TESTING THE SPEED OF GRAVITY WITH

BLACK HOLE RINGDOWN

YITP KYOTO - FEBRUARY 2024

SERGI SIRERA

[2301.10272] SS + JOHANNES NOWER







- SO WHY SHOULD WE TEST GR ?
 - · DARK ENERGY
 - · SINGULARITIES
 - · NOT QUANTIZABLE
 - • •
 - · WHY NOT?

(LOVELOCK'S THEOREM)

$$\Rightarrow S = \int d^4x \sqrt{-g} R[g_m]$$

guv

LOCAL

2nd order EOM

$$S = \int d^4x \sqrt{-g} R[g_m]$$

(LOVELOCK'S THEOREM)

LOCAL

2 order EOM

$$g_{\mu\nu} + \Phi$$
 HORNDESKI \rightarrow S = $\int d^4x \sqrt{-g^2} H[g_{\mu\nu}, \phi]$

$$S = \int d^4x \sqrt{-g'} \left(L_2 + L_3 + L_4 + L_5 \right)$$

HORNDESKI GRAVITY

$$\mathcal{L}_2 = G_2(\phi, X)$$

$$\mathcal{L}_3 = G_3(\phi, X) \Box \phi$$

$$\mathcal{L}_{4} = G_{4}(\phi, X)R + G_{4x}(\phi, X)[(\Box \phi)^{2} - (\phi_{\mu\nu})^{2}]$$

$$\mathcal{L}_{5} = G_{5}(\phi, X) G_{\mu\nu} \phi^{\mu\nu} - \frac{1}{6} G_{5\chi}(\phi, X) \left[(\Box \phi)^{3} - 3(\phi_{\mu\nu})^{2} \Box \phi + 2(\phi_{\mu\nu})^{3} \right]$$

WHERE
$$X = -\frac{1}{2} \nabla_{\mu} \Phi \nabla^{\mu} \Phi$$
 , $\Phi_{\mu} := \nabla_{\mu} \Phi$, $\Phi_{\mu\nu} := \nabla_{\nu} \nabla_{\mu} \Phi$, ...
$$G_{4x} := \partial_{x} G_{4} \qquad (\Phi_{\mu\nu})^{2} := \Phi_{\mu\nu} \Phi^{\mu\nu} \Phi^{\nu} \Phi^$$

$$S = \int d^4x \sqrt{-g} \left(L_2 + L_3 + L_4 + L_5 \right)$$

HORNDESKI GRAVITY

$$\mathcal{L}_2 = G_2(\phi, X)$$

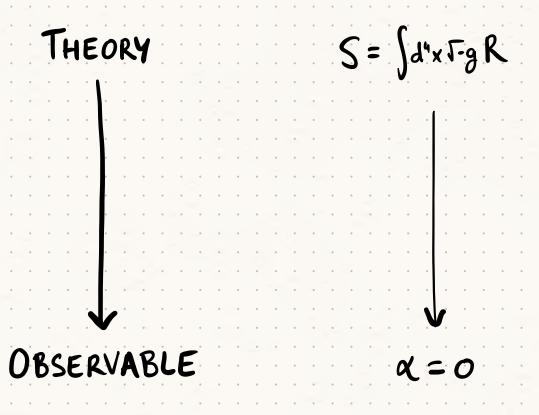
$$\mathcal{L}_3 = G_3(\phi, X) \Box \phi$$

$$L_4 = G_4(\phi, X)R + G_{4x}(\phi, X)[(\Box \phi)^2 - (\phi_{\mu\nu})^2]$$

$$\mathcal{L}_{5} = G_{5}(\phi, X) G_{\mu\nu} \phi^{\mu\nu} - \frac{1}{6} G_{5\chi}(\phi, X) \left[(\Box \phi)^{3} - 3(\phi_{\mu\nu})^{2} \Box \phi + 2(\phi_{\mu\nu})^{3} \right]$$

When Prof. Lovelock and I saw how complex the Lagrangian which yields the most general second-order scalar-tensor field equations in a space of four-dimensions were, we felt that clearly puts the kibosh on scalar-tensor field theories. There were just too many of them, and they are way too complicated. We wondered who would be crazy enough to work with such equations. Then crazy showed up! And is still here today. It will be the task of my

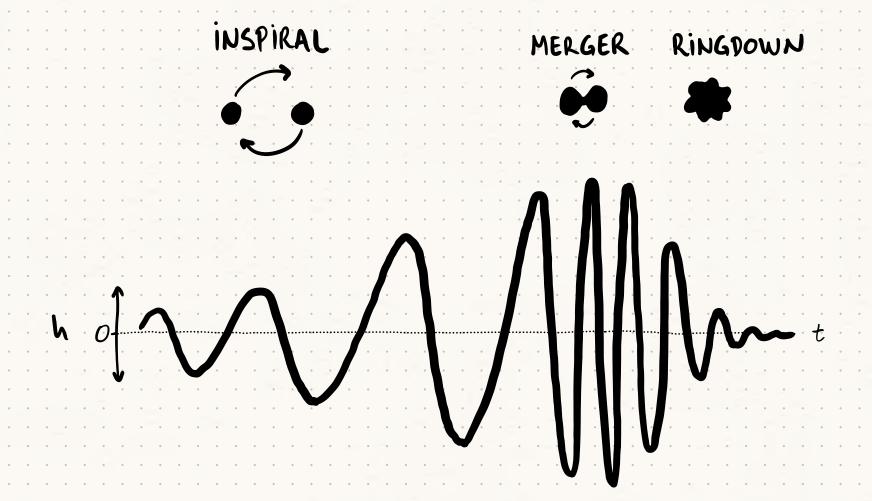
[2402.07538] HORNDESKI + SILVESTRI



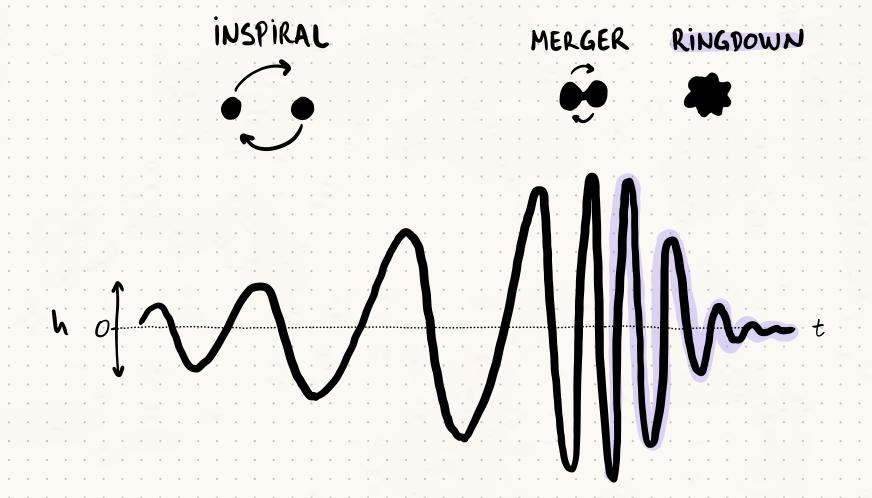
$$S = \int d^4x \, \nabla g \, H$$

"SMOKING
GUN SIGNAL"

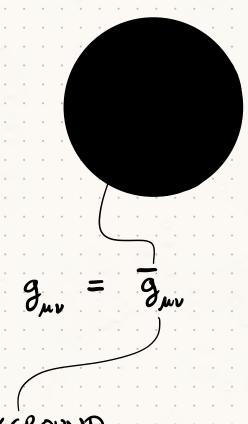
ASTROPHYSICAL SOURCES: MERGERS (BLACK HOLES / NEUTRON STARS)



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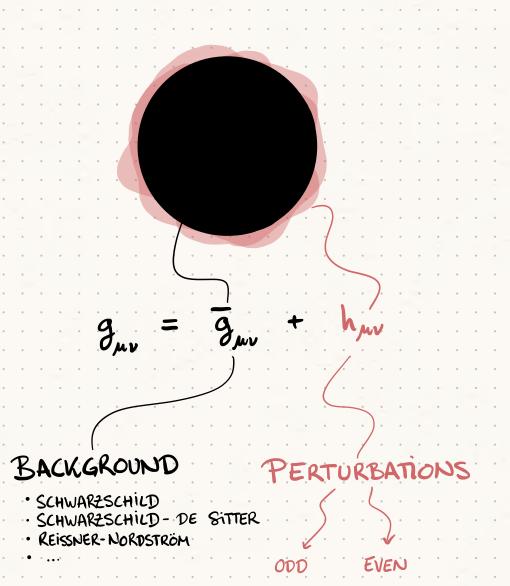
RINGDOWN: BLACK HOLE PERTURBATION THEORY



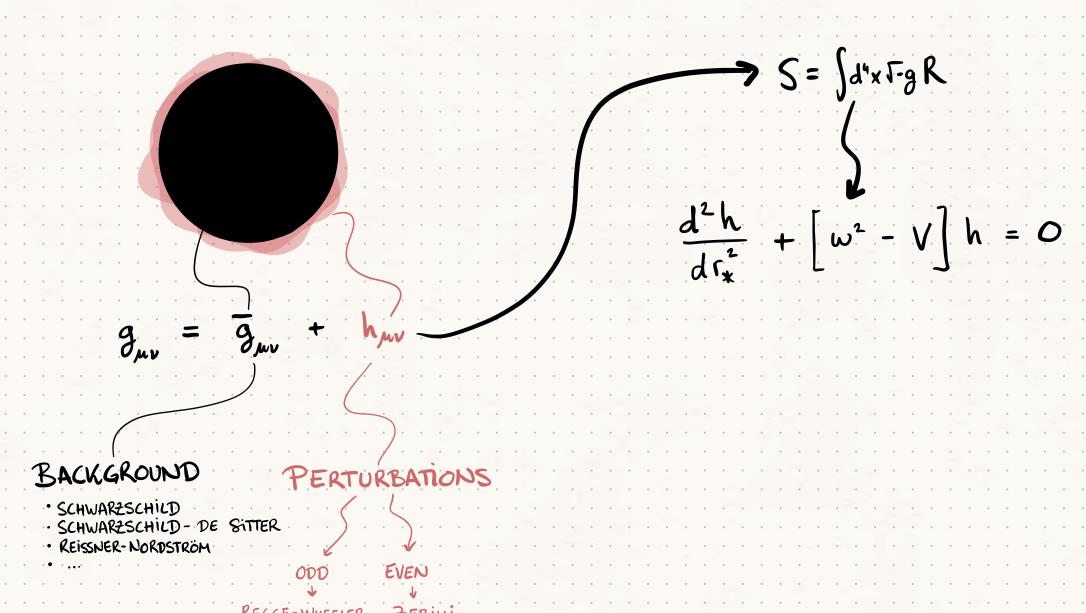
BACKGROUND

- · SCHWARZSCHILD DE SITTER
- · REISSNER-NORDSTRÖM

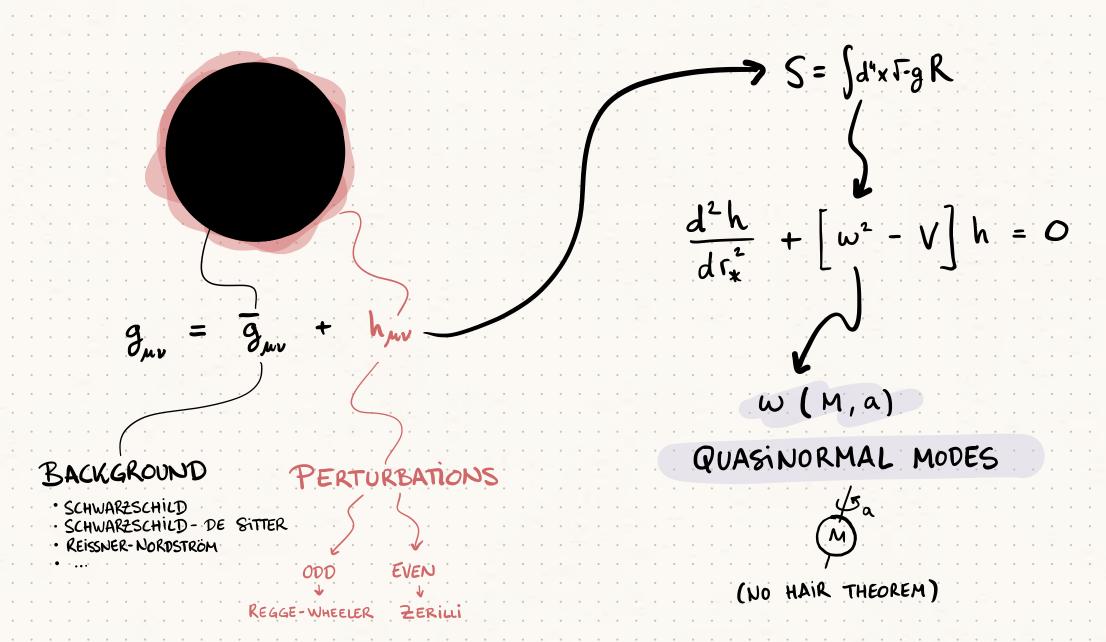
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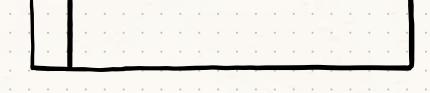


BLACK HOLE SPECTROSCOPY

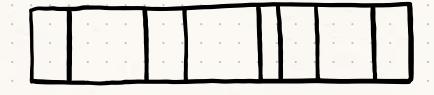
W(M,a) · 1st QNM sets (M,a)

BLACK HOLE SPECTROSCOPY

w (M,a) . 1st QNM sets (M,a)



· All other QNMs are fixed in GR

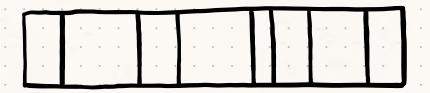


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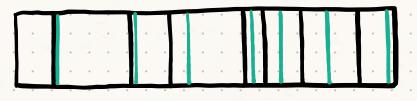
W (M,a) . 1st QNM sets (M,a)



· All other QNMs are fixed in GR



MEASURING QNMs PROVIDES CLEAN TESTS OF BACKGROUND GEOMETRY AND UNDERLYING THEORY



GR w(M,a)

GR

$$S = \int d^4x \sqrt{-g} R(g_m)$$

$$\frac{d^2h}{dr_*^2} + \left[w^2 + V\right]h = 0$$

$$w(M, a)$$

$$\alpha_T = 0$$

HORNDESKI

$$S = \int d^4x \sqrt{-g} H(g_{\mu\nu}, \Phi)$$

$$\frac{d^2h}{dr_*^2} + \left[\omega^2(1+\alpha_T) + V + \alpha_T SV\right]h = 0$$

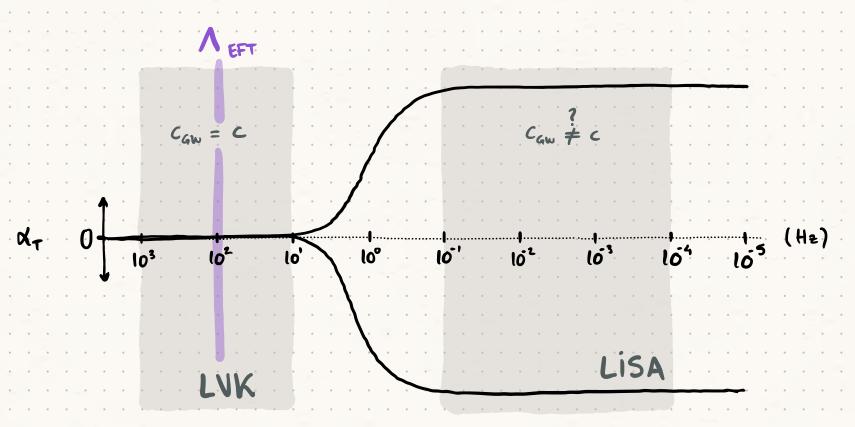
$$\omega(M, \alpha, \alpha_T)$$

$$\alpha_{T} = \frac{C_{GW} - C}{C} \neq 0$$

GRAVITATIONAL WAVE SPEED EXCESS

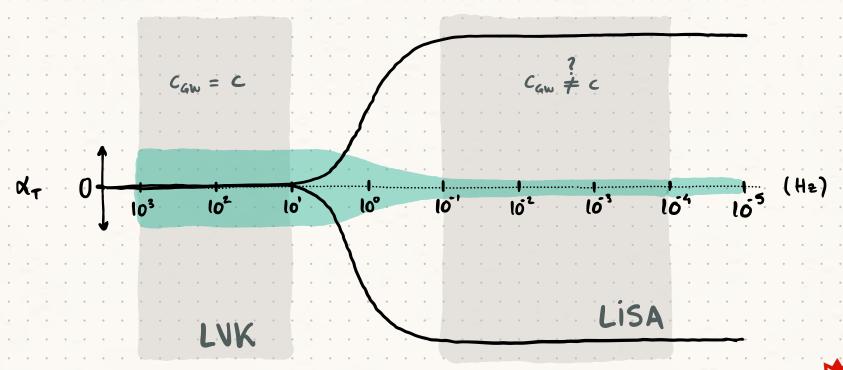
WHAT DO WE KNOW ABOUT QT?

- Ligo: $\alpha_{\tau} \lesssim 10^{-15}$ (GW170817)
- DARK ENERGY EFTS: CUTOFF AT ~10 Hz [1806.09417] MELMILE + DE RHAM



WHAT DO WE KNOW ABOUT QT?

- Ligo: dt & 1015 (GW170817)
- DARK ENERGY EFTS: CUTOFF AT ~102 Hz



FISCHER FORECASTS:

FOR 1 LOUD MERGER:

[2301.10272]

SS, JOHANNES NOLLER



☐ sergisl / ringdown-calculations Public



[2301.10272] SS+ JOHANNES NOUER

BACKGROUND:

$$\bar{g}_{\mu\nu} = -\int dt^2 + \int dr^2 + r^2 d\Omega_2^2, \quad f = 1 - \frac{2M}{r}$$

$$\frac{1}{\phi} = \phi + \varepsilon \delta \phi (r) , \quad \delta \phi = \varphi_c \frac{2M}{c}$$





[2301.10272] SS + JOHANNES NOWER

BACKGROUND:

$$\overline{\phi} = \phi + \varepsilon \delta \phi (r) , \quad \delta \phi = \varphi_c \frac{2M}{r}$$

THEORY :

HORNDESKI WITH G40 = 0







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BACKGROUND:

$$\overline{g}_{\mu\nu} = -\int dt^2 + \int dr^2 + r^2 d\Omega_2^2, \quad f = 1 - \frac{2M}{c}$$

$$\frac{1}{\phi} = \frac{\lambda}{\phi} + \varepsilon \delta \phi (r) , \quad \delta \phi = \varphi_c \frac{2M}{c}$$

THEORY :

HORNDESKI WITH G40 = 0

MODIFIED REGGE - WHEELER EQUATION

$$\frac{d^{2}h}{ds_{+}^{2}} + \left[w^{2} (1 + d_{T}) + V + d_{T} SV \right] h = 0$$

$$XT = -\frac{1}{3}(2M)^2 G_T S\phi^{1/2}$$
 $G_T = \frac{G_{4x} - G_{5\phi}}{G_4}$





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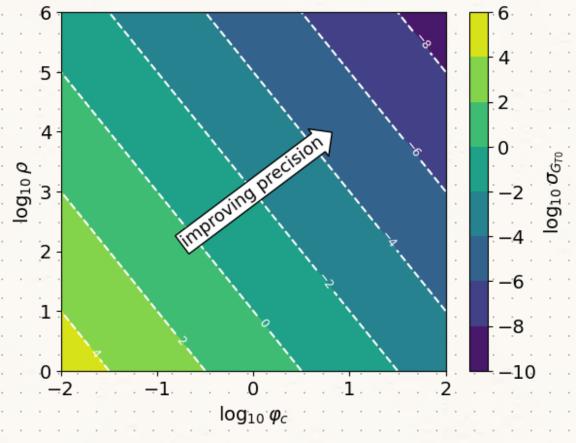
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MODIFIED REGGE - WHEELER EQUATION

$$\frac{d^{2}h}{dr_{*}^{2}} + \left[\omega^{2} (1 + d_{T}) + V + d_{T} SV \right] h = 0$$

$$X_T = - \frac{1}{2} (2M)^2 G_T S_{\phi}^{1/2}$$

$$G_T = \frac{G_{4x} - G_{5\phi}}{G_4}$$









$$\overline{g}_{\mu\nu} = -\int dt^{2} + \int dr^{2} + r^{2} d\Omega_{2}^{2}, \quad \int = 1 - \frac{2M}{c} - \frac{1}{3} \Lambda c^{2}$$

$$\overline{\Phi} = qt + V(c)$$

SOLUTIONS FOR SHIFT + REFLECTION SYMMETRIC HORNDESKI: G2(X), G4(X)

[1312.3204] BABICHEV + CHARMOUSIS, [1403.4364] KOBAYASHI + TANAHASHI



$$\overline{g}_{mv} = -\int dt^2 + \int dr^2 + r^2 d\Omega_{2}^2, \quad \int = 1 - \frac{2M}{c} - \frac{1}{3} \Lambda r^2$$

$$\bar{\phi} = qt + \gamma(c)$$

SOLUTIONS FOR SHIFT + REFLECTION SYMMETRIC HORNDESKI: G2(X), G4(X)

[1312.3204] BABICHEV + CHARMOUSIS, [1403.4364] KOBAYASHI + TANAHASHI

HOWEVER, THEY ARE PRONE TO INSTABILITY ISSUES

[1510.07400] OGAWA + KOBAYASHI + SUYAMA , [1803.11444] BABICHEV + CHARMOUSIS + ESPOSITO - FARÈSE + LEHÉBEL [1610.00432] TAKAHASHI + SUYAMA, [1904.03554] TAKAHASHI + MOTOHASHI + MINAMITSUSI, [1907.00699] DE RHAH + ZHANG



$$\bar{g}_{\mu\nu} = -\int dt^2 + \int dr^2 + r^2 d\Omega_{2}^2, \quad \int = 1 - \frac{2M}{c} - \frac{1}{3} \Lambda c^2$$

$$\overline{\phi} = 4 + \gamma \gamma(c)$$

SOLUTIONS FOR SHIFT + REFLECTION SYMMETRIC HORNDESKI: G2(X), G4(X)

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ALL CASES STUDIED ASSUMED X = - 1 2 4 7 4 = constant

SOLUTION WITH X = constant FOR Gz = -21 + 27/X, G4 = 1 + NX

L [2310.11919] BAKOPOULOS + CHARMOUSIS + KANTI + LECOEUR + NAKAS

CAN X = constant HELP?

BACKGROUND

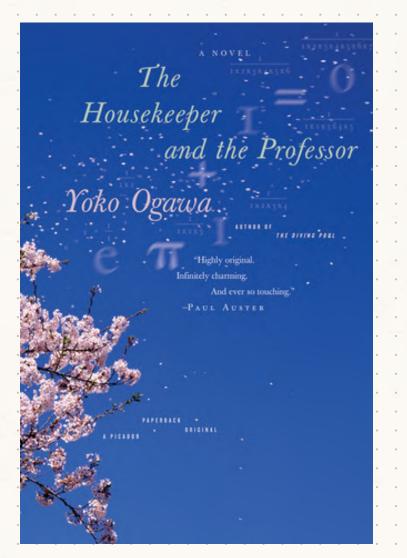
Sas,
$$\phi = qt + \gamma(c)$$

THEORY

$$\mathcal{L} = -2\Lambda + 2\eta \sqrt{X} + (1 + \lambda \sqrt{X})R + \frac{\lambda}{2\sqrt{X}} (\Box \phi^2 + \phi_{\mu\nu}^2)$$

BACKGROUND

Sas,
$$\phi = qt + V(r)$$



THEORY

$$\mathcal{L} = -2\Lambda + 2\eta \sqrt{X} + (1 + \lambda \sqrt{X})R + \frac{\lambda}{2\sqrt{X}} (\Box \phi^2 + \phi_{\mu\nu}^2)$$

1

We called him the Professor. And he called my son Root, because, he said, the flat top of his head reminded him of the square root sign.

"There's a fine brain in there," the Professor said, mussing my son's hair. Root, who wore a cap to avoid being teased by his friends, gave a wary shrug. "With this one little sign we can come to know an infinite range of numbers, even those we can't see." He traced the symbol in the thick layer of dust on his desk.



Of all the countless things my son and I learned from the Professor, the meaning of the square root was among the most important. No doubt he would have been bothered by my use of the word *countless*—too sloppy, for he believed that the very origins of the universe could be explained in the exact language of numbers—but I don't know how else to put it. He taught us about enormous prime numbers with more than a hundred thousand places, and the largest number of all, which was used in mathematical proofs and was in the *Guinness Book of Records*, and about the idea of something beyond infinity. As interesting as all this was, it could never match the experience of simply spending time with the Professor. I remember when he taught us about the spell cast by placing numbers under this square root sign. It was a rainy evening in early April. My son's schoolbag lay abandoned on

"I'm going to call you Root," he said. "The square root sign is a generous symbol, it gives shelter to all the numbers." And he quickly took off the note on his sleeve and made the addition: "The new housekeeper ... and her son, ten years old, "."

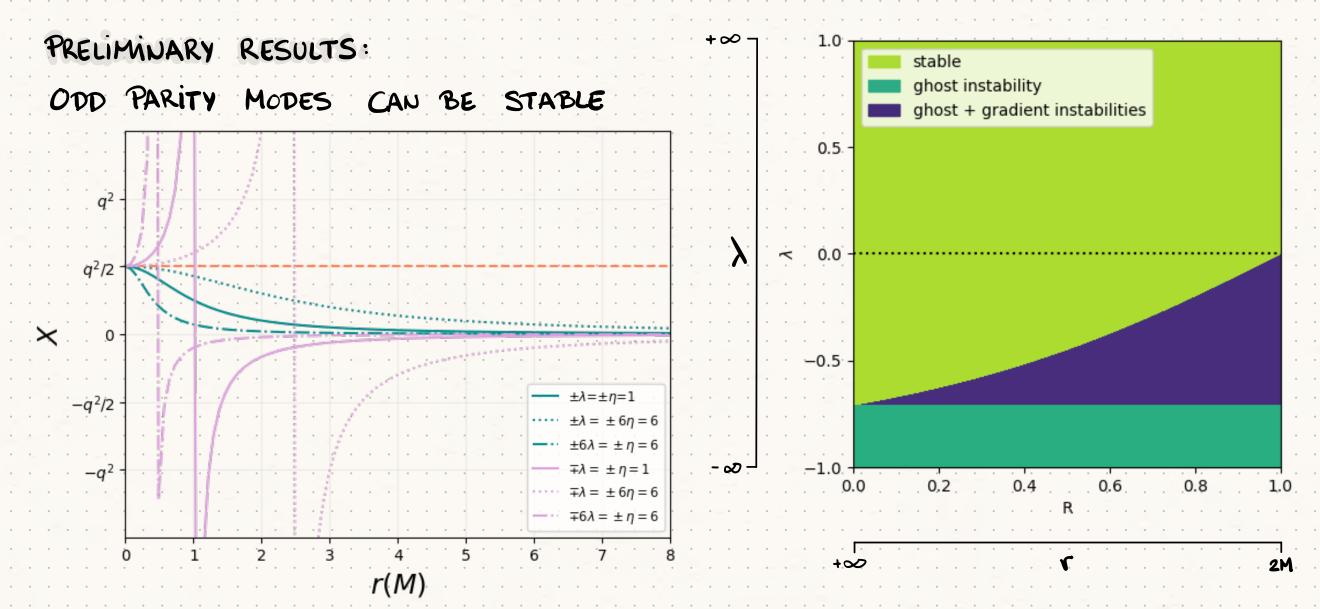


BACKGROUND

THEORY

Sas,
$$\phi = qt + \psi(r)$$

$$\mathcal{L} = -2\Lambda + 22\sqrt{X} + (1 + \lambda \sqrt{X})R + \frac{\lambda}{2\sqrt{X}} \left(\Box \phi^2 + \phi_{\mu\nu}^2\right)$$



SUMMARY

- · QNMs CAN BE USED TO TEST NEW GRAVITATIONAL PHYSICS
- · SPEED OF GWS # SPEED OF LIGHT IN SOME HORNDESKI THEORIES
- · QNMs ARE AT-DEPENDENT IF 3 SCALAR HAIR
- · LISA CAN CONSTRAIN IDTIS 104 WITH RINGDOWN OF ONE SMBH MERGER

ONGOING WORK:

- PROUNG STABILITY OF ODD PARITY MODES FOR TIME-DEPENDENT SOWTIONS IN 'ROOT-X' THEORY
- · QUASINORMAL MODES ?

THANKS!

Osergisirera

BACKUP SLIDES

BLACK HOLE PERTURBATIONS IN REGGE-WHEELER GAUGE

$$h_{\mu\nu} = h_{\mu\nu}^{odd} + h_{\mu\nu}^{even}$$

$$h_{\mu\nu}^{odd} = \begin{pmatrix} 0 & 0 & -h_0 \frac{1}{\sin \theta} \partial_{\theta} Y_{em} & h_0 \sin \theta \partial_{\theta} Y_{em} \\ -h_0 \frac{1}{\sin \theta} \partial_{\theta} Y_{em} & -h_1 \frac{1}{\sin \theta} \partial_{\theta} Y_{em} & 0 \\ h_0 \sin \theta \partial_{\theta} Y_{em} & h_1 \sin \theta \partial_{\theta} Y_{em} & 0 \end{pmatrix}$$

QUADRATIC ACTION IN GR

$$S^{(2)} = \frac{1}{4} \int \sqrt{-g} d^4x \left[-h_{\mu\nu}h^{\mu\nu} + \nabla_{c}h\nabla^{c}h - \nabla_{\mu}h_{\nu\sigma}\nabla^{\mu}h^{\nu\sigma} + 2\nabla_{\mu}h^{\mu\nu}\nabla_{\sigma}h^{\nu\sigma} - 2\nabla^{\mu}h\nabla_{\nu}h_{\mu\nu} + 2(h_{\sigma}^{\nu}h^{\sigma\mu} - h_{\mu}h^{\mu\nu})R_{\mu\nu} - (h_{\mu\nu}h^{\mu\nu} - \frac{1}{2}h^2)R + 2h^{\mu\nu}h^{\sigma\lambda}R_{\mu\sigma\nu\lambda} \right]$$

QUADRATIC ACTION HORNDESKI ODD SECTOR IN COMPONENTS

$$S^{(2)} = \int dt dr \left[\alpha_{1} h_{o}^{2} + \alpha_{2} h_{i}^{4} + \alpha_{3} \left(\dot{h}_{i}^{2} + \dot{h}_{o}^{12} - 2 \dot{h}_{o}^{2} \dot{h}_{i} + \frac{4}{5} \dot{h}_{i} \dot{h}_{o} \right) \right]$$

$$= \alpha_{i} = \frac{L(1+i)}{2c^{4}} \left[(r \mathcal{H})^{2} + \frac{(l-i)(l+2)\mathcal{G}}{2\mathcal{B}} + \frac{c^{2}}{6} \mathcal{E}_{h} \right]$$

$$= \alpha_{2} = -\frac{L(l+i)}{2} \mathcal{B} \left[\frac{(l-i)(l+2)\mathcal{G}}{2c^{4}} + \mathcal{E}_{B} \right]$$

$$= \alpha_{3} = \frac{L(l+i)}{4} \mathcal{H}$$

$$= 2 \left[G_{4} - 2 \chi G_{4\chi} + \chi \left(\frac{\mathcal{B}}{2} \dot{d} \dot{d} G_{5\chi} + G_{5\varphi} \right) \right]$$

$$= \frac{L(l+i)}{4(l-i)(l+2)} \int dt dr_{*} \left[\frac{\mathcal{F}}{3} \dot{\mathcal{G}}^{2} - \left(\frac{d\mathcal{Q}}{dr_{*}} \right)^{2} - V(i)\mathcal{Q}^{2} \right]$$

$$= \frac{L(l+i)}{4(l-i)(l+2)} \int dt dr_{*} \left[\frac{\mathcal{F}}{3} \dot{\mathcal{G}}^{2} - \left(\frac{d\mathcal{Q}}{dr_{*}} \right)^{2} - V(i)\mathcal{Q}^{2} \right]$$

$$= \frac{\alpha_{3}}{6} \dot{q}$$

EXISTING & UPCOMING XT CONSTRAINTS

10/1 & 10° f~ 10" - 10" Ha	CMB & LSS
$ x_{T} \lesssim 10^{-2}$ $f \sim 10^{5}$ Hz	HULSE - TAYLOR BINARY [1507.05047] BELTRAN SIMENEZ ET. AL.
10/1 10 10 1 10 - 104 Hz	ECLIPSING WHITE-DWARF BINARY [1908.00678] LITTENBERG ET.
d ₇ % 10 ⁴	REDSHIFT-INDUCED &-DEPENDENCE [2203.00566] BAKER ET. AI
10/1 × 1017 }~ 10'-104 Ha	1-DEPENDENT WAVEFORMS [2207.10096] HARRY AND NOLLER
$ \alpha_{T} \lesssim \bar{0}^{15} $ $\int_{10^{15}}^{15} d^{3} - \bar{0}^{4} H_{4}$	MULTIBAND [2209.14398] BAKER ET AL. [1602.06951] SESANA [2207.10096] HARRY AND NOLLER
10-1 & 10 ¹⁵ }~ 10 ² HZ	Gw170817