

Results from the first part of LIGO-Virgo-KAGRA's fourth observing run

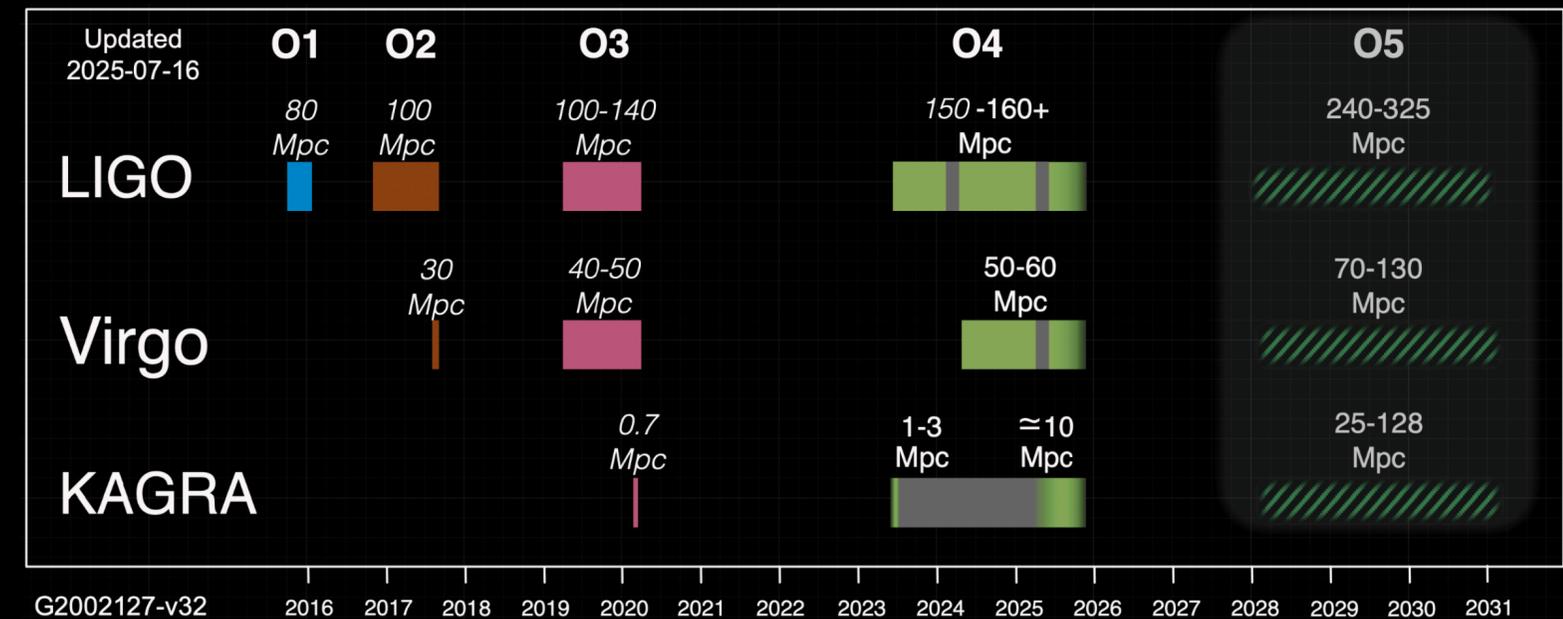
with a special

Focus on correlations

Salvatore Vitale

Where are we?

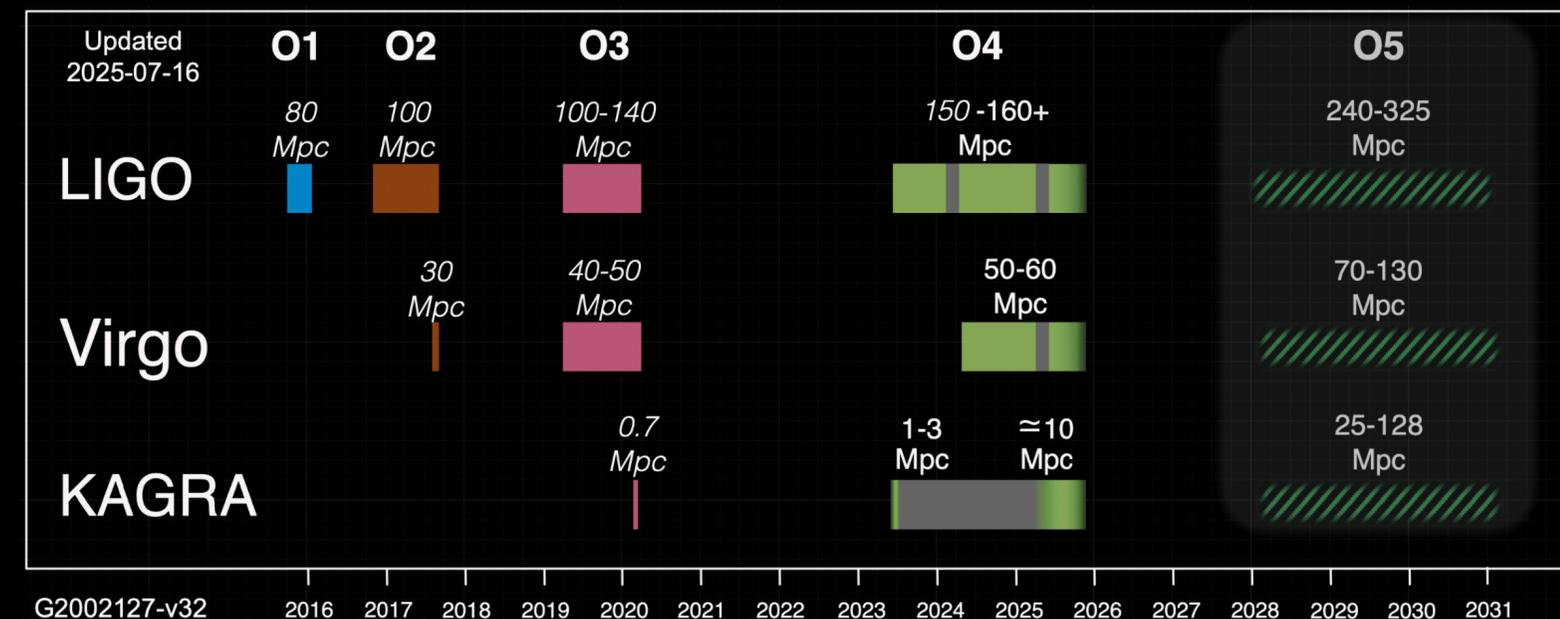
- Over the last 10 years, we have gone through 4 observing runs
- Detectors have steadily increased their sensitivity
- We have detected 218 binary mergers (+ ~150 candidates in O4b and O4c)
 - Mostly binary black holes
 - Two neutron star binaries
 - Six neutron star - black hole binaries



LVK <https://observing.docs.ligo.org/plan/>

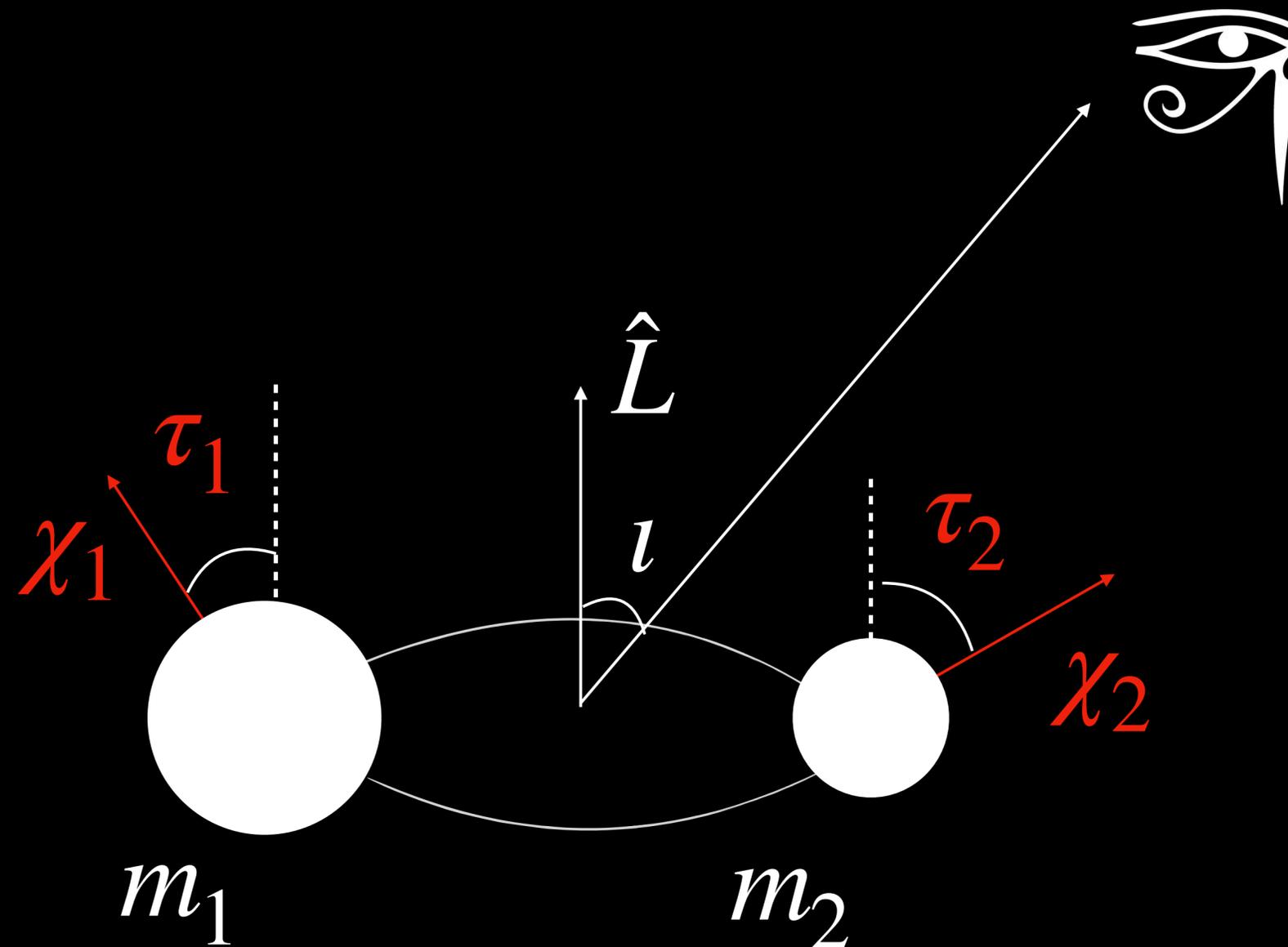
Where are we?

- We have detected 218 binary mergers (+ ~150 candidates in O4b and O4c)
 - Mostly binary black holes
 - Two neutron star binaries
 - Six neutron star - black hole binaries
- Each source has unique properties that can teach us about its history, encoded in the gravitational waves we receive



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Gravitational-wave anatomy: source

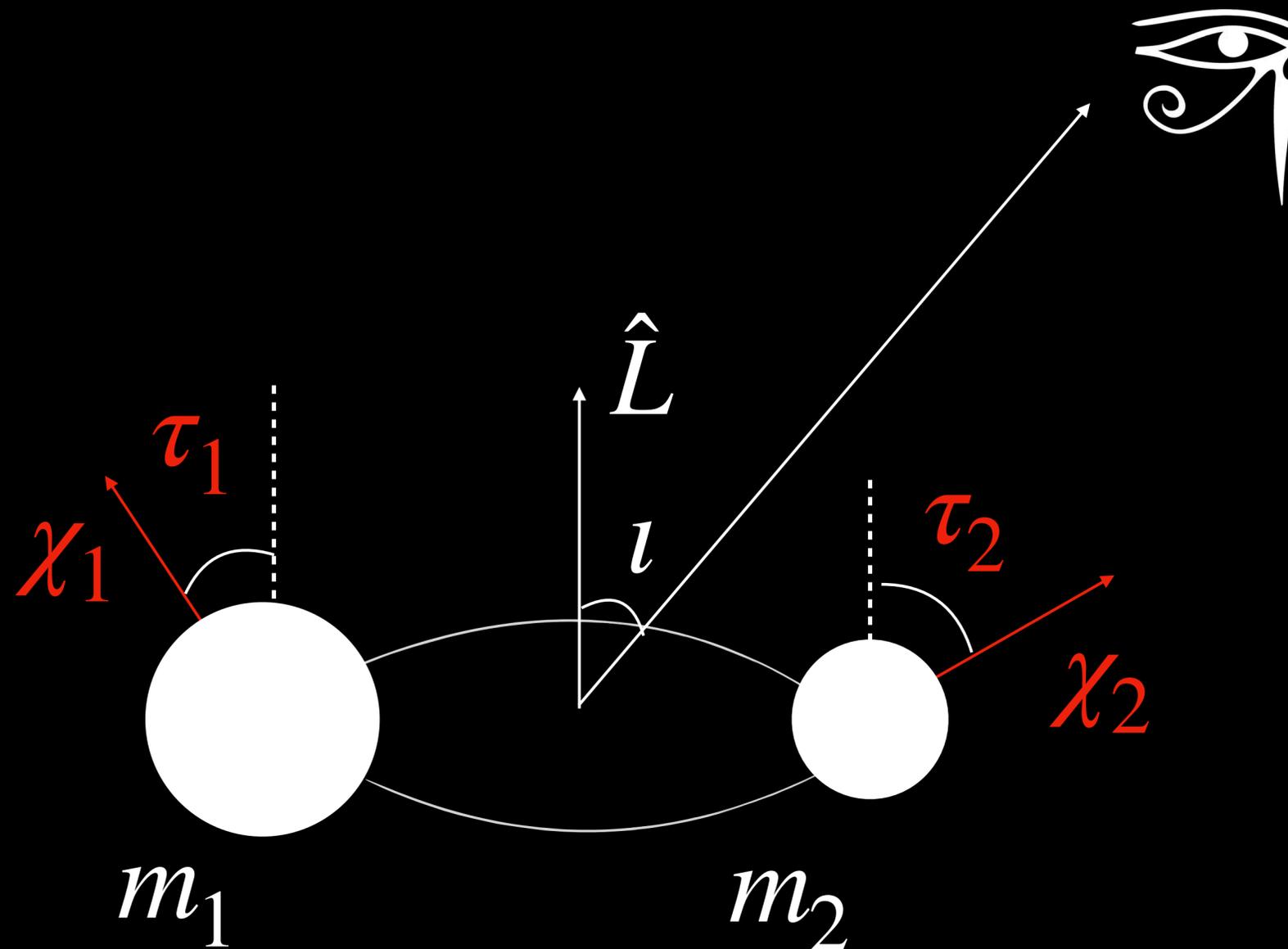


Index 1 for the most massive object

Gravitational-wave anatomy: source

Chirp mass

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$



Index 1 for the most massive object

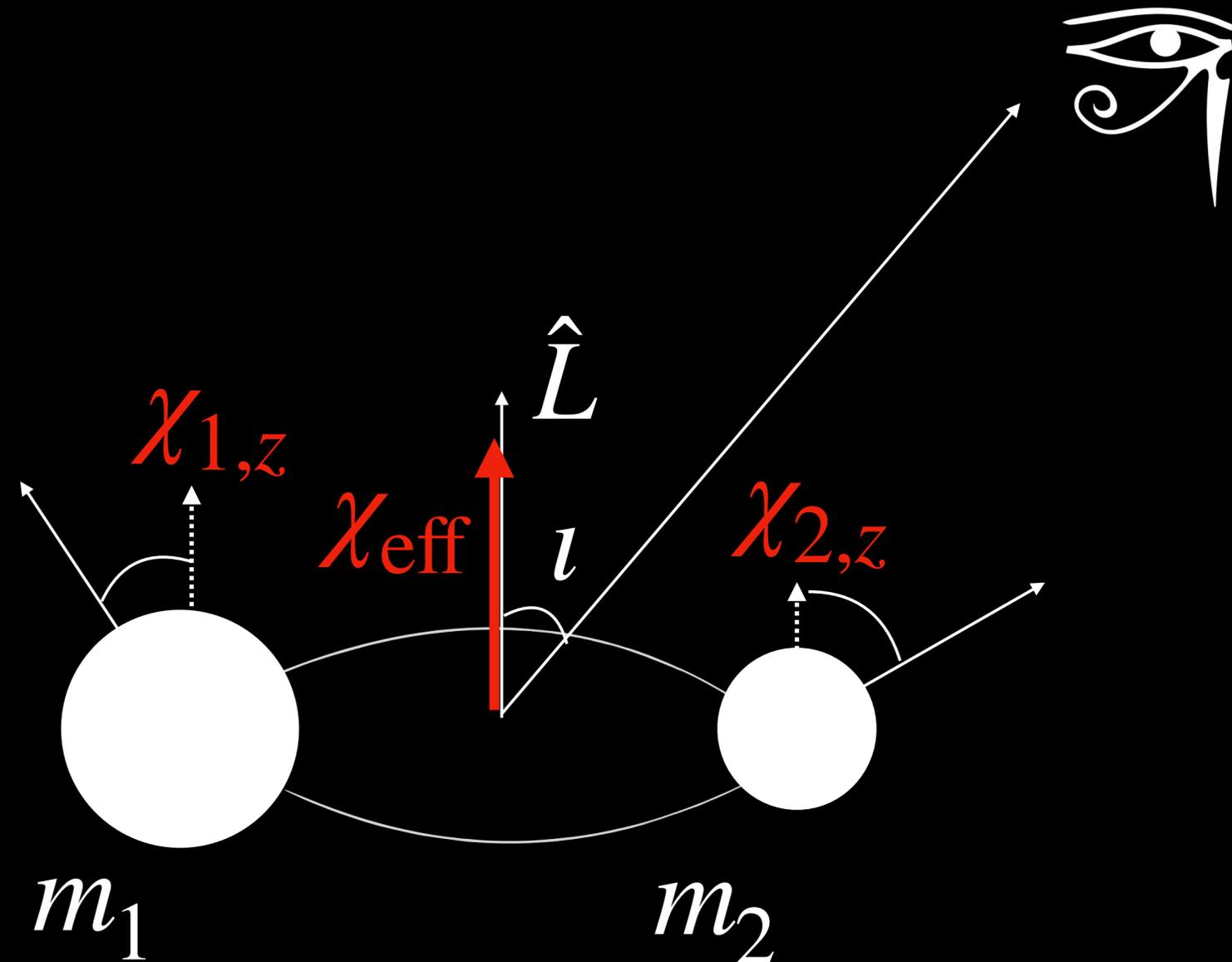
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Chirp mass

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

Chi effective

$$\chi_{\text{eff}} = \frac{m_1 \chi_{1,z} + m_2 \chi_{2,z}}{m_1 + m_2}$$



From single events to populations

- Now that we have hundreds of sources, we can start learning about the underlying astrophysical populations of compact binary coalescences

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- Do we know what to expect?

From single events to populations

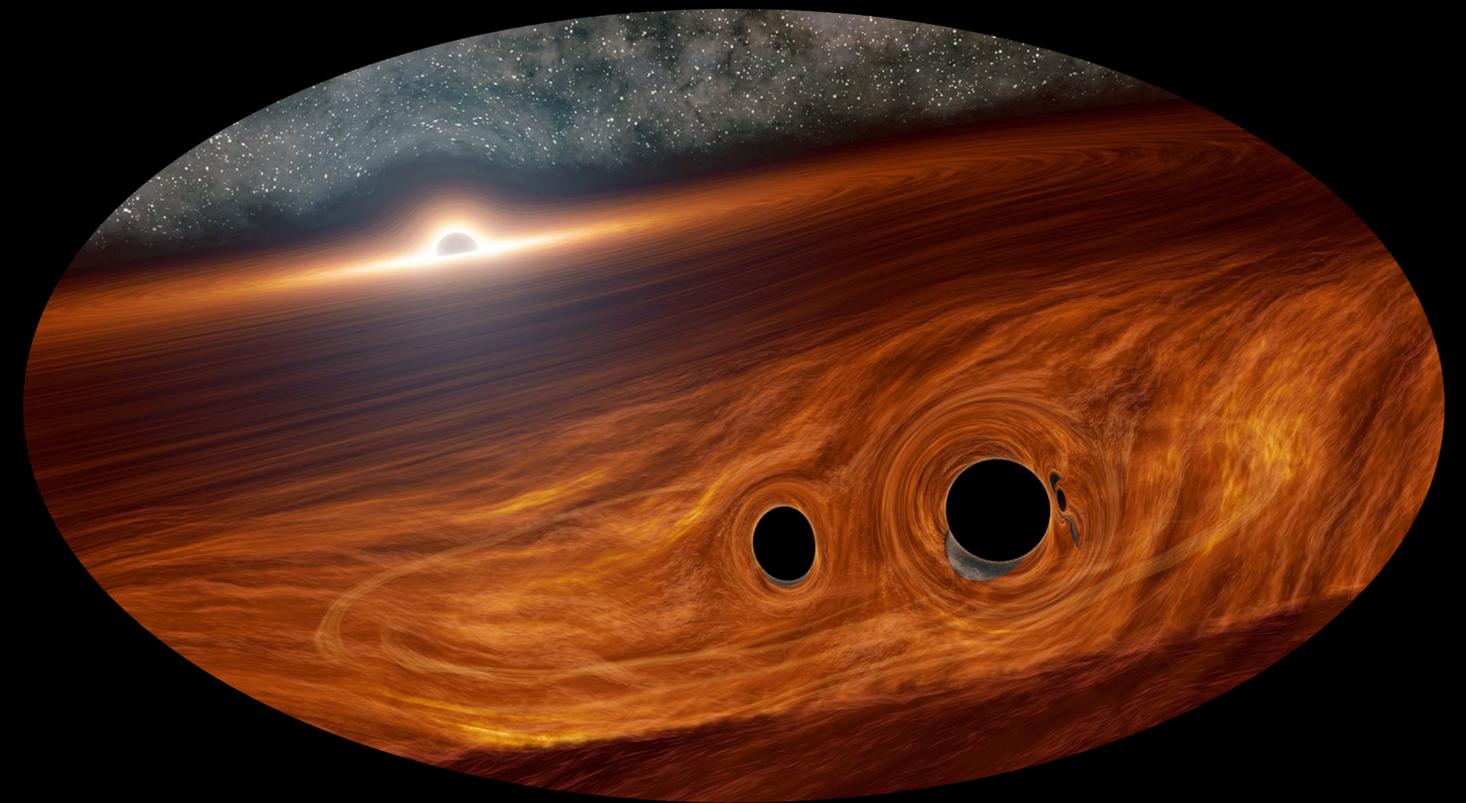
- Now that we have hundreds of sources, we can start learning about the underlying astrophysical populations of compact binary coalescences
- Do we know what to expect?
- It's complicated...

Expectations pre-2015

- Before the discovery of gravitational waves, most of the community considered two formation scenarios
 - Common envelope evolution in field binaries (common envelope)
 - Dynamical formation in globular clusters

More recent developments

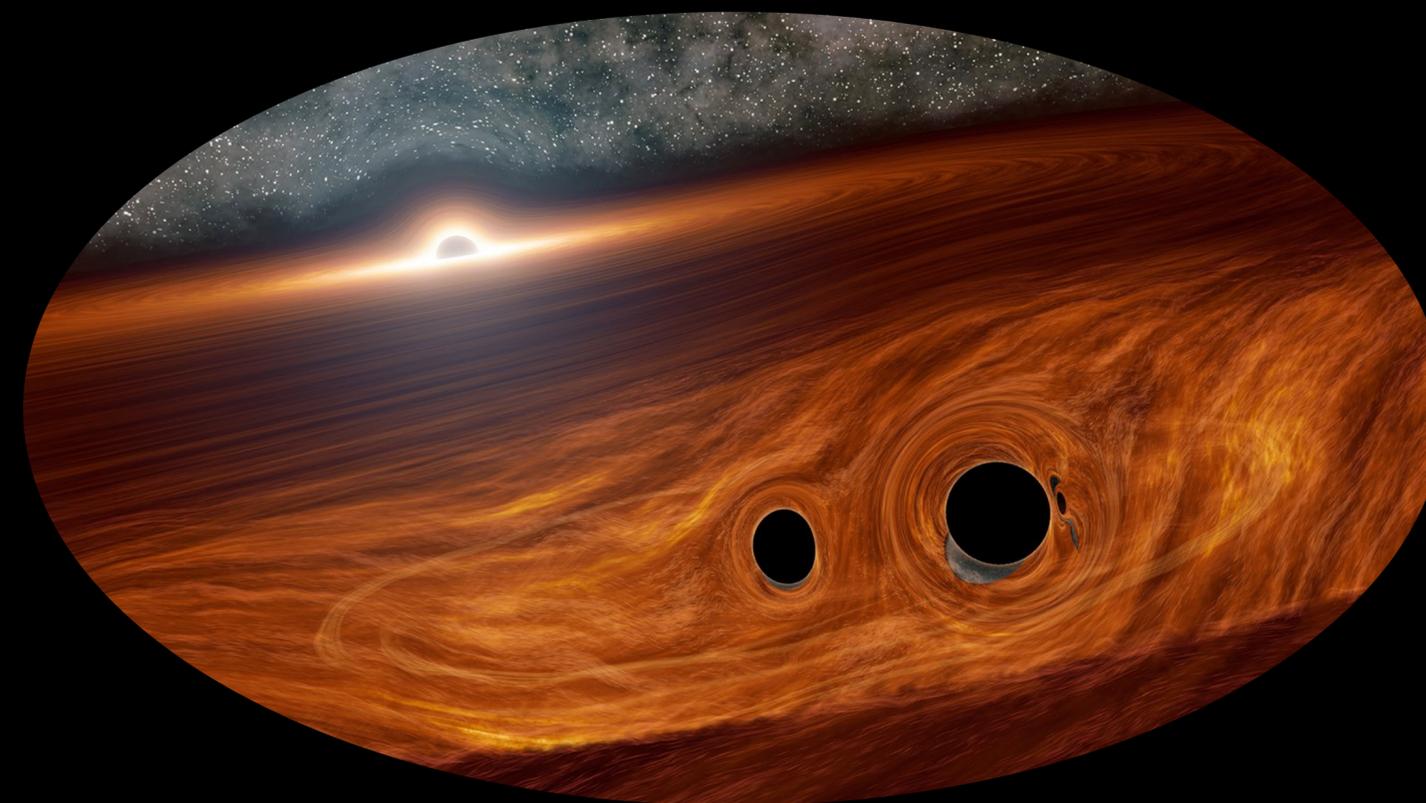
- In a **field binary**, all mass transfer episodes might be stable. Or the progenitor stars might not even exchange mass due to efficient mixing (chemically homogeneous evolution)
- **Dynamical formation** might happen not only in globular clusters but also in nuclear star clusters or the disks around supermassive black holes. Triples might contribute significantly to the rates



Credit: Caltech/R. Hurt

More recent developments

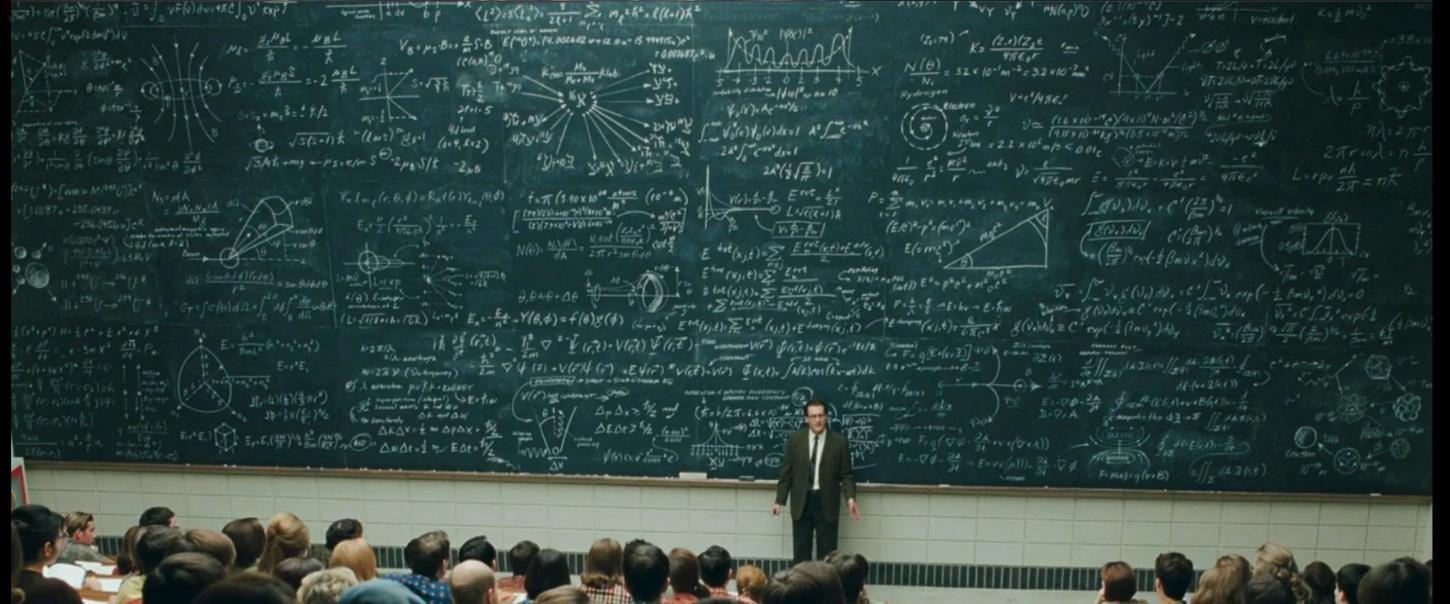
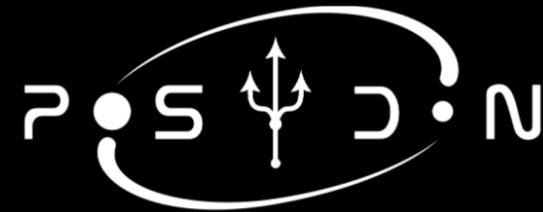
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- **Dynamical formation** might happen not only in globular clusters but also in nuclear star clusters or the disks around supermassive black holes. Triples might contribute significantly to the rates
- **Or Pop III stars? Primordial BHs?**



Credit: Caltech/R. Hurt

How do we find out?

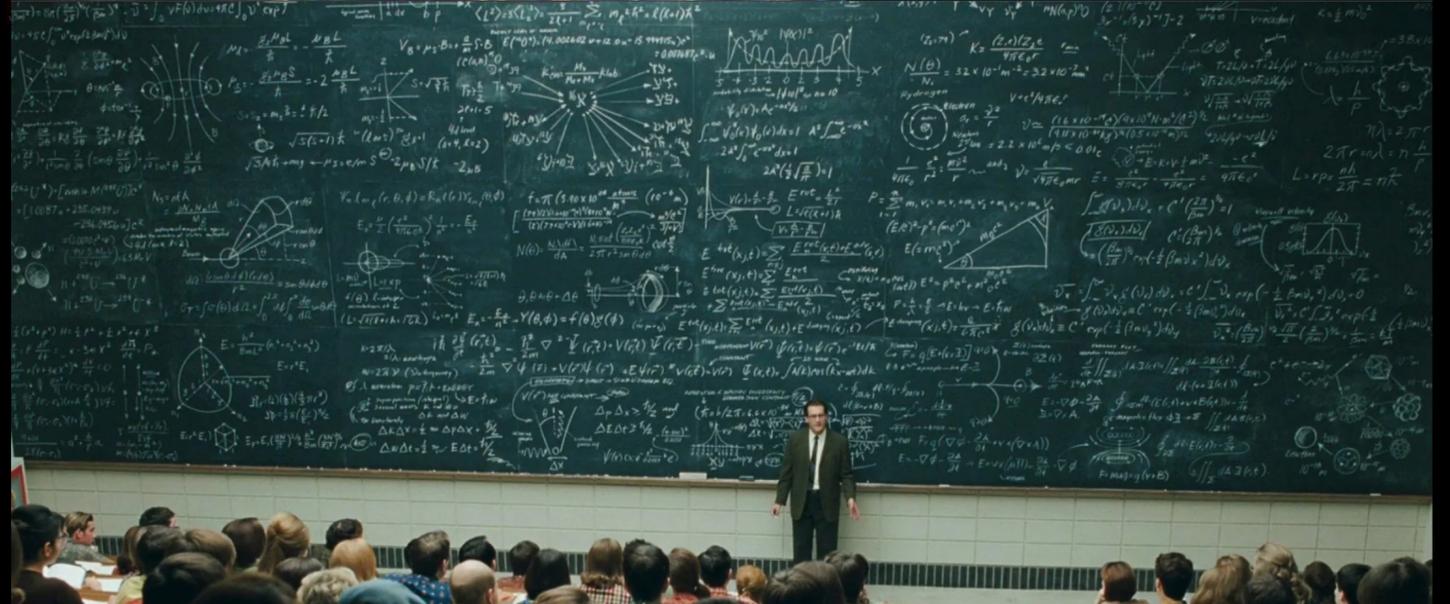
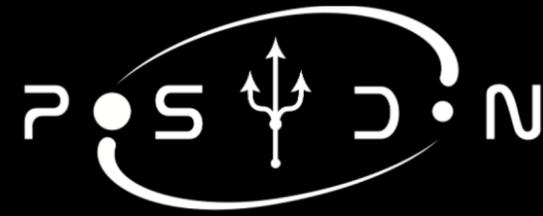
- Theoretical and numerical simulations can predict the properties that compact binary systems from different channels should have
- “Just” compare those with the properties of the population we are detecting!



Credits: Focus Features

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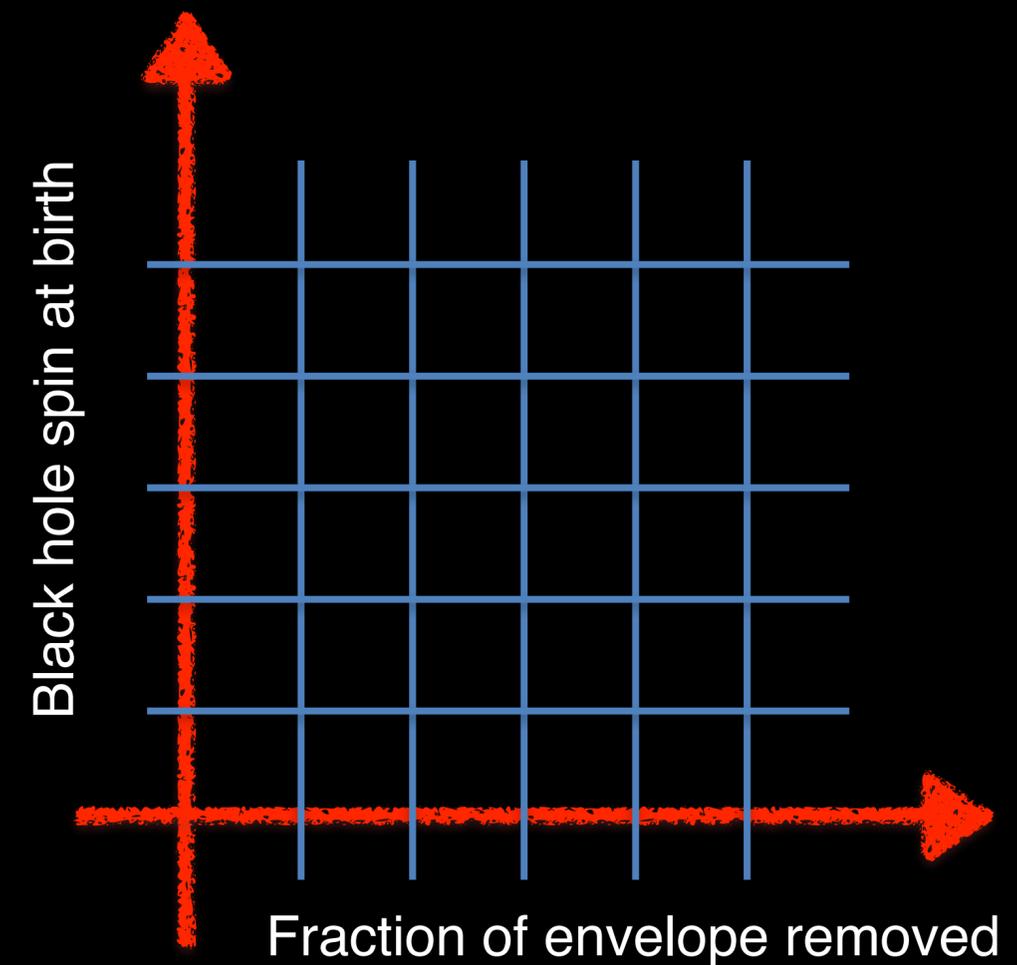
- Theoretical and numerical simulations can predict the properties that compact binary systems from different channels should have
- “Just” compare those with the properties of the population we are detecting!
- The simulations are costly and don't capture all of the physics



Credits: Focus Features

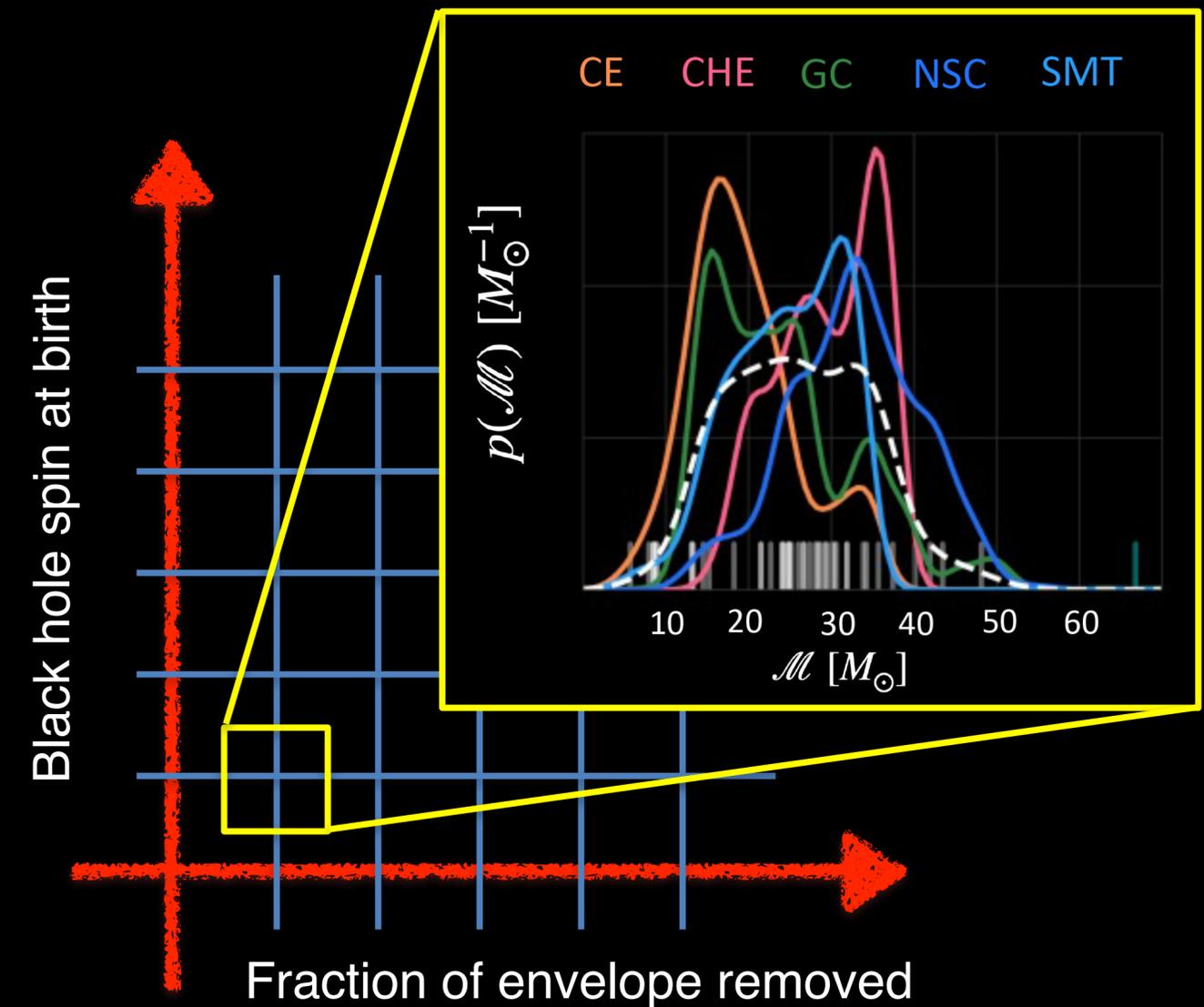
Astrophysical models!

- Direct approach (Zevin+ Apj 910 152)
 - Models for common envelope (CE), chemically homogeneous evolution (CHE), stable mass transfer (SMT), globular clusters (GC), nuclear star clusters (NSC)
 - Parametrize by fraction of common envelope that is removed and black hole spin at birth



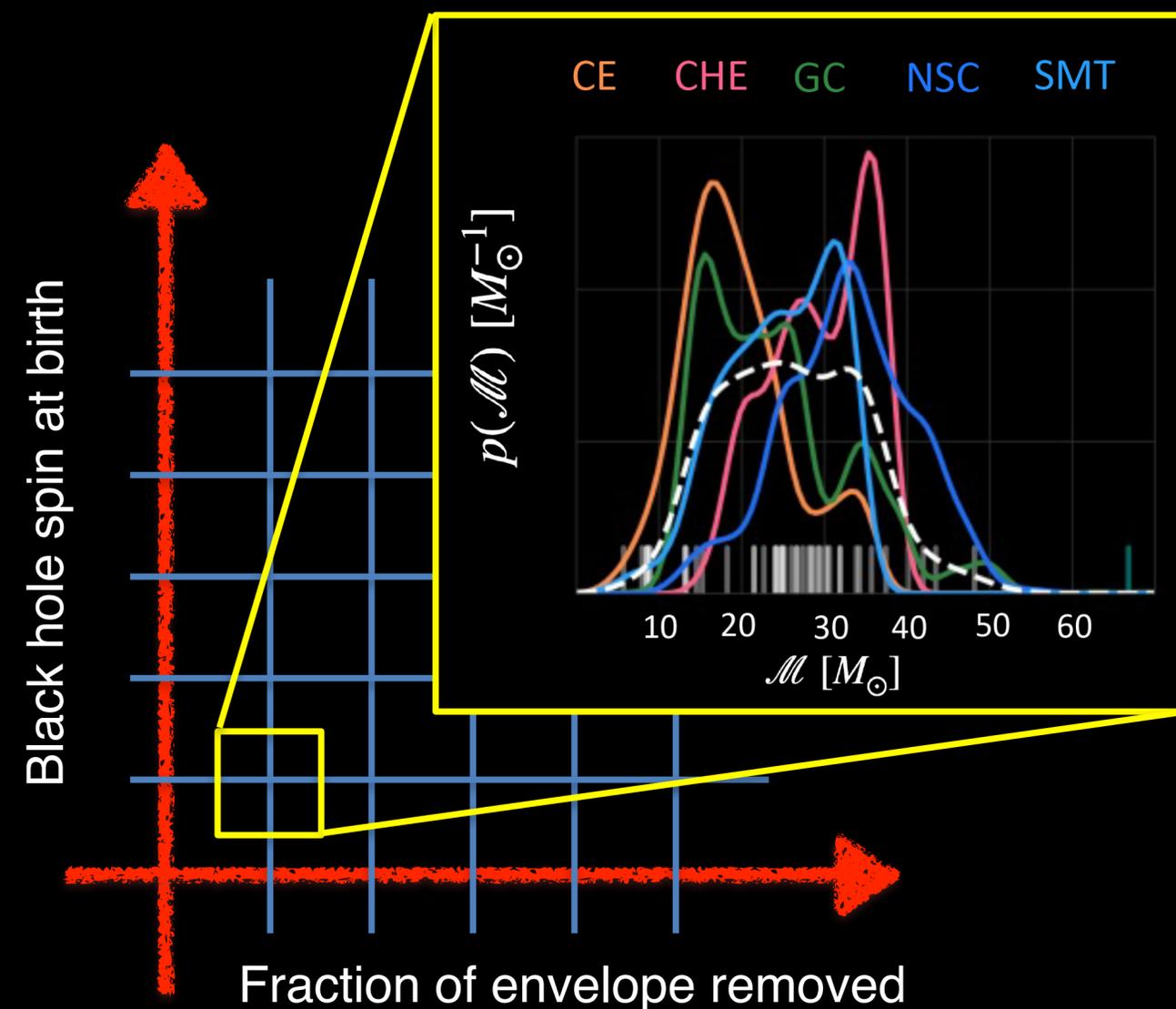
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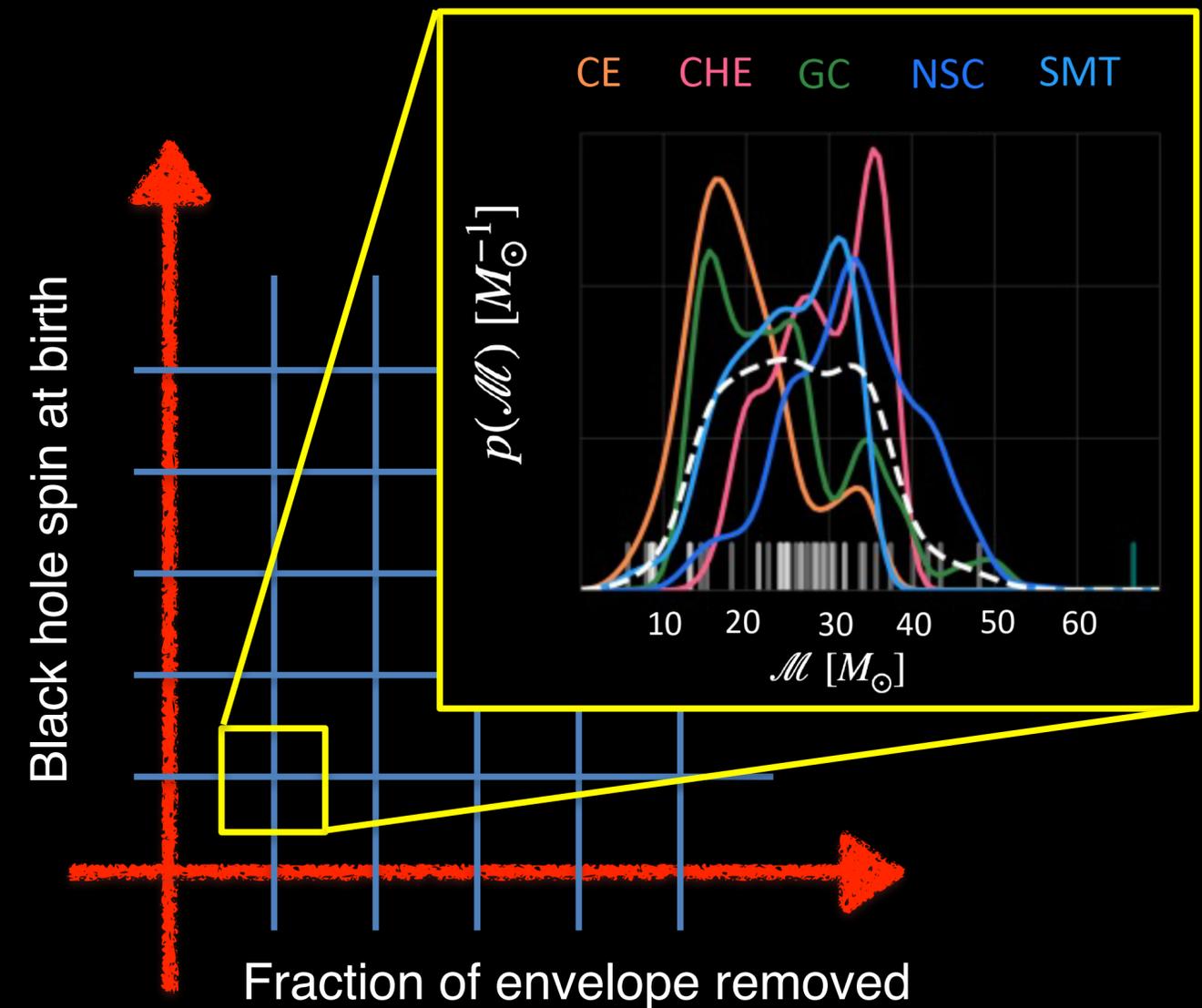
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- Compare with the data on a grid or using machine learning emulators (Colloms+ ApJ 988 189)



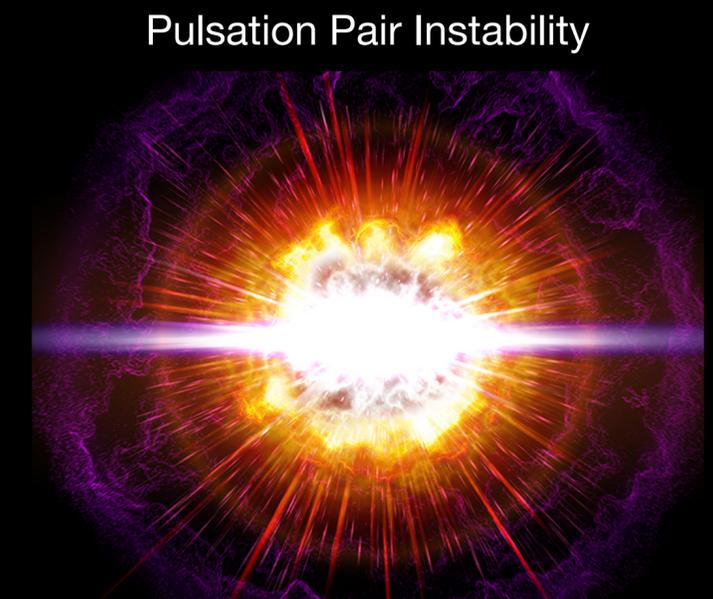
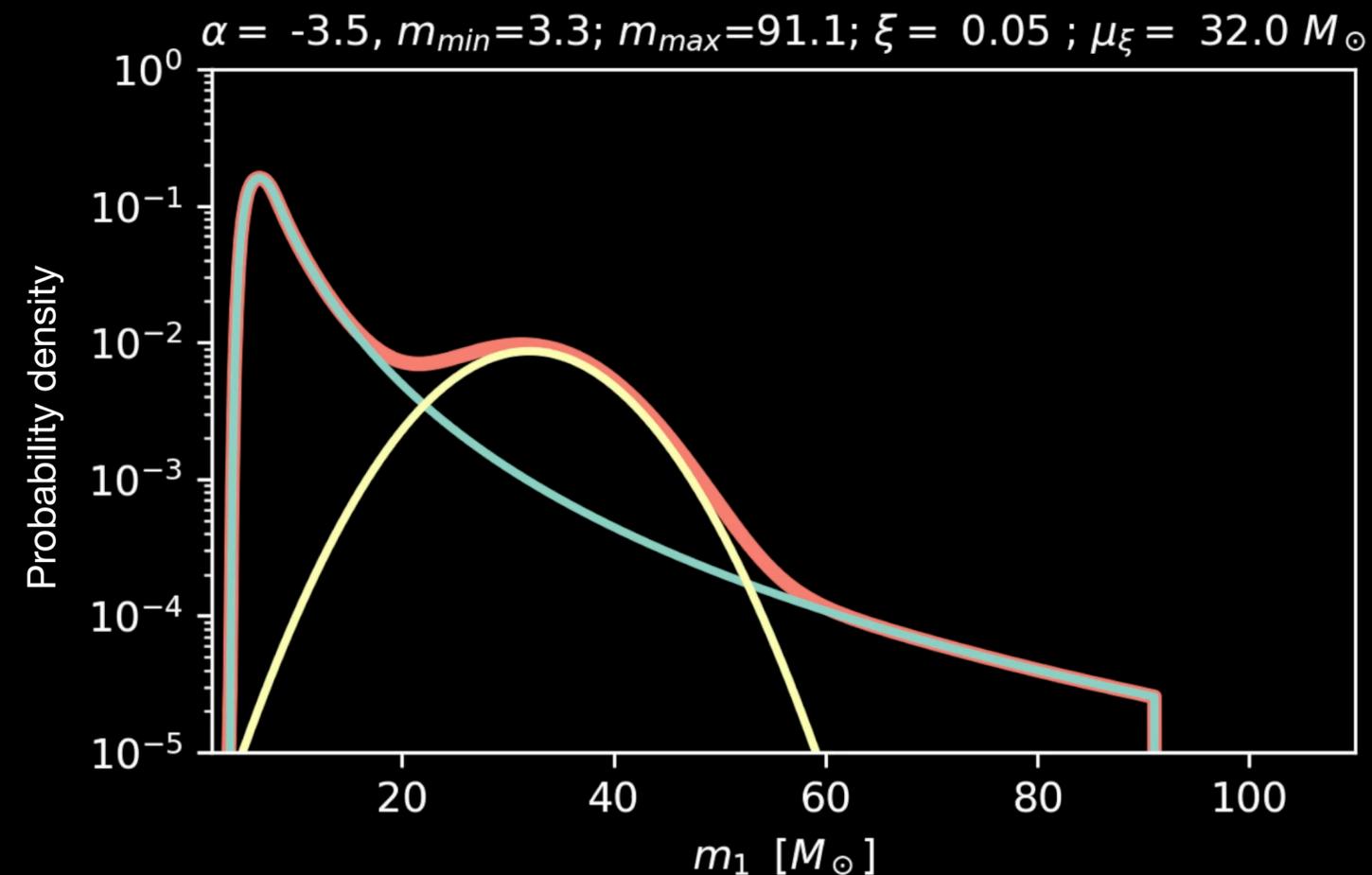
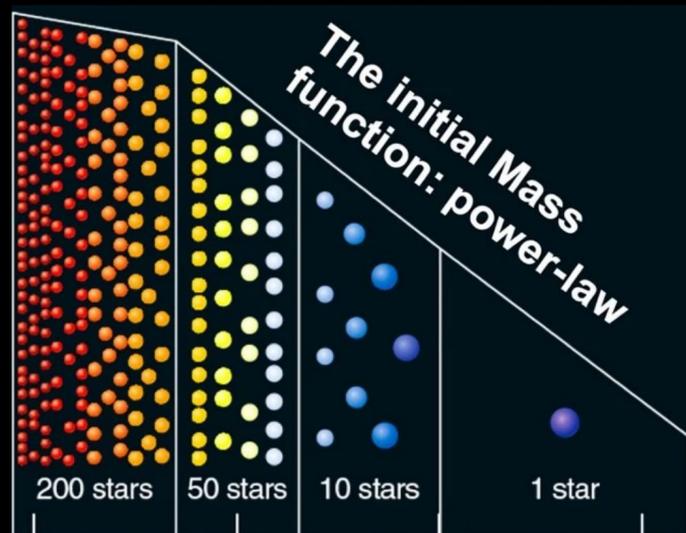
Astrophysical models!

- Analysis on **O3a** data (2019): at least two astrophysical channels are needed
- Is this the way forward?
- In **Cheng+ ApJ 955 127** we revealed limitations in this approach
 - The astrophysical models are rough approximations
 - We are not likely to have complete set of astrophysical models
 - This can introduce very large **biases**



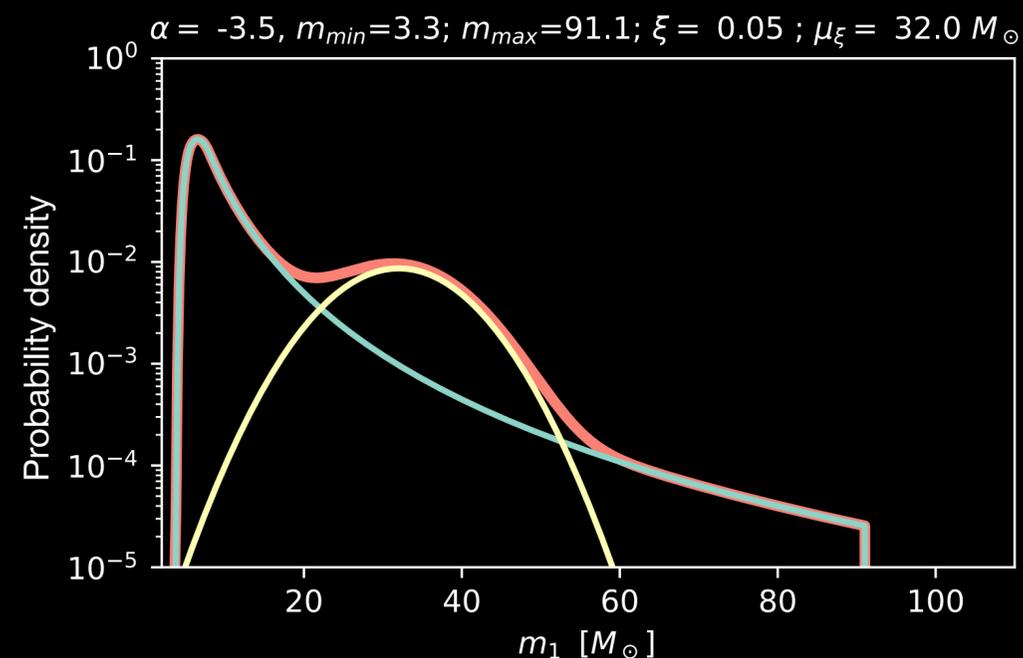
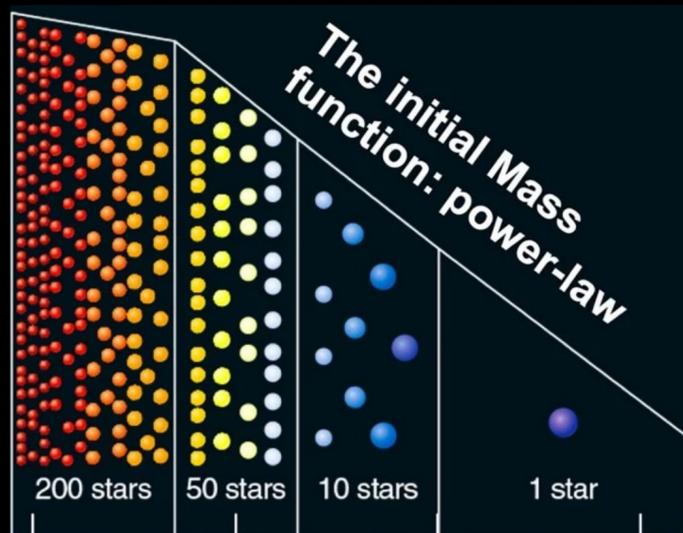
Phenomenological models

- Another avenue is to use phenomenological models, inspired by astrophysical expectations
- For example, the astrophysical distribution of the black hole mass can be parametrized as a combination of a power law and a gaussian

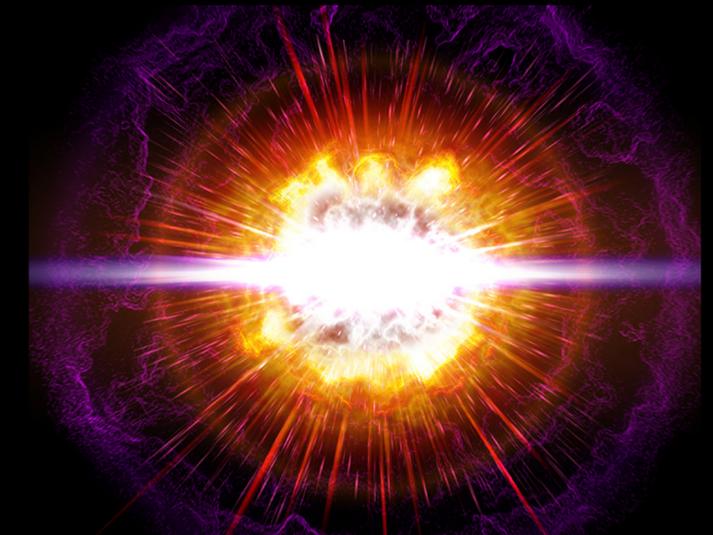


Phenomenological models

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- Will skip all technical details, see e.g, [Vitale+ 2007.05579](#), [Mandel+ 1809.02063](#), LIGO/Virgo/KAGRA (LVK) catalog [2508.18083](#) for more details



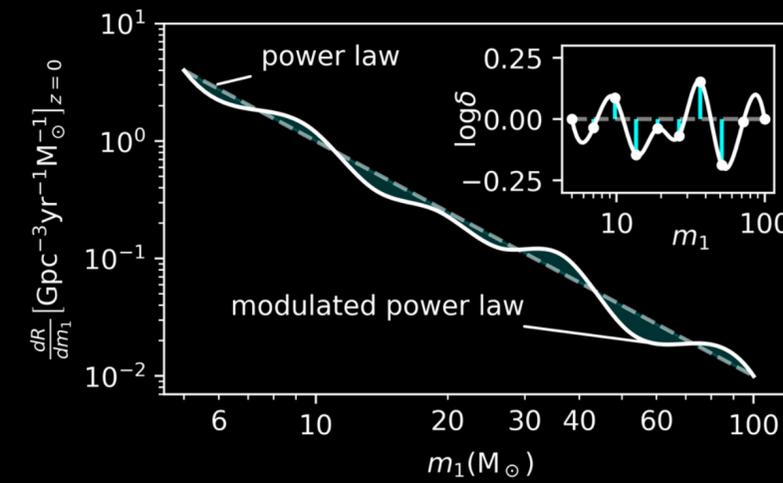
Pulsation Pair Instability



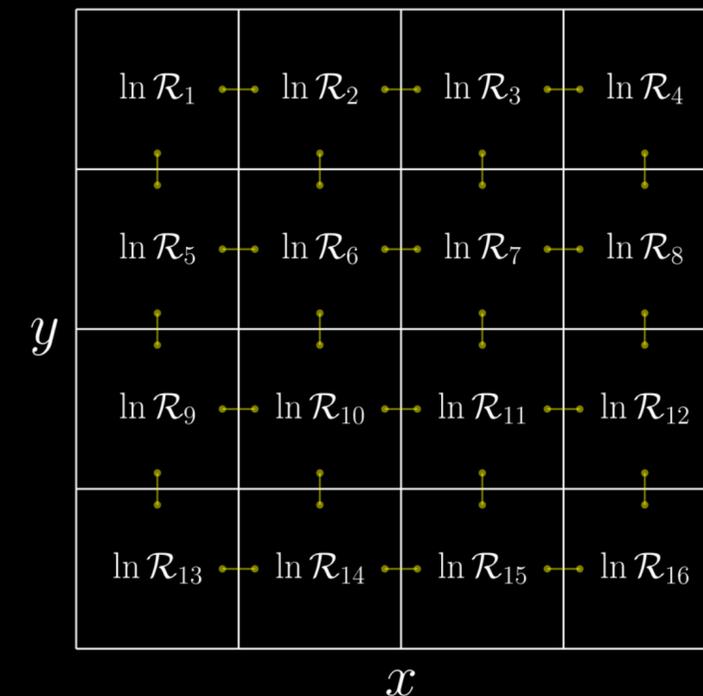
Agnostic models

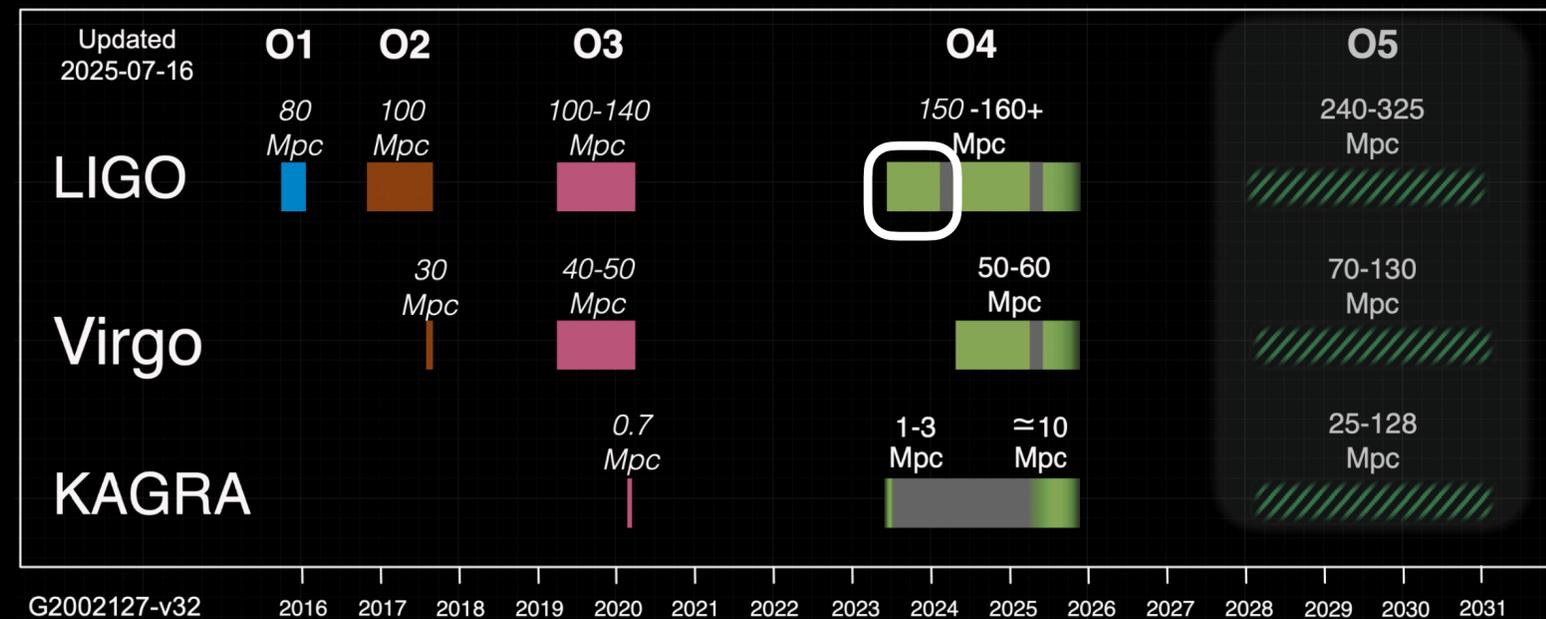
- To allow for more complicated distributions we use “unmodeled” approaches
- A variety of possibility exists, e.g.
 - Splines (alone or in mixture models)
 - Autoregressive models
 - Gaussian mixture models
 - Gaussian processes
 - New ideas every day

Edelman+ ApJ 946 16



Heinzel+ PRD 111, 063043

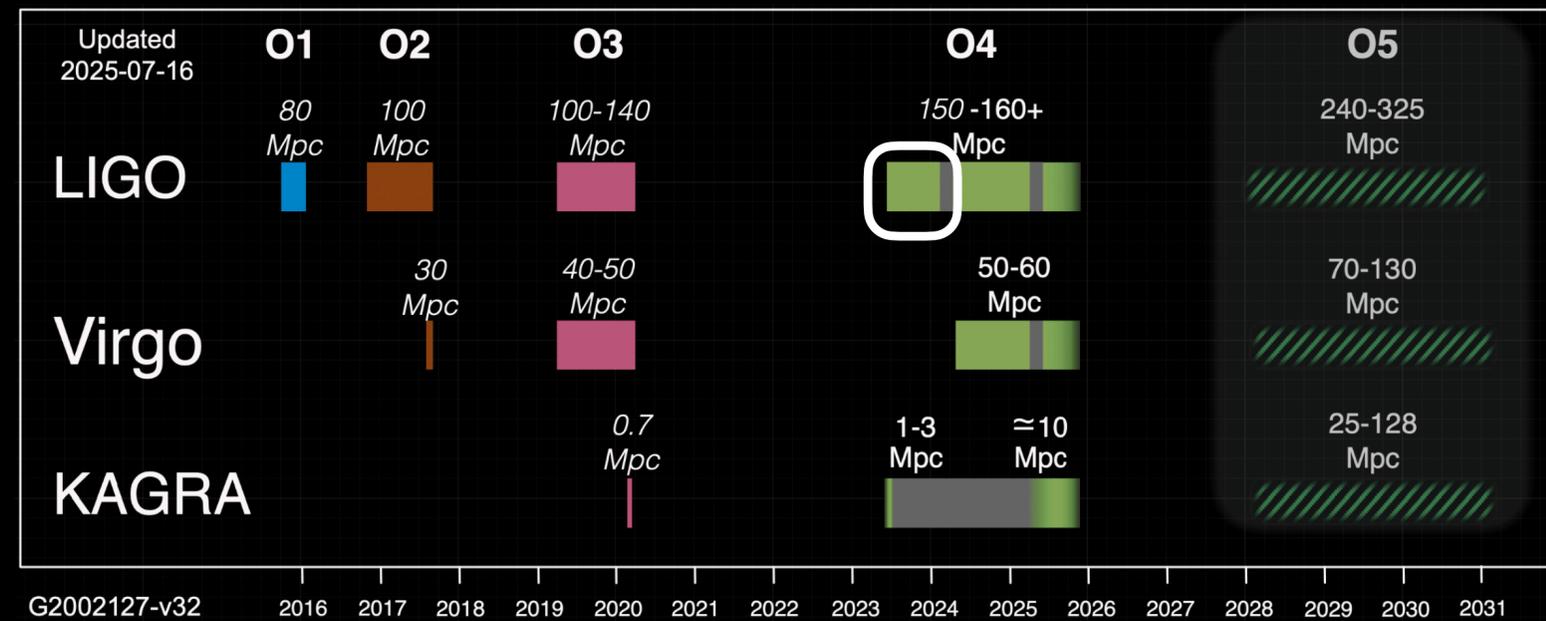




LVK <https://observing.docs.ligo.org/plan/>

Results from GWTC-4

LVK 2508.18080, 2508.18081, 2508.18082, 2508.18083



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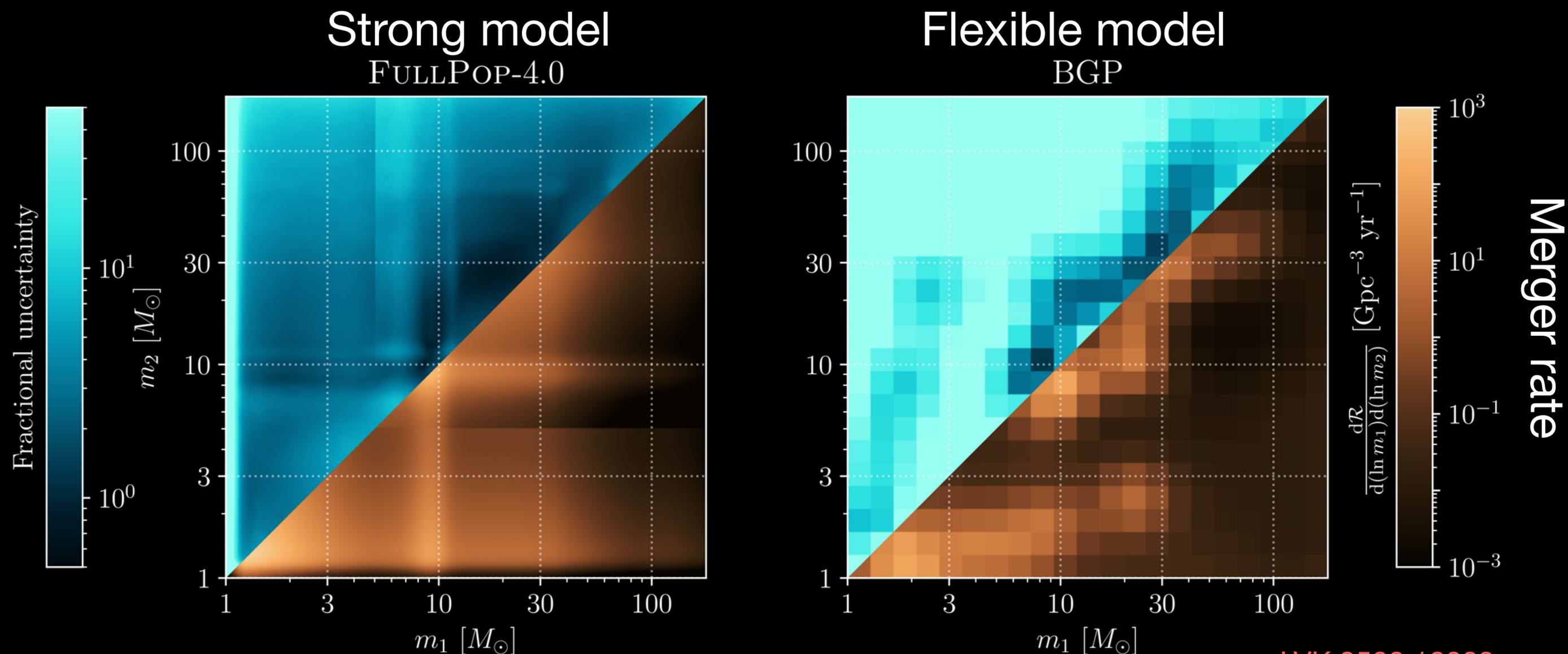
Results from GWTC-4

LVK 2508.18080, 2508.18081, 2508.18082, 2508.18083

There is a ton of science in these papers, I cannot possibly cover it all.

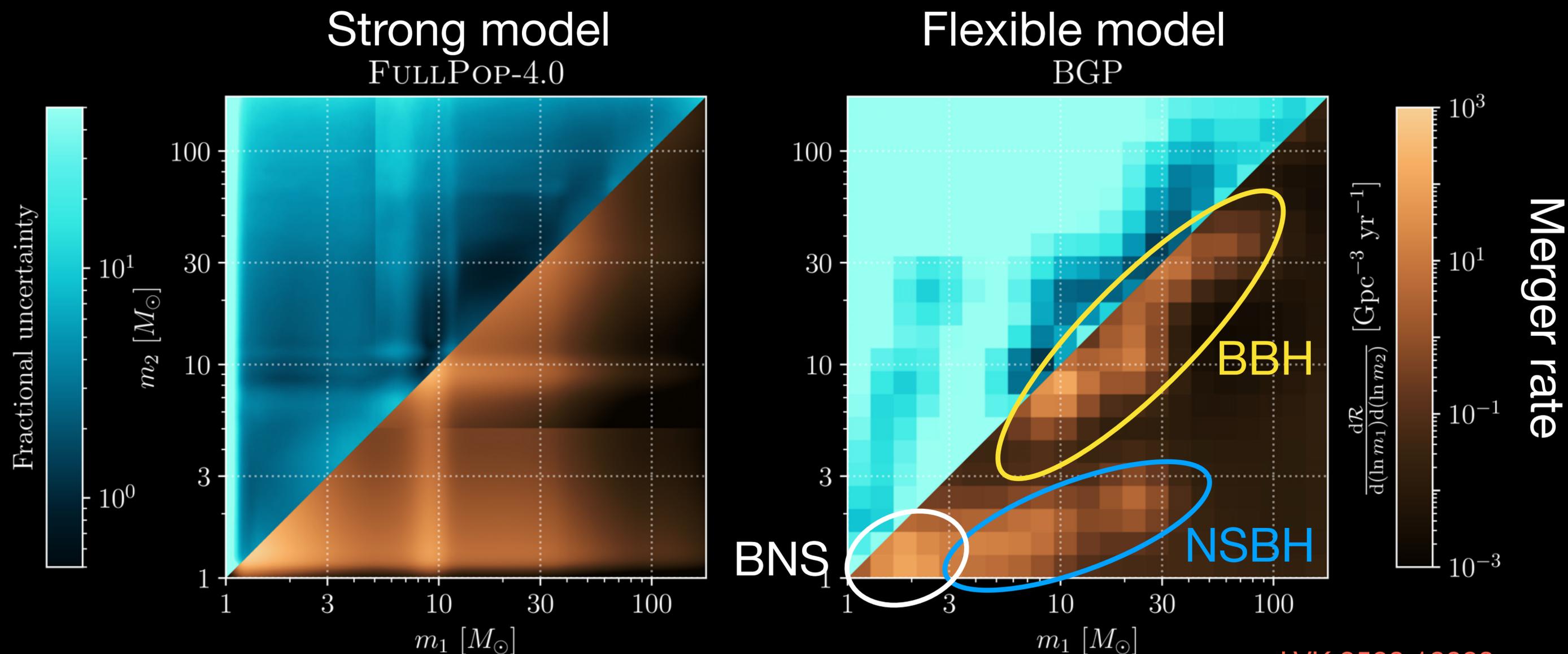
Full spectrum mass distribution

- A strong and flexible model are run and compared on **all** types of binaries (not just binary black holes)



Full spectrum mass distribution

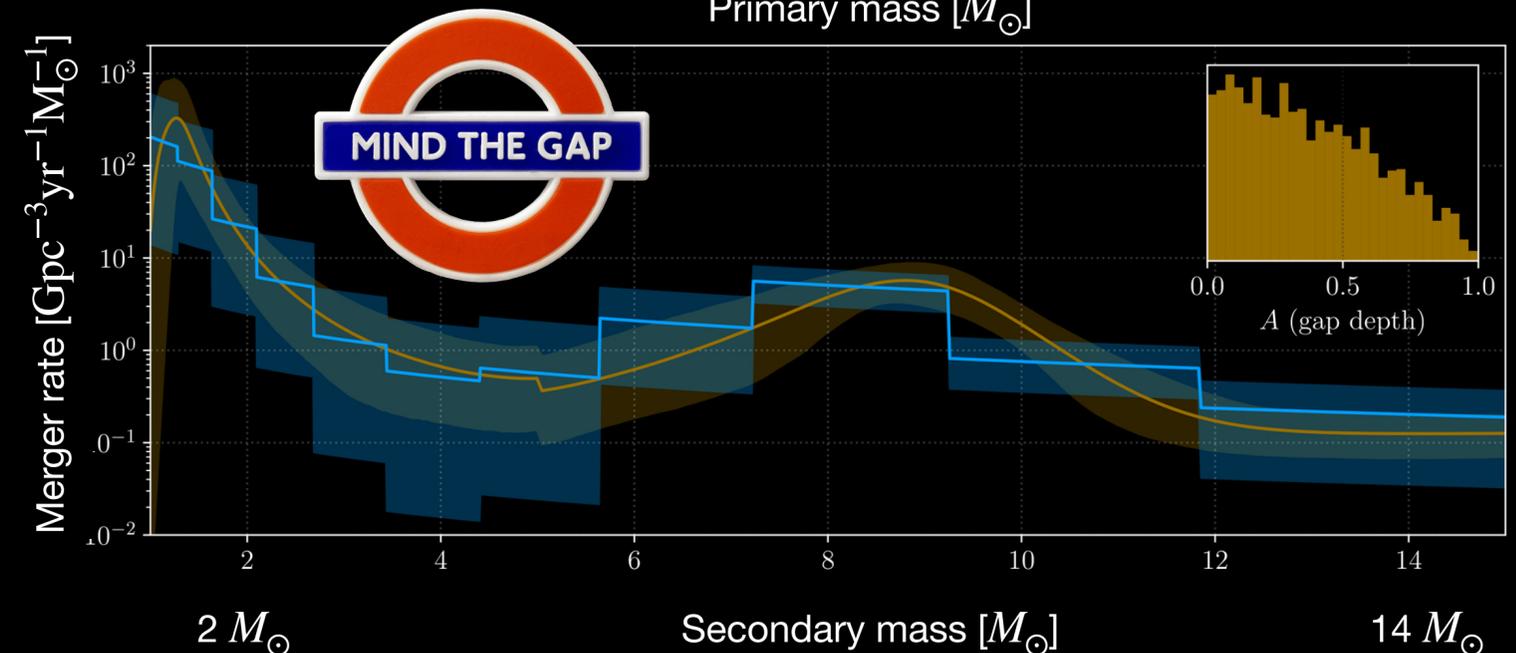
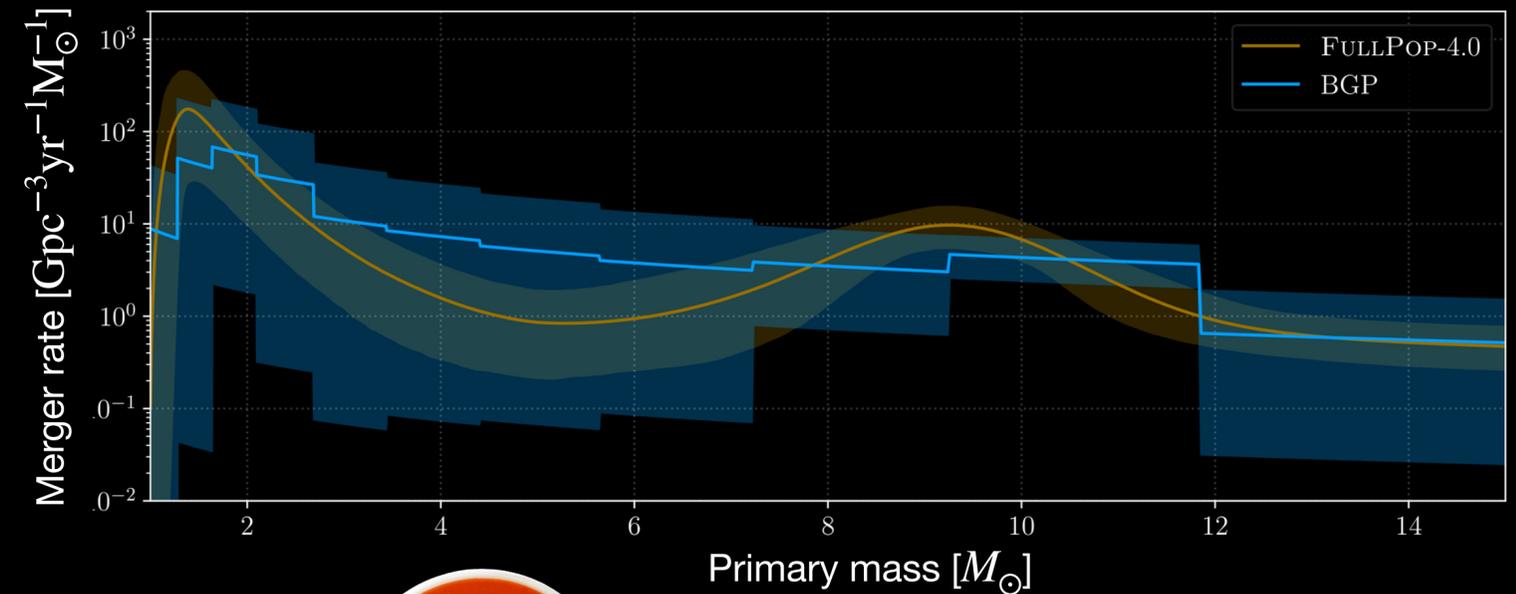
- A strong and flexible model are run and compared on **all** types of binaries (not just binary black holes)



Full spectrum mass distribution

- The overall peak in the merger rate is below $2 M_{\odot}$ (i.e., neutron stars)
- The peak for the black holes mass function is around $8-10 M_{\odot}$
- Electromagnetic observations had suggested a possible gap between neutron stars and black holes
 - The LVK finds that the merger rate decreases there but doesn't go to zero
 - No evidence for an empty gap

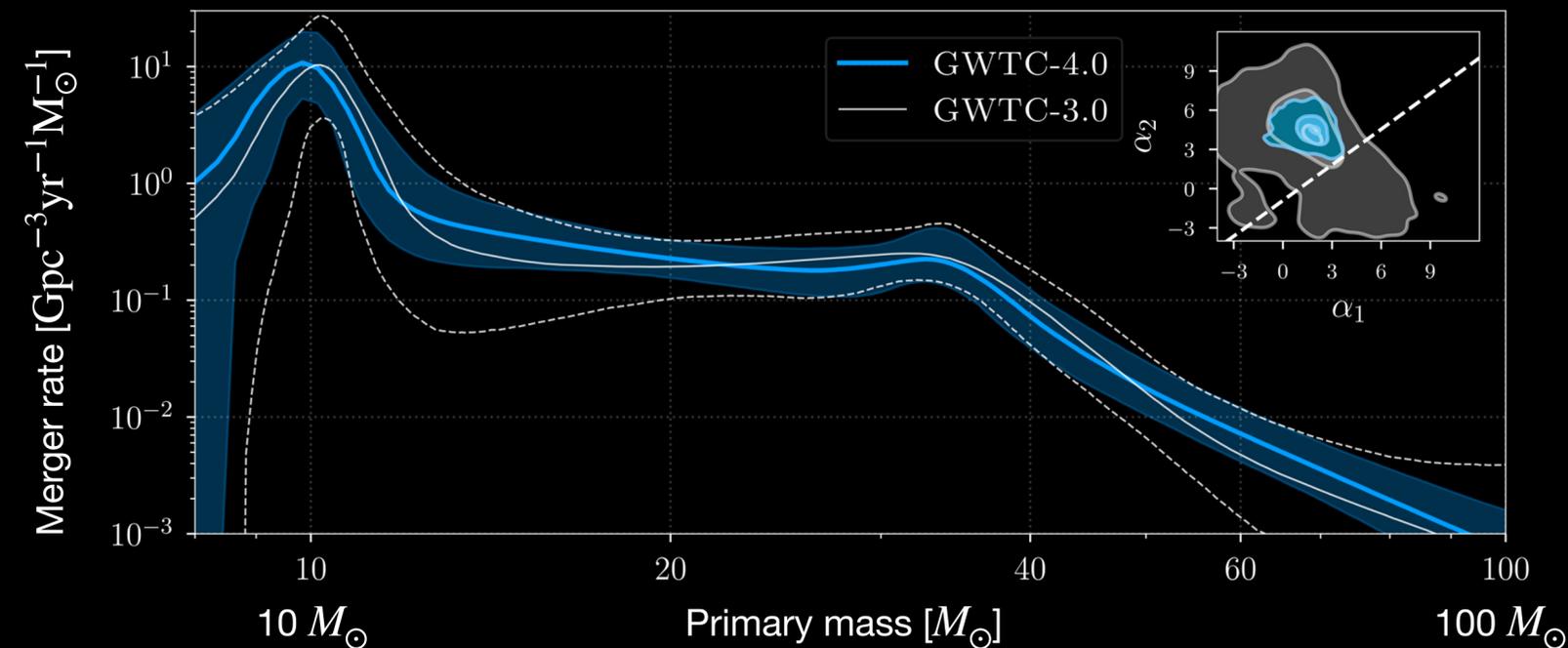
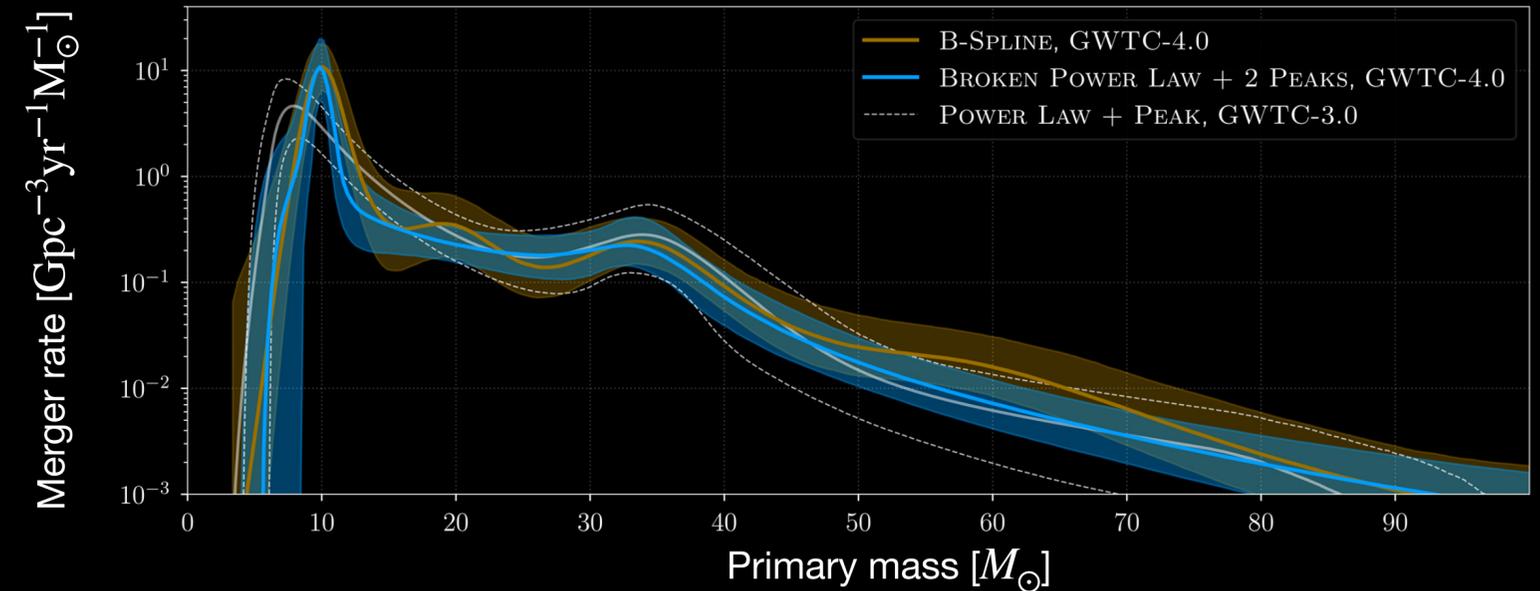
LVK 2508.18083



Binary black hole mass distribution

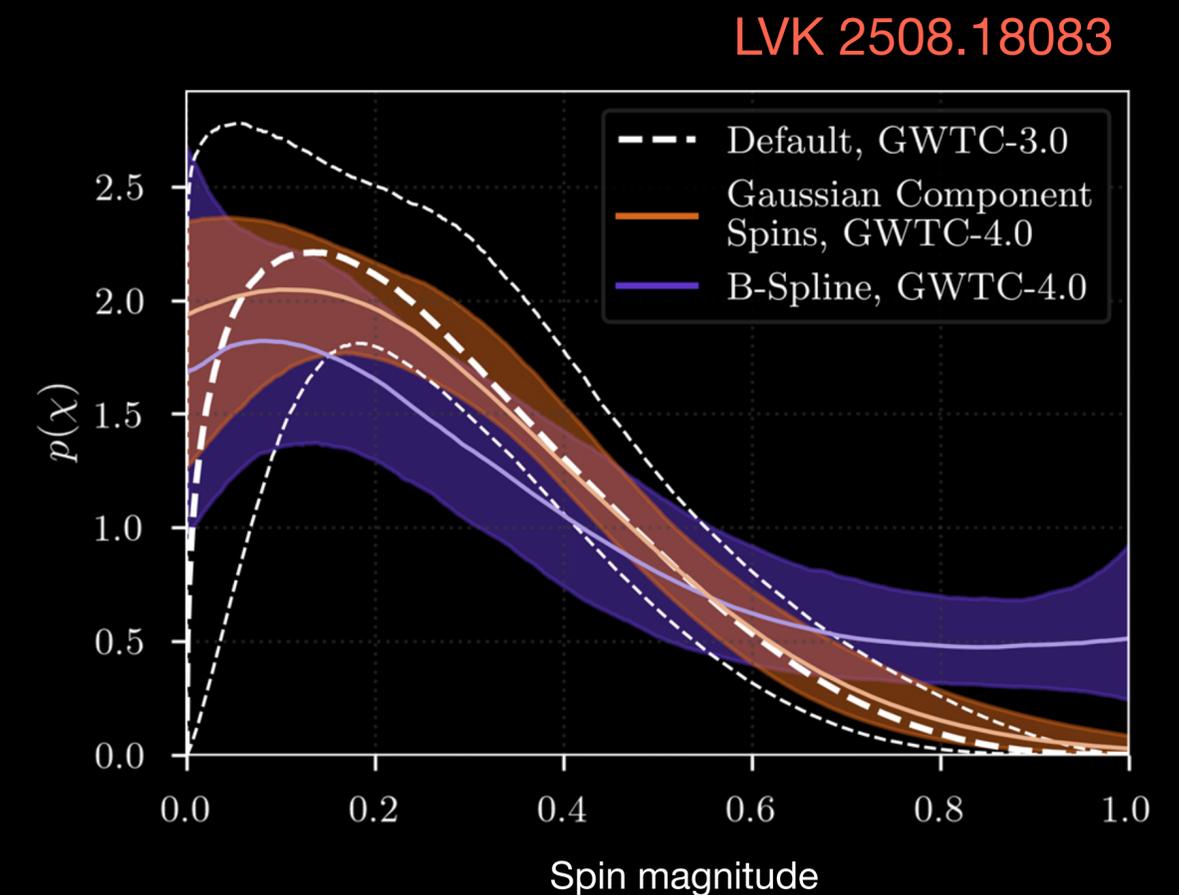
LVK 2508.18083

- Most of the analyses focus specifically on the binary black hole sources
- Main takeaways
 - Clear features at $\sim 10 M_{\odot}$ and $\sim 35 M_{\odot}$ (M_{\odot} already found)
 - Hints of something at $\sim 20 M_{\odot}$?
 - Evidence that the slope of the continuum steepens after the $35 M_{\odot}$ peak



Binary black hole spins distribution

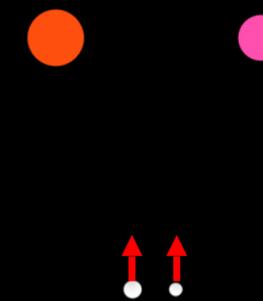
- The LVK find that the **component** spins in black holes are usually small
- Assuming the same underlying distribution for the two spins, the population has a peak at $\lesssim 0.2$
- Seems to support theory and numerical work (e.g. Fuller & Ma ApJL 881 L1)



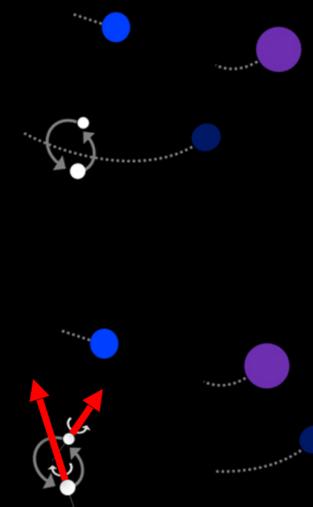
Spin tilts and formation channels

- The *orientation* of the black hole spins can yield precious information about their formation channels - Vitale+ CQG 34, 03LT01; Rodriguez+ ApJL 832 L2; Farr+ Nature 548 426; Talbot & Thrane PRD 96 023012
- **Field evolution** is expected to yield spins which are (roughly) **aligned** to one another and to the angular momentum
- **Dynamical formation** in clusters should yield **isotropic** spin orientation

Field evolution

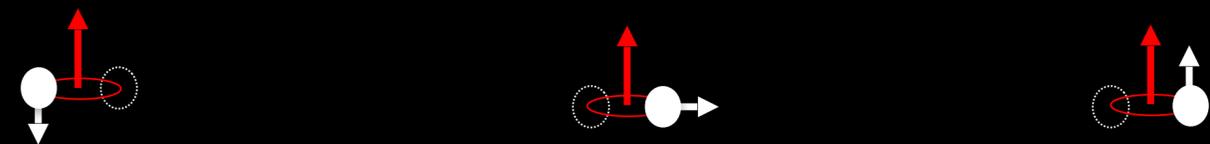
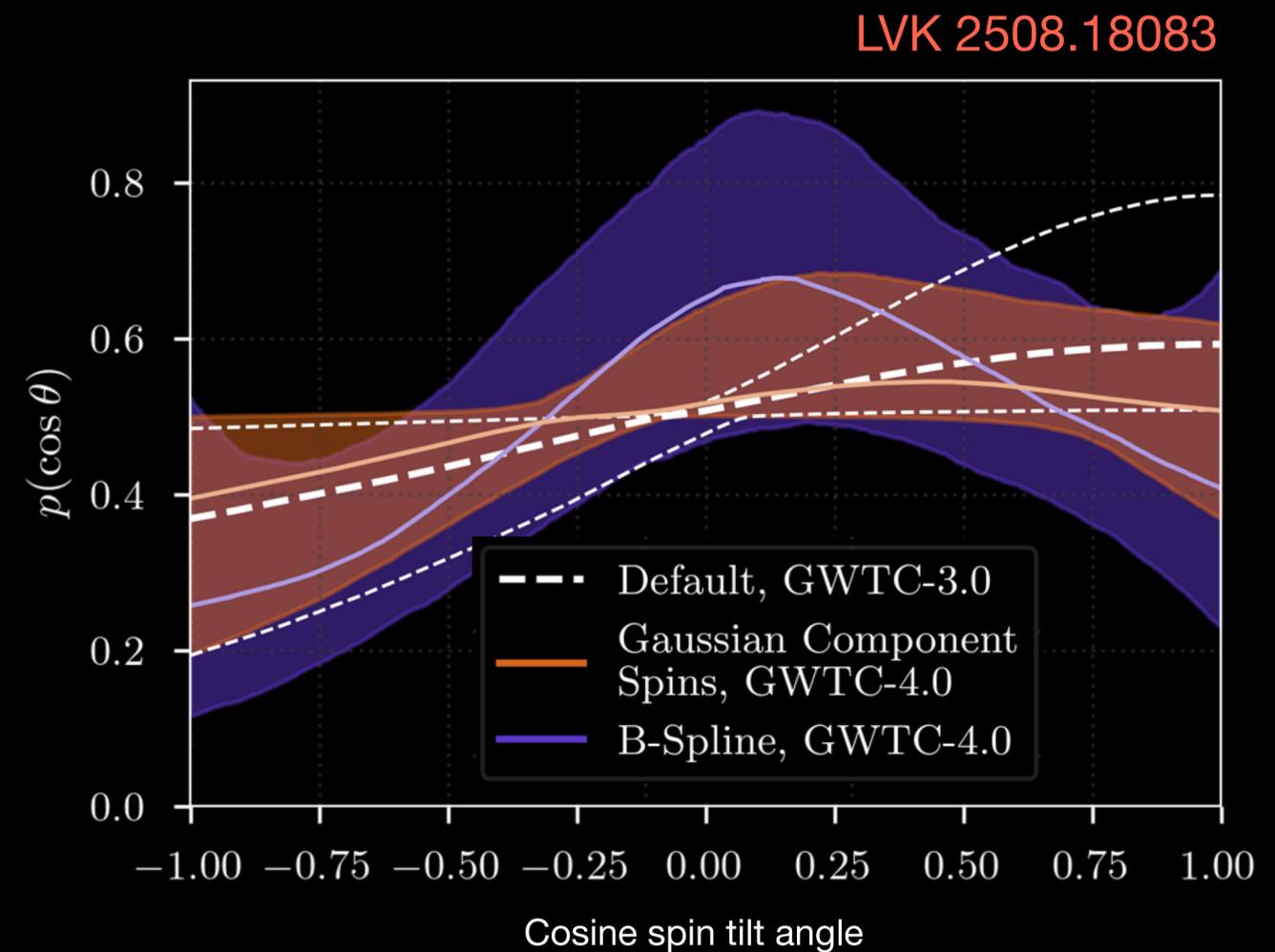


Dynamical formation



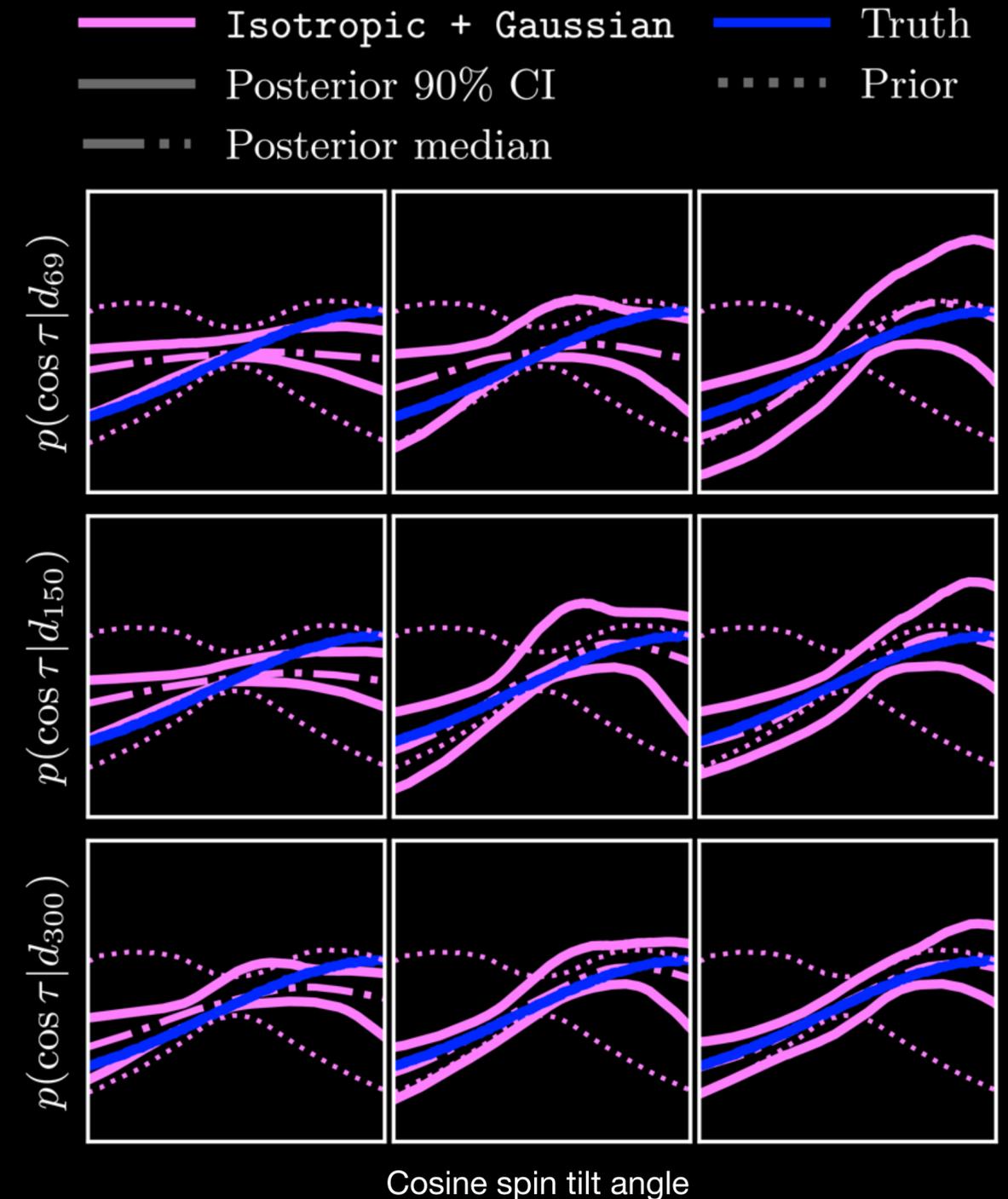
Binary black hole spin tilts distribution

- Model the distribution of spin orientations as a sum of an isotropic component and a Gaussian with mean and scale measured from the data (Vitale+ A&A 668 L2)
- Or as a flexible spline model (Edelman+ ApJ 946 16)
- No obvious sign of a peak at +1, expected for aligned spins
 - Possible peak away from +1?
 - Triples? (Stegman+ 2512.15873)



Binary black hole spin tilts distribution

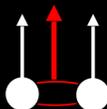
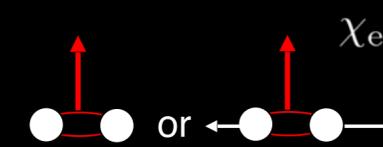
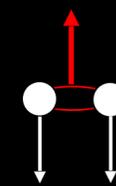
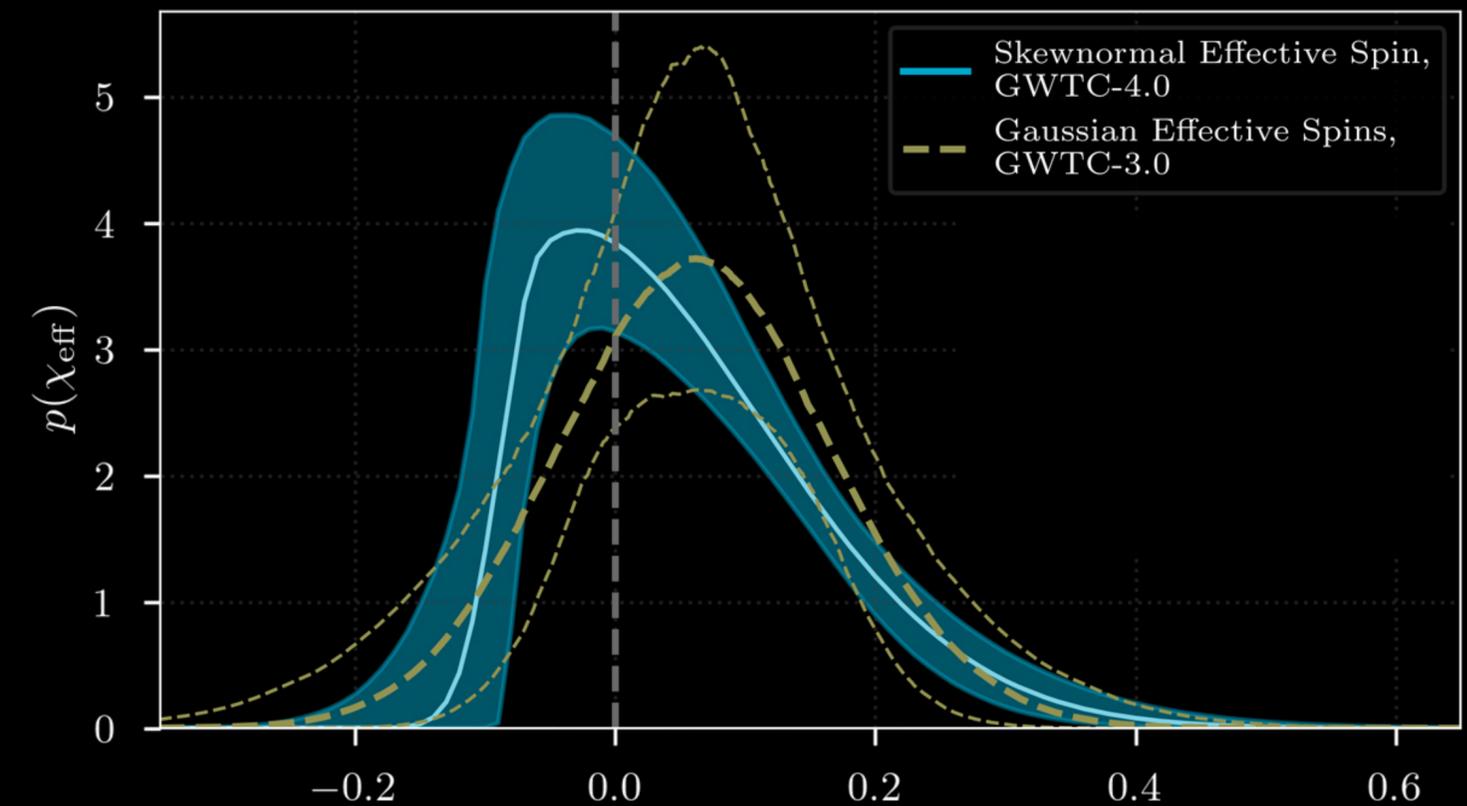
- In [Vitale & Mould 2505.14875](#) we caution that spurious peaks are possible
 - Even if the true population has a peak at +1
 - With catalog sizes comparable to GWTC-4 or larger



Binary black hole χ_{eff} distribution

- The effective spin χ_{eff} is measured to be peaking at ~ 0 and skewed to the right at 99.3% credibility
- Suggestive of a subpopulation of sources evolved in isolation
- No more than 84% of the sources can come from dynamical channels (imply isotropy, χ_{eff} symmetric around zero)

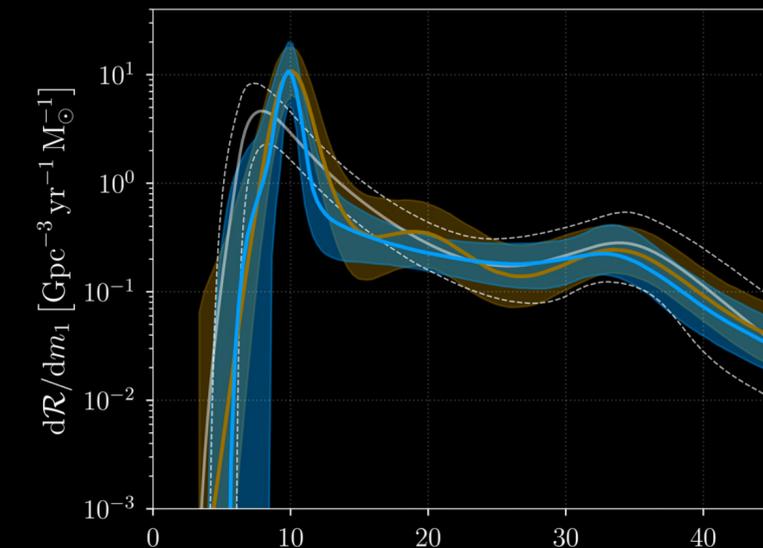
LVK 2508.18083



Astrophysical correlations

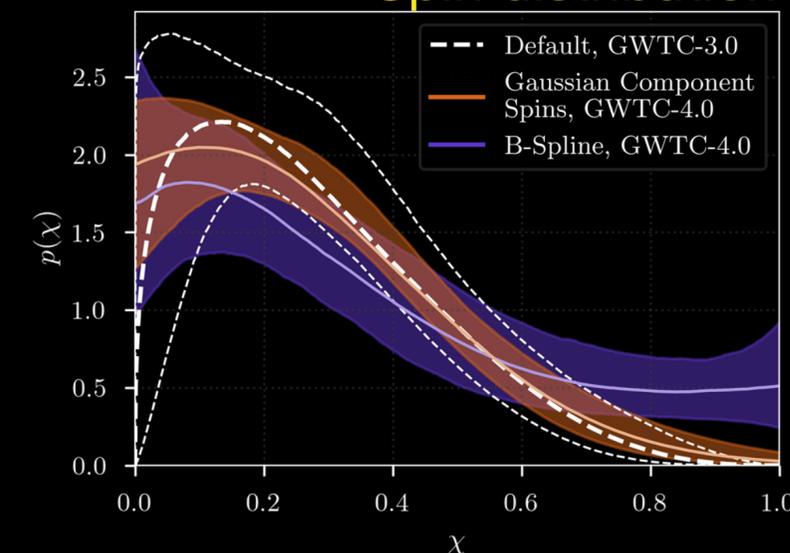
- Many of the models described so far assume independence among parameters
- There are good reasons to believe astrophysical processes *will* correlated source parameters
- Correlations can be probed with larger datasets

Mass distribution



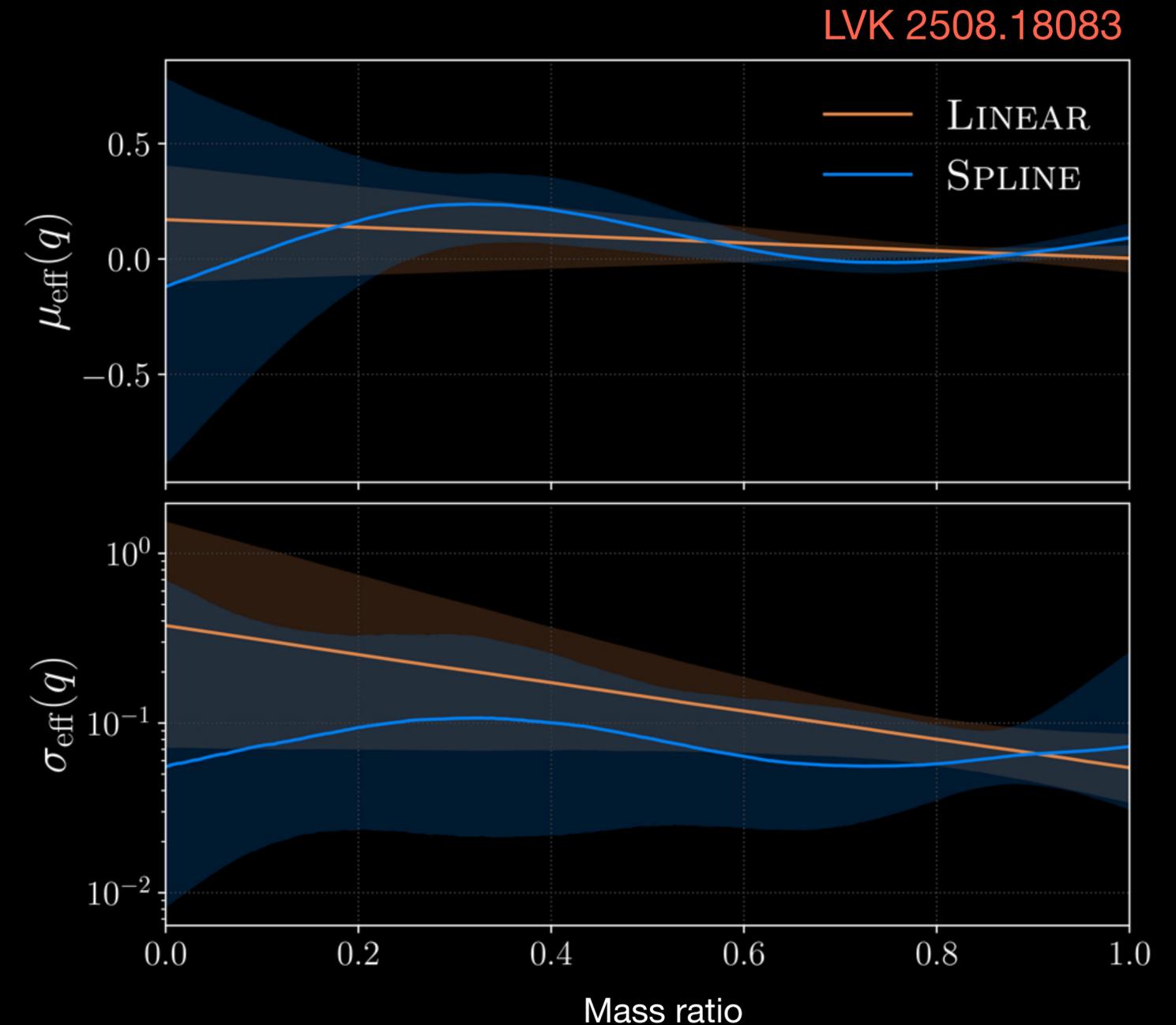
Statistically independent?? \leftrightarrow

Spin distribution



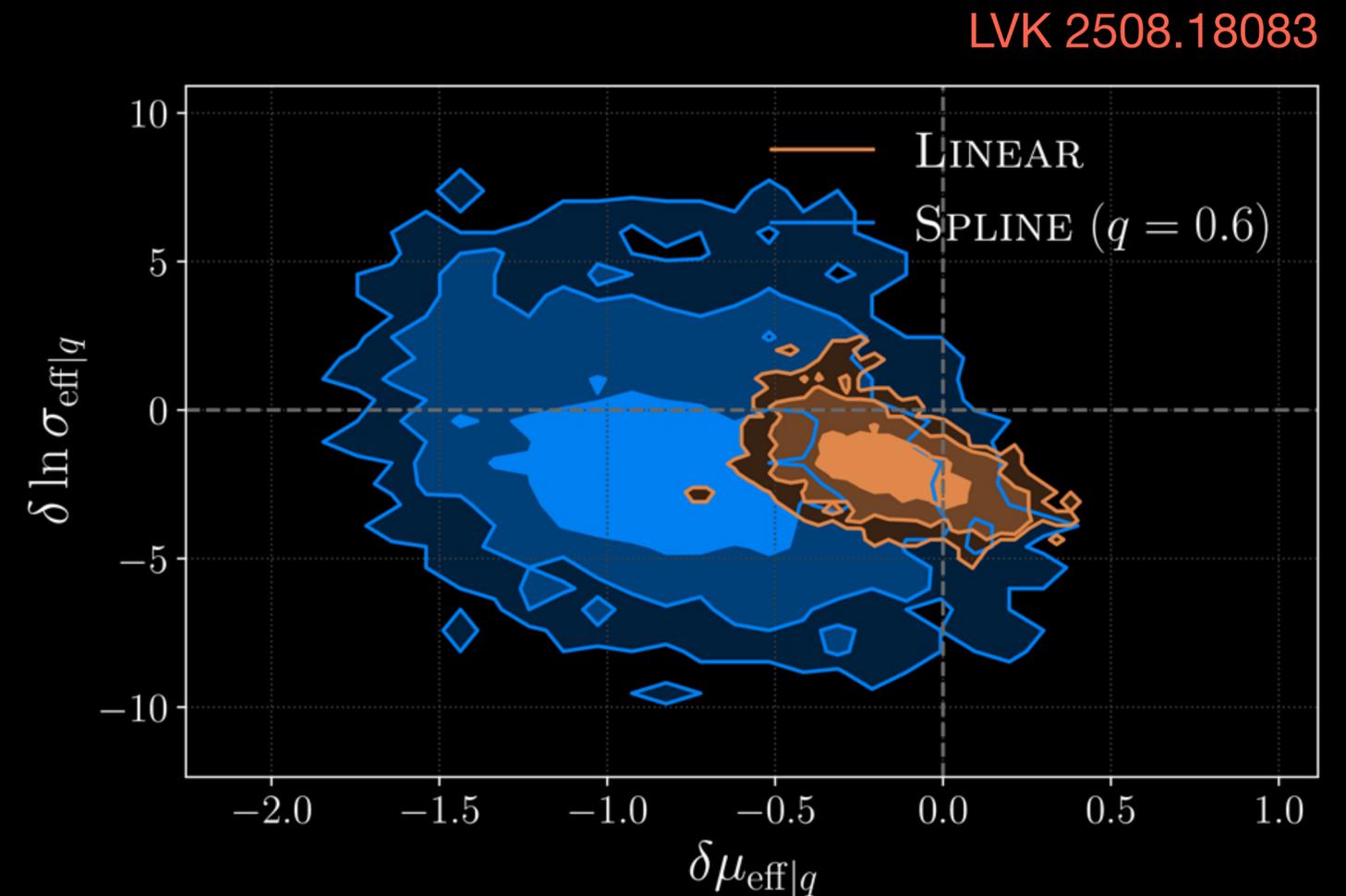
Mass ratio/ χ_{eff} correlation

- First reported by [Callister+ ApJL 922 L5](#) in GWTC-2 data with a linear correlation
- Corroborated by [Adamcewicz & Thrane MNRAS 517 3928](#) with copulas
- And by [Heinzel+ PRD 109 103006](#) with splines
- In GWTC-4, it is unclear if is the mean or the width of χ_{eff} that evolve with the mass ratio



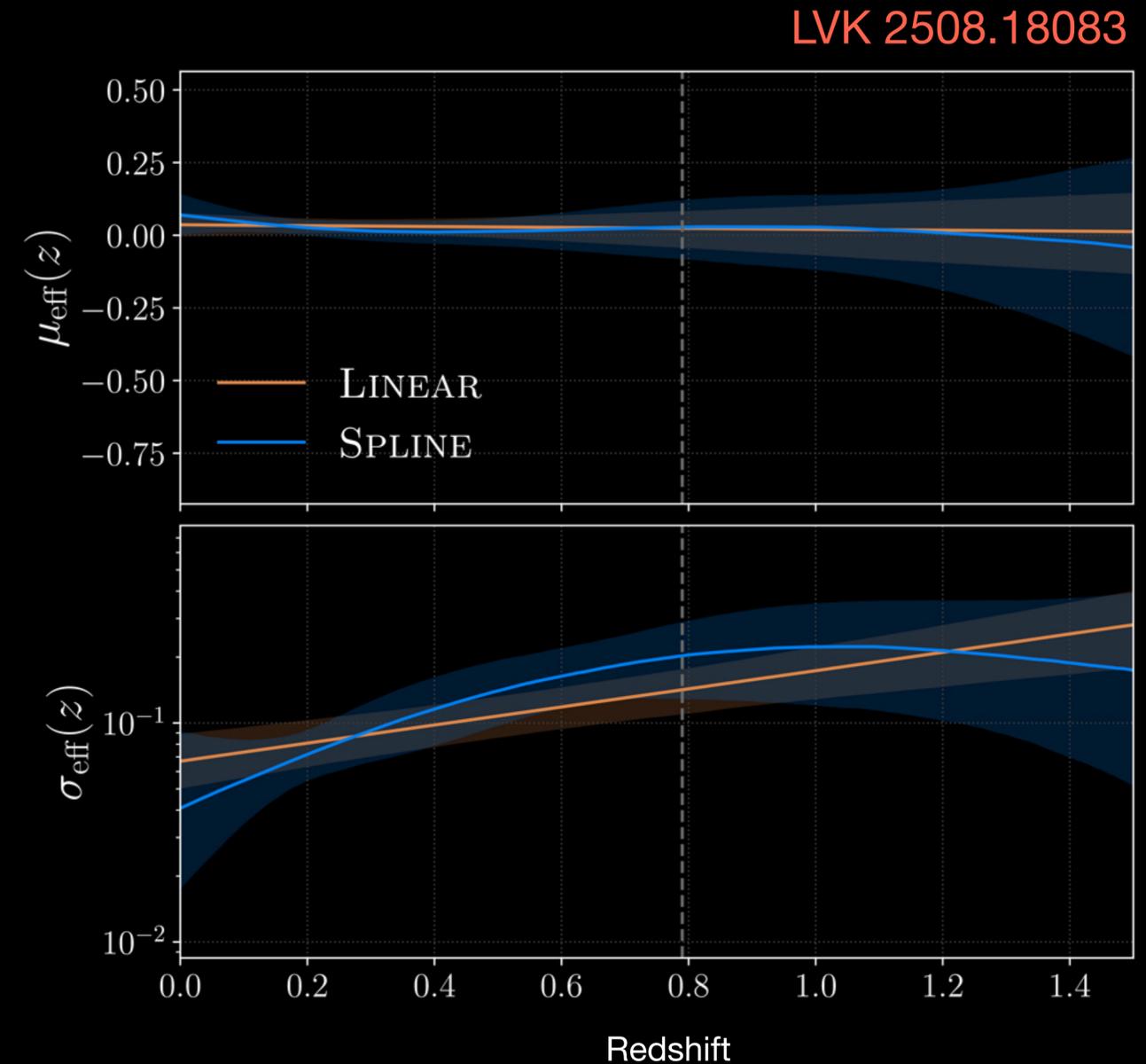
Mass ratio/ χ_{eff} correlation

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- But configurations where neither evolve are disfavored at 99% credibility for the linear model (92% with a copula model)



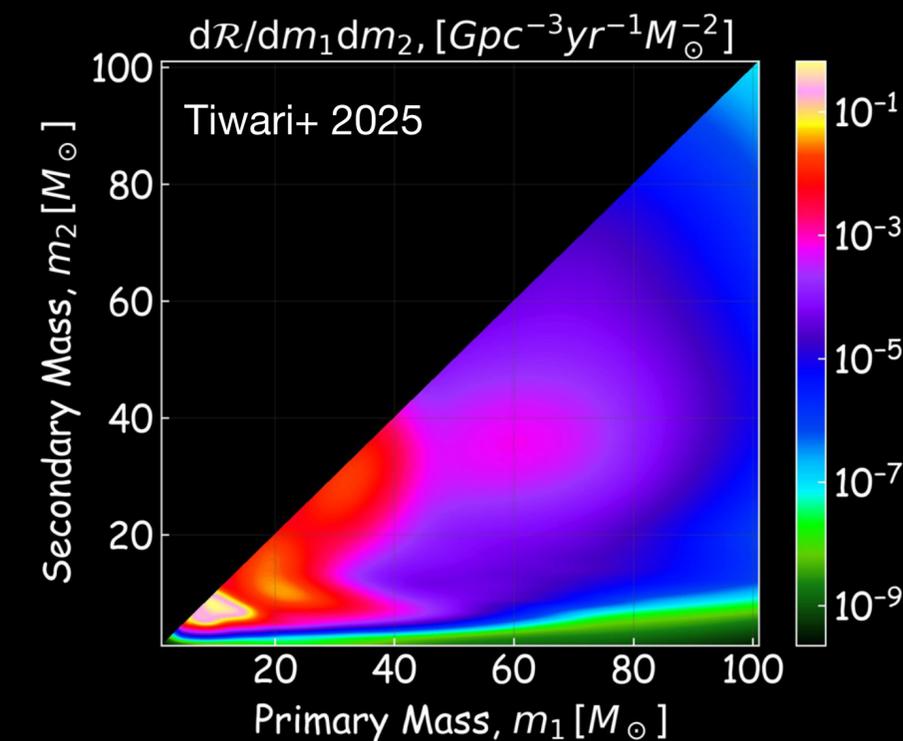
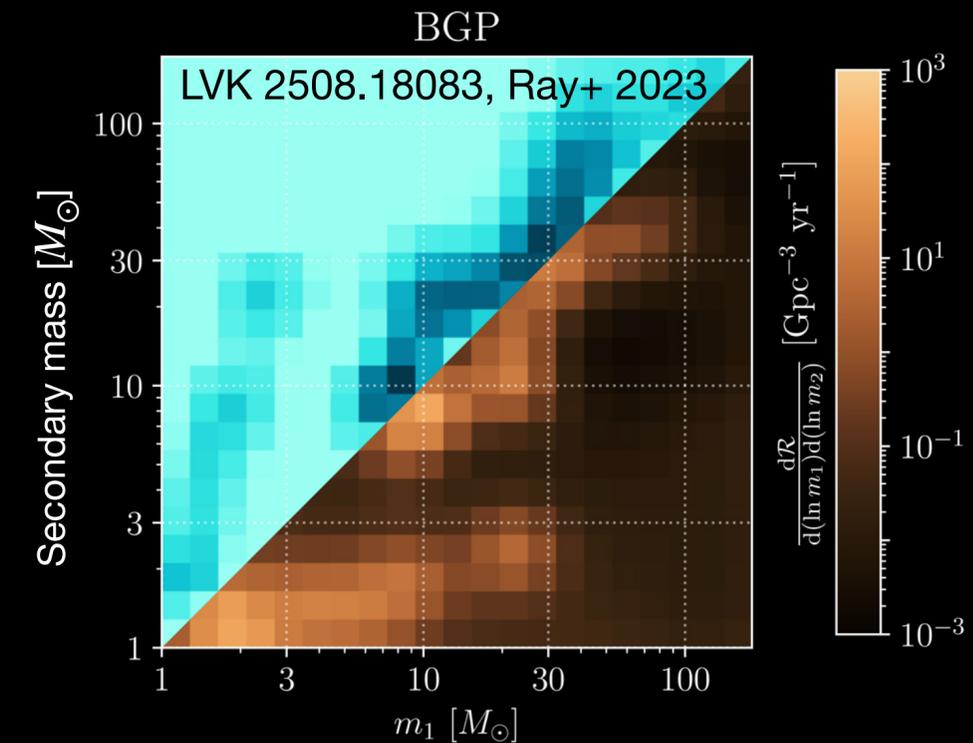
Redshift/ χ_{eff} correlation

- In [Biscoveanu+ ApjL 932 L19](#) we reported evidence that the distribution of χ_{eff} broadens with redshift in GWTC-3 data
 - ...while the position does not evolve
 - Maybe due to metallicity evolution with redshift - [Bavera+ A&A 665 A59](#)
- This finding is confirmed in GWTC-4 with both linear and agnostic approaches



Toward generic correlations

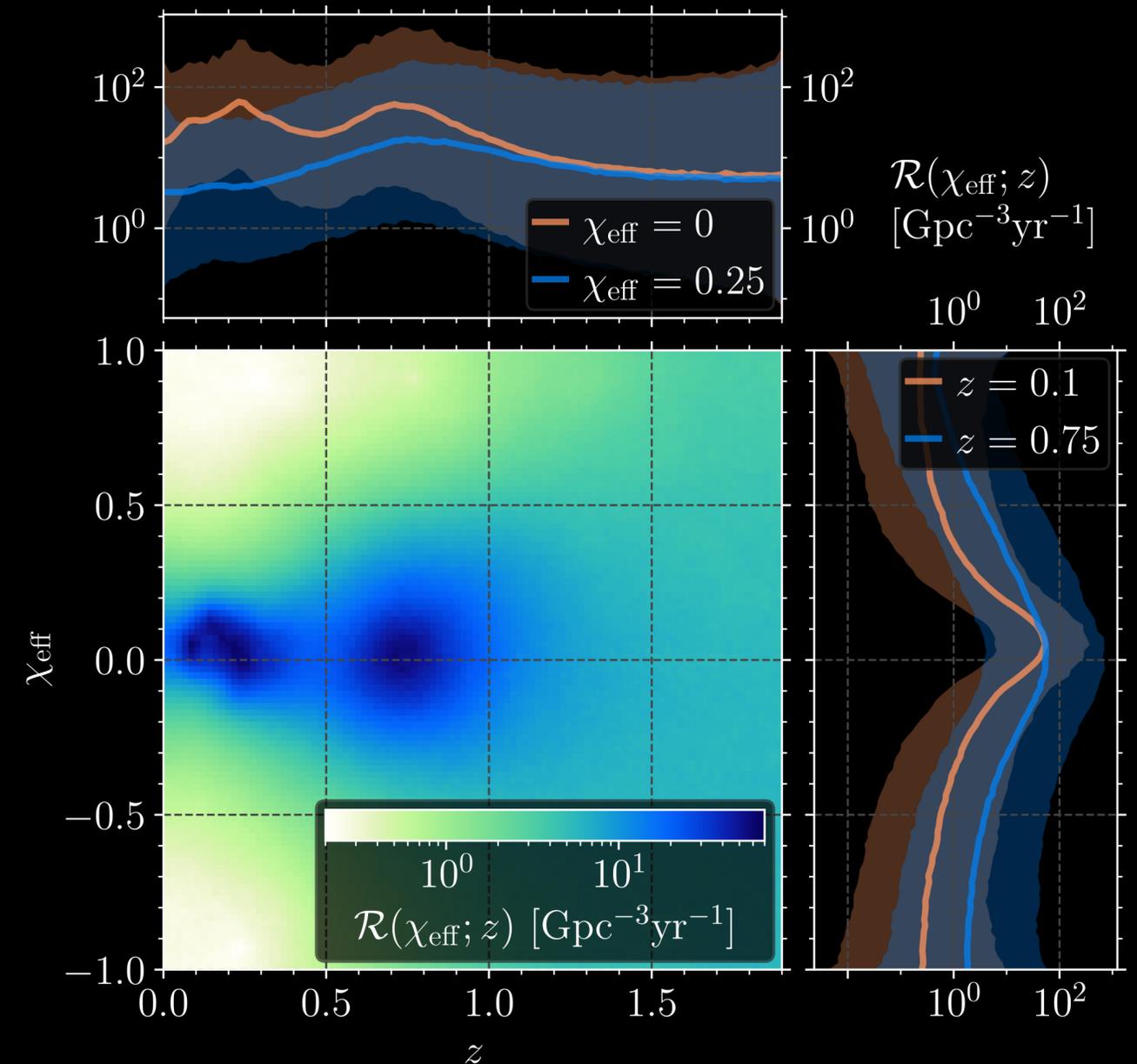
- As the dataset increases in size, more generic models are needed
- Several have been proposed in the last few years
 - VAMANA (Mixture Model) - Tiwari+ 2020*
 - Binned Gaussian processes -Ray+ 2023
- Incorporated by LVK in the GWTC-4 paper



* Really a mixture of strong-ish pieces

What comes next - PixelPop

- At MIT, we have been developing a high-resolution high-dimensional agnostic approach to population inference, based on gaussian processes
- PixelPop - [Heinzel+, PRD 111, 063043 and PRD 111, L061305](#)

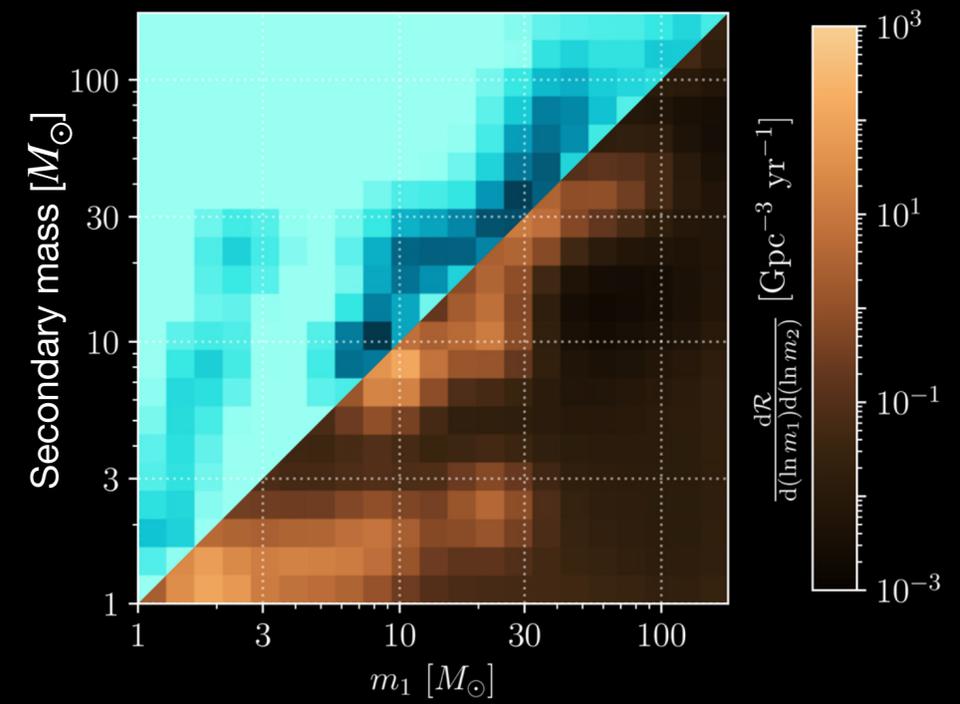
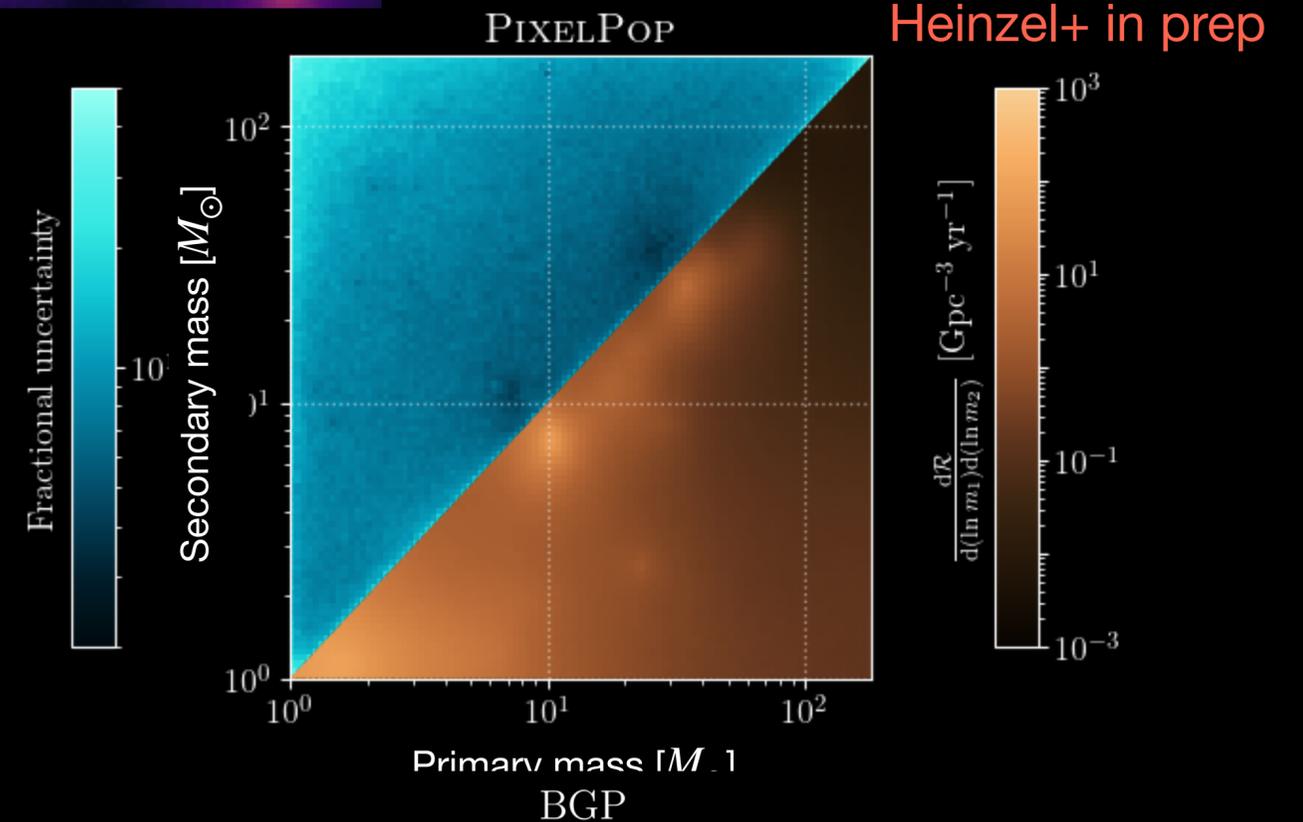


Heinzel+ PRD 111, L061305

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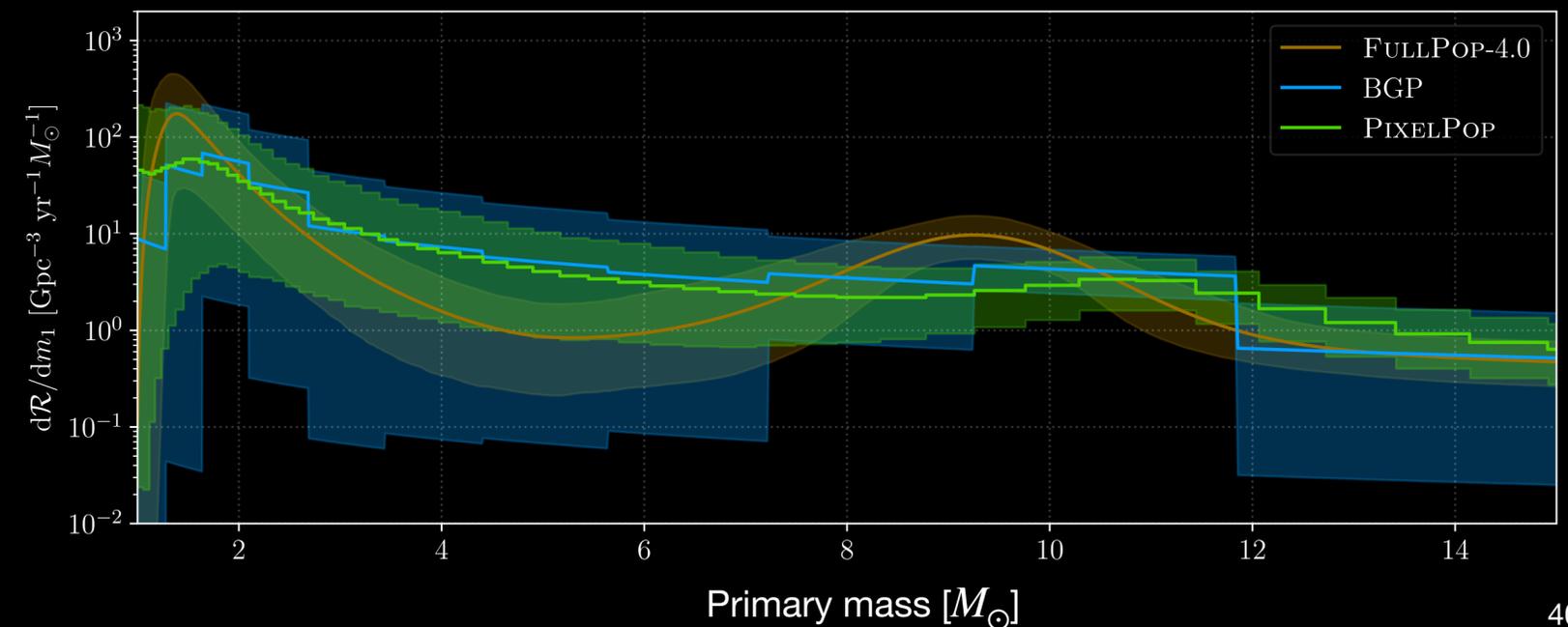
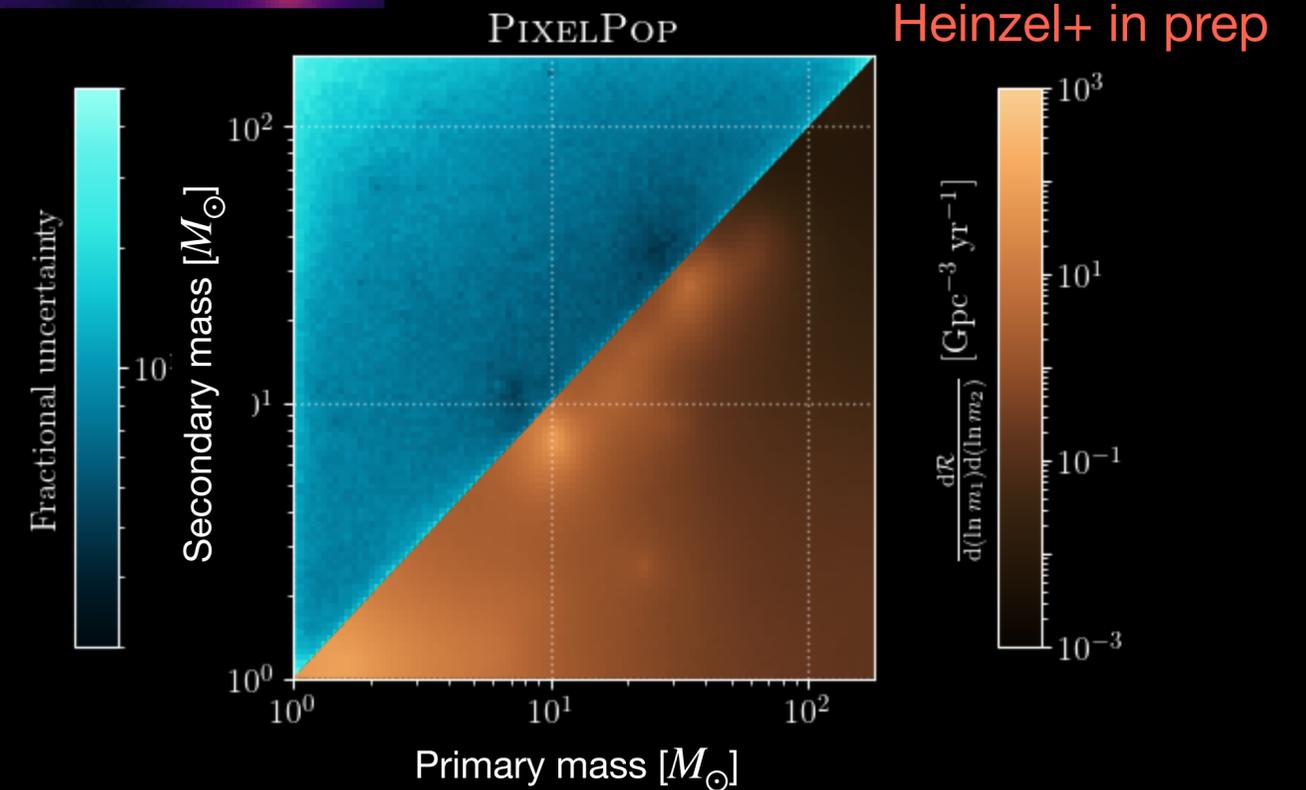
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 - Can already run with 3 correlated parameters
 - Nothing assumed but smoothness



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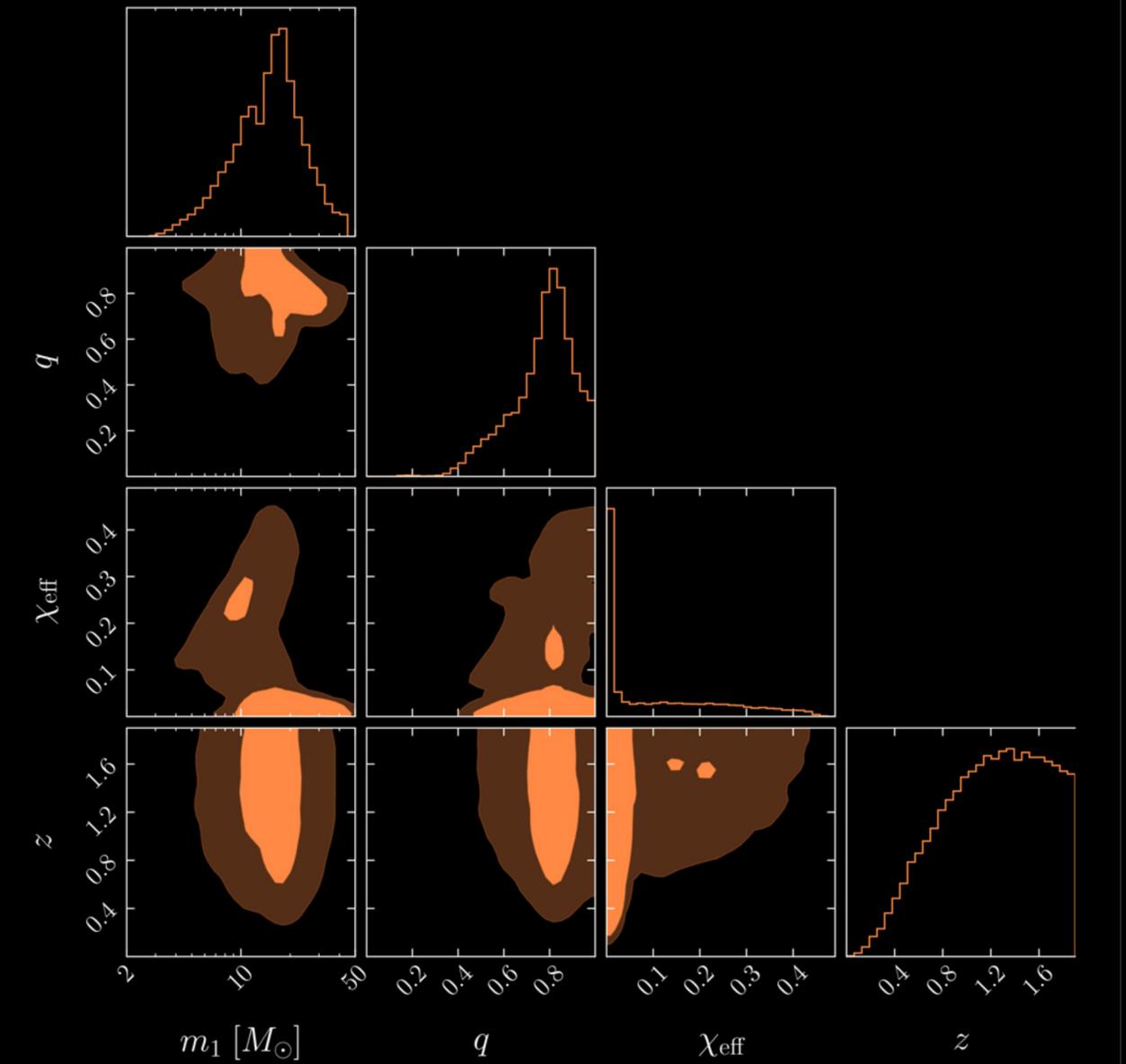
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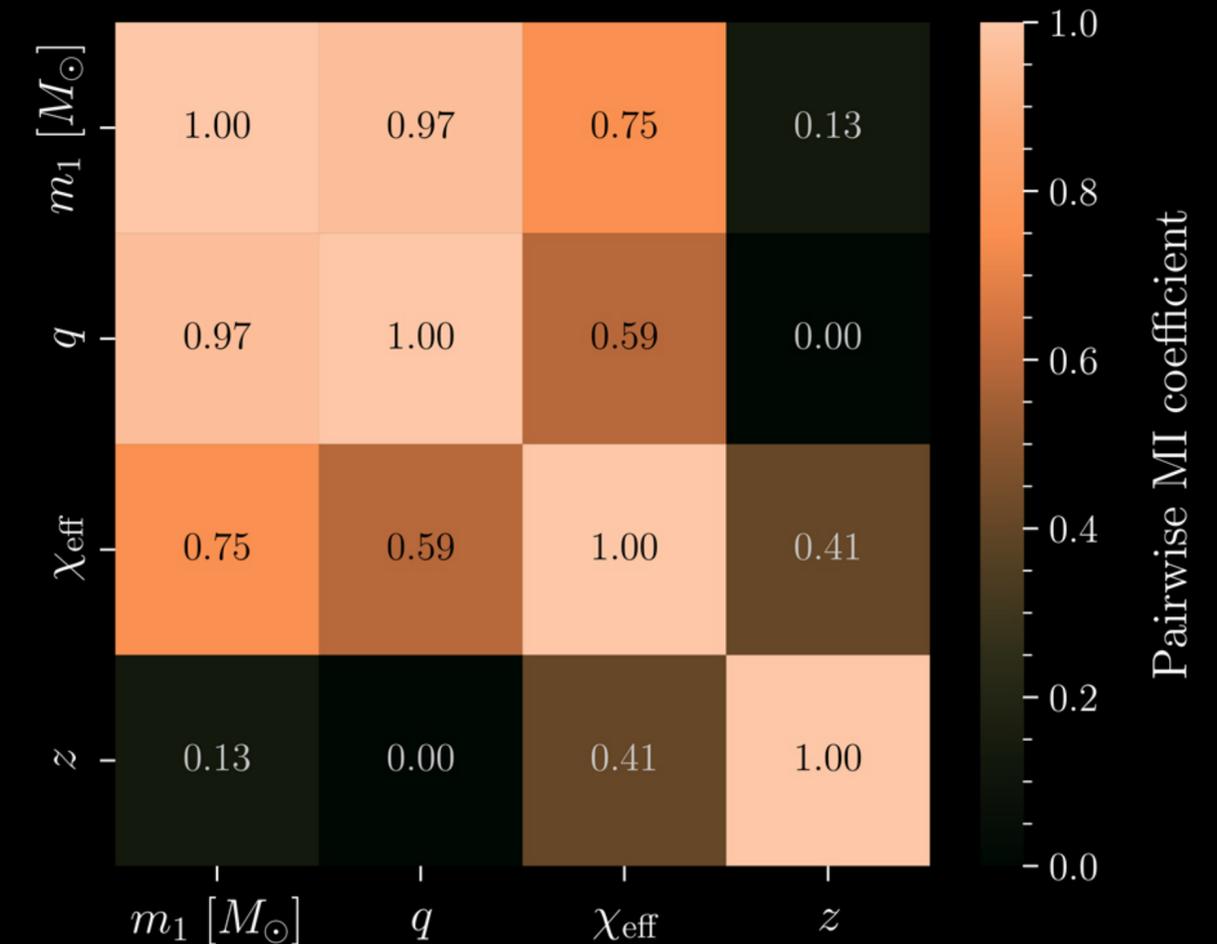
PixelPop's view of non-trivial correlations

- In [Alvarez-Lopez+ 2506.20731](#) we have applied PixelPop to a common envelope population as predicted by pop synth
- Simulated a universe with 400 BBHs from common envelope
 - Highly non-trivial high-D correlations



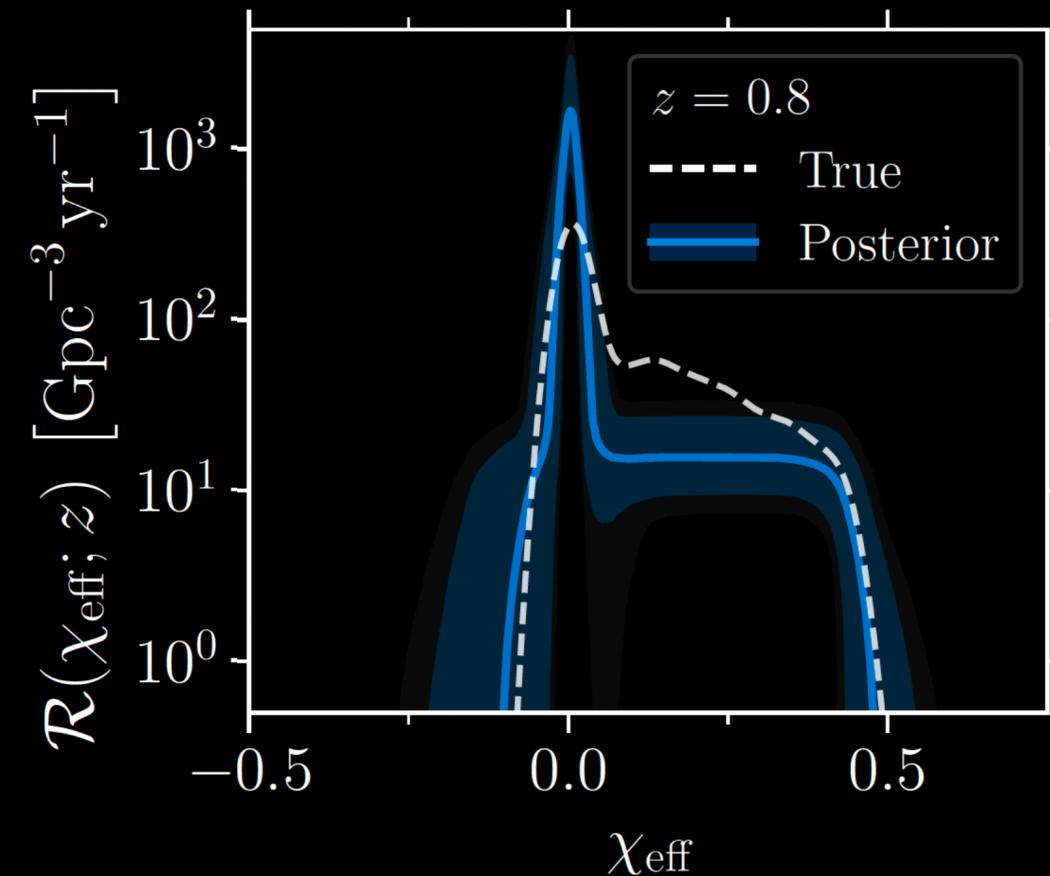
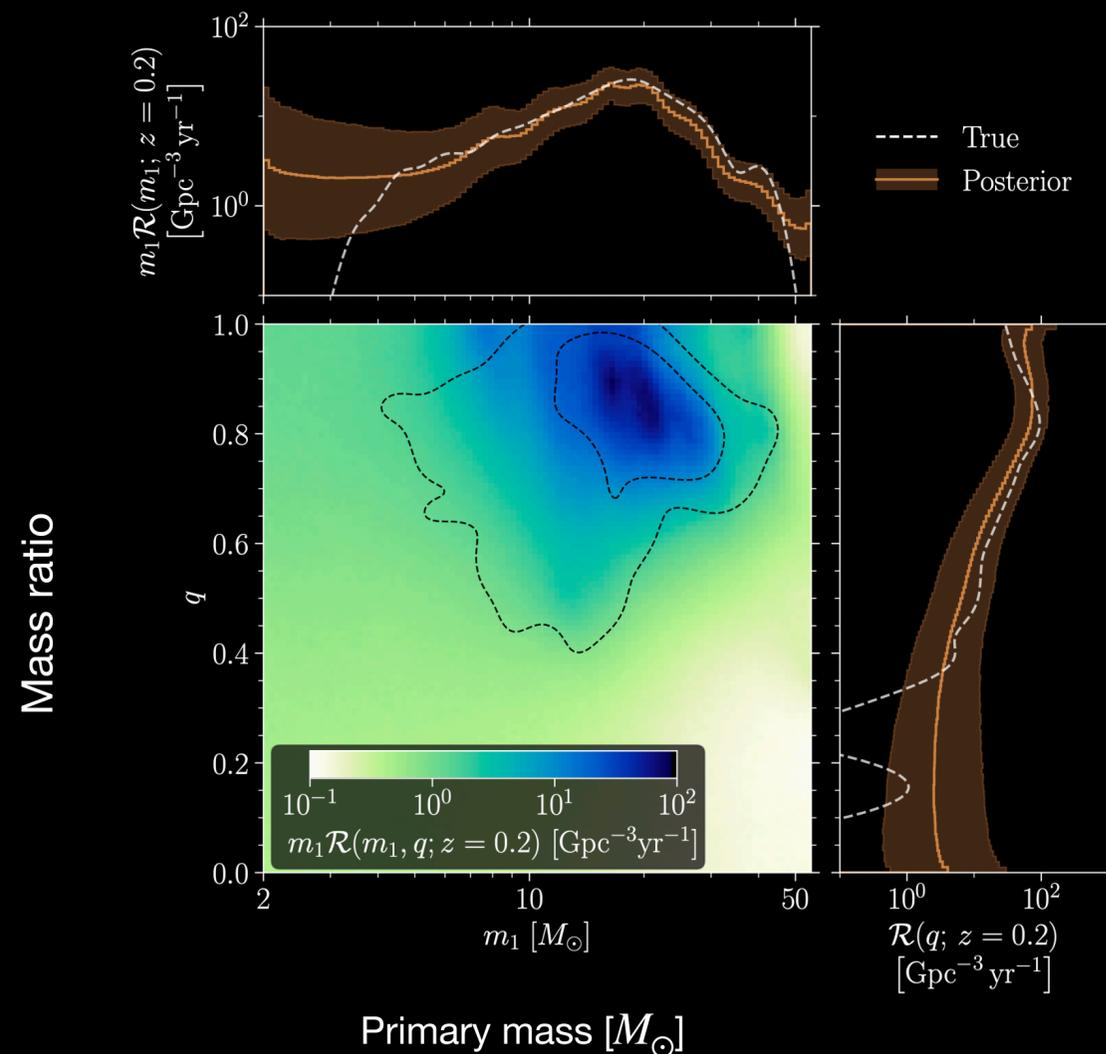
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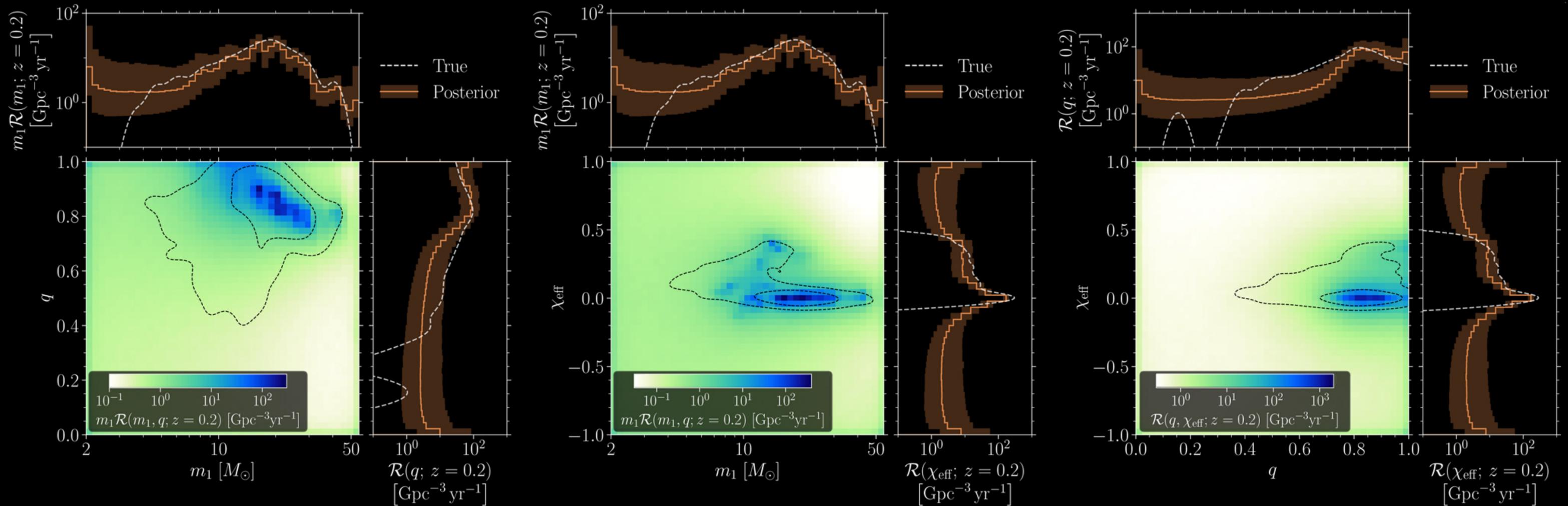
PixelPop's view of non-trivial correlations

- We showed how a simple 2-D correlation is insufficient
 - Model m_1/q with PixelPop, but use strong models for z and χ_{eff}



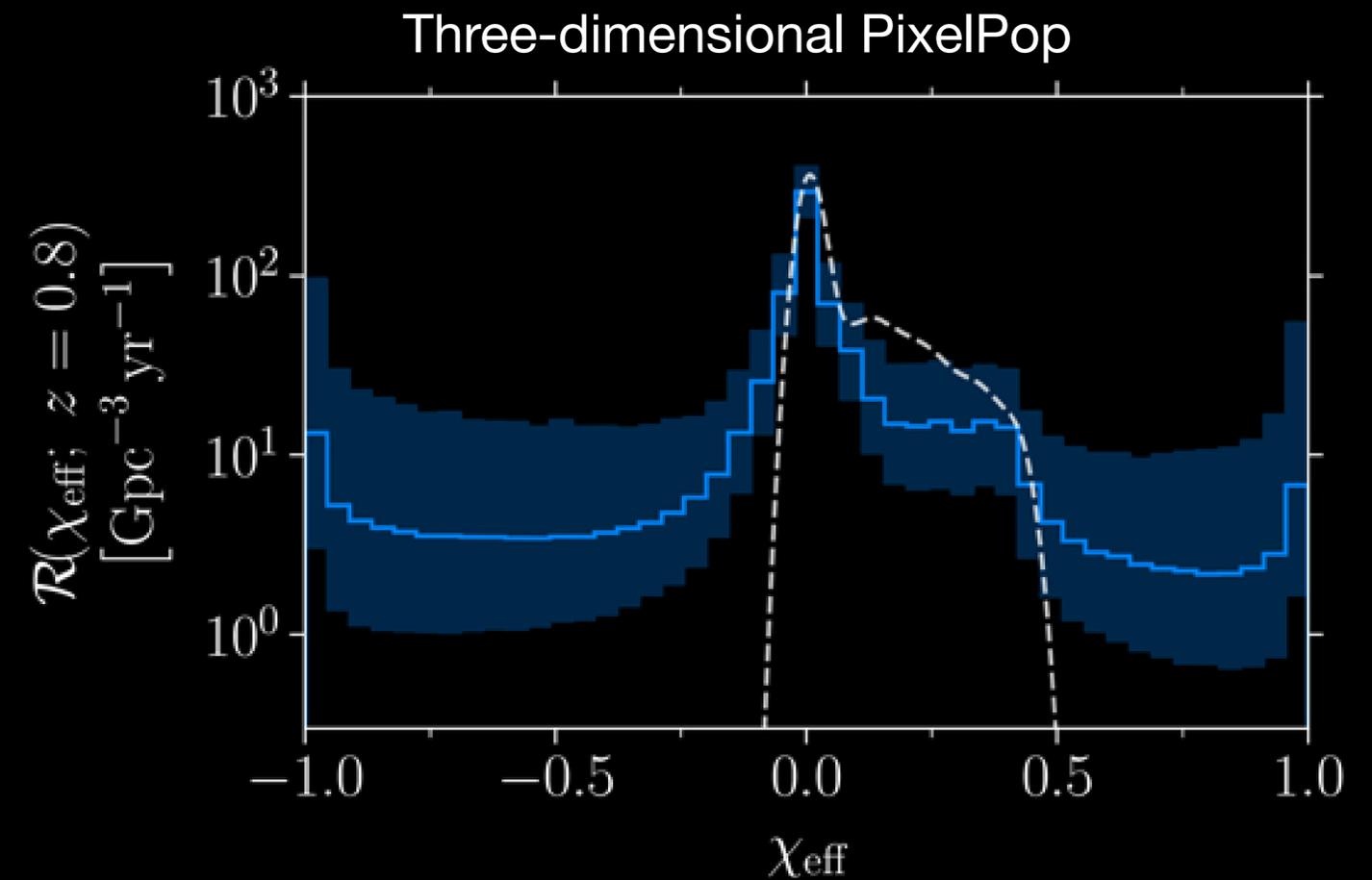
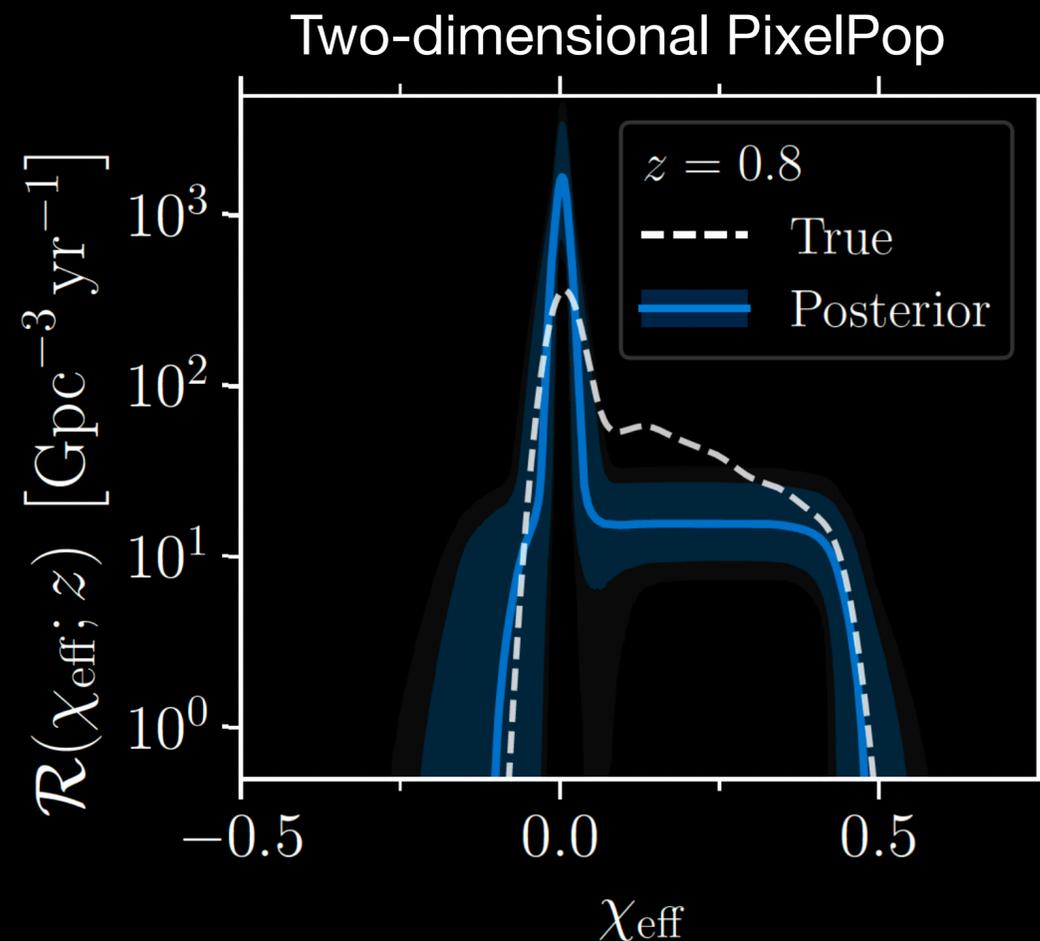
PixelPop's view of non-trivial correlations

- We also showed how a simple 2-D 3-D correlation is insufficient
 - Model $m_1/q/\chi_{\text{eff}}$ with PixelPop, but use strong model for z



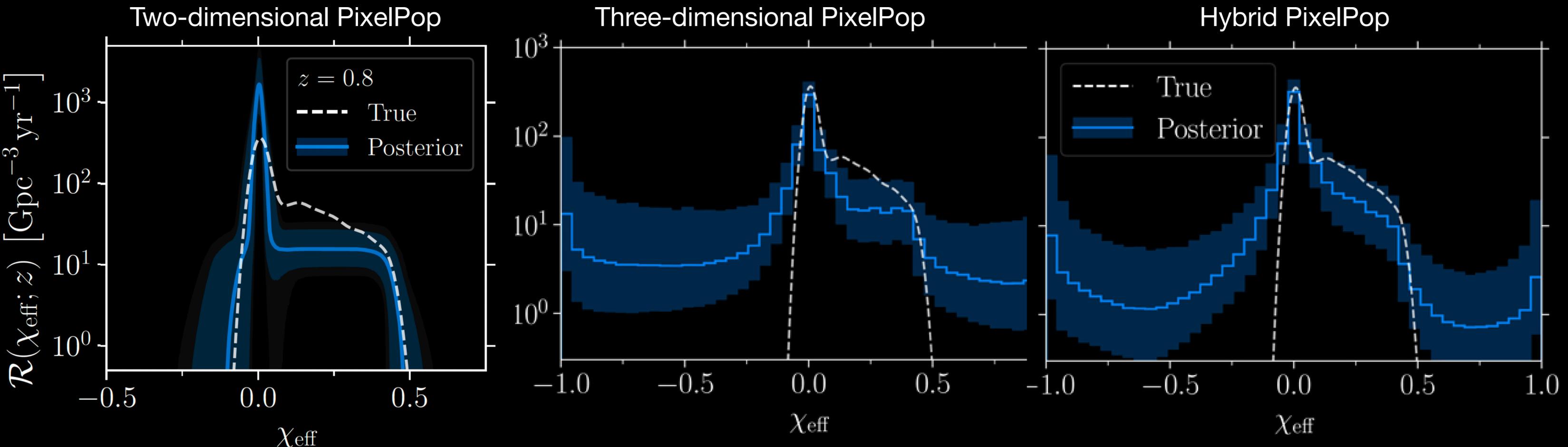
PixelPop's view of non-trivial correlations

- We also showed how a simple 2-D 3-D correlation is insufficient
 - Model $m_1/q/\chi_{\text{eff}}$ with PixelPop, but use strong correlated model for z



PixelPop's view of non-trivial correlations

- We also showed how a 4-D correlated model is needed
 - Model $m_1/q/\chi_{\text{eff}}$ with PixelPop, but use strong correlated models for $p(z | \chi_{\text{eff}})$ (“Hybrid PixelPop” - **ask me about clairvoyance**)

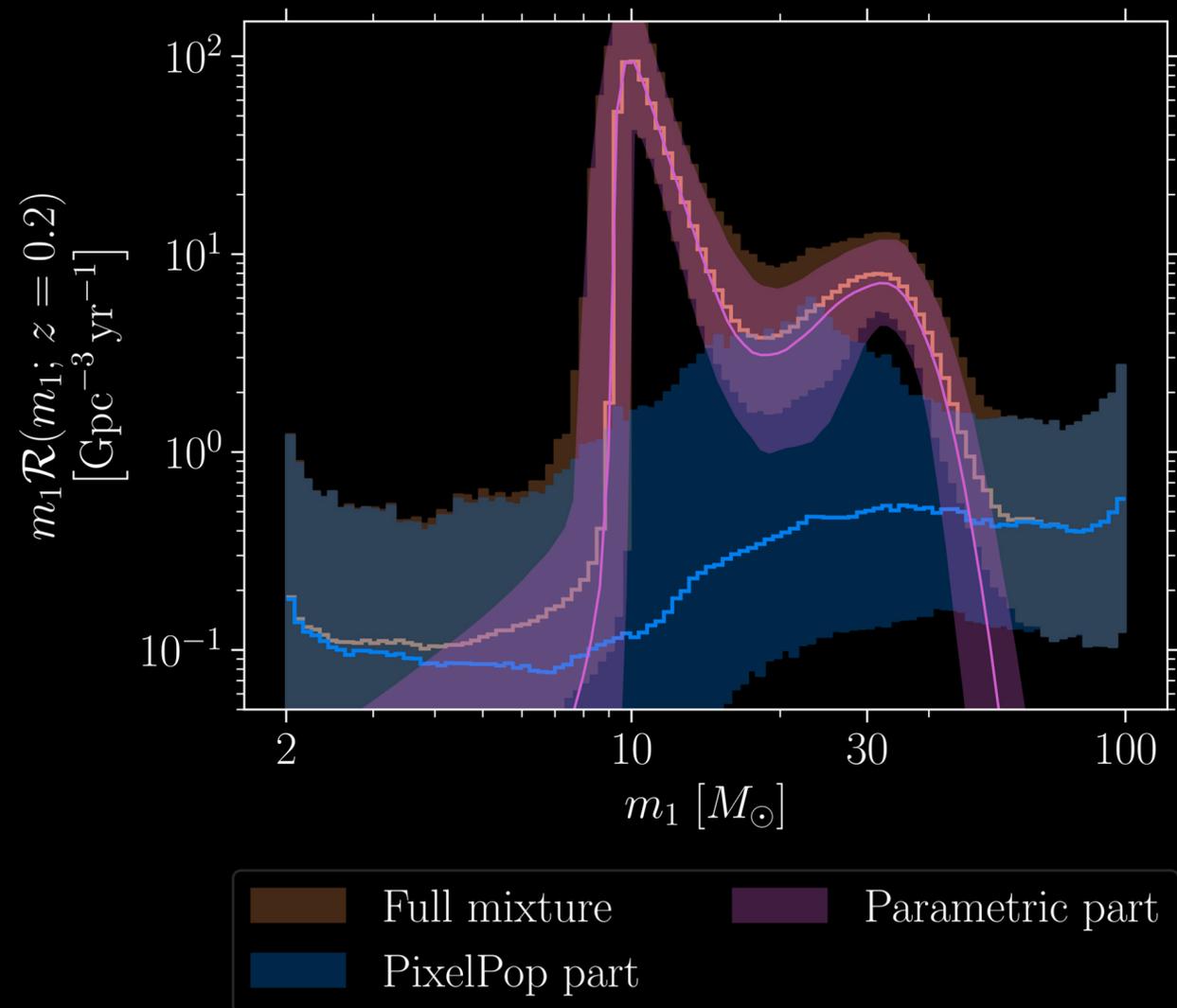


PixelPop's next steps

- Working on an a version with actual 4-D generic correlations (Jack Heinzel)
 - The main issue is the estimation of the detectors' sensitivity
- Working on mixture models of PixelPop with strong models (Sofia Alvarez-Lopez)
 - Best of both worlds?
 - Strong model can do its thing while PixelPop hooks on glitches/outliers/oddballs and captures residual correlations
- Working on interpretability and tails

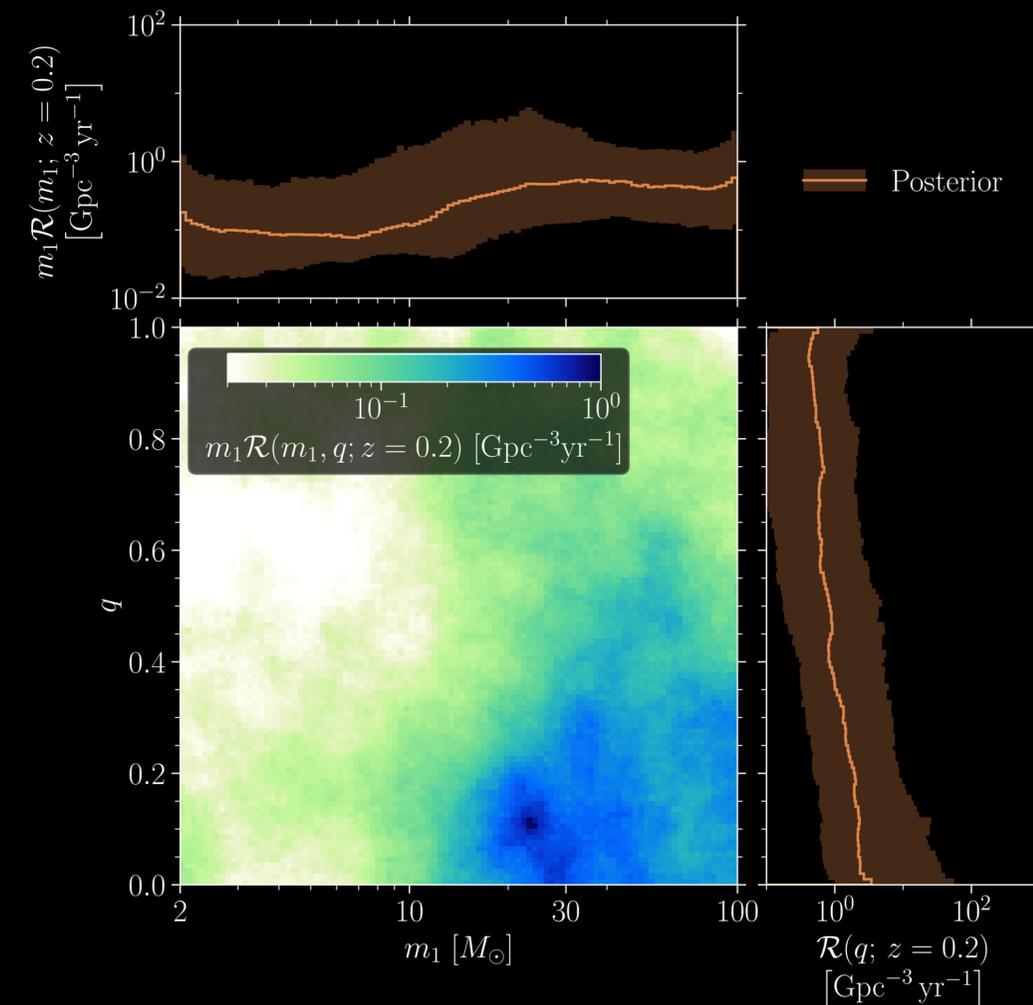
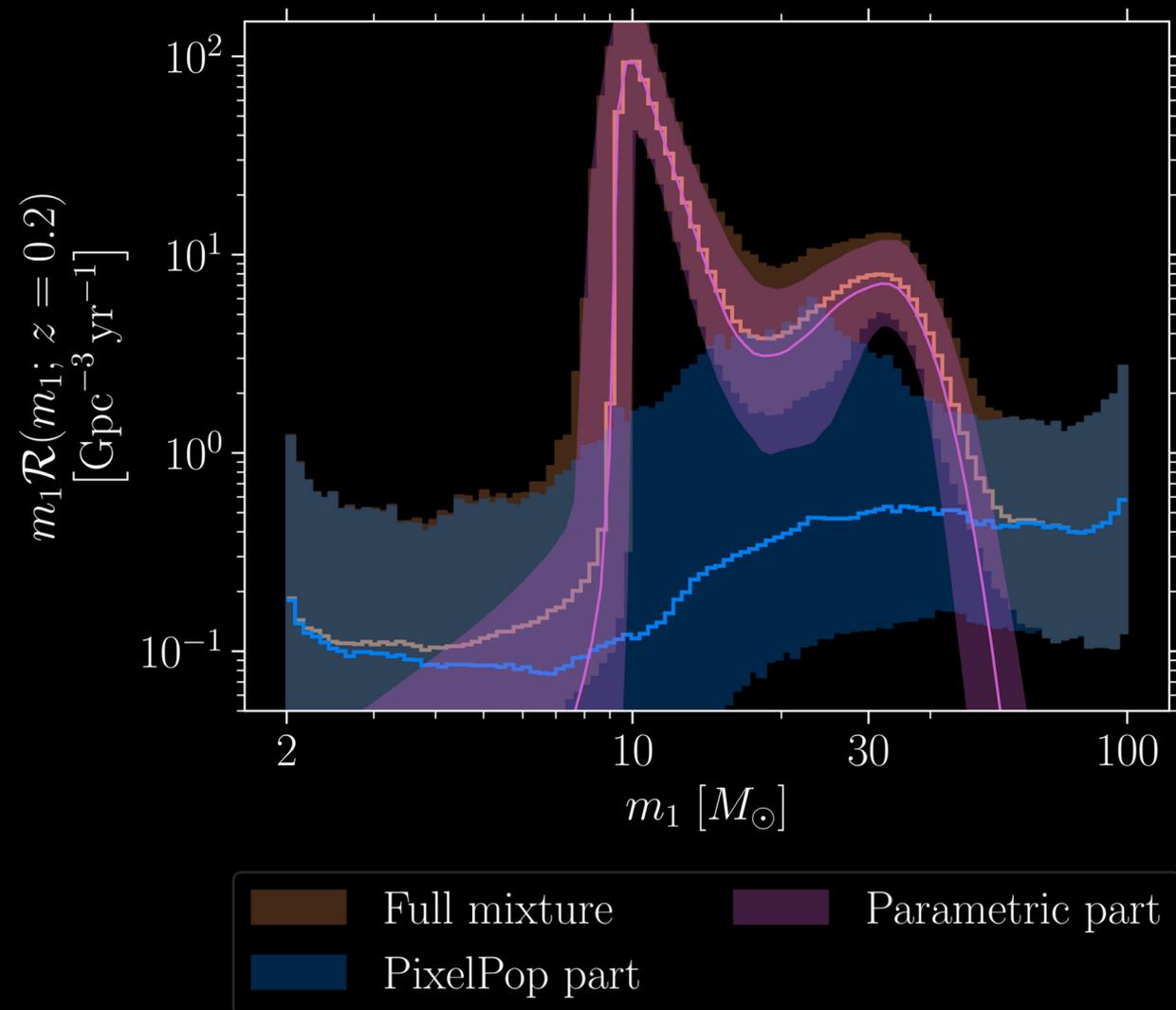
PixelPop's next steps

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PixelPop's next steps

- Strong model can do its thing while PixelPop hooks on glitches/outliers/oddballs and captures residual correlations
- For example, run on GWTC-3 w/o excluding GW190814 ($m_2 = 2.6M_\odot$)



Conclusions

- GTWC-4 has doubled the number of known sources and revealed
 - Excesses of $10 M_{\odot}$ and $35 M_{\odot}$ black holes
 - Existence of black holes with masses below $5 M_{\odot}$ (i.e., no mass gap) and above $100 M_{\odot}$
 - Dearth of large spins, and preference for positively aligned spins
 - Larger spins at larger redshifts; mass ratio pairing evolving with mass; correlation between χ_{eff} and mass ratio
 - Are we seeing hints of multiple populations?
- Will probably double again the size of the catalog by the end of O4c!
- We urgently need agnostic methods to measure correlations in the data