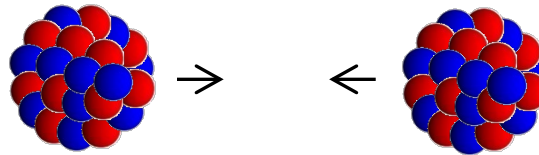


# Imaging quantum decoherence in nuclear reactions

Kouichi Hagino

Kyoto University, Kyoto, Japan



- ✓ nuclear reactions as a tool
- ✓ nuclear reactions as many-body phenomena ←

1. Introduction: interferences in nuclear reactions
2. A new attempt: imaging of nuclear reactions
3. Summary

# Nuclear Reactions

## nucleus: a composite system

- ✓ a rich reaction processes
- ✓ a rich interplay between nuclear structure and reaction

- ✓ elastic scattering
- ✓ inelastic scattering
- ✓ transfer reactions
- ✓ fusion reactions
- ✓ .....

- ✓ g.s. properties (mass, size, **shape**....)
- ✓ **excitations**

## physics of nuclear reactions:

a unified description of these nuclear reaction processes

cf. Francesco Cappuzzello's talk

**Nuclear Reactions: a variety of quantum mechanical natures**

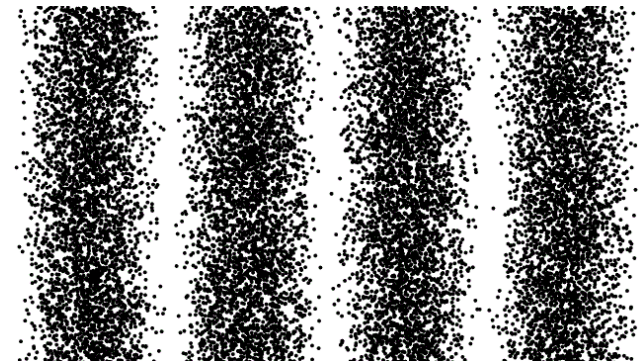
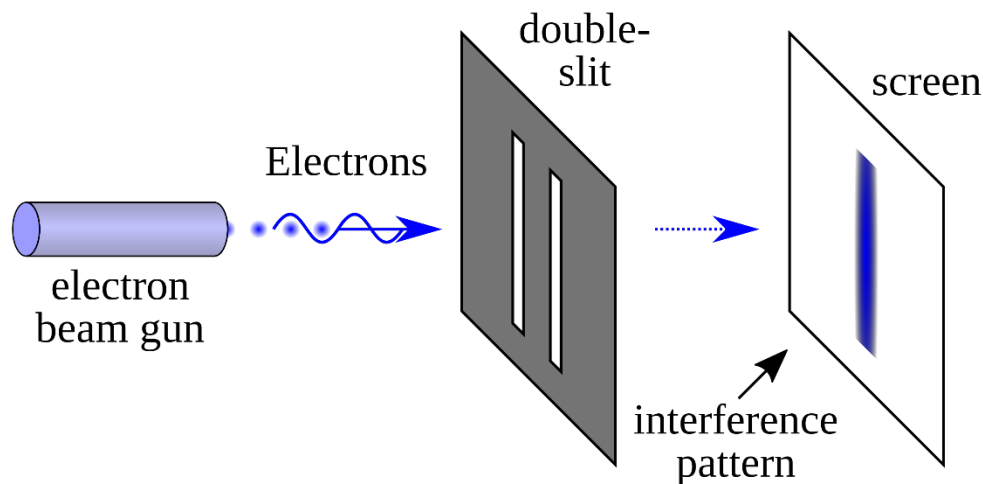
# Manifestation of Quantum Nature in Nuclear Reactions

a superposition principle

$$\psi = \alpha\psi_1 + \beta\psi_2$$

$$\rightarrow |\psi|^2 = |\alpha\psi_1|^2 + |\beta\psi_2|^2 + \underbrace{(\alpha\psi_1)^*(\beta\psi_2) + (\alpha\psi_1)(\beta\psi_2)^*}_{\text{interference}}$$

when two processes are in principle indistinguishable  
→ take square after adding two amplitudes

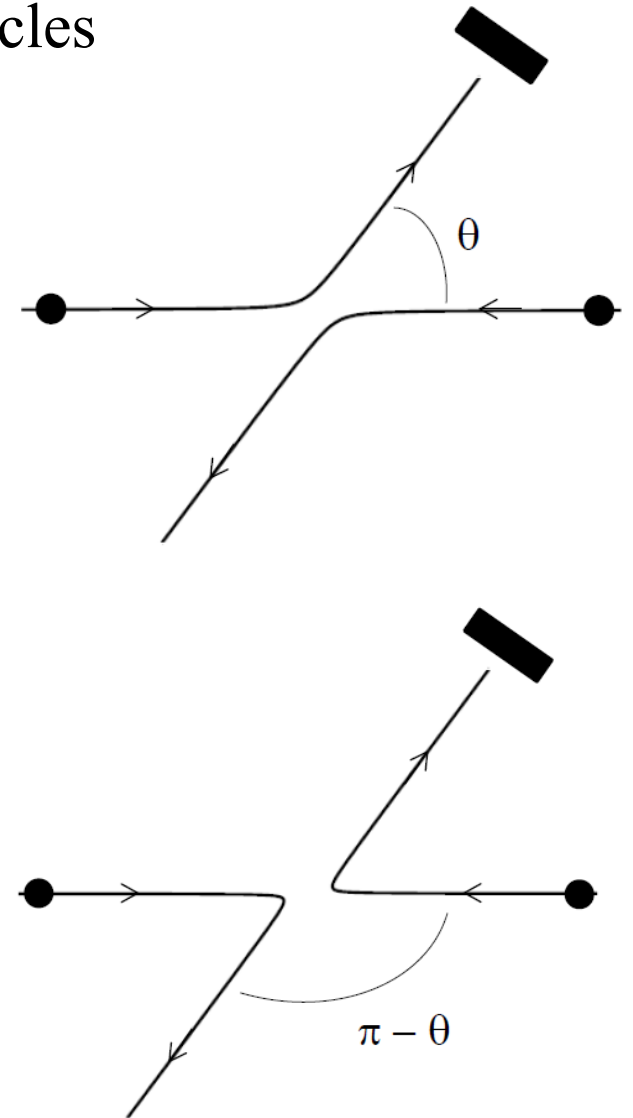
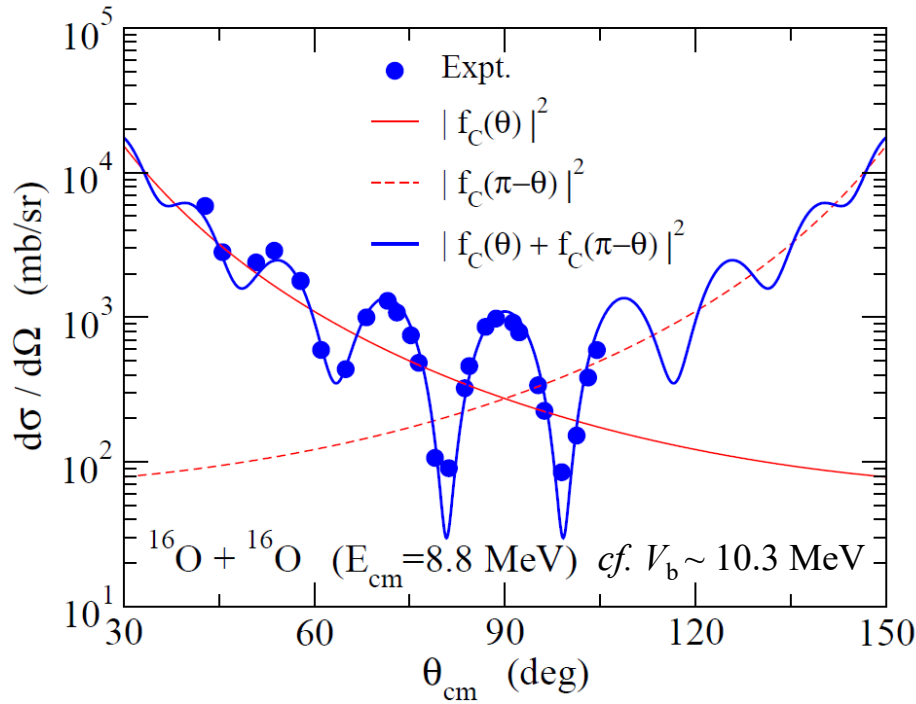


Wikipedia

# Manifestation of Quantum Nature in Nuclear Reactions

Mott Scattering: scattering of identical particles

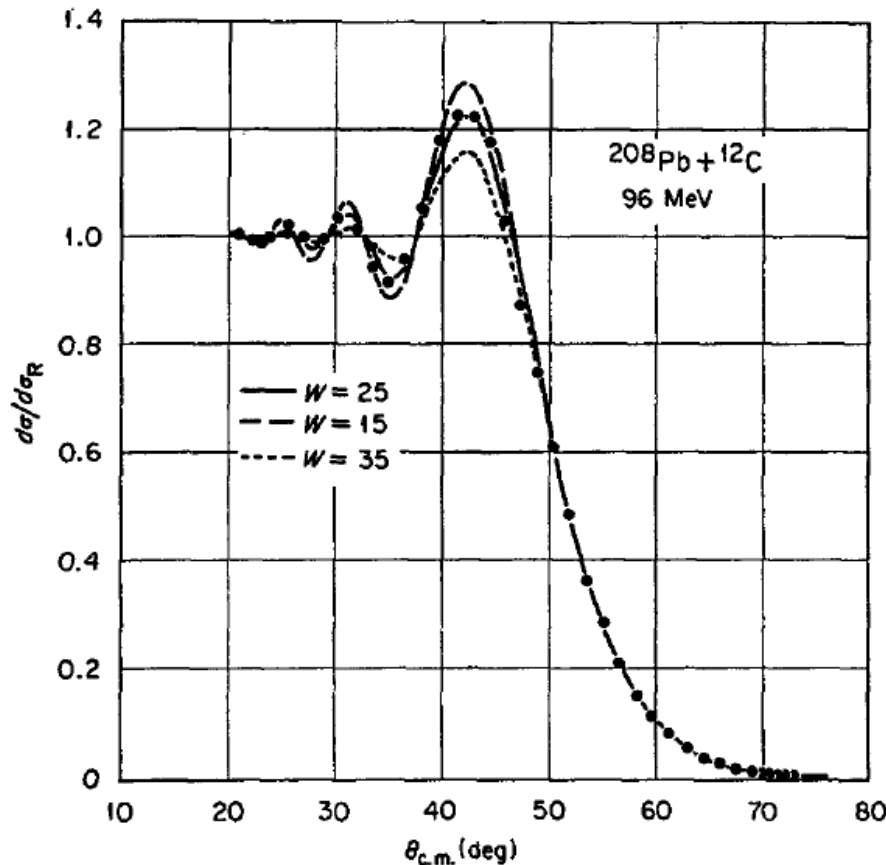
$$\frac{d\sigma}{d\Omega} = |f(\theta) \pm f(\pi - \theta)|^2$$



expt: D.A. Bromley et al., Phys. Rev. 123 ('61)878

➤ Coulomb-Nuclear interference

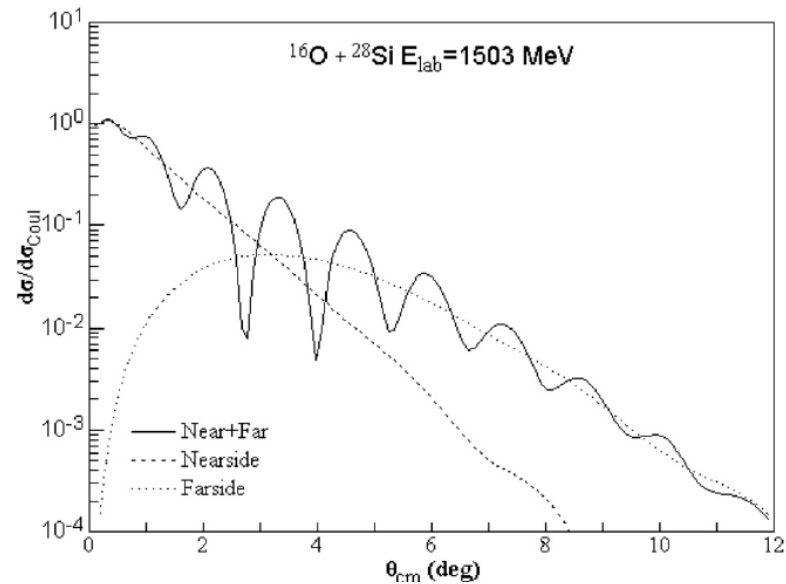
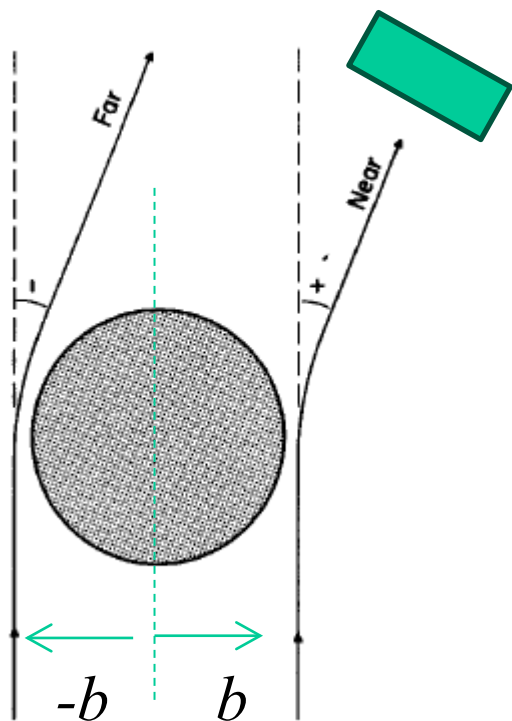
$$f(\theta) = f_C(\theta) + f_N(\theta) \rightarrow \frac{d\sigma}{d\Omega} = |f(\theta)|^2$$



J.B. Ball et al.,  
NPA252 ('75) 208

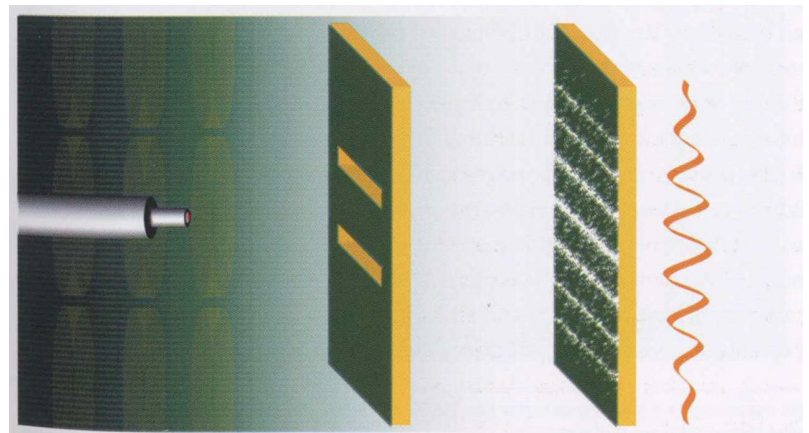
a special case: Fresnel oscillations ( $S_l = 0$  ( $l < l_g$ );  $S_l = e^{2i\sigma_l}$  ( $l > l_g$ ))

➤ near side - far side interference



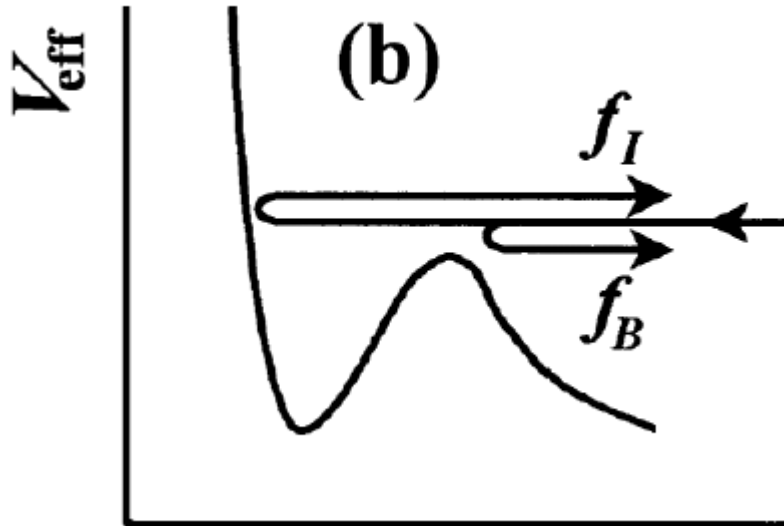
M.H. Cha,  
Comp. Phys. Comm. 176 ('07) 318

R.C. Fuller, PRC12('75)1561  
N. Rowley and C. Marty,  
NPA266('76)494  
M.S. Hussein and K.W. McVoy,  
Prog. in Part. and Nucl. Phys.  
12 ('84)103

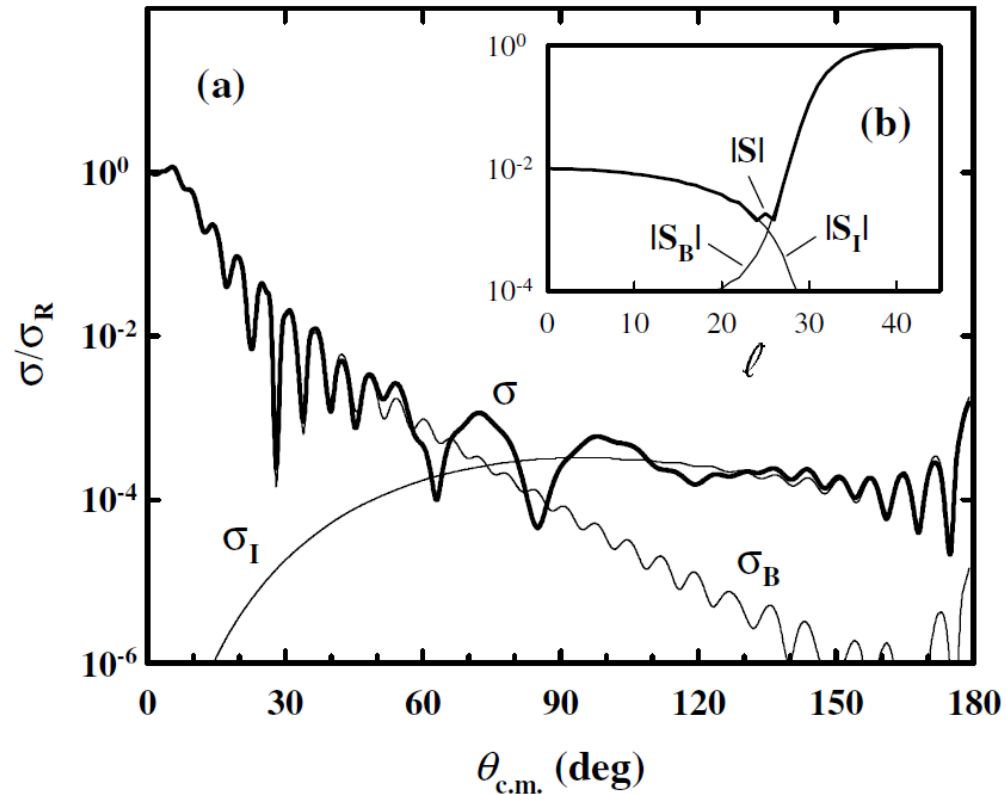


➤ barrier wave – internal wave interference

cf. D.M. Brink and N. Takigawa, NPA279 ('77) 159



$^{16}\text{O}+^{16}\text{O}$  at 124 MeV



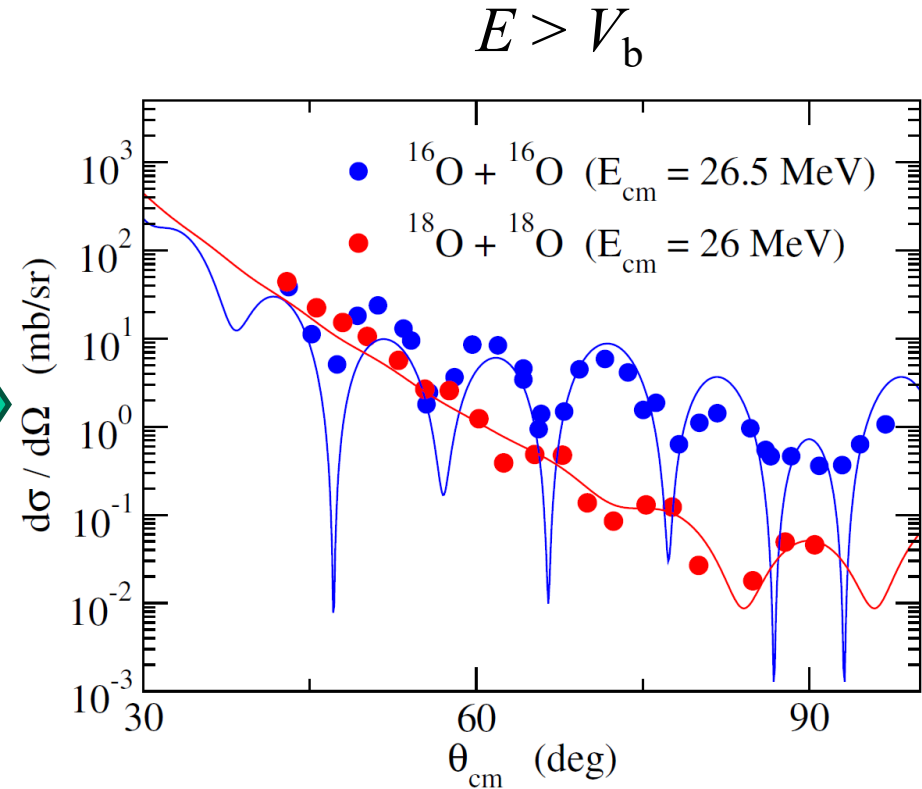
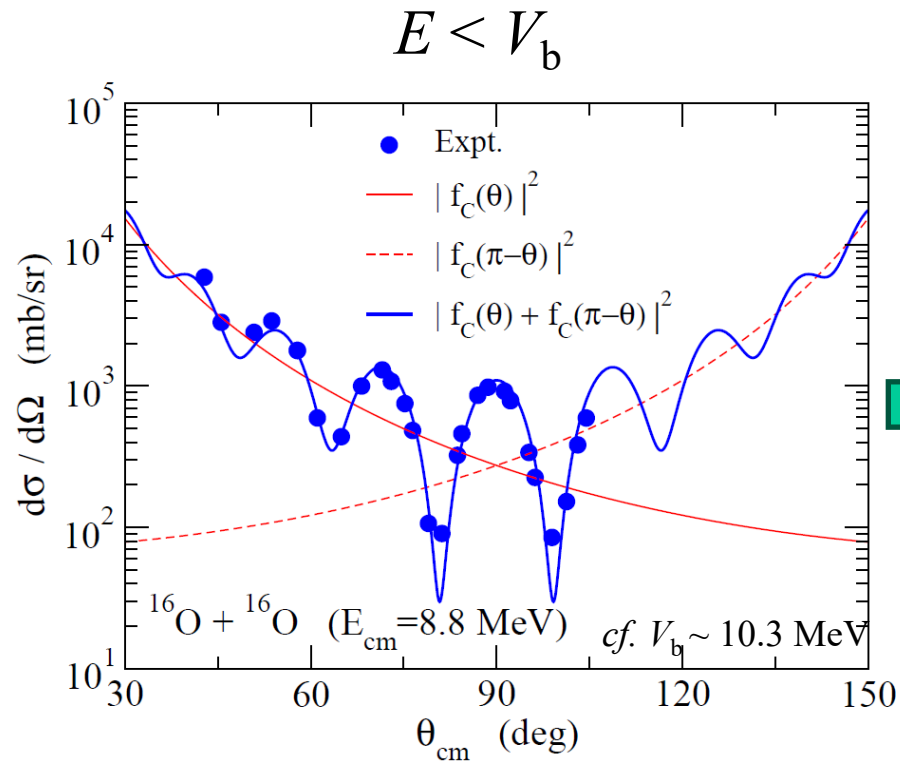
David M Brink



F. Michel et al., PRL85 ('00) 1823

anomalous large angle scattering

# $^{16}\text{O}+^{16}\text{O}$ system

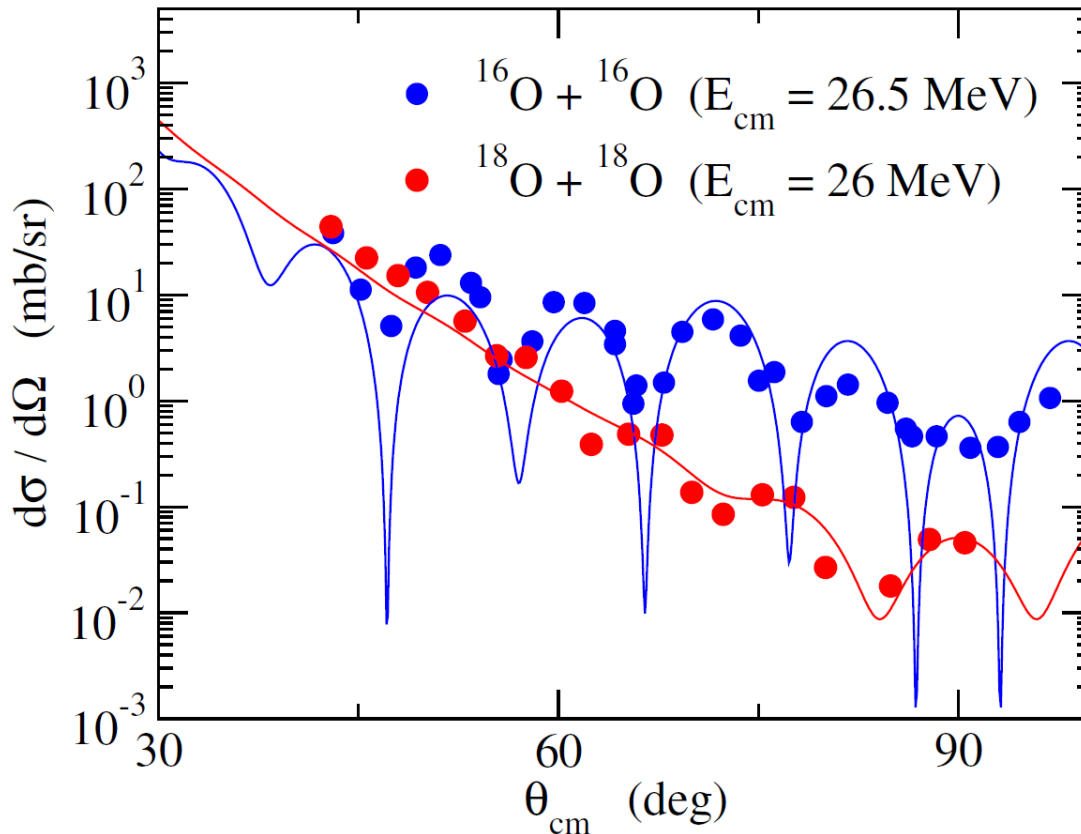


expt: D.A. Bromley et al., Phys. Rev. 123 ('61)878

R.H. Siemessen et al., PRL19 ('67) 369  
R. Vandenbosch et al., NPA230 ('74) 59



# Comparison between $^{16}\text{O}+^{16}\text{O}$ and $^{18}\text{O}+^{18}\text{O}$



$^{16}\text{O}, ^{18}\text{O}: I^\pi(\text{g.s.}) = 0^+$   
(both are bosons)

$$V_b \sim 10.3 \text{ MeV}$$

$$\longrightarrow E_{\text{cm}} \sim 2.5 V_b$$

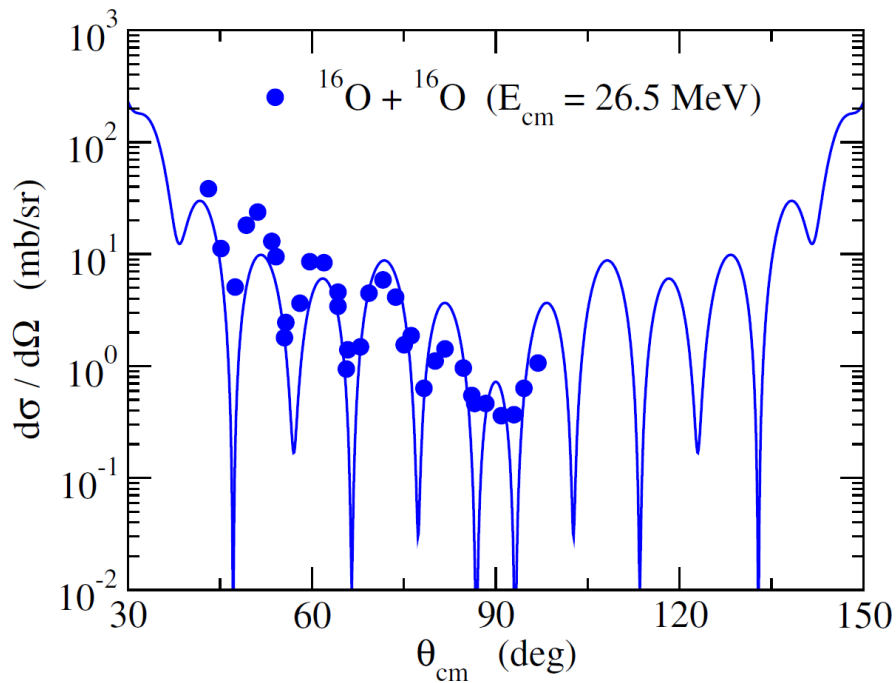
$^{18}\text{O}+^{18}\text{O}$  : much less pronounced interference pattern

$^{18}\text{O} = ^{16}\text{O}$  (double closed shell) + 2n

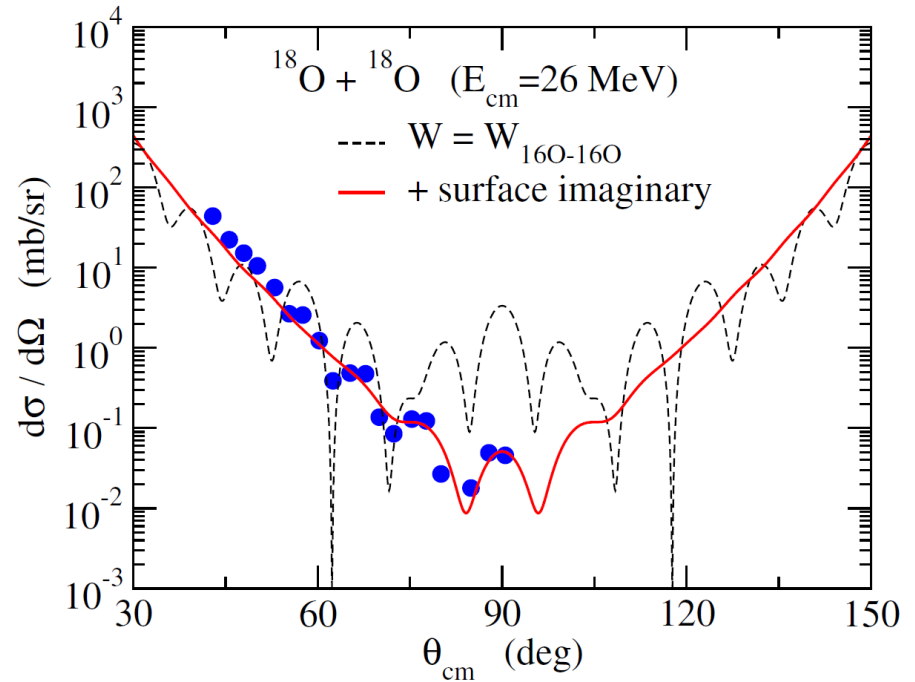
→ stronger coupling to environment

**→** manifestation of environmental decoherence?

# Optical potential model calculation



an opt. pot. model calculation  
with a deep  $WS^2$  potential.

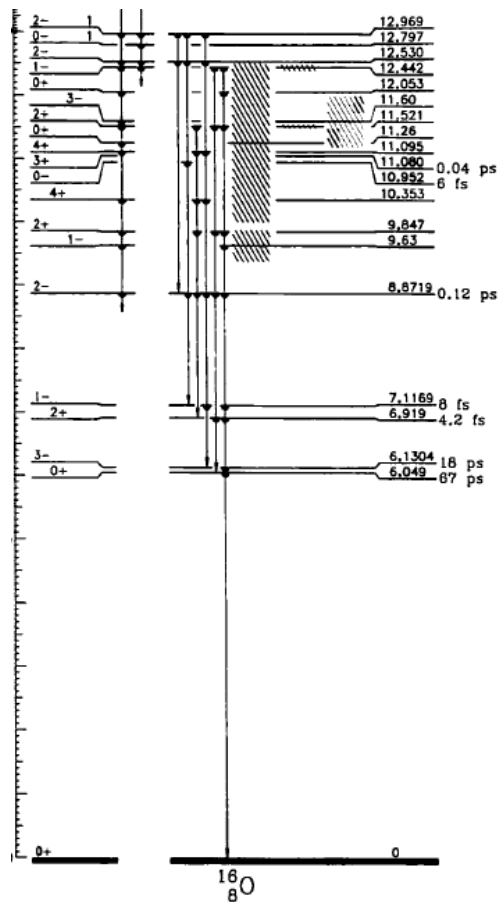


**However**, the same opt. pot.  
does not fit  $^{18}\text{O} + ^{18}\text{O}$



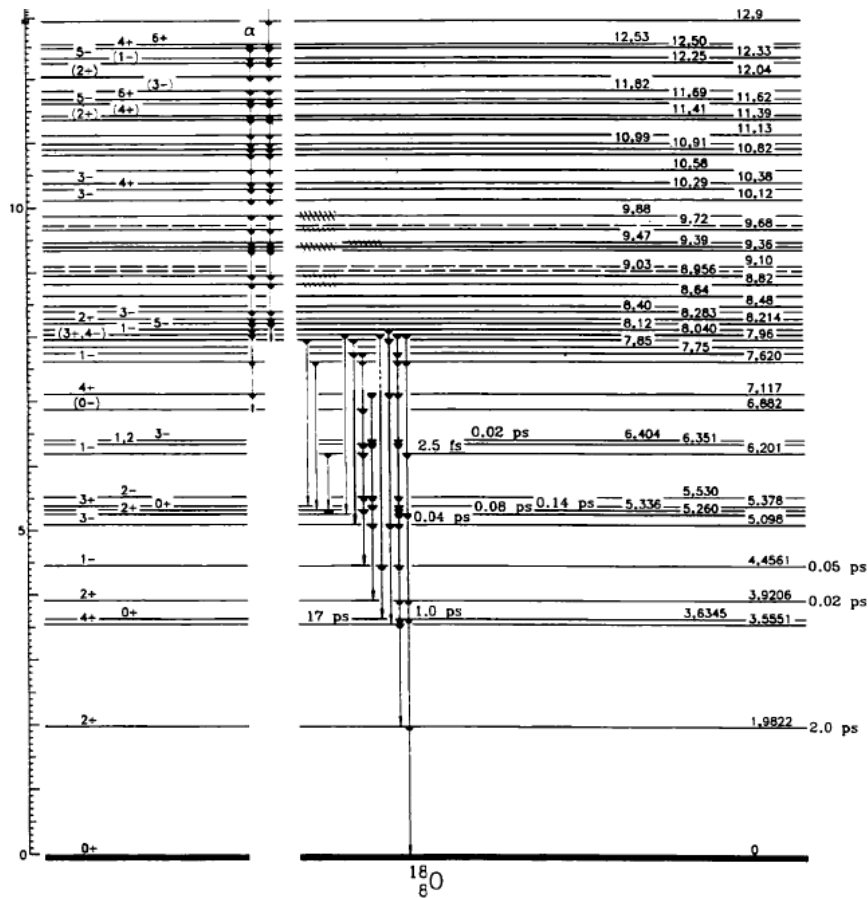
need to increase  $W$   
(with a surface imaginary pot.)

# Spectra up to $E^* = 13$ MeV



$^{16}\text{O}$

20 levels

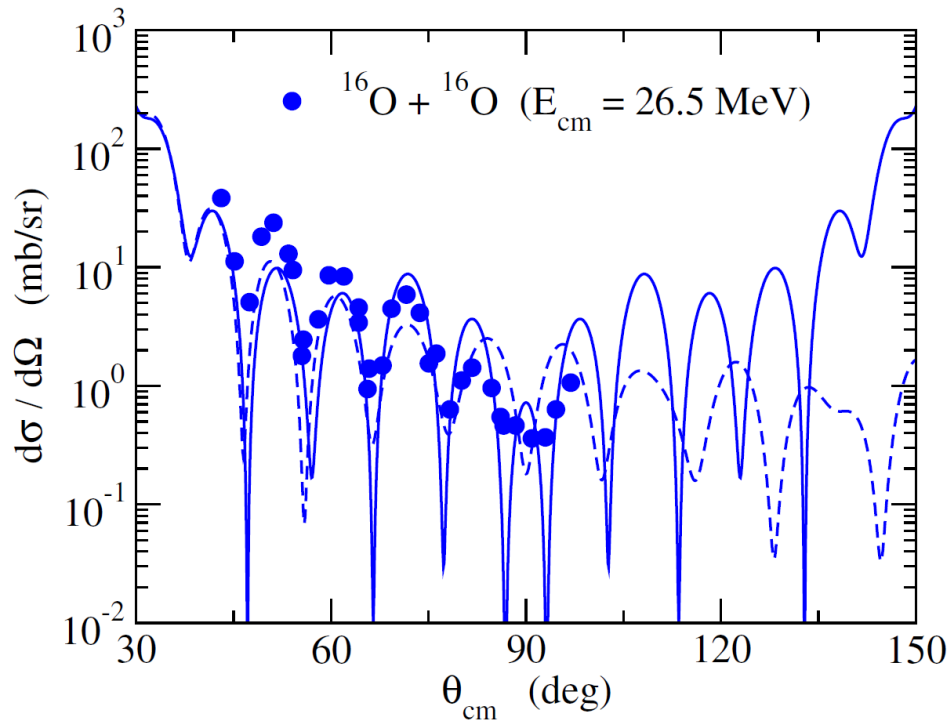


$^{18}\text{O}$

56 levels

cf. the number of open channels, F. Haas and Y. Abe, PRL46('81)1667

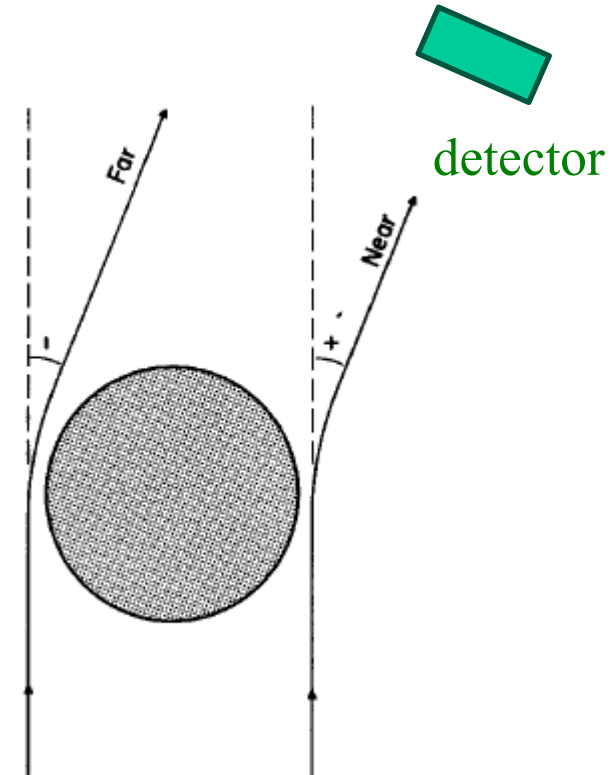
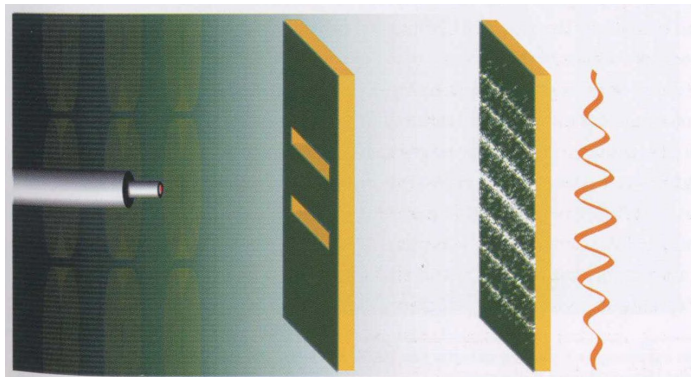
# Origins of oscillations

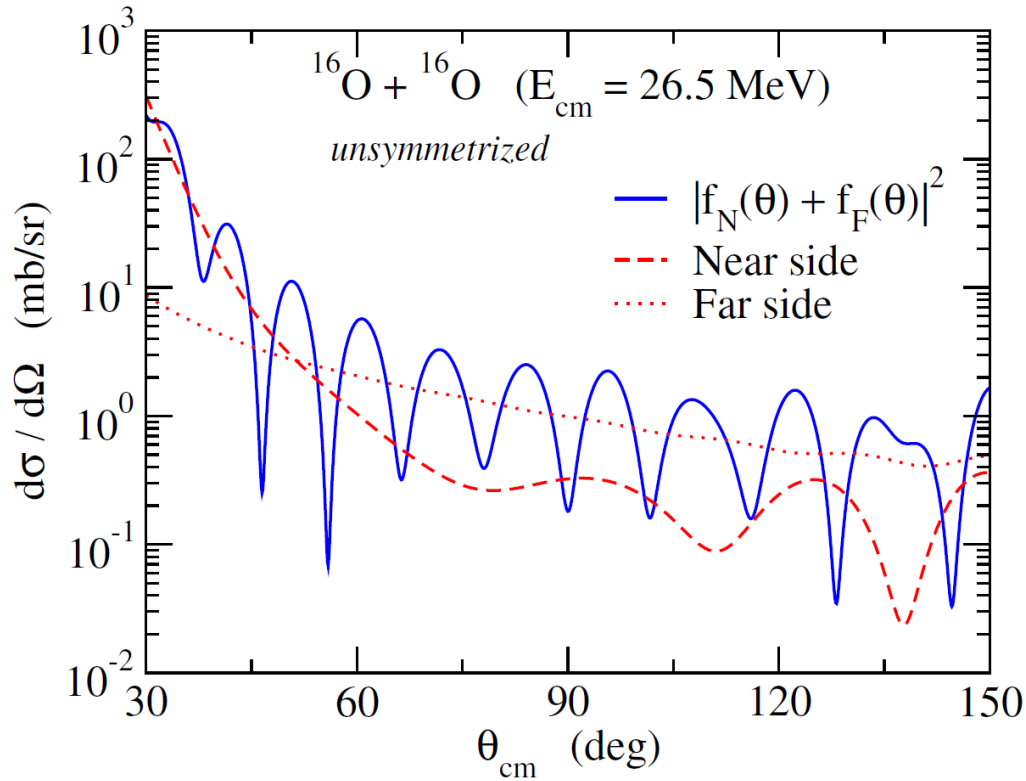


strong oscillations even in unsymmetrized cross sections

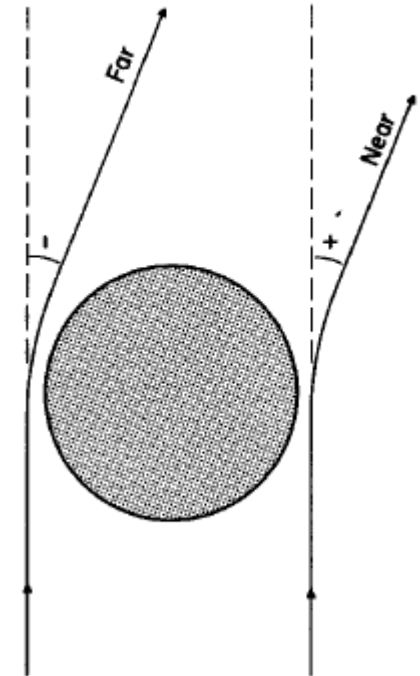


- ✓ symmetrization: minor
- ✓ the main origin: near-side-far-side interference





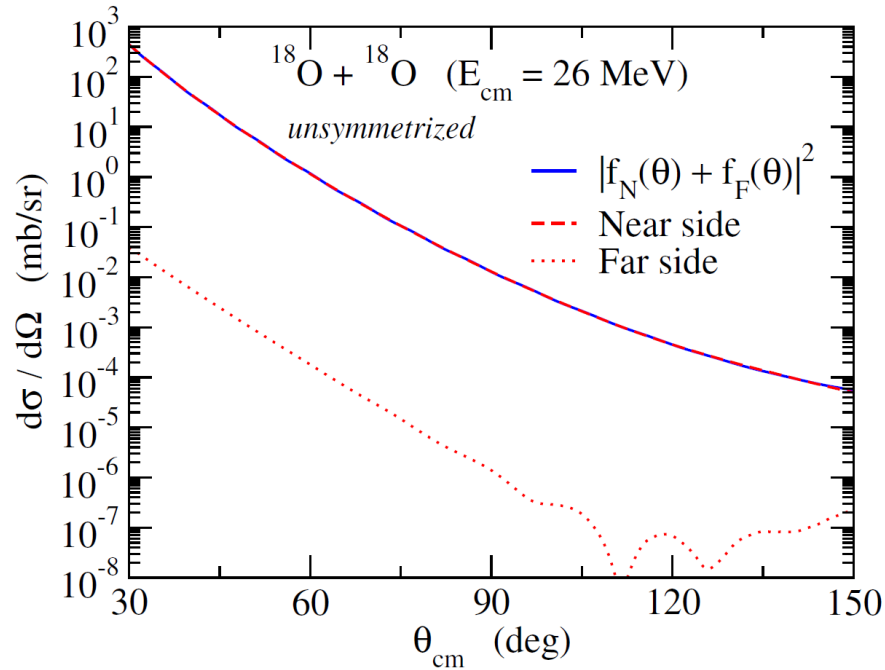
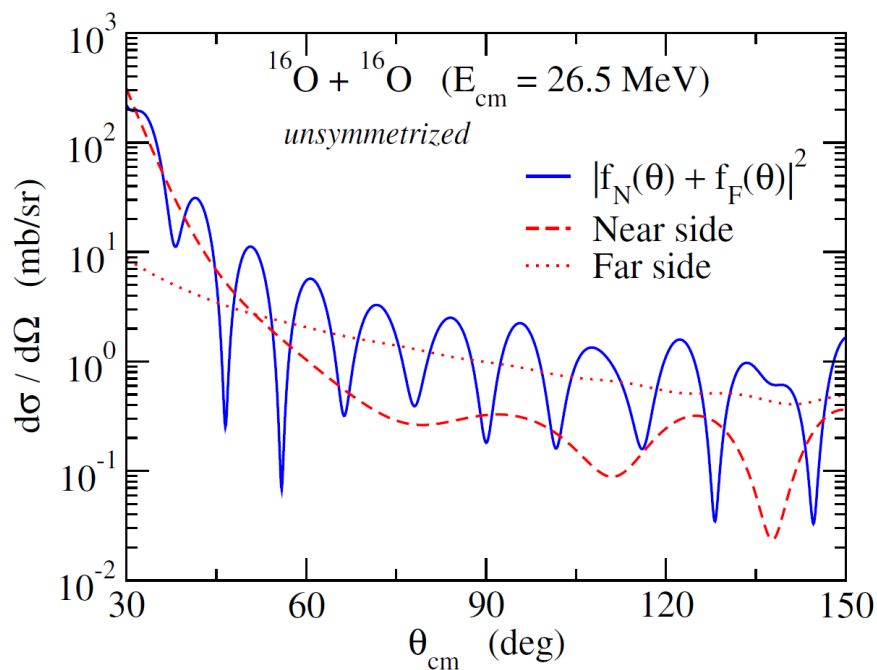
near side-far side interference



$$P_l(\cos \theta) \rightarrow \frac{1}{2} \left[ P_l(\cos \theta) \mp i \frac{2}{\pi} Q_l(\cos \theta) \right]$$

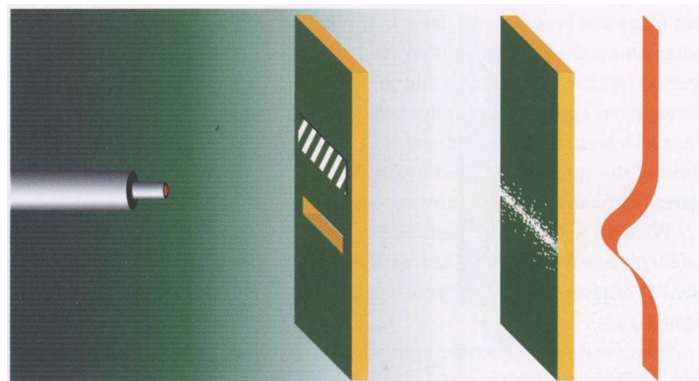
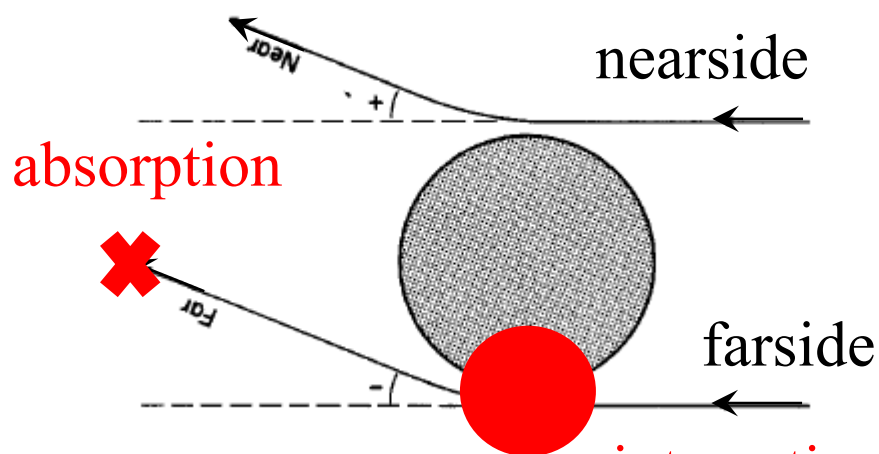
↗ N  
↘ F

$Q_l$ : Legendre function of the second kind



the far-side component is largely damped in  $^{18}\text{O} + ^{18}\text{O}$  due to absorption  
 → almost no interference oscillations

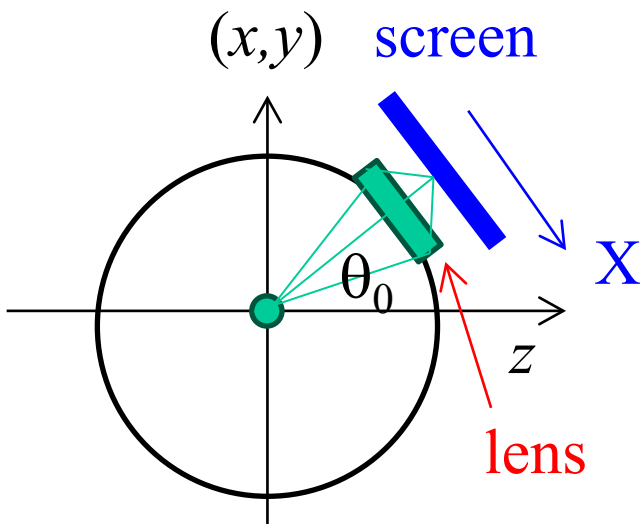
cf. a single slit



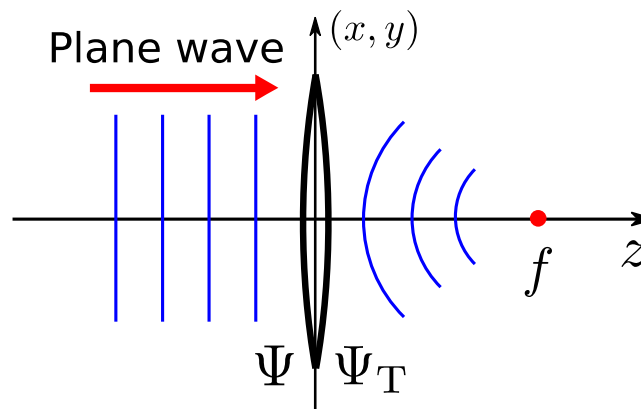
interaction → decoherence

# Imaging of nuclear reactions

K. Hagino and T. Yoda,  
in preparation



“condensing” scattering waves with a lens



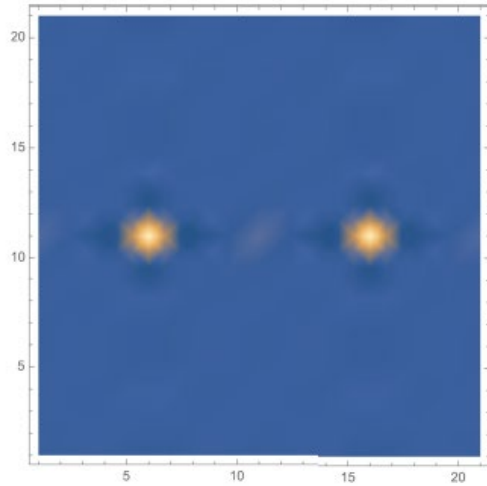
K. Hashimoto et al., PRD101, 066018 (2020)

## Fourier transform of scattering amplitude

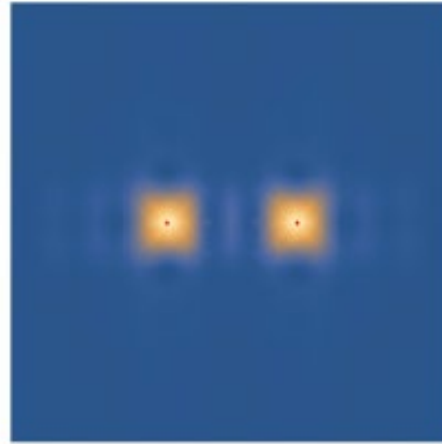
$$\Phi(X, Y) \propto \int_{\theta_0 - \Delta\theta}^{\theta_0 + \Delta\theta} \sin \theta d\theta \int_{\varphi_0 - \Delta\varphi}^{\varphi_0 + \Delta\varphi} d\varphi \\ \times e^{i\alpha((\theta - \theta_0)X + (\varphi - \varphi_0)Y)} f(\theta, \varphi)$$

$$I(X, Y) = |\Phi(X, Y)|^2$$

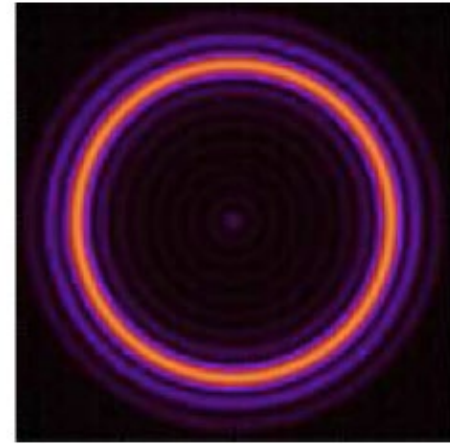
# applications in particle physics



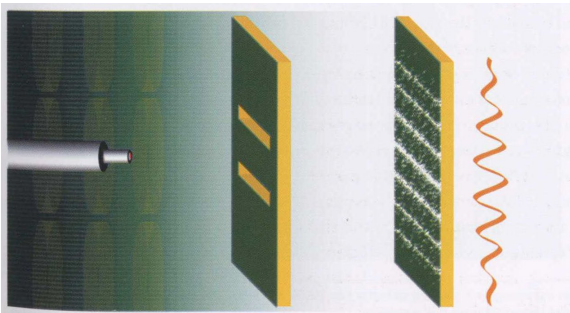
a double slit  
problem



scattering of  
string



imaging black holes  
through AdS/CFT



K. Hashimoto, Y. Matsuo, and T. Yoda, PTEP2023, 043B04 (2023)

K. Hashimoto, S. Kinoshita, and K. Murata, PRL123, 031602 (2019)

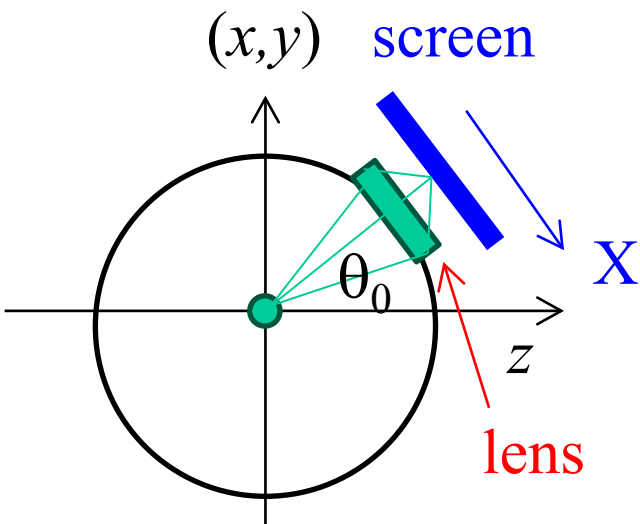
PRD101, 066018 (2020)



# Imaging of nuclear reactions

K. Hagino and T. Yoda,  
in preparation

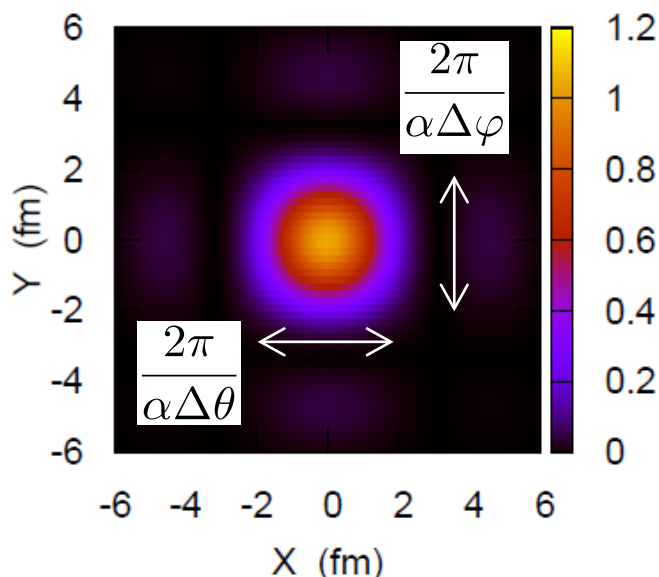
## Fourier transform of scattering amplitude



$$\Phi(X, Y) \propto \int_{\theta_0 - \Delta\theta}^{\theta_0 + \Delta\theta} \sin \theta d\theta \int_{\varphi_0 - \Delta\varphi}^{\varphi_0 + \Delta\varphi} d\varphi \times e^{i\alpha((\theta - \theta_0)X + (\varphi - \varphi_0)Y)} f(\theta, \varphi)$$

$$I(X, Y) = |\Phi(X, Y)|^2$$

for a flat distribution,  $f(\theta, \phi) = \text{const.}$ ,



$$\int_{\varphi_0 - \Delta\varphi}^{\varphi_0 + \Delta\varphi} d\varphi e^{i\alpha(\varphi - \varphi_0)Y} = 2\Delta\varphi \frac{\sin(\alpha Y \Delta\varphi)}{\alpha Y \Delta\varphi}$$

# Imaging of nuclear reactions

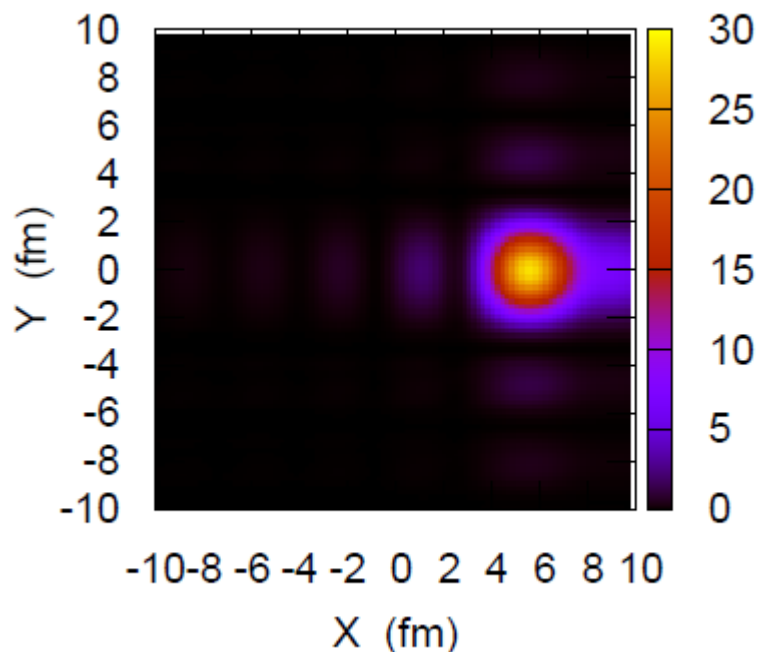
K. Hagino and T. Yoda,  
in preparation

## Fourier transform of scattering amplitude

$$\Phi(X, Y) \propto \int_{\theta_0 - \Delta\theta}^{\theta_0 + \Delta\theta} \sin \theta d\theta \int_{\varphi_0 - \Delta\varphi}^{\varphi_0 + \Delta\varphi} d\varphi e^{i\alpha((\theta - \theta_0)X + (\varphi - \varphi_0)Y)} f(\theta, \varphi)$$

$$I(X, Y) = |\Phi(X, Y)|^2$$

for the Rutherford scattering,  $f(\theta, \phi) = f_C(\theta, \phi)$ ,



$^{16}\text{O} + ^{16}\text{O}$  at  $E_{\text{cm}} = 8.8$  MeV

$$\alpha = k$$

$$\theta_0 = 90 \text{ deg.}$$

$$\Delta\theta = \Delta\phi = 30 \text{ deg.}$$



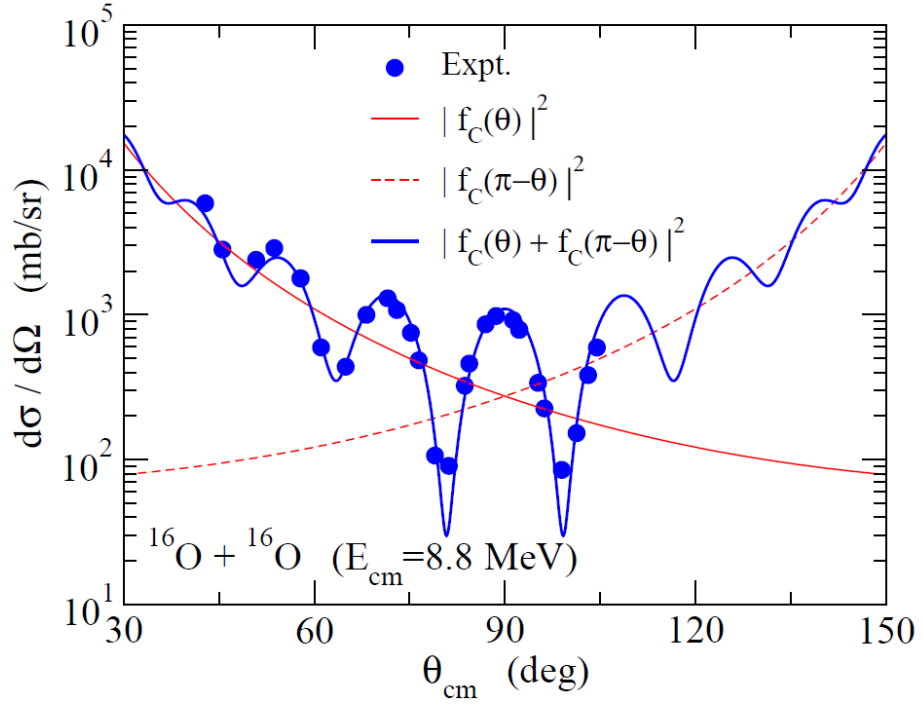
$$b_{\text{cl}} = 5.24 \text{ fm} \sim X_{\text{peak}}$$

# Imaging of nuclear reactions

$$\Phi(X, Y) \propto \int_{\theta_0 - \Delta\theta}^{\theta_0 + \Delta\theta} \sin \theta d\theta \int_{\varphi_0 - \Delta\varphi}^{\varphi_0 + \Delta\varphi} d\varphi e^{i\alpha((\theta - \theta_0)X + (\varphi - \varphi_0)Y)} f(\theta, \varphi)$$

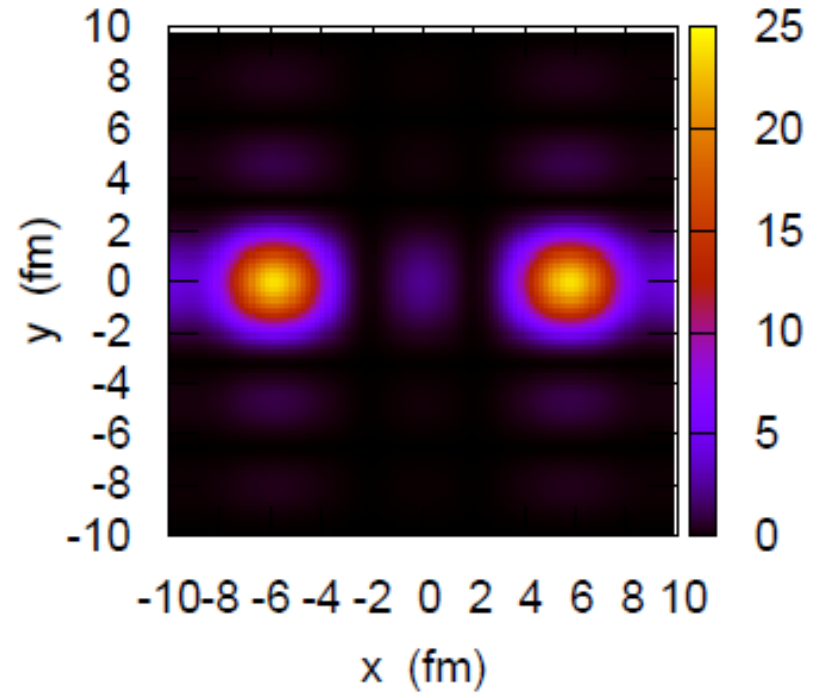
## Imaging of Mott scattering

$$I(X, Y) = |\Phi(X, Y)|^2$$



$$\alpha = k$$

$$\theta_0 = 90 \text{ deg.}, \Delta\theta = \Delta\phi = 30 \text{ deg.}$$



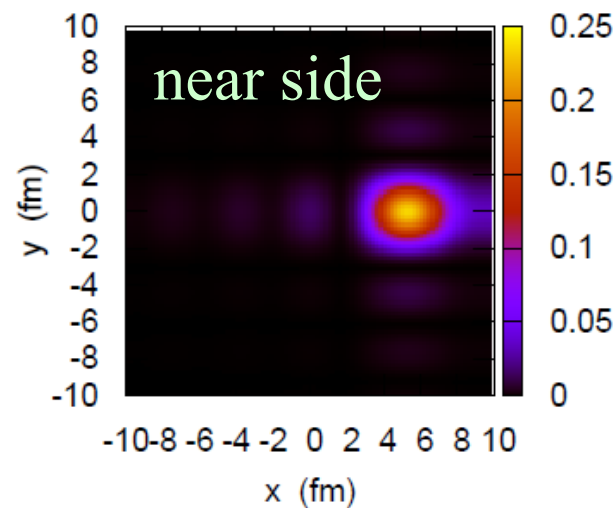
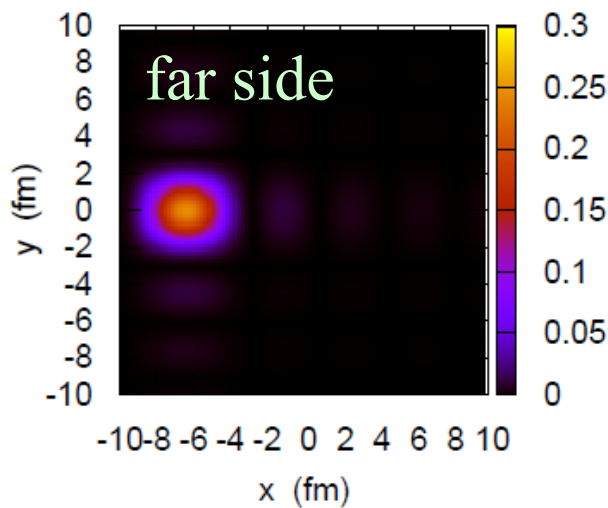
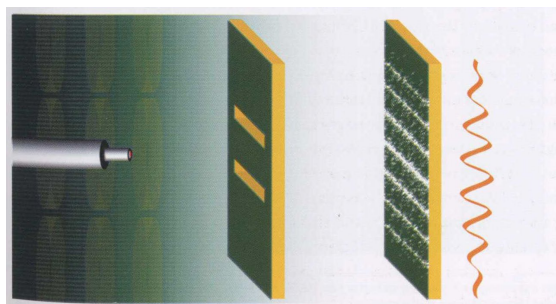
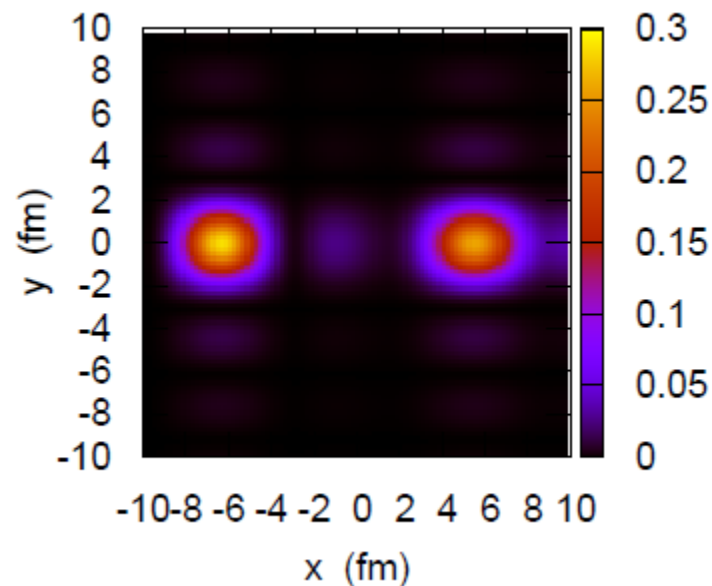
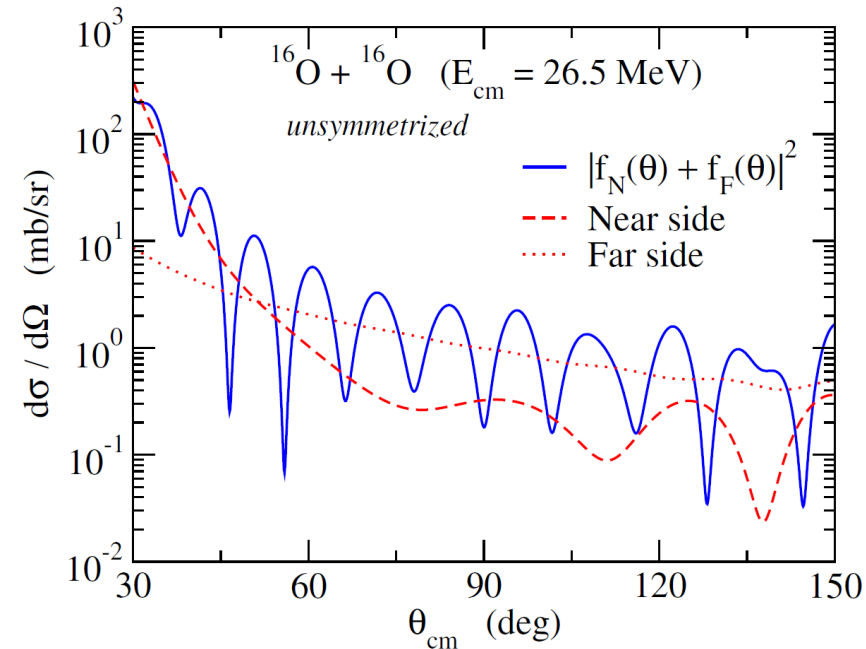
(note) for  $\theta_0 = 90 \text{ deg.}$ ,

$$\Phi_\theta(X, Y) = \Phi_{\pi - \theta}(-X, Y)$$

# Imaging of nuclear reactions

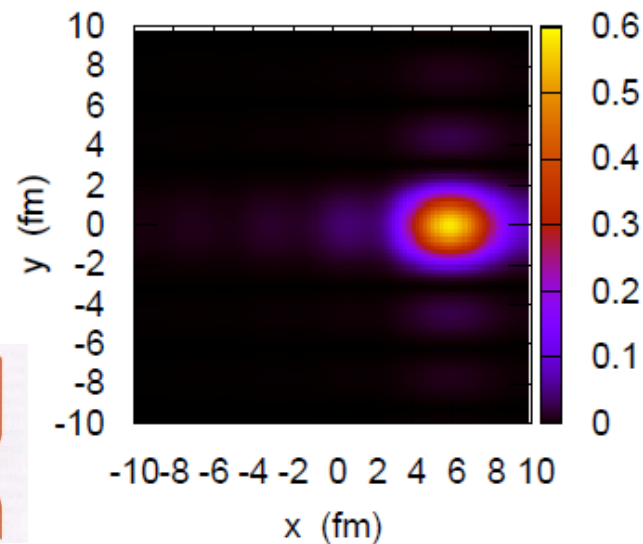
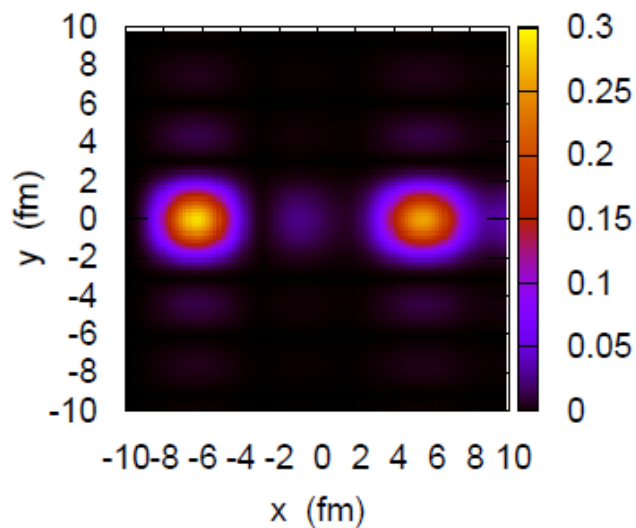
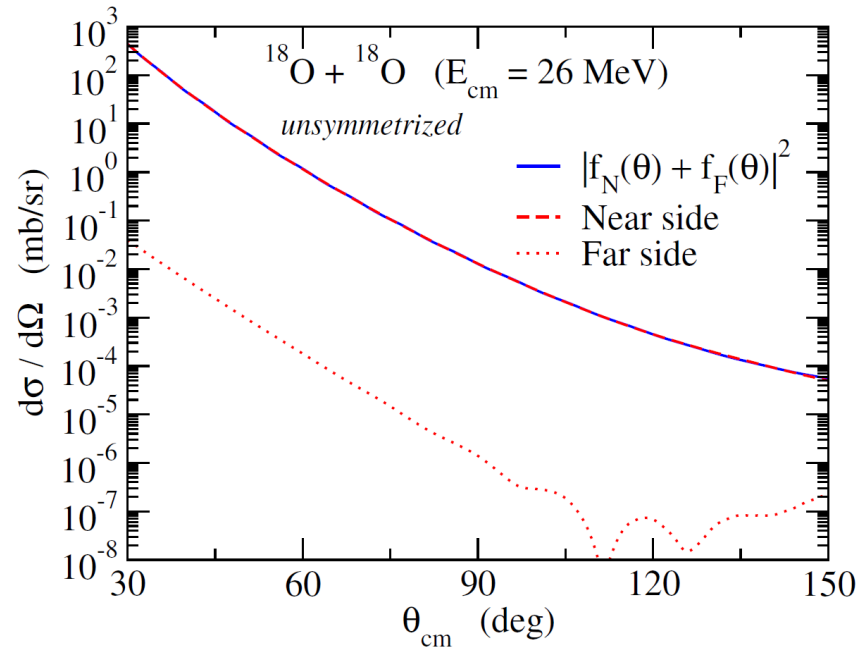
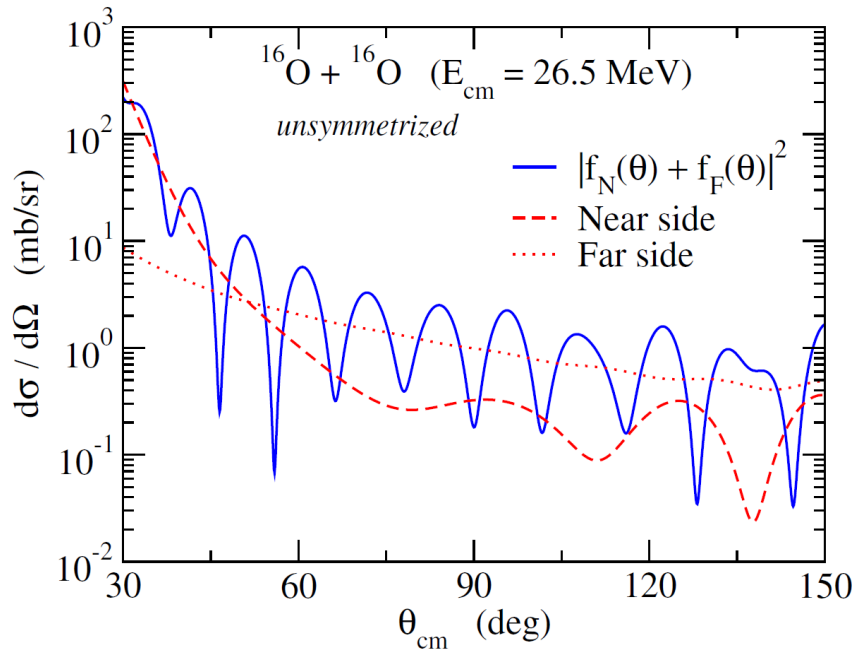
K.H. and T. Yoda, in preparation

$\alpha=k$ ,  $\theta_0=55$  deg.,  $\Delta\theta=15$  deg.



# Imaging of nuclear reactions

K.H. and T. Yoda, in preparation



# Summary

## Nuclear Reactions as quantum many-body phenomena

- ✓ strong interplay with nuclear structure
- ✓ several nuclear intrinsic motions
- ✓ Coupled-channels approach
  
- ✓ a variety of interference phenomena
  - scattering of identical nuclei
  - farside-nearside interference
  - barrier-wave-internal-wave interference
  
- ✓ **Imaging: a new approach**
  - a Fourier transform of scatt. amplitudes
  - an intuitive way to understand physics of interferences

