

MCD2022 – 5th week
Yukawa Institute
June 7 (6-10), 2022

Structure evolutions towards neutron driplines

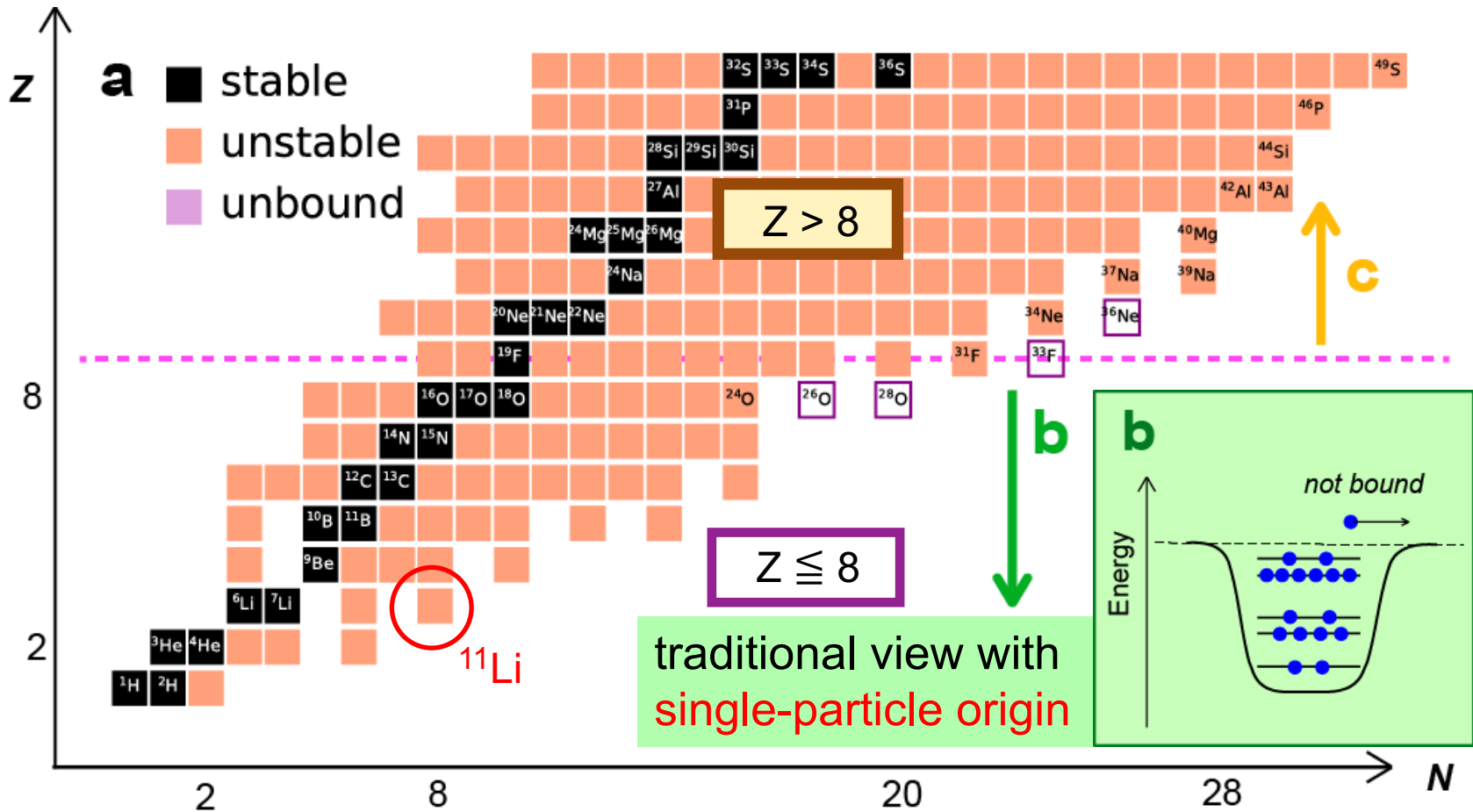
Takaharu Otsuka

N. Tsunoda, T. Takayanagi, N. Shimizu, T. Suzuki, Y. Utsuno, H. Ueno
U. Tokyo, CNS, Sophia U., JAEA, RIKEN, Nihon U.



This work was supported also by MEXT as “Program for Promoting Researches on the Supercomputer Fugaku” (Simulation for basic science: from fundamental laws of particles to creation of nuclei) and “Priority Issue on post-K computer” (Elucidation of the Fundamental Laws and Evolution of the Universe), and by JICFuS.

Neutron driplines : traditional view (somewhat vague)



Neutron halo appears in some cases.

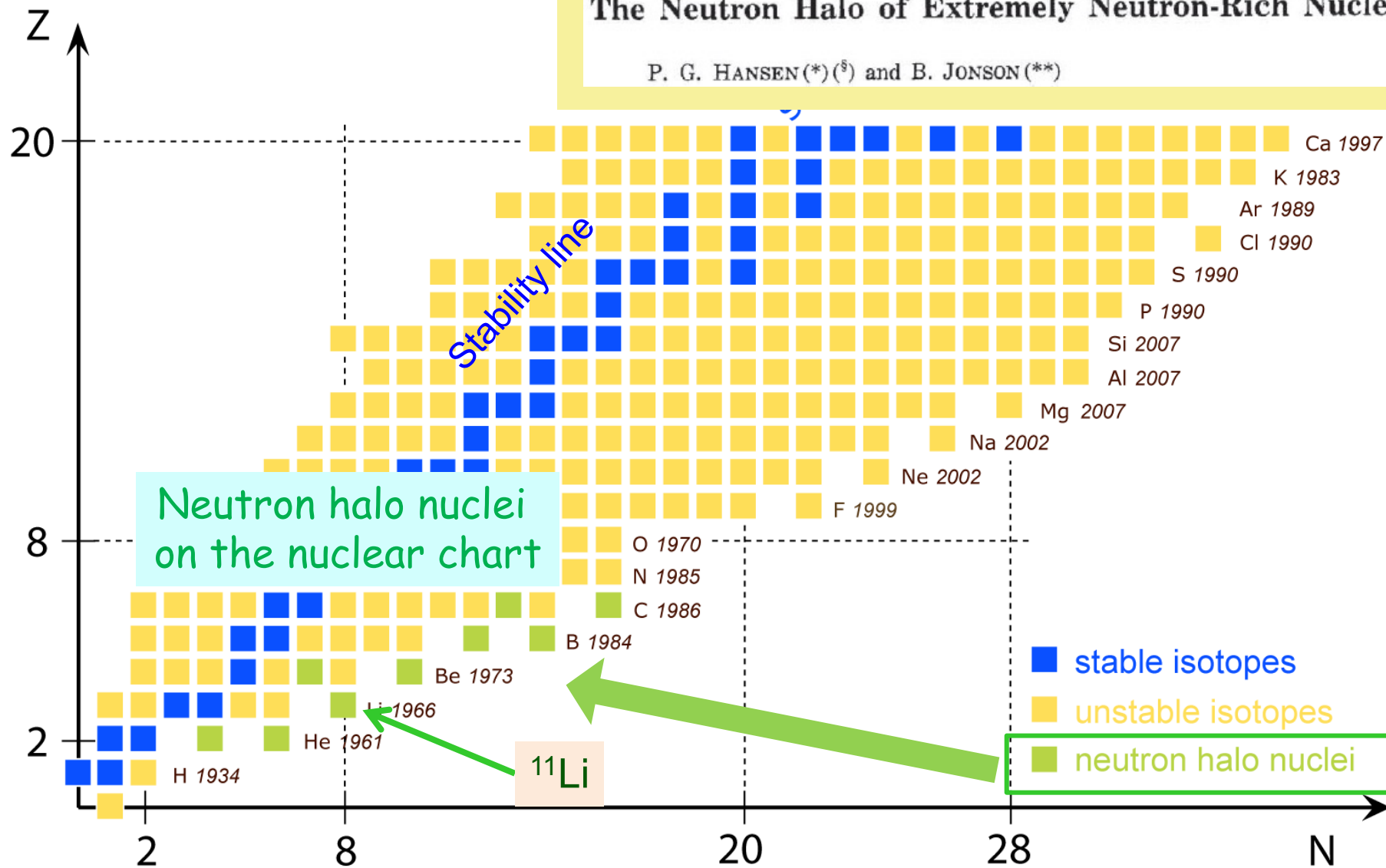
The large radius is due to neutron halo, a tunneling of loosely bound neutrons.

EUROPHYSICS LETTERS

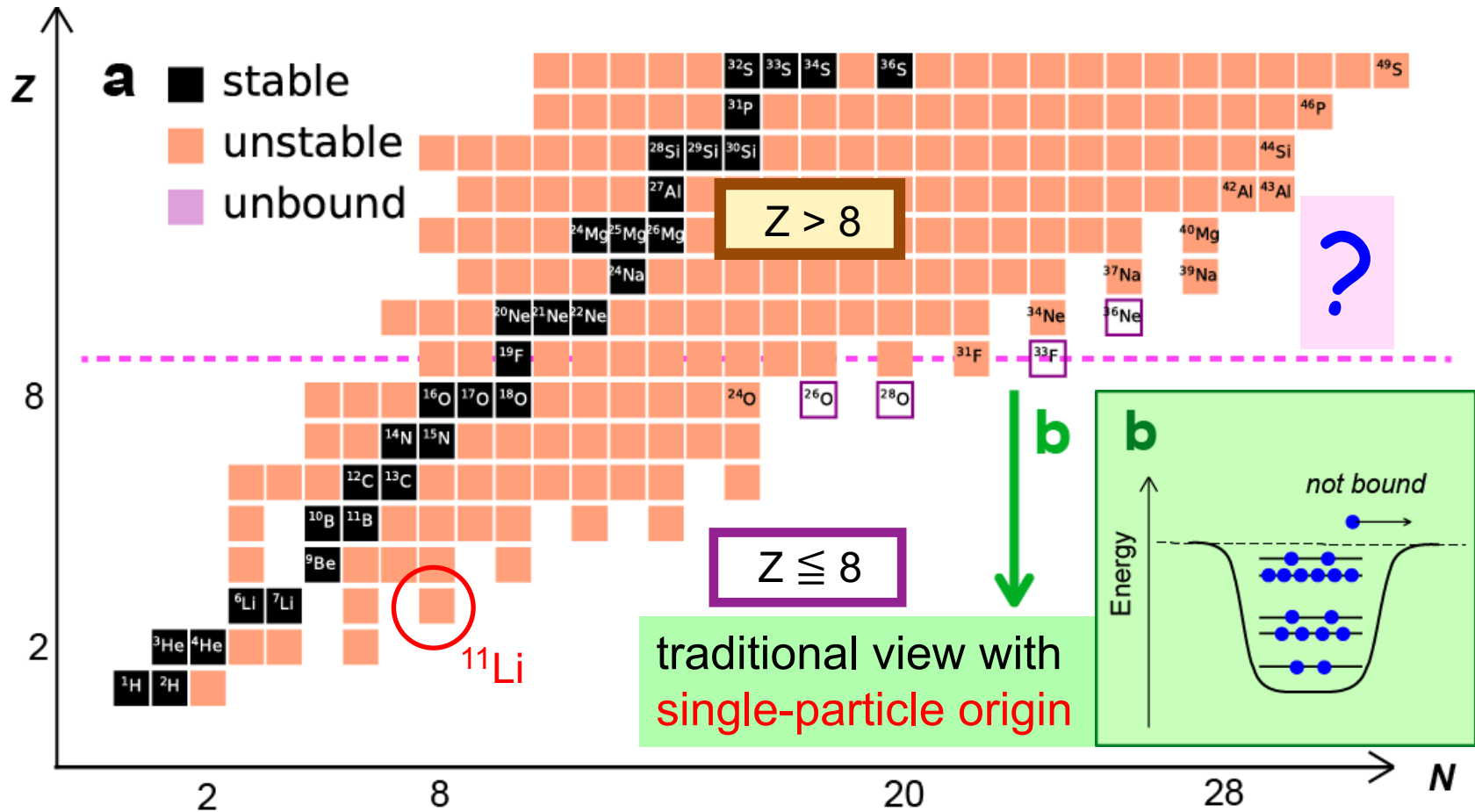
Europhys. Lett., 4 (4), pp. 409-414 (1987)

The Neutron Halo of Extremely Neutron-Rich Nuclei.

P. G. HANSEN(*)^(§) and B. JONSON(**)



Neutron driplines in heavier elements and the nuclear structure there




Neutron halo appears in some cases.

This talk is mainly based on

nature

Article | Published: 04 November 2020




The impact of nuclear shape on the emergence of the neutron dripline

Naofumi Tsunoda, Takaharu Otsuka , Kazuo Takayanagi, Noritaka Shimizu, Toshio Suzuki, Yutaka Utsuno, Sota Yoshida & Hideki Ueno

Nature **587**, 66–71(2020) | [Cite this article](#)

PHYSICAL REVIEW C **105**, 014319 (2022)

Moments and radii of exotic Na and Mg isotopes

Takaharu Otsuka , ^{1,2,3,*} Noritaka Shimizu , ⁴ and Yusuke Tsunoda  ⁴

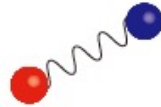
QCD



Lattice QCD

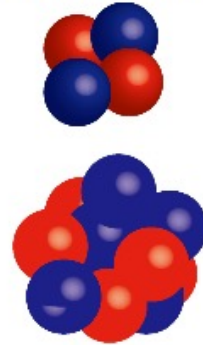
Effective Field Theory

Nuclear force

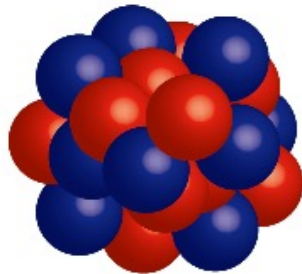


Few body techniques
No core shell model
and many others...

Light nuclei $\sim A \approx 10-20$



Medium mass nuclei $\sim A \approx 20-100$



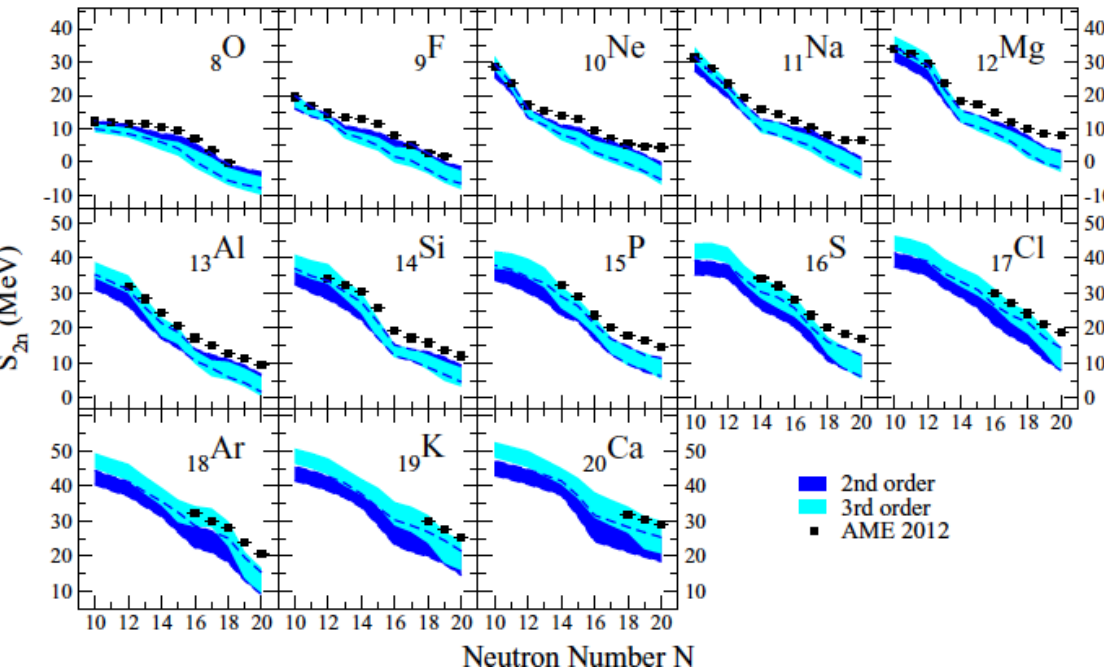
shell model with core
via the **effective interaction**
derived from **nuclear force**

Examples of structure calculations starting from chiral EFT forces

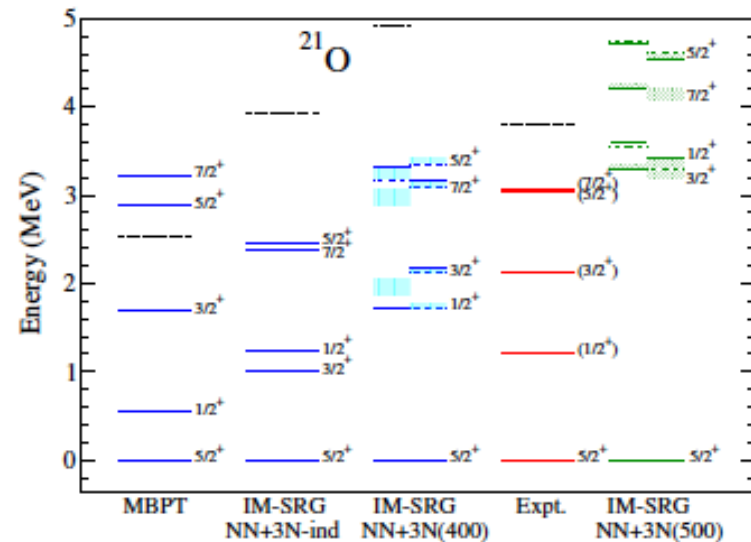
NN force: N3LO + 3N force: N2LO
 -> valence shell interaction

MBPT
 (Many-body Perturbation Theory)
 applicable to one major shell

IM-SRG
 (In-Medium Similarity Renormalization Group)



Simonis et al. PRC 93, 011302(R) (2016)



Bogner et al. PRL 113, 142501 (2014)

+ Coupled Cluster calculation + N2LOsat potential +

Chiral EFT NN int. + Fujita-Miyazawa $3N$ int. with averaging
(to be replaced by EFT N2LO $3N$ int.)



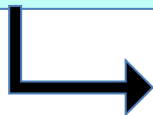
$V_{\text{low } k}$: treatment of high-momentum components

EKK : in-medium correction (core polarization)
(conventional MBPT may diverge in two major shells)

Krenciglwa and Kuo (1971) -> **Extended KK** (by Takayanagi)

***ab initio* effective interaction : EEdf1**

Shell model (or Configuration Interaction; **CI**) calculation
by the conventional matrix diagonalization
or by the Monte Carlo Shell Model



Energy levels, electromagnetic matrix elements
(diagonalization of Hamiltonian matrix)

A development starting from chiral EFT

EKK method* to handle consistently
two (or more) major shells

-> Effective shell-model interaction

(i) **without fit of two-body m. e.**,

(ii) applicable to **broken magicity**, or
merging two shells,

both are crucial for exotic nuclei.



***) Extended Krenciglwa-Kuo method is a magic by Takayanagi**

K. Takayanagi, Nucl. Phys. A 852, 61 (2011).

N. Tsunoda, **K. Takayanagi**, M. Hjorth-Jensen, and T. Otsuka, Phys. Rev. C 89, 024313 (2014).

K. Takayanagi, Annals of Physics 350, 501 (2014).

Extended KK method and conventional KK method

EKK method

New parameter E (arbitrary parameter)

$$H = H'_0 + V'$$
$$= \begin{pmatrix} E & 0 \\ 0 & QH_0Q \end{pmatrix} + \begin{pmatrix} P\tilde{H}P & PVQ \\ QVP & QVQ \end{pmatrix},$$

$$H_{\text{BH}}(E) = PHP + PVQ \frac{1}{E - QH_0Q} QVP.$$

$$\tilde{H}_{\text{eff}}^{(n)} = \tilde{H}_{\text{BH}}(E) + \sum_{k=1}^{\infty} \hat{Q}_k(E) \{\tilde{H}_{\text{eff}}^{(n-1)}\}^k,$$

KK method (conventional)

Krenciglwa and Kuo (1971)

Divergence problem in multi-shell

$$H = H_0 + V$$
$$= \begin{pmatrix} PH_0P & 0 \\ 0 & QH_0Q \end{pmatrix} + \begin{pmatrix} PVP & PVQ \\ QVP & QVQ \end{pmatrix}$$

$$\hat{Q}(E) = PVP + PVQ \frac{1}{E - QH_0Q} QVP$$

$$V_{\text{eff}}^{(n)} = \hat{Q}(\epsilon_0) + \sum_{k=1}^{\infty} \hat{Q}_k(\epsilon_0) \{V_{\text{eff}}^{(n-1)}\}^k.$$

- **EKK method enables us to construct effective interaction for multi-major shell**

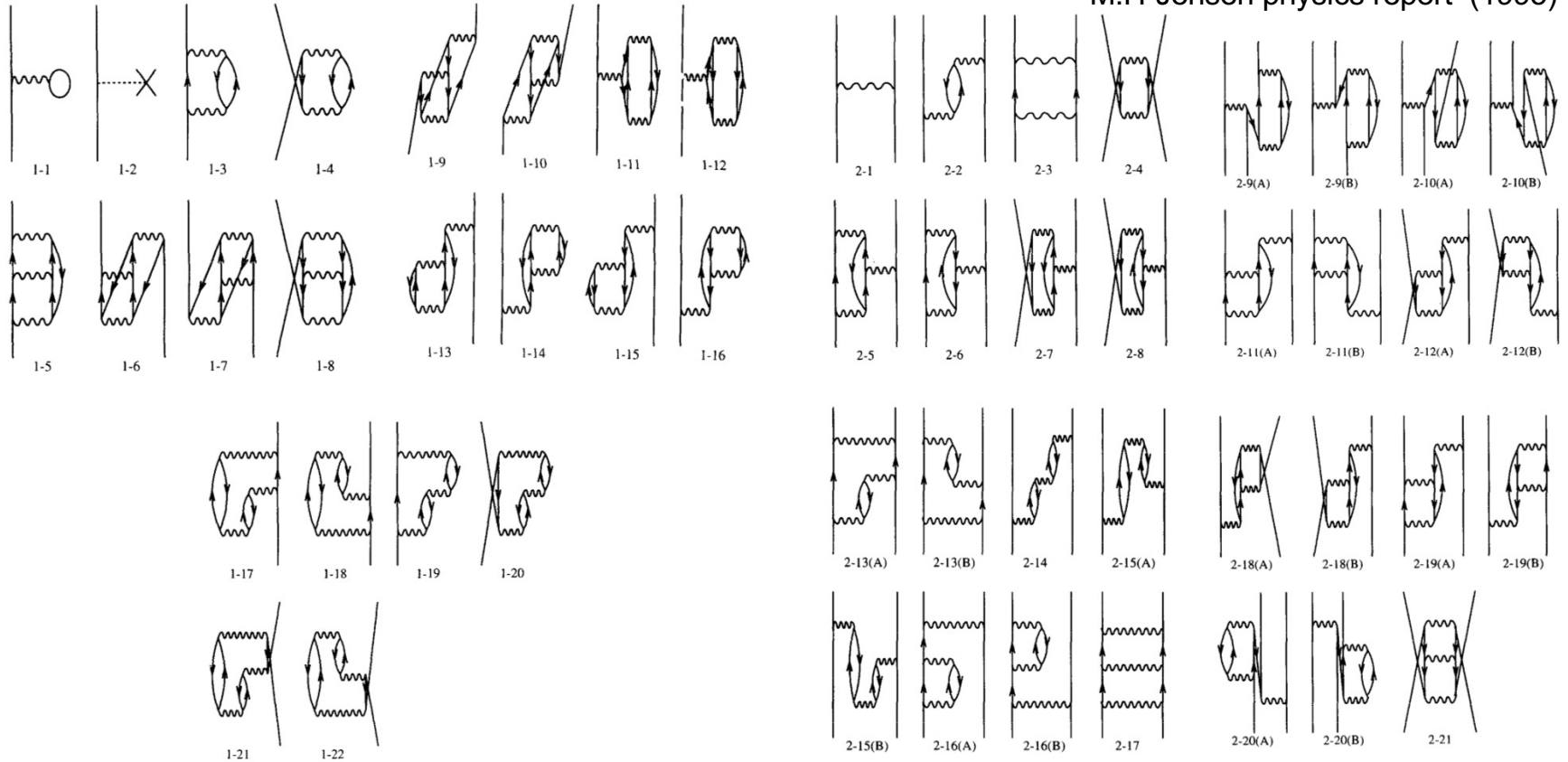
N. Tsunoda, K. Takayanagi, M. Hjorth-Jensen, and T. Otsuka, Phys. Rev. C 89, 024313 (2014).

K. Takayanagi, Annals of Physics 350, 501 (2014).

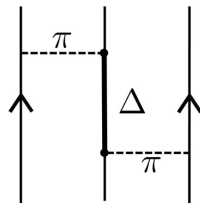
K. Takayanagi, Nucl. Phys. A 852, 61 (2011).

Many-body perturbation theory

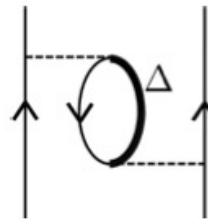
M.H-Jensen physics report (1995)



Fujita-Miyazawa type
3N interaction

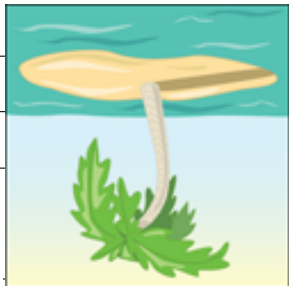


summation with hole state

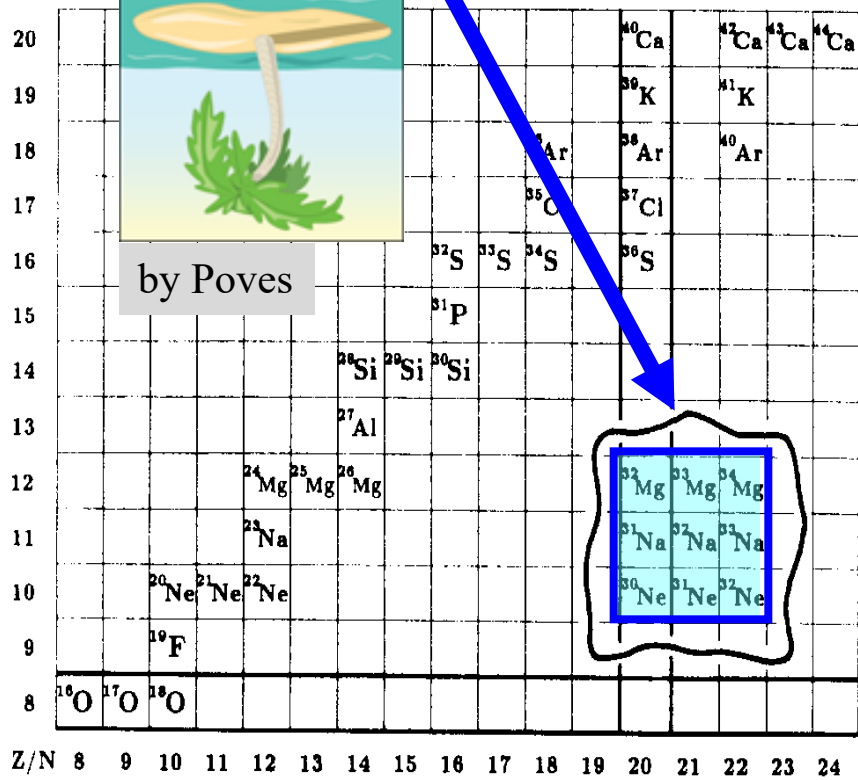


Effective
2N interaction

Island of Inversion



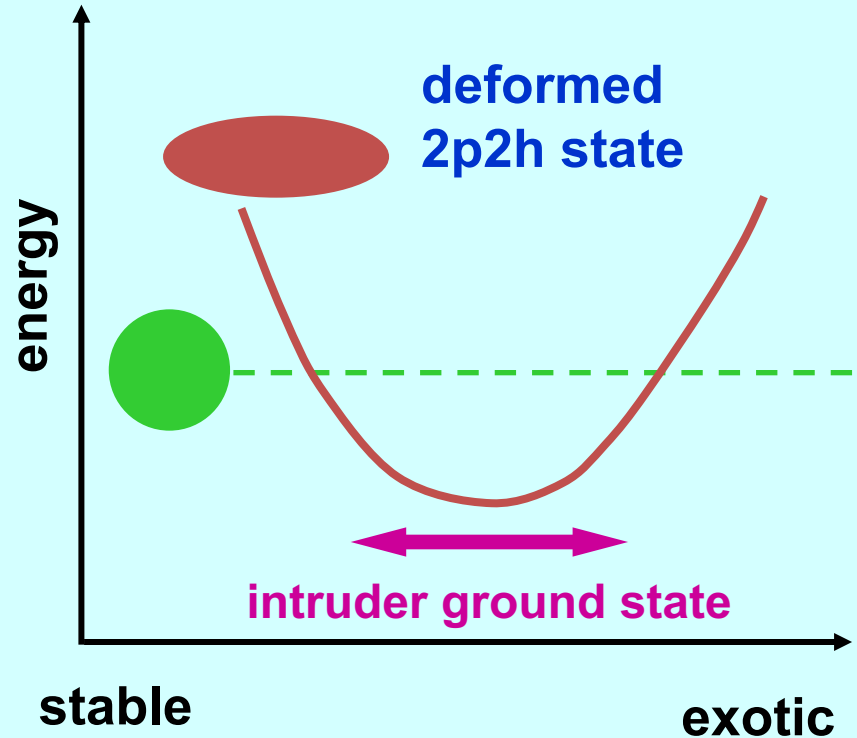
by Povos



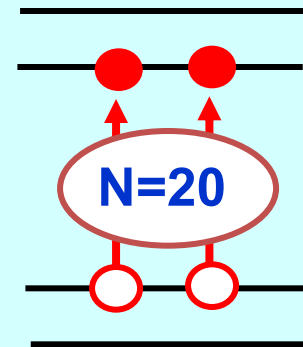
9 nuclei:
Ne, Na, Mg with N=20-22

Phys. Rev. C 41, 1147 (1990),
Warburton, Becker and
Brown

Traditional picture



pf shell



sd shell

gap ~
constant

Anomaly in energy levels : not expected from a magicity

β -DECAY SCHEMES OF VERY NEUTRON-RICH SODIUM ISOTOPES AND THEIR DESCENDANTS

D. GUILLEMAUD-MUELLER*, C. DETRAZ*, M. LANGEVIN and F. NAULIN

Institut de Physique Nucléaire, BP 1, F-91406 Orsay, France

M. DE SAINT-SIMON, C. THIBAUT and F. TOUCHARD

*Laboratoire René Bernas du Centre de Spectrométrie Nucléaire
BP 1, F-91406 Orsay, France*

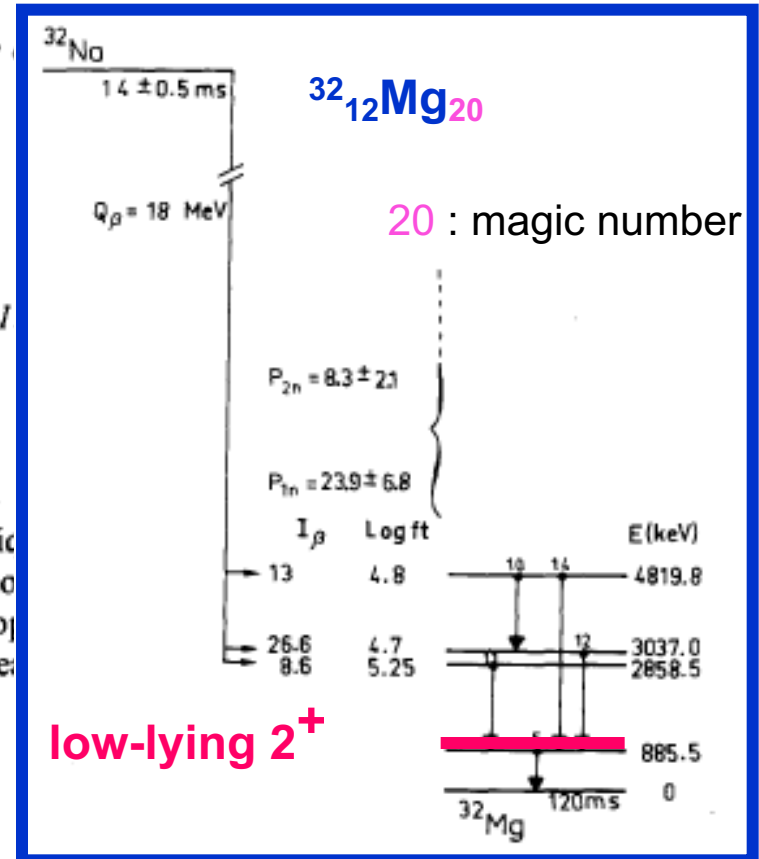
and

M. EPHERRE

Laboratoire René Bernas and CERN, Division EP, CH-1211

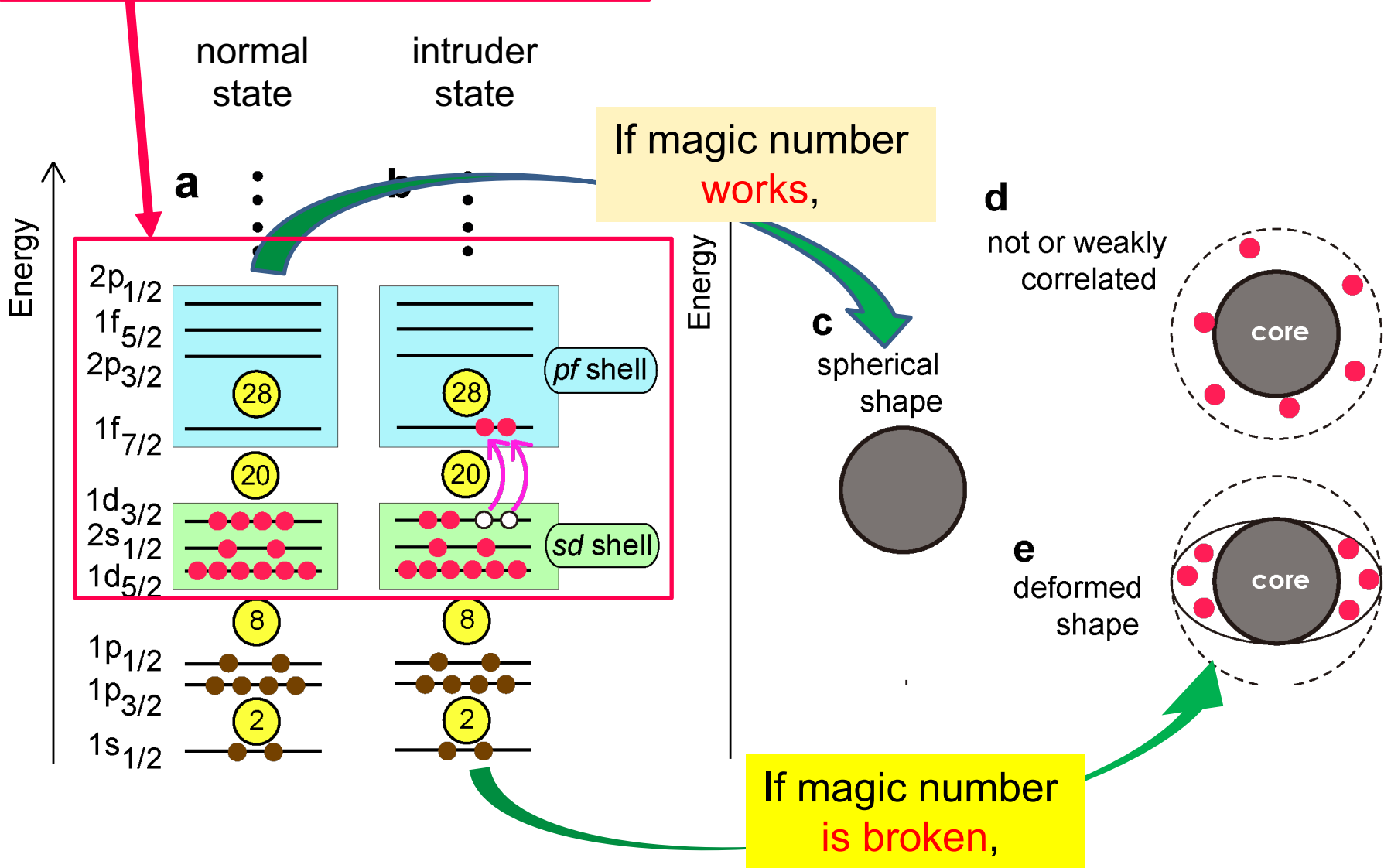
Received 6 February 1984

Abstract: The γ -activities from the β -decay of Na isotopes up to ^{32}Na were measured and analysed through mass-spectrometry technique from their Mg descendants. The I_γ intensities, the β -delayed γ activities and the I_β intensities are measured. Decay schemes are proposed. The location of the first 2^+ level of ^{32}Mg , the occurrence of a nucle-



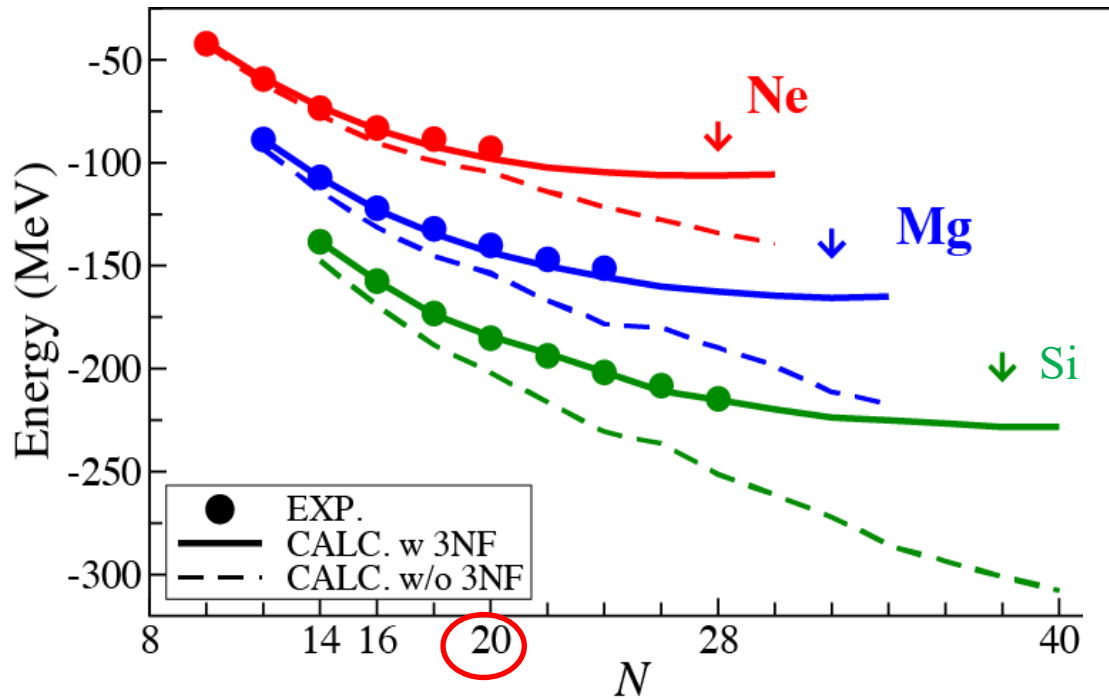
Relation to the magic number N=20 and the present valence shell

The valence shell in the present work



ground-state energies

Earlier (2017 PRC) work by EEdf1



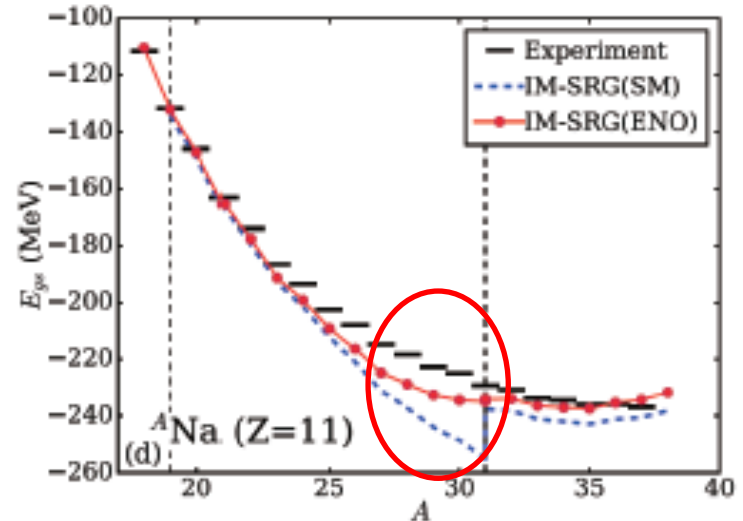
Calculations with full $sd + pf$ shell

PHYSICAL REVIEW C 95, 021304(R) (2017)

Exotic neutron-rich medium-mass nuclei with realistic nuclear forces

Naofumi Tsunoda,¹ Takaharu Otsuka,^{1,2,3,4} Noritaka Shimizu,¹ Morten Hjorth-Jensen,^{5,6}
Kazuo Takayanagi,⁷ and Toshio Suzuki⁸

Earlier *ab initio* work
on **Na** isotopes

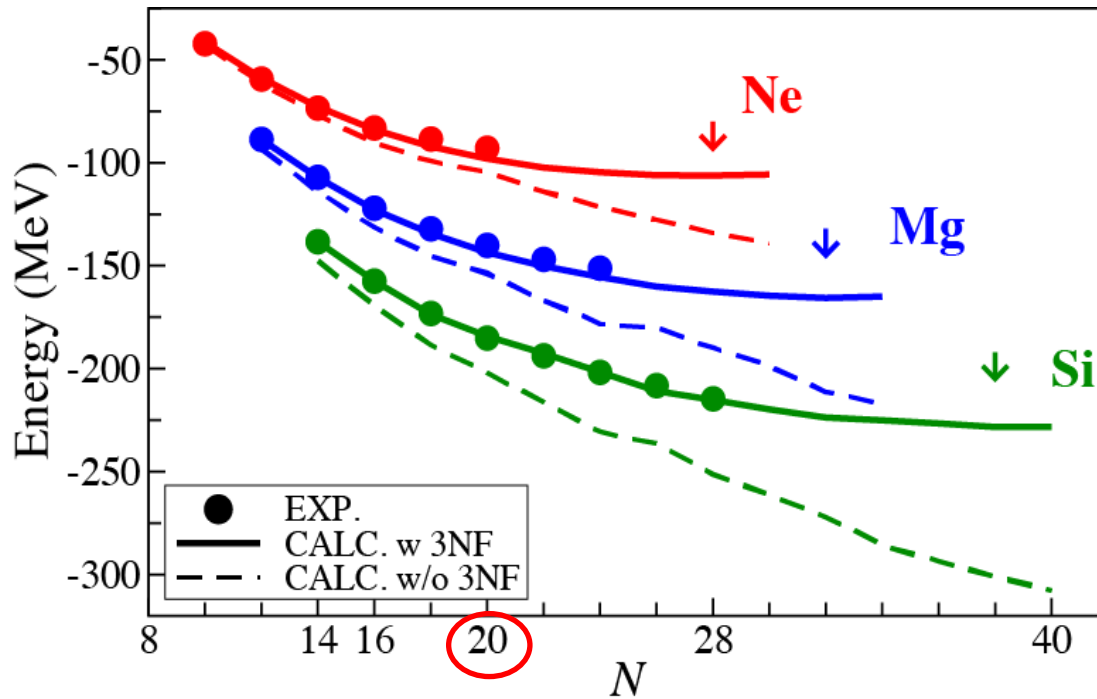


IM-SRG (SM) : core reference
IM-SRG (ENO) : ensemble reference
Stroberg et al. PRL 118, 032502 (2017)

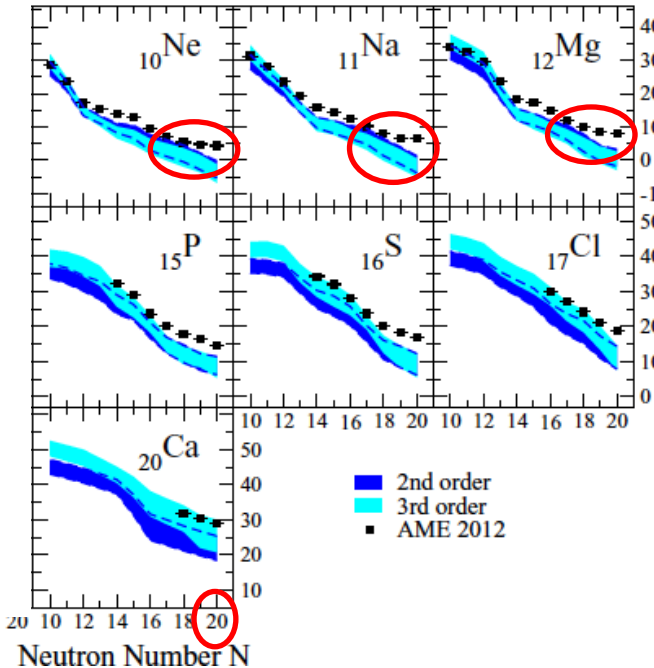


ground-state energies

Earlier (2017 PRC) work by EEdf1



Earlier work



Calculations with full sd + pf shell

PHYSICAL REVIEW C 95, 021304(R) (2017)

Exotic neutron-rich medium-mass nuclei with realistic nuclear forces

Naofumi Tsunoda,¹ Takaharu Otsuka,^{1,2,3,4} Noritaka Shimizu,¹ Morten Hjorth-Jensen,^{5,6}
Kazuo Takayanagi,⁷ and Toshio Suzuki⁸

Simonis et al.

PRC 93, 011302(R) (2016)

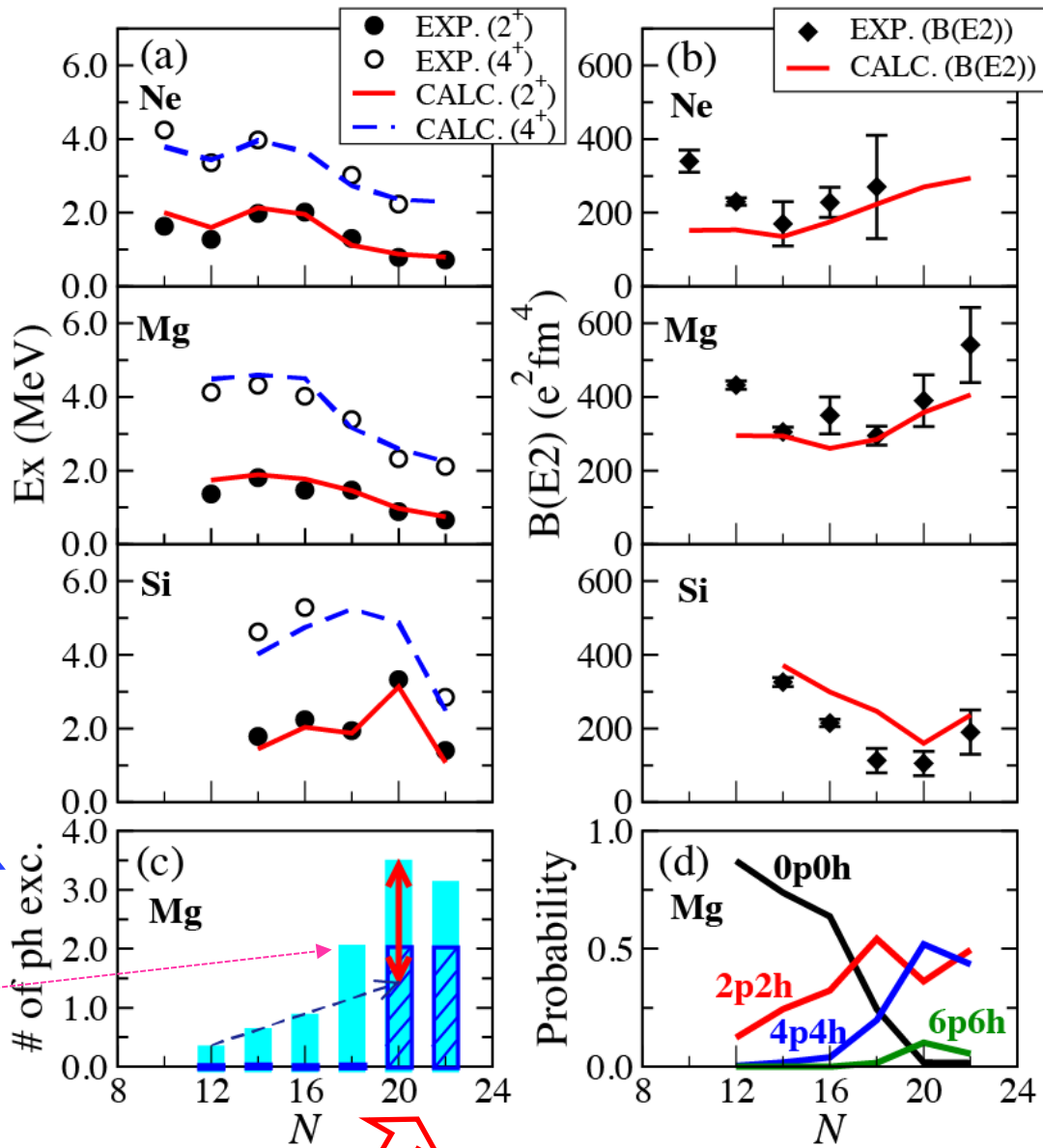


Earlier (2017 PRC) work by EEdf1

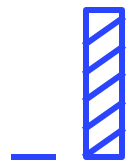
Ne-Mg-Si

2^+ & 4^+ levels and $B(E2)$ values

of particle-hole excitations across $N=20$ gap :
 (modest) steady increase
 +
 abrupt increase after $N=18$



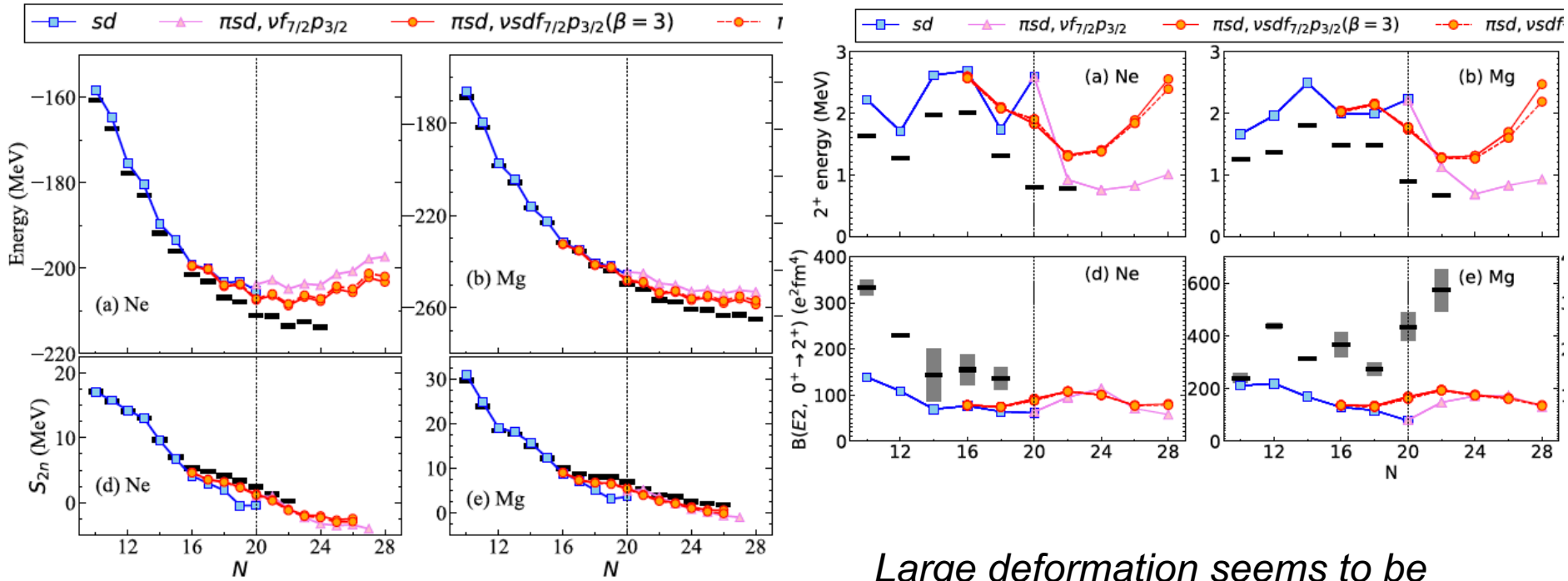
ground states of Mg isotopes



Early idea of the **Island of Inversion** (WBB)
 $0p-0h$ or $2p-2h$ (discrete)

Ab initio multishell valence-space Hamiltonians and the island of inversion

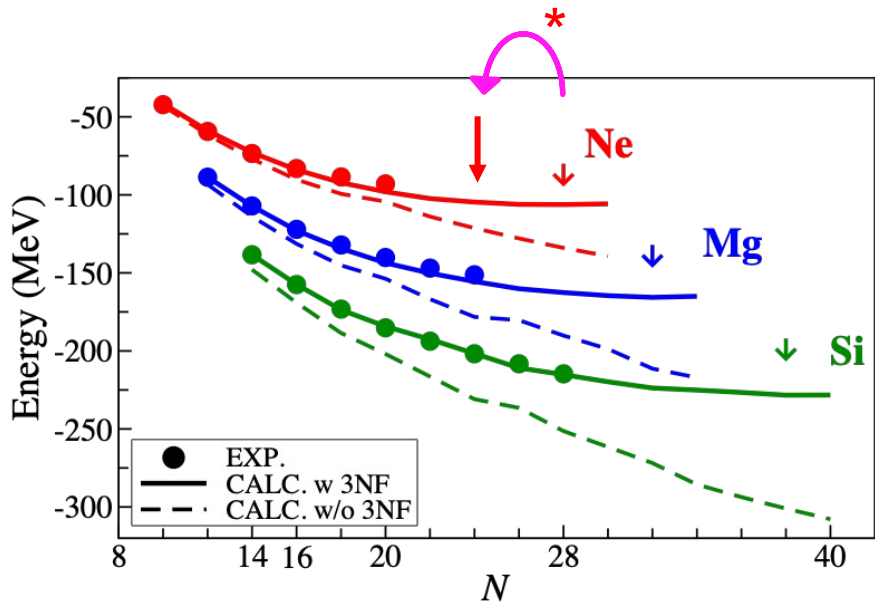
T. Miyagi¹, S. R. Stroberg², J. D. Holt^{1,3} and N. Shimizu⁴



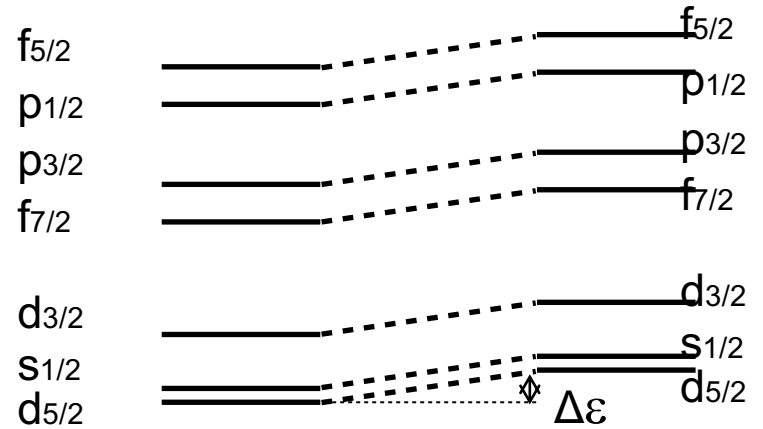
Large deformation seems to be a challenge.

Dripline mechanism

Our earlier (2017) calculation was not perfect;
fine-tuning of SPEs for EEdf1 is done



- We **fine-tuned** the SPEs to reproduce **recent experimental findings***.



Tsunoda, *et al.* Phys. Rev. C 95, 021304 (2017).

0.82 < $\Delta\epsilon$ < 0.87 is needed

PHYSICAL REVIEW LETTERS 123, 212501 (2019)

Editors' Suggestion

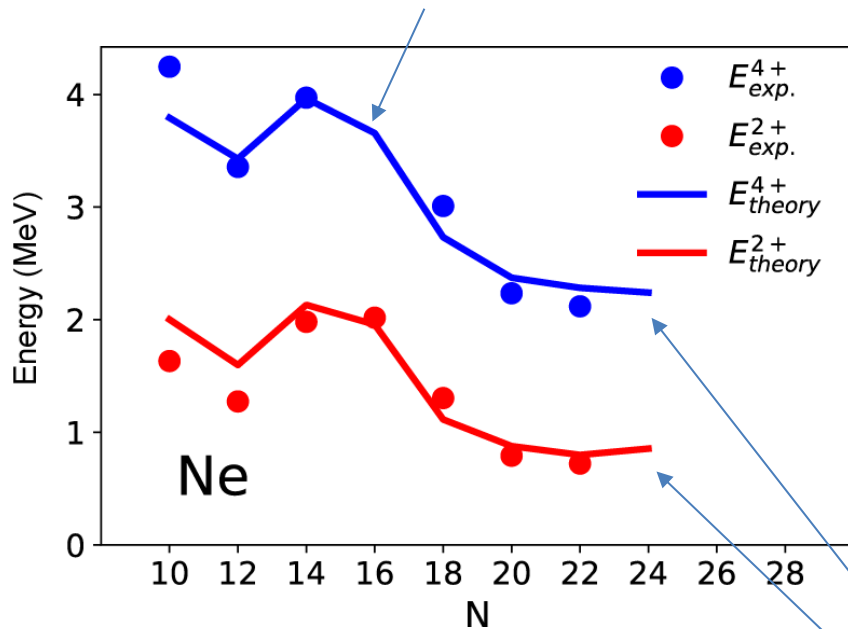
Featured in Physics

Location of the Neutron Dripline at Fluorine and Neon

D. S. Ahn,¹ N. Fukuda,¹ H. Geissel,⁵ N. Inabe,¹ N. Iwasa,⁴ T. Kubo,^{1,*†} K. Kusaka,¹ D. J. Morrissey,⁶ D. Murai,³ T. Nakamura,² M. Ohtake,¹ H. Otsu,¹ H. Sato,¹ B. M. Sherrill,⁶ Y. Shimizu,¹ H. Suzuki,¹ H. Takeda,¹ O. B. Tarasov,⁶ H. Ueno,¹ Y. Yanagisawa,¹ and K. Yoshida¹

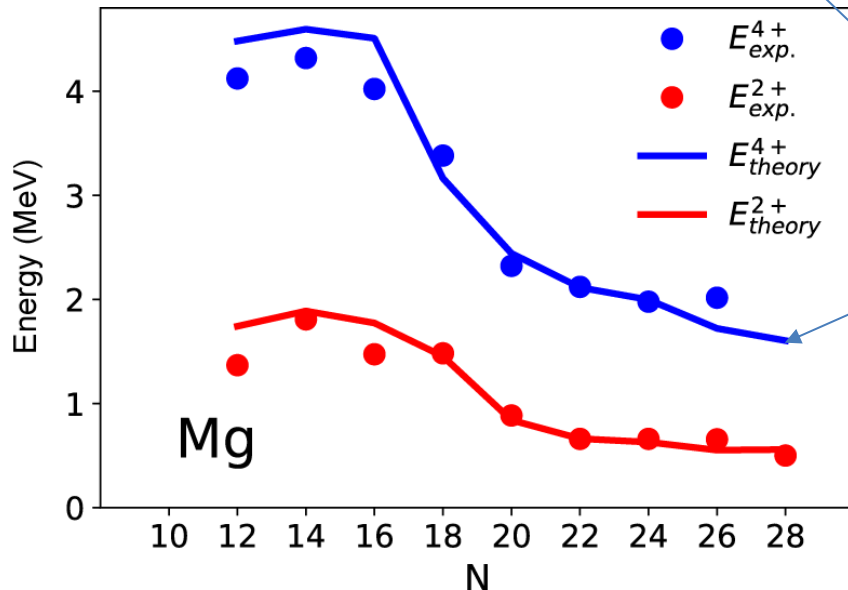
³¹F and ³⁴Ne are dripline nuclei,
+
1 event of ³⁹Na

Ne and Mg systematics



$\Delta\varepsilon$ changes neither excitation energies nor wave functions.

The EEdf1 Hamiltonian appears to be reasonable up to N~28 for Z=9-12.



Levels do not exist as bound states, because their energies are above the threshold of neutron emission.

Decomposition of the Hamiltonian

monopole part

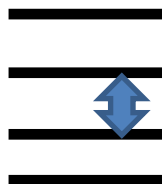
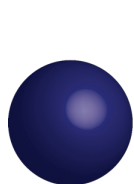
bare SPE

$$\sum \epsilon_i a_i^+ a_i$$

monopole

$$\sum_{i,j} V_{\text{mono}}^{ab} a_i^+ a_j^+ a_j a_i$$

$$V_{\text{mono}}^{ab} = \sum_J \frac{(2J+1) \langle ab|V|ab \rangle_J}{2J+1}$$



monopole: shift of SPE

multipole part

pairing

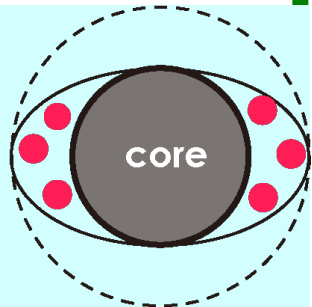
$J=0$ nn + pp

pairing correlations

rest

quadrupole deformation, etc

deformed shape



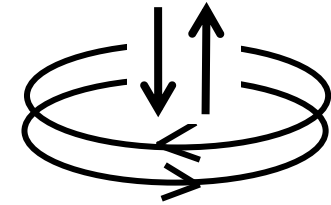
Pairing interaction

*Pairing interaction

$$\langle j_1^2 \ J=0 | V | j_2^2 \ J=0 \rangle \quad j_1^2 = j_1 \times j_1$$

in $T=1$ channel

(identical particles)

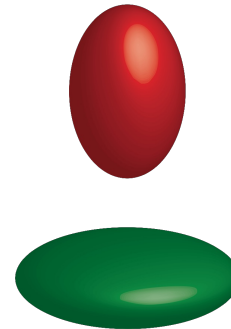
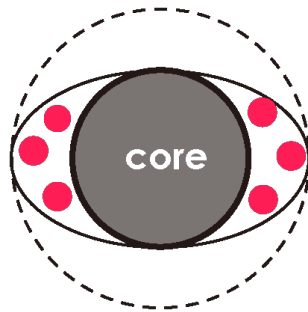


*time reversal states
-> strong attraction*

Rest of the interaction

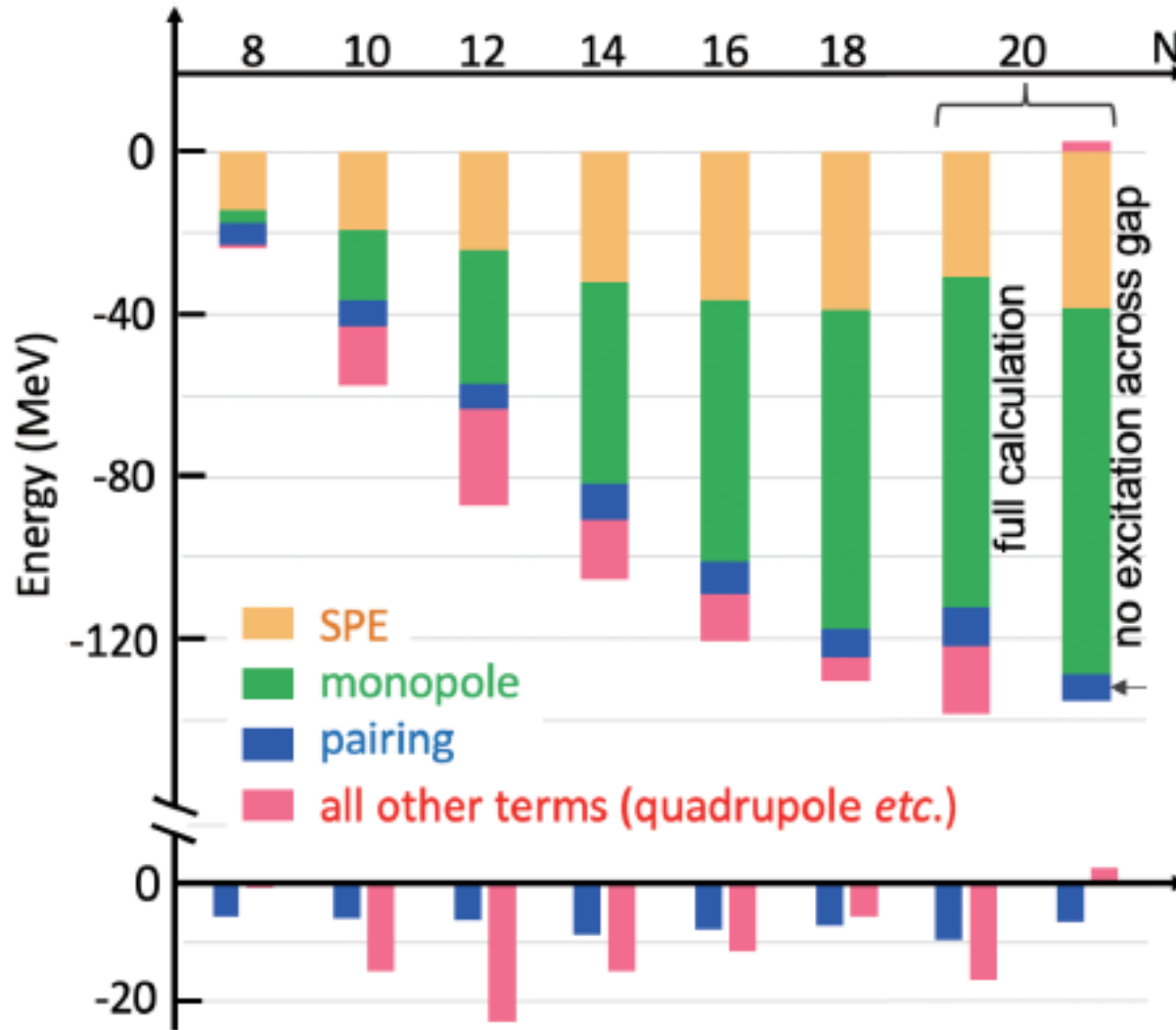
major effect ~ quadrupole shape deformation

deformed
shape



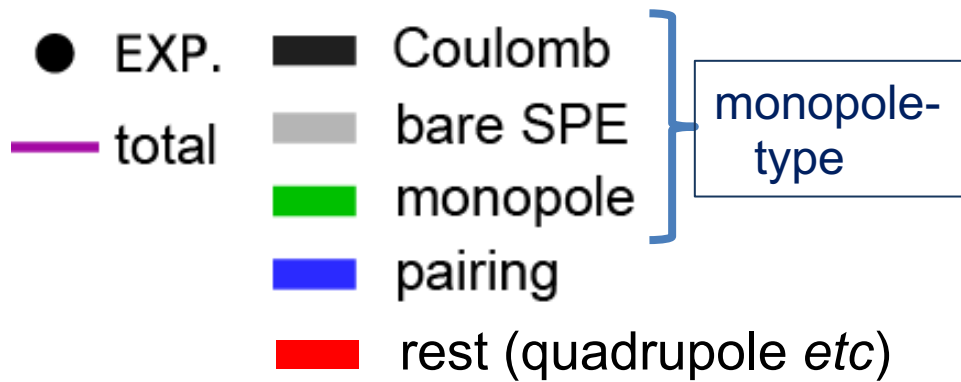
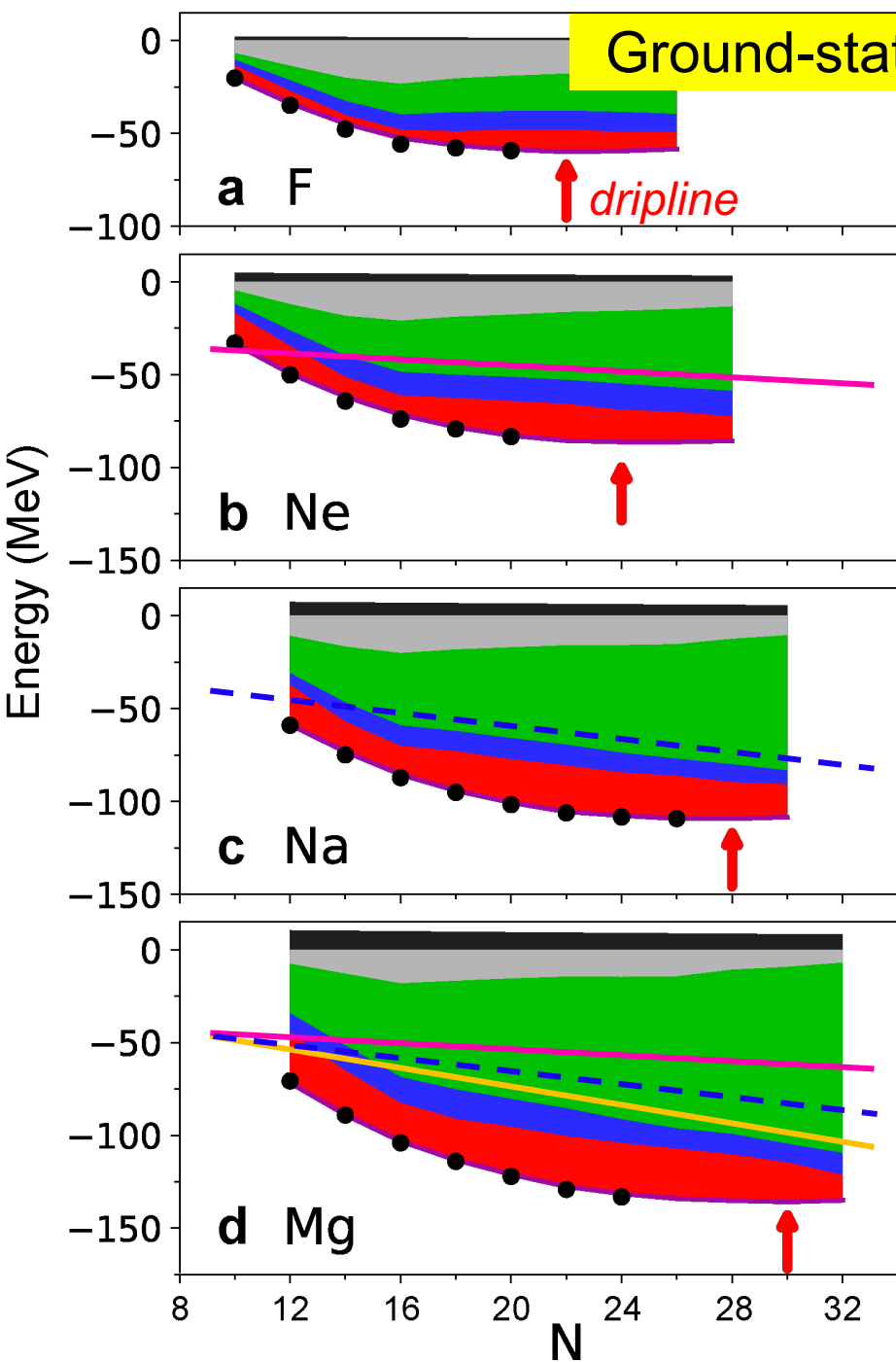
Ground-state energies of Mg isotopes up to N=20 (USD int. up to N=18)

Otsuka *et al.*: RMP 92, 015002 (2020)



sd-pf-m int.
for N=20

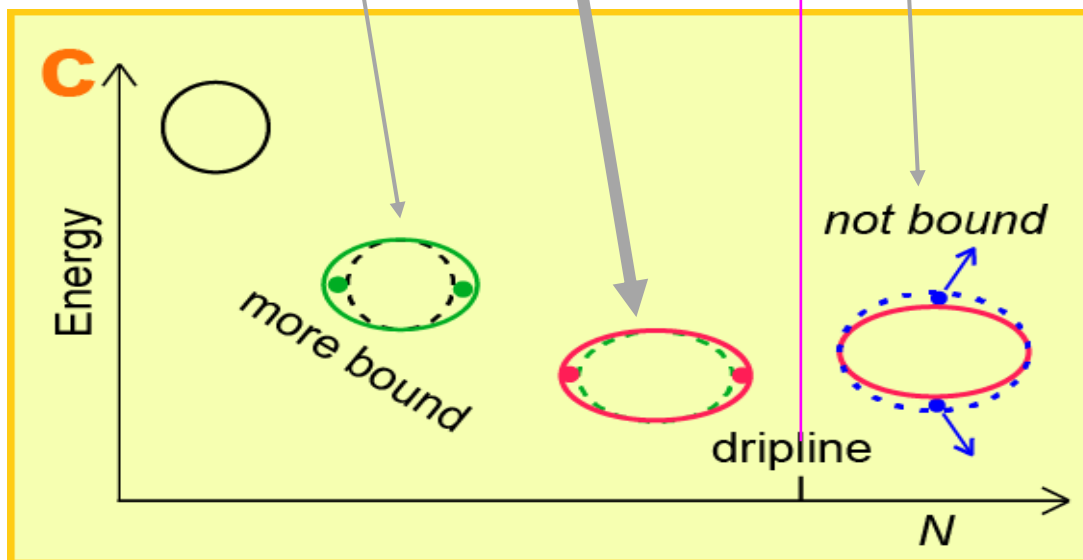
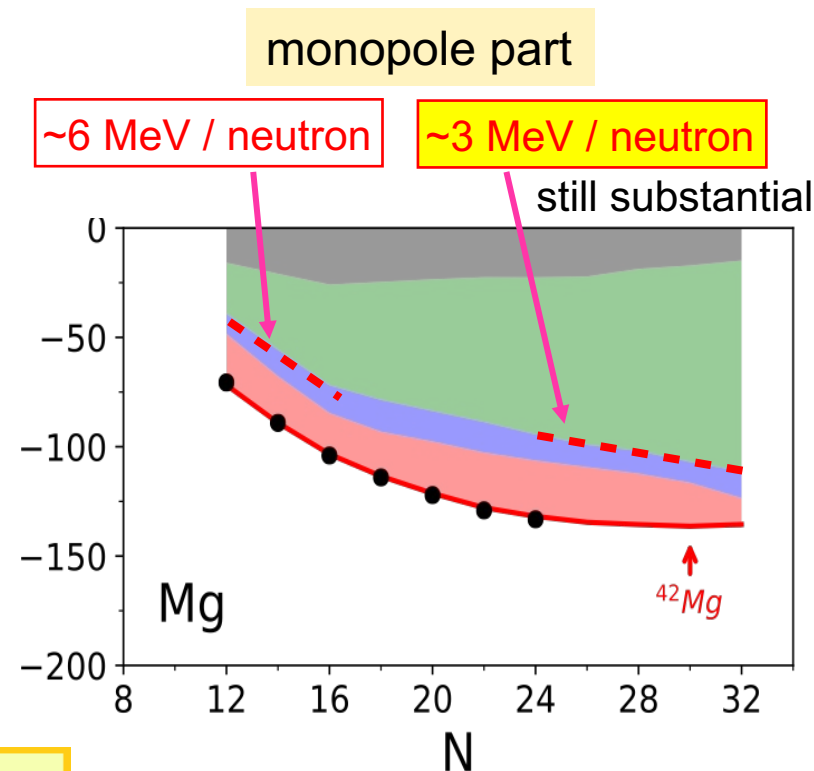
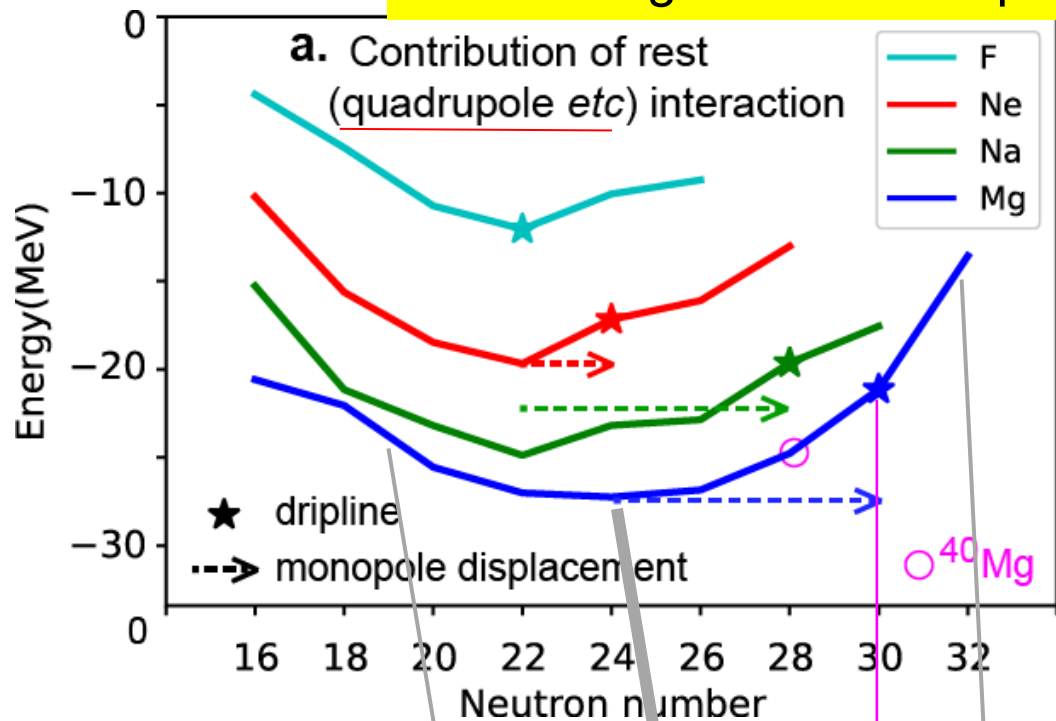
Ground-state energy is decomposed (EEdf1 int.)



The **monopole** effect (**lower edge of green part**) lowers the energy as a function of N , and its **slope** becomes **steeper as Z** because of the **p-n monopole int.**, as shown by **three lines** fitted to different slopes.

The **rest** (\sim quadrupole deformation) effect (**red part**) varies locally.
 ... see next page

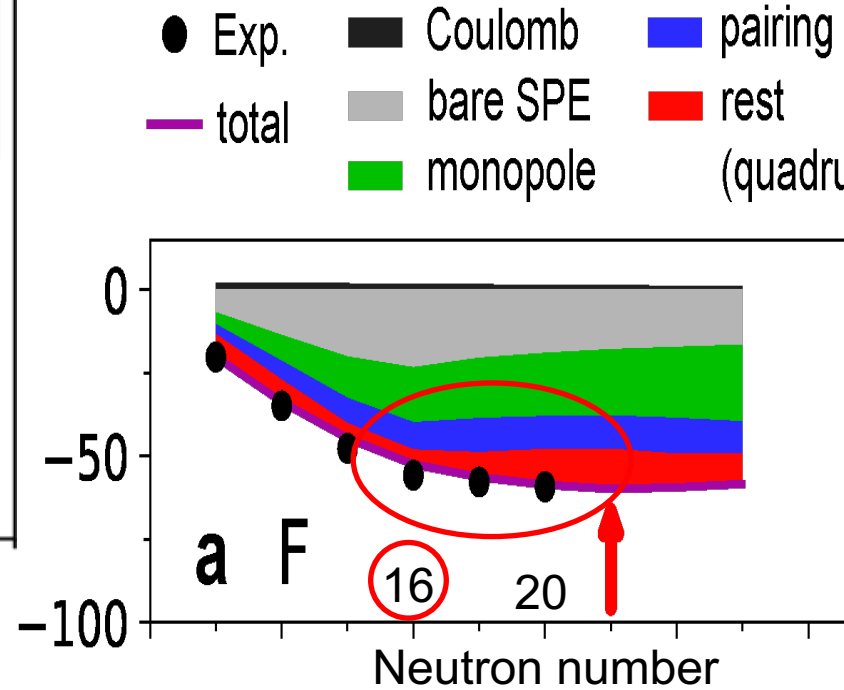
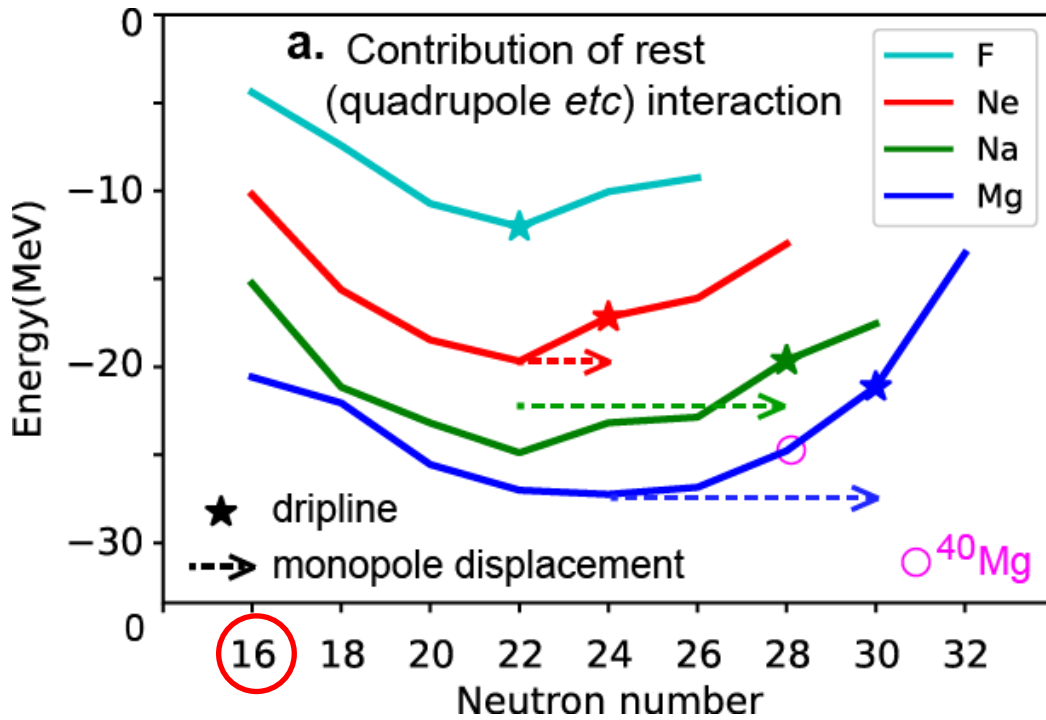
Two driving forces: example from Mg isotopes



The rest (mainly deformation energy) part is saturated at $N=24$.

The monopole effects compensate it, and pushes the dripline away (dashed arrows).

Dripline of F isotopes

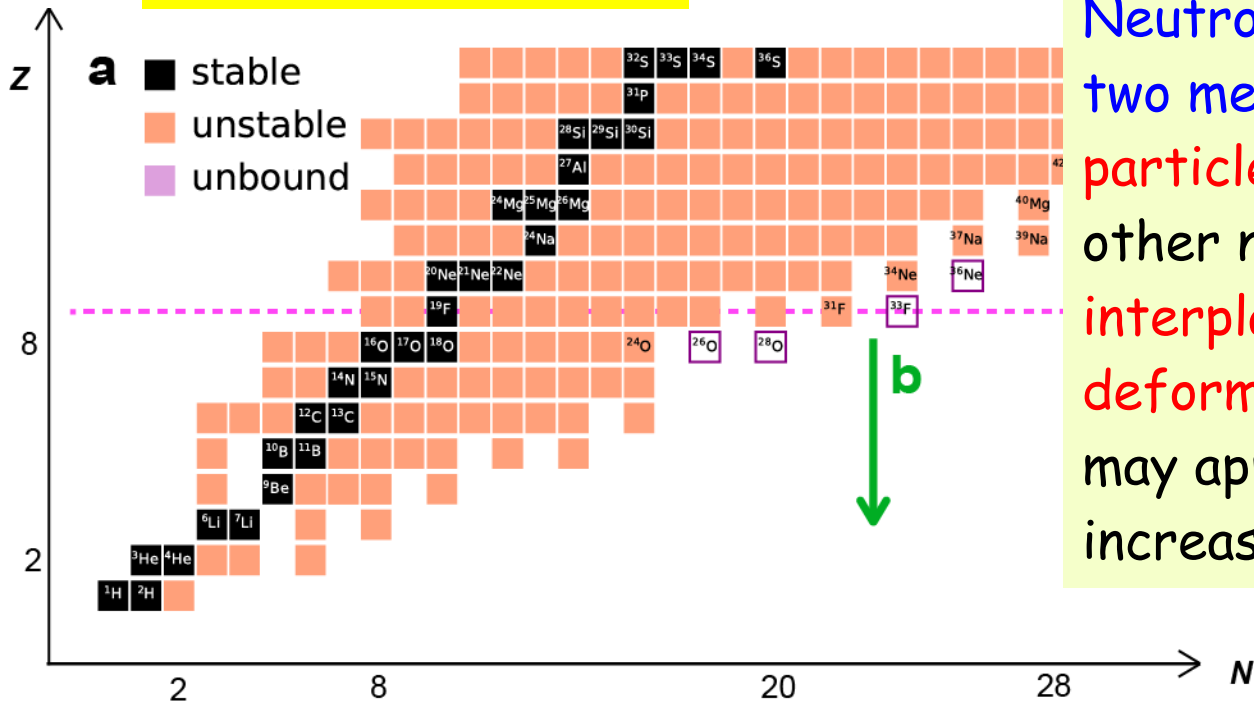


Monopole effect (edge of green part) becomes weaker for $N > 16$ in F isotopes. It even decreases because of high-lying $d_{3/2}$ (see gray edge).

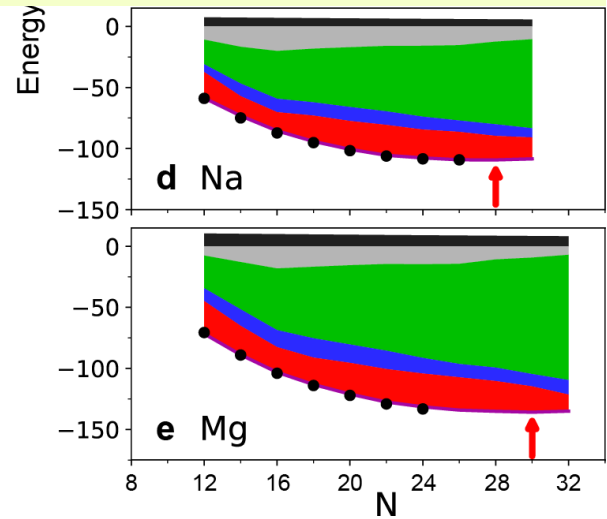
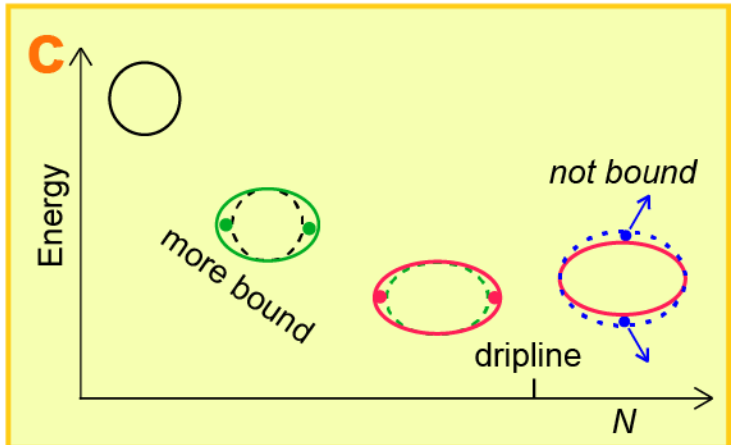
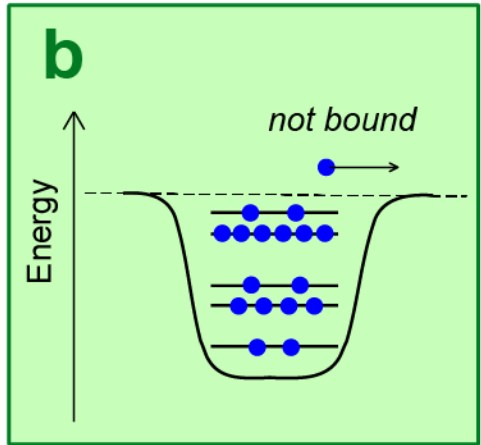
If there were no "rest" (~ quadrupole deformation) effect (red part), the dripline would be at $N = 16$, which is the same as oxygen isotopes.

Loose binding phenomena may be seen (?), in contrast to Ne, Na or Mg.

Dripline mechanisms



Neutron driplines are due to two mechanisms: one has **single-particle origin** (b), while the other new one (c) is due to the **interplay of monopole and deformation energies**. They may appear alternatively as Z increases.



Traditional (vague) view
 -> extreme: neutron halo

New view

Intermediate case: ^{22}C
 Suzuki, O, Yuan & Alahari,
 PLB 753, 199 (2016).

A probe of this mechanism : magnetic moment of Na isotopes

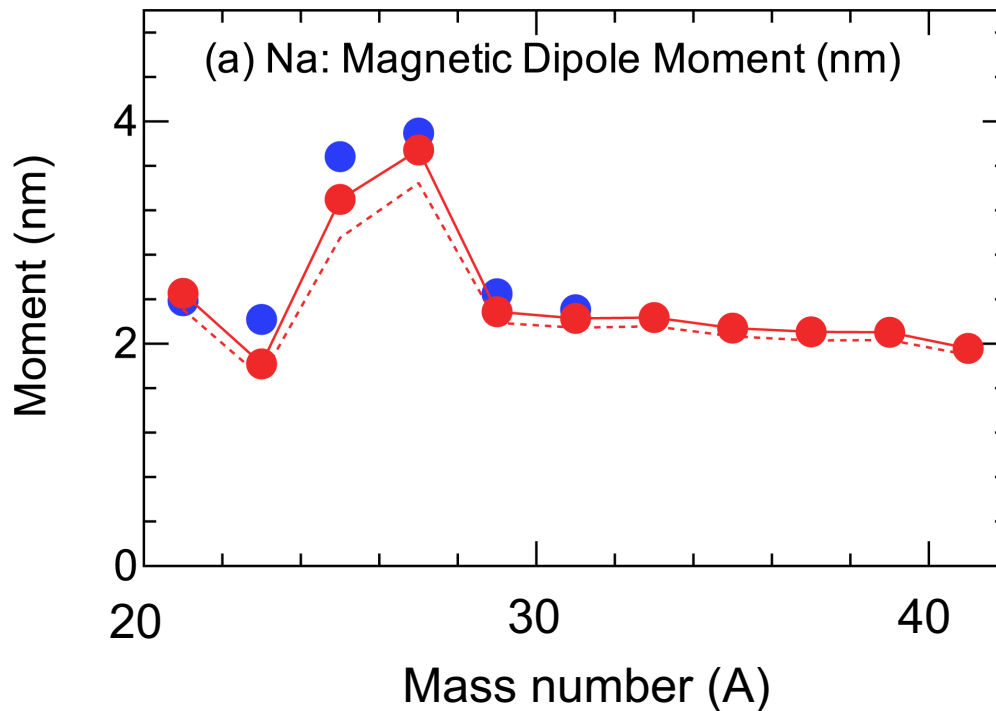
PHYSICAL REVIEW C **105**, 014319 (2022)

Moments and radii of exotic Na and Mg isotopes

Takaharu Otsuka^{1,2,3,*}, Noritaka Shimizu^{1b,4} and Yusuke Tsunoda^{1b,4}

- exp
- — present calc. (g_l shifted: 1.2 for proton and -0.2 for neutron)
- - - - present calc. (free g factors)

A pionic effect on the M1 operator.



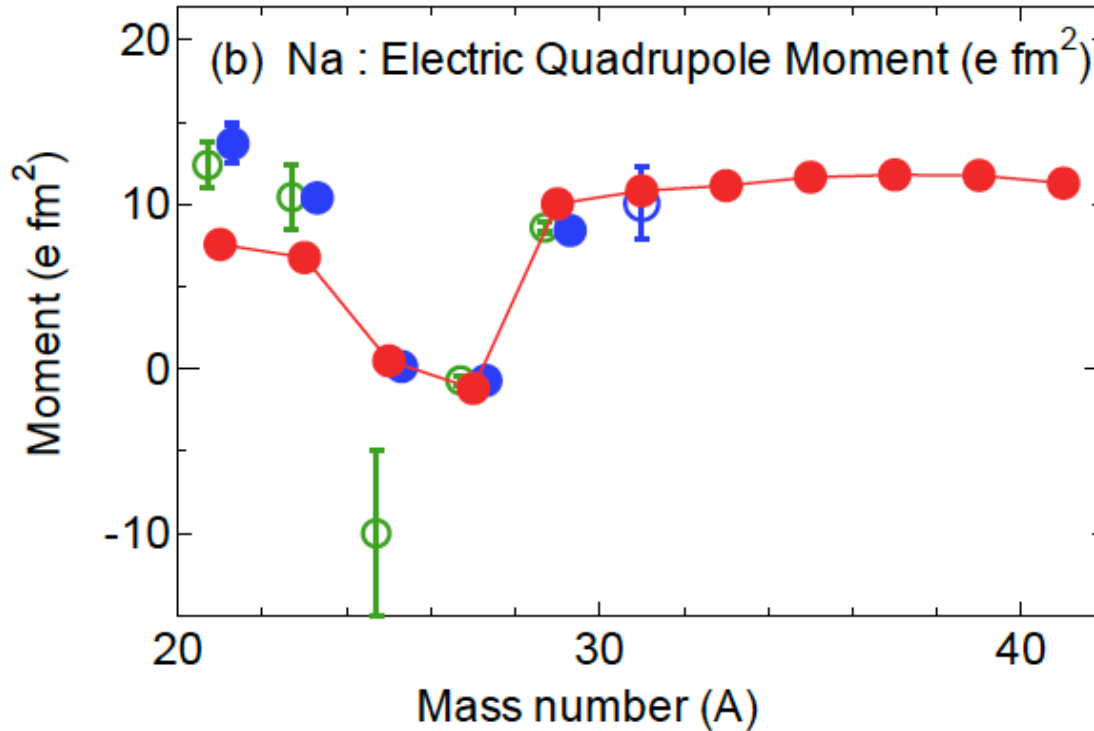
The quenching of spin g-factor (g_s) is needed to incorporate 2p2h cross shell excitations.



Most of such excitations are treated **explicitly in this work**, and the mixing occurs due to the ***ab initio* interaction EEdf1**. It looks natural that free spin g-factors work well around ^{31}Na . But, how far ?

exp

Electric quadrupole moments of Na isotopes



○ National Nuclear Data Center. Evaluated Nuclear Structure Data File, <https://www.nndc.bnl.gov/ensdf/>.

● M. De Rydt, M. Depuydt and G. Neyens, *At. Data Nucl. Data Tab.* **99**, 391 (2013).
○ M. Keim, in *Proc. of the Int. Conf. on Exotic Nuclei and Atomic Masses (ENAM98)*, edited by B. M. Sherrill, D. J. Morrissey, and C. N. Davis, AIP Conf. Proc. No. 455 (AIP, New York, 1998), p. 50.

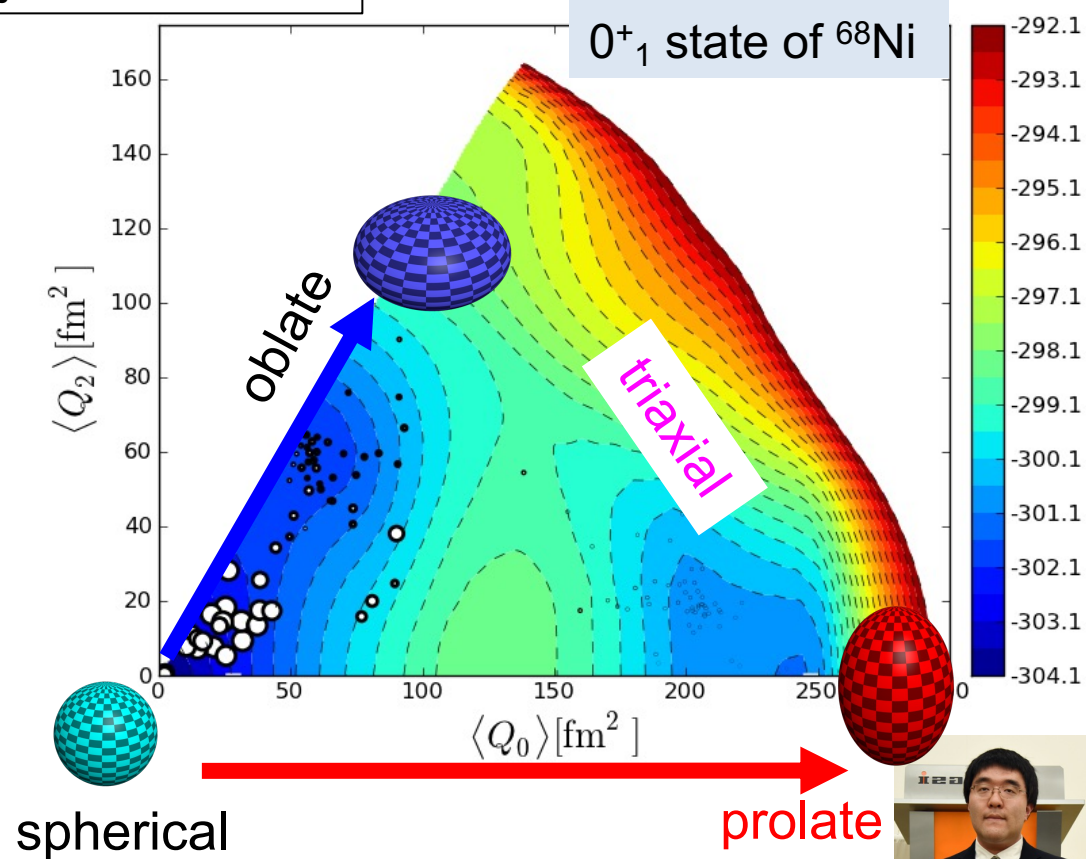
Can we obtain deformation parameters β_2 and γ ?

T-plot : visualization of MCSM eigenvector on Potential Energy Surface

eigenstate $\Psi = \sum_i c_i P[J^\pi](\Phi_i)$

amplitude c_i
 projection onto J^π $P[J^\pi]$
 stochastically deformed Slater determinant Φ_i
 → intrinsic shape

- PES is calculated by CHF for the shell-model Hamiltonian
- **Location of circle** : quadrupole deformation of unprojected MCSM basis vectors
- **Area of circle** : overlap probability between each projected basis and eigen wave function



Y. Tsunoda, *et al.*

PRC 89, 031301 (R) (2014)

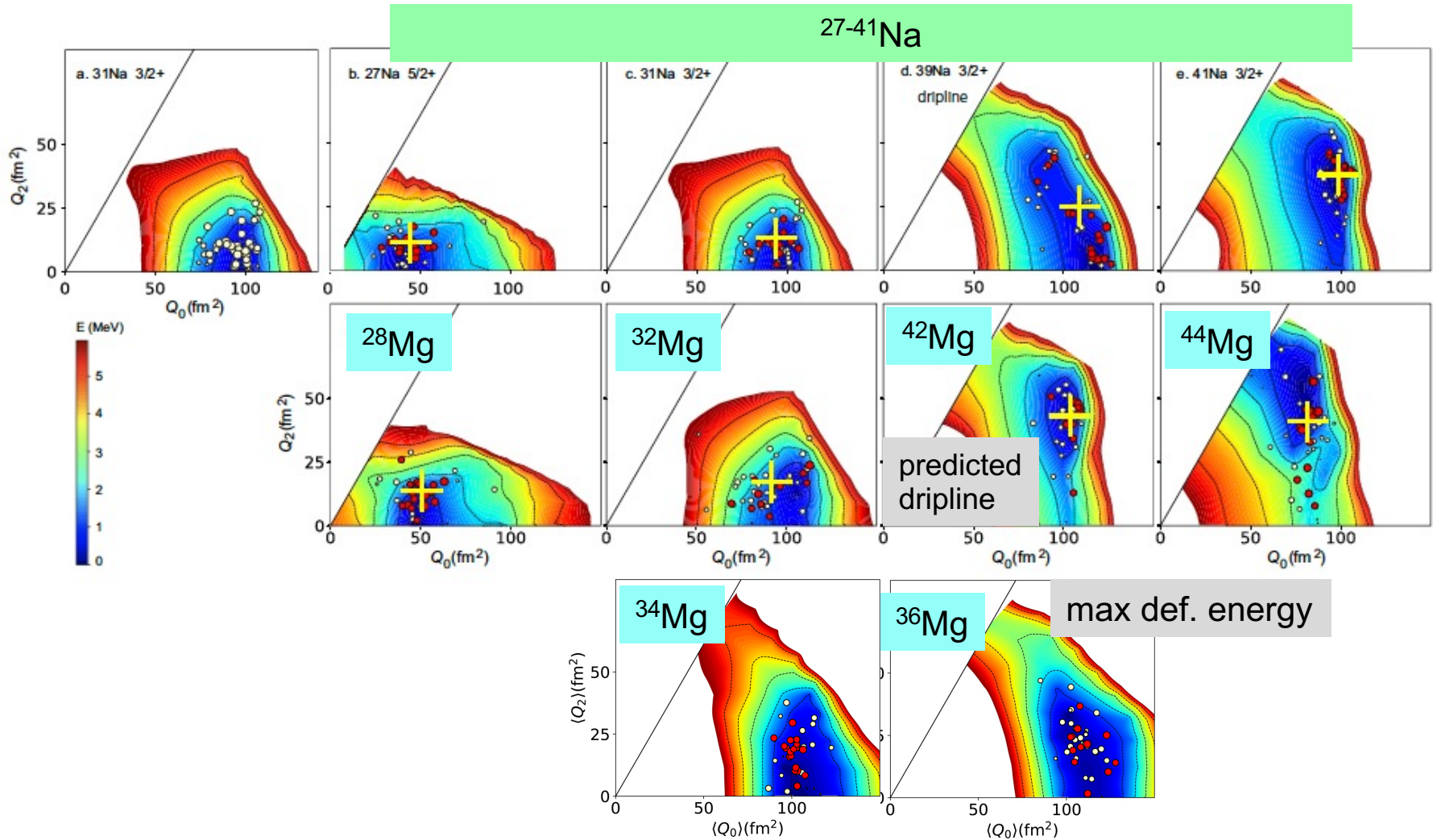


T plots for the ground states of Na and Mg isotopes

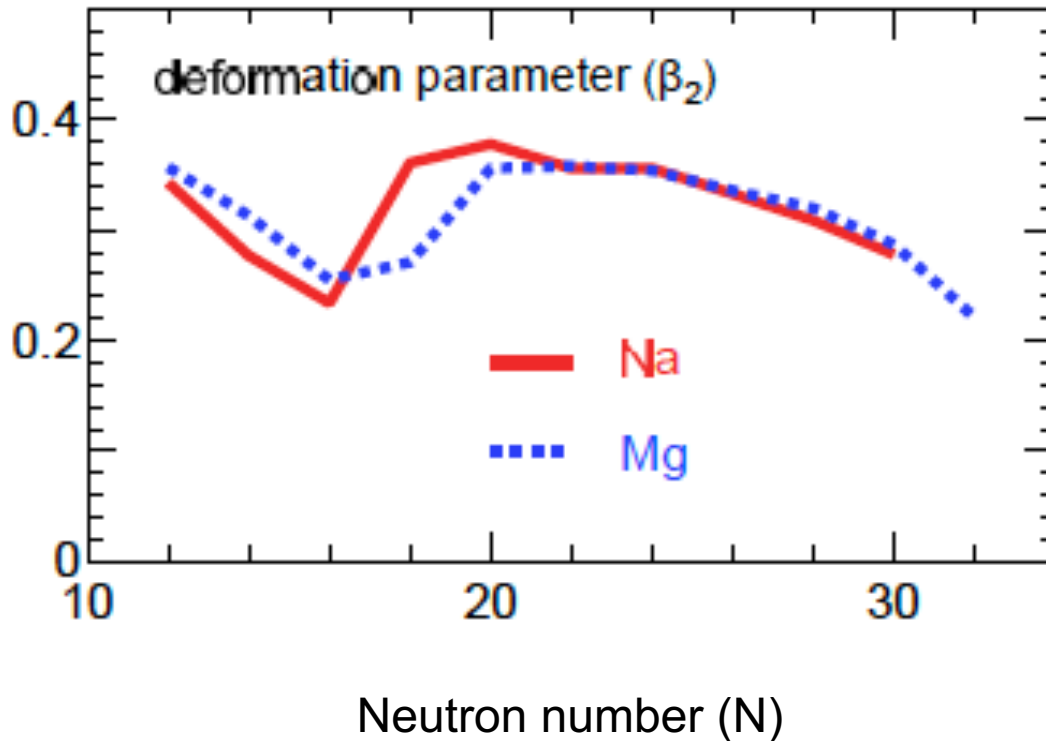
Crosses indicate representative values of Q_0 and Q_2

Deformation parameter β_2 is obtained from (Utsuno et al. PRL 114, 032501 (2015))

$$\beta_2 = \sqrt{5/16\pi} \{(e + e'_p + e'_n)/e\} (4\pi/3R_0^2 A^{5/3}) \sqrt{(Q_0)^2 + 2(Q_2)^2}$$



Deformation parameters extracted from T-plot



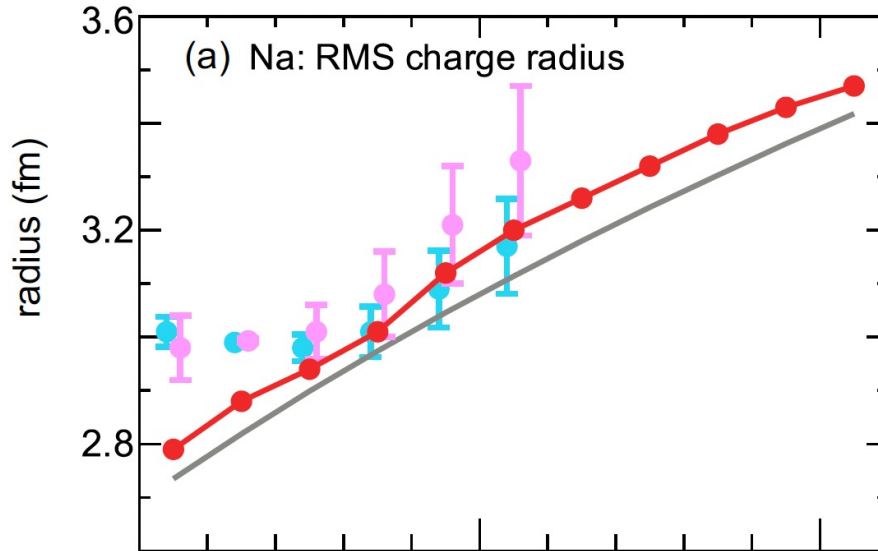
Charge radius is calculated from the usual relation

$$\langle r^2 \rangle_{ch} = \langle r^2 \rangle_{DM} \{ 1 + (5/4\pi) \beta_2^2 \}$$

with a droplet model term,

$$\langle r^2 \rangle_{DM} = (3/5) (R_0 A^{1/3})^2 \quad R_0 = 1.28(\text{fm})$$

charge and matter radii (fm)



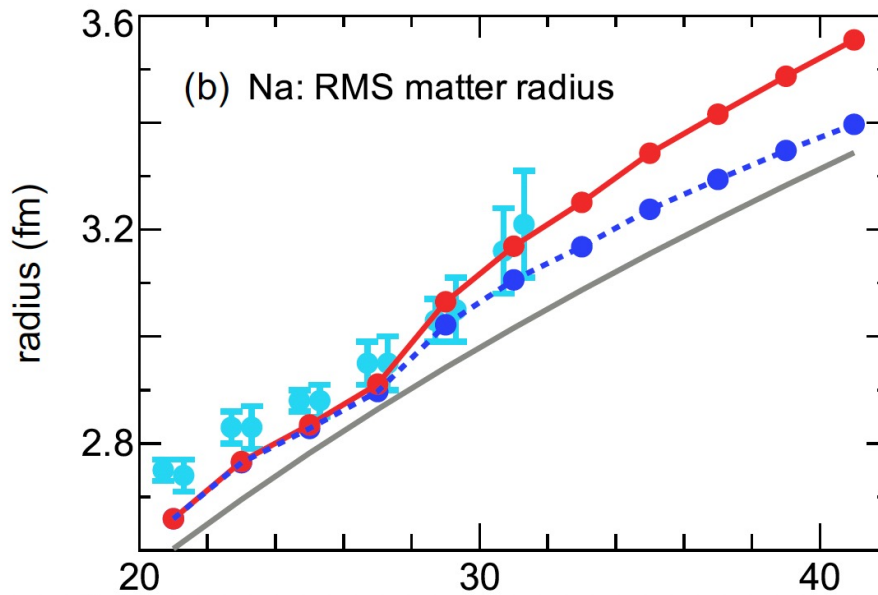
● ● exp

I. Angelo and K. P. Marinova, *At. Data Nucl. Data Tab.* **99**, 69 (2013).

B. Ohayon, R. F. Garcia Ruiz, Z. H. Sun, G. Hagen, T. Papenbrock,4 and B. K. Sahoo, *arXiv:2019.10539v1*.

● — present calc.

— Droplet model



● ● exp

from the interaction cross section

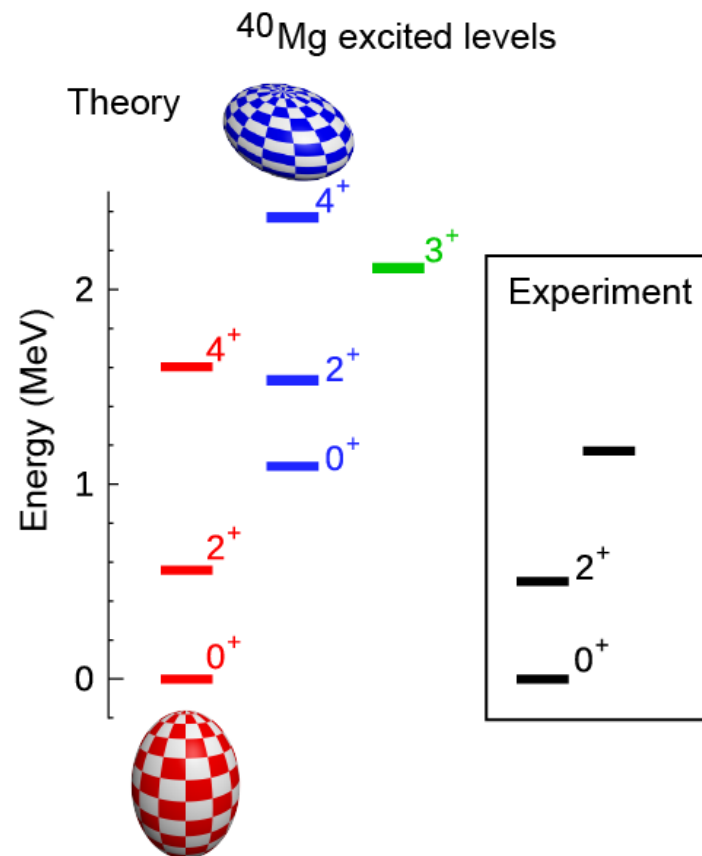
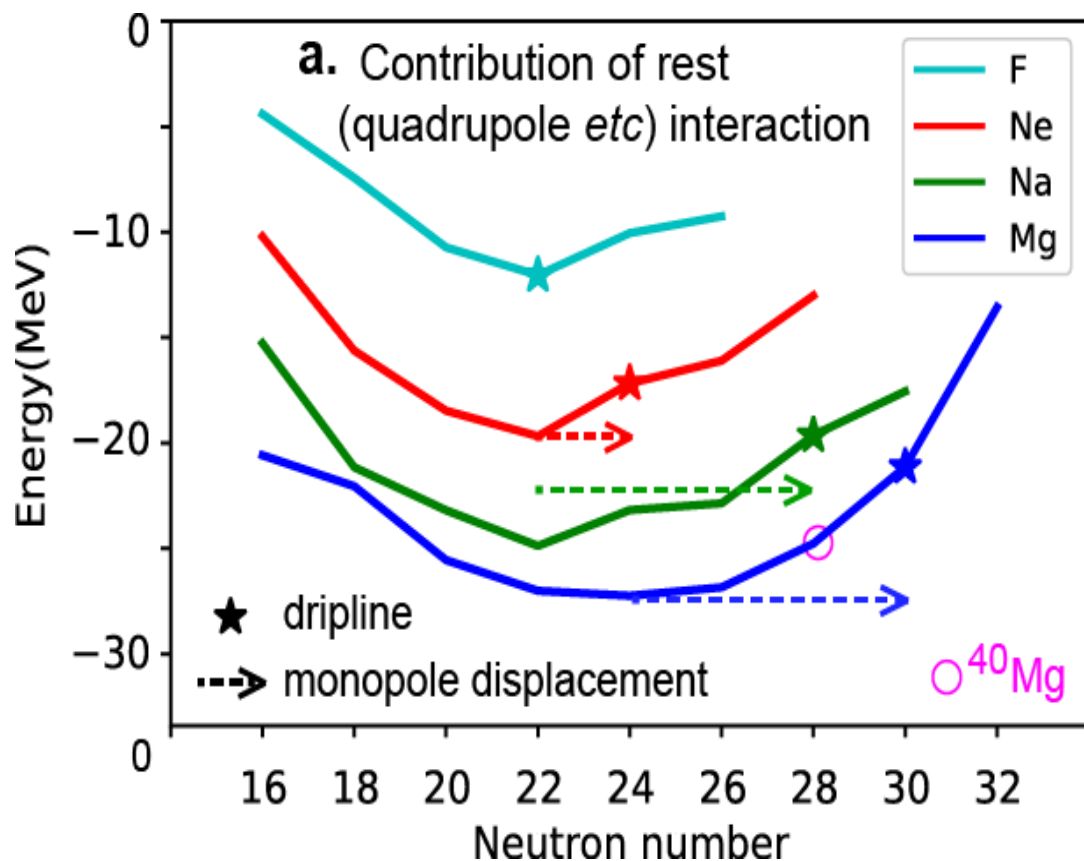
T. Suzuki *et al.*, *Nucl. Phys. A* **630**, 661 (1998).

● — calc. (full)

● - - - calc.

— Droplet model

Validity of the EEdf1 interaction : still “yes” at ^{40}Mg



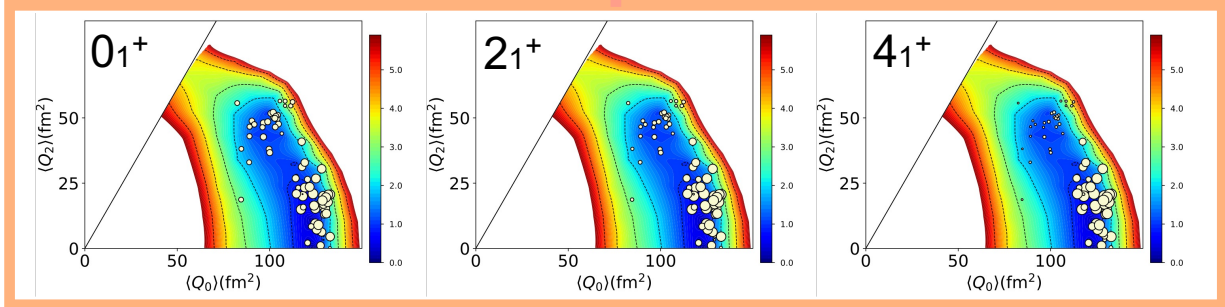
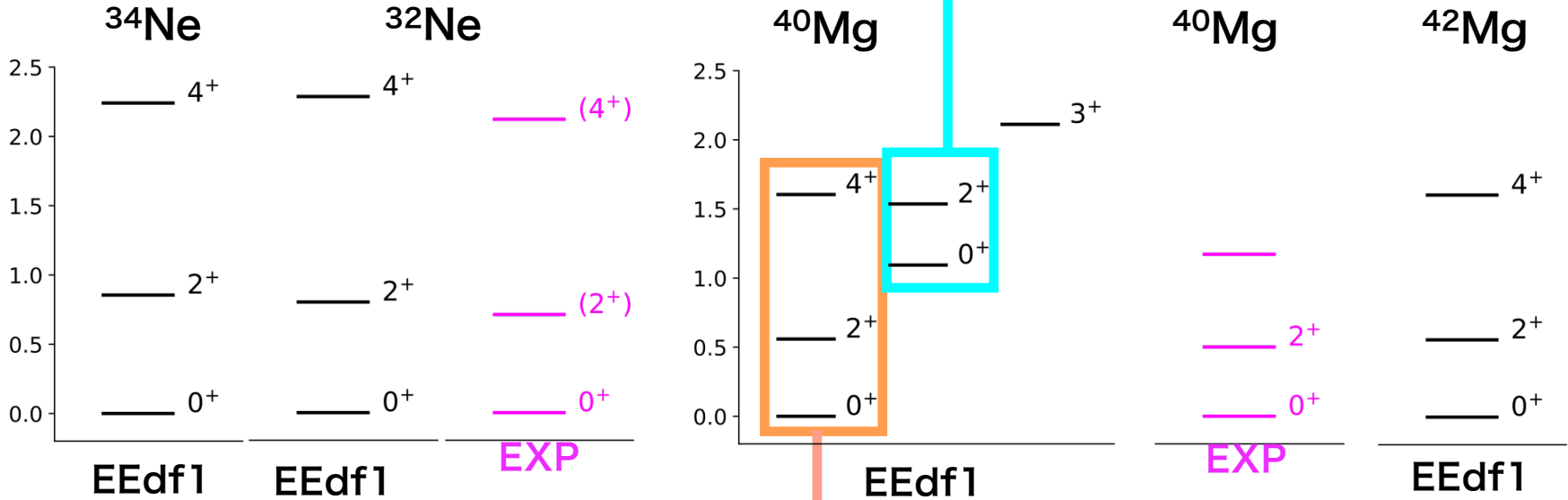
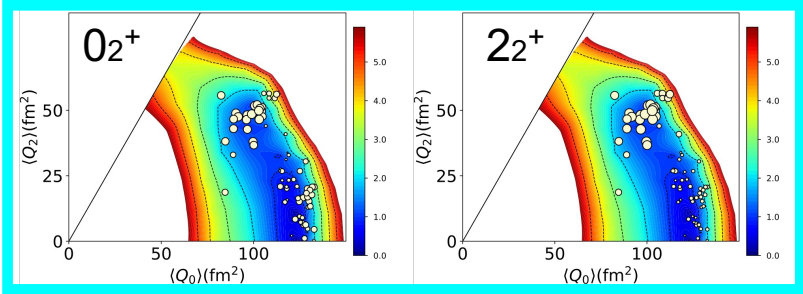
PHYSICAL REVIEW LETTERS 122, 052501 (2019)

Editors' Suggestion

First Spectroscopy of the Near Drip-line Nucleus ^{40}Mg

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Shape coexistence near dripline



N=28 gap is not working

Summary

0. Correlation energies are crucial to driplines. Perhaps unexpected from the viewpoint of mass formulas.
1. There are, at least, two dripline mechanisms:
one with a single-particle origin, while the other due to the interplay between the monopole and quadrupole (deformation) effects.
2. The driplines of F, Ne, Na and Mg isotopes follow the new mechanism. Two mechanisms may appear alternatively for Z larger.
3. Those isotopes are described well by the EEdf1 interaction derived by the EKK method from the chiral EFT interaction.
4. Monopole effects per ΔN depends on # of valence protons:
in exotic region, \sim none for F, ..., -3 MeV for Mg. \rightarrow makes F unique.
Without the monopole effect, F, Ne and Na would have the same dripline. Virtually all these nuclei show large triaxial shapes.
5. These isotopes remain deformed up to dripline, and have intruder ground states with $d_{3/2}$ half occupied; not an “*island*”.
6. Magnetic moments of the ground states of Na isotopes are described well without the quenching of the spin g factor (g_s).
Deformation parameters are deduced, and charge radius is estimated.

THANK YOU

ご清聴ありがとうございました