

# Shape evolution of atomic nucleus and clustering

Kouichi Hagino  
Kyoto University



G.F. Bertsch (Seattle)  
Kotaro Uzawa (Kyoto)

1. Introduction
2. CI model for cluster decays
3. Extension to induced fission
4. Summary

# Introduction: particle emission decays of unstable nuclei

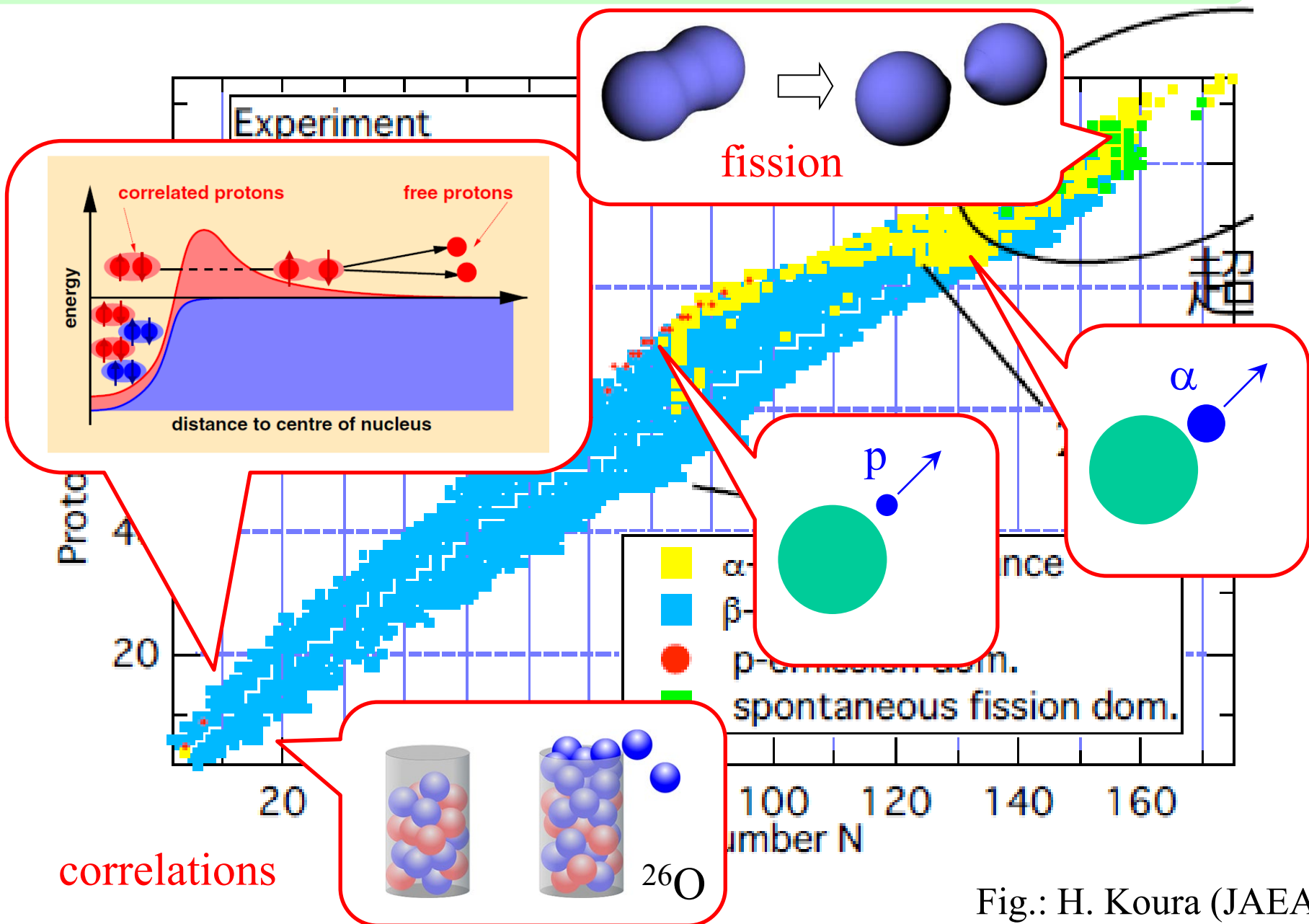
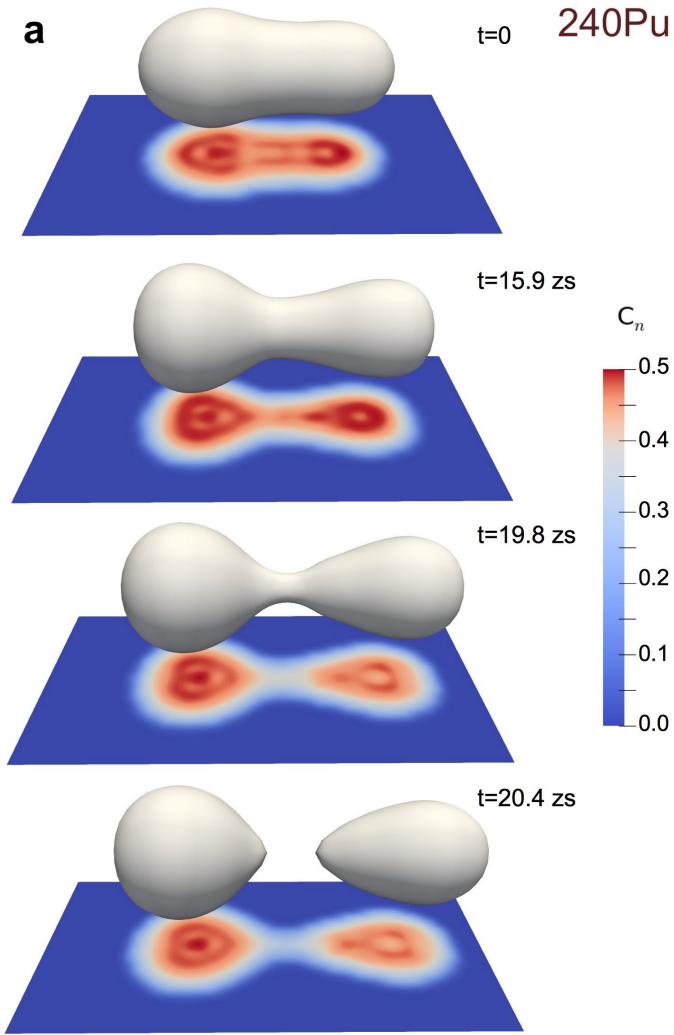


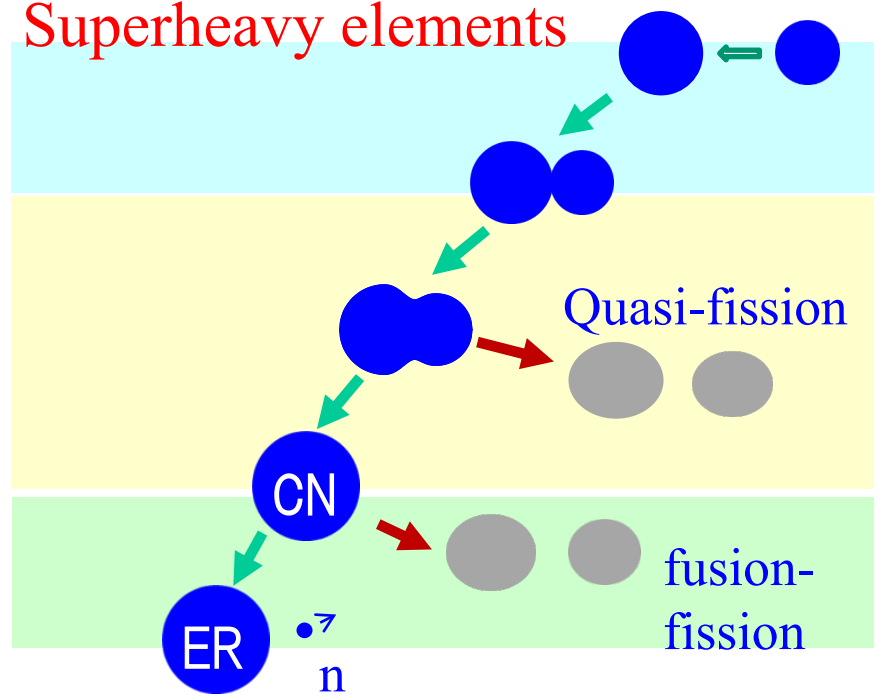
Fig.: H. Koura (JAEA)

# Importance of fission

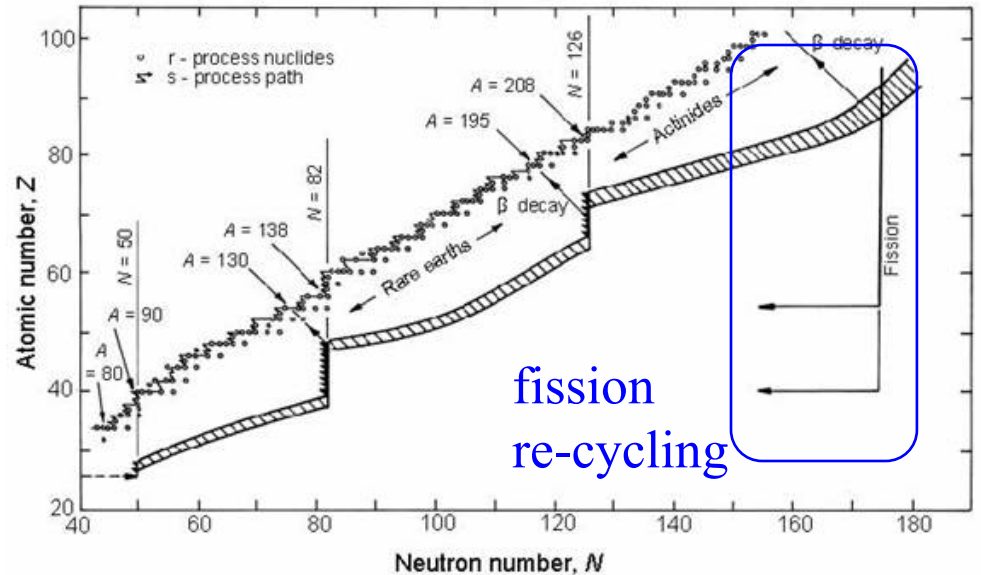


G. Scamps and C. Simenel,  
Nature 564 (2018) 382

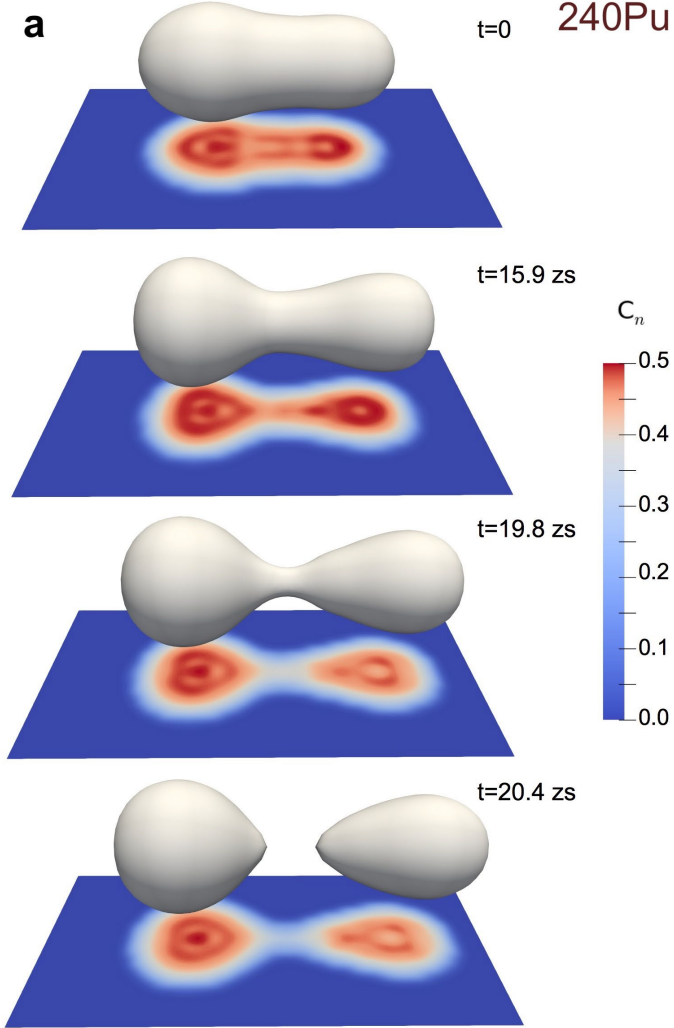
# Superheavy elements



# r-process nucleosynthesis



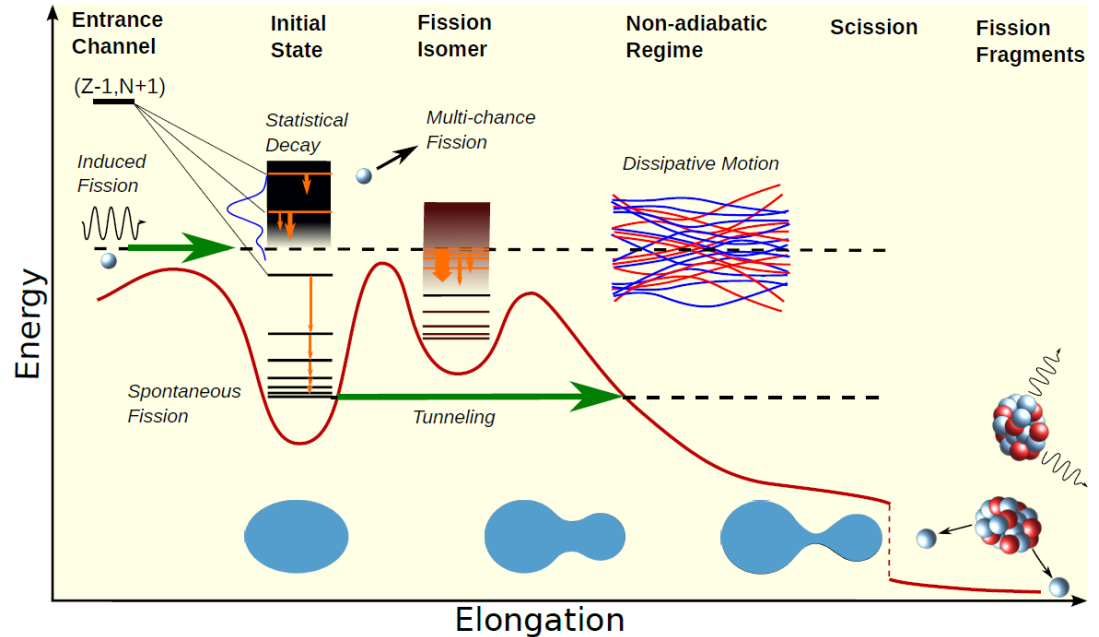
# microscopic understanding of fission



G. Scamps and C. Simenel,  
Nature 564 (2018) 382

large change of nuclear shape  
→ microscopic description  
: far from complete

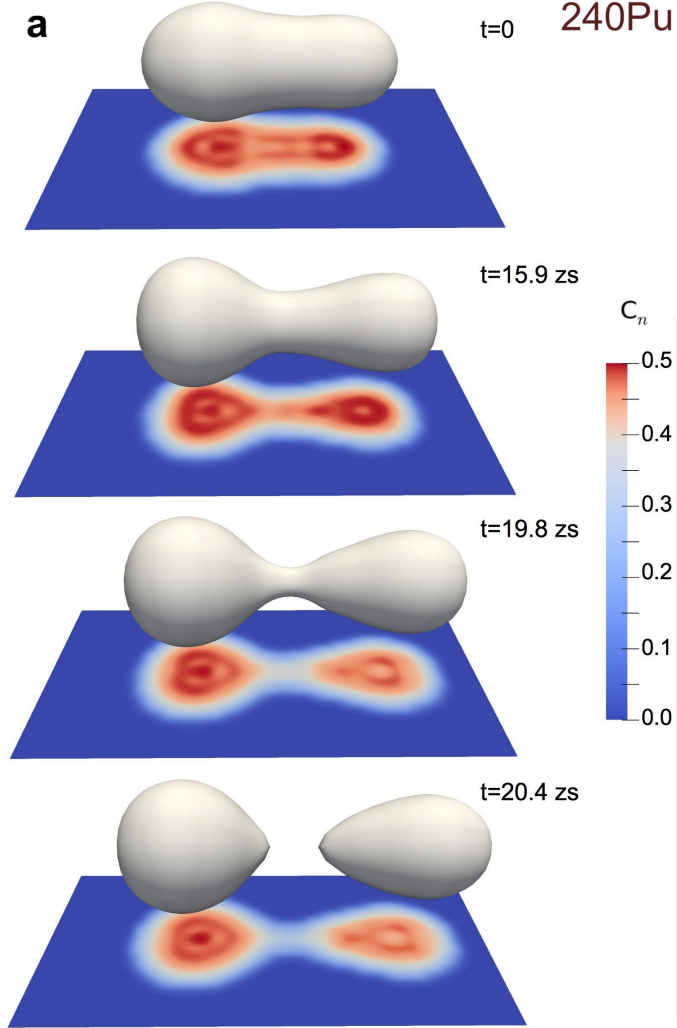
an ultimate goal of nuclear physics



M. Bender et al.,  
J. of Phys. G47, 113002 (2020)

“Future of fission theory” White paper

# microscopic understanding of fission



large change of nuclear shape

→ microscopic description

: far from complete

**the aim of this work:**

to construct a microscopic fission theory  
based on a many-body Hamiltonian

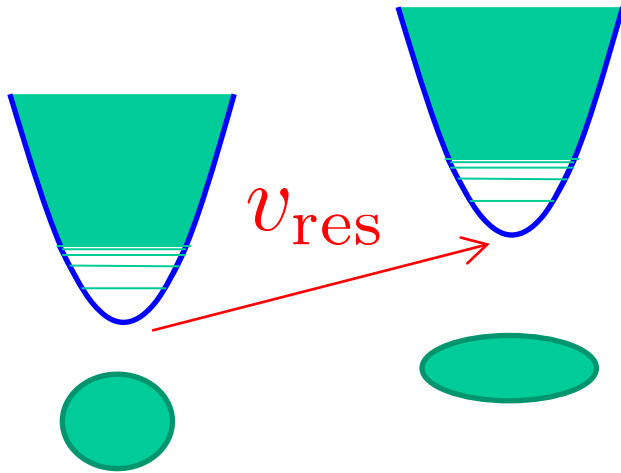
**the method:**

configurations based on DFT

→ shell model

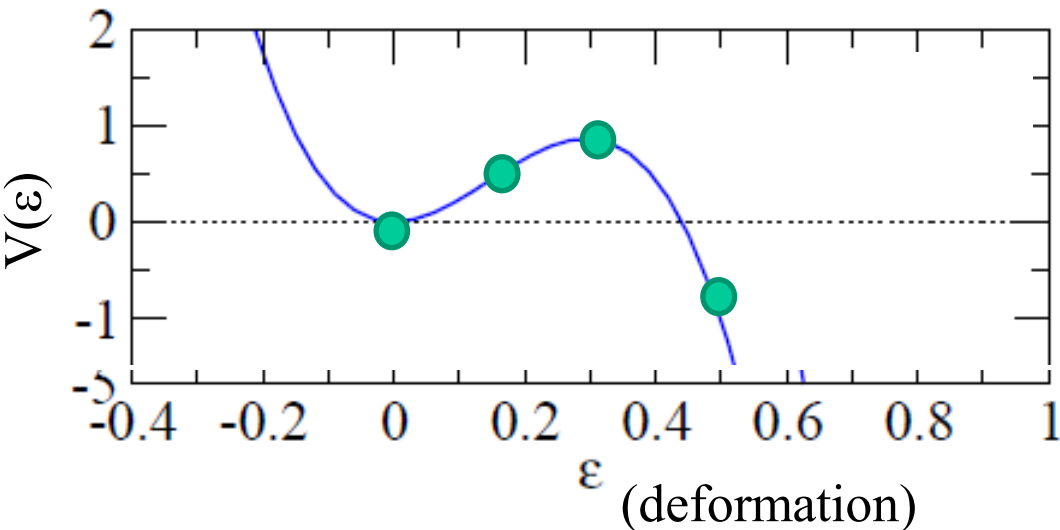
G. Scamps and C. Simenel,  
Nature 564 (2018) 382

# Generator Coordinate Method + CI approach

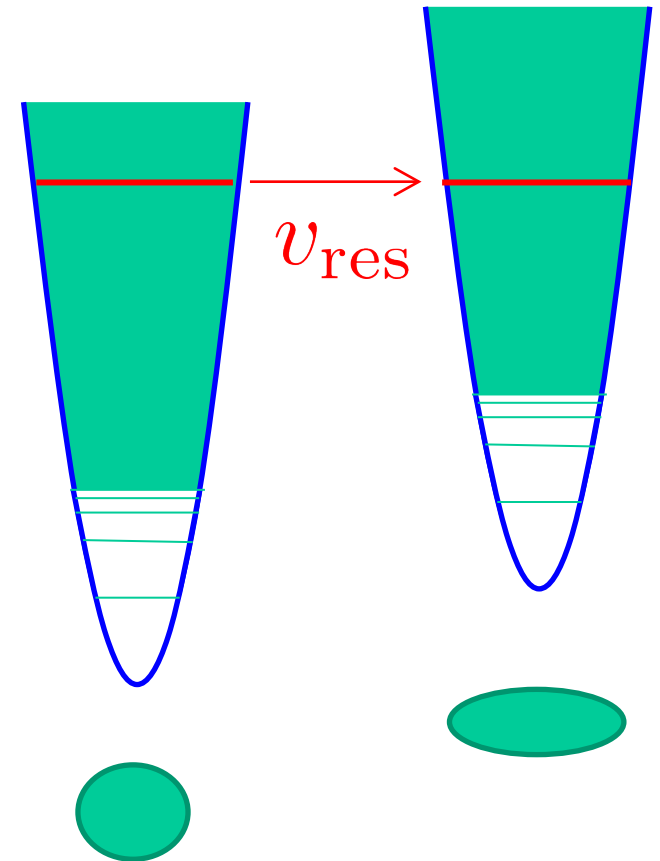


hopping due to residual interactions

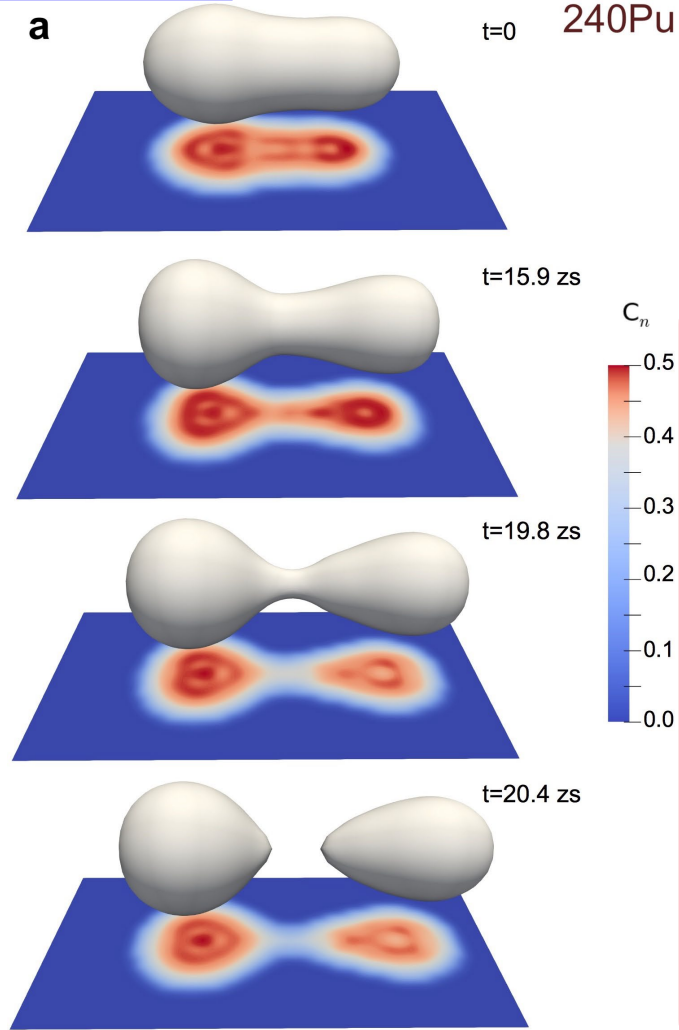
→ shape evolution



in the case of induced fission



# microscopic understanding of fission



large change of nuclear shape

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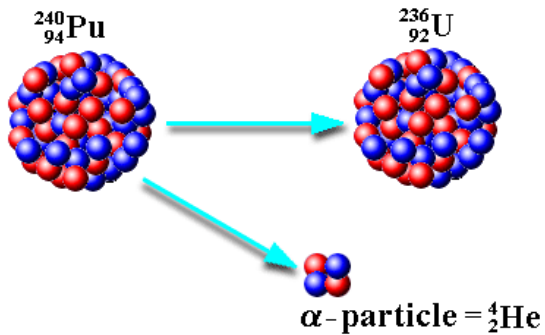
**objects:**

- cluster decays from the ground state
- induced fission of  $^{236}\text{U}$
- (spontaneous fission of heavy nuclei)

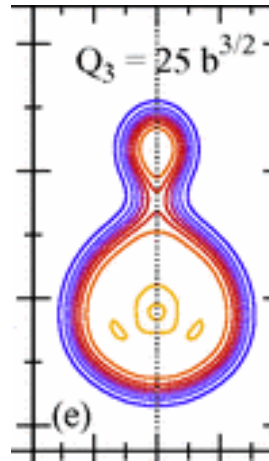
G. Scamps and C. Simenel,  
Nature 564 (2018) 382

# Cluster Radioactivities

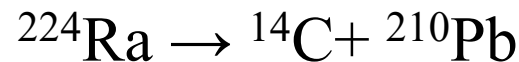
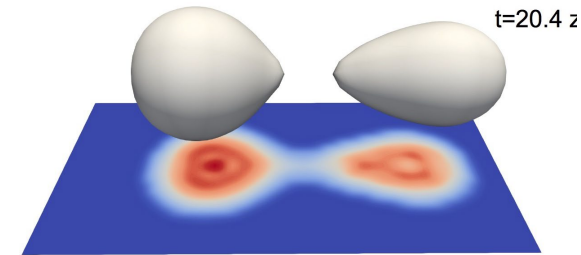
$\alpha$  decays



cluster decays

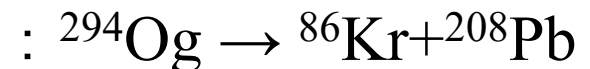


fission



M. Warda and L.M. Robledo,  
PRC84, 044608 (2011)

- ✓ intermediate between  $\alpha$ -decay and fission (very asymmetric fission)
- ✓ first observation in 1984 by Rose and Jones ( $^{223}\text{Ra} \rightarrow ^{14}\text{C} + ^{209}\text{Pb}$ )
- ✓ very small branching to  $\alpha$  decays (“rare decay”)  $^{224}\text{Ra}$ :  $4.3 \times 10^{-11}$
- ✓ may become a dominant decay mode in superheavy nuclei



Z. Mateson, Giuliani, Nazarewicz, Sadhukhan, Schunck, PRC99(‘19) 041304(R)



# GCM+CI approach to cluster decays

K. Uzawa, K. Hagino, and K. Yoshida, PRC105 (2022) 034326

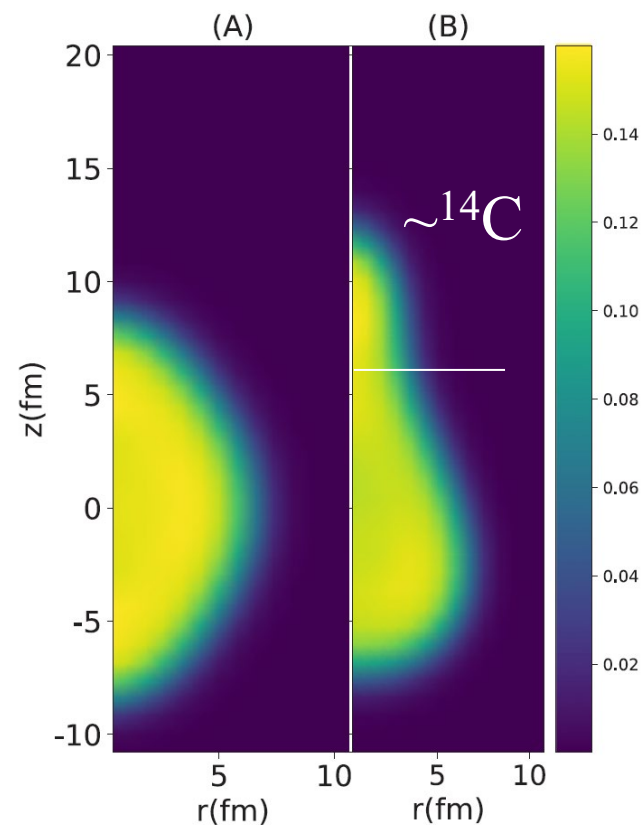
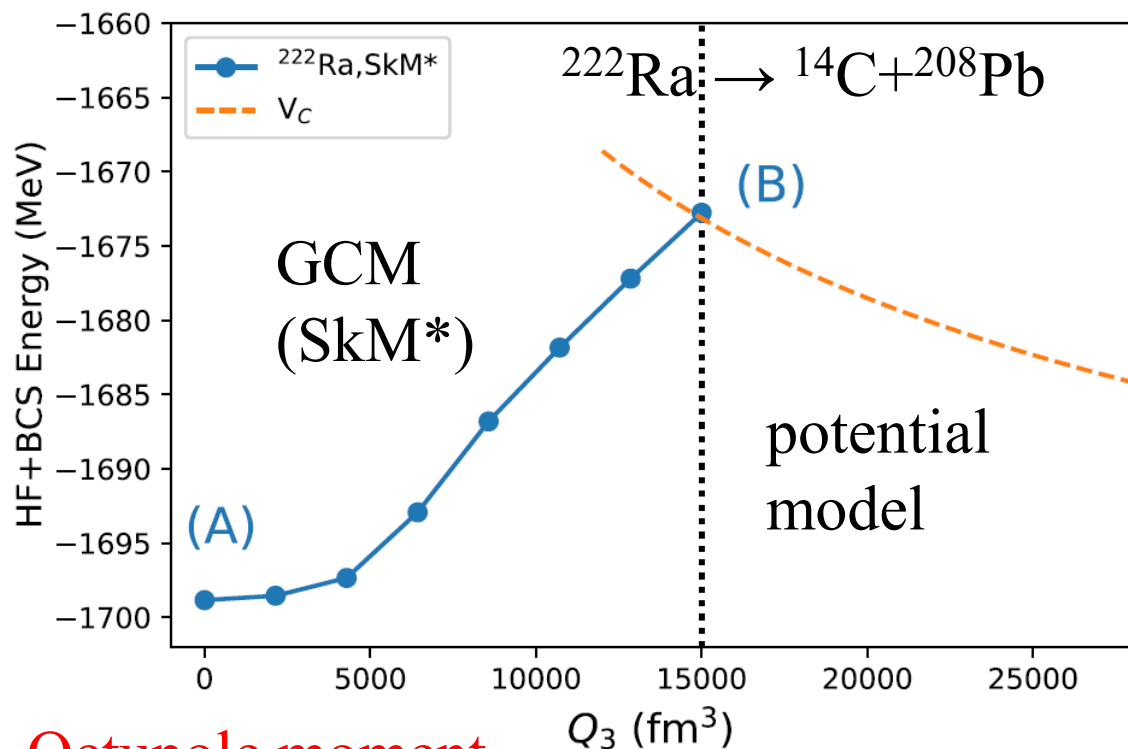
Gamow theory:  $w = S f P_{\text{tunnel}}$

$S$ : Cluster formation prob. → GCM with  $Q_3$

$f$ : attempt frequency

$P$ : tunnel prob.

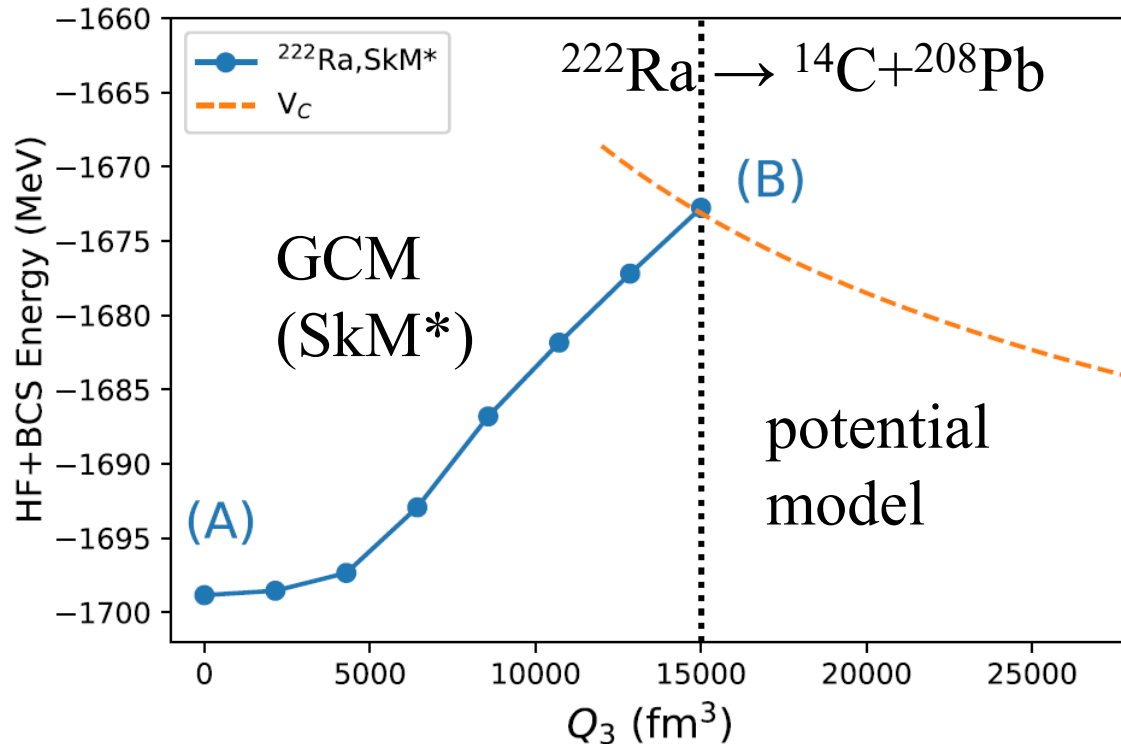
→ two-body potential model



# GCM+CI approach to cluster decays

K. Uzawa, K. Hagino, and K. Yoshida, PRC105 (2022) 034326

Gamow theory:  $w = S f P_{\text{tunnel}}$



$$\Psi = \int dQ_3 f(Q_3) |\Psi_{Q_3}\rangle$$

↑  
GCM

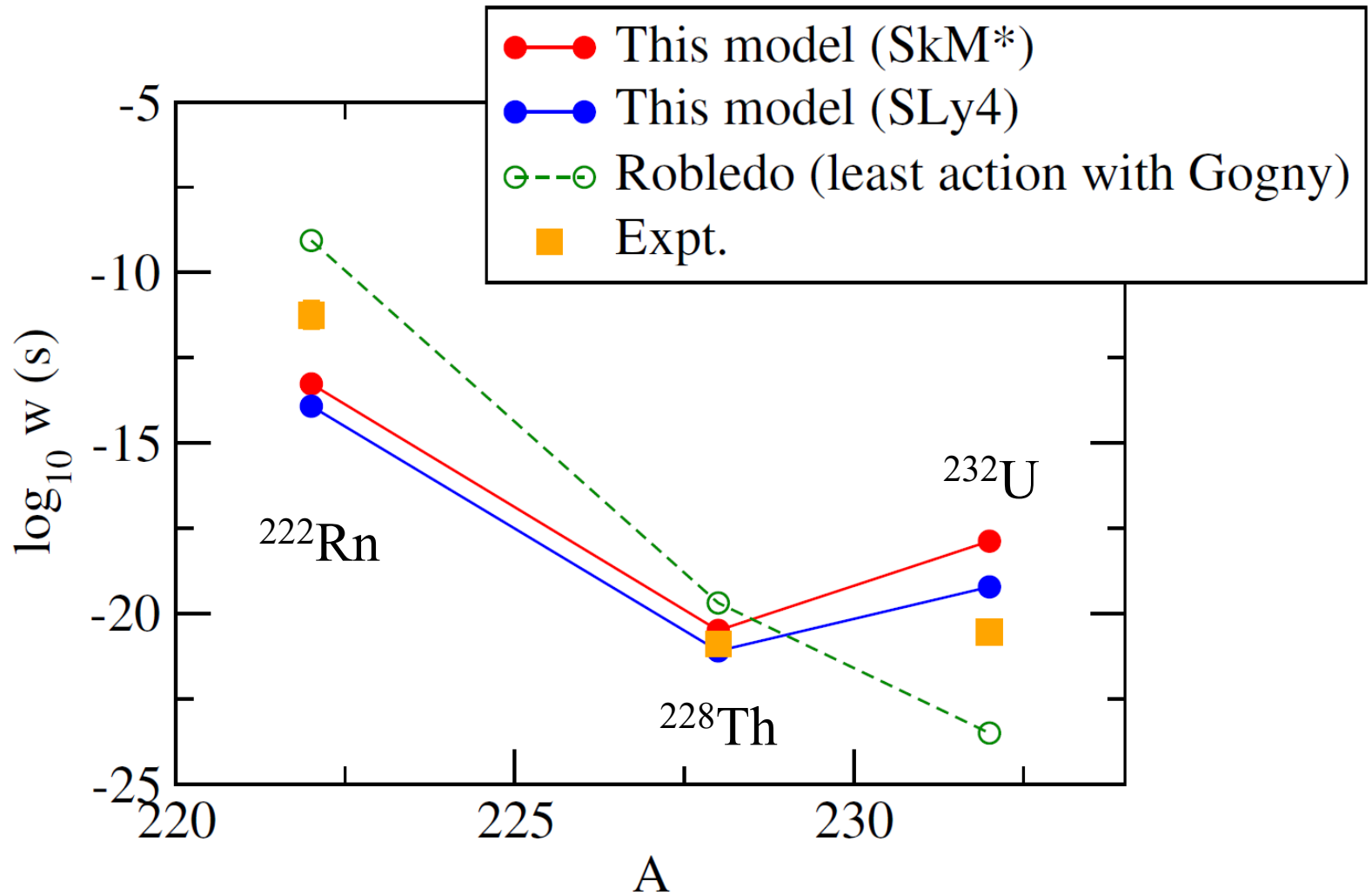
$$S \sim |\sqrt{N} f(Q_{3B})|^2$$

excited configurations at each  $Q_3 \leftarrow$  shell model aspect

$$|\Psi\rangle = \int dQ_3 \sum_i f_i(Q_3) |\Phi_{Q_3}(i)\rangle$$

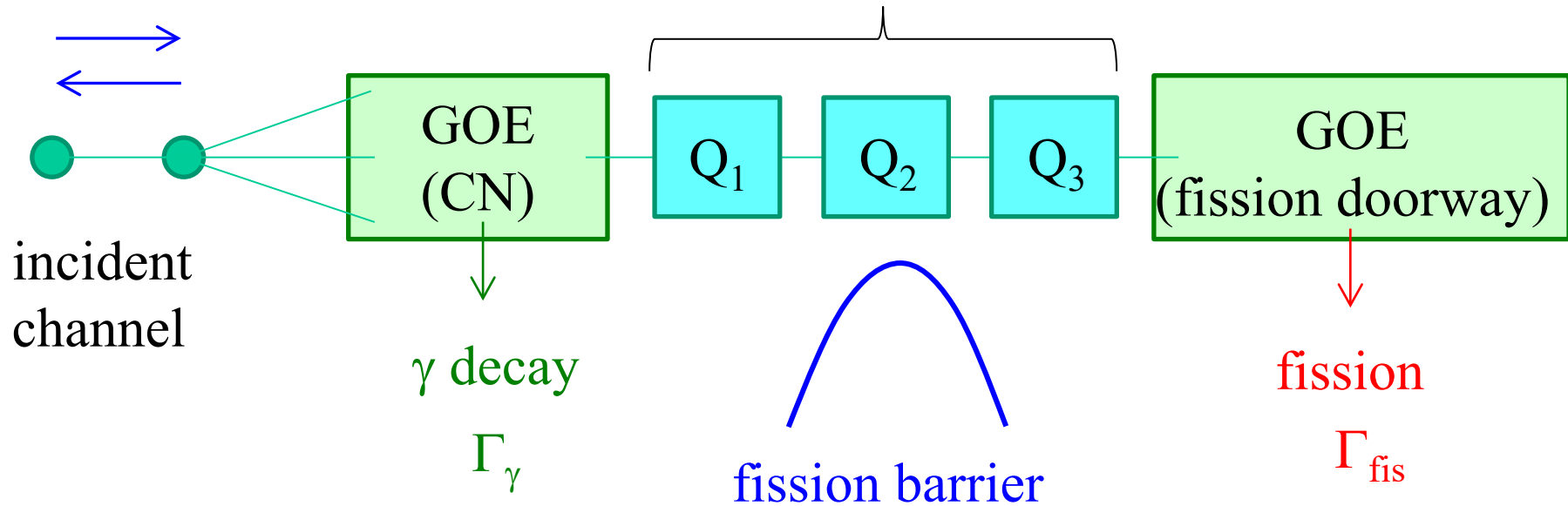
## GCM+CI approach to cluster decays

K. Uzawa, K. Hagino, and K. Yoshida, PRC105 (2022) 034326



# Induced Fission

a set of many-particle many-hole config.  
generated with Skyrme DFT



reaction theory:

$$T_{\text{fis}} = \text{Tr}[\Gamma_{\text{in}} G(E) \Gamma_{\text{fis}} G^\dagger(E)]$$

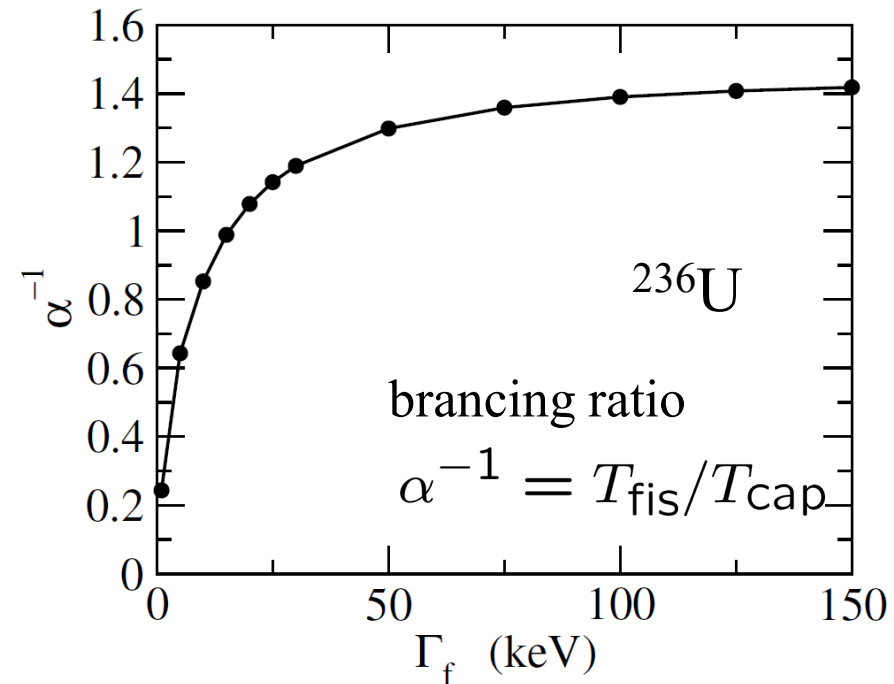
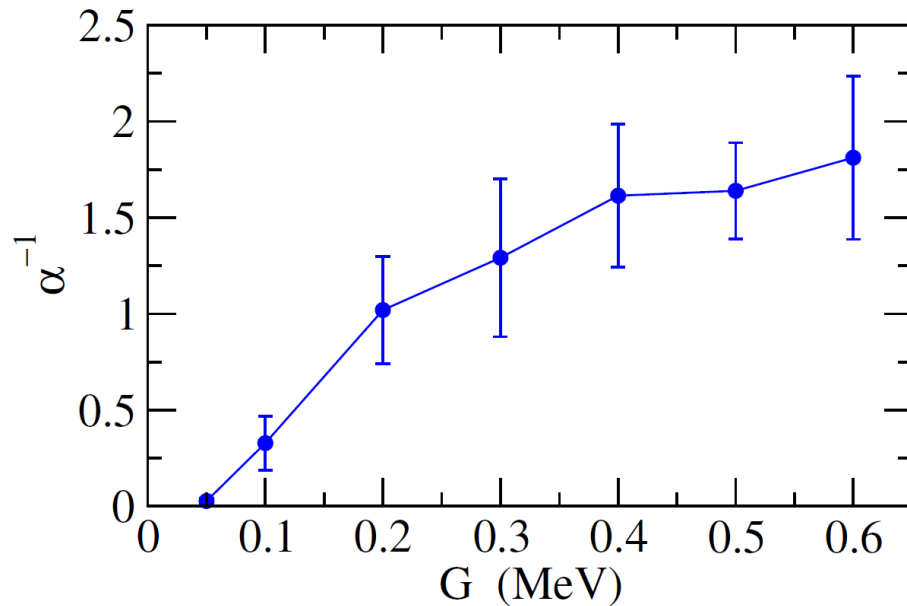
$$G(E) = [H - i\Gamma/2 - EO]^{-1}$$

decay branching ratio:  $\alpha^{-1} = T_{\text{fis}}/T_{\text{cap}}$

# Induced Fission

G.F. Bertsch and K. Hagino, arXiv: 2302.00572 (2023).

K. Uzawa, K. Hagino, and G.F. Bertsch, in preparation (2023).

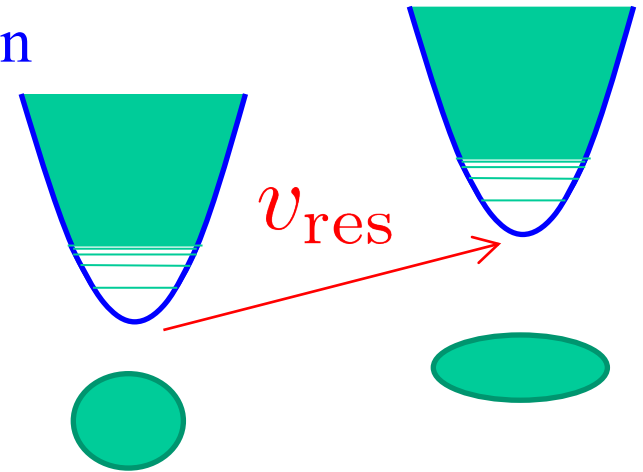


- ✓ pairing: enhances  $T_{\text{fis}}$  at energies around the barrier
- ✓  $T_{\text{fis}}$ : insensitive to the dynamics after the barrier  
→ transition state theory (TST)

## Summary

### CI approach to nuclear fission

$$|\Psi\rangle = \int dQ \sum_i f_i(Q) |\Phi_Q(i)\rangle$$



- ✓ a microscopic theory based on a many-body Hamiltonian
- ✓ applied to cluster decays and induced fission
- ✓ so far, one degree of freedom
  - a challenge: extension to many degrees of freedom
    - how clusters are emerged inside a nucleus
    - competition between alpha decays and cluster decays
- ✓ another challenge: realistic calculations for induced fission
  - the inversion of a Hamiltonian with a large dimension