[LIGO, PRD 100 '(19)] Anomalous Acceleration

Scalar Dipole Radiation

$$\tilde{h}(f) = \tilde{h}_{\text{GR}}(f) e^{i\beta f^b}$$

RN order (related to b)

Lorentz Violation

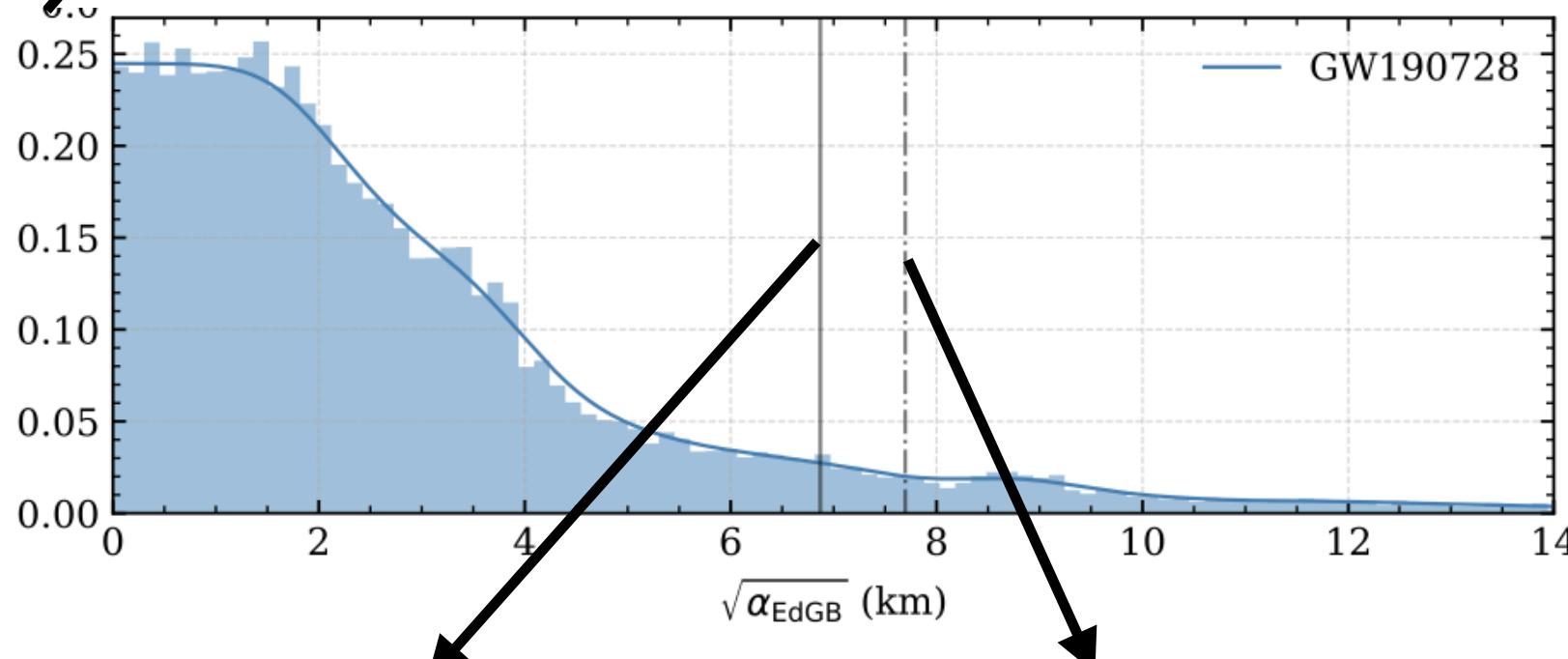
Parity Violation

[Yunes, Yagi, Pretorius, PRD 94 '(16), Editor's suggestion]

# Mapping ppE constraints to specific theories

Marginalized posterior distribution of

$$\sqrt{\alpha_{\text{EdGB}}}$$



90% confidence limit

Max  $\sqrt{\alpha_{\text{EdGB}}}$  for validity of small coupling approximation

First constraints on quadratic gravity with gravitational waves!

$$\sqrt{\alpha_{\text{EdGB}}} \leq 1.7 \text{ km}$$

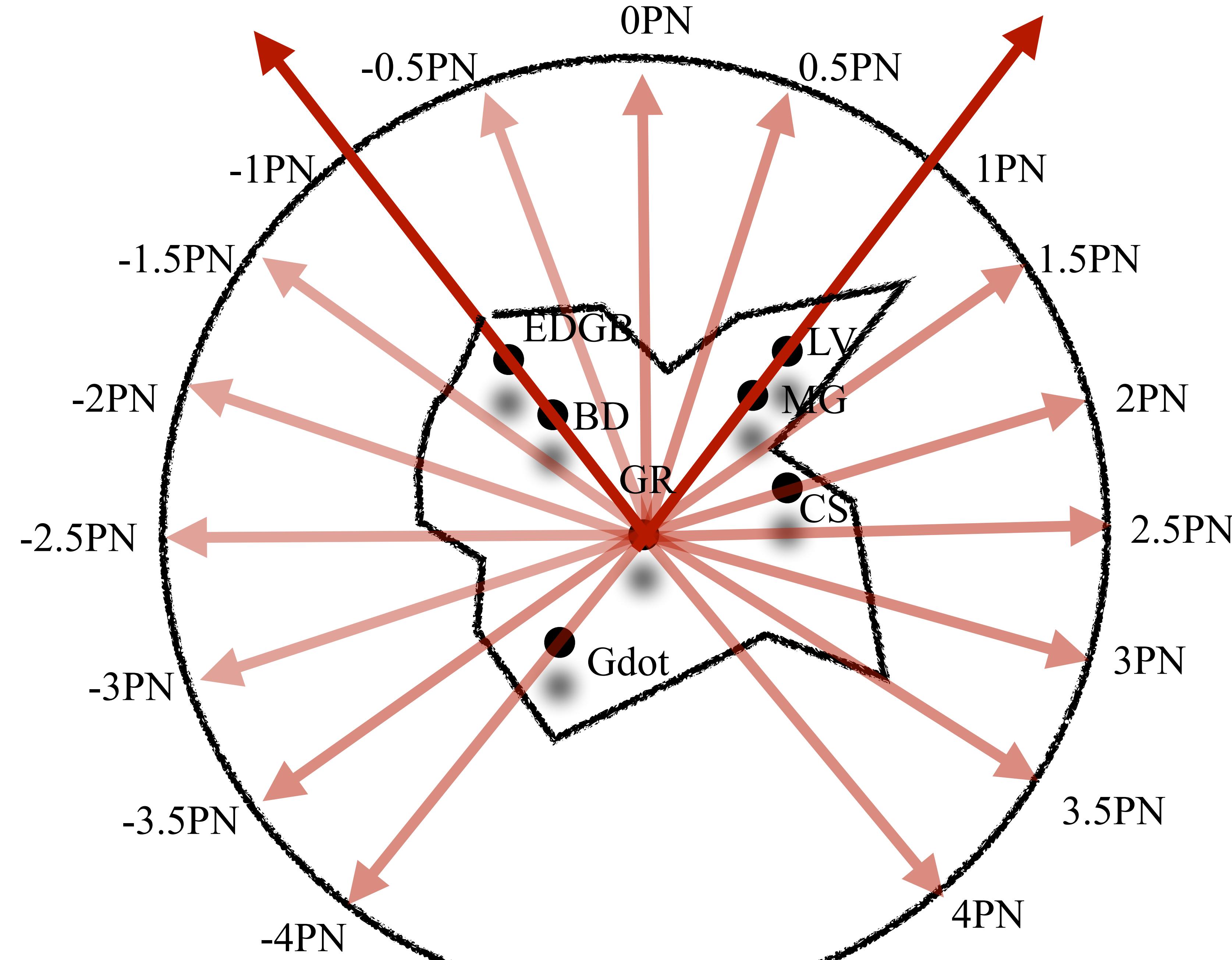
[Nair, Perkins, Silva & Yunes,  
*Phys.Rev.Lett.* 123 (2019) 19, 191101,  
Perkins, Nair, Silva & Yunes,  
*Phys.Rev.D* 104 (2021) 2, 024060,  
Lyu, et al, *Phys.Rev.D* 105 (2022)]

**ABC of GWs**

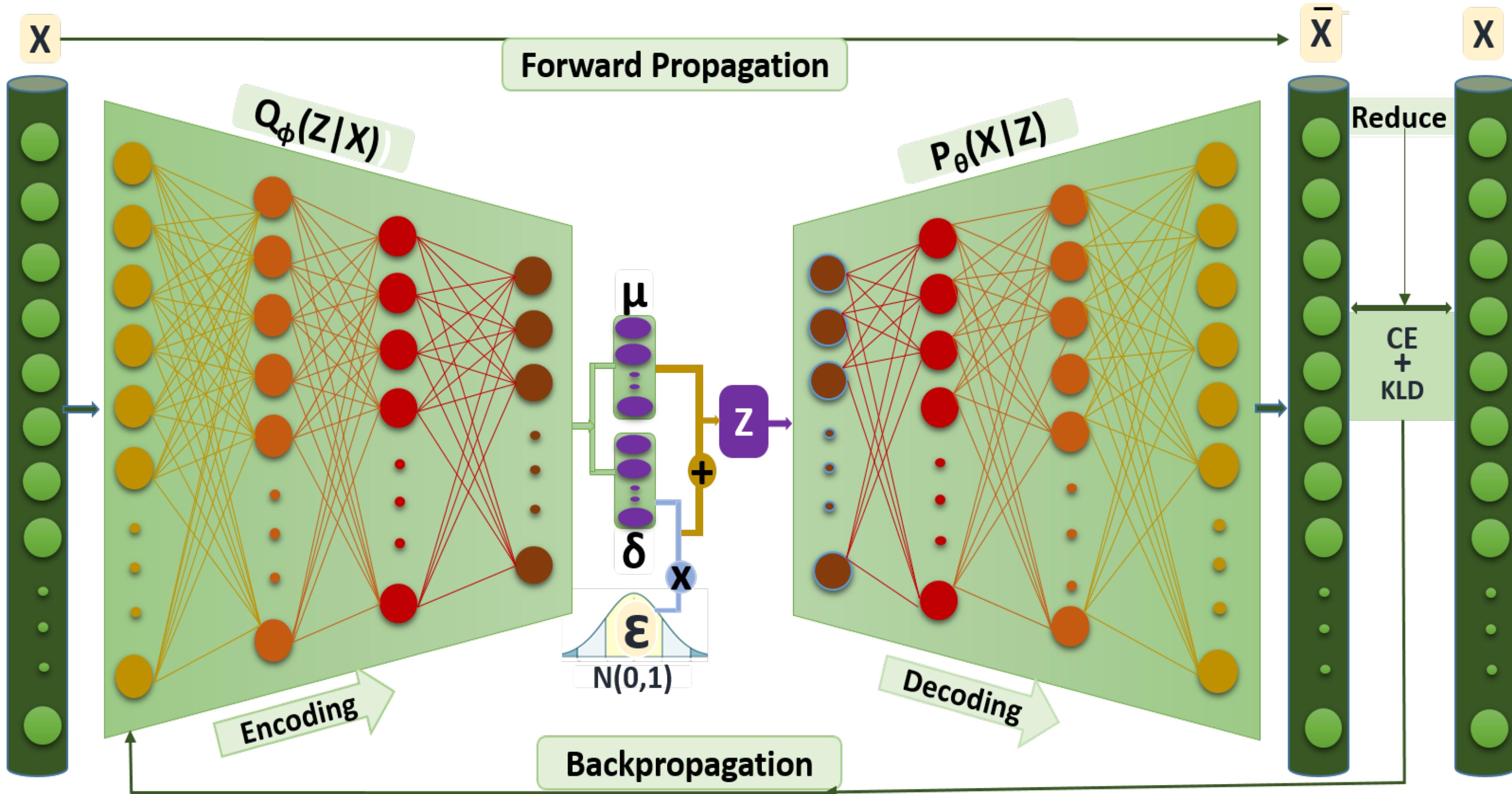
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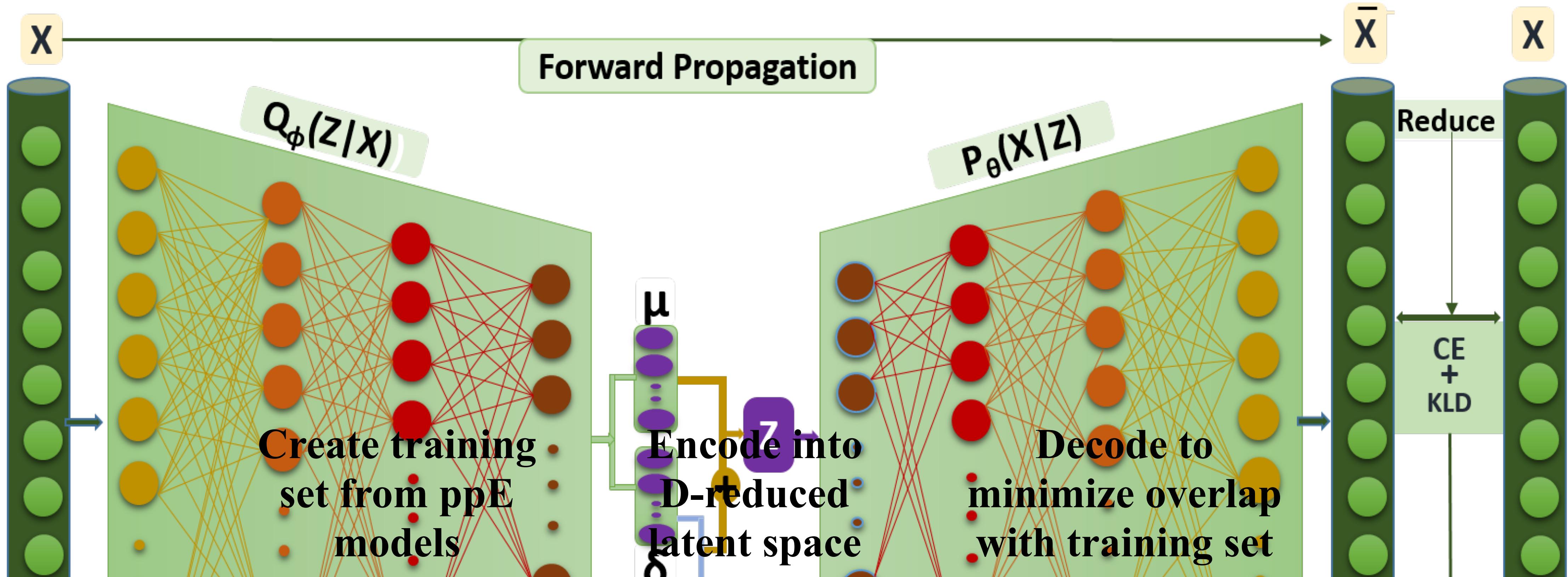
# Understanding $p_E$



# Beyond ppE tests of general relativity



# Neural post-Einsteinian (NPE) framework

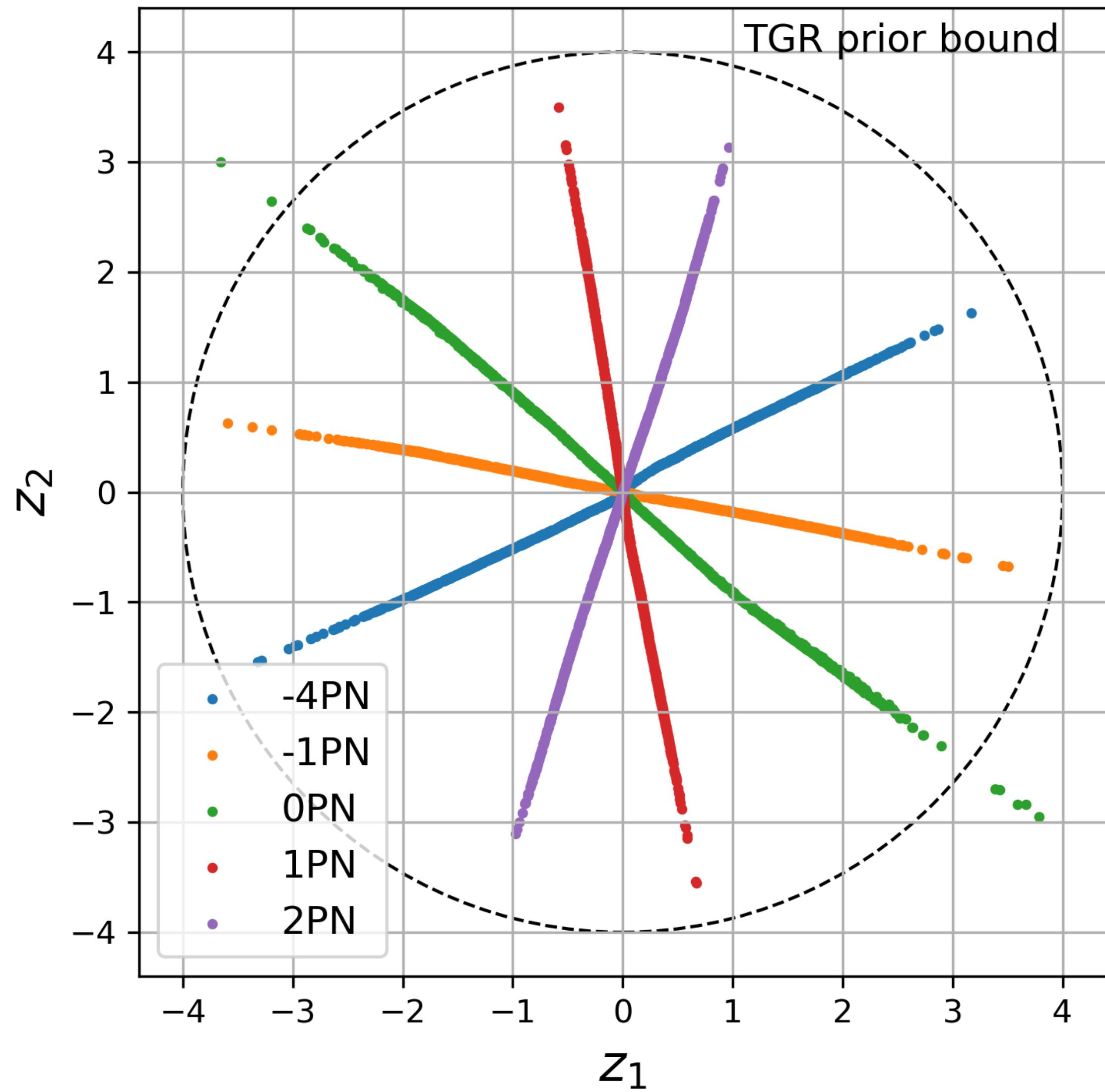


VAE-ppE should be able to:

- (i) detect (leading-PN order) ppE deviations efficiently,
- (ii) detect untrained higher-PN order deviations,
- (iii) detect untrained non-polynomial deviations.

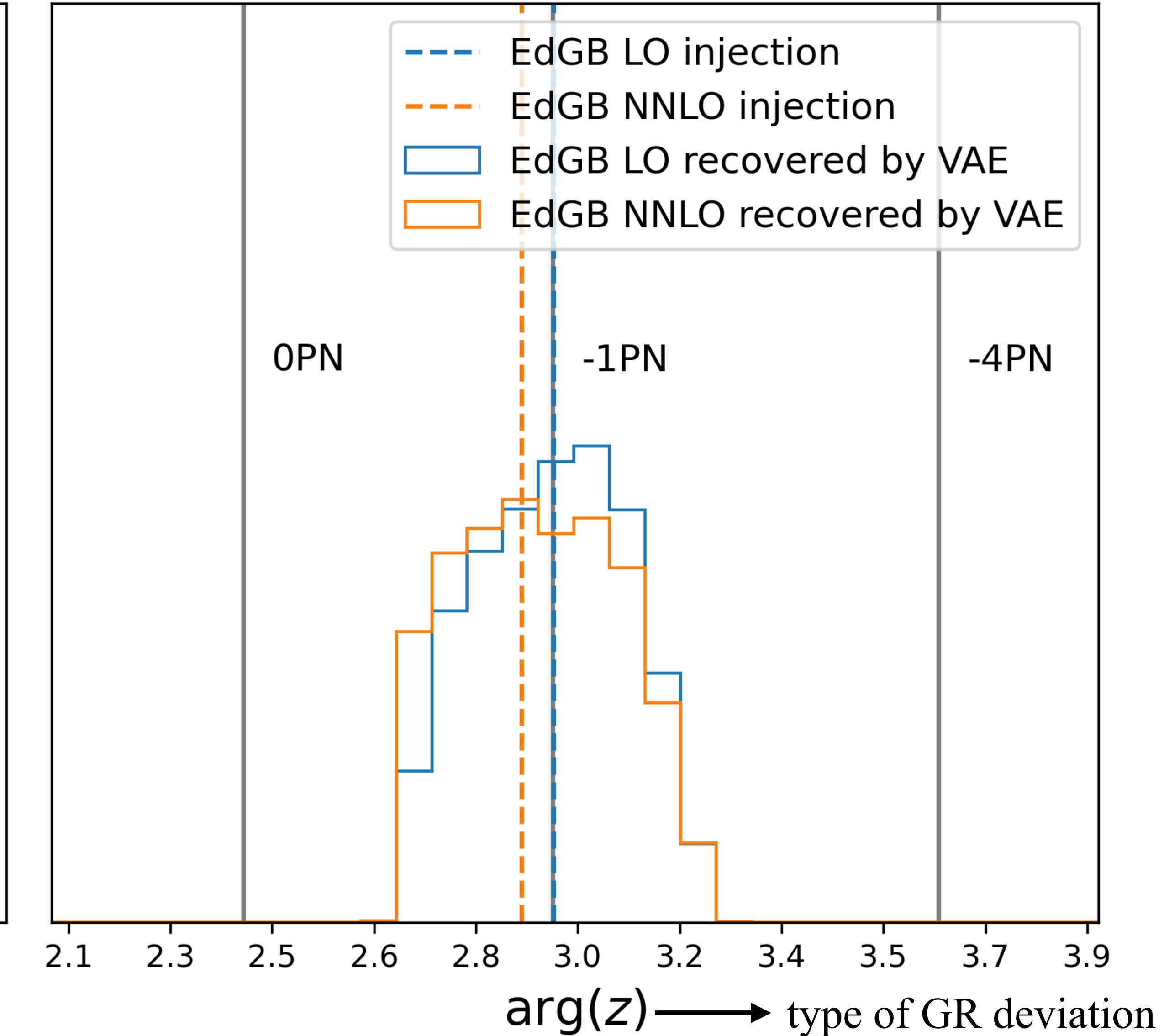
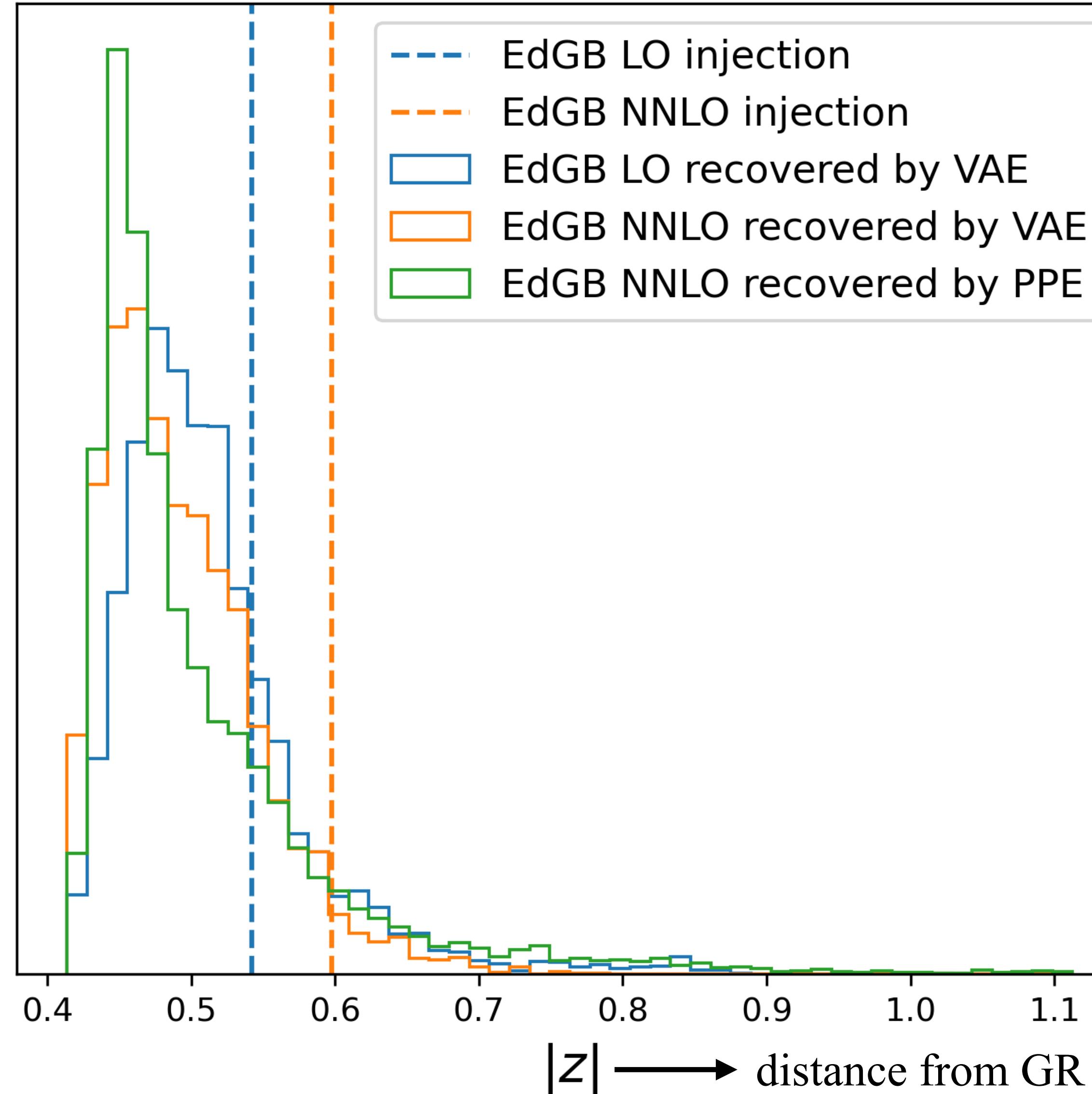
[Xi, Narayan & Yunes, in prep]

# NPE in action



[Xi, Narayan & Yunes, in prep]

# Bayesian Parameter Estimation with NPE



# Summary and Outlook

**Gravitational waves are beginning to place strong constraints on  
“fundamental” physics in extreme gravity**

