

Magnetosphere origin of Fast Radio Bursts

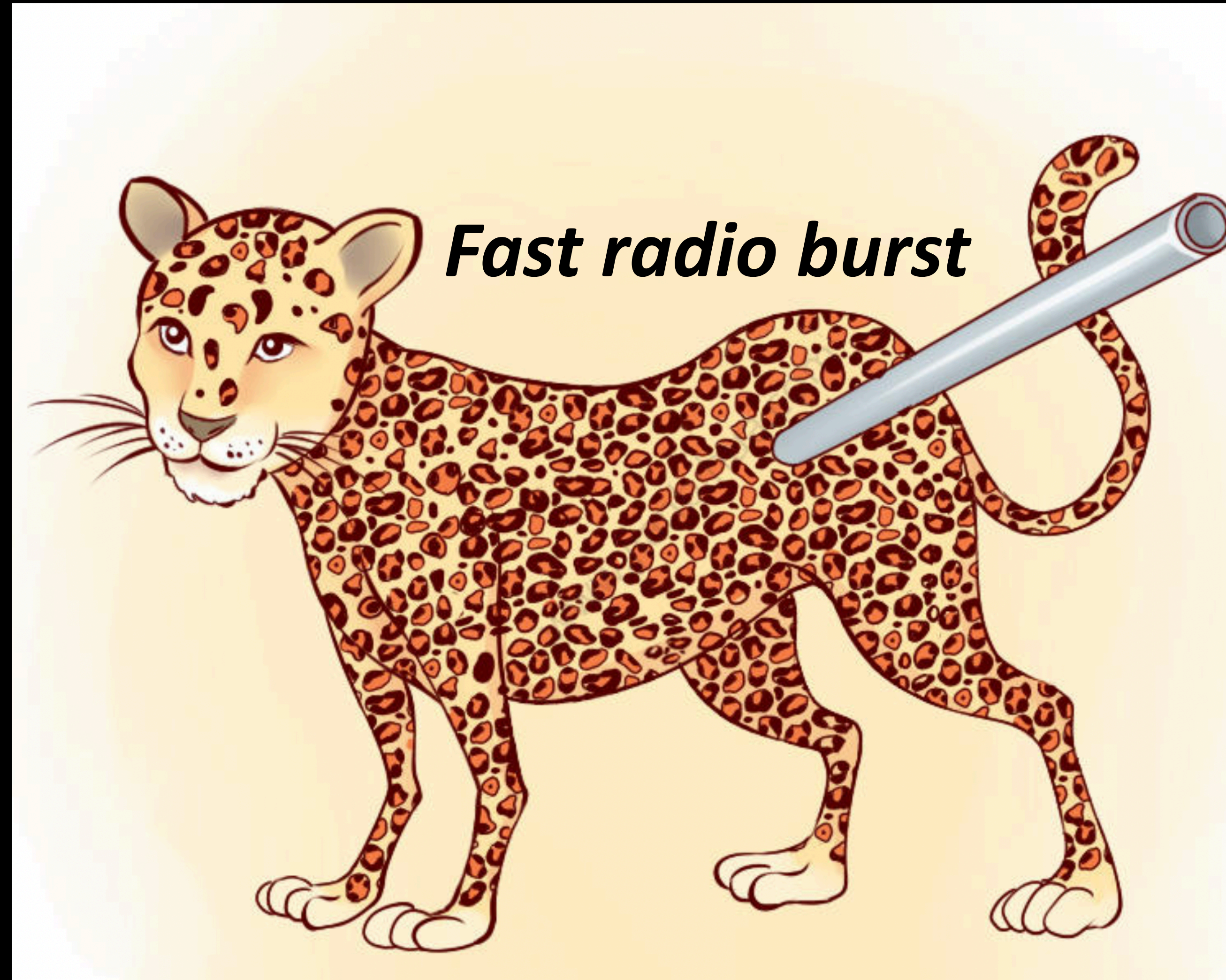
Yuanhong Qu

University of Nevada, Las Vegas

Outline:

1. Multi-messenger: neutrino emission?
2. Plasma effect on bunching mechanisms
3. Propagation in the magnetosphere

管中窺豹 Look at a leopard through a tube



observer

FRB could origin from magnetosphere

We need to collect observational results to predict the origin of FRB

Highly dispersed short radio pulse

Dispersion

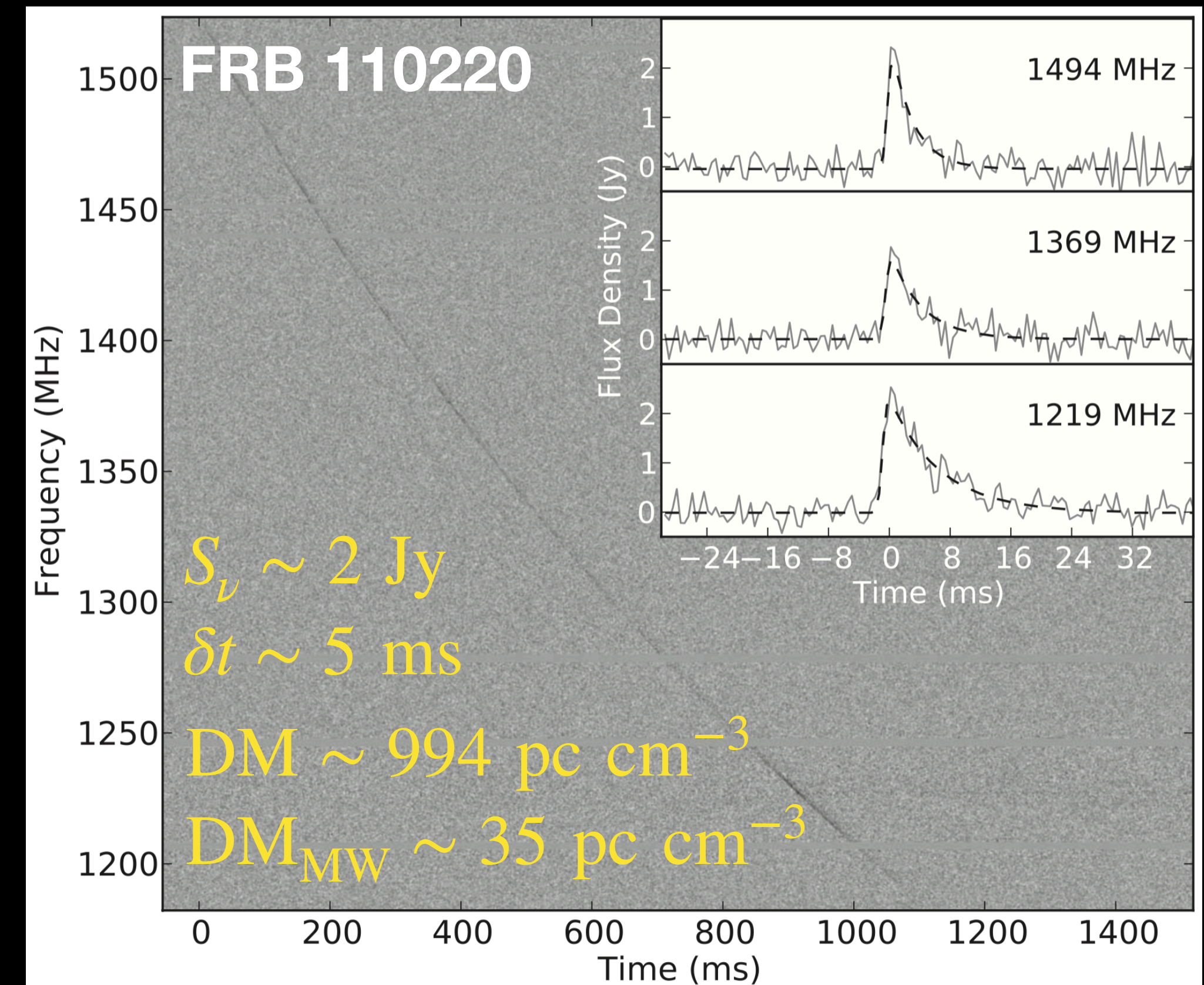
$$t(\nu) - t(\infty) = (4.416 \text{ s}) \nu_{\text{GHz}}^{-2} \frac{\text{DM}}{10^3 \text{ pc cm}^{-3}}$$

Brightness temperature

$$T_b \sim \frac{F_\nu D_A^2}{2\pi k \nu^2 \delta t^2} \simeq 10^{35} \text{ K} \left(\frac{F_\nu}{\text{Jy}} \right) \left(\frac{\nu}{\text{GHz}} \right)^{-2} \left(\frac{\delta t}{\text{ms}} \right)^{-2} \left(\frac{D_A}{\text{Gpc}} \right)^2$$

Strong wave factor Luan & Goldreich 2014

$$a = \frac{eE_w}{m_e c \omega} = \frac{eL_{\text{frb}}^{1/2}}{m_e c^{3/2} \omega r} \simeq 1.6 \times 10^4 L_{\text{frb},42}^{1/2} \nu_9^{-1} r_9^{-1}$$



Thornton et al. 2013

FRB Radiation Mechanisms

Kumar et al. 2017

Kumar & Bosnjak. 2020

Metzger et al. 2019

Beloborodov. 2020

Yang & Zhang. 2018

Zhang. 2022

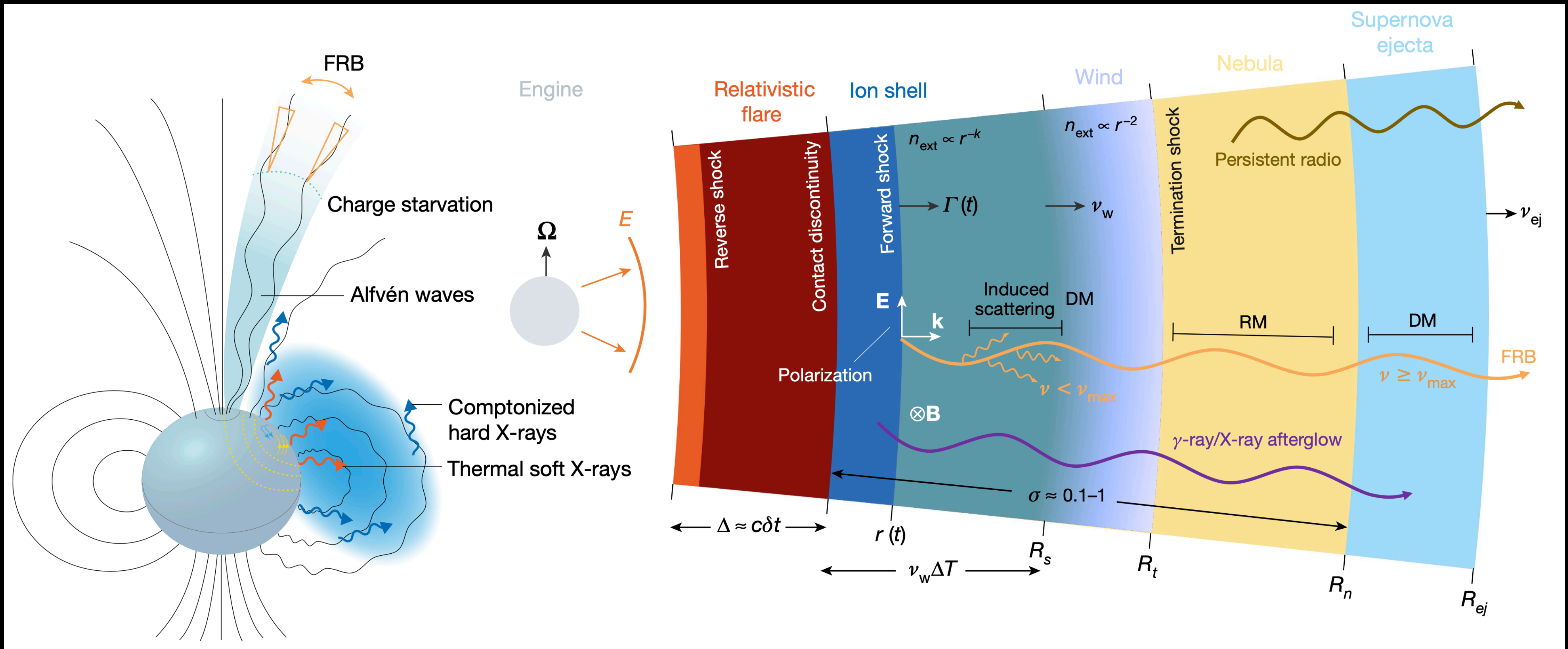
Yuan et al. 2020

Sironi et al. 2021

Lu et al. 2020

Waxman. 2017

Plotnikov & Sironi. 2019



Zhang. 2020

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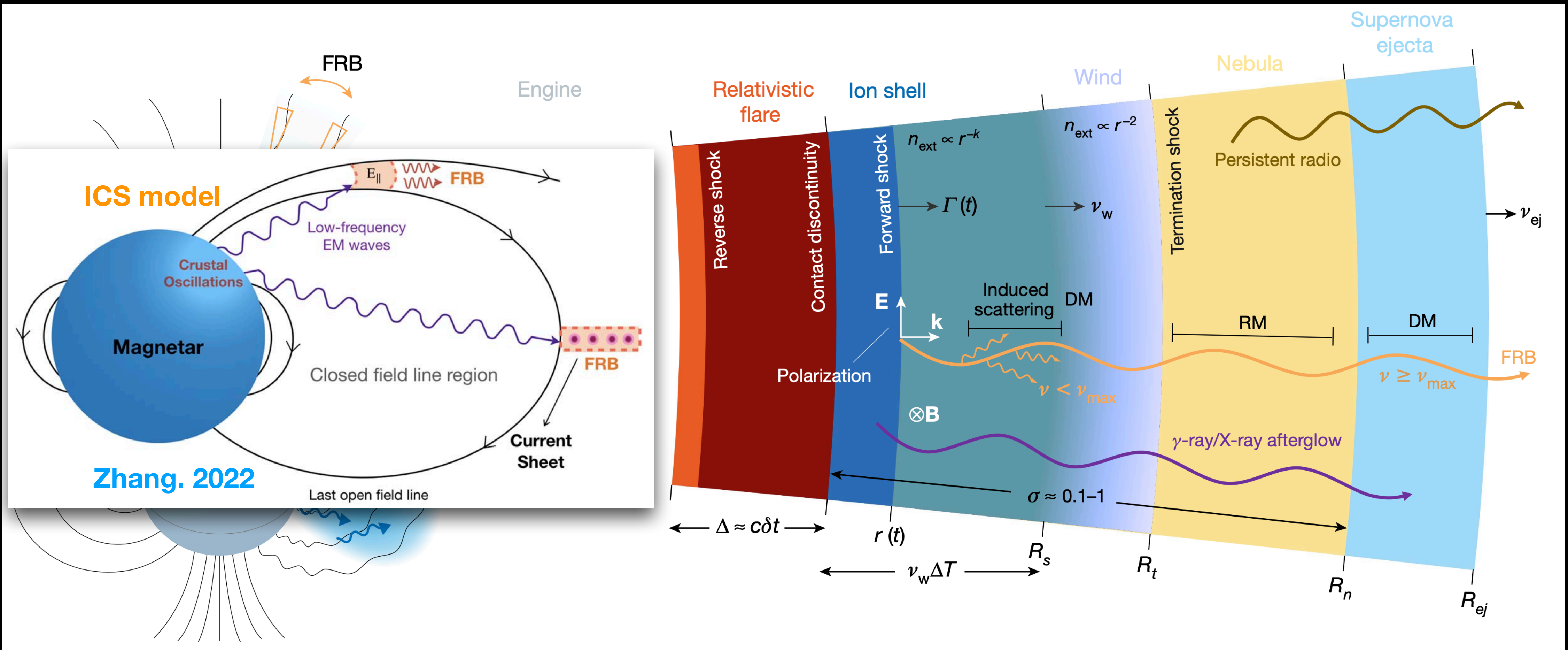
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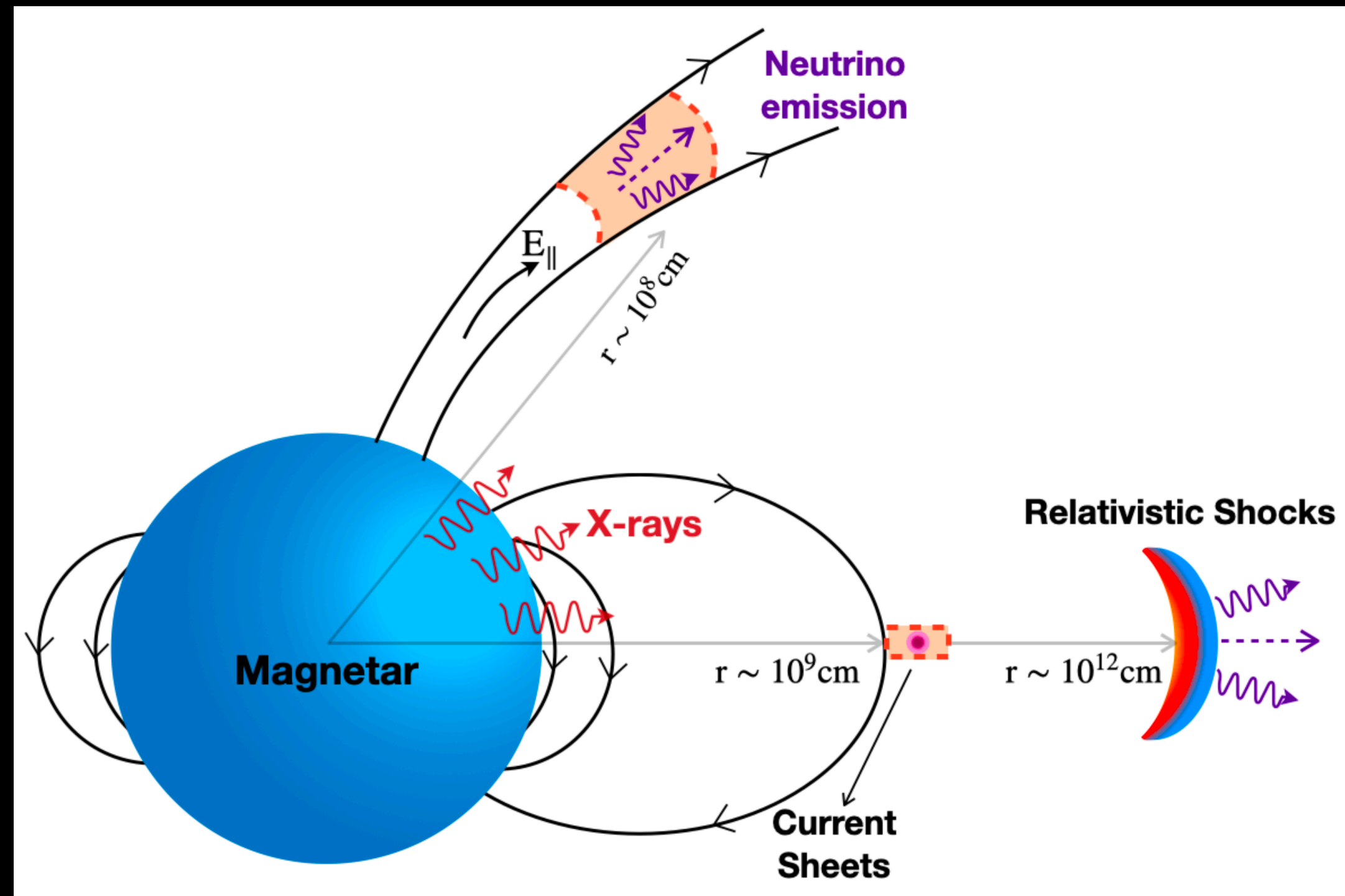
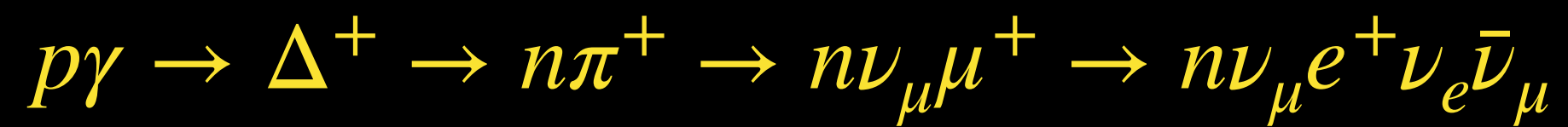
Zhang. 2020

Neutrino emission from FRB-emitting magnetars?

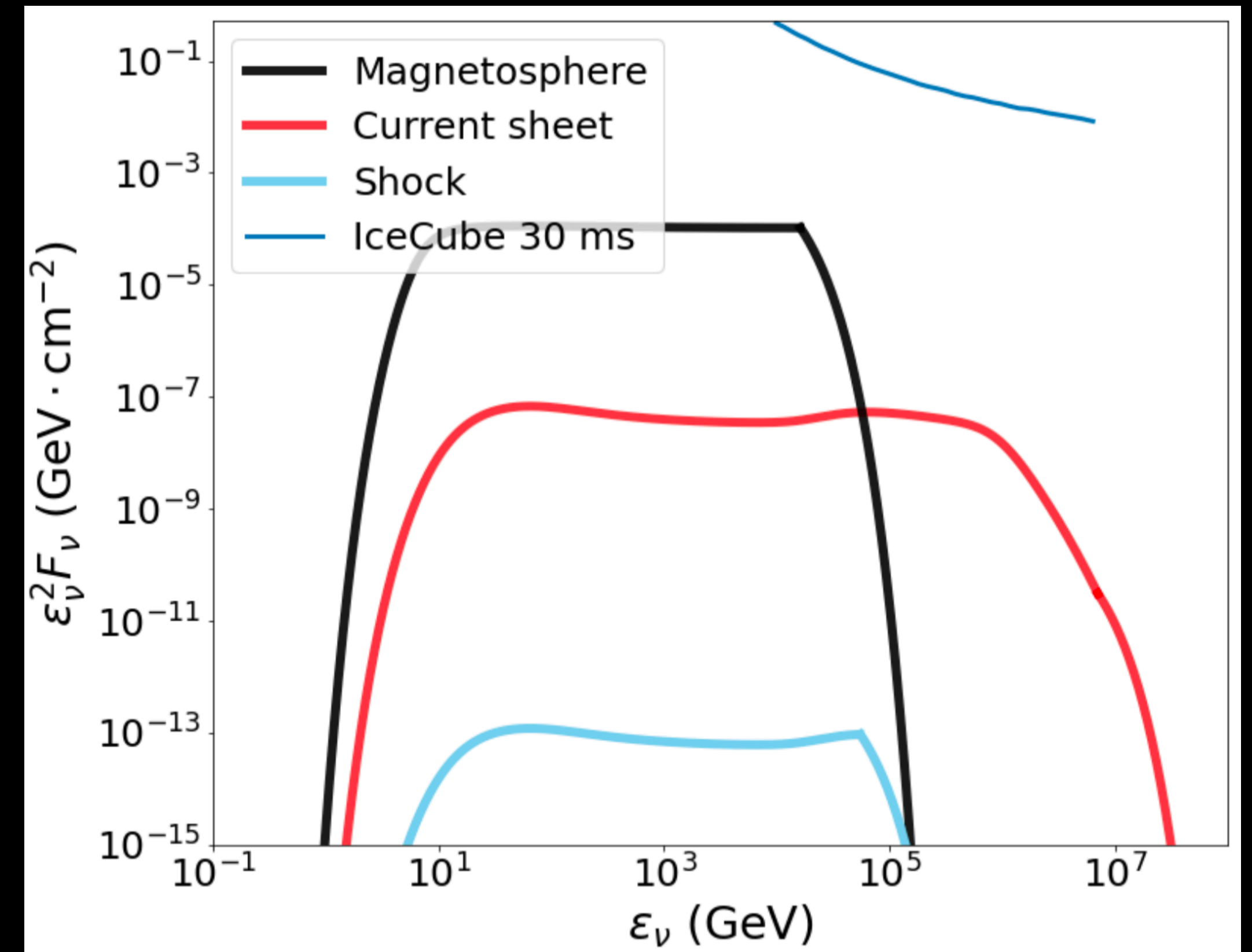
Qu & Zhang 2022 (2111.04121)

Metzger et al. 2020 (shock acceleration)

Photomeson interaction



FRB 200428

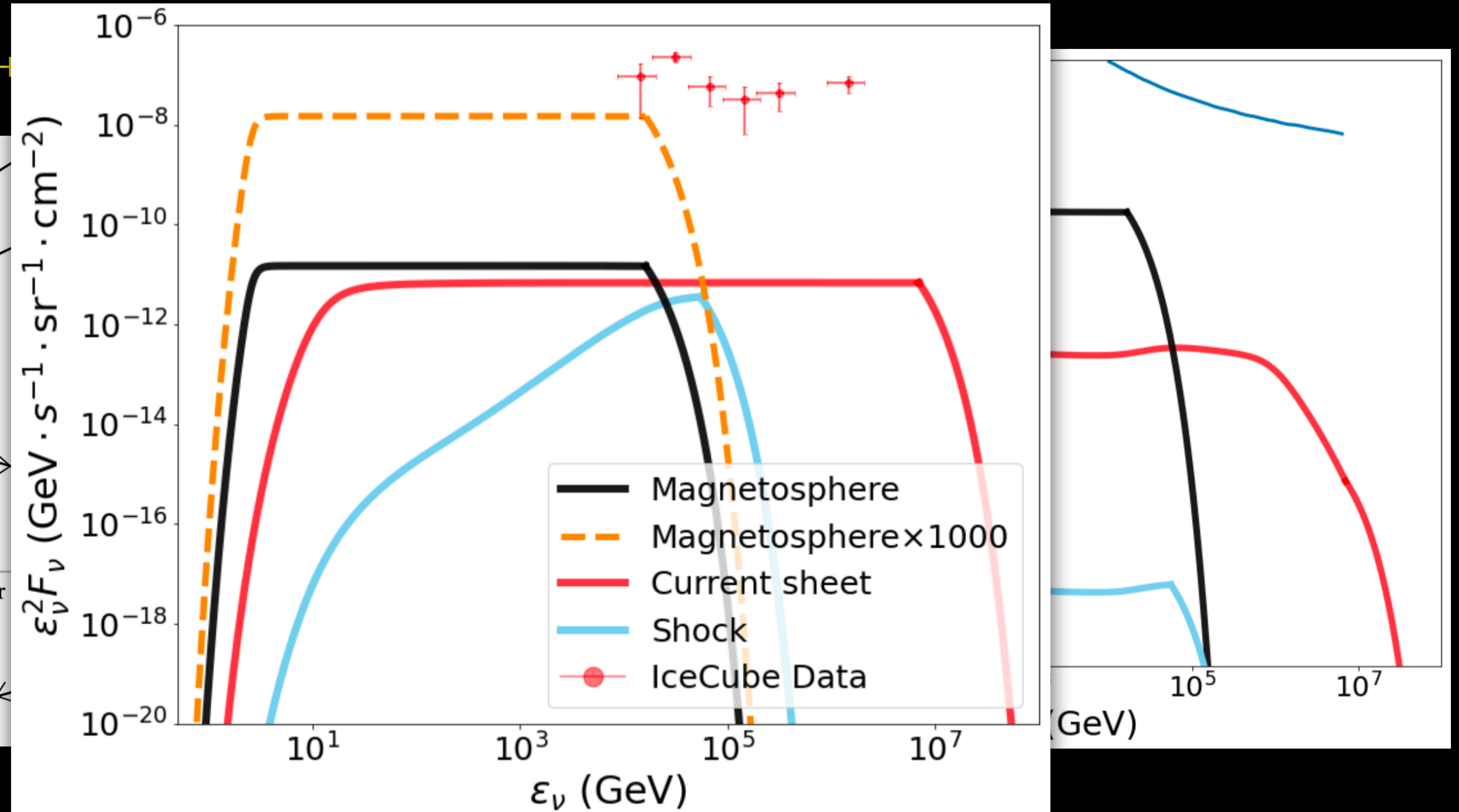
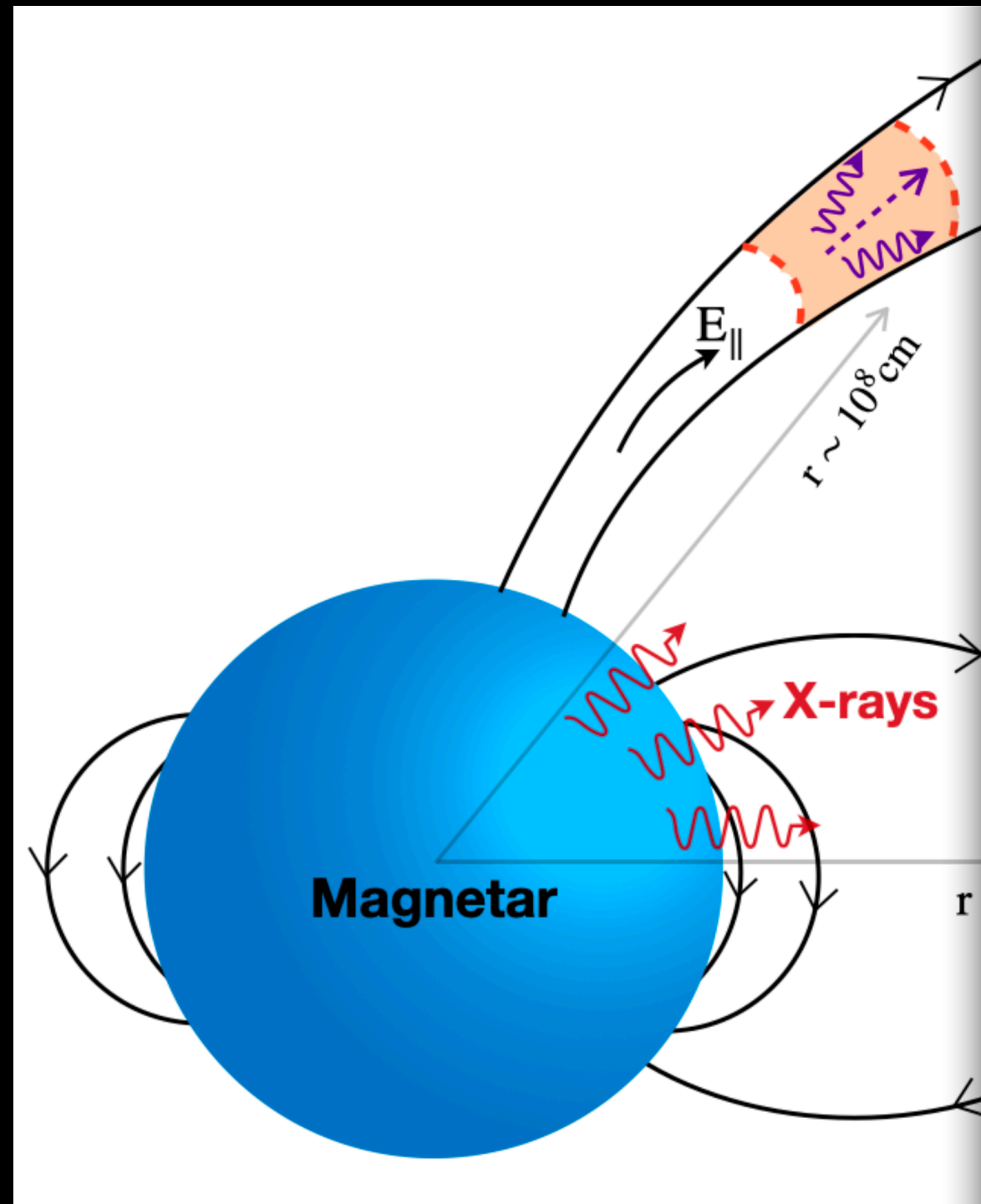
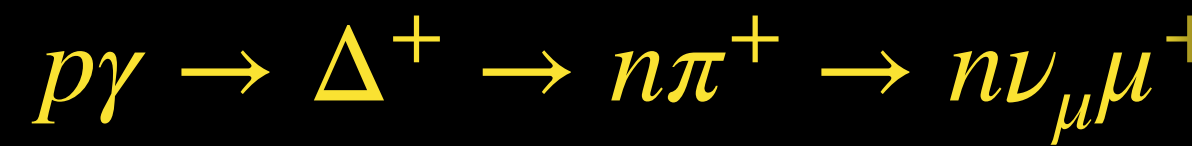


Neutrino emission from FRB-emitting magnetars?

Qu & Zhang 2022 (2111.04121)

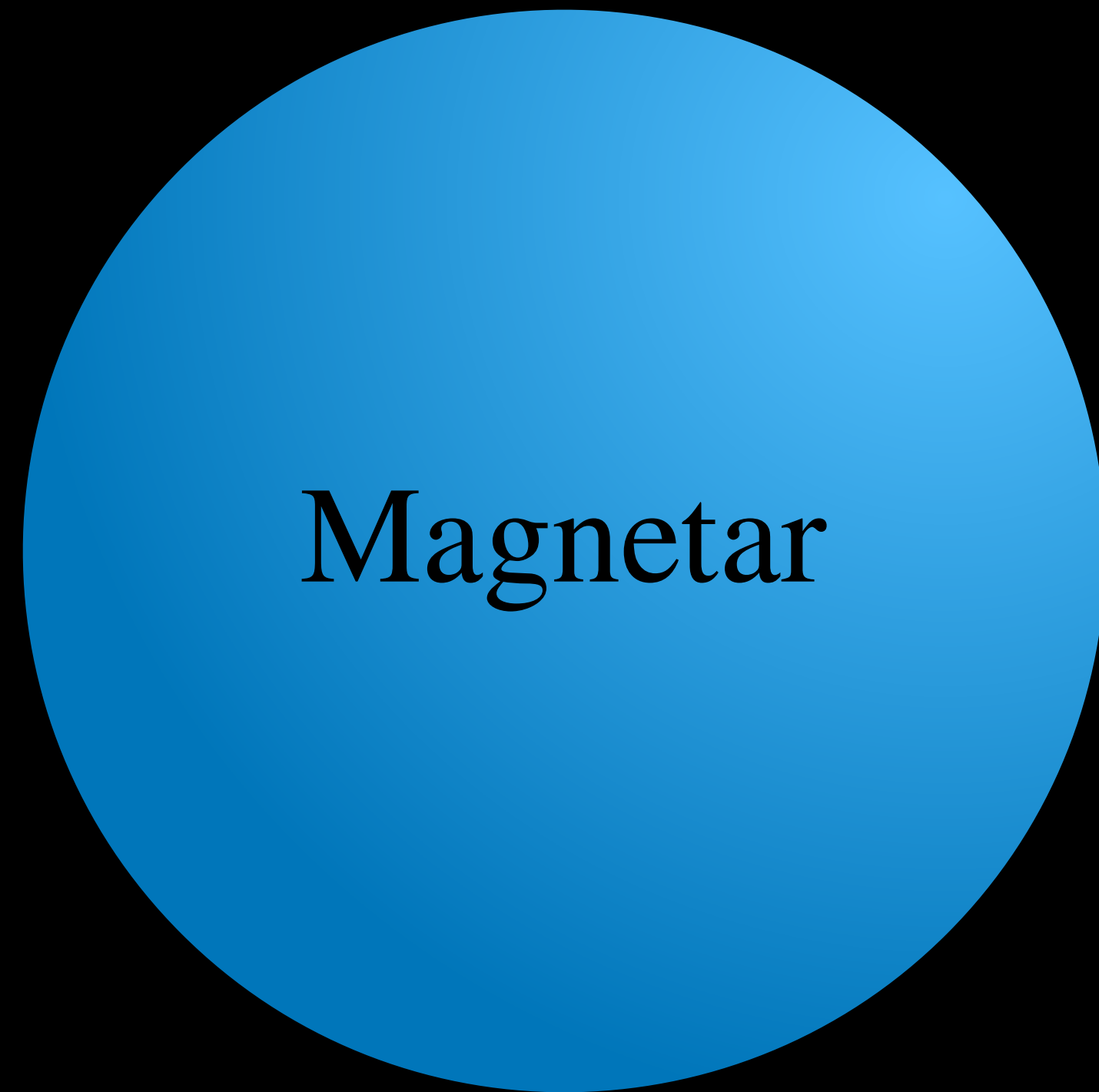
FRB 200428

Photomeson interaction



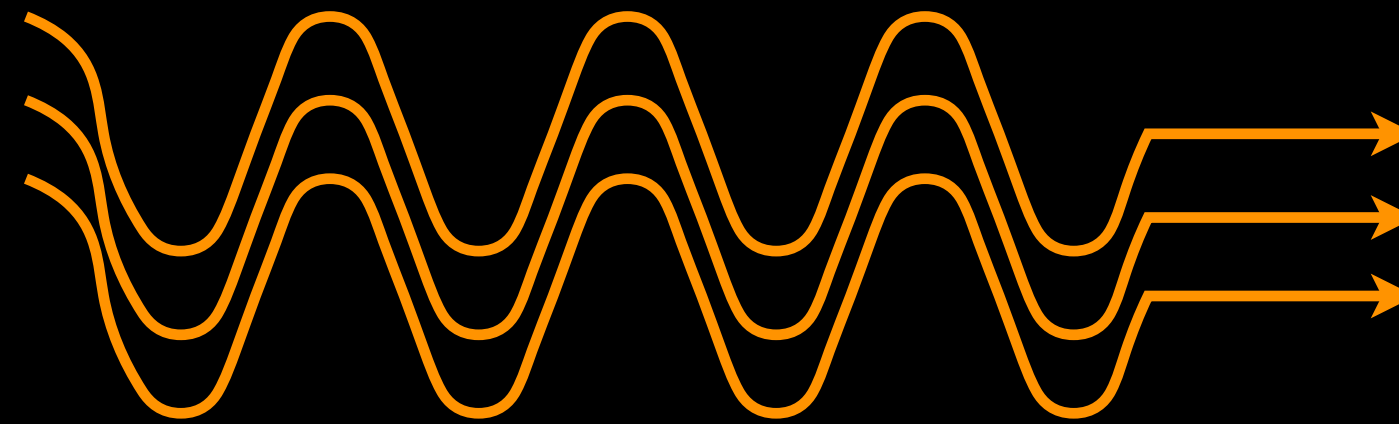
Diffuse background neutrino fluence spectrum for all FRB-emitting magnetars

Radiation produced inside the magnetosphere model

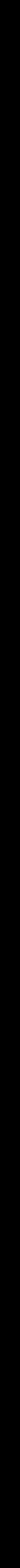


$$R_{\star} = 10^6 \text{ cm}$$

Coherent emission



Light cylinder

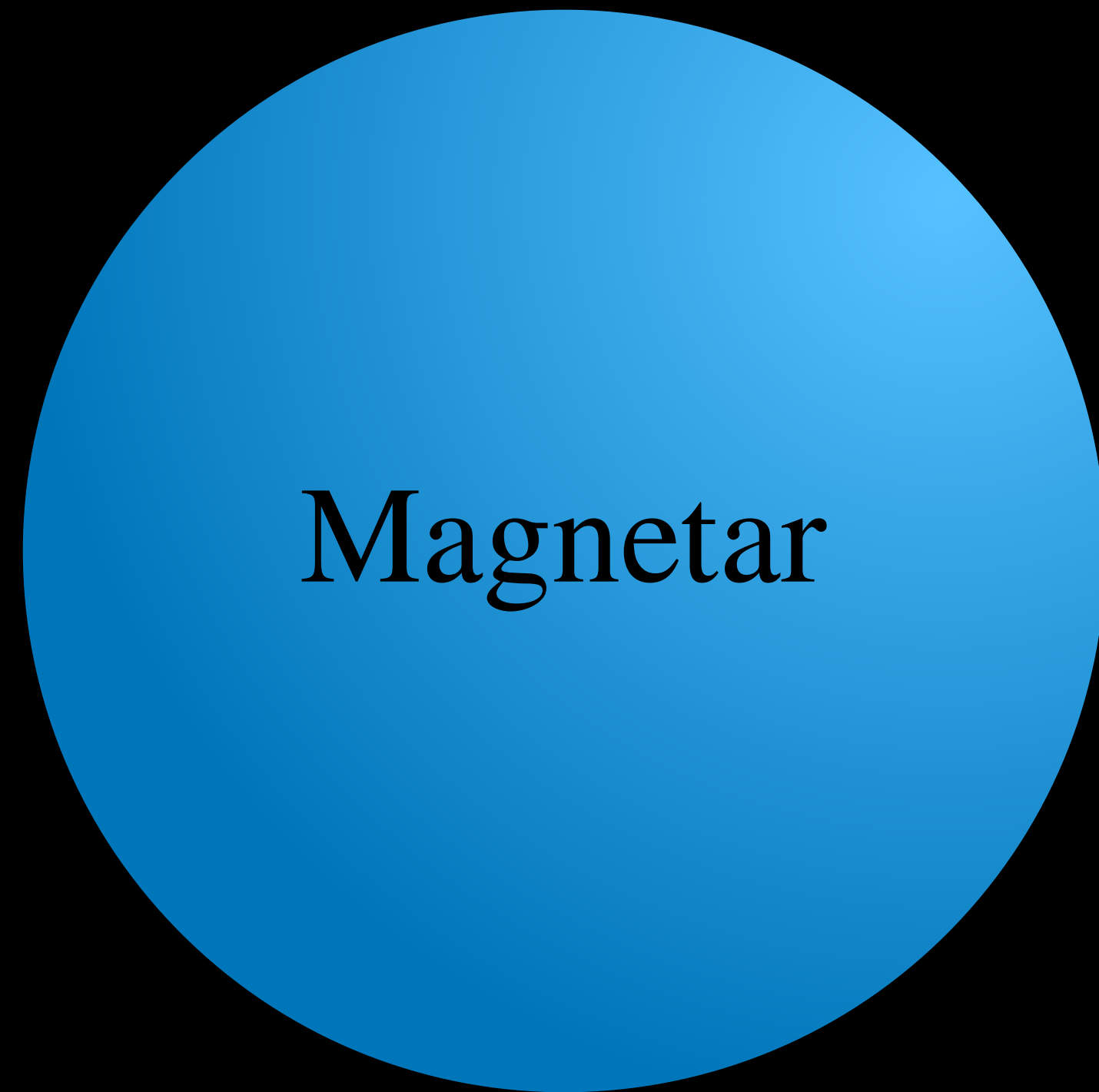


$$\sim 10^{10} \text{ cm}$$

$$E \sim N e^{i\phi}$$

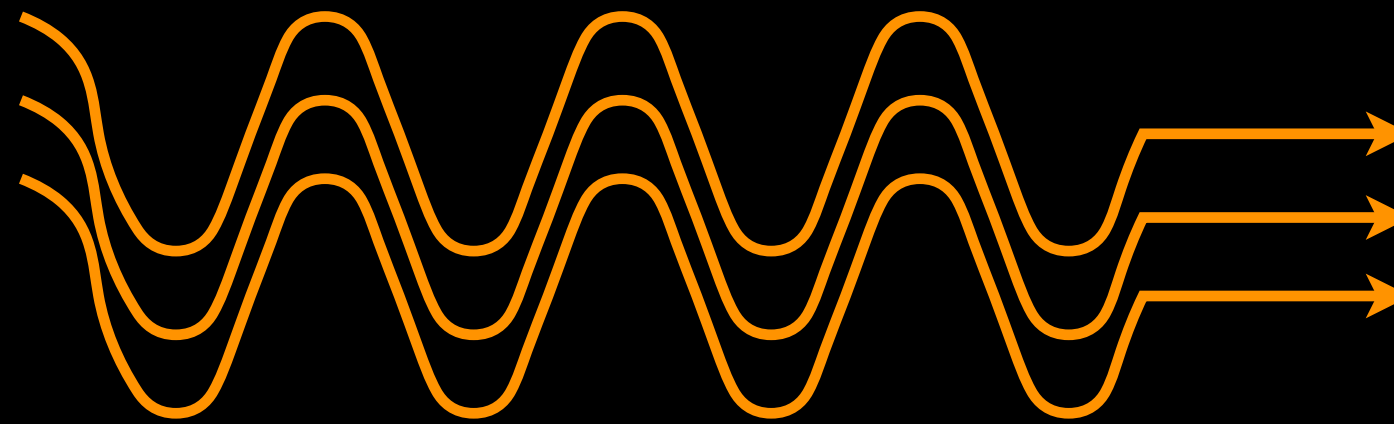
$$S \sim N^2$$

Radiation produced inside the magnetosphere model



$$R_{\star} = 10^6 \text{ cm}$$

Coherent emission



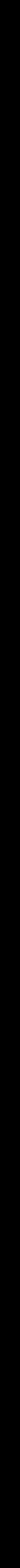
The 1st question is

Can FRB photons be suppressed by pair plasma?

Gil et al. 2004

Lyubarsky. 2021

Light cylinder



$$\sim 10^{10} \text{ cm}$$

$$E \sim N e^{i\phi}$$

$$S \sim N^2$$

Physical conditions for significant plasma suppression

Qu & Zhang 2021 (2111.12269)

$$\omega_p \gg \omega_{\text{FRB}} \Rightarrow \xi \gg 10^2$$

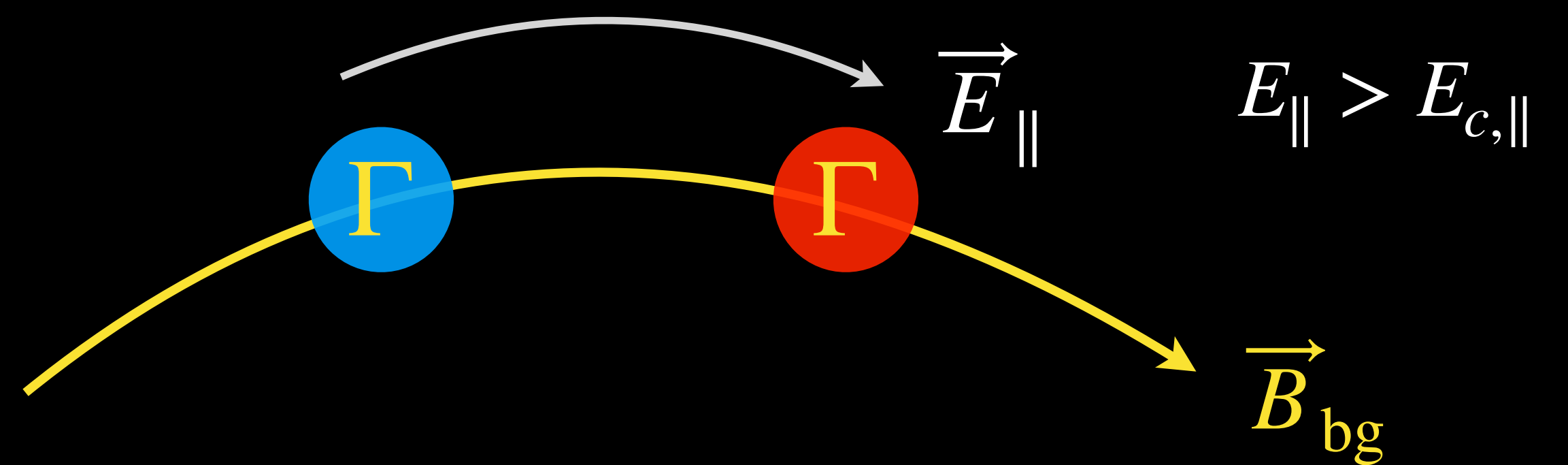
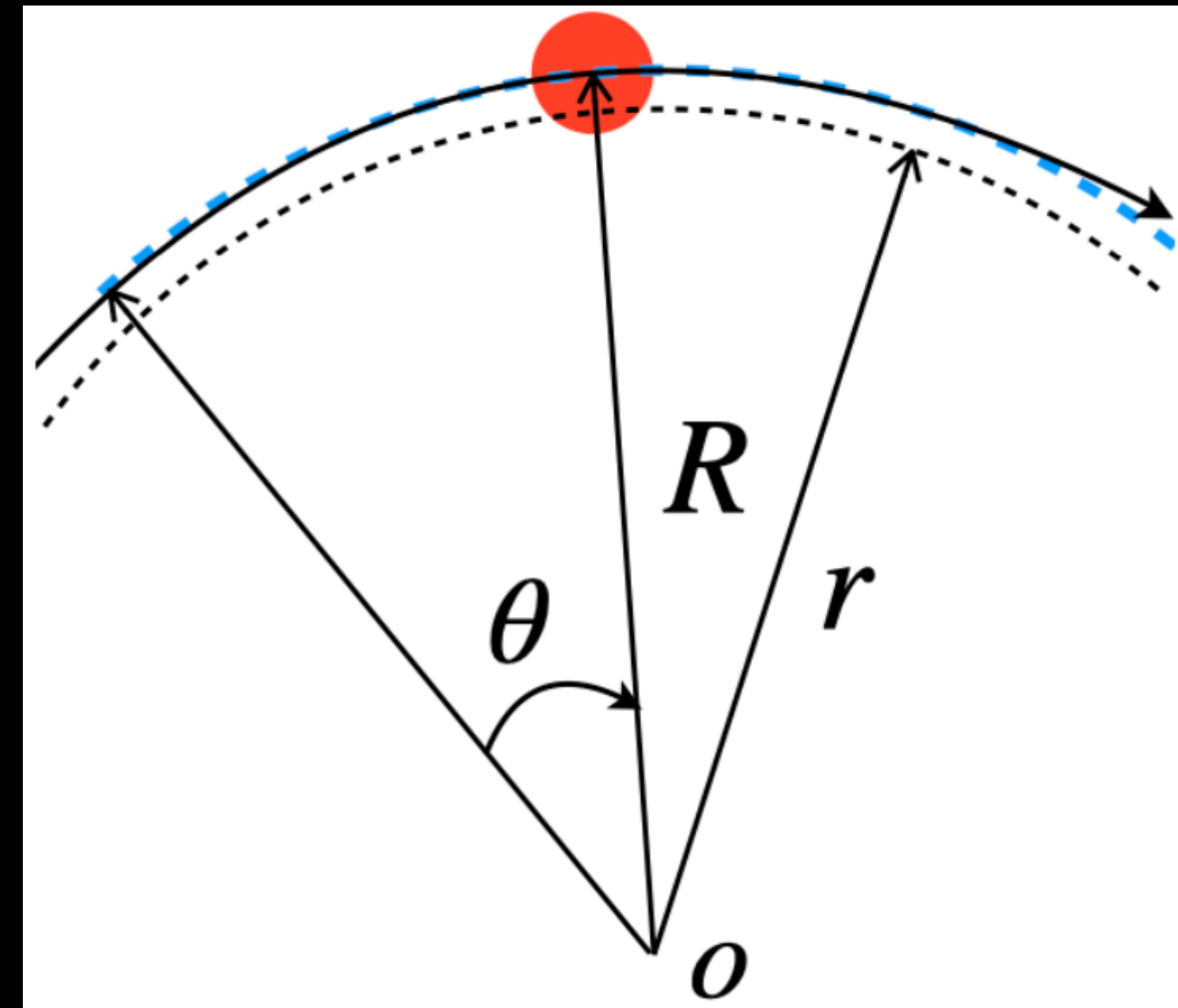
Parallel electric field is required

$$N^2 P_e = NeE_{\parallel} c \quad \text{Kumar \& Bosnjak. 2020}$$

Critical parallel electric field

$$E_{c,\parallel} \simeq \frac{eN}{\lambda_{\text{FRB}}^2} \simeq (2.7 \times 10^7 \text{ esu}) \xi_2 B_{\star,15} P^{-1} \hat{r}_2^{-3} \nu_9^{-4}$$

$$E_{\parallel} < E_{c,\parallel}$$



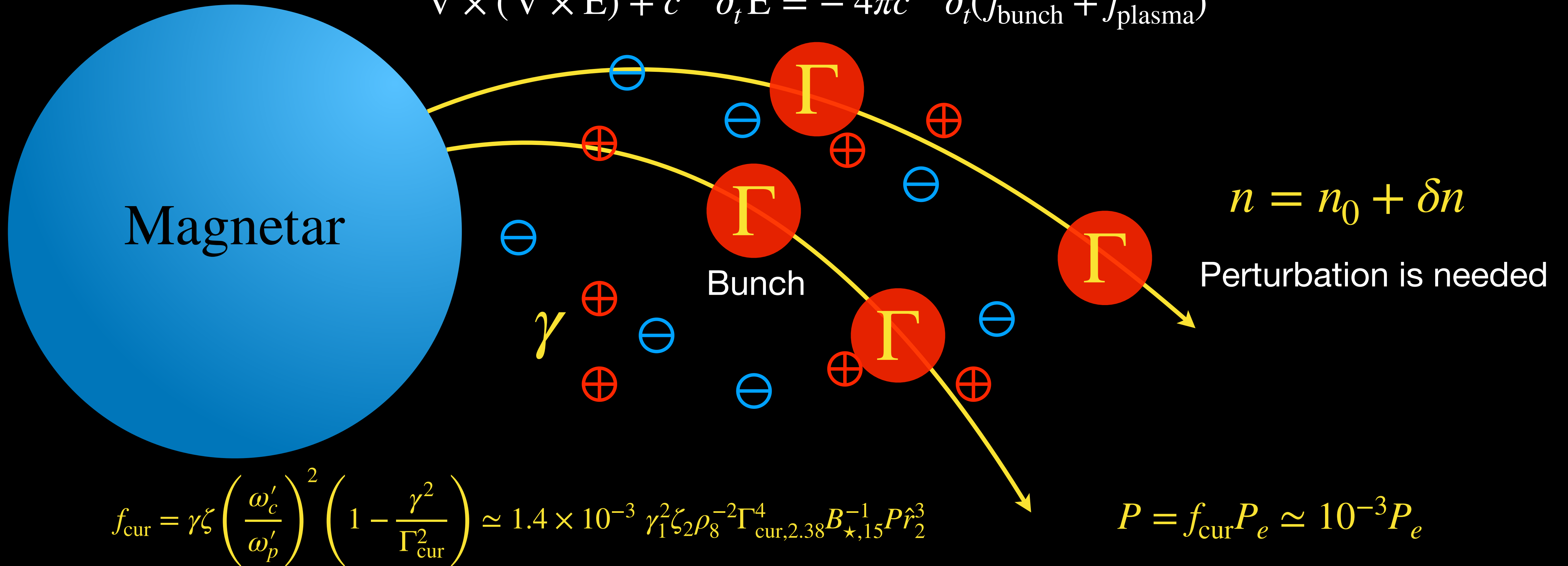
This scenario can interpret the narrow spectra of FRBs [Yang et al. 2020](#)

Plasma effect on coherent radio emission mechanism

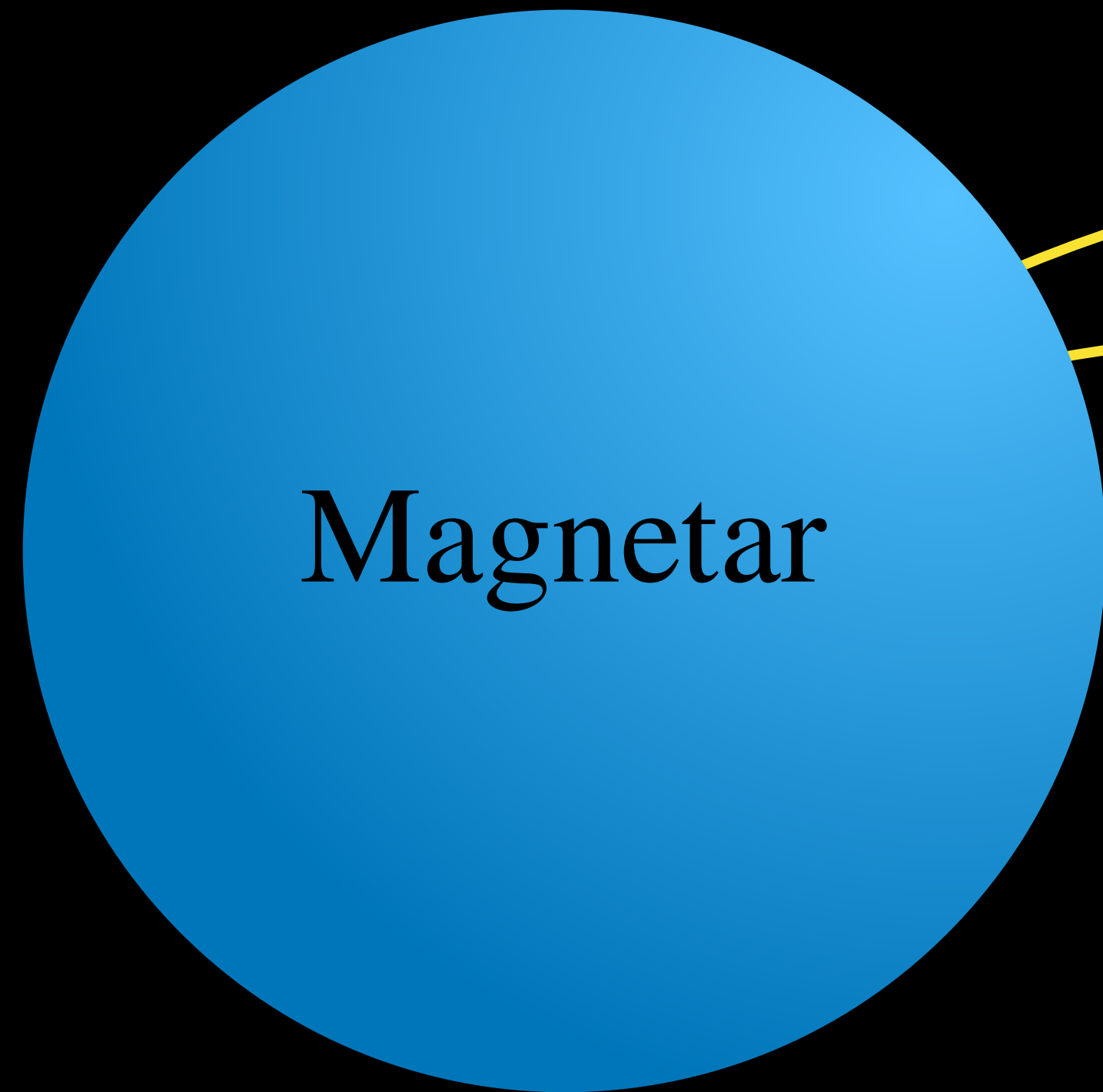
Qu & Zhang 2021 (2111.12269)

Electrons can only stay at Landau levels in strong magnetic fields $\frac{d(\gamma m_e v)}{dt} = eE_\theta$

$$\nabla \times (\nabla \times \mathbf{E}) + c^{-2} \partial_t^2 \mathbf{E} = -4\pi c^{-2} \partial_t (j_{\text{bunch}} + j_{\text{plasma}})$$

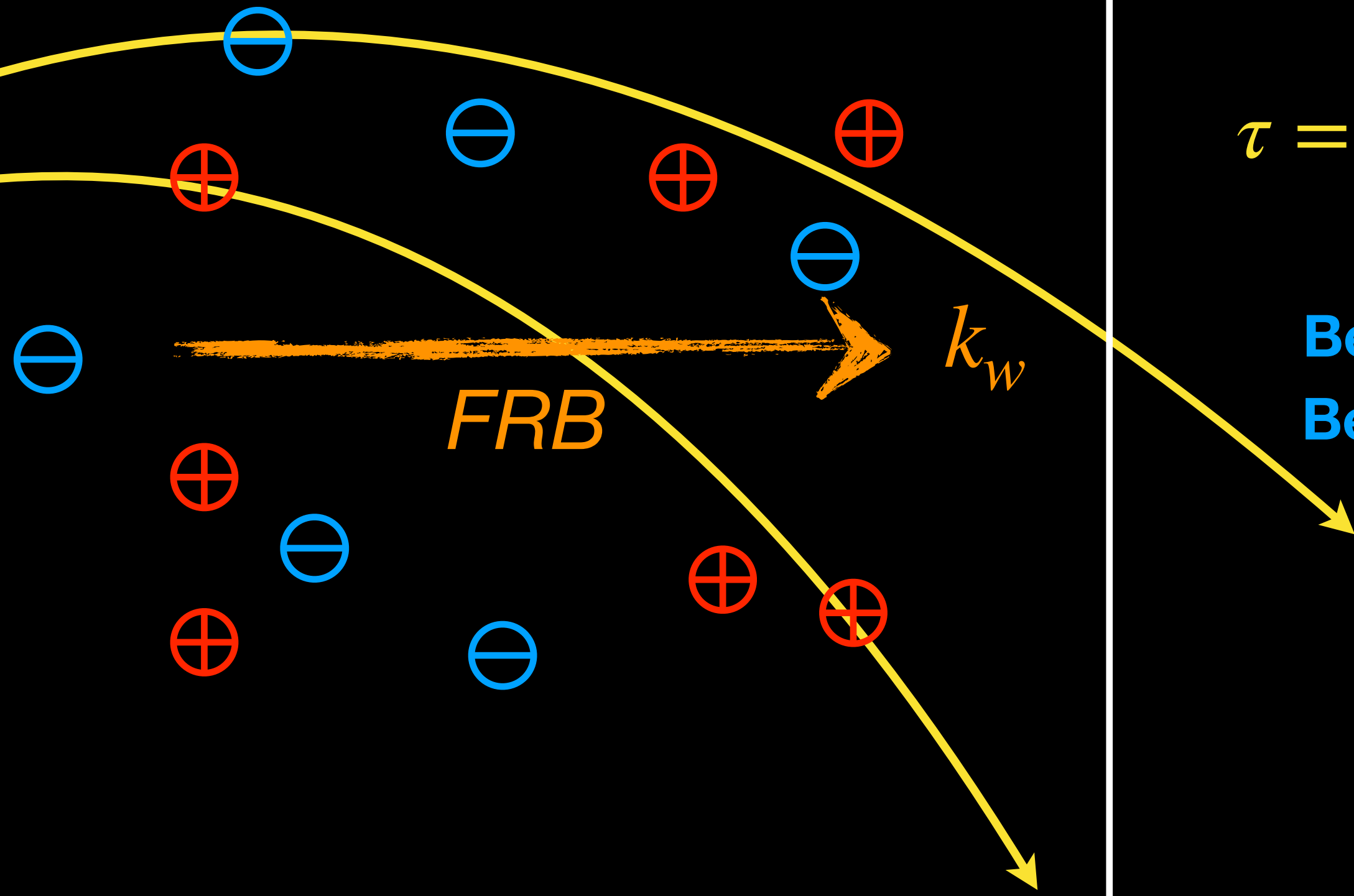


Radiation produced inside the magnetosphere model



Magnetar

$R_{\star} = 10^6$ cm



Light cylinder

The 2nd question is

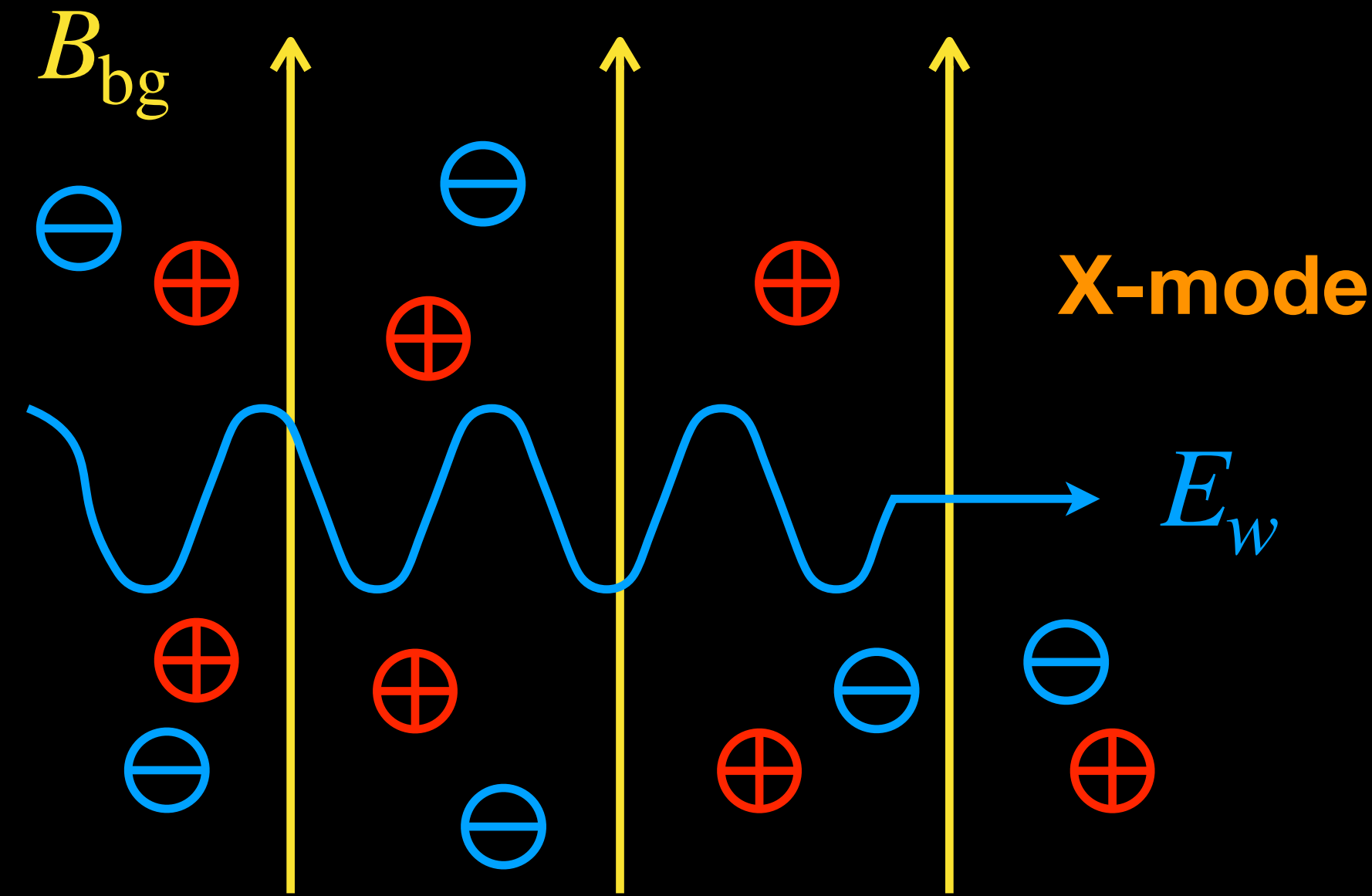
$$\tau = \int n_e \sigma dl \leq 1 \quad ?$$

Beloborodov. 2021a

Beloborodov. 2021b

$\sim 10^{10}$ cm

Classical scattering theory



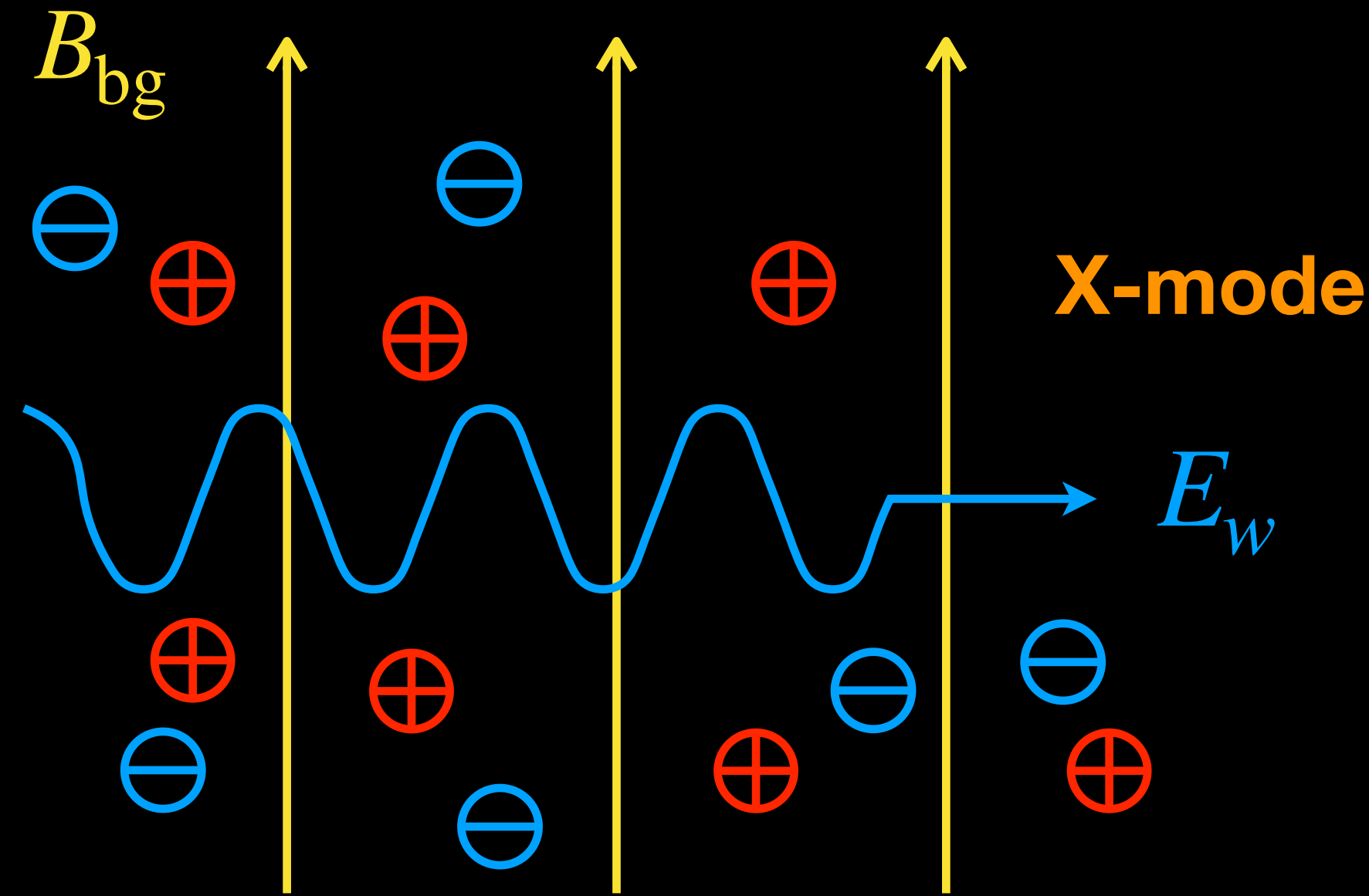
$$a = \frac{eE_w}{m_e c \omega} \sim 10^4 L_{\text{frb},42}^{1/2} r_9^{-1}$$

$$\frac{\omega_B}{\omega} = \frac{eB_{\text{bg}}}{m_e c \omega} \sim 10^3 r_9^{-1}$$

$$\sigma \sim \left(\frac{\omega^2}{\omega_B^2} \right) \sigma_T \quad \text{Assumption: } \omega_B \gg \omega \Rightarrow \text{The cross-section is suppressed for the EM X-mode photons}$$

Canuto et al. 1971
Gunn & Ostriker 1971
Herold, H. 1979

Classical scattering theory



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Gunn & Ostriker 1971
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Classical theory is invalid when $E_w \gg B_{\text{bg}}$

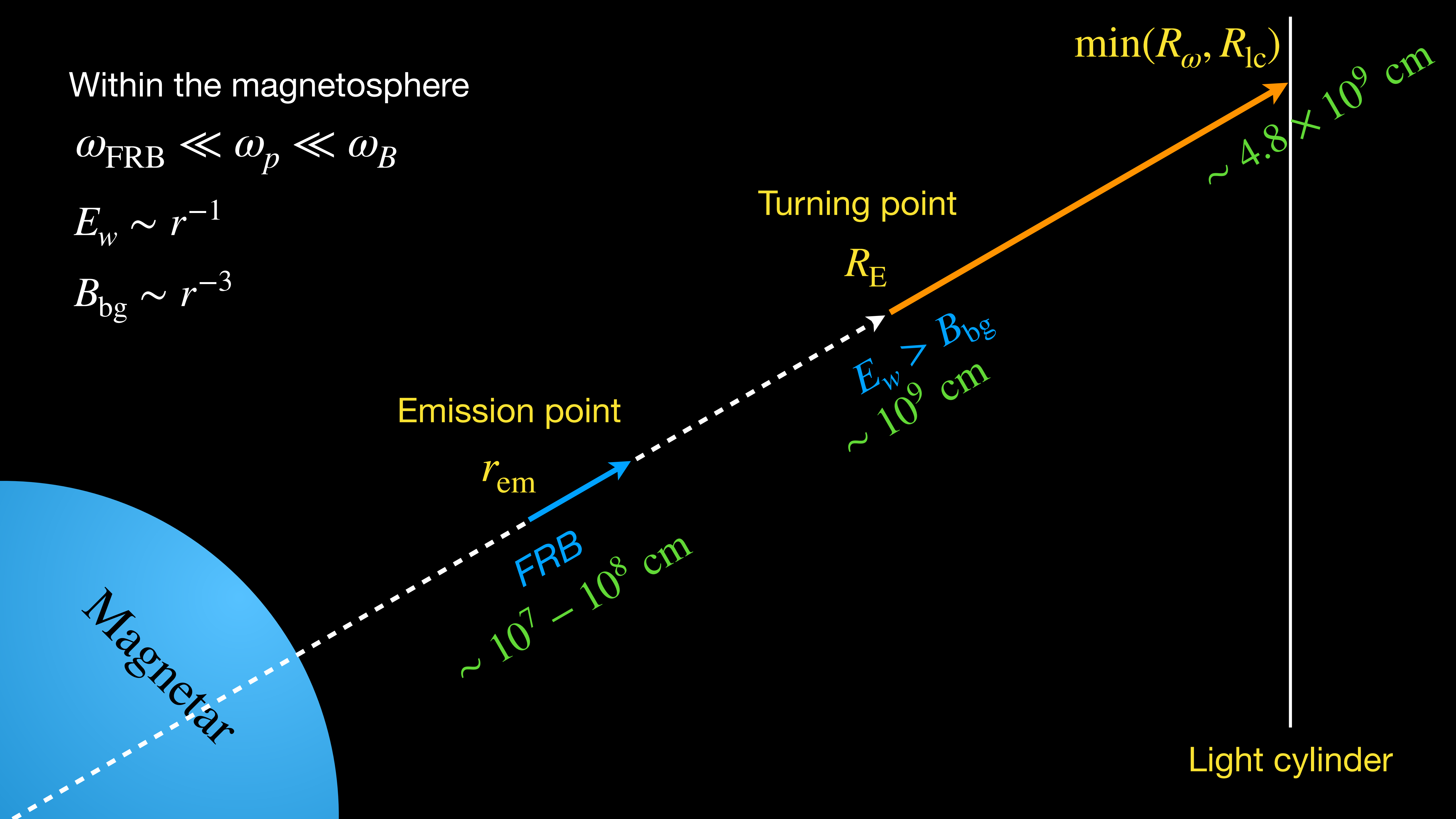
$$E_w > B_{\text{bg}} \Rightarrow a > \frac{\omega_B}{\omega} \quad \sigma \simeq a^2 \sigma_T$$

Within the magnetosphere

$$\omega_{\text{FRB}} \ll \omega_p \ll \omega_B$$

$$E_w \sim r^{-1}$$

$$B_{\text{bg}} \sim r^{-3}$$



$\min(R_\omega, R_{\text{lc}})$

$\sim 4.8 \times 10^9$ cm

Turning point

R_E

$E_w > B_{\text{bg}}$
 $\sim 10^9$ cm

Emission point

r_{em}

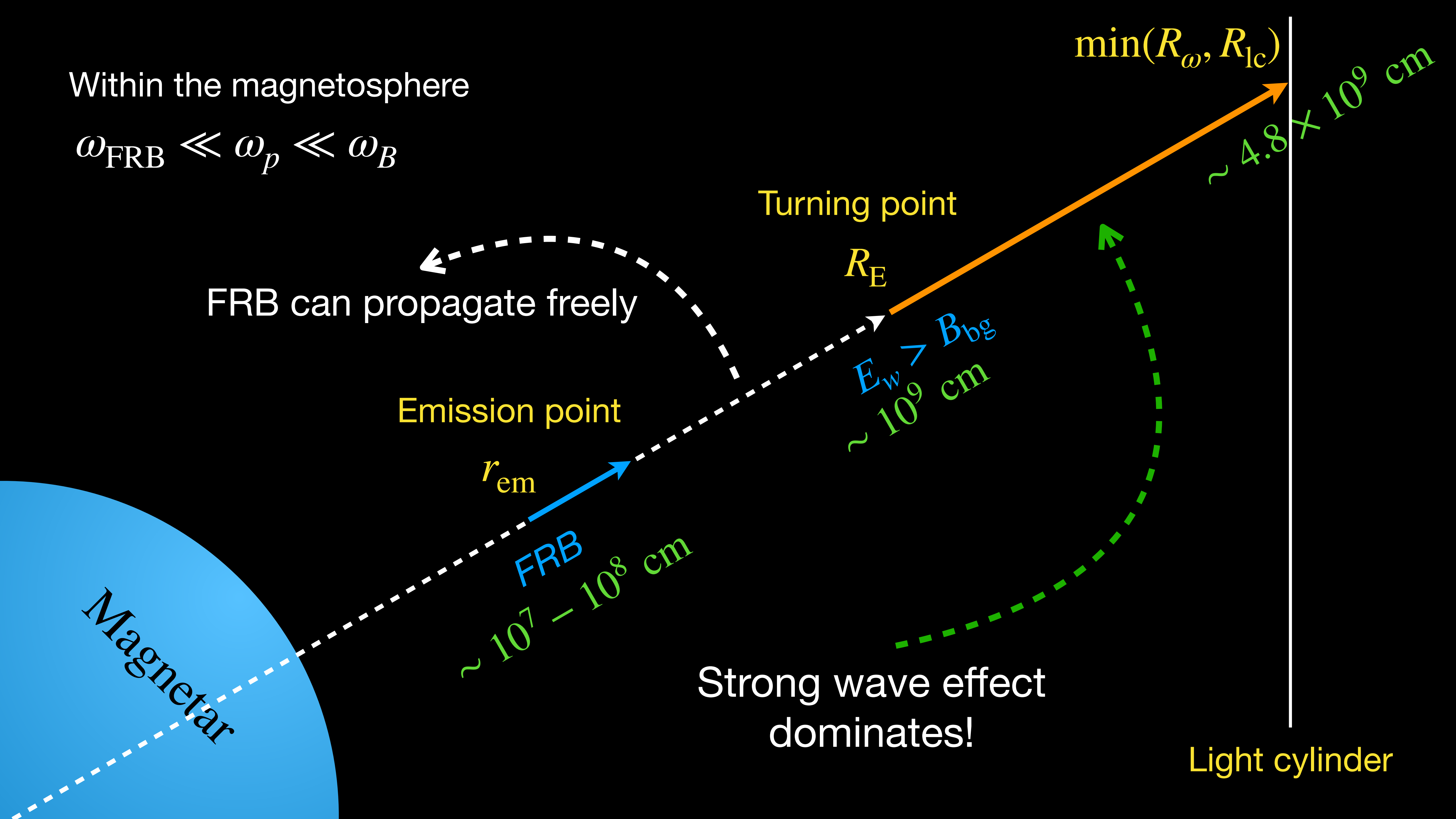
FRB
 $\sim 10^7 - 10^8$ cm

Magnetar

Light cylinder

Within the magnetosphere

$$\omega_{\text{FRB}} \ll \omega_p \ll \omega_B$$



FRB can propagate freely

Emission point

r_{em}

FRB

$\sim 10^7 - 10^8$ cm

Turning point

R_E

$E_w > B_{\text{bg}}$
 $\sim 10^9$ cm

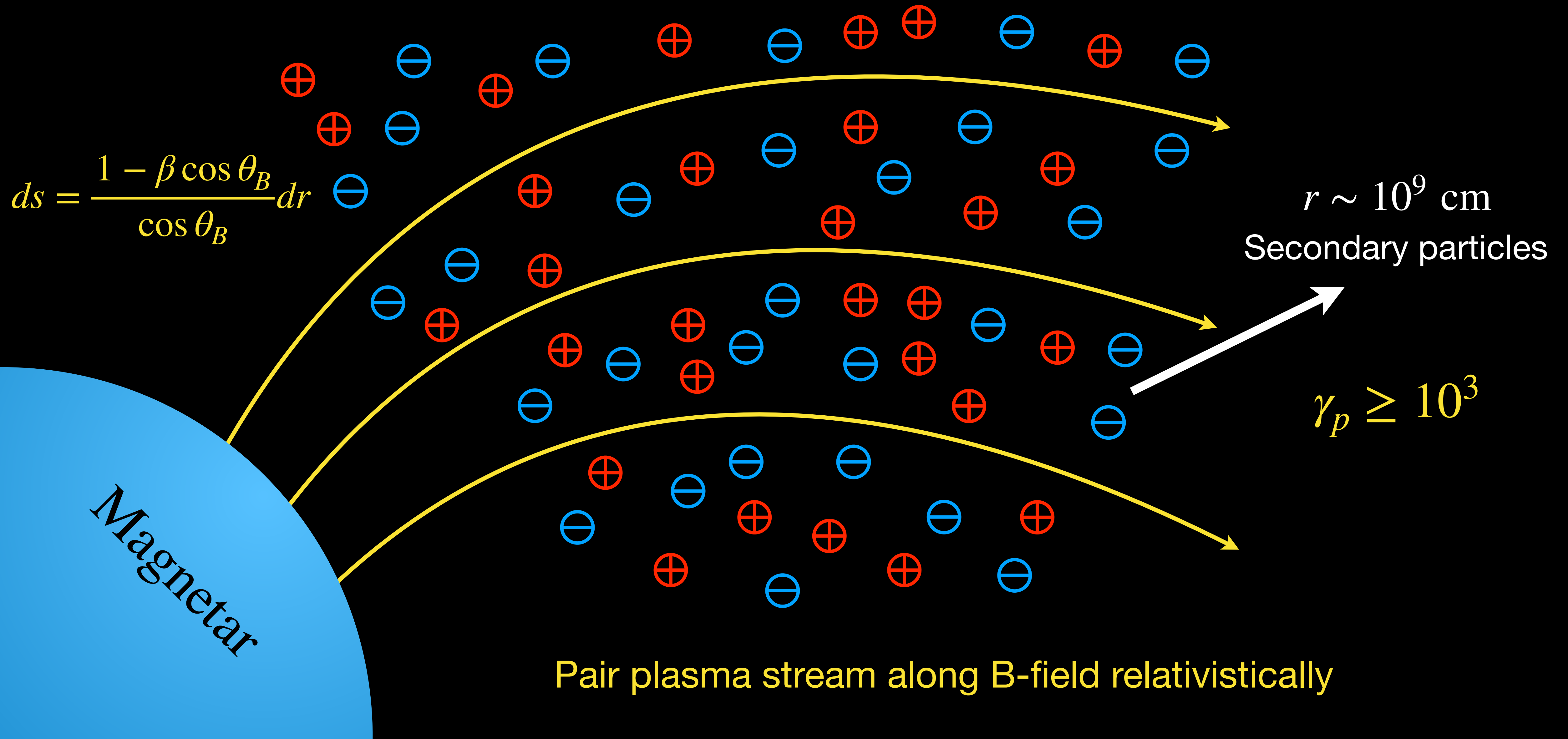
Strong wave effect
dominates!

$\min(R_\omega, R_{1c})$

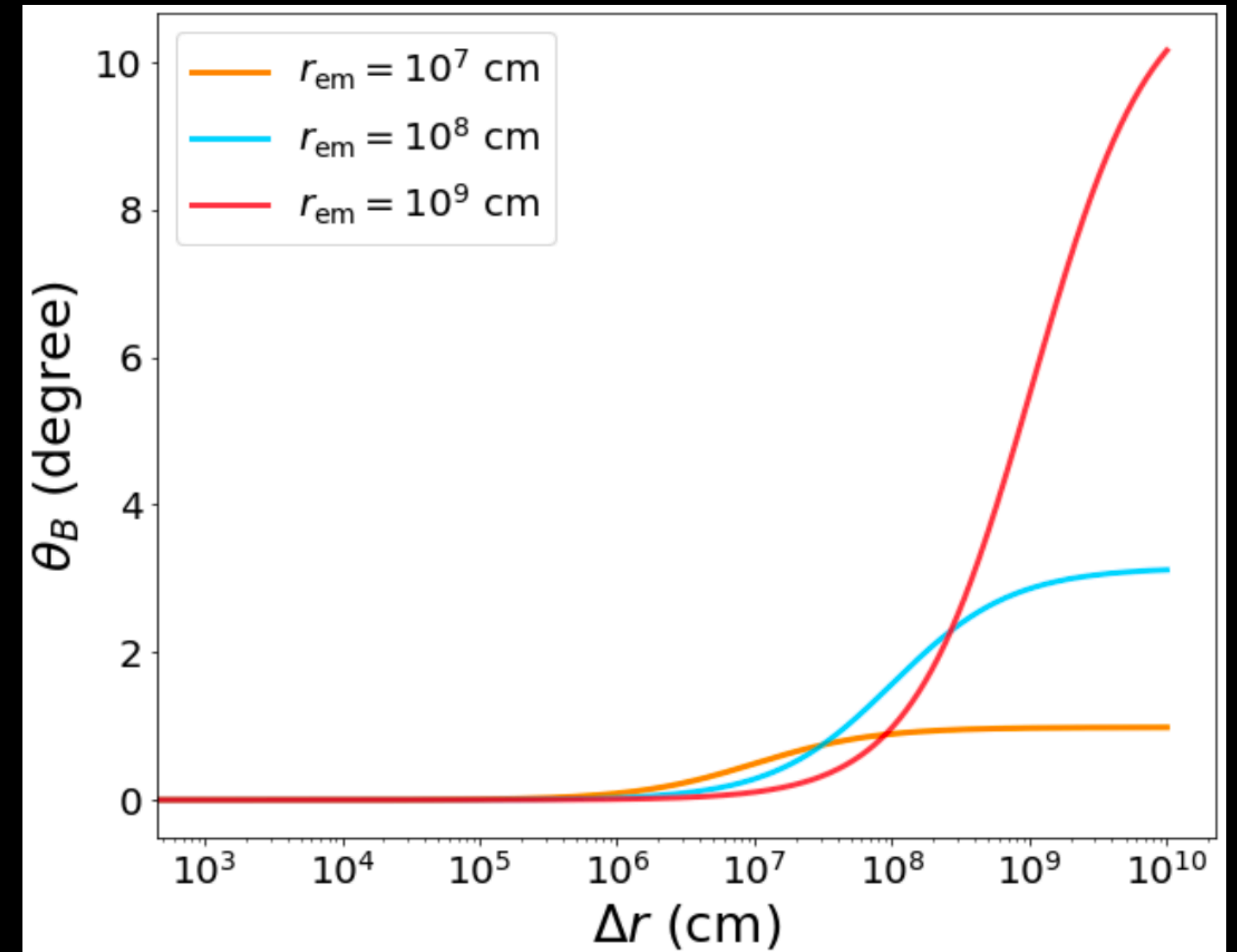
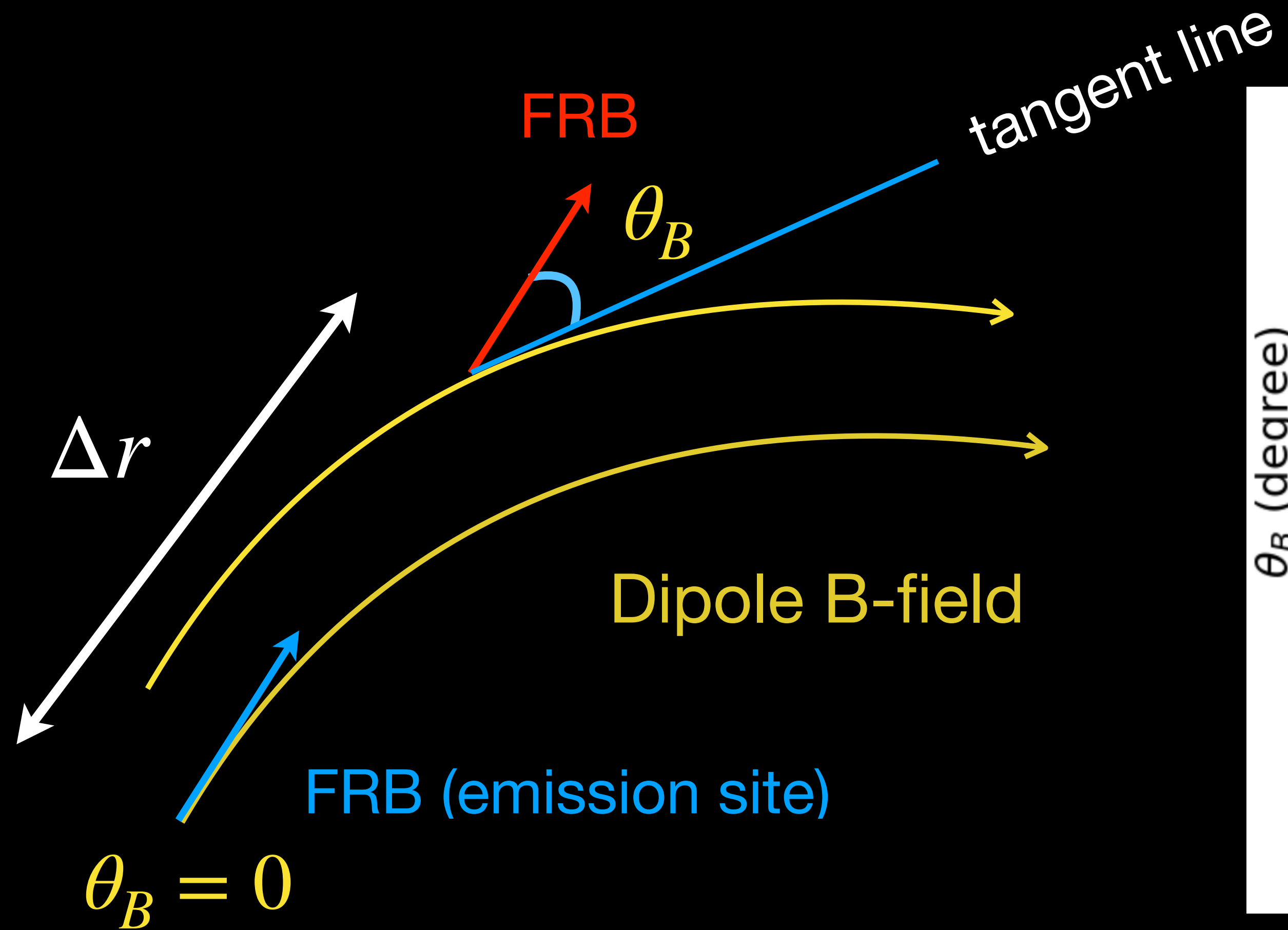
$\sim 4.8 \times 10^9$ cm

Light cylinder

Standard NS magnetosphere scenario

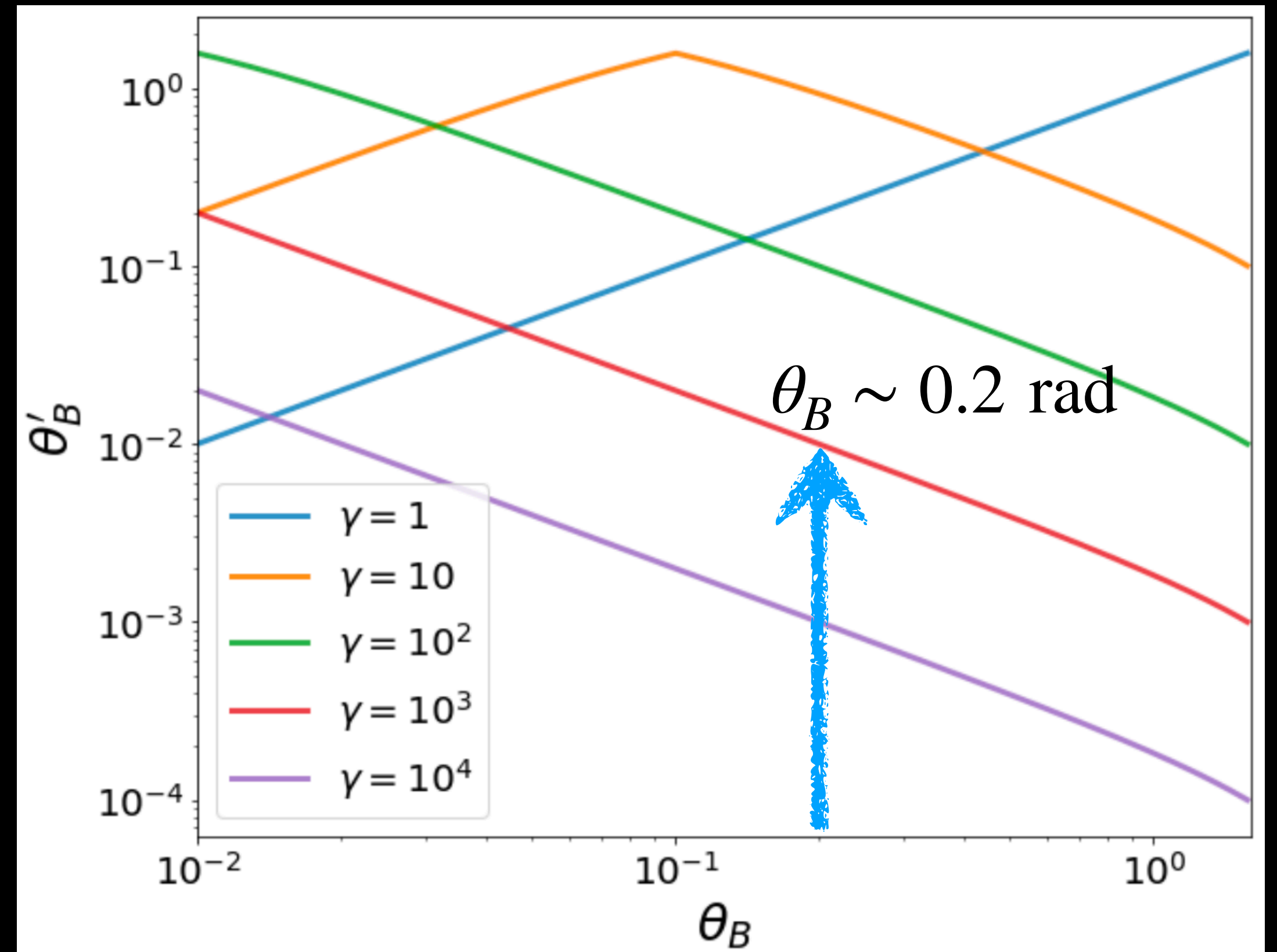
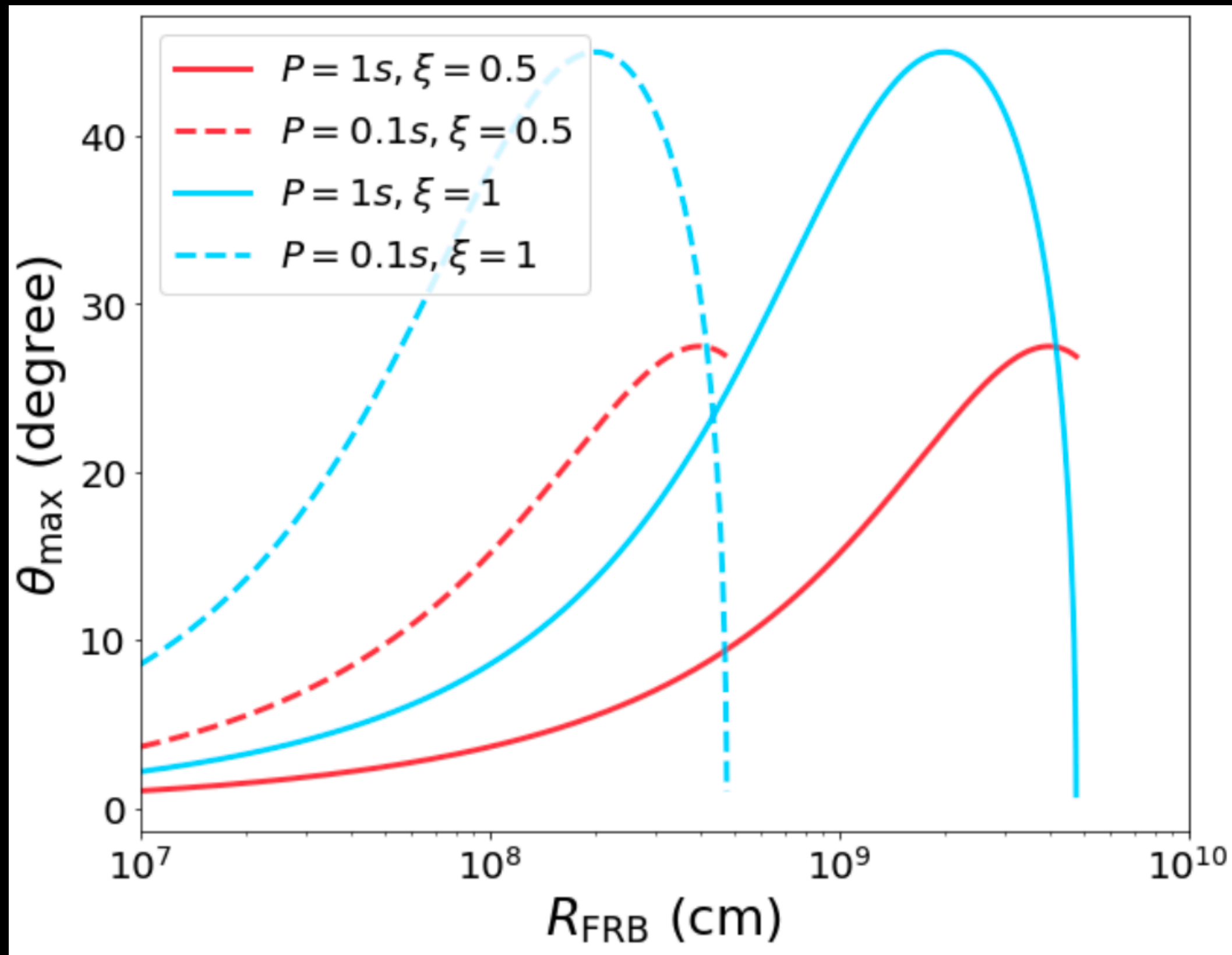


Angle between k-B is important to cross section



Qu, Kumar & Zhang 2022 (2204.10953)

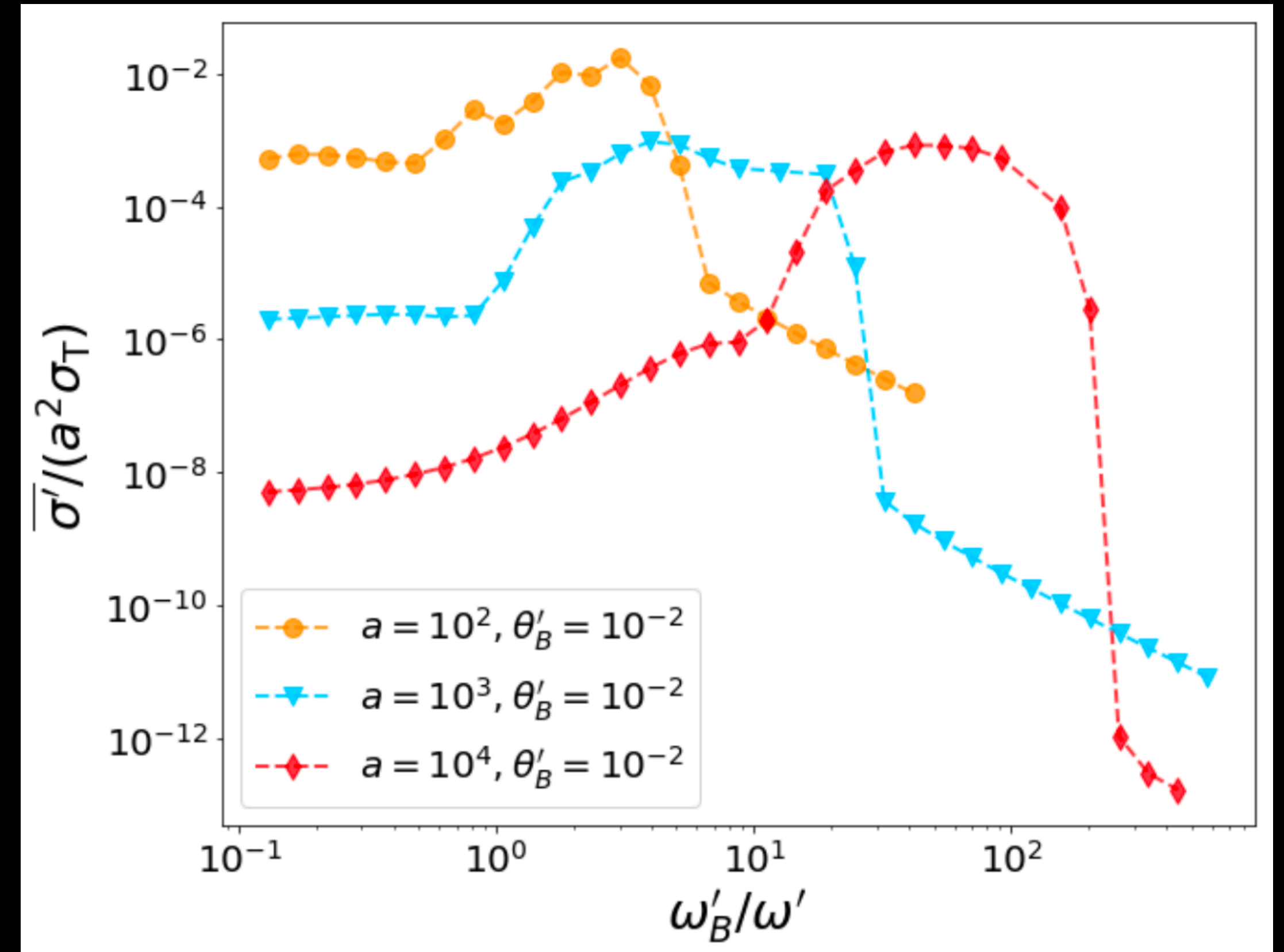
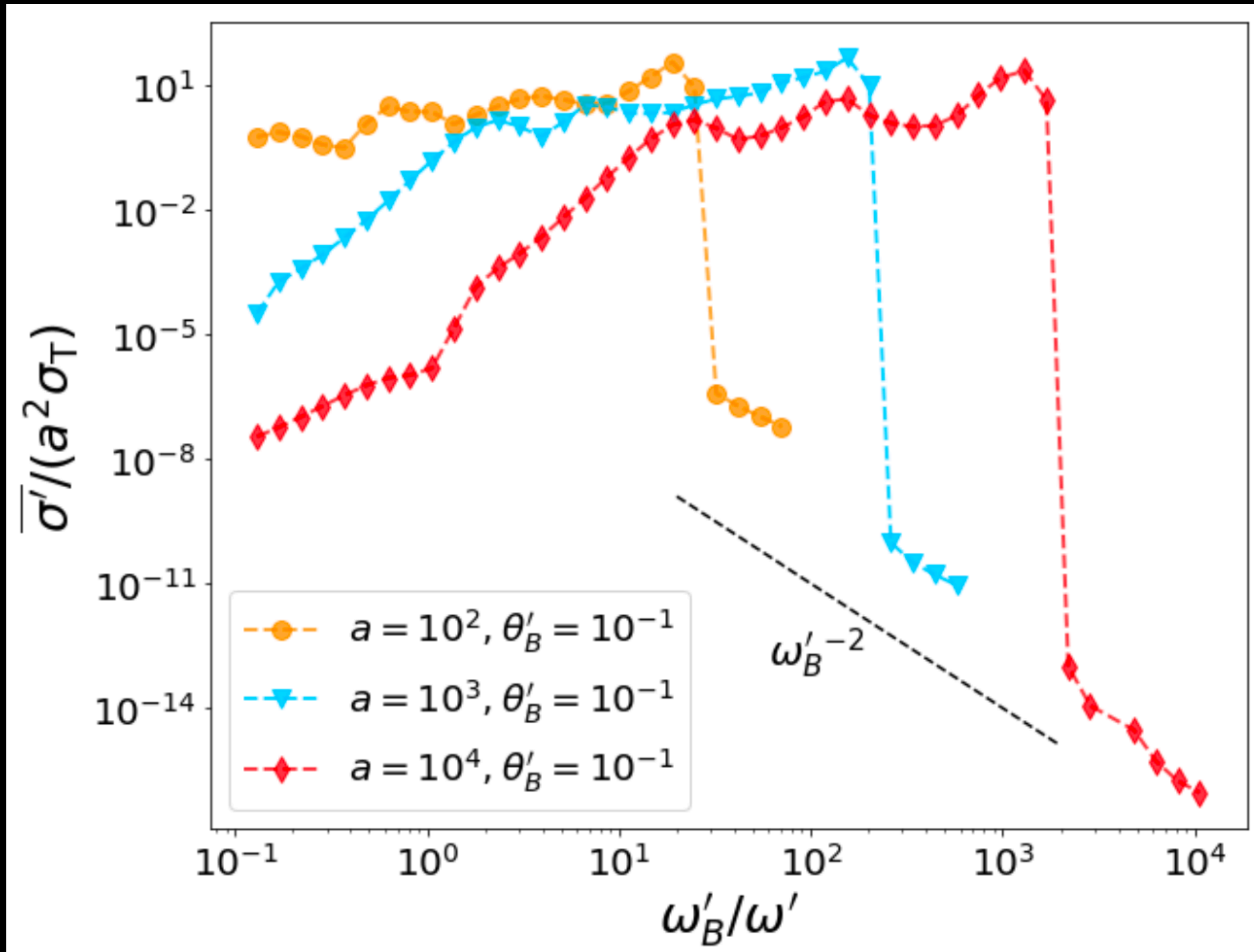
Fiducial value: $P = 1 \text{ s}$ $R_{\text{FRB}} = 10^8 \text{ cm}$ $\theta_{\text{max}} \sim 10 \text{ degree} \sim 0.2 \text{ rad}$



Maximum angle θ_B

Transformation to the plasma co-moving frame

Numerical Results

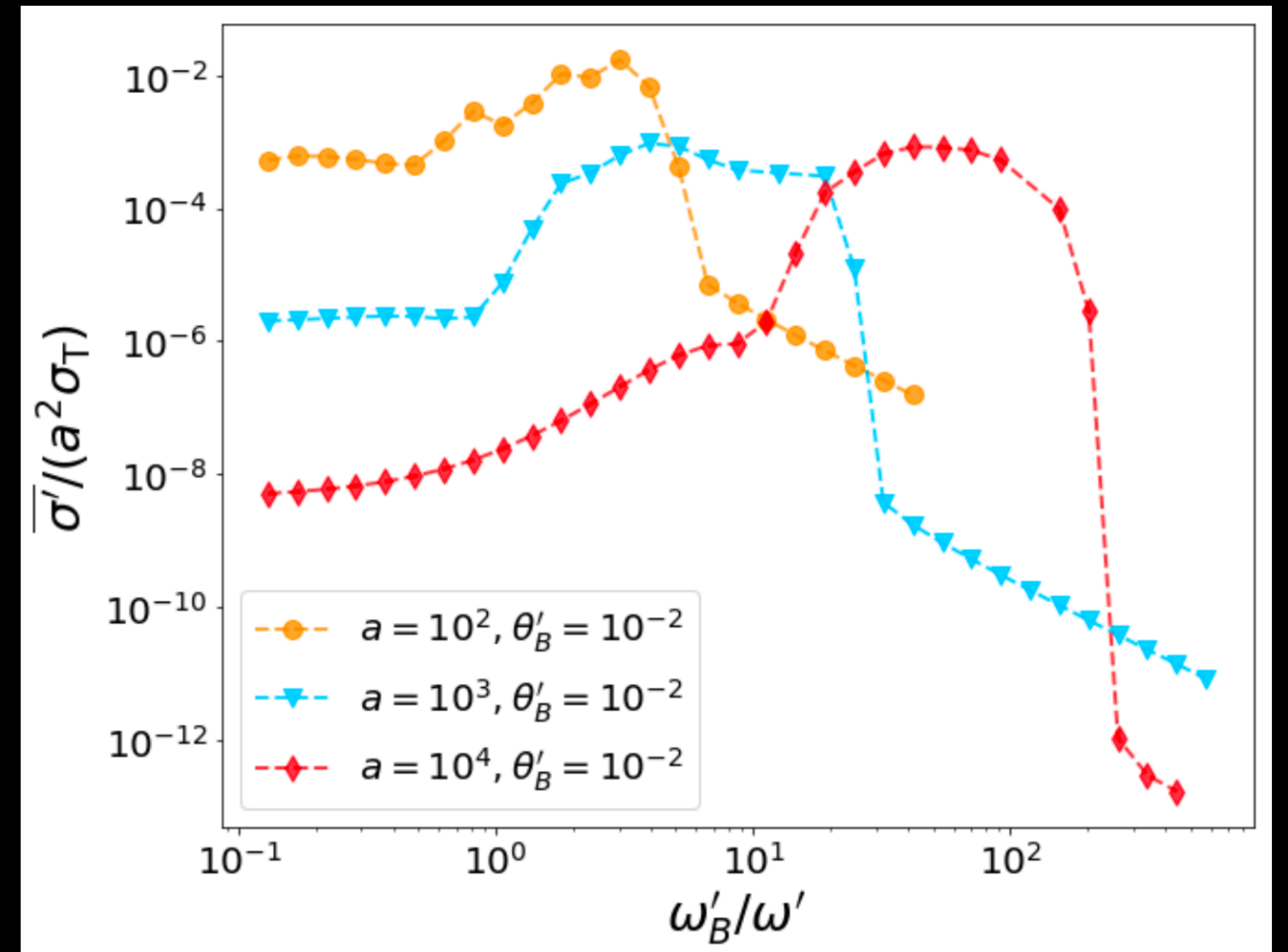
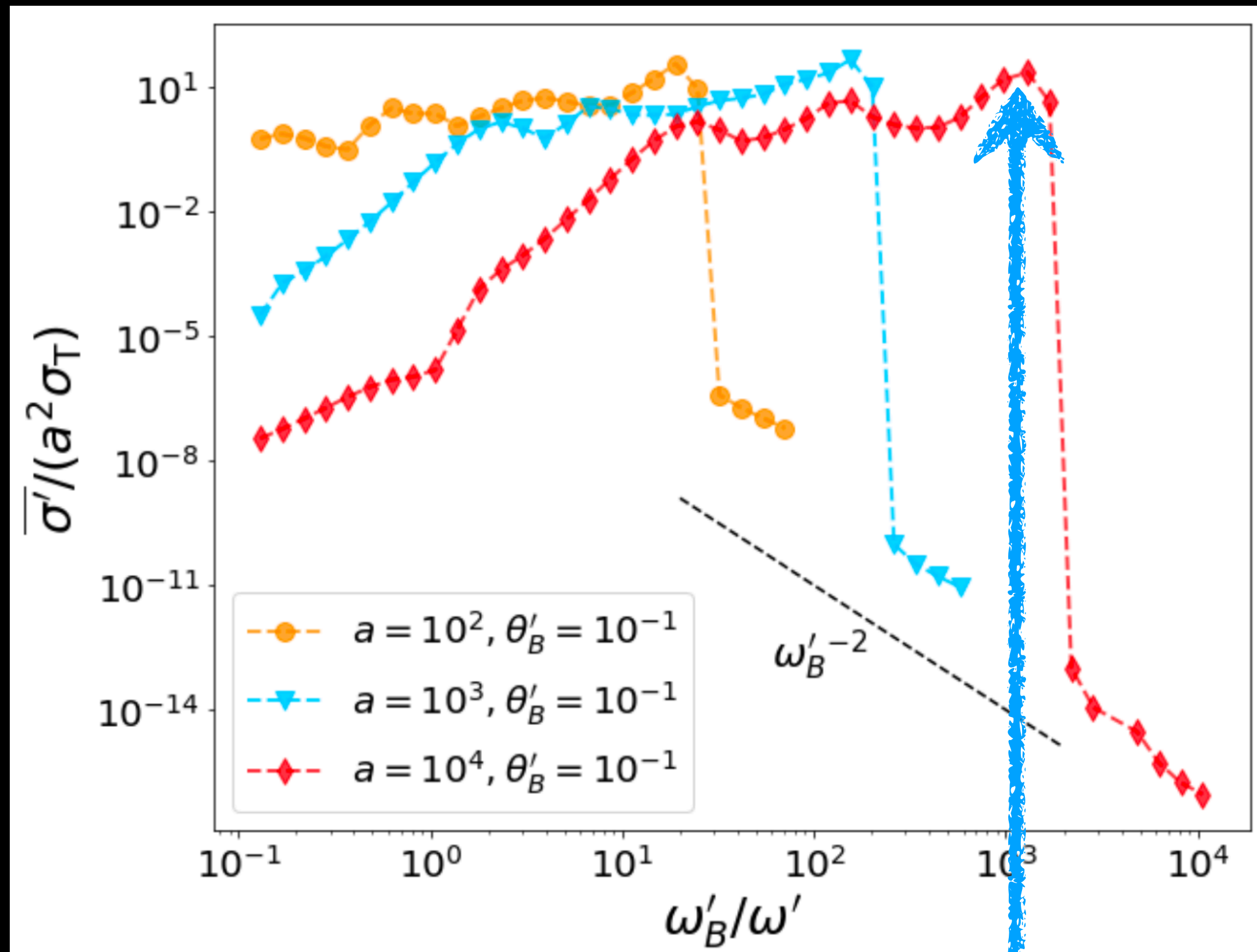


Qu, Kumar & Zhang 2022 (2204.10953)

Numerical Results

$$\theta'_B = 10^{-1} \text{ rad}$$

$$\theta'_B = 10^{-2} \text{ rad}$$

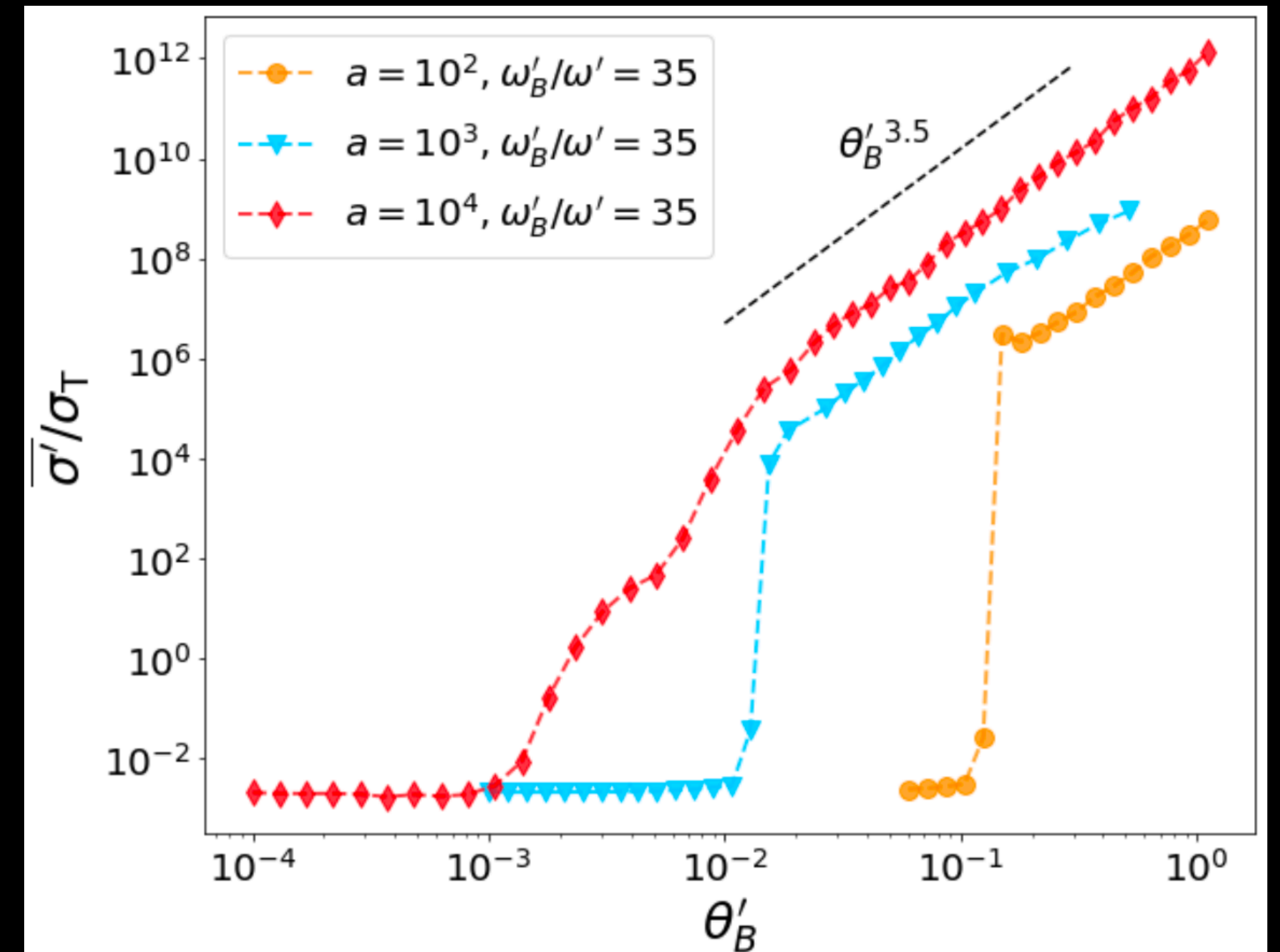
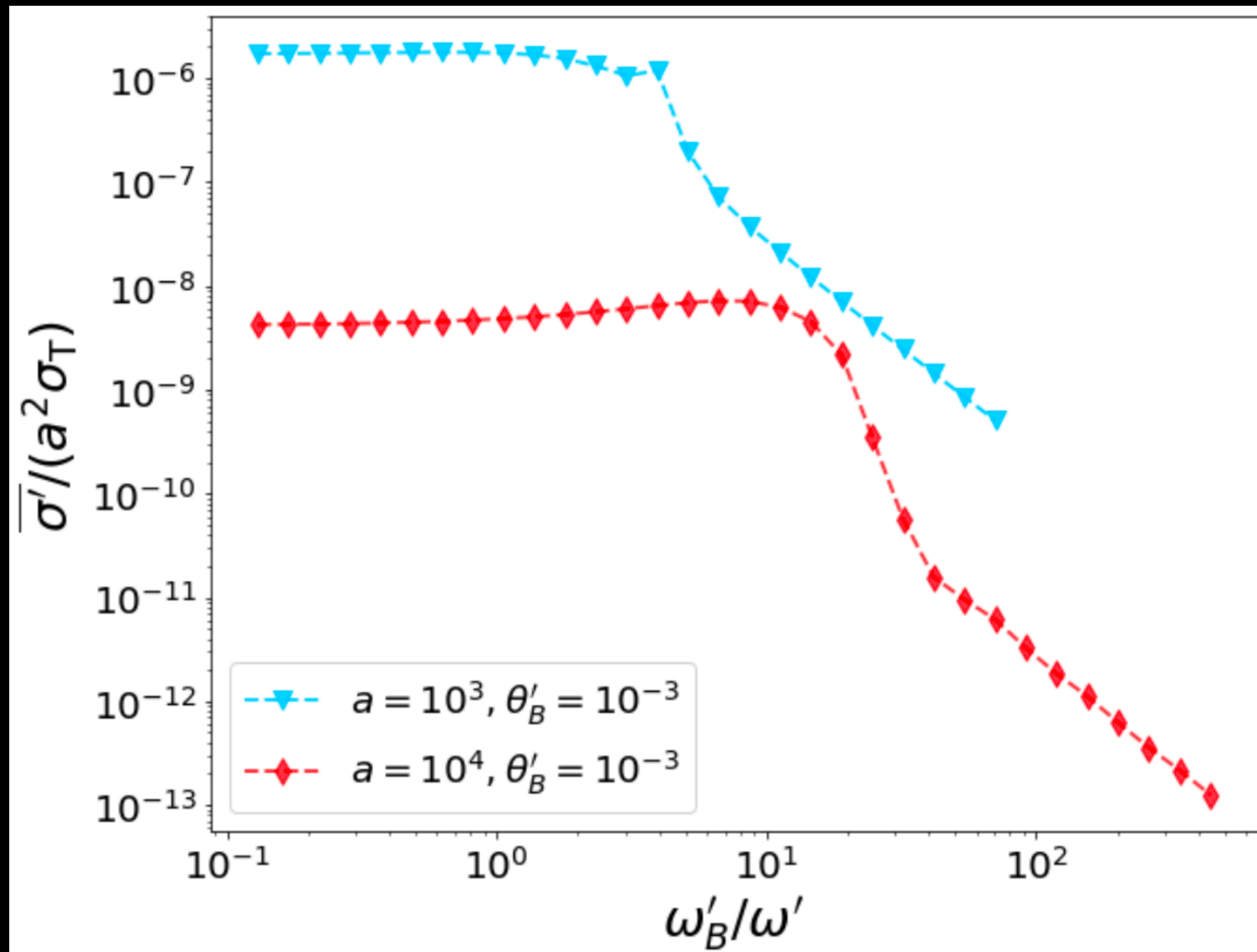


New turning point $\frac{\omega'_B}{\omega'} = a\theta'_B$

Numerical Results

$$\theta'_B = 10^{-3} \text{ rad}$$

$$\sigma' \sim \theta_B'^{3.5}$$



Smaller θ_B , smaller cross section

Within the magnetosphere

$$\omega_{\text{FRB}} \ll \omega_p \ll \omega_B$$

FRB can propagate freely

Emission point

r_{em}

FRB

$\sim 10^7 - 10^8 \text{ cm}$

Turning point

$\max(R_{\theta_B}, R_E)$

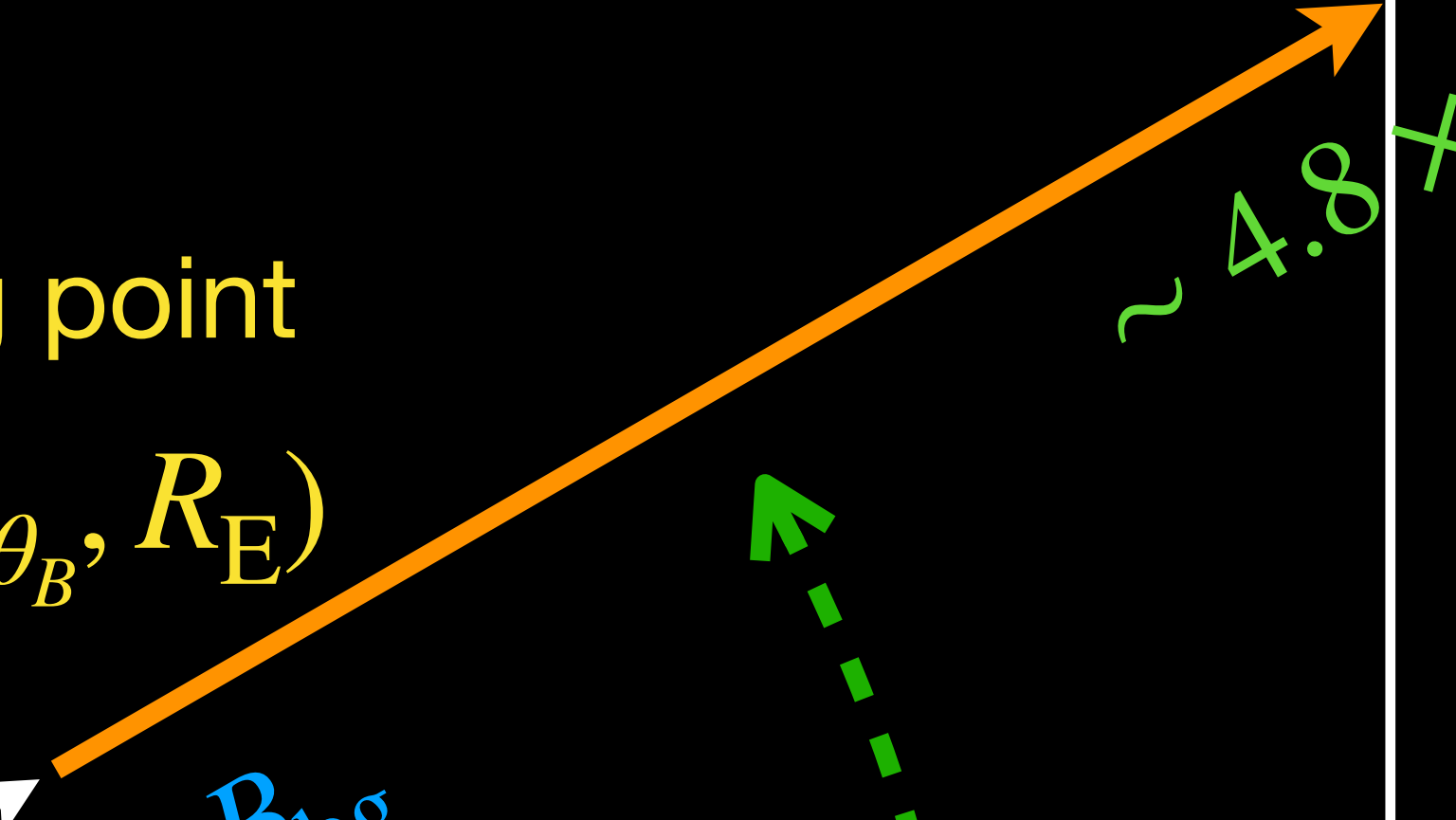
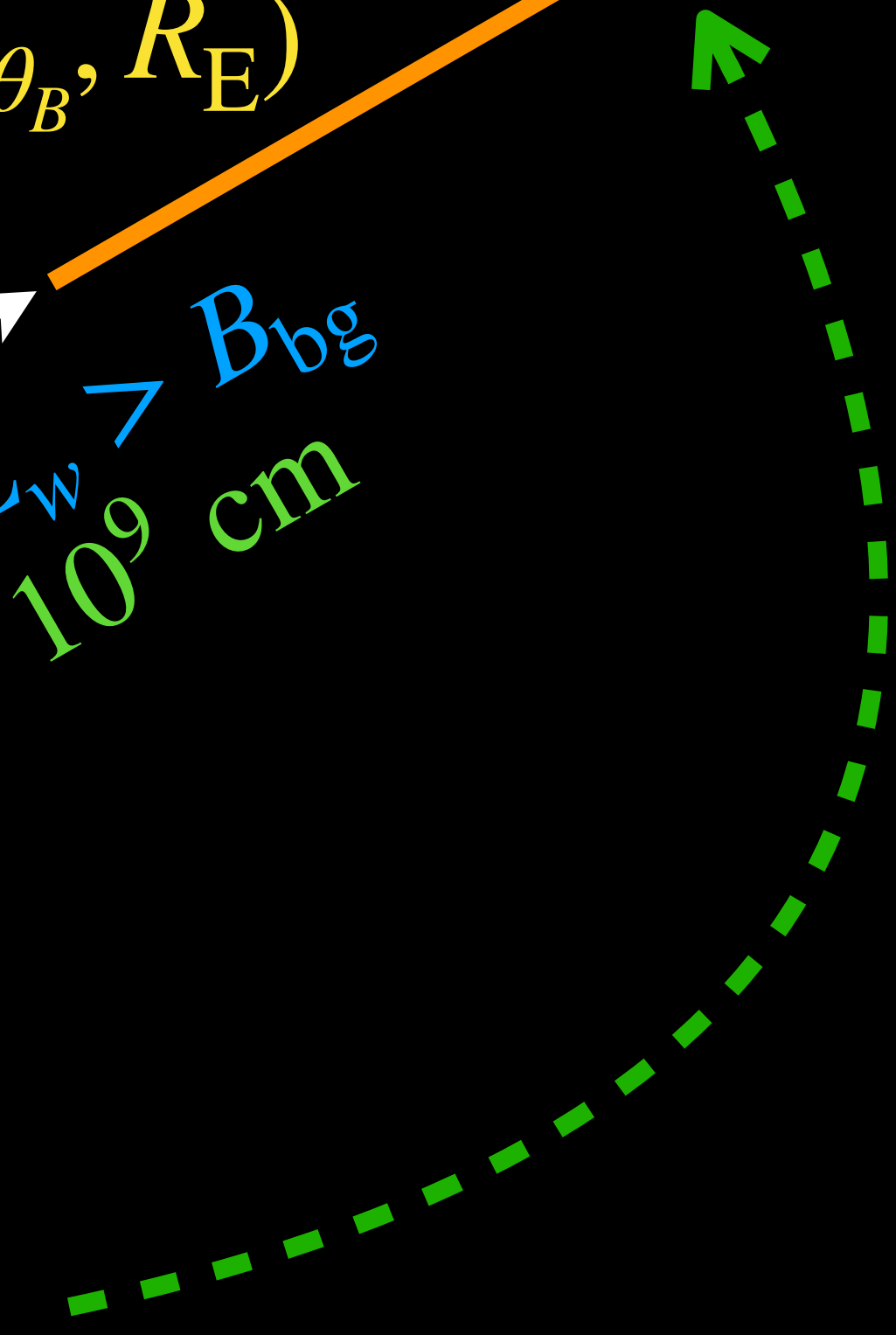
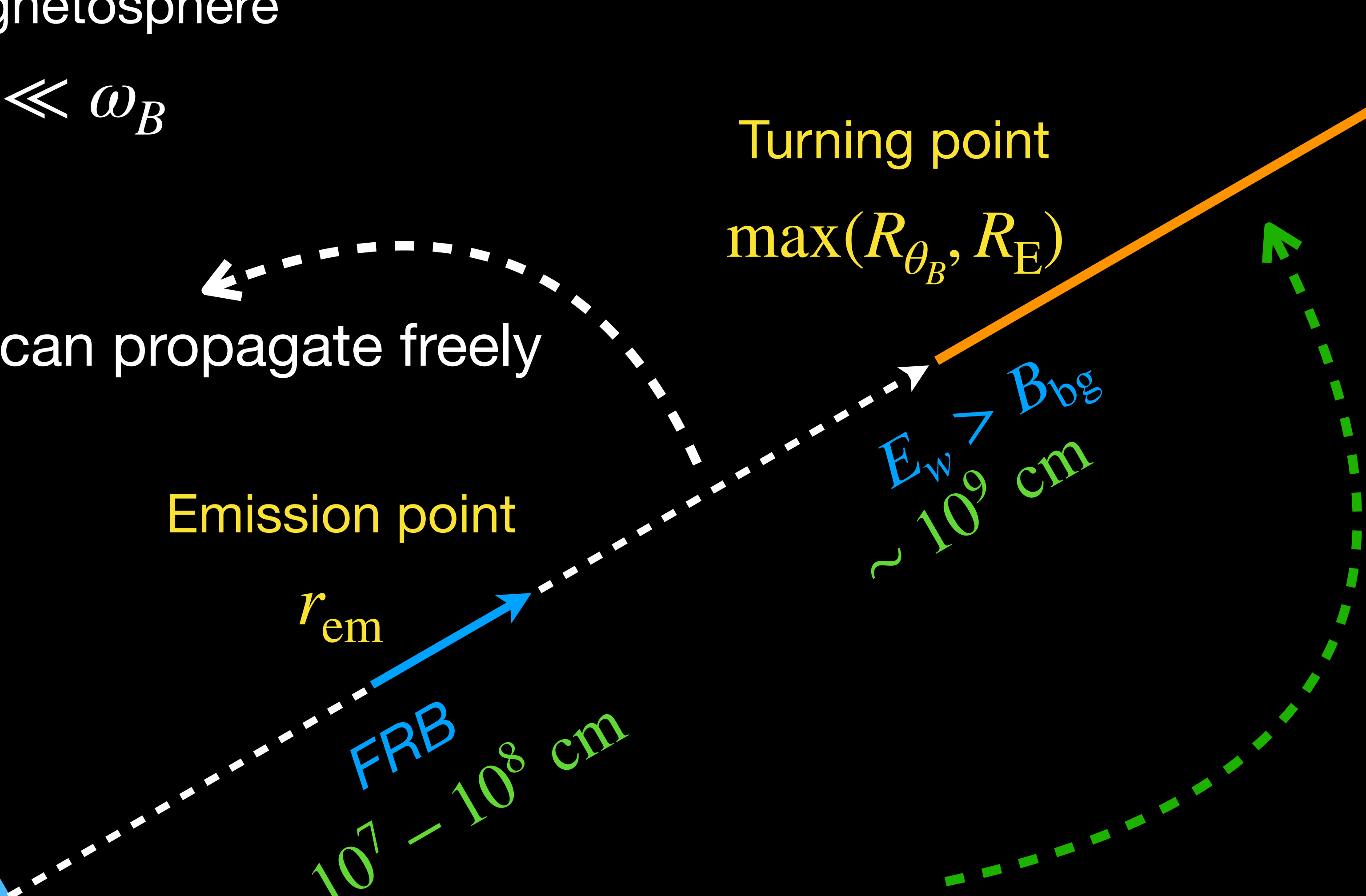
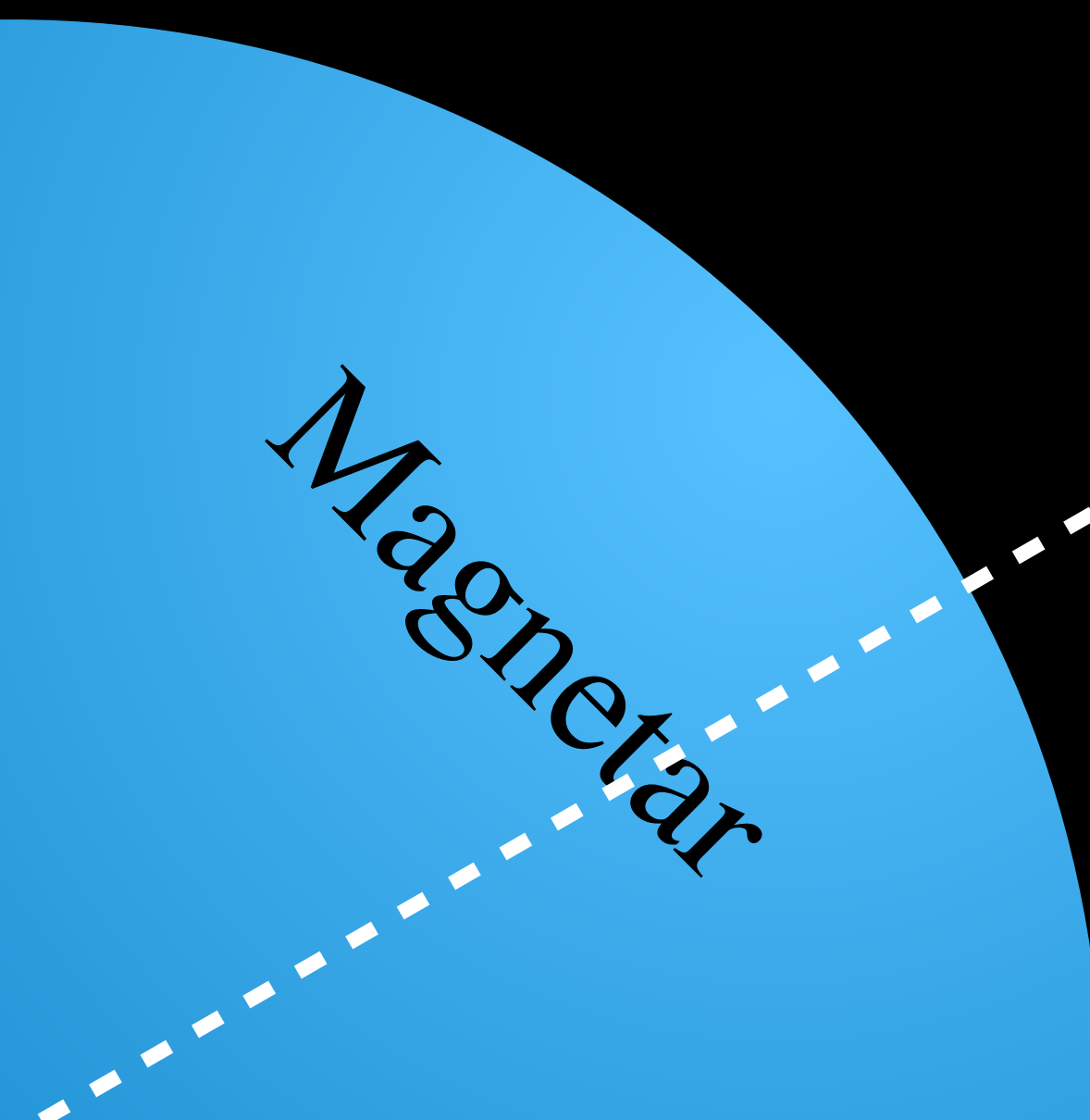
$E_w > B_{\text{bg}}$
 $\sim 10^9 \text{ cm}$

$\min(R_\omega, R_{\text{lc}})$

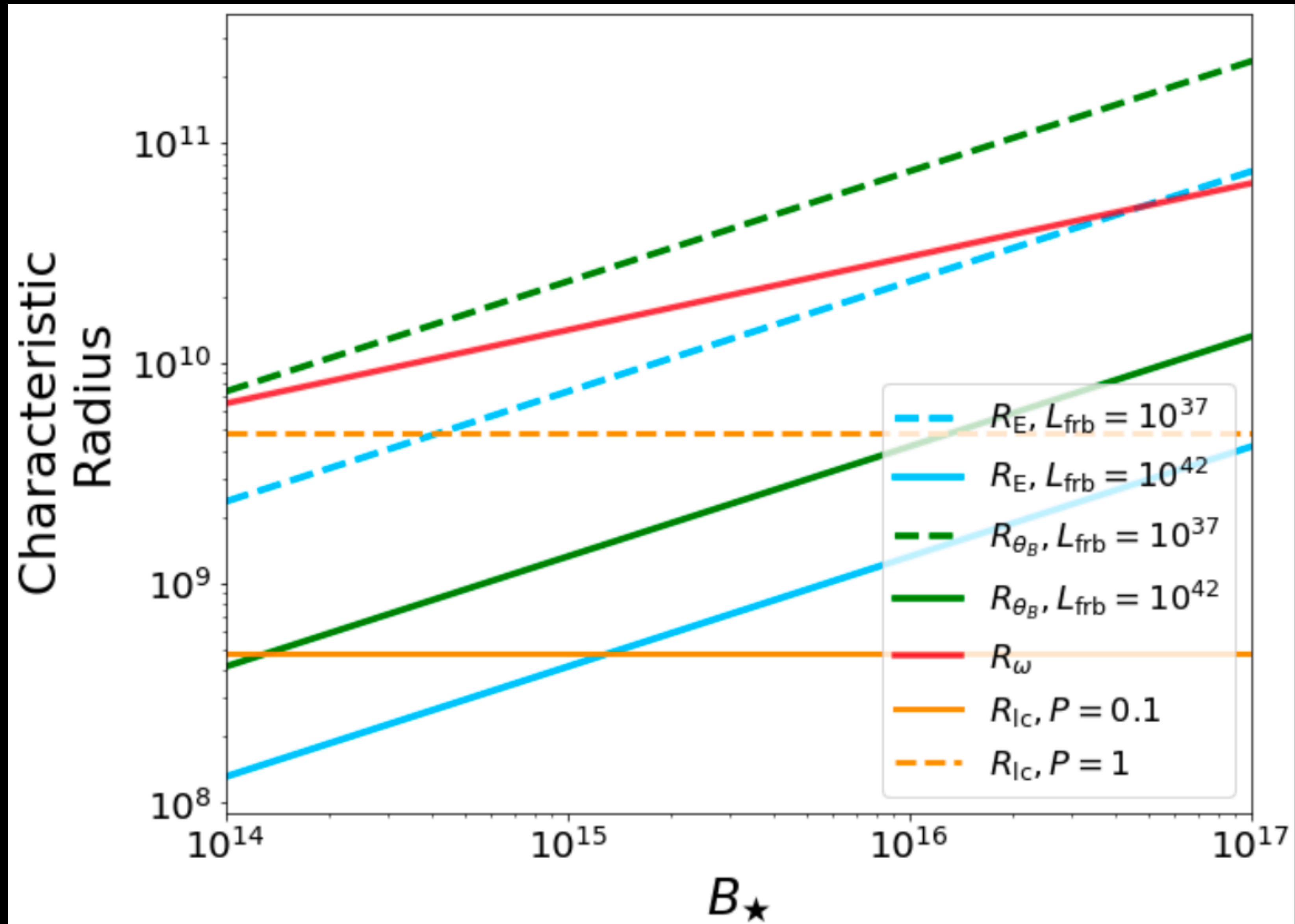
$\sim 4.8 \times 10^9 \text{ cm}$

Strong wave effect dominates!

Light cylinder



Characteristic radius

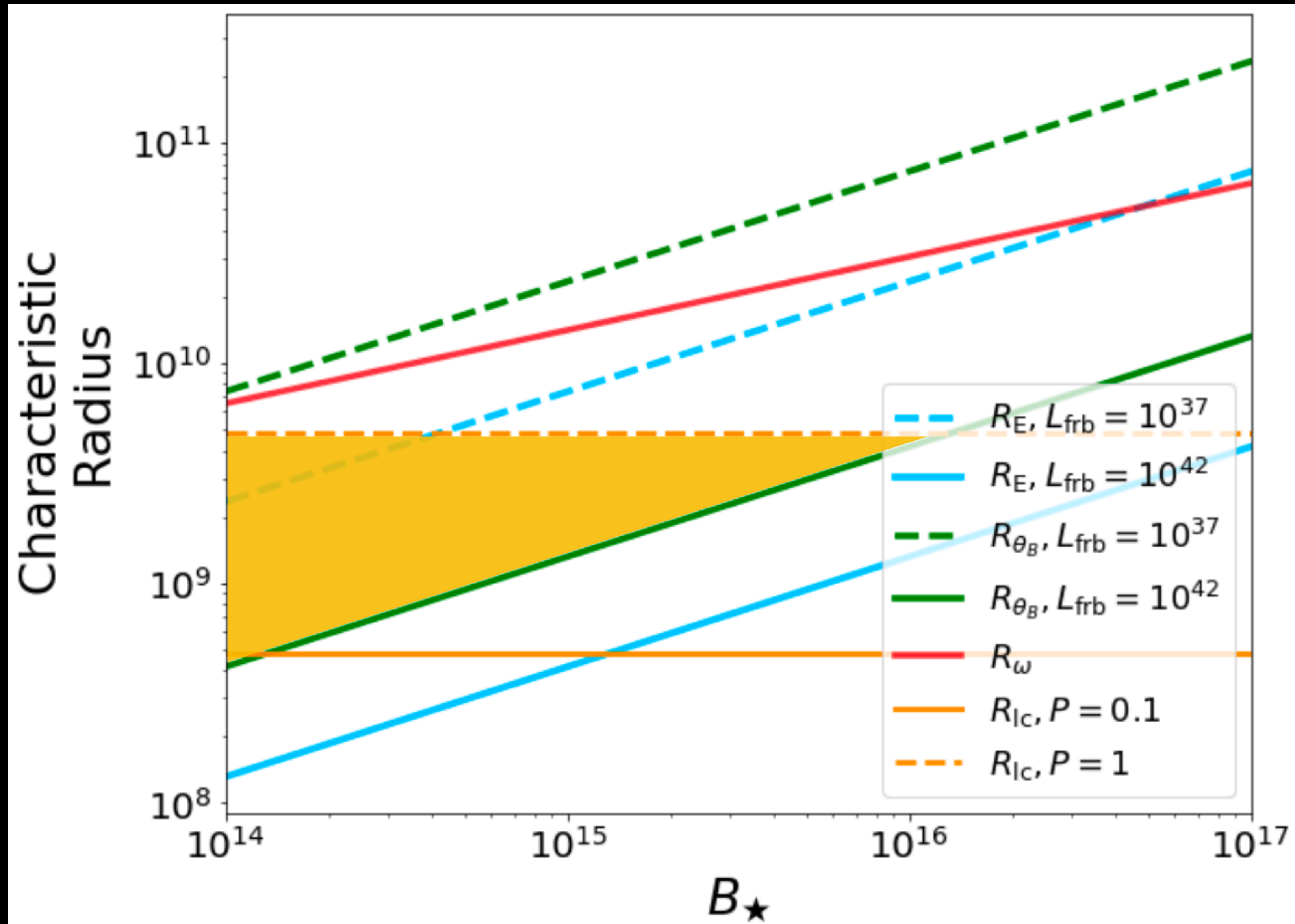


$$\max(R_E, R_{\theta_B}) \leq R \leq \min(R_\omega, R_{\text{lc}})$$

Characteristic radius

$$L_{\text{frb}} = 10^{42} \text{ erg s}^{-1}$$

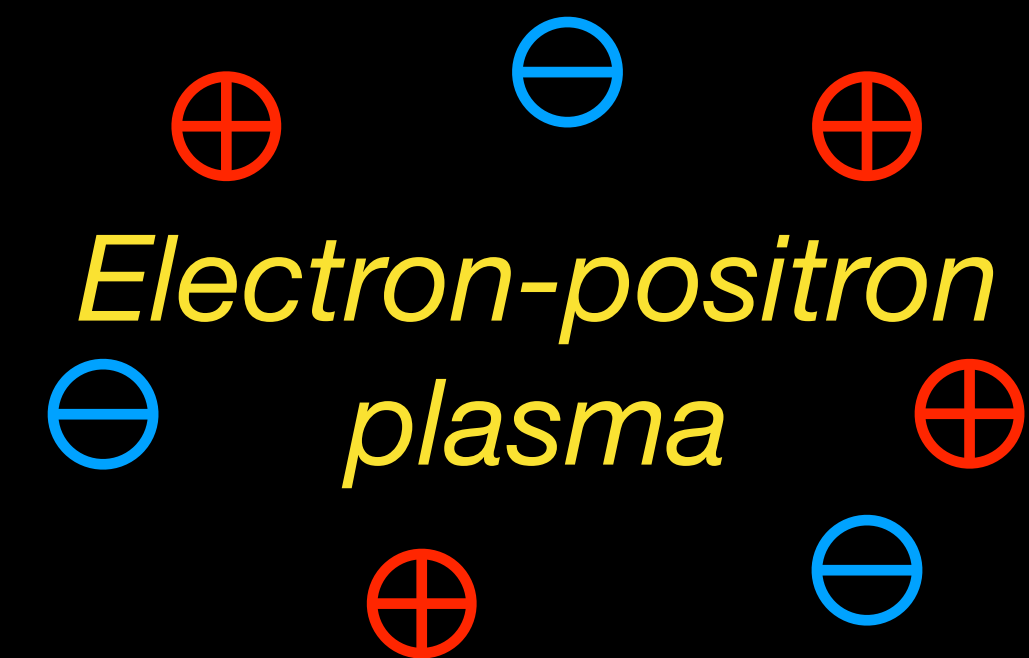
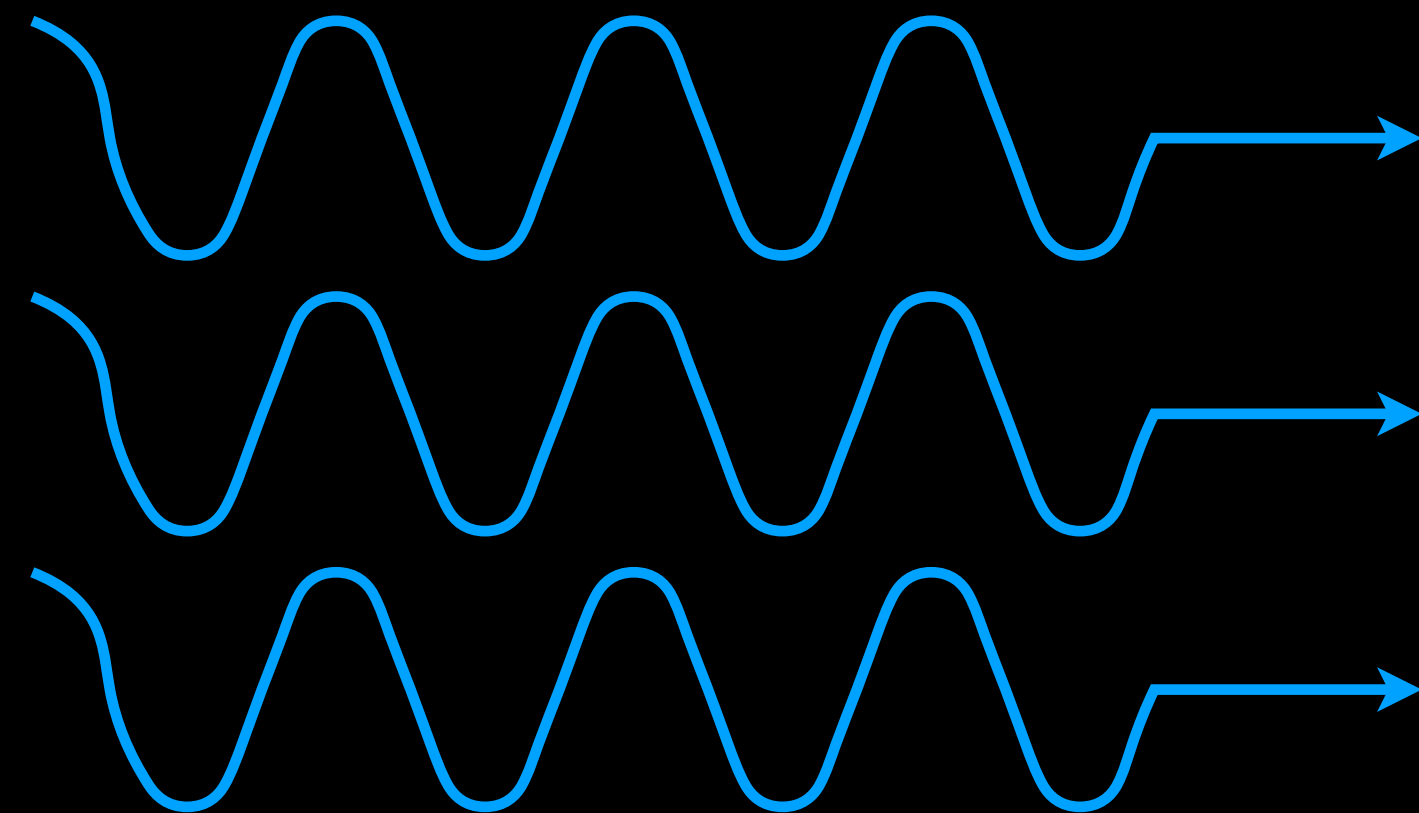
$$P = 1 \text{ s}$$



$$\max(R_E, R_{\theta_B}) \leq R \leq \min(R_\omega, R_{\text{lc}})$$

Estimation of maximum multiplicity

FRB pulse



FRB energy goes to pairs → *Curvature radiation*

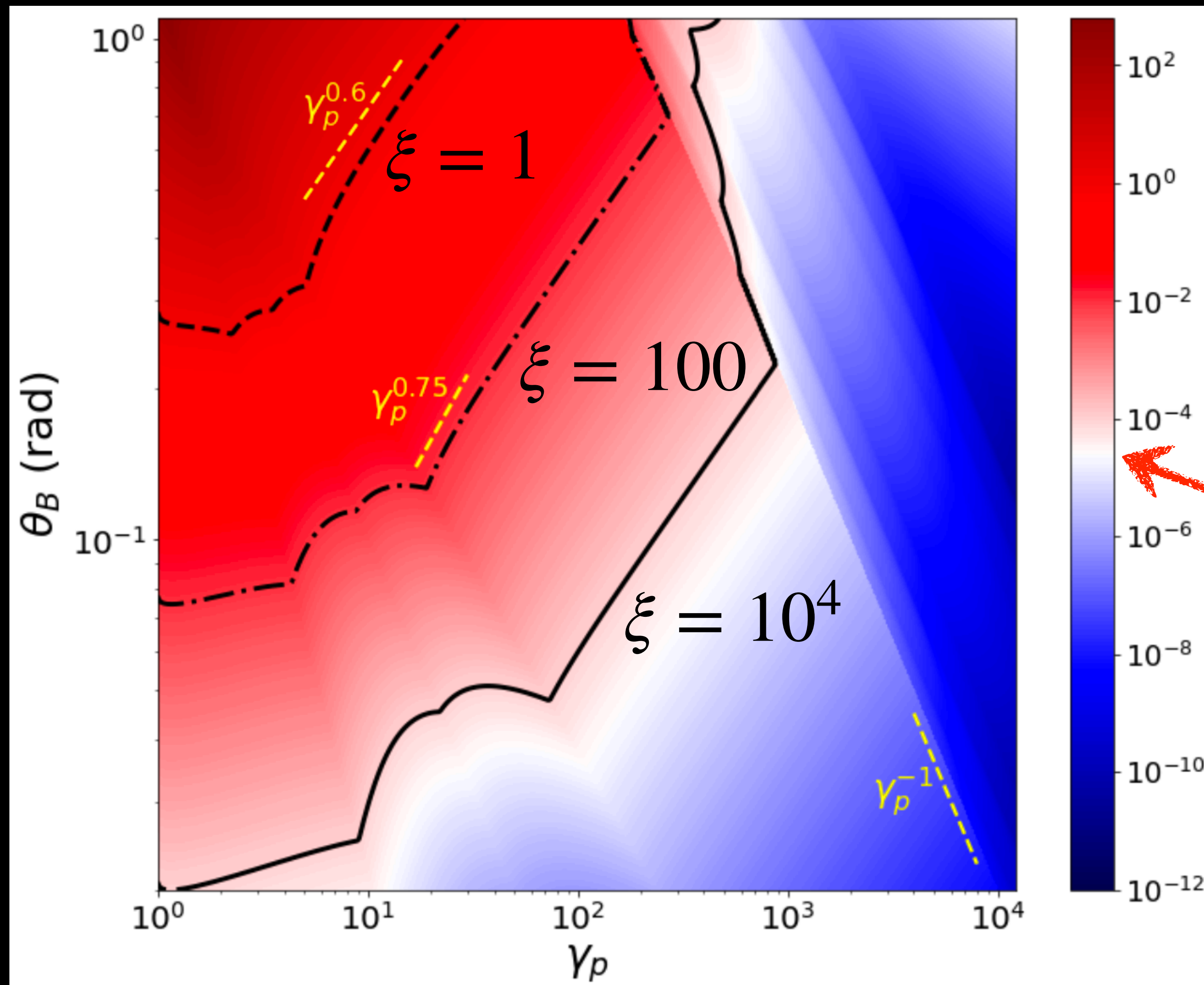


$\xi_{\max} = 10^4$ ← *Pair production*

Magnetar

Optical depth as a function of γ_p and θ_B

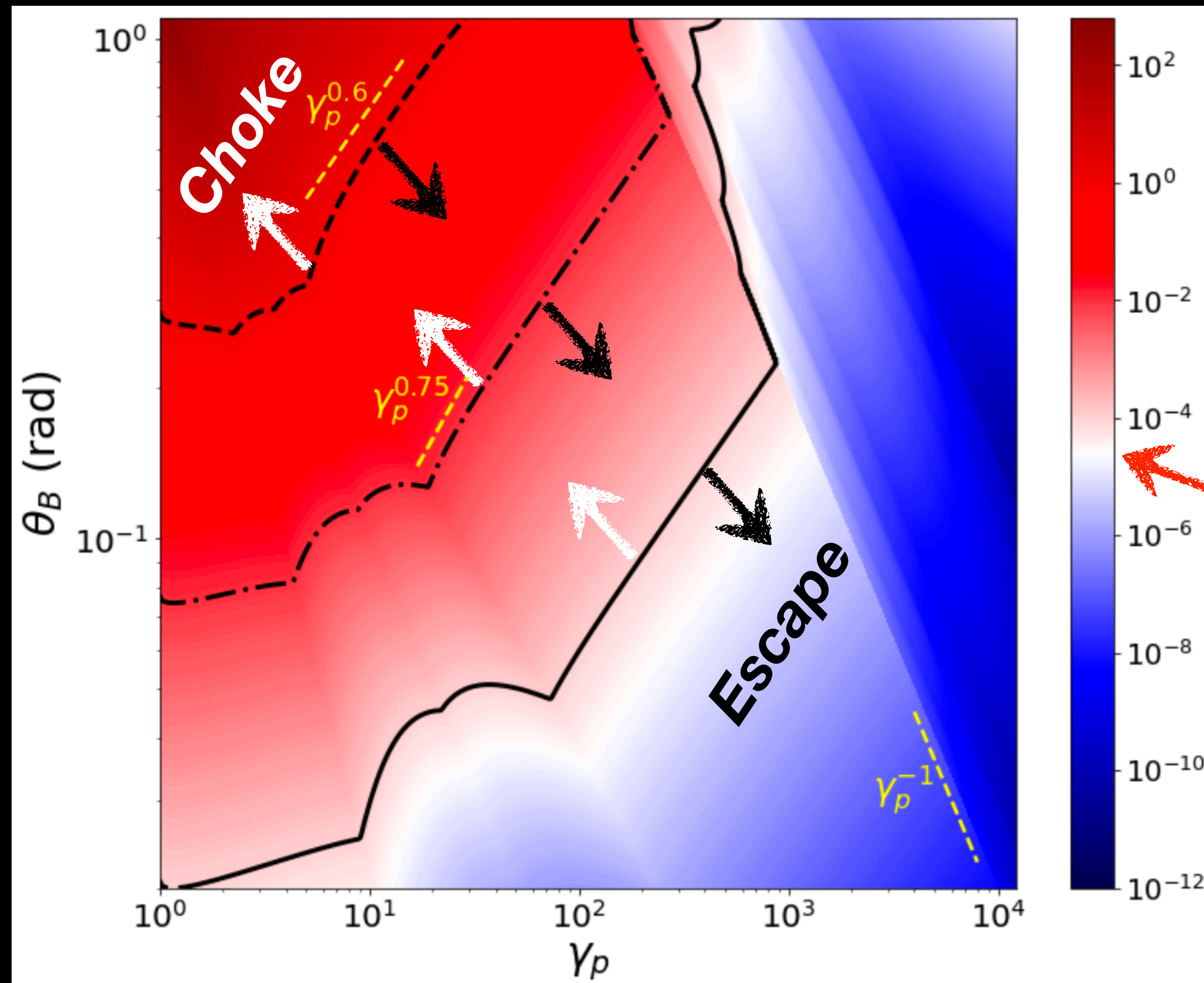
Transparency condition
 $\tau = 1$
(The three black lines)



optical depth

Optical depth as a function of γ_p and θ_B

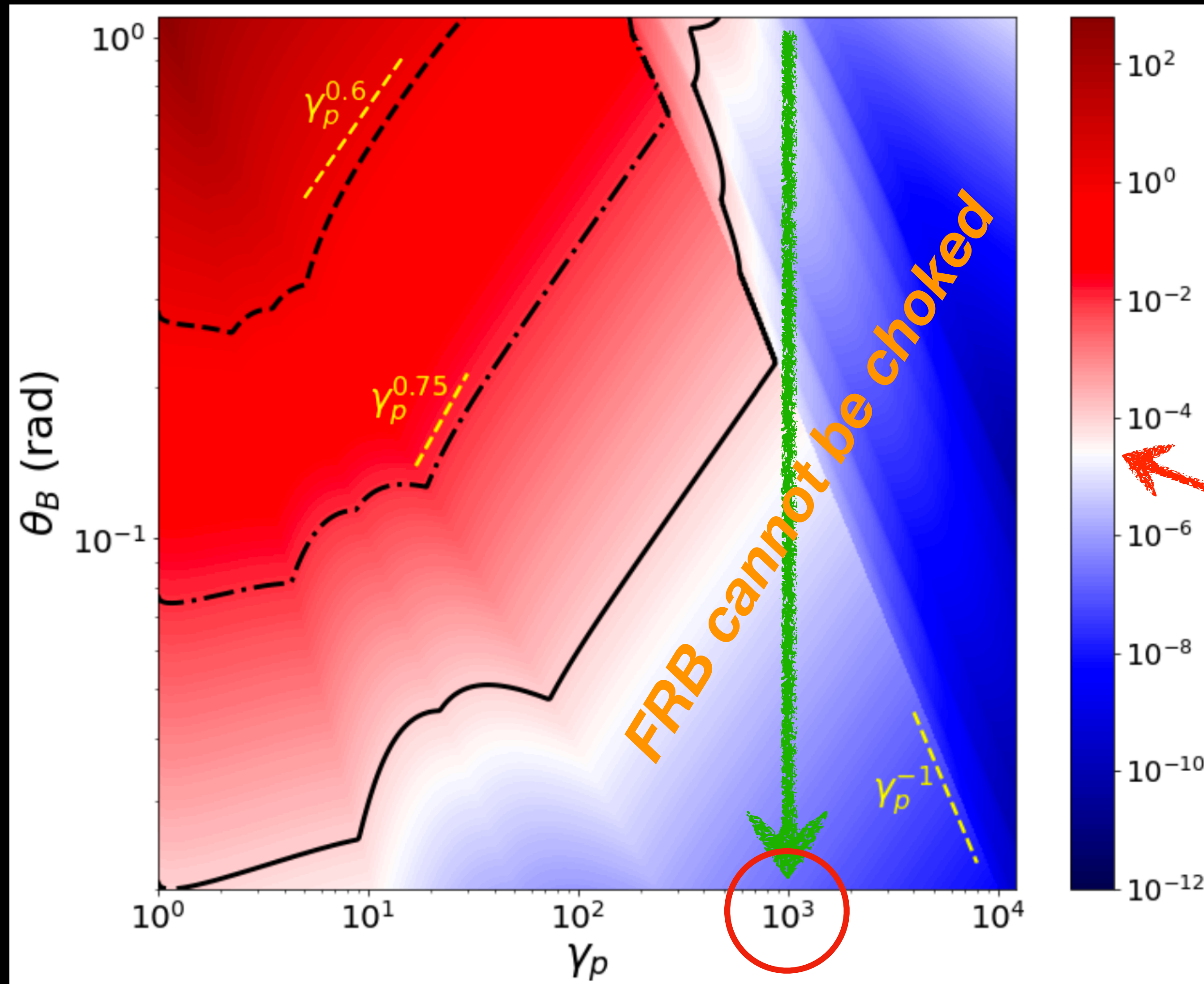
Transparency condition
 $\tau = 1$
(The three black lines)



optical depth

Optical depth as a function of γ_p and θ_B

Transparency condition
 $\tau = 1$
(The three black lines)



Summary

1. The detection or non-detection of neutrino may provide a diagnosis on the radio emission site in magnetars.
2. The plasma suppression effect can be ignored in the bunching mechanisms.
3. FRB can propagate freely in the magnetar magnetosphere.