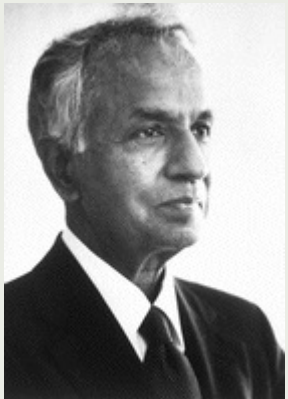


# GRAVITATIONAL PHYSICS FRONTIERS IN THE PTA ~~AND SKA~~ ERA

ascl:2211.001, arXiv:2312.03383, in prep, in prep

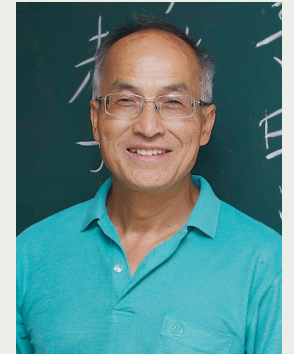


**Reggie Bernardo**

*and* **Kin-Wang Ng**

*with* **Guo-Chin Liu** (TKU)

*with* **Gopakumar Achamveedu** (InPTA)

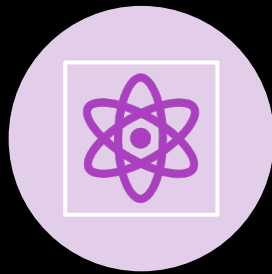


nHzGravCosmo @ GC2024/YITP @ 19 Feb 2024

# OUTLINE



**NANOHERTZ GWS  
SGWB AND PTA**



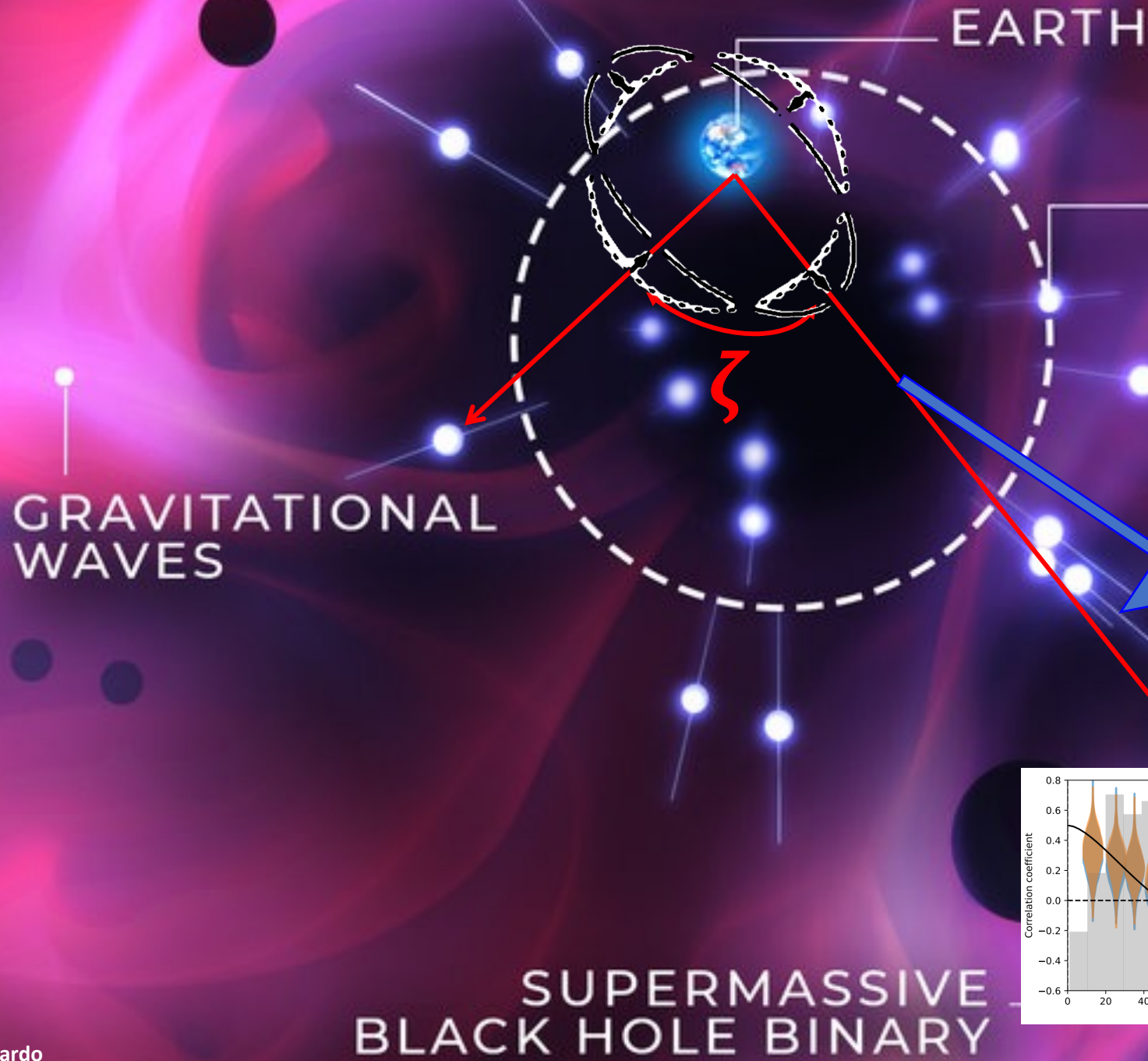
**ANISOTROPIC  
POLARIZED SGWB**



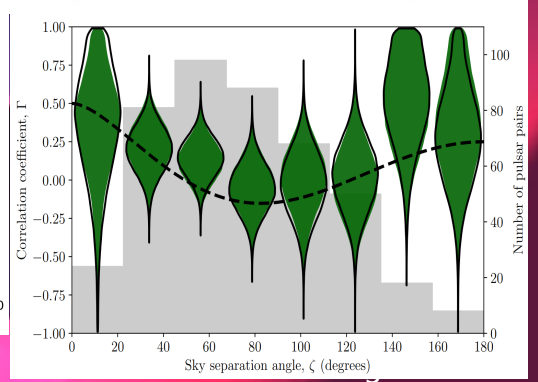
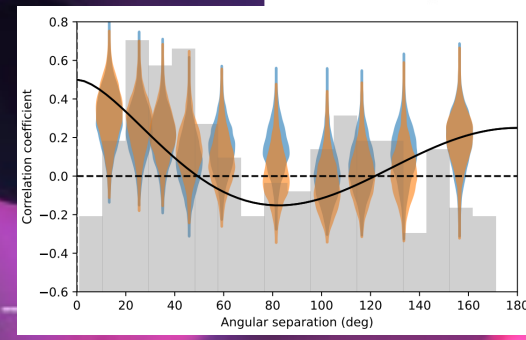
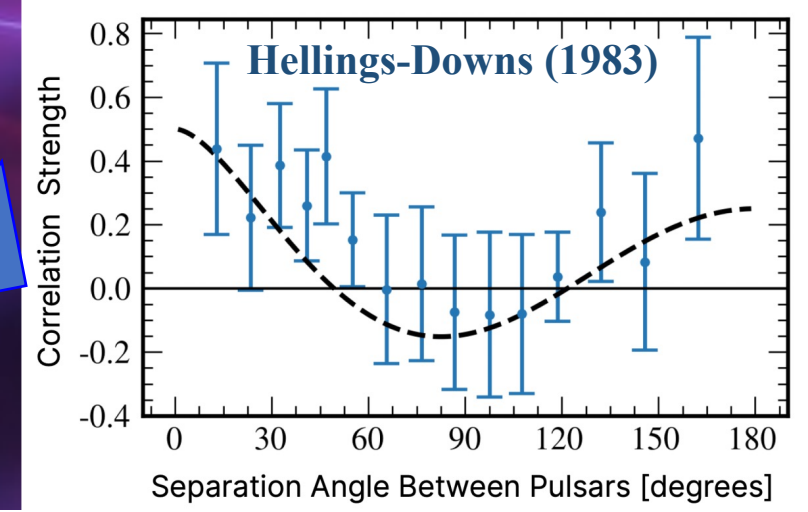
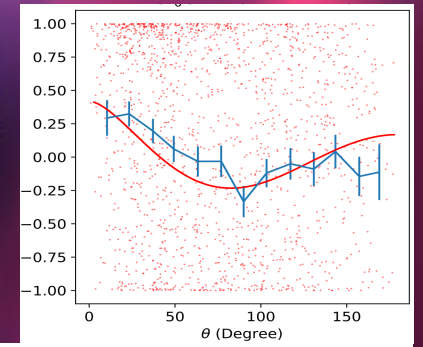
**FUZZY DM IN PTA**



**OUTLOOK**



PULSAR  
TIMING  
ARRAY



# Pulsar Timing

- The **timing residual** = observation - timing model

$$r(t) = \int dt' z(t') = \text{Earth Term} - \text{Pulsar Term}$$

- Redshift fluctuation from **GW  $h_{ij}(t)$** :

$$z(t) = -\frac{1}{2} \int d\eta \hat{e}^i \otimes \hat{e}^j \partial_\eta h_{ij}(\eta)$$

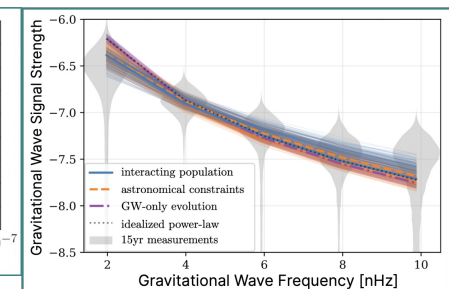
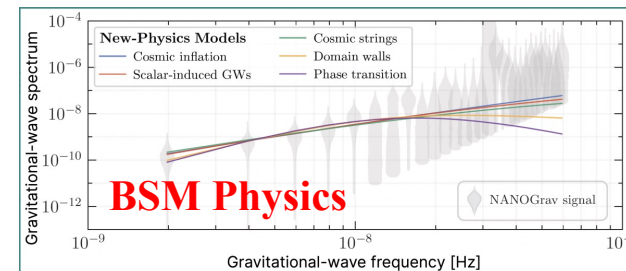
- Two-point function

**Frequency Spectrum**

~SMBHBs, SIGWs, FOPT, etc.

$$\langle r_a(t) r_b(t) \rangle = \sum \langle a_{l_1 m_1} a_{l_2 m_2} \rangle Y_{l_1 m_1}^*(\hat{e}_a) Y_{l_2 m_2}^*(\hat{e}_b)$$

$$\sim \sum_A \int df (1 - e^{-2\pi i f t})(1 - e^{2\pi i f t}) \times \frac{P_{AA}(f)}{f^2} \times \gamma_{ab}^A(\hat{e}_a \cdot \hat{e}_b)$$



# Pulsar Timing

- The **timing residual** = observation - timing model

$$r(t) = \int dt' z(t')$$

- Redshift fluctuation from **GW  $h_{ij}(t)$** :

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$$\langle r_a(t) r_b(t) \rangle = \sum \langle a_{l_1 m_1} a_{l_2 m_2} \rangle Y_{l_1 m_1}^*(\hat{e}_a) Y_{l_2 m_2}^*(\hat{e}_b)$$

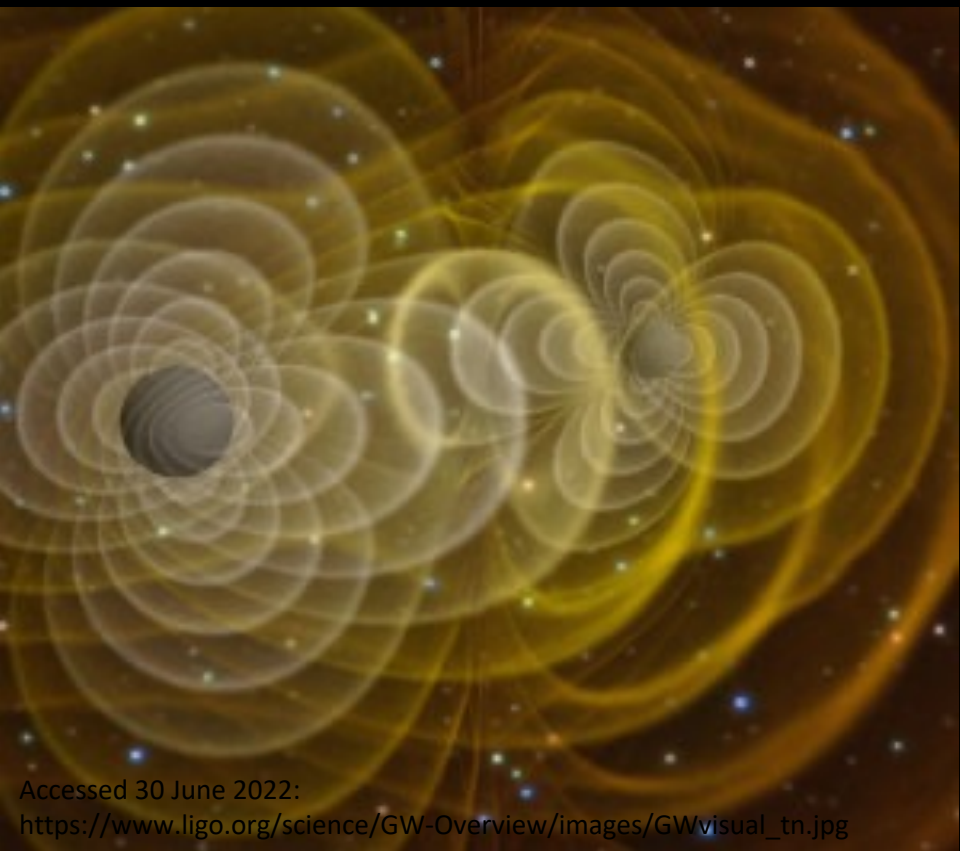
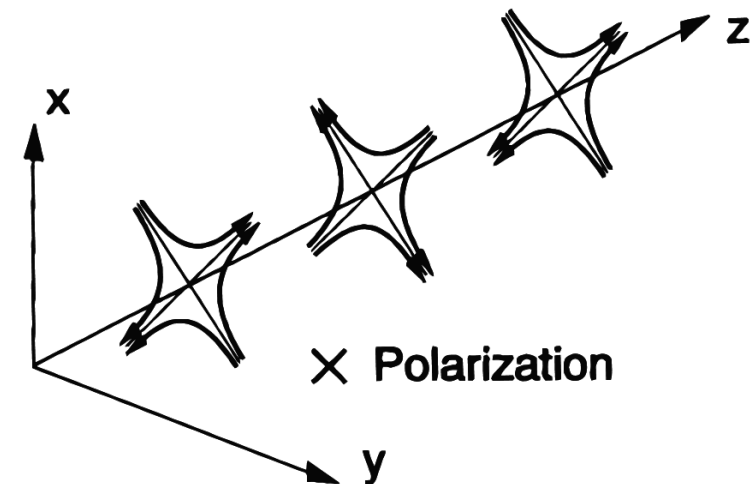
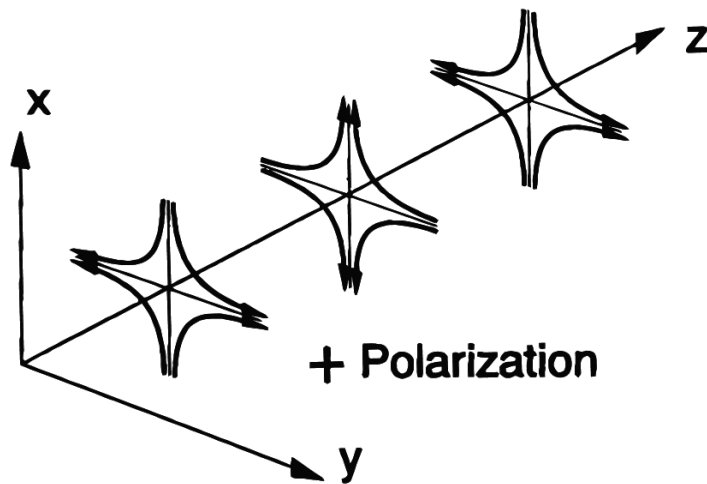
$$\sim \sum_A \int df (1 - e^{-2\pi i f t})(1 - e^{2\pi i f t}) \times \frac{P_{AA}(f)}{f^2} \times \underbrace{\gamma_{ab}^A(\hat{e}_a \cdot \hat{e}_b)}_{\text{Correlation/ORF}}$$

**Correlation/ORF**

~GW, Fuzzy Dark Matter, etc.

- Quantifies SGWB induced correlation between pulsars  $a$  and  $b$ ;
- A function of the frequency and the angle between pulsars across PTA.

# Gravitational Wave Polarizations



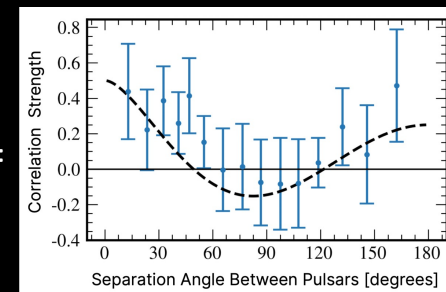
GW amplitude  $\rightarrow$  Omega

$$h_{ij}(\eta, \vec{x}) = \sum_A \int df \int d\hat{k} \tilde{h}_A(f, \hat{k}) \epsilon_{ij}^A e^{-2\pi i f(\eta - v\hat{k} \cdot \vec{x})}$$

Polarization Tensor  $\rightarrow$  ORF

velocity

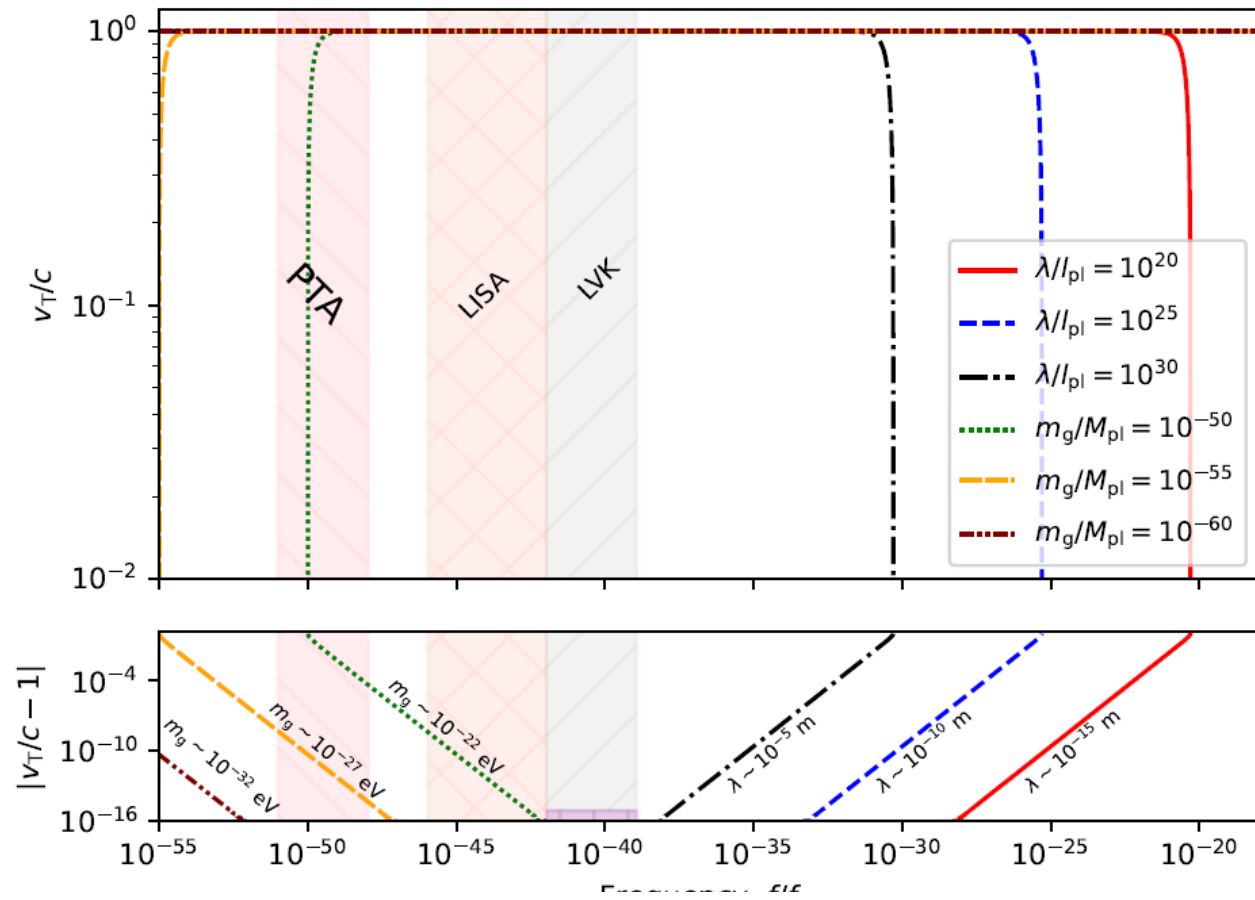
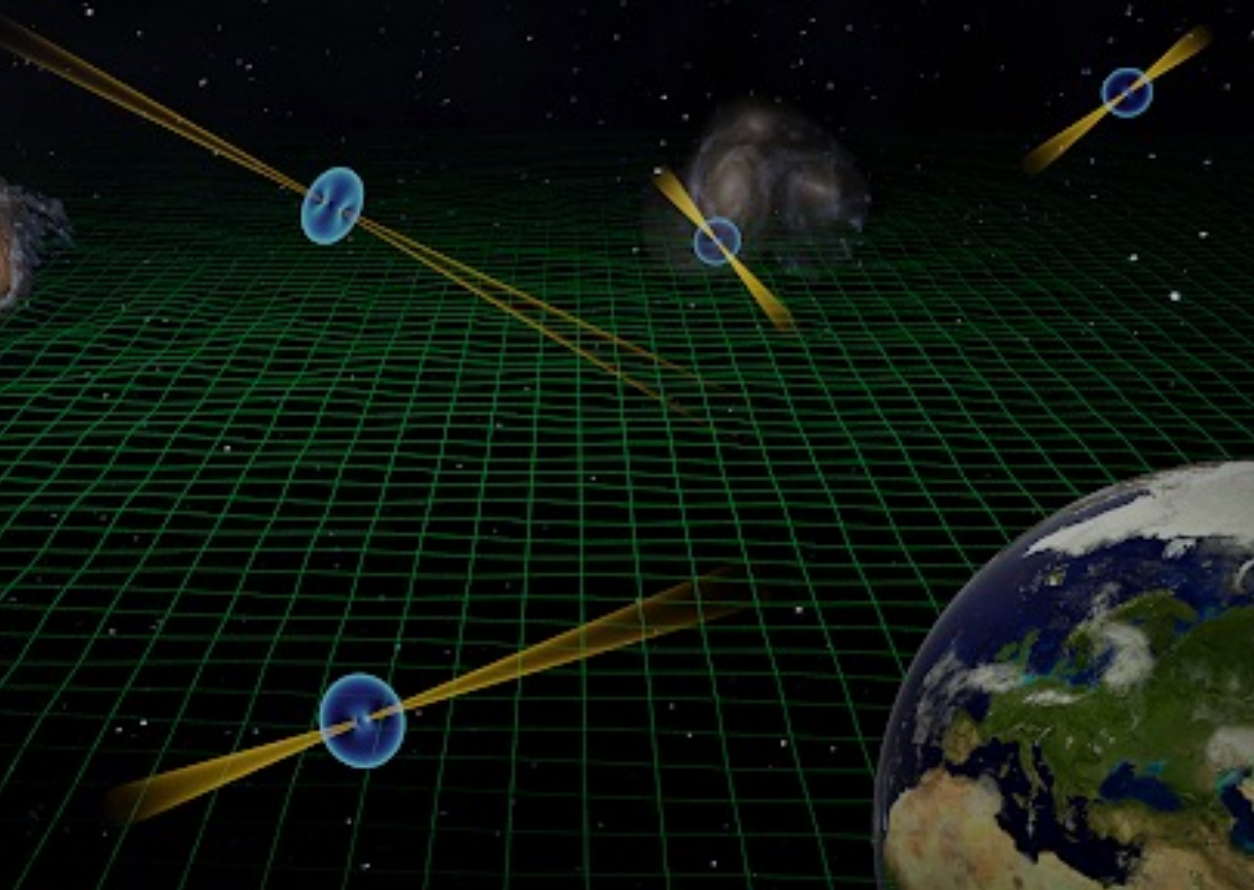
TT tensor +  $\underline{v} = \underline{1} + \underline{D} \rightarrow \infty$  + Isotropic =



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# What's next?

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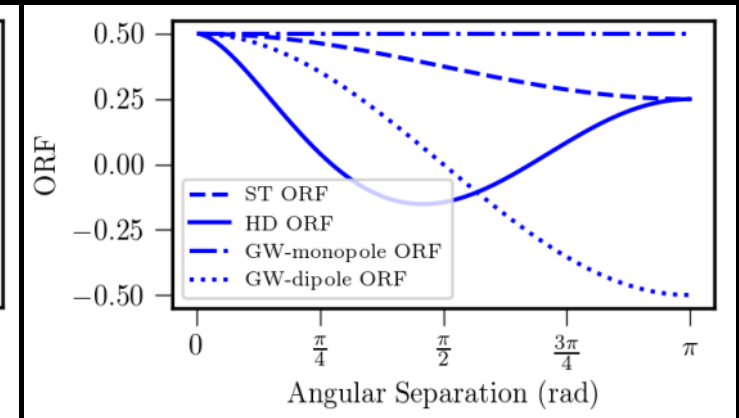
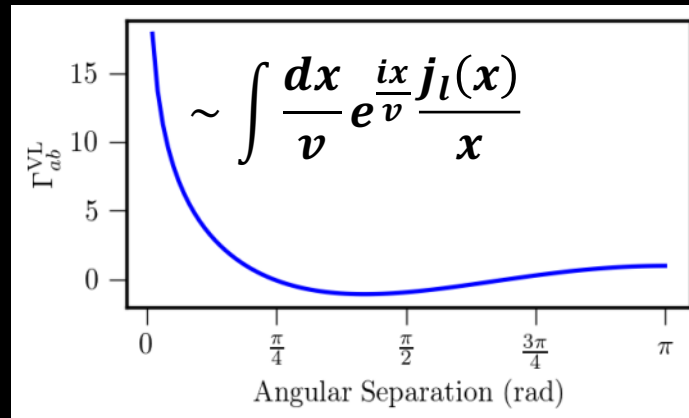
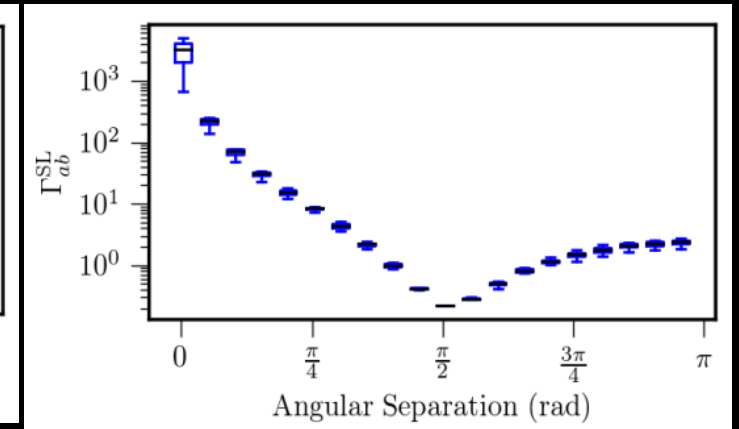
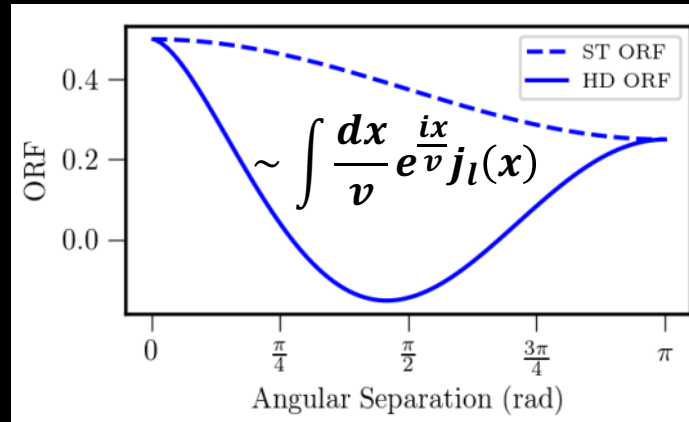
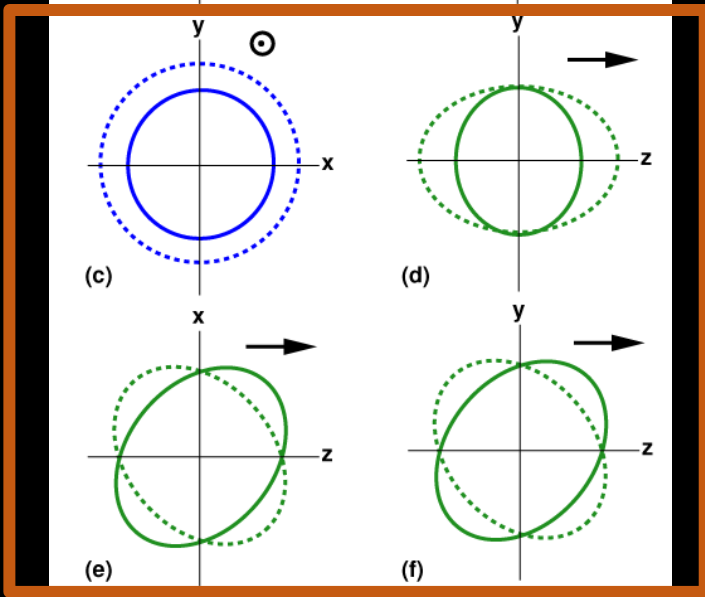
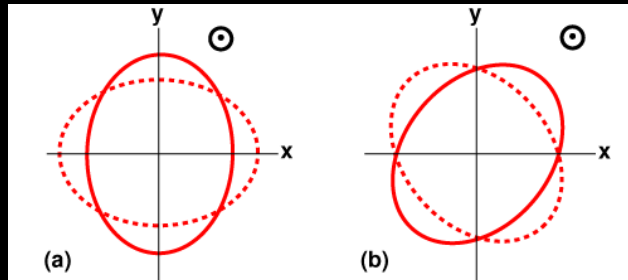


# PTA Playbook: Testing Gravity

$$S[g, \phi] = \int d^4x \sqrt{-g} \left( \frac{M_{\text{Pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 + \text{Horndeski} - \text{GB terms} + \dots \right)$$



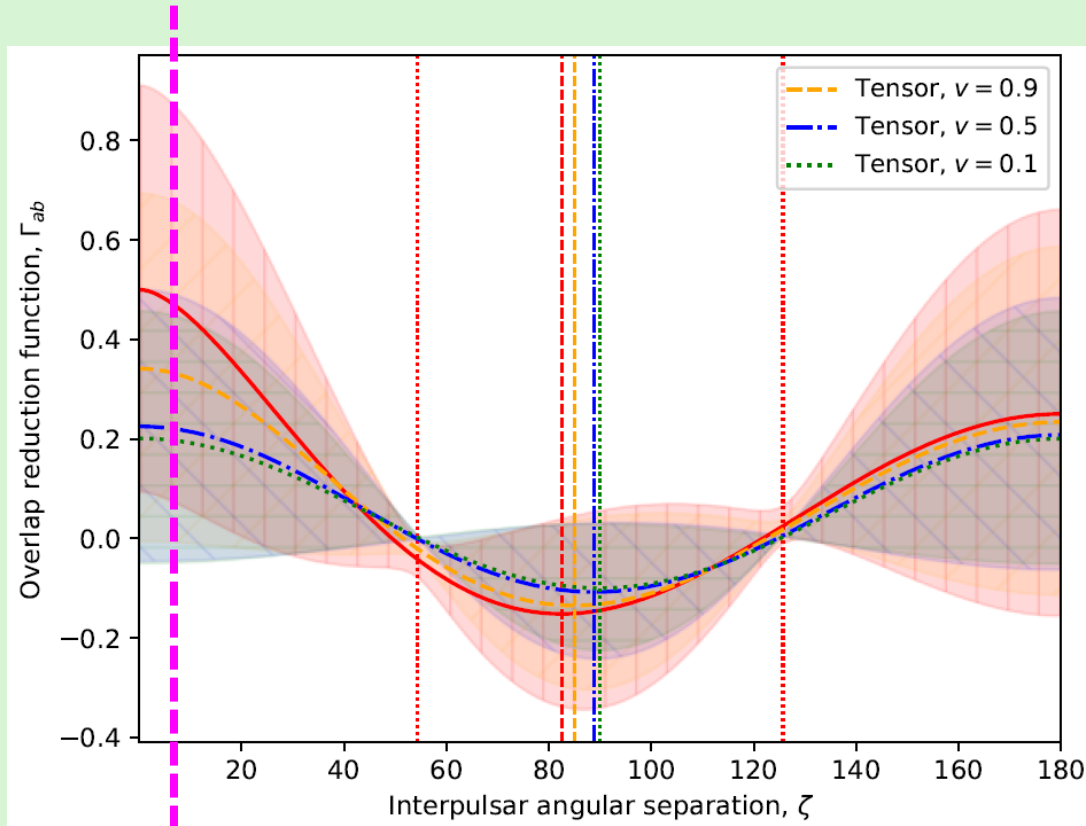
# GW Polarizations: Beyond Einstein



Accessed 30 June 2022:  
<https://www.ligo.org/science/Publication-GW170814/images/figure5.png>

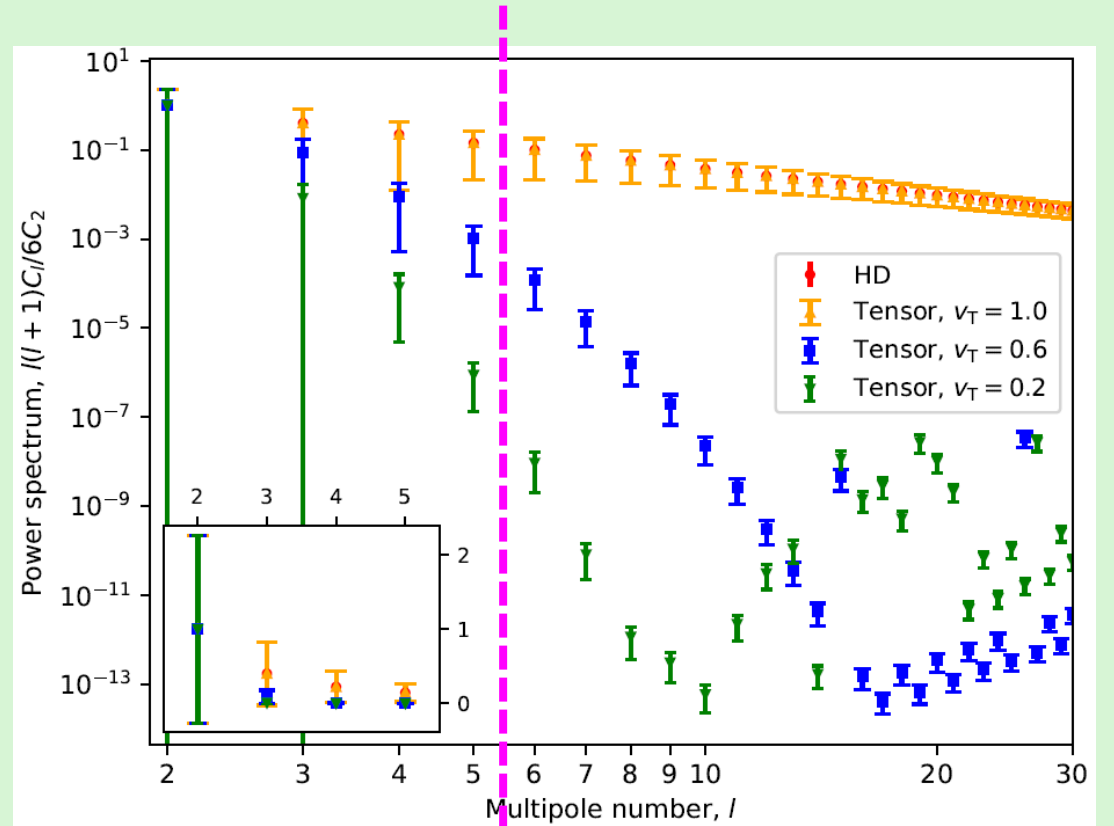
NANOGrav: arXiv:2109.14706

# CORRELATION



NG15

# POWER SPECTRUM



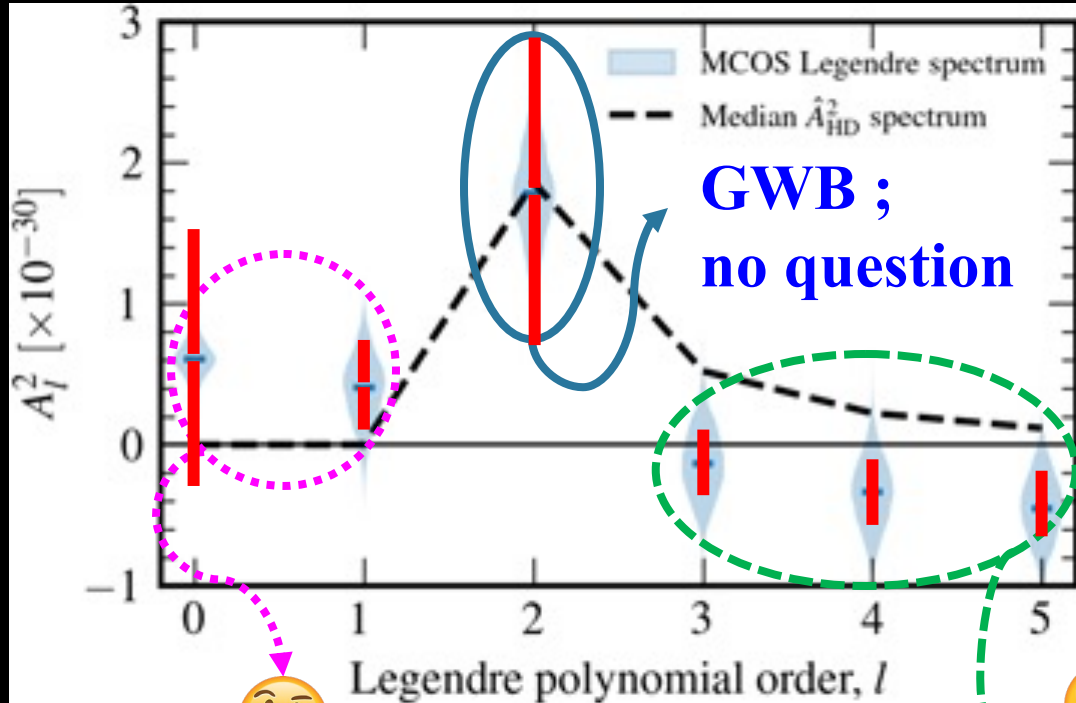
NG15



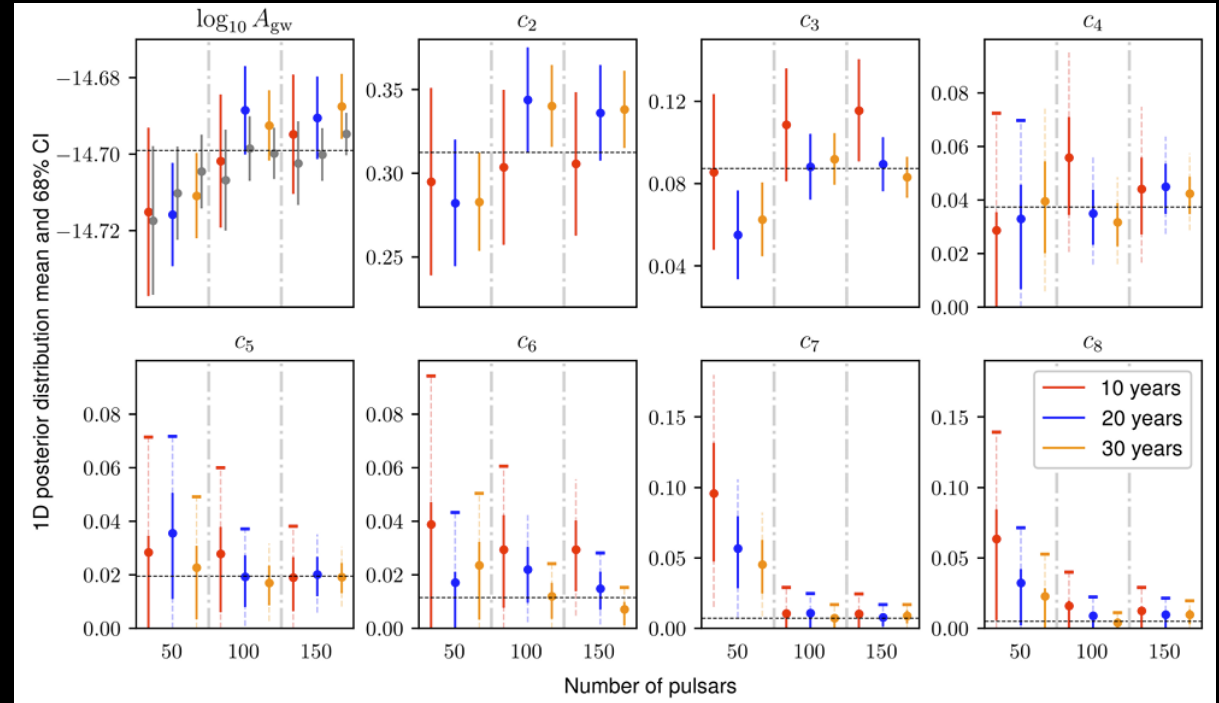
apctp

# NG15 + future projections ~ CV-precise

NANOGrav 15 years detection paper



2306.06168 (Nay, Boddy, Smith, Mingarelli)



Forecast ~ 150 MSPs + 30 yrs PTA ~  $l \leq 8$

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# Anisotropy and Polarization

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# Anisotropy and Polarization

- Cosmological source  $\sim$  Isotropic
- Individual SMBHBs  $\sim$  Anisotropy
- Finite  $N_{\text{sources}} \sim$  Anisotropy
- Linear/Circular GW Polarization

What if?

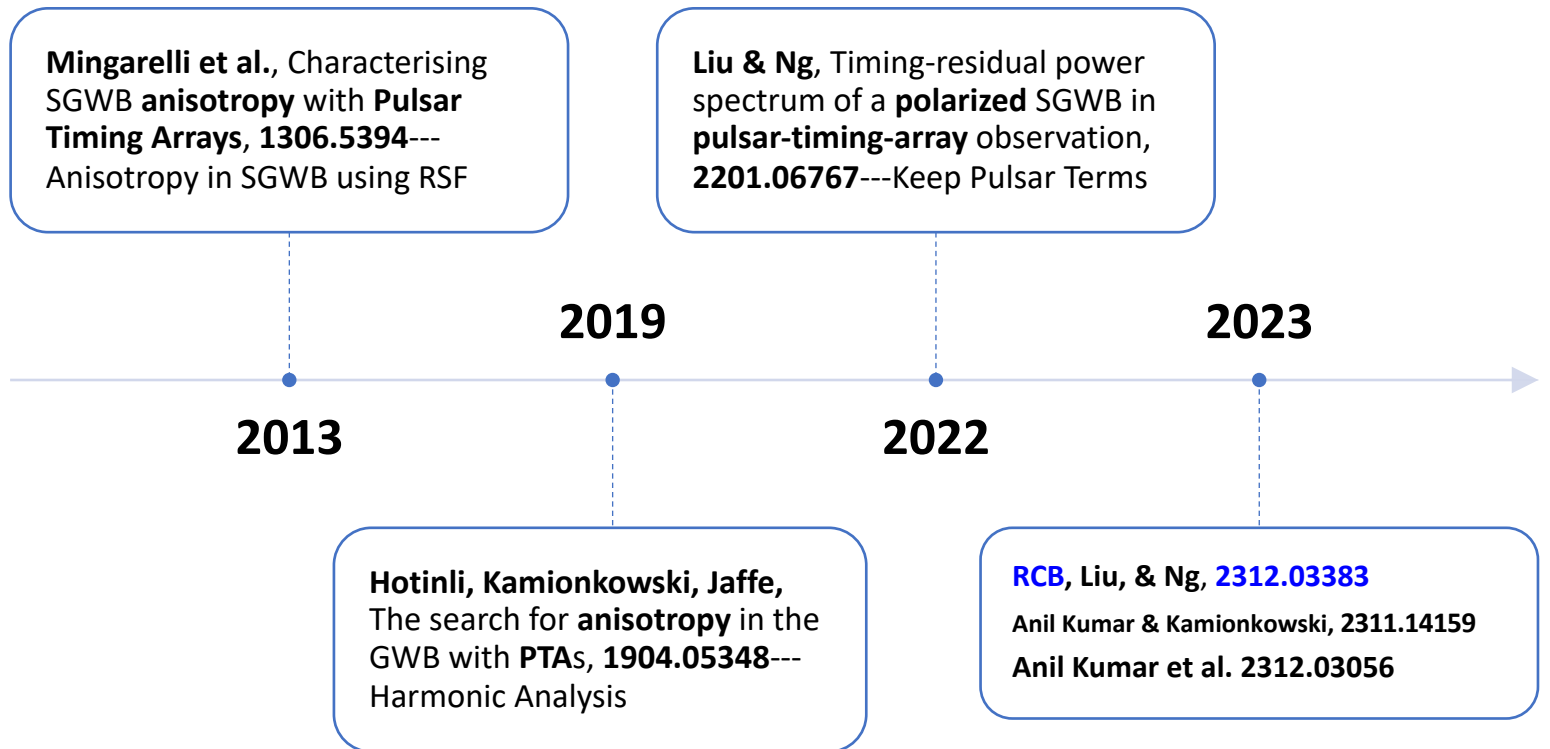
## Correlation = Hellings-Downs

+ Anisotropy + Polarization



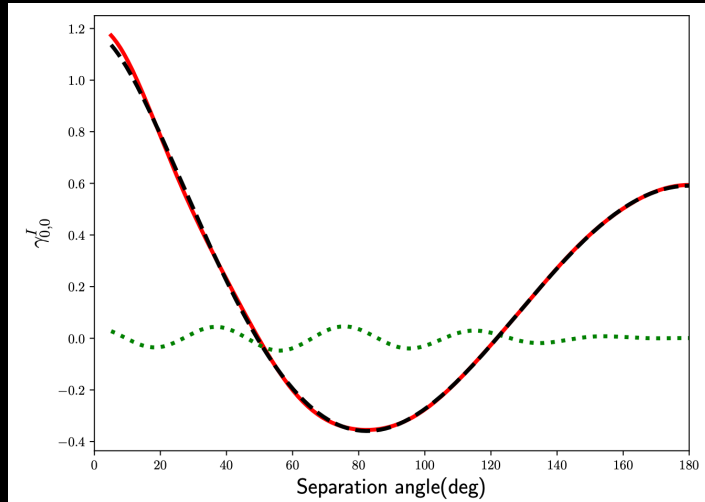


# Some Highlights



# Standard GR-Tensor Case

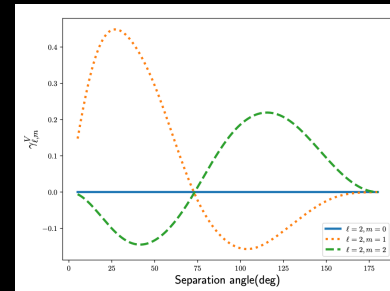
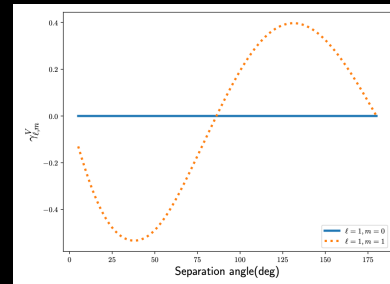
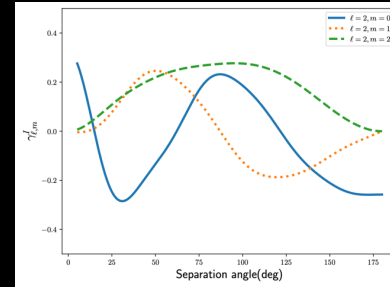
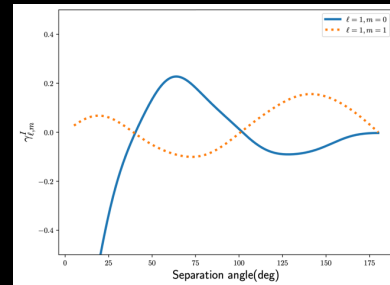
Chu, Liu, & Ng, 2107.00536



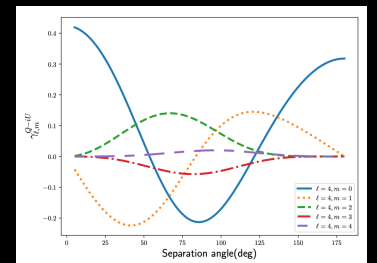
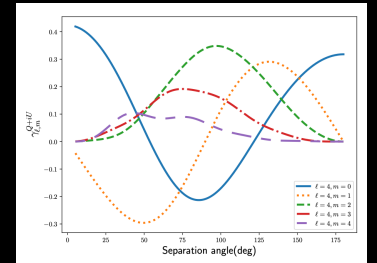
HD/Isotropic

NG15/CPTA

Leading Anisotropy



Leading Polarization



# Correlations for anisotropic polarized SGWB

$$\gamma_{lm}^{I,V}(fD_a, fD_b, \zeta) = \sum_{l_1 l_2} (-1)^m \left( \frac{2l_1 + 1}{4\pi} \right) [1 \pm (-1)^{l+l_1+l_2}] C_l^{\mathbf{T}}(fD_a, fD_b) Y_{l_2 m}(\zeta, 0)$$

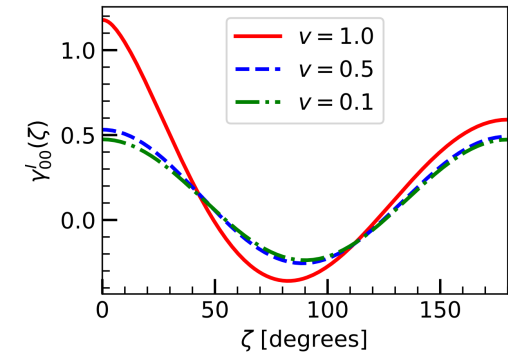
$$\times \sqrt{(2l+1)(2l_2+1)} \begin{pmatrix} l & l_1 & l_2 \\ 0 & -2 & 2 \end{pmatrix} \begin{pmatrix} l & l_1 & l_2 \\ m & 0 & -m \end{pmatrix}$$

**3j-symbols  
spin-2 field**

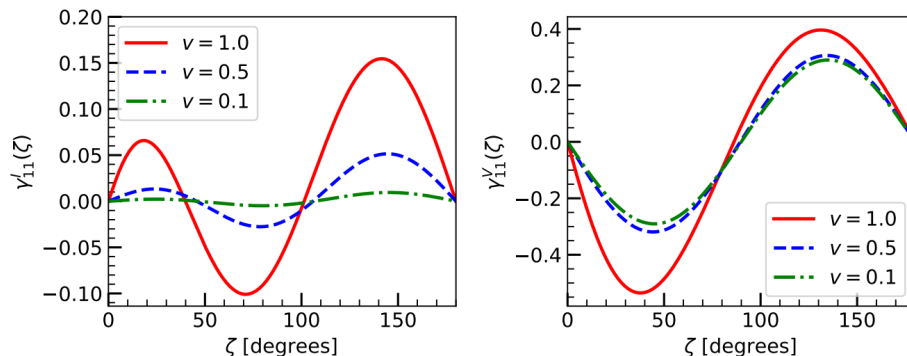
$$\gamma_{lm}^{Q\pm iU}(fD_a, fD_b, \zeta) = \sum_{l_1 l_2} (-1)^m \left( \frac{2l_1 + 1}{4\pi} \right) C_l^{\mathbf{T}}(fD_a, fD_b) Y_{l_2 m}(\zeta, 0)$$

$$\times \sqrt{(2l+1)(2l_2+1)} \begin{pmatrix} l & l_1 & l_2 \\ \mp 4 & \pm 2 & \pm 2 \end{pmatrix} \begin{pmatrix} l & l_1 & l_2 \\ m & 0 & -m \end{pmatrix}$$

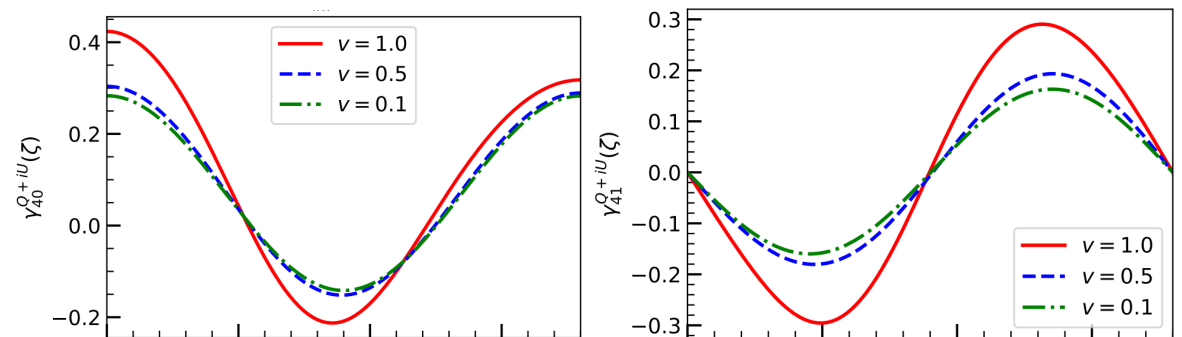
**Isotropic SGWB— $l = m = 0$**



**Anisotropic SGWB— $l = 1, m = 1$**



**Anisotropic Polarized SGWB— $l = 4, m = 0, 1$**



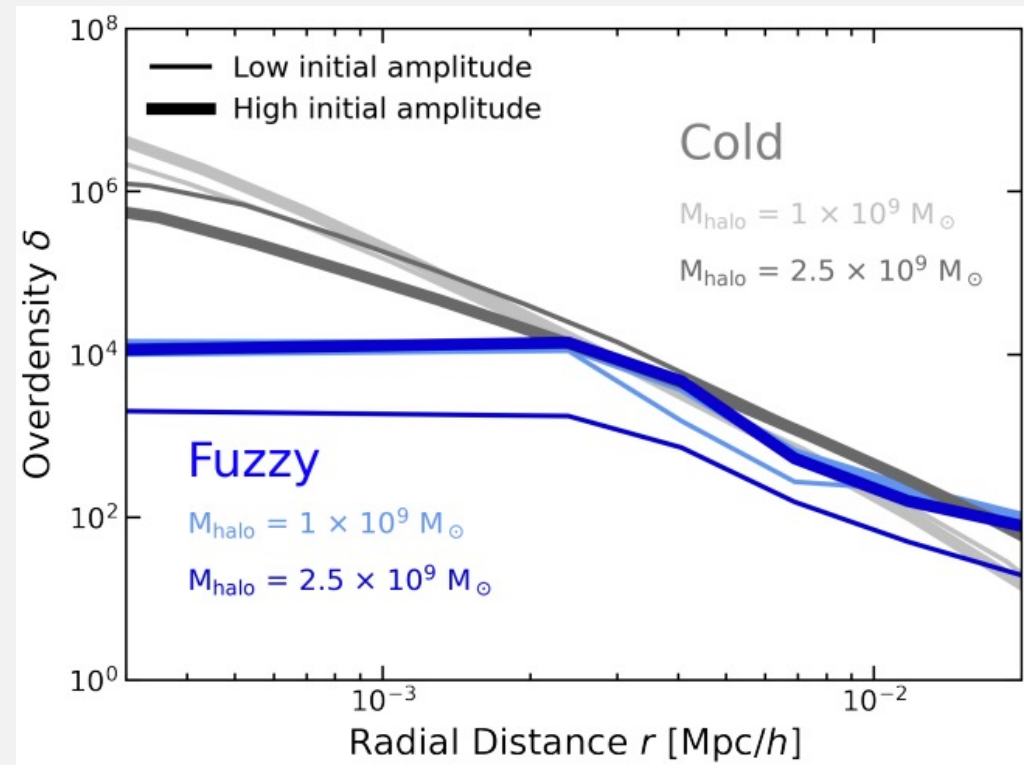




# Fuzzy Dark Matter

# Fuzzy Dark Matter

- CDM~good enough for cosmology
- Fuzzy Dark Matter
  - $m \sim 10^{-22}$  eV
  - Core-cusp problem
  - Satellites problem
  - Central Black Holes



Accessed 22 Jan 2024—<https://curj.files.wordpress.com/2022/05/screen-shot-2022-05-30-at-3.26.29-pm.png>

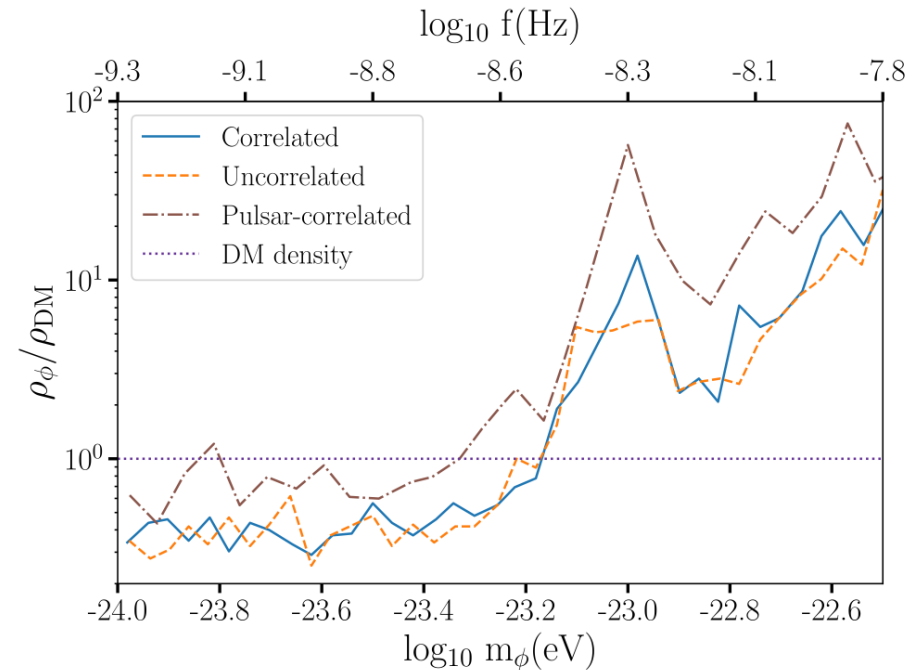
# Pulsar Timing Array Searches

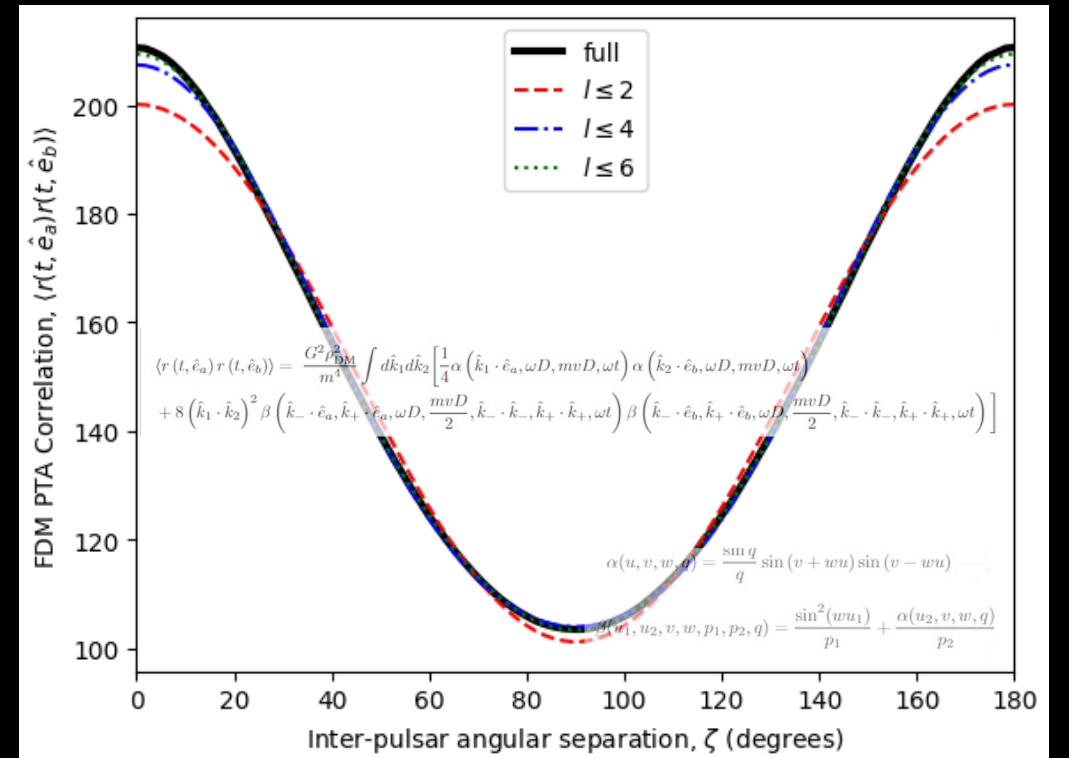
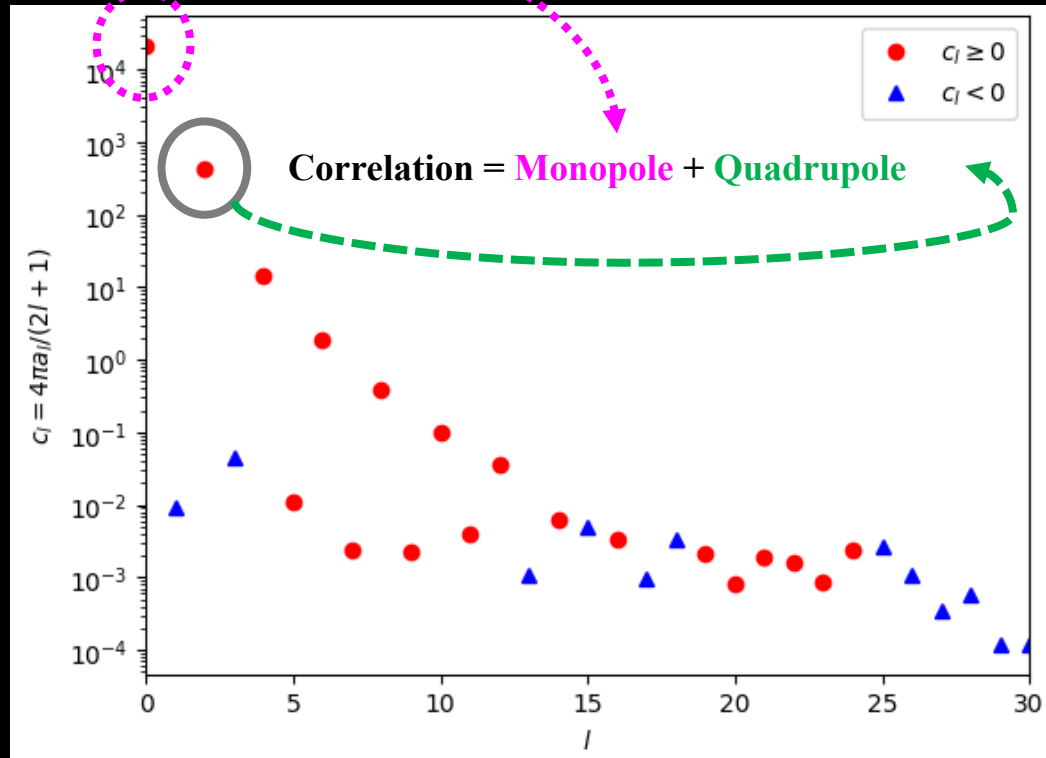
- Khmelnitsky & Rubakov, Pulsar timing signal from ultralight scalar dark matter, 1309.5888
- N.K. Porayko, K.A. Postnov, Constraints on ultralight scalar dark matter from pulsar timing, 1408.4670
- Inter-pulsar correlation  $\sim$  Monopole

$$r(t) = \text{FDM}$$

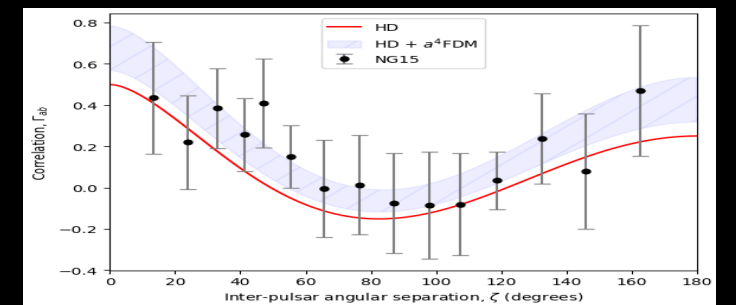
$$\zeta_{\alpha\beta} = 1/2(1 + \delta_{\alpha\beta})$$

EPTA PRL 2023





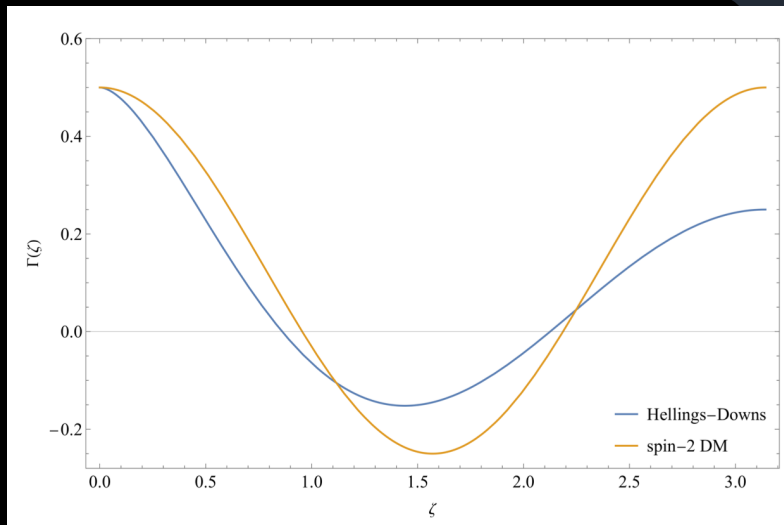
# Fuzzy Dark Matter (*in prep*)



$$\sigma_{\text{pol}}^2 = \sigma_{\text{unpol}}^2 + \frac{103}{6300} \mu_{\text{u}}^2(\gamma) \sum_j A_j^4$$

## Recent highlights by others (zero credits to me!)

- Allen & Valtolina, 2401.14329—finite sources
- Cai, Zhang, & Zhang, 2402.03984—spin-2 ULDM
- Kehagias & Riotto, 2401.10680—HD unmasked

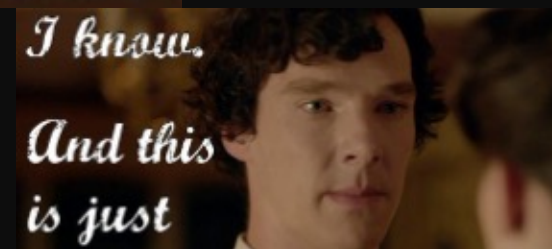


$$\Gamma_{ab} = \alpha \sigma_{ab} \ln \sigma_{ab} + \beta \sigma_{ab} + \Gamma_v$$

# Outlook



Accessed 24 Nov. 2023  
<https://i.pining.com/736x/60/5d/0f/605d0fe6df4cc7b1f37dd1fde87bf897.jpg>



## PTAfast: PTA correlations from SGWB [ascl:2211.001]

RCB & KWN

- ✓ **PS formalism** for mean and variance of **SGWB correlations**;
  - ✓ **Phenomenology** of subluminal **GW polarizations** for finite pulsar distances;
  - ✓ Analysis of **tensor & vector polarizations** off the light cone;
  - ✓ **Scalar/Vector** constraints;
  - ✓ **Playbook** for **Testing Nanohertz Gravity**.
- **Anisotropy; Fuzzy DM correlations; Coding; Coding; Coding**