ICEPP, The University of Tokyo Koji Terashi

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ExU Public Online Colloquium October 16, 2024

Quantum Algorithm and Qubit Technology Applications for Particle Physics

Particle physics aims to answer:

- ‣ What is the origin and future of the Universe?
- ‣ What is the nature of elementary particles?
- ‣ How do they interact?

Why is the Universe like the one we see now?

How Answer to the Questions?

High-energy accelerator can directly probe fundamental constituents in nature by colliding particles

Accelerator physics can probe the epoch of the birth of the Universe

Why is the Universe like the one we see now?

How Answer to the Questions?

The cosmic microwave background

Temperature anisotropies

?

Cooled down by expansion

Universe becomes visible at 3×10^5 years

Soup of elementary particles at very high temperature and density

Fundamental physics to understand properties/ dynamics of elementary particles and nuclear matters \triangleright Governed by $U(1) \times SU(2) \times SU(3)$ gauge theory

Particle Physics and Quantum

- **Quantum Field Theory (QFT)** at cores in particle
- Quantum mechanics as a foundation of QFT
	- Quantum computer may offer a unique opportunity to probe phenomena governed by particle physics

- ‣How did the known phenomena (e.g, Higgs condensation, quark confnement) occur in early Universe?
- ‣Can we exploit quantum resources to reach beyond conventional experimental techniques?

Particle Physics and Quantum

How did the Universe become the one we see now?

Quantum technology might be able to address the questions:

Highlight a few selected results on:

- learning quantum states/processes
- ‣ simulating quantum dynamics in Lattice Gauge Theory
- ‣ searching for dark matter with superconducting qubits

Present our recent studies at ICEPP that utilize quantum resources for

\rightarrow Quantum Machine Learning

\rightarrow Quantum Simulation

the application to particle physics

Quantum Sensing

- \blacktriangleright Given a dataset $D = \{(x_i, y_i)\}_{i=1}^N$ (x_i = Classical or Quantum) $\sum_{i=1}^N$ (x_i)
- \triangleright Consider a hypothesis h_{θ} which predicts the true label y_i from input x_i in D ► Define Loss function $L(y_i, h_{\theta}(x_i))$ to quantify the difference between the label y_i
- and prediction *hθ*
-

► Minimize the training error
$$
\hat{R}_S(\theta) = \frac{1}{N} \sum_{i=1}^N L(y_i, h_{\theta}(x_i))
$$
 over input data in *D*

Machine Learning of Quantum States

State preparation and optimization as key processes for learning task

- ‣ Suitable for near-term quantum devices
- ‣ Applicable to a wide range of problems in quantum simulation (e.g, VQE),

 \blacktriangleright Prepare an input state $|\psi_{\rm in}\rangle = U(x)|\psi_0\rangle$ for classical or $|\psi_{\rm in}\rangle = |\psi_q\rangle$ for quantum \blacktriangleright Apply a parameterized unitary $U(\theta)$ to generate $|\psi(\theta)\rangle = U(\theta) |\psi_{\rm in}\rangle$ **•** Prepare the desired state by optimizing the parameter θ with classical computer \blacktriangleright Calculate, e.g, expectation value of observable O with optimized parameter $\boldsymbol{\theta}^*$

Variational State Preparation and Optimization

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-
-
-

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Learning classical data *x*

 $|0\rangle$

E.g, digitized detector signals

Quantum Neural Networks

Classifcation, Regression

Quantum Machine Learning

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Learning HEP Data with QML

- ‣ Early attempt of QML looks encouraging with small system and dataset sizes
- discussed later)

Simulator results Classify new physics events from background with classical detector information KT et al., [Comput. Softw. Big Sci. 5, 2 \(2021\)](https://doi.org/10.1007/s41781-020-00047-7)

‣ Limited scalability to large-size problem (due to infamous Barren Plateau problem

Learning Quantum Data

-
- (e.g, Hamiltonian parameters)
- E.g, quantum state from another quantum system

Directly learn quantum states without classical measurement, e.g, to ‣ Extract entanglement properties of a quantum system ‣ Determine classical parameters that control a physical system

L. Nagano, KT et al., [Phys. Rev. Res. 5, 043250 \(2023\)](https://doi.org/10.1103/PhysRevResearch.5.043250)

Quantum Convolutional Neural Networks

Learning Quantum Data

(1 + 1)*d U***(1) Gauge Theory (Schwinger Model)**

$$
H = J \sum_{j=0}^{N_s - 2} \left(\sum_{k=0}^{j} \frac{Z_k + (-1)^k \left(\frac{\theta}{2} \right)^2}{2} + \frac{\omega}{2\pi} \sum_{j=0}^{N_s - 2} (X_j X_{j+1}) \right)
$$

- ‣ Non-trivial properties such as chiral condensate, though the model is simple
- \triangleright Phase transition at $\theta = \pi$, $m/g = m_c/g \approx 0.33$ due to topological θ -term

- Physical parameters: $N = N_s = 8$, $ag = 2$, $\theta = \pi$
- \triangleright Generate ground states $|\psi_{\text{GS}}(m)\rangle$ using VQE within parameter range of $m/g \in [-2,2]$
- ‣ Phase recognition as a classifcation with label:

Quantum data generation and classifcation

$$
y_m = \begin{cases} +1 & (m > m_c) \\ -1 & (m < m_c) \end{cases}
$$

QML to Quantum Data (I)

$$
\frac{1}{N} \sum_{i=1}^{N} L(y_i, h_{\theta}(x_i))
$$

: $R(\theta) = \mathbb{E}_{(x,y)\sim P} [L(y, h_{\theta}(x))]$

Finding a hypothesis h_{θ} that minimizes the prediction error is a goal of machine learning

Assuming that the data (x, y) has a underlying distribution P , and a dataset

Revisiting Machine Learning

 $D = \{(x_i, y_i)\}_{i=1}^N$ is created by sampling the distribution P : $\sum\limits_{i=1}^N$ is created by sampling the distribution P

Training Error from $D : \hat{R}_S(\theta) =$

Prediction Error (for unseen data)

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ML model class $F = \{h : x_i \to y_i\}$ *h** : True map *h* \widetilde{h} : Selected Model *^N* γ

 h \widetilde{h} $N \approx h^*$

Likely that the problems considered so far were simple enough, so that the true map could easily fall inside the model class :

h^{*}: True map that faithfully outputs the true label *y* from an input *x*

A given ML architecture would enable certain class of models (model class)

True map may not necessarily reside in a given model class for more complex problems

Best model within the model class may be obtained when input distribution *P* is directly used in the training

However, input distribution P is usually unknown

True map may not necessarily reside in a given model class for more complex problems

 $R(h^*) - R(h_F) =$ Model Error $R(h_F) - R(\hat{h}_N) =$ Estimation Error ̂ $R(h_N) - R(h_N) =$ Optimization Error ̂ \widetilde{h} *^N*) =

- Best *trained* model is likely diferent from the best model because the fnite dataset *D* is used instead of *P*
- Diferent sources contribute to errors:

True map may not necessarily reside in a given model class for more complex problems

Cost function $C(\theta) = Tr[OU(\theta)\rho U^{\dagger}(\theta)]$

with increasing system size (*Curse of dimensionality*)

Barren Plateau (BP) problem

J. R. McClean et al., [Nat. Commun. 9, 4812 \(2018\)](https://www.nature.com/articles/s41467-018-07090-4)

Concentration of cost function or vanishing gradient

Known that the training of parameterized quantum circuit generally becomes difficult

^Vθ∼uniform [*C*(*θ*) or

∂*C*(*θ*)

Optimization Errors

Insufficient training would be an important source of optimization errors

Examine how data-encoding unitary $U(x)$ can cause BP (when QNN part is assumed be BP-free)

Learning classical data requires the data to be encoded into quantum state

Barren Plateau from Data Encoding

ズム 量子機械学習 バレンプラトー (BP) U_COD y Corr Γ \mathbf{U} $\text{Var}_{\theta}[\partial_{\theta_{\nu}}\mathscr{L}(\theta)] \leq A_f \times r_{n,s} \times \int_{\mathbb{U}_x} dU \left[D_{HS}(\rho_{x}^{(h)}, \mathbb{I}/2^s) \right]$ Hilbert-Schmidt distance $dU_{\frac{1}{2}}^{i}D_{HS}(\rho_{x}^{(h)},\mathbb{I}/2^{s})$ \blacktriangleright Derived condition where the $\bigcup dU$ D_{HS} term does not decay exponentially (→ A necessary condition to avoid Barren Plateau) Provided a new upper bound on the variance of cost function gradient: \rightarrow A necessary condition to avoid Ba

Barren Plateau from Data Encoding

Too expressive circuit or too entangled states known to cause Barren Plateau Parameter initialization technique proposed as a way to avoid Barren Plateau angled sta μ proposed as a way to avoid \cup *p*Useu ds a way to avoid! \overline{a} \overline{a} \blacksquare **112** *i,* \mathbf{C} \blacksquare

Barren Plateau from Circuit Expressibility

Estimation Errors

Estimation Error $= R(h_F) - R(\hat{h}_N)$ quantifies the distance between the models ̂ that we can get with *D* and *P*

very general or specifc

Symmetry of the problem at hand is a useful guide to build efficient machine learning model

Model Error $= R(h^*) - R(h_F)$ typically hard to quantify unless the model is

the Model Error could be reduced

When a *priori* knowledge of the problem is accounted for in model building, Inductive Bias

Information of symmetry provides a useful resource in machine learning

- ‣ Symmetry ubiquitous in physics, e.g, Lorentz symmetry, Permutation symmetry, … ‣ Not obvious to incorporate general (continuous) symmetries in quantum setting
-
- Investigate a generic QNN architecture to efficiently encode rotational and permutational symmetries \triangleright Inner products as inputs (e.g, inner products of particle 4-vectors) → Weyl's theorem Z. Li, L. Nagano, KT, [Phys. Rev. Res. 6, 043028 \(2024\)](https://journals.aps.org/prresearch/abstract/10.1103/PhysRevResearch.6.043028)
	- ‣ Twirling method to make quantum gates invariant against input permutation

Equivariant Quantum Machine Learning

→ L. Schatzki et al., [npj Quantum Inf. 10, 12 \(2024\)](https://www.nature.com/articles/s41534-024-00804-1)

Particle decay

 O

rification as a honc $H \rightarrow ZZ \rightarrow 4$ -leptons classification as a benchmark • Hard to convolute but easy to take inner products.

-
- ► Lorentz symmetry in particle decay
► Ad-hoc non-linearity added after quantum measurement:

Fully symmetric circuit • Rotations handled by dot products **Equivariant Quantum Machine Learning**

Have demonstrated very efficient training without any indication of BP

$$
L(\theta, b) = \left[-|f_{Q}(\theta) - b| - y \right]
$$

2

 H

Fully symmetric circuit

- ‣ Rotations handled by inner products ‣ Permutations handled by twirling
-

Z. Li, L. Nagano, KT, [Phys. Rev. Res. 6, 043028 \(2024\)](https://journals.aps.org/prresearch/abstract/10.1103/PhysRevResearch.6.043028)

Argued that operator actions in BP-free quantum circuit are likely constrained in polynomially-large subspace, hence can classically simulated

Example:

Hamiltonian Variational Ansatz (HVA) for a given H expressed as $H = \sum a_i h_i$ If h_i is $\mathcal{O}(1)$ -local operator, the problem class of HVA can be classically simulated

Classical Simulability

M. Cerezo et al., [arXiv:2312.09121](https://arxiv.org/abs/2312.09121) Skepticism around variational QML approach … QML models with provable absence of Barren Plateau in literatures can be classically simulated(?)

Hamiltonian simulation as a useful computational resource with near-term QC Lattice gauge theory for calculating non-perturbative physics

Quantum Simulation

ation and α • discretize **spacetime Quantum Simulation**

\mathbf{L} which \mathbf{L} and method method • infamous sign problem \rightarrow $Z =$ Z $[d\phi]e^{-S[\phi]}$ Hamiltonian simulation \vec{a} s a useful computational resource with near-term QC Lattice gauge theory for calculating non-perturbative physics

‣ Discretize spacetime ‣ MC sampling for phase-space integrals of *e*−*^S*

• topological term • simulation **Conventional LGT simulation**

Infamous sign problem with

- non-zero density, temperature
- topological term, etc.

rce with nea $|\psi(t)\rangle = e^{-iHt}|\psi(0)\rangle$

• topological term • simulation

ation and α • discretize **spacetime Quantum Simulation**

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- still need exponential resource
- infinite Hilbert spaces for gauge dof's

‣ Discretize spacetime ‣ MC sampling for phase-space integrals of *e*−*^S*

Infamous sign problem with

- non-zero density, temperature
- topological term, etc.

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‣ Discretize spacetime ‣ MC sampling for phase-space integrals of *e*−*^S*

Simulation of real-time phenomena, e.g, out-of-equilibrium dynamics, particle scattering, is a promising example of quantum enhanced applications

rce with nea $|\psi(t)\rangle = e^{-iHt}|\psi(0)\rangle$

Infamous sign problem with

- non-zero density, temperature
- topological term, etc.

-
-

Quantum Dynamics Simulation in Schwinger Model

Simulation of quench dynamics in (1 + 1)*d U*(1) LGT (**Schwinger model**)

Particle creation due to strong external electric feld ➡ **Schwinger efect**

Prepare quantum states using time evolution of circuit parameters **Possible to simulate with fixed-depth quantum circuit**

✓⇤ **Variational Quantum Simulation (VQS)**

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- L. Nagano, A. Bapat, C. W. Bauer, [Phys. Rev. D 108, 034501 \(2023\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.108.034501)

$$
\operatorname{Re}\frac{\partial \langle \psi(\theta)|}{\partial \theta_i} \frac{\partial |\psi(\theta)\rangle}{\partial \theta_j} \qquad \qquad \overbrace{\sum_{j=1}^{n} \sum_{j=1}^{n} M_{ij} \dot{\theta}_j}^{\text{Solve classically}}
$$

Simulation of quench dynamics in (1 + 1)*d U*(1) LGT (**Schwinger model**)

Particle creation due to strong external electric feld ➡ **Schwinger efect**

Quantum Dynamics Simulation in Schwinger Model

WILIT TICLE ASHIY SYSLEITI VOIUIT with increasing system volume

Simulation of quench dynamics in (1 + 1)*d U*(1) LGT (**Schwinger model**)

Particle creation due to strong external electric feld ➡ **Schwinger efect**

Quantum Dynamics Simulation in Schwinger Model

Dynamical Phase Transition in Schwinger Model

Investigating topological properties through *θ*-term in real-time dynamics

Simulation of quench dynamics in (1 + 1)*d U*(1) LGT (**Schwinger model**)

Investigating topological properties through *θ*-term in real-time dynamics Strong quenches generate dynamical phase transition Rate function: ω_{\prime}

Dynamical Phase Transition in Schwinger Model

Simulation of quench dynamics in $(1 + 1)d$ $U(1)$ LGT (Schwinger model)

Loschmidt echo: $L(t) = \langle \Omega | e^{-iHt} | \Omega \rangle$ with initial state $|\Omega\rangle$

$$
H = J \sum_{j=0}^{N-2} \left(\sum_{k=0}^{j} \frac{Z_k + (-1)^k}{2} \frac{\left| \frac{\partial}{\partial z_j} \right|}{\left| \frac{\partial}{\partial z_j} \right|} \right)^2 + \frac{1}{2} \sum_{k=0}^{N-2} \left(\frac{\partial}{\partial z_k} \frac{\partial}{\partial z_k} \right)^2
$$

$$
\Gamma(t) = \lim_{N \to \infty} \left\{ -\frac{1}{N} \log(|L(t)|) \right\}
$$

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Qubit technologies offer interesting opportunities to experimentally probe nature in diferent ways from conventional methods

Qubit Technology as a Sensor

Certain types of qubits will work as a probe to nature **Quantum Sensor**

What quantum system can work as a quantum sensor? 1. Identifed, discretized energy levels (usually 2-levels)

-
- 2. Initialization and measurement
- 3. Coherent manipulation of state
-

4. Can couple to what we want to measure (e.g, electric/magnetic feld, ..)

Utilizing sensor response, e.g, qubit transition energy E or rate Γ , to what we want to measure

Superconducting qubits potentially a powerful probe to nature

- ► Low threshold ($\sim \mu$ eV) at $\mathcal{O}(mK)$ temperature
- ► Coherent manipulation of states within $\mathcal{O}(100 \,\mu s)$ or longer coherence time ‣ Robust measurement with non-demolition technique
-

Strong coupling to electromagnetic feld $\mathcal{O}(10^6)$ stronger than single atom

Qubits as Quantum Sensor

Qubits as a Dark Matter Sensor

- Exploring superconducting qubit technology for Dark Matter searches
	- Most recent results presented at 19th Patras Workshop on Axions, [WIMPs and WISPs](https://agenda.infn.it/event/40078/overview) on Sep. 16-20, 2024:
		- ‣ **K. Nakazono** First results from a cavity haloscope experiment with a novel frequency tuning system using a qubit [\(talk](https://agenda.infn.it/event/40078/contributions/240711/))
		- ‣ **K. Watanabe** Search for dark photons using direct excitations of superconducting qubits ([poster\)](https://agenda.infn.it/event/40078/contributions/240732/)
		- **T. Nitta** Towards axion searches using superconducting qubits (**poster**)
		- ‣ **S. Chen** Search for dark photon dark matter using large-scale superconducting quantum computers as detectors [\(poster](https://agenda.infn.it/event/40078/contributions/240696/))
			- Please take a look at their talks/posters for details Just highlight one of them today

Dark Matter Search with Direct Qub...

- \triangleright Co by photons
	- col converted from DM (e.g, dark photon)
- ‣ Directly drive Qubit as a *DM-induced* microwave Cuy anve Quoit as a Divi-induced micro

Extrong coupling of strong coupling S. Chen et al., [PRL 131, 211001 \(2023\)](https://doi.org/10.1103/PhysRevLett.131.211001)

Wave-like DM, e.g, Axion, Dark Photon with mass $\sim \mathscr{O}(\mu \text{eV}-\text{meV})$, well motivated Chen et al. γ *A*′ *γ*

Qubit Fabrication

Create our own qubits and cavity for the experiment K . Watanabe, K. Nak Create our own qubits and cavity for the experiment

element representation of a *LC* circuit capacitively coupled to a single-junction transmon and the associated the potential of each mode

Frequency Modulation

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Expected noise sources of $|0\rangle \rightarrow |1\rangle$ transition

Expected Sensitivity for Direct Qubit Excitation

‣ Thermal noise:

 $p \sim e^{-\hbar \omega / k_B T} \sim 0.01\% - 1\%$ @ 30 mK

► Readout error : $\sim 0.1\%$

Possible to probe into unexplored region even with the excitation rate of **0.1%-10%**

S. Chen et al., [PRL 131, 211001 \(2023\)](https://doi.org/10.1103/PhysRevLett.131.211001)

Mass [GHz]

First Results from Direct Qubit Excitation

from the baseline of observed data (mainly from thermal noise)

Expected sensitivity at $C = 0.1$ pF, $d = 100 \,\mu \text{m}$, *τ* = 30 *μ*s

‣ Sensitivity enhancement with quantum interference S. Chen et al., [PRL 133, 021801 \(2024\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.133.021801) S. Chen et al., [arXiv:2407.19755](https://arxiv.org/abs/2407.19755)

- Amplifier
- Circulator/Isolator, etc.

-
-

- Design optimization (e.g, larger C/d , smaller JJs) *C d*
- Magnetic field tolerance

Application/Algorithm

Eforts on Quantum Computing/Sensing

Summary

Aiming at demonstrating quantum advantage and/or quantum as useful resources in the *computational particle physics* in future

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- New opportunities in technology development and scientifc discovery

(e.g, DM search with superconducting qubits)

- Presented selected results at ICEPP on quantum computing and
	-

the application to particle physics:

- ‣ learning quantum states/processes
-
- ‣ simulating quantum dynamics in Lattice Gauge Theory ‣ searching for dark matter with superconducting qubits

Summary

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