

PS-B11

Symmetry protected topological  
phase of one-dimensional two  
orbital  $SU(N)$  fermionic system

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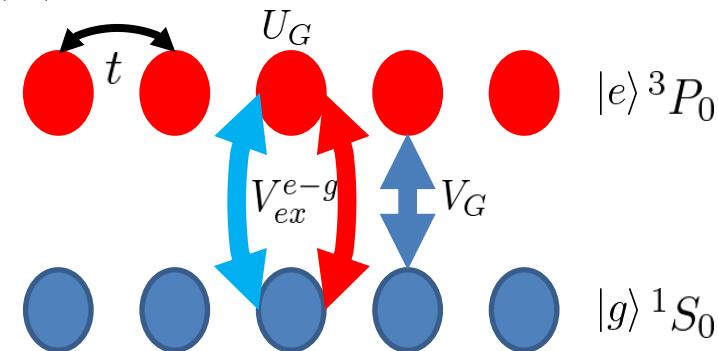


$SU(N)$  fermionic systems using alkaline-earth atoms ( $^{87}\text{Sr}$ ,  $^{173}\text{Yb}$ , etc) in optical lattice was realized.

$$H = -t \sum_{\langle i,j \rangle} \sum_{\beta=g,e} \sum_{m=-I}^I \left( c_{i,\beta,m}^\dagger c_{j,\beta,m} + h.c. \right) - \mu_G \sum_i n_i + \frac{U_G}{2} \sum_i \sum_{\beta=g,e} n_{i,\beta} (n_{i,\beta} - 1) \\ + V_G \sum_i n_{i,e} n_{i,g} + V_{ex}^{e-g} \sum_{i,m,m'} c_{i,g,m}^\dagger c_{i,e,m'}^\dagger c_{i,g,m'} c_{i,e,m}$$

$SU(N)$  symmetry comes from nuclear spin. ( $N=\text{even}$ )

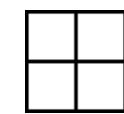
At half-filling, Large  $U_G, V_G, V_{ex}$  limit



Second order perturbation for  $t \rightarrow SU(N)$  Heisenberg chain

$$H_{\text{eff}} = K \sum_i \mathbf{S}_i \cdot \mathbf{S}_{i+1}$$

Onsite rep. for  $N = 4$  case

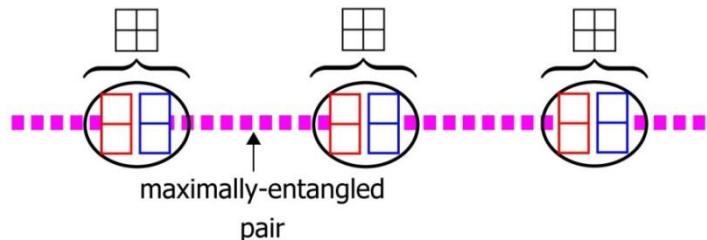


20 dimensional rep.

## String order parameter

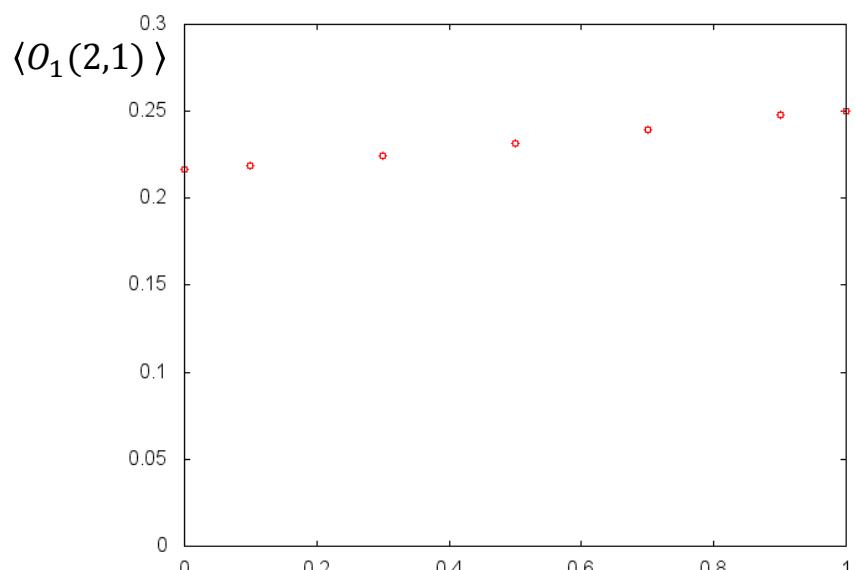
$$O_1(a, b) = \lim_{|i-j| \rightarrow \infty} \{X_P(i)\}^a \exp \left[ b \frac{2\pi i}{N} \sum_{i \leq k < j} H_k^\rho \right] \{X_P^\dagger(j)\}^a$$

## SU(4) Valence Bond Solid state

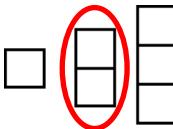


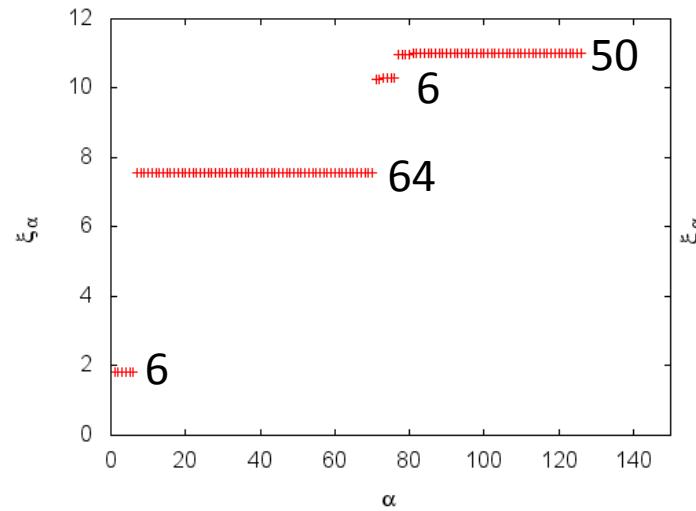
## Parent Hamiltonian

$$H_\alpha = \sum_i \{ \mathbf{S}_i \cdot \mathbf{S}_{i+1} + a \left[ \frac{13}{108} (\mathbf{S}_i \cdot \mathbf{S}_{i+1})^2 + \frac{1}{216} (\mathbf{S}_i \cdot \mathbf{S}_{i+1})^3 \right] \}$$



## Topological class 2

  
 $\{0, 1, 2, 3 \text{ mod } 4\}$   
 trivial      nontrivial



a

SU(4) VBS

