

(Ultra-light) Cold Dark Matter and Dark Energy from α - attractors

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**Swagat Saurav Mishra, Senior Research Fellow
(SRF-CSIR),
Inter-University Centre for Astronomy and Astrophysics
(IUCAA), Pune, India.**

Ph.D. supervisor: Prof. Varun Sahni (IUCAA)

**Other Collaborators: Yuri Shtanov(BITP), Aleksey
Toporensky (Moscow State University), Satadru
Bag(IUCAA)**

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Coherent Oscillations of a Scalar Field

Action for a canonical scalar field minimally coupled to gravity

$$S[\varphi] = - \int d^4x \sqrt{-g} \left(\frac{1}{2} g^{\mu\nu} \partial_\mu \varphi \partial_\nu \varphi + V(\varphi) \right) \quad (1)$$

The equation of state (EOS) parameter is

$$w_\varphi = \frac{p_\varphi}{\rho_\varphi} = \frac{\frac{1}{2} \dot{\varphi}^2 - V(\varphi)}{\frac{1}{2} \dot{\varphi}^2 + V(\varphi)} \quad (2)$$

The equation of motion of the scalar field is given by

$$\ddot{\varphi} + 3H\dot{\varphi} + V'(\varphi) = 0. \quad (3)$$

For a scalar field coherently oscillating ($\dot{\varphi}/\varphi \gg H$) around $V(\varphi) \sim \varphi^{2p}$, the time average EOS is [Turner 1983]

$$\langle w_\varphi \rangle = \frac{p-1}{p+1} \quad (4)$$

Hence a scalar field oscillating around the minimum of any $V(\phi)$ having a φ^2 asymptote behaves like **Dark Matter (DM)**.

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- Emphasizing and removing enormous fine-tuning of initial conditions faced by the $m^2\varphi^2$ potential.
- α -attractors, originally proposed by [(Kallosh and Linde, 2013a, 2013b)] in the context of cosmic inflation, can have wider appeal in describing DM [**Mishra, Sahni and Shtanov, JCAP 2017 [arXiv:1703.03295]**] (and even DE **Bag, Mishra and Sahni 2017 [arXiv:1709.09193]** submitted).

Dark Matter

For the canonical massive scalar field potential

$$V(\varphi) = \frac{1}{2}m^2\varphi^2,$$

the expression for Jeans length is [Khlopov, Malomed and Zeldovich 1985; Hu, Barkana, Gruzinov 2000]

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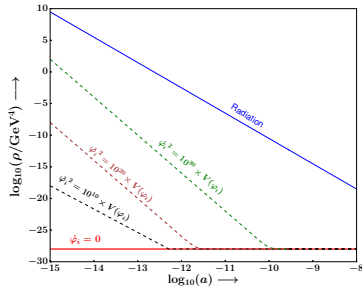
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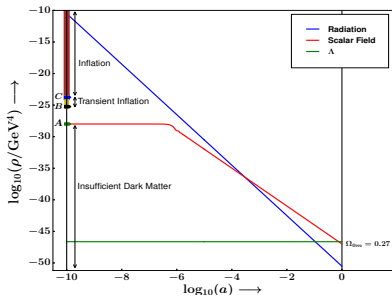
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The scalar field equation of motion is $\ddot{\varphi} + 3H\dot{\varphi} + V'(\varphi) = 0$. During the radiation dominated epoch $\rightarrow \varphi$ is frozen due to overdamping (like a cosmological constant until the Hubble parameter $H \geq m$)

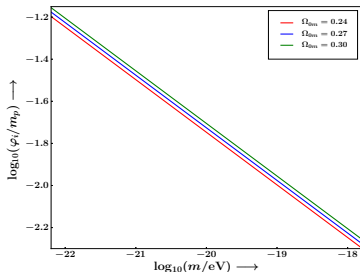


Fine-tuning problem associated with $V(\varphi) = \frac{1}{2}m^2\varphi^2$

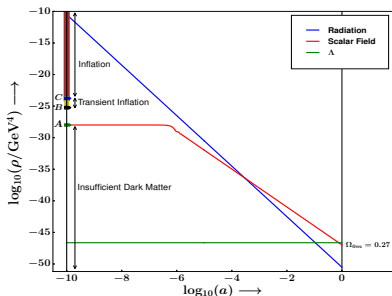


Only a particular given value of φ_i yields $\Omega_{0m} = 0.27$ at the present epoch. These results support the earlier findings of [Zlatev and Steinhardt 1999].

$$\varphi_i = (0.06 m_p) \times \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1/4}$$



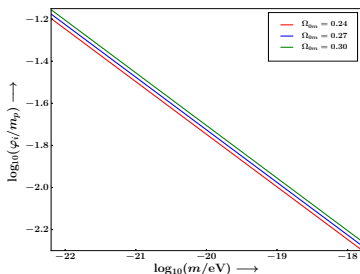
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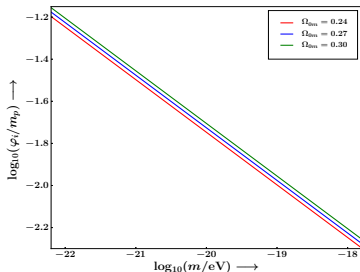
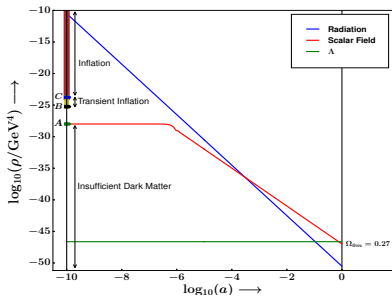
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The general form of α -attractor potentials can be written as [[Kallos and Linde 2013b](#)]

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- 1 The asymmetric *E-Model* [Kallosh and Linde 2013a]

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- 2 The tracker-potential [[Sahni and Wang, 2000](#)]

$$V(\varphi) = V_0 \sinh^2 \sqrt{\frac{2}{3\alpha}} \frac{\varphi}{m_p}. \quad (7)$$

Dark Matter from the *E-Model*

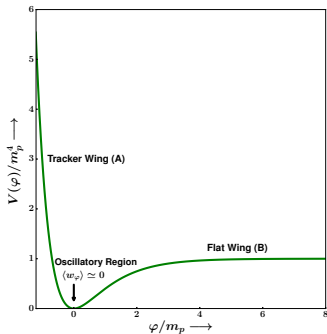
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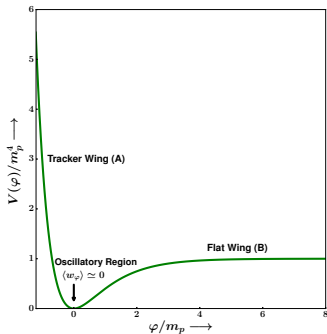
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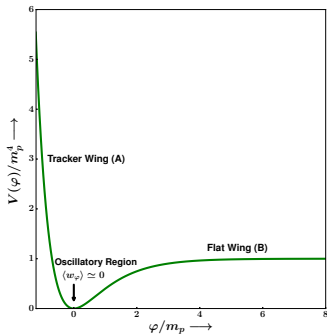
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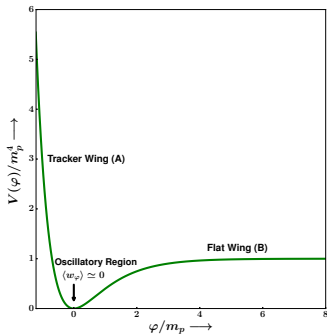
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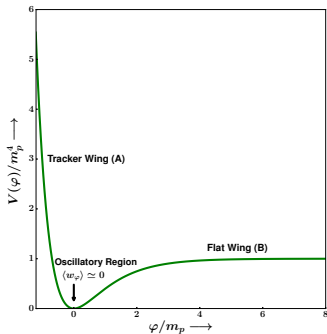
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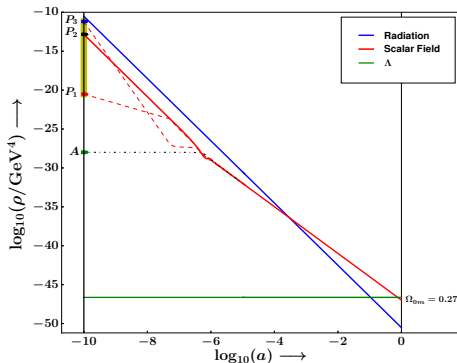
where $m^2 = \frac{2V_0\lambda^2}{m_p^2}$, $\lambda = \sqrt{\frac{2}{3\alpha}}$
and the Scaling solution obeys

$$\Omega_\varphi = \frac{3(1 + w_B)}{\lambda^2} = \frac{4}{\lambda^2}, \quad w_\varphi = w_B = \frac{1}{3}$$

Attractor Behaviour the E -Model

For $m = 10^{-22}$ eV, $\lambda = 14.5$ ($\alpha = 3.2 \times 10^{-3}$),
 $V_0 = 1.37 \times 10^{-28}$ GeV⁴, $z_{osc} \simeq 2.8 \times 10^6$

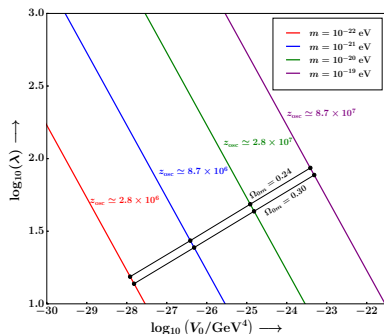
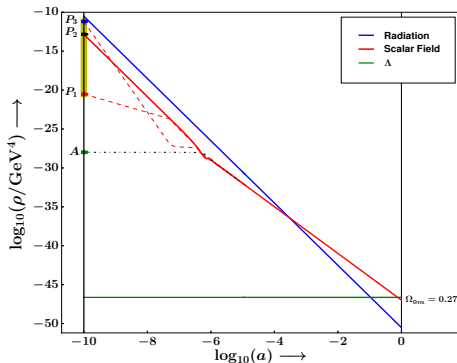
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- 2 For the tracker-potential (7), which has the asymptote $V(\varphi) \sim \frac{1}{2}m^2\varphi^2 + \frac{\lambda}{4}\varphi^4$, the Jeans scale is given by [Johnson and Kamionkowski 2008]

$$k_J^2 = -\frac{3}{2}\lambda^2\rho + \left[\left(\frac{3}{2}\lambda^2\rho \right)^2 + \rho \frac{m^2}{m_p^2} \right]^{1/2} , \quad (12)$$

where $m^2 = \frac{2V_0\lambda^2}{m_p^2}$.

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- ① For small oscillations around the minimum of the asymmetric *E-Model* potential which has the asymptote $V(\varphi) \sim \frac{1}{2}m^2\varphi^2 - \frac{1}{3}\mu\varphi^3 + \frac{\lambda}{4}\varphi^4$, the Jeans scale is given by [**Mishra, Sahni and Shtanov JCAP 2017**]

$$k_J^2 = \left(\frac{5}{3} \frac{\mu^2 \rho}{m^4} - \frac{9}{4} \frac{\lambda_0 \rho}{m^2} \right) + \left[\frac{2m^2}{m_p^2} \rho + \left(\frac{25}{9} \frac{\mu^4}{m^8} + \frac{81}{16} \frac{\lambda_0^2}{m^4} - \frac{15}{2} \frac{\lambda_0 \mu^2}{m^6} \right) \rho^2 \right]^{\frac{1}{2}}$$

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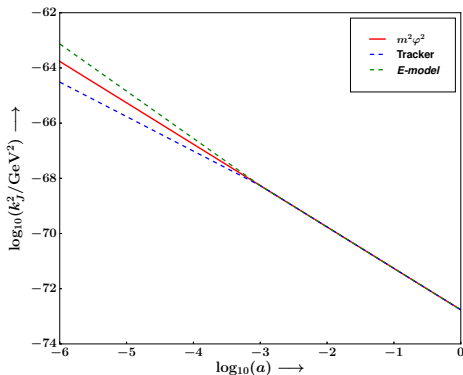
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The figure below shows that k_J^2 in all three models converge to that of the $\frac{1}{2}m^2\varphi^2$ model at late enough times (i.e by $z \sim 10^3$).

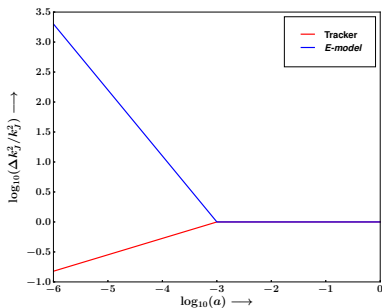
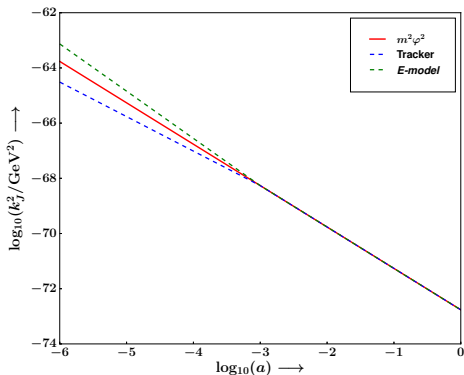
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We notice that the differences between the value of k_J^2 in all three models decrease rapidly and they all converge to that of the $\frac{1}{2}m^2\varphi^2$ model at late enough times (i.e by $z \sim 10^3$).



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- Our analysis of gravitational instability demonstrates that, despite significant differences in dynamics, the Jeans scale in all of our DM models converges to the same late-time expression.

Discussion and further plans

- Canonical scalar field potential for DM $V(\varphi) \simeq \frac{1}{2}m^2\varphi^2$ suffers from severe fine-tuning problem of initial conditions. (This problem also appears in axionic dark matter.)
- This difficulty is easily avoided if dark matter is sourced by α -attractors possessing at least one tracker wing like the *E-model* and the tracker potential where one arrives at the late-time dark matter asymptote from a very wide range of initial conditions.
- Our analysis of gravitational instability demonstrates that, despite significant differences in dynamics, the Jeans scale in all of our DM models converges to the same late-time expression.
- Observational Signatures - Matter power spectrum, Pulsar Timing Array, Gravitational Waves (Future Work), CMB and BAO phases.

$$\text{Strain } h_c = 2 \times 10^{-16} \left(\frac{10^{-22} \text{ eV}}{m} \right)^2,$$

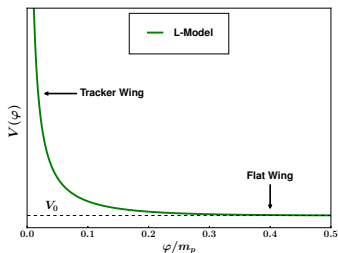
$$\text{Frequency } f_c = 50 \times 10^{-9} \left(\frac{m}{10^{-22} \text{ eV}} \right) \text{ Hz}$$

Important References

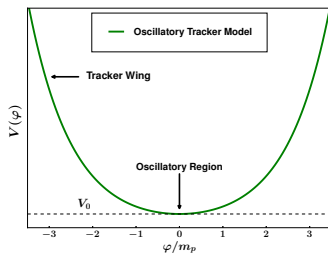
- 1 "Cold and fuzzy dark matter", W. Hu, R. Barkana and A. Gruzinov, Phys. Rev. Lett. 85 (2000) 1158 [astro-ph/0003365].
- 2 "Ultralight scalars as cosmological dark matter", L. Hui, Ostriker, S. Tremaine and Ed. Witten, Phys. Rev. D 95 (2017) 043541 [arXiv:1610.08297].
- 3 "Sourcing DM and DE from α -attractors", S.S Mishra, V. Sahni and Y. Shtanov, JCAP 1706 (2017) no.06, 045 [arXiv:1703.03295]
- 4 "Axion Cosmology", DJE Marsh, Phys.Rept. 643 (2016) 1-79 [arXiv:1510.07633].

Dark Energy from α -attractors

In addition to the dark matter models alluded to above, we have also discovered 4 new **Tracker Models** of **Dark Energy** (**Bag, Mishra and Sahni 2017 [arXiv:1709.09193]** submitted) and explored the possibility that these models give rise to an equation of state close to -1 at the present epoch, as demanded by observations.

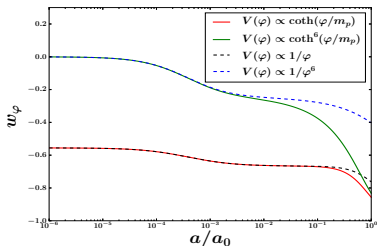
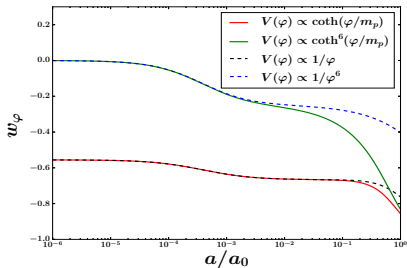


(a)



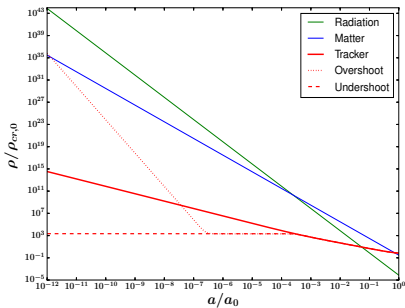
(b)

Dark Energy from the L-Model

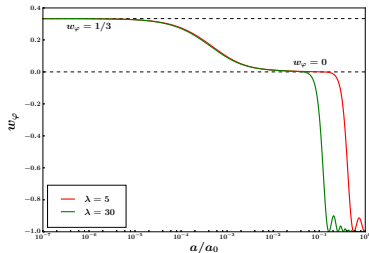


$V(\varphi) = V_0 \coth^p \left(\frac{\varphi}{m_p} \right)$, which for small values of the argument, $0 < \frac{\lambda\varphi}{m_p} \ll 1$, becomes Inverse Power-law (Ratra-Peebles) potential $V \simeq \frac{V_0}{(\lambda\varphi/m_p)^p}$ which has an attractor solution

$$w_\varphi = \frac{p w_B - 2}{p + 2}$$

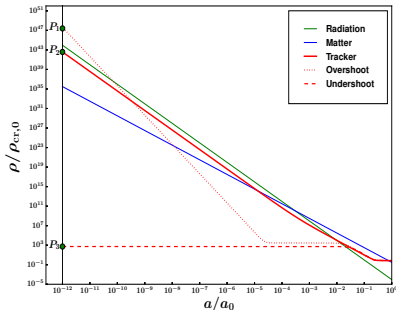
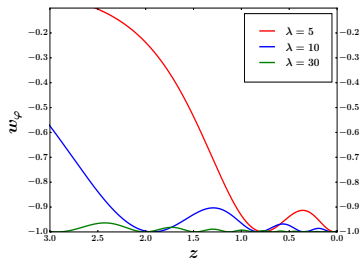


Dark Energy from the OLT-Model



$V(\varphi) = V_0 \cosh\left(\lambda \frac{\varphi}{m_p}\right)$, for large values $\frac{\lambda|\varphi|}{m_p} \gg 1$, has the asymptotic form $V \simeq \frac{V_0}{2} \exp\left(\frac{\lambda\varphi}{m_p}\right)$ which has an attractor scaling solution

$$\Omega_\varphi = \frac{3(1 + w_B)}{\lambda^2}, \quad w_\varphi = w_B$$



Final Remarks

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- 2 As well as producing a negative enough equation of state, $\langle w_\varphi \rangle \longrightarrow -1$ for Dark Energy at the present epoch.

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Other Project I am involved in →

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Other Project I am involved in \rightarrow Investigation of initial conditions for inflation for relevant Inflationary Potentials, with particular emphasis on the difference between Power-law Potentials and Asymptotically Flat Potentials.

"Initial Conditions for Inflation in an FRW Universe", [S.S Mishra, V. Sahni and A.V. Toporensky](#), [[arXiv:1801.04948](https://arxiv.org/abs/1801.04948)].