



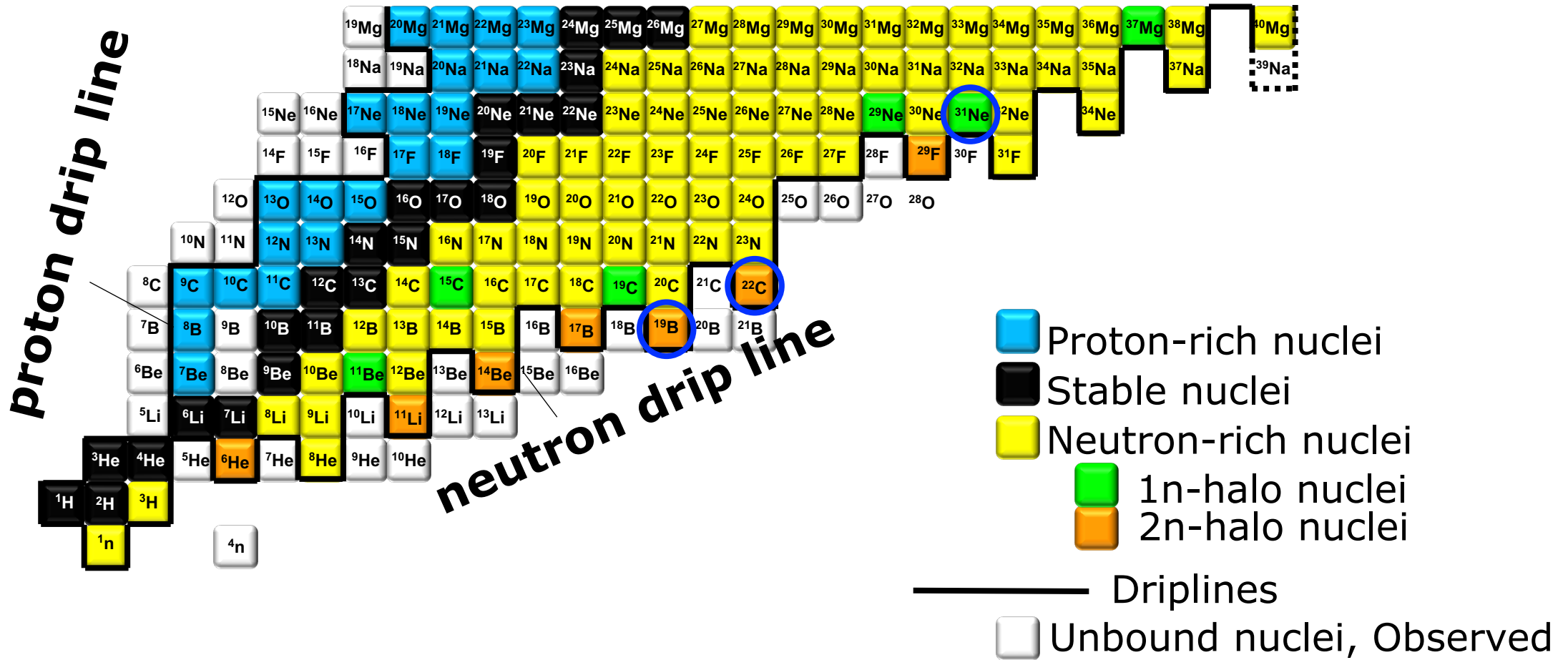
Spectroscopy of neutron dripline nuclei

Takashi Nakamura
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- Introduction
- Halo-Shell Interplay— ^{31}Ne
 - Coulomb breakup and double-halo components of ^{31}Ne
 - Low-lying resonances in ^{31}Ne
- Two-neutron halo— $^{19}\text{B}/^{22}\text{C}$
 - Coulomb breakup of ^{19}B and neutron-halo structure
 - Coulomb breakup of ^{22}C and neutron-halo structure
- Summary

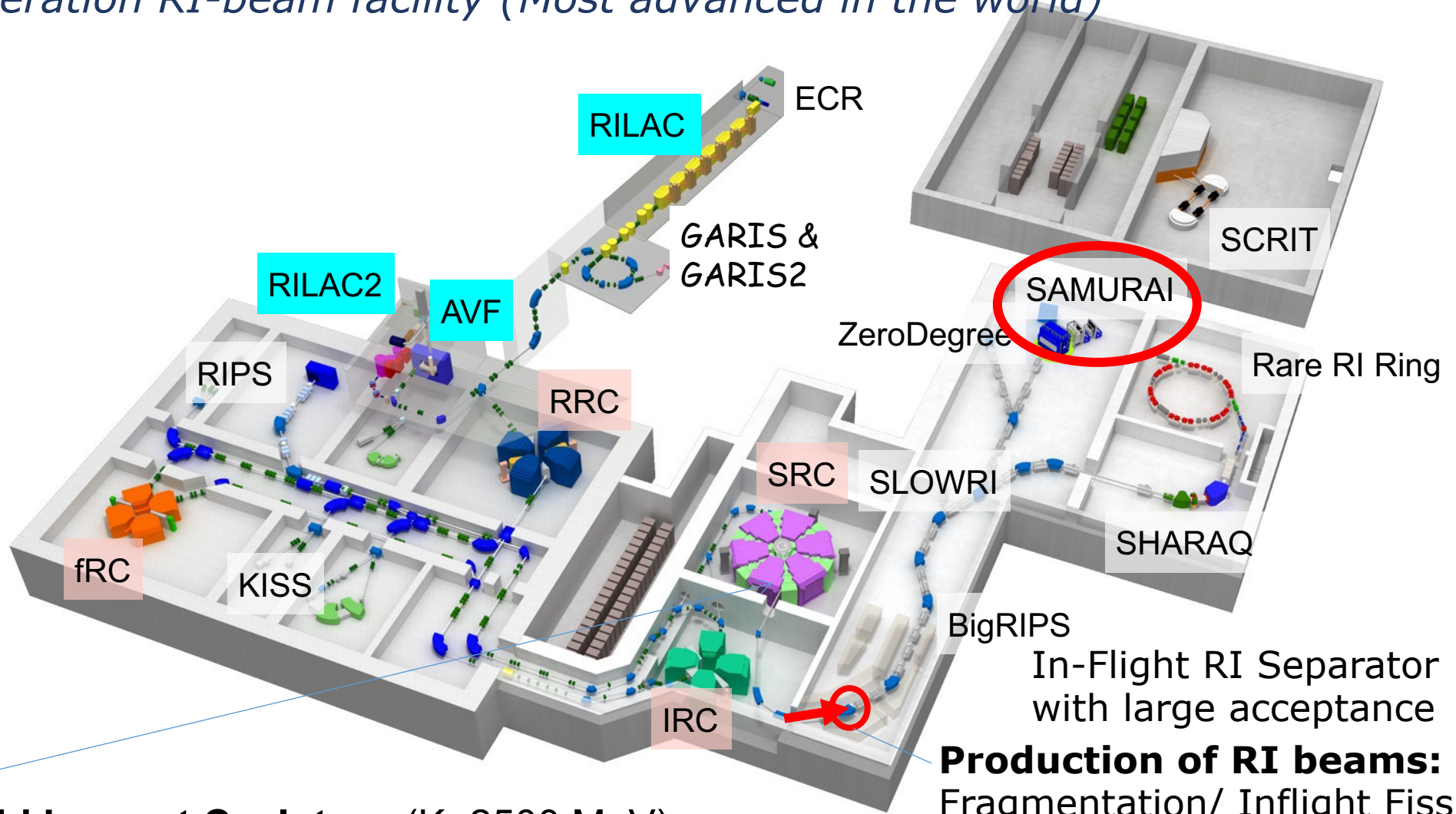
Nuclear Landscape at the limit

Dripline— Boundary of Closed/Open quantum systems
 → Clusters/Halo/Shell Evolution



RI Beam Factory (RIBF) at RIKEN 2007~

The 3rd-generation RI-beam facility (Most advanced in the world)



SRC: World Largest Cyclotron (K=2500 MeV)

High-Intense Heavy Ion Beams up to ^{238}U at 345MeV/u

eg. ^{48}Ca : ~700pA (~ 4×10^{12} pps) ~10 times compared to 2008

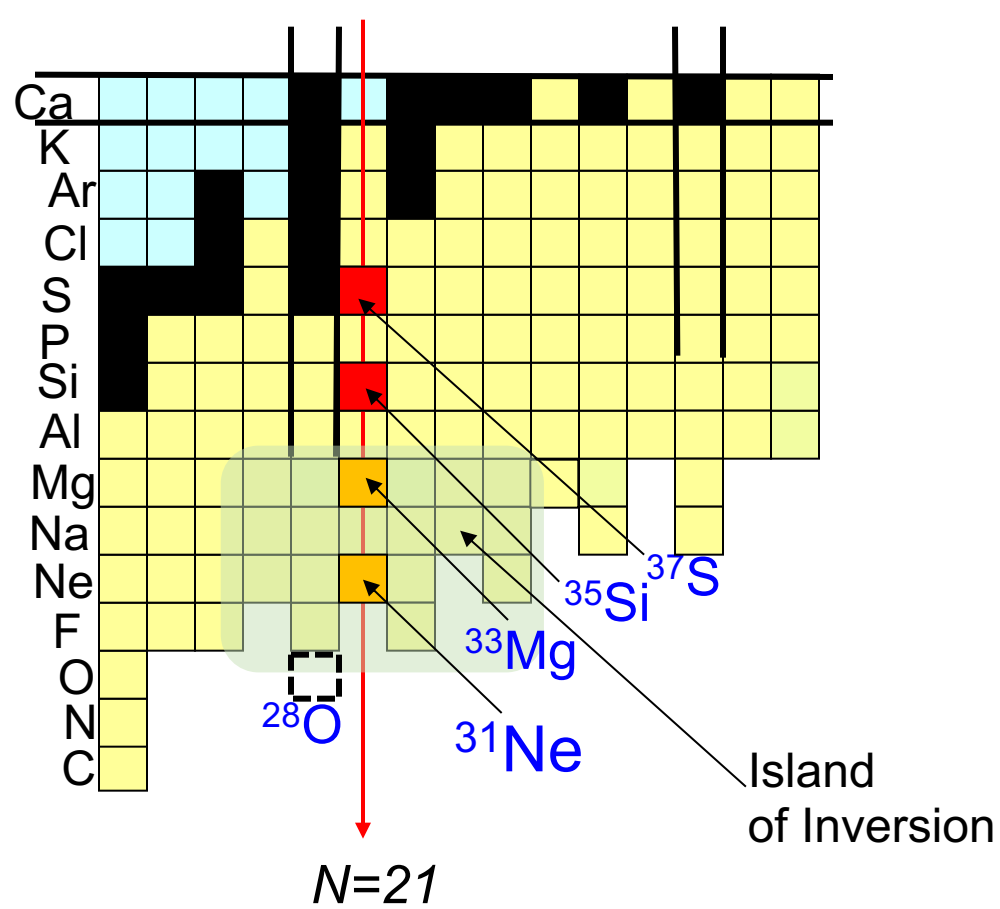
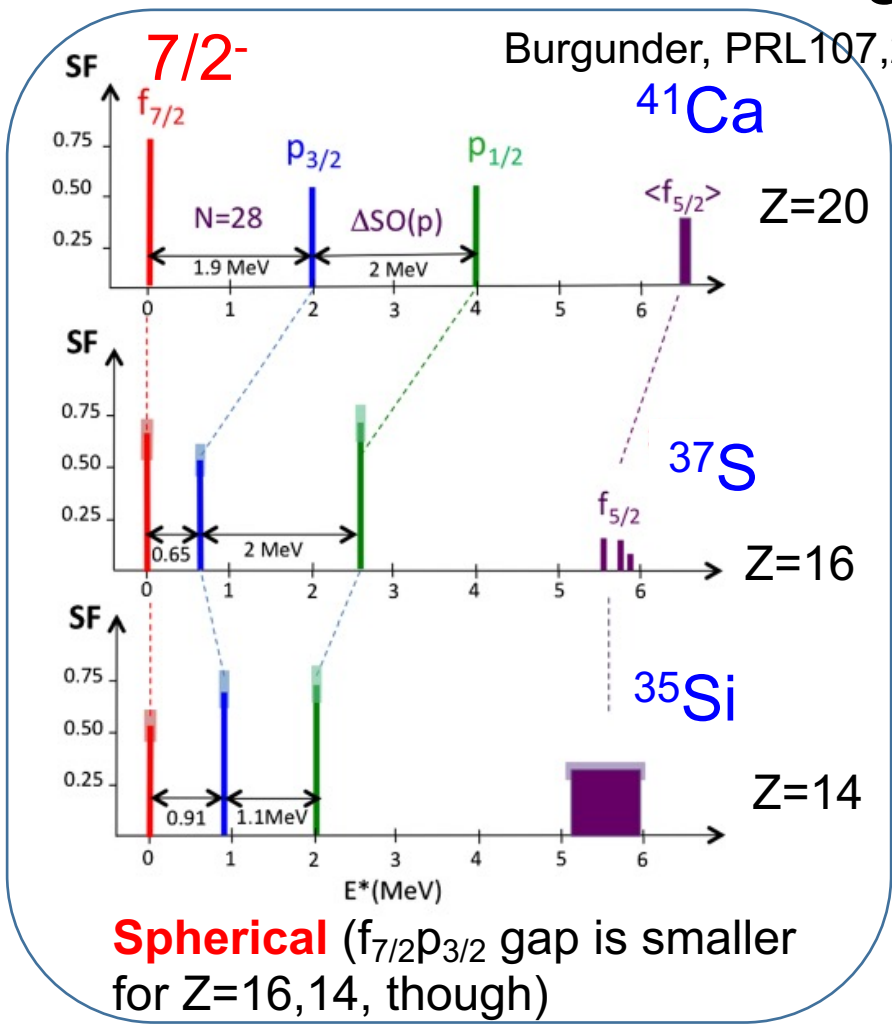
^{238}U : ~100pA (~ 6×10^{11} pps) ~ 10^3 times compared to 2007

Production of RI beams:
Fragmentation/ Inflight Fission

● Halo-Shell Interplay -- ^{31}Ne

[T. Tomai, et al.](#)

Shell Evolution along N=21



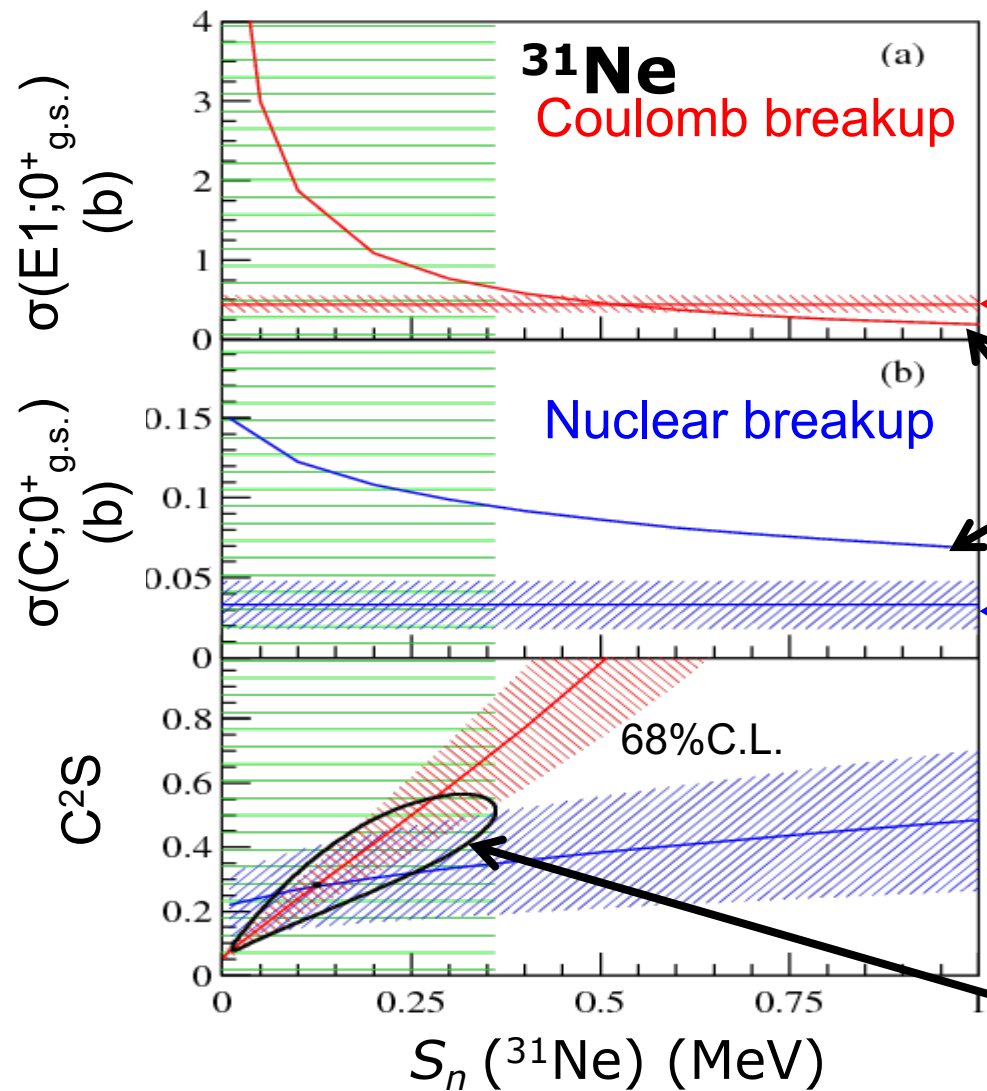
^{33}Mg gs: $3/2^-$ $Z=12$
 ^{31}Ne gs: $3/2^-$ $Z=10$
Deformed: Island of inversion

Both $N=20$, $N=28$ Shell gaps: LOST!

^{33}Mg : R.Kanungo PLB685, 253 (2010).
 D.Bazin PRC103, 064318 (2021).
 ^{31}Ne : TN, N.Kobayashi et al., PRL103,262501(2009),
 PRL112, 142501(2014)

Previous work: **Inclusive** Coulomb/nuclear breakup of ^{31}Ne ($\rightarrow ^{30}\text{Ne}+X+(\gamma)$)

TN, N.Kobayashi et al., PRL **112**, 142501 (2014).



$|^{31}\text{Ne}_{\text{g.s.}}\rangle : 3/2^- \quad |^{30}\text{Ne}(0^+_{\text{g.s.}}) \otimes p_{3/2}\rangle$ component

← Exp. $\sigma_{-1n}(E1; 0^+_{\text{g.s.}}) = 448(108)$ mb

Theoretical calc. for
 $|^{31}\text{Ne}_{\text{g.s.}}\rangle = |^{30}\text{Ne}(0^+_{\text{g.s.}}) \otimes p_{3/2}\rangle \quad (C^2S = 1)$

← Exp. $\sigma_{-1n}(C; 0^+_{\text{g.s.}}) = 33(15)$ mb

^{31}Ne : **$3/2^-$** **p-wave halo**
Deformed in spite of **$N=21$**

$C^2S = 0.32^{+0.21}_{-0.17}$

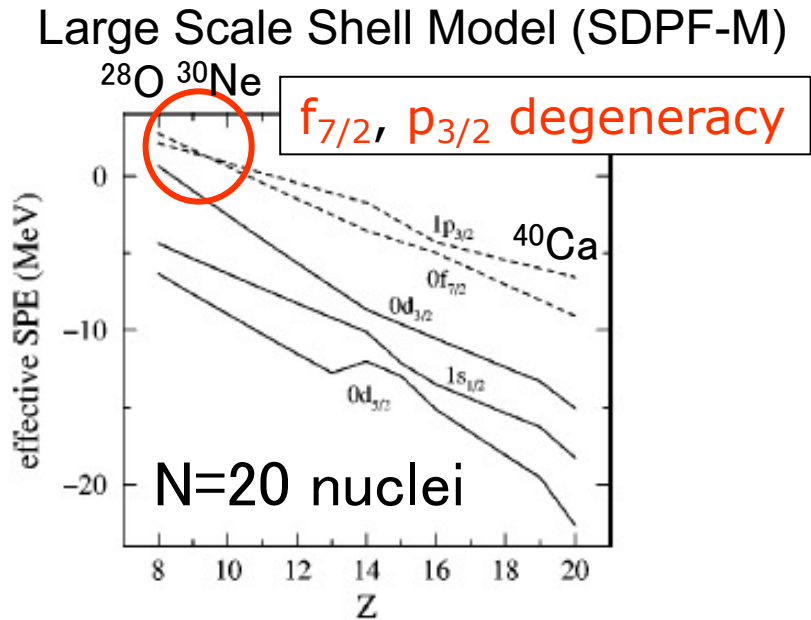
$S_n = 0.15^{+0.16}_{-0.10}$ MeV

$S_n(^{31}\text{Ne}) = -0.06(0.42)$ MeV L.Gaudefroy et al., PRL(2012)

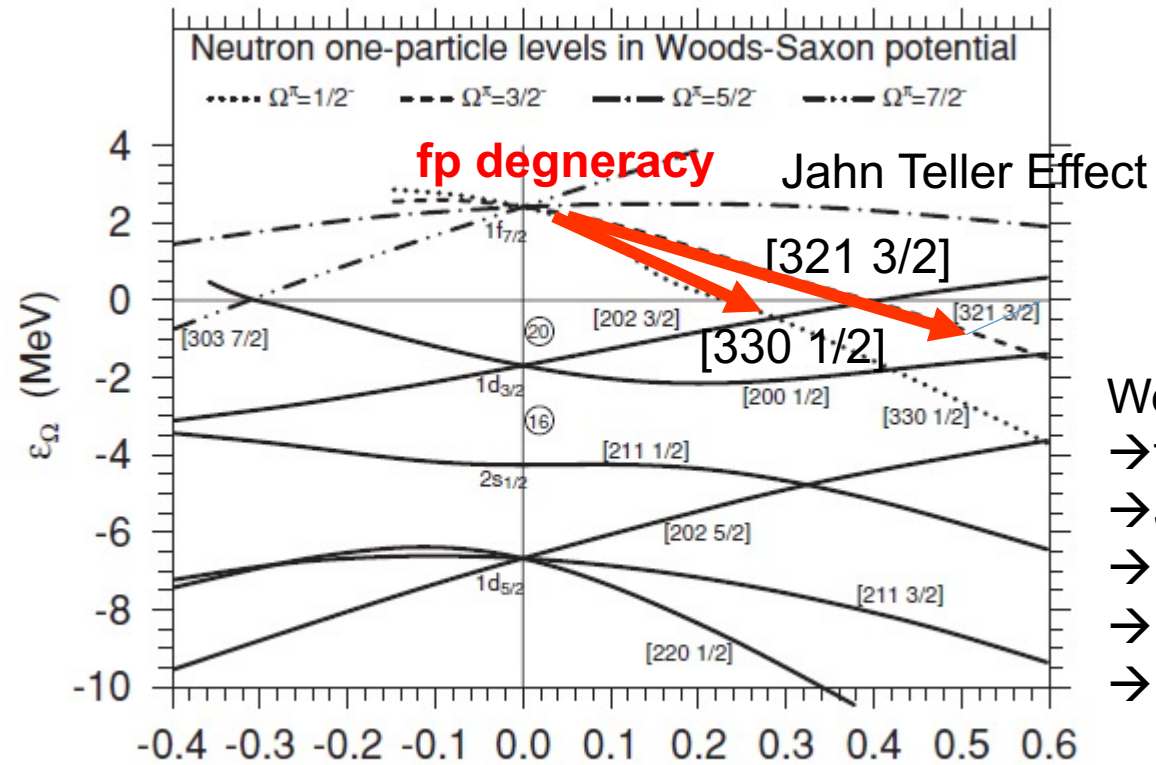
^{37}Mg : N.Kobayashi, TN et al., PRL **112**, 242501 (2014). $3/2^-/1/2^-$ $S_n = 220(12)$ keV

^{29}Ne : N.Kobayashi, TN et al., PRC **93**, 014613 (2016). $3/2^-$ $S_n = 960(140)$ keV

Deformation Driven p-wave Halo nucleus ^{31}Ne



Y.Utsuno, T.Otsuka et al.
PRC 054315 (1999).



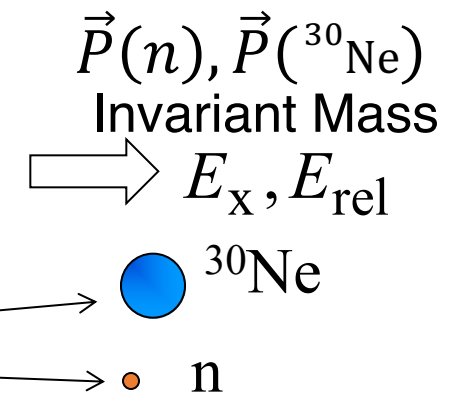
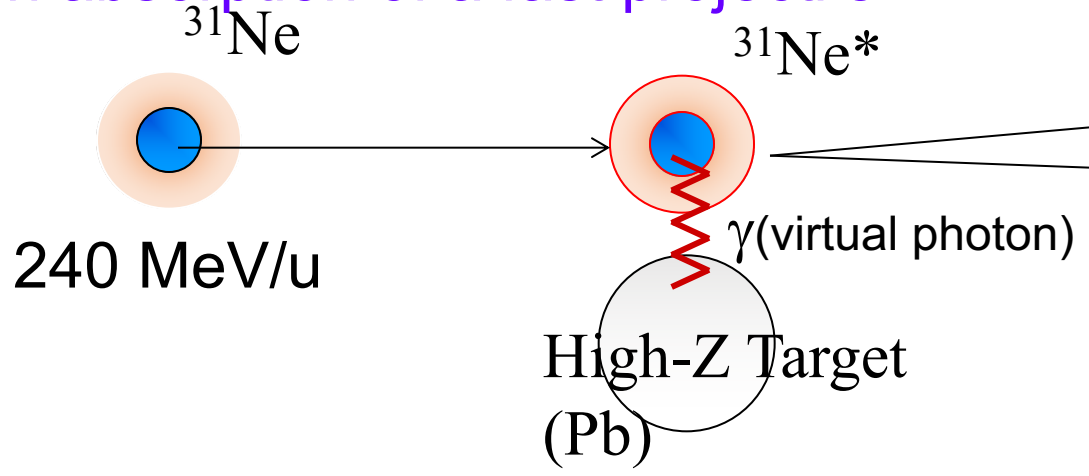
Weakly-bound effect
 → fp degeneracy
 → Jahn Teller effect
 → Strongly deformed
 → pf mixed, p enhanced
 → Halo developed

I.Hamamoto PRC 81, 021304(R) (2010)
 I.Hamamoto PRC 85, 064329 (2012)

How deformed quantitatively?, [330 1/2] or [321 3/2]?,
 Shell Structure of halo nuclei (Weakly-bound/continuum effects)?
 What is the mechanism of fp degeneracy?

Exclusive Coulomb Breakup

→ Photon absorption of a fast projectile



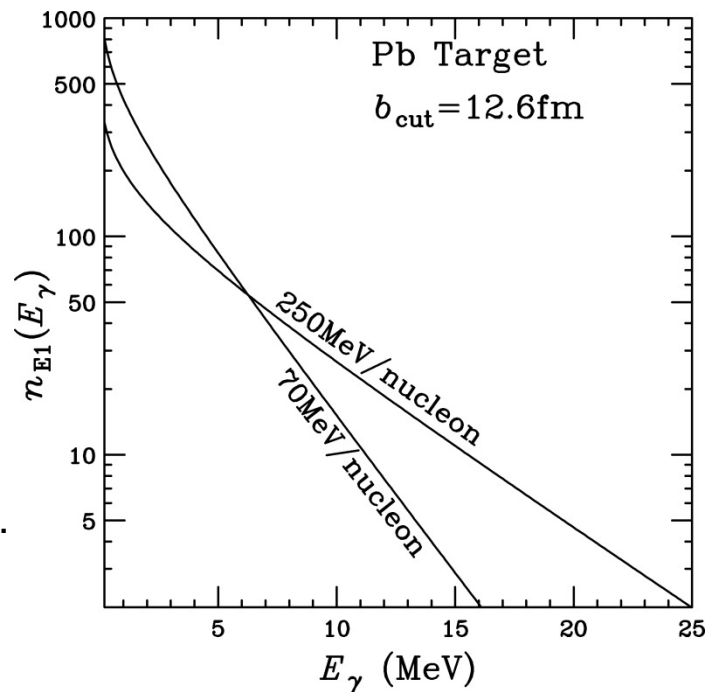
Equivalent Photon Method

$$\frac{d\sigma_{CB}}{dE_x} = \frac{16\pi^3}{9\hbar c} N_{E1}(E_x) \frac{dB(E1)}{dE_x}$$

Cross section = (Photon Number) x (Transition Probability)

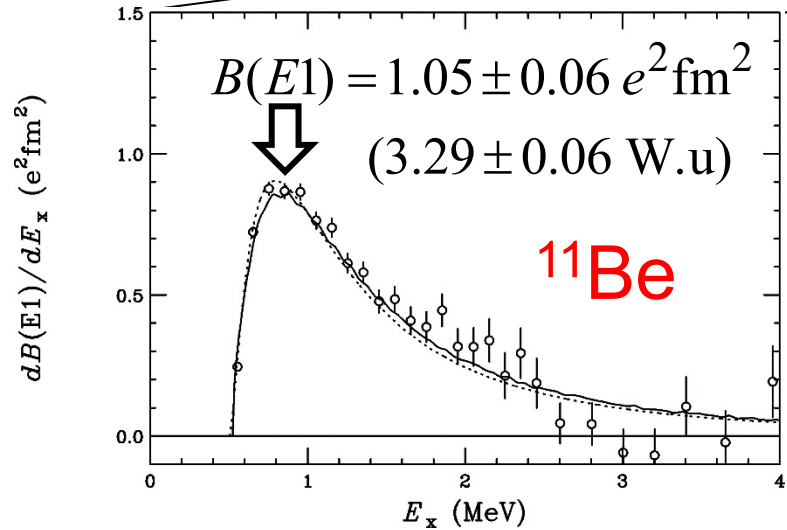
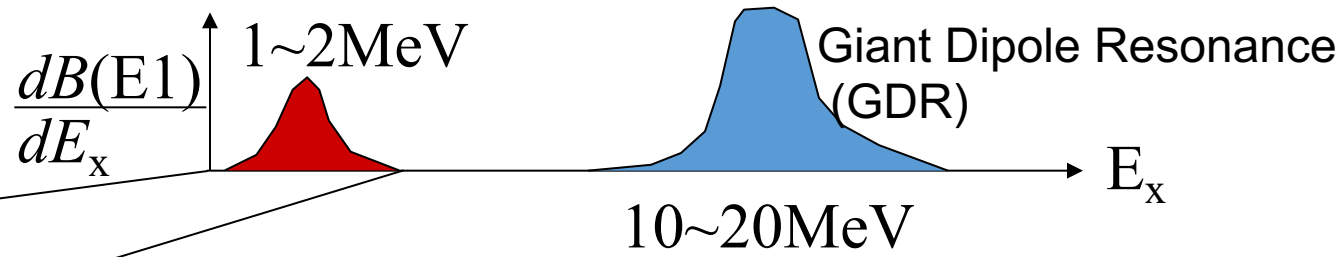
C.A. Bertulani, G. Baur, Phys. Rep. **163**, 299(1988).
 T. Aumann, T. Nakamura, Phys. Scr. T**152**, 014142(2013).

Halo → Soft E1 Excitation
 (E1 Concentration at $E_x < 1\text{MeV}$)

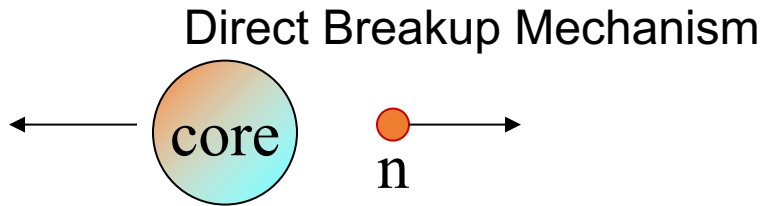


Coulomb Breakup and E1 Response--Case of 1n Halo

Low-lying E1 Strength (Soft E1 excitation)



N.Fukuda, TN et al., PRC70, 054606 (2004)
 TN et al., PLB 331, 296 (1994)
 Palit et al., PRC68, 034318 (2003)

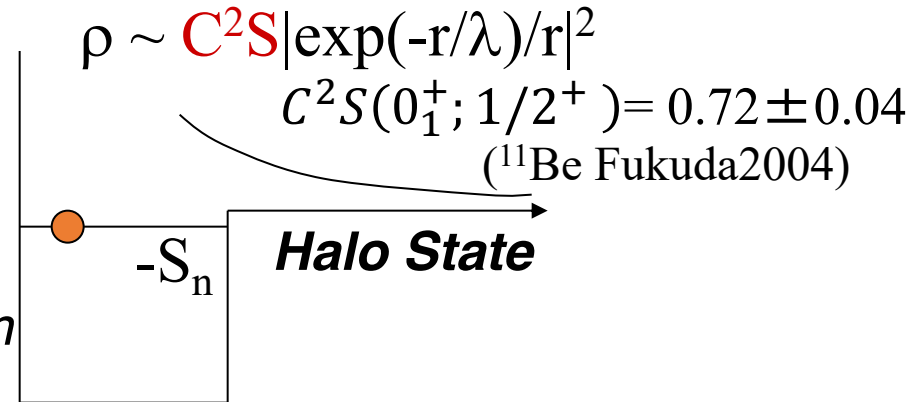


E1 Strength

$$\frac{dB(E1)}{dE_x} \propto \left| \langle \exp(iqr) \left| \frac{Z}{A} r Y^1_m \right| \Phi_{gs} \rangle \right|^2$$

$$\propto C^2S \left| \langle \exp(iqr) \left| \frac{Z}{A} r Y^1_m \right| s_{1/2} \rangle \right|^2$$

Fourier Transform



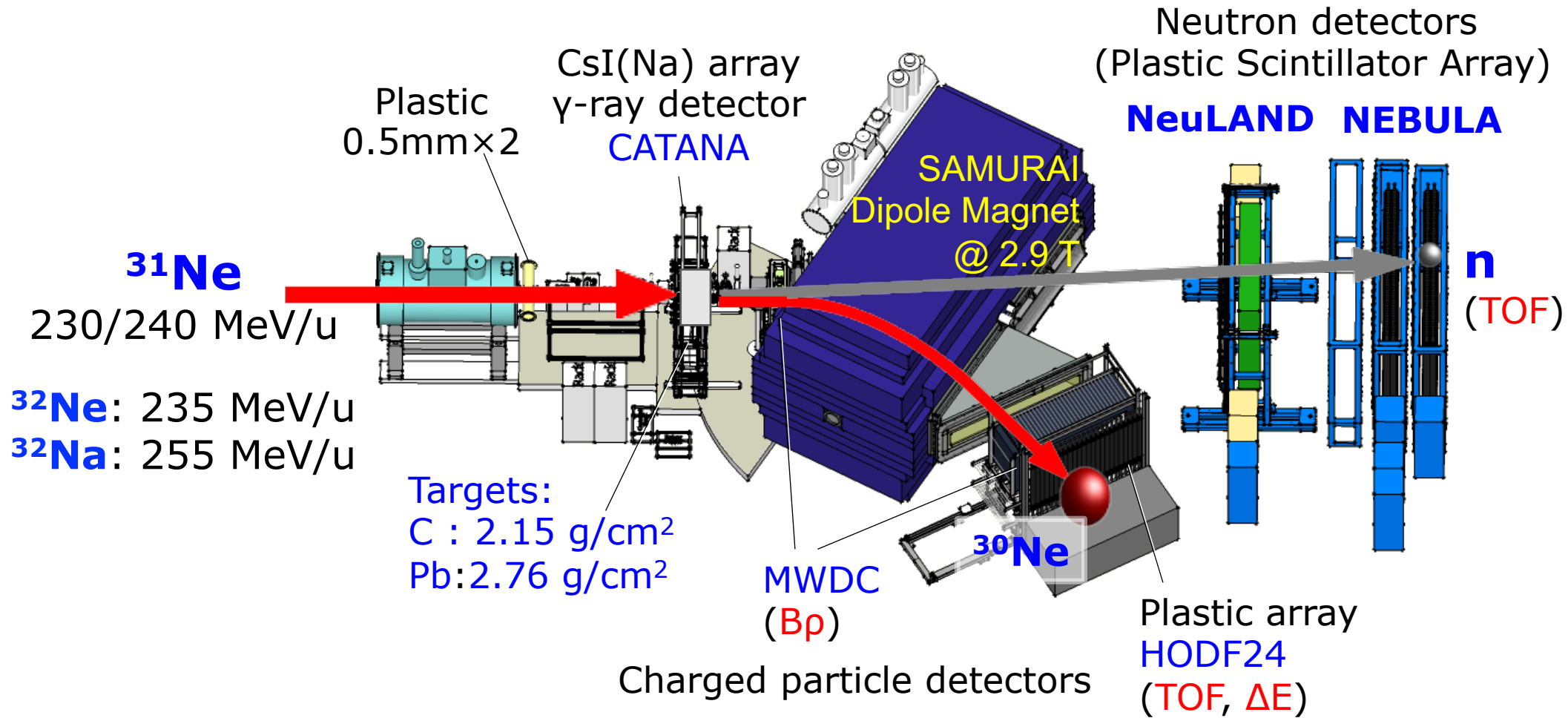
Soft E1 Excitation of 1n halo—Sensitive to S_n, l, C^2S

e.g. Peak Energy

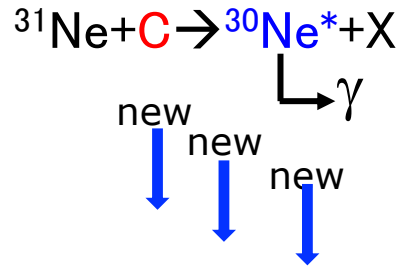
s-wave halo: $E_{rel}^{(peak)} \cong \frac{3}{5} S_n$

p-wave halo (p → s): $E_{rel}^{(peak)} \cong 0.18 S_n$

Full **Exclusive** Coulomb Breakup Measurement of ^{31}Ne T.Tomai et al.



γ -ray spectrum : Excited-core component



$$|{}^{31}\text{Ne}(3/2^-) \rangle = \alpha |{}^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \rangle + \beta |{}^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2} \rangle + \dots$$

	$\sigma_{\text{CB}}({}^{30}\text{Ne}+n)$ [mb]
Coulomb breakup	Integral $E_{\text{rel}}=0-5\text{MeV}$
${}^{31}\text{Ne} \rightarrow {}^{30}\text{Ne}(\text{total})$	
${}^{31}\text{Ne} \rightarrow {}^{30}\text{Ne}(0^+)$	
${}^{31}\text{Ne} \rightarrow {}^{30}\text{Ne}(2^+)$	
Ratio($0^+ : 2^+$)	

Coulomb breakup of ^{31}Ne : Energy Spectrum

Preliminary

$d\sigma_{\text{CD}}/dE_{\text{rel}}$ (mb/MeV)

Total

$^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2}$

$^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2}$

E_{rel} (MeV)

Preliminary

$^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2}$

$^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2}$

	S_n (MeV)	$C^2S(0_1^+; 3/2^-)$	$C^2S(2_1^+; 3/2^-)$
This work			
Prev. work*	$0.15^{+0.16}_{-0.10}$	$0.32^{+0.21}_{-0.17}$	-
SM(SDPF-M)		0.21	0.34

*TN, N. Kobayashi et al., PRL**112**, 142501 (2014).

$$|^{31}\text{Ne}(3/2^-) \rangle = \alpha |^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \rangle + \beta |^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2} \rangle$$

$$\alpha^2 = C^2S(0_1^+; 3/2^-) \quad \beta^2 = C^2S(2_1^+; 3/2^-)$$

Double-Component Halo

$$|^{31}\text{Ne}(3/2^-) \rangle = \alpha |^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \rangle + \beta |^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2} \rangle$$

Double-Component Halo:

- ✓ Unique feature of **p-wave halo**
(Single-component for s-wave halo)
- ✓ Coupled to **Rotation** → **Deformed halo**

Amplitude ratio of 0^+ , 2^+
With Particle Rotor Model (PRM)
→ Quadrupole deformation

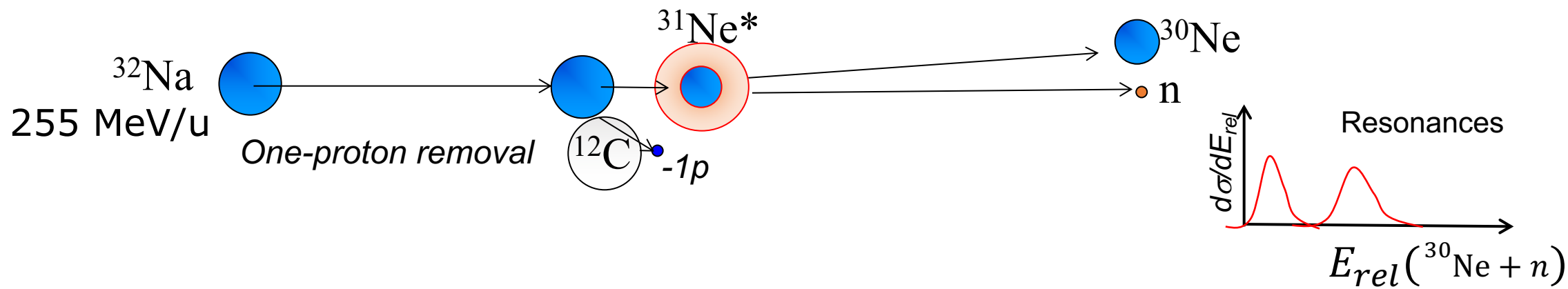
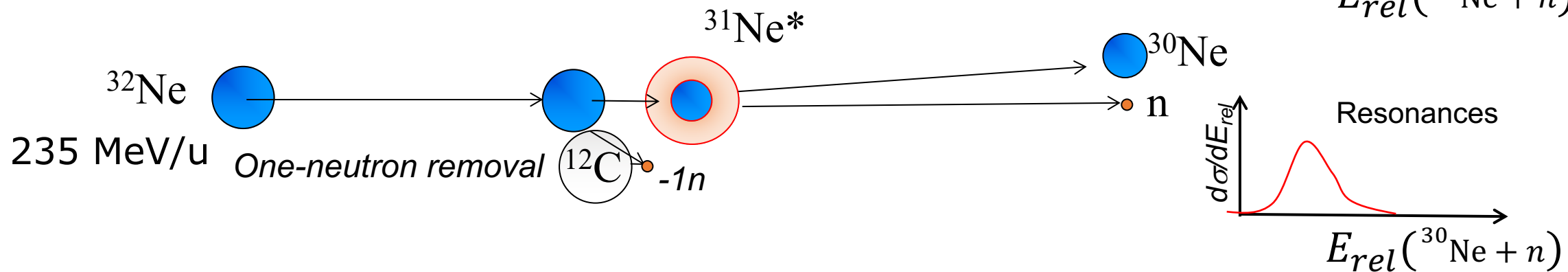
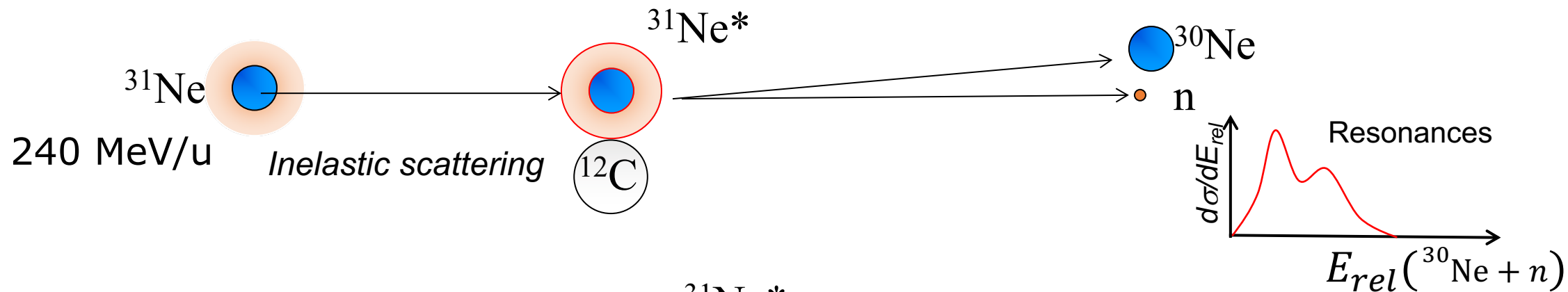
→ $\beta \sim 0.2 - 0.6$

➤ PRM Calculation for $S_n = 0.3$ MeV

β_2	$[0^+ \otimes p_{3/2}]$	$[2^+ \otimes p_{3/2}]$	$[2^+ \otimes p_{1/2}]$
0.1	0%	6.5%	0%
0.2	44.9%	8.4%	2.0%
0.55	1.9%	29.7%	4.4%

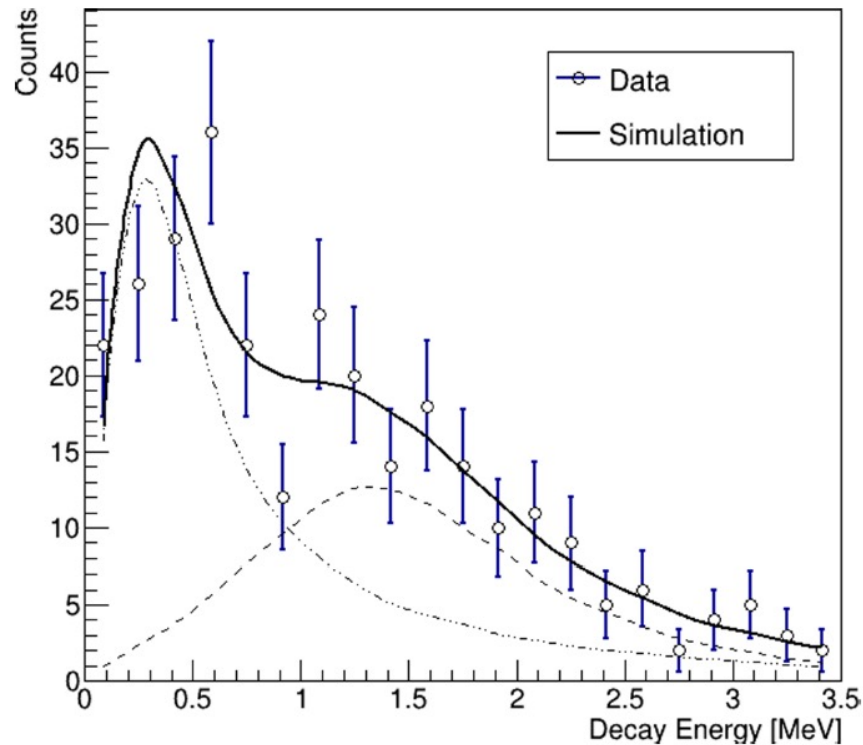
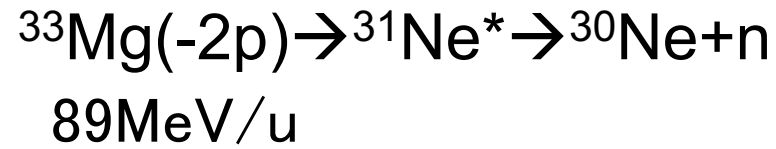
c.f. ^{11}Be : $\sqrt{\langle r^2 \rangle} = 5.77 \pm 0.16$ fm
N.Fukuda PRC70, 054606 (2004).

Exclusive Nuclear Breakup



Previous Work: @MSU

D. Chrisman et al., PRC 104, 034313 (2021)



$$E_{rel} = 0.30(17), 1.50(33)\text{MeV}$$

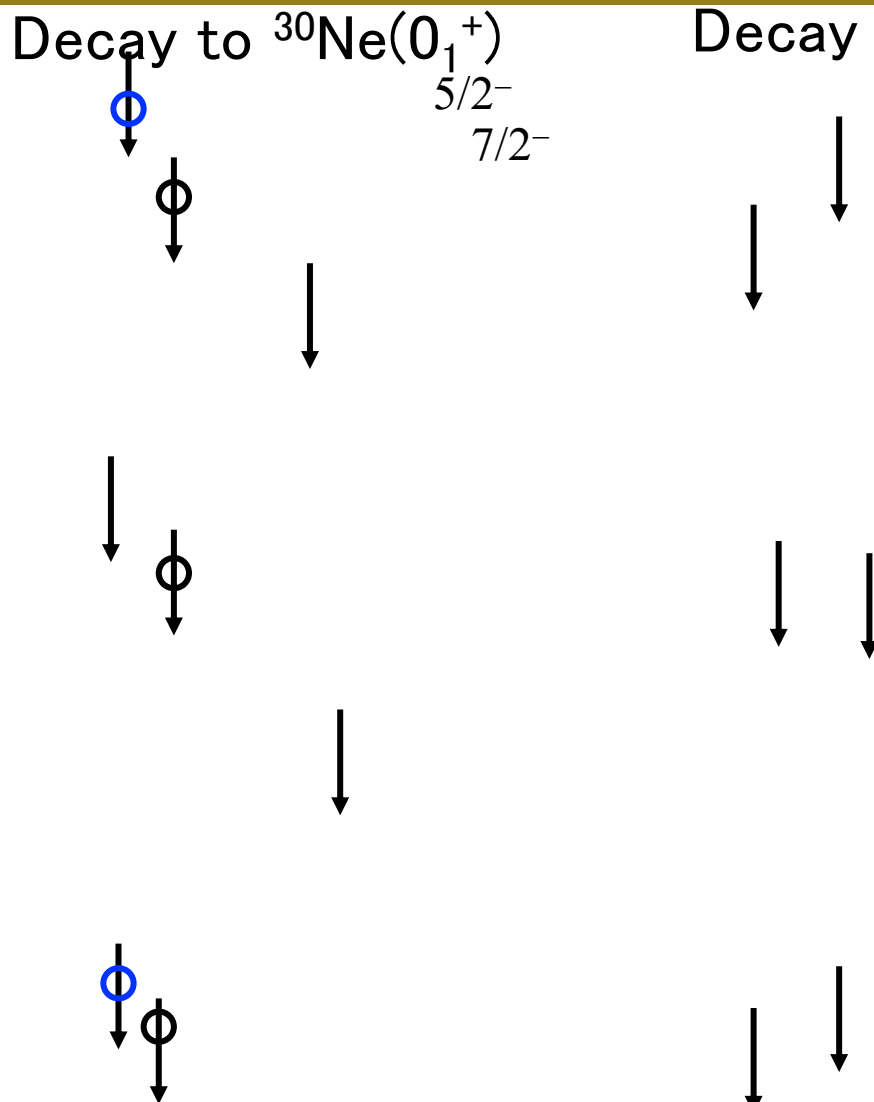
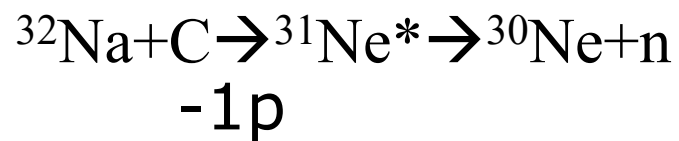
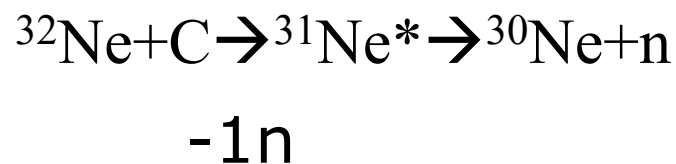
No γ coincidence measurement done

Results

Preliminary

Decay to $^{30}\text{Ne}(0_1^+)$
 $5/2^-$
 $7/2^-$

Decay to $^{30}\text{Ne}(2_1^+)$
 ($E_\gamma=792\text{keV}$ coincidence)

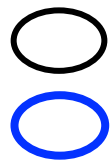


In addition,
 Observed
 resonances
 decay to $^{30}\text{Ne}(4^+)$

^{31}Ne Levels observed by ^{31}Ne , ^{32}Ne , ^{32}Na induced reactions



Preliminary



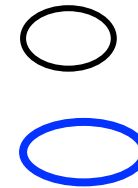
$3/2^-$

Inelastic



$3/2^-$

$^{32}\text{Ne} - 1n$



$3/2^-$

$^{32}\text{Na} - 1p$

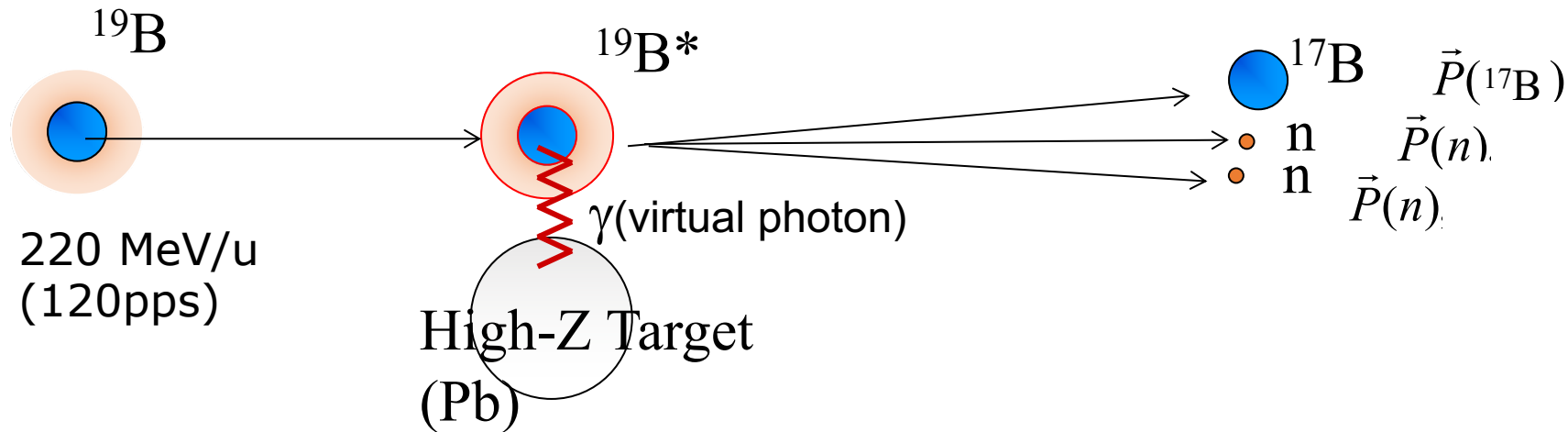
Two-neutron halo— $^{19}\text{B}/^{22}\text{C}$

Coulomb breakup of ^{19}B : K.J. Cook et al., PRL2020

Coulomb breakup of ^{22}C : N. Nakatsuka et al., in preparation

Coulomb Breakup of ^{19}B


K. J. Cook, TN et al. PRL124, 212503, 2020



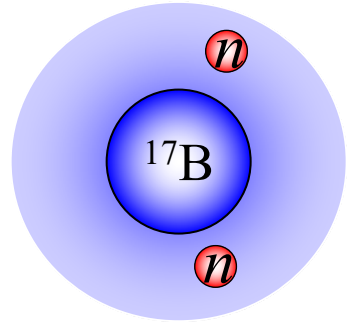
PHYSICAL REVIEW LETTERS **124**, 212503 (2020)

Editors' Suggestion

Halo Structure of the Neutron-Dripline Nucleus ^{19}B

K. J. Cook ^{1,*}, T. Nakamura,¹ Y. Kondo,¹ K. Hagino,² K. Ogata,^{3,4} A. T. Saito,¹ N. L. Achouri,⁵ T. Aumann,^{6,7} H. Baba,⁸ F. Delaunay,⁵ Q. Deshayes,⁵ P. Doornenbal,⁸ N. Fukuda,⁸ J. Gibelin,⁵ J. W. Hwang,⁹ N. Inabe,⁸ T. Isobe,⁸ D. Kameda,⁸ D. Kanno,¹ S. Kim,⁹ N. Kobayashi,¹ T. Kobayashi,¹⁰ T. Kubo,⁸ S. Leblond,^{5,†} J. Lee,^{8,‡} F. M. Marqués,⁵ R. Minakata,¹ T. Motobayashi,⁸ K. Muto,¹⁰ T. Murakami,² D. Murai,¹¹ T. Nakashima,¹ N. Nakatsuka,² A. Navin,¹² S. Nishi,¹ S. Ogoshi,¹ N. A. Orr,⁵ H. Otsu,⁸ H. Sato,⁸ Y. Satou,⁹ Y. Shimizu,⁸ H. Suzuki,⁸ K. Takahashi,¹⁰ H. Takeda,⁸ S. Takeuchi,^{8,1} R. Tanaka,¹ Y. Togano,^{7,11} J. Tsubota,¹ A. G. Tuff,¹³ M. Vandebrouck,^{14,§} and K. Yoneda⁸

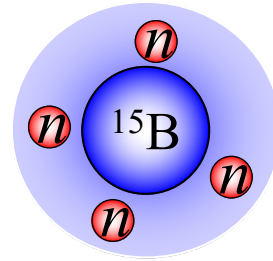
^{19}B : Two-neutron halo or Four neutron skin?



$$^{19}\text{B} = ^{17}\text{B} + 2n(\text{halo})?$$

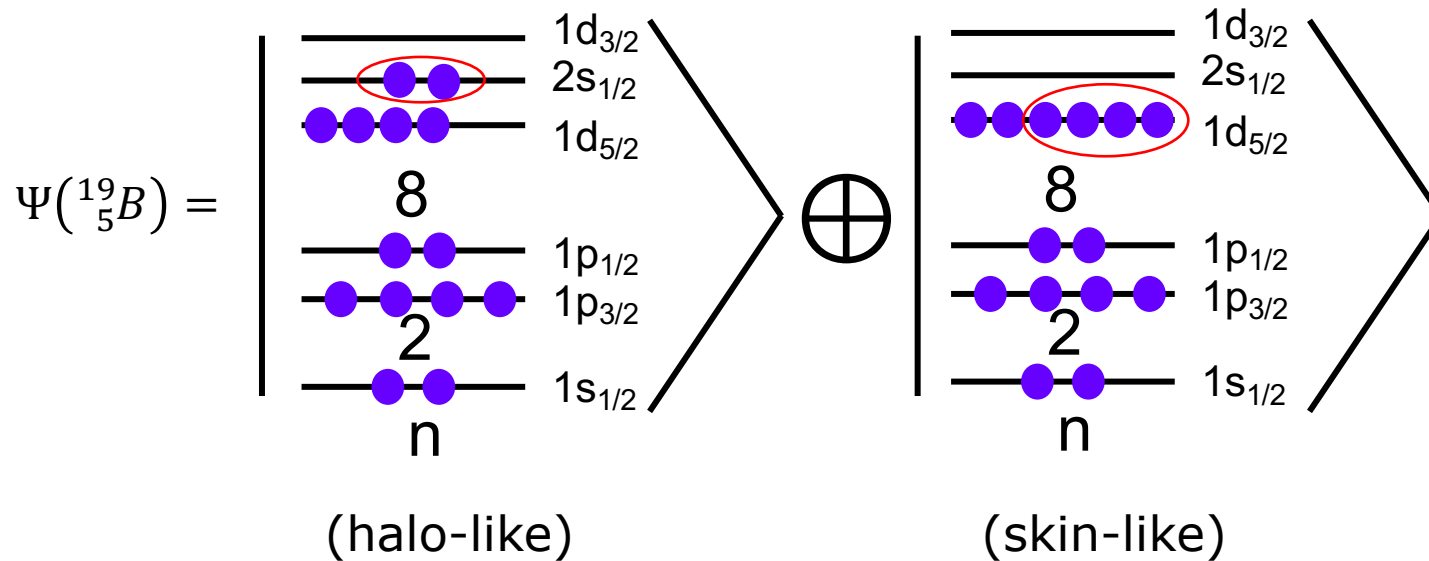
$$S_{2n} = 0.089(560) \text{ MeV}$$

Or?



$$^{19}\text{B} = ^{15}\text{B} + 4n(\text{skin})?$$

$$S_{4n} = 1.47(35) \text{ MeV}$$

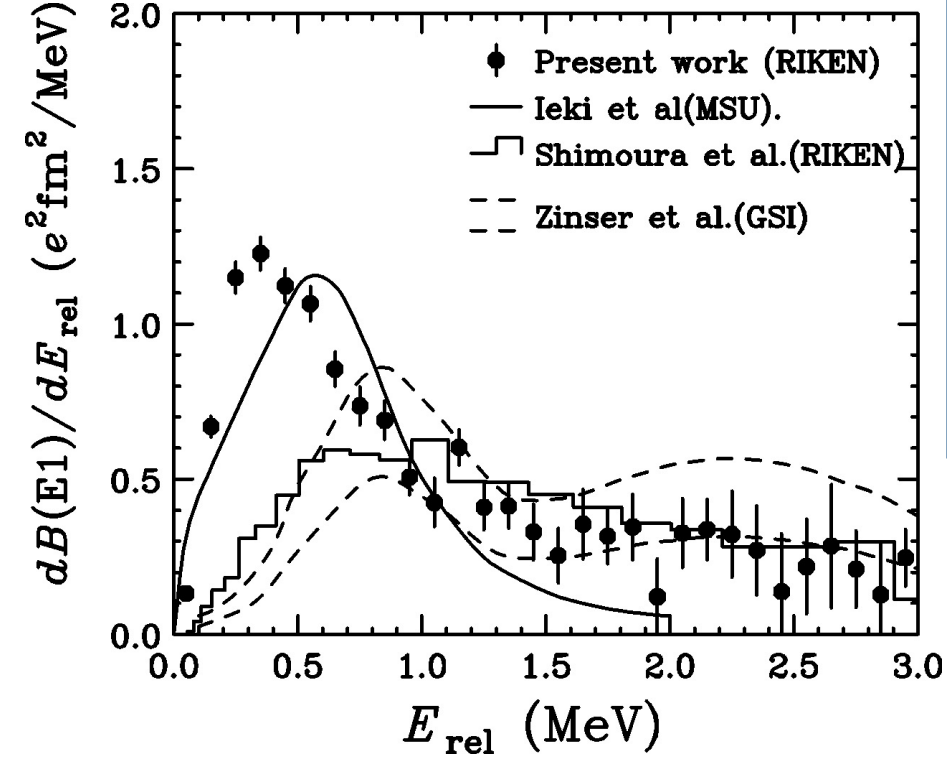


Coulomb Breakup of ^{11}Li

T. Nakamura et al. PRL96,252502(2006).

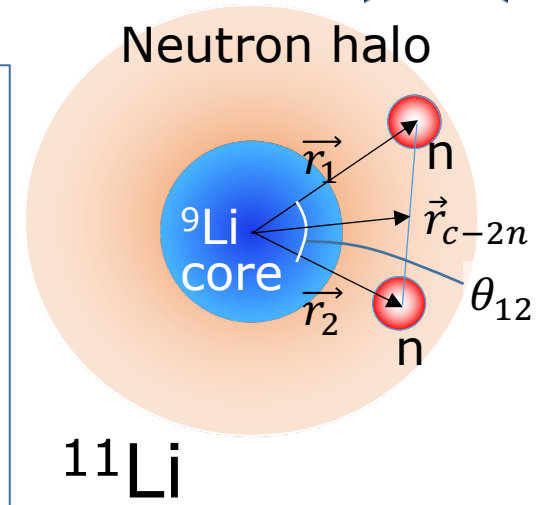


→ Probe of Dineutron Correlation



E1 Non-energy weighted cluster sum rule

$$\begin{aligned} B(E1) &= \int_{-\infty}^{\infty} \frac{dB(E1)}{dE_x} dE_x \\ &= \frac{3}{4\pi} \left(Ze \frac{2}{A} \right)^2 \langle r_{c-2n}^2 \rangle \\ &= \frac{3}{4\pi} \left(\frac{Ze}{A} \right)^2 \langle r_1^2 + r_2^2 + 2(\vec{r}_1 \cdot \vec{r}_2) \rangle \end{aligned}$$



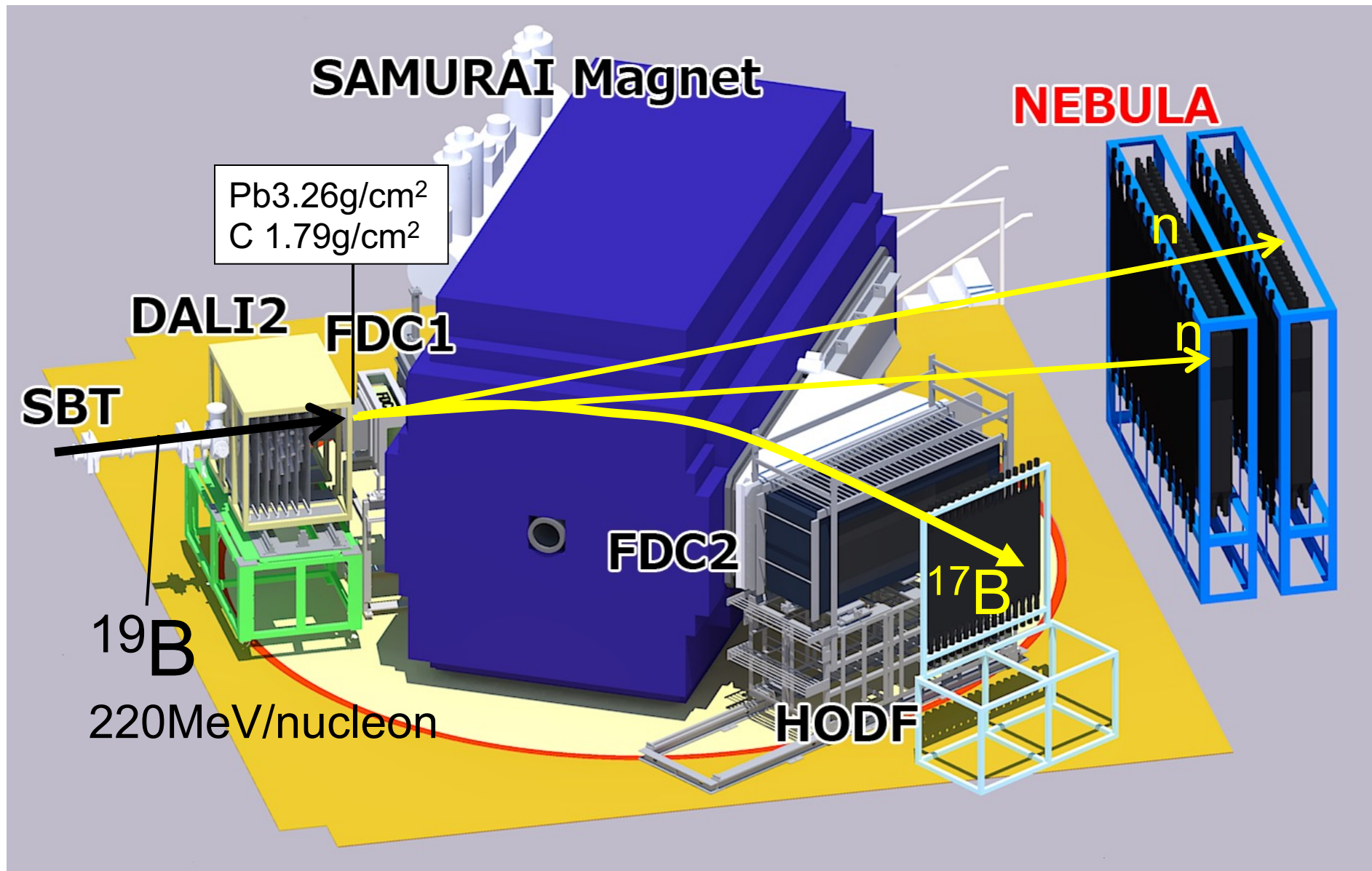
$$\begin{aligned} B(E1) &= 1.42 \pm 0.18 e^2 fm^2 (E_{rel} \leq 3\text{MeV}) \\ &\rightarrow 1.78(22) e^2 fm^2 \rightarrow \langle \theta_{12} \rangle = 48_{-18}^{+14} \text{ deg.} \end{aligned}$$

Spatial Correlation in the Ground State of ^{11}Li

Soft E1 Excitation of 2n-halo

→ dineutron correlation

Experimental Setup at SAMURAI at RIBF



	Exclusive $\sigma_{^{17}\text{B}+2n}$ (mb)	Inclusive σ_{-2n} (mb)	Inclusive σ_{-4n} (mb)
$^{19}\text{B} + \text{Pb}$	1160(30)(70)	1800(60)	600(30)
$^{19}\text{B} + \text{C}$	54(3)(3)	251(5)	185(3)
$\sigma_{\text{Pb}}/\sigma_{\text{C}}$	22(1)	7.1(3)	3.3(2)

-2n: $\sigma_{\text{Pb}} \gg \sigma_{\text{C}}$ \longrightarrow Coulomb Breakup Dominant in -2n channel

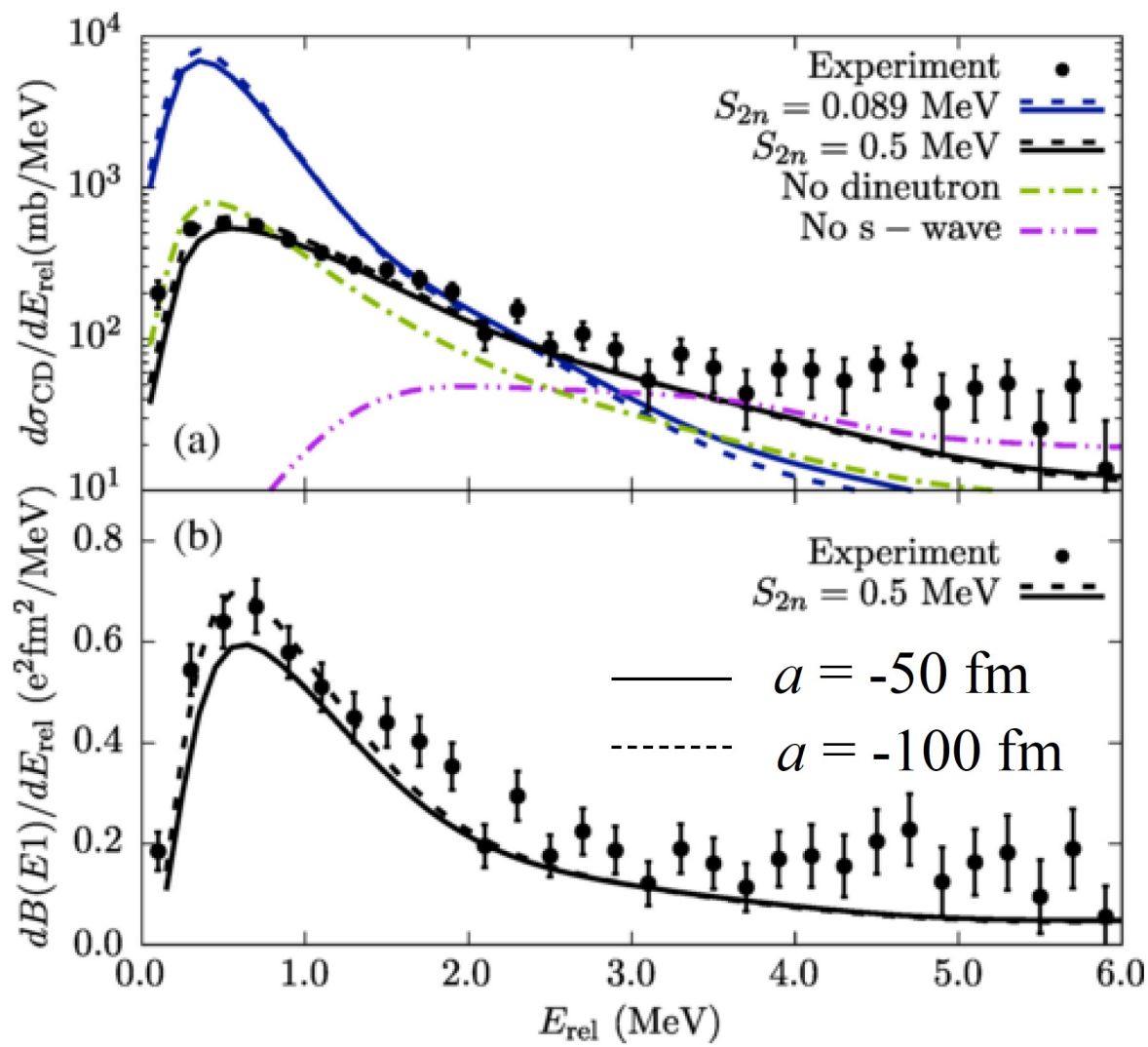
-4n: $\sigma_{\text{Pb}} \sim 3\sigma_{\text{C}}$ \longrightarrow Nuclear Breakup Dominant in -4n channel

$^{17}\text{B}+2n$ more likely rather than $^{15}\text{B}+4n$

c.f. Z.H. Yang et al., PRL 126, 082501, (2021).

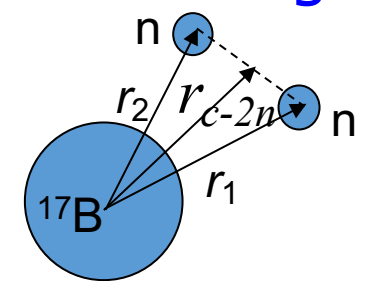
$^{17}\text{B}(p,pn)^{16}\text{B} \rightarrow$ Valence neutrons of ^{17}B : d-wave dominant

E1 Response of ^{19}B



- $B(E1) = 1.64 \pm 0.06$ (stat) ± 0.12 (sys) $e^2\text{fm}^2$
 \rightarrow **Signature of Halo!**
 Similar $B(E1)$ to ^{11}Li , ^{11}Be .
 Core-2n distance (Sum rule)
 $|\sqrt{\langle r_{c-2n}^2 \rangle} = 5.75 \pm 0.11$ (stat) ± 0.21 (sys) fm
- $S_{2n} = 0.5$ MeV
- substantial **s-wave component** with a **well-developed dineutron correlation**.
- Consistent with **large scattering length**:

$^{17}\text{B-n}$ ($a < -50$ fm)



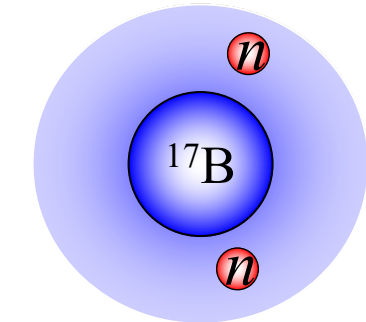
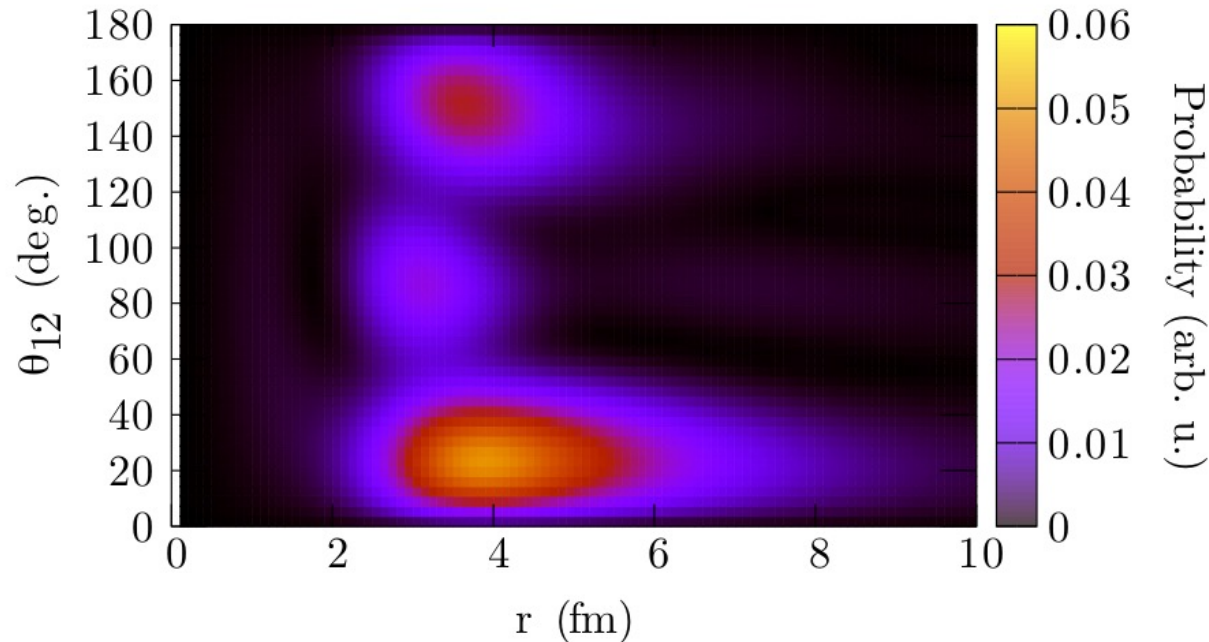
Dineutron correlation in ^{19}B

K.J Cook et al. PRL2020



Three-body model (by K.Hagino) reproduces $d\sigma/dE$ coul very well!

Valence neutron density distribution for $S_{2n} = 0.5 \text{ MeV}$, $a = -50 \text{ fm}$.



$$^{19}\text{B} = ^{17}\text{B} + 2n(\text{halo})$$

$$S_{2n} \sim 0.5 \text{ MeV}$$

- ✓ Enhanced nn probability at $\theta_{12} \sim 25^\circ$
- ✓ Configuration: **Negative:6%**, **s: 35%**, **d: 56%**
- ✓ Asymmetry: Due to Negative-parity mixture

Coulomb breakup of ^{22}C

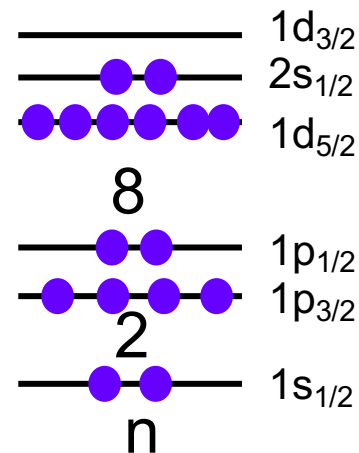
N. Nakatsuka, TN et al.,

Large Cross Section (typical halo),

but **twice broader than ^{19}B**

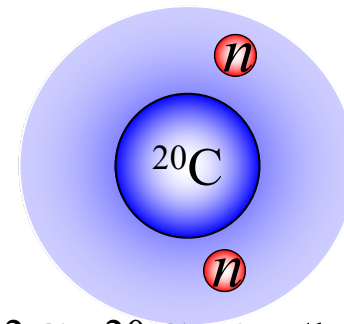
^{22}C :

^{19}B : $E(\text{peak}) \sim 0.5 \text{ MeV}$, $\text{FWHM} \sim 1.5 \text{ MeV}$



(halo-like)

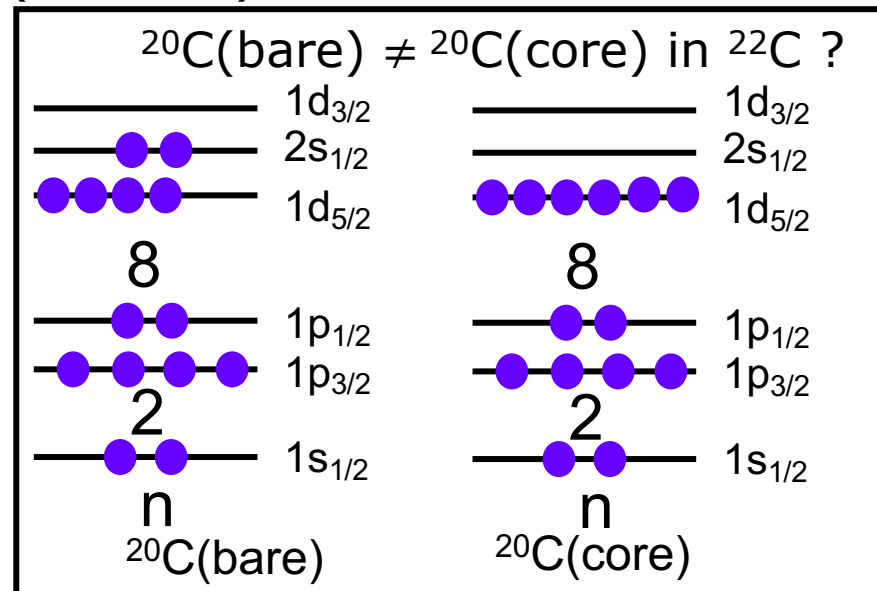
s-wave halo?



$$^{22}\text{C} = ^{20}\text{C} + 2n(\text{halo})$$

$$S_{2n} < \sim 0.5 \text{ MeV}$$

VERY PRELIMINARY



c.f. N. Kobayashi PRC2012, $^{20}\text{C} + \text{C} \rightarrow ^{19}\text{C}_{\text{gs}}(1/2^+)$ ($C^2S \sim 1$)

$^{20}\text{C} + n + n : S_{2n}^{(eff)} = S_{2n} + \Delta$ (T.Suzuki, T.Otsuka PLB753,199(2016)) or **Need $^{20}\text{C} + 4n$ Description?** 27

Summary

✓ Neutron dripline:

Boundary of Open/Closed Quantum Systems → Clusters/Halo/Shell Evolution

✓ Halo-Shell Interplay: ^{31}Ne

- Coulomb Breakup of ^{31}Ne : Soft E1 Excitation ← Doubly-halo components
 $^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2}$ $^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2}$
- Nuclear Breakup ($^{31}\text{Ne} \rightarrow ^{31}\text{Ne}^*$, $^{32}\text{Ne}(-1n) \rightarrow ^{31}\text{Ne}$, $^{32}\text{Na}(-1p) \rightarrow ^{31}\text{Ne}$)

T. Tomai et al., in preparation

✓ Two-neutron halo

- Coulomb Breakup of ^{19}B :
 Strong Soft E1 Excitation, Consistent with dineutron picture $S_{2n} \sim 0.5$ MeV
 K.J. Cook et al., PRL **124**, 212503, 2020.
- Coulomb Breakup of ^{22}C :
 Soft E1 Excitation, but broader peak → Core is different from Bare ^{20}C ?

Perspectives

More exotic neutron states → Nuclear interactions/Many-body effects at the limit

$^{27}\text{O}, ^{28}\text{O}$ (Y.Kondo et al.), ...

Exclusive Coulomb/nuclear breakup of ^{31}Ne

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Coulomb breakup of ^{19}B

K.J. Cook et al., Physical Review Letters 124, 212503 (2020).

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