NON-MINIMALLY COUPLED INFLATON AND EW VACUUM STABILITY

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1608.08848, 1711.10554, ongoing work

WHY ARE WE HERE?

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- · Obtains a vacuum expectation value $\langle h \rangle = \nu \approx 246$ GeV.
- · Particle masses:

$$\begin{split} M_{H} &= 125.09 \pm 0.32 \text{GeV} \\ M_{\mathrm{top}} &= 173.34 \pm 0.76 \text{GeV} \end{split}$$

· Renormalization group evolution:

$$\begin{split} \mu^2 \frac{d\lambda_h}{d\mu^2} &\equiv \beta_{\lambda_h} = \frac{1}{16\pi^2} \left(12\lambda^2 + 6\lambda y_t^2 - 3y_t^4 \right) + \dots \\ \mu^2 \frac{dy_t}{d\mu^2} &\equiv \beta_{y_t} = \frac{1}{16\pi^2} y_t \left(\frac{9}{4} y_t^2 - 4g_s^2 \right) + \dots \\ \mu^2 \frac{dg_s}{d\mu^2} &\equiv \beta_{g_s} = \frac{1}{16\pi^2} g_s^3 \left(-\frac{11}{2} + \frac{n_f}{3} \right) + \dots \end{split}$$

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- $\cdot\,$ Couplings run with energy.
- At high energies the RG improved effective potential V(h) $\simeq \frac{\lambda_h(h)}{4}h^4$.



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 - $\cdot~$ Quantum effects \rightarrow tunnelling into the true vacuum.
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- 2. How did we end up here?
 - · Why did we end up in an energetically disfavoured state?

STABILITY OF THE ELECTROWEAK VACUUM



 $\cdot\,$ Precision calculations suggest our vacuum is metastable: $t_{\rm decay} \gg t_{\rm universe}$

Buttazzo et al. '13

· No immediate problem.

WHERE DID WE COME FROM? INFLATION.

- $\cdot\,$ An almost-exponential expansion of the universe a $\sim e^{Ht}.$
- · Driven by a scalar field ϕ slowly rolling down a flat potential slope:

$$\frac{M_{\rm P}^2}{2} \left(\frac{V'}{V}\right)^2, \ M_{\rm P}^2 \frac{V''}{V} \ll 1$$



- Once inflation ends the field starts to oscillate around the minimum of its potential and eventually decays into radiation.
- Simplest model: $V = \frac{1}{2}m^2\phi^2$.

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 - · Consider fluctuations $\phi(x) = \overline{\phi}(t) + \delta \phi(x)$:

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· Outside the horizon (k \ll aH): $\ddot{\phi} + 3H\dot{\phi} = 0$. Solution

$$\delta \phi \simeq {\rm constant} \simeq {{\sf H}_*\over \sqrt{2{\sf k}^3}}$$



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· Inside the horizon (k \gg aH): $\ddot{\delta \phi} + \frac{k^2}{a^2} \delta \phi = 0$. Solution



$$\delta\phi \simeq \frac{1}{\sqrt{2k/a}} e^{-i\int \frac{k}{a}dt}$$
Subside the horizon (k << aH): $\ddot{\delta\phi} + 3H\dot{\delta\phi} = 0$. Solution

$$\delta \phi \simeq {\rm constant} \simeq {{\sf H}_*\over \sqrt{2{\sf k}^3}}$$

- \cdot The SM Higgs is light during inflation.
- Stochastic formalism: field averaged on superhorizon scales obeys Langevin equation

Starobinsky '82

$$\dot{h} + \frac{V'(h)}{3H} = f(t); \qquad \langle f(t)f(t') \rangle = \frac{H^3}{4\pi^2}\delta(t-t').$$

 \cdot Equilibrium probability distribution at the end of inflation

$$\mathsf{P}(\mathsf{h}) \propto \exp\left(-\frac{2\lambda\pi^2\mathsf{h}^4}{3\mathsf{H}^4}\right).$$

- $\cdot\,$ Equilibrium value of the field $\sqrt{\langle h^2\rangle}\sim\lambda^{-1/4}H.$
- \cdot If H > μ_c the field is driven into the true vacuum during inflation!

HOW TO RESOLVE THIS?

- $\cdot\,$ Scale of inflation must be low: $H_{\rm inf} < 10^{10}$ GeV.
 - $\cdot\,$ However, $H_{\rm inf}$ up to 10^{13} GeV still consistent with observations.
- · Critical scale must be high.

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- $\cdot\,$ Top mass is lower than its central value.
- $\cdot\,$ New physics stabilizes the potential during inflation.

Higgs inflaton coupling
$$\delta \mathcal{L} = -\frac{\lambda_{\mathrm{h}\phi}}{4}\phi^2 \mathrm{h}^2 - \frac{\sigma_{\mathrm{h}\phi}}{2}\phi \mathrm{h}^2$$

this talk

2. Non-minimal coupling to gravity $\delta \mathcal{L} = -\xi \mathrm{Rh}^2 \label{eq:linear}$

eg. 1407.3141, 1602.00483, 1703.04681

COUPLING TO THE INFLATON

$$V_{h\phi} = \frac{\lambda_{h\phi}}{4}\phi^2 h^2 + \frac{\sigma_{h\phi}}{2}\phi h^2$$

• Quantum corrections must not spoil the flatness of the inflaton potential:

$$\lambda_{h\phi} < 10^{-6}.$$

 $\cdot\,$ New instability scale

$$\tilde{\mu}_{\rm C}\sim \sqrt{\frac{\lambda_{\rm h\phi}\phi^2+2\sigma_{\rm h\phi}\phi}{|\lambda_{\rm h}|}}$$

- $\cdot \phi$, m, H Can be obtained from cosmological observatiobs.
- $\cdot \,\, \lambda_{\rm h}$ can be calculated from SM RG running.
- · Higgs is stabilized for $\lambda_{h\phi} > 10^{-10}$, $|\sigma_{h\phi}| < \lambda_{h\phi}M_P$.

WHAT HAPPENS AFTER INFLATION?

• Once inflation ends the inflaton starts to oscillate around the mimimum of the potential.

$$\phi(t) = \frac{\Phi_0}{a^3} \sin(mt).$$

• Can be thought of as a condensate of massive particles at rest; perturbative decay

$$\Gamma(\phi \rightarrow hh) = \frac{\sigma_{h\phi}^2}{32\pi m}$$

- $\cdot\,$ Reheating when $H\sim\Gamma$ with reheating temperature $T\sim\sqrt{\Gamma M_P}.$
- · Not the whole story!

 \cdot The equation of motion for the (rescaled) Higgs modes ($\sigma_{
m h\phi}=$ 0)

$$\ddot{h}_{k} + \left[\frac{k^{2}}{a^{2}} + 4q(t)\sin^{2}(mt) + 3\lambda_{h}a^{-3}\langle h^{2}\rangle\right]h_{k} = 0$$

- · Mathieu-type equation.
- · Characterised by resonance parameter q(t) = $\frac{\lambda_{h\phi} \Phi^2(t)}{2m^2}$.
- \cdot Within the blue bands modes are amplified $h_k \sim e^{\mu t}.$
- \cdot In white regions oscillating modes $h_k \sim e^{i \int \omega_k dt}.$



PREHEATING: PARAMETRIC RESONANCE

 \cdot The particle number density $n_\kappa^{j+1}=|\beta_k^{j+1}|\simeq e^{2\pi\mu_\kappa^j}n_\kappa^j$ with Floquet index

$$\mu_{\kappa}^{j} \equiv \frac{1}{2\pi} \ln \left[1 + 2W_{\kappa}^{j} - 2\sin\theta_{tot^{j}} \sqrt{W_{\kappa}^{j}(1 + W_{\kappa}^{j})} \right], \qquad W = e^{-\pi\kappa^{2}}$$

 $\cdot\,$ The Higgs evolves as

$$\langle h^2 \rangle = \frac{3^j m^2 \kappa_{\rm max}^3}{2^{5/2} e \pi^{3/2} a^3 \sqrt{q}}$$

 $\cdot\,$ Production ends when $q \sim 1/4.$


- $\cdot\,$ Naively: vacuum is safe if the resonance shuts down before $\langle h^2 \rangle \sim \tilde{\mu}_c^2.$
- $\cdot\,$ After only a single zero-crossing $\sqrt{\langle {\rm h}^2\rangle}>\mu_{\rm c}^{\rm SM}.$
- $\cdot \lambda_{h}(\sqrt{\langle h^{2} \rangle}) < 0$ throughout the resonance.
- $\cdot 3\lambda_h \langle h^2 \rangle$ contributes a tachyonic mass term. This is larger than the inflaton contribution for a time Δt near the zero-crossing

$$\Delta t = \sqrt{\frac{6|\lambda_h|\langle h^2\rangle}{\lambda_{h\phi}\Phi^2m^2}}.$$

- $\cdot \;$ Condition for stability $\sqrt{3|\lambda_h|\langle h^2\rangle}|\Delta t| <$ 1.
- $\cdot\,$ Bound on the Higgs-inflaton coupling $\lambda_{\mathrm{h}\phi} < 3\times10^{-8}.$

Enqvist E., Karciauskas M., Lebedev O., SR, Zatta M., 2016

AMPLIFICATION OF THE HIGGS



· Analytic bound $\lambda_{h\phi} \lesssim 3 \times 10^{-8}$.

Enqvist E., Karciauskas M., Lebedev O., SR, Zatta M., 2016

CONSTRAINTS ON INFLATIONARY MODELS



NON-MINIMALLY COUPLED INFLATON

 $\cdot\,$ Jordan frame action

$$\begin{split} \mathsf{S} &= \int \mathrm{d}^4 \mathsf{x} \sqrt{-\mathsf{g}_J} \left[\frac{\mathsf{M}_{\mathrm{pl}}^2}{2} \Omega^2(\phi_J) \mathsf{R}_J - \frac{1}{2} \mathsf{g}_J^{\mu\nu} \partial_\mu \phi_J \partial_\nu \phi_J - \mathsf{V}(\phi_J) \right] \\ \Omega^2(\phi_J) &= \mathsf{1} + \xi \frac{\phi_J^2}{\mathsf{M}_{\mathrm{pl}}^2}, \qquad \mathsf{V}(\phi_J) = \frac{\lambda}{4} \phi_J^4 \end{split}$$

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$$S = \int d^4x \sqrt{-g_J} \left[\frac{M_{p1}^2}{2} \Omega^2(\phi_J) R_J - \frac{1}{2} g_J^{\mu\nu} \partial_\mu \phi_J \partial_\nu \phi_J - V(\phi_J) \right]$$

$$\Omega^{2}(\phi_{J}) = 1 + \xi \frac{\phi_{J}^{2}}{M_{\rm pl}^{2}}, \qquad \mathsf{V}(\phi_{J}) = \frac{\lambda}{4}\phi_{J}^{4}$$

 $\cdot\,$ Define new, "Einstein frame", metric $g^{E}_{\mu\nu}\equiv\Omega^{2}g^{J}_{\mu\nu}.$

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- $\cdot\,$ Einstein frame action

$$\begin{split} \mathrm{S} &= \int \mathrm{d}^{4} \mathrm{X} \sqrt{-\mathrm{g}_{\mathrm{E}}} \left[\frac{\mathrm{M}_{\mathrm{pl}}^{2}}{2} \mathrm{R}_{\mathrm{E}} - \frac{1}{2} \mathrm{g}_{\mathrm{E}}^{\mu\nu} \partial_{\mu} \phi_{\mathrm{E}} \partial_{\nu} \phi_{\mathrm{E}} - \mathrm{V}_{\mathrm{E}}(\phi_{\mathrm{E}}) \right] \\ \mathrm{d}\phi_{\mathrm{E}} &\equiv \frac{\sqrt{1 + \xi (1 + 6\xi) \frac{\phi_{j}^{2}}{\mathrm{M}_{\mathrm{pl}}^{2}}}}{\Omega^{2}} \mathrm{d}\phi_{\mathrm{J}}, \qquad \mathrm{V}_{\mathrm{E}} \equiv \frac{\lambda}{4} \left(\frac{\phi_{\mathrm{J}}}{\Omega} \right)^{4} \end{split}$$

· Einstein frame field

$$\frac{\phi_{\rm E}}{M_{\rm pl}} = \sqrt{\frac{1+6\xi}{\xi}} \operatorname{arsinh}\left(\sqrt{\xi(1+6\xi)}\frac{\phi_{\rm j}}{M_{\rm pl}}\right) - \sqrt{6} \operatorname{arsinh}\left(\sqrt{\frac{6\xi^2}{1+\xi\phi_{\rm j}^2/M_{\rm pl}^2}}\frac{\phi_{\rm j}}{M_{\rm pl}}\right)$$

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$$\sqrt{\frac{6\xi^{2}}{1+\xi\phi_{\rm l}^{2}/M_{\rm pl}^{2}}} \frac{\phi_{\rm l}}{M_{\rm pl}}$$

 \cdot When $6\xi \gg 1$

$$\frac{\phi_{\text{E}}}{M_{\text{pl}}} \simeq \begin{cases} \frac{\phi_{\text{I}}}{M_{\text{pl}}}, & \phi_{\text{J}}^2 \ll \frac{M_{\text{pl}}^2}{6\xi_{\phi}^2} \\ \text{sign}(\phi_{\text{J}})\sqrt{\frac{3}{2}}\xi_{\phi} \left(\frac{\phi_{\text{J}}}{M_{\text{pl}}}\right)^2, & \frac{M_{\text{pl}}^2}{6\xi_{\phi}^2} \ll \phi_{\text{J}}^2 \ll \frac{M_{\text{pl}}^2}{\xi_{\phi}} \\ \text{sign}(\phi_{\text{J}})\sqrt{\frac{3}{2}}\log\left[1 + \xi_{\phi} \left(\frac{\phi_{\text{J}}}{M_{\text{pl}}}\right)^2\right], & \phi_{\text{J}}^2 \gg \frac{M_{\text{pl}}^2}{\xi_{\phi}} \end{cases}$$

$$V_{E}(\phi_{E}) \simeq \begin{cases} \frac{\lambda}{4} \phi_{E}^{4}, \\ \frac{\lambda M_{\rm pl}^{2}}{6\xi_{\phi}^{2}} \phi_{E}^{2}, \\ \frac{\lambda M_{\rm pl}^{4}}{4\xi_{\phi}^{2}} \left(1 - e^{-\sqrt{\frac{2}{3}} \frac{|\phi_{E}|}{M_{\rm pl}}}\right)^{2}, \end{cases}$$

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- Negligible tensor-to-scalar ratio
 r.



 $\cdot\,$ Consider a spectator field χ coupled to the inflaton. In the Jordan frame

$$S_{\chi} = \int \mathrm{d}^4 x \sqrt{-g_J} \left[-\frac{1}{2} g_J^{\mu\nu} \partial_{\mu} \chi \partial_{\nu} \chi - \frac{1}{2} g^2 \phi_J^2 \chi^2 \right] \label{eq:S_constraint}$$

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· Equation of motion for canonical variable $X \equiv \frac{a^{3/2}}{\Omega} \chi$

$$\ddot{X}_k + \omega_k^2 X_k = 0, \quad \omega_k^2 = \frac{k^2}{a^2} + g^2 \left(\frac{\phi_J}{\Omega}\right)^2 + \partial_t^2 \log \frac{\Omega}{a^{3/2}} - \left(\partial_t \log \frac{\Omega}{a^{3/2}}\right)^2$$

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$$S_{\chi} = \int \mathrm{d}^4 x \sqrt{-g_J} \left[-\frac{1}{2} g_J^{\mu\nu} \partial_{\mu} \chi \partial_{\nu} \chi - \frac{1}{2} g^2 \phi_J^2 \chi^2 \right].$$

 \cdot In the Einstein frame this becomes

$$S_{\chi} = \int \mathrm{d}^4 x \sqrt{-g_E} \left[-\frac{1}{2} \Omega^{-2} g_E^{\mu\nu} \partial_{\mu} \chi \partial_{\nu} \chi - \frac{1}{2} g^2 \Omega^{-4} \phi_J^2 \chi^2 \right]. \label{eq:S_constraint}$$

· Equation of motion for canonical variable $X \equiv \frac{a^{3/2}}{\Omega} \chi$

$$\ddot{X}_k + \omega_k^2 X_k = 0, \quad \omega_k^2 = \frac{k^2}{a^2} + g^2 \left(\frac{\phi_J}{\Omega}\right)^2 + \partial_t^2 \log \frac{\Omega}{a^{3/2}} - \left(\partial_t \log \frac{\Omega}{a^{3/2}}\right)^2$$

$$-\frac{\Omega^2}{\sqrt{-g_M}}\partial_\mu\left(\frac{\sqrt{-g_M}}{\Omega^2}g_M^{\mu\nu}\partial_\nu h\right) + \Omega^{-2}V_h' - \xi_h\Omega^{-2}R_Jh = 0$$

· Ricci scalar

$$\mathsf{R}_{\mathsf{J}} = \Omega^2 \left(\mathsf{R}_{\mathsf{M}} + 3\Box \log \Omega^2 - \frac{3}{2} \partial_\mu \log \Omega^2 \partial^\mu \log \Omega^2 \right)$$

· Stability during inflation

$$\frac{\mathrm{m}_{\mathrm{eff}}^{2}}{\mathrm{H}_{\mathrm{M}}^{2}} = 12 \left[\frac{\lambda_{\mathrm{h}\phi}}{\lambda_{\phi}} \left(\frac{\phi_{\mathrm{J}}}{\mathrm{M}_{\mathrm{pl}}} \right)^{-2} - \xi_{\mathrm{h}} \right] \gg 1$$

· Stabilized by inflaton if

$$\left(\frac{\lambda_{\mathrm{h}\phi}}{\xi_{\phi}}\right) \gg \frac{\lambda_{\phi}(3\mathrm{N}-4)}{48\xi_{\phi}^{2}} \approx 1.3..1.9 \times 10^{-9}$$

· Einstein frame potential for the inflaton

$$V_{E}(\phi_{E}) \simeq \begin{cases} \frac{\lambda}{4} \phi_{E}^{4}, \\ \frac{\lambda M_{p1}^{2}}{6\xi_{\phi}^{2}} \phi_{E}^{2}, \\ \frac{\lambda M_{p1}^{4}}{4\xi_{\phi}^{2}} \left(1 - e^{-\sqrt{\frac{2}{3}} \frac{|\phi_{E}|}{M_{p1}}}\right)^{2}, \end{cases}$$



 \cdot Einstein frame potential for the inflaton

$$V_{E}(\phi_{E}) \simeq \begin{cases} \frac{\lambda}{4} \phi_{E}^{4}, \\ \frac{\lambda M_{pl}^{2}}{6\xi_{\phi}^{2}} \phi_{E}^{2}, \\ \frac{\lambda M_{pl}^{4}}{4\xi_{\phi}^{2}} \left(1 - e^{-\sqrt{\frac{2}{3}} \frac{|\phi_{E}|}{M_{pl}}}\right)^{2}, \end{cases}$$

$$\begin{split} \phi_J^2 \ll \frac{M_{\rm pl}^2}{6\xi_\phi^2} \\ \frac{M_{\rm pl}^2}{6\xi_\phi^2} \ll \phi_J^2 \ll \frac{M_{\rm pl}^2}{\xi_\phi} \\ \phi_J^2 \gg \frac{M_{\rm pl}^2}{\xi_\phi} \end{split}$$

• After inflation is over the field starts to oscillate around zero.



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- After inflation is over the field starts to oscillate around zero.
- \cdot The potential is effectively $V_E \simeq \tfrac{1}{2}m^2\phi_E^2. \label{eq:VE}$



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$$\begin{split} \phi_{J}^{2} \ll \frac{M_{\rm pl}^{2}}{6\xi_{\phi}^{2}} \\ \frac{M_{\rm pl}^{2}}{6\xi_{\phi}^{2}} \ll \phi_{J}^{2} \ll \frac{M_{\rm pl}^{2}}{\xi_{\phi}} \\ \phi_{J}^{2} \gg \frac{M_{\rm pl}^{2}}{\xi_{\phi}} \end{split}$$

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- \cdot The potential is effectively $V_{\rm E} \simeq {\textstyle \frac{1}{2}} m^2 \phi_{\rm E}^2. \label{eq:VE}$

· Inflaton mass
$$m^2 \equiv \frac{\lambda M_{pl}^2}{3\xi^2}$$



· Einstein frame potential for the inflaton

$$V_{E}(\phi_{E}) \simeq \begin{cases} \frac{\lambda}{4}\phi_{E}^{4}, \\ \frac{\lambda M_{\mathrm{Pl}}^{2}}{6\xi_{\phi}^{2}}\phi_{E}^{2}, \\ \frac{\lambda M_{\mathrm{Pl}}^{4}}{4\xi_{\phi}^{2}} \left(1 - e^{-\sqrt{\frac{2}{3}}\frac{|\phi_{E}|}{M_{\mathrm{Pl}}}}\right)^{2}, \end{cases}$$

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- After inflation is over the field starts to oscillate around zero.
- \cdot The potential is effectively $V_{\rm E} \simeq {\textstyle \frac{1}{2}} m^2 \phi_{\rm E}^2. \label{eq:VE}$
- · Inflaton mass m² $\equiv \frac{\lambda M_{\rm pl}^2}{3\xi^2}$.
- Field evolution $\phi_{\rm E} \simeq \frac{\Phi_0}{{
 m mt}} \sin({
 m mt})$.



CONSTRAINTS FROM PREHEATING

· Mapping between frames

$$\frac{\phi_{\mathsf{E}}}{\mathsf{M}_{\mathrm{pl}}} \simeq \begin{cases} \frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}, \\ \operatorname{sign}(\phi_{\mathrm{l}})\sqrt{\frac{3}{2}}\xi_{\phi}\left(\frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}\right)^{2}, \\ \operatorname{sign}(\phi_{\mathrm{l}})\sqrt{\frac{3}{2}}\log\left[1+\xi_{\phi}\left(\frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}\right)^{2}\right], \end{cases}$$

$$\begin{split} \phi_{\rm J}^2 \ll \frac{M_{\rm Pl}^2}{6\xi_{\phi}^2} \\ \frac{M_{\rm Pl}^2}{6\xi_{\phi}^2} \ll \phi_{\rm J}^2 \ll \frac{M_{\rm Pl}^2}{\xi_{\phi}} \\ \phi_{\rm J}^2 \gg \frac{M_{\rm Pl}^2}{\xi_{\phi}} \end{split}$$

$$\frac{\phi_{\mathsf{E}}}{\mathsf{M}_{\mathsf{pl}}} \simeq \begin{cases} \frac{\phi_{\mathsf{l}}}{\mathsf{M}_{\mathsf{pl}}}, & \phi_{\mathsf{l}}^2 \ll \frac{\mathsf{M}_{\mathsf{pl}}^2}{6\xi_{\phi}^2} \\ \operatorname{sign}(\phi_{\mathsf{l}})\sqrt{\frac{3}{2}}\xi_{\phi} \left(\frac{\phi_{\mathsf{l}}}{\mathsf{M}_{\mathsf{pl}}}\right)^2, & \frac{\mathsf{M}_{\mathsf{pl}}^2}{6\xi_{\phi}^2} \ll \phi_{\mathsf{l}}^2 \ll \frac{\mathsf{M}_{\mathsf{pl}}^2}{\xi_{\phi}} \\ \operatorname{sign}(\phi_{\mathsf{l}})\sqrt{\frac{3}{2}}\log\left[1 + \xi_{\phi} \left(\frac{\phi_{\mathsf{l}}}{\mathsf{M}_{\mathsf{pl}}}\right)^2\right], & \phi_{\mathsf{l}}^2 \gg \frac{\mathsf{M}_{\mathsf{pl}}^2}{\xi_{\phi}} \end{cases}$$

 \cdot In the intermediate regime $\phi_J^2\simeq \sqrt{\frac{2}{3}}\frac{M_{\rm pl}}{\xi}|\phi_{\rm E}|,\,\Omega^2\sim$ 1.

$$\frac{\phi_{\mathsf{E}}}{\mathsf{M}_{\mathrm{pl}}} \simeq \begin{cases} \frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}, & \phi_{\mathrm{l}}^{2} < \\ \operatorname{sign}(\phi_{\mathrm{l}})\sqrt{\frac{3}{2}}\xi_{\phi}\left(\frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}\right)^{2}, & \frac{\mathsf{M}_{\mathrm{pl}}^{2}}{\mathsf{6}\xi_{\phi}^{2}} \\ \operatorname{sign}(\phi_{\mathrm{l}})\sqrt{\frac{3}{2}}\log\left[1+\xi_{\phi}\left(\frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}\right)^{2}\right], & \phi_{\mathrm{l}}^{2} > \end{cases}$$

$$\begin{split} \phi_{J}^{2} \ll & \frac{^{m}\mathbf{p}\mathbf{l}}{6\xi_{\phi}^{2}} \\ \frac{^{M}\mathbf{p}\mathbf{l}}{6\xi_{\phi}^{2}} \ll \phi_{J}^{2} \ll \frac{^{M}\mathbf{p}\mathbf{l}}{\xi_{\phi}} \\ \phi_{J}^{2} \gg \frac{^{M}\mathbf{p}\mathbf{l}}{\xi_{\phi}} \end{split}$$

MA2

- \cdot In the intermediate regime $\phi_J^2\simeq \sqrt{\frac{2}{3}}\frac{M_{\rm pl}}{\xi}|\phi_{\rm E}|$, $\Omega^2\sim$ 1.
- \cdot Then the fluctuations of χ evolve according to

$$\ddot{X}_k + \omega_k^2 X = 0, \quad \omega_k^2 = \frac{k^2}{a^2} + \frac{g^2}{\xi} \Phi^2(t) |\sin(mt)|$$

$$\frac{\phi_{\mathsf{E}}}{\mathsf{M}_{\mathrm{pl}}} \simeq \begin{cases} \frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}, & \phi_{\mathrm{l}}^{2} \ll \frac{\mathsf{M}_{\mathrm{pl}}^{2}}{\mathsf{6}\xi_{\phi}^{2}} \\ \operatorname{sign}(\phi_{\mathrm{l}})\sqrt{\frac{3}{2}}\xi_{\phi} \left(\frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}\right)^{2}, & \frac{\mathsf{M}_{\mathrm{pl}}^{2}}{\mathsf{6}\xi_{\phi}^{2}} \ll \phi_{\mathrm{l}}^{2} \ll \frac{\mathsf{M}_{\mathrm{pl}}^{2}}{\xi_{\phi}} \\ \operatorname{sign}(\phi_{\mathrm{l}})\sqrt{\frac{3}{2}}\log\left[1+\xi_{\phi} \left(\frac{\phi_{\mathrm{l}}}{\mathsf{M}_{\mathrm{pl}}}\right)^{2}\right], & \phi_{\mathrm{l}}^{2} \gg \frac{\mathsf{M}_{\mathrm{pl}}^{2}}{\xi_{\phi}} \end{cases}$$

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· Compared to the minimally coupled case: $g^2 \rightarrow g^2/\xi$, $sin^2(mt) \rightarrow |sin(mt)|$.

$$\frac{\phi_{\text{E}}}{M_{\text{pl}}} \simeq \begin{cases} \frac{\phi_{\text{I}}}{M_{\text{pl}}}, & \phi_{\text{J}}^2 \ll \frac{M_{\text{pl}}^2}{6\xi_{\phi}^2} \\ \text{sign}(\phi_{\text{J}})\sqrt{\frac{3}{2}}\xi_{\phi} \left(\frac{\phi_{\text{J}}}{M_{\text{pl}}}\right)^2, & \frac{M_{\text{pl}}^2}{6\xi_{\phi}^2} \ll \phi_{\text{J}}^2 \ll \frac{M_{\text{pl}}^2}{\xi_{\phi}} \\ \text{sign}(\phi_{\text{J}})\sqrt{\frac{3}{2}}\log\left[1 + \xi_{\phi} \left(\frac{\phi_{\text{I}}}{M_{\text{pl}}}\right)^2\right], & \phi_{\text{J}}^2 \gg \frac{M_{\text{pl}}^2}{\xi_{\phi}} \end{cases}$$

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· Compared to the minimally coupled case: $g^2 \rightarrow g^2/\xi$, $sin^2(mt) \rightarrow |sin(mt)|$.

NON-MINIMALLY COUPLED INFLATON

· Particle production

$$\mathbf{n}_{k}^{j+1} \simeq e^{2\pi\mu_{k}^{j}}\mathbf{n}_{k}^{j}, \qquad \mu_{k}^{j} \equiv \frac{1}{2\pi}\log\left[1+2C_{k}^{j}+2\cos\theta_{j}\sqrt{C_{k}^{j}\left(1+C_{k}^{j}\right)}\right].$$

with

$$C_{k}^{j}(z) \equiv \pi^{2} \left[\mathsf{Ai}\left(-z^{2}\right) \mathsf{Ai}'\left(-z^{2}\right) + \mathsf{Bi}\left(-z^{2}\right) \mathsf{Bi}'\left(-z^{2}\right) \right]^{2}, \qquad z^{2} \equiv \frac{\kappa_{j}^{2}}{q_{j}^{2/3}}$$

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· Dispersion of fluctuations

$$\langle h^2 \rangle \simeq 5 \times 10^{-2} \frac{\sqrt{q}m^2}{a^3} \left(\frac{\sqrt{a}}{\sqrt{a}-1}\right)^{3/2} \left(\frac{5}{3}\right)^j$$

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· Constraints from stability

$$\frac{\lambda_{\mathrm{h}\phi}}{\xi_{\phi}} < 4 \times 10^{-9} \frac{\mathrm{M}_{\mathrm{pl}}}{\Phi_{0}}$$

HIGGS-INFLATON MIXING

$$V(\phi, h) = \frac{\lambda_{h}}{4}h^{4} - \frac{\mu_{h}^{2}}{2}h^{2} + \frac{\lambda_{h\phi}}{2}h^{2}\phi^{2} + \sigma h^{2}\phi + \frac{\lambda_{\phi}}{4}\phi^{4} + \frac{b_{3}}{3}\phi^{3} - \frac{\mu_{\phi}^{2}}{2}\phi^{2} + b_{1}\phi$$

 \cdot Low energy mass eigenstates h_1, h_2 :

$$\begin{array}{rcl} 2\lambda_{\rm h}\nu^2 &=& m_1^2\cos^2\theta + m_2^2\sin^2\theta,\\ \lambda_{\rm h\phi}\nu^2 - \mu_{\phi}^2 &=& m_1^2\sin^2\theta + m_2^2\cos^2\theta,\\ \sigma\nu &=& \frac{\sin 2\theta}{4}\left(m_1^2 - m_2^2\right) \end{array}$$

- Higgs-inflaton mixing lifts the value of higgs self-coupling.
- Stability ensured with moderate values of $\sin \theta$, m₂.



Ema Y., Karciauskas M., Lebedev O., SR, Zatta M., 2016

INFLATION

- \cdot For inflation run the parameters to the inflationary scale.
- We require that no vacua deeper than the EW one develop at higher energies.
- 6 4 • We also require: unitarity violation 2 $o'_{3}(M_{t})$ [GeV] instability 1. overall stability: 0 $\lambda_{\mathrm{h}\phi} > -\sqrt{\lambda_{\mathrm{h}}\lambda_{\phi}}$ -2 2. unitarity $\lambda_{\phi} \xi_{\phi}^2 \lesssim 1$ -4EW vacuum not global 3. perturbativity -6 $\lambda_{\rm i} > 4\pi$ -0.002-0.0010.000 0.001 0.002 $\lambda_{\mathrm{h}\phi}(M_t)$

Enqvist E., Karciauskas M., Lebedev O., SR, Zatta M., 2016
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Enqvist E., Karciauskas M., Lebedev O., SR, Zatta M., 2016

HIGGS-INFLATON MIXING

- \cdot Within the allowed regions inflation proceeds as before.
- · Higgs is stable both during inflation and preheating due to the mixing-induced running of λ .



• The model is viable for mixing of $\sin \theta \sim O(0.1)$ and $m_2 \sim O(100 \text{GeV})$, offering prospects of collider detection.

Ema Y., Karciauskas M., Lebedev O., SR, Zatta M., 2016

SUMMARY

SUMMARY

- $\cdot\,$ High scale inflation pushes the higgs into the true vacuum.
- In order to avoid this need to couple higgs to something else: inflaton or spacetime curvature.
- This results in non-perturbative, resonant amplification of the higgs during preheating and may lead to destabilization.
- Thus preheating puts new constraints on such models and significantly reduces the available parameter space in this scenario.
- In non-minimally coupled inflation, the mixing between the higgs and the inflaton provides a viable model which could be accessible to collider searches in the near future.

THANK YOU!

· Higgs may decay between inflaton zero-crossing through



PREHEATING: TACHYONIC RESONANCE

• If $\sigma_{h\phi} \neq 0$ then the inflaton contributes a tachyonic mass to the higgs every other oscillation while $2\sigma_{h\phi} > \lambda_{h\phi} \Phi$.

$$\ddot{h}_{k} + \left[\frac{4k^{2}}{a^{2}} + 2qm^{2} + 2p\cos 2mt + 2qm^{2}\cos 4mt + 3\lambda_{h}a^{-3}\langle h^{2}\rangle\right]h_{k} = 0$$

· Whittaker-Hill-type equation. · Again there are oscillating and exponentially growing solutions. 4 Evolution of the number density ٠ q 3 1: $\sigma = 8 \times 10^{-11}$; $\lambda_{hb} = 1.5 \times 10^{-11}$ 1×10^{11} , $\lambda_{14} = 3 \times 10^{10}$ 2 10 $n_{k}10^5$ 10^{4} 10 -2 4 -4100

PREHEATING: TACHYONIC RESONANCE

· Field evolution ($\lambda_{\rm h}=0$)



DESTABILIZATION WITH TRILINEAR COUPLINGS

- · Critical scale at late times $\tilde{\mu}_{c} \simeq \frac{2|\sigma_{h\phi}|\Phi}{|\lambda_{h}|}$.
- \cdot Can evaluate the Higgs as before

$$\langle h^2 \rangle \simeq \frac{m^2}{2a^3} \frac{e^{\mu_* m t}}{\sqrt{|\sigma_{h\phi}|} \Phi} \label{eq:alpha}$$

 $\cdot\,$ Constraint on the coupling $|\sigma_{{\rm h}\phi}| \lesssim 10^9$ GeV.





• Alternatively the Higgs may be stabilized during inflation via a non-minimal coupling to gravity

$$-\delta \mathcal{L} = \frac{1}{2} \xi \mathrm{Rh}^2.$$

- · Critical scale $\tilde{\mu}_{c}^{2} = \frac{2\xi R}{\lambda_{h}}$.
- · During inflation R \simeq 12H² so $\xi \sim \mathcal{O}(0.1)$ can stabilize the potential.
- · During preheating $R = 6(\dot{H} + 2H^2)$ oscillates \Rightarrow similar dynamics as in the tachyonic preheating case.
- \cdot Constraint $\xi < 2.5 \left(rac{\sqrt{2}M_{
 m p}}{\Phi_{
 m inf}}
 ight)^2$ (Ema et al. '16).

Ema et. at '17

 $\cdot\,$ If Higgs couples to both gravity and the inflaton

$$-\delta \mathcal{L} = \frac{1}{2} \lambda_{\mathrm{h}\phi} \phi^2 \mathrm{h}^2 + \frac{1}{2} \xi \mathrm{R} \mathrm{h}^2.$$

 $\cdot\,$ In the Einstein frame

$$-\delta \mathcal{L} = \frac{1}{2} (\lambda_{\mathrm{h}\phi} + 2\xi \mathrm{m}^2) \phi^2 \mathrm{h}_{\mathrm{c}}^2.$$

· Stability during inflation

$$10^{-10} < \lambda_{\mathrm{h}\phi} + 2\xi \mathrm{m}^2 < 10^{-6}$$

- · Resonance parameter $q = (\lambda_{h\phi} + 3\xi m^2)\Phi^2 m^{-2}$.
- · Suppression of resonance for $\lambda_{h\phi} \simeq -3\xi m^2$.



COMBINED CASE: VACUUM STABILITY

