

Quantum many-body dynamics in heavy-ion fusion reactions around the Coulomb barrier

Kouichi Hagino

Kyoto University, Kyoto, Japan



from my slide on
Sep. 21, 2018

감사합니다



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Quantum many-body dynamics in heavy-ion fusion reactions around the Coulomb barrier



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1. Nuclear Reactions: overview
2. Fusion of light nuclei and Feshbach resonances
3. Fusion of medium-heavy nuclei and quantum tunneling
4. Fusion for superheavy nuclei
5. Microscopic modelling of low-energy nuclear reactions
6. Fission
7. Summary

Introduction: low-energy nuclear physics

□ behaviors of atomic nuclei as a quantum many-body systems

← understanding based on strong interaction

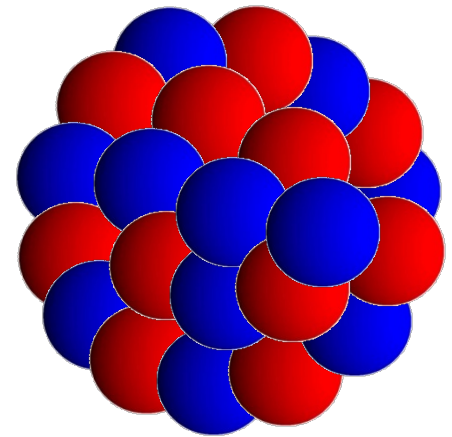
➤ static properties: nuclear structure

- ✓ ground state properties
(mass, size, shape,...)
- ✓ excitations
- ✓ nuclear matter
- ✓ decays

➤ dynamics: nuclear reactions

nucleus: a composite system

- ✓ various sort of reactions



- elastic scattering
- inelastic scattering
- transfer reaction
- breakup reactions
- fusion reactions

Introduction: low-energy nuclear physics

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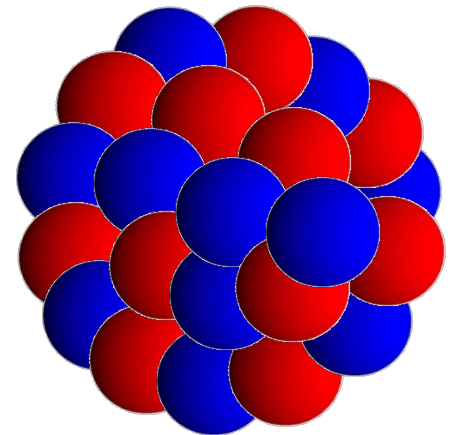
➤ static properties: nuclear structure

- ✓ ground state properties
(mass, size, **shape,...**)
- ✓ **excitations**
- ✓ nuclear matter
- ✓ decays

➤ dynamics: nuclear reactions

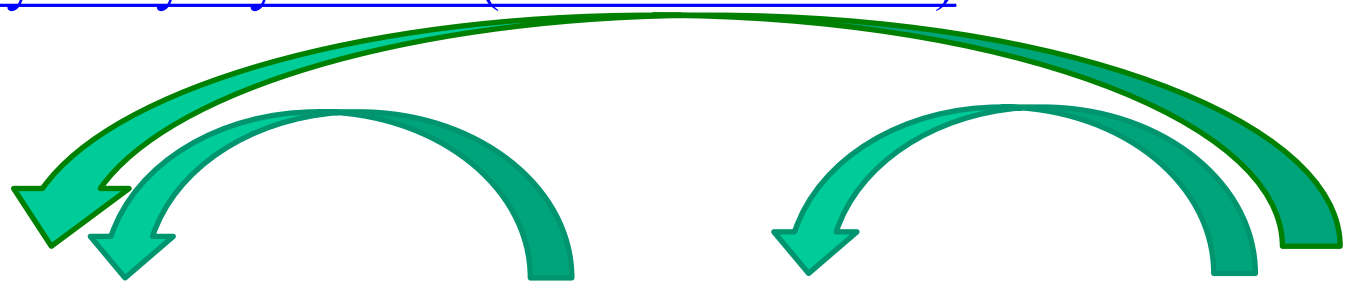
nucleus: a composite system

- ✓ various sort of reactions
- ✓ **an interplay between nuclear structure and reaction**



- elastic scattering
- inelastic scattering
- transfer reaction
- breakup reactions
- fusion reactions

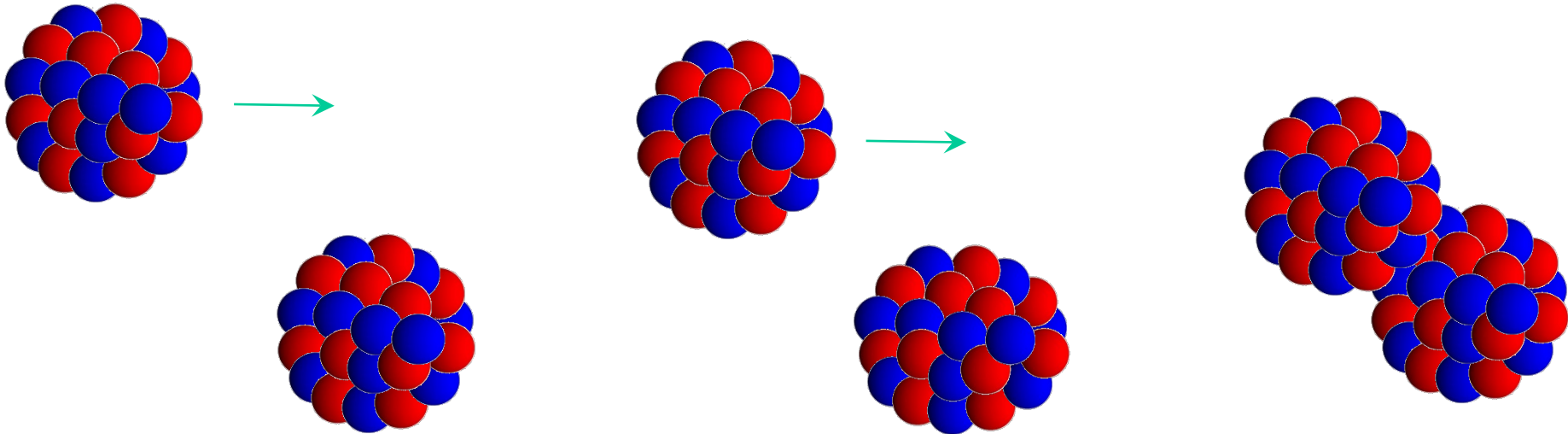
Quantum Many-body Dynamics (nuclear reactions)



elastic scattering

inel. scattering

fusion

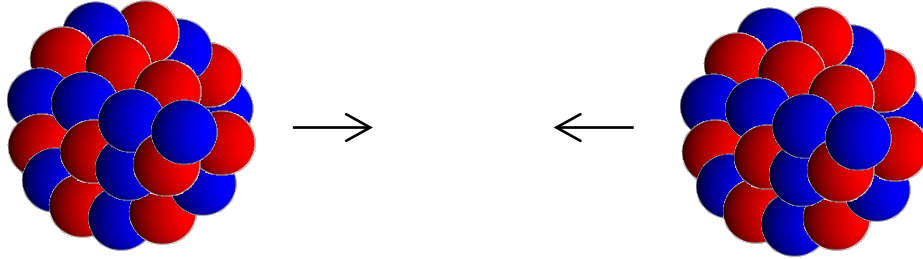


a quantum reaction theory
to describe several reaction processes
simultaneously



Coupled-channels method: a quantal scattering theory with excitations

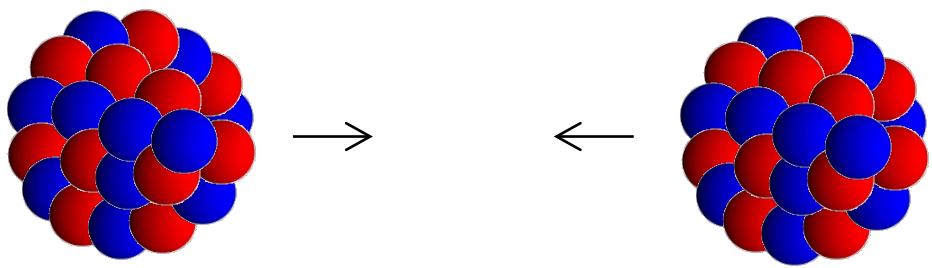
many-body problem



still very challenging

Coupled-channels method: a quantal scattering theory with excitations

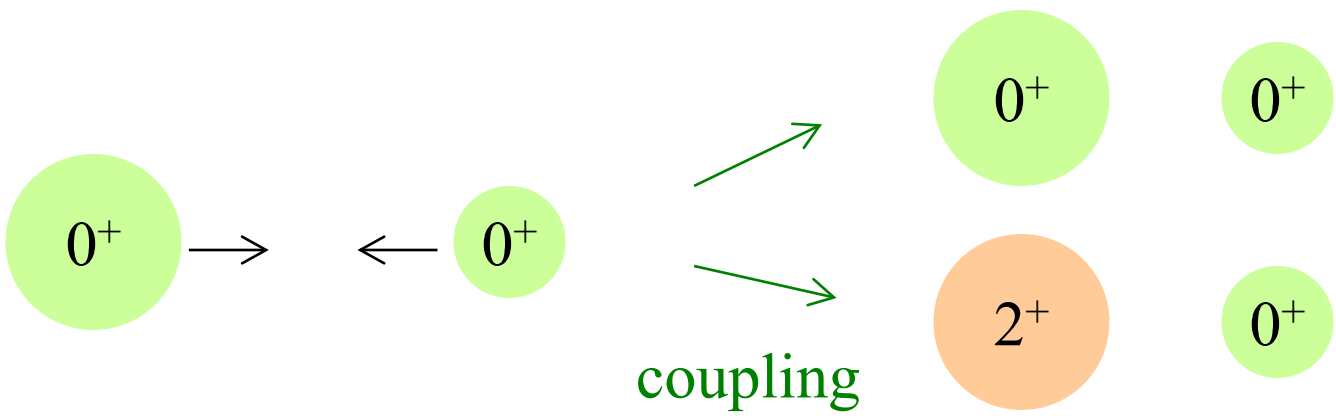
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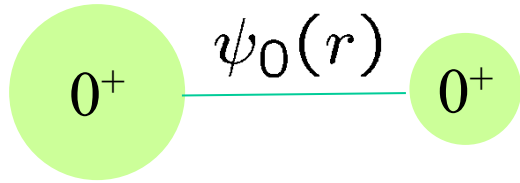


two-body problem, but with excitations
(the coupled-channels approach)



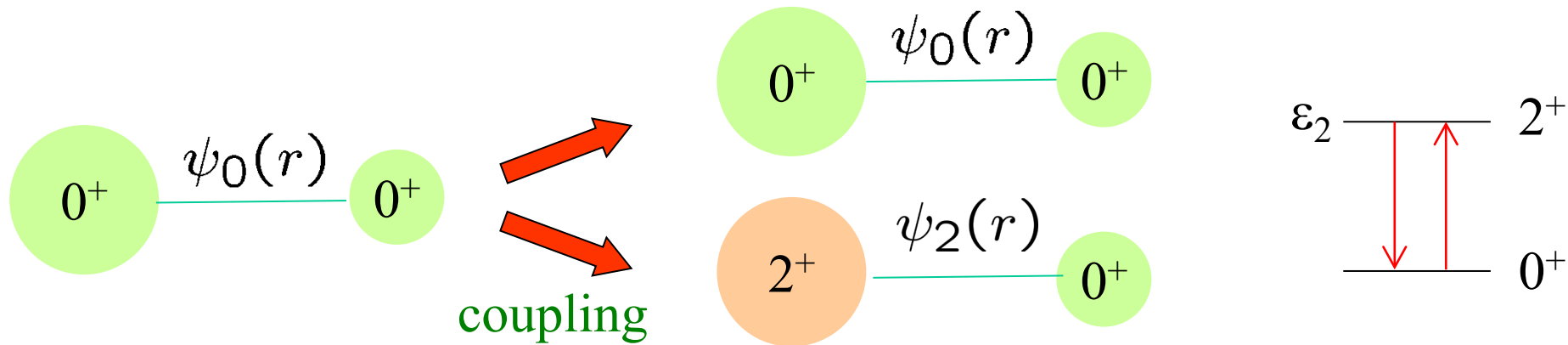
scattering theory with excitations

Coupled-channels method: a quantal scattering theory with excitations



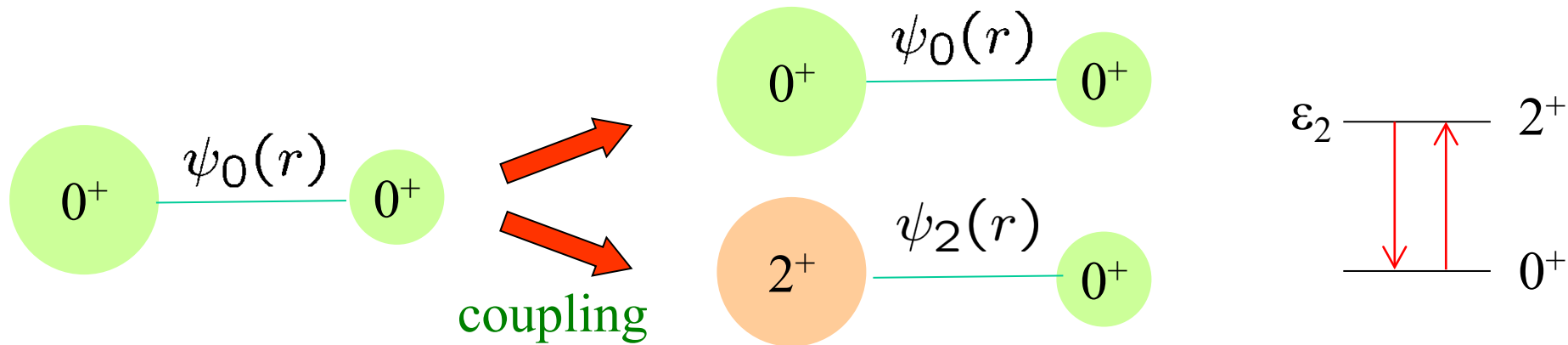
$$\left[-\frac{\hbar^2}{2\mu} \nabla^2 + V_0(r) - E \right] \psi_0(\mathbf{r}) = 0$$

Coupled-channels method: a quantal scattering theory with excitations



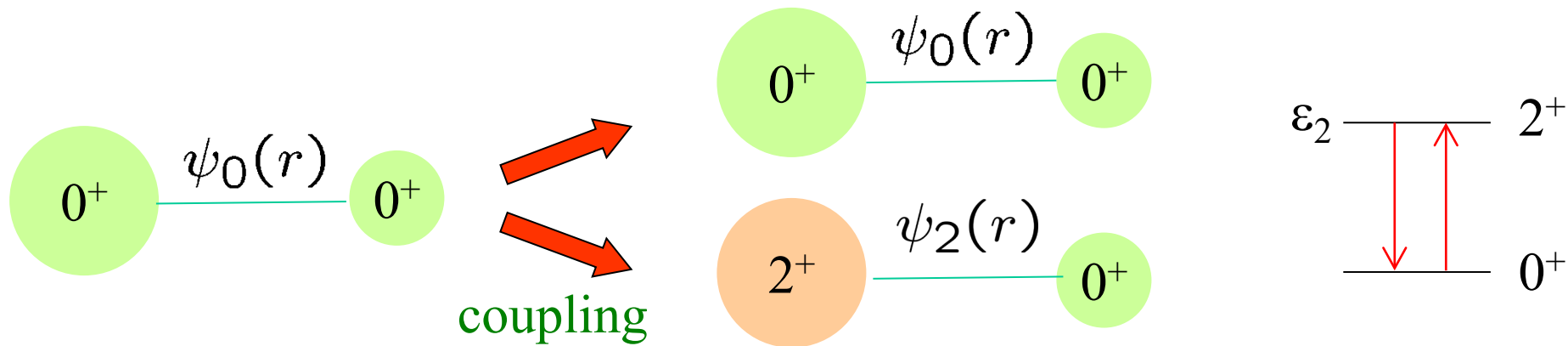
$$\left[-\frac{\hbar^2}{2\mu} \nabla^2 + V_0(r) - E \right] \psi_0(\mathbf{r}) = -F_{0 \rightarrow 2}(r) \psi_2(\mathbf{r})$$

Coupled-channels method: a quantal scattering theory with excitations



$$\left[-\frac{\hbar^2}{2\mu} \nabla^2 + V_0(r) - E \right] \psi_0(\mathbf{r}) = -F_{0 \rightarrow 2}(r) \psi_2(\mathbf{r})$$
$$\left[-\frac{\hbar^2}{2\mu} \nabla^2 + V_2(r) - (E - \epsilon_2) \right] \psi_2(\mathbf{r}) = -F_{2 \rightarrow 0}(r) \psi_0(\mathbf{r})$$

Coupled-channels method: a quantal scattering theory with excitations



$$\left[-\frac{\hbar^2}{2\mu} \nabla^2 + V_0(r) - E \right] \psi_0(\mathbf{r}) = -F_{0 \rightarrow 2}(r) \psi_2(\mathbf{r})$$

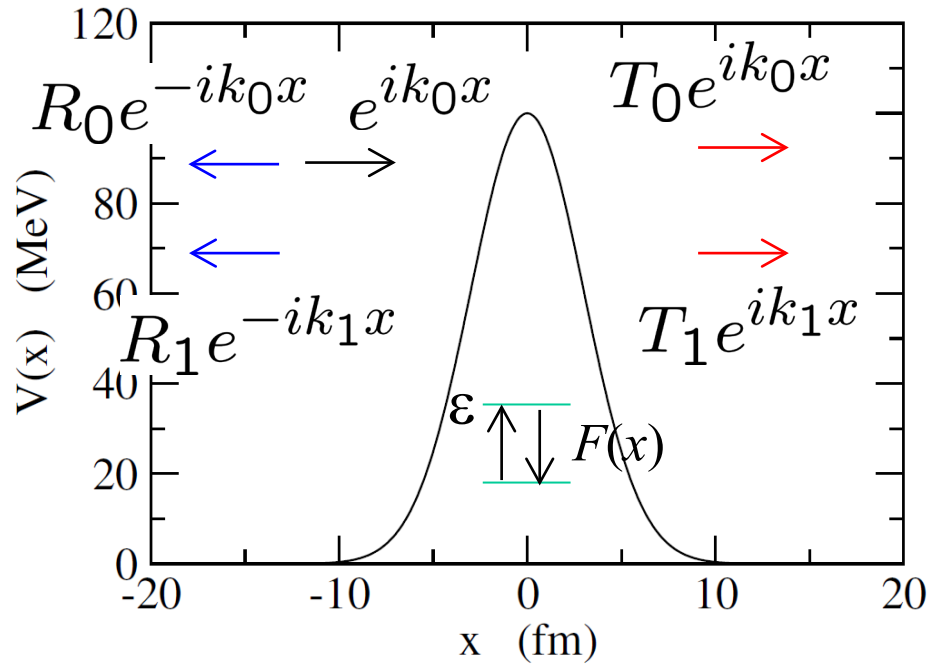
$$\left[-\frac{\hbar^2}{2\mu} \nabla^2 + V_2(r) - (E - \epsilon_2) \right] \psi_2(\mathbf{r}) = -F_{2 \rightarrow 0}(r) \psi_0(\mathbf{r})$$

- Fusion \rightarrow an absorbing potential (an optical potential)
- excitations to unbound states \rightarrow breakup reactions
(neutron-rich nuclei)

a recent review: K. Hagino, K. Ogata, and A.M. Moro, PPNP in press.

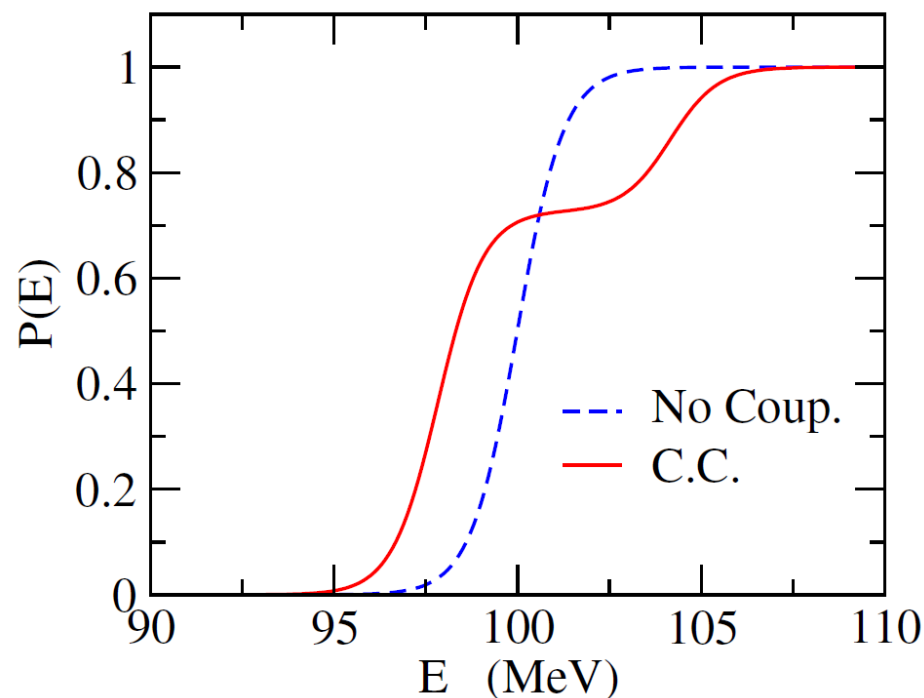
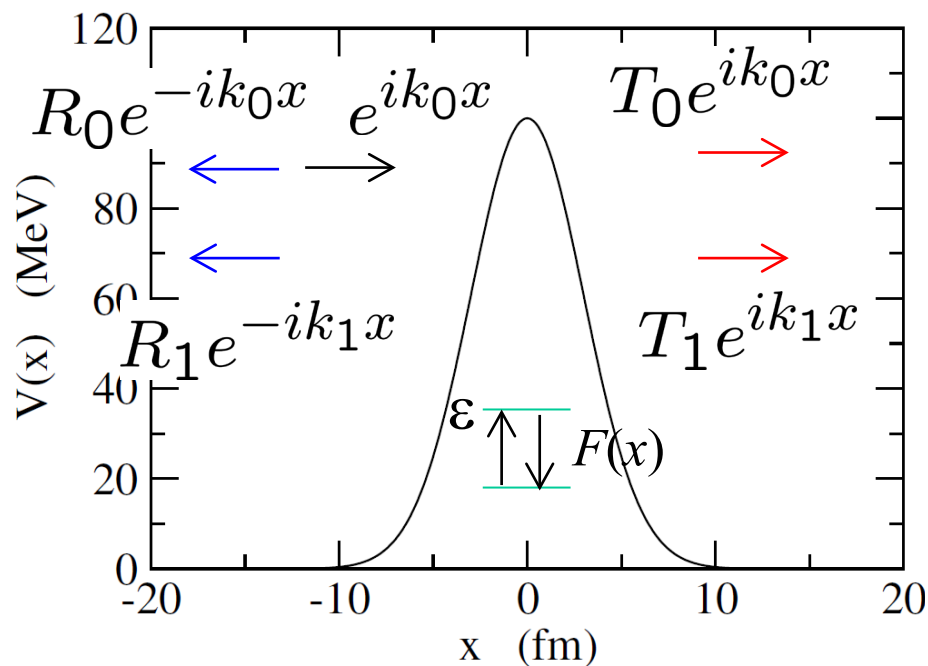
arXiv: 2201.09512

one-dimensional 2 level problem



$$P(E) = |T_0|^2 + \frac{k_1}{k_0} |T_1|^2$$

one-dimensional 2 level problem



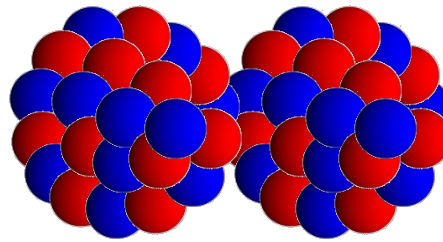
$$P(E) = |T_0|^2 + \frac{k_1}{k_0} |T_1|^2$$

$$V(x) = V_0 e^{-x^2/2s^2}$$

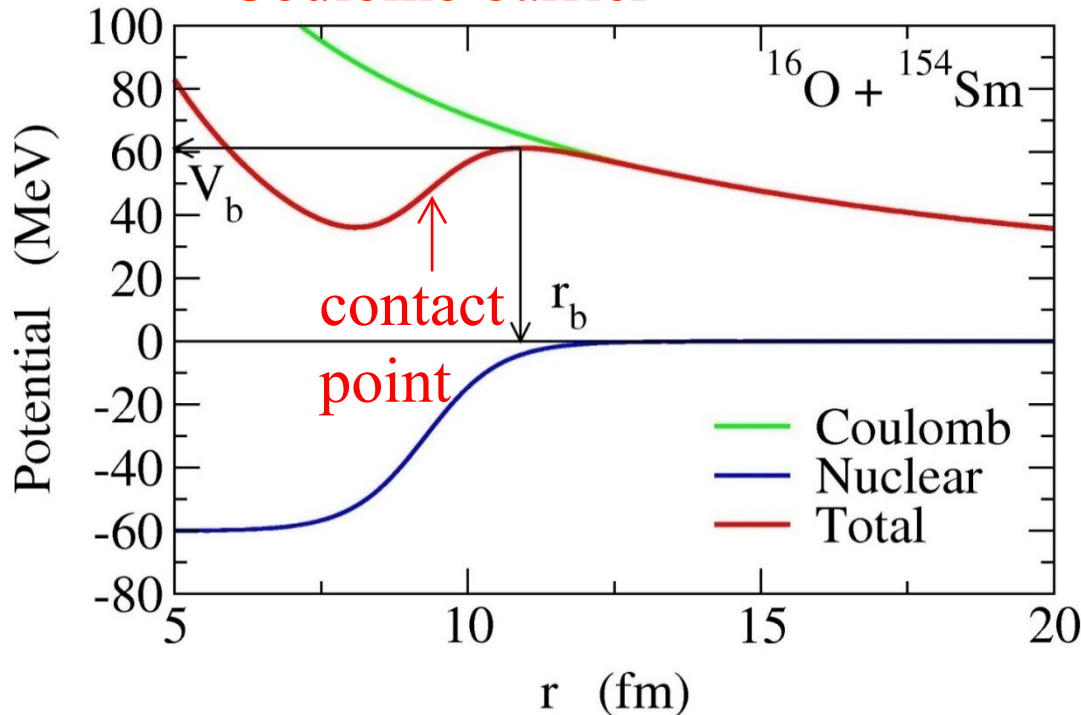
$$F(x) = F_0 e^{-x^2/2s^2}$$

$$V_0 = 100 \text{ MeV}, F_0 = 3 \text{ MeV}, s = 3 \text{ fm}, \\ \varepsilon = 2 \text{ MeV}, m = 29 m_N$$

Fusion Reactions



Coulomb barrier



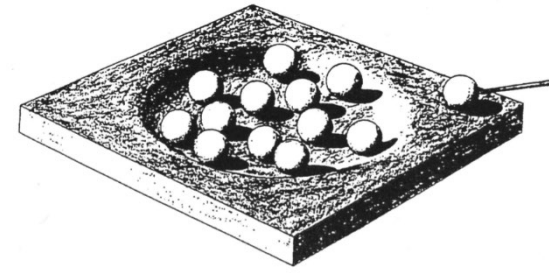
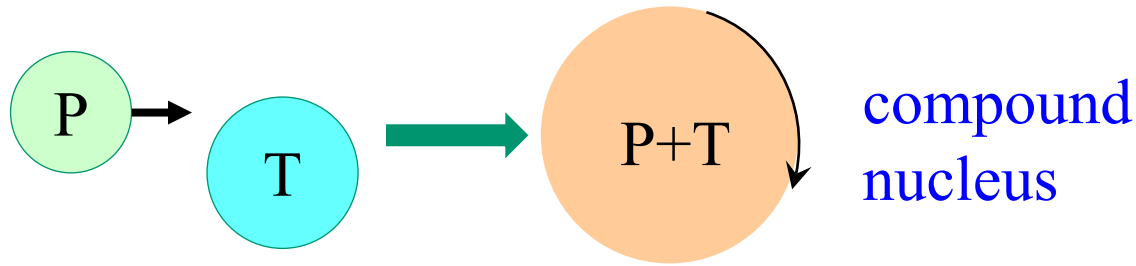
- Nuclear interaction (attractive)
- Coulomb interaction (repulsive)



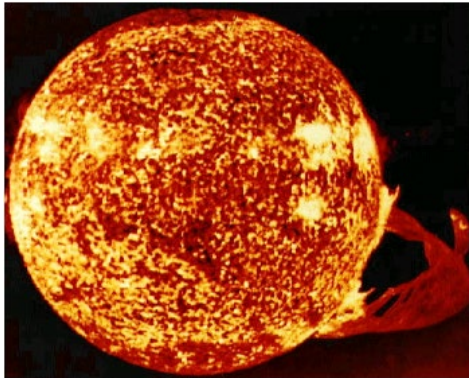
potential barrier

Fusion reactions → a many-body quantum tunneling

Fusion Reactions

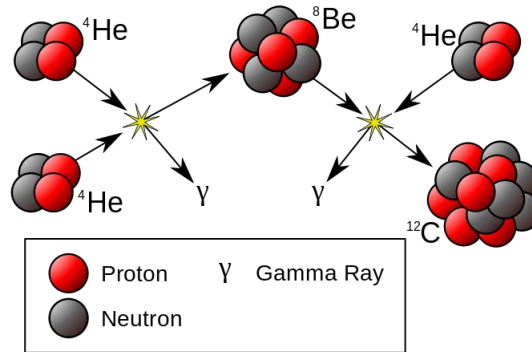


cf. Bohr '36

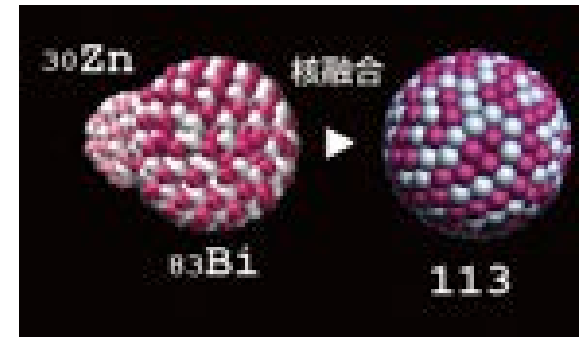


NASA, Skylab space station on December 19, 1973, solar flare reaching 588 000 km off solar surface

energy production
in stars (Bethe '39)



nucleosynthesis

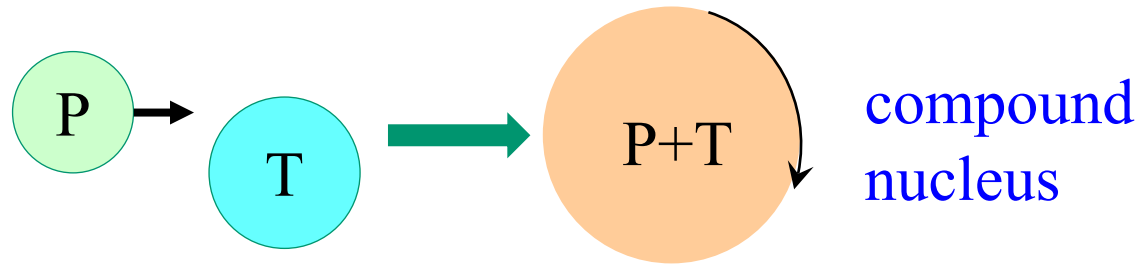


superheavy elements

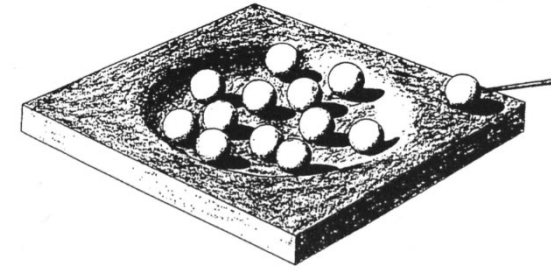
Fusion and fission: large amplitude motions of quantum many-body systems with strong interaction

← microscopic understanding: **an ultimate goal of nuclear physics**

Fusion Reactions



compound
nucleus



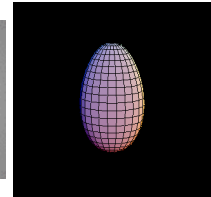
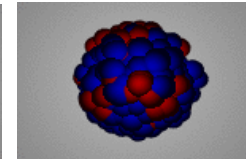
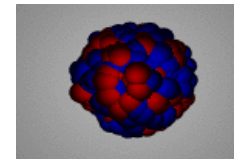
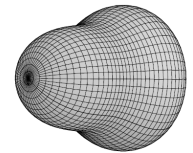
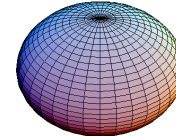
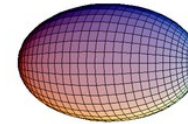
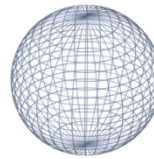
cf. Bohr '36

✓ Many-particle tunneling

▪ rich intrinsic motions

- several nuclear shapes

- several surface vibrations

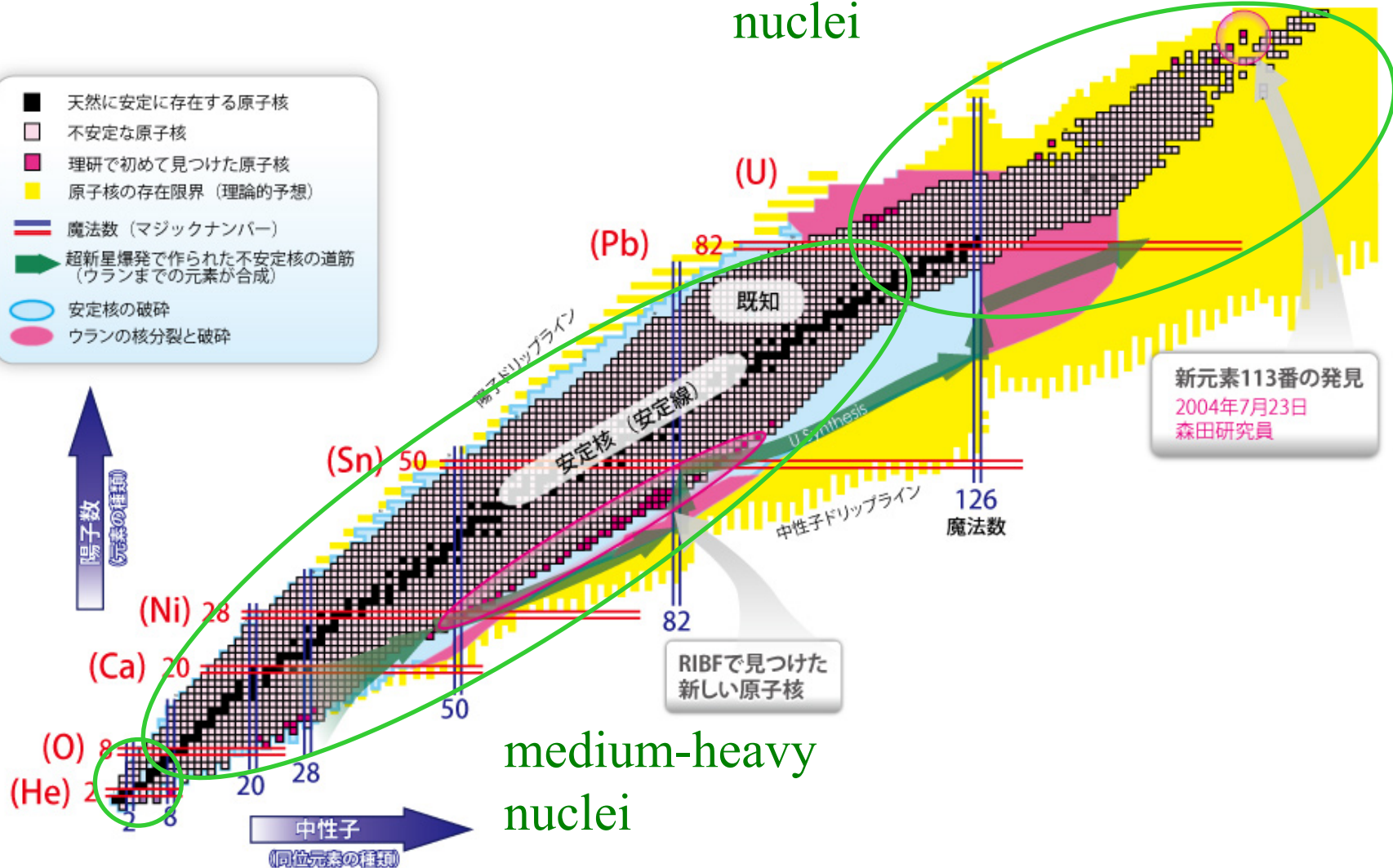


several modes
and adiabaticities

H.I. fusion reaction = an ideal playground to study quantum tunneling with many degrees of freedom

Heavy and Superheavy nuclei

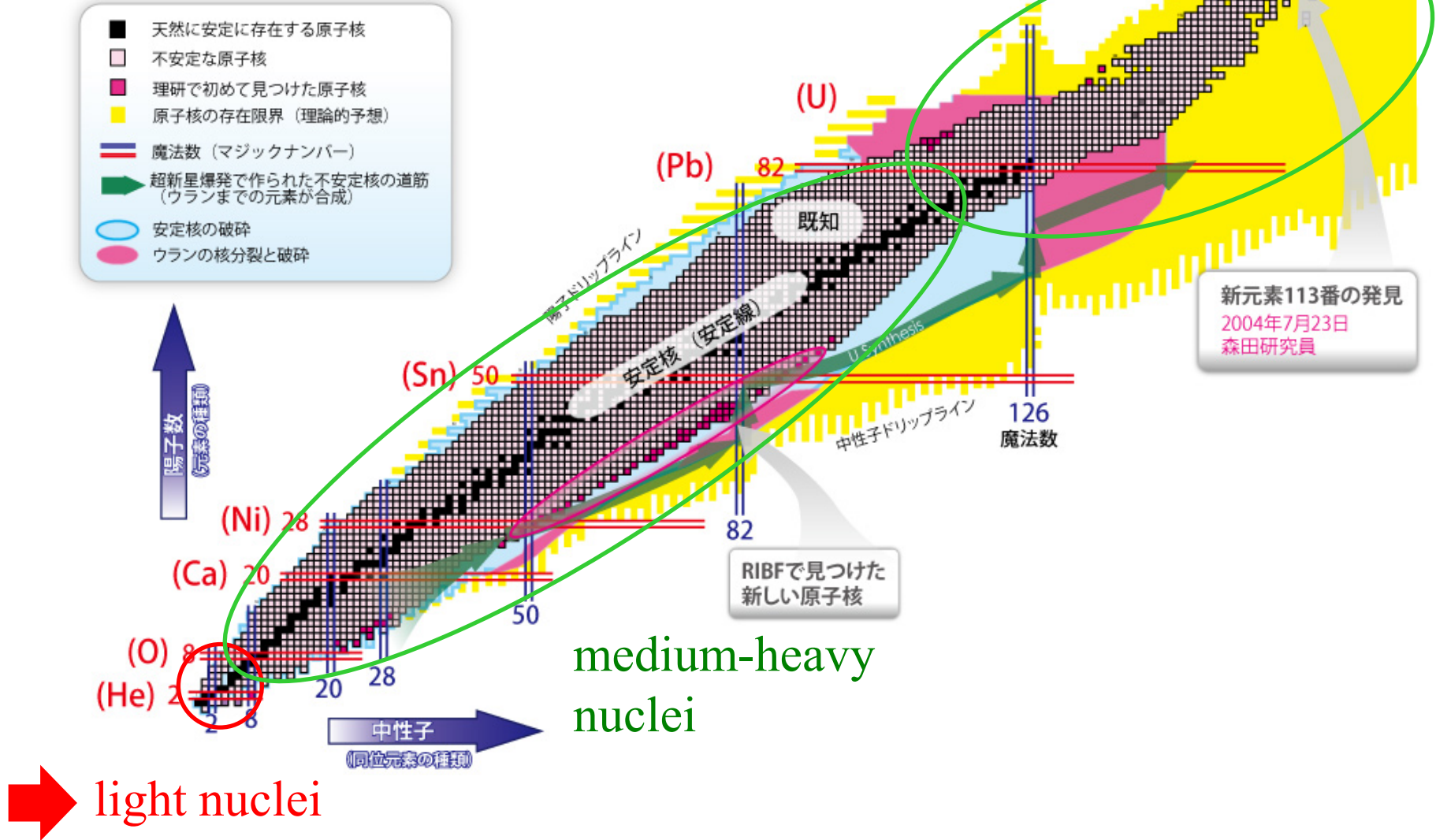
- 天然に安定に存在する原子核
- 不安定な原子核
- 理研で初めて見つけた原子核
- 原子核の存在限界 (理論的予想)
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- ➔ 超新星爆発で作られた不安定核の道筋 (ウランまでの元素が合成)
- 安定核の破碎
- ウランの核分裂と破碎



light nuclei

medium-heavy nuclei

Heavy and Superheavy nuclei



Fusion of light nuclei: nuclear astrophysics

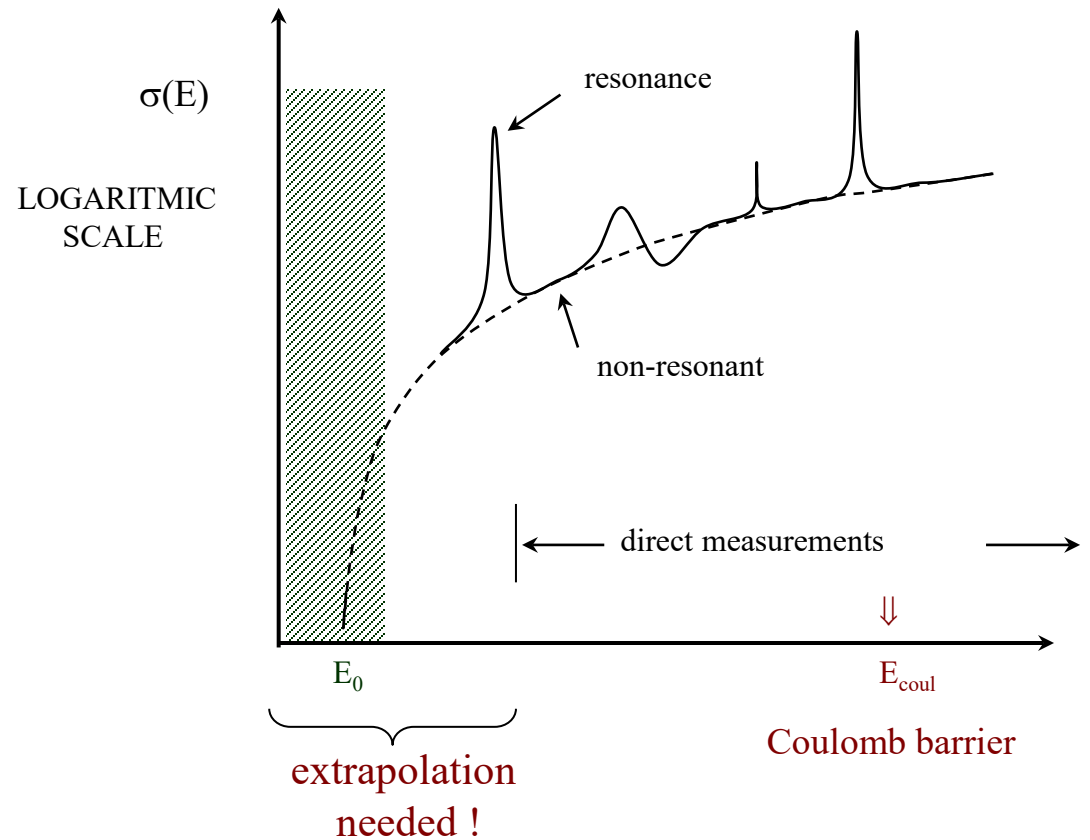
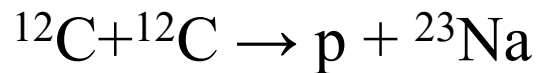
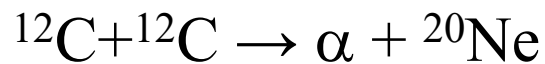
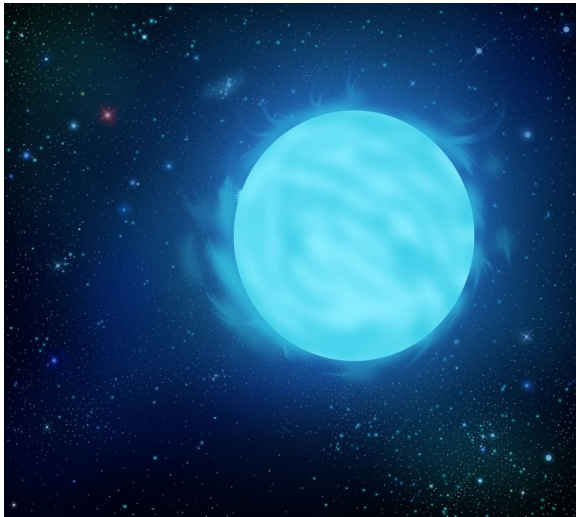


figure: M. Aliotta

Fusion of light nuclei: nuclear astrophysics

$^{12}\text{C}+^{12}\text{C}$ fusion : a key reaction in nuclear astrophysics

Carbon burning
in massive stars



also

- ✓ Type Ia supernovae
- ✓ X-ray superburst

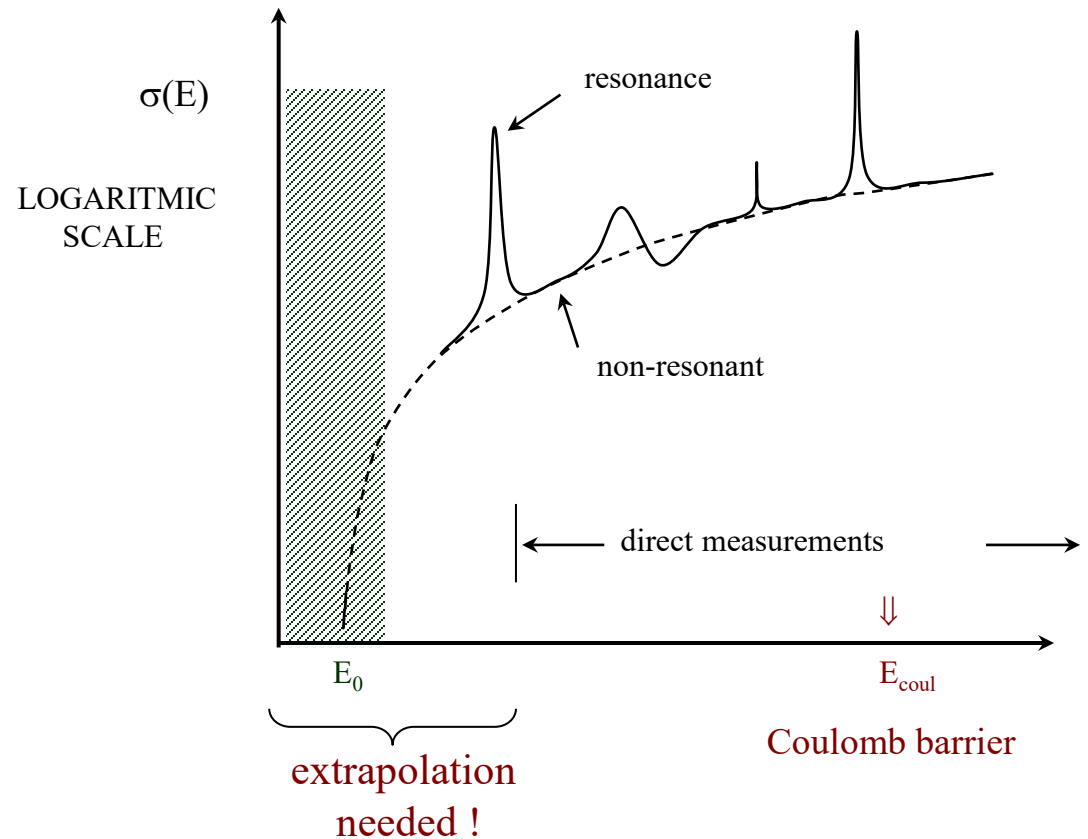
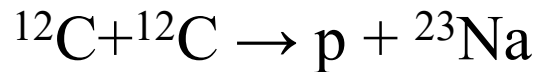
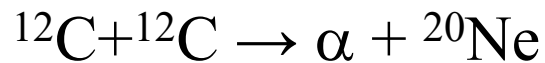
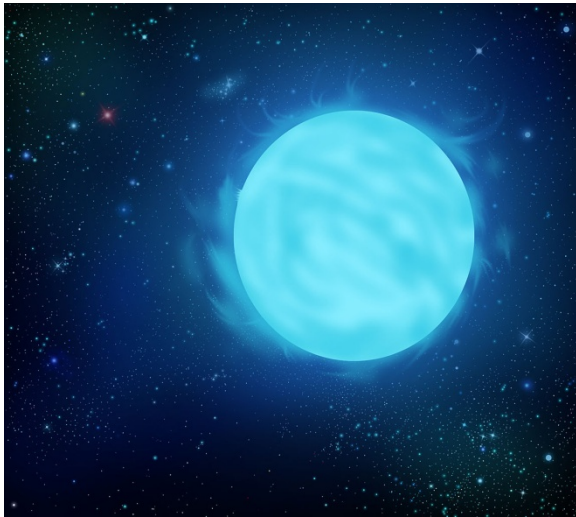


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Fusion of light nuclei: nuclear astrophysics

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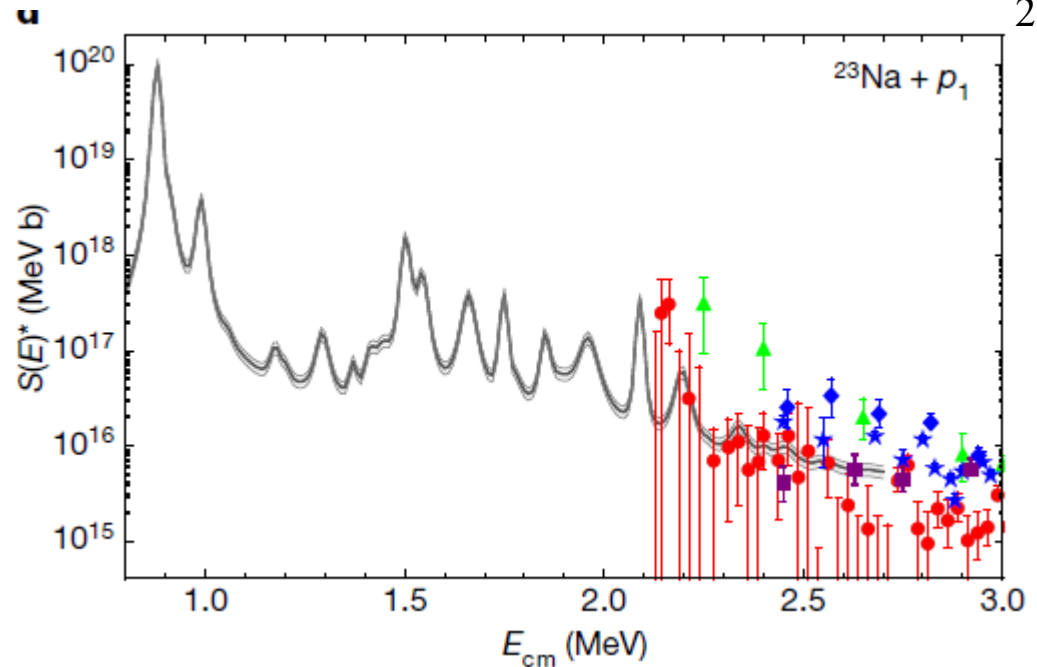
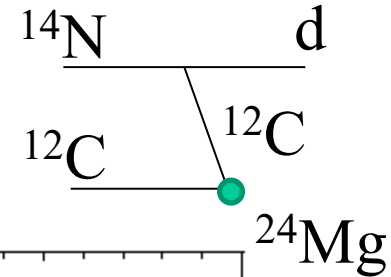
Carbon burning
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also

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Trojan Horse Method

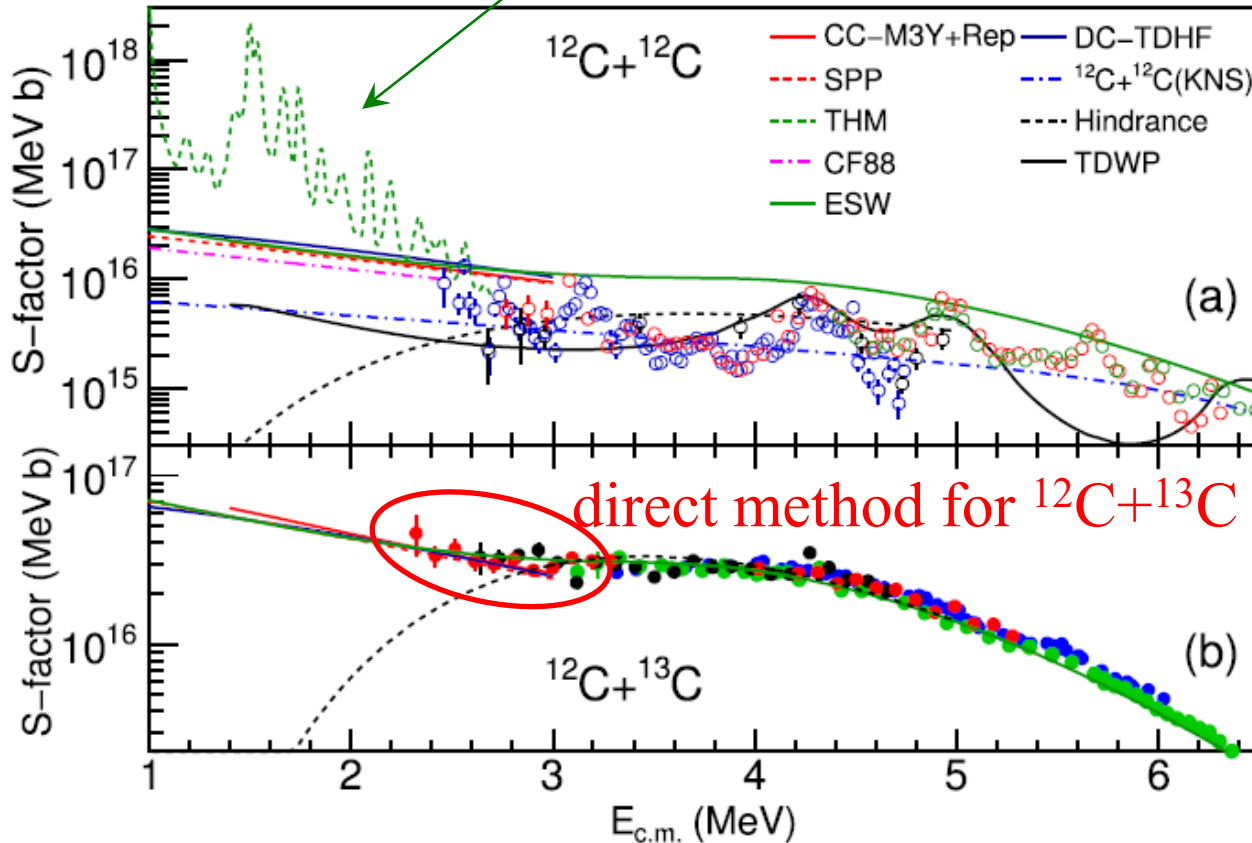


A. Tumino et al., Nature 557 ('18) 687

~ 25 times larger than before
→ lots of debates

$^{12}\text{C}+^{12}\text{C}$ fusion reaction

Trojan Horse Method



The THM data are not supported.

PWIA \rightarrow DWIA?

A.M. Mukhamedzhanov et al.,
PRC99 ('19) 064618

cf. recent direct measurement for $^{12}\text{C}+^{12}\text{C}$:

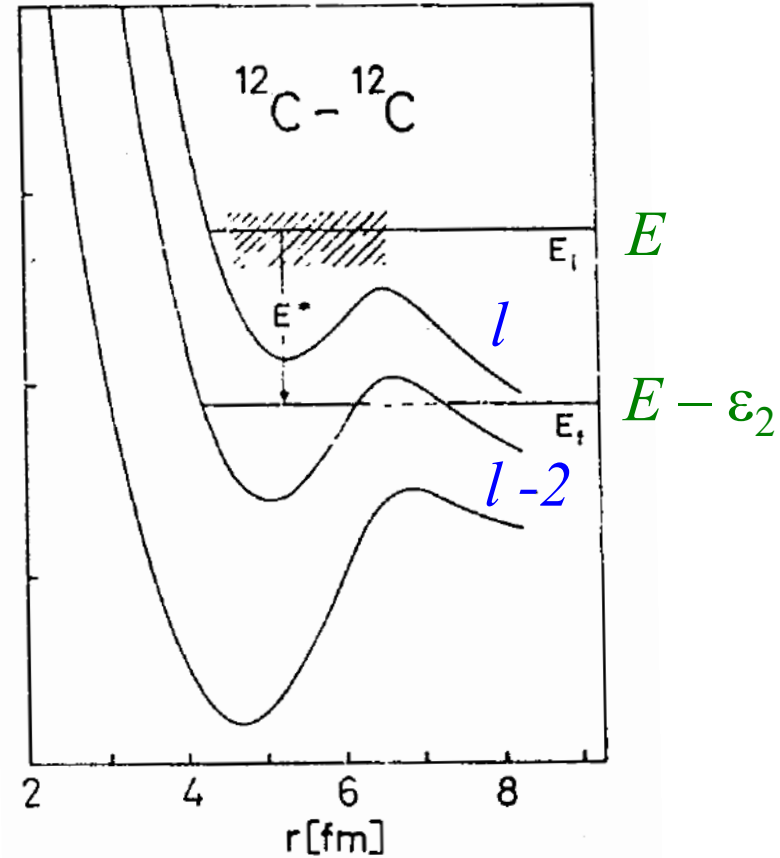
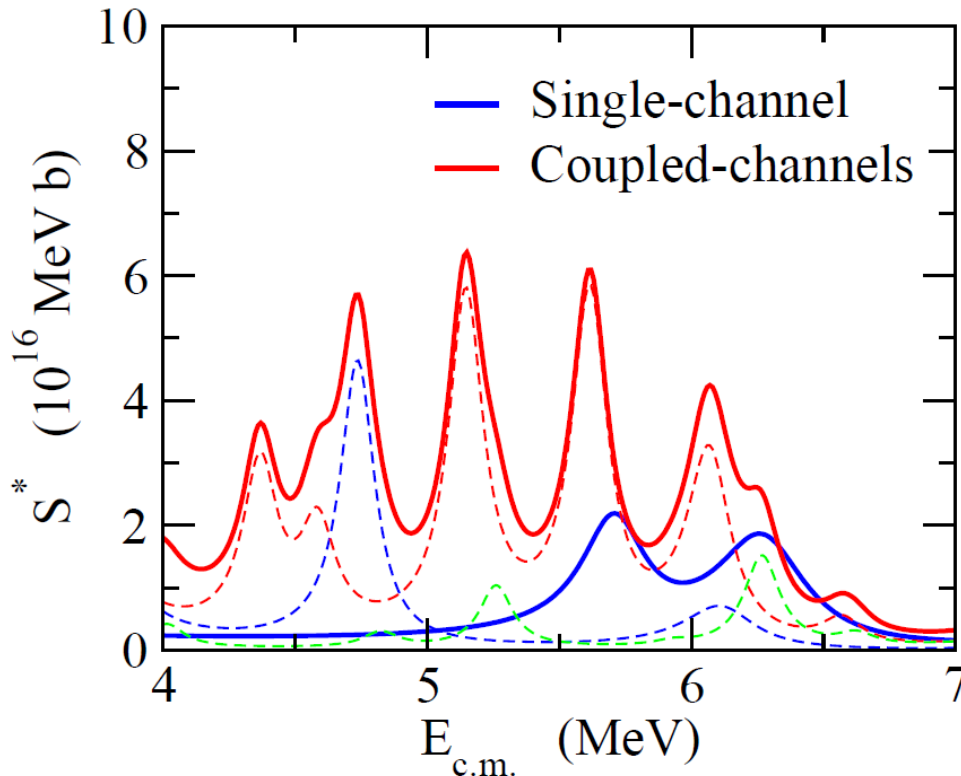
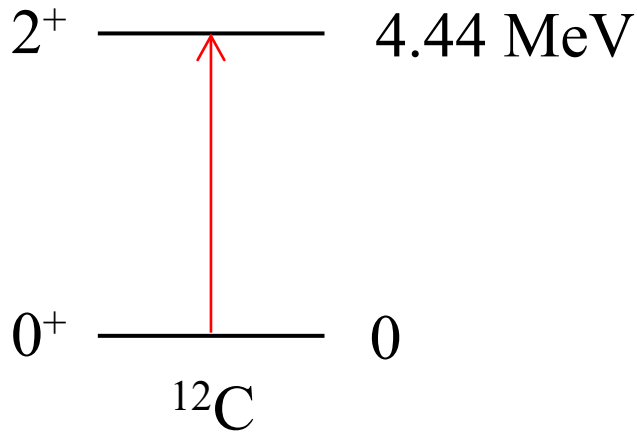
W.P. Tan et al.,
PRL124 ('20) 192702



N.T. Zhang, ..., K.H., S. Kubono, ..., C.J. Lin, ...

XiaoDong Tang (IMP) et al., Phys. Lett. B801 (2020) 135170

$^{12}\text{C}+^{12}\text{C}$ fusion: many resonance peaks

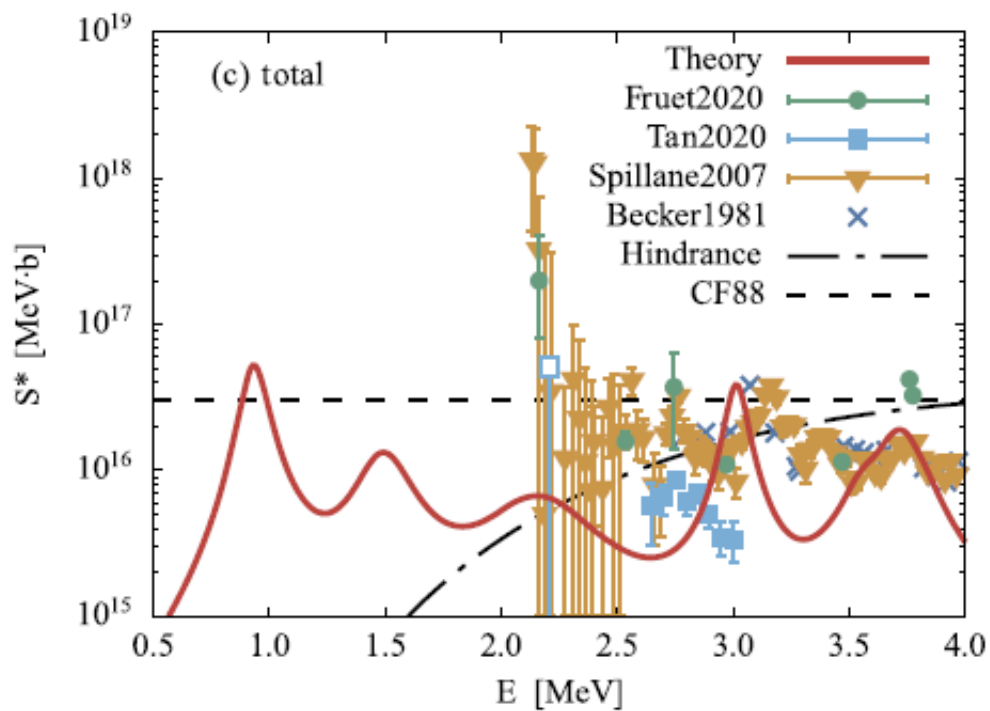
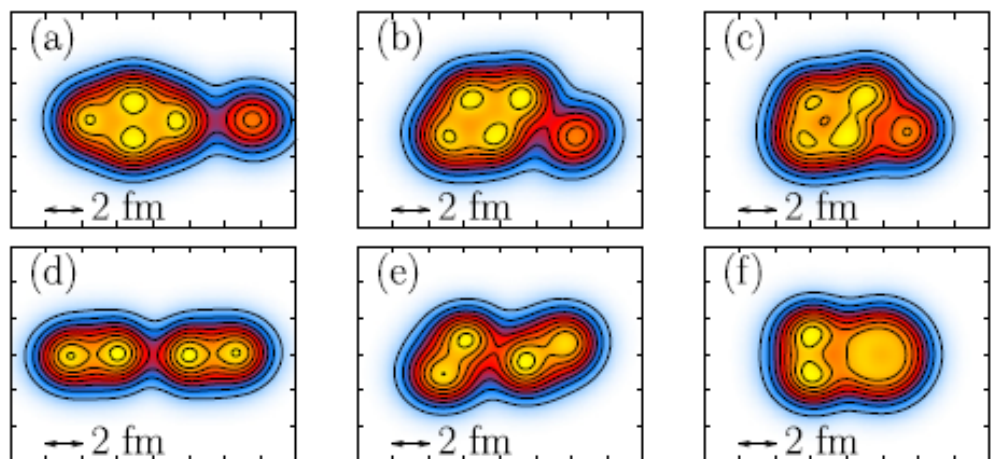


H.-J. Fink, W. Scheid,
and W. Greiner,
NPA188 ('72) 259

a kind of
Feshbach resonance

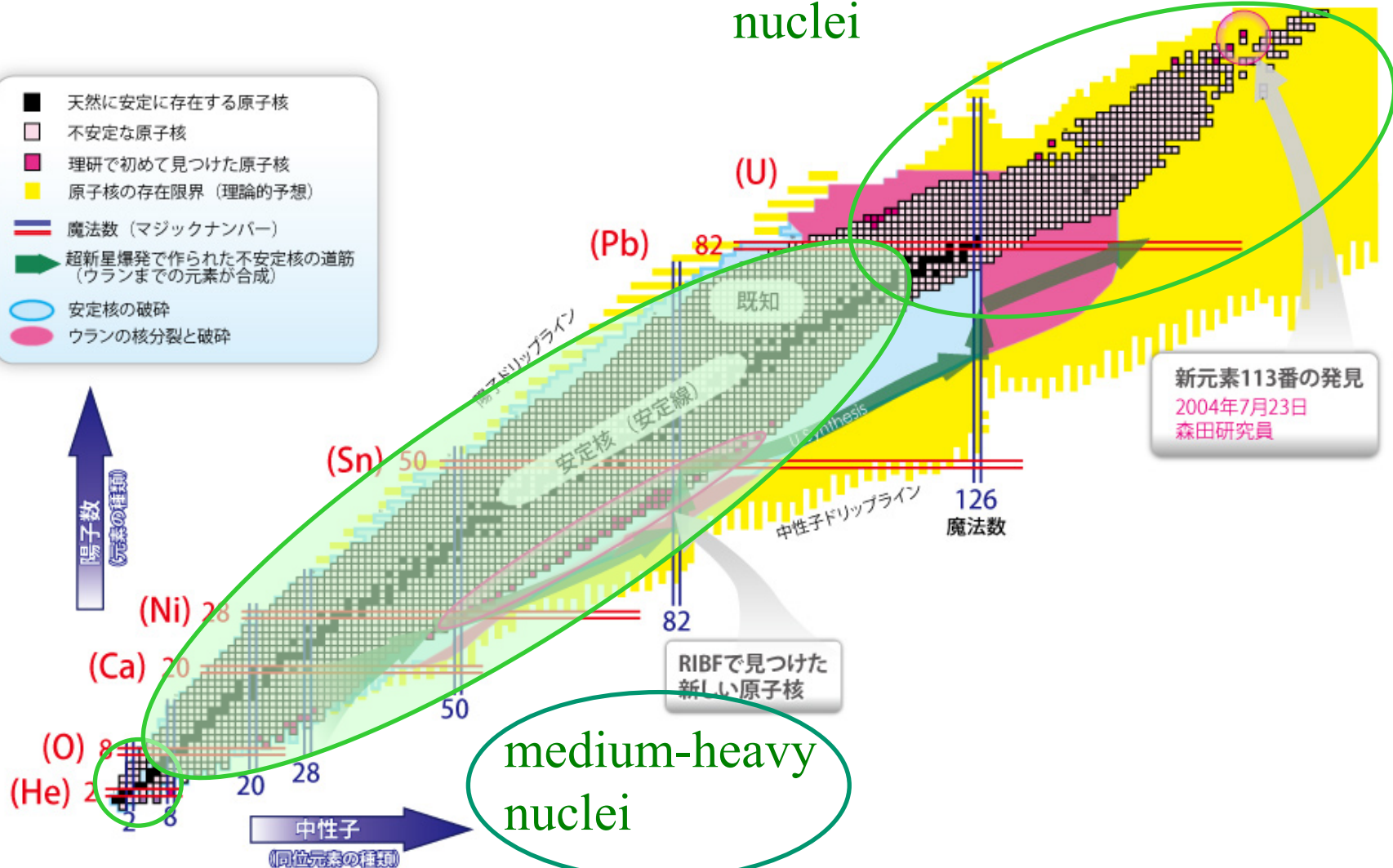
A recent AMD calculation

Y. Taniguchi and M. Kimura, PLB823 ('21) 136790



Heavy and Superheavy nuclei

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- 不安定な原子核
- 理研で初めて見つけた原子核
- 原子核の存在限界 (理論的予想)
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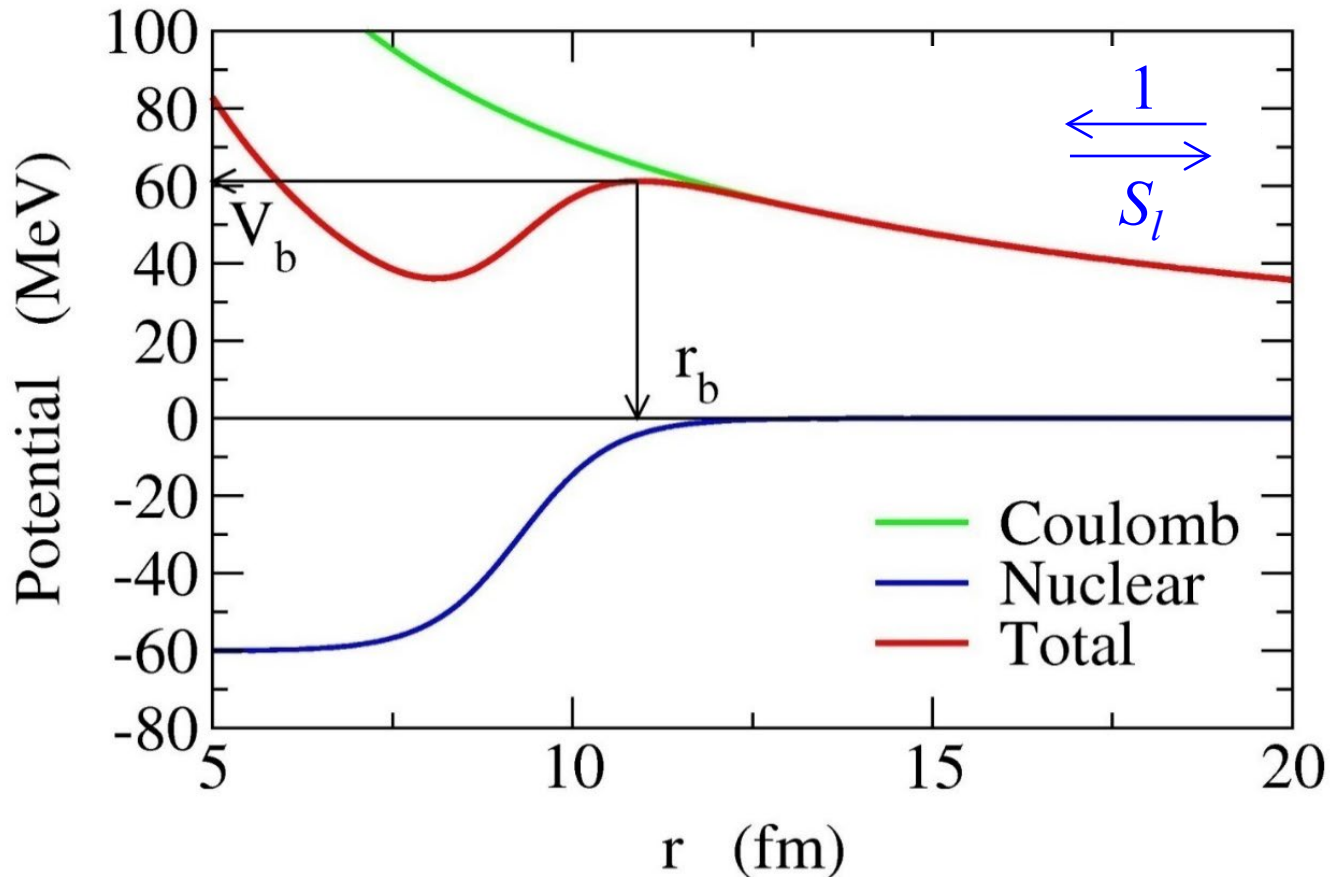
light nuclei

medium-heavy nuclei

Fusion reactions of medium-heavy nuclei

potential model: inert nuclei (no structure)

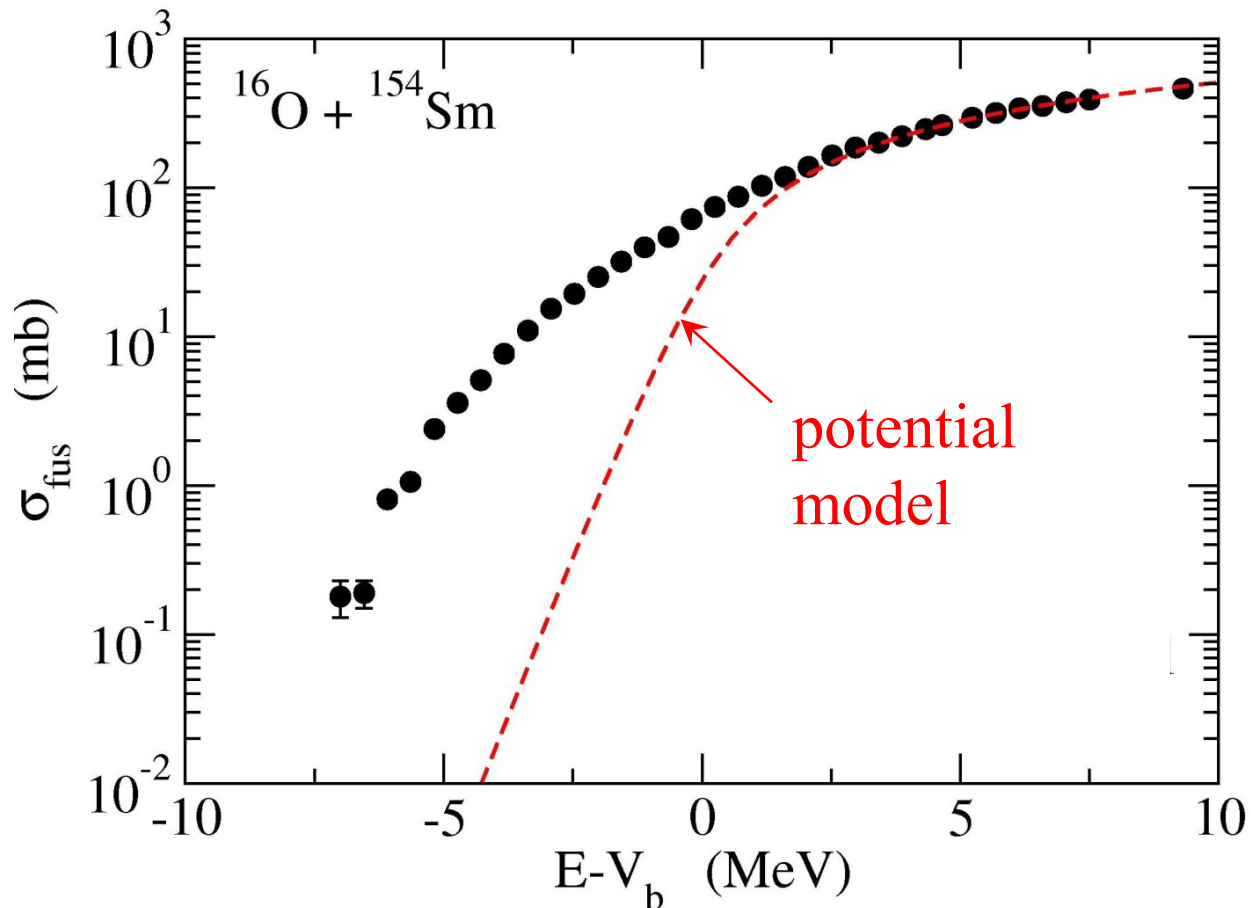
$$\sigma_{\text{fus}} = \frac{\pi}{k^2} \sum_l (2l + 1)(1 - |S_l|^2)$$



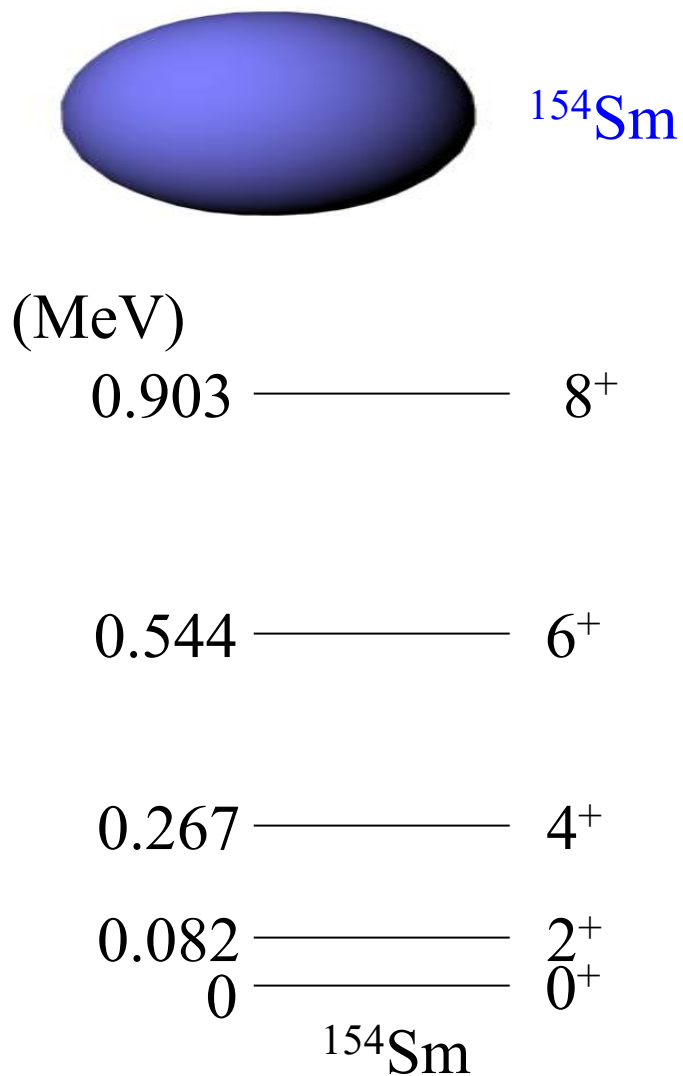
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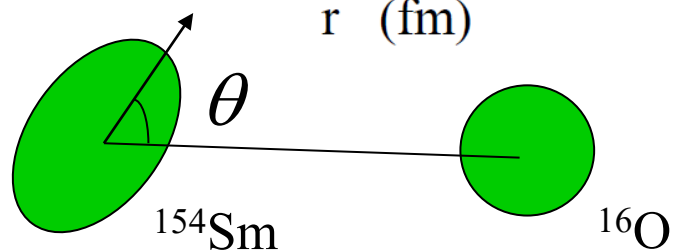
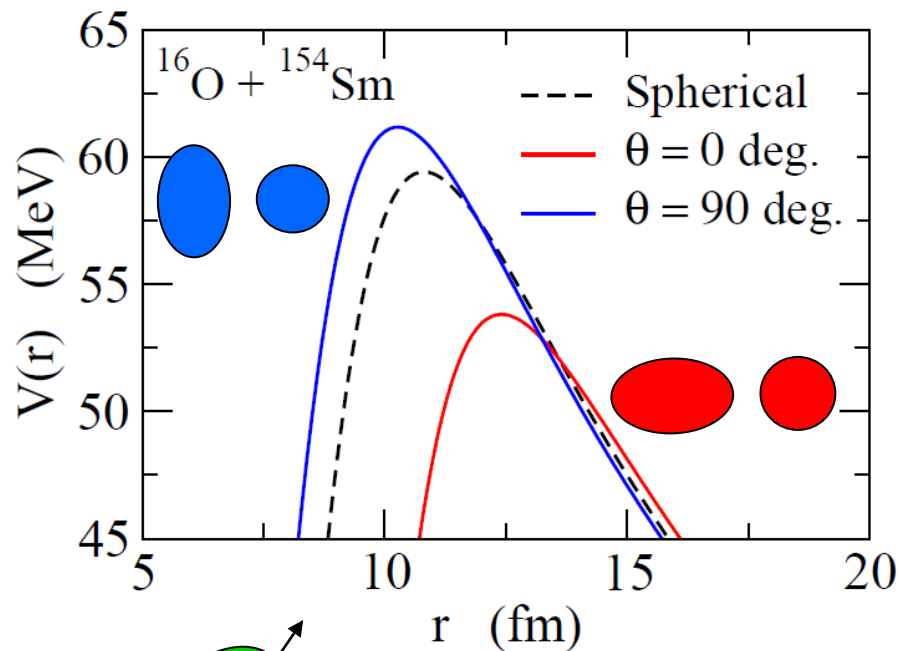
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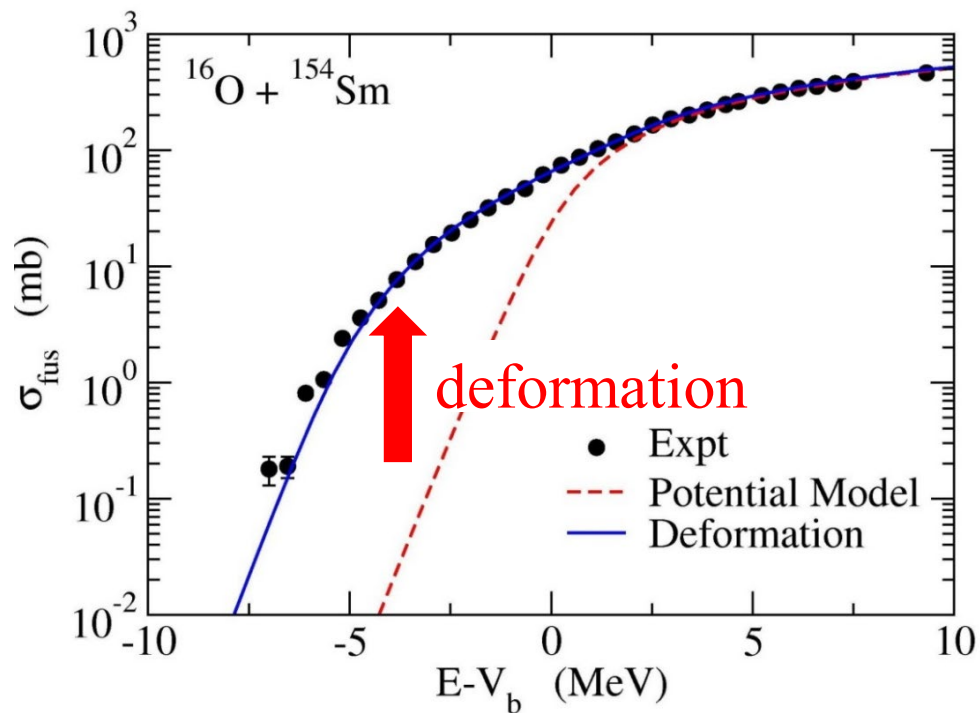
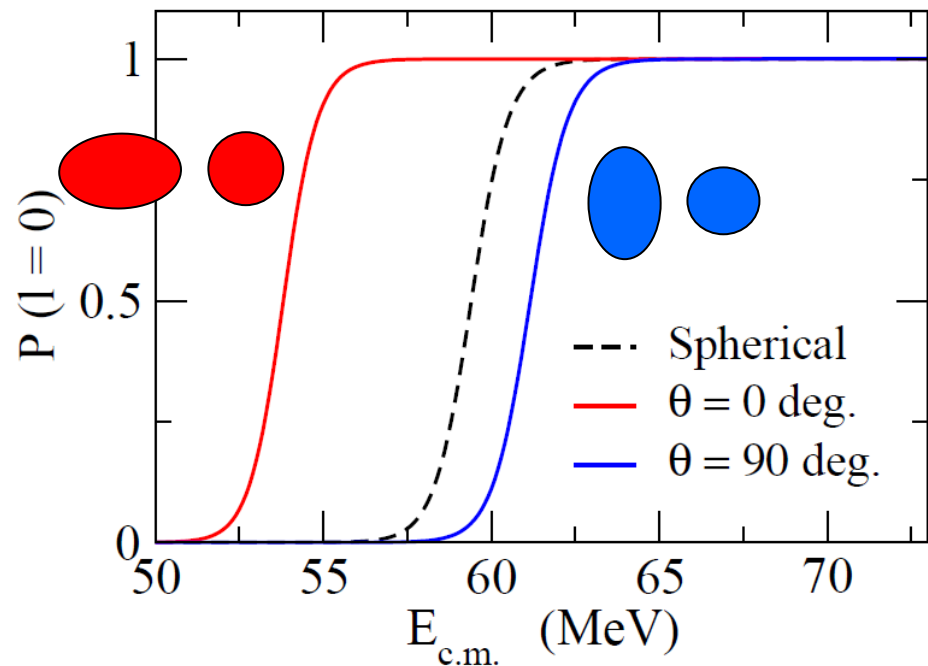
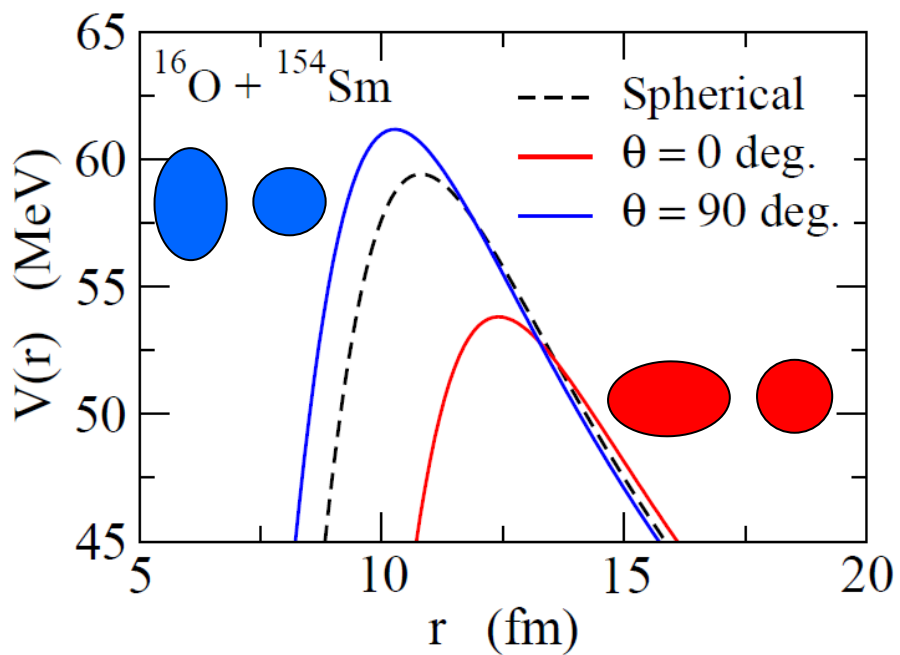
^{154}Sm : a typical deformed nucleus

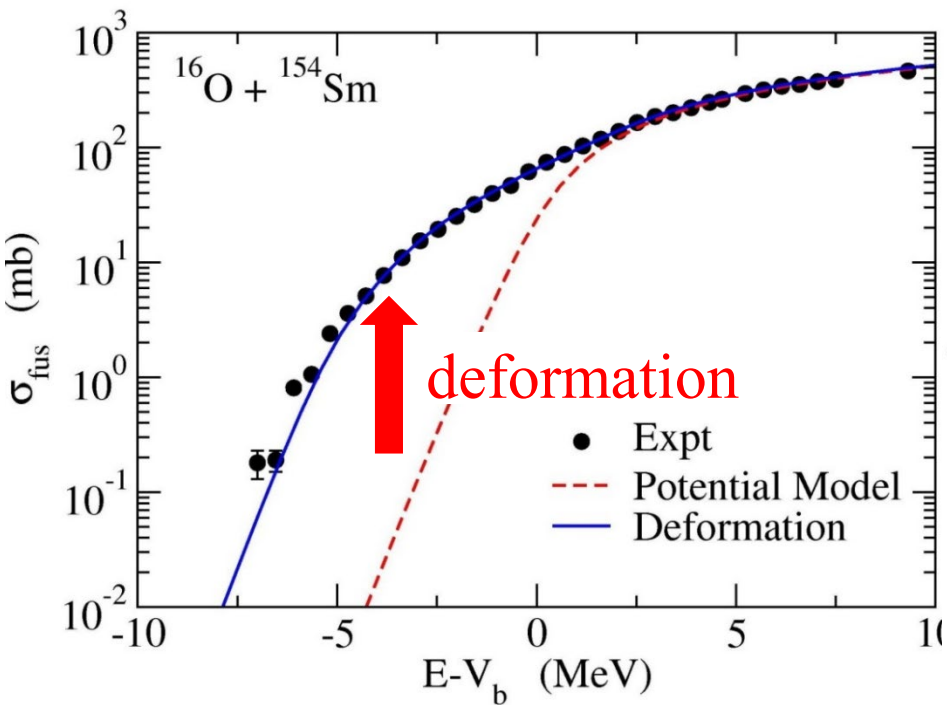


rotational spectrum

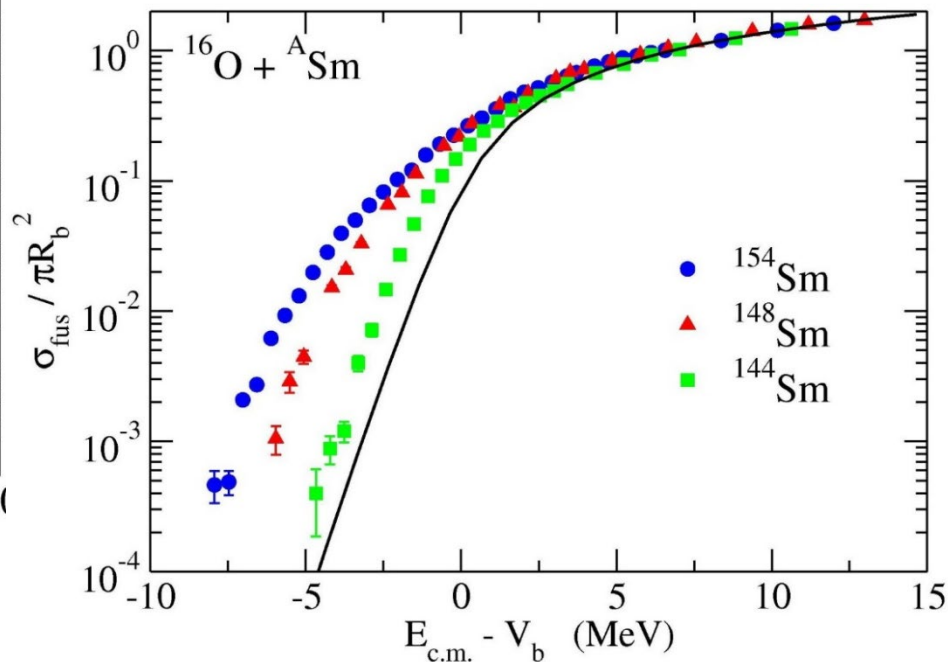


$$\sigma_{\text{fus}}(E) = \int_0^1 d(\cos \theta) \sigma_{\text{fus}}(E; \theta)$$

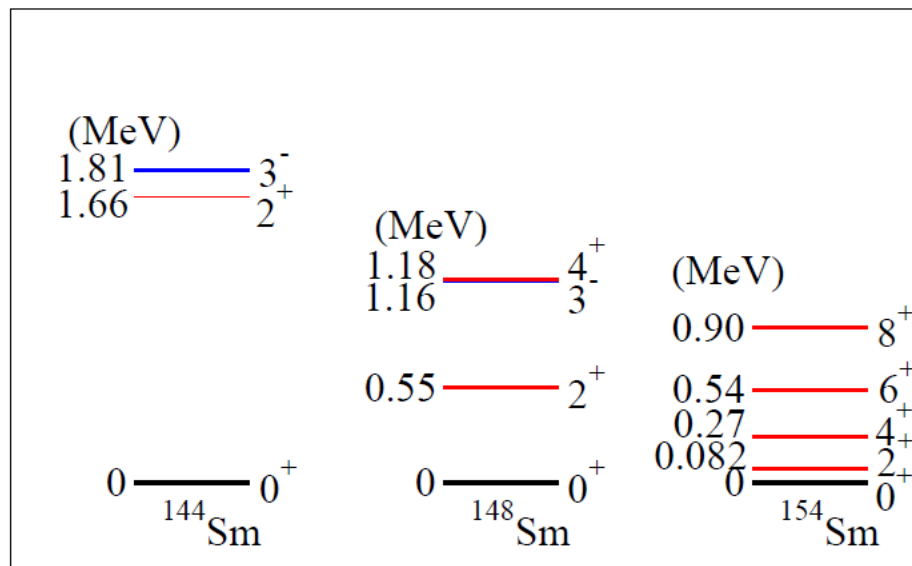




similar enhancement
for non-deformed nuclei

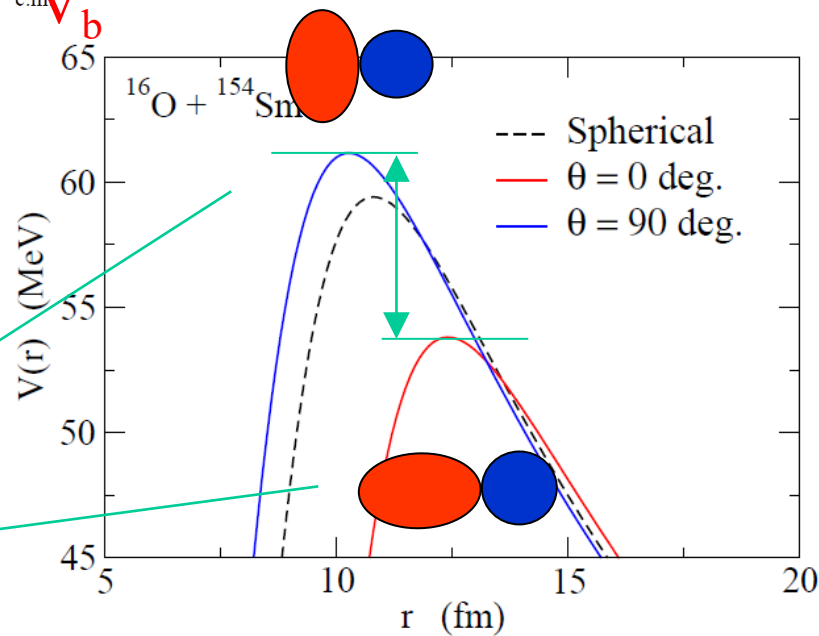
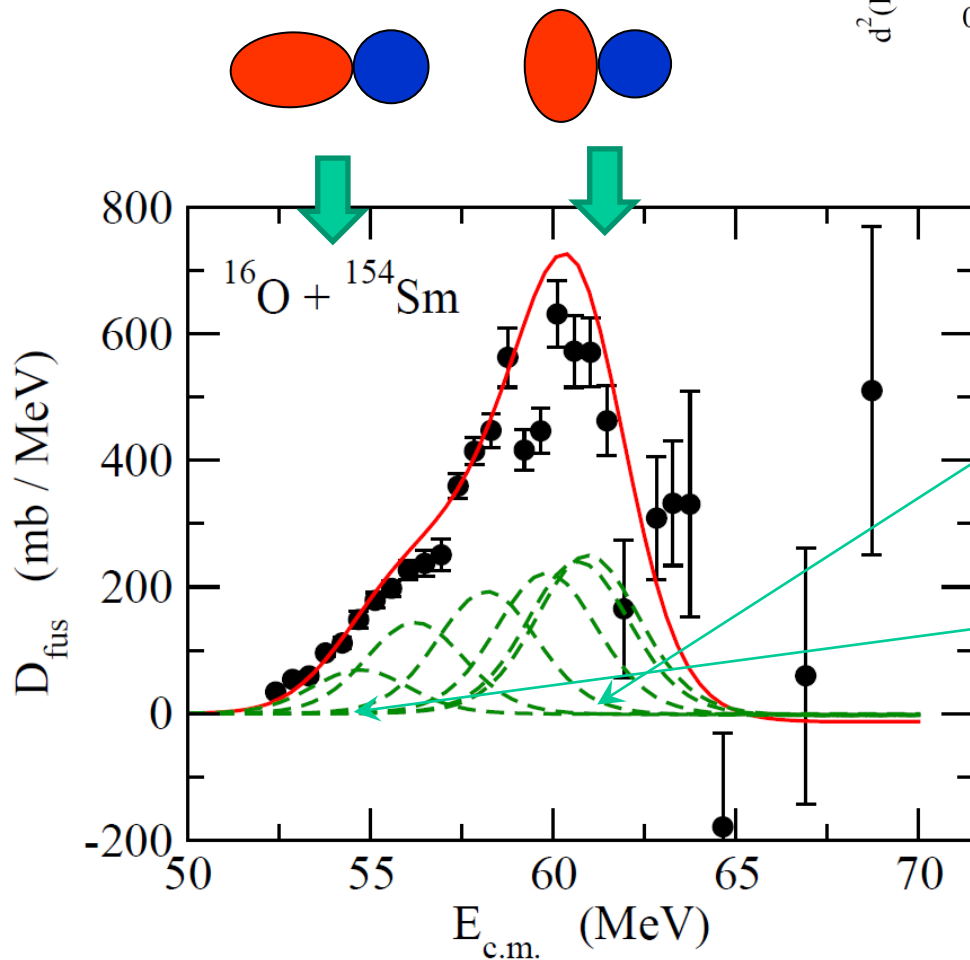
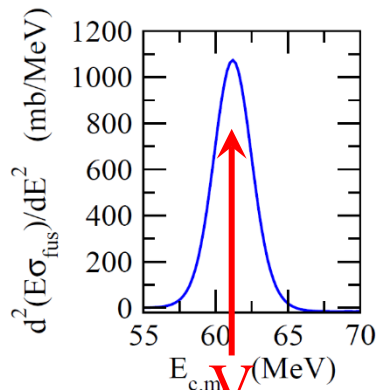


strong correlation
with nuclear spectrum
→ coupling assisted
tunneling phenomena



✓ Fusion barrier distribution (Rowley, Satchler, Stelson, PLB254('91))

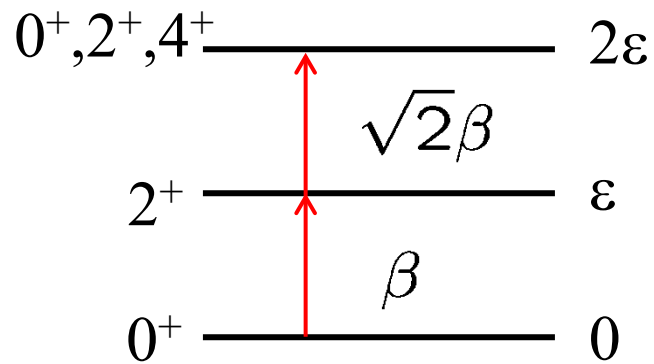
$$D_{\text{fus}}(E) = \frac{d^2(E\sigma_{\text{fus}})}{dE^2}$$



Semi-microscopic modelling of subbarrier fusion reactions

K.H. and J.M. Yao, PRC91('15) 064606

simple harmonic
oscillator



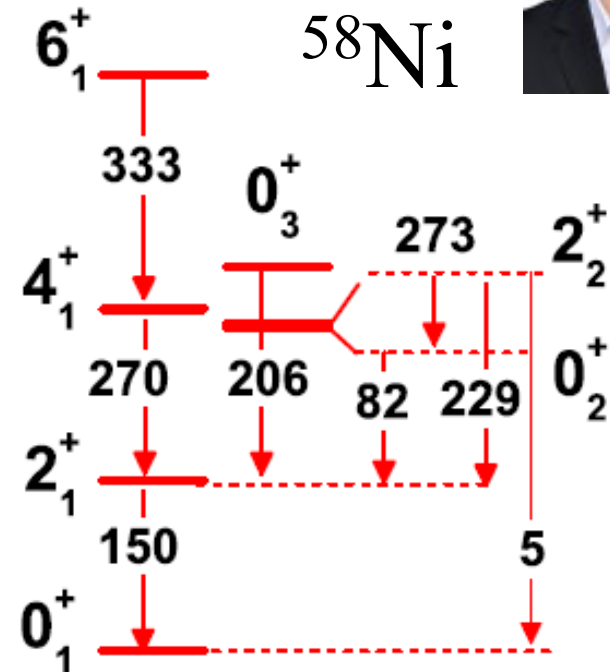
Semi-microscopic modelling of subbarrier fusion reactions

K.H. and J.M. Yao, PRC91('15) 064606



$$|JM\rangle = \int d\beta f_J(\beta) \hat{P}_{M0}^J |\Phi(\beta)\rangle$$

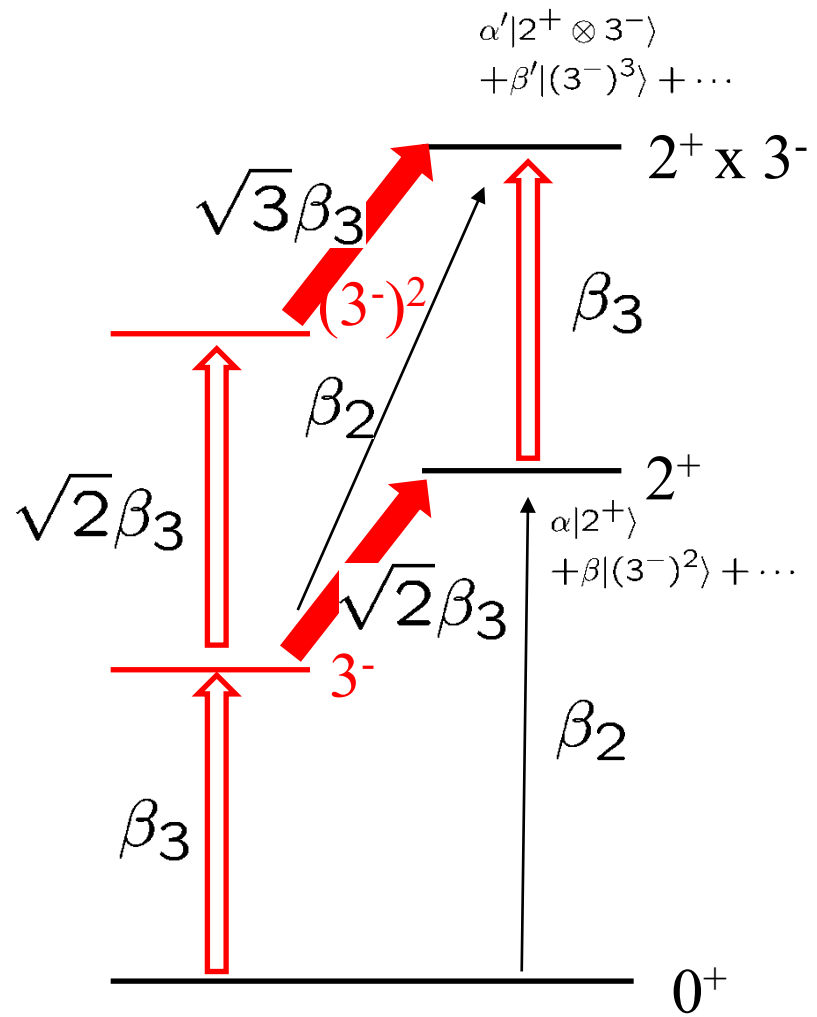
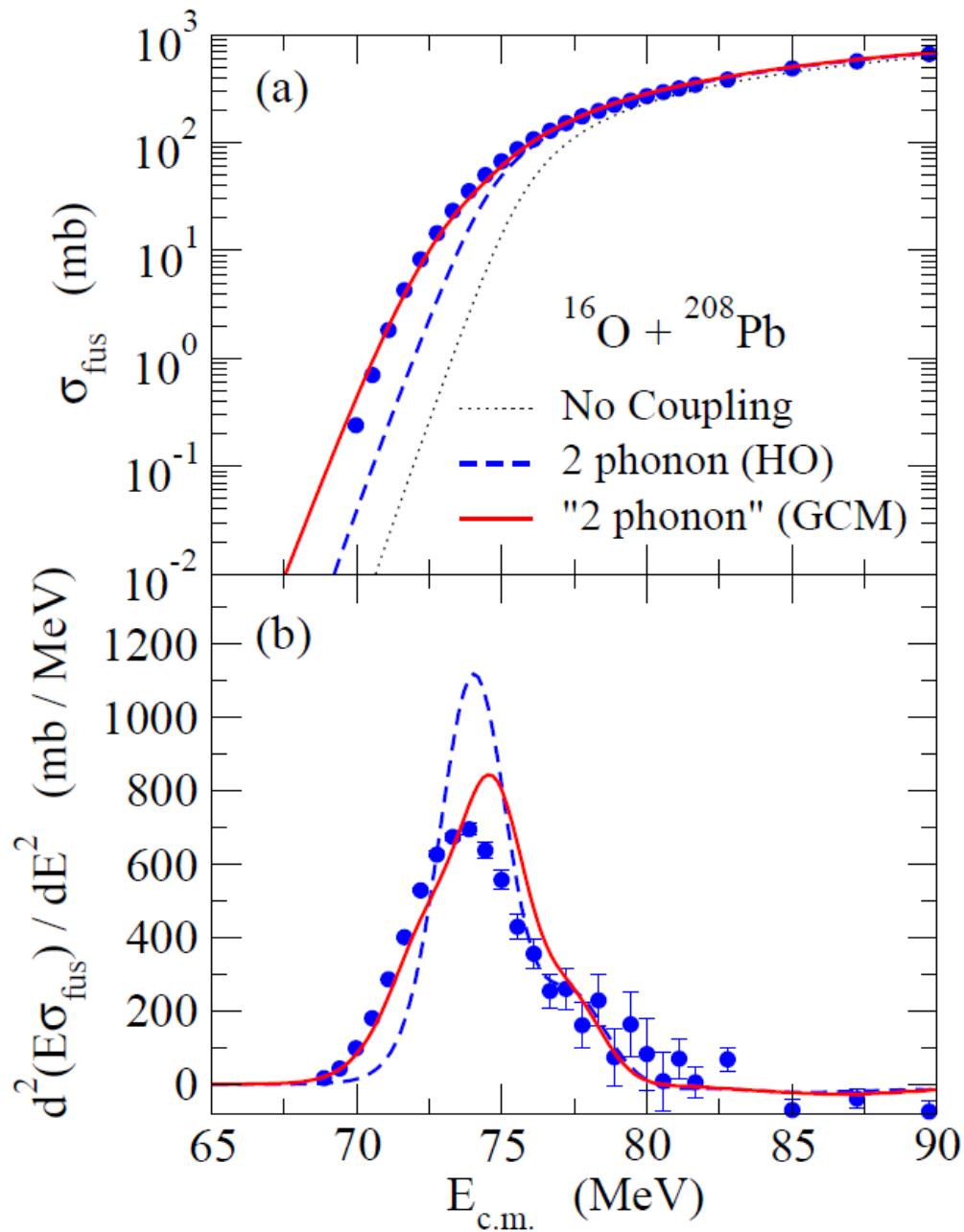
- ✓ MF + ang. mom. projection
- + particle number projection
- + generator coordinate method (GCM)



PC-PK1

Beyond-mean-field method
anharmonicity of phonon spectra

→ C.C. calculations with
a phenomenological potential



J.M. Yao and K.H.,
PRC94 ('16) 11303(R)

From phenomenological approach to microscopic approach

Macroscopic (phenomenological)

C.C. with collective model

C.C. with inputs from
microscopic nuclear
structure calculations

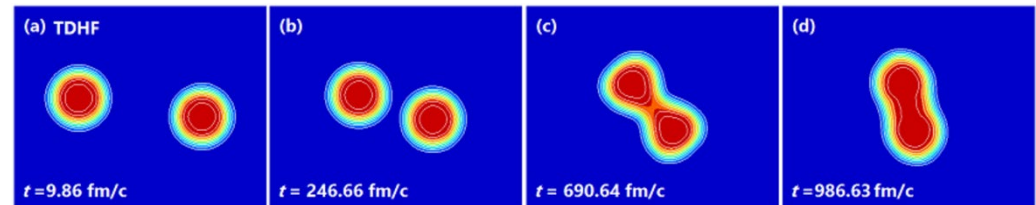
C.C. with inputs based
on TDHF

TDHF simulations



Microscopic

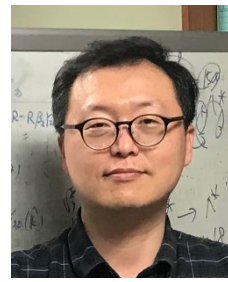
TDHF = Time Dependent Hartree-Fock



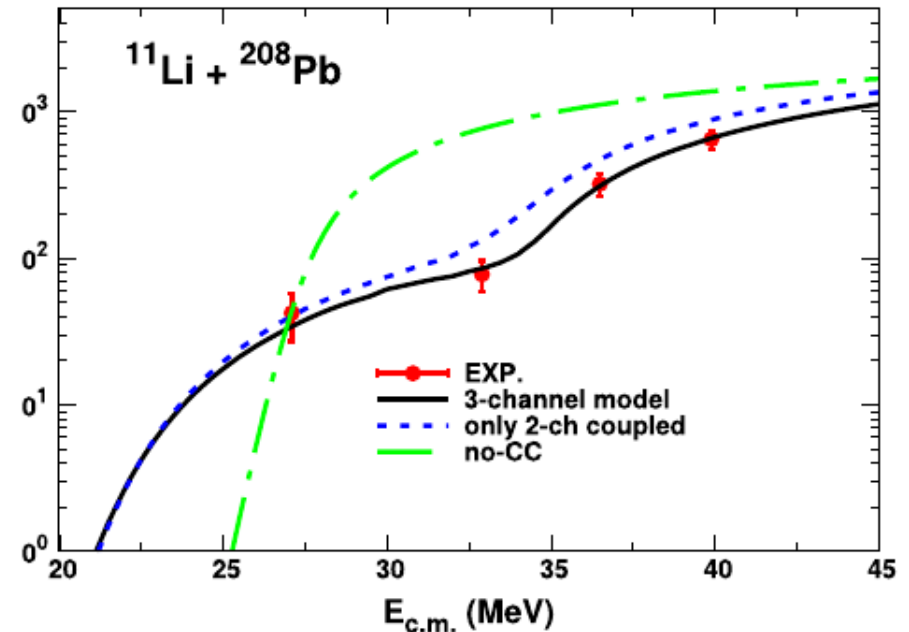
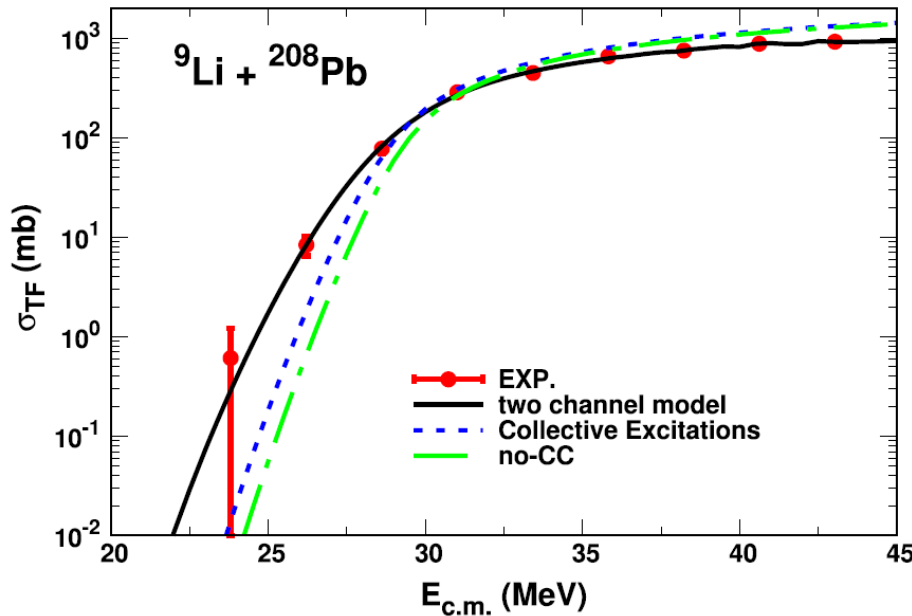
S. Ebata, T. Nakatsukasa, JPC Conf. Proc. 6 ('15)

ab initio, but no tunneling

Fusion of neutron-rich nuclei



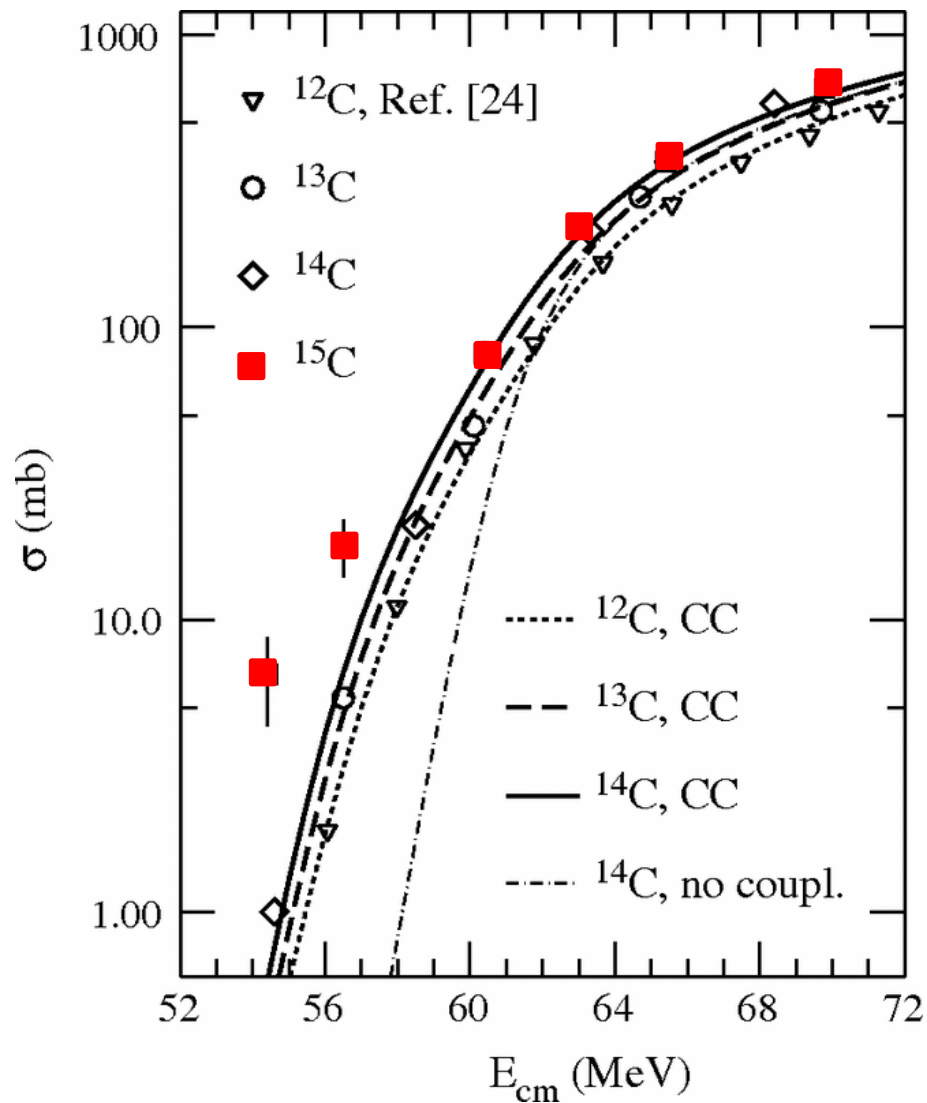
K.-S. Choi, M.-K. Cheoun, W.Y. So, K.H.,
and K.S. Kim, Phys. Lett. B780 ('18) 455



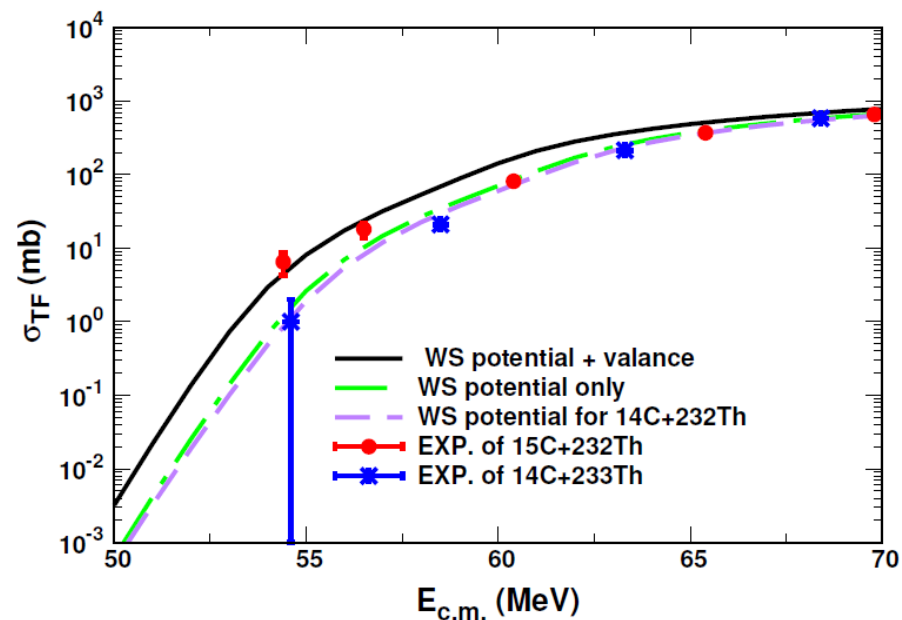
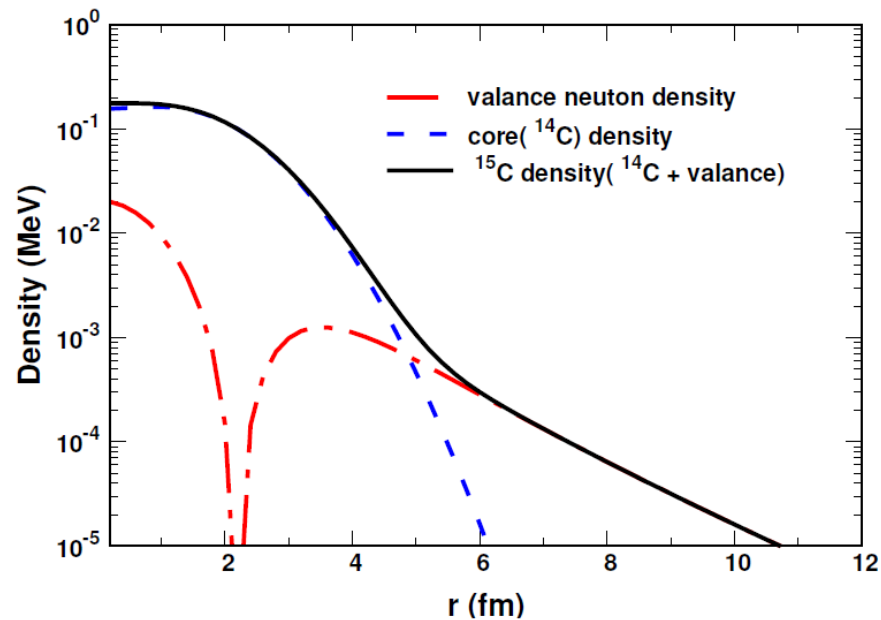
simultaneous explanation for ${}^9\text{Li} + {}^{208}\text{Pb}$ and ${}^{11}\text{Li} + {}^{208}\text{Pb}$ with:
 ${}^{11}\text{Li} + {}^{208}\text{Pb} \longleftrightarrow {}^9\text{Li} + {}^{210}\text{Pb} \longleftrightarrow {}^7\text{Li} + {}^{212}\text{Pb}$ transfer couplings

Fusion of neutron-rich nuclei

$^{12,13,14,15}\text{C} + ^{232}\text{Th}$



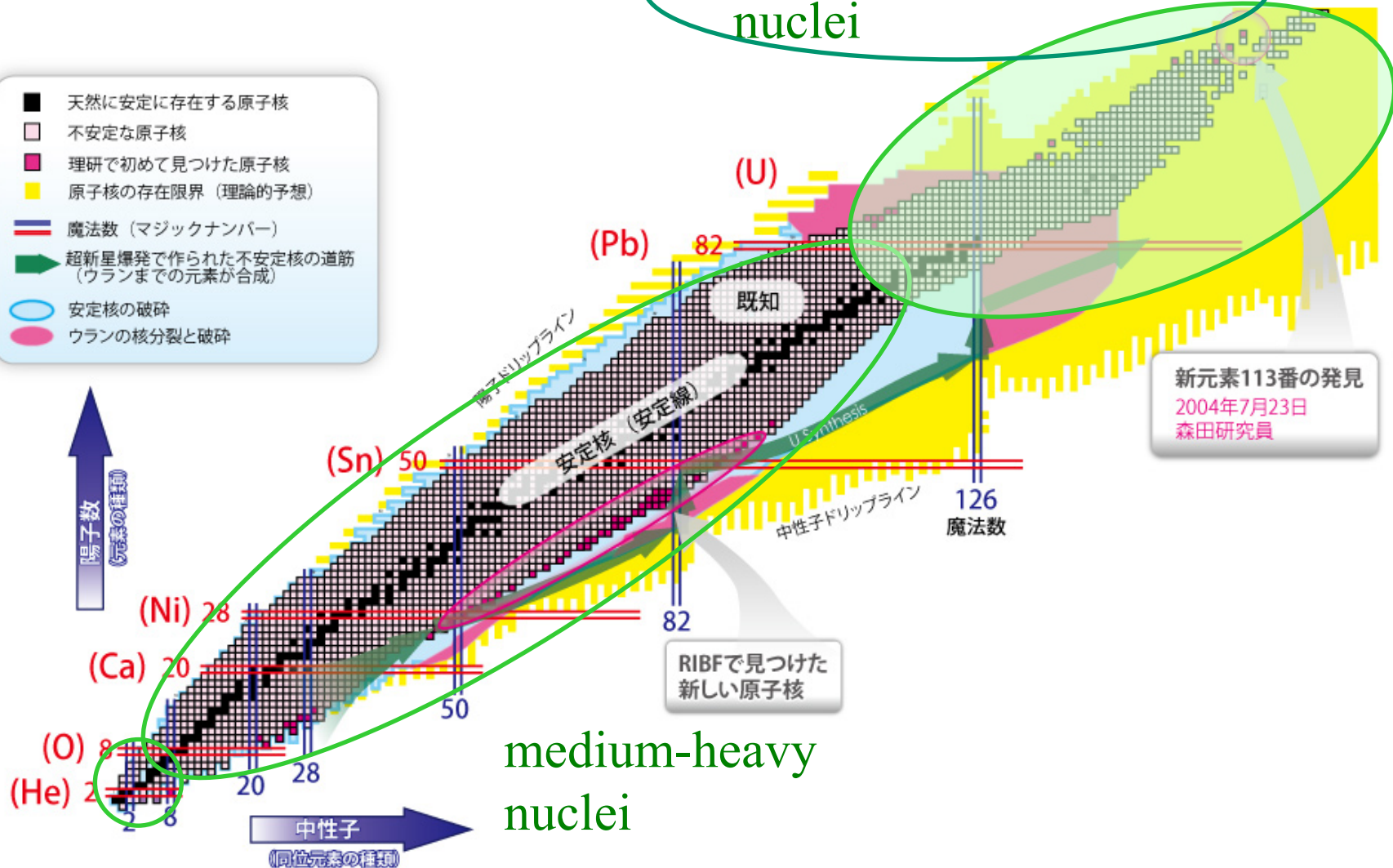
M. Alcorta et al., PRL106('11)



K.-S. Choi, ..., K.H. et al., in preparation

Heavy and Superheavy nuclei

- 天然に安定に存在する原子核
- 不安定な原子核
- 理研で初めて見つけた原子核
- 原子核の存在限界 (理論的予想)
- 魔法数 (マジックナンバー)
- ➔ 超新星爆発で作られた不安定核の道筋 (ウランまでの元素が合成)
- 安定核の破碎
- ウランの核分裂と破碎



light nuclei

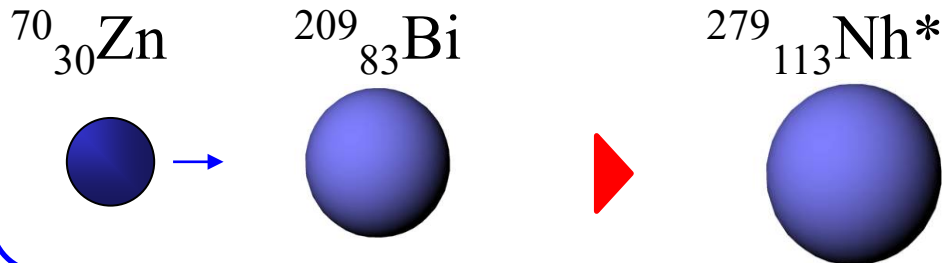
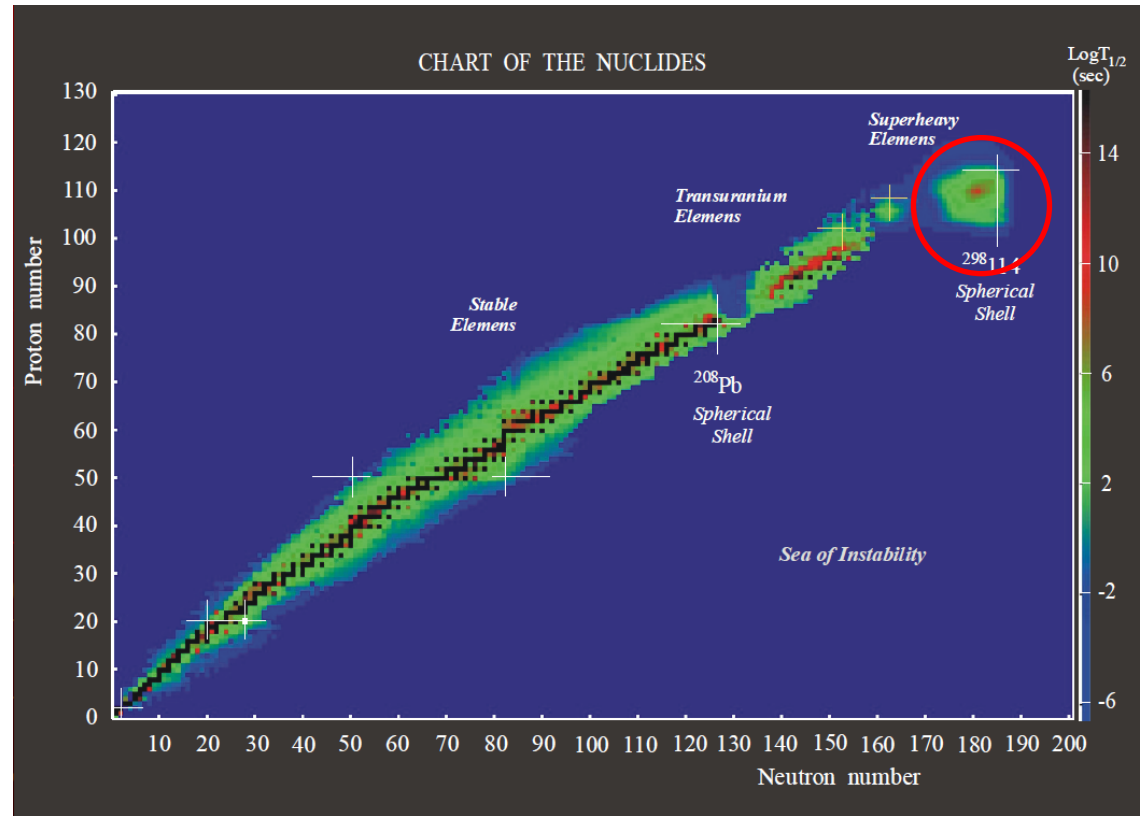
medium-heavy nuclei

Superheavy elements

113 Nh nihonium	115 Mc moscovium
117 Ts tennessine	118 Og oganeson

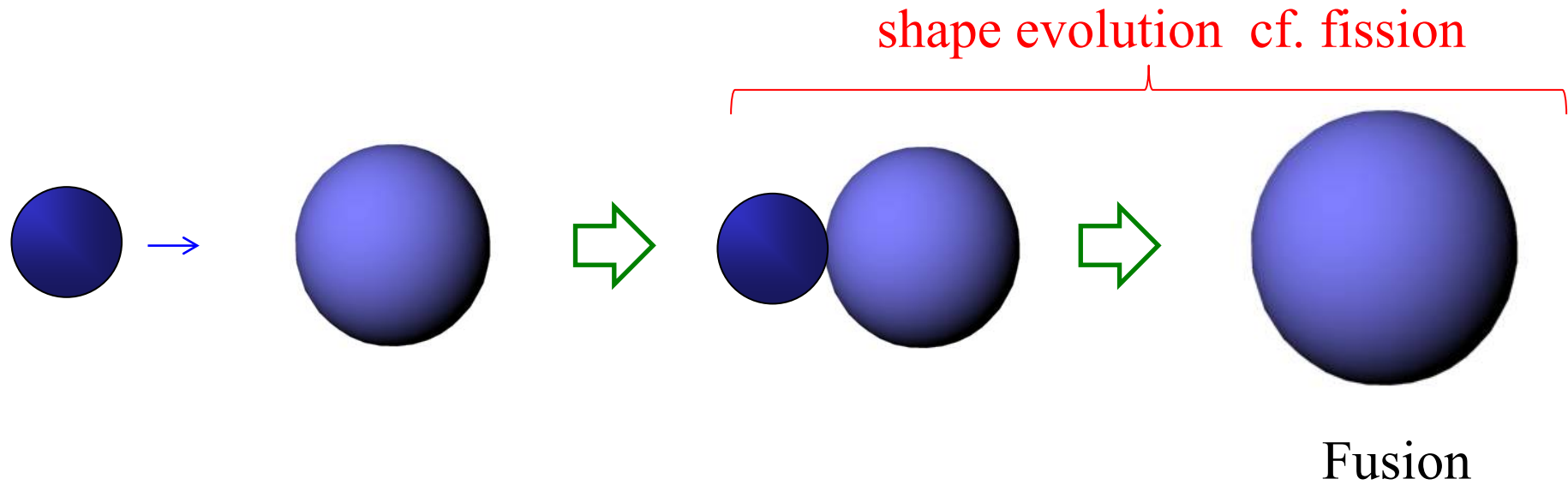
November, 2016

the island of stability (安定的島)



Heavy-ion fusion reaction

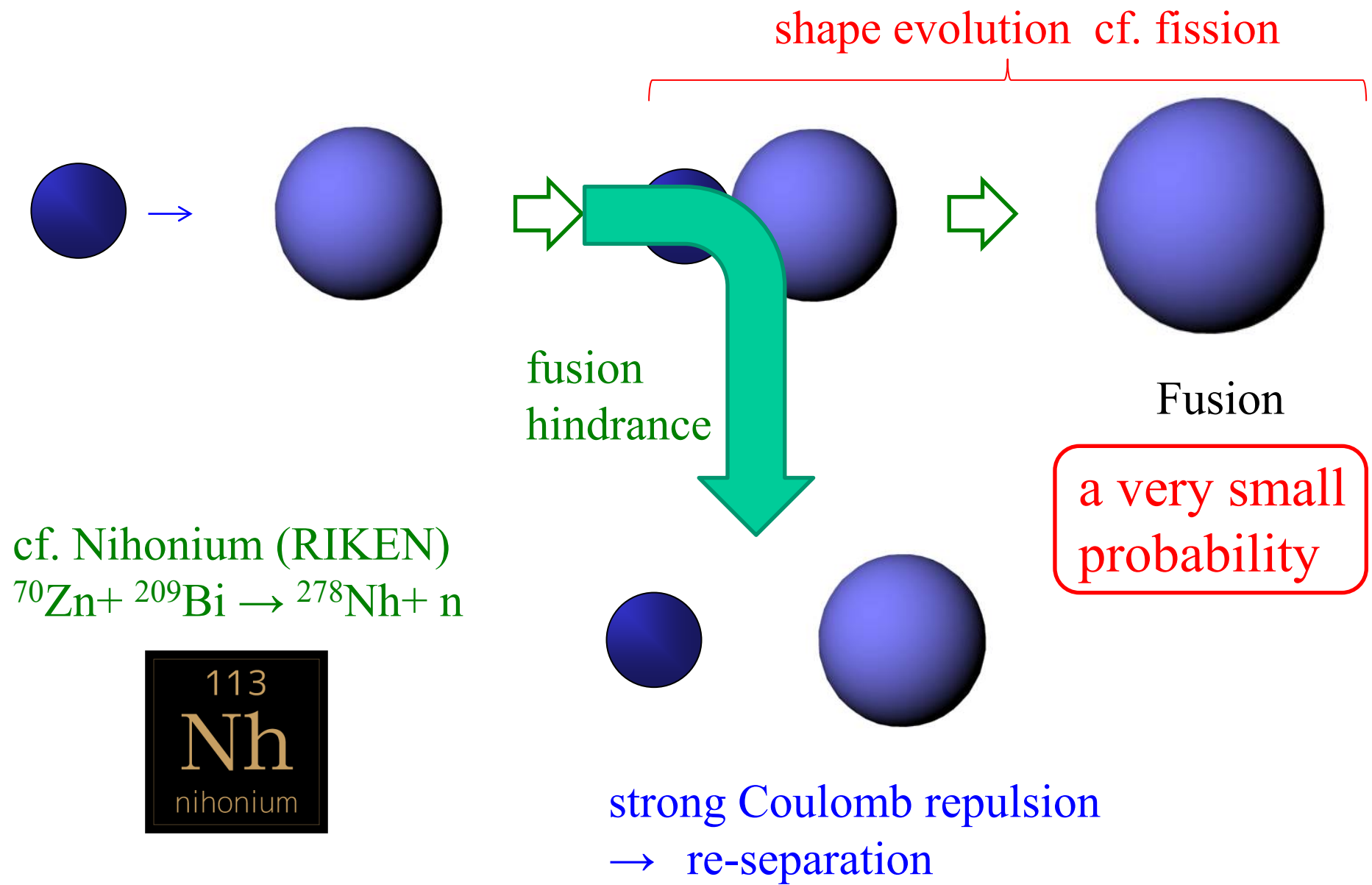
Fusion of heavy nuclei and superheavy elements



cf. Nihonium (RIKEN)



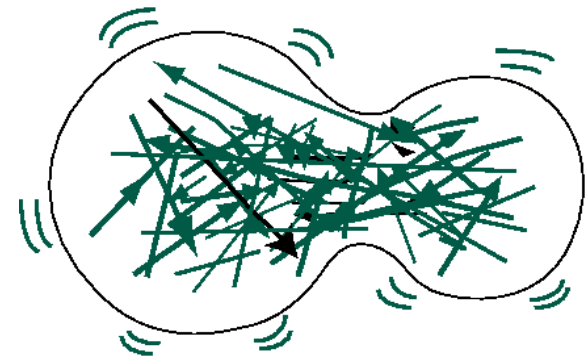
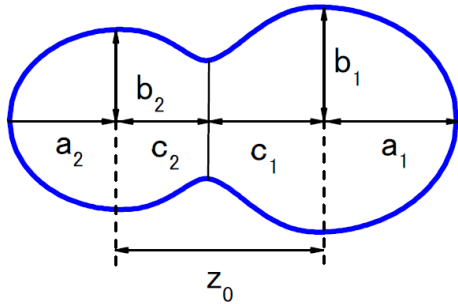
Fusion of heavy nuclei and superheavy elements



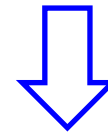
cf. Nihonium (RIKEN)
 $^{70}\text{Zn} + ^{209}\text{Bi} \rightarrow ^{278}\text{Nh} + n$



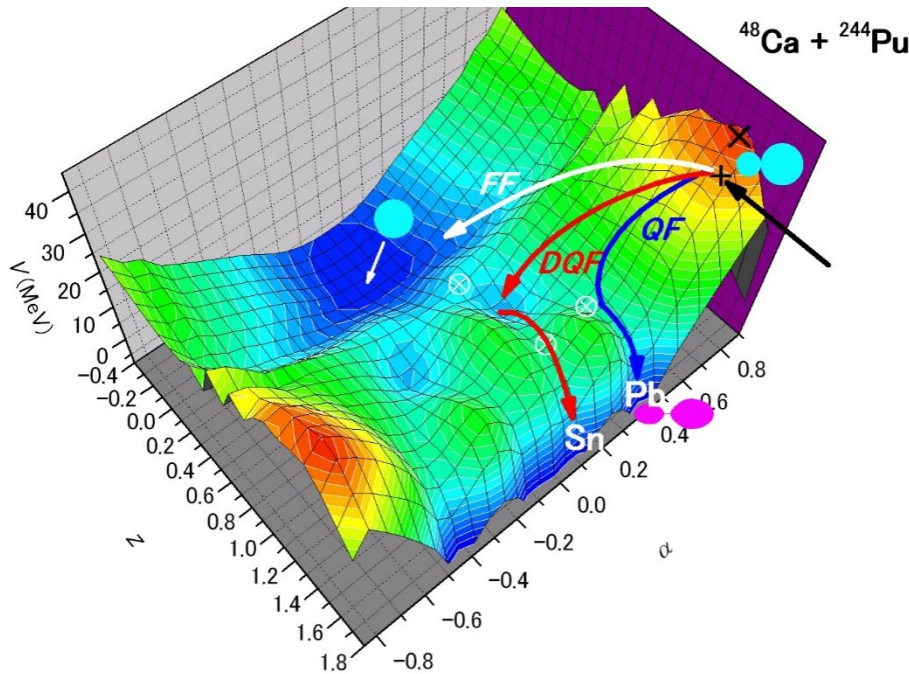
Nuclear shape evolution



nucleus = many-body system
of nucleons



nuclear intrinsic d.o.f.
: internal environment
→ physics of open quantum
systems

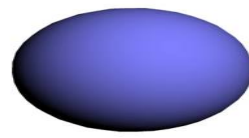


cf. Classical Langevin equation

$$m \frac{d^2 q}{dt^2} = - \frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

Y. Aritomo, K. Hagino, K. Nishio,
and S. Chiba, PRC85 (2012) 044614

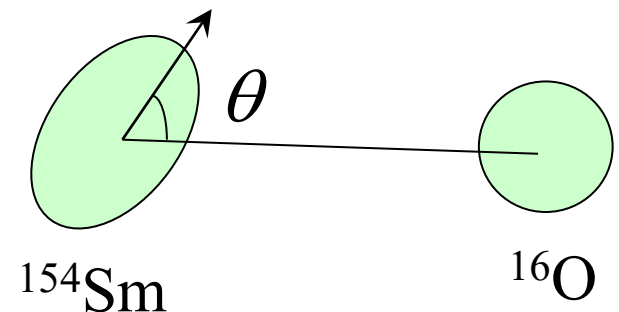
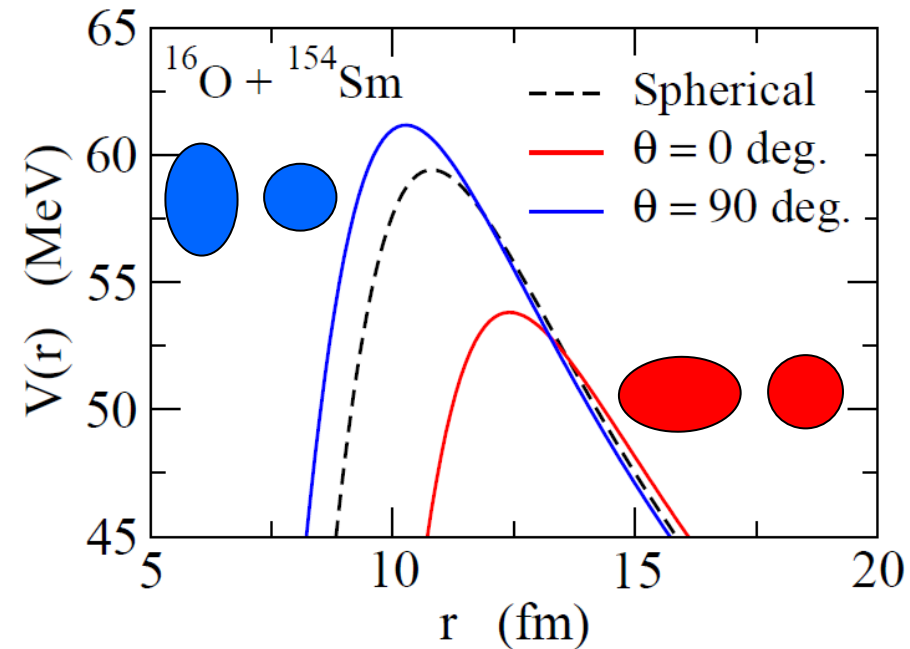
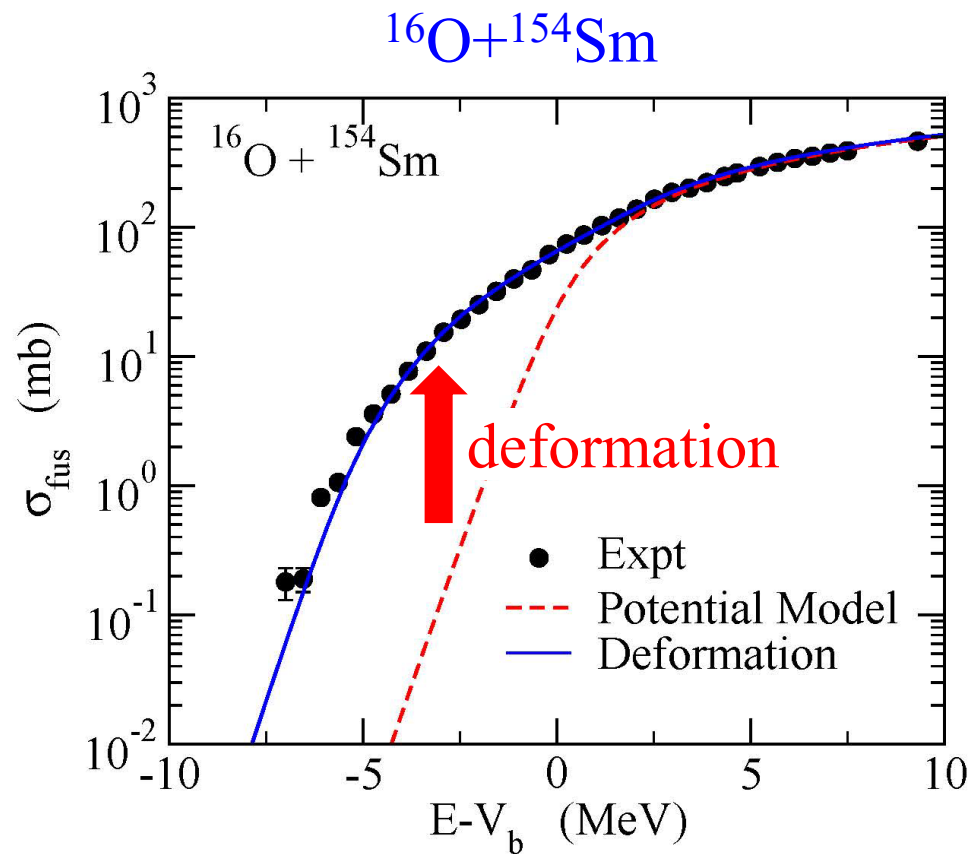
optimum bombarding energy



the role of deformation
in heavy-ion reactions?

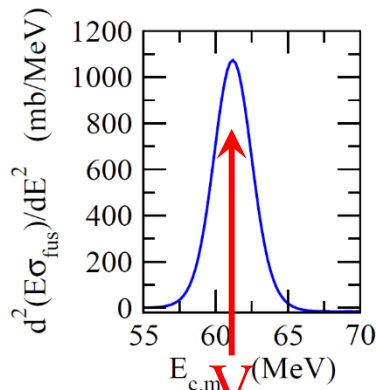
hot fusion: ^{48}Ca + deformed target

Nuclear deformation \rightarrow a large sub-barrier enhancement
of fusion (capture) cross sections

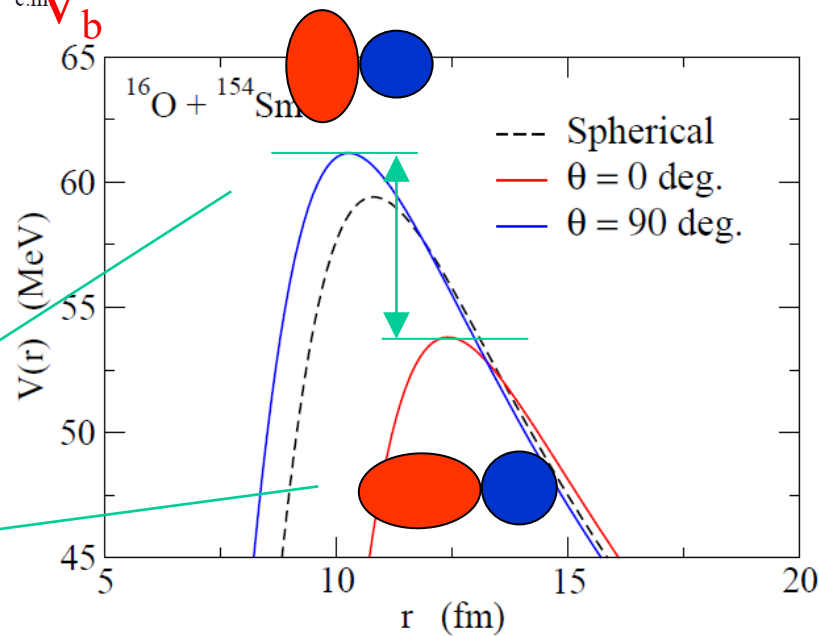
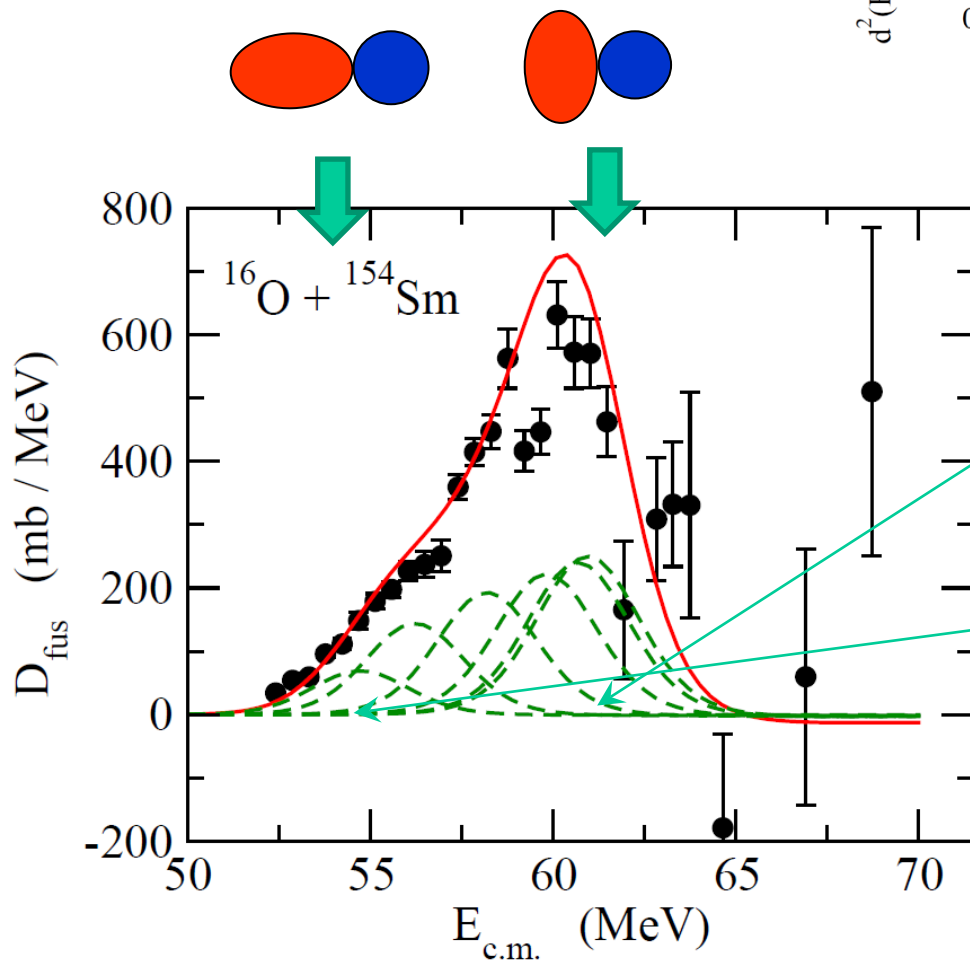


✓ Fusion barrier distribution (Rowley, Satchler, Stelson, PLB254('91))

$$D_{\text{fus}}(E) = \frac{d^2(E\sigma_{\text{fus}})}{dE^2}$$

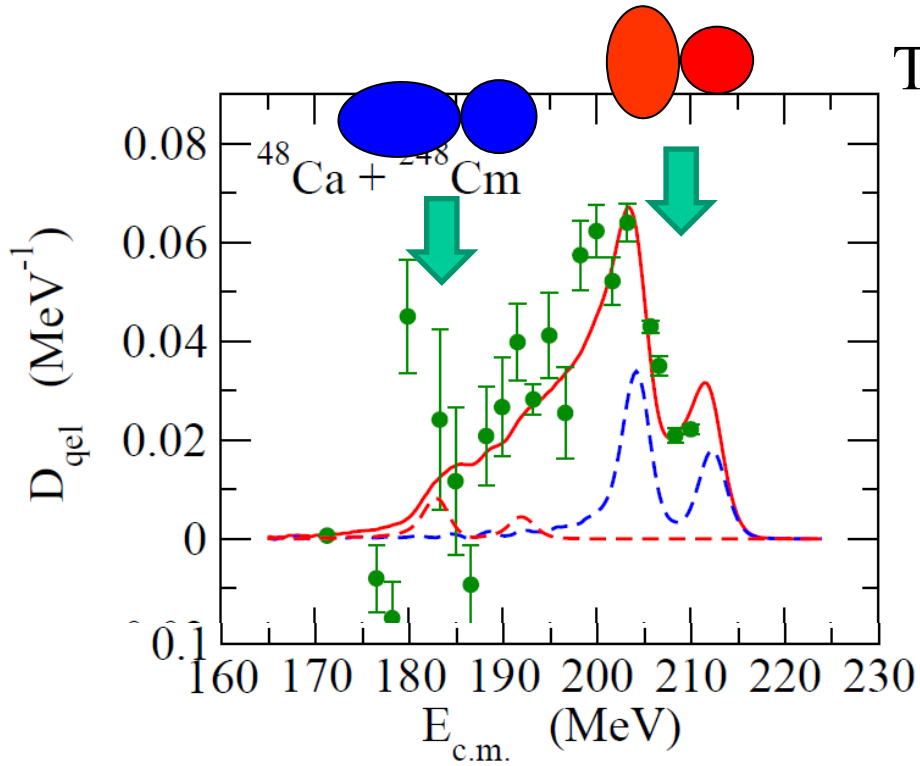
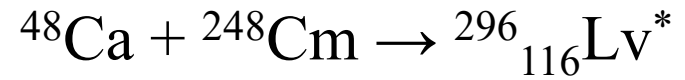


single channel



can be used to identify the side/tip collisions

Application to hot fusion reactions

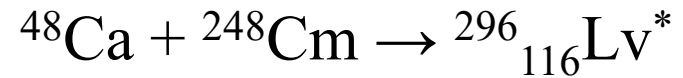


T. Tanaka,..., K.H., et al.,
JPSJ 87 ('18) 014201
PRL124 ('20) 052502

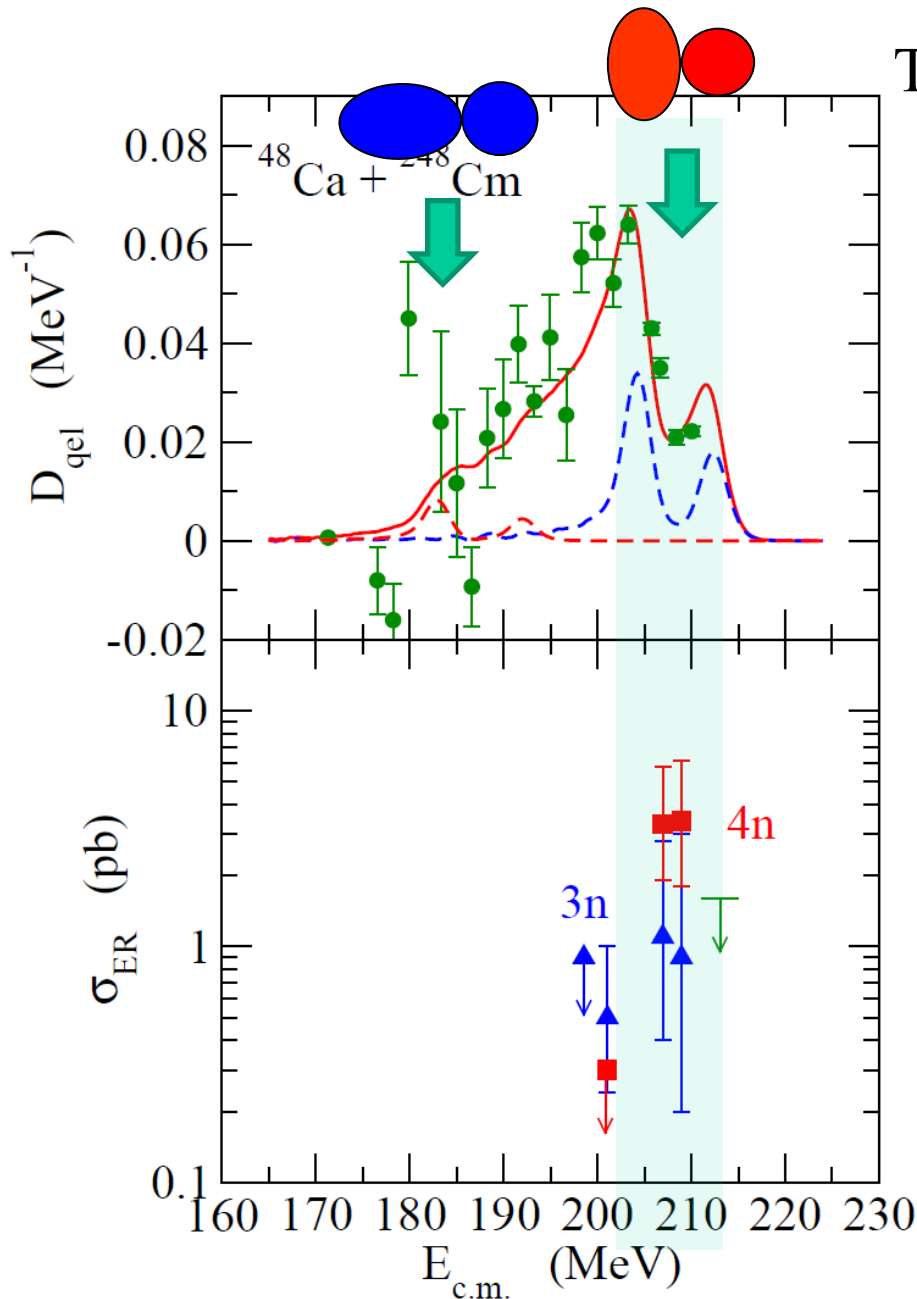


capture barrier distribution

Application to hot fusion reactions



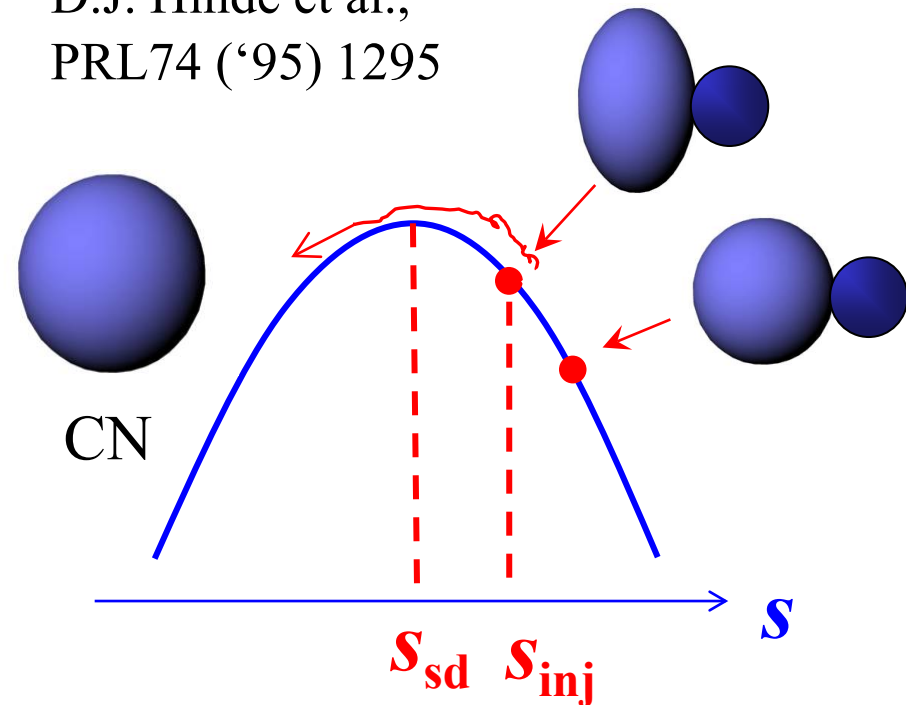
T. Tanaka, ..., K.H., et al.,
 JPSJ 87 ('18) 014201
 PRL 124 ('20) 052502



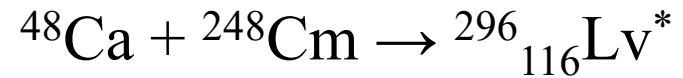
capture barrier distribution

cf. notion of compactness:

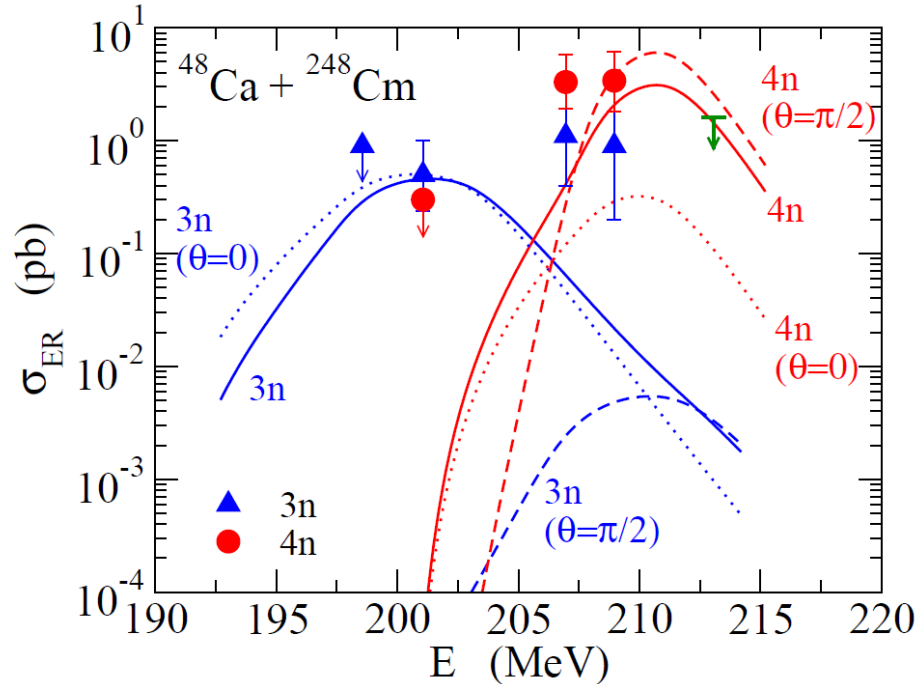
D.J. Hinde et al.,
 PRL 74 ('95) 1295



Application to hot fusion reactions



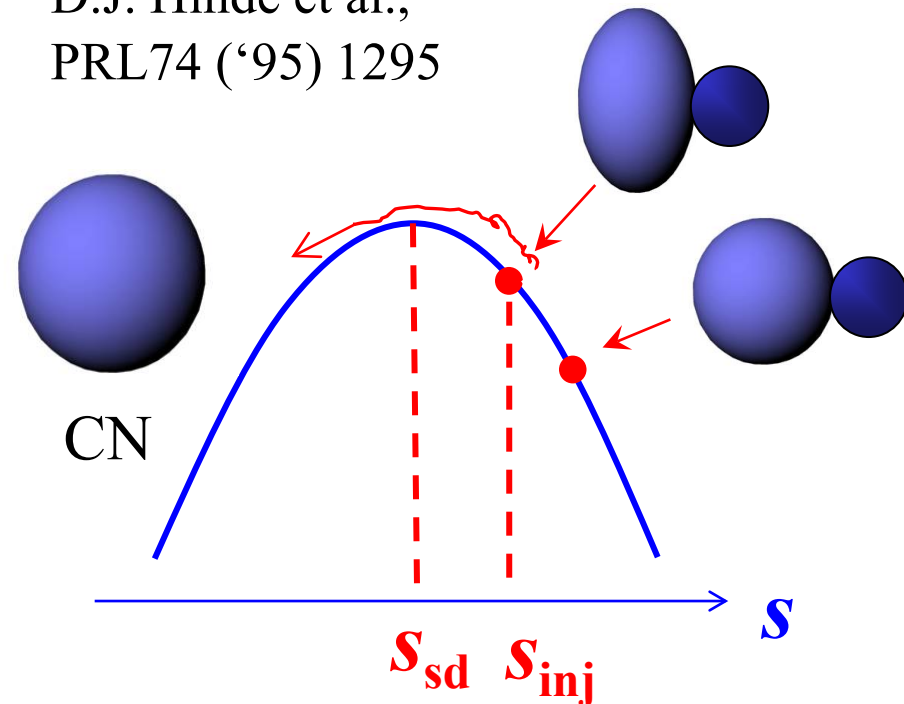
T. Tanaka, ..., K.H., et al.,
 JPSJ 87 ('18) 014201
 PRL 124 ('20) 052502



capture barrier distribution

cf. notion of compactness:

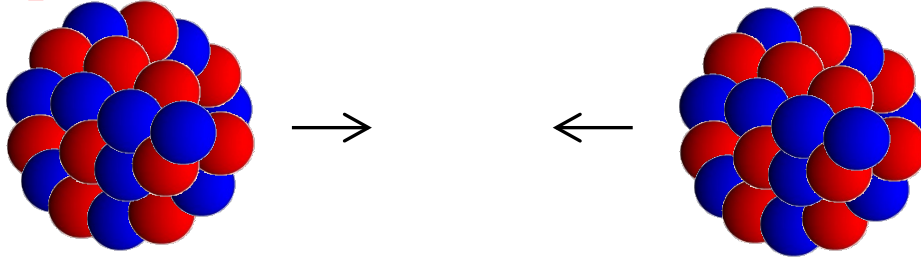
D.J. Hinde et al.,
 PRL 74 ('95) 1295



K. Hagino, PRC 98 ('18) 014607

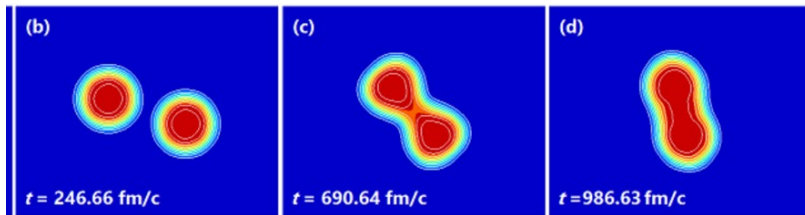
Towards a microscopic nuclear reaction theory

many-body problems



still very challenging

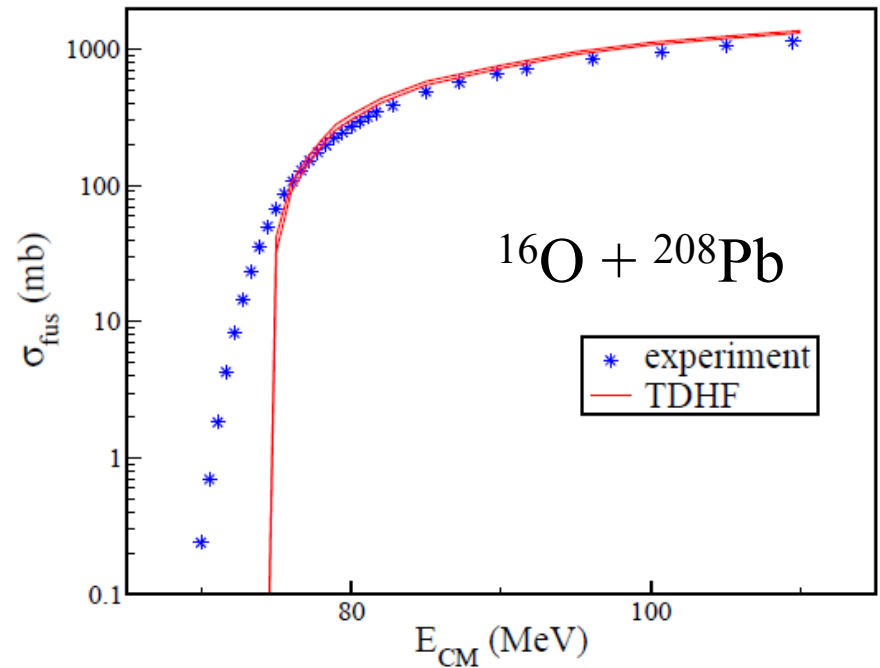
Time-dependent mean-field theory (TDHF/TDDFT)



S. Ebata, T. Nakatsukasa,
JPC Conf. Proc. 6 ('15) 020056

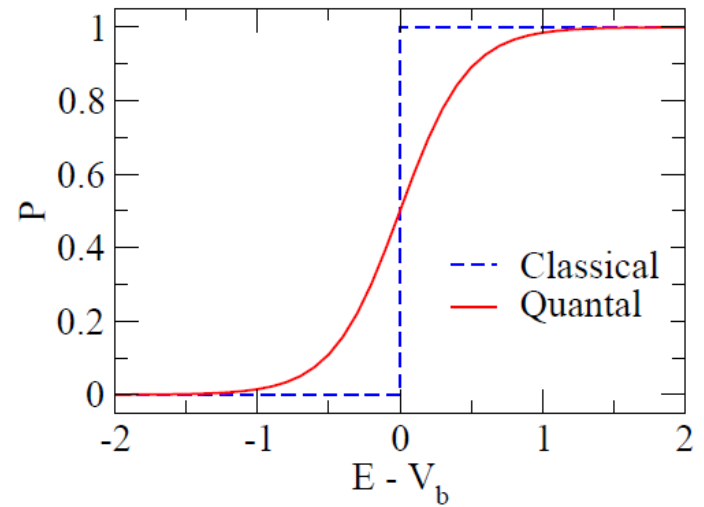
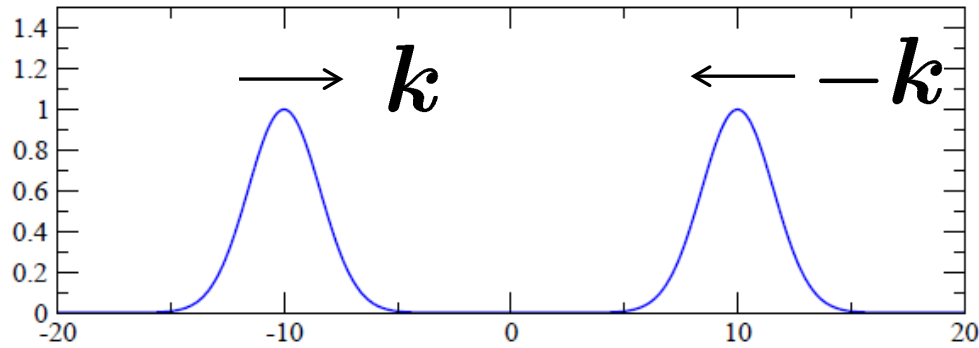
(semi) classical \rightarrow no tunneling

a microscopic understanding of
many-body tunneling?



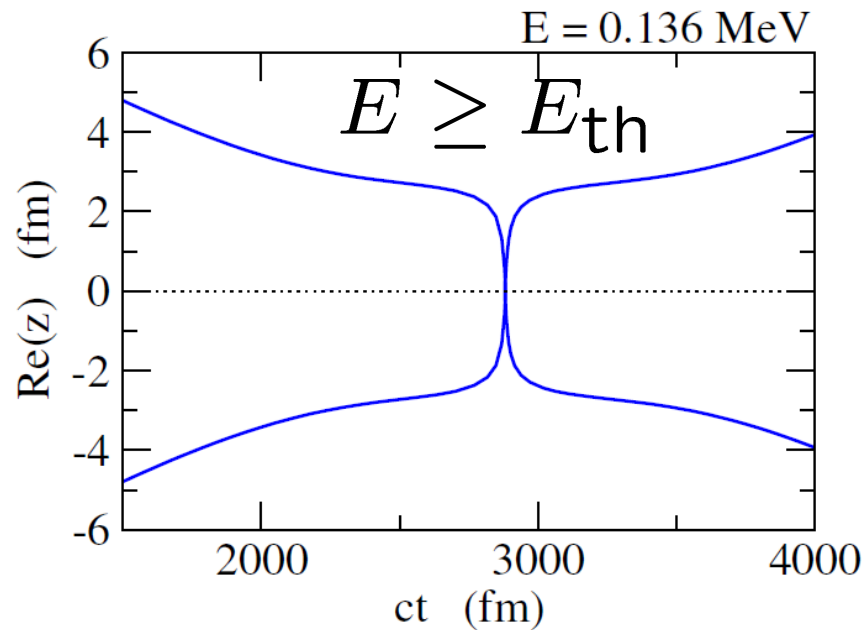
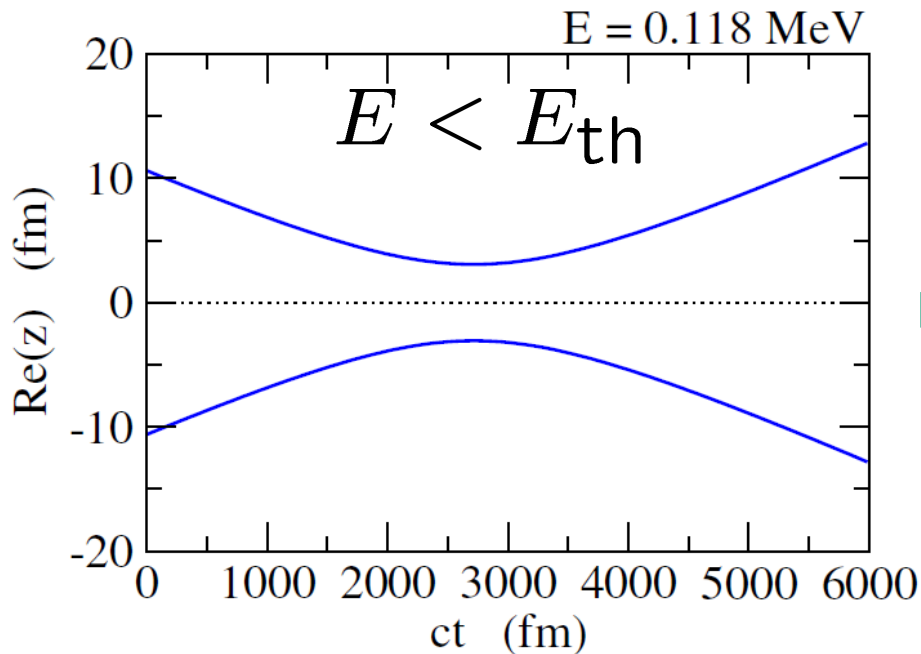
TDHF

$$\Psi(t) = \Phi_{SD}(t)$$

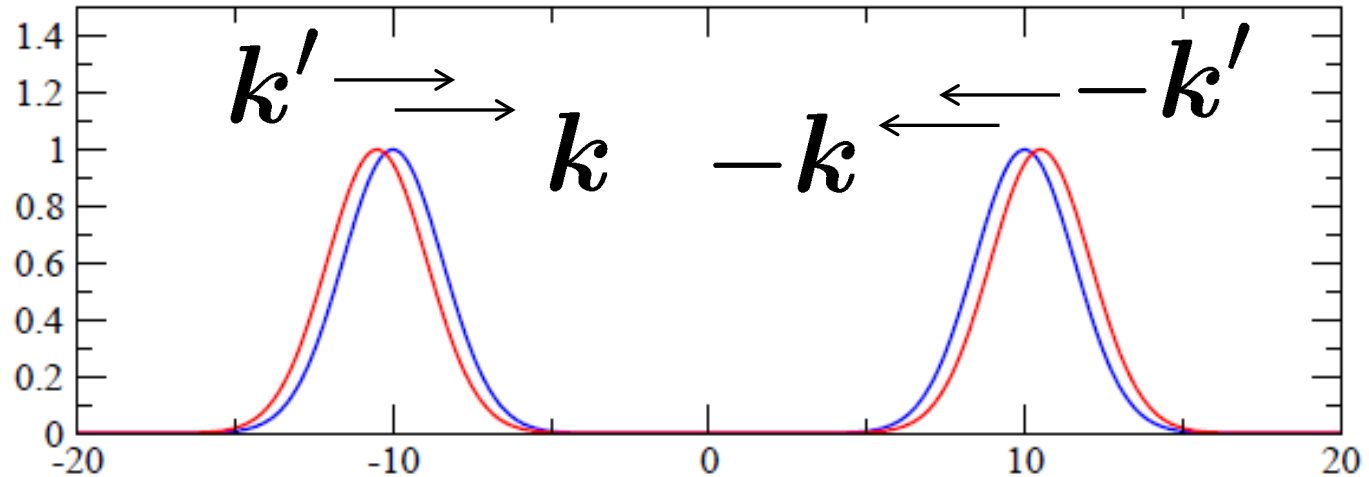


a single Slater determinat for a many-body wave function

$\alpha + \alpha$ in 1D



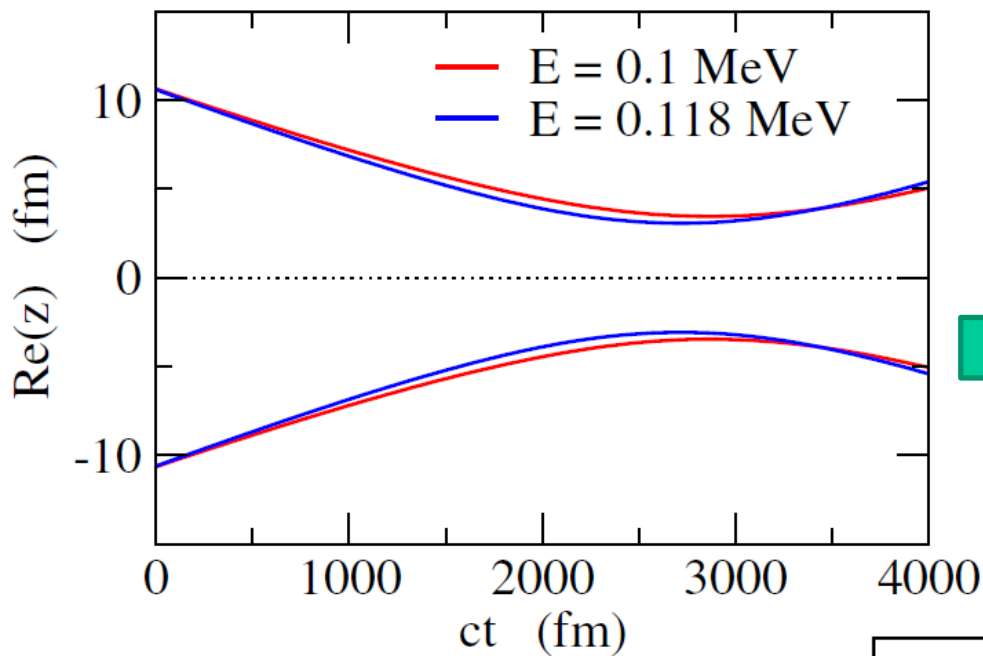
a linear superposition of many Slater determinants



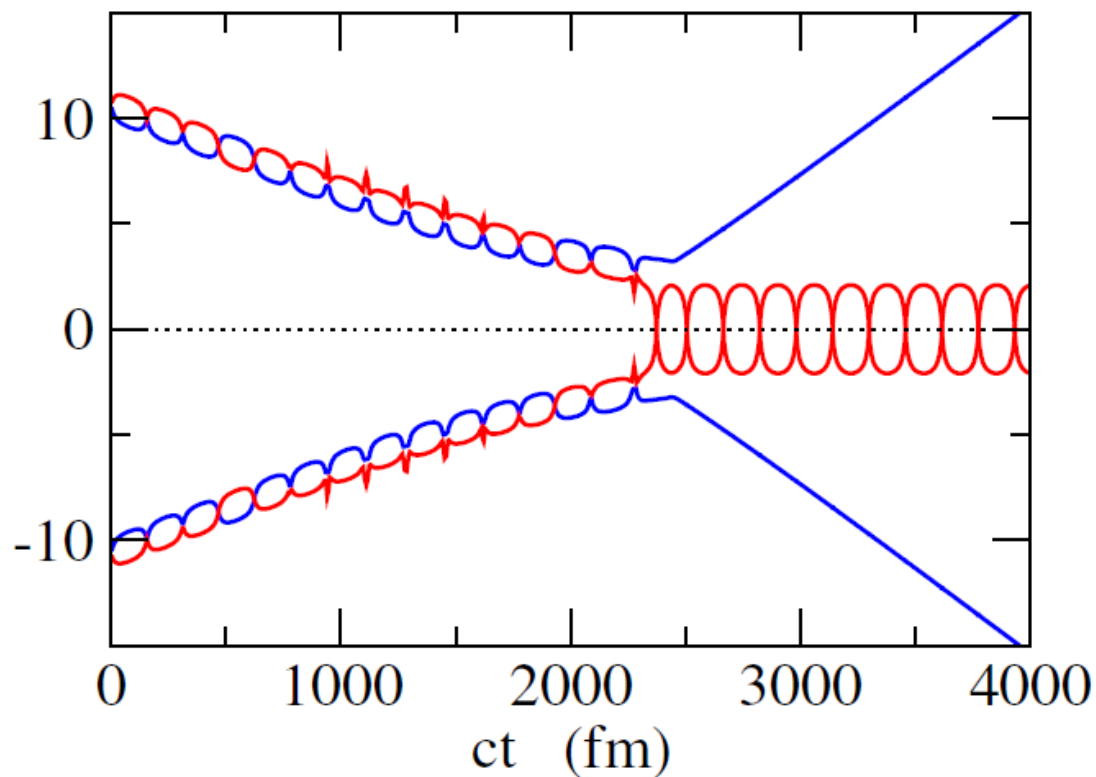
$$\Psi(t) = \sum_k \underbrace{f_k(t)}_{\text{time-dependent}} \underbrace{\Phi_{\text{SD},k}(t)}_{\text{variational principle}}$$

time-dependent variational principle

$$\delta \int dt \frac{\langle \Psi(t) | i\hbar \partial_t - H | \Psi(t) \rangle}{\langle \Psi(t) | \Psi(t) \rangle} = 0$$

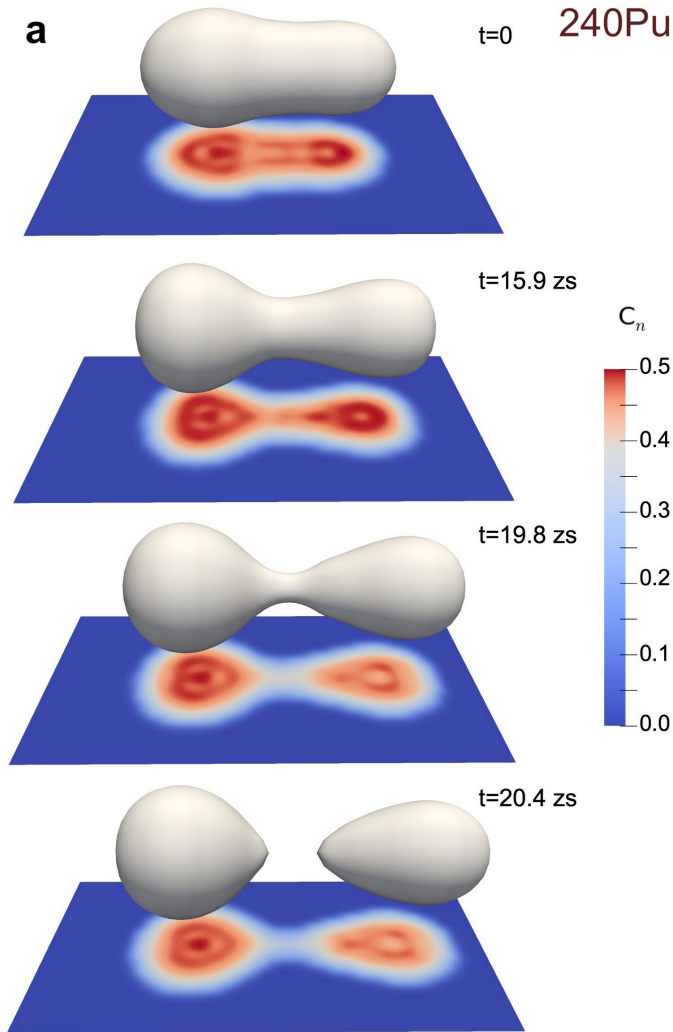


TDGCM
 (a superposition of 2 SD)



N. Hasegawa, K.H.,
 and Y. Tanimura,
 PLB808, 135693 (2020)

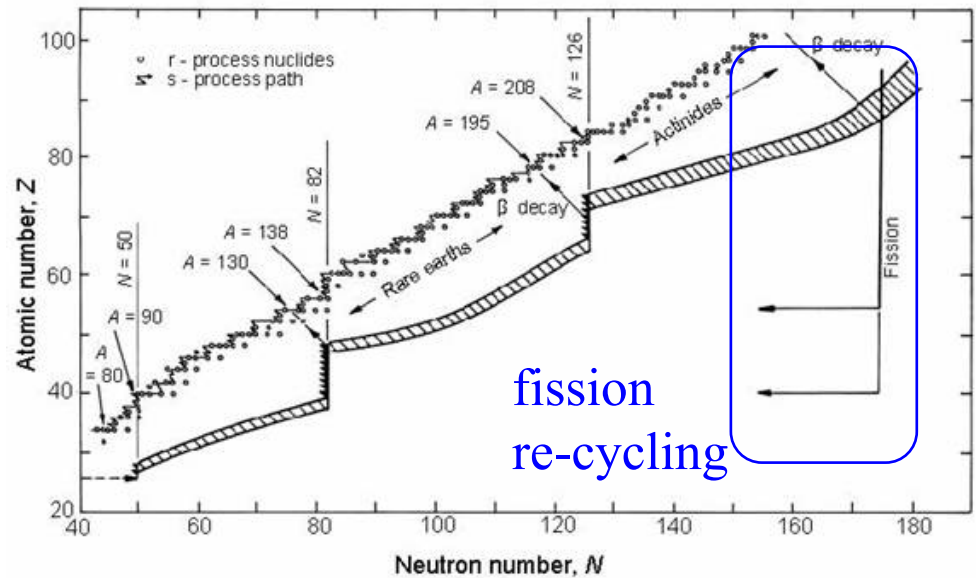
Nuclear Fission



G. Scamps and C. Simenel,
Nature 564 (2018) 382

➤ important role in:

- energy production
- superheavy elements
- r-process nucleosynthesis
- production of neutron-rich nuclei



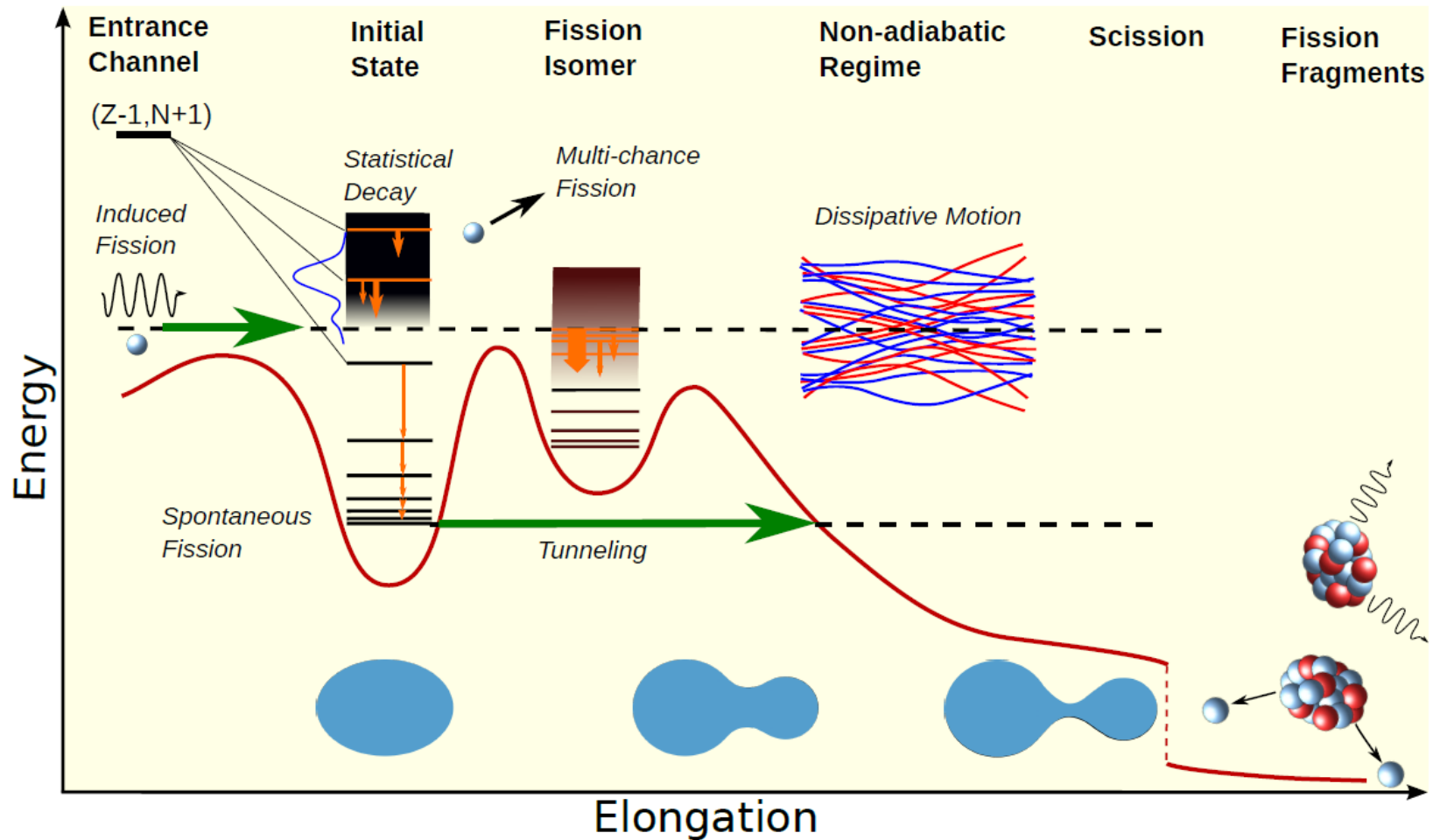
very complicated dynamics:

a microscopic understanding

→ far from complete

very complicated dynamics:

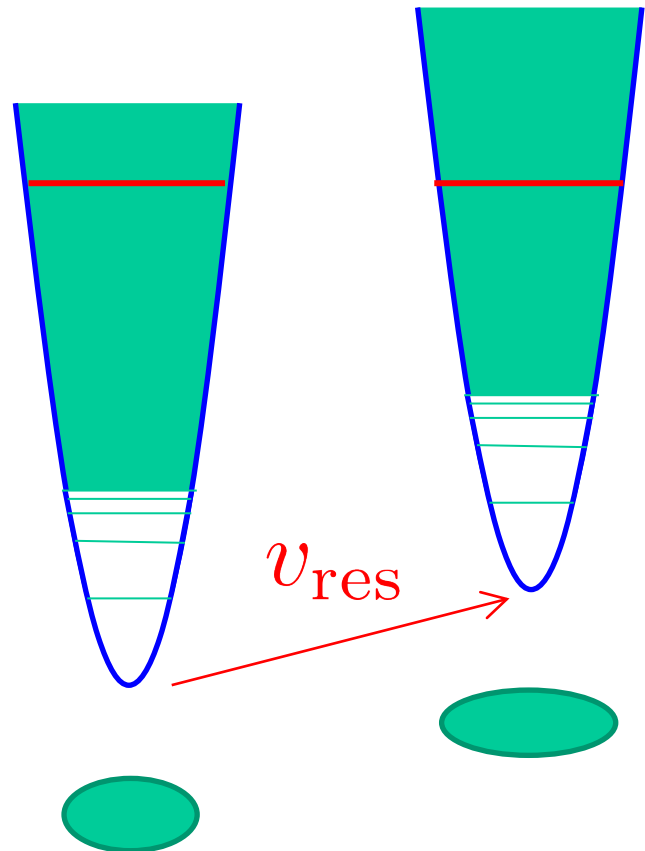
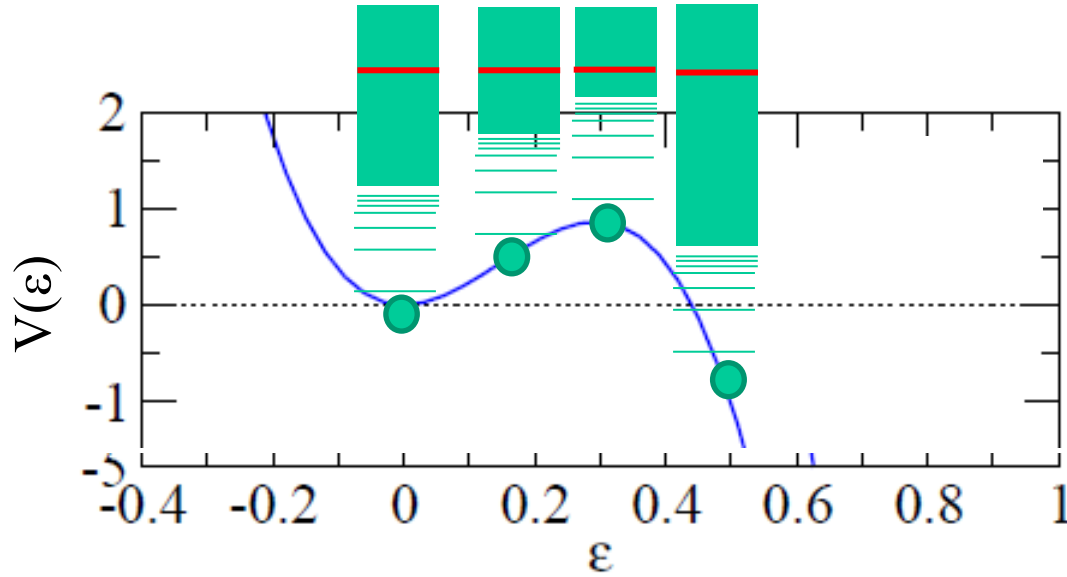
a microscopic understanding \rightarrow far from complete



M. Bender et al., J. of Phys. G47, 113002 (2020)

CI approach: a novel way to understand fission

K.H. and G.F. Bertsch



c.f. Generator Coordinate Method (GCM)

$$|\Psi\rangle = \int dQ f(Q) |\Phi_Q\rangle$$

→ CI approach

$$|\Psi\rangle = \int dQ \sum_i f_i(Q) |\Phi_Q(i)\rangle$$

hopping due to the residual interaction

→ shape evolution

Summary

Nuclear Reactions: a variety of many-body dynamics

Recent developments
in nuclear fusion reactions

National Nuclear Data Center

Towards microscopic understanding

- TDGCM
- CI approach
(nuclear fission)

Heavy and Superheavy
nuclei

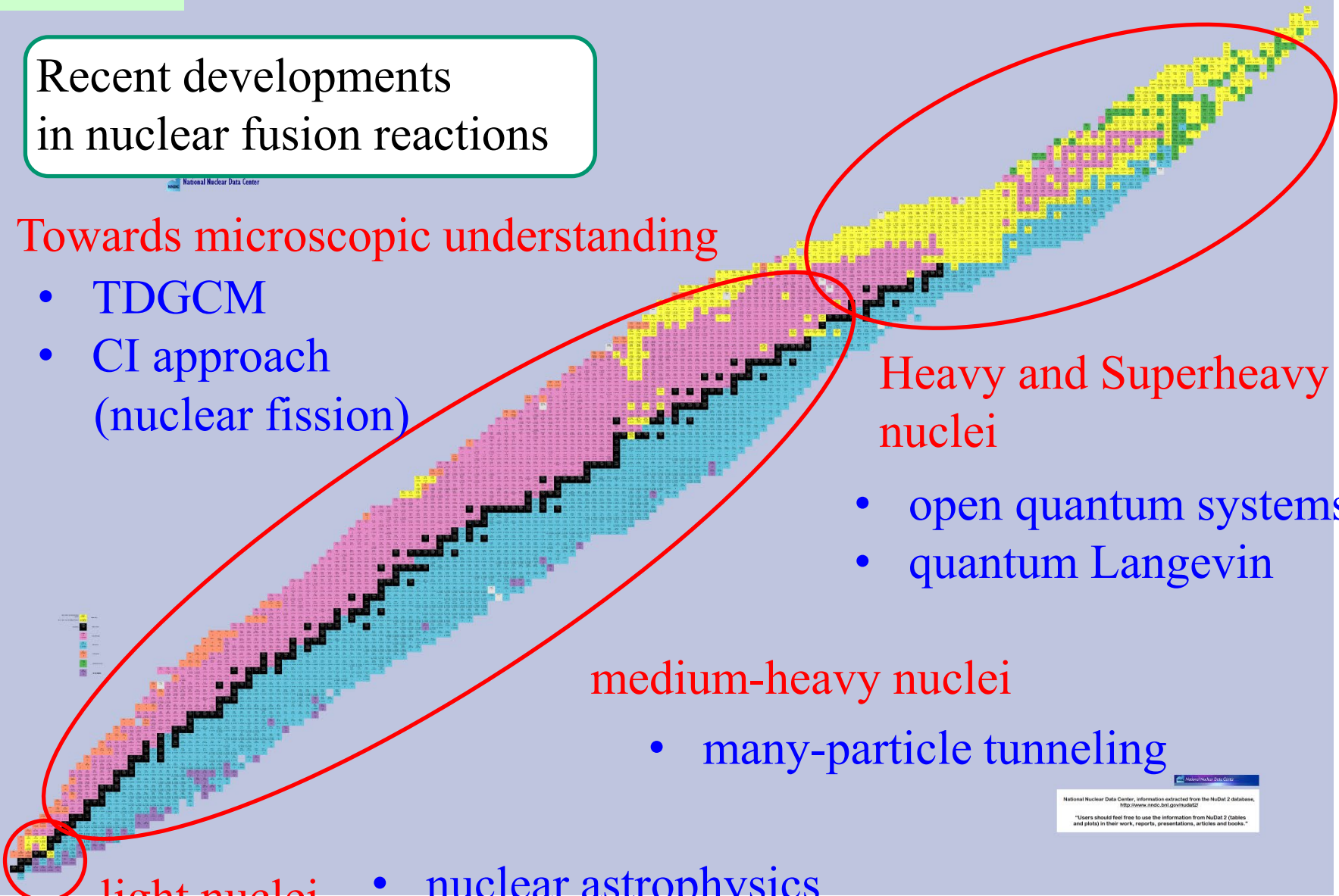
- open quantum systems
- quantum Langevin

medium-heavy nuclei

- many-particle tunneling

light nuclei

- nuclear astrophysics
- resonances



National Nuclear Data Center, information extracted from the NuDat 2 database,
<http://www.nndc.gov/nudat2/>
"Users should feel free to use the information from NuDat 2 (tables
and plots) in their work, reports, presentations, articles and books."

Summary

From phenomenological to microscopic nuclear reaction theories

Macroscopic (phenomenological)

C.C. with collective model

C.C. with beyond MF

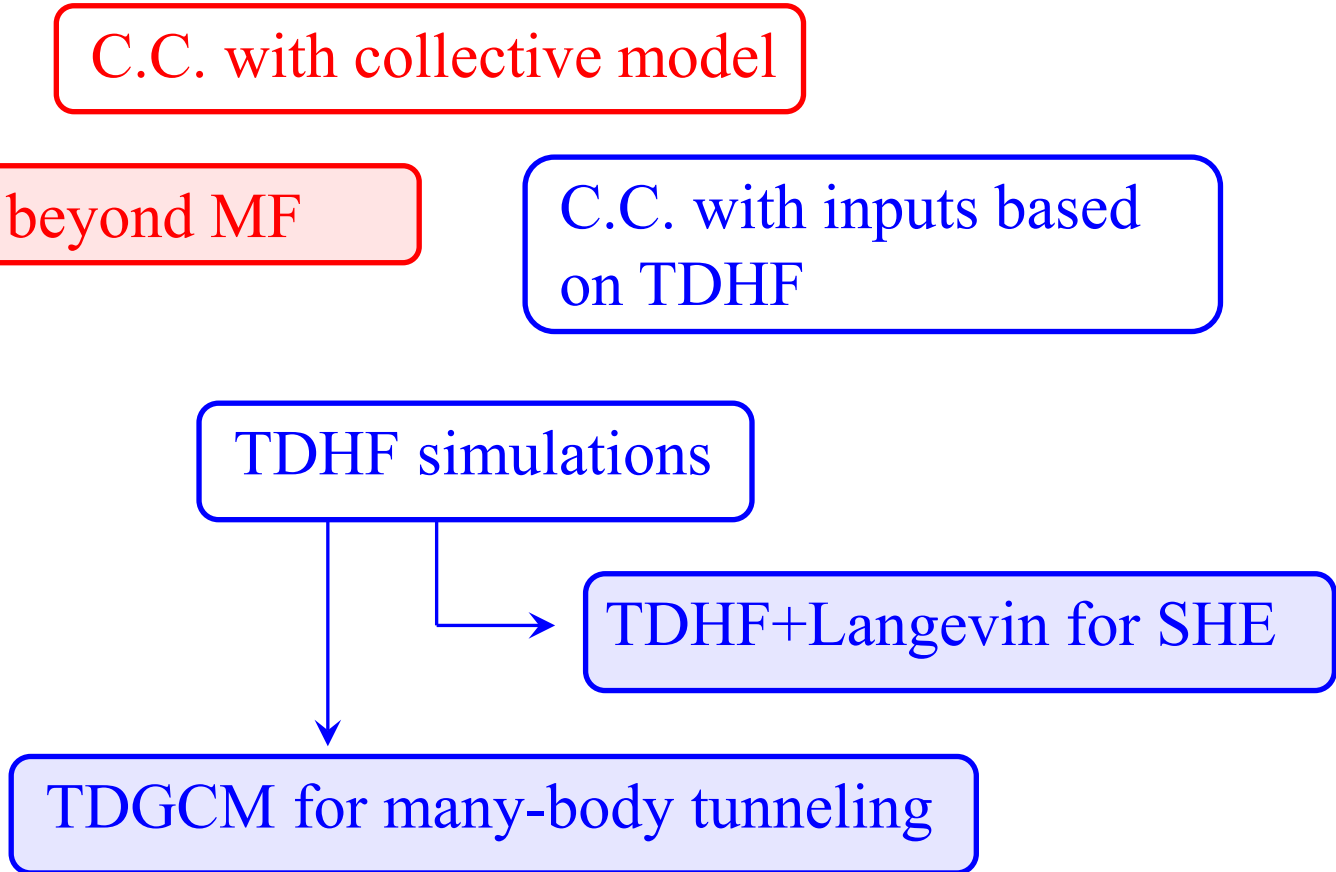
C.C. with inputs based on TDHF

TDHF simulations

TDHF+Langevin for SHE

TDGCM for many-body tunneling

Microscopic



A folding potential does not work for subbarrier fusion reactions

